



Experimental Physics at Lepton Colliders

CERN Summer Student Lecture, 2019

Lecture 2

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Physics at Lepton Colliders

◆ Lecture 1 (Wednesday 31 July, 9:15)

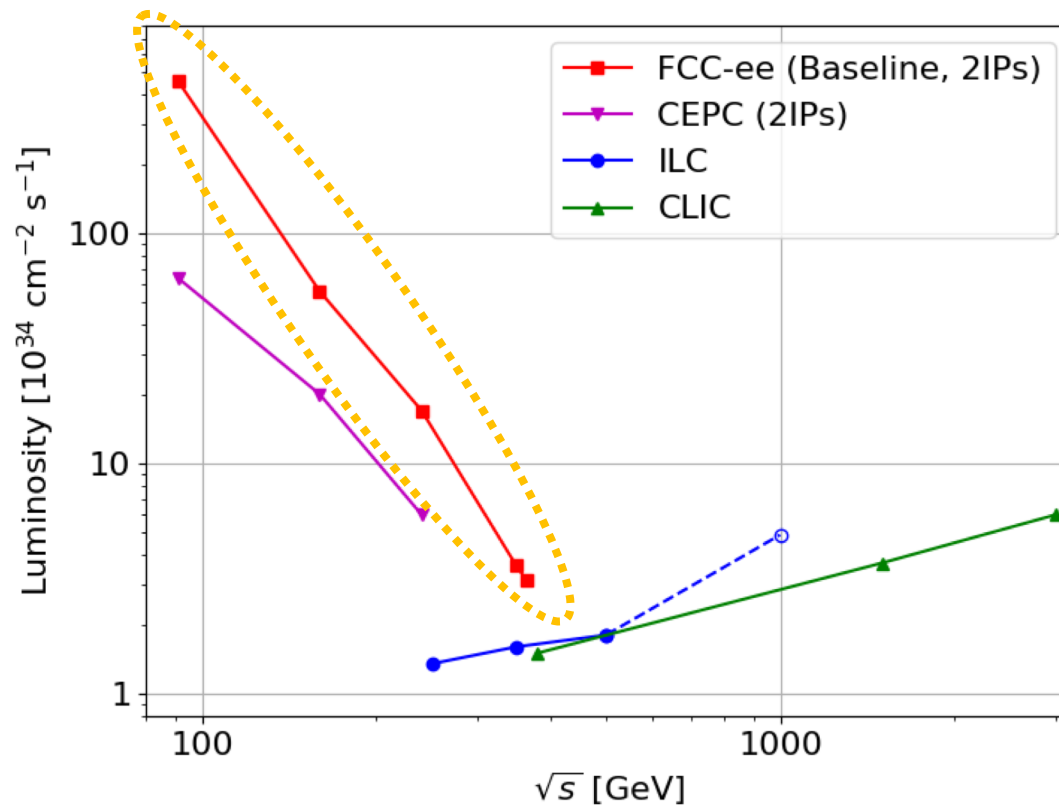
- Introduction: **Why Lepton Colliders ?**
- Where we stand: **Status of the Standard Model**
- An experimental strategy for the future: **e^+e^- colliders**
- Precision Higgs Physics

◆ Lecture 2 (Thursday 1 August, 10:25)

- Electroweak Precision Physics: **FCC-ee**
- GigaZ physics: **Flavour Physics and Direct Discoveries**
- High Energy e^+e^- Physics: **CLIC**
- Instrumentation: **Detectors for e^+e^- physics**
- Thinking out of the box: **Muon colliders**
- Rounding off: **Summary and Conclusions**

Electroweak Precision Physics

FCC-ee



FCC-ee Goals in Numbers

Working point	Z, years 1-2	Z, later	WW	HZ	$t\bar{t}$ threshold...	... and above
\sqrt{s} (GeV)	88, 91, 94		157, 163	240	340 – 350	365
Lumi/IP ($10^{34} \text{ cm}^{-2}\text{s}^{-1}$)	100	200	25	7	0.8	1.4
Lumi/year (2 IP)	24 ab^{-1}	48 ab^{-1}	6 ab^{-1}	1.7 ab^{-1}	0.2 ab^{-1}	0.34 ab^{-1}
Physics goal	150 ab^{-1}		10 ab^{-1}	5 ab^{-1}	0.2 ab^{-1}	1.5 ab^{-1}
# events	$5 \times 10^{12} \text{ Z}$		10^8 WW	10^6 HZ	$10^6 t\bar{t}$	$45000 \text{ WW} \rightarrow \text{H}$
Run time (years)	2	2	2	3	1	4

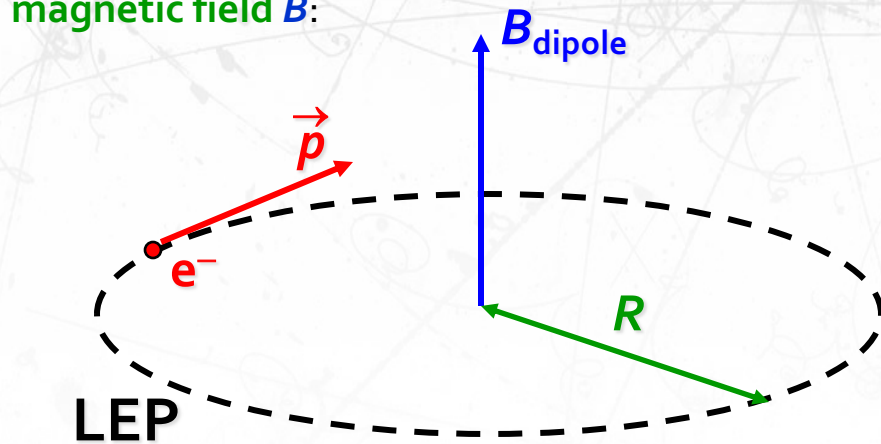
- ◆ FCC-ee is the ultimate Z, W, Higgs and top factory
 - 10^5 times more Zs and 10^3 times more Ws than LEP1 and LEP2
 - ❖ Potential statistical accuracies are mind-boggling !
- ◆ Predicting accuracies with 200 times smaller statistical precision than at LEP is hard
 - Conservatively, use LEP experience for systematics
- ◆ Example: The uncertainty on E_{BEAM} (2 MeV) was the dominant uncertainty on m_Z, Γ_Z
 - Can we do significantly better at FCC-ee ?

FCC-ee Precision Physics: Beam Energy (1)

◆ Measurement of the beam energy at LEP

- Ultra-precise measurement crucial for m_Z, Γ_Z, \dots
- Unique to circular colliders

Electron with momentum \vec{p} in a uniform vertical magnetic field B :



$$L = 2\pi R = 27\text{km}$$

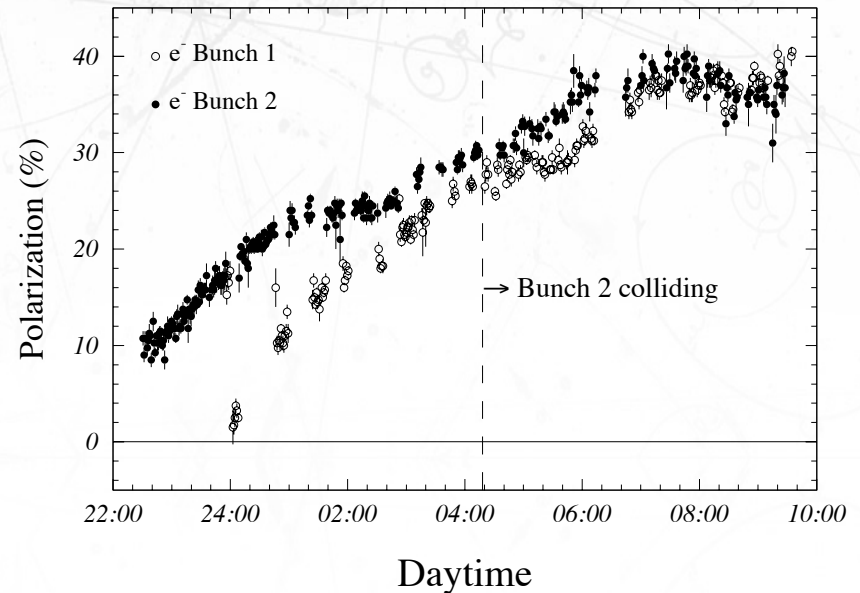
$$E \sim p = e B R = (e/2\pi) B L$$

In real life, B non-uniform, LEP ring not circular

$$E = \frac{e}{2\pi} \oint_{\text{LEP}} B dl$$

To be measured

The electrons get transversally polarized (i.e., their spin tends to align with B)

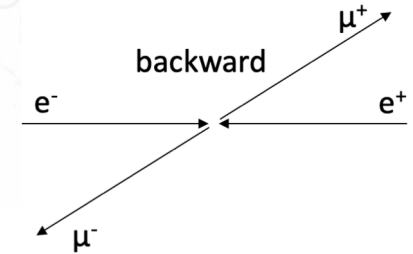
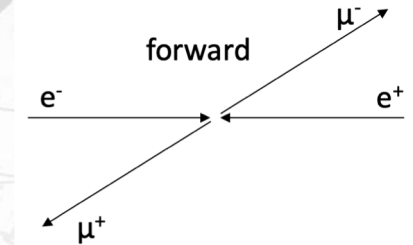
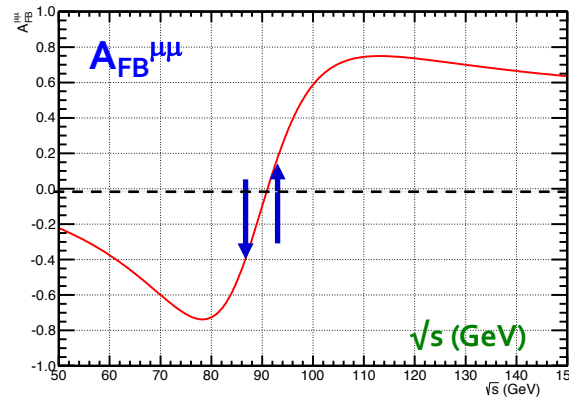
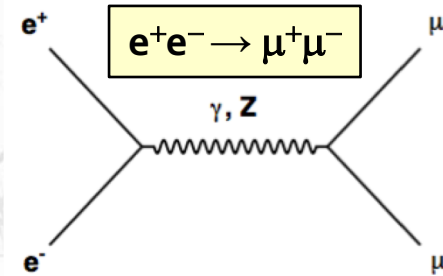
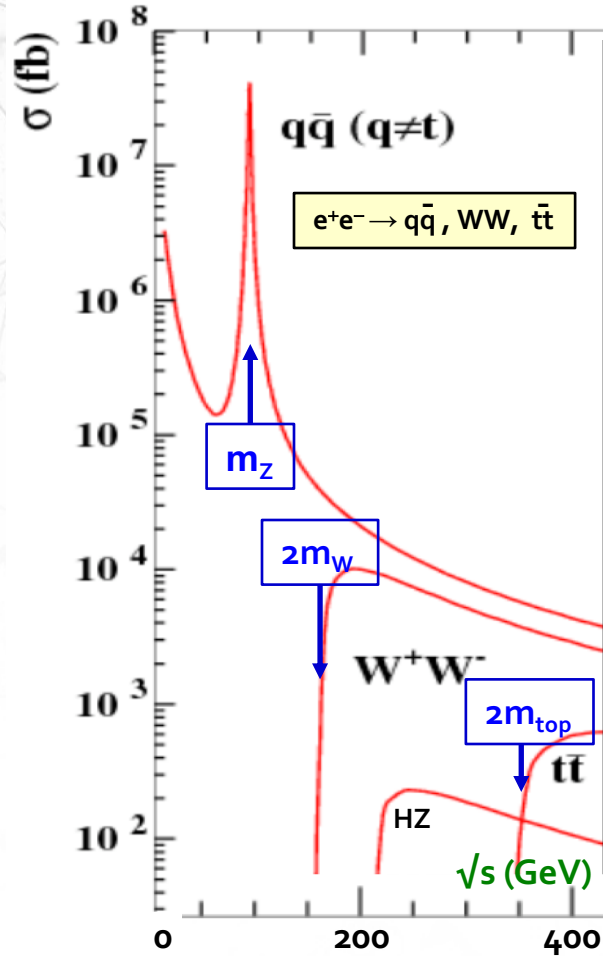


Slow process (~ 1 hour to get 10% polarization)

NB. Polarization can be kept in collision (was attempted only once at LEP).

FCC-ee Precision EW Physics Measurements (1)

- ◆ Boils down to measuring cross sections and asymmetries



$$A_{FB}^{\mu\mu} = \frac{N_F^{\mu+} - N_B^{\mu+}}{N_F^{\mu+} + N_B^{\mu+}} \approx f(\sin^2 \vartheta_W^{eff}) + \alpha_{QED}(s) \frac{s - m_Z^2}{2s} g(\sin^2 \vartheta_W^{eff})$$

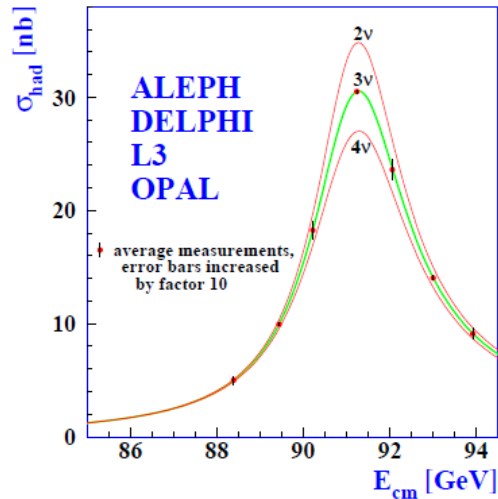
- Measure $\sin^2\theta_W$ with A_{FB} at $\sqrt{s} = m_Z$
- Measure $\alpha_{QED}(m_Z)$ with A_{FB} at $\sqrt{s} = 87.9$ and 94.3 GeV

□ The dominant experimental uncertainties (still!) come from the beam energy knowledge

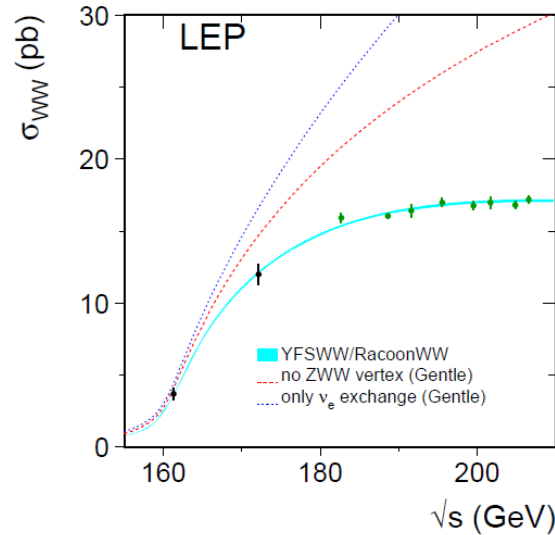
FCC-ee Precision EW Physics Measurements (2)

- EW precision measurements at FCC-ee (see [arXiv:1308.6176](https://arxiv.org/abs/1308.6176) and CDR)

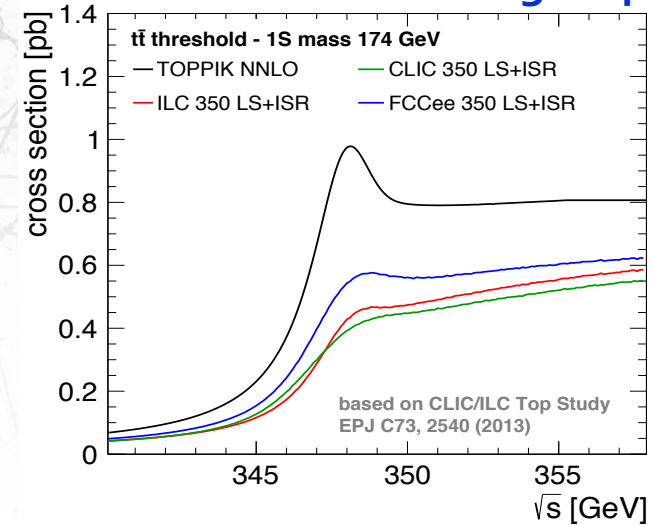
Z resonance: TeraZ



WW threshold scan: OkuW



tt threshold scan: MegaTop



Lineshape

- Exquisite E_{beam} (unique!)
- m_Z, Γ_Z to < 100 keV (2.2 MeV)

Asymmetries

- $\sin^2\theta_W$ to 6×10^{-6} (1.6×10^{-4})
- $\alpha_{\text{QED}}(m_Z)$ to 3×10^{-5} (1.5×10^{-4})

Branching ratios R_l, R_b

- $\alpha_S(m_Z)$ to 0.0002 (0.002)

Threshold scan

- m_W to 0.6 MeV (12 MeV)

Branching ratios R_l, R_b

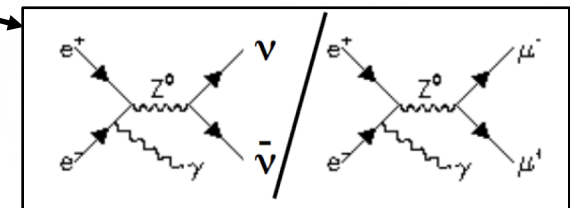
- $\alpha_S(m_W)$ to 0.0002

Radiative return $e^+e^- \rightarrow Z\gamma$

- N_ν to 0.001 (0.008)

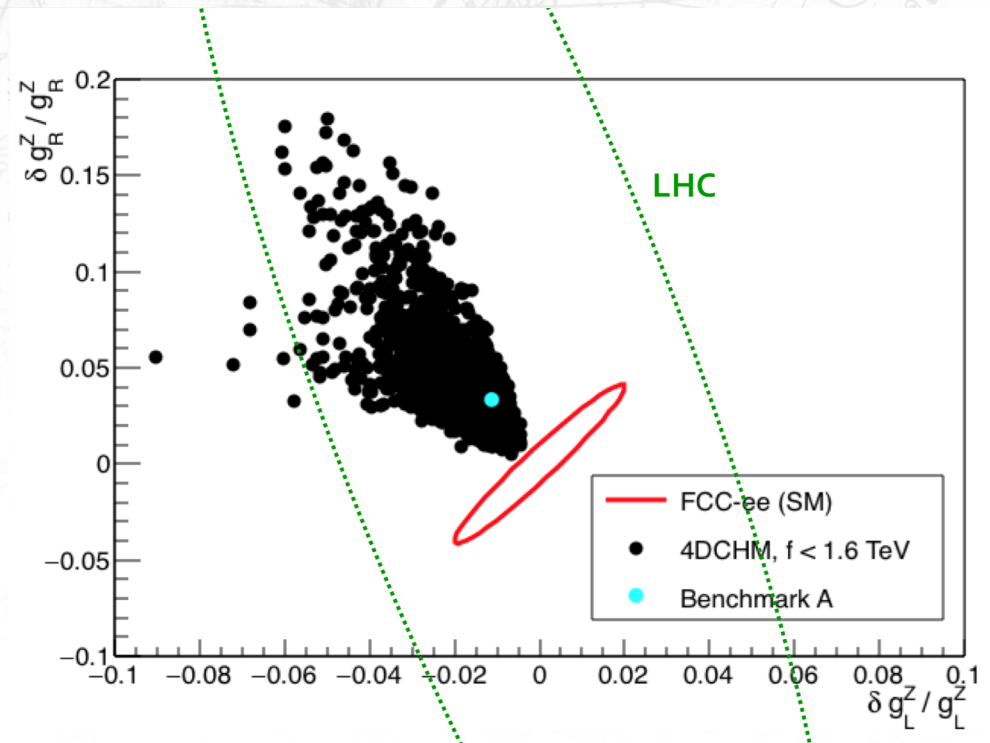
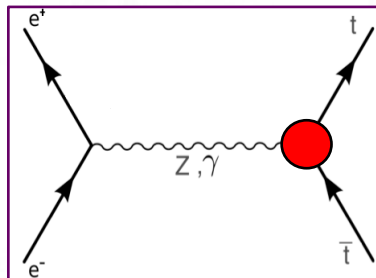
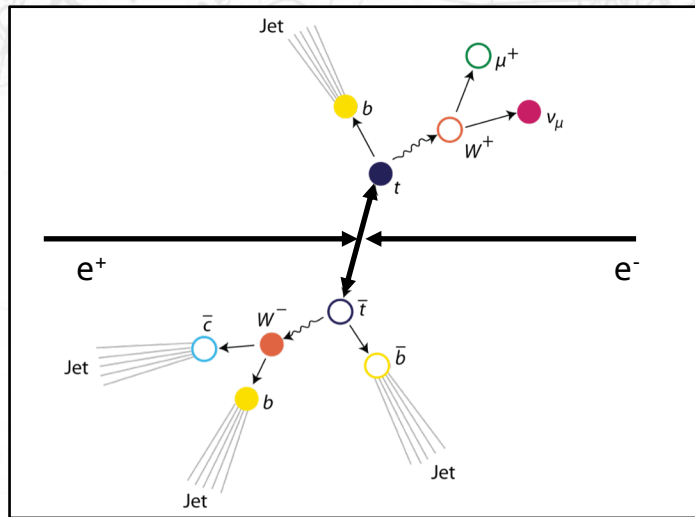
Threshold scan

- m_{top} to 20 MeV (500 MeV)
- λ_{top} to 10%
- EW couplings to 2%



FCC-ee Precision EW Physics Measurements (3)

- ◆ Measurements of $t_L t_L Z$ and $t_R t_R Z$ couplings, g_L and g_R
 - At FCC-ee@365 GeV, couplings extracted from “top polarization measurement”: Leptons and b-jet distributions
 - Couplings sensitive to, e.g., composite Higgs models



FCC-ee EW Measurements: Summary of Precisions

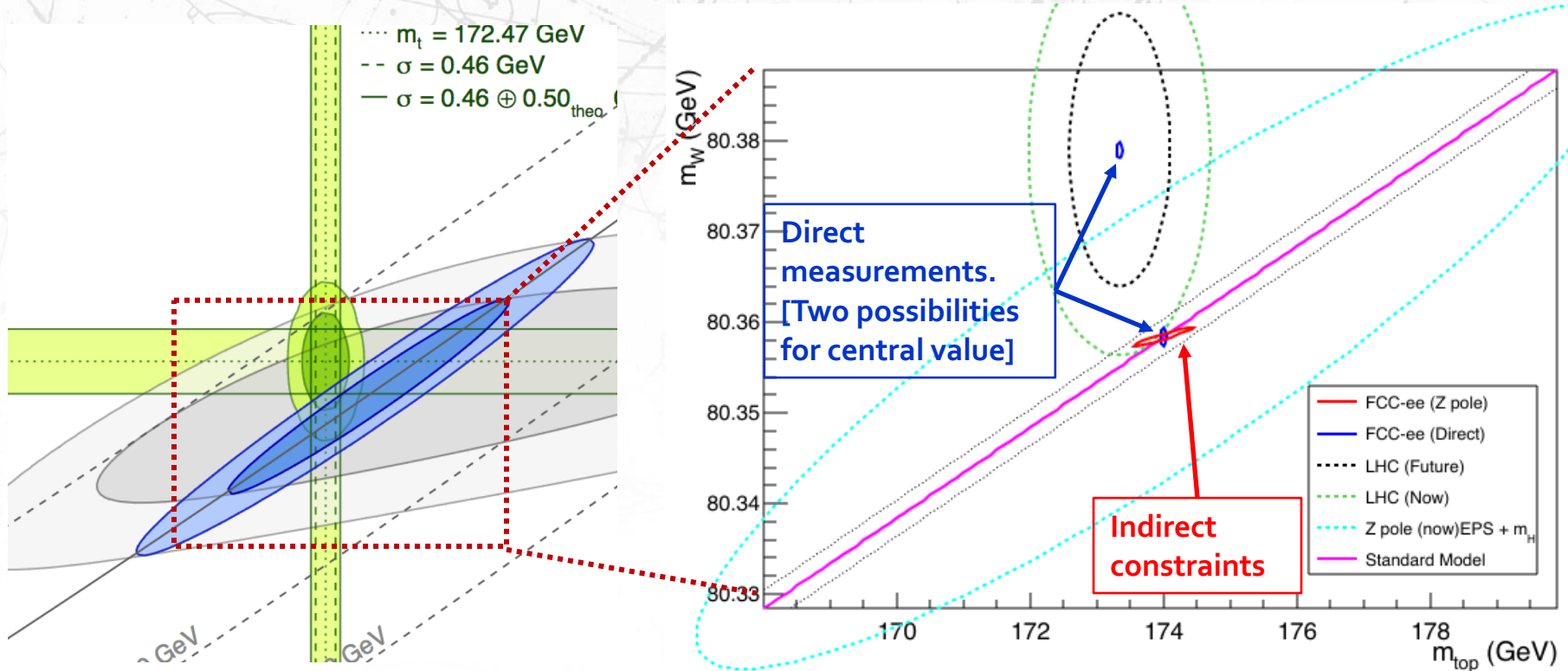
Observable	Measurement	Current precision	FCC-ee stat.	FCC-ee syst.	Challenge
m_Z (keV)	Z lineshape	91186700 \pm 2200	5	100	Beam energy calib
Γ_Z (keV)	Z lineshape	2495200 \pm 2300	8	100	Beam energy calib
R_l ($\times 10^3$)	Ratio of hadrons to leptons	20767 \pm 25	0.01	0.2-1	Acceptance for leptons
$\alpha_s(m_Z)$ ($\times 10^4$)	From R_ℓ	1196 \pm 30	0.1	0.4-1.6	ditto
R_b ($\times 10^6$)	Ratio of bb to hadrons	216290 \pm 660	0.3	< 60	$g \rightarrow bb$
N_ν ($\times 10^3$)	Peak hadronic cross section	2991 \pm 7	0.005	< 1	Lumi meast
$\sin^2\theta_W^{\text{eff}}$ ($\times 10^6$)	From $A_{\text{FB}}^{\text{had}}$ at Z peak	231480 \pm 160	3	2-5	Beam energy calib
$1/\alpha_{\text{QED}}(m_Z)$ ($\times 10^3$)	From $A_{\text{FB}}^{\text{had}}$ off-peak	128952 \pm 14	4	small	QED corr.
$A_{\text{FB}}^{\text{pol},\tau}$ (10^4)	τ polarization charge assym	1498 \pm 49	0.15	< 2	τ decay physics
m_W (MeV)	WW threshold scan	80385000 \pm 15000	600	300	Beam energy calib
N_ν	$e^+e^- \rightarrow \gamma Z, Z \rightarrow \nu\nu, \ell\ell$	2.92 \pm 0.05	0.001	< 0.001	?
$\alpha_s(m_W)$ ($\times 10^4$)	From R_ℓ^W	1170 \pm 420	3	small	Lepton acceptance
m_{top} (MeV)	tt threshold scan	172740 \pm 500	20	small	QCD corr
Γ_{top} (MeV)	tt threshold scan	1410 \pm 190	40	small	QCD corr
$\lambda_{\text{top}} / \lambda_{\text{top}}^{\text{SM}}$	tt threshold scan	1.2 \pm 0.3	0.08	small	QCD corr

Extremely Precise EW Consistency Checks

- ◆ Combination of all precision electroweak measurements

- FCC-ee precision allows m_{top} , m_W , $\sin^2\theta_W$ to be predicted within the SM

- ❖ ... and to be compared to the direct measurements



- New Physics ?

- ❖ Direct measurement (blue ellipse) and indirect constraints (red ellipse) may or may not overlap

SMEFT Fit to FCC-ee EW Measurements

◆ Higher-dimensional operators as a parametrization of new physics

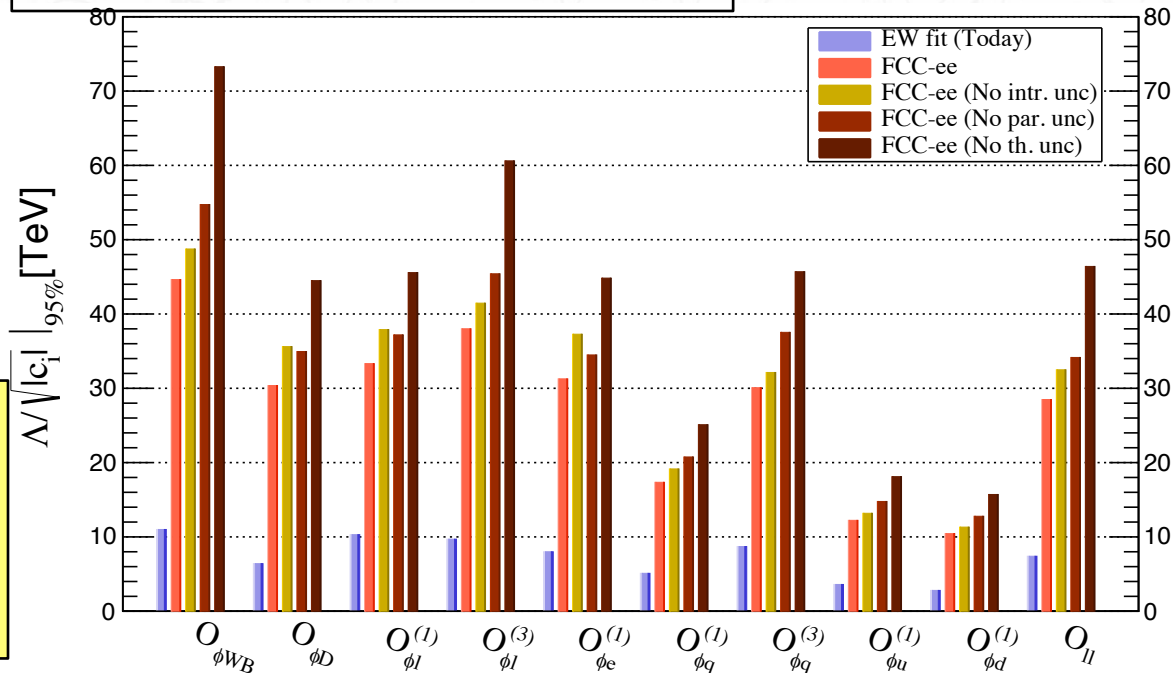
□ Possible corrections to the Standard Model

❖ Standard Model Effective Theories (SMEFT)

$$\mathcal{L}_{\text{SMEFT}} = \underbrace{\mathcal{L}_{\text{SM}}}_{\text{Standard Model}} + \sum_i \underbrace{\frac{c_i}{\Lambda^2}}_{\text{Dimension-6 operators}} \mathcal{O}_i$$

~scale of new decoupled physics

Electroweak precision measurements



Limits on new physics scale, Λ :

Today:
 $\Lambda > 4-10 \text{ TeV}$

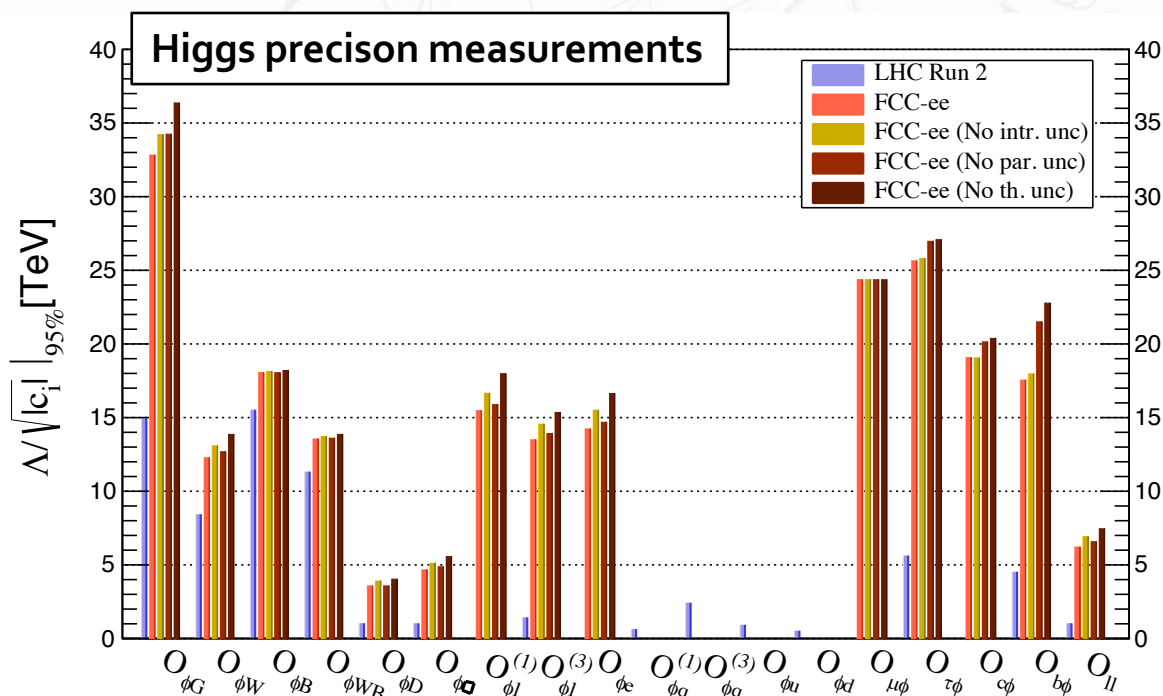
Sensitivity to new physics scale, Λ :

After FCC-ee:
 $\Lambda > 20-70 \text{ TeV}$

SMEFT Fit to FCC-ee Higgs Measurements

- ◆ Interpret also precisely measured Higgs couplings (Lecture 1) in terms of higher-dimension operators

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \sum_i \frac{c_i}{\Lambda^2} \mathcal{O}_i$$



Limits on new physics scale, Λ :

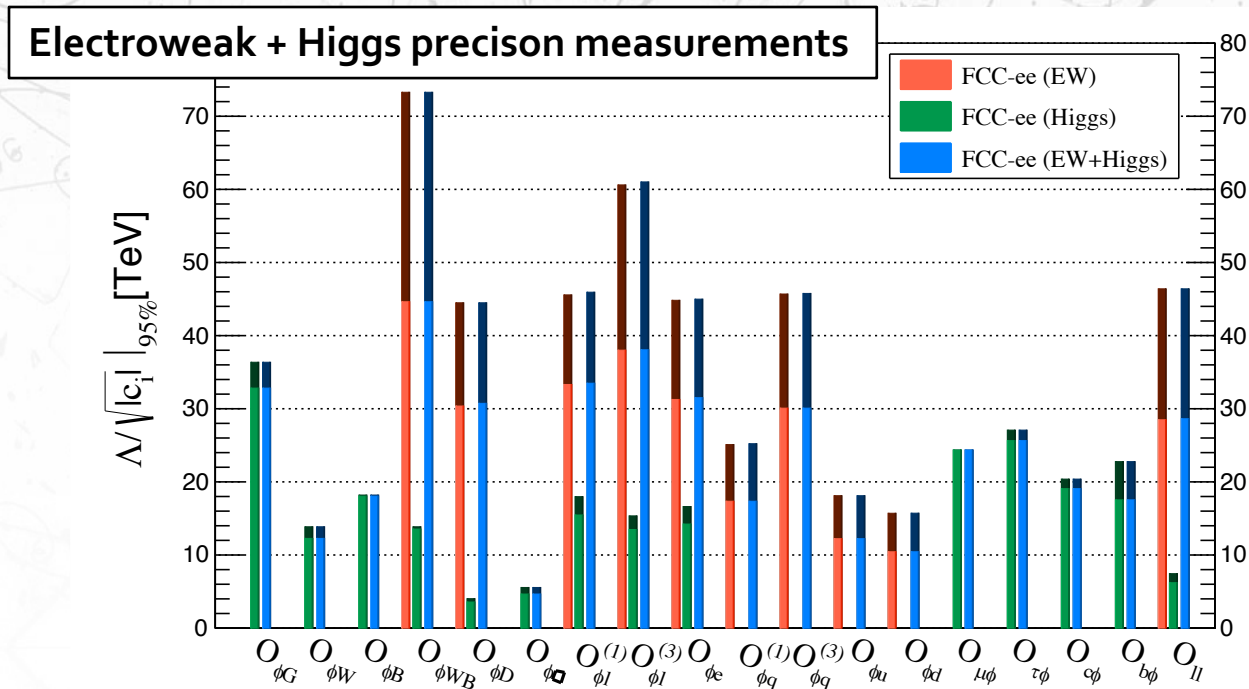
Today:
 $\Lambda > 1-15$ TeV

Sensitivity to new physics scale, Λ :

After FCC-ee:
 $\Lambda > 1-35$ TeV

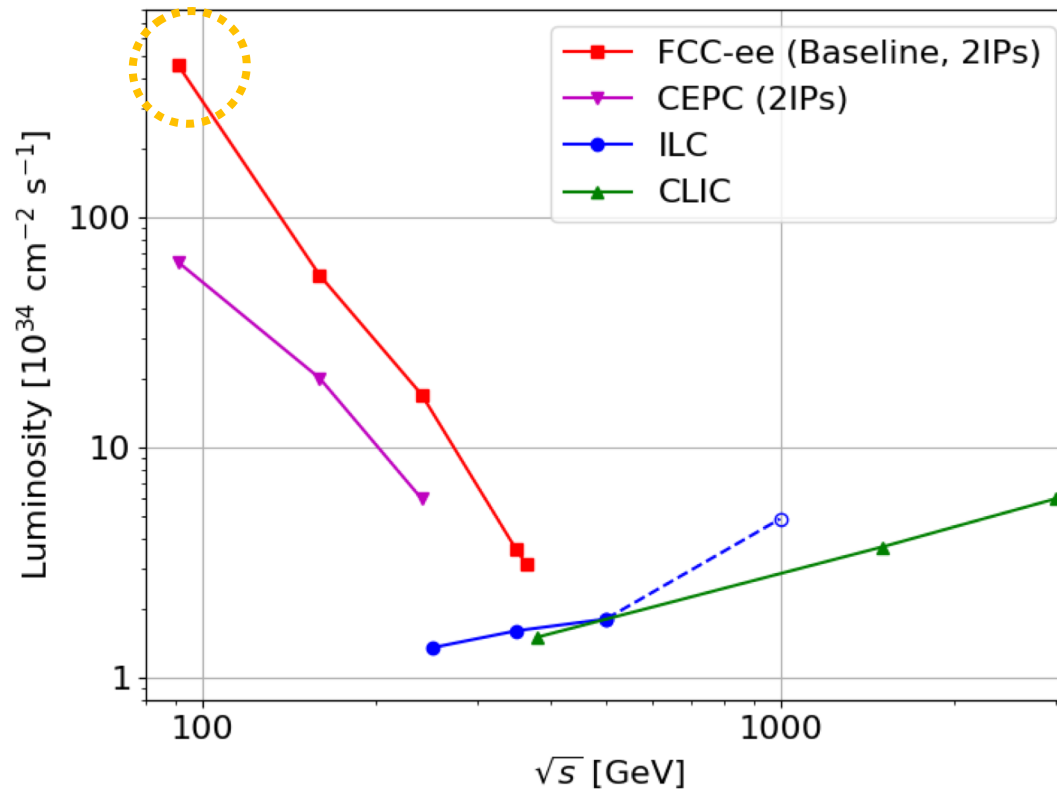
Combined FCC-ee SMEFT Fit

- ◆ Combine EW precision observables with precise Higgs coupling measurements via higher-dimensional operators



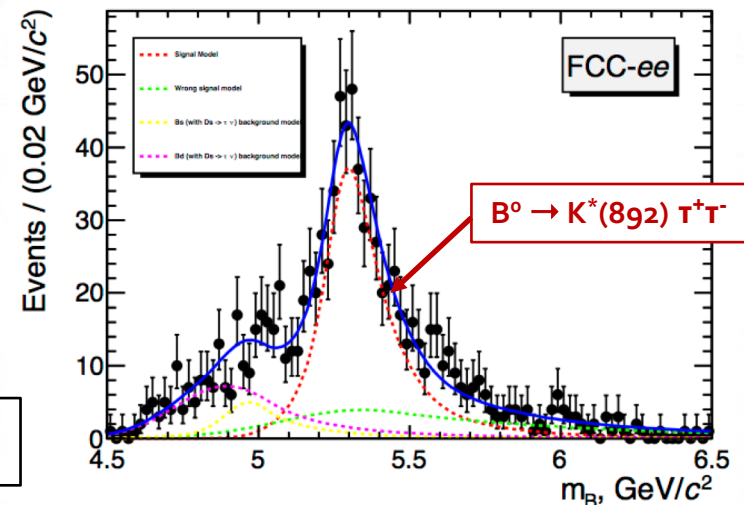
- The EW and Higgs measurements are highly complementary
 - ❖ Together they provide precise constraints on a large number of operators
 - ❖ Different New Physics models give different pattern of deviations from SM
 - Pattern provides fingerprint to differentiate among models

GigaZ Physics: Flavour Physics and Direct Discoveries



Flavour Physics at FCC-ee

- ◆ 5×10^{12} Z decays: 10^{12} $b\bar{b}$ events, 1.7×10^{11} $\tau^+\tau^-$ events
 - FCC-ee is also the ultimate factory for the study of (heavy) flavours
 - ❖ lifetime, branching fractions, rare decays, test of Universality
- ◆ Example from b-physics:
 - Current tensions (several 2–3 σ deviations) of LHCb data with SM predictions
 - ❖ In particular, lepton flavour universality is challenged in $b \rightarrow s \ell^+\ell^-$ transitions
 - For example, the rates of $B^0 (B^+) \rightarrow K^{*0} (K^+) \ell^+\ell^-$ are different for $\ell = e$ and $\ell = \mu$
 - Differences are also observed in the lepton angular distributions
 - ❖ This effect, if real, could be enhanced for $\ell = \tau$, in $B \rightarrow K^{(*)} \tau^+\tau^-$
 - With 10^{12} $Z \rightarrow b\bar{b}$, FCC-ee is beyond any foreseeable competition
 - Decay can be fully reconstructed
 - Full angular analysis possible



J.F. Kamenik et al.
[arXiv:1705.11106](https://arxiv.org/abs/1705.11106)

τ physics

τ Properties and Universality

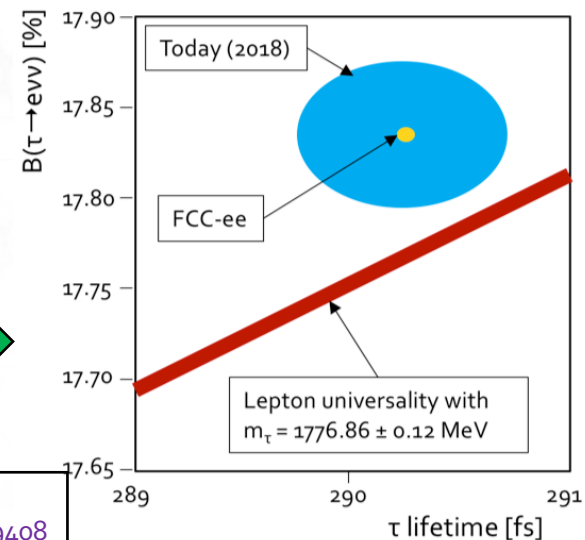
◆ τ branching fractions and lifetime provide strong test of Universality of the α - ν_α CC coupling, $\alpha = e, \mu, \tau$

- Sensitive to light-heavy neutrino mixing
- Need also (more) precise mass measurement

Observable	Current precision	FCC-ee stat.	Possible syst.
m_τ [MeV]	1776.86 ± 0.12	0.004	0.1
τ_τ [fs]	290.3 ± 0.5 fs	0.001	0.04
$B(\tau \rightarrow e\nu\nu)$ [%]	17.82 ± 0.05	0.0001	0.003
$B(\tau \rightarrow \mu\nu\nu)$ [%]	17.39 ± 0.05		



Quantity	Measurement	Current precision	FCC-ee precision
$ g_\mu/g_e $	$\Gamma_{\tau \rightarrow \mu} / \Gamma_{\tau \rightarrow e}$	1.0018 ± 0.0014	Improvement by a factor 10 or more
$ g_\tau/g_\mu $	$\Gamma_{\tau \rightarrow e} / \Gamma_{\mu \rightarrow e}$	1.0030 ± 0.0015	



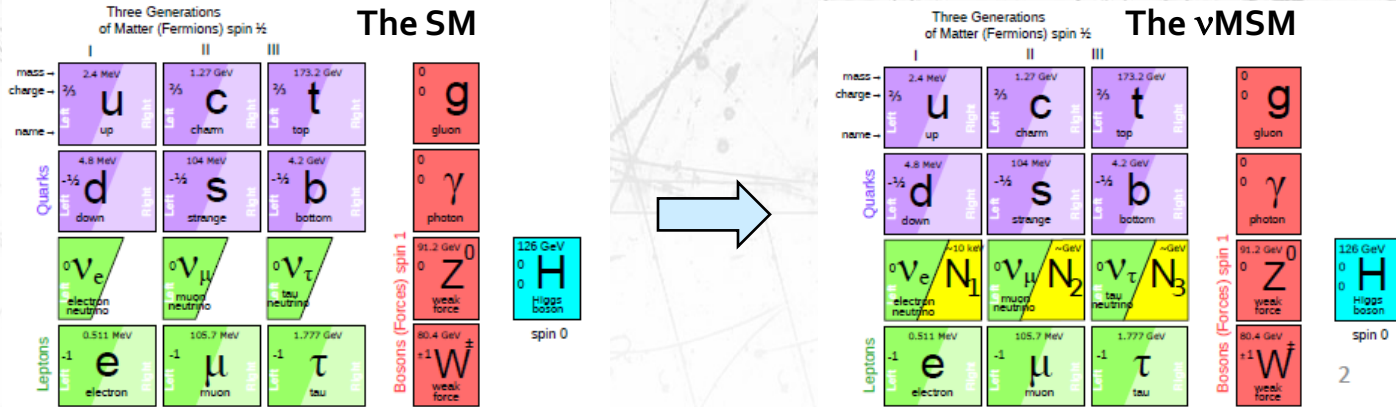
M.Dam
arXiv:1811.09408

Visible Z decays	3×10^{12}
$Z \rightarrow \tau^+\tau^-$	1.3×10^{11}
1 vs. 3 prongs	3.2×10^{10}
3 vs. 3 prong	2.8×10^9
1 vs. 5 prong	2.1×10^8
1 vs. 7 prong	$< 67,000$
1 vs 9 prong	?

Direct discoveries from Z decays

◆ Discover right-handed neutrinos

□ **vMSM** : Complete particle spectrum with the missing three right-handed neutrinos

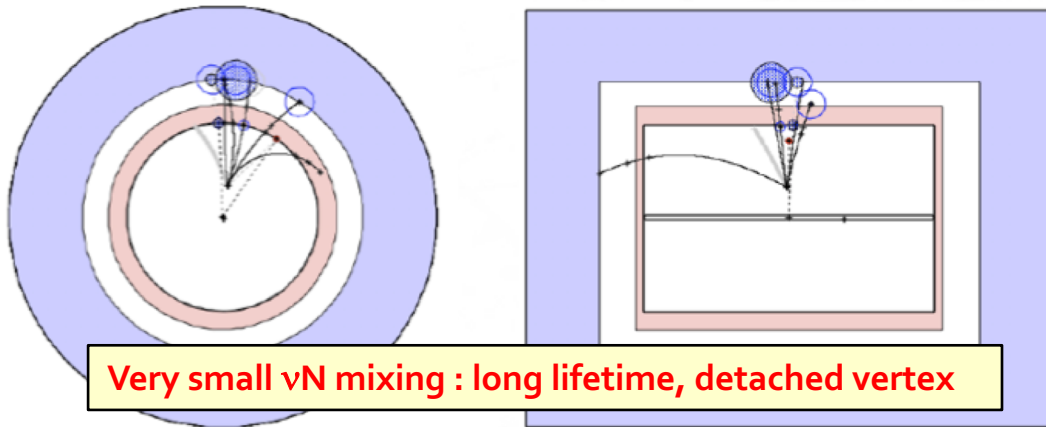


◆ Could explain everything: Dark matter (N_1), Baryon asymmetry, Neutrino masses

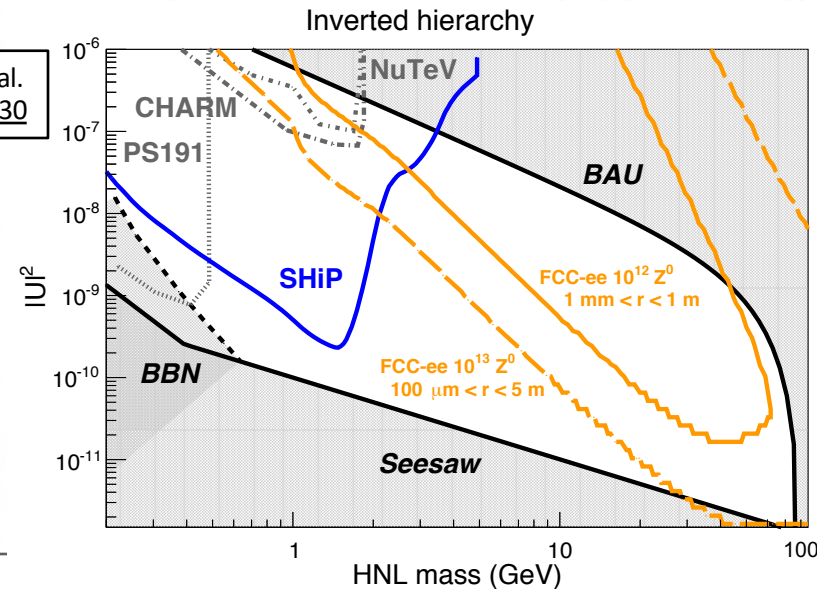
□ Searched for in very rare $Z \rightarrow \nu N_{2,3}$ decays

◆ Followed by $N_{2,3} \rightarrow W^* \ell$ or $Z^* \nu$

A. Blondel et al.
arXiv:1411.5230



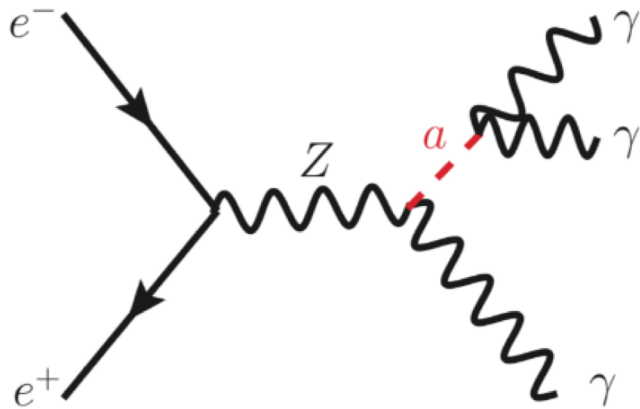
Physics at Lepton Colliders



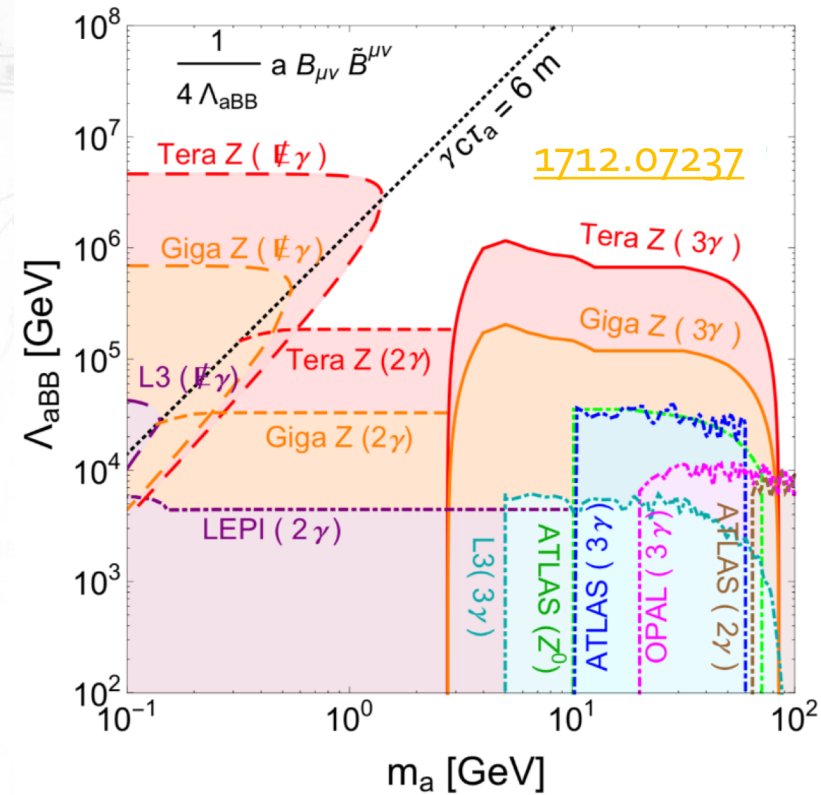
Direct discoveries (cont'd)

◆ Discover the dark sector

- A very-weakly-coupled window to the dark sector is through light "Axion-Like Particles" (ALPs)



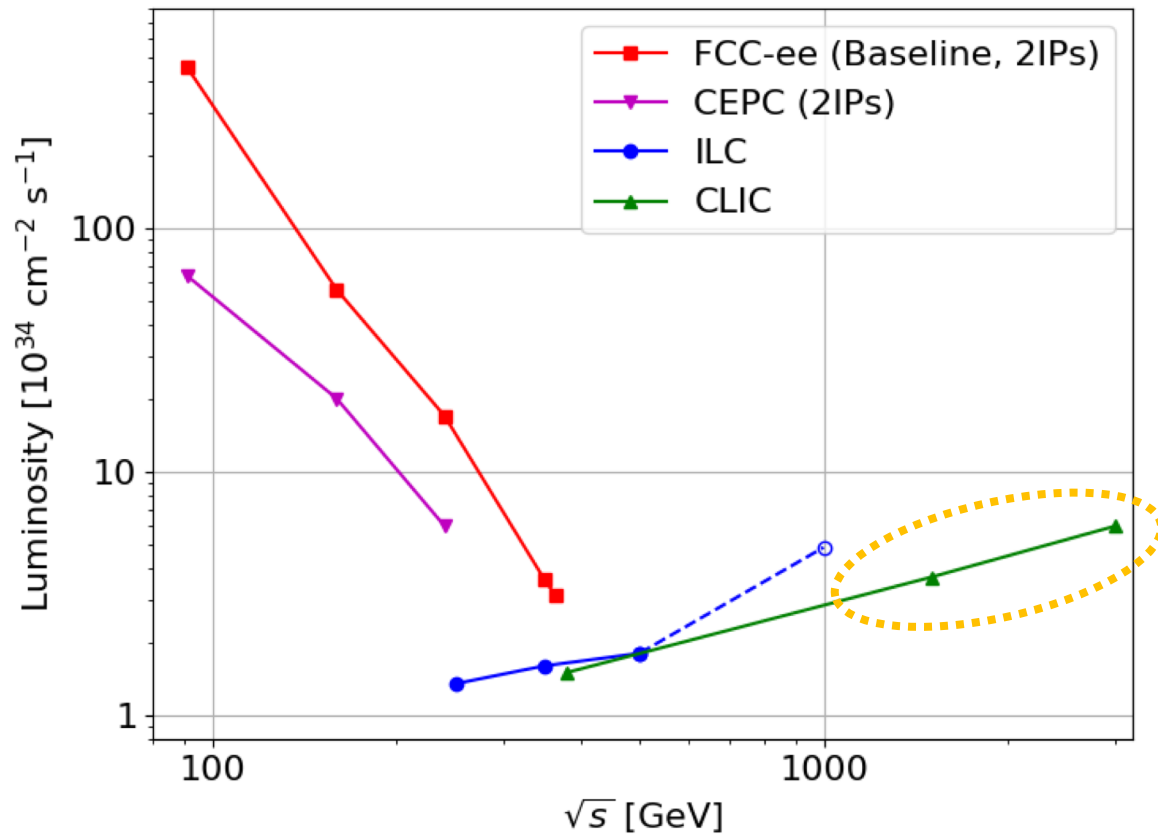
- $\gamma + E_{\text{MISS}}$ for very light a
- $\gamma\gamma$ for light a
- $\gamma\gamma\gamma$ for heavier a



◆ Orders of magnitude of parameter space accessible at FCC-ee

Lecture 2

High Energy e^+e^- Physics CLIC



Precision: Higgs properties at high energy (1)

◆ Why do precision Higgs physics at high \sqrt{s} ?

▣ Precision achieved with e^+e^- colliders at $\sqrt{s}=240-500$ GeV : 0.1% - 1%

◆ Superior to what can be done at higher energy

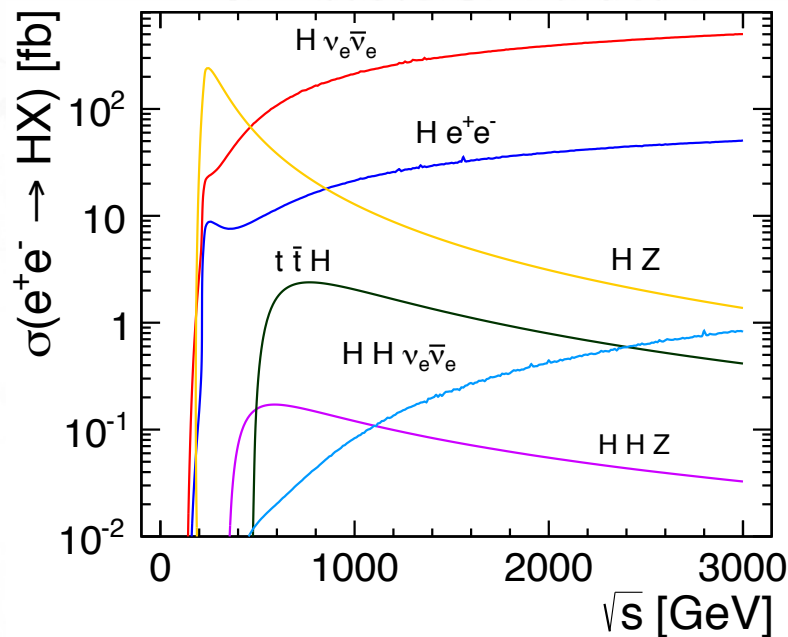
▪ σ_{HZ} decreases, kinematics less favourable, backgrounds increase, ...

◆ However ...

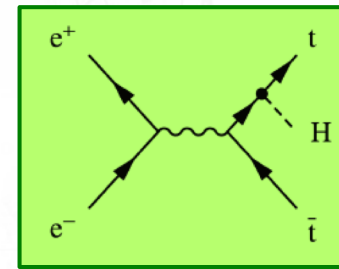
▣ Some production processes are not directly accessible at low-energy e^+e^- colliders

◆ Hence more couplings might become measurable at larger energy

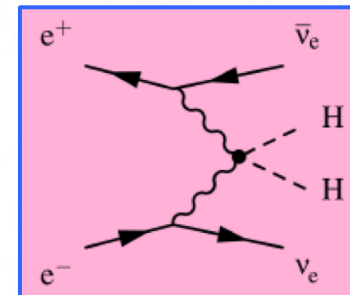
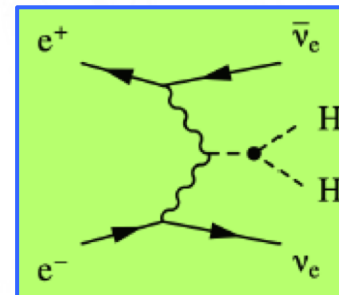
▪ Htt , HHH , $HHHH$, ...



Htt
 $\sqrt{s} > 500$ GeV



HHH
 $\sqrt{s} > 1$ TeV



Background

Precision: Higgs properties at high energy (2)

◆ Achievable precisions

Collider	HL-LHC	CLIC ₃₀₀₀	FCC-ee	FCC-ee+hh
$\Delta g_{Htt}/g_{Htt}$	3%	2.6%	10% (*)	1%
$\Delta g_{HHH}/g_{HHH}$	50%	$^{+11}_{-7}$ %	19%	5%

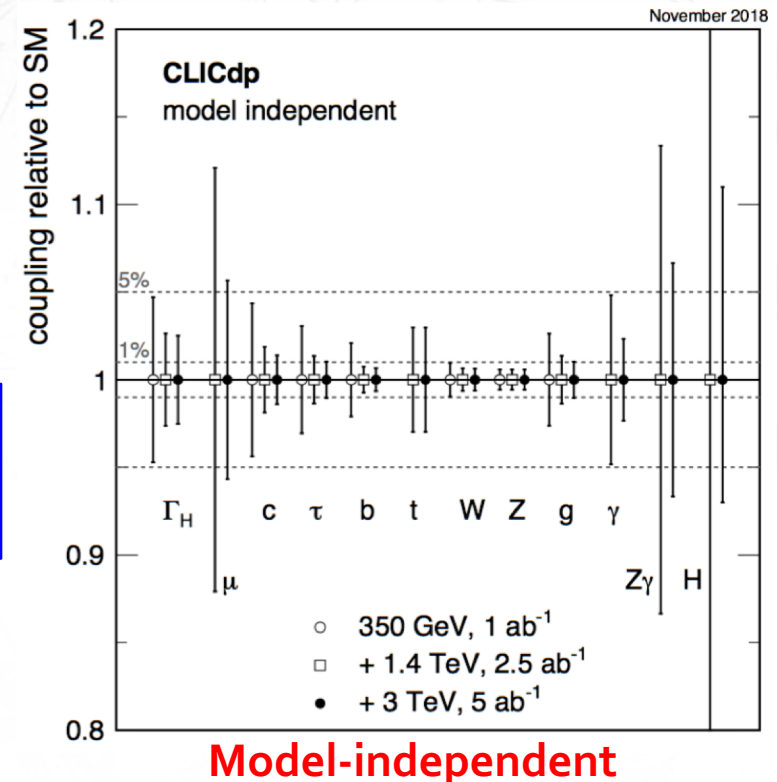
(*) indirect

◆ Combined CLIC Higgs results

□ 380 GeV; 1.5 TeV, 3.0 TeV

Full CLIC program, ~27 yrs of running in total

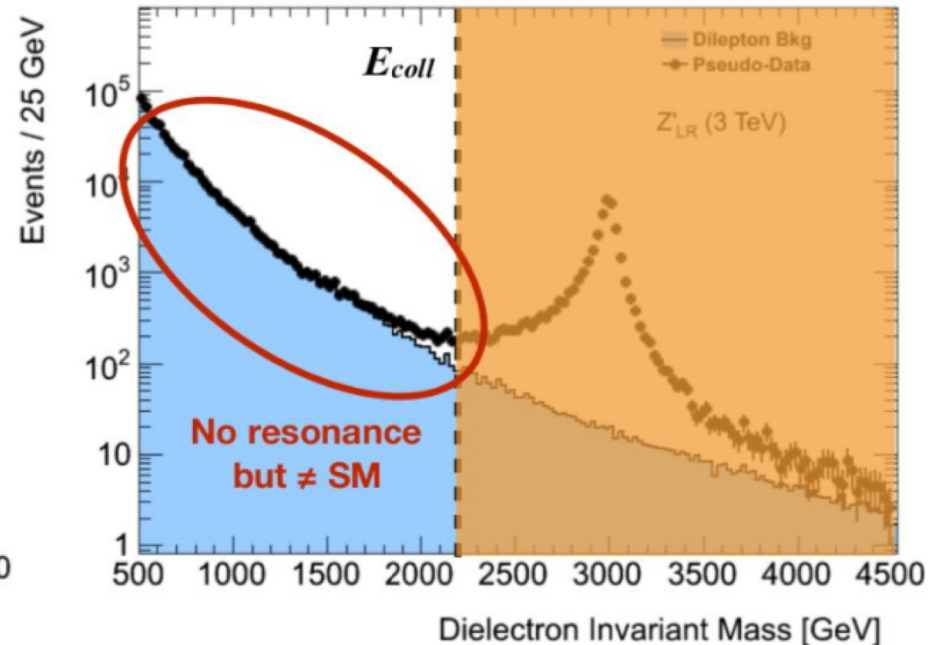
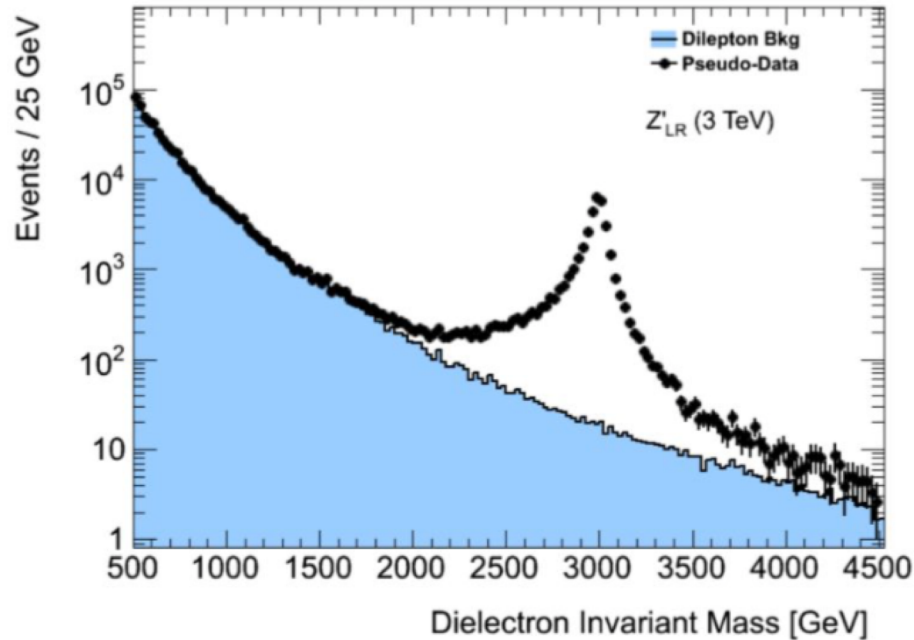
- Precision of $\mathcal{O}(1\%)$ for most couplings
- Accuracy on Higgs width: $\pm 1.6\%$



High-mass searches: peak vs. mass tails

Example: Z' at 3 TeV

accelerator only goes to $\sqrt{s} = 2.2$ TeV



- ◆ Seeing the “peak”. Mass reach:
 - mass $< \sqrt{s}$ for lepton colliders
 - mass $\lesssim 0.3-0.5 \sqrt{s}$ at hadron for couplings \sim weak couplings

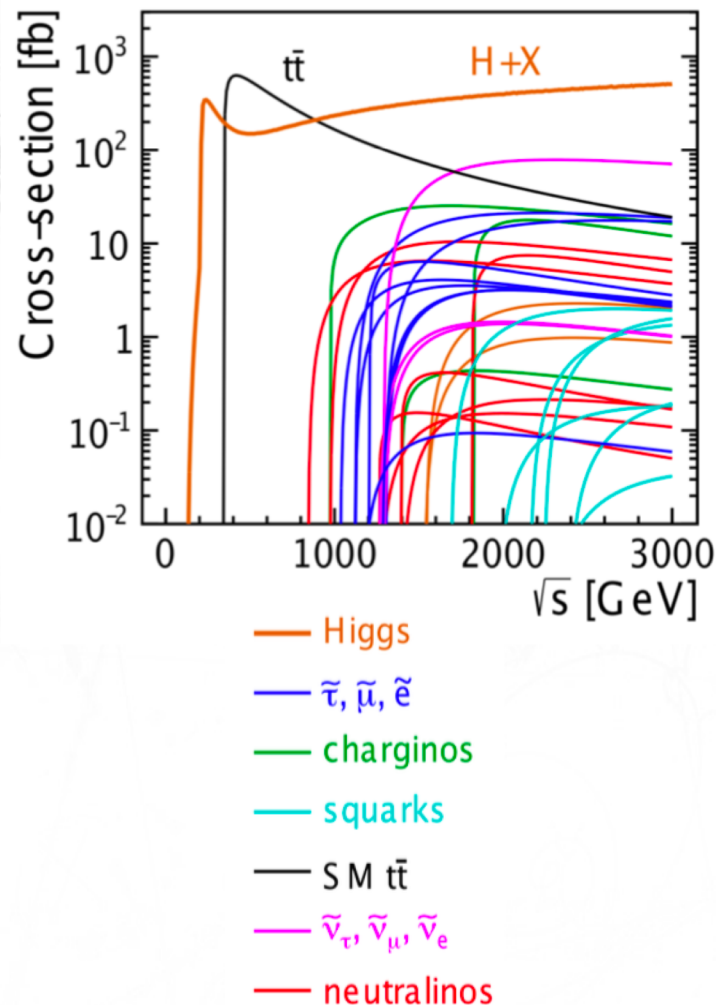
- ◆ Deviations in high-mass tails:
 - Very well suited for lepton colliders; sensitive to $[\text{mass/couplings}] \gg \sqrt{s}$

Direct BSM sensitivity – Example SUSY

“model III”

• smuons, selectrons,
staus, gauginos

- ◆ Unique opportunity to directly probe new particles with masses up to 1.5 TeV
- ◆ Direct observation of particles coupling to $\gamma^*/Z/W$
 - precision measurement, $\mathcal{O}(1\%)$, of new particle masses and couplings
- ◆ Wider capability than only SUSY: reconstructed particles can be interpreted as “states of given mass, spin and quantum numbers”
- ◆ Very rare processes accessible due to low backgrounds
 - CLIC especially suited for electroweak states
- ◆ Polarised electron beam and threshold scans may be useful to constrain the underlying theory



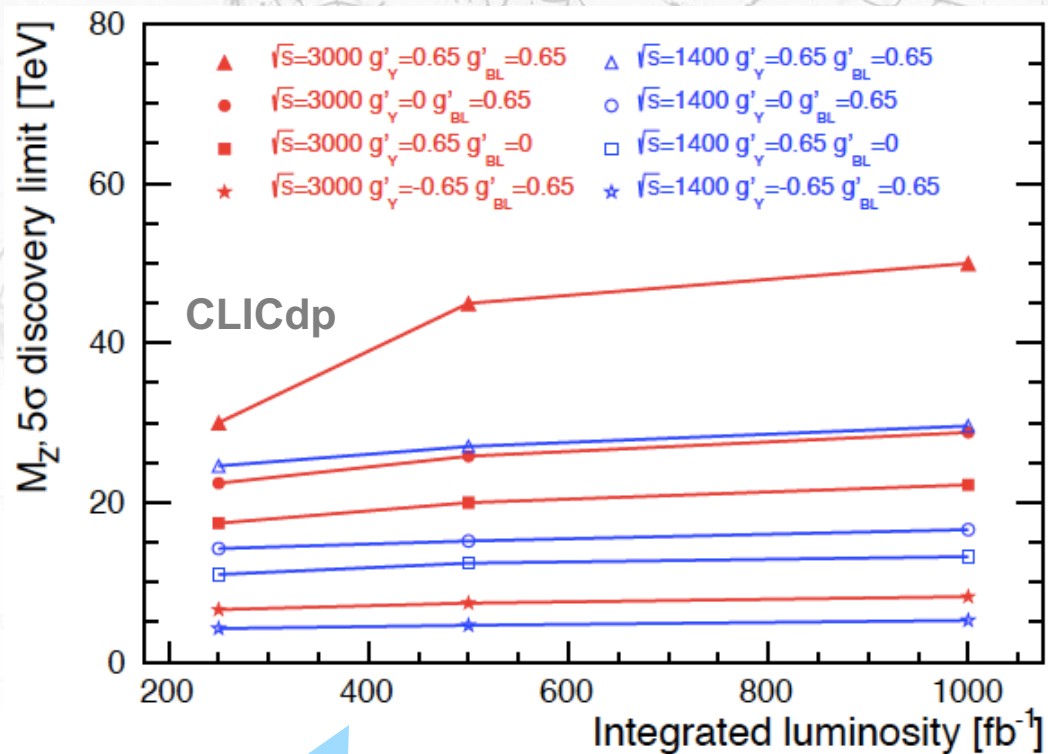
BSM example: Z' sensitivity

Minimal anomaly-free Z' model

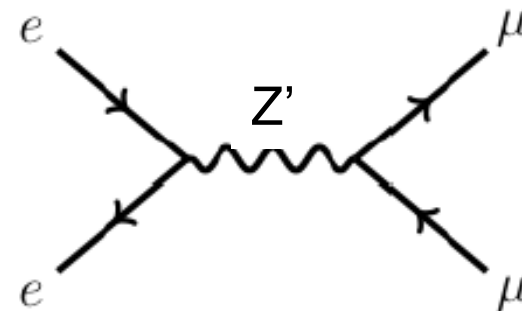
$$Q_f = g_Y'(Y_f) + g'_{BL}(B-L)_f$$

Observables:

- Total $e^+e^- \rightarrow \mu^+\mu^-$ cross section
- Forward-backward asymmetry
- Left-right asymmetry
(with $\pm 80\%$ e^- polarisation)



- ◆ If LHC discovers Z' (e.g. for $M_{Z'} = 5$ TeV)
 - CLIC precision measurement of effective couplings
- ◆ Otherwise:
 - CLIC discovery reach up to tens of TeV
(depending on the couplings)



CLIC Global Sensitivity to BSM Effects

Standard Model

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \sum_i \frac{c_i}{\Lambda^2} \mathcal{O}_i$$

Scale of new decoupled physics Λ^2

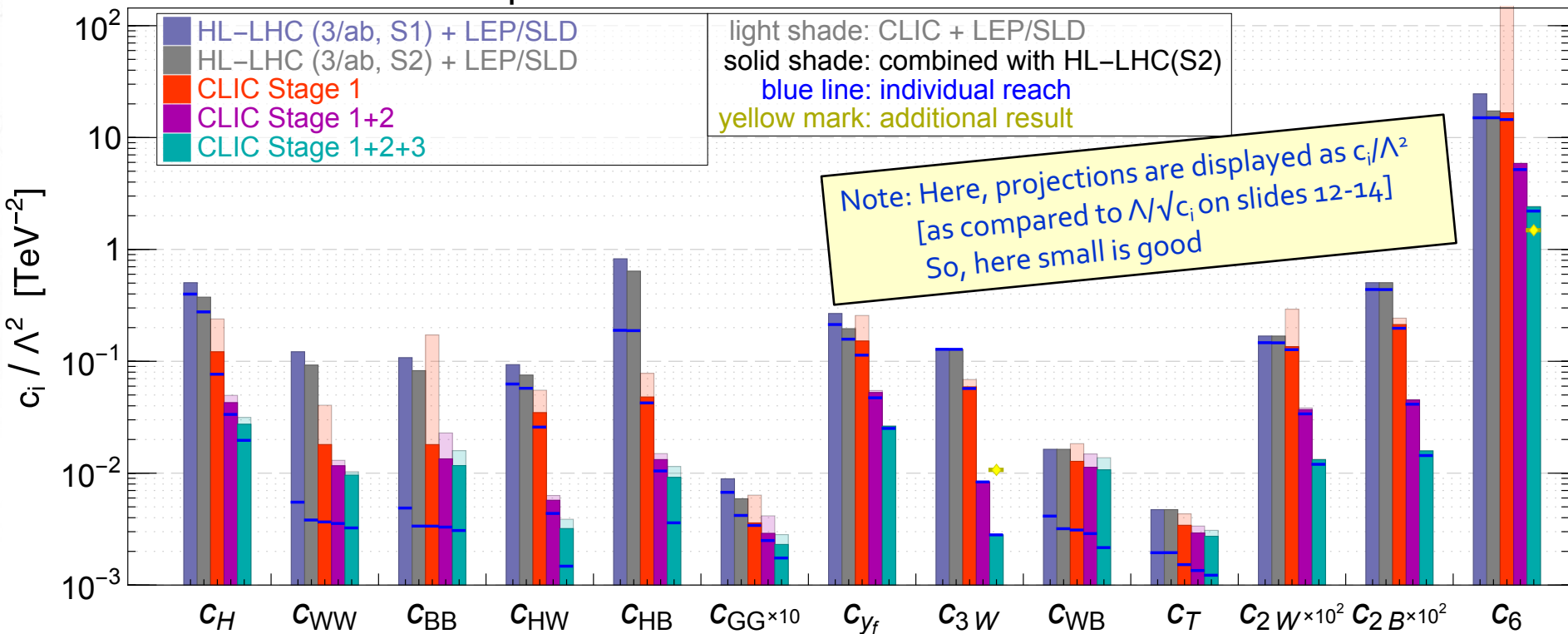
Dimension-6 operators \mathcal{O}_i

Includes CLIC measurements of:

- ◆ Higgs
- ◆ Top
- ◆ WW
- ◆ $e^+e^- \rightarrow f\bar{f}$

Universal EFT fit

Strong benefits from high-energy running

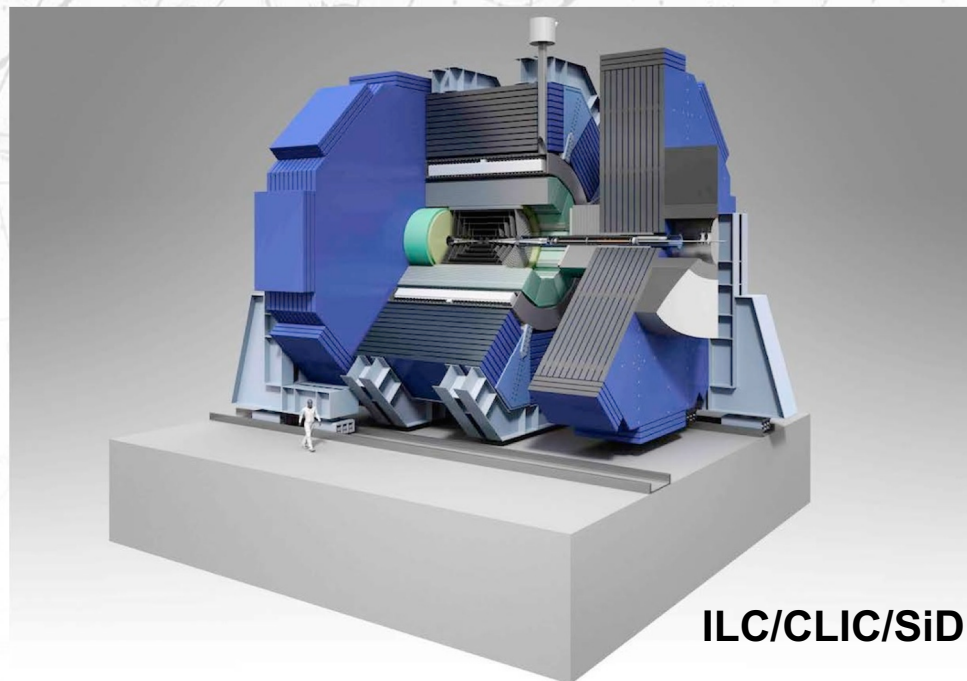
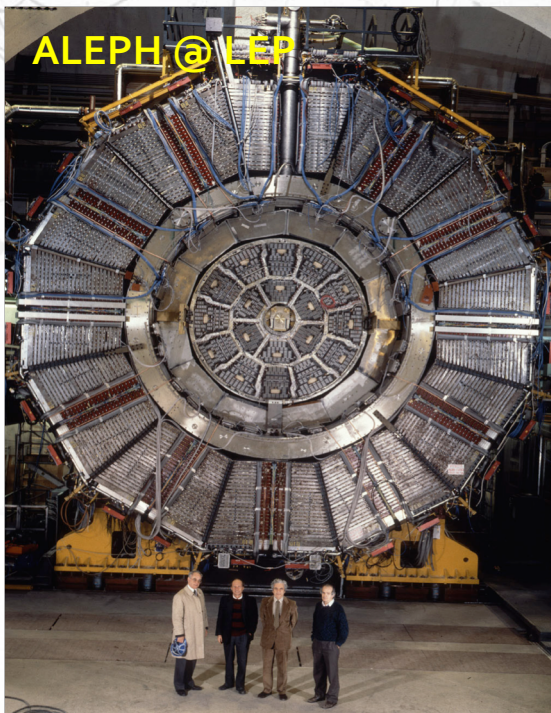


Lecture 2

Instrumentation **Detectors for e^+e^- physics**

Detectors e⁺e⁻ colliders

- ◆ We know today how to build a detector for e⁺e⁻ precision physics
 - Experience with LEP detectors and 20-years R&D with ILC/CLIC detectors



- Compared to LHC, less challenging w.r.t. radiation damage, pile-up, etc.
- However, need ultimate systematic precision to match the formidable statistical precision
 - ❖ Remember, up to 6×10^{12} Z decays

Typical Modern e^+e^- Detector

B-field: 2-5 Tesla

- Limited to 2 Tesla at FCC-ee due to the 30 mrad crossing angle

Calorimetry:

- Jet energy (1/3 x LEP)

$$\frac{\sigma_E}{E} \approx 3 - 4\%$$

Momentum: (1/10 x LEP)

$$\sigma_{1/p} < 5 \times 10^{-5} \text{ GeV}^{-1}$$

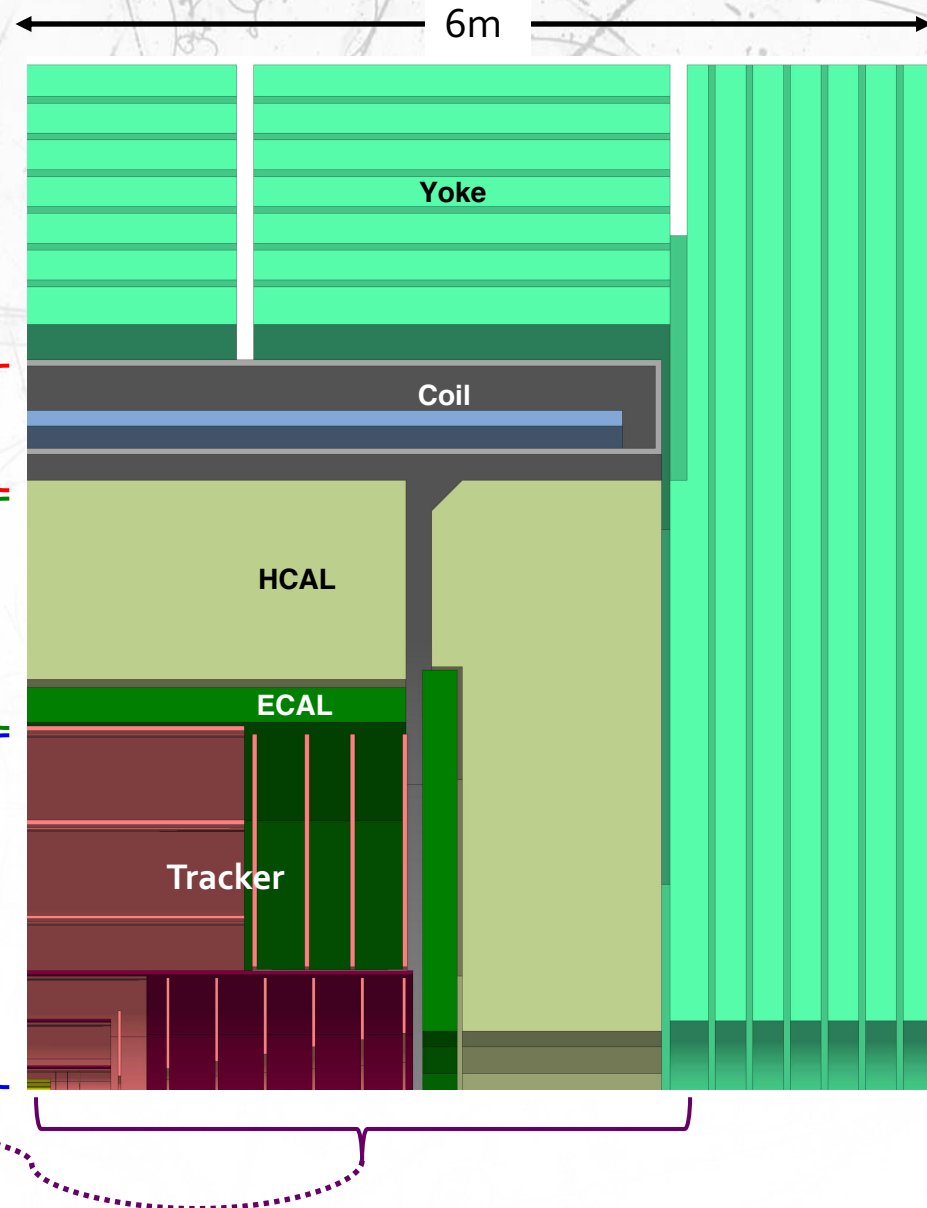
Impact parameter: (1/3 x SLD)

- e.g. b/c-tagging

$$\sigma_{r\phi} = 5 \oplus 10 / (p \sin^2 \theta) \mu\text{m}$$

Hermetic: down to $\theta \approx 5$ mrad

- Not possible with 30 mrad crossing angle, however

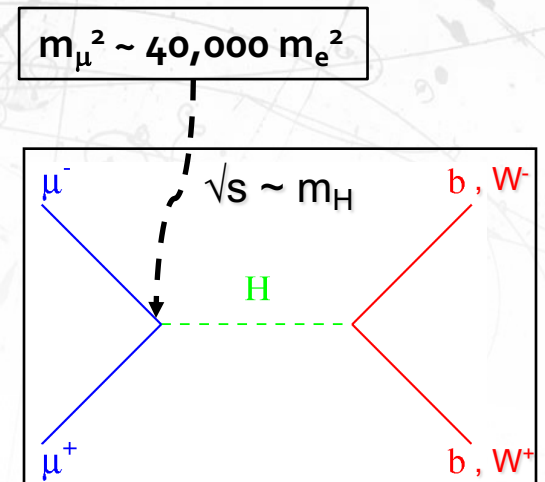


Lecture 3 (2nd part)

Thinking out of the box Muon Colliders

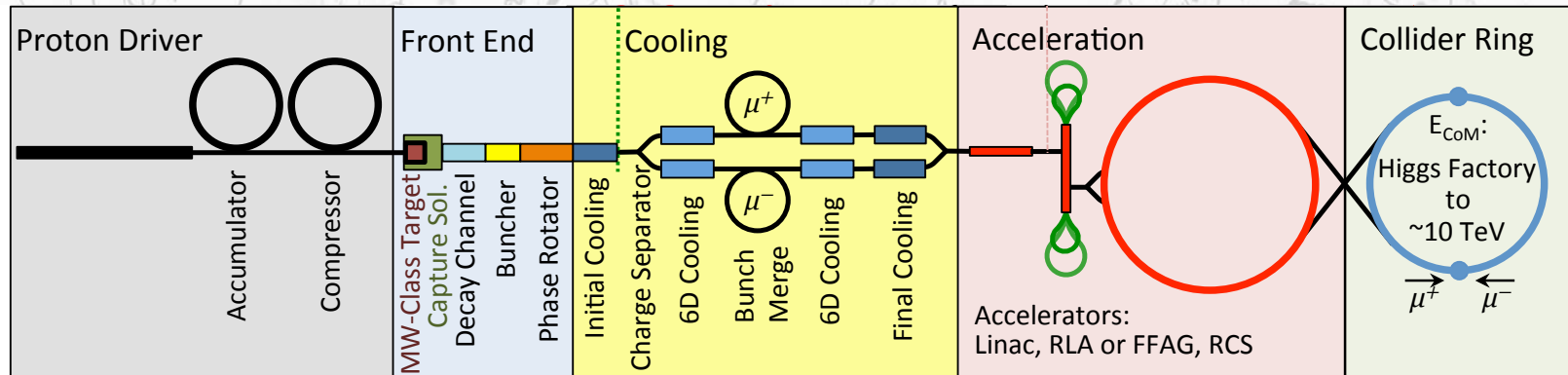
Why muon colliders ?

- ◆ Muons are leptons (like electrons)
 - Collisions at the full energy, small physics background, (E,p) conservation
 - ❖ Muons can *a priori* do all what electrons can do
- ◆ Muons are heavy (like protons)
 - Negligible synchrotron radiation, no beamstrahlung
 - ❖ Small circular colliders, up to large \sqrt{s}
 - ❖ Excellent energy definition (up to a few 10^{-5})
 - Large direct coupling to the Higgs boson
 - ❖ Unique s-channel Higgs factory at $\sqrt{s} = 125.093$ GeV
- ◆ Muons are naturally longitudinally polarized (100%)
 - Because arising from π^\pm decays to $\mu^\pm \nu_\mu$
 - ❖ Ultra-precise beam energy and beam energy spread measurement
- ◆ Muons eventually decay (in $2.2 \mu\text{s}$) to $e \nu_\mu \bar{\nu}_e$
 - Outstanding neutrino physics programme
 - ❖ Muon colliders could be the natural successors of neutrino factories ?



Muon colliders challenges

- ◆ Muons decay: Produce, Collect, Cool, Accelerate and Collide them *fast* !



- Intense proton driver to get the adequate number of muons
 - ❖ At least 4 MW for the desired muon luminosities
- Robust target to not evaporate at the first proton bunch
 - ❖ Re-circulating liquid metal
- Efficient muon collector from pion decays
 - ❖ Magnetic fields of 20T
- Unique 6D muon cooling
 - ❖ To reduce beam sizes and beam energy spread
- Fast acceleration and injection into circular ring(s)

All these aspects are at the level of intense R&D. Will require decades to demonstrate feasibility

Muon collider challenges since 2014 ?

◆ Clever alternative muon source



- Intense e^+ beam with $E \approx 45$ GeV
 - ❖ 100 kW for the desired muon intensity
- Non-destructive target for $e^+e^- \rightarrow \mu^+\mu^-$
 - ❖ Keep the e^+ beam in a ring
 - Possible synergy with FCC-ee
 - Energy Recovery Linac is also a possibility
- Production at $\mu^+\mu^-$ threshold ($\sqrt{s} \approx 2 m_\mu$)
 - ❖ Quasi-monochromatic muons, much less need for cooling
 - Except for a Higgs factory
 - ❖ Not obvious it is possible to cool at 23 GeV anyway ??
- Fast acceleration and injection into circular ring(s) remain as in the proton-driver option

If feasible, this design would probably be faster, cheaper, and easier than the proton-driver option

Muon collider optimal circumference(s)

◆ Muon decay: Minimize the ring circumference

□ To allow the produced muons to collide as many times as possible before they decay

❖ Optimal ring size is proportional to E_μ . With 14 T state-of-the-art dipoles:

\sqrt{s}	91 GeV	125 GeV	161 GeV	350 GeV	6 TeV	24 TeV
$t = \gamma\tau_m$	0.94 ms	1.30 ms	1.67 ms	3.64 ms	62.3 ms	249 ms
$L = \gamma\beta c t_m$	283 km	389 km	501 km	1090 km	18700 km	74000 km
Ring	100 m	140 m	180 m	390 m	6.6 km	27 km
N_{turns}	~2800 turns					

□ One ring per centre-of-mass energy

❖ Two very small rings for precision studies

- One for Z and H factories (140 m circumference)
- One for W and top pair thresholds (390 m circumference)

❖ Larger ring(s) for the energy frontier

- $\sqrt{s} = 6$ TeV can fit, for example, in the Tevatron tunnel (6.6 km circumference)
- $\sqrt{s} = 24$ TeV can fit in the LHC tunnel

❖ Plus a number of rings for first stages of fast acceleration

Muon collider as a Higgs factory (1)

◆ Challenges for the Higgs factory

□ Γ_H is small (4.2 MeV in the SM)

❖ Similar or smaller beam energy spread is required (3×10^{-5})

▪ Fast longitudinal cooling to reduce energy spread

❖ Beam energy reproducibility must be at the same level or better

□ $\sigma(\mu^+\mu^- \rightarrow H)$ is about 20 pb

❖ Luminosity must be at the level of $1.6 \times 10^{32} \text{ cm}^{-2}\text{s}^{-1}$ for the same number of Higgs bosons as ILC ...

❖ and at the level of $1.6 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$ for the same number of Higgs bosons as FCC-ee

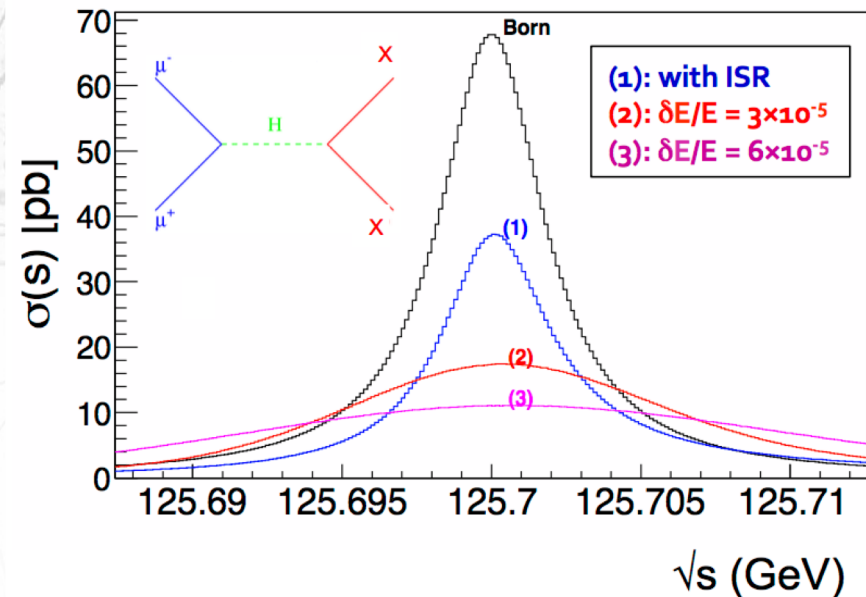
▪ Fast transverse cooling to reduce beam spot dimensions

And the Higgs bosons produced are not tagged with a Z anyway ...

□ Problem

❖ Longitudinal and transverse cooling are antagonistic

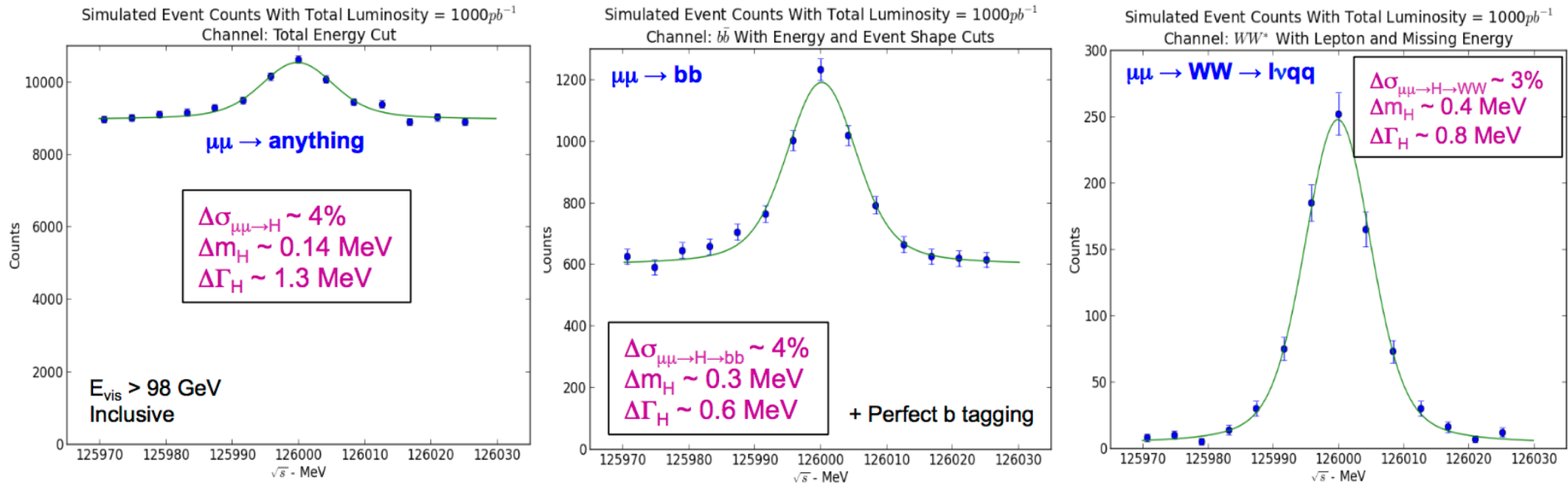
▪ Luminosity is limited (as of today's knowledge) to a few $10^{31} \text{ cm}^{-2}\text{s}^{-1}$



Muon collider as a Higgs factory (2)

◆ Physics performance of a Higgs factory

- Scan of Higgs resonance in the inclusive $b\bar{b}$ and WW final states
- ❖ Ten years of data taking at $10^{31} \text{ cm}^{-2}\text{s}^{-1}$, just count events



- Measure Γ_H to 5% in 10 years (cf. 4% at ILC, <1% at FCC-ee)
 - ❖ Only way to see a structure in the resonance (several Higgs bosons?)
- Measure $\sigma_{\text{peak}} \sim \text{BR}_{\mu\mu}$ to 2-3% in 10 years
- Other expected measurement on the figures

Muon collider as a Higgs factory (3)

◆ Summary of precision measurements (after ~10 years of running)

Error on	$\mu\mu$ collider	ILC ₂₅₀	FCC-ee
m_H (MeV)	0.06	14	8
Γ_H (MeV)	0.17	0.11	0.06
g_{Hbb}	2.3%	1.8%	0.61%
g_{HWW}	2.2%	1.7%	0.43%
$g_{H\tau\tau}$	5%	1.9%	0.80%
$g_{H\gamma\gamma}$	10%	6.4%	3.8%
$g_{H\mu\mu}$	2.1%	13%	8.6%
g_{HZZ}	-	0.35%	0.17%
g_{Hcc}	-	2.3%	1.2%
g_{Hgg}	-	2.2%	1.0%
BR_{invis}	-	<0.5%	<0.1%

Not obvious what is the practical use of such high precision on m_H

The Higgs width is best measured at ee colliders

These Higgs couplings are best measured at ee colliders

The Higgs coupling to muons is *the* added value of a $\mu\mu$ collider

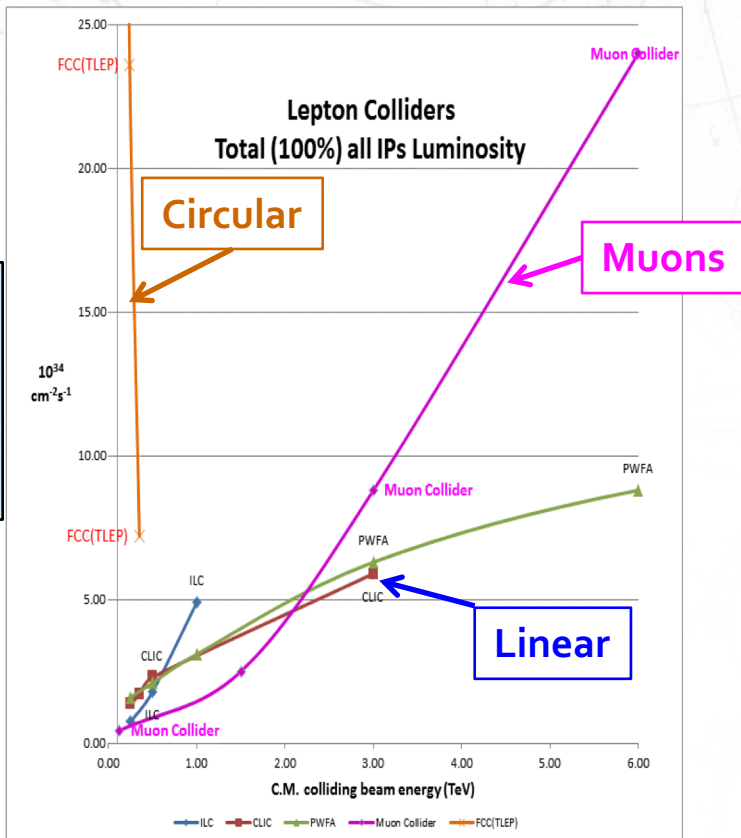
These Higgs couplings are *only* measured at ee colliders *)

□ Note: $BR(H \rightarrow \mu\mu)$ can be also measured with % precision at FCC-hh (Will be already 5% after HL-LHC)

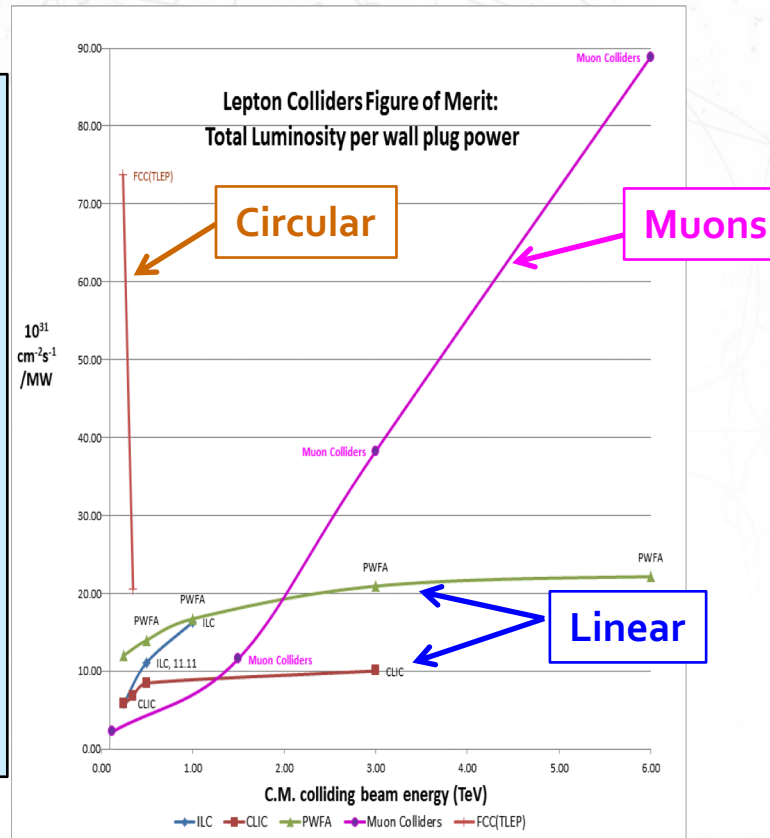
Muon colliders at the energy frontier

- ◆ Muon colliders might be a solution for high energy in the (far?) future
 - Many challenges to solve with sustained R&D and innovative thinking, as to
 - ❖ Increase luminosity for precision studies
 - ❖ Solve the radiation hazard at high energy (decay neutrino interactions in Earth)
 - Target luminosity competitive with CLIC above 2-3 TeV
 - ❖ With the possibility of several IPs

Luminosity

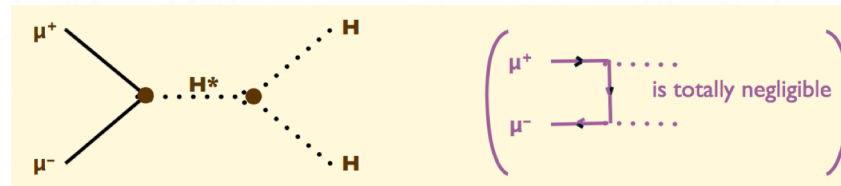


Luminosity per wall plug power unit



Muon colliders: Summary

- ◆ A muon collider may be the best way to get lepton collisions at $\sqrt{s} \geq 3$ TeV
 - Much R&D remain in, e.g., muon cooling/acceleration
- ◆ A muon collider at $\sqrt{s} = 125$ GeV is a very pretty Higgs factory ($\mu^+\mu^- \rightarrow H$)
 - But not necessarily the one we need
 - ❖ If H(125) is a single particle, the process $e^+e^- \rightarrow HZ$ @ 240 GeV is better suited
 - In particular, the Higgs width can be measured very well in e^+e^- collisions
 - ❖ A muon collider can also do that, but much higher luminosity would be necessary
 - At least two orders of magnitude – limited by the proton/positron source
- ◆ Several quasi-degenerate Higgs bosons is a strong case for $\mu\mu$ Higgs factory
 - If Δm is between 4 MeV (Γ_H) and ~100 MeV (LHC resolution)
 - ❖ Such a situation may occur with two Higgs doublets, and quasi-degenerate H & A
 - Isolate the two peaks and perform nice CP studies !
- ◆ A muon collider at $\sqrt{s} > 2 m_H$ provides the only way to *cleanly* probe HHH coupling



- ◆ A muon collider is the natural second step of neutrino factories
- ◆ Conclusion: don't write them off completely, but don't oversell them !

Lecture 2

Rounding off **Summary and Conclusions**

Summary & Conclusions (1)

- ◆ Since LEP, there has been a dramatic development in e^+e^- accelerator technology
 - **Linear colliders: Energy reach up to $\sqrt{s} = 3$ TeV**
 - **Circular colliders: Increase of instantaneous luminosity by 4-5 orders of magnitude**
 - ❖ **For $\sqrt{s} < 400$ GeV, circular colliders provide very high luminosities**
 - **Repeat of LEP1 programme every ~5 min !**
- ◆ **With the discovery of the light Higgs boson and the non-discovery (so far) of new heavier states, e^+e^- communities are now zooming in on the $\sqrt{s} < 400$ GeV region**
 - **ILC: Higgs factory at $\sqrt{s} = 250$ GeV as first stage (12 years)**
 - ❖ **Possibly later upgraded to $\sqrt{s} = 500$ GeV (and $\sqrt{s} = 1$ TeV ?)**
 - **CLIC: "Affordable" Higgs/top factory at $\sqrt{s} = 380$ GeV as first stage**
 - ❖ **Later upgraded to $\sqrt{s} = 1.5$ TeV and possibly $\sqrt{s} = 3$ TeV**
- ◆ **An e^+e^- Higgs factory with $\mathcal{O}(10^6)$ Higgs decays provides sub-% level measurement of (most) Higgs couplings**
 - **Strong New Physics reach !**
- ◆ **Electroweak precision measurements provide a strong test of SM**
 - **A e^+e^- collider with $90 < \sqrt{s} < 400$ GeV could improve precision of all electroweak parameters by 1 – 2 orders of magnitude**
 - ❖ **Ultimate precision for Z, W, Higgs, and top (and flavour: b and τ)**
 - **Strong New Physics reach !**

Summary & Conclusions (2)

- ◆ CLIC programme at $\sqrt{s} = 1.5$ and 3 TeV, has access to complementary measurements
 - Higgs self-coupling to sub-10% level
 - Precise top quark studies
 - Direct (indirect) access to new physics if $m < 1.5$ TeV ($m > 1.5$ TeV)
- ◆ In the long-term future, muon colliders may be the way to go for energy frontier lepton colliders

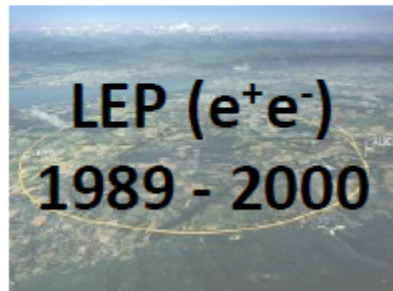
Personal views

- ◆ Muon colliders provide a potential interesting option for *long-term* future high energy lepton colliders
 - Without major technological breakthroughs they unfortunately do not provide sufficient luminosity to be interesting as a Higgs factory
- ◆ Very clear physics case for an e^+e^- collider with $90 < \sqrt{s} < 370-500$ GeV
 - Precision Higgs and electroweak physics
 - ❖ Strong complementary programmes
- ◆ Slightly harder to make physics case for e^+e^- colliders with $\sqrt{s} > 370-500$ GeV
 - At least without clear evidence for accessible new particles
 - ❖ Produced copiously in e^+e^- or $\gamma\gamma$ collisions
- ◆ Exploration of energy frontier seems best done with a hadron collider
 - e.g., the 100 TeV FCC-hh proton-proton collider

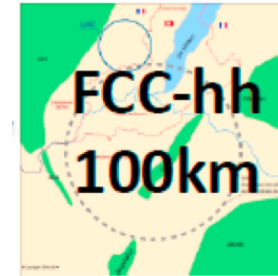
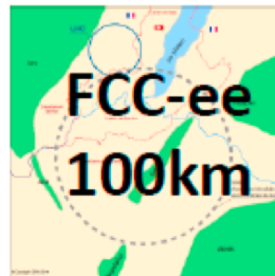
The FCC integrated programme

Base the next generation of colliders on a proven model

- ◆ 27 km tunnel



- ◆ The next step: 100 km tunnel



End of the second lecture

Questions...

"No doubt that future high energy colliders are extremely challenging projects.

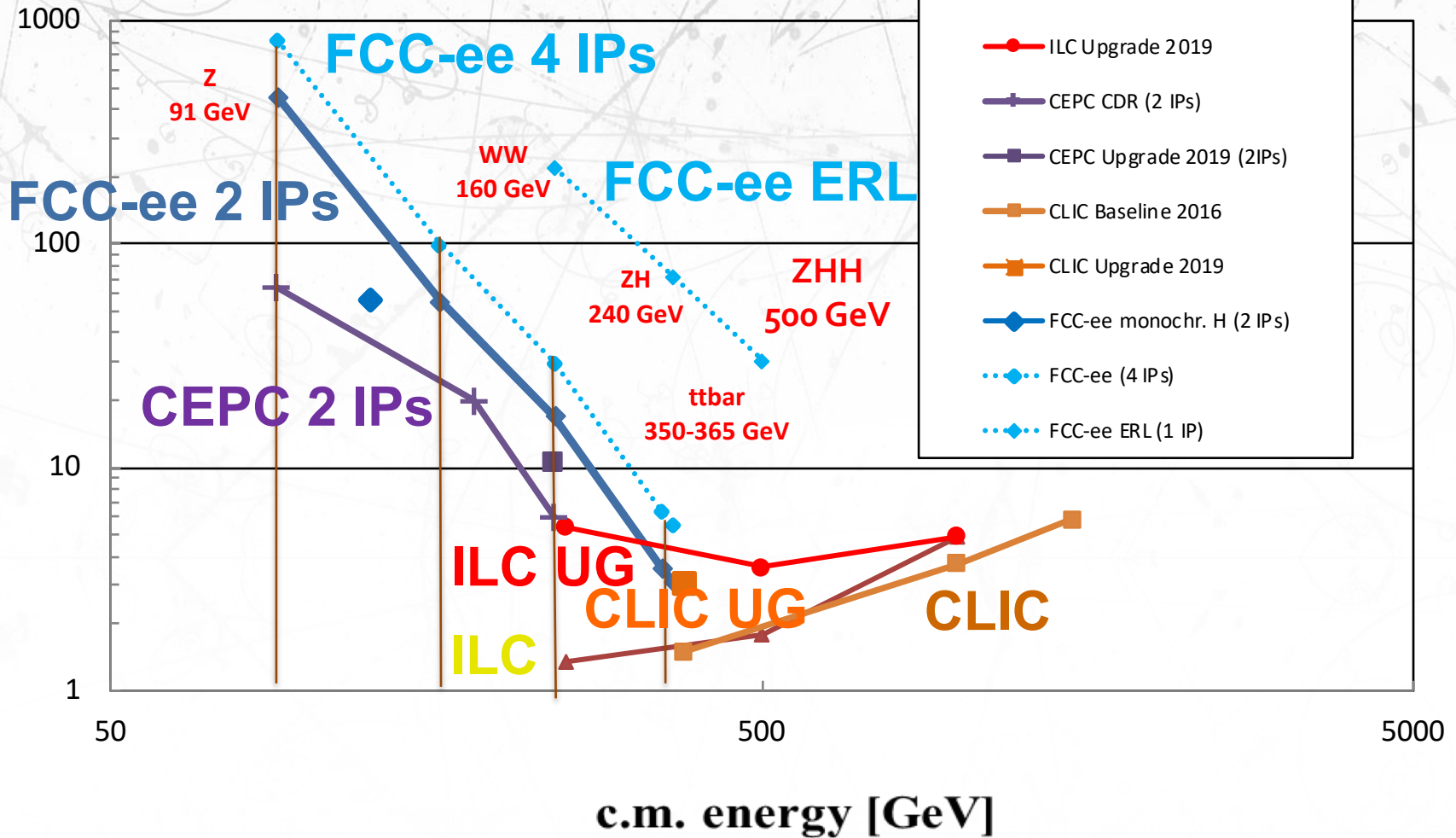
However, the correct approach, as scientists, is not to abandon our exploratory spirit, nor give in to financial and technical challenges. The correct approach is to use our creativity to develop the technologies needed to make future projects financially and technically affordable."

Fabiola Gianotti, DG CERN

Extra Material

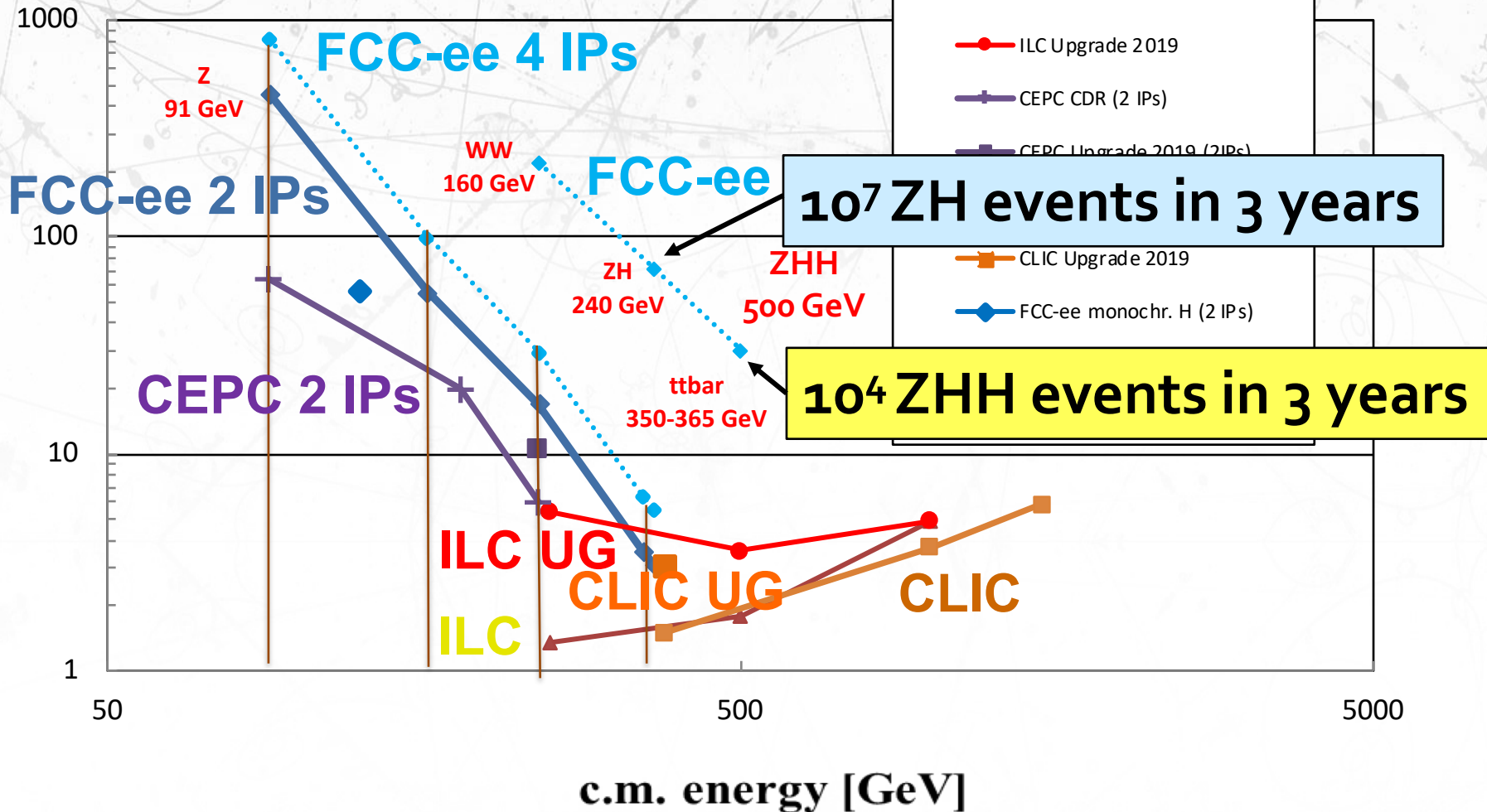
e^+e^- colliders – a field in very rapid development

luminosity [$10^{34} \text{ cm}^{-2}\text{s}^{-1}$]



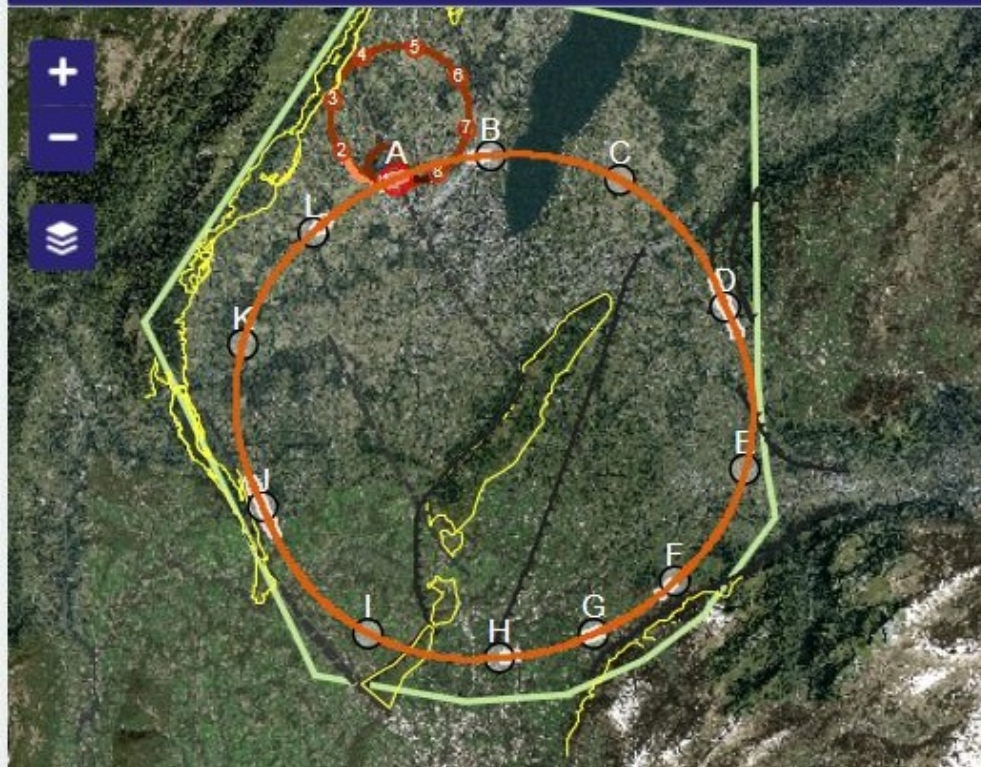
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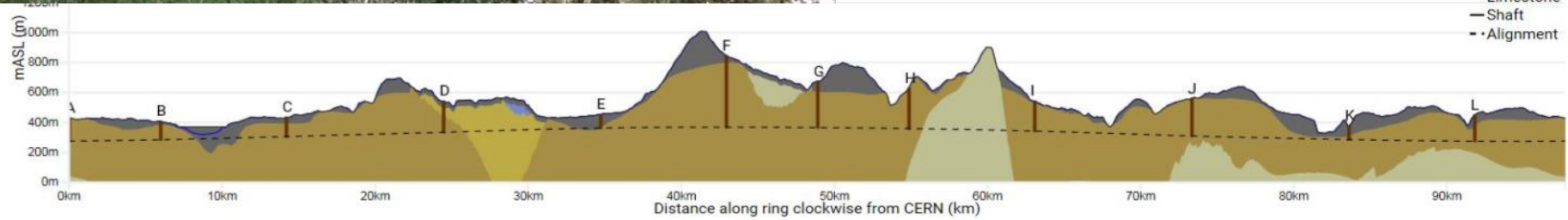


The FCC Home

Alignment Location



- ◆ **Optimized length: 97.5 km**
 - Accessibility, rock type, shaft depth, etc.
 - Tried different options from 80 to 100 km
- ◆ **Tunneling**
 - Molasse 90% (easy to dig)
 - Limestone 5%, Moraines 5% (tougher)
- ◆ **Shallow implementation**
 - 30m below Lemman lakebed
 - Only one very deep shaft (F, 476m)
 - ❖ Alternatives studied (e.g. inclined access)



- Quaternary
- Lake
- Wildflysch
- Molasse subalpine
- Molasse
- Limestone
- Shaft
- - Alignment

Geology Intersected by Tunnel

Geology Intersected by Section

84.6%

5.2%

5.5%

4.7%

double ring e^+e^- collider ~ 100 km

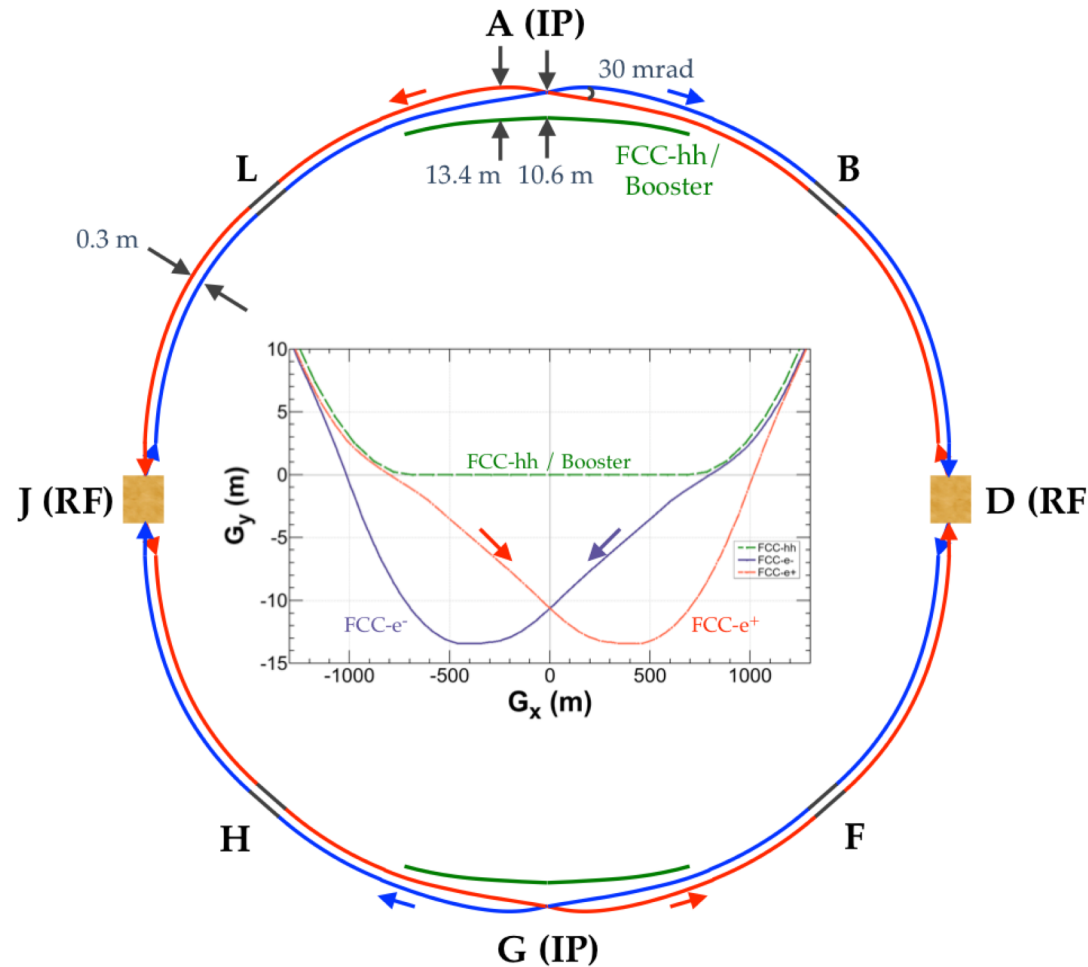
follows footprint of FCC-hh, except around IPs

asymmetric IR layout & optics to limit synchrotron radiation towards the detector

presently 2 IPs (alternative layouts with 3 or 4 IPs under study), large horizontal crossing angle 30 mrad, crab-waist optics

synchrotron radiation power 50 MW/beam at all beam energies; tapering of arc magnet strengths to match local energy

top-up injection scheme; requires booster synchrotron in collider tunnel



FCC-ee Machine Parameters

FCC-ee parameters		Z	W ⁺ W ⁻	ZH	ttbar	
Beam energy	GeV	45.6	80	120	175	182.5
Luminosity / IP	10 ³⁴ cm ⁻² s ⁻¹	230	28	8.5	1.8	1.55
Beam current	mA	1390	147	29	6.4	5.4
Bunches per beam	#	16640	2000	328	59	48
Average bunch spacing	ns	19.6	163	994	2763	3396
Bunch population	10 ¹¹	1.7	1.5	1.8	2.2	2.3
Horizontal emittance ϵ_x	nm	0.27	0.84	0.63	1.34	1.46
Vertical emittance ϵ_y	pm	1.0	1.7	1.3	2.7	2.9
β_x^* / β_y^*	m / mm	0.15 / 0.8	0.2 / 1.0	0.3 / 1.0	1.0 / 1.6	
beam size at IP: σ_x^* / σ_y^*	$\mu\text{m} / \text{nm}$	6.4 / 28	13 / 41	13.7 / 36	36.7 / 66	38.2/68
Energy spread: SR / total (w BS)	%	0.038 / 0.132	0.066 / 0.131	0.099 / 0.165	0.144 / 0.196	0.15 / 0.192
Bunch length: SR / total	mm	3.5 / 12.1	3 / 6.0	3.15 / 5.3	2.75 / 3.82	1.97 / 2.54
Energy loss per turn	GeV	0.036	0.34	1.72	7.8	9.2
RF Voltage /station	GV	0.1	0.75	2.0	4/5.4	4/6.9
Longitudinal damping time	turns	1273	236	70.3	23.1	20.4
Acceptance RF / energy (DA)	%	1.9 / ± 1.3	2.3 / ± 1.3	2.3 / ± 1.7	3.5 / (-2.8; +2.4)	3.36 / (-2.8; +2.4)
Rad. Bhabha/ actual Beamstr. Lifetime	min	68 / > 200	59 / >200	38 / 18	37/ 24	40 / 18
Beam-beam parameter ξ_x / ξ_y		0.004 / 0.133	0.01 / 0.141	0.016 / 0.118	0.088 / 0.148	0.099 / 0.126
Interaction region length	mm	0.42	0.85	0.9	1.8	1.8

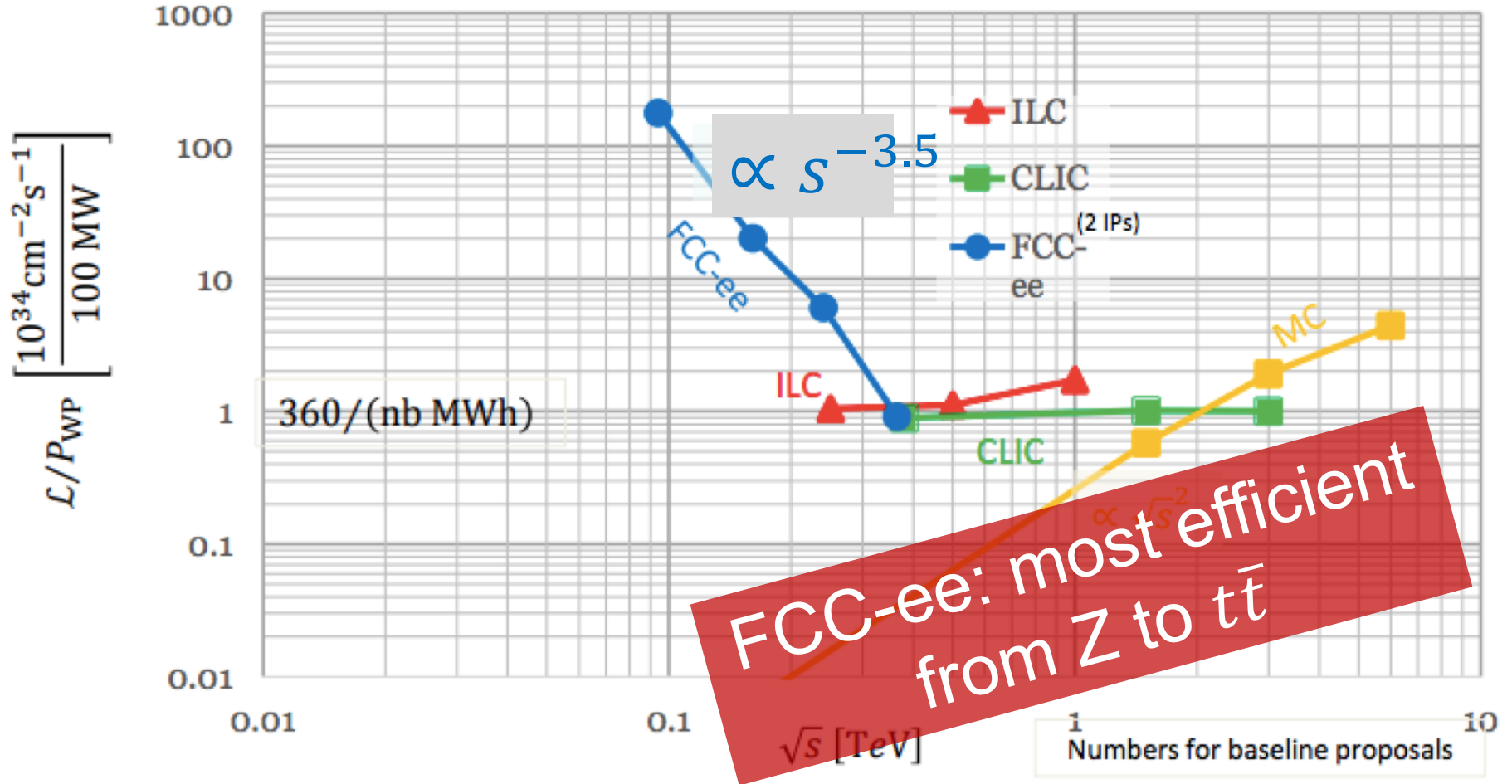
FCC-ee Power consumption

- ◆ The RF system needs to compensate for 100 MW SR losses
 - Corresponds to 200 MW electric power with 50% RF power sources (klystrons)
 - ❖ Klystron efficiency was ~55% at LEP2
 - Recent (2015) breakthroughs in klystron design promise 90% efficiency
 - ❖ Assume 85% will be achieved and take 10 – 20% margins

lepton collider	Z	W	ZH	$t\bar{t}$	LEP2
luminosity / interaction point [$10^{34} \text{ cm}^{-2}\text{s}^{-1}$]	207	90	19	5	1.3
total RF power [MW]	163	163	145	145	42
collider cryogenics [MW]	3	2	5	23	39
collider magnets [MW]	3	10	24	50	16
booster RF & cryogenics [MW]	4	4	6	7	N/A
booster magnets [MW]	0	1	2	5	N/A
pre-injector complex [MW]	10	10	10	10	10
physics detectors (2) [MW]	10	10	10	10	9
cooling & ventilation [MW]	47	49	52	62	16
general services [MW]	36	36	36	36	9
total electrical power [MW]	276	~275	~288	~308	~364

- For comparison
 - ❖ LHC Run1: 210 MW, HL-LHC: 260 MW, FCC-hh: ~500 MW
 - ❖ CLIC: 250 MW (at 380 GeV) to 580 MW (at 3 TeV)

figure of merit for lepton colliders



Precision electroweak physics at FCC-ee (12)

- ◆ The predictions of m_{top} , m_W , m_H , $\sin^2\theta_W$ have theoretical uncertainties
 - Which may cancel the sensitivity to new physics
- ◆ For m_W and $\sin^2\theta_W$ today, these uncertainties are as follows

$$\begin{aligned}
 m_W &= 80.3584 \pm 0.0055_{m_{\text{top}}} \pm 0.0025_{m_Z} \pm 0.0018_{\alpha_{\text{QED}}} \\
 &\quad \pm 0.0020_{\alpha_S} \pm 0.0001_{m_H} \pm 0.0040_{\text{theory}} \text{ GeV} \\
 &= 80.358 \pm 0.008_{\text{total}} \text{ GeV},
 \end{aligned}$$

Exp: 0.012 GeV

$$\begin{aligned}
 \sin^2 \theta_W^{\text{eff}} &= 0.231488 \pm 0.000029_{m_{\text{top}}} \pm 0.000015_{m_Z} \pm 0.000035_{\alpha_{\text{QED}}} \\
 &\quad \pm 0.000010_{\alpha_S} \pm 0.000001_{m_H} \pm 0.000047_{\text{theory}} \\
 &= 0.23149 \pm 0.00007_{\text{total}},
 \end{aligned}$$

Exp: 0.00016

- Parametric uncertainties and missing higher orders in theoretical calculations:
 - ❖ Are of the same order
 - ❖ Smaller than experimental uncertainties

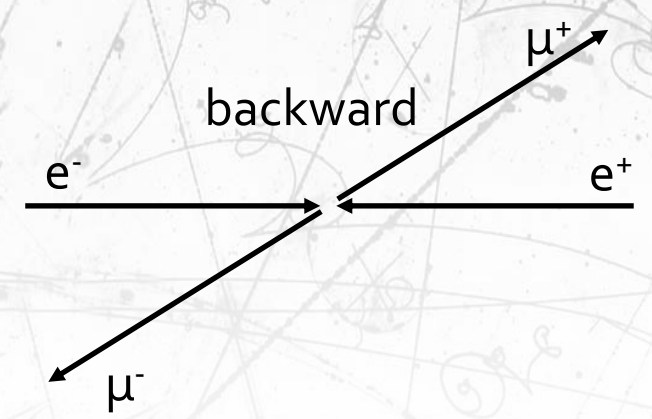
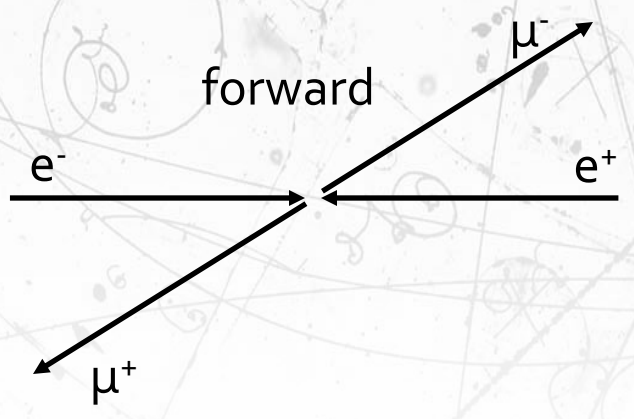
Precision electroweak physics at FCC-ee (13)

- ◆ Most of the parametric uncertainties will reduce at the FCC-ee
 - New generation of theoretical calculations is necessary to gain a factor 10 in precision
 - ❖ To match the precision of the direct FCC-ee measurements

$$\begin{aligned}
 m_W &= 80.3584 \pm 0.0001 \quad m_{\text{top}} \pm 0.0001 \quad m_Z \pm 0.0003 \quad \alpha_{\text{QED}} \\
 &\pm 0.0002 \quad \alpha_S \pm 0.0000 \quad m_H \pm 0.0040_{\text{theory}} \text{ GeV} \\
 &= 80.358 \pm 0.005_{\text{total}} \text{ GeV}, \quad \text{Exp: } 0.0005
 \end{aligned}$$

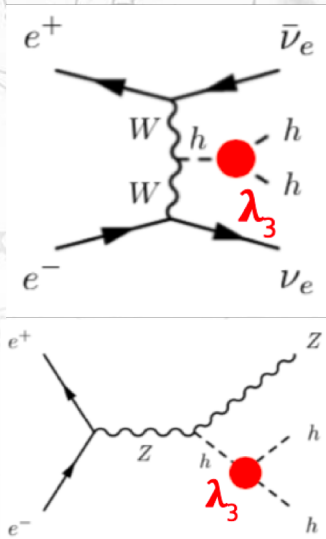
$$\begin{aligned}
 \sin^2 \theta_W^{\text{eff}} &= 0.231488 \pm 0.000001 \quad m_{\text{top}} \pm 0.000001 \quad m_Z \pm 0.000008 \quad \alpha_{\text{QED}} \\
 &\pm 0.000001 \quad \alpha_S \pm 0.000000 \quad m_H \pm 0.000047_{\text{theory}} \\
 &= 0.23149 \pm 0.00006_{\text{total}}, \quad \text{Exp: } 0.000006
 \end{aligned}$$

- Will require calculations up to three or four loops to gain an order of magnitude
 - ❖ Might need a new paradigm in the actual computing methods
 - Lots of interesting work for future generations of theorists (you?)

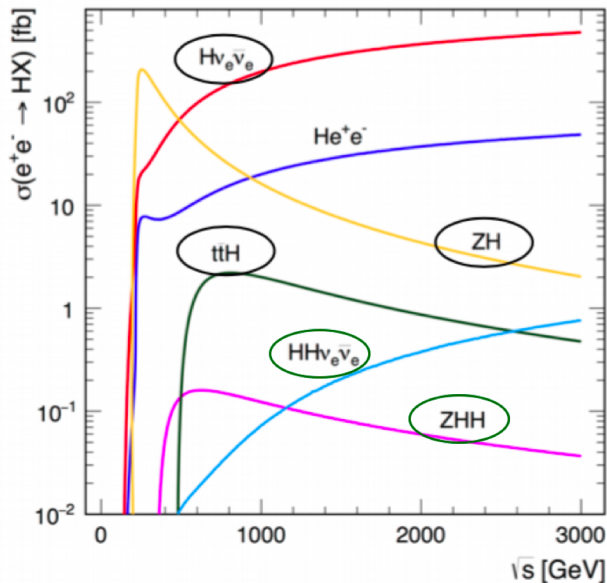


Higgs Self-coupling

◆ Higgs pair production requires high energy



	1.4 TeV	3 TeV
$\sigma(\text{HH}\nu_e\nu_e)$	$>3\sigma$ EVIDENCE = 28%	$>5\sigma$ OBSERVATION = 7.3%
$\sigma(\text{ZHH})$	$>5\sigma$ OBSERVATION	
$g_{\text{HHH}}/g_{\text{HHH}}^{\text{SM}}$	1.4 TeV: -34%, +36% rate-only analysis	1.4 + 3 TeV: -7%, +11% differential analysis



Among e^+e^- colliders, unrivalled sensitivity to Higgs self-coupling

$$\Delta g_{\text{HHH}}/g_{\text{HHH}} = \begin{matrix} +11\% \\ -7\% \end{matrix}$$