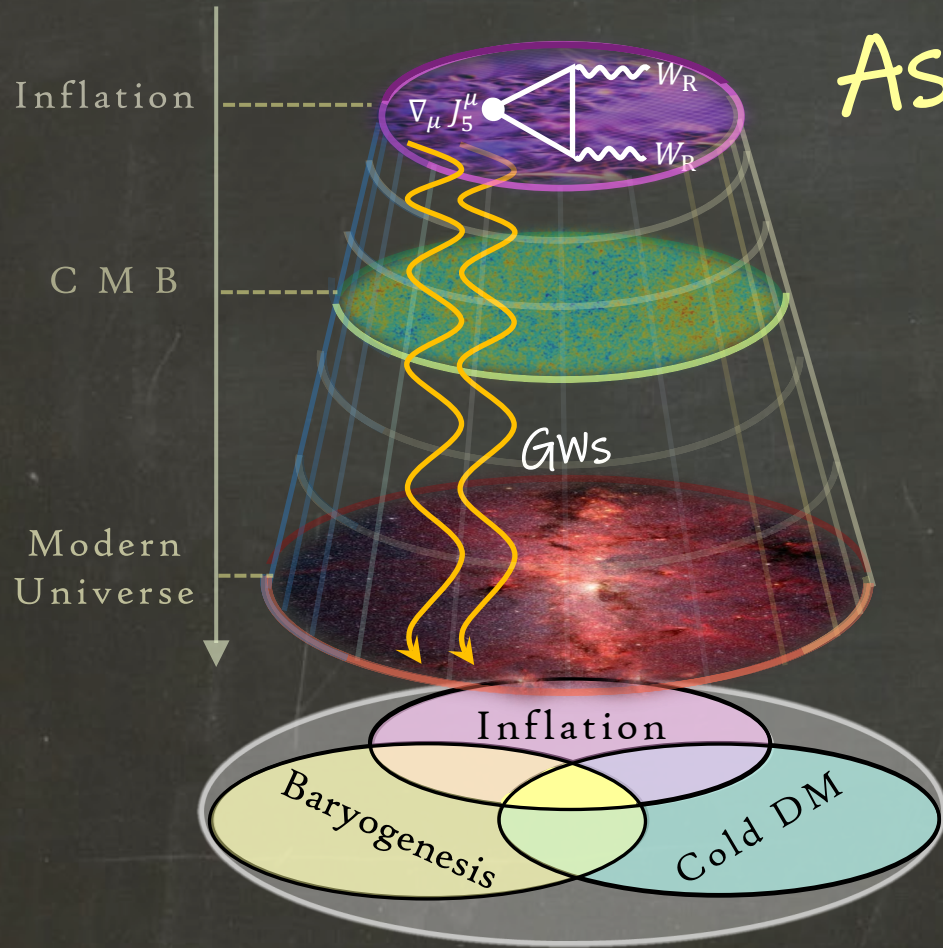


# Inflation, Origin of Matter Asymmetry, and GW Background



Azadeh Malek-Nejad  
CERN

# Cosmic History



# Cosmic History

Our Universe is too simple,  
too symmetric at  
very large scales!

**CMB** is nearly  
homogenous & isotropic!

$$T_{\text{CMB}} = 2.7 \text{ K}$$

with  
tiny fluctuation

$$\frac{\Delta T}{T_{\text{CMB}}} = 10^{-5}!$$

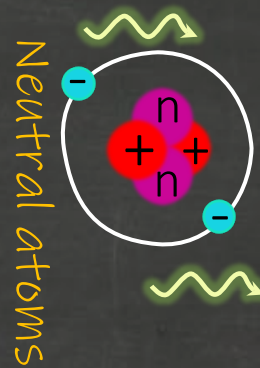
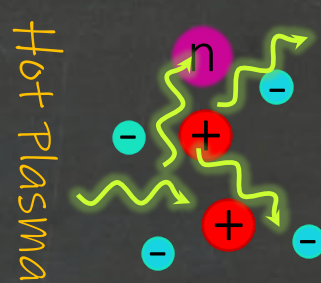
Big Bang Singularity

Hot

$T = 1 \text{ eV}$

Cold

Time



Gravitational  
collapse



Large Scale  
Structures

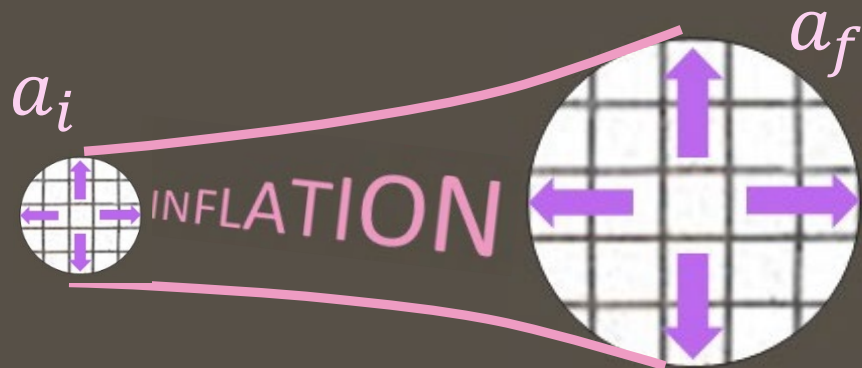


# Cosmic Inflation

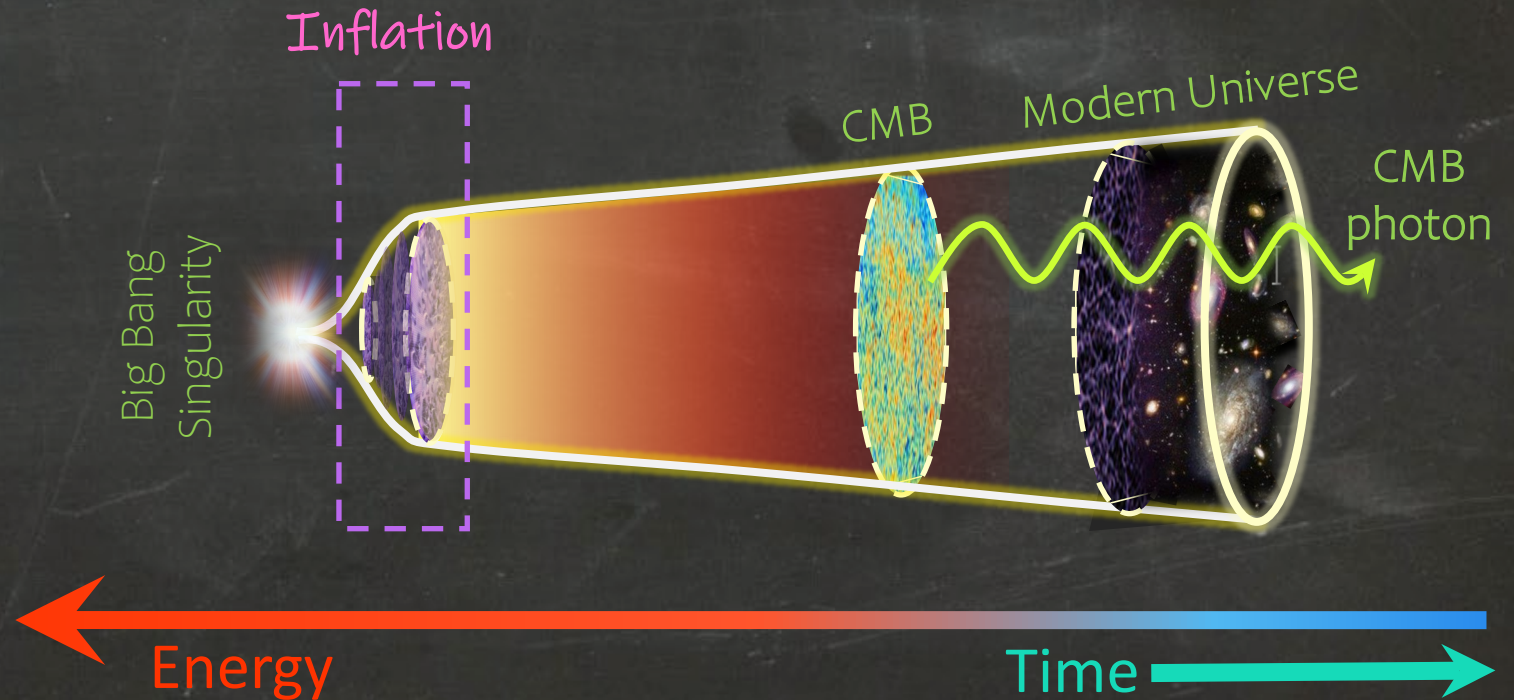
Guth Phys. Rev. D23 (1981)

Linde Phys. Lett. B 108 (1982)

A period of exponential expansion of space shortly after the Big Bang



$$\frac{a_f}{a_i} = e^{60} \approx 10^{26}!$$

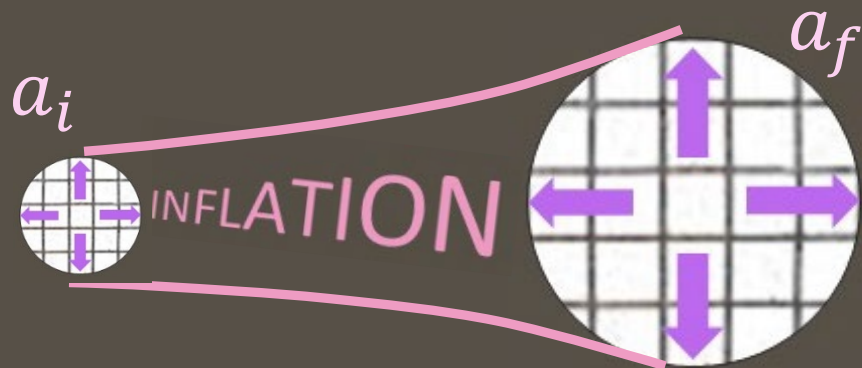


# Cosmic Inflation

Guth Phys. Rev. D23 (1981)

Linde Phys. Lett. B 108 (1982)

A period of exponential expansion of space shortly after the Big Bang



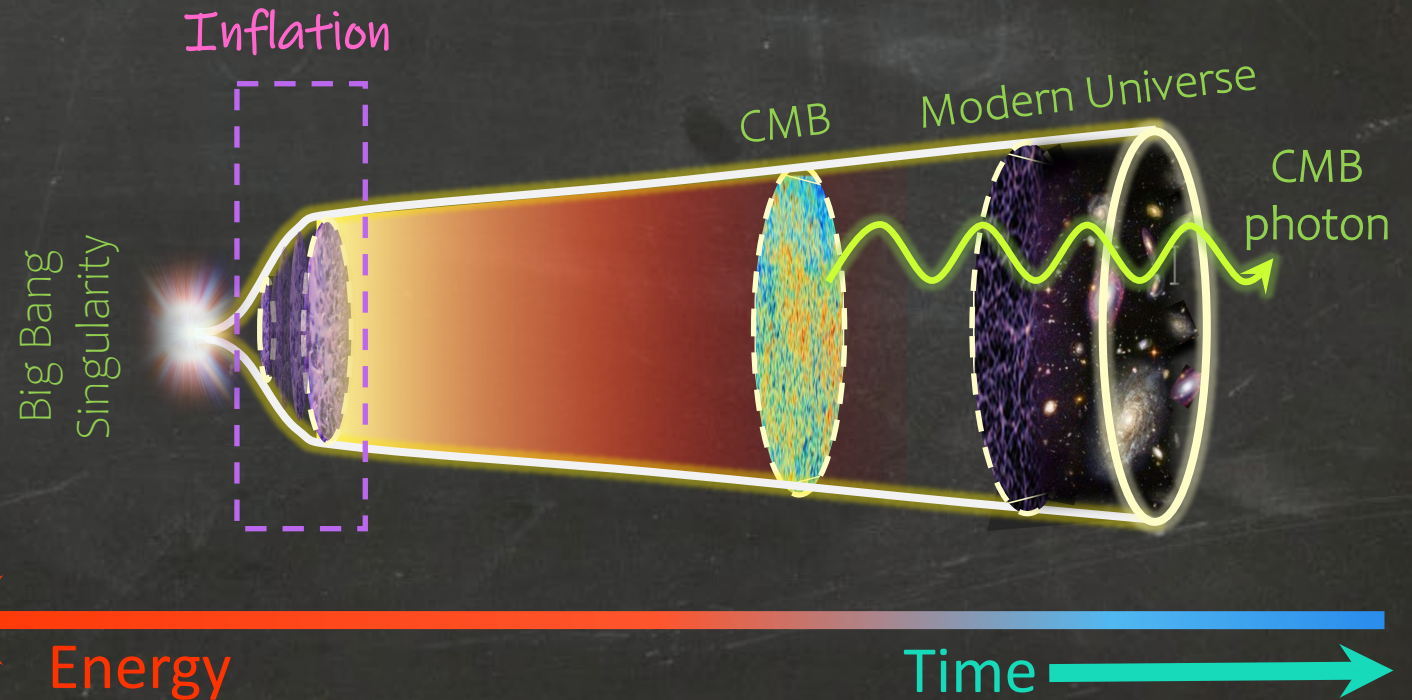
$$\frac{a_f}{a_i} = e^{60} \approx 10^{26}!$$

Bacterium

$D \approx 10 \mu\text{m}$



Milky Way

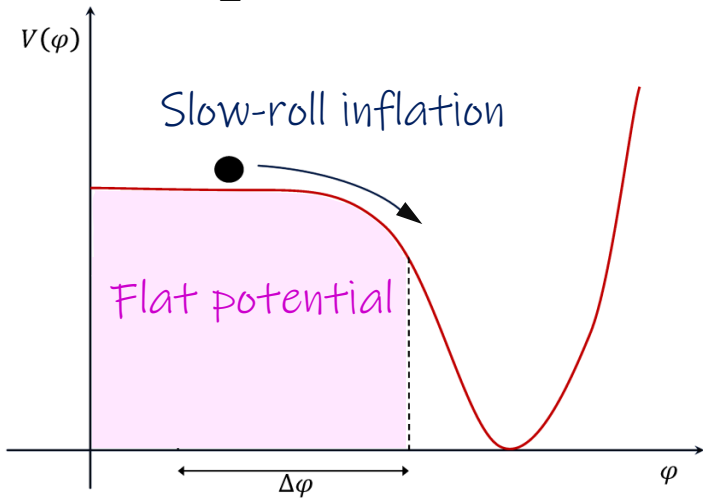


# What caused inflation?

A *scalar field* "slow-rolling" toward its true vacuum provides a simple model for inflation.

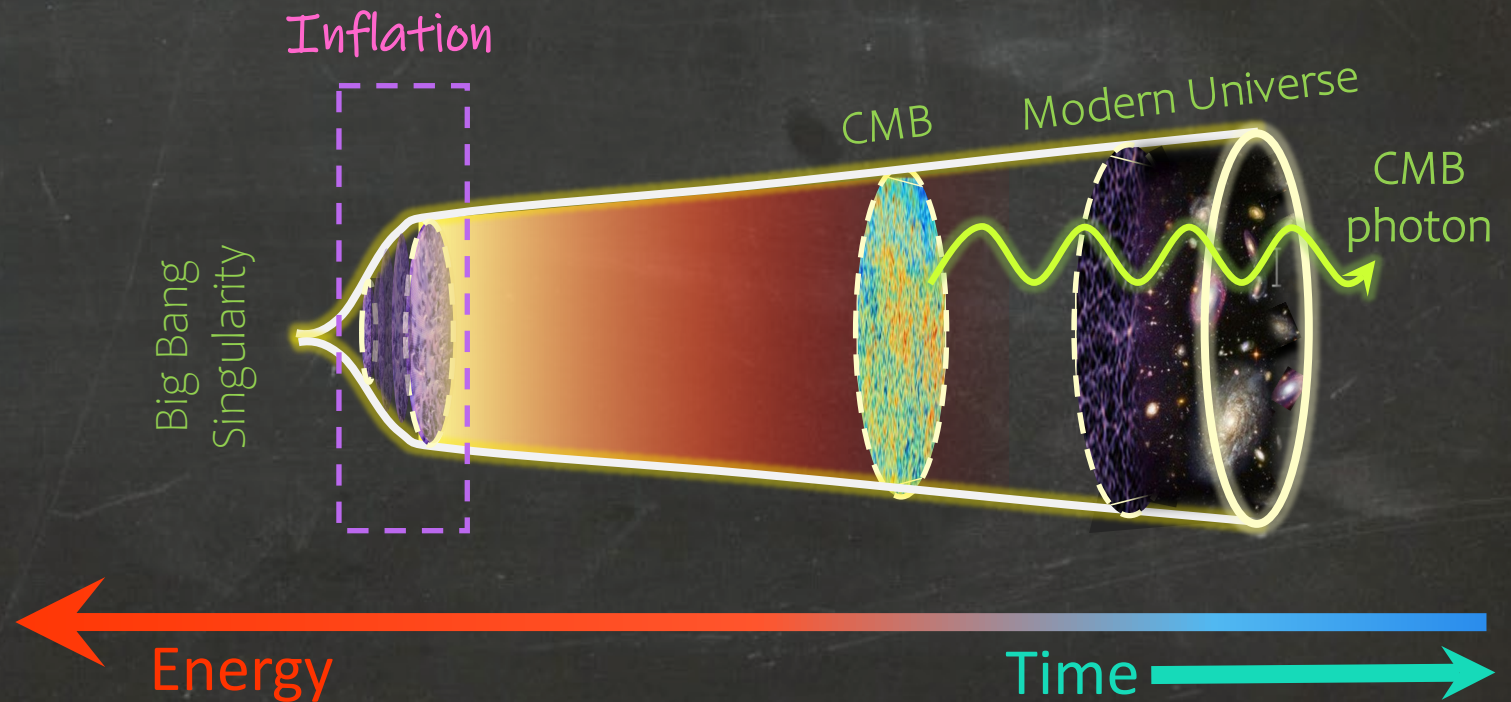
$$\rho = \frac{1}{2} \dot{\phi}^2 + V(\phi)$$

$$P = \frac{1}{2} \dot{\phi}^2 - V(\phi)$$



It is assumed that the cosmos was filled with a homogenous scalar field beyond the SM in inflation

$$\phi(t, \vec{x}) = \phi(t)$$



# Quantum Fluctuations

---

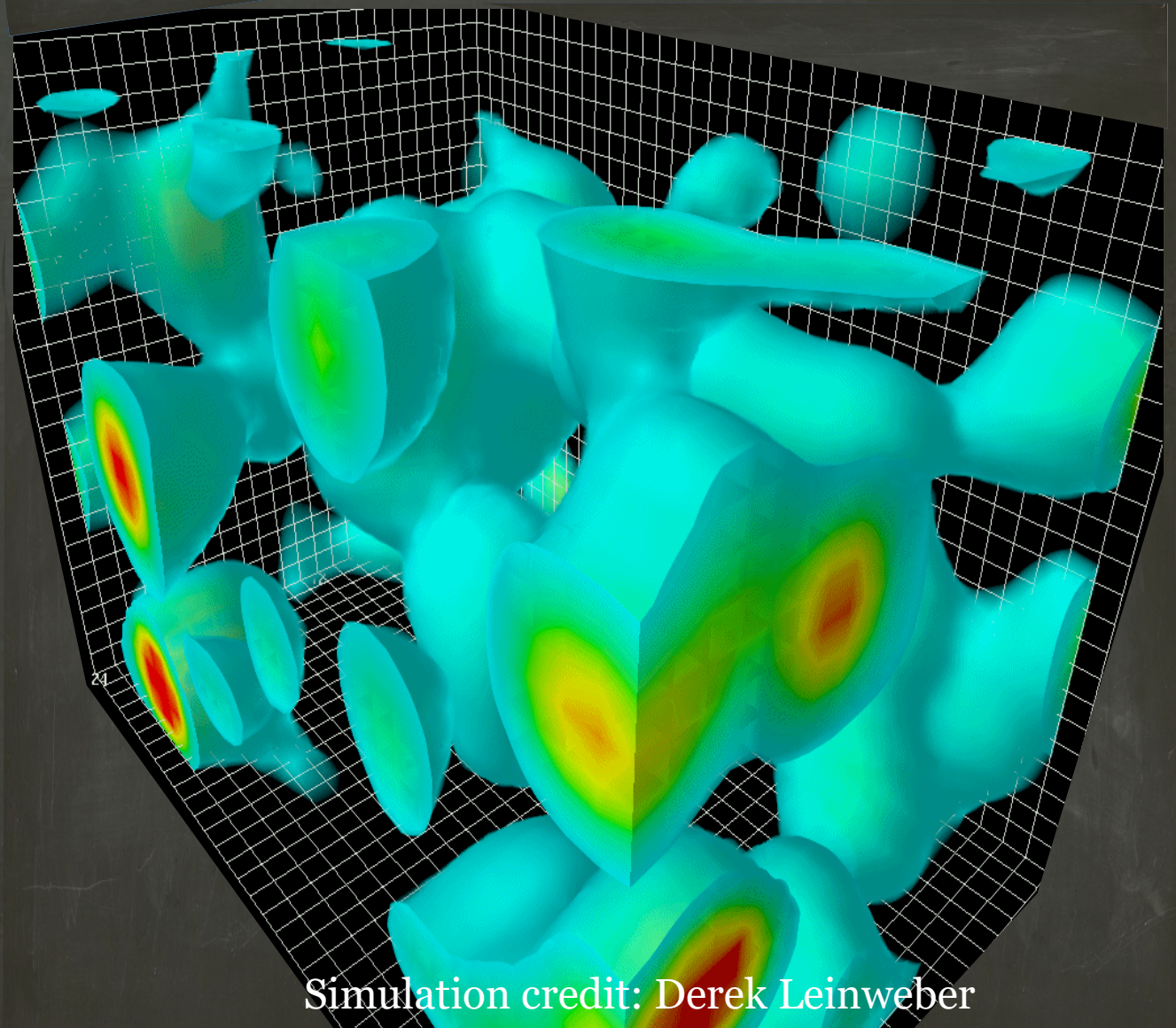
$$\hbar \neq 0$$

# Quantum Vacuum $\hbar \neq 0$

Due to Uncertainty Principle

$$\Delta x \Delta p \geq \hbar/2$$

quantum vacuum is NOT nothing!



Simulation credit: Derek Leinweber



# Quantum Vacuum $\hbar \neq 0$

Due to Uncertainty Principle

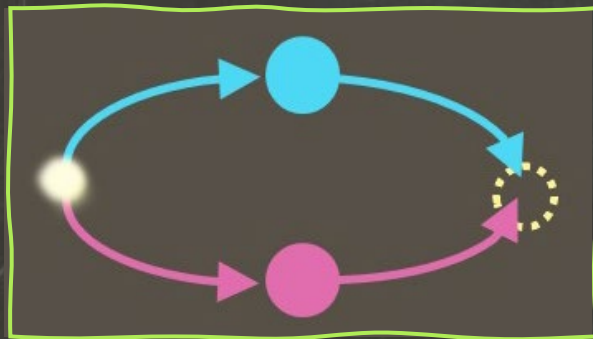
$$\Delta x \Delta p \geq \hbar/2$$

quantum vacuum is NOT nothing!

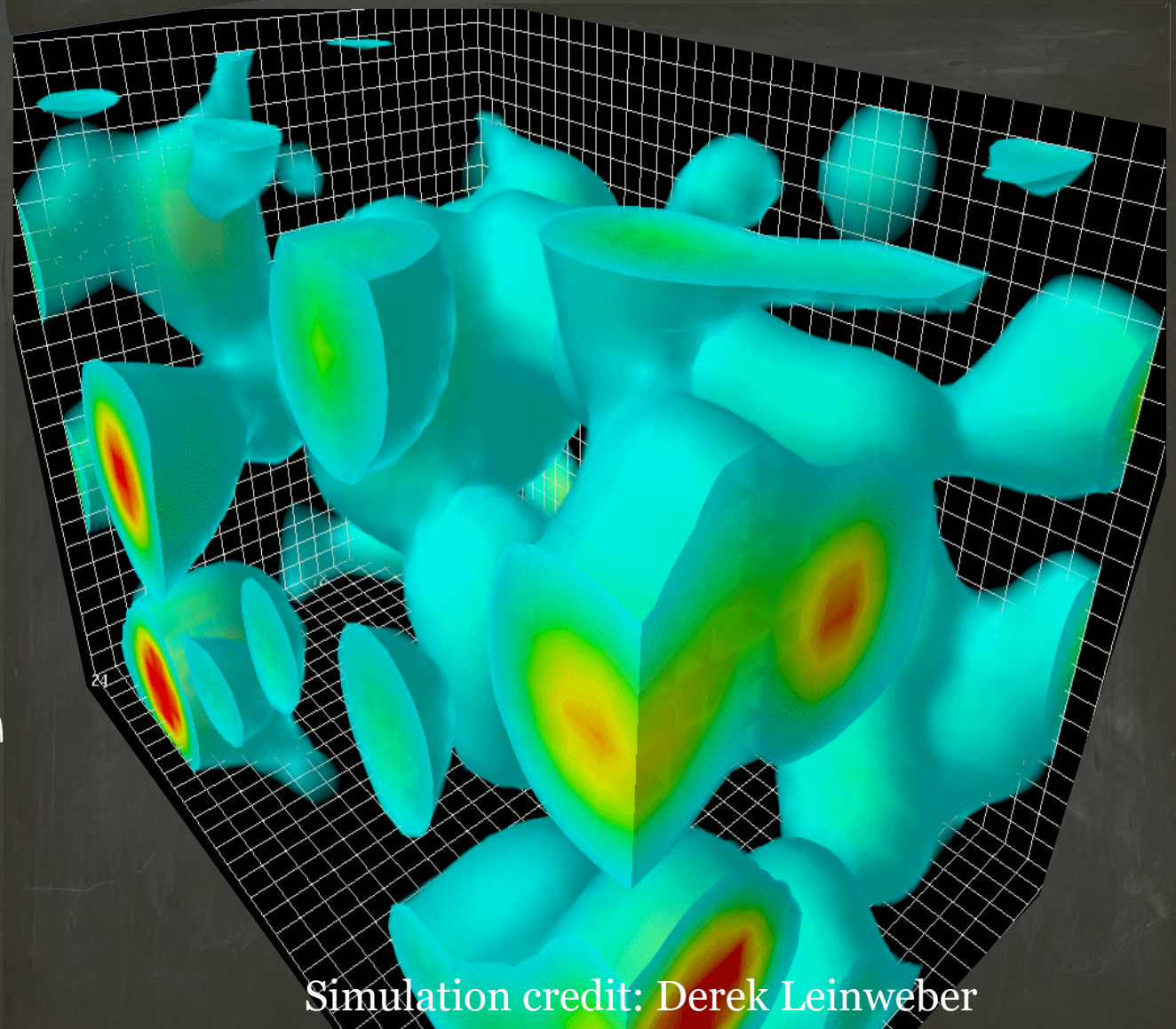
But, a vast ocean made of

**Virtual particles**

vacuum



vacuum



Simulation credit: Derek Leinweber

# Quantum Vacuum



# Particle Production

Due to Uncertainty Principle

$$\Delta x \Delta p \geq \hbar/2$$

the quantum vacuum is  
**NOT** nothing!

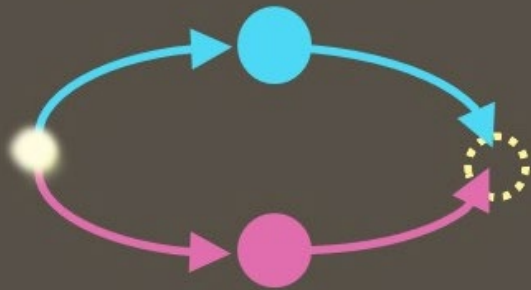
But, a vast ocean made of

**Background field** can upgrade  
them into **actual particles**!

Examples of such BG fields:

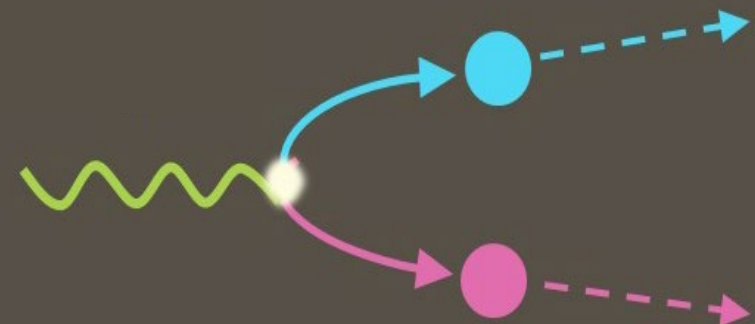
- 1) Electric (Schwinger effect)
- 2) Gravitational (Gravitational production)

Virtual particles



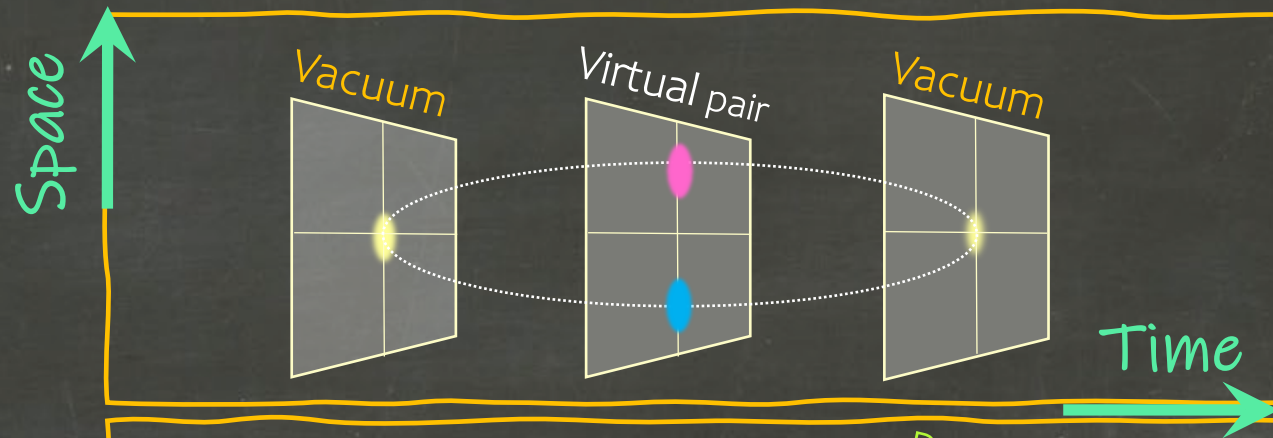
BG field

Actual particles



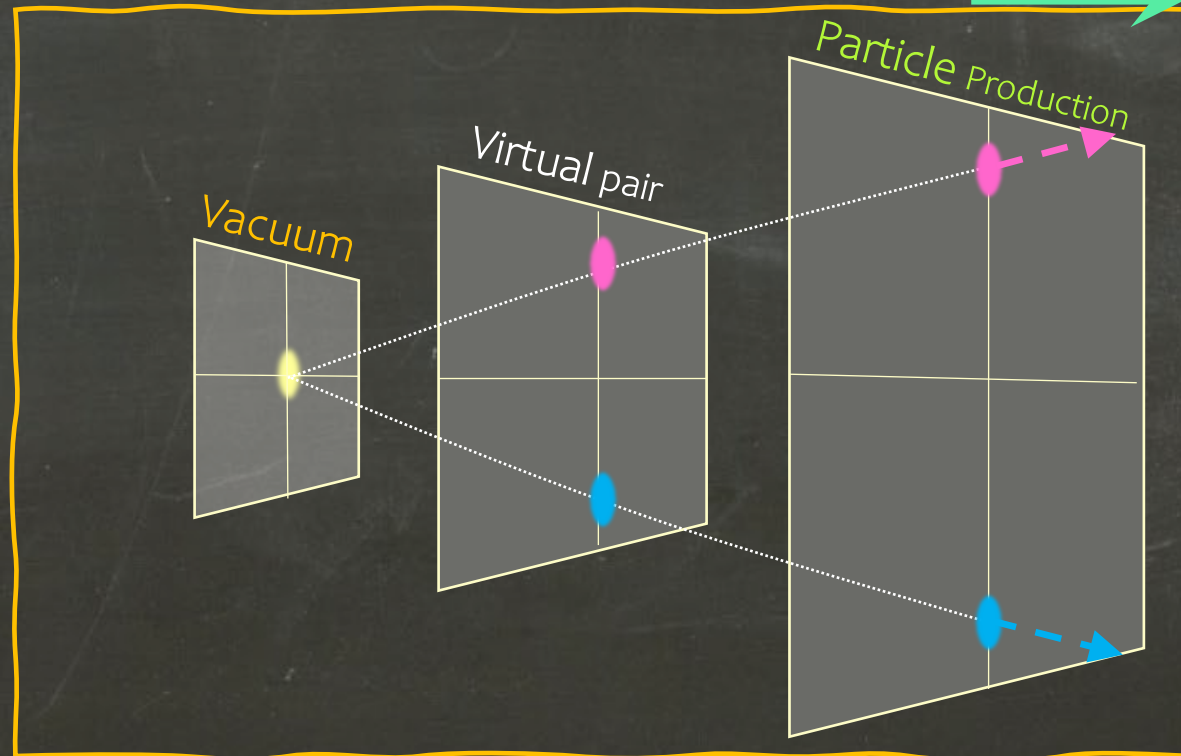
# Inflation Produces Particles!

Flat Space:



Vacuum

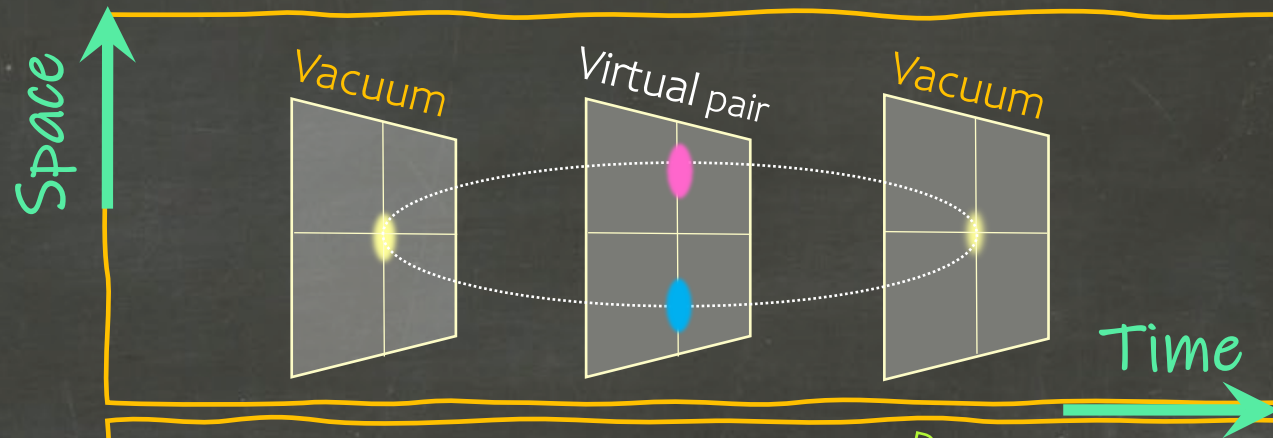
Expanding space:



Particle Production

# Inflation Produces Particles!

Flat Space:



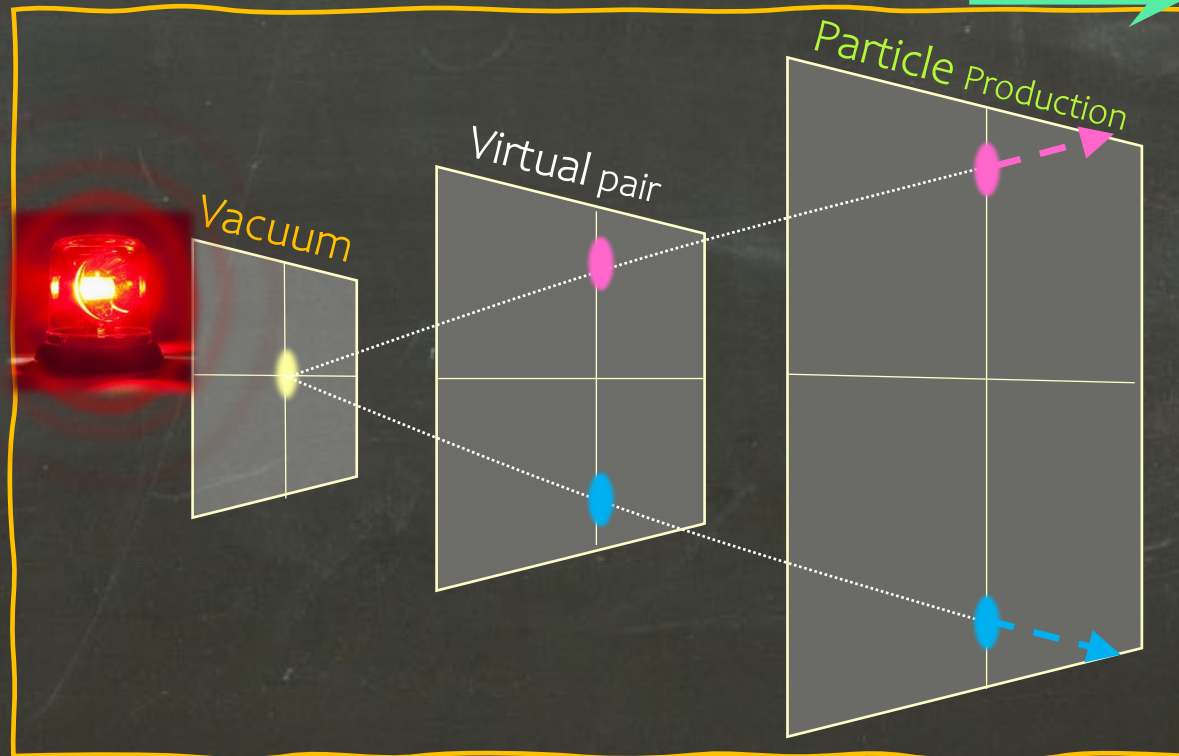
Vacuum

Expanding space:

Edwin Schrödinger  
(1939)



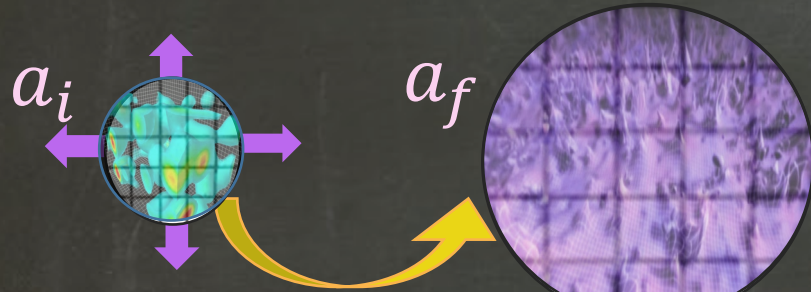
Shocked by his discovery,  
Schrödinger found it  
an alarming phenomenon!



Particle  
Production

# Cosmic Perturbations

Exponential expansion turns initial quantum vacuum fluctuations into

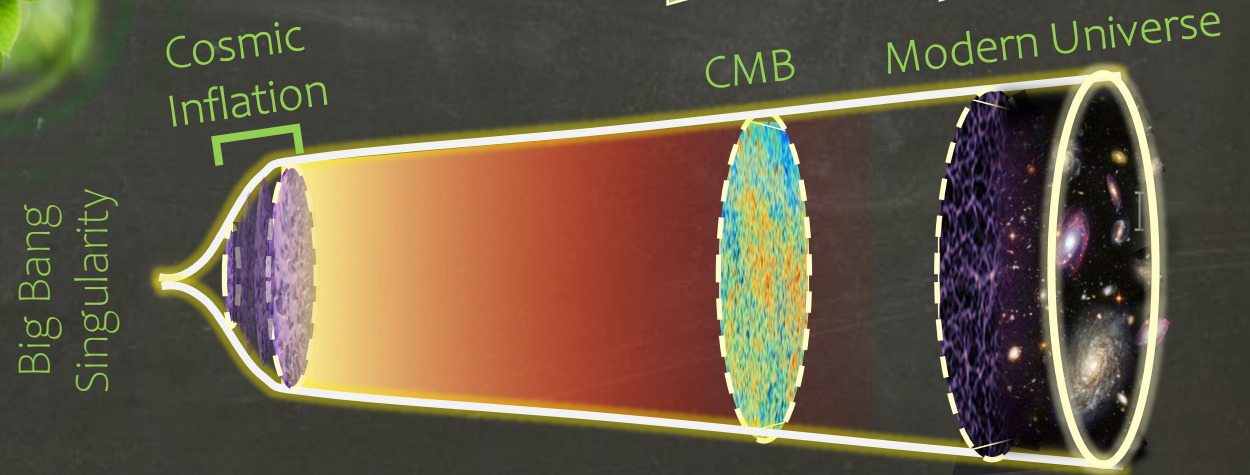
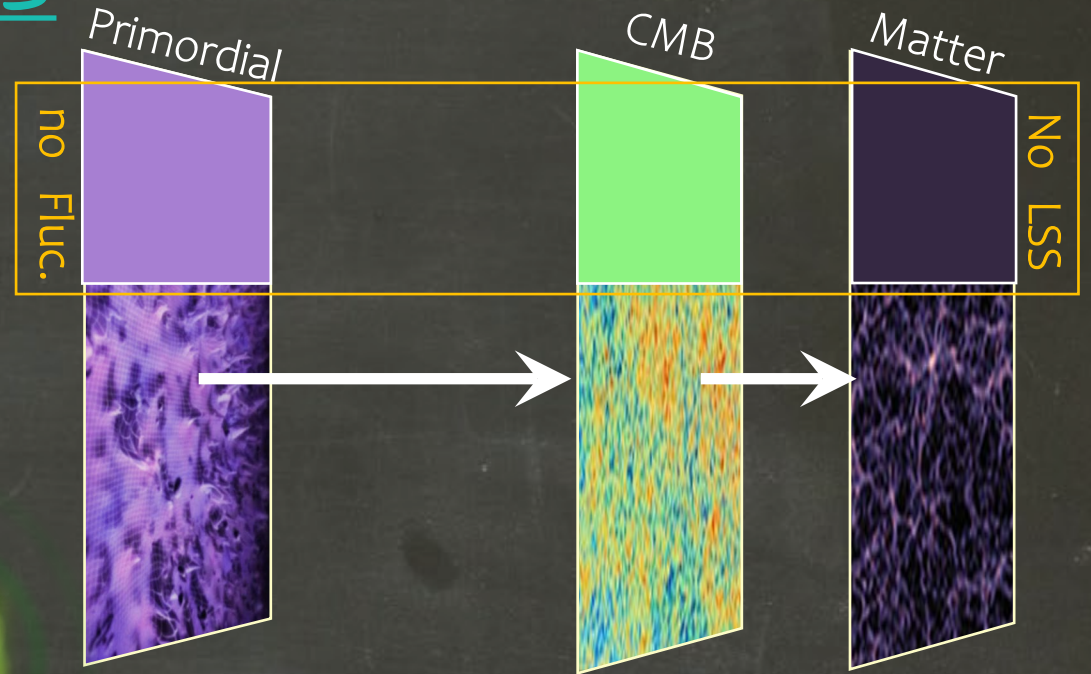


actual cosmic perturbations!



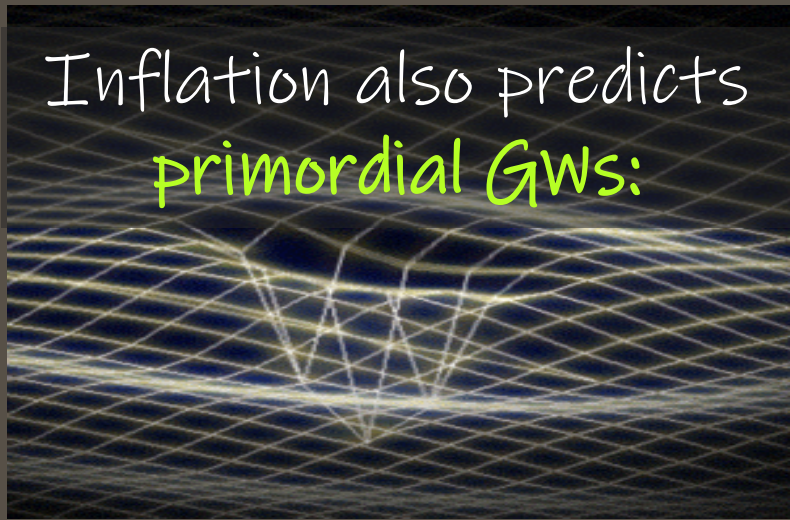
We are the product of quantum fluctuations in the very early universe!

(Stephen Hawking)

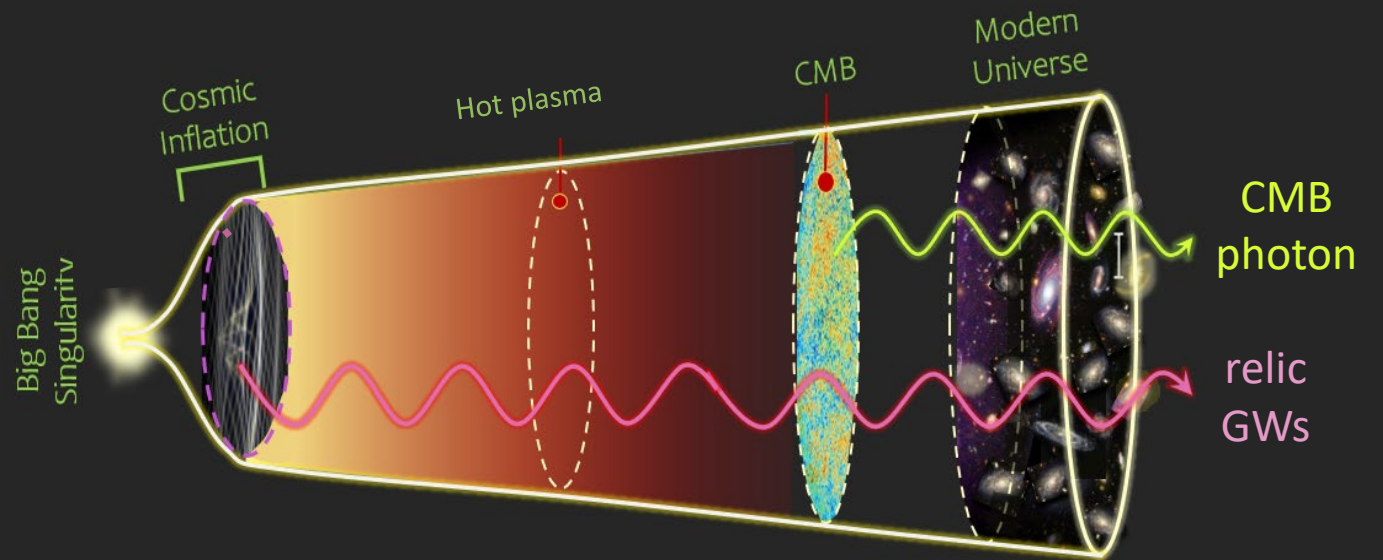
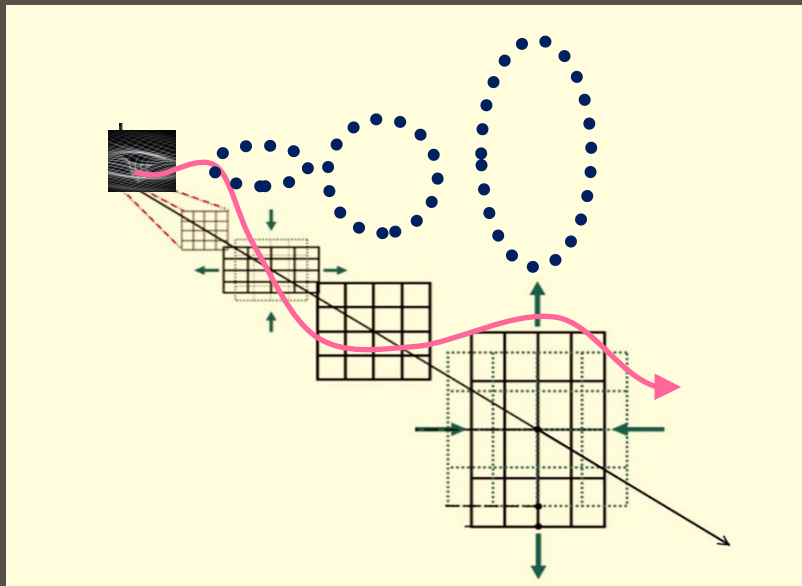


# Primordial Gravitational Waves

Inflation also predicts  
**primordial GWs:**



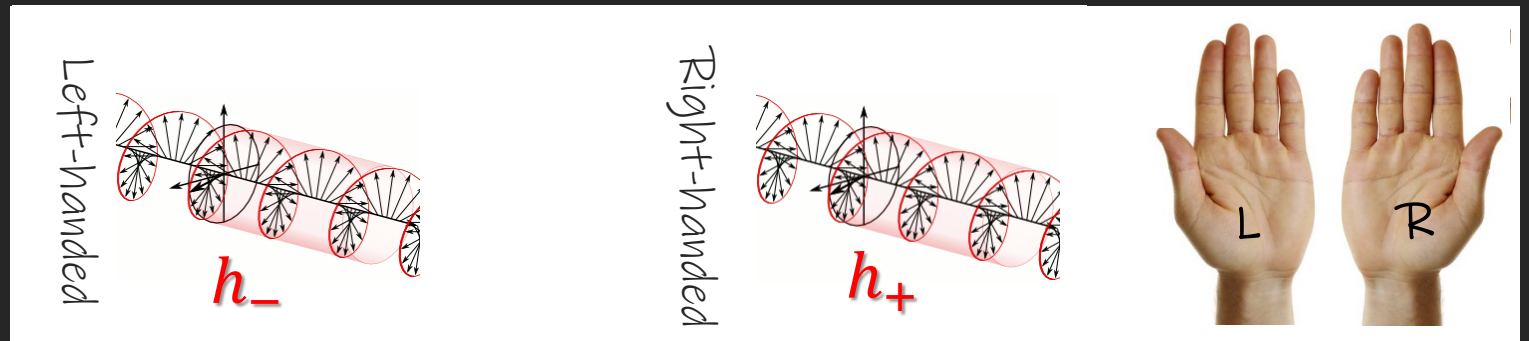
**Primordial GWs:** tiny waves in the fabrics of the space-time that squeeze and stretch anything in their path as they pass by.



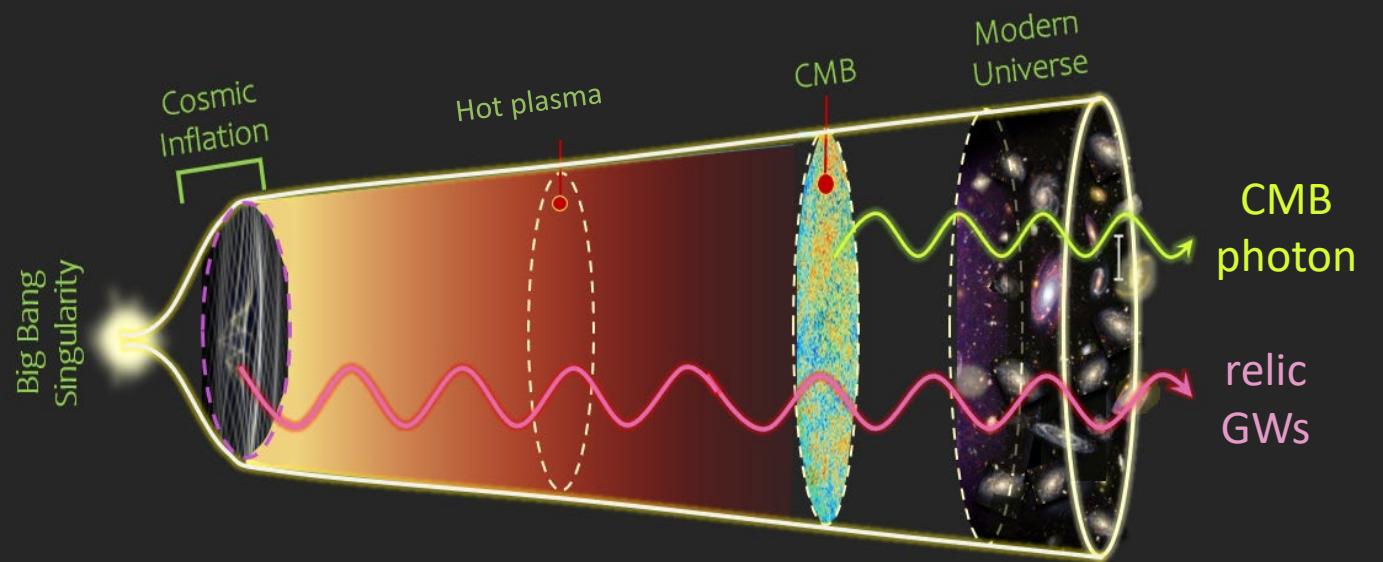
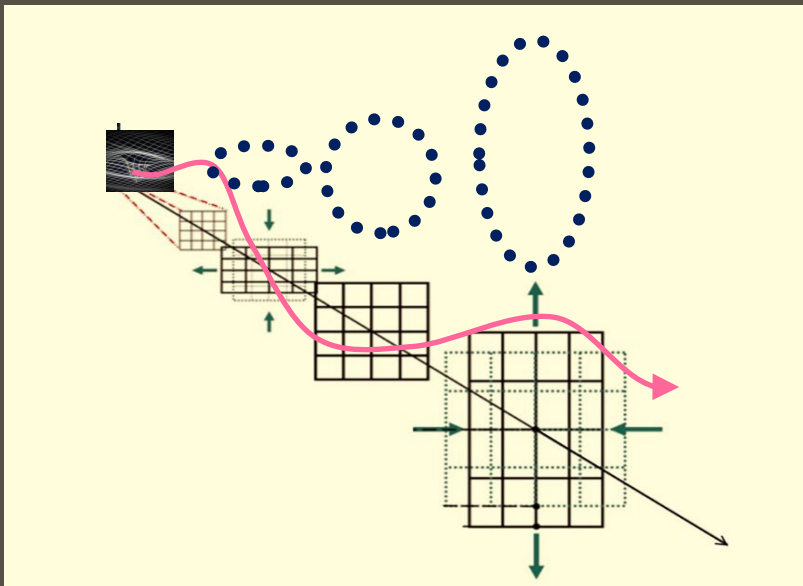
# Primordial Gravitational Waves

o Vacuum GWs

$$\square h_{ij}=0 \rightarrow h_{\pm} = h_{\pm}^{vac}$$



Circular polarizations



# Primordial Gravitational Waves

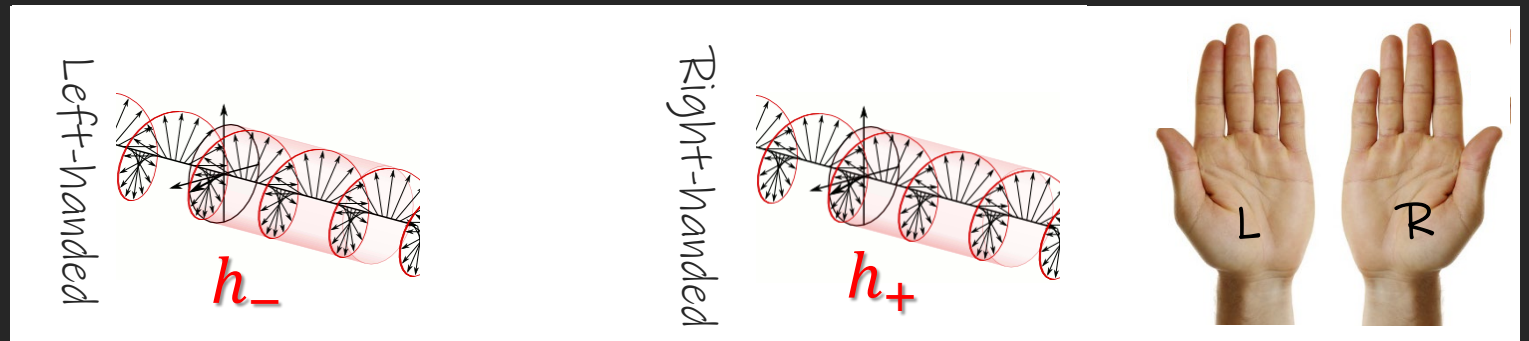
- o Vacuum GWs

$$\square h_{ij}=0 \rightarrow h_{\pm} = h_{\pm}^{vac}$$

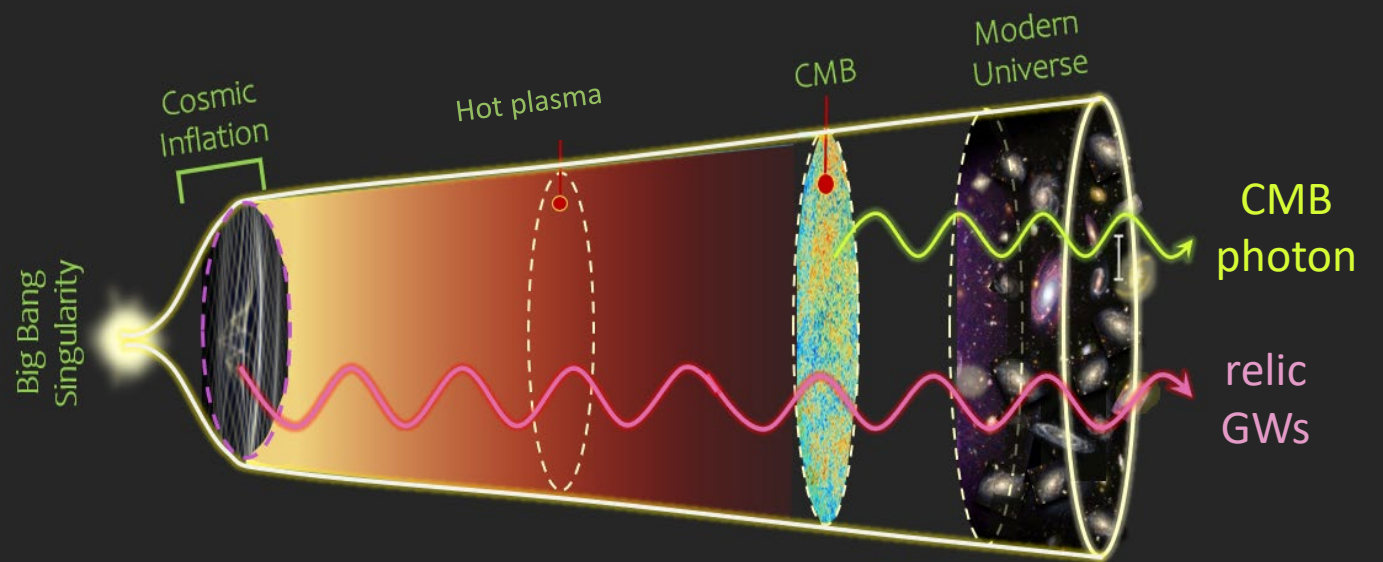
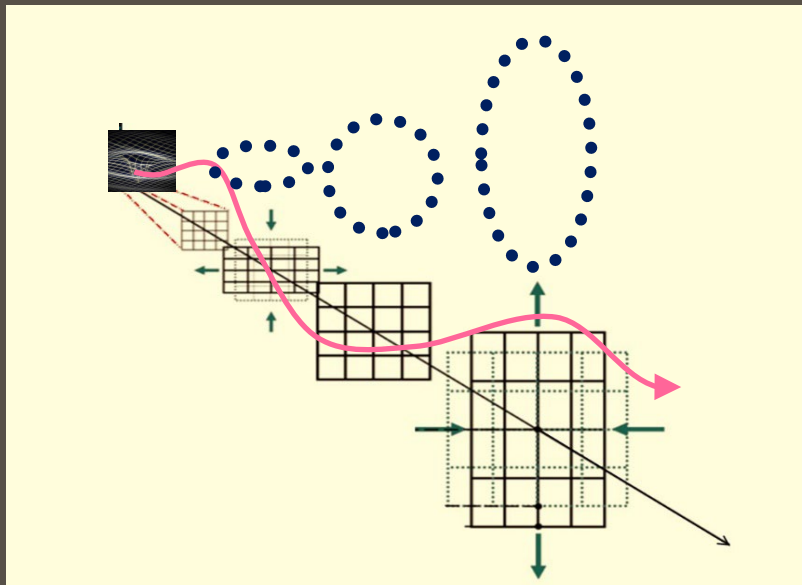
- o Unpolarized

$$\langle |h_{+}^{vac}|^2 \rangle = \langle |h_{-}^{vac}|^2 \rangle$$

- o Nearly Gaussian



Circular polarizations





# Cosmic Perturbations - Gravitational Waves

- Inflation also predicts primordial GWs:

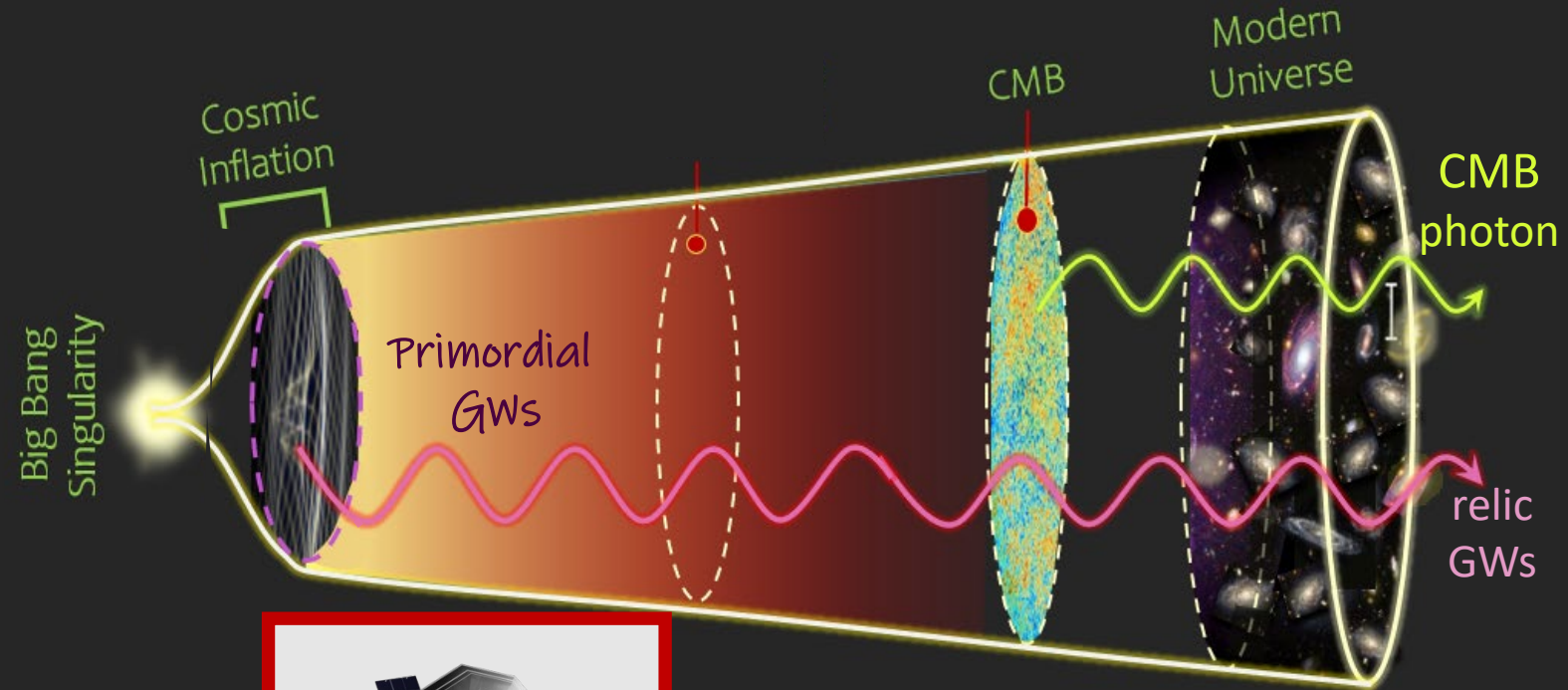
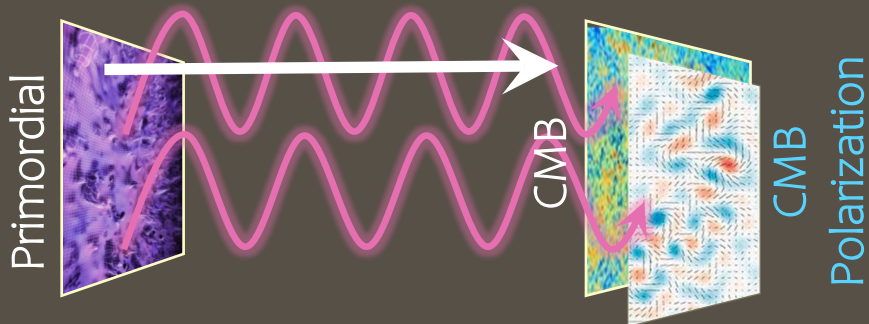
$$\square h_{ij}=0 \rightarrow h_{\pm} = h_{\pm}^{vac}$$

- Unpolarized

$$\langle |h_{+}^{vac}|^2 \rangle = \langle |h_{-}^{vac}|^2 \rangle$$

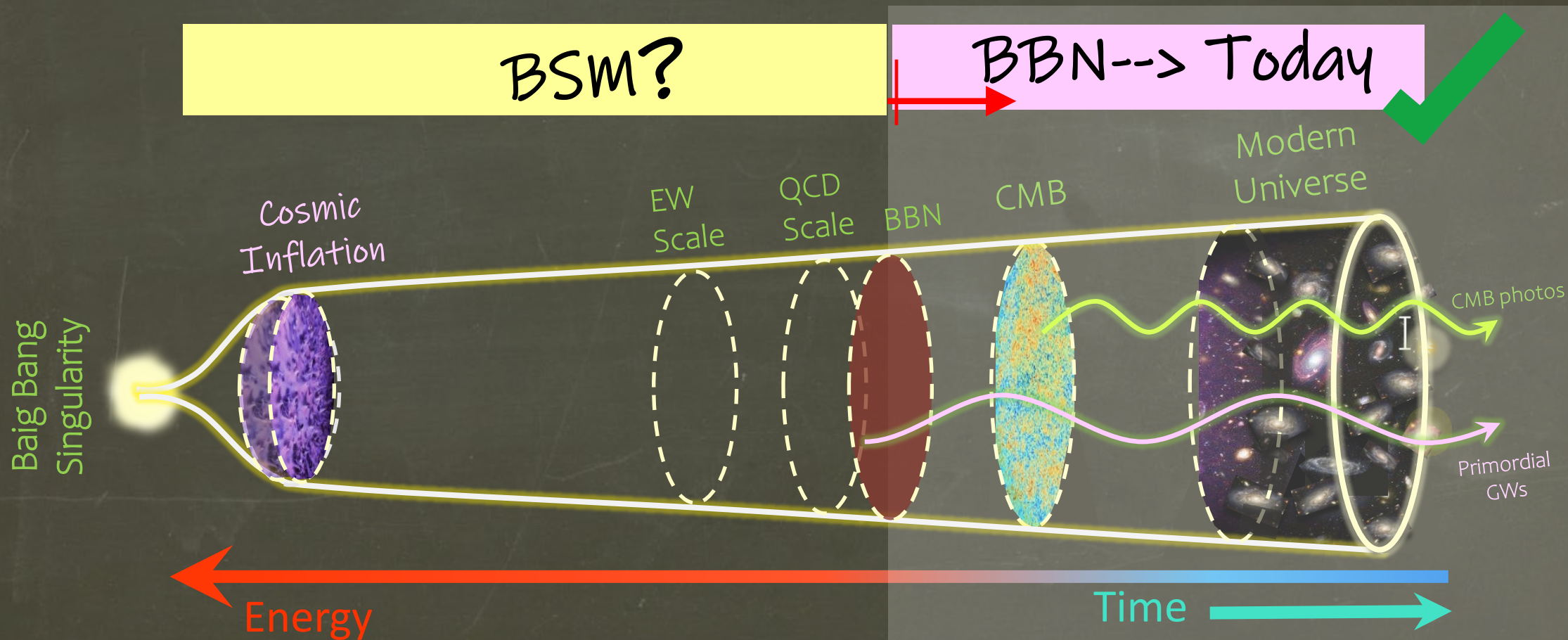
- Nearly Gaussian

- CMB polarization



# Puzzles of SM & Cosmology

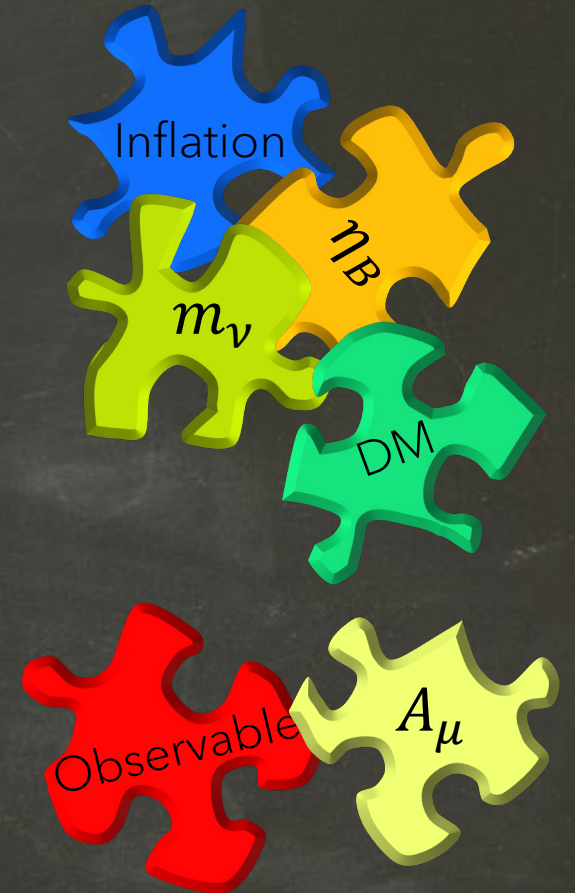
Modern cosmology remarkably successful from BBN until today!  
But the physics before BBN is still much less certain!



# Puzzles of SM & Cosmology

- I) Particle physics of Inflation
- II) Origin of matter asymmetry
- III) Origin of Neutrino mass
- IV) Particle nature of DM

Puzzles of  
Standard Model of Particle Physics (SM)  
& Cosmology which need  
Physics Beyond SM



# Puzzles of SM & Cosmology

- I) Particle physics of Inflation
- II) Origin of matter asymmetry
- III) Origin of Neutrino mass
- IV) Particle nature of DM

Puzzles of  
Standard Model of Particle Physics (SM)  
& Cosmology Which need  
Physics Beyond SM

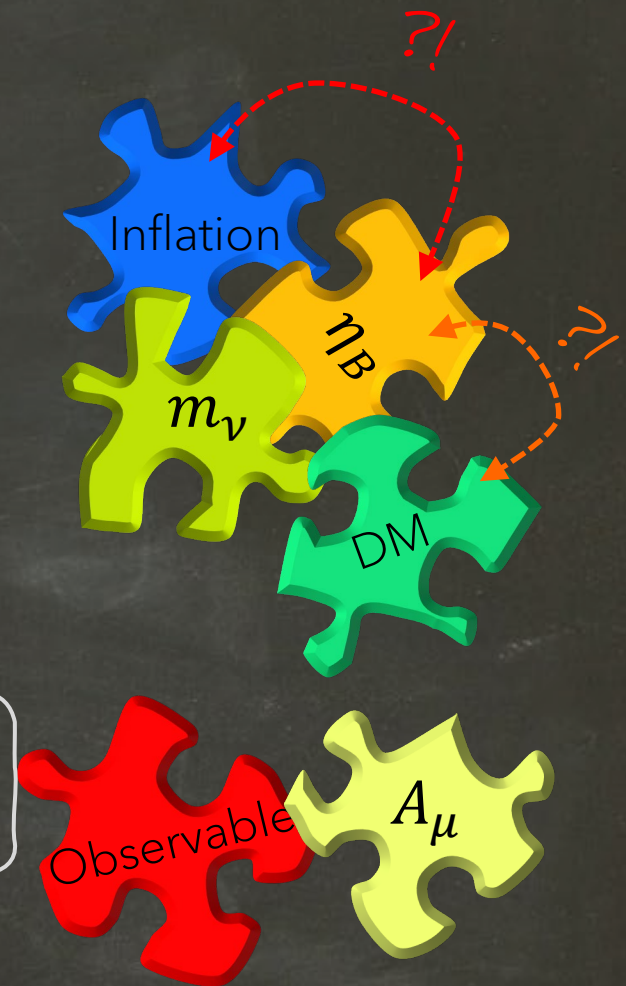
◆ Curious cosmological coincidences  $\eta_B \approx 0.3 P_\zeta$  and  $\Omega_{DM} \approx 5\Omega_B$ !

$$\eta_B = \frac{n_B - n_{\bar{B}}}{n_\gamma} \approx 6 \times 10^{-10}$$

Baryon to Photon Ratio  
Today

$$P_\zeta = \frac{1}{2\epsilon} \left( \frac{1}{2\pi} \frac{H}{M_{pl}} \right)^2 \approx 2 \times 10^{-9}$$

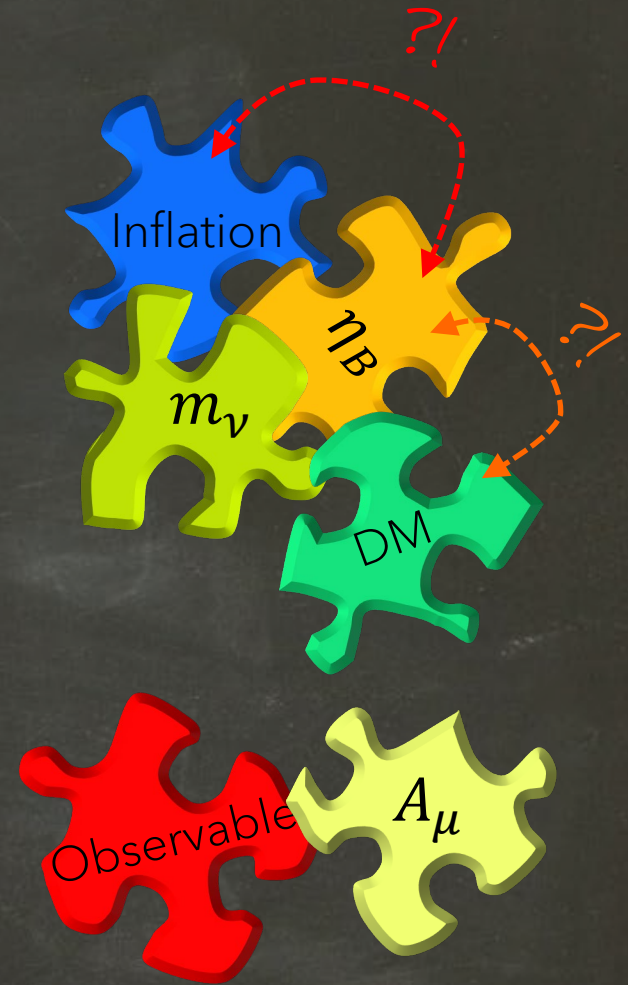
Curvature Power Spectrum in  
Inflation



# Puzzles of SM & Cosmology

- I) Particle physics of Inflation
- II) Origin of matter asymmetry
- III) Origin of Neutrino mass
- IV) Particle nature of DM

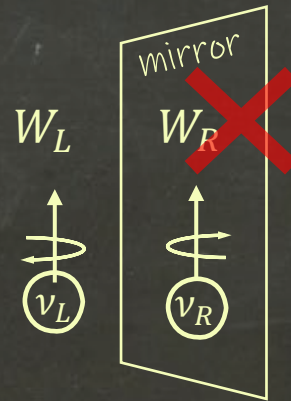
Puzzles of Standard Model of Particle Physics (SM) & Cosmology Which need Physics Beyond SM



Curious cosmological coincidences  $\eta_B \simeq 0.3 P_z$  and  $\Omega_{DM} \simeq 5\Omega_B!$

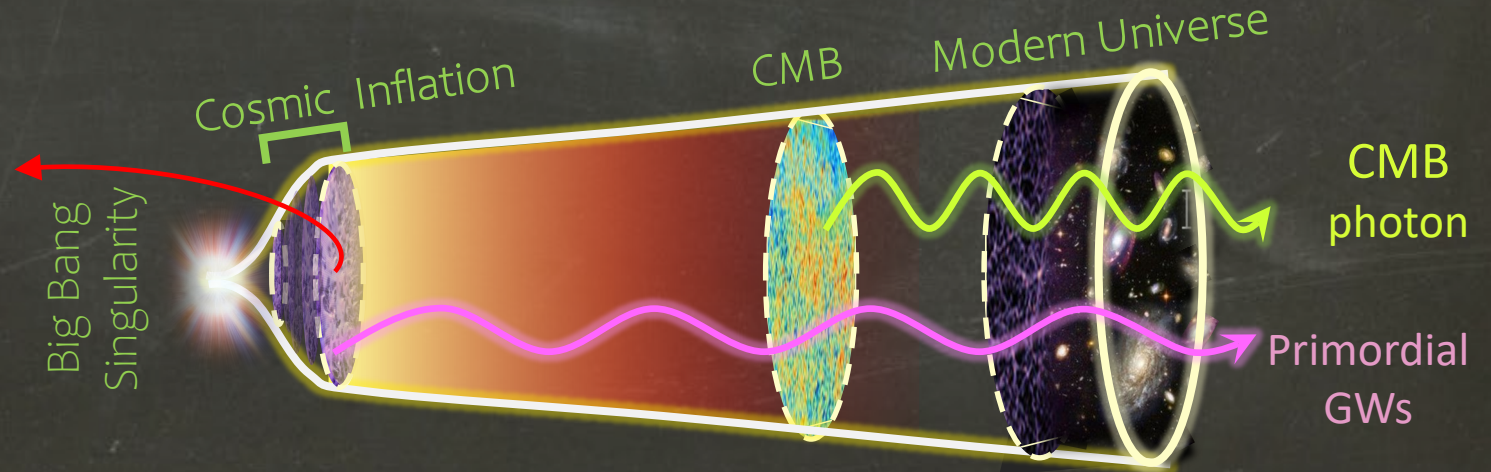
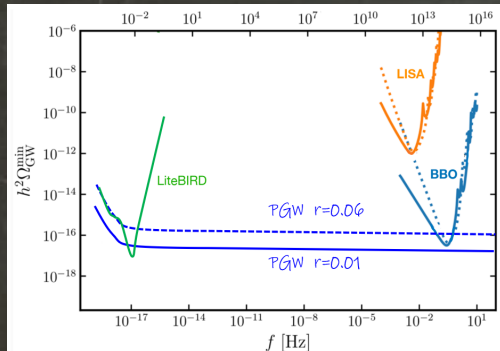
- 1. Ad hoc parity violation
- 2. Accidental B-L global symmetry
- 3. Vacuum Stability problem

SM as a particle physics model also faces some conceptual issues



# As Yet

- Observations are in perfect agreement with Inflation.
- The Particle Physics of Inflation is still unknown.
- The Standard models of inflation are based on Scalars.  
Inflation Particle Physics: a scalar singlet BSM
- Primordial Gravitational Waves  
Unpolarized, Gaussian



# As Yet

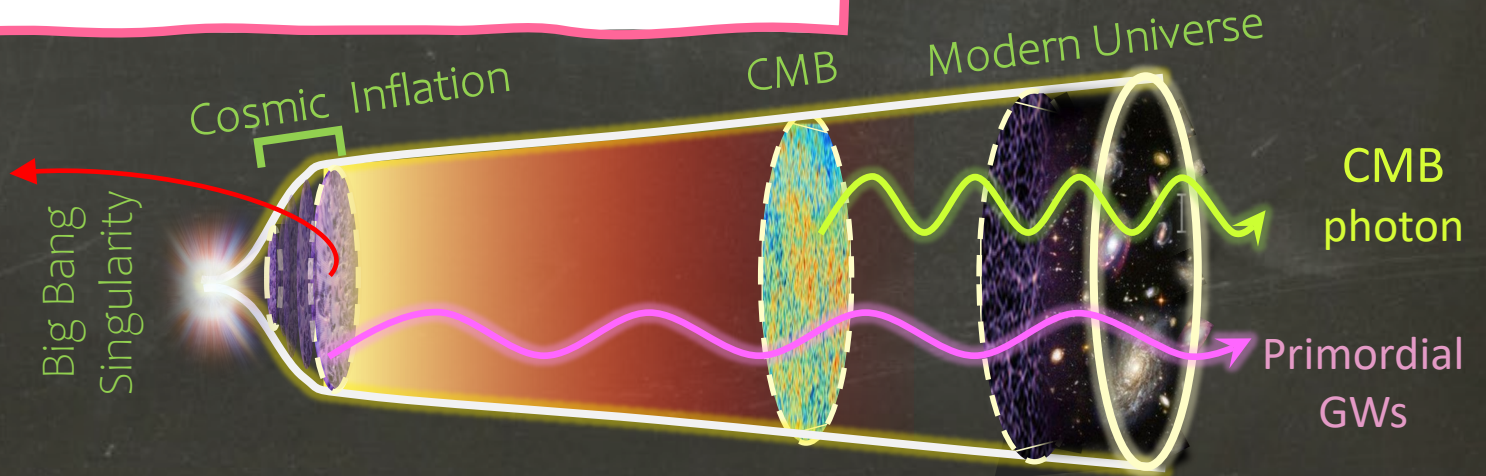
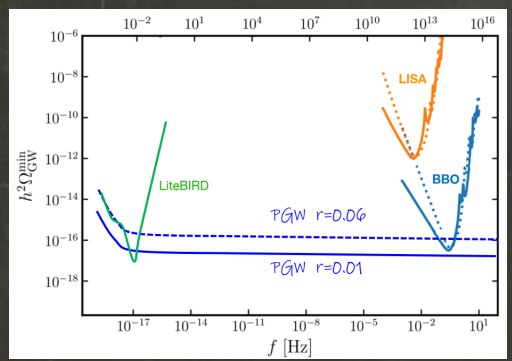
- Observations are in perfect agreement with Inflation.
- The Particle Physics of Inflation is still unknown.
- The Standard models of inflation are based on Scalars.

IV

What about Gauge Fields?!

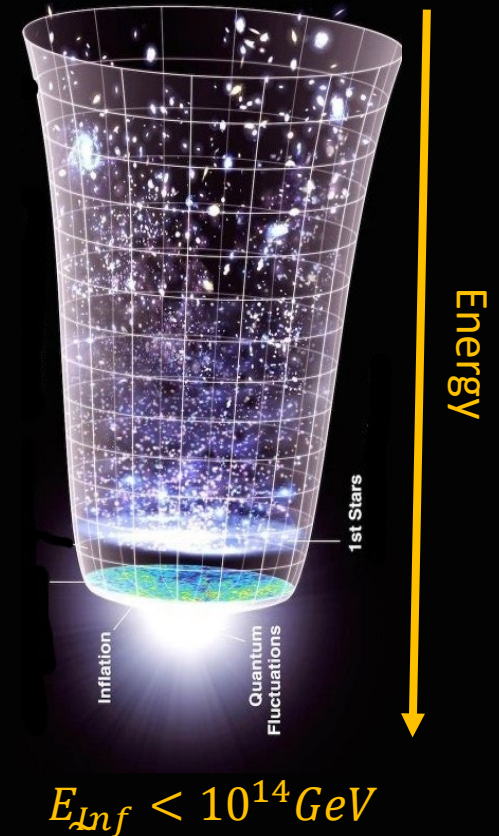
- Pr

Unpolarized, Gaussian



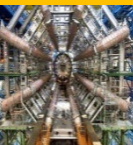
# Why Gauge Fields in Inflation?!

- Why not?
  - Inflation happened at highest energy scales observable!
  - Gauge fields are ubiquitous, building blocks of SM & beyond.
- What do they do in inflation?



Comparing to LHC

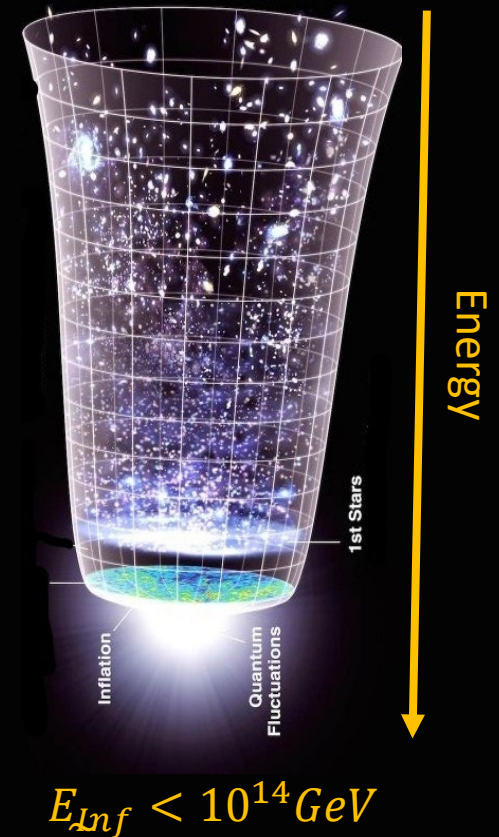
$$\frac{E_{Inf}}{E_{LHC}} \sim 10^{11} \text{ !!!!}$$





# Why Gauge Fields in Inflation?!

- Why not?
  - Inflation happened at highest energy scales observable!
  - Gauge fields are ubiquitous, building blocks of SM & beyond.
- What do they do in inflation?
  - I. Can Gauge Fields Contribute to Physics of Inflation?  
Yes!
  - II. Do they leave an observable signature?  
Yes! Robust prediction for GW background.
  - III. How much they can change the cosmic history?  
A lot! Novel mechanisms for Baryo- and Dark-genesis.



Comparing to LHC

$$\frac{E_{Inf}}{E_{LHC}} \sim 10^{11} \text{ !!!!}$$



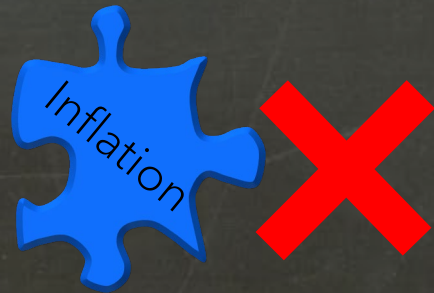
# I) Axion-inflation & gauge fields (non-Abelian)

---

# Challenges:

Gauge fields given by Yang-Mills

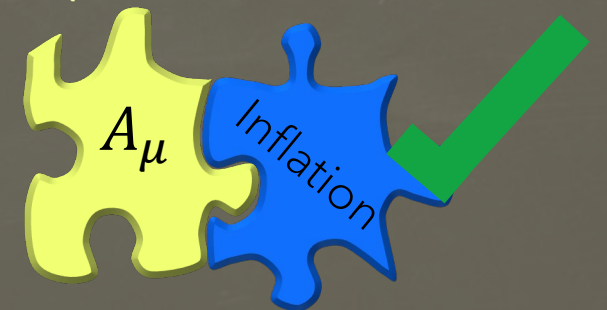
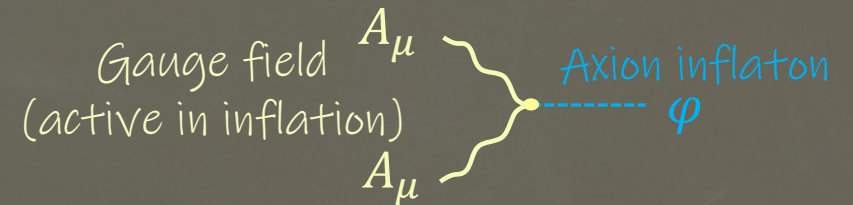
dilutes like radiation  $A_\mu \sim 1/a$



Gauge fields coupled to inflaton  
are generated in inflation.

$$\frac{\lambda}{8f} F \tilde{F} \varphi \quad \text{Axion}$$

(Axion fields are naturally  
coupled to gauge fields.)



# Challenges:

Gauge fields given by Yang-Mills

dilutes like radiation  $A_\mu \sim 1/a$

Spatial isotropy & homogeneity

U(1) vacuum  $A_\mu$

$$A_i = Q(t) \delta_i^3$$



Gauge fields coupled to inflaton  
are generated in inflation.

$$\frac{\lambda}{8f} F \tilde{F} \varphi \quad \text{Axion}$$

(Axion fields are naturally  
coupled to gauge fields.)

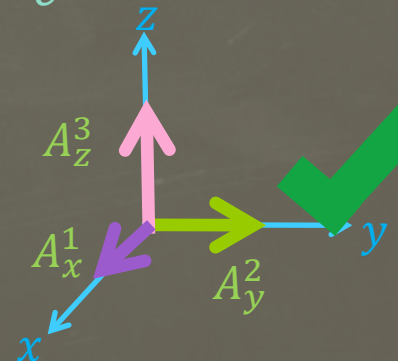
A.M. & Sheikh-Jabbari, 2011

SU(2) vacuum  $A_\mu = A_\mu^a T_a$

$$[T_a, T_b] = i \varepsilon^{abc} T_c$$

Spatially isotropic

$$A_i^a = Q(t) \delta_i^a$$



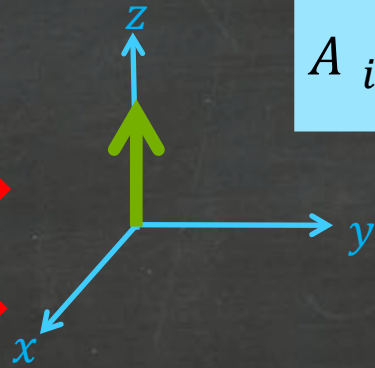
so(3) & su(2) are isomorphic

# How SU(2) restores isotropy?

Let us work in temporal gauge,  $A_0 = 0$ .

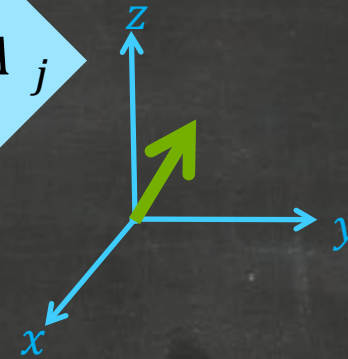
U(1) vacuum  $A_\mu$

$$A_i = Q(t)\delta_i^3$$



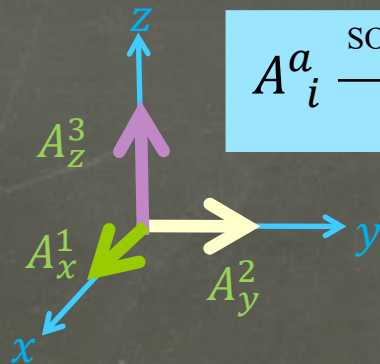
Rotation

$$A_i \xrightarrow{SO(3)} R_{ij} A_j$$



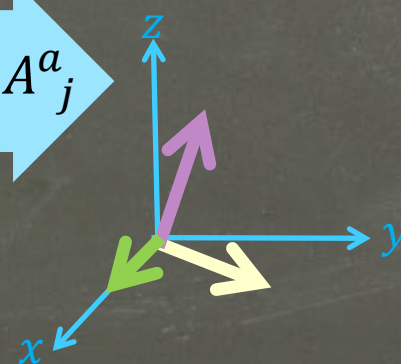
SU(2) VEV,  $A_\mu = A_\mu^a T_a$

$$A_i^a = Q(t)\delta_i^a$$



Rotation

$$A_i^a \xrightarrow{SO(3)} R_{ij} A_j^a$$

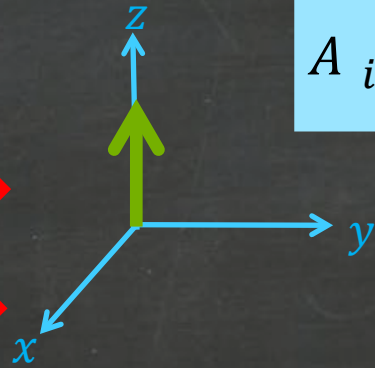


# How SU(2) restores isotropy?

Let us work in temporal gauge,  $A_0 = 0$ .

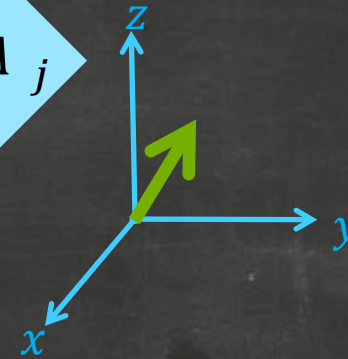
U(1) vacuum  $A_\mu$

$$A_i = Q(t)\delta_i^3$$



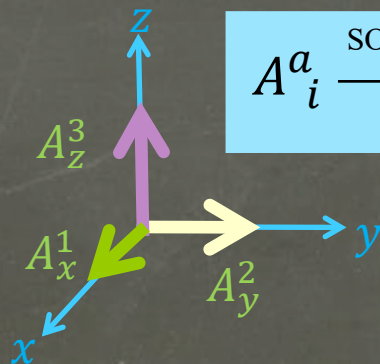
Rotation

$$A_i \xrightarrow{SO(3)} R_{ij} A_j$$



SU(2) VEV,  $A_\mu = A_\mu^a T_a$

$$A_i^a = Q(t)\delta_i^a$$

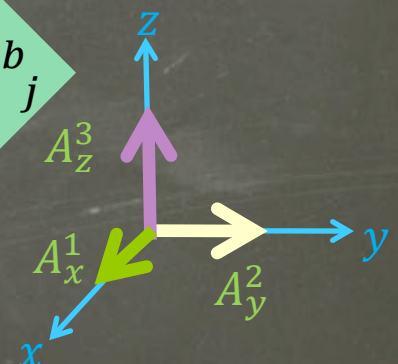
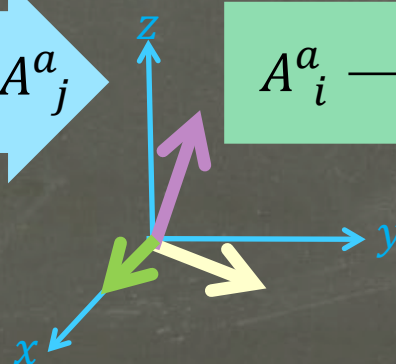


Rotation

$$A_i^a \xrightarrow{SO(3)} R_{ij} A_j^a$$

Gauge Transformation

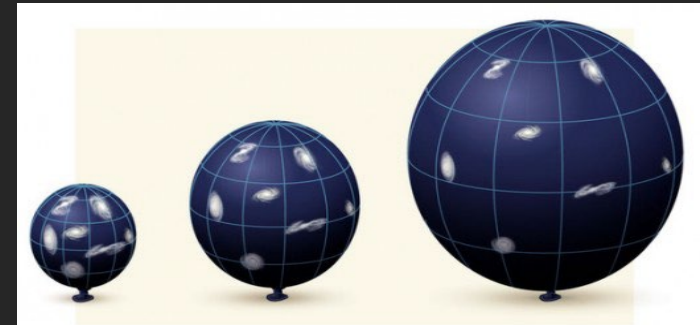
$$A_i^a \rightarrow R_{ab} A_j^b$$



# SU(2) Gauge fields and Initial Anisotropies

- SU(2) gauge fields are **FRW friendly**: (respect isotropy & homogeneity)

$$A_{\mu}^a(t) = \begin{cases} 0 & \mu = 0 \\ Q(t)a(t)\delta_i^a & \mu = i \end{cases}$$

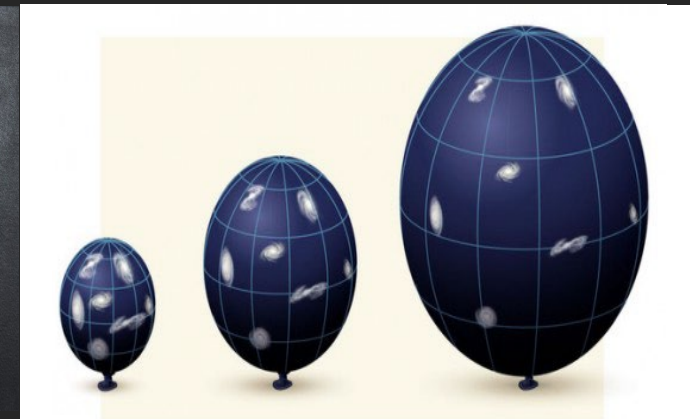
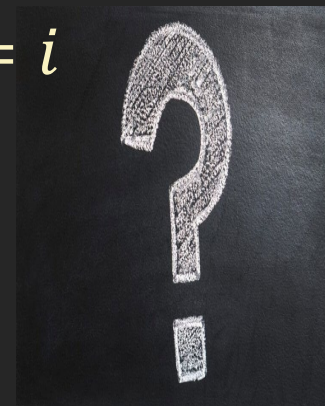


Isotropic  
Background

- How stable is the isotropic ansatz against **initial anisotropies**, i.e. Bianchi

$$A_{\mu}^a(t) = \begin{cases} 0 & \mu = 0 \\ Q(t)a(t)\delta_j^a e^{\lambda_{ij}(t)} & \mu = i \end{cases}$$

Anisotropies in gauge field  $Tr[\lambda_{ij}(t)] = 0$

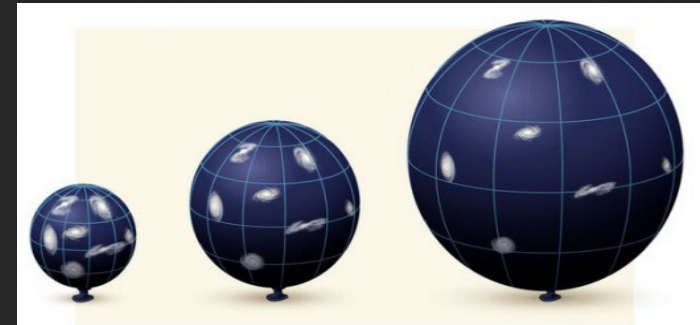


Anisotropic  
Background

# SU(2) Gauge fields and Initial Anisotropies

- SU(2) gauge fields are **FRW friendly**: (respect isotropy & homogeneity)

$$A_{\mu}^a(t) = \begin{cases} 0 & \mu = 0 \\ Q(t)a(t)\delta_i^a & \mu = i \end{cases}$$



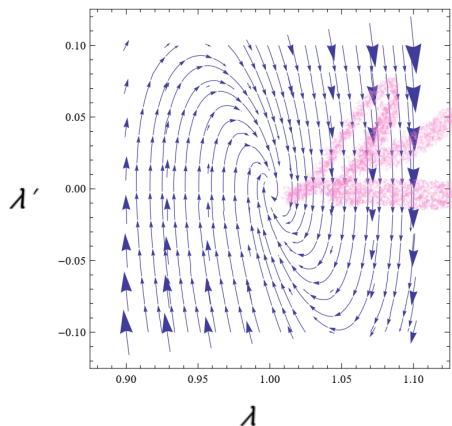
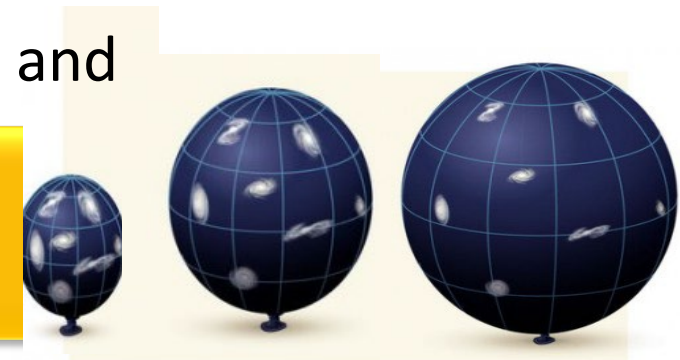
- How stable is the isotropic ansatz against **initial anisotropies**, i.e. Bianchi

I. Wolfson, A. M., T. Murata, E. Komatsu, T. Kobayashi arXiv:2105.06259

Axion is only coupled to the isotropic part of the gauge field,

Anisotropic part decays like radiation and

**Isotropic Solution is the Attractor!**



A. M. and M.M. Sheikh-Jabbari, J. Soda, 2012  
A. M. and E. Erfani, 2013

Isotropic  
Background

~~Anisotropic~~  
Background



# SU(2)-Axion Model Building

- **Gauge-flation** A. M., & Sheikh-Jabbari, 2011

$$S_{Gf} = \int d^4x \sqrt{-g} \left( -\frac{R}{2} - \frac{1}{4} F^2 + \frac{\kappa}{384} (F\tilde{F})^2 \right) \quad \mathcal{S} = -\mathcal{P}$$

- **Chromo-natural** P. Adshead, M. Wyman, 2012

$$S_{cn} = \int d^4x \sqrt{-g} \left( -\frac{R}{2} - \frac{1}{2} \left( (\partial_\mu \varphi)^2 - \mu^4 \left( 1 + \cos\left(\frac{\varphi}{f}\right) \right) \right) - \frac{1}{4} F^2 - \frac{\lambda}{8f} \varphi F\tilde{F} \right)$$

Natural inflation

Friction

K. Freese, J. A. Frieman and A. V. Olinto 1990

# SU(2)-Axion Model Building

- **Gauge-flation**

A. M., & Sheikh-Jabbari, 2011

$$S_{Gf} = \int d^4x \sqrt{-g} \left( -\frac{R}{2} - \frac{1}{4} F^2 + \frac{\kappa}{384} (F\tilde{F})^2 \right)$$

*Ruled-out by the data*

R. Namba, E. Dimastrogiovanni, M. Peloso 2013

P. Adshead, E. Martinec, M. Wyman 2013

+ Theoretical issue:  
Very large  $\lambda \sim 100!$

D. Baumann & L. McAllister 2014

- **Chromo-natural**

P. Adshead, M. Wyman, 2012

$$S_{cn} = \int d^4x \sqrt{-g} \left( -\frac{R}{2} - \frac{1}{2} \left( (\partial_\mu \varphi)^2 - \mu^4 \left( 1 + \cos\left(\frac{\varphi}{f}\right) \right) \right) - \frac{1}{4} F^2 - \frac{\lambda}{8f} \varphi F\tilde{F} \right)$$

Inspired by them, several different models with SU(2) fields have been proposed & studied.

# An incomplete list of Different Realizations of the SU(2)-Axion Inflation:

1. **A. M.** and M. M. Sheikh-Jabbari, Phys. Rev. D 84:043515, 2011 [[arXiv:1102.1513](#)]
2. P. Adshead, M. Wyman, Phys. Rev. Lett.(2012) [[arXiv:1202.2366](#)]
3. **A. M.** JHEP 07 (2016) 104 [[arXiv:1604.03327](#)]
4. C. M. Nieto and Y. Rodriguez Mod. Phys. Lett. A31 (2016) [[arXiv:1602.07197](#)]
5. E. Dimastrogiovanni, M. Fasiello, and T. Fujita JCAP 1701 (2017) [[arXiv:1608.04216](#)]
6. P. Adshead, E. Martinec, E. I. Sfakianakis, and M. Wyman JHEP 12 (2016) 137 [[arXiv:1609.04025](#)]
7. P. Adshead and E. I. Sfakianakis JHEP 08 (2017) 130 [[arXiv:1705.03024](#)]
8. R. R. Caldwell and C. Devulder Phys. Rev. D97 (2018) [[arXiv:1706.03765](#)]
9. E. McDonough, S. Alexander, JCAP11 (2018) 030 [[arXiv:1806.05684](#) ]
10. L. Mirzaghali, E. Komatsu, K. D. Lozanov, and Y. Watanabe, [[arXiv:2003.04350](#)]
11. Y. Watanabe, E. Komatsu, [[arXiv:2004.04350](#)]
12. J. Holland, I. Zavala, G. Tasinato, [[arXiv:2009.00653](#)]
13. **A. M.** **SU(2)R –axion inflation** [[arXiv:2012.11516](#)]
14. Oksana Iarygina, Evangelos I. Sfakianakis, [[arXiv:2105.06972](#)]
15. T. Fujita, Nakatsuka, K. Mukaida, & K. Murai [[arXiv:2110.03228](#)]

# SU(2)-Axion Model Building

- **Gauge-flation** A. M., & Sheikh-Jabbari, 2011

$$S_{Gf} = \int d^4x \sqrt{-g} \left( -\frac{R}{2} - \frac{1}{4} F^2 + \frac{\kappa}{384} (F\tilde{F})^2 \right)$$

Ruled-out by the data

R. Namba, E. Dimastrogiovanni, M. Peloso 2013  
P. Adshead, E. Martinec, M. Wyman 2013

+ Theoretical issue:  
Very large  $\lambda \sim 100!$

D. Baumann & L. McAllister 2014

- **Chromo-natural** P. Adshead, M. Wyman, 2012

$$S_{Cn} = \int d^4x \sqrt{-g} \left( -\frac{R}{2} - \frac{1}{4} F^2 - \frac{1}{2} \left( (\partial_\mu \varphi)^2 - \mu^4 \left( 1 + \cos\left(\frac{\varphi}{f}\right) \right) \right) - \frac{\lambda}{8f} \varphi F\tilde{F} \right)$$

SU(2)-Axion inflation has a very rich phenomenology:

- A new mechanism for generation of Primordial Gravitational Waves
- All Sakharov conditions are satisfied in inflation: a new baryogenesis mechanism
- Particle Production in inflation by Schwinger effect and chiral anomaly
- Common Origin for inflation, Baryogenesis & CDM production

P. Adshead et. al 2013

Dimastrogiovanni et. al 2013

A. M. et. al, 2013

A. M. 2014 & A.M. 2016

R. Caldwell et. al 2017

A. M. 2021

K. Lozanov, A. M, E. Komatsu 2017,

L. Mirzagholi, A. M, K. Lozanov 2019,

Domcke et al 2019, A.M. 2019

A.M. 2021

# SU(2)-Axion Model Building

- Gauge-flation A. M., & Sheikh-Jabbari, 2011

$$S_{Gf} = \int d^4x \sqrt{-g} \left( -\frac{R}{2} - \frac{1}{4} F^2 + \frac{\kappa}{384} (F\tilde{F})^2 \right)$$

- Chromo-natural P. Adshead, M. Wyman, 2012

$$S_{Cn} = \int d^4x \sqrt{-g} \left( -\frac{R}{2} - \frac{1}{4} F^2 - \frac{1}{2} \left( (\partial_\mu \varphi)^2 - \mu^4 \left( 1 + \cos\left(\frac{\varphi}{f}\right) \right) \right) - \frac{\lambda}{8f} \varphi F\tilde{F} \right)$$

- Minimal Scenario of **SU(2)-axion inflation** A. M., 2016  $f < 0.1 M_{\text{pl}}$  &  $\lambda < 0.1$

$$S_{AM} = \int d^4x \sqrt{-g} \left( -\frac{R}{2} - \frac{1}{2} \left( (\partial_\mu \varphi)^2 - V(\varphi) \right) - \frac{1}{4} F^2 - \frac{\lambda}{8f} \varphi F\tilde{F} \right)$$

Axion Monodromy or any mechanism that gives a flat potential

## II) Cosmic Perturbations

Axion field perturbations  $\delta\varphi$

Metric perturbations  $\delta g_{\mu\nu}$

Decomposition of fluctuation

Scalar  
Vector  
Tensor

The only tensorial modes are in the metric, i.e, GWs!  $\square h_{ij}=0$

Primordial GWs are sourceless

## II) Cosmic Perturbations

Axion field perturbations  $\delta\varphi$

Metric perturbations  $\delta g_{\mu\nu}$

+

Gauge field perturbations  $\delta A_i^a$

Decomposition of fluctuation

Scalar  
Vector  
Tensor

$$\square h_{ij} = S_{ij}$$

The perturbed gauge field has a tensorial which sources GWs!

# New Tensorial mode in SU(2) Gauge Field

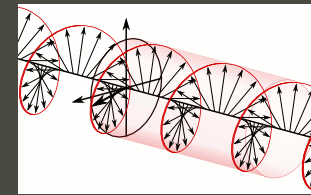
$$\bullet \delta A_i^a = (B_+(t, k)e_{ij}^+(\vec{k}) + B_-(t, k)e_{ij}^-(\vec{k})) \delta_j^a$$

$$B_{\pm}'' + \underbrace{\left[ k^2 \mp \delta_c k \mathcal{H} + \frac{m^2}{H^2} \mathcal{H}^2 - \frac{a''}{a} \right]}_{\text{effective frequency}} B_{\pm} \approx 0$$

( $\delta_c$  and  $\frac{m^2}{H^2}$  are given by BG)

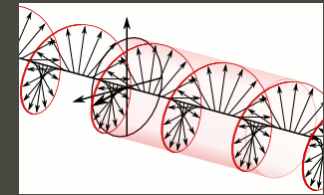
Right-handed

Circular polarizations



$B_+$

Left-handed



$B_-$

$B_{\pm}$  is a new tensorial mode in the perturbed SU(2) gauge field!

A.M. & Sheikh-Jabbari, 2011



# New Tensorial mode in SU(2) Gauge Field

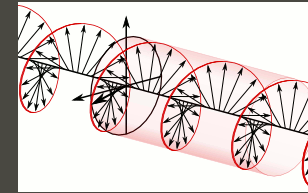
- $\delta A_i^a = (B_+(t, k)e_{ij}^+(\vec{k}) + B_-(t, k)e_{ij}^-(\vec{k})) \delta_j^a$

$$B_{\pm}'' + \underbrace{\left[ k^2 \mp \delta_c k \mathcal{H} + \frac{m^2}{H^2} \mathcal{H}^2 - \frac{a''}{a} \right]}_{\text{effective frequency}} B_{\pm} \approx 0$$

( $\delta_c$  and  $\frac{m^2}{H^2}$  are given by BG)

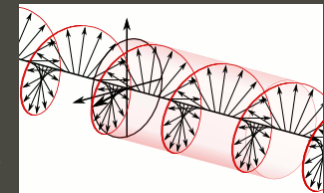
Right-handed

Circular polarizations



$B_+$

Left-handed



$B_-$

Vacuum structure

Axion field  $\langle \varphi \rangle$

( $\delta_c > 0$ )

Slow-roll A

$\langle \delta_a^i A_i^a \rangle$

Slow-roll  $A_p$

Parity

( $\delta_c < 0$ )

$B_{\pm}$  is a new tensorial mode in the perturbed SU(2) gauge field!

A.M. & Sheikh-Jabbari, 2011

# New Tensorial mode in SU(2) Gauge Field

- $\delta A_i^a = (B_+(t, k)e_{ij}^+(\vec{k}) + B_-(t, k)e_{ij}^-(\vec{k})) \delta_j^a$

$$B_{\pm}'' + \underbrace{\left[ k^2 \mp \delta_c k \mathcal{H} + \frac{m^2}{H^2} \mathcal{H}^2 - \frac{a''}{a} \right]}_{\text{effective frequency}} B_{\pm} \approx 0$$

( $\delta_c$  and  $\frac{m^2}{H^2}$  are given by BG)

For  $\delta_c > 0$

Short tachyonic growth of  $B_+$



Chiral Field

$$n_B \sim \frac{H^3}{6\pi^2} \delta_c^3 e^{\frac{(2-\sqrt{2})\pi}{2} \delta_c}$$

Particle Production

A. M. and E. Komatsu, 2018

## Vacuum structure

Axion field  $\langle \phi \rangle$

( $\delta_c > 0$ )

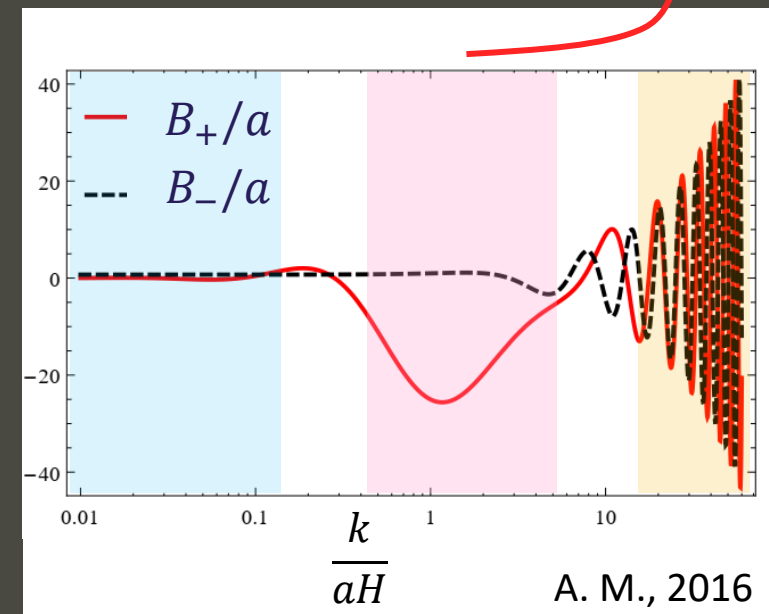
Slow-roll A

$\langle \delta_a^i A_i^a \rangle$

Slow-roll  $A_p$

Parity

( $\delta_c < 0$ )



A. M., 2016

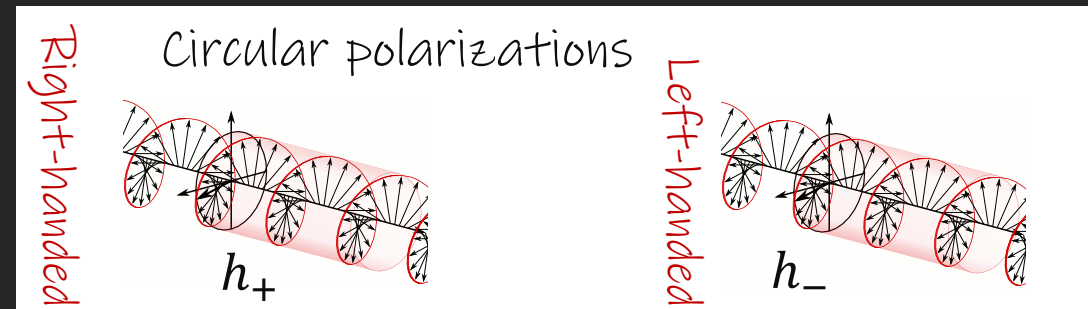
# Gauge Field sources Primordial GWs

- $\delta A_i^a = (B_+(t, k)e_{ij}^+(\vec{k}) + B_-(t, k)e_{ij}^-(\vec{k})) \delta_j^a$
- The field equation:  $B_{\pm}'' + [k^2 \mp \delta_c k \mathcal{H} + \frac{m^2}{H^2} \mathcal{H}^2 - \frac{a''}{a}] B_{\pm} \approx 0$



- That sourced the GWs

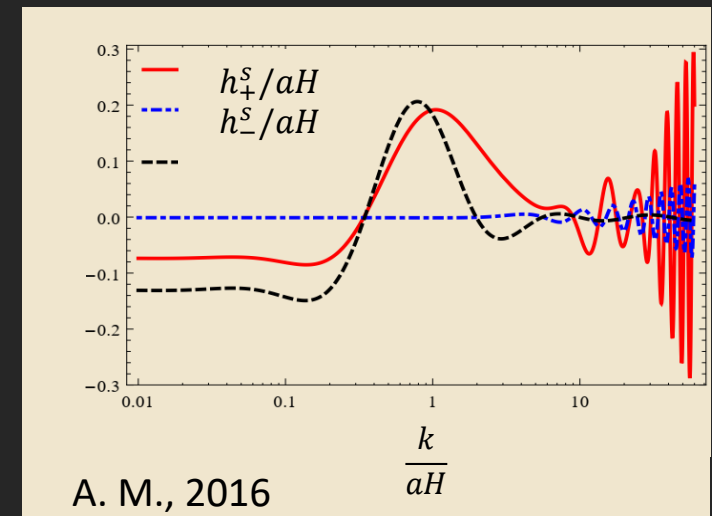
$$h_{\pm}'' + [k^2 - \frac{a''}{a}] h_{\pm} = \mathcal{H}^2 \Pi_{\pm}[B_{\pm}]$$



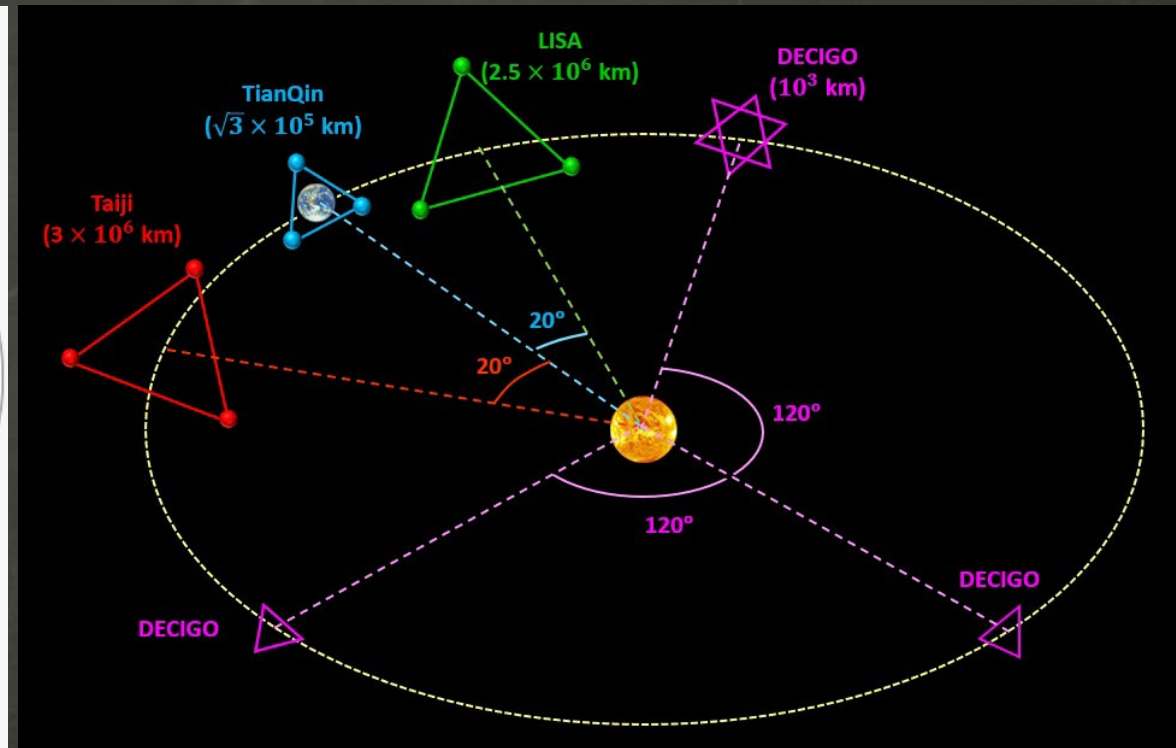
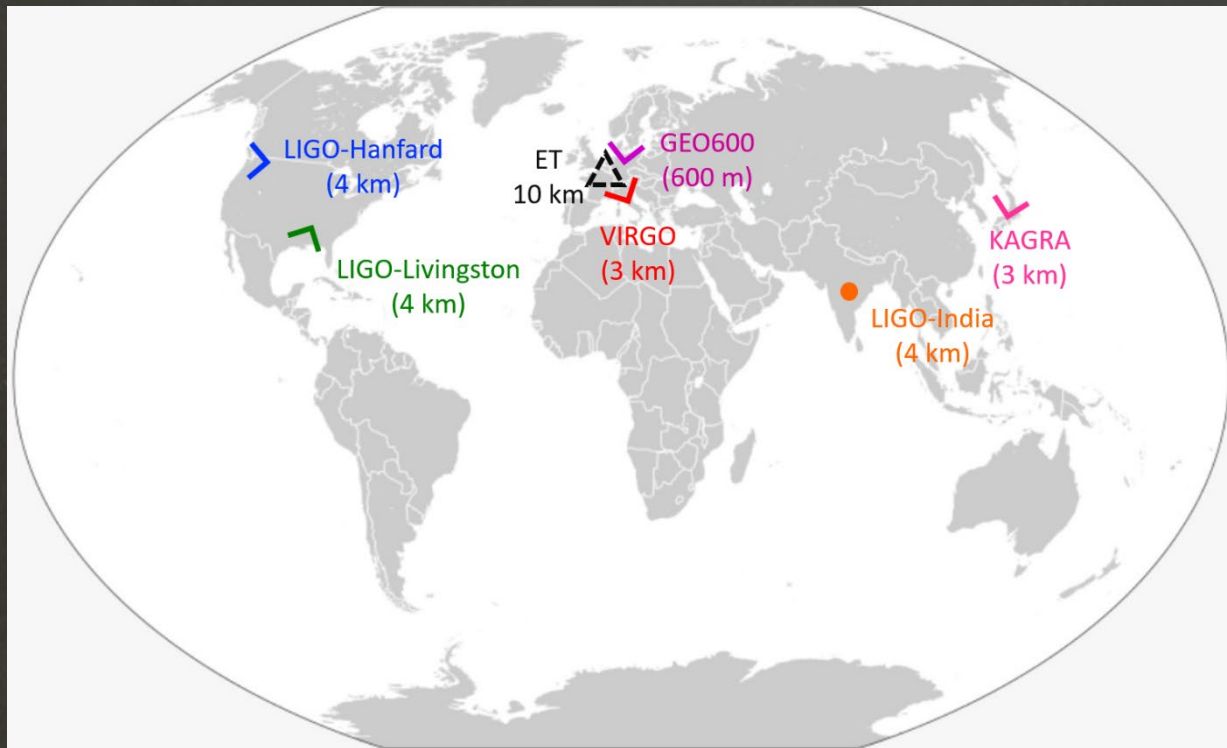
- Gravitational waves have two uncorrelated terms



$$h_{\pm} = \underbrace{h_{\pm}^{vac}}_{\substack{\text{Vacuum} \\ \text{GWs} \\ \text{unpolarized} \\ h_+^{vac} = h_-^{vac}}} + \underbrace{h_{\pm}^s}_{\substack{\text{Sourced by} \\ B_{\pm} \\ \text{Polarized} \\ h_+^s \neq h_-^s}}$$



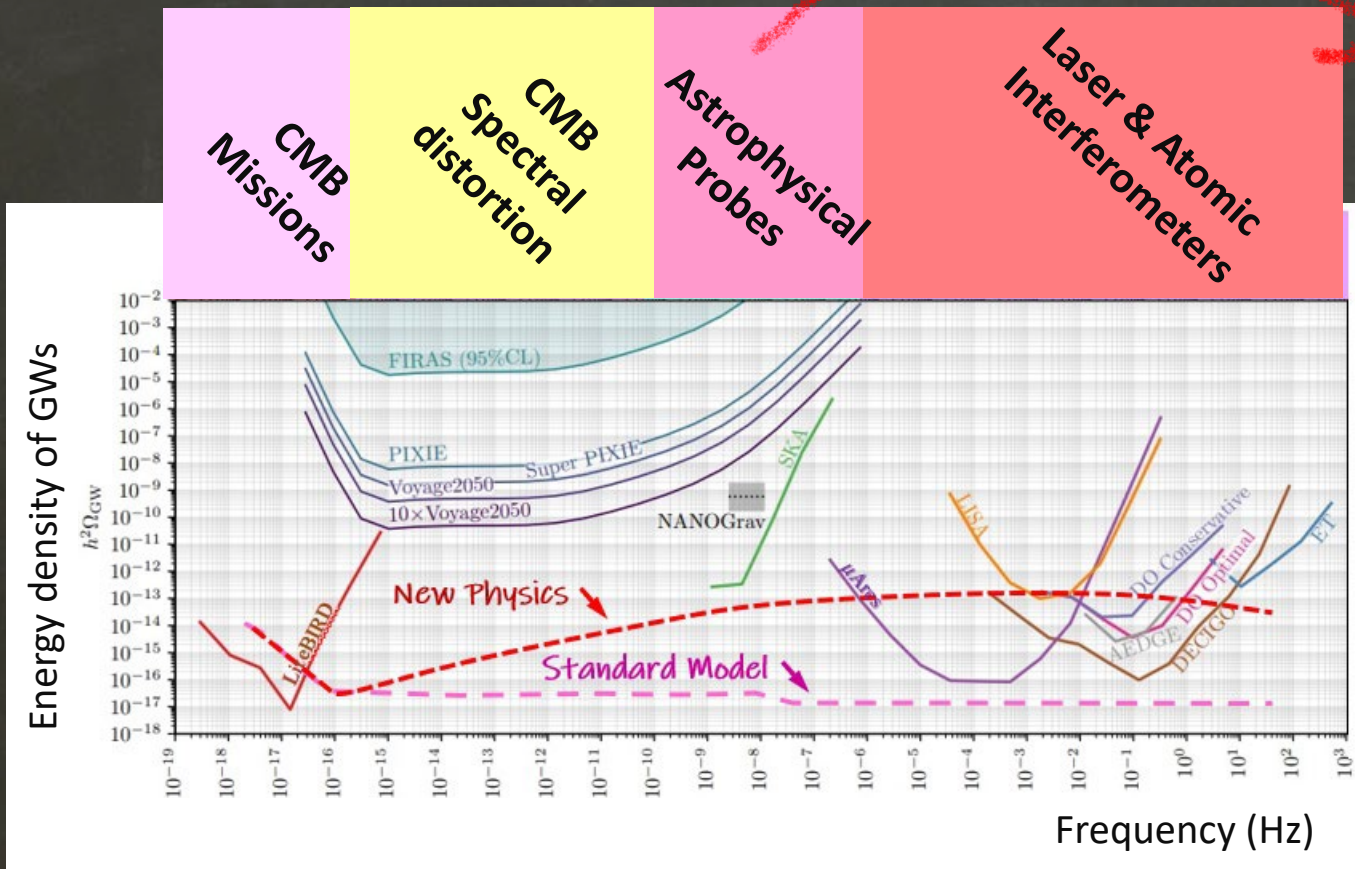
# Networks of GWs Detectors



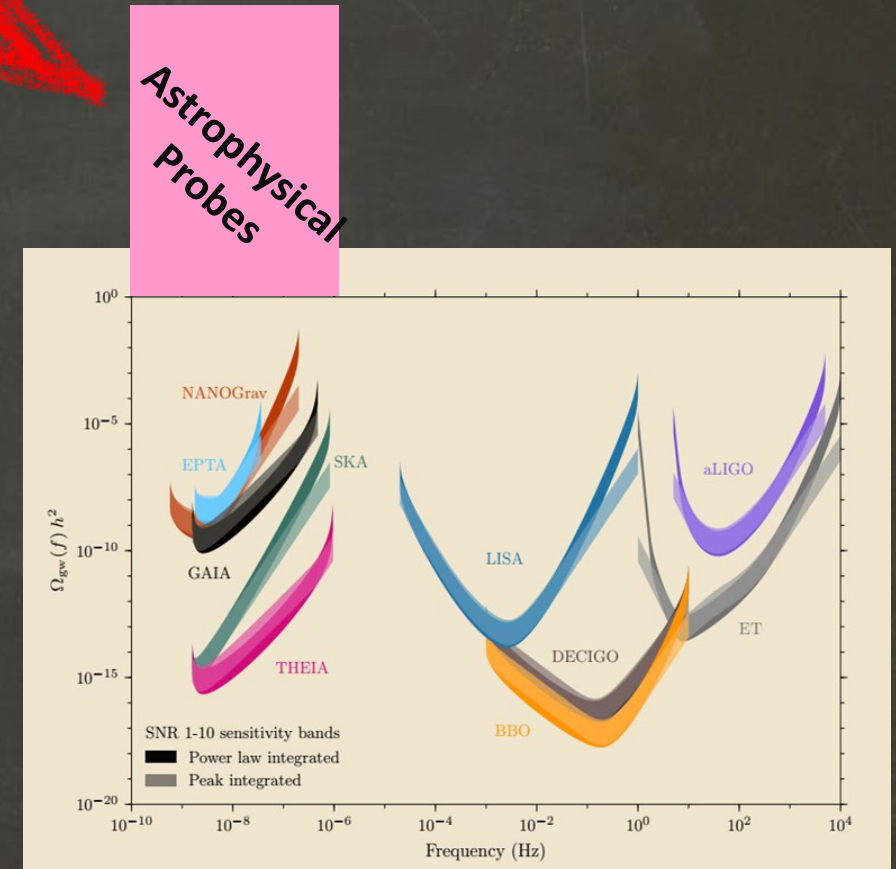
Network of laser interferometer detectors of GWs on Earth (left) & in the sky (right)

# Sensitivity curves on energy density of GWs

Detection of this background is an excellent target for all GW experiments across at least 21 decades in frequencies.



P. Campeti, E. Komatsu, D. Poletti, C. Baccigalupi 2021



J. Garcia-Bellido, H. Murayama, and G. White 2021

# Novel Observable Signature: CMB

- The sourced tensor modes is Highly non-Gaussian.

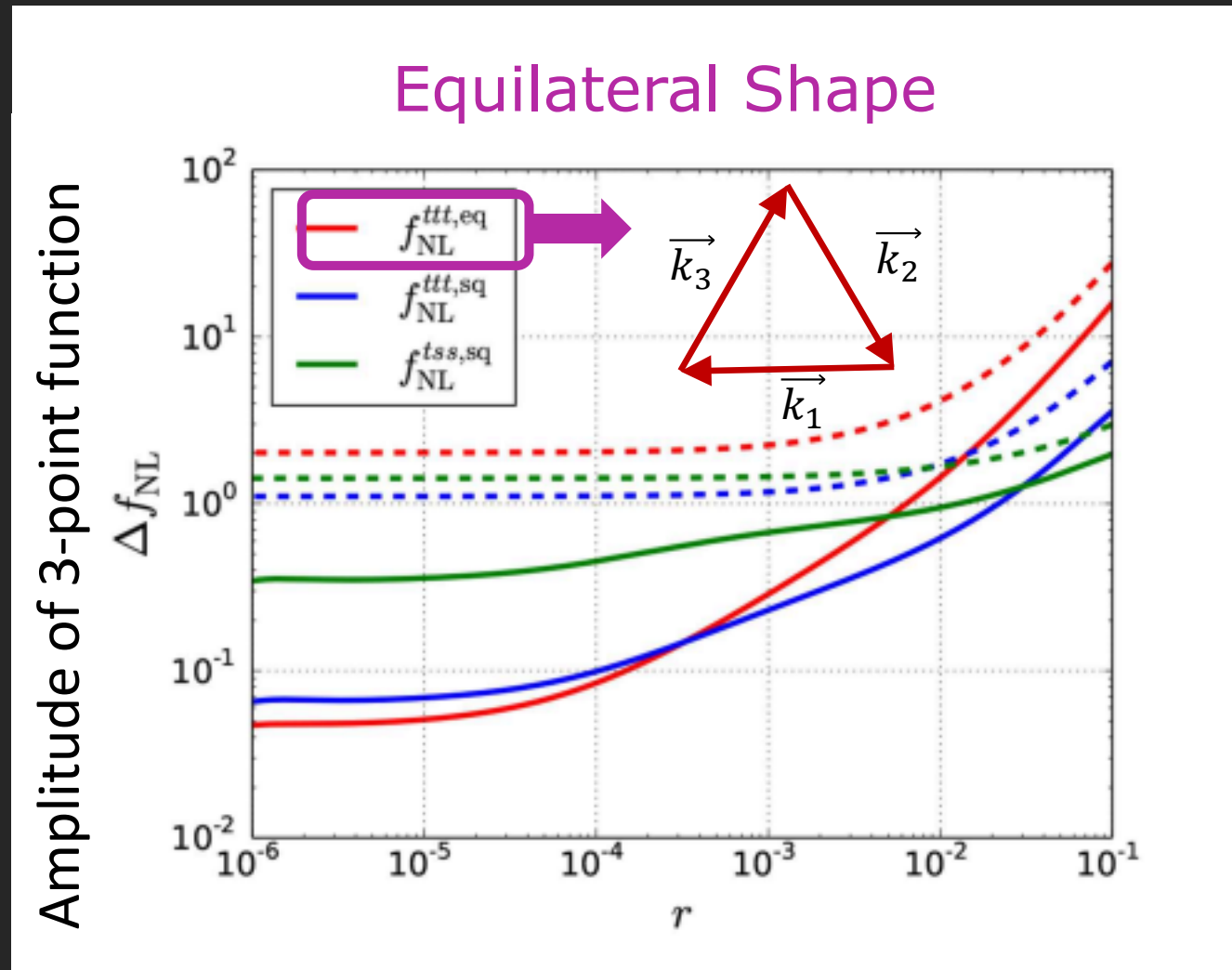
$$F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu - \underbrace{ig [A_\mu, A_\nu]}_{\text{Self-interaction}}$$

Agrawal, Fujita, Komatsu 2018

- That can be probe with future CMB missions., e.g. *Litebird*



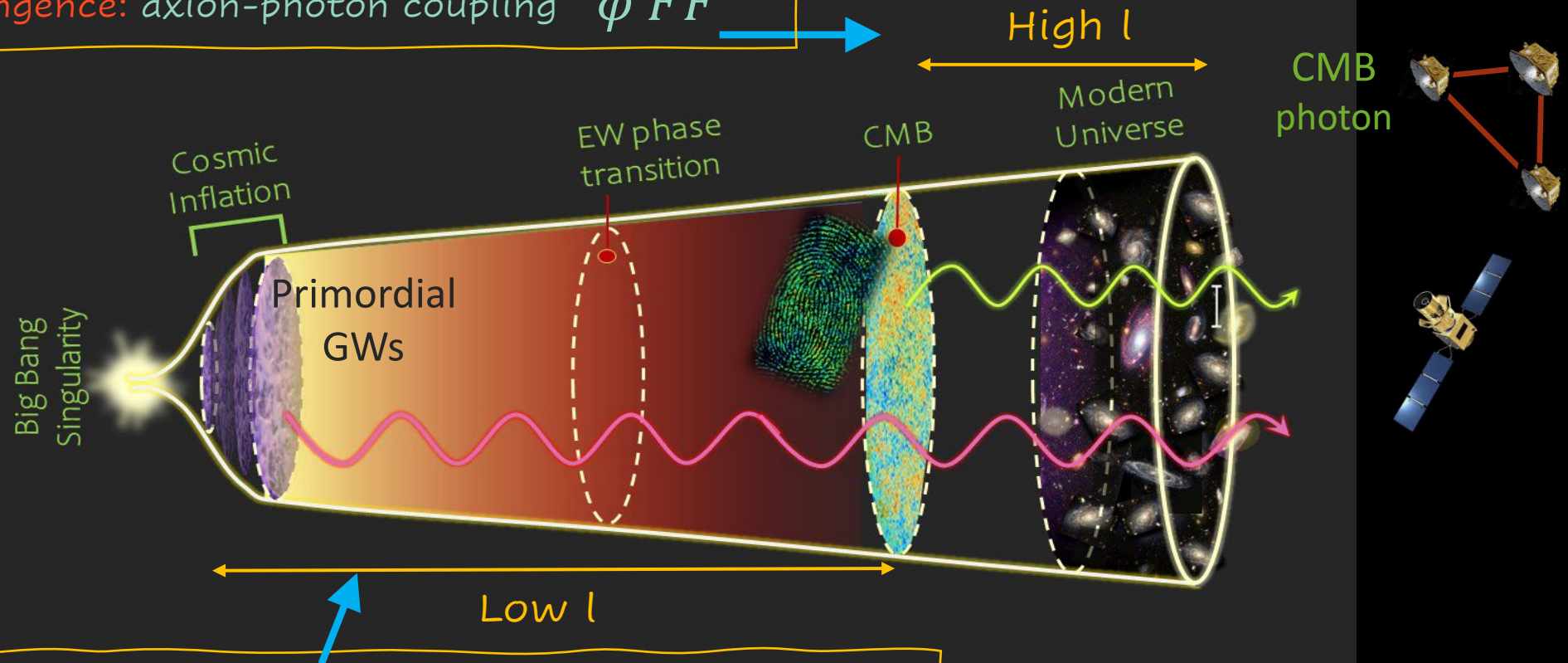
and *CMB-S4*!



# Parity Odd CMB Correlations: TB & EB $\neq 0$

Sources of Parity violation on CMB:

- Cosmic Birefringence: axion-photon coupling  $\varphi F \tilde{F}$



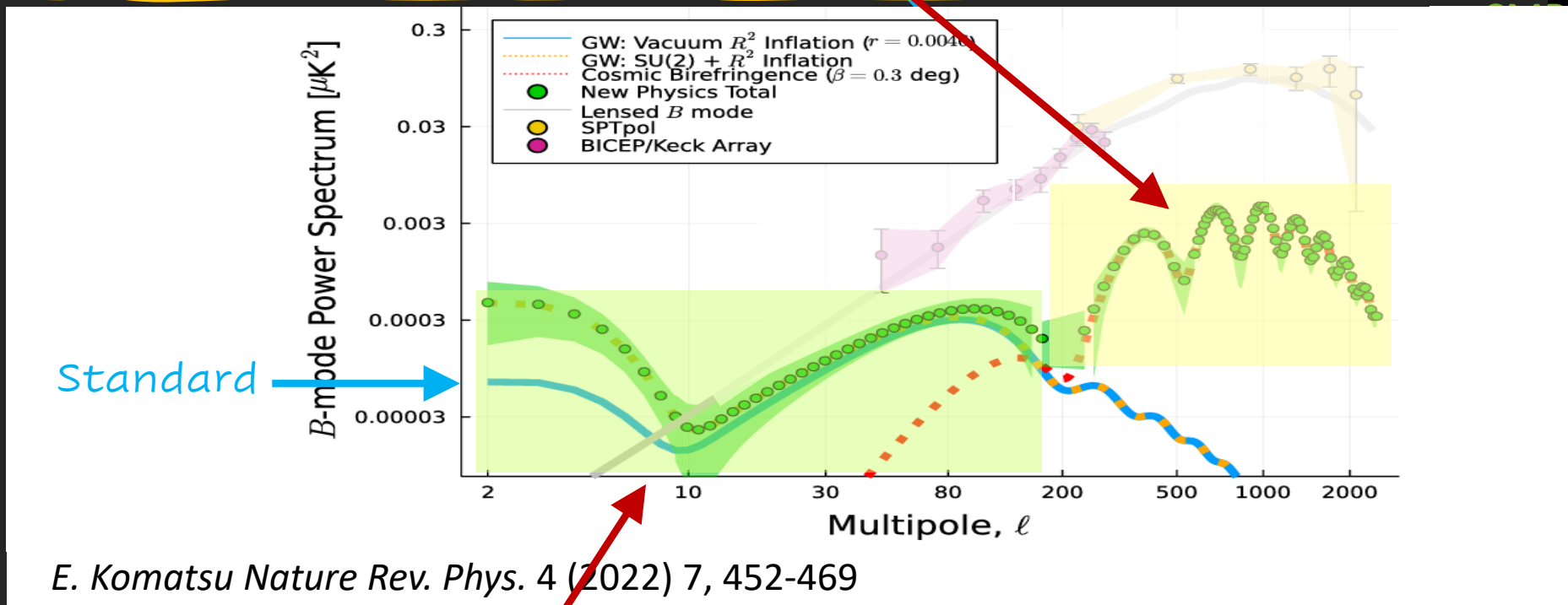
- SU(2)-axion Inflation: SU(2) field-Graviton coupling

- Gravitational Chern-Simons: axion-graviton coupling  $\varphi R \tilde{R}$

# Parity Odd CMB Correlations: TB & EB $\neq 0$

Sources of Parity violation on CMB:

- Cosmic Birefringence: axion-photon coupling  $\varphi F \tilde{F}$



E. Komatsu Nature Rev. Phys. 4 (2022) 7, 452-469

- SU(2)-axion Inflation: SU(2) field-Graviton coupling

- Gravitational Chern-Simons: axion-graviton coupling  $\varphi R \tilde{R}$



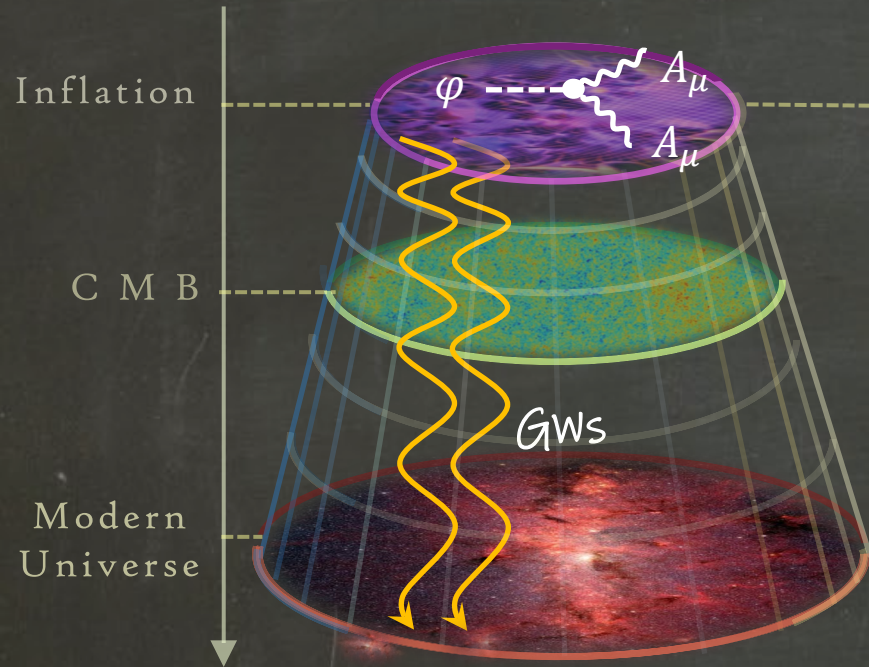
# III) Particle Production in Inflation



# A New Class of Inflation Models

(closer to Particle Physics)

A. M., & Sheikh-Jabbari, 2011  
P. Adshead, M. Wyman, 2012



## Axion-inflation and gauge fields (non-Abelian)

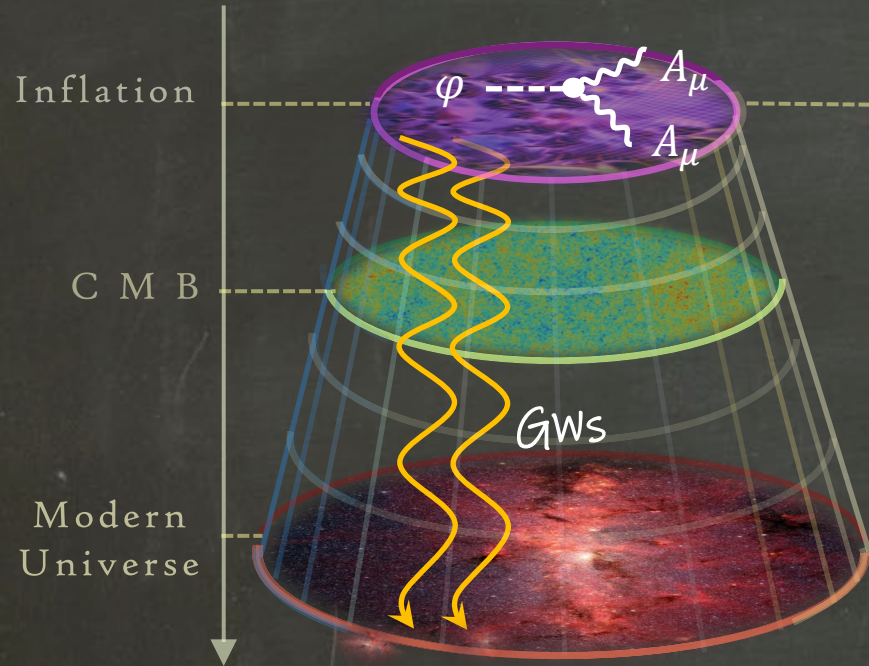
Particle Production  
In Axion-Inflation



# A New Class of Inflation Models

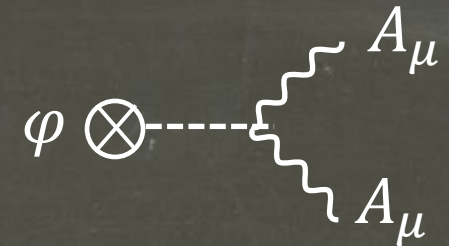
(closer to Particle Physics)

A. M., & Sheikh-Jabbari, 2011  
P. Adshead, M. Wyman, 2012



## Axion-inflation and gauge fields (non-Abelian)

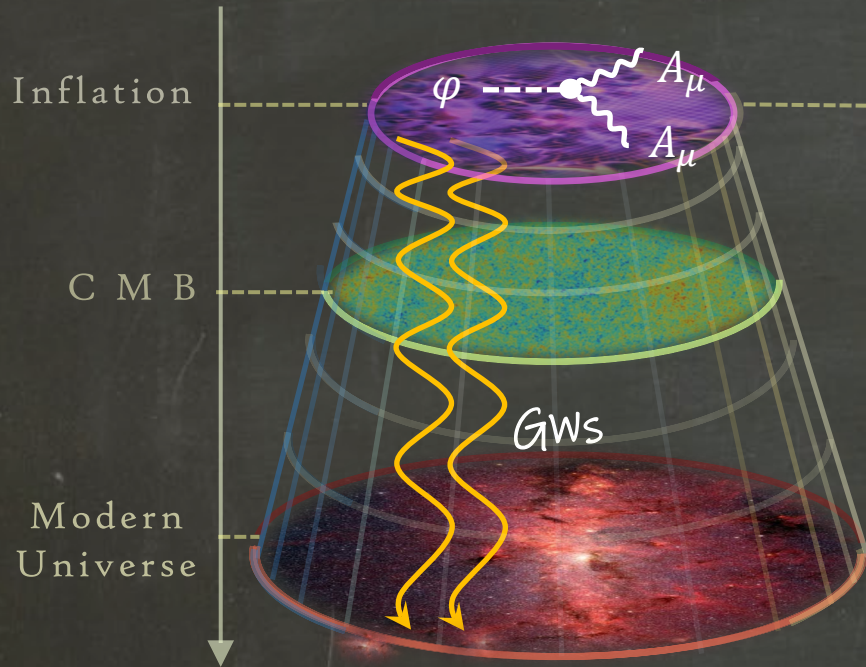
Particle Production  
In Axion-Inflation



# A New Class of Inflation Models

(closer to Particle Physics)

A. M., & Sheikh-Jabbari, 2011  
P. Adshead, M. Wyman, 2012



## Axion-inflation and gauge fields (non-Abelian)

Particle Production  
In Axion-Inflation



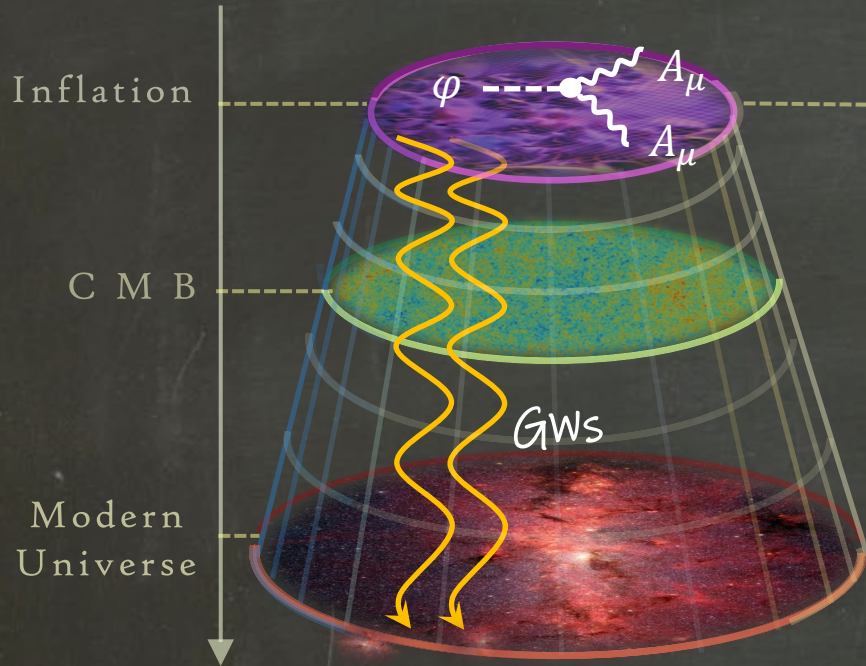
A new mechanism  
for Fermion Production in  
Inflation!

A.M., 2019  
Mirzagholfi, A.M., Lozanov 2019

# A New Class of Inflation Models

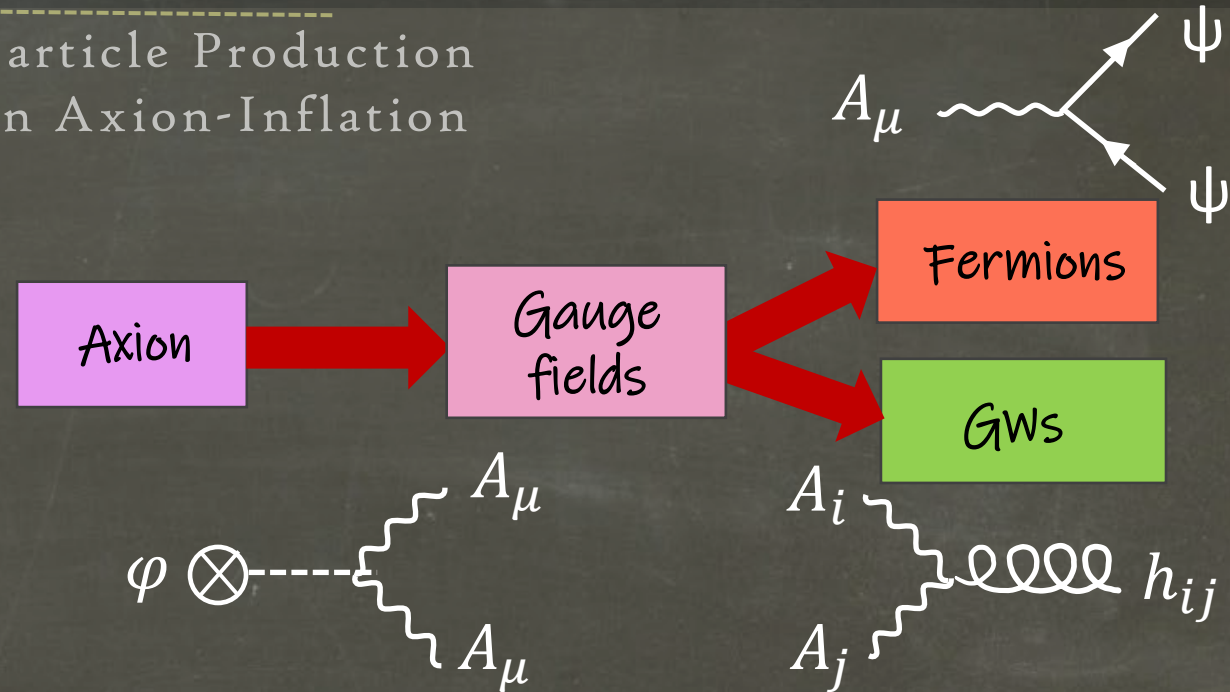
(closer to Particle Physics)

A. M., & Sheikh-Jabbari, 2011  
P. Adshead, M. Wyman, 2012



## Axion-inflation and gauge fields (non-Abelian)

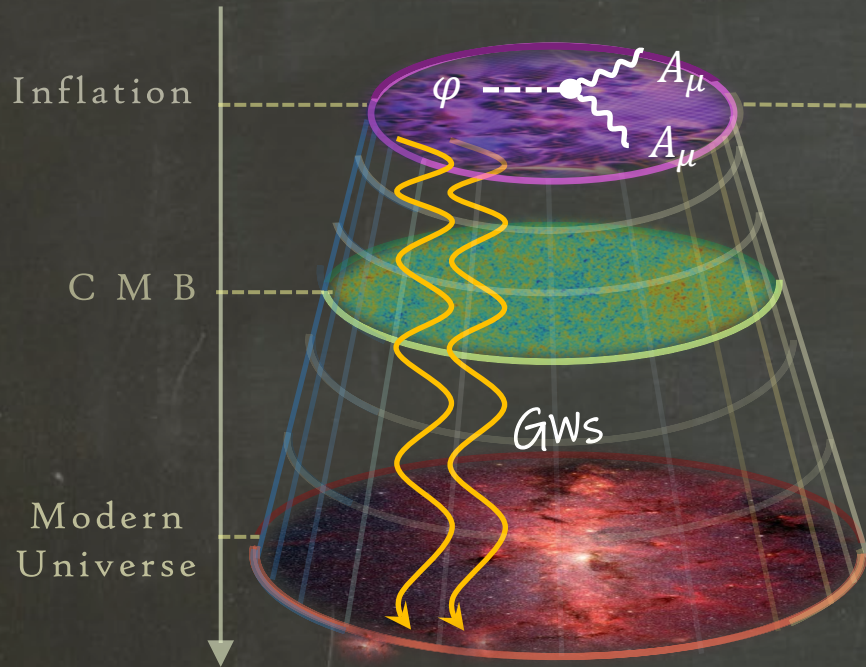
Particle Production  
In Axion-Inflation



# A New Class of Inflation Models

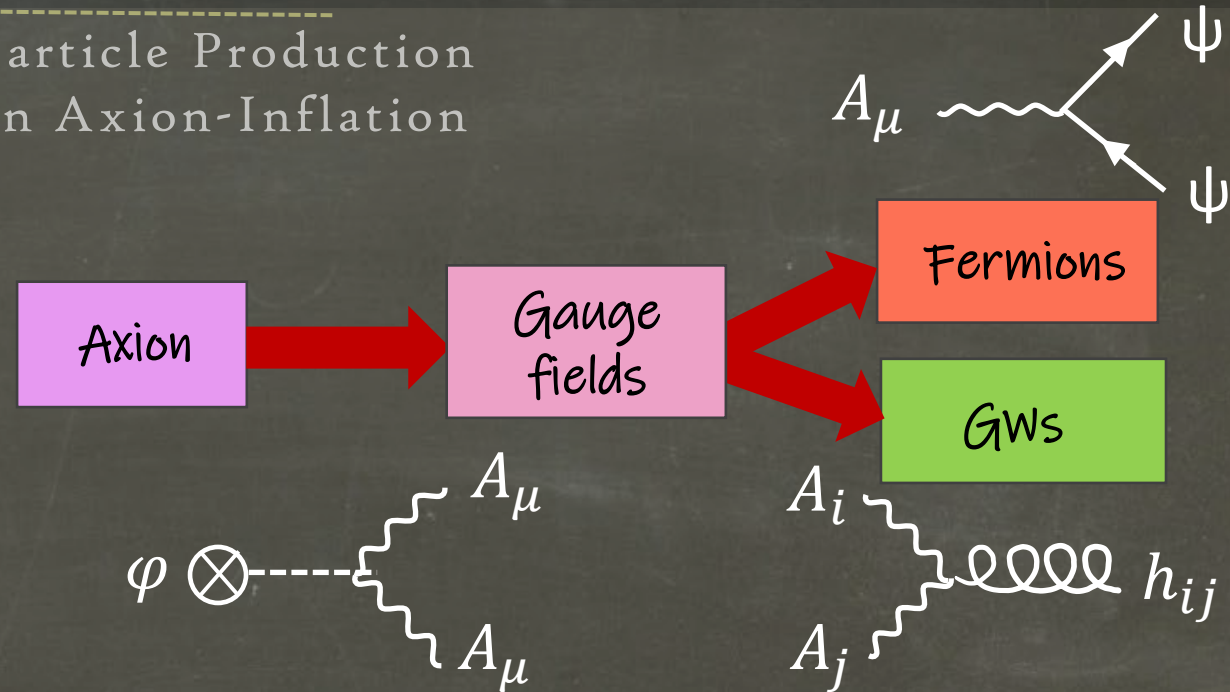
(closer to Particle Physics)

A. M., & Sheikh-Jabbari, 2011  
P. Adshead, M. Wyman, 2012



## Axion-inflation and gauge fields (non-Abelian)

Particle Production  
In Axion-Inflation



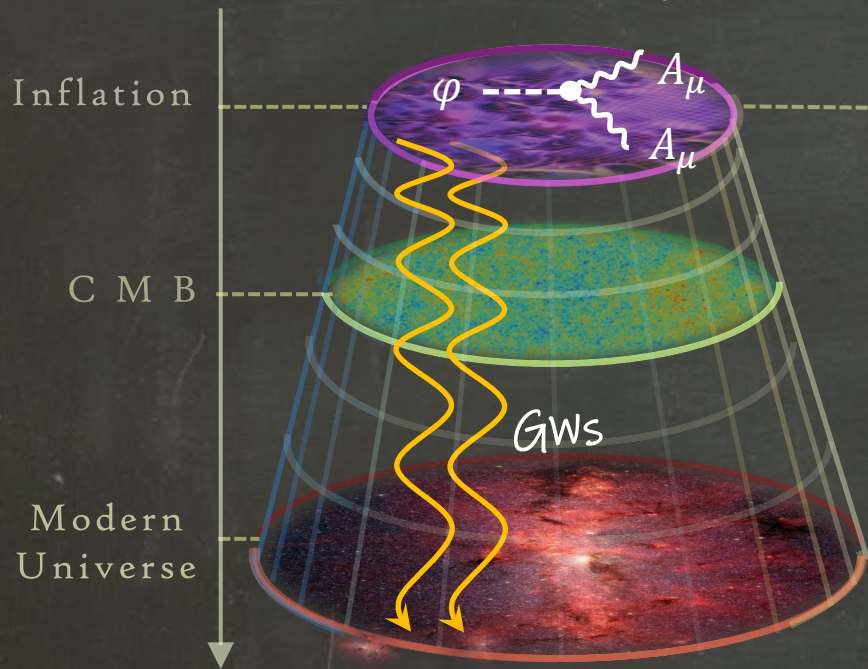
Sourced GWs:  
Chiral & non-Gaussian

A. M., 2019  
Mirzaghohi, A.M., Lozanov 2019  
A. M. et. al, 2011 & 2013  
Dimastrogiovanni et. al 2013  
P. Adshead et. al, 2013

# A New Class of Inflation Models

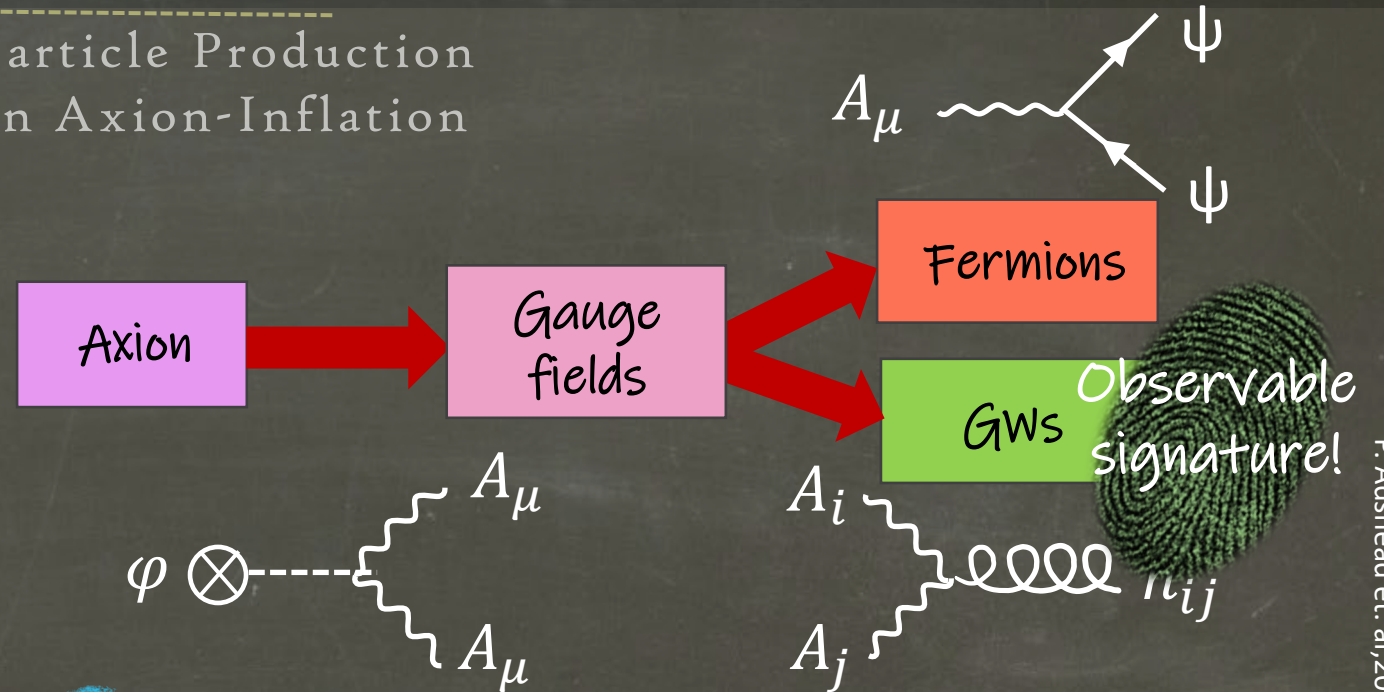
(closer to Particle Physics)

A. M., & Sheikh-Jabbari, 2011  
P. Adshead, M. Wyman, 2012



## Axion-inflation and gauge fields (non-Abelian)

Particle Production  
In Axion-Inflation



Vacuum GWs:  
Unpolarized & Gaussian



Sourced GWs:  
Chiral & non-Gaussian



A. M., 2019  
Mirzaghohi, A.M., Lozanov 2019  
A. M. et. al, 2011 & 2013  
Dimastrogiovanni et. al 2013  
P. Adshead et. al, 2013

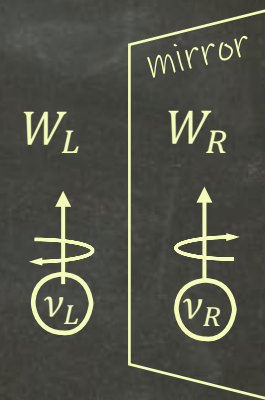
# IV) Embedding axion-inflation in Left-Right Symmetric Models

(How to Connect Inflaton to SM?)

Axion-Inflation



Left-Right Symmetric  
Model (LRSM)



LRSM: the minimal beyond SM

with

**SU(2)<sub>R</sub> Gauge Symmetry**  
& **Right-handed Neutrinos**



# IV) Embedding axion-inflation in Left-Right Symmetric Models

(How to Connect Inflaton to SM?)

Axion-Inflation



Left-Right Symmetric Model (LRSM)

LRSM: the minimal beyond SM

with

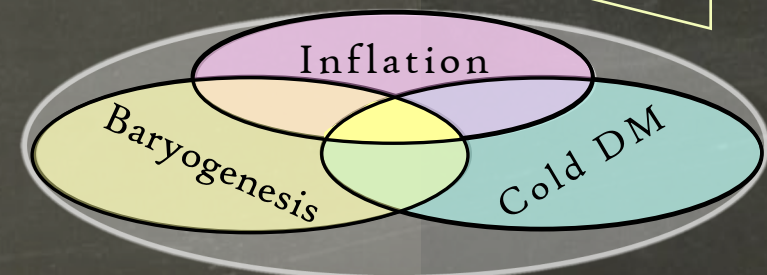
$SU(2)_R$  Gauge Symmetry  
& Right-handed Neutrinos

$W_L$



mirror

$W_R$



A.M. 2021

# How to Connect it to the SM?

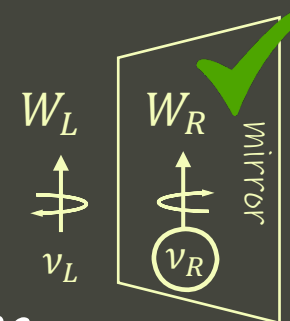
Let us Extend SM Gauge Symmetry by an  $SU(2)_R$  and couple it to Axion Inflaton!

- Left-Right Symmetric Model + axion!

$$SU(2)_R \times SU(2)_L \times U(1)_{B-L} \longrightarrow SU(2)_L \times U(1)_Y$$

Left-Right Symmetric

SM Left-handed Weak force



- Minimal Scenario of **SU(2)-axion inflation** A. M., 2016  $f < 0.1 M_{pl}$  &  $\lambda < 0.1$

$$S_{AM} = \int d^4x \sqrt{-g} \left( -\frac{R}{2} - \frac{1}{4} F^2 - \frac{1}{2} ((\partial_\mu \varphi)^2 - V(\varphi)) - \frac{\lambda}{8f} \varphi F \tilde{F} \right)$$

Axion Monodromy or any mechanism that gives a flat potential

Gauge field is  $SU(2)_R$

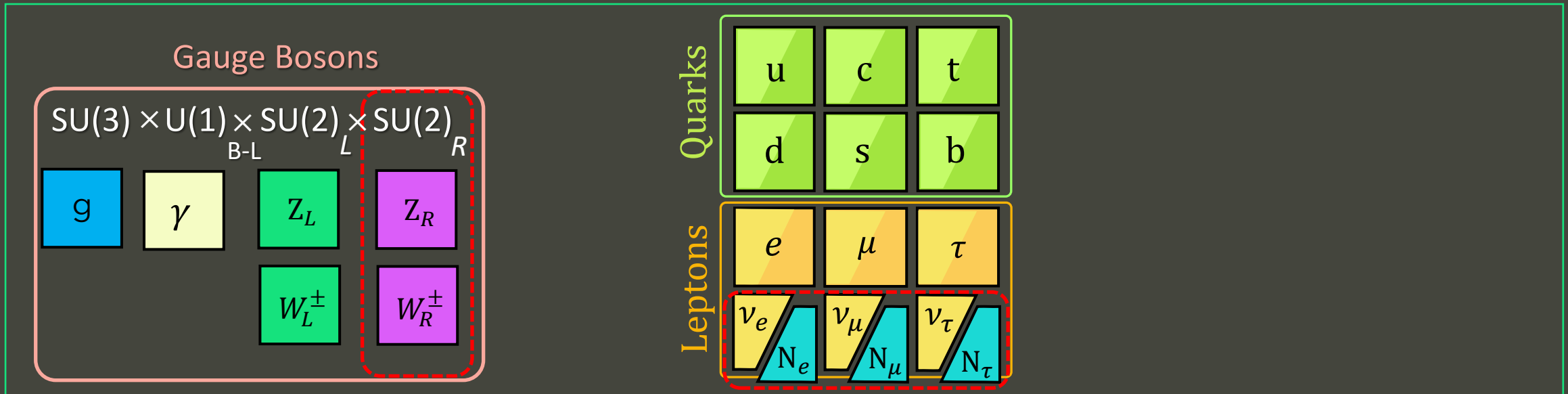
A. M. arXiv: 2012.11516

A.M. arXiv:2103.14611

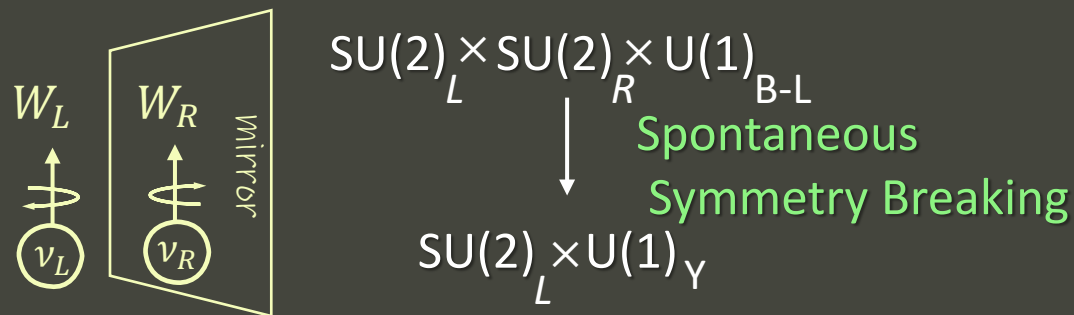
# Left-Right Symmetric Model

Minimal Left-Right Symmetric model

- An  $SU(2)$ -gauge extension of SM with 3 Right-handed Neutrinos coupled to it.



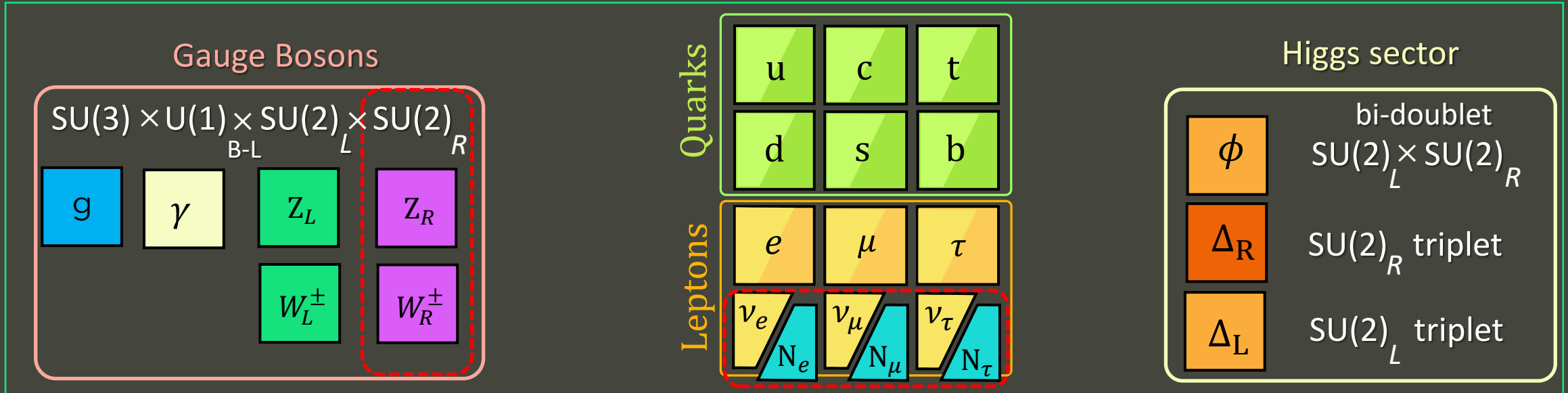
J. C. Pati and A. Salam, Phys. Rev. D 10, 275-289 (1974) R. N. Mohapatra and J. C. Pati, Phys. Rev. D 11, 2558 (1975) G. Senjanovic and R. N. Mohapatra, Phys. Rev. D 12, 1502 (1975)



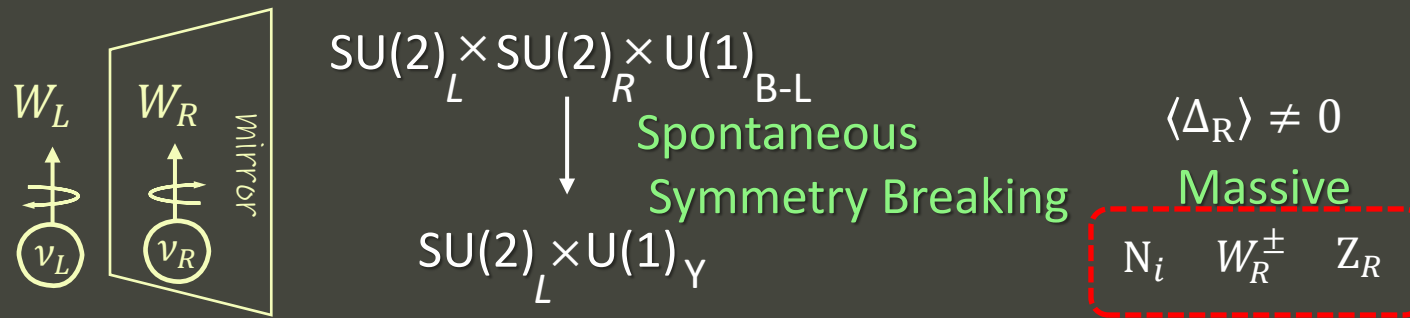
# Left-Right Symmetric Model

Minimal Left-Right Symmetric model

- An  $SU(2)$  gauge extension of SM with 3 Right-handed Neutrinos coupled to it.



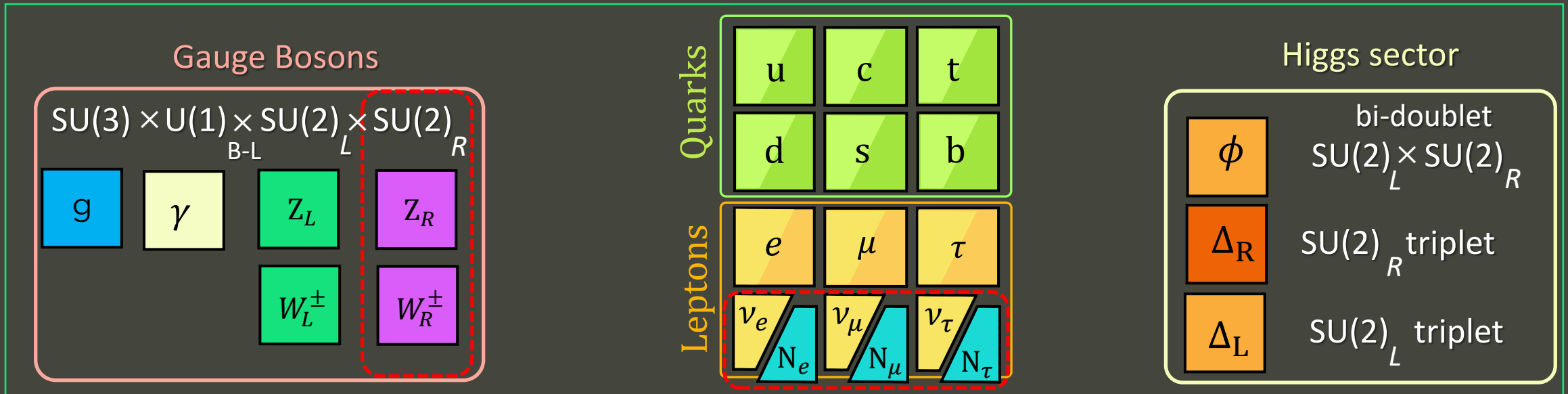
J. C. Pati and A. Salam, Phys. Rev. D 10, 275-289 (1974) R. N. Mohapatra and J. C. Pati, Phys. Rev. D 11, 2558 (1975) G. Senjanovic and R. N. Mohapatra, Phys. Rev. D 12, 1502 (1975)



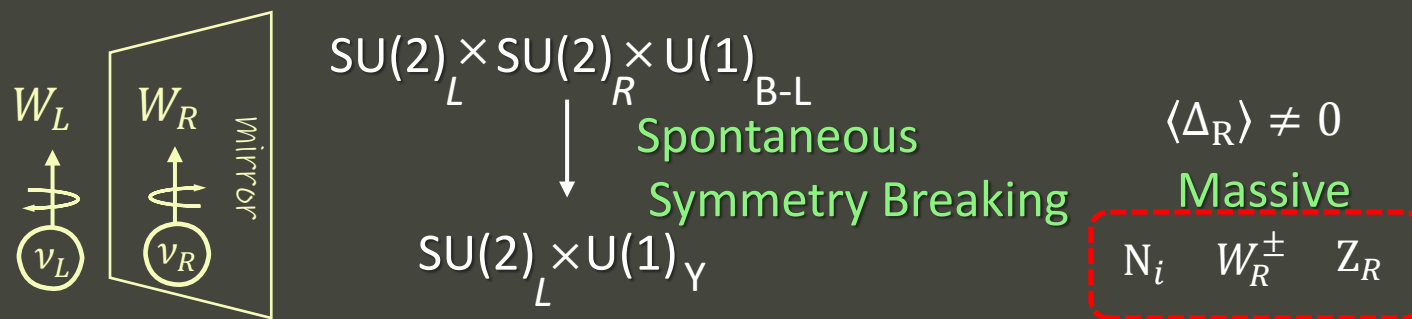
# Left-Right Symmetric Model

Minimal Left-Right Symmetric model

- An  $SU(2)$  gauge extension of SM with 3 Right-handed Neutrinos coupled to it.



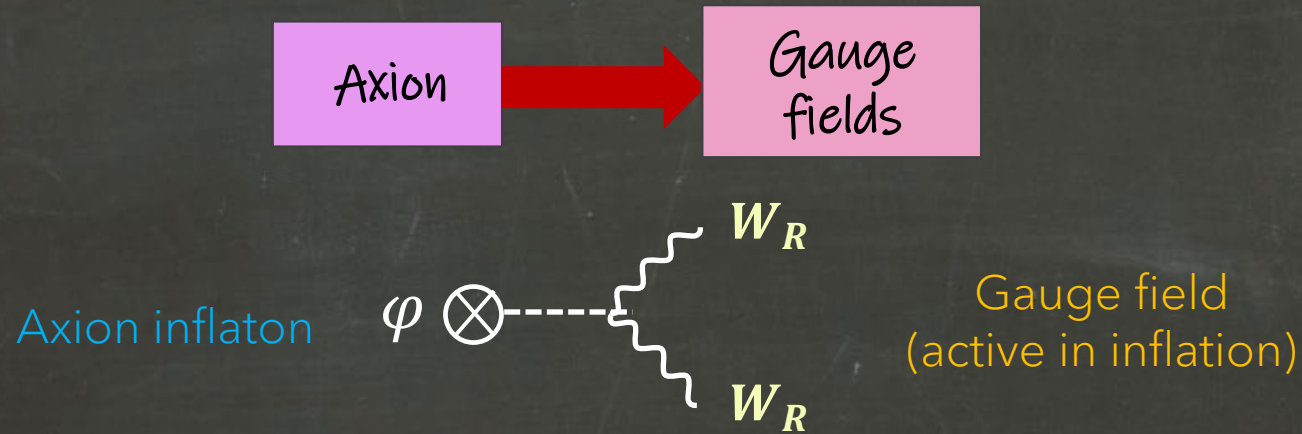
J. C. Pati and A. Salam, Phys. Rev. D 10, 275-289 (1974) R. N. Mohapatra and J. C. Pati, Phys. Rev. D 11, 2558 (1975) G. Senjanovic and R. N. Mohapatra, Phys. Rev. D 12, 1502 (1975)



- Ad hoc parity violation
- Accidental B-L global symmetry
- Vacuum Stability problem

# Gauge field Production in Inflation

- SM Gauge fields are diluted by inflation & unimportant, BUT  $SU(2)_R$ :



# SU(2)<sub>R</sub> Gauge Field

- $\delta A_i^a = B_+^a(t, k) e_i^+(\vec{k}) + B_-^a(t, k) e_i^-(\vec{k})$

$$B_{\pm}'' + [k^2 \mp \xi k\mathcal{H}] B_{\pm} \approx 0$$

effective frequency

Given by the BG ( $\xi = \frac{2\lambda\partial_t\varphi}{fH}$ )

## Vacuum structure

Axion field  $\langle\varphi\rangle$

( $\xi > 0$ )

Slow-roll A

Slow-roll A<sub>P</sub>

Parity

( $\xi < 0$ )

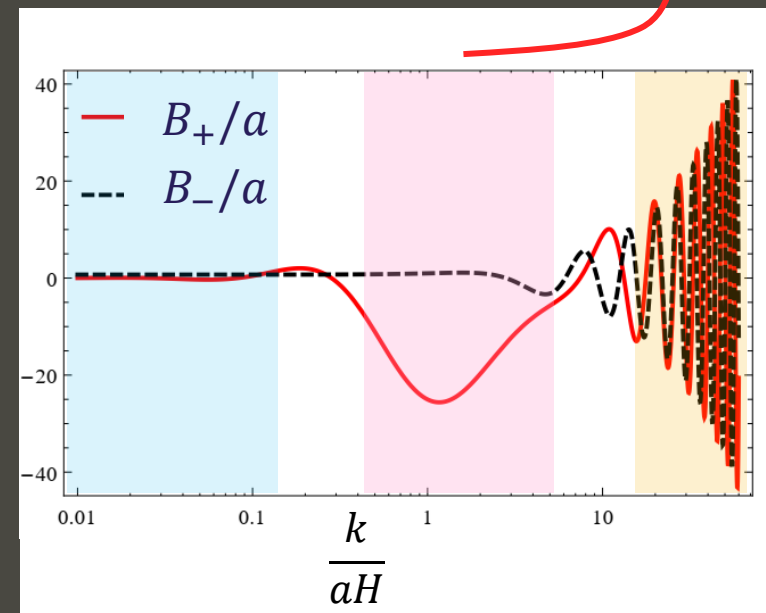
For  $\xi > 0$   
Short tachyonic growth of  $B_+$



Chiral Field

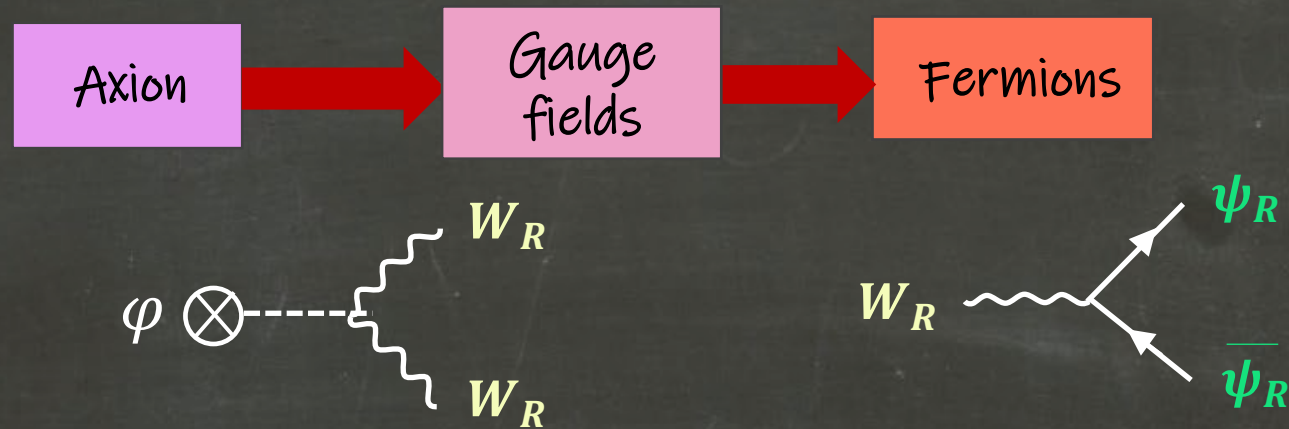
$$n_B \sim \frac{H^3}{6\pi^2} \xi^3 e^{\frac{(2-\sqrt{2})\pi}{2}\xi}$$

Particle Production



# Lepton & quark Production in Inflation

- Left-handed fermions are diluted by inflation, BUT
- Right-handed fermions are generated by  $SU(2)_R$  gauge field:



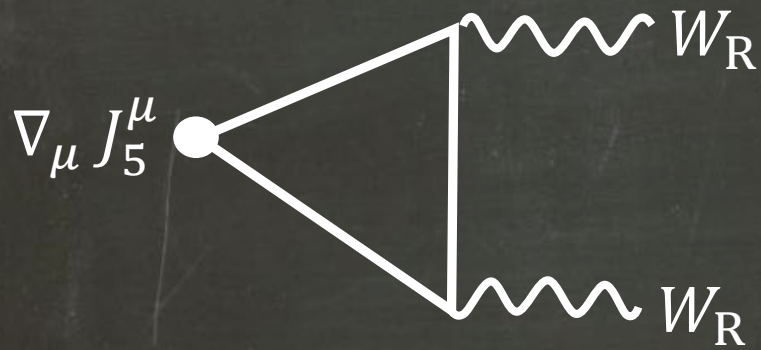


# Lepton & quark Production in Inflation

- Left-handed fermions are diluted by inflation, BUT
- Right-handed fermions are generated by  $SU(2)_R$  gauge field:



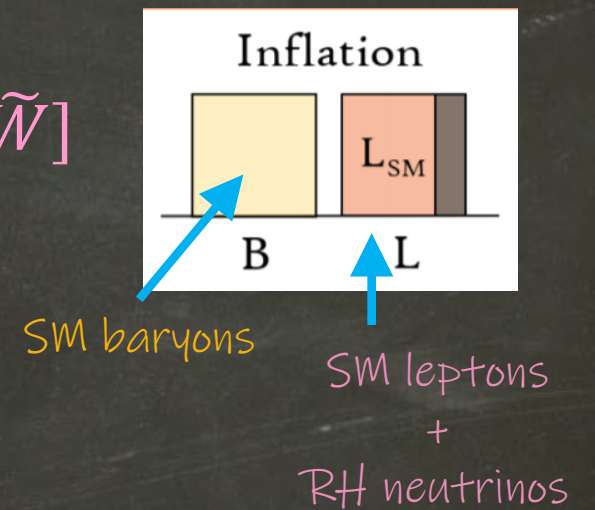
The key ingredient is the Chiral anomaly of  $SU(2)_R$  in inflation:



$$\nabla_\mu J_B^\mu = \nabla_\mu J_L^\mu = \frac{g^2}{16\pi^2} \text{tr}[W\tilde{W}]$$

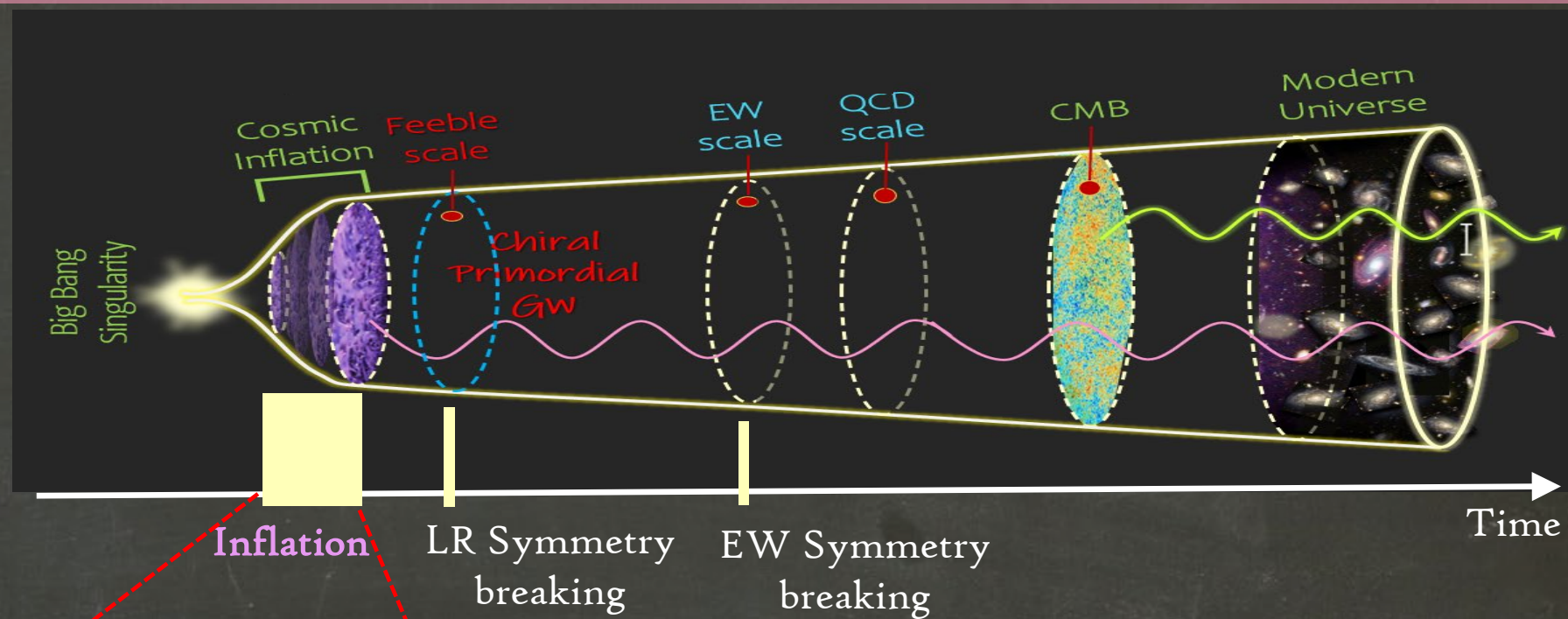
$$n_B = n_L = \alpha_{inf}(\xi) H^3$$

$$\alpha_{inf}(\xi) \sim \frac{g^2}{(2\pi)^4} e^{2\pi\xi}$$

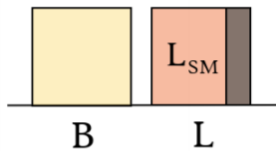
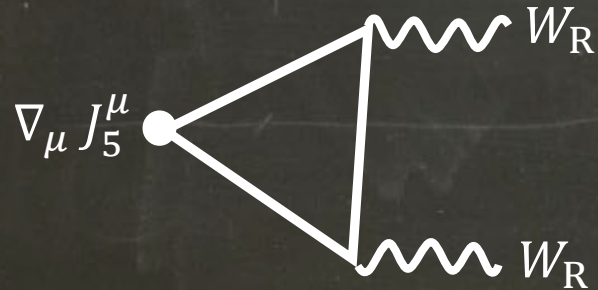


# Summary of the mechanism:

Quarks	u	c	t
	d	s	b
Leptons	e	$\mu$	$\tau$
	$\nu_e$	$\nu_\mu$	$\nu_\tau$
	$N_e$	$N_\mu$	$N_\tau$



Chiral anomaly of  $SU(2)_R$   
In inflation



$$B = L = 3n_{CS}$$

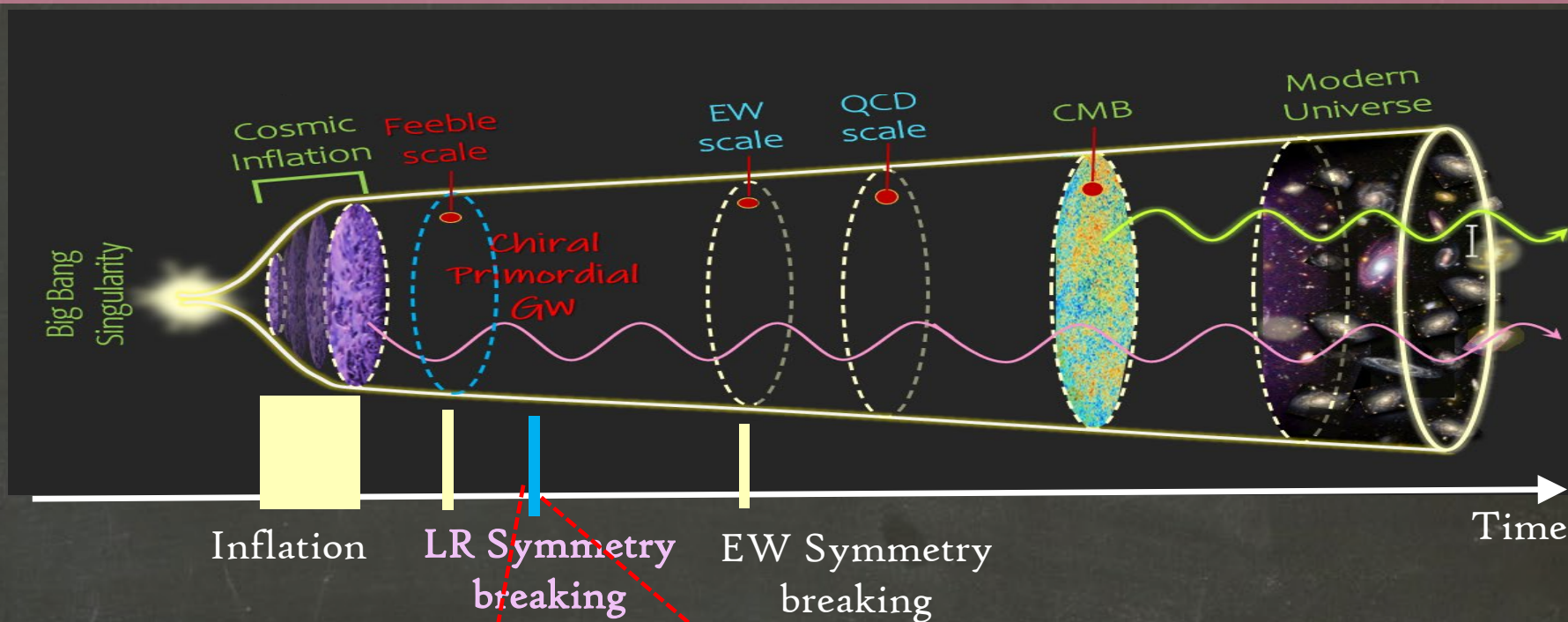
$$B - L_{SM} \neq 0$$

B = SM baryons

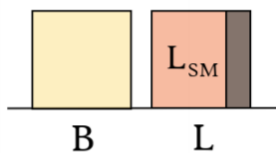
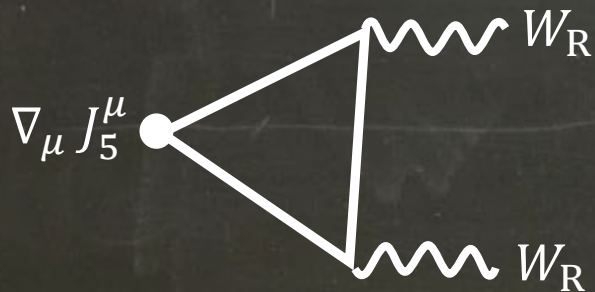
L = SM leptons + RH neutrinos

# Summary of the mechanism:

Quarks	u	c	t
	d	s	b
Leptons	e	$\mu$	$\tau$
	$\nu_e$	$\nu_\mu$	$\nu_\tau$
	$N_e$	$N_\mu$	$N_\tau$

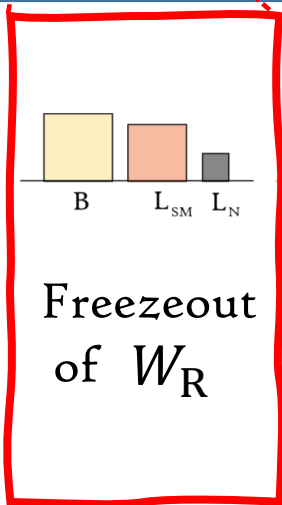
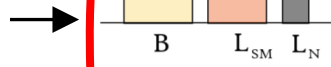


Chiral anomaly of  $SU(2)_R$   
In inflation



$$B = L = 3n_{CS}$$

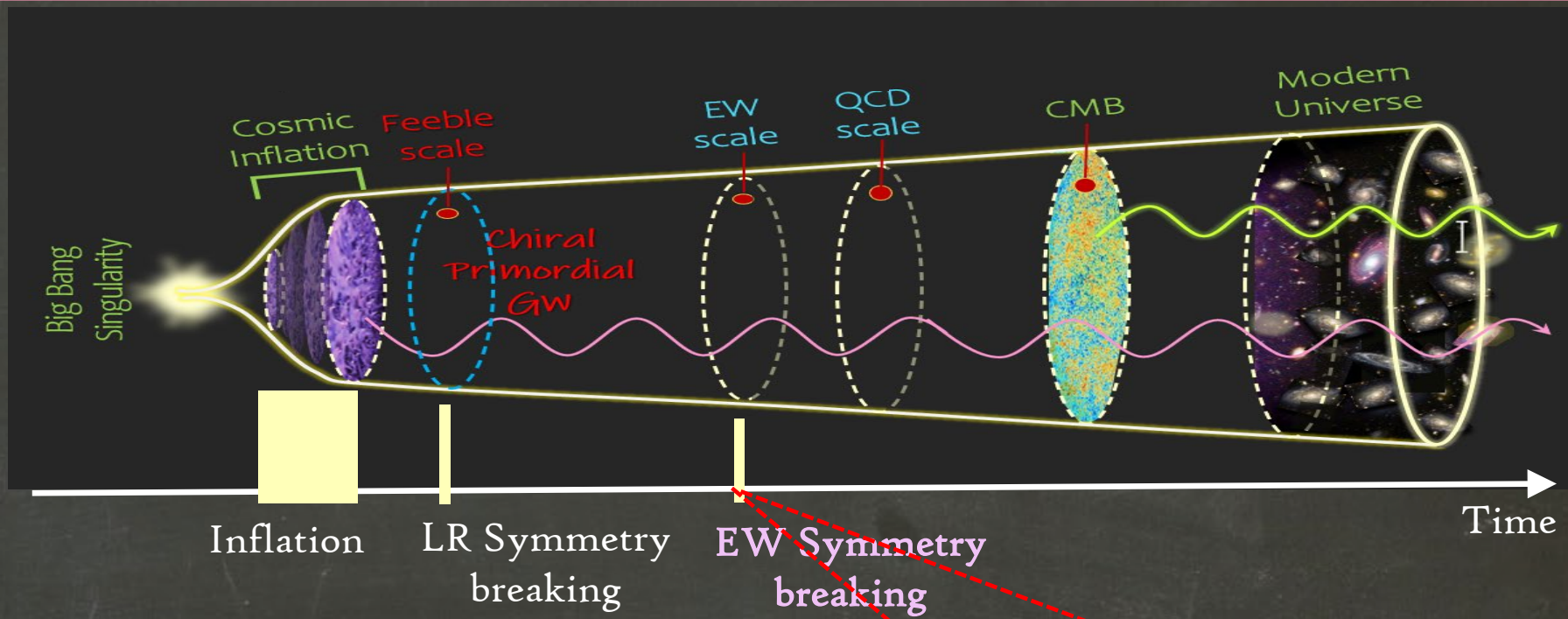
$$B - L_{SM} \neq 0$$



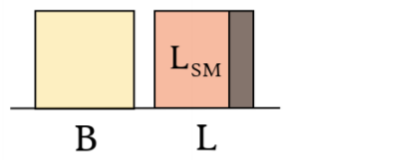
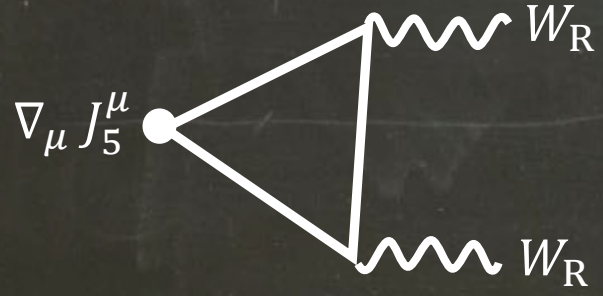
Freezeout  
of  $W_R$

# Summary of the mechanism:

Quarks	u	c	t
	d	s	b
Leptons	e	$\mu$	$\tau$
	$\nu_e$	$\nu_\mu$	$\nu_\tau$
	$N_e$	$N_\mu$	$N_\tau$

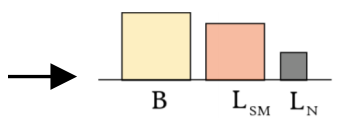


Chiral anomaly of  $SU(2)_R$   
In inflation

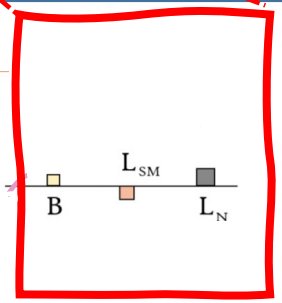


$$B = L = 3n_{CS}$$

$$B - L_{SM} \neq 0$$



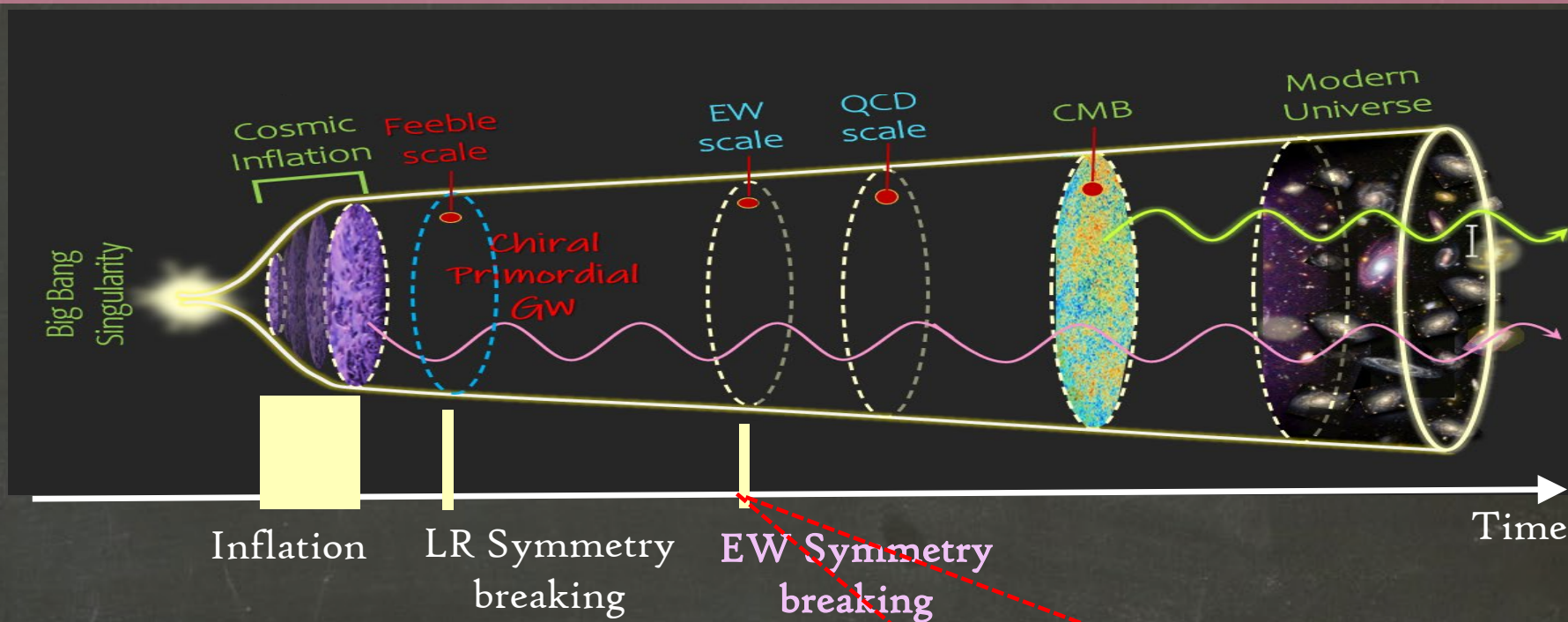
Freezeout of  $W_R$



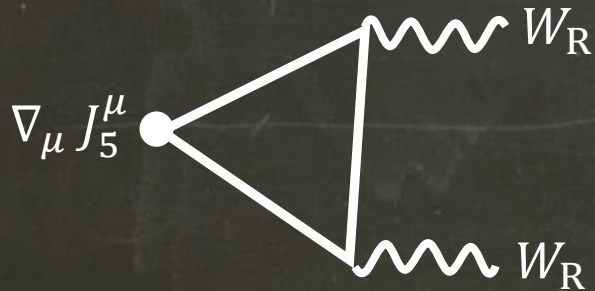
Spectator effects reshuffle  $B$ ,  $L_{SM}$  &  $L_N$

# Summary of the mechanism:

Quarks	u	c	t
	d	s	b
Leptons	e	$\mu$	$\tau$
	$\nu_e$	$\nu_\mu$	$\nu_\tau$
	$N_e$	$N_\mu$	$N_\tau$



Chiral anomaly of  $SU(2)_R$   
In inflation

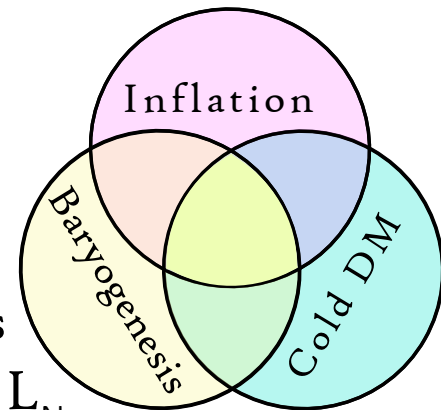


Bar chart showing the evolution of Baryon number (B) and Lepton number (L) during inflation and LR symmetry breaking.

$B = L = 3n_{CS}$   
 $B - L_{SM} \neq 0$

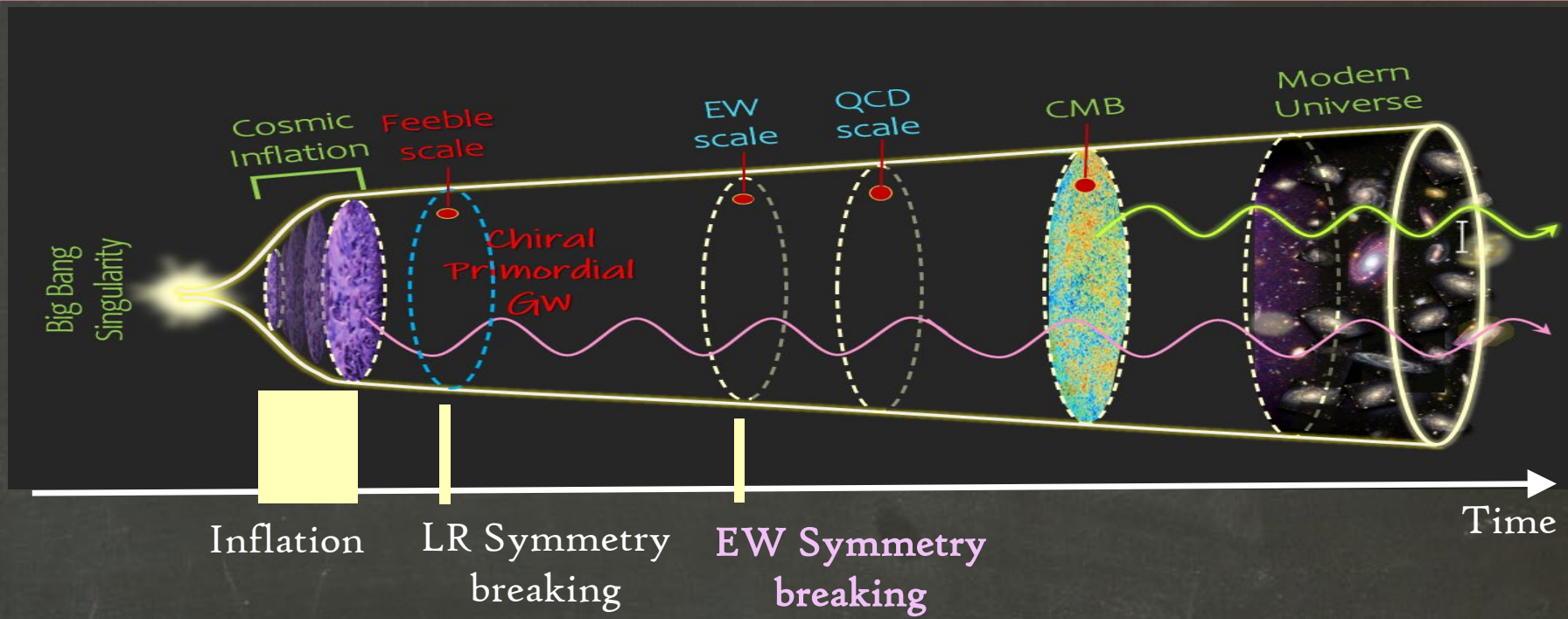
Freezeout of  $W_R$

Spectator effects reshuffle B,  $L_{SM}$  &  $L_N$

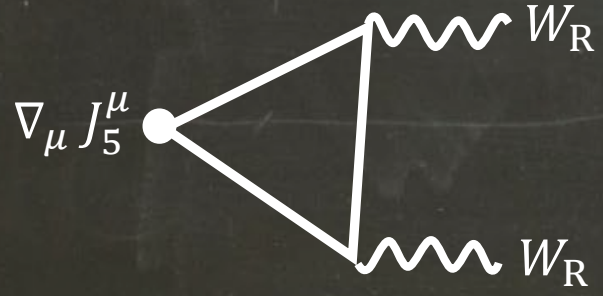


# Summary of the mechanism:

Quarks	u	c	t
	d	s	b
Leptons	e	$\mu$	$\tau$
	$\nu_e$	$\nu_\mu$	$\nu_\tau$
	$N_e$	$N_\mu$	$N_\tau$



Chiral anomaly of  $SU(2)_R$   
In inflation



Initial state (before freezeout):

$$B = L = 3n_{CS}$$

$$B - L_{SM} \neq 0$$

Freezeout of  $W_R$

Baryogenesis

$$\eta_B^0 \approx 3 \left( \frac{g_{eff}}{100} \right)^{\frac{3}{4}} \frac{\alpha_{inf}(\xi)}{(\delta_{reh})^{\frac{3}{4}}} \left( \frac{H}{M_{Pl}} \right)^{\frac{3}{2}}$$

DM

$$\Omega_{N_1} \approx 2.8 \frac{m_{N_1}}{m_p} \Omega_B$$

$$m_{N_1} \approx 1.8 m_p = 1.7 \text{ GeV.}$$

# Summary & Conclusions

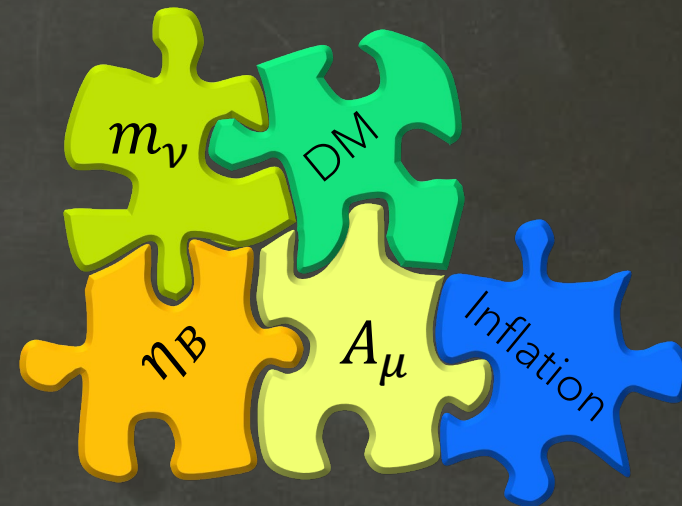


Gauge fields are expected to contribute to physics of axion inflation.

## Compelling Consequences:

This Set-up is a **complete BSM** that can solve **I-IV**:

- I) Particle physics of Inflation
- II) Origin of matter asymmetry
- III) Origin of Neutrino mass
- IV) Particle nature of DM



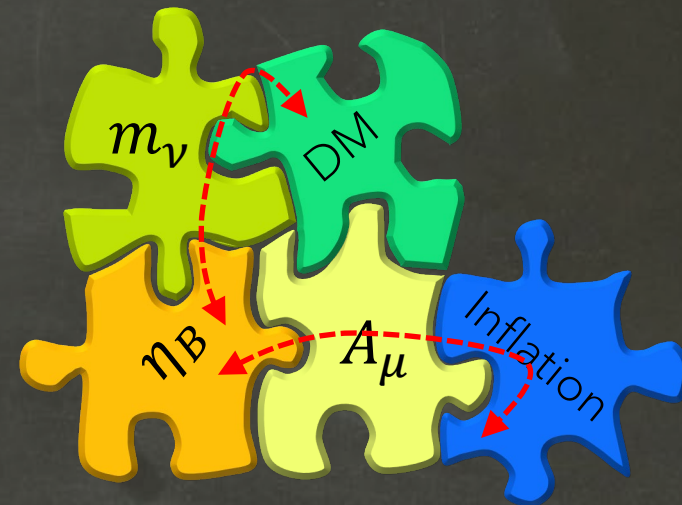


Gauge fields are expected to contribute in physics of axion inflation.

## Compelling Consequences:

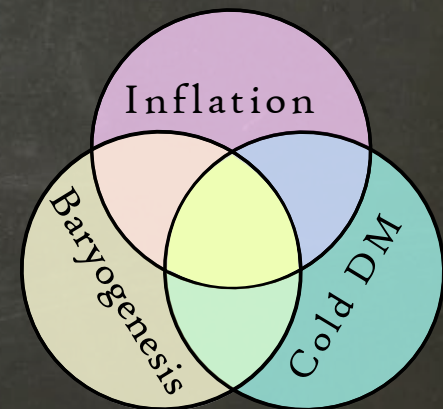
This Set-up is a **complete BSM** that can solve **I-IV**:

- I) Particle physics of Inflation
- II) Origin of matter asymmetry
- III) Origin of Neutrino mass
- IV) Particle nature of DM



It provides a deep connection between **inflation**, **baryogenesis** & **DM**,

So naturally explains **cosmological coincidences**  $\eta_B \simeq 0.3 P_\zeta$  and  $\Omega_{DM} \simeq 5\Omega_B$ !

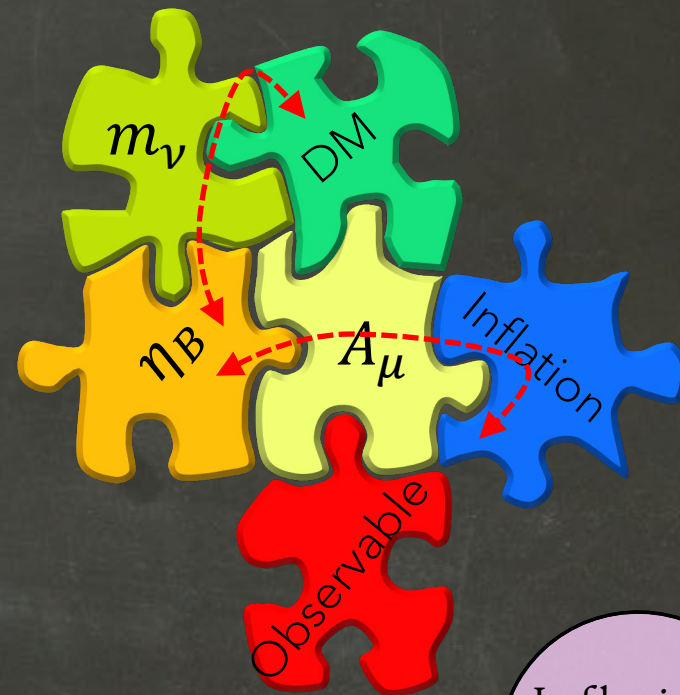


Gauge fields are expected to contribute in physics of axion inflation.

## Compelling Consequences:

This Set-up is a **complete BSM** that can solve **I-IV**:

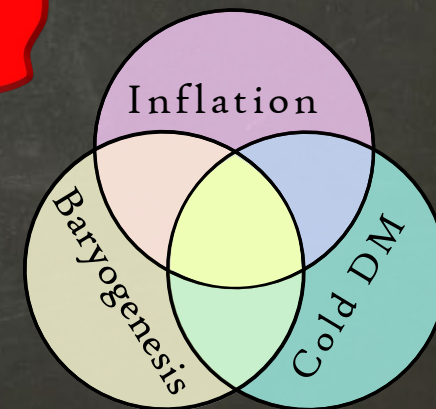
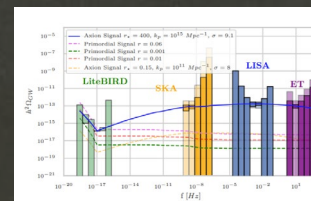
- I) Particle physics of Inflation
- II) Origin of matter asymmetry
- III) Origin of Neutrino mass
- IV) Particle nature of DM



It provides a deep connection between **inflation**, **baryogenesis** & **DM**,

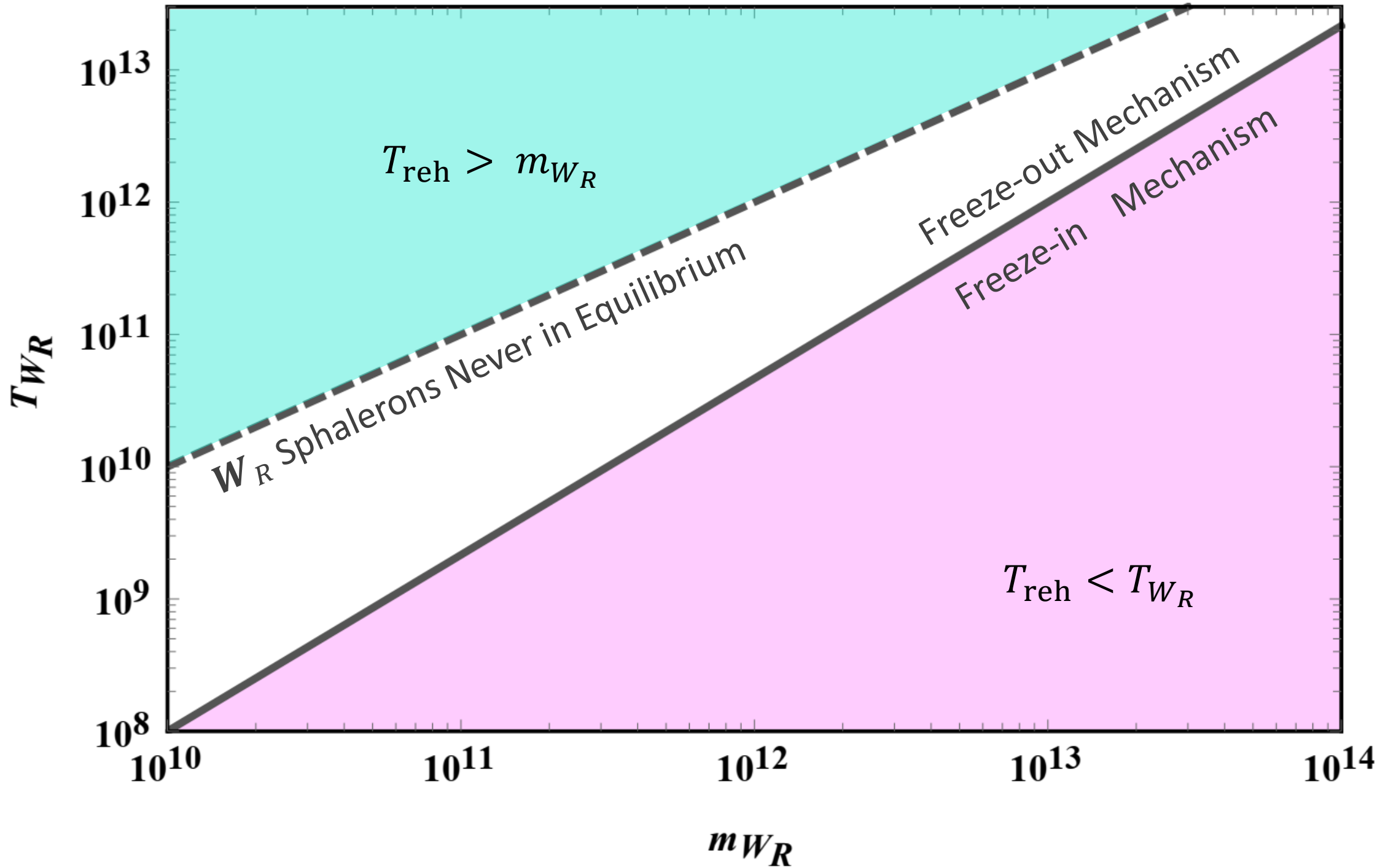
So naturally explains **cosmological coincidences**  $\eta_B \simeq 0.3 P_\zeta$  and  $\Omega_{DM} \simeq 5\Omega_B$ !

It comes with a **cosmological smoking gun** on **Primordial GWs**.

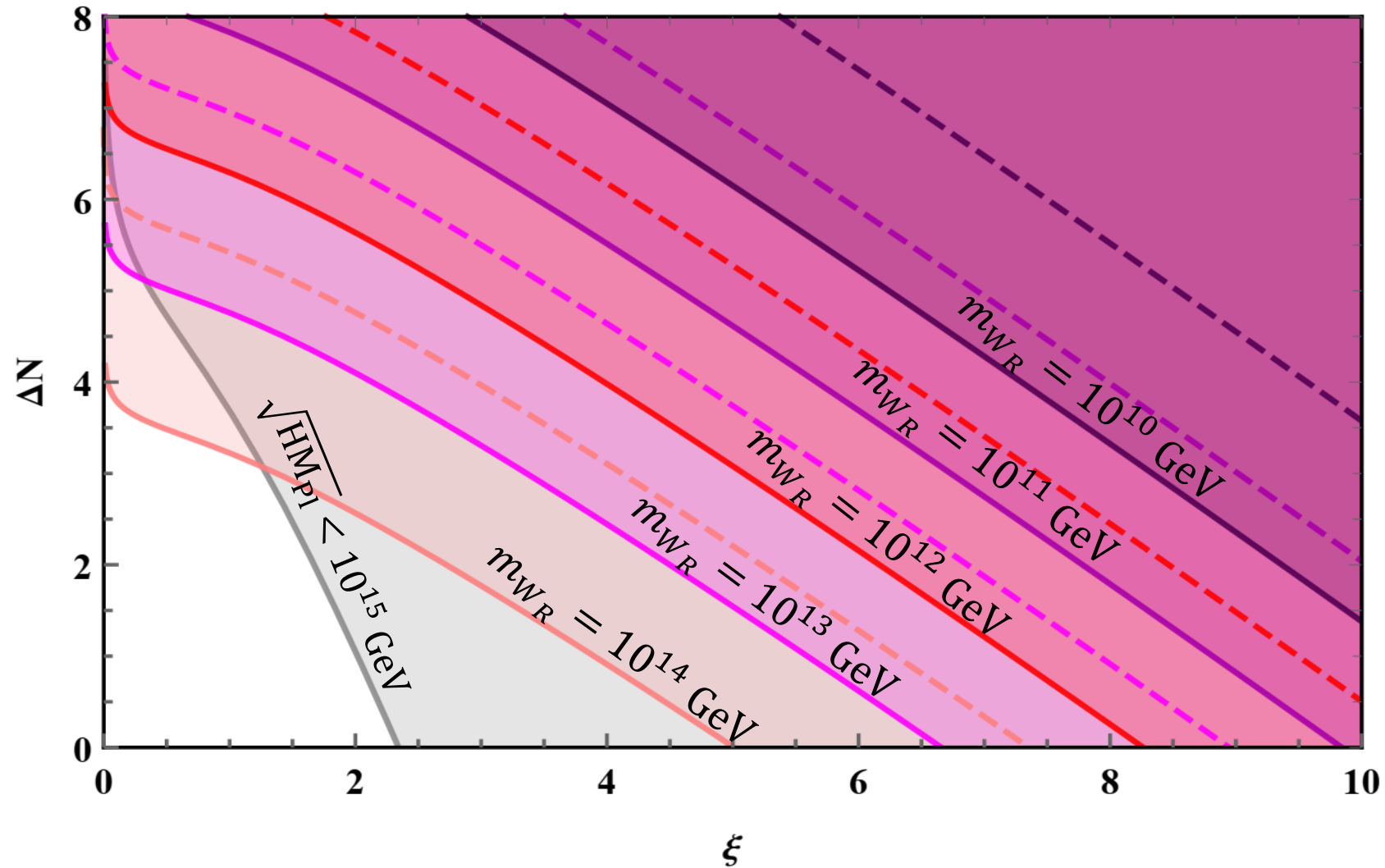


*Questions?!*



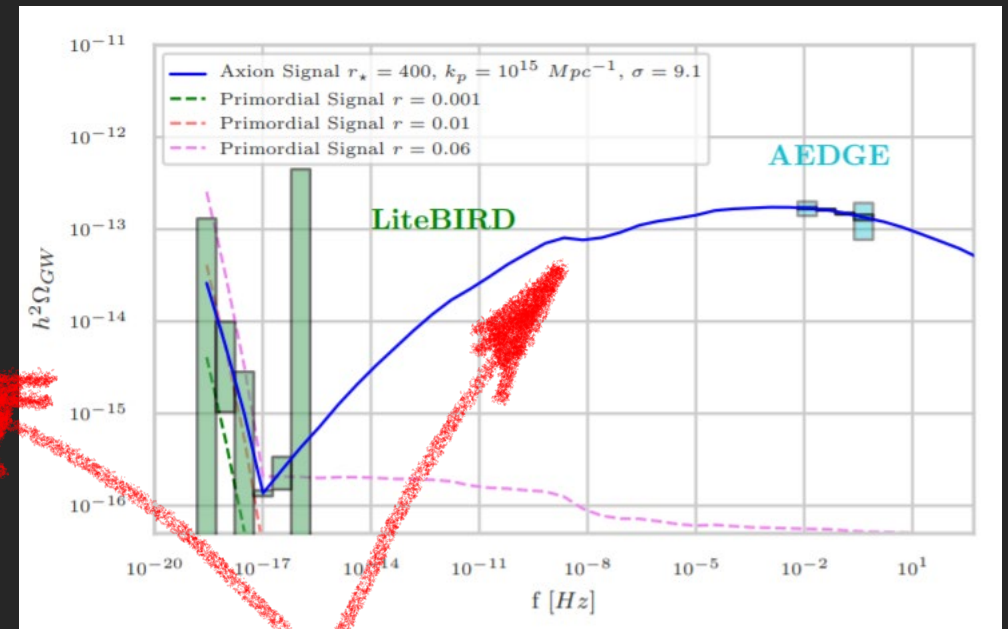
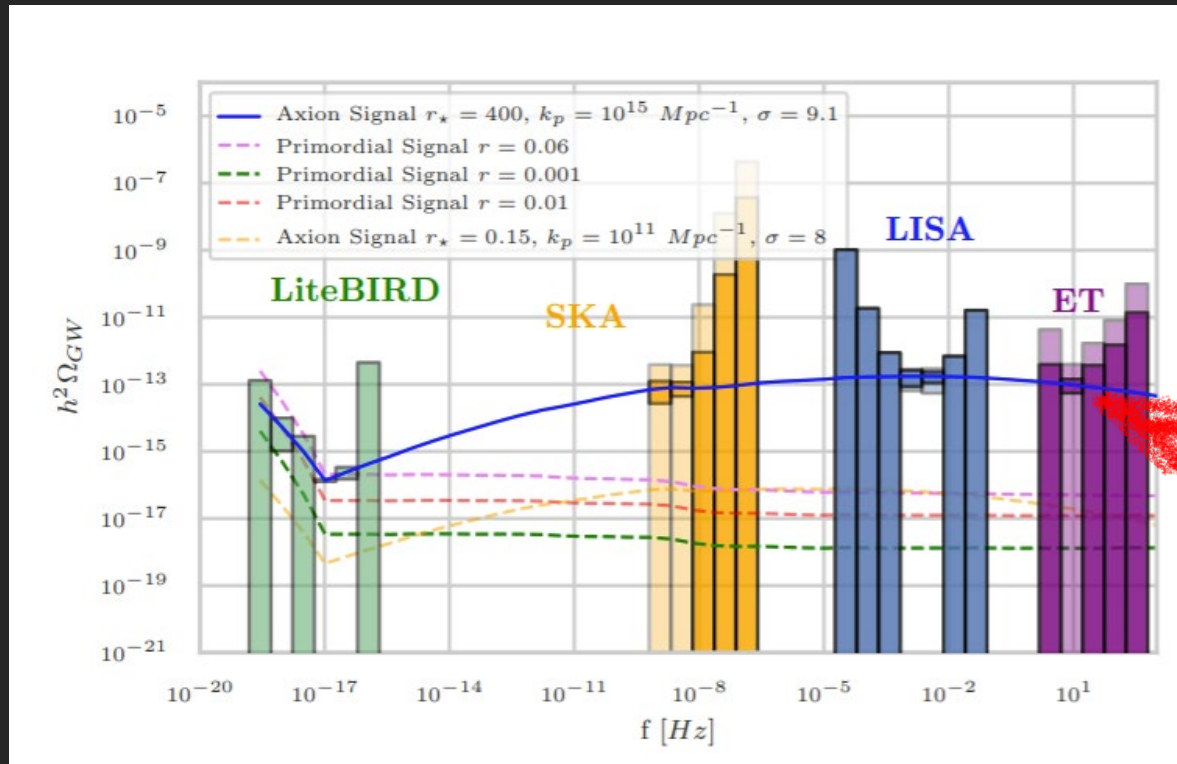


This setup prefers Left-Right symmetry breaking scales above  $m_{W_R} = 10^{10}$  GeV !  
(same as scales suggested by the non-SUSY SO(10) GUT models with intermediate LR symmetry scale.)



# Novel Observable Signature: Beyond CMB

Detection of this background is an excellent target for all GW experiments across at least 21 decades in frequencies.



P. Campeti, E. Komatsu, D. Poletti, C. Baccigalupi 2020

New Physics