

An improved Full Reconstruction tool utilizing NeuroBayes

ACAT 2011

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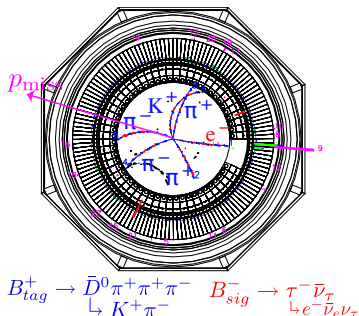
INSTITUT FÜR EXPERIMENTELLE KERNPHYSIK, KARLSRUHE INSTITUTE OF TECHNOLOGY (KIT)



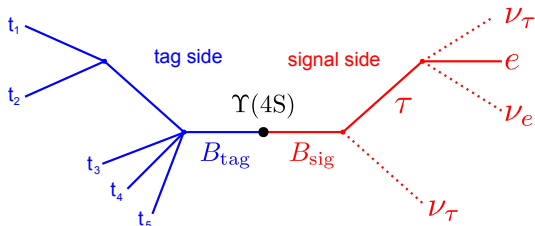
- 1 The Full Reconstruction
 - The Method
 - Use-cases
- 2 NeuroBayes
 - Overview
- 3 Efficiency and Purity
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 - Tag Side
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The Full Reconstruction method

- **B factories:** e^+e^- colliders with center of mass energy of $\sqrt{s} = 10.58$ GeV at the $\Upsilon(4S)$ resonance
- $B(\Upsilon(4S) \rightarrow B\bar{B}) > 96\%$
 - $\Rightarrow p_{CMS}(B) + p_{CMS}(\bar{B}) + p_{CMS}(\text{Beam}) = 0$
 - \Rightarrow Clean event topologies (typically ~ 10 tracks)



Typical B factory event



Tag and signal side of the full reconstruction

Typical use-cases

The full reconstruction allows to measure missing momentum and additional energy.

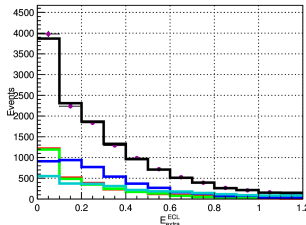
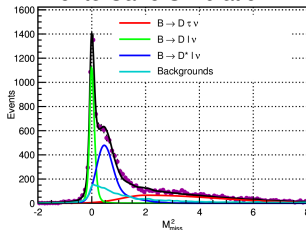
(Semi-)leptonic decays

- $B \rightarrow \tau \nu$
- $B \rightarrow \ell \nu \gamma$
- $B \rightarrow D^{(*)} \ell \nu$
- $B \rightarrow D^{(*)} \tau \nu$
- $B \rightarrow h \nu \nu$
- $B \rightarrow \nu \nu$

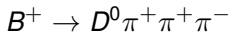
Inclusive searches

- $B \rightarrow K + X_{c\bar{c}}$

Monte Carlo Simulation:

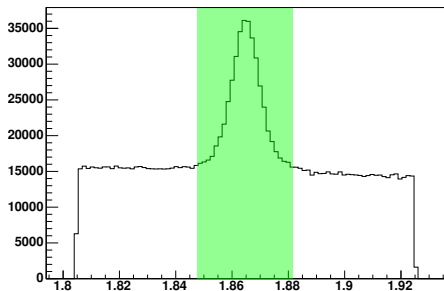


Exemplary reconstruction of the tag side



First step

- Reconstruction of D^0 meson (exemplary $\bar{D}^0 \rightarrow K^+ \pi^-$)
- Specific cuts on Particle ID
- Cut on D^0 mass



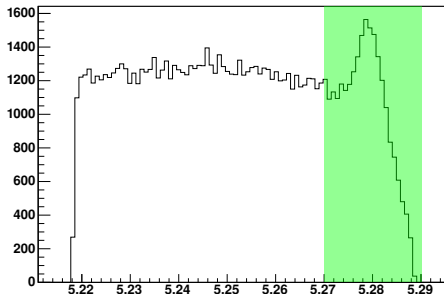
Mass of the D^0 meson

B reconstruction: Important variables

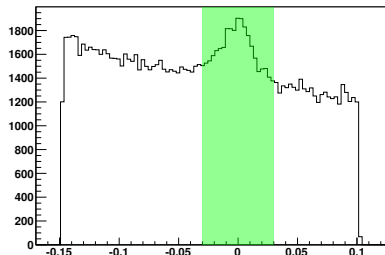
$$M_{bc} \equiv \sqrt{E_{beam}^2 - p_B^2}$$

$$\Delta E \equiv E_{B\text{-meson}} - E_{Beam}$$

Exemplary reconstruction of the tag side



M_{bc} of the B^+ meson

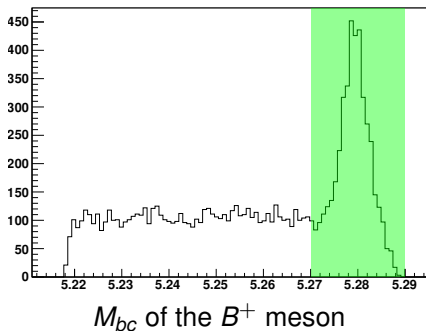


ΔE of the B^+ meson

Often necessary: Improvement of significance

- Usage of multivariate techniques

Exemplary reconstruction of the tag side



Typical variables:

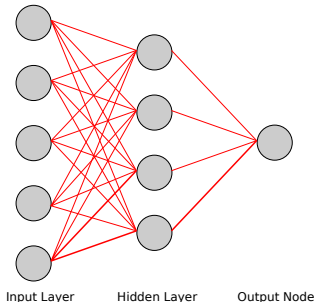
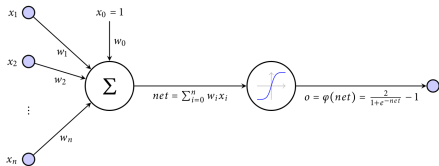
- Vertex fit information
- Kinematic Variables
- Particle ID information
- M_{bc} or ΔE

Full Reconstruction

This procedure is performed for hundreds of different channels

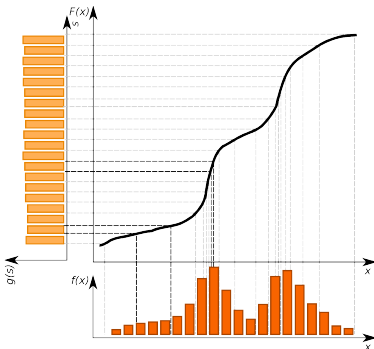
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- Multivariate analysis software combining a **Neural** Network with sophisticated pre-processing

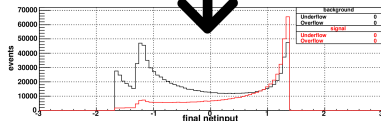
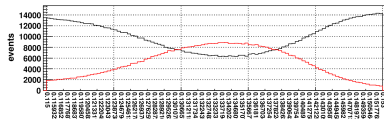


- The output of the Network can be interpreted as **Bayesian** probability

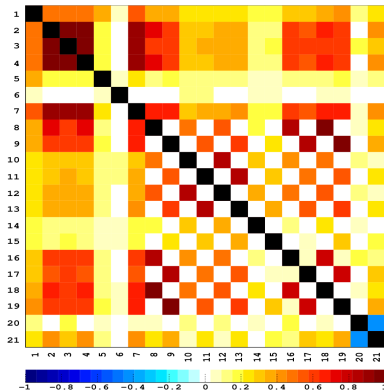
- Input variables are flattened



- Purity is taken and transformed to have mean 0 and width 1.



- Input variables are decorrelated



Pre-processing ...

- Speeds up the training process
- Facilitates the weight finding
- Increases the robustness of the algorithm

Probability

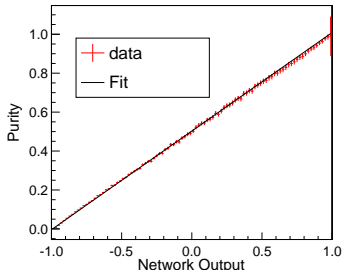
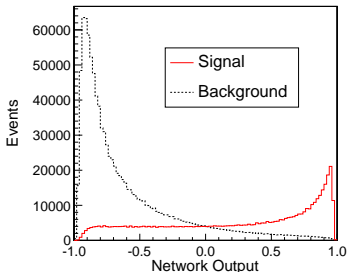
1) Signal to background ratio in training is the same as on data

(Output of NeuroBayes+1)/2 is the signal probability by construction.

2) Signal to background ratio in training is **not** the same as on data

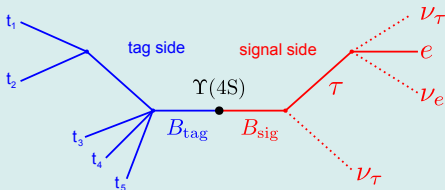
- It is often necessary to artificially enhance the signal component for the training.
- The output can be corrected:

$$O_p = \frac{1}{1 + \left(\frac{1}{O_t} - 1\right) \frac{P_p(B) P_t(S)}{P_p(S) P_t(B)}}$$



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Two premises



- 1 The more **correct** tag side B mesons, the more signal side B mesons are available for analysis.
⇒ **Need for good efficiency**
- 2 The more **incorrect** tag side B mesons, the more background pollutes the signal side.
⇒ **Need for good purity**

Channel	BR	Channel	BR
$B^+ \rightarrow \bar{D}^0 \pi^+$	0.484%	$B^0 \rightarrow D^- \pi^+$	0.268%
$B^+ \rightarrow \bar{D}^0 \pi^+ \pi^0$	1.340%	$B^0 \rightarrow D^- \pi^+ \pi^0$	0.760%
$B^+ \rightarrow \bar{D}^0 \pi^+ \pi^+ \pi^-$	1.100%	$B^0 \rightarrow D^- \pi^+ \pi^+ \pi^-$	0.800%
$B^+ \rightarrow D_S^+ \bar{D}^0$	1.000%	$B^0 \rightarrow \bar{D}^0 \pi^0$	0.026%
$B^+ \rightarrow \bar{D}^{0*} \pi^+$	0.519%	$B^0 \rightarrow D_S^+ D^-$	0.720%
$B^+ \rightarrow \bar{D}^{0*} \pi^+ \pi^0$	0.980%	$B^0 \rightarrow D^{*-} \pi^+$	0.276%
$B^+ \rightarrow \bar{D}^{0*} \pi^+ \pi^+ \pi^-$	1.030%	$B^0 \rightarrow D^{*-} \pi^+ \pi^0$	1.500%
$B^+ \rightarrow \bar{D}^{0*} \pi^+ \pi^+ \pi^- \pi^0$	1.800%	$B^0 \rightarrow D^{*-} \pi^+ \pi^+ \pi^-$	0.700%
$B^+ \rightarrow D_S^{+*} \bar{D}^0$	0.760%	$B^0 \rightarrow D^{*-} \pi^+ \pi^+ \pi^- \pi^0$	1.760%
$B^+ \rightarrow D_S^{+*} \bar{D}^{0*}$	0.820%	$B^0 \rightarrow D_S^{+*} D^-$	0.740%
$B^+ \rightarrow D_S^{+*} \bar{D}^{0*}$	1.710%	$B^0 \rightarrow D_S^+ D^{*-}$	0.800%
$B^+ \rightarrow \bar{D}^0 K^+$	0.037%	$B^0 \rightarrow D_S^{+*} D^{*-}$	1.770%
$B^+ \rightarrow D^- \pi^+ \pi^+$	0.107%	$B^0 \rightarrow J/\psi K_S^0$	0.087%
$B^+ \rightarrow J/\psi K^+$	0.101%	$B^0 \rightarrow J/\psi K^+ \pi^-$	0.120%
$B^+ \rightarrow J/\psi K^+ \pi^+ \pi^-$	0.107%	$B^0 \rightarrow J/\psi K_S^0 \pi^+ \pi^-$	0.100%
$B^+ \rightarrow J/\psi K^+ \pi^0$	0.047%		
$B^+ \rightarrow J/\psi K_S^0 \pi^+$	0.094%		

Channels

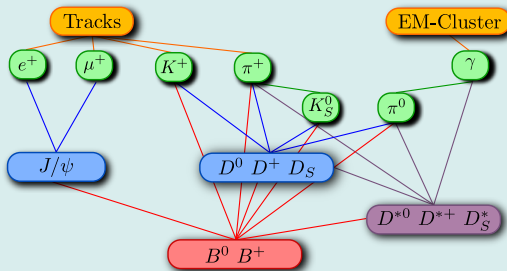
Channel	BR	Channel	BR
$D^0 \rightarrow K^- \pi^+$	3.89%	$D^+ \rightarrow K^- \pi^+ \pi^+$	9.40%
$D^0 \rightarrow K^- \pi^+ \pi^+ \pi^-$	8.09%	$D^+ \rightarrow K_S^0 \pi^+$	1.49%
$D^0 \rightarrow K^- \pi^+ \pi^0$	6.90%	$D^+ \rightarrow K_S^0 \pi^+ \pi^0$	6.90%
$D^0 \rightarrow \pi^+ \pi^-$	0.14%	$D^+ \rightarrow K^- \pi^+ \pi^+ \pi^0$	6.08%
$D^0 \rightarrow \pi^+ \pi^- \pi^0$	1.44%	$D^+ \rightarrow K_S^0 \pi^+ \pi^+ \pi^-$	3.10%
$D^0 \rightarrow K_S^0 \pi^0$	1.22%	$D^+ \rightarrow K^+ K^- \pi^+$	0.98%
$D^0 \rightarrow K_S^0 \pi^+ \pi^-$	2.94%	$D^+ \rightarrow K^+ K^- \pi^+ \pi^0$	1.50%
$D^0 \rightarrow K_S^0 \pi^+ \pi^- \pi^0$	5.40%	$D^{+*} \rightarrow D^0 \pi^+$	67.70%
$D^0 \rightarrow K^+ K^-$	0.39%	$D^{+*} \rightarrow D^+ \pi^0$	30.70%
$D^0 \rightarrow K^+ K^- K_S^0$	0.47%		
$D^{0*} \rightarrow D^0 \pi^0$	61.9%	$D^{0*} \rightarrow D^0 \gamma$	38.10%
$D_S^+ \rightarrow K^+ K_S^0$	1.49%	$D_S^+ \rightarrow K^+ K^- \pi^+ \pi^+ \pi^-$	0.88%
$D_S^+ \rightarrow K^+ \pi^+ \pi^-$	0.69%	$D_S^+ \rightarrow \pi^+ \pi^+ \pi^-$	1.10%
$D_S^+ \rightarrow K^+ K^- \pi^+$	5.50%	$D_S^{+*} \rightarrow D_S^+ \gamma$	94.20%
$D_S^+ \rightarrow K^+ K^- \pi^+ \pi^0$	5.60%	$J/\psi \rightarrow e^- e^+$	5.94%
$D_S^+ \rightarrow K^+ K_S^0 \pi^+ \pi^-$	0.96%	$J/\psi \rightarrow \mu^- \mu^+$	5.93%
$D_S^+ \rightarrow K^- K_S^0 \pi^+ \pi^+$	1.64%		

Channels

Channels	\mathcal{BR}	Channels	\mathcal{BR}	Channels	\mathcal{BR}
D^+	7	29.4%	D^{*+}	2	98.4%
D^0	10	37.9%	D^{*0}	2	100.0%
D_S^+	8	17.9%	D_S^{*+}	1	94.2%
J/ψ	2	11.9%			
			B^+	17	12.0%
			B^0	15	10.4%

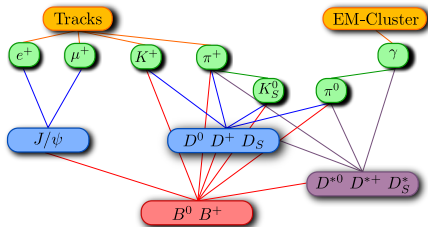
Exclusive reconstruction of **1104 decay channels** and code maintenance would be a futile task.

Hierarchical Reconstruction



How to make the smartest cuts possible?

- How do you compare $D^0 \rightarrow K^- \pi^+$ to $D^0 \rightarrow K_S^0 \pi^+ \pi^- \pi^0$?
- Even worse: The cut depends on the next level: The D^0 meson in $B^+ \rightarrow \bar{D}^0 \pi^+ \pi^+ \pi^-$ should get a different cut than in $B^+ \rightarrow \bar{D}^0 \pi^+$.
- Solution:** Multiply the signal probability (given by the NeuroBayes training) of all children and use that to cut.

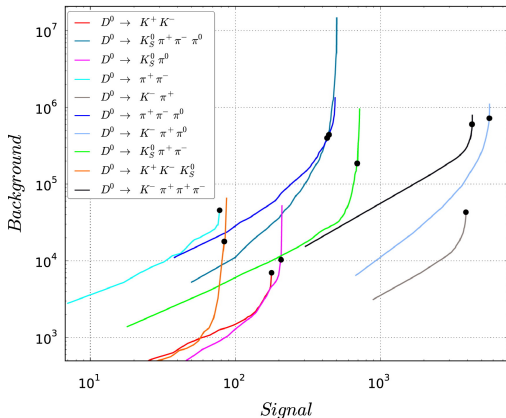


Cut decisions are postponed to a later level

Not only the reconstruction is **hierarchical**, but also the **information flow**.

Pre-cuts

- Cut on the product of the **signal probabilities** (= **NeuroBayes outputs**) of the children.



- Choose a cut to have roughly the same slope for all curves.
- This slope corresponds to the number of candidates.
- Very soft cuts, usage of probability product on next level.
- Trade-off: Efficiency \leftrightarrow Purity and CPU time.

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- Run the Full Reconstruction on your data set
- The “fullrecon table” is added to certain events of your data set (Belle specific)
- Choose your candidate

```
-----  
ID TAG_ID DECAYDDEC(1)DDEC(2)DDEC(3)DDEC(4) NBRANK NBOUTCNT_NBCONT_NB MCINFO DELTAE MBC NFS BREC  
-----  
1 521 521743 421421 0 0 0 2 0.09 0 0.00 -2 -0.09 5.29 7 1  
2 -521-521743 421421 0 0 0 3 0.01 0 0.00 -2 0.06 5.26 7 13  
3 -521-521743 421421 0 0 0 1 0.25 0 0.00 1 -0.09 5.28 7 25  
-----
```

What is the result of the Full Reconstruction?

- A collection of B_{tag} candidates
- Visualisation of results: *beam constrained mass* M_{bc}

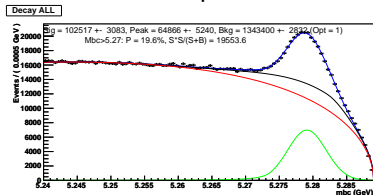
$$M_{bc} \equiv \sqrt{E_{\text{beam}}^2 - p_B^2}$$

Any basis for comparison?

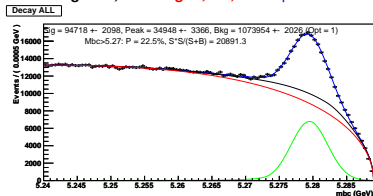
- Yes! The cut-based predecessor to this Full Reconstruction.

Adjusting Cut on NeuroBayes output

Cut-based predecessor

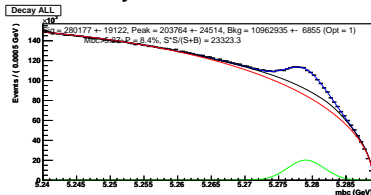


sig: 103,000 bg: 1,300,000 pur: 19.6 %

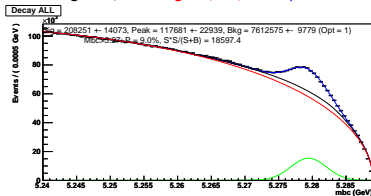


sig: 95,000 bg: 1,100,000 pur: 22.5 %

NeuroBayes Full Reconstruction



sig: 280,000 bg: 11,000,000 pur: 8.4 %



sig: 209,000 bg: 7,600,000 pur: 9.0 %

The Full Reconstruction

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NeuroBayes

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Efficiency and Purity

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Results

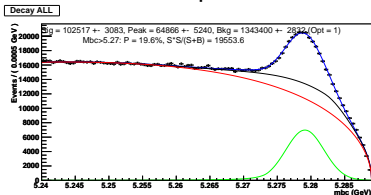
●○○○○○○○○○○

Adjusting Cut on NeuroBayes output

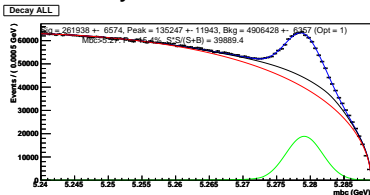
Cut-based predecessor

NeuroBayes Full Reconstruction

B^+

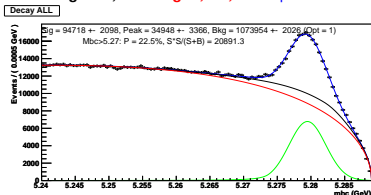


sig: 103,000 bg: 1,300,000 pur: 19.6 %

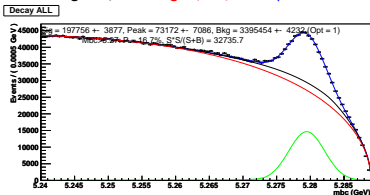


sig: 262,000 bg: 4,900,000 pur: 15.4 %

B^0



sig: 95,000 bg: 1,100,000 pur: 22.5 %



sig: 198,000 bg: 3,400,000 pur: 16.7 %

The Full Reconstruction

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NeuroBayes

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Efficiency and Purity

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Results

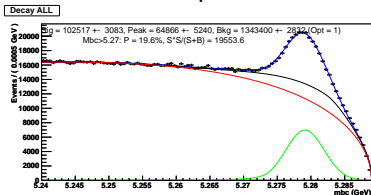
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Adjusting Cut on NeuroBayes output

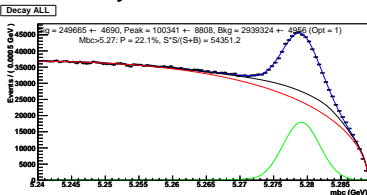
Cut-based predecessor

NeuroBayes Full Reconstruction

B^+

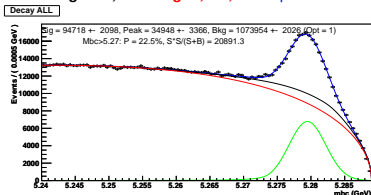


sig: 103,000 bg: 1,300,000 pur: 19.6 %

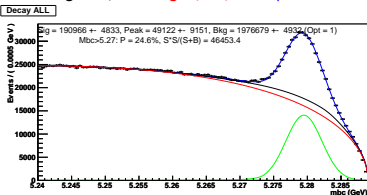


sig: 250,000 bg: 2,900,000 pur: 22.1 %

B^0



sig: 95,000 bg: 1,100,000 pur: 22.5 %



sig: 191,000 bg: 2,000,000 pur: 24.6 %

The Full Reconstruction

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NeuroBayes

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Efficiency and Purity

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Results

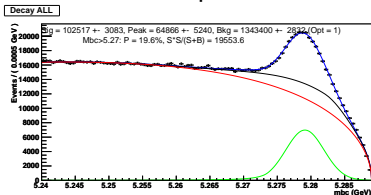
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Adjusting Cut on NeuroBayes output

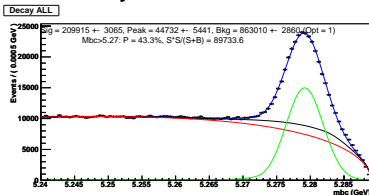
Cut-based predecessor

NeuroBayes Full Reconstruction

B^+

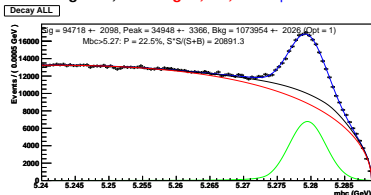


sig: 103,000 bg: 1,300,000 pur: 19.6 %

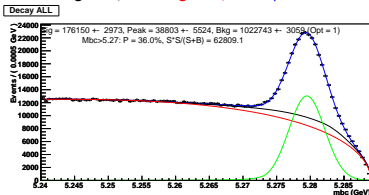


sig: 210,000 bg: 860,000 pur: 43.3 %

B^0



sig: 95,000 bg: 1,100,000 pur: 22.5 %



sig: 176,000 bg: 1,000,000 pur: 36.0 %

The Full Reconstruction

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NeuroBayes

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Efficiency and Purity

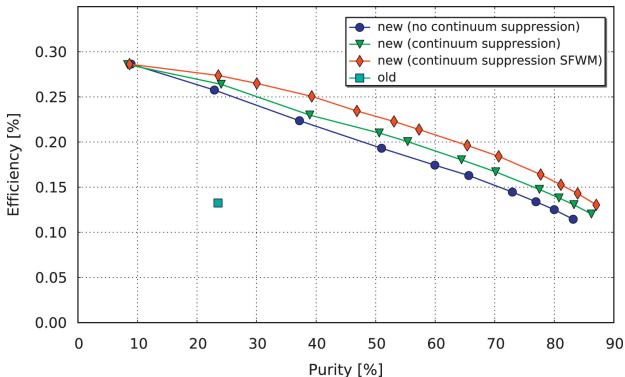
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Results

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Purity-Efficiency

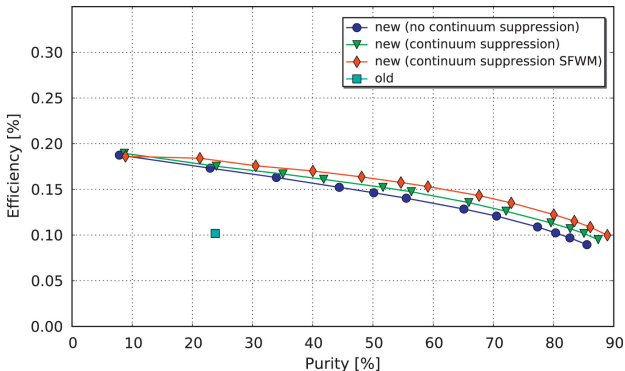
- Classification of B^+ mesons, cut on the signal probability



With high efficiency: 2.1 Million B_{tag}^+ mesons

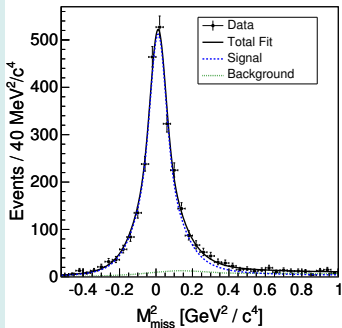
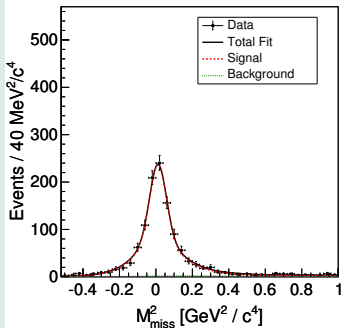
Purity-Efficiency

- Classification of B^0 mesons, cut on the signal probability



With high efficiency: 1.4 Million B_{tag}^0 mesons

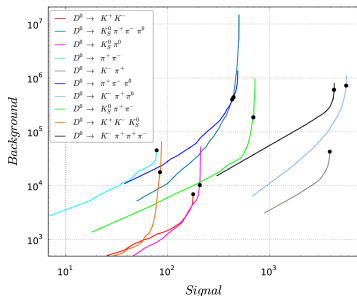
Exemplary signal side reconstruction: $B^0 \rightarrow D^{*-} l^+ \nu_l$



Comparison between the cut based (**left**) and the NeuroBayes (**right**) Full Reconstruction.

Reduced Channels

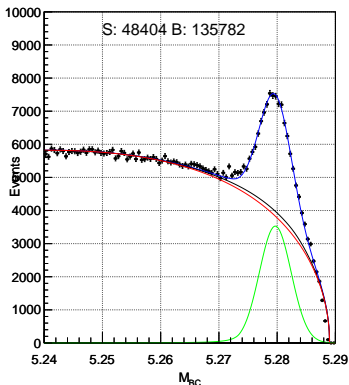
- The question has popped up:
“How much of the improvement is due to new channels and how much due to NeuroBayes?”
- Hard to answer, as the two aspects are connected.



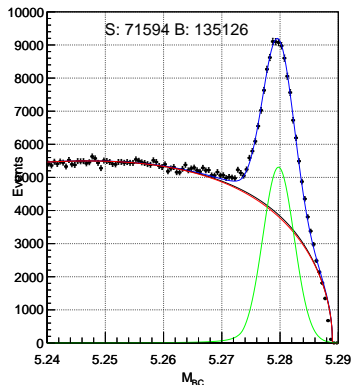
Approximation: Only use channels that are common to both Full Reconstructions.

Reduced Channels B^0

old: All shared B^0 modes combined



ekp: All shared B^0 modes combined



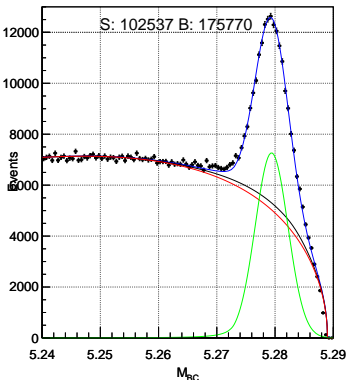
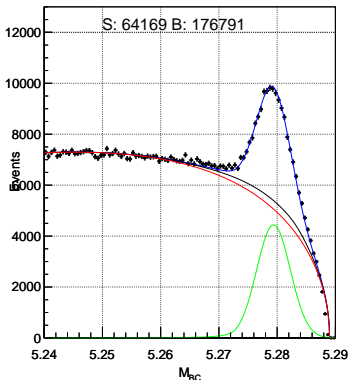
Still a factor ~ 1.5 improvement

Tag side for only common channels for the cut based (**left**) and the NeuroBayes (**right**) Full Reconstruction.

Reduced Channels B^+

old: All shared B^+ modes combined

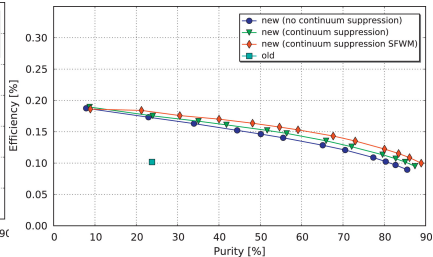
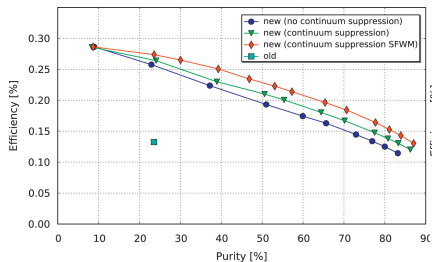
ekp: All shared B^+ modes combined



Still a factor ~ 1.6 improvement

Tag side for only common channels for the cut based (**left**) and the NeuroBayes (**right**) Full Reconstruction.

Summary and Conclusion



- The Full Reconstruction allows to **measure missing momentum** and is therefore **crucial for numerous analyses**.
- NeuroBayes and a hierarchical information flow \Rightarrow **improvement of factor ~ 2** .
- Corresponds to 10 years of data taking.



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A hierarchical NeuroBayes-based algorithm for full reconstruction of B mesons at B factories

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