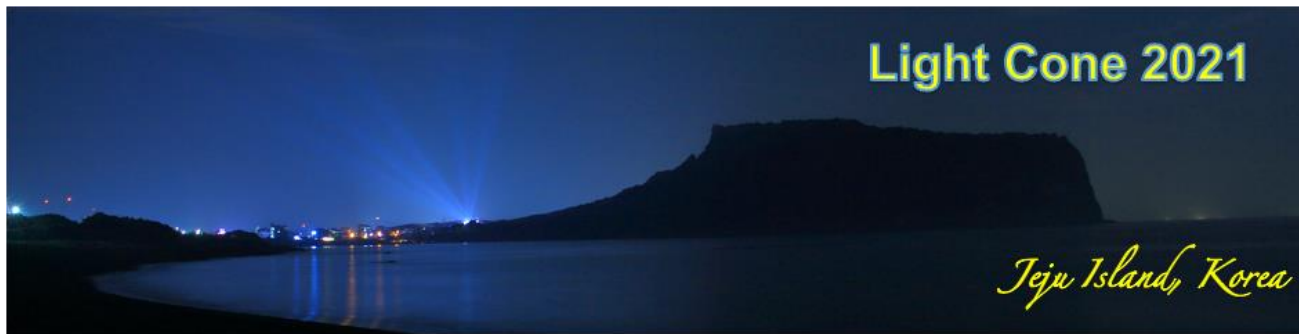


Production of multi-charmed and exotic hadrons in heavy ion collisions

Light Cone 2021 :
Physics of Hadrons on the Light Front



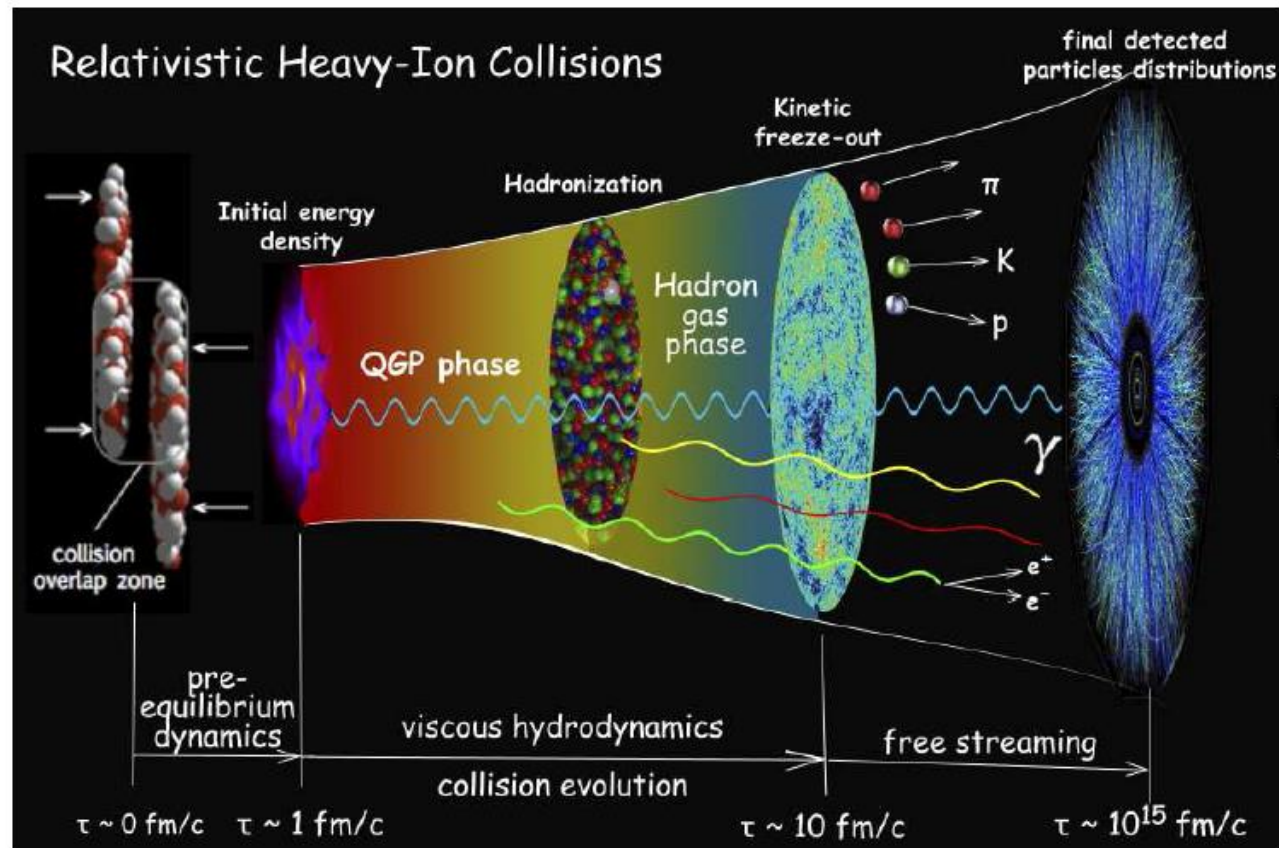
December 1st 2021
Booyoung Hotel, Jeju



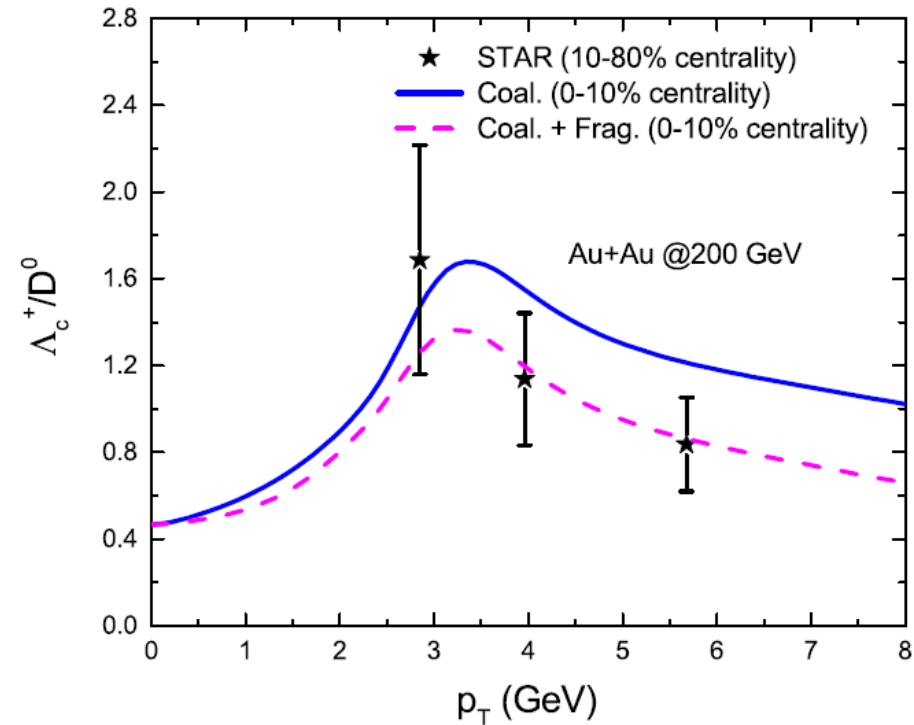
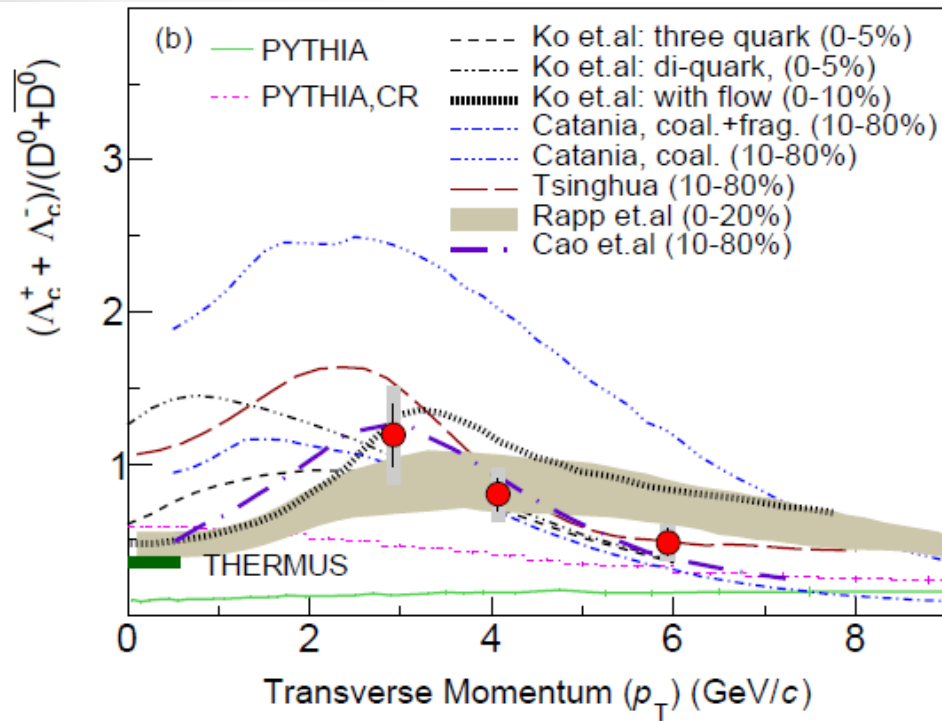
Sungtae Cho
Kangwon National University

Introduction

– Relativistic heavy ion collisions



– Regeneration of charmed hadrons : Λ_c/D_0



J. Adams et al, (STAR Collaboration), Phys. Rev. Lett. **124**, 172301 (2021)

Y. Oh, C. M. Ko, S. H. Lee, and S. Yasui, Phys. Rev. C **79**, 044905 (2009)

S. Cho, K-J. Sun, C. M. Ko, S. H. Lee, and Y. Oh, Phys. Rev. C **101**, 024909 (2020)

- X(3872) mesons

X(3872)

$$I^G(J^{PC}) = 0^+(1^{++})$$

J. Beringer *et al.* (PDG), Phys. Rev. D **86**, 010001 (2012)

Mass $m = 3871.68 \pm 0.17$ MeV
 $m_{X(3872)} - m_{J/\psi} = 775 \pm 4$ MeV
 $m_{X(3872)} - m_{\psi(2S)}$
 Full width $\Gamma < 1.2$ MeV, CL = 90%

S.K. Choi *et al.* [Belle Collaboration], Phys. Rev. Lett. **90**, 242001 (2003)

- T_{cc} (ccqq) mesons

Particle	m [MeV]	(I, J^P)
T_{cc}^1	3797	$(0, 1^+)$

S. Cho *et al.* (EXHIC Collaboration), Prog. Part. Nucl. Phys. **95**, 279 (2017)

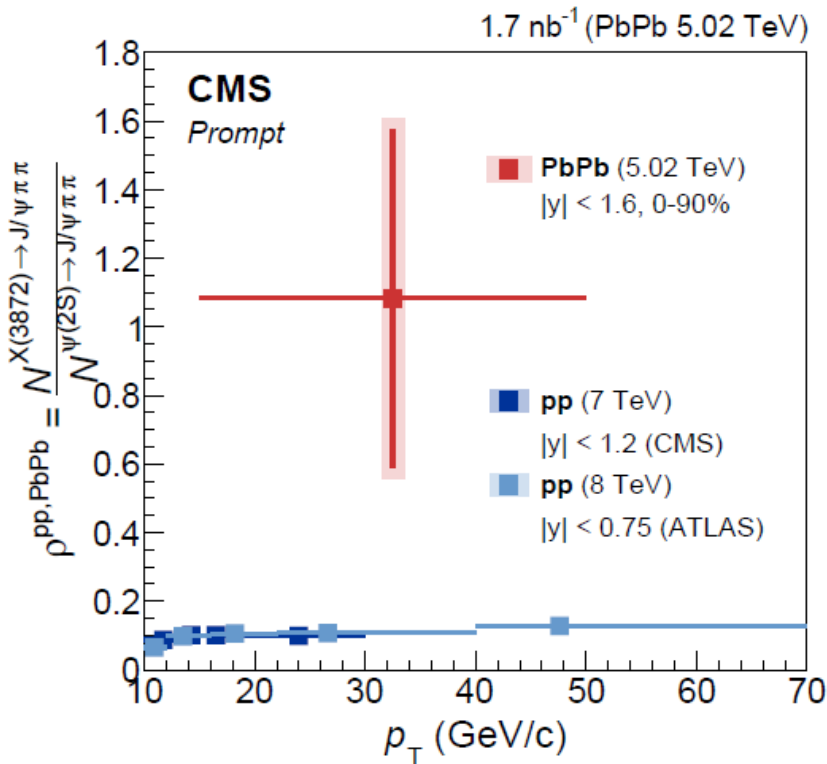
- Estimated yields of X(3872) and T_{cc} mesons

	RHIC				LHC			
	$2q/3q/6q$	$4q/5q/8q$	Mol.	Stat.	$2q/3q/6q$	$4q/5q/8q$	Mol.	Stat.
T_{cc}^{1a}	—	4.0×10^{-5}	2.4×10^{-5}	4.3×10^{-4}	—	6.6×10^{-4}	4.1×10^{-4}	7.1×10^{-3}
X(3872)	1.0×10^{-4}	4.0×10^{-5}	7.8×10^{-4}	2.9×10^{-4}	1.7×10^{-3}	6.6×10^{-4}	1.3×10^{-2}	4.7×10^{-3}

^aParticles that are newly predicted by theoretical model.

S. Cho *et al.* (EXHIC Collaboration), Phys. Rev. C **84**, 064910 (2011)

- Recent measurements of X(3872) in Pb+Pb collisions and an exotic doubly charmed tetraquark, T_{cc} in p+p collisions



$$\rho^{pp} = 0.106 \pm 0.008 \text{ (stat)} \pm 0.004 \text{ (syst)}$$

$$\rho^{PbPb} = 1.08 \pm 0.49 \text{ (stat)} \pm 0.52 \text{ (syst)}$$

Albert M. Sirunyan et al. [CMS Collaboration],

arXiv: 2102.13048



CERN-EP-2021-165
LHCb-PAPER-2021-031
September 2, 2021

Observation of an exotic narrow doubly charmed tetraquark

LHCb collaboration[†]

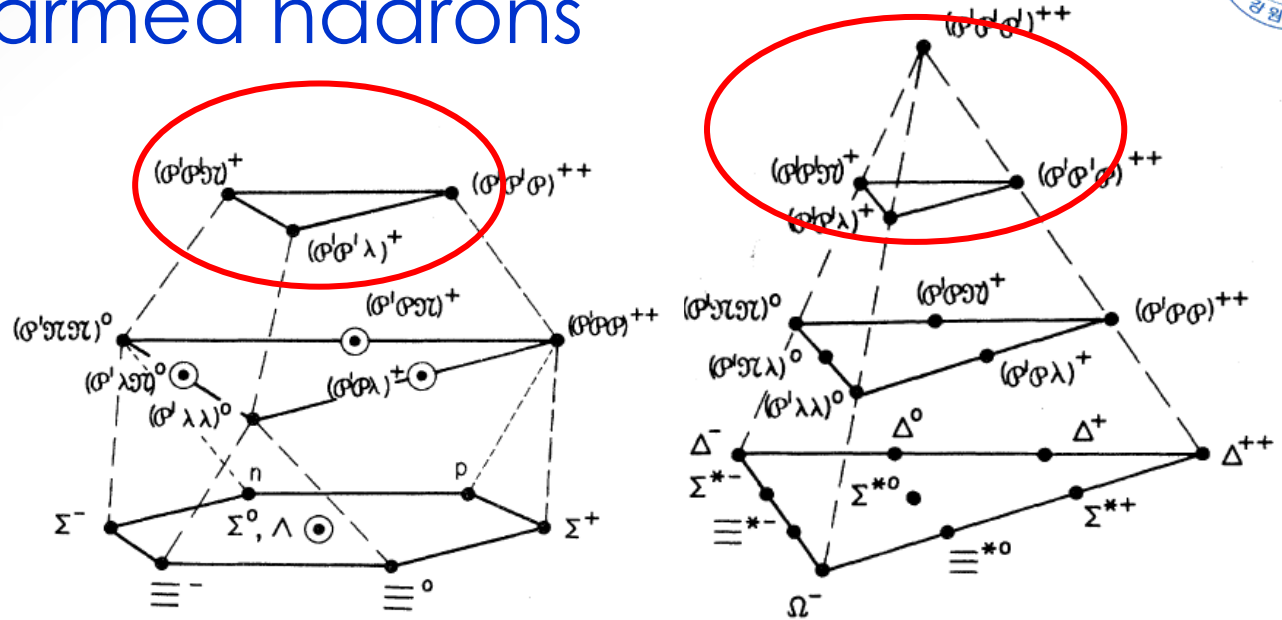
Abstract

Conventional hadronic matter consists of baryons and mesons made of three quarks and quark-antiquark pairs, respectively. The observation of a new type of hadronic state, a doubly charmed tetraquark containing two charm quarks, an anti-u and an anti-d quark, is reported using data collected by the LHCb experiment at the Large Hadron Collider. This exotic state with a mass of about 3875 MeV/c² manifests itself as a narrow peak in the mass spectrum of D⁰D⁰π⁺ mesons just below the D^{*+}D⁰ mass threshold. The near-threshold mass together with a strikingly narrow width reveals the resonance nature of the state.

19.01038v2 [hep-ex] 3 Sep 2021

R. Aaji et al. (LHCb Collaboration),
arXiv:2109.01038

- Multi-charmed hadrons



A. De Rujula, H. Georgi,
and S. Glashaw
Phys. Rev. D **12**, 147 (1975)

1) Doubly and triply charmed hadrons, Ξ_{cc} , Ξ_{cc}^* , Ω_{cc} , Ω_{cc}^* , Ω_{ccc}

- Observation of the doubly charmed baryon in 2017

PRL **119**, 112001 (2017)

PHYSICAL REVIEW LETTERS

Wook Chung
15 SEPTEMBER 2017

Observation of the Doubly Charmed Baryon Ξ_{cc}^{++}

R. Aaij *et al.**

(LHCb Collaboration)

(Received 6 July 2017; revised manuscript received 2 August 2017; published 11 September 2017)

Hadron production in heavy ion collisions

– Quark coalescence

V. Greco, C. M. Ko, and P. Levai, Phys. Rev. C **68**, 034904 (2003)

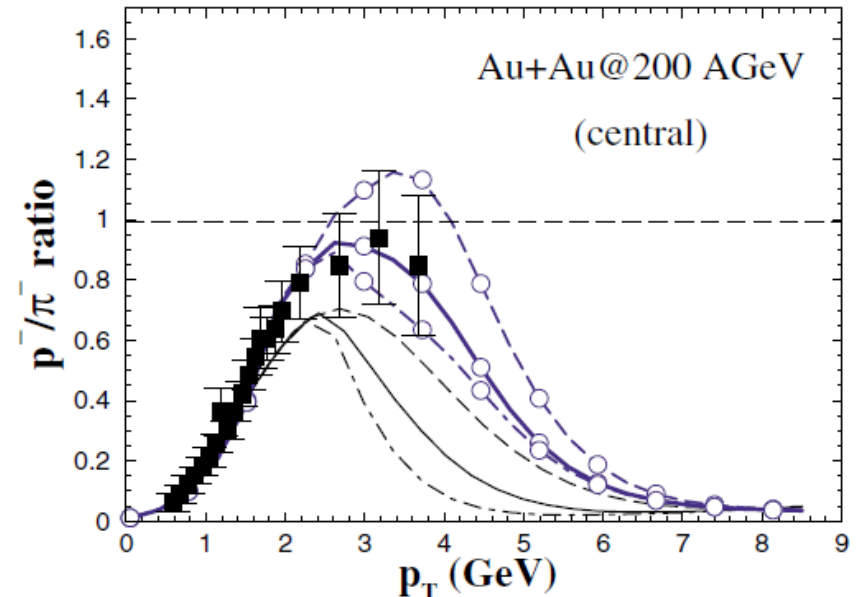
R. J. Freis, B. Muller, C. Nonaka, and S. Bass, Phys. Rev. C **68**, 044902 (2003)

$$N^{Coal} = g \int \left[\prod_{i=1}^n \frac{1}{g_i} \frac{p_i \cdot d\sigma_i}{(2\pi)^3} \frac{d^3 p_i}{E_i} f(x_i, p_i) \right] f^W(x_1, \dots, x_n; p_1, \dots, p_n)$$

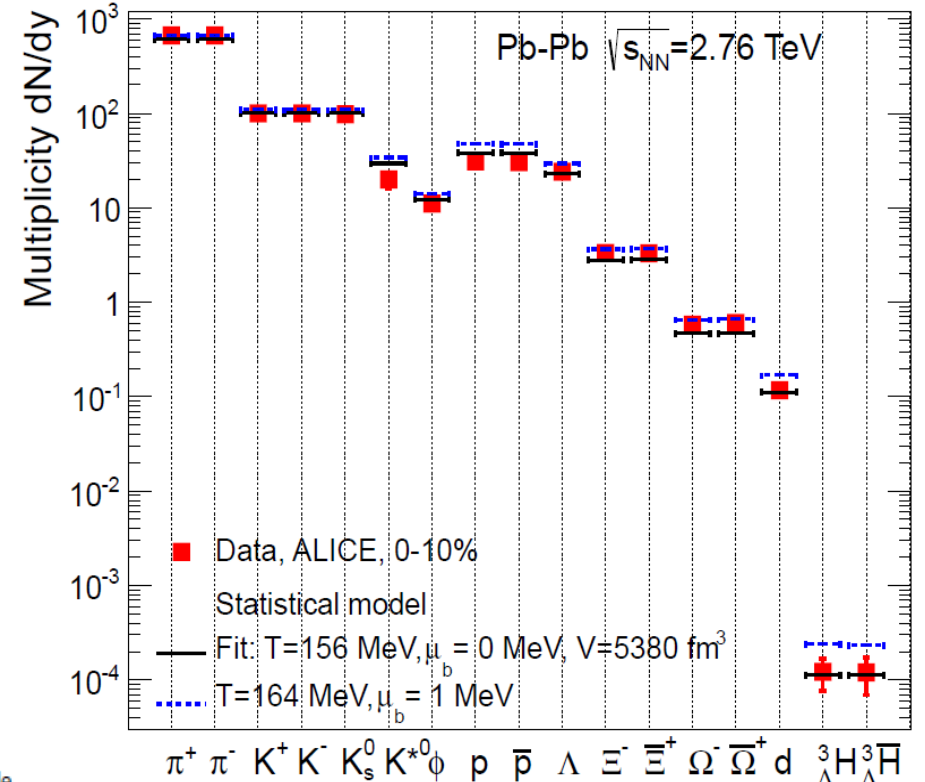
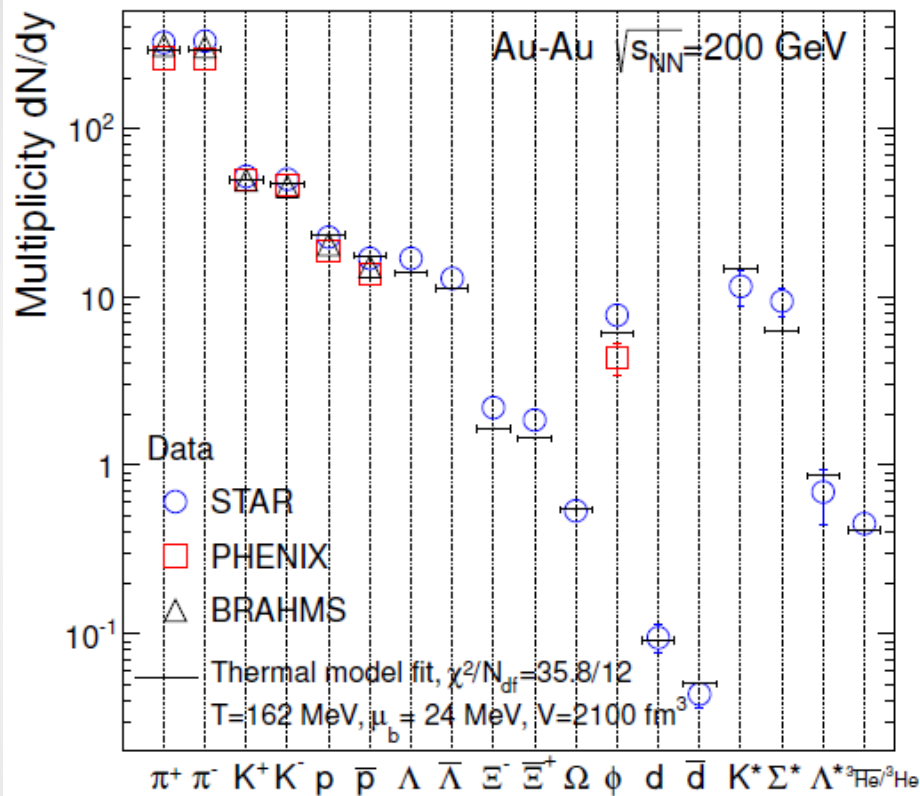
1) The coalescence probability function, the Wigner function

2) Constraints on constituents in the system

$$\int p_i \cdot d\sigma_i \frac{d^3 p_i}{(2\pi)^3 E_i} f(x_i, p_i) = N_i$$



– Statistical hadronization



A. Andronic, P. Braun-Munzinger, K. Redlich and J. Stachel, Nucl. Phys. A **904-905**, 535c (2013)

J. Stachel, A. Andronic, P. Braun-Munzinger, and K. Redlich, J. Phys. Conf. Ser. **509**, 012019 (2014)

Multi-charmed and exotic hadron production



S. Cho *et al.* [ExHIC Collaboration], Prog. Part. Nucl. Phys. **95**, 279 (2017)

S. Cho and S. H. Lee, Phys. Rev. C **101**, 024902 (2020)

	RHIC		LHC (2.76 TeV)	
	Sc. 1	Sc. 2	Sc. 1	Sc. 2
T_H (MeV)		162		156
V_H (fm ³)		2100		5380
μ_B (MeV)		24		0
μ_s (MeV)		10		0
γ_c		22		39
γ_b		4.0×10^7		8.6×10^8
T_C (MeV)	162	166	156	166
V_C (fm ³)	2100	1791	5380	3533
$N_u = N_d$	320	302	700	593
$N_s = N_{\bar{s}}$	183	176	386	347
$N_c = N_{\bar{c}}$		4.1		11
$N_b = N_{\bar{b}}$		0.03		0.44

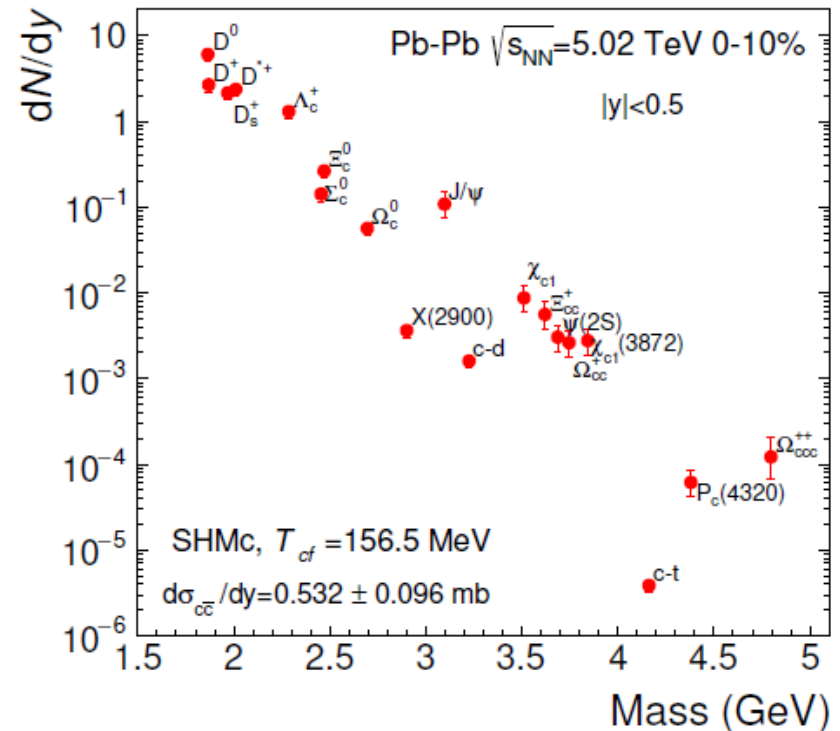
$$N_h^{\text{coal}} = \frac{g_h V_c}{(4\pi)^{3/2}} \frac{(\omega_c \sum_i^3 m_i)^{3/2}}{(1 + 2T_c/\omega_c)^2} \prod_{i=1}^3 \frac{N_i (4\pi)^{3/2}}{g_i V_c (m_i \omega_c)^{3/2}}.$$

$$N_h^{\text{stat}} = V_H \frac{g_h}{2\pi^2} \int_0^\infty \frac{p^2 dp}{\gamma_c^{-n} e^{E_h/T_H} \pm 1},$$

– Comparison with results from the statistical hadronization model

	RHIC		LHC	
	Stat.	Coal.	Stat.	Coal.
Ξ_{cc}	1.0×10^{-2}	1.3×10^{-3}	2.8×10^{-2}	4.9×10^{-3}
Ξ_{cc}^*	6.4×10^{-3}	9.0×10^{-4}	1.8×10^{-2}	3.3×10^{-3}
Ω_{scc}	2.8×10^{-3}	2.5×10^{-4}	8.0×10^{-3}	9.0×10^{-4}
Ω_{scc}^*	1.5×10^{-3}	1.6×10^{-4}	4.3×10^{-3}	6.0×10^{-4}
Ω_{ccc}	1.1×10^{-4}	1.1×10^{-6}	4.0×10^{-4}	5.3×10^{-6}
T_{cc}	8.9×10^{-4}	5.3×10^{-5}	2.7×10^{-3}	1.3×10^{-4}
X_2	5.7×10^{-4}	5.6×10^{-4}	1.7×10^{-3}	1.7×10^{-3}
X_4	5.7×10^{-4}	5.3×10^{-5}	1.7×10^{-3}	1.3×10^{-4}

the ratios of the yield in the coalescence model compared to that in the statistical model are 0.010 (0.013) for the Ω_{ccc} , 0.089 (0.11) for the Ω_{scc} , 0.13 (0.18) for the Ξ_{cc} , 0.060 (0.048) for the T_{cc} , and 0.093 (0.077) for the X_4 at RHIC (LHC).



A. Andronic, P. Braun-Munzinger, M. K. Kohler, A. Mazeliauskas, K. Redlich, J. Stachel, and V. Viskovic, J. High Energy Phys. **2021**, 35 (2021).

– Transverse momentum distribution of multi-charmed hadrons

S. Cho and S. H. Lee, Phys. Rev. C **101**, 024902 (2020)

1) Charmed hadron yields in the coalescence model

$$N_{\Xi_{cc}} = g_{\Xi_{cc}} \int p_l \cdot d\sigma_l p_{c_1} \cdot d\sigma_{c_1} p_{c_2} \cdot d\sigma_{c_2} \frac{d^3 \vec{p}_l}{(2\pi)^3 E_l} \frac{d^3 \vec{p}_{c_1}}{(2\pi)^3 E_{c_1}} \frac{d^3 \vec{p}_{c_2}}{(2\pi)^3 E_{c_2}} f_l(r_l, p_l) f_{c_1}(r_{c_1}, p_{c_1})$$

$$\times f_{c_2}(r_{c_2}, p_{c_2}) W_{\Xi_{cc}}(r_l, r_{c_1}, r_{c_2}; p_l, p_{c_1}, p_{c_2})$$

$$N_X = g_X \int p_l \cdot d\sigma_l p_{\bar{l}} \cdot d\sigma_{\bar{l}} p_c \cdot d\sigma_c p_{\bar{c}} \cdot d\sigma_{\bar{c}} \frac{d^3 \vec{p}_l}{(2\pi)^3 E_l} \frac{d^3 \vec{p}_{\bar{l}}}{(2\pi)^3 E_{\bar{l}}} \frac{d^3 \vec{p}_c}{(2\pi)^3 E_c} \frac{d^3 \vec{p}_{\bar{c}}}{(2\pi)^3 E_{\bar{c}}}$$

$$\times f_l(r_l, p_l) f_{\bar{l}}(r_{\bar{l}}, p_{\bar{l}}) f_c(r_c, p_c) f_{\bar{c}}(r_{\bar{c}}, p_{\bar{c}}) W_X(r_l, r_{\bar{l}}, r_c, r_{\bar{c}}; p_l, p_{\bar{l}}, p_c, p_{\bar{c}})$$

2) Transverse momentum distributions

$$\frac{d^2 N_{\Xi_{cc}}}{d^2 \vec{p}_T} = \frac{g_{\Xi_{cc}}}{V^2} \int d^3 \vec{r}_1 d^3 \vec{r}_2 d^2 \vec{p}_{lT} d^2 \vec{p}_{c_1T} d^2 \vec{p}_{c_2T} \delta^{(2)}(\vec{p}_T - \vec{p}_{lT} - \vec{p}_{c_1T} - \vec{p}_{c_2T}) \frac{d^2 N_l}{d^2 \vec{p}_{lT}}$$

$$\times \frac{d^2 N_{c_1}}{d^2 \vec{p}_{c_1T}} \frac{d^2 N_{c_2}}{d^2 \vec{p}_{c_2T}} W_{\Xi_{cc}}(\vec{r}'_1, \vec{r}'_2, \vec{r}'_3, \vec{k}_1, \vec{k}_2, \vec{k}_3),$$

$$\frac{d^2 N_X}{d^2 \vec{p}_T} = \frac{g_X}{V^3} \int d^3 \vec{r}_1 d^3 \vec{r}_2 d^3 \vec{r}_3 d^2 \vec{p}_{lT} d^2 \vec{p}_{\bar{l}T} d^2 \vec{p}_{cT} d^2 \vec{p}_{\bar{c}T} \delta^{(2)}(\vec{p}_T - \vec{p}_{lT} - \vec{p}_{\bar{l}T} - \vec{p}_{cT} - \vec{p}_{\bar{c}T}) \frac{d^2 N_l}{d^2 \vec{p}_{lT}} \frac{d^2 N_{\bar{l}}}{d^2 \vec{p}_{\bar{l}T}}$$

$$\times \frac{d^2 N_c}{d^2 \vec{p}_{cT}} \frac{d^2 N_{\bar{c}}}{d^2 \vec{p}_{\bar{c}T}} W_X(\vec{r}'_1, \vec{r}'_2, \vec{r}'_3, \vec{k}_1, \vec{k}_2, \vec{k}_3)$$

3) Transverse momentum distributions of charm, light quarks and D⁰ mesons

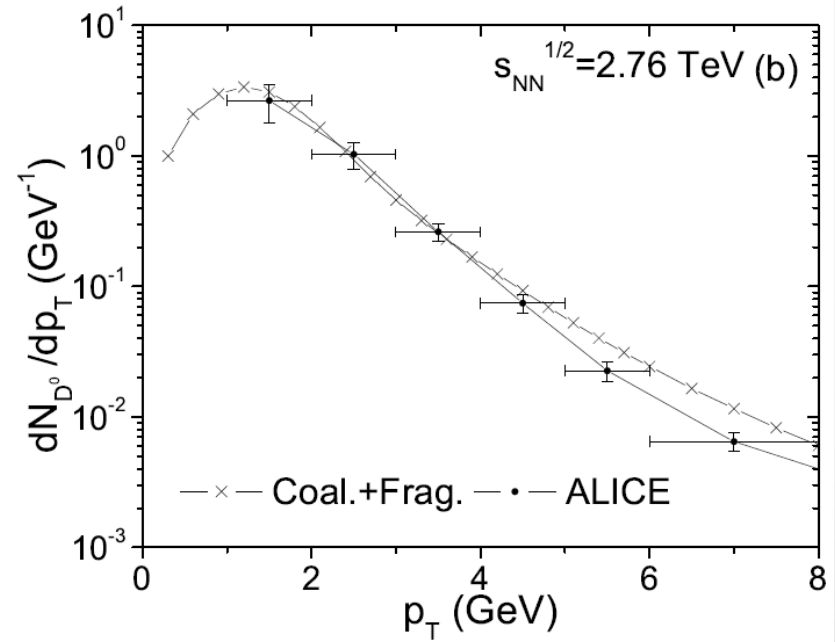
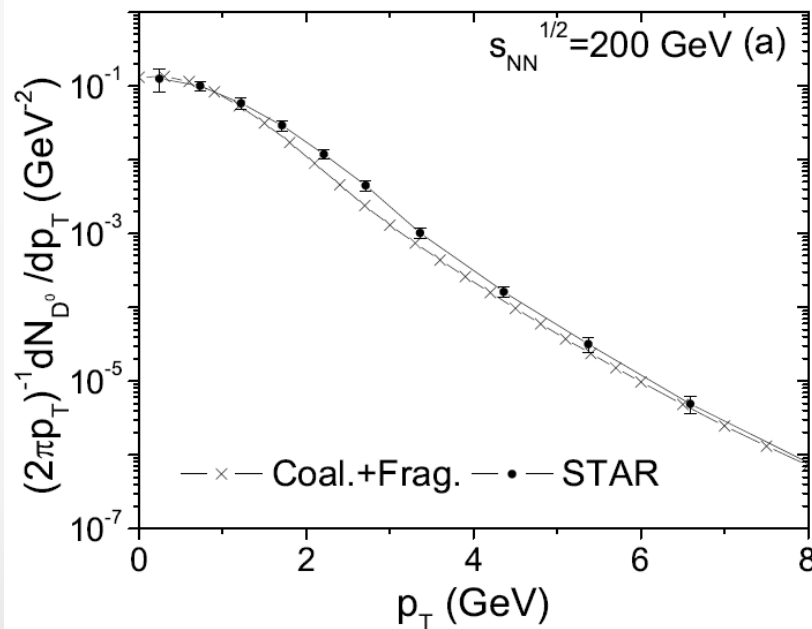
$$\frac{dN_c}{d^2p_T} = \begin{cases} a_0 \exp[-a_1 p_T^{a_2}] & p_T \leq p_0 \\ a_0 \exp[-a_1 p_T^{a_2}] + a_3(1 + p_T^{a_4})^{-a_5} & p_T \geq p_0 \end{cases}$$

$$\frac{d^2N_l}{d^2p_T} = g_l \frac{V}{(2\pi)^3} m_T e^{-m_T/T_{eff}},$$

	a_0	a_1	a_2	a_3	a_4	a_5
RHIC						
$p_T \leq p_0$	0.69	1.22	1.57			
$p_T \geq p_0$	1.08	3.04	0.71	3.79	2.02	3.48
LHC						
$p_T \leq p_0$	1.97	0.35	2.47			
$p_T \geq p_0$	7.95	3.49	3.59	87335	0.5	14.31

S. Plumari, V. Minissale, S. K. Das, G. Coci and V. Greco, Eur. Phys. J. C **78**:348 (2017)

Y. Oh, C. M. Ko, S.-H. Lee, and S. Yasui, Phys. Rev. C **79** 044905 (2009)



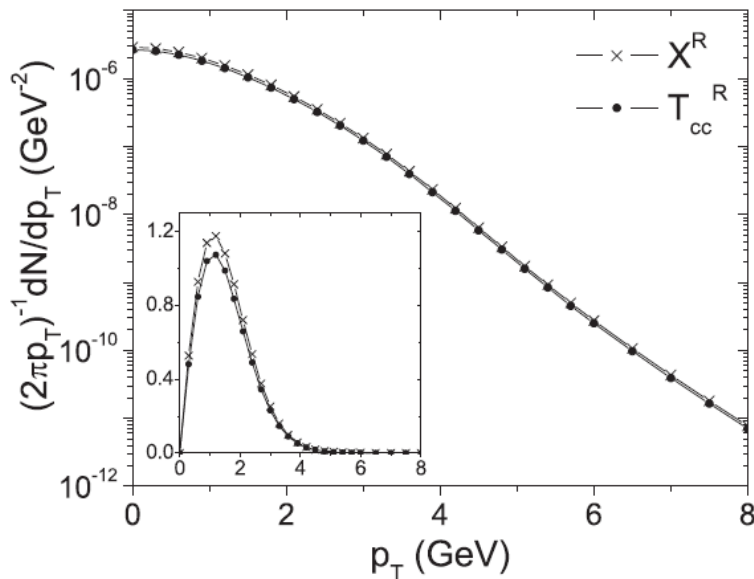
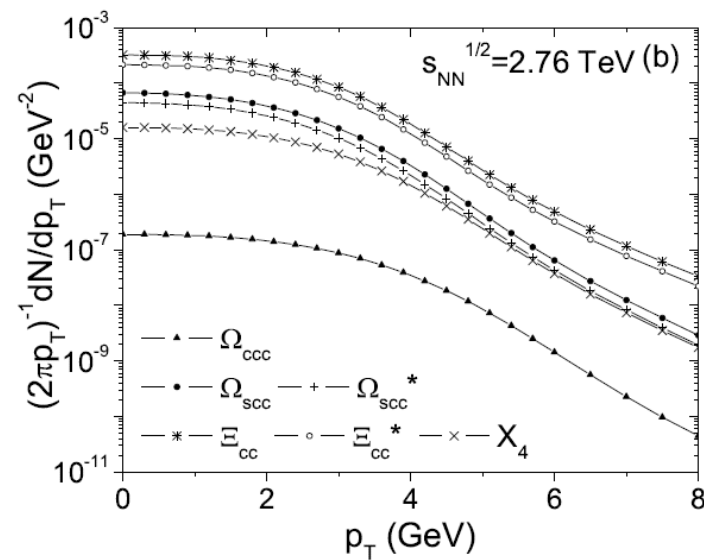
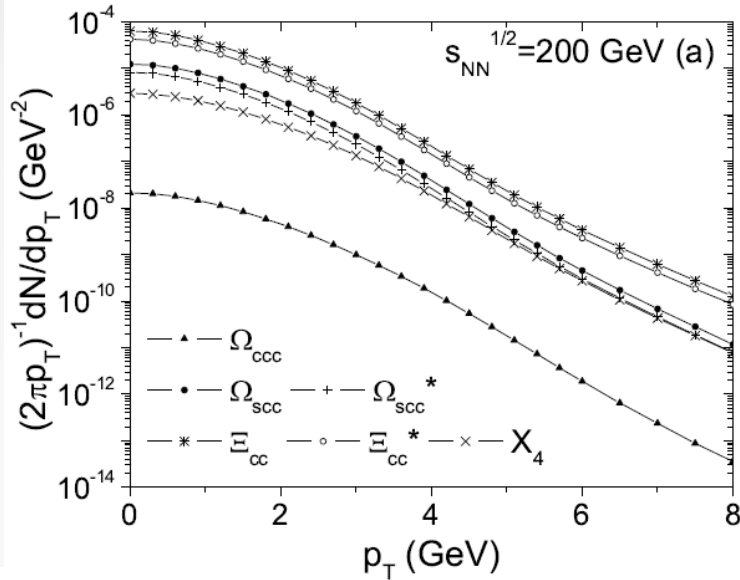
J. Adam et al. [STAR Collaboration], Phys. Rev. C **99**, no. 3, 034908 (2019)

J. Adam et al. [ALICE Collaboration], JHEP **1603**, 081 (2016)

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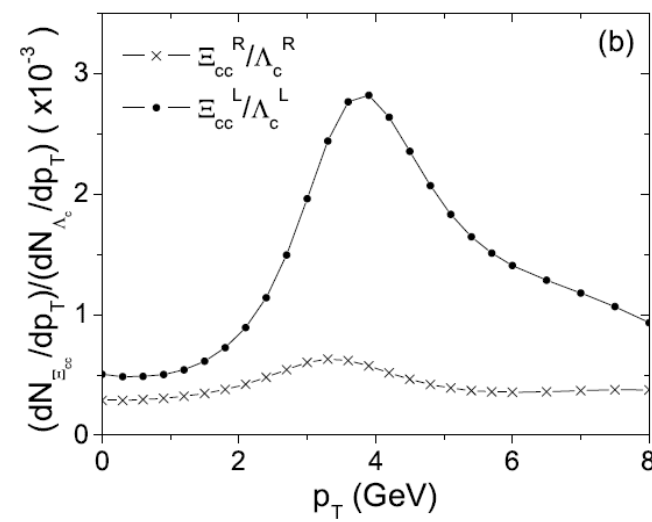
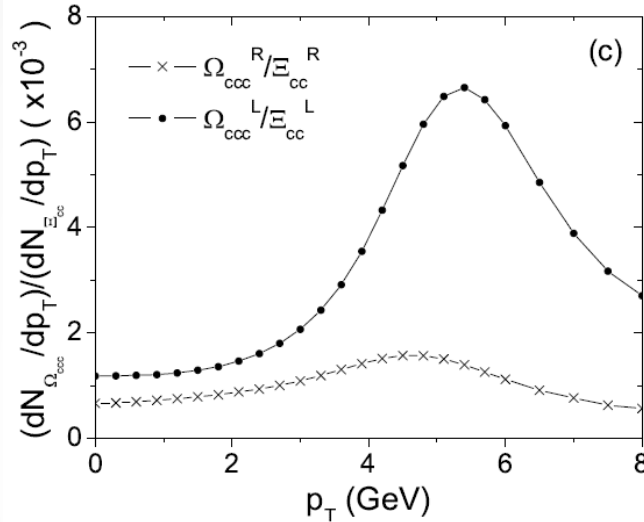
4) Transverse momentum distributions of charmed hadrons



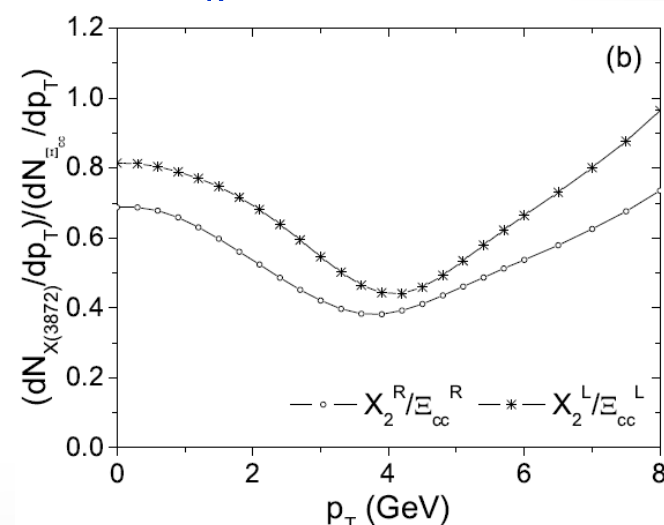
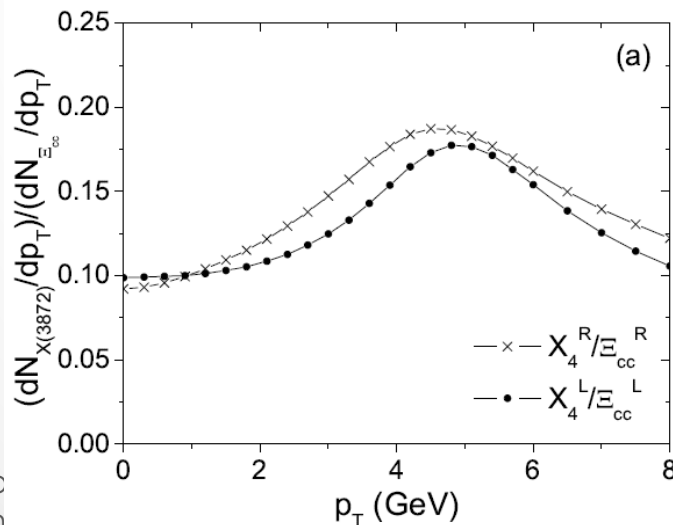
	RHIC	LHC
$[\Xi]_{cc}$	4.4×10^{-4}	6.7×10^{-3}
$[\Xi]_{cc}^*$	2.9×10^{-4}	4.5×10^{-3}
Ω_{scc}	8.6×10^{-5}	1.3×10^{-3}
Ω_{scc}^*	5.7×10^{-5}	8.5×10^{-4}
Ω_{ccc}	1.7×10^{-7}	5.9×10^{-6}
T_{cc}	2.2×10^{-5}	3.8×10^{-4}
X_4	2.4×10^{-5}	3.8×10^{-4}
X_2	2.6×10^{-4}	4.5×10^{-3}
D^0	0.71	6.0
Λ_c	0.63	4.0

– Transverse momentum distribution ratios

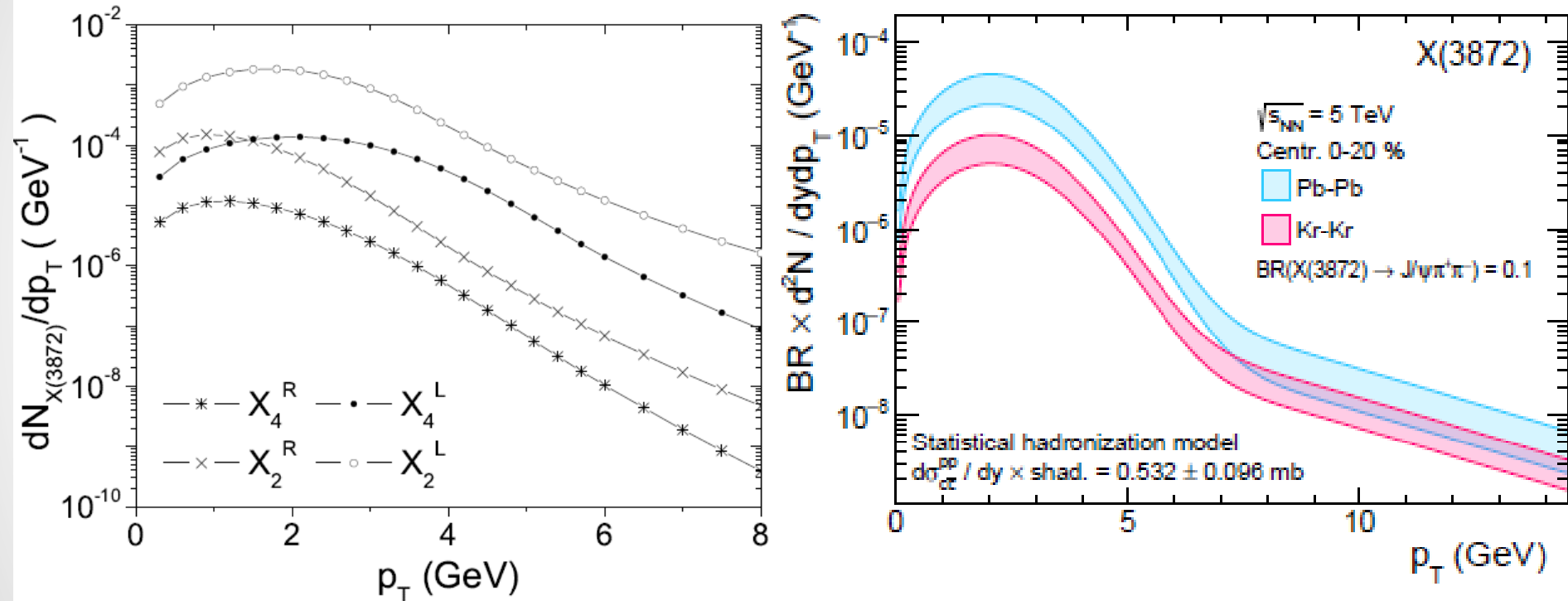
1) Baryon/baryon (ccc/ccq, or ccq/cqq)



2) Meson/baryon (ccqq/ccq, or cc/ccq)



– Comparison with results from the statistical hadronization model



A. Andronic, P. Braun-Munzinger, M. K. Kohler, K. Redlich and J. Stachel, Phys. Lett. B **797**, 134836 (2019).

Conclusion

- Production of multi-charmed and exotic hadrons in heavy ion collisions
- 1) Studying the yield and transverse momentum distribution of charmed hadrons in heavy ion collisions can help us understand hadron production mechanism as well as the properties of the quark- gluon plasma
 - 2) Heavy ion collision experiments can provide better chances to study production of multi-charm hadrons as well as exotic hadrons
 - 3) Transverse momentum distributions, and also the ratio between transverse momentum distributions of various hadrons can give us information on the internal structure of hadrons

Many more experimental and theoretical studies are expected.



Thank you for your attention!