

Recent progress of Hypernuclear physics

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Major goals of hypernuclear physics

To understand baryon-baryon interactions

Fundamental and important for the study of nuclear physics

Total number of
Nucleon (N) -Nucleon (N) data: 4,000



- Total number of differential cross section
Hyperon (Y) -Nucleon (N) data: 40
- **NO** YY scattering data

YN and YY potential models so far proposed (ex. Nijmegen, Julich, Kyoto-Niigata) have large ambiguity.

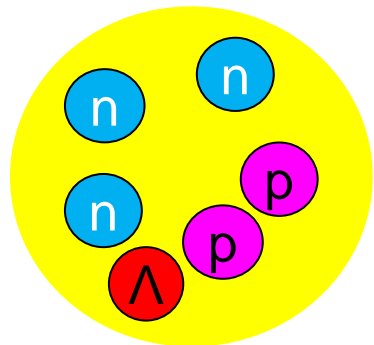
Therefore, for the study of YN and YY interactions, the systematic investigation of the structure of light hypernuclei is one of the important way.

(it is planned to perform YN scattering data at J-PARC.)

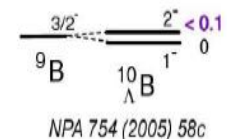
Once YN and YY interactions are determined, we can predict interesting phenomena which cannot be imagined so far. In addition, we could study inner part of neutron stars which have been observed.

Since 1998

Hypernuclear γ -ray data (2019)

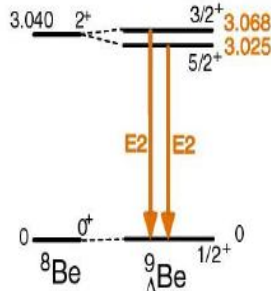


$^{10}\text{B} (K^-, \pi^+ \gamma)$ BNL E930('01)



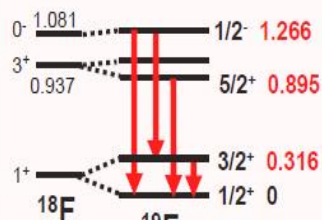
NPA 754 (2005) 58c

$^9\text{Be} (K^-, \pi^+ \gamma)$ BNL E930('98)



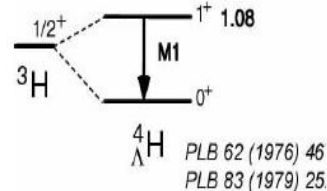
PRL 88 (2002) 082501
NPA 754 (2005) 58c

$^{19}\text{F} (K^-, \pi^+ \gamma)$ J-PARC E13



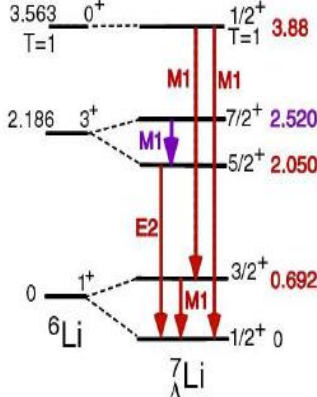
PRL 120 (2018) 132505

^7Li etc. ($K^{\text{stop}}, \gamma \pi^-$)



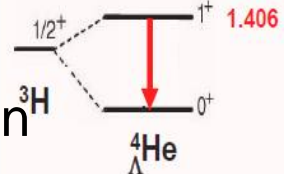
PLB 62 (1976) 46
PLB 83 (1979) 25

$^7\text{Li} (\pi^+, K^+ \gamma)$ KEK E419



PRL 84 (2000) 5963
PRL 86 (2001) 1982
PLB 579 (2004) 258
PRC 73 (2006) 012501

$^4\text{He} (K^-, \pi^+ \gamma)$ J-PARC E13

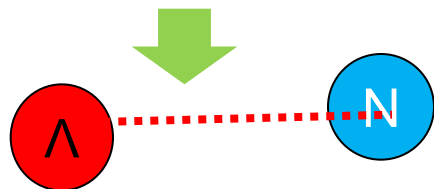


PRL 115 (2015) 222501

Few-body calculation
Shell model calculation

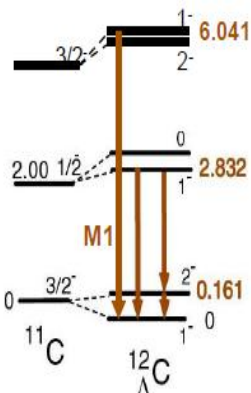
+

High-resolution experiments



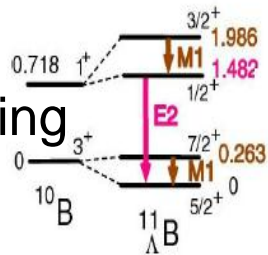
We have been obtaining information on ΛN two-body interaction.

$^{12}\text{C} (\pi^+, K^+ \gamma)$ KEK E566



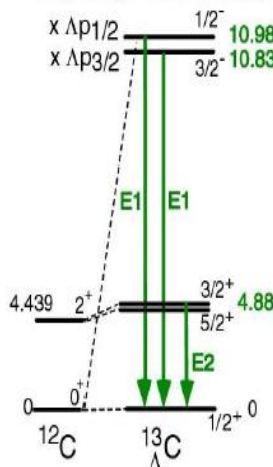
PTEP (2015) 081D01

$^{11}\text{B} (\pi^+, K^+ \gamma)$ KEK E518



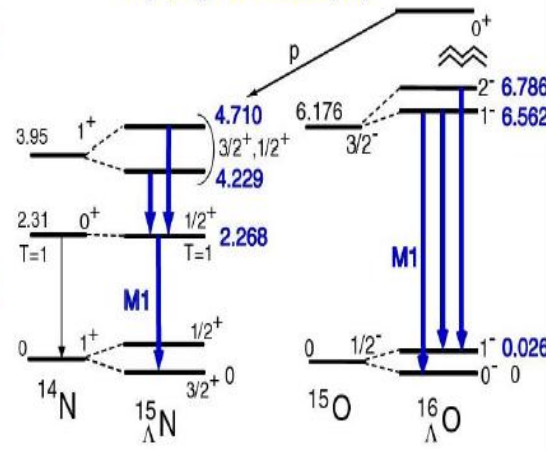
NPA835 (2010) 422

$^{13}\text{C} (K^-, \pi^+ \gamma)$ BNL E929 (NaI)



PRL 86 (2001) 4255
PRC 65 (2002) 034607

$^{16}\text{O} (K^-, \pi^+ \gamma)$ BNL E930('01)



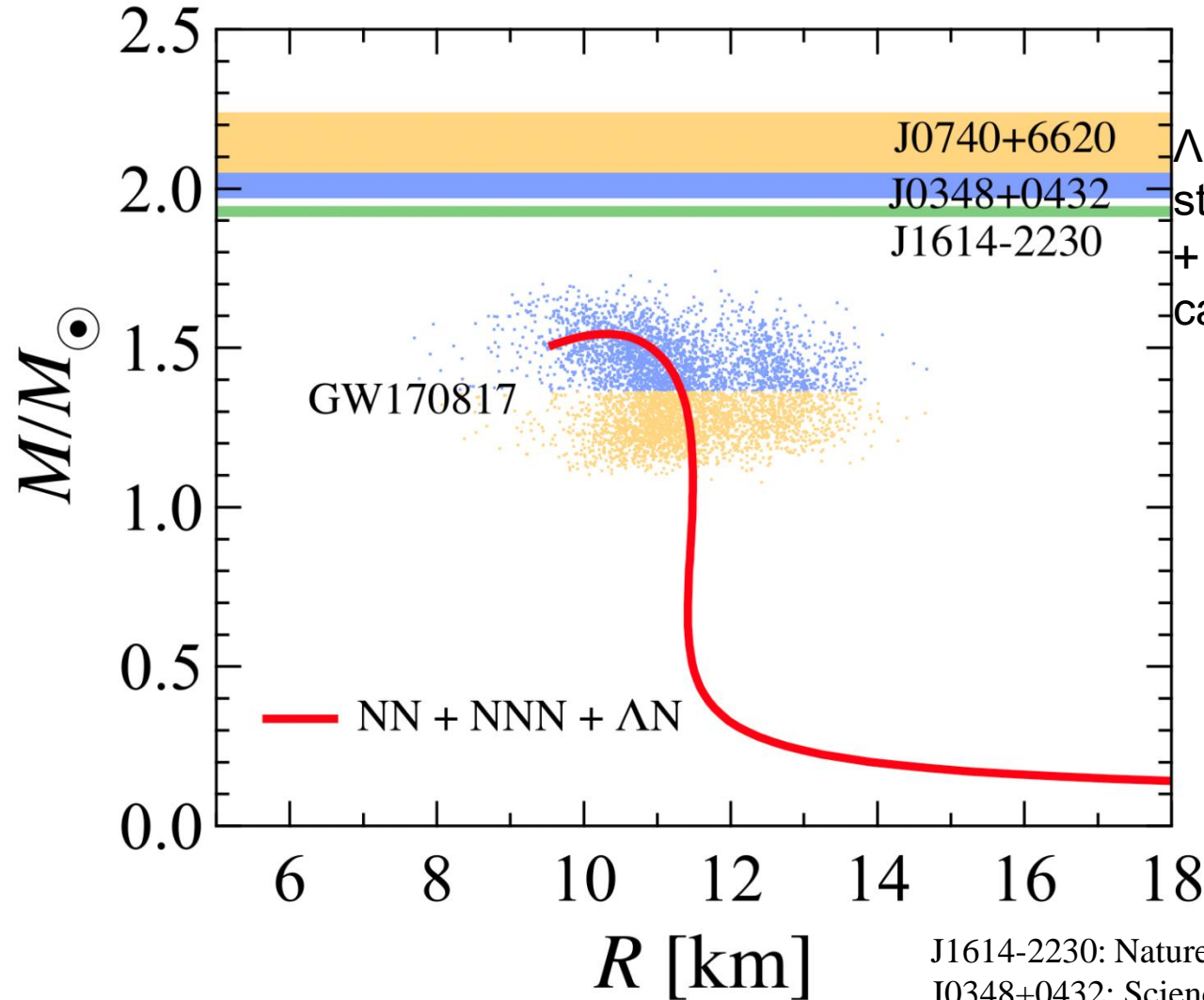
PRC 77 (2008) 054315

PRL 93 (2004) 232501
EPJ A33 (2007) 247

$$V_{\Lambda N} = V_0 + \sigma_{\Lambda} \cdot \sigma_N V_{\sigma\sigma} + \mathbf{L} \cdot (\mathbf{s}_{\Lambda} + \mathbf{s}_N) V_{\text{SLS}} + \mathbf{L} \cdot (\mathbf{s}_{\Lambda} - \mathbf{s}_N) V_{\text{ALS}} + S_{12} V_{\text{tensor}} + \dots$$

Mass-Radius Relation of Neutron Stars

2021



Λ N interaction updated by
structure study of Λ hypernuclei
+ EoS by cluster variational
calculation done by Togashi

Still, the maximum mass of
neutron star is less than twice
of solar mass.

Hyperon puzzle

J1614-2230: Nature 467 (2010) 1081, APJ 832 (2016) 167

J0348+0432: Science 340 (2013) 1233232

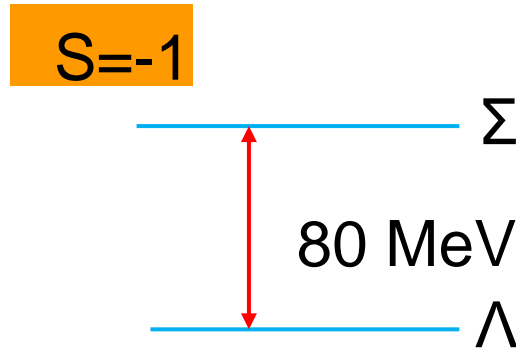
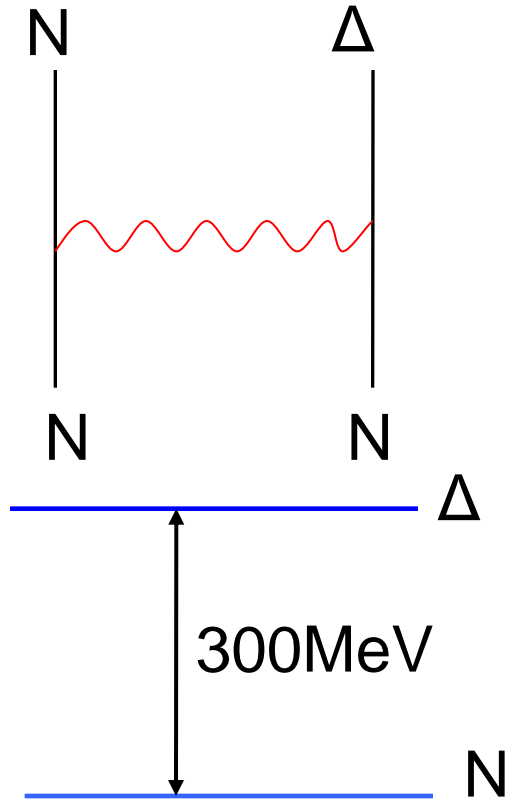
J0740+6620: Nat. Astron. (2019)

GW170817: PRL 121 (2018) 161101

missing part of YN interaction: Λ N- Σ N coupling

$\Lambda N - \Sigma N$ coupling

Non-strangeness sector



Mass is smaller.
It is expected that Λ - Σ conversion might affect in structure of Λ hypernuclei.

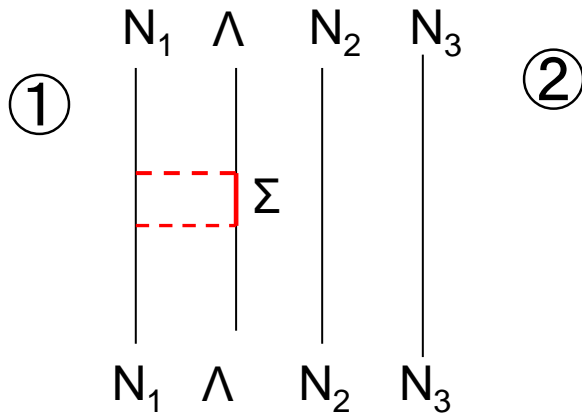
Probability of Δ in nuclei is not large.

ΛN - ΣN coupling is key issue to construct YN two-body interaction completely.

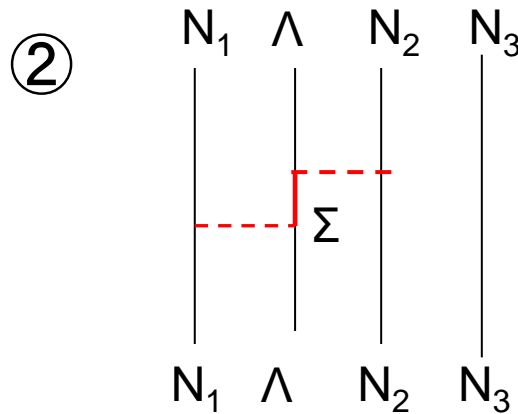
Role of the ΛN - ΣN interaction

- Three-body effect

Question : How large is the Σ -excitation as effective three-body ΛNN force?



Effective two-body force

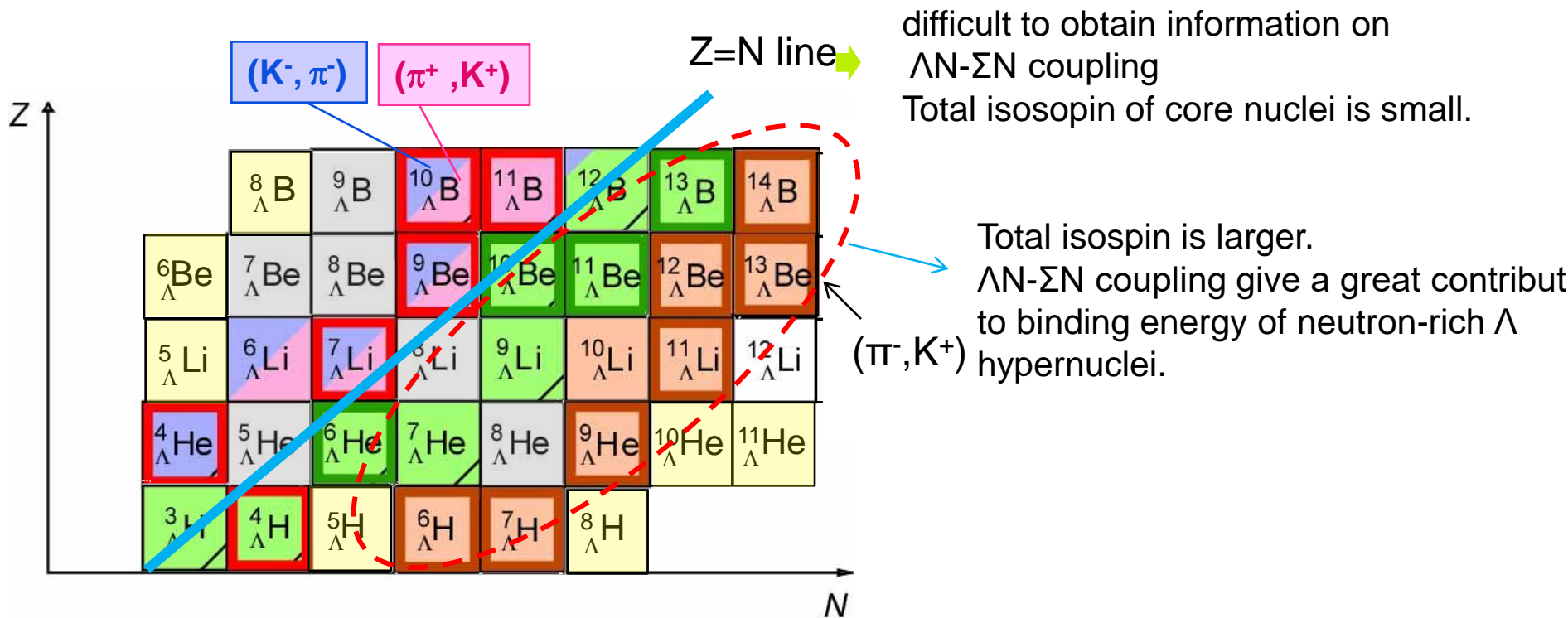


Three-body force

In the neutron matter or neutron star, three-body force might play important role.

How do we obtain information on ΛN - ΣN coupling?

- (1) ΛN scattering experiment at J-PARC, Femtoscopic experiment
- (2) To study neutron-rich Λ hypernuclei at J-PARC



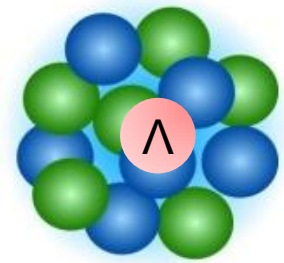
These neutron-rich Λ hypernuclei are important.

By neutron-rich Λ hypernuclei, we could obtain information on **long-range part** of ΛN - ΣN coupling. **Long-range part** of ΛNN three-body force

Furthermore, we need short-range part of ΛNN three-body force.: important for **the study neutron star**

heavier Λ hypernuclei

For example: Pb, Sn, Zr, La, Y etc. Istopes



Density of heavier nuclei is high and then, Λ particle is acting in such high dense matter. => We could obtain information on the short-range part of Λ NN interaction.

In heavier nuclei, density becomes high.

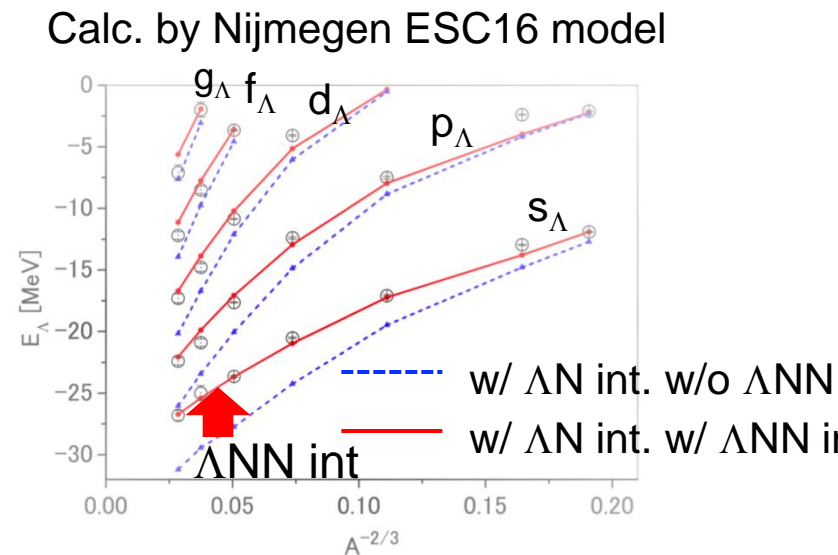
$^{208}_{\Lambda}\text{Pb}$, $^{139}_{\Lambda}\text{La}$, $^{89}_{\Lambda}\text{Y}$: plan in the project at HIHR

Heavy Λ hypernuclei exp. + theoretical cal.

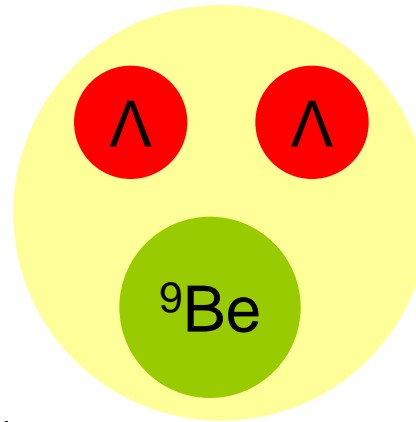
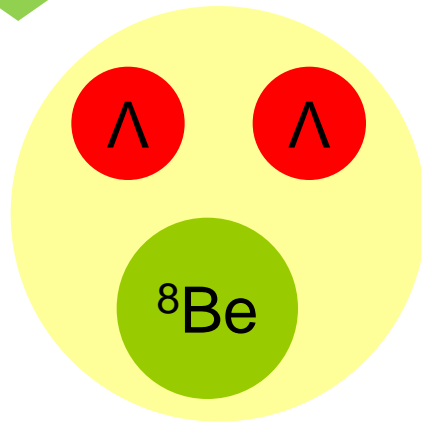
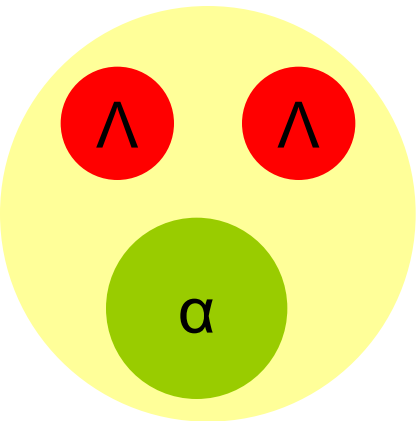
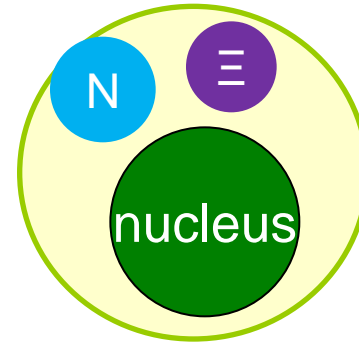
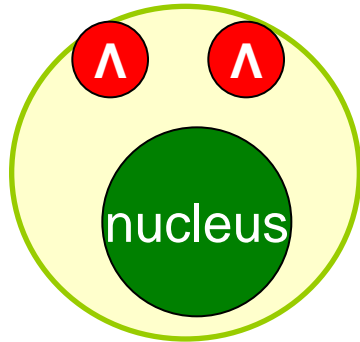
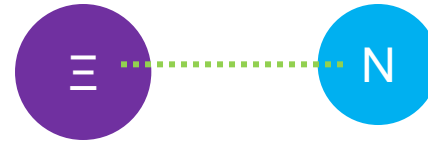
Isotope dependence of Λ NN three-body force

Determine Λ NN interaction

Reliable EOS



Next step: $S=-2$ sector



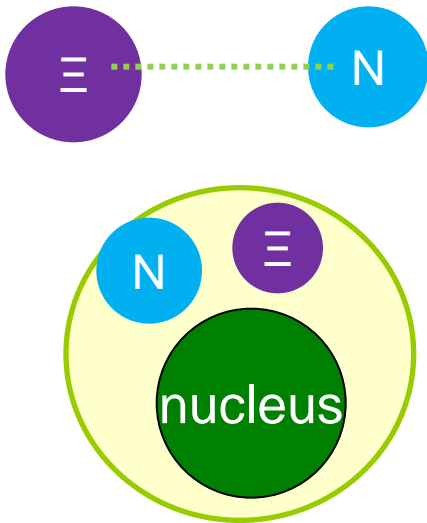
1S_0 of $\Lambda\Lambda$ interaction
attractive

$\Lambda\Lambda$ ^6He

$\Lambda\Lambda$ ^{10}Be

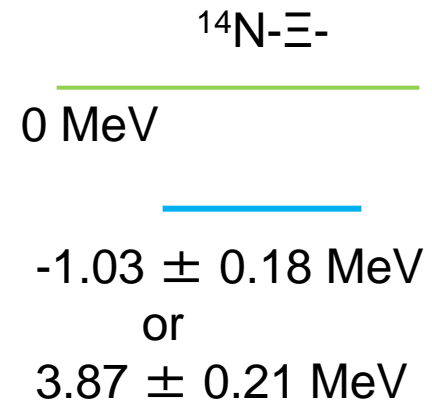
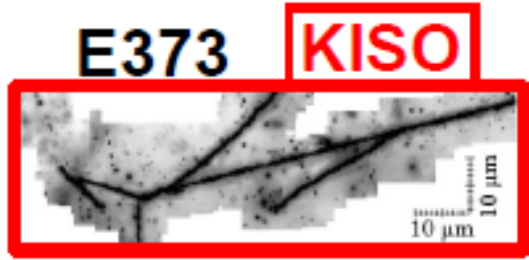
$\Lambda\Lambda$ ^{11}Be

[1] K. Nakazawa, et. al., Prog. Theor. Exp. Phys. 2015, 033D02 (2015),
E. Hiyama and K. Nakazawa, Ann. Rev. Nucl. Part. Sci. 68, 131 (2018).



Before 2015, there was no confirmed bound Ξ hypernucleus. Then, we do not know Ξ N potential should be repulsive or attractive?

The first measurement of bound Ξ hypernucleus, $^{14}\text{N}-\Xi$.



PTEP

Prog. Theor. Exp. Phys. **2015**, 033D02 (11 pages)
DOI: 10.1093/ptep/ptv008

The first evidence of a deeply bound state of $\Xi^- - ^{14}\text{N}$ system

K. Nakazawa^{1,*}, Y. Endo¹, S. Fukunaga², K. Hoshino¹, S. H. Hwang³, K. Imai³, H. Ito¹, K. Itonaga¹, T. Kanda¹, M. Kawasaki¹, J. H. Kim⁴, S. Kinbara¹, H. Kobayashi¹, A. Mishina¹, S. Ogawa², H. Shibuya², T. Sugimura¹, M. K. Soe¹, H. Takahashi⁵, T. Takahashi⁵, K. T. Tint¹, K. Umehara¹, C. S. Yoon⁴, and J. Yoshida¹

¹Physics Department, Gifu University, 1-1 Yanagido, Gifu 501-1193, Japan

²Department of Physics, Toho University, Funabashi 274-8510, Japan

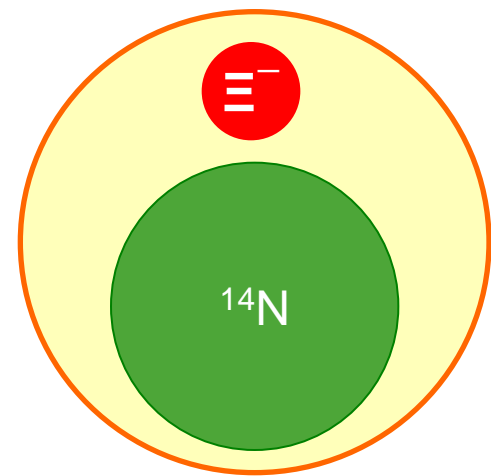
³Advanced Science Research Center, JAEA, Tokai 319-1195, Japan

⁴Department of Physics, Gyeongsang National University, Jinju 660-701, Korea

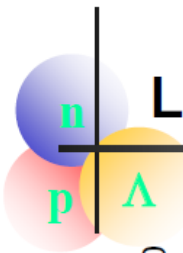
⁵Institute of Particle and Nuclear Studies, KEK, Tsukuba 305-0801, Japan

*E-mail: nakazawa@gifu-u.ac.jp

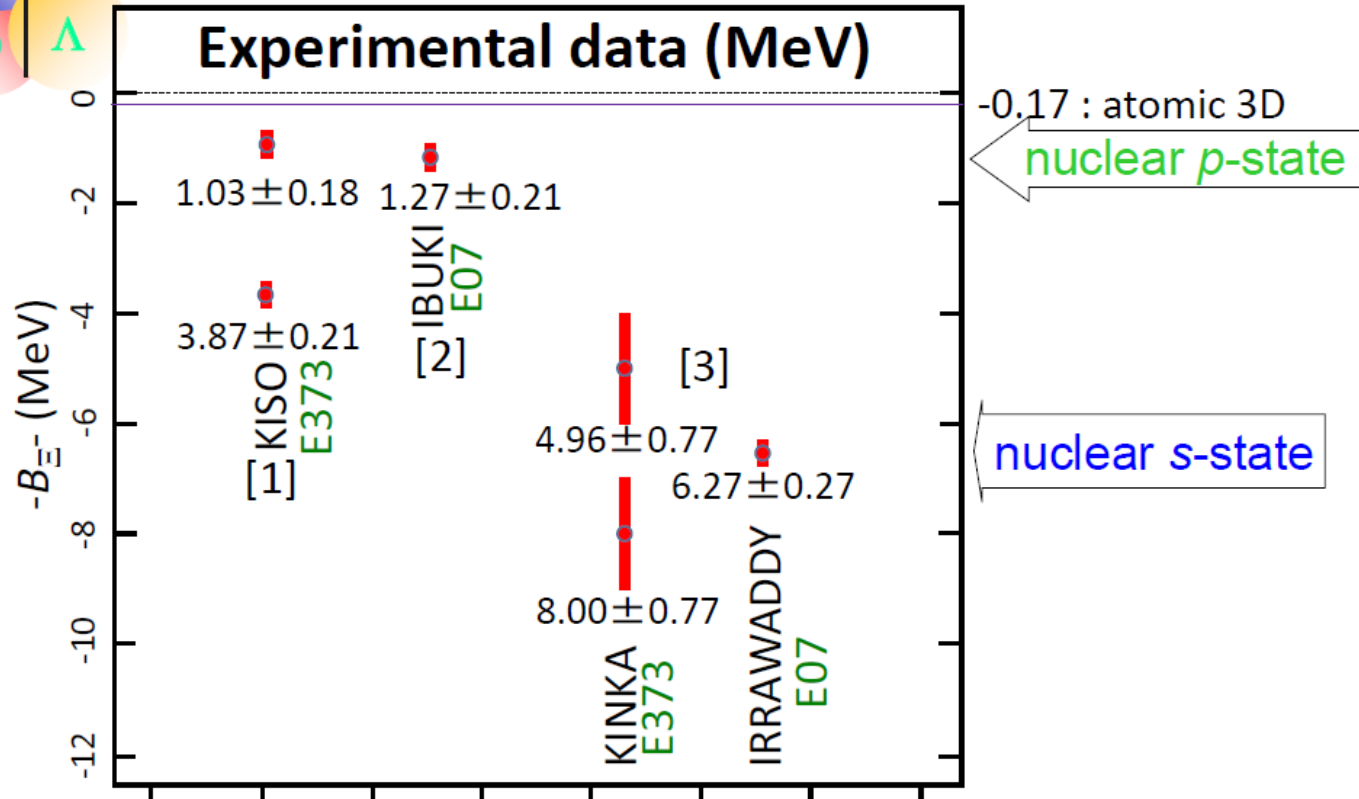
Received October 27, 2014; Revised December 25, 2014; Accepted January 9, 2015; Published March 5, 2015



We understood Ξ -nuclear potential should be attractive.



Level scheme of Ξ hypernucleus (${}^{15}_{\Xi}\text{C}$ [Ξ^{-} - ${}^{14}\text{N}$])



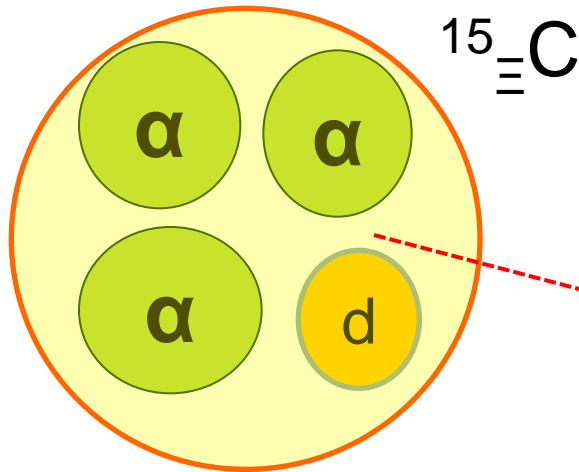
- [1] K. Nakazawa, et. al., Prog. Theor. Exp. Phys. 2015, 033D02 (2015), E. Hiyama and K. Nakazawa, Ann. Rev. Nucl. Part. Sci. 68, 131 (2018).
- [2] S. Hayakawa, et. al., Phy. Rev. Lett., 126, 062501 (2021).
- [3] M. Yoshimoto, et. al., Prog. Theor. Exp. Phys. 2021, 073D02 (2021).

Slide by Nakazawa

After observation of Kiso event, they observed several events of ${}^{14}\text{N}-\Xi$ hypernucleus. Some are observed as excited state and some are observed as ground state.

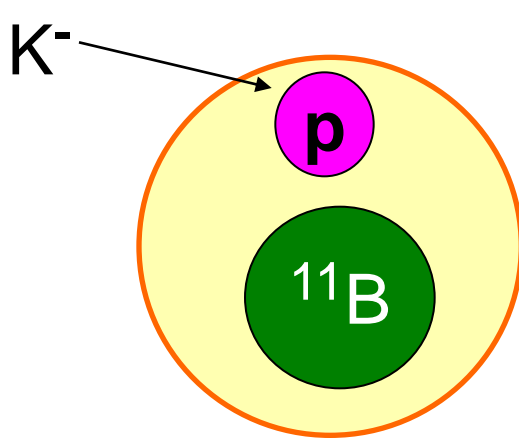
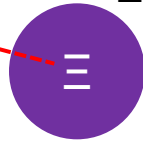
What parts of ΞN interaction can we obtain?

$$V_{\Xi N} = V_0 + \boldsymbol{\sigma} \cdot \boldsymbol{\sigma} V_{\sigma \cdot \sigma} + \boldsymbol{\tau} \cdot \boldsymbol{\tau} V_{\tau \cdot \tau} + (\boldsymbol{\sigma} \cdot \boldsymbol{\sigma})(\boldsymbol{\tau} \cdot \boldsymbol{\tau}) V_{\sigma \cdot \sigma \tau \cdot \tau}$$

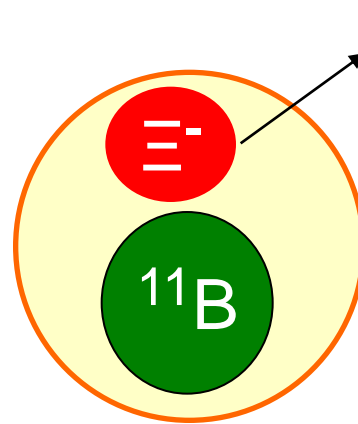
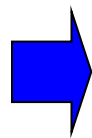


$^{15}_{\Xi}\text{C}$

All terms contribute to the binding energies of $^{15}_{\Xi}\text{C}$.



^{12}C



Ξ hypernucleus

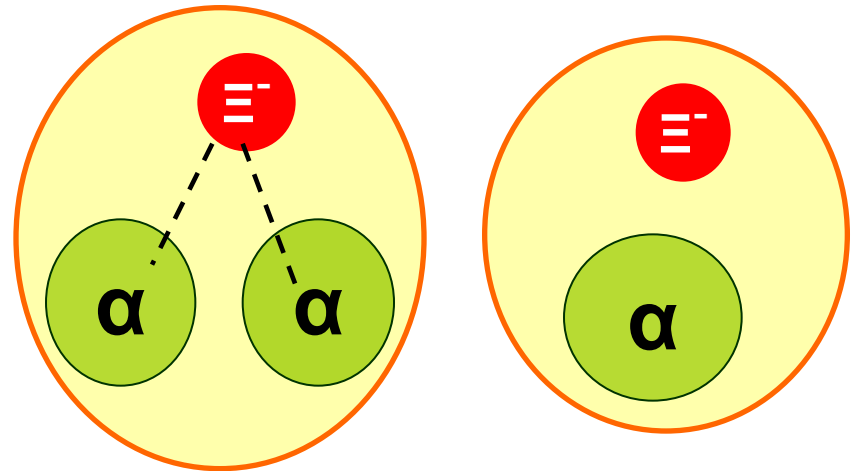
J-PARC: E70: spokesperson
T. Nagae

It is possible to observe decay width which corresponds to $\Lambda\Lambda$ - ΞN coupling.

After observation of $11\text{B}-\Xi$ (J-PARC-E70 exp.), we want to know V_0 term, first.

$$V_{\Xi N} = V_0 + \sigma \cdot \sigma V_{\sigma \cdot \sigma} + \tau \cdot \tau V_{\tau \cdot \tau} + (\sigma \cdot \sigma)(\tau \cdot \tau) V_{\sigma \cdot \sigma \tau \cdot \tau}$$

the $(\sigma \cdot \sigma)$, $(\tau \cdot \tau)$ and $(\sigma \cdot \sigma)(\tau \cdot \tau)$ terms of $V_{\Xi N}$ vanish by folding them into the α -cluster wave function that are spin-, isospin-saturated.



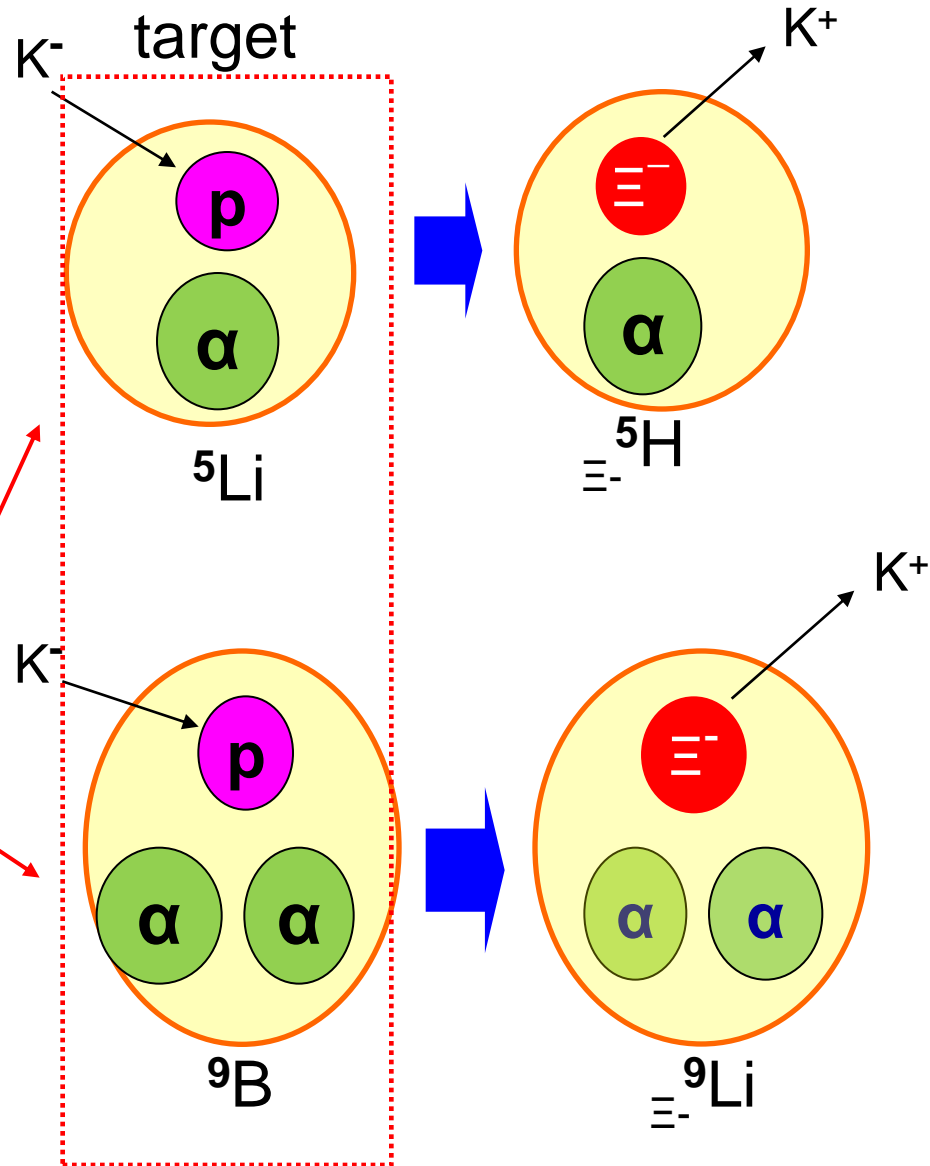
problem : there is NO target to produce them by the (K^-, K^+) experiment .

Because, ...

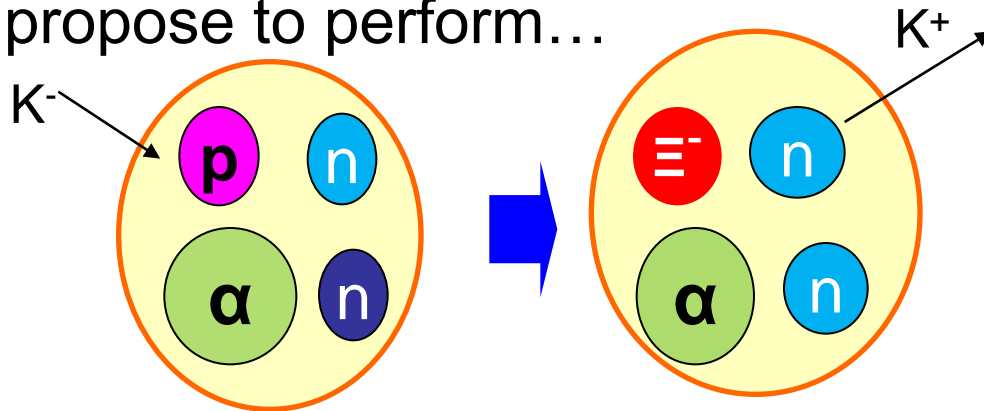
To produce $\alpha\Xi^-$ and $\alpha\alpha\Xi^-$ systems by (K^-, K^+) reaction,

These systems are unbound.

Then, we cannot use them as targets.



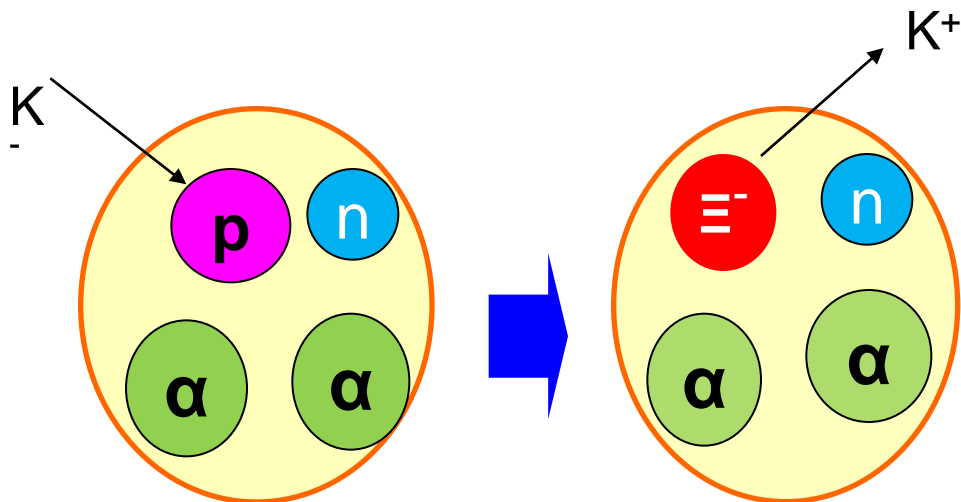
As the second best candidates to extract information about the spin-, isospin-independent term V_0 , we propose to perform...



${}^7\text{Li} (T=1/2)$

${}^7\text{H} (T=3/2)$
≡-

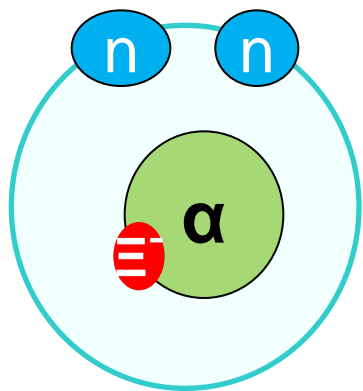
Why they are suited for investigating V_0 ?



${}^{10}\text{B} (T=0)$

${}^{10}\text{Li} (T=1)$
≡-

(more realistic illustration)



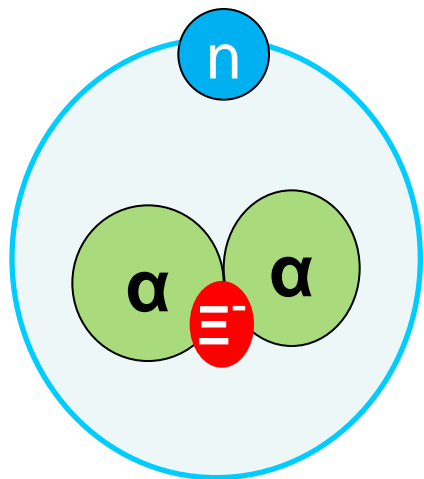
Core nucleus ${}^6\text{He}$ is known to be halo nucleus. Then, valence neutrons are located far away from α particle.

Valence neutrons n are located in p-orbit, whereas Ξ particle Ξ is located in 0s-orbit.

${}^7\text{H} (T=3/2)$
 Ξ

Then, distance between Ξ and n

is much larger than the interaction range of Ξ and n .



Then, $\alpha\Xi$ potential, in which only V_0 term works, plays a dominant role in the binding

${}^{10}\text{Li} (T=1)$ energies of these system.

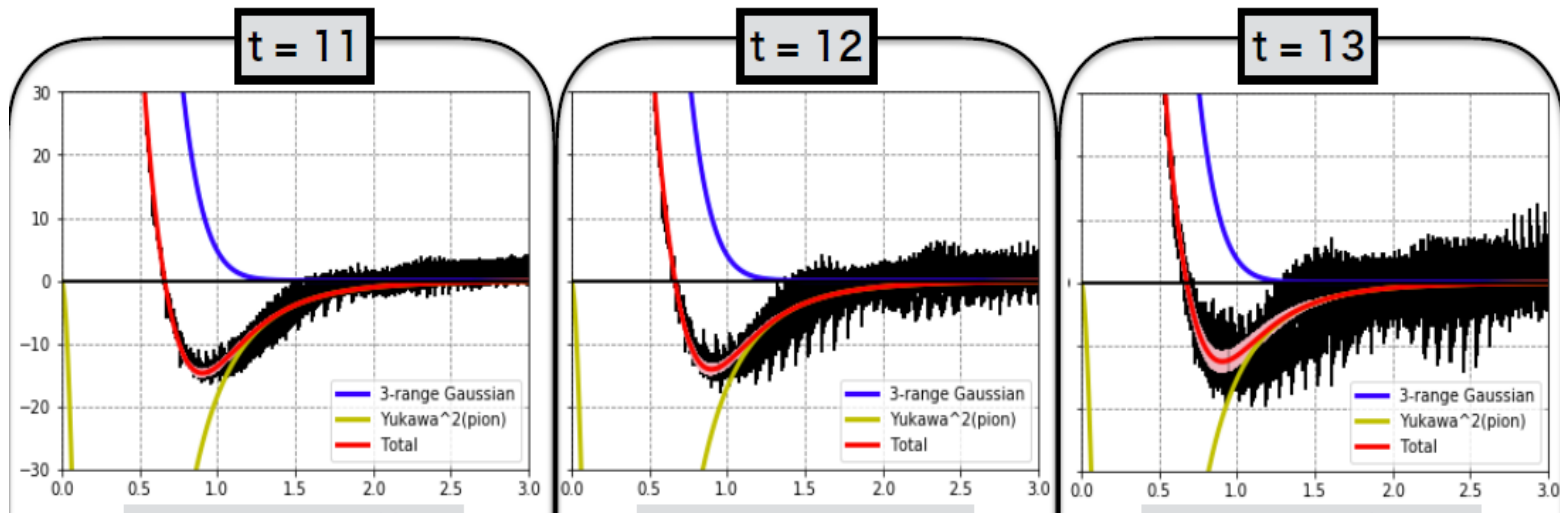
ΞN interaction

Nijmegen potential : Nijmegen model-D(ND),
Extended soft core '04d

HAL potential(Base on Lattice QCD potential:HAL collaboration)
by K. Sasaki, Miyamoto, T. Doi, T. Hatsuda et al.

$$V_{\Xi N} = V_0(r) + (\sigma_{\Xi} \cdot \sigma_N) V_s(r) + (\tau_{\Xi} \cdot \tau_N) V_t(r) + (\sigma_{\Xi} \cdot \sigma_N)(\tau_{\Xi} \cdot \tau_N) V_{ts}(r)$$

All terms are central parts only.



Property of the spin- and isospin-components of ESC04, ND, HAL

V(T,S)	ESC04	ND	HAL
T=0, S=1	strongly attractive (a bound state)	} weakly attractive	Weakly attractive
T=0, S=0	weakly repulsive		Strongly attractive
T=1, S=1	weakly attractive		Weakly attractive
T=1, S=0	weakly repulsive		Weakly repulsive

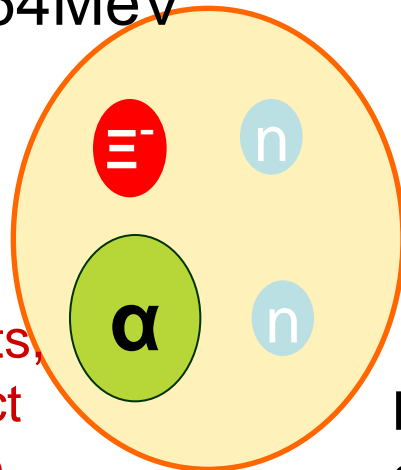
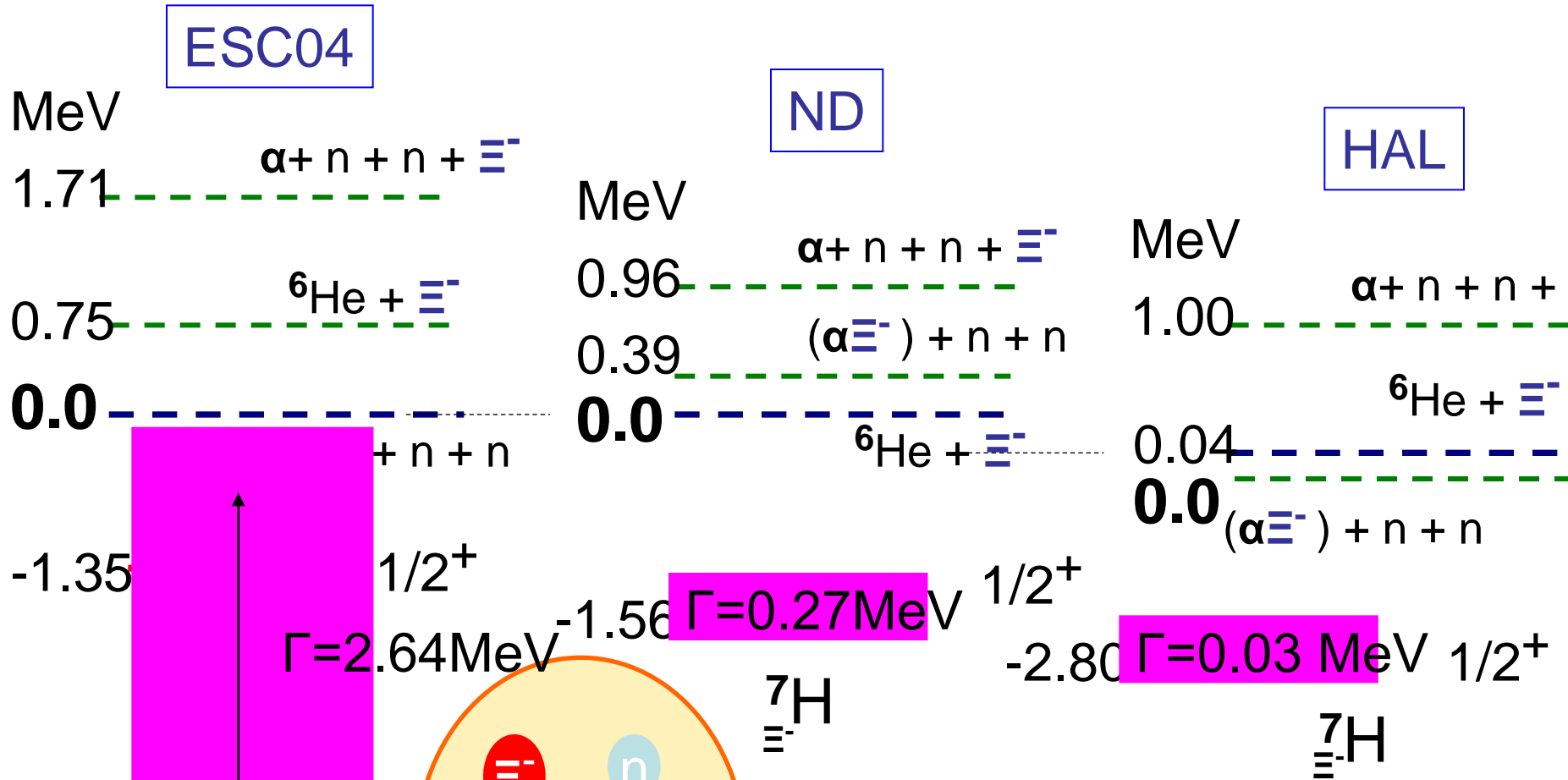
Although the spin- and isospin-components of these potentials are very different (due to the different meson contributions), we find that the spin- and isospin-averaged property,

$$V_0 = [V(0,0) + 3V(0,1) + 3V(1,0) + 9V(1,1)] / 16,$$

namely, strength of the V_0 - term is similar to each other.

4-body calculation of ${}^7_{\Xi^-}\text{H}$

E. Hiyama et al.,
PRC78 (2008) 054316



In experiments,
we can expect
a bound state.

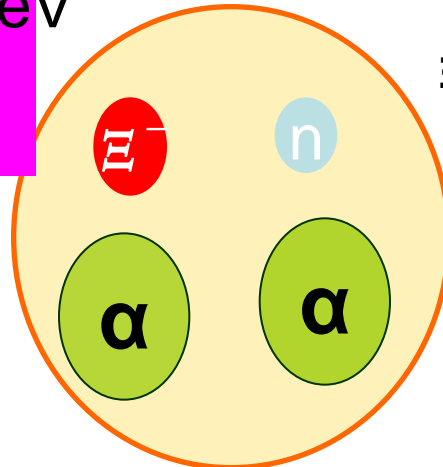
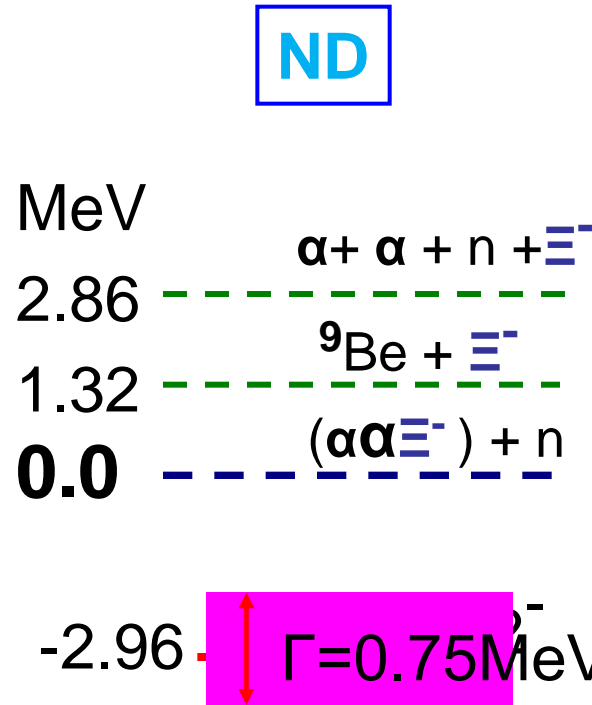
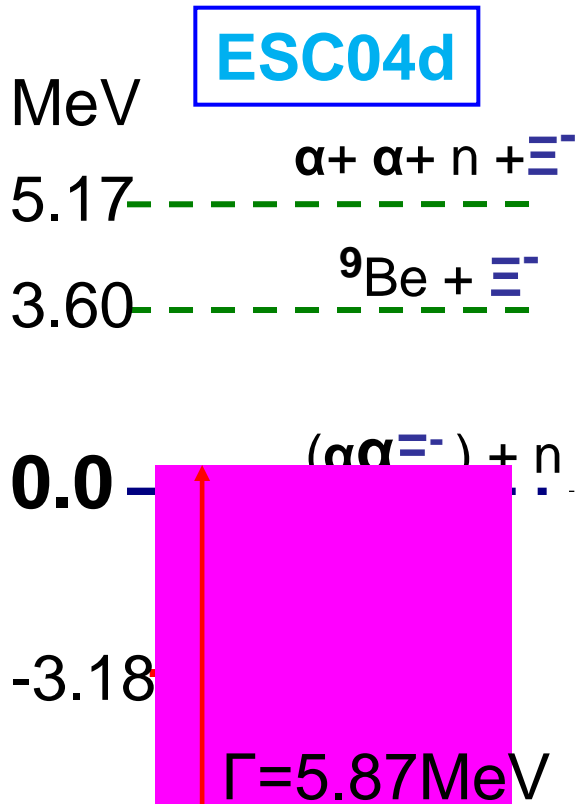
${}^7_{\Xi^-}\text{H}$

Similar binding
energies using ND and
ESC04.

However, decay width is dependent on
on employed ΞN potential

4-body calculation of ${}_{\Xi}^{10}\text{Li}$

${}_{\Xi}^{10}\text{Li}$ E. Hiyama et al.,
PRC78 (2008) 054316



${}_{\Xi}^{10}\text{Li}$

Similar binding energies using ND and ESC04d.

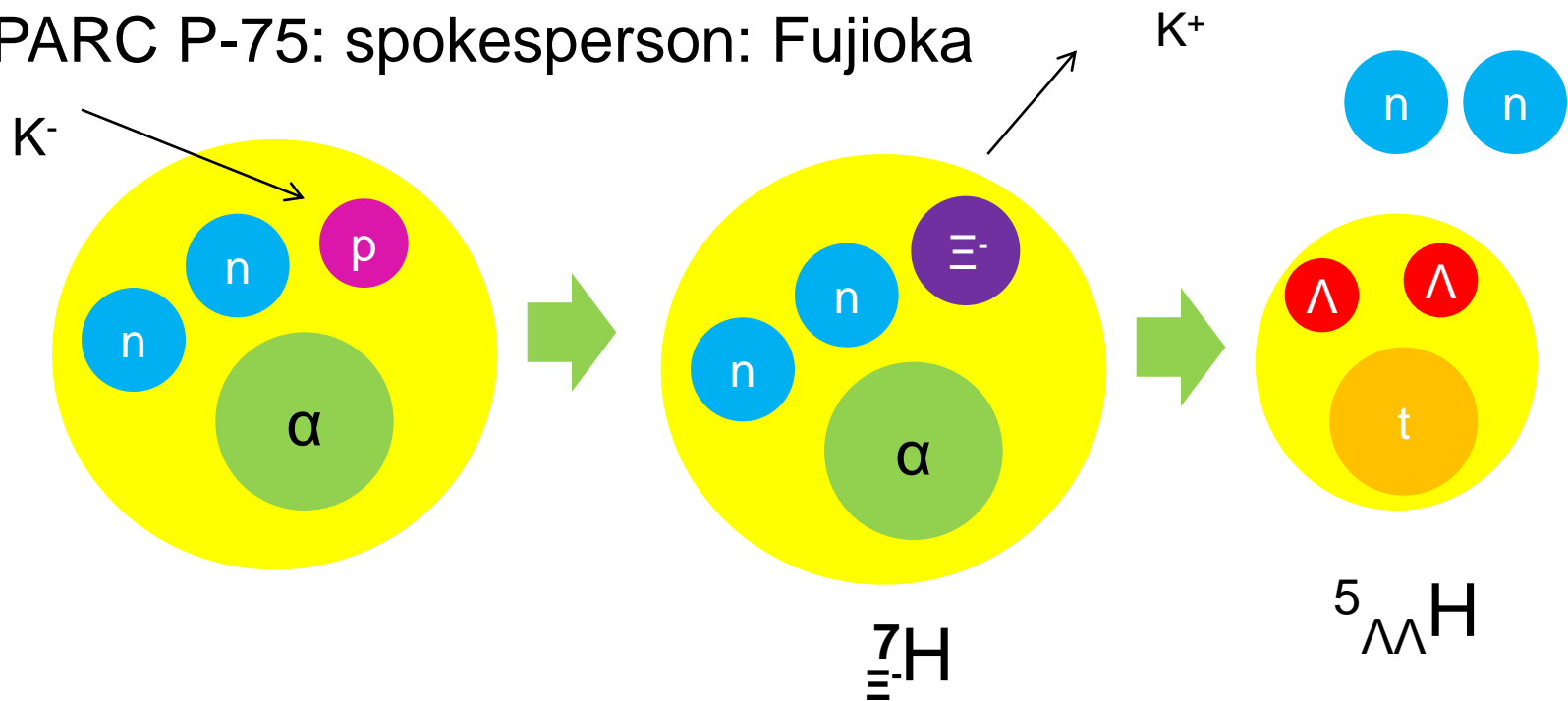
Independent on employed ΞN potential

But, decay width is dependent on employed ΞN interaction.

In experiments, we can expect a bound state.

In this way, the binding energies of Ξ hypernuclei with $A=7$ and 10 are dominated by $\alpha\Xi$ potential, namely, spin-, and iso-spin independent ΞN interaction (V_0).


J-PARC P-75: spokesperson: Fujioka



$$V_0 = [V(0,0) + 3V(0,1) + 3V(1,0) + 9V(1,1)] / 16,$$

which partial contribution makes attractive for V_0 ?

ΞN interaction:

$T=0, S=0$	
$T=0, S=1$	
$T=1, S=0$	
$T=1, S=1$	

$t=1/2$ $t=1/2$
 $S=1/2$ $S=1/2$

we have a two-body bound state for ΞN system?
No idea

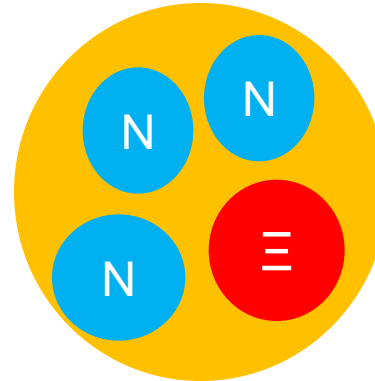
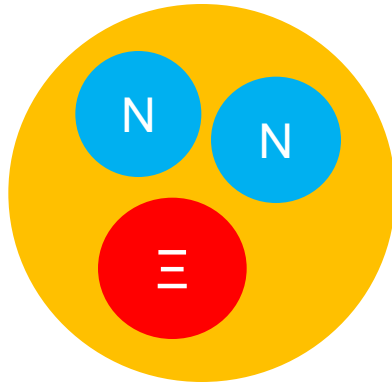
Cf. NN interaction



$T=0, S=0$
 $T=0, S=1$ ➔ strong attraction to have a bound state as a deuteron
 $T=1, S=0$
 $T=1, S=1$

To obtain ΞN two-body interaction, the suited systems to study are s-shell Ξ hypernuclei such as $NN\Xi$ and $NNN\Xi$ systems.

E. Hiyama et al., PRL124, 092501 (2020)



I show my new results of these light systems.

NN interaction: AV8 potential

ΞN interaction :

Nijmegen extended soft core potential (ESC08c)

Realistic potential (only ΞN channel)

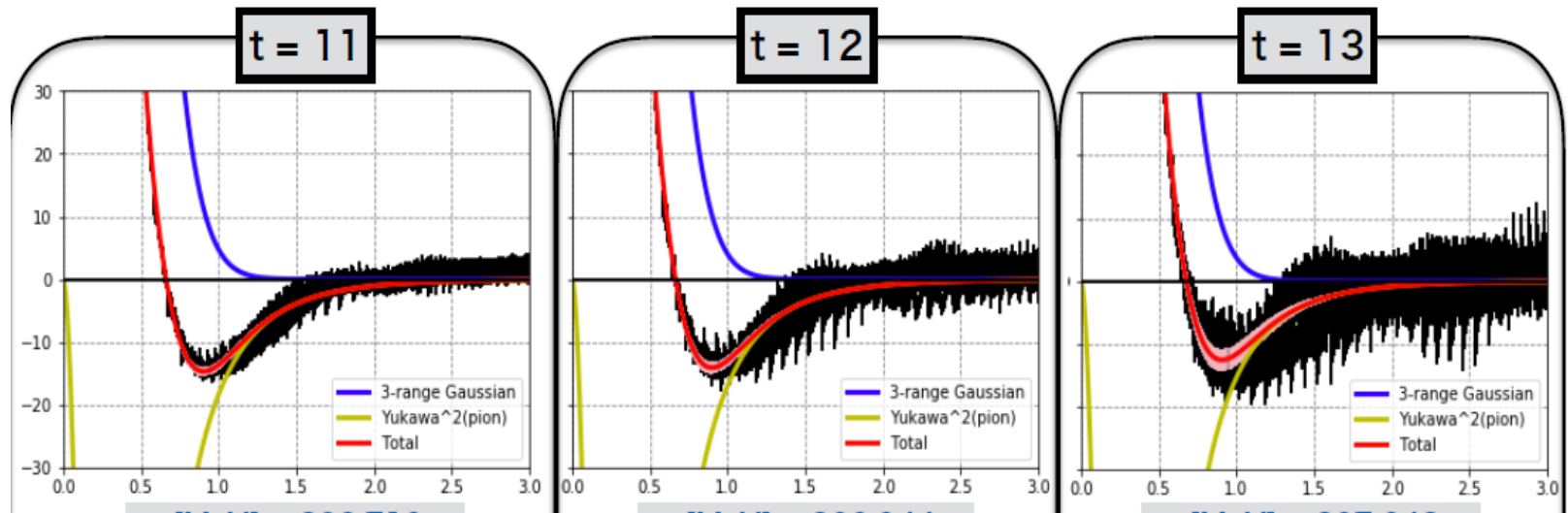
ΞN interaction by HAL collaboration (Lattice QCD calculation)

The potential was made by K. Sasaki, Miyamoto, Hatsuda and Aoki.

HAL potential

$$V_{\Xi N} = V_0(r) + (\sigma_{\Xi} \cdot \sigma_N) V_s(r) + (\tau_{\Xi} \cdot \tau_N) V_t(r) + (\sigma_{\Xi} \cdot \sigma_N)(\tau_{\Xi} \cdot \tau_N) V_{ts}(r)$$

All terms are central parts only.



$$V_0(r)$$

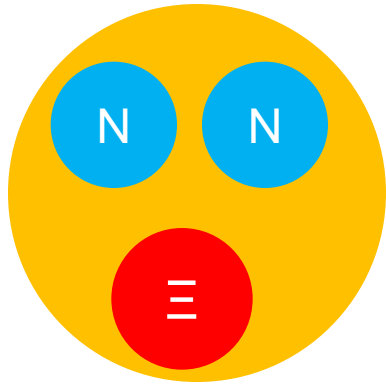
In HAL potential, the statistical errors are NOT included.

Property of the spin- and isospin-components of ESC08 and HAL

V(T,S)	ESC08c	HAL
T=0, S=1	strongly attractive	Weakly attractive
T=0, S=0	weakly repulsive	Strongly attractive
T=1, S=1	strong attractive	Weakly attractive
T=1, S=0	weakly repulsive	Weakly repulsive

Although the spin- and isospin-components of these two models are very different between them.

It is interesting to see the difference in the energy spectra in s-shell Ξ hypernuclei.

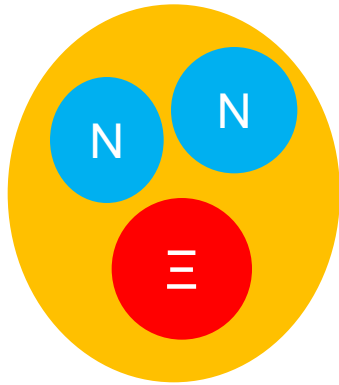


$T=1/2, J=1/2^+$ and $J=3/2^+$

ESC08c



However, I also have two bound states in three-body system.



$T=1/2, J=1/2^+$ and $J=3/2^+$

HAL potential

0 MeV

$d + \Xi$

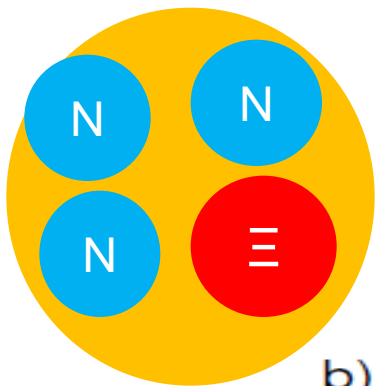
0 MeV

$d + \Xi$

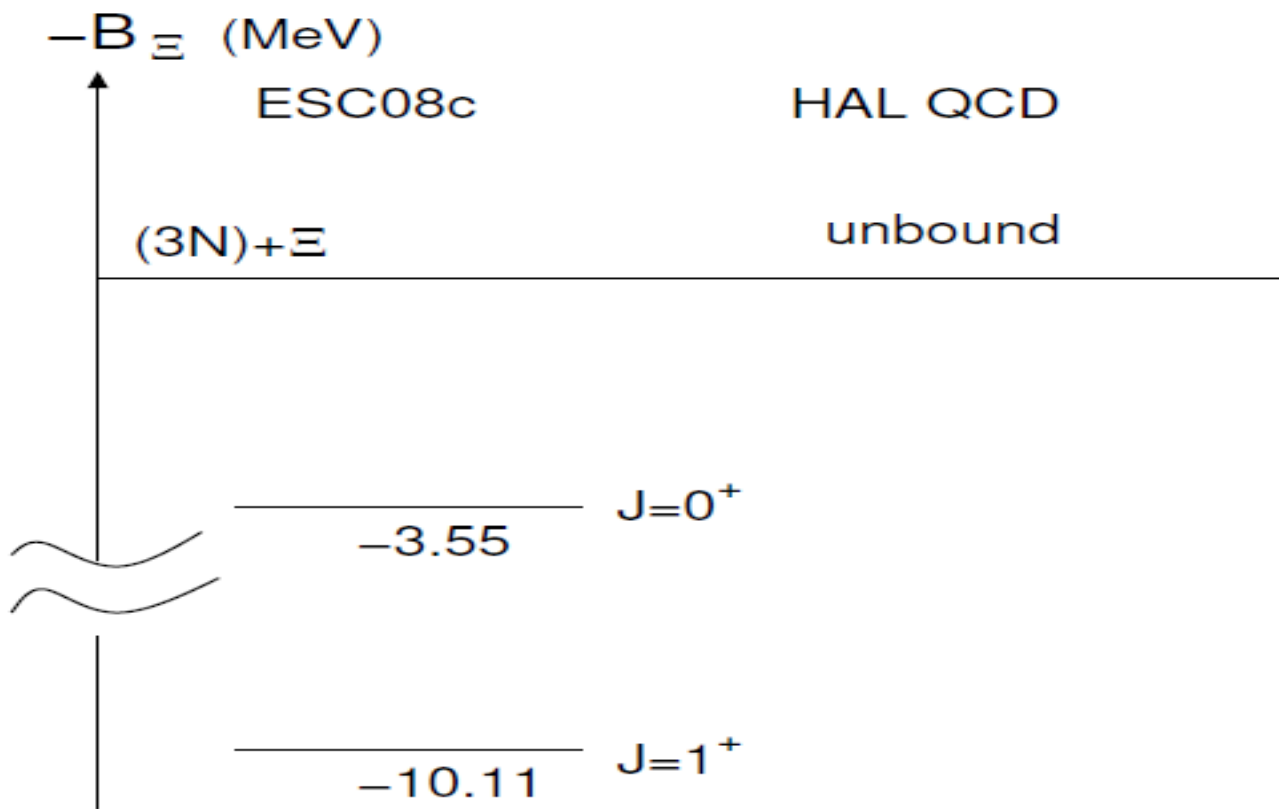
No bound state

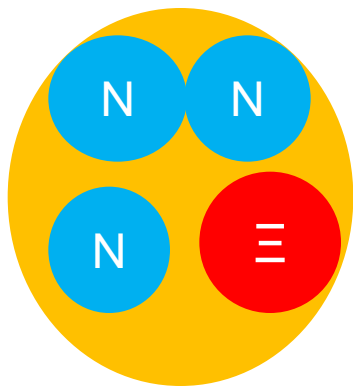
$J=1/2^+$

$J=3/2^+$

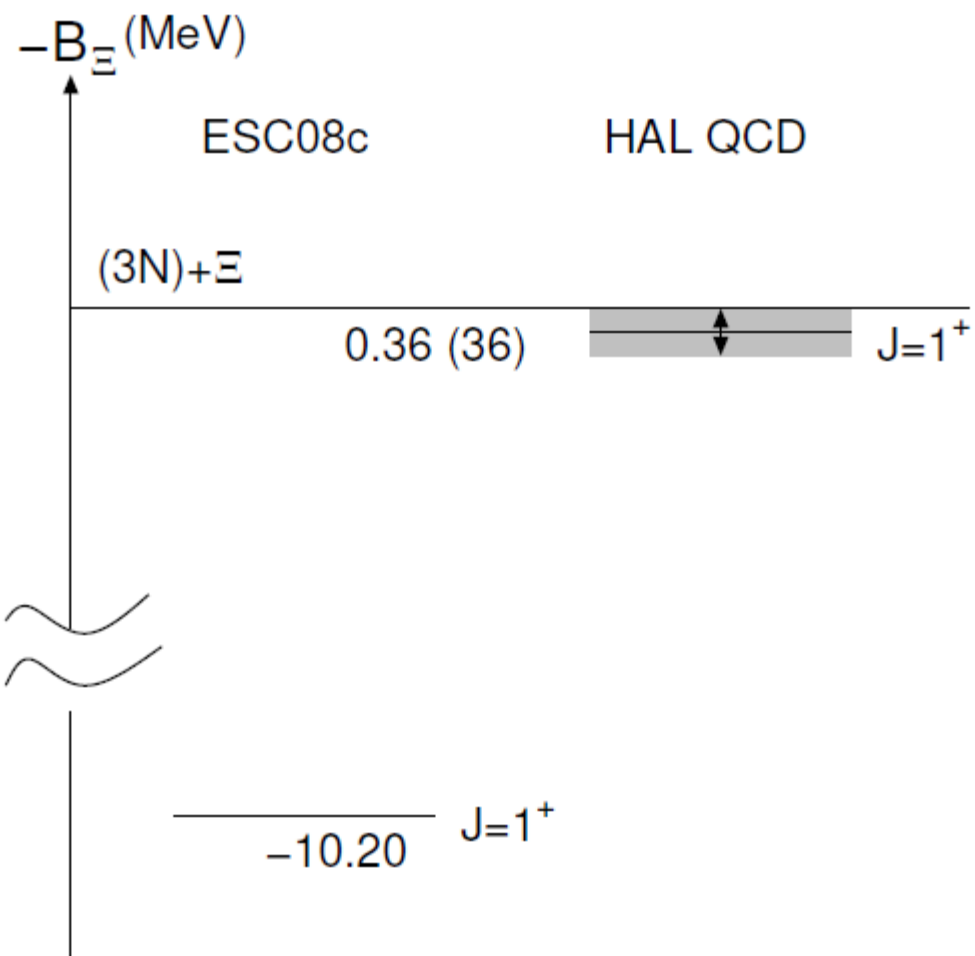


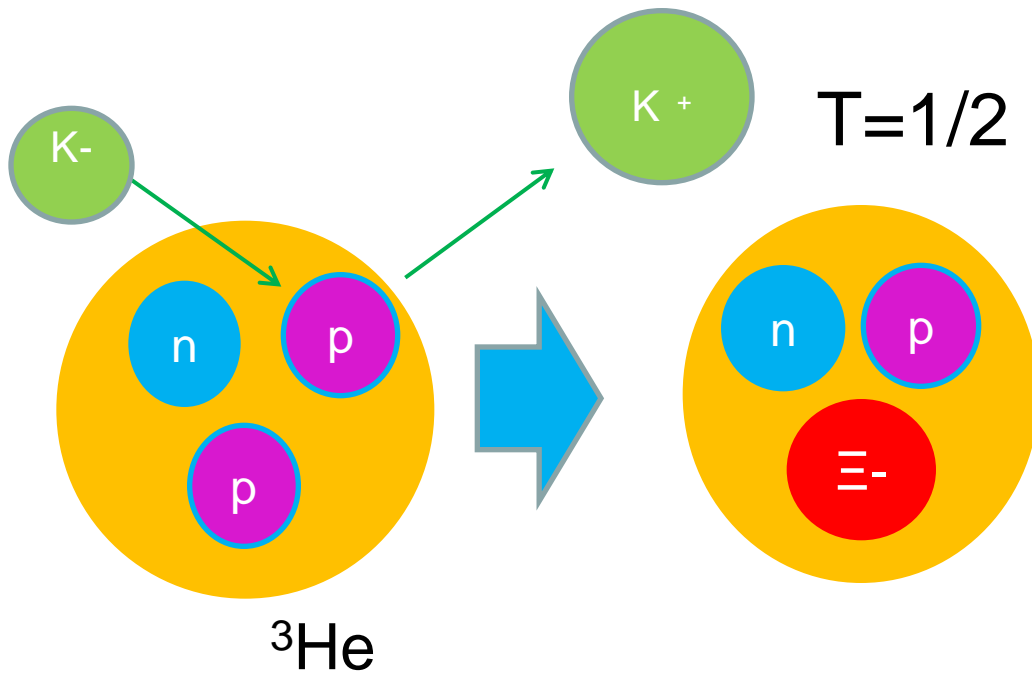
b) $T=1$





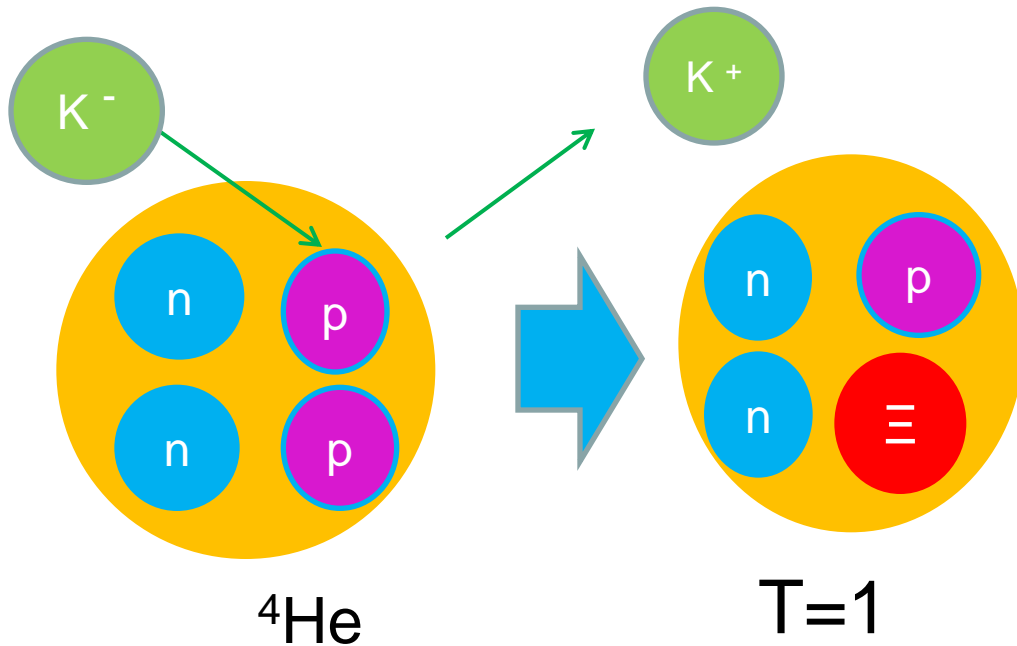
a) $T=0$





Using ${}^3\text{He}$ and ${}^4\text{He}$ target,
It might be possible
to produce $\text{NN}\Xi$ and $\text{NNN}\Xi$
systems by (K^-, K^+) reaction.

Another tool is to use
Heavy ion collision.

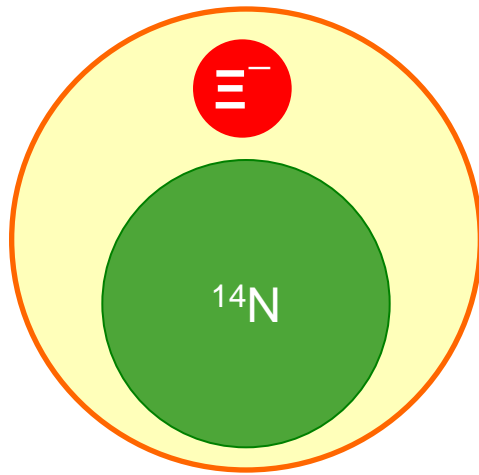


In the future,
we hope to observe
these light Ξ hypernuclei.

Conclucision

In hypernuclear physics, we have been obtaining YN and YY interactions.

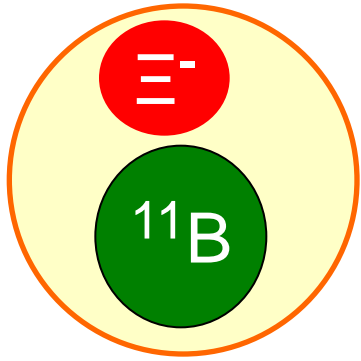
In this talk, I focus on present status of study of Ξ hypernuclei.



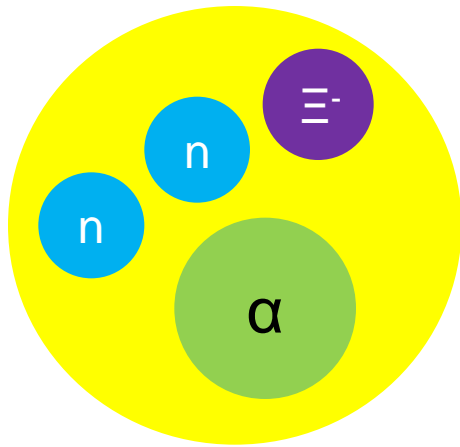
Observed!

ΞN interaction is attractive.

In near future,



J-PARC: E70: spokesperson
T. Nagae



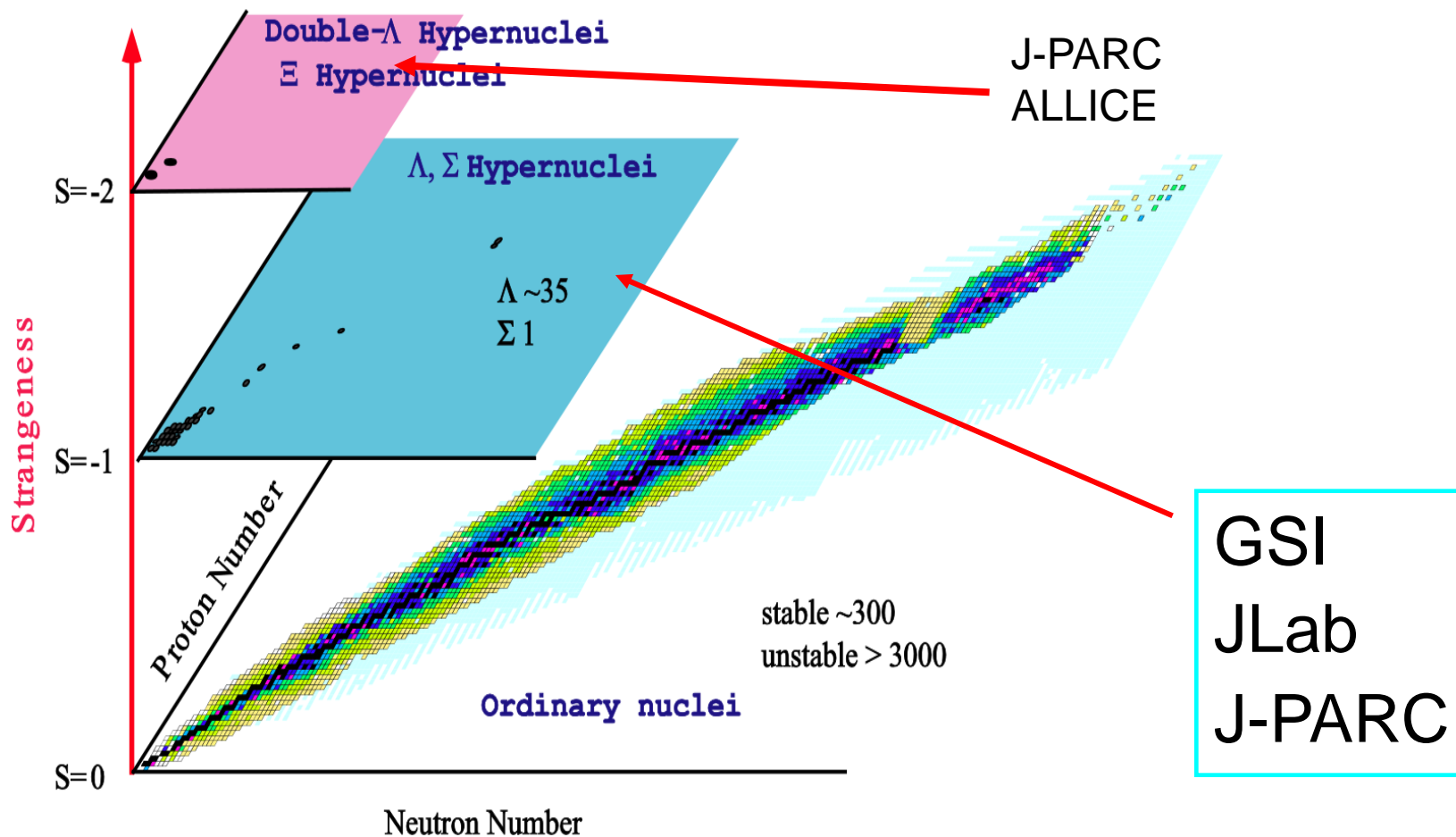
J-PARC P-75
Spokesperson: Fujioka

${}^7_3\text{H}$

Concluding remark

Multi-strangeness system
such as Neutron star

Three-Dimensional Nuclear Chart



Thank you!