

# SM is defined by its gauge symmetry and its field content

gauge fields

$$SU(3) \times SU(2) \times U(1)_Y \times \text{diffs}$$

Higgs field

$$H = (\mathbf{1}, \mathbf{2}, 1)$$

spinors

$$q_L$$
 ,  $u_R$  ,  $d_R$  ,  $\ell_L$  ,  $e_R$   $imes$  3 families (3,2,1/3) (3,1,4/3) (3,1,-2/3) (1,2,-1) (1,1,-2)



Write most general EFT lagrangian as expansion in inverse powers of microphysics cut-off  $\Lambda_{UV} = 1/a$ 

$$+ c_0 \, \Lambda_{UV}^4 \, \sqrt{g}$$
  $c_0 \sim -10^{-60} \left( rac{ ext{TeV}}{\Lambda_{UV}} 
ight)^4$  d=0  $+ c_2 \, \Lambda_{UV}^2 \, H^\dagger H$   $c_2 \simeq 0.008 \left( rac{ ext{TeV}}{\Lambda_{UV}} 
ight)^2$  d=2  $+ heta \, \tilde{G}_{\mu\nu} \tilde{G}^{\mu\nu}$   $heta \, \lesssim \, 10^{-10}$  d=4

$$\mathcal{L}_{SM} = \mathcal{L}_{kin} + gA_{\mu}\bar{F}\gamma_{\mu}F + Y_{ij}\bar{F}_{i}HF_{j} + \lambda(H^{\dagger}H)^{2}$$

$$+ \frac{b_{ij}}{\Lambda_{UV}}L_{i}L_{j}HH$$

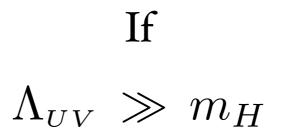
$$+ \frac{c_{ijkl}}{\Lambda_{UV}^{2}}\bar{F}_{i}F_{j}\bar{F}_{k}F_{\ell} + \frac{c_{ij}}{\Lambda_{UV}}\bar{F}_{i}\sigma_{\mu\nu}F_{j}G^{\mu\nu} + \dots$$

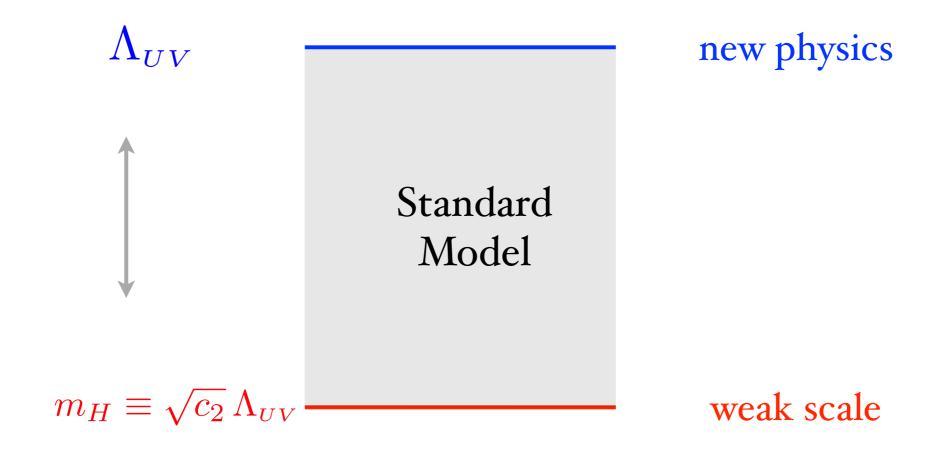
$$+ \dots$$

$$^{3}$$

$$d \ge 4$$

 $\Lambda_{\scriptscriptstyle UV} \gg {
m TeV}$  (pointlike limit ) nicely accounts for 'what we see'





some basic features of physical reality beautifully explained

by the magic of 
$$\mathcal{L}_{d=4}$$

### The magic of $\mathcal{L}_{d=4}$

$$\mathcal{L}_{4} = -\frac{1}{4g_{3}^{2}}G_{\mu\nu}^{2} - \frac{1}{4g_{2}^{2}}W_{\mu\nu}^{2} - \frac{1}{4g_{Y}^{2}}B_{\mu\nu}^{2} + |D_{\mu}H|^{2} + V(H)$$

$$+ \bar{q}_{L} \not\!\!{D}q_{L} + \bar{u}_{R} \not\!\!{D}u_{R} + \bar{d}_{R} \not\!{D}d_{R} + \bar{\ell}_{L} \not\!{D}\ell_{L} + \bar{e}_{R} \not\!{D}e_{R}$$

$$+ Y_{u}^{ij}\bar{q}_{L}^{i}H^{\dagger}u_{R}^{j} + Y_{d}^{ij}\bar{q}_{L}^{i}Hd_{R}^{j} + Y_{e}^{ij}\bar{\ell}_{L}^{i}He_{R}^{j}$$

- $U(3)_q \times U(3)_u \times U(3)_d \times U(3)_\ell \times U(3)_e$  broken only by  $Y_{u,d,e}$
- only  $\bar{f}f$  terms  $\rightarrow$  fermion number conserved
- ullet can always redefine  $Y_e$  to make it diagonal

 $U(1)_{L_1} \times U(1)_{L_2} \times U(1)_{L_3} \times U(1)_B$  and massless  $\nu$ 's emerge just accidentally but in nice qualitative agreement with observations

$$q_L^{\,i}\,,\;\;u_R^{\,\,i}\,,\;\;d_R^{\,\,i}\,,\;\;\ell_L^{\,\,i}\,,\;\;e_R^{\,\,i}$$

i = 1, 2, 3

(3, 2, 1/3) (3, 1, 4/3) (3, 1, -2/3) (1, 2, -1) (1, 1, -2)

$$q_L^i = \begin{pmatrix} u_L^i \\ d_L^i \end{pmatrix} \qquad q_L^i \to U_q^{ij} q_L^j$$

$$u_R^i \to U_u^{ij} u_R^j$$

$$d_R^i \to U_d^{ij} d_R^j$$

$$\ell_L^i = \begin{pmatrix} \nu_L^i \\ e_L^i \end{pmatrix} \qquad \qquad \ell_L^i \to U_\ell^{ij} \, \ell_L^j$$

$$e_R^i \to U_e^{ij} \, e_R^j$$

$$U(3)_q \times U(3)_u \times U(3)_d \times U(3)_\ell \times U(3)_e \equiv \text{Flavor Symmetry}$$

### The magic of $\mathcal{L}_{d=4}$

$$\mathcal{L}_{4} = -\frac{1}{4g_{3}^{2}}G_{\mu\nu}^{2} - \frac{1}{4g_{2}^{2}}W_{\mu\nu}^{2} - \frac{1}{4g_{Y}^{2}}B_{\mu\nu}^{2} + |D_{\mu}H|^{2} + V(H)$$

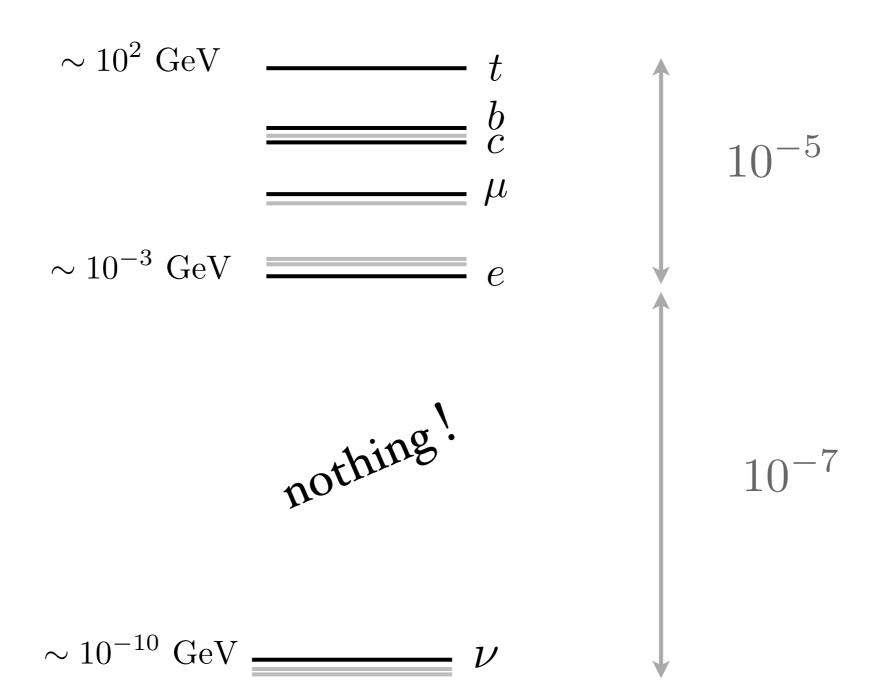
$$+ \bar{q}_{L} \not\!\!\!D q_{L} + \bar{u}_{R} \not\!\!\!D u_{R} + \bar{d}_{R} \not\!\!\!D d_{R} + \bar{\ell}_{L} \not\!\!\!D \ell_{L} + \bar{e}_{R} \not\!\!\!D e_{R}$$

$$+ Y_{u}^{ij} \bar{q}_{L}^{i} H^{\dagger} u_{R}^{j} + Y_{d}^{ij} \bar{q}_{L}^{i} H d_{R}^{j} + Y_{e}^{ij} \bar{\ell}_{L}^{i} H e_{R}^{j}$$

- $U(3)_q \times U(3)_u \times U(3)_d \times U(3)_\ell \times U(3)_e$  broken only by  $Y_{u,d,e}$
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Data seem to speak for a qualitatively different origin for the v mass

The next order in the  $1/\Lambda_{UV}$  expansion offers indeed such source

$$\mathcal{L}_{d=5} = \frac{b_{ij}}{\Lambda_{UV}} \ell_i^a C \ell_j^b H_a H_b \qquad \qquad m_{ij}^{\nu} = b_{ij} \frac{v_F^2}{\Lambda_{UV}}$$

taking grossly  $m_{\nu} \sim 0.1 \, \mathrm{eV}$   $\Lambda_{UV} \sim 10^{14} \, \mathrm{GeV} \times |b_{ij}|$ 



for  $|b_{ij}| = O(1)$  this is not too far from the unification scale

$$U(1)_{L_1} \times U(1)_{L_2} \times U(1)_{L_3} \times U(1)_B$$

baryon number conserved: the proton is stable (...and life possible)

proton lifetime from SuperKamiokande Collab.

$$\tau(p \to e^+ \pi^0) > 1.6 \times 10^{34} \,\mathrm{yrs}$$
 90% CL

individual lepton number conserved

$$\mu \to e \gamma$$

$$\tau \to \mu \gamma$$

$$\mu^- \to e^- e^+ e^-$$

$$\cdots$$
forbidden

Ex. MEG experiment

$$Br(\mu \to e \gamma) < 4.2 \times 10^{-13}$$

90% CL

### but all these effects are generated by terms in $\mathcal{L}_6$

$$\mathcal{L}_6 \supset \frac{\kappa_{uude}}{\Lambda_{uu}^2} \left( u_R^{\alpha} C d_R^{\beta} \right) \left( u_R^{\gamma} C e_R \right) \epsilon^{\alpha\beta\gamma}$$

B+L violation: proton decay

$$\frac{u}{d}$$

$$p \to e^+ \pi^0$$

$$p \to e^+ \pi^0$$
 
$$\Lambda_{UV} > \sqrt{\kappa_{uude}} \ 10^{15} \ \mathrm{GeV}$$

$$\mathcal{L}_6 \supset \sqrt{y_e y_\mu} \, \frac{c_{e\mu}}{\Lambda_{UV}^2} \, \left( \bar{\ell}_e \sigma_{\rho\sigma} \mu \, H \right) \, B^{\rho\sigma}$$

$$\operatorname{Br}(\mu \to e \gamma)\Big|_{exp} \implies \Lambda_{UV} \gtrsim \sqrt{c_{e\mu}} \, 300 \, \text{TeV}$$

### The remarkable 'flavor' of $\mathcal{L}_4$ (GIM mechanism)

$$Y_u^{ij} \, \bar{q}_L^i H^\dagger u_R^j + Y_d^{ij} \, \bar{q}_L^i H d_R^j \qquad \text{flavor rotations} \qquad \begin{cases} Y_u \, = \, D_u \\ Y_d \, = \, V D_d \end{cases} \qquad D_u = \operatorname{diag}(y_u, \, y_c, \, y_t) \\ Y_u \, = \, V^\dagger D_u \\ Y_d \, = \, D_d \end{cases} \qquad D_d = \operatorname{diag}(y_d, \, y_s, \, y_b)$$

Flavor violation purely in the interplay between u- and d-type quarks If either  $D_u$  or  $D_d$  degenerate, then V can be eliminated

Flavor Changing Neutral Currents

tree: none

loop: depend on the mass (differences) in the other charge sector

### **CP** violation

•  $V \neq V^*$  only source of CP violation

• V physical up to quark phase rotations  $V^{jk} o e^{i(\theta_u^j - \theta_d^k)} V^{jk}$ 

• truly physical CP violation  $J_{ijk\ell} \equiv \operatorname{Im} \left\{ V_{ij} V_{kj}^* V_{k\ell} V_{i\ell}^* \right\}$ 

ullet unitarity  $V_{ij}V_{ik}^* = \delta_{jk}$  2-families  $J_{ijk\ell} = 0$  3-families  $J_{ijk\ell} \equiv J$   $i 
eq k, j 
eq \ell$ 

• Jarlskog invariant  $J = \operatorname{Im} \{V_{ud}V_{td}^*V_{tb}V_{ub}^*\} < |V_{td}V_{ub}| \lesssim 3 \times 10^{-5}$ 

ullet if any two quarks of the same charge degenerate, J unphysical

# Consequences

Ex: 
$$K\bar{K}$$
 – mixing

$$A_{\Delta S=2}=egin{array}{c} a & \longrightarrow & \overline{s} \\ \overline{s} & \longrightarrow & d \end{array}$$

$$\operatorname{Re}(\mathcal{A}_{\Delta S=2})$$

$$\operatorname{Re}(\mathcal{A}_{\Delta S=2}) \qquad \qquad \frac{\Delta m_K}{m_K} \sim \frac{\alpha_W}{4\pi} \left(\frac{f_K}{v_F}\right)^2 \left(\frac{m_c}{m_W}\right)^2 \sin^2\theta_c \cos^2\theta_c$$

$$\operatorname{Im}(\mathcal{A}_{\Delta S=2})$$

$$\operatorname{Im}(\mathcal{A}_{\Delta S=2}) \qquad \bullet \qquad \bullet_{K} = \frac{\operatorname{Im}(\mathcal{A}_{\Delta S=2})}{\operatorname{Re}(\mathcal{A}_{\Delta S=2})} \sim \frac{J}{\cos^{2}\theta_{c}\sin^{2}\theta_{c}} \sim 10^{-3}$$

### Electric dipole moments

state with definite

$$\vec{J} \cdot \vec{J} = j(j+1)$$

$$\langle \Psi(J) | \vec{D} \, | \Psi(J) \rangle \; = \; \begin{array}{c} c \, \langle \Psi(J) | \, \vec{J} \, | \Psi(J) \rangle \\ \text{T-even} \end{array}$$

non-vanishing edm

$$\leftrightarrow$$

broken T

broken CP

neutron

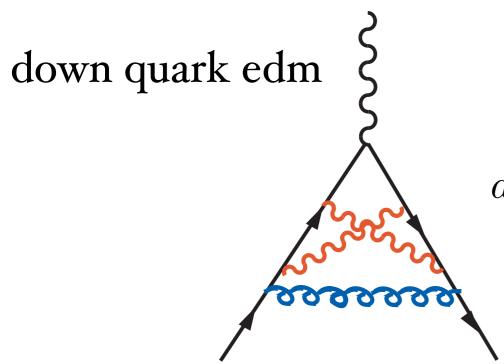
$$d_n < 10^{-26} e \, \text{cm}$$
 nEDM 2020

Experimentally

electron

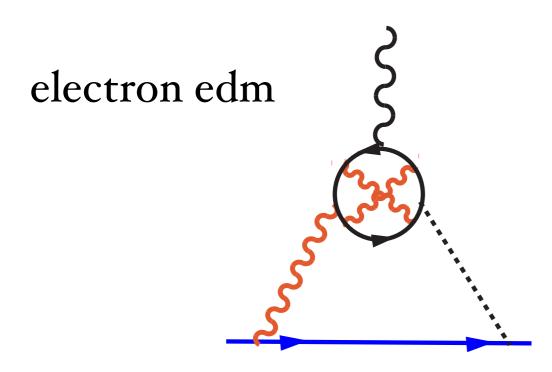
$$d_e < 10^{-29} e \, \mathrm{cm}$$
 ACME 2018

## $\mathcal{L}_4$ contribution to edms: J and QCD vacuum angle $\theta_{QCD}$



$$d_d \sim e \frac{\alpha_s}{4\pi} \left(\frac{\alpha_W}{4\pi}\right)^2 \frac{m_d}{m_W^2} \frac{m_c^2}{m_W^2} J \sim 10^{-34} e \,\mathrm{cm}$$

Czarnecki, Krause 1997



$$d_e \sim 10^{-38} e \, \text{cm}$$

Khriplovich, Pospelov 1991

### While $\mathcal{L}_6$ contributes to all these processes at tree level

$$\mathcal{L}_6 \supset \frac{c_{\Delta S=2}}{\Lambda_{UV}^2} (\bar{d}\gamma^{\mu}s)^2$$

$$\Lambda_{UV} > \sqrt{\mathrm{Re}(c_{\Delta S=2})} \times 10^6 \text{ GeV}$$

$$\Lambda_{UV} > \sqrt{\mathrm{Im}(c_{\Delta S=2})} \times 10^7 \text{ GeV}$$

$$\mathcal{L}_6 \supset \frac{c_e y_e}{\Lambda_{\mu\nu}^2} \left( \bar{\ell}_L \sigma^\mu e_R H \right) B_{\mu\nu}$$

$$\Lambda_{UV} > \sqrt{\mathrm{Im}(c_e)} \times 10^6 \text{ GeV}$$

QCD vacuum angle

$$\theta_{QCD}$$

neutron edm

$$d_n \sim \theta_{QCD} \times 10^{-16} e \,\mathrm{cm}$$

$$\theta_{QCD} \lesssim 10^{-10}$$

hard to understand given CP violation in CKM seems just small by accident

# This is the Strong CP Problem

The Strong CP problem looks like a stain on the magic of  $\mathcal{L}_4$ 

However this stain is remarkably mitigated by the existence of a dynamical solution, entailing the existence of an ultralight scalar, the axion, and compatible with a fundamental new physics scale  $f_a$  many orders of magnitude above the weak scale ( $f_a \sim 10^{10} - 10^{12} \,\text{GeV}$ )

### More magic of $\mathcal{L}_4$ : custodial symmetry

$$\mathbf{H} = \left( egin{array}{c} H^+ \ H^0 \end{array} 
ight) \qquad \qquad \mathbf{H} \stackrel{SU(2)_L}{\longrightarrow} \quad \hat{U}\mathbf{H}$$

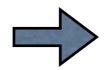
$$\mathbf{H} = (\operatorname{Re} H^+, \operatorname{Im} H^+, \operatorname{Re} H^0, \operatorname{Im} H^0)$$
 **4 of**  $O(4) \sim SU(2)_L \times SU(2)_R$ 

$$O(4)$$
  $\wedge$   $\wedge +$ 

$$\mathbf{\Phi} \equiv \begin{pmatrix} H^{0*} & H^{+} \\ -H^{+*} & H^{0} \end{pmatrix} \qquad \mathbf{\Phi} \stackrel{O(4)}{\longrightarrow} \hat{U}_{L} \mathbf{\Phi} \hat{U}_{R}^{\dagger}$$

$$D_{\mu}\mathbf{\Phi} = \partial_{\mu}\mathbf{\Phi} + ig_2T_L^AW_{\mu}^A\mathbf{\Phi} - ig_Y\mathbf{\Phi}T_R^3B_{\mu}$$

$$\mathcal{L}_{Higgs} = \frac{1}{2} \text{Tr}(D_{\mu} \mathbf{\Phi}^{\dagger} D_{\mu} \mathbf{\Phi}) - \frac{m^{2}}{2} \text{Tr}(\mathbf{\Phi}^{\dagger} \mathbf{\Phi}) - \frac{\lambda}{4} \left[ \text{Tr}(\mathbf{\Phi}^{\dagger} \mathbf{\Phi}) \right]^{2}$$



lack lack hypercharge Y acts like  $T_R^3$  lack lac

 ${\cal O}(4)$  is only broken by hypercharge and other small effects

$$\langle \mathbf{\Phi} \rangle = \begin{pmatrix} \langle H^{0*} \rangle & \langle H^+ \rangle \\ -\langle H^{+*} \rangle & \langle H^0 \rangle \end{pmatrix} = \begin{pmatrix} v_F & 0 \\ 0 & v_F \end{pmatrix}$$

$$oldsymbol{\Phi} \longrightarrow \hat{U} oldsymbol{\Phi} \hat{U}^\dagger$$
 is a residual approx symmetry:  $SU(2)_c$  (custodial)

$$(W_{\mu}^{1},W_{\mu}^{2},W_{\mu}^{3})$$
 form a triplet under  $SU(2)_{c}$ 

$$\mathcal{L}_{mass} = \frac{v_F^2}{4} \begin{pmatrix} W_{\mu}^1 & W_{\mu}^2 & W_{\mu}^3 & B_{\mu} \end{pmatrix} \begin{pmatrix} g_2^2 & & & & \\ & g_2^2 & & & & \\ & & g_2 g_Y & g_Y^2 \end{pmatrix} \begin{pmatrix} W_{\mu}^1 & & & \\ W_{\mu}^2 & & & \\ W_{\mu}^3 & & & \\ B_{\mu} & & & \end{pmatrix}$$

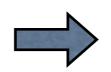
$$m_Z^2 = \frac{v_F^2}{2} (g_2^2 + g_Y^2) = \frac{m_W^2}{\cos^2 \theta_W}$$
  $\rho \equiv \frac{m_W^2}{m_Z^2 \cos^2 \theta_W} = 1$ 

$$\rho \equiv \frac{m_W^2}{m_Z^2 \cos^2 \theta_W} = 1$$

$$\Diamond$$

 $SU(2)_C$  is also an accidental symmetry

$$\mathcal{L}^{d=6} = \frac{1}{\Lambda^2} (\mathbf{H}^{\dagger} D_{\mu} \mathbf{H}) (\mathbf{H}^{\dagger} D^{\mu} \mathbf{H}) \qquad \qquad \delta \rho \sim \frac{v_F^2}{\Lambda^2}$$



$$\delta 
ho \sim \frac{v_F^2}{\Lambda^2}$$

Electroweak Precision Tests (LEP/SLC/Tevatron)





 $\delta \rho_{BSM} \lesssim 10^{-3}$   $\Lambda \gtrsim 10 \,\mathrm{TeV}$ 

- It is remarkable how the hypothesis  $\Lambda_{uv} \gg 1$ TeV, the *desert*, very simply explains many structural aspects of particle physics
- This encourages us to try and understand how can  $m_H$  be plausibly made hierarchically separated from  $\Lambda_{UV}$

... to our great frustration we find we cannot!

$$+ m_H^2 H^{\dagger} H$$

d<4

$$\mathcal{L}_{SM} = \mathcal{L}_{kin} + gA_{\mu}\bar{F}\gamma_{\mu}F + Y_{ij}\bar{F}_{i}HF_{j} + \lambda(H^{\dagger}H)^{2}$$

$$d=4$$

$$+ \frac{b_{ij}}{\Lambda_{UV}} L_i L_j H H$$

$$+ \frac{c_{ijkl}}{\Lambda_{UV}^2} \bar{F}_i F_j \bar{F}_k F_\ell + \frac{c_{ij}}{\Lambda_{UV}^2} \bar{F}_i \sigma_{\mu\nu} F_j H G^{\mu\nu} + \dots$$

$$+$$

According to our philosophy

$$m_H^2 = c_2 \Lambda_{UV}^2$$

$$\Lambda_{UV} = 10^6 \,\text{GeV} \implies c_2 \sim 10^{-8}$$

$$\Lambda_{UV} = 10^{15} \,\text{GeV} \implies c_2 \sim 10^{-26}$$

$$\Lambda_{UV} = 10^6 \, \mathrm{GeV} \implies c_2 \sim 10^{-8}$$

$$\Lambda_{UV} = 10^{15} \, \mathrm{GeV} \implies c_2 \sim 10^{-26}$$

Is it reasonable to expect such a tremendously small c?

### $UV \Rightarrow IR$ mapping of parameters

$$\int D\varphi_{UV} \, D\varphi_{IR} \, e^{iS(G_a,\varphi)} = \int D\varphi_{IR} \, e^{iS_{eff}(g_i,\varphi_{IR})}$$

$$g_i = g_i(G_a)$$

$$= g_i - g_i($$

Ex: scalar masses

$$m_i^2 = \sum_a C_{ia} M_a^2$$

 $M_a^2 \sim \Lambda_{UV}^2$ 

Ex: fermion masses

$$m_i = \sum_a C_{ia} M_a$$

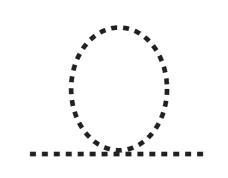
$$complex$$

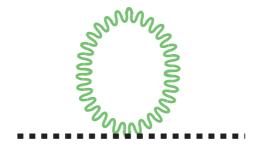
tranforming under phase rotations: can happen that q-numbers forbid contribution of all  $M_a$ 

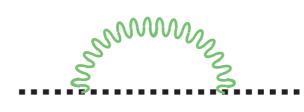
In order to write the detailed mapping of parameters we need of course the full UV theory

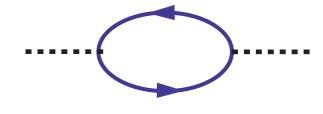
However in order to estimate roughly what to expect based on symmetry considerations it is enough to consider the effects of quantum fluctutation within the EFT

The basic point is that  $\varphi_{IR}(k \lesssim \Lambda_{UV})$  are not so distinguished from  $\varphi_{UV}(k \gtrsim \Lambda_{UV})$ 









$$\delta m_H^2 = +\frac{3\lambda}{2(2\pi)^4} \int^{\Lambda_{UV}} \frac{d^4p}{p^2} + \frac{9g_W^2}{8(2\pi)^4} \int^{\Lambda_{UV}} \frac{d^4p}{p^2} - \frac{3y_t^2}{(2\pi)^4} \int^{\Lambda_{UV}} \frac{d^4p}{p^2}$$

$$+\frac{9g_W^2}{8(2\pi)^4}\int^{\Lambda_{UV}}\frac{d^4p}{p^2}$$

$$-\frac{3y_t^2}{(2\pi)^4} \int^{\Lambda_{UV}} \frac{d^4p}{p^2}$$

$$= \# \frac{33\lambda}{166\pi^2} \Lambda_{UV}^{3} + + \# \frac{992}{64\pi^2} \Lambda_{UW}^{2} - \frac{3y_5^3y_1^2}{8\pi^8\pi^2} \Lambda_{UV}^{2}$$

$$\# \frac{9g_{22}^{22}}{64\pi^2} \Lambda_{ww}^2$$

$$\frac{3y_{0}^{3}y_{t}^{2}}{8\pi8\pi^{2}}V_{UV}^{2}$$

$$\delta m_H^2 \lesssim m_H^2|_{exp}$$



 $\Lambda_{UV} \lesssim 500 \, {
m GeV}$ 

It seem we have a problem understanding  $\,m_H \ll \Lambda_{\scriptscriptstyle UV}\,$ 

Notice

$$\delta m_H^2 \sim \frac{y_t^2}{8\pi^2} \, \Lambda_{\scriptscriptstyle UV}^2$$
 higher dilatation

spin

symm

fully fixed by symmetries

see, e.g. RR, TASI 2015

very much like the frequency of pendulum

$$\omega = c \sqrt{\frac{g}{L}}$$

Galileo would surely have gasped had he found

$$c = 10^{-20}$$

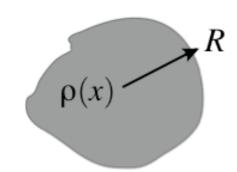


symm

But why didn't people worry about the electron mass?

....well, actually at a certain point they did

naive classical picture of electron



$$E \sim \frac{e^2}{R}$$

relativity 
$$m = E \sim \frac{e^2}{R} \xrightarrow{R \to 0} \infty$$

$$e^2$$

$$e^2$$

$$\Delta m_e = + \frac{e^2}{16\pi^2} \Lambda$$

$$-\frac{e}{16\pi^2}\Lambda = 0$$

### The reason for this cancellation is chiral symmetry

$$\psi_L \to \psi_L e^{-i\theta}$$
 $\psi_R \to \psi_R e^{i\theta}$ 
 $m_e \to m_e e^{i2\theta}$ 

$$\Delta m_e \sim m_e \frac{e^2}{(2\pi)^4} \int \frac{d^4p}{(p^2)^2}$$

Fermion mass is only multiplicatively renormalized no additive, possibly large, contribution

And what about the photon?

Shouldn't we worry for the origin of his vanishing mass?

No!

as long as  $2 \neq 3$