

Emergence of a gluon mass

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Perceiving the Emergence
of Hadron Mass through
AMBER@CERN

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[Perceiving the Emergence of Hadron Mass through AMBER@CERN \(II\)](#)

*Emergence : low-level rules producing high-level phenomena
with enormous apparent complexity*

Start from the QCD Lagrangian :

$$\mathcal{L}_{QCD} = - \frac{1}{4} G_a^{\mu\nu} G_{\mu\nu}^a + \frac{1}{2\xi} (\partial^\mu A_\mu^a)^2 + \partial^\mu \bar{c}^a \partial_\mu c^a + g f^{abc} (\partial^\mu \bar{c}^a) A_\mu^b c^c$$

+ Quarks



SDE, lattice, BSE ...

and obtain

Dynamical generation of a fundamental mass scale in pure Yang-Mills (gluon mass)

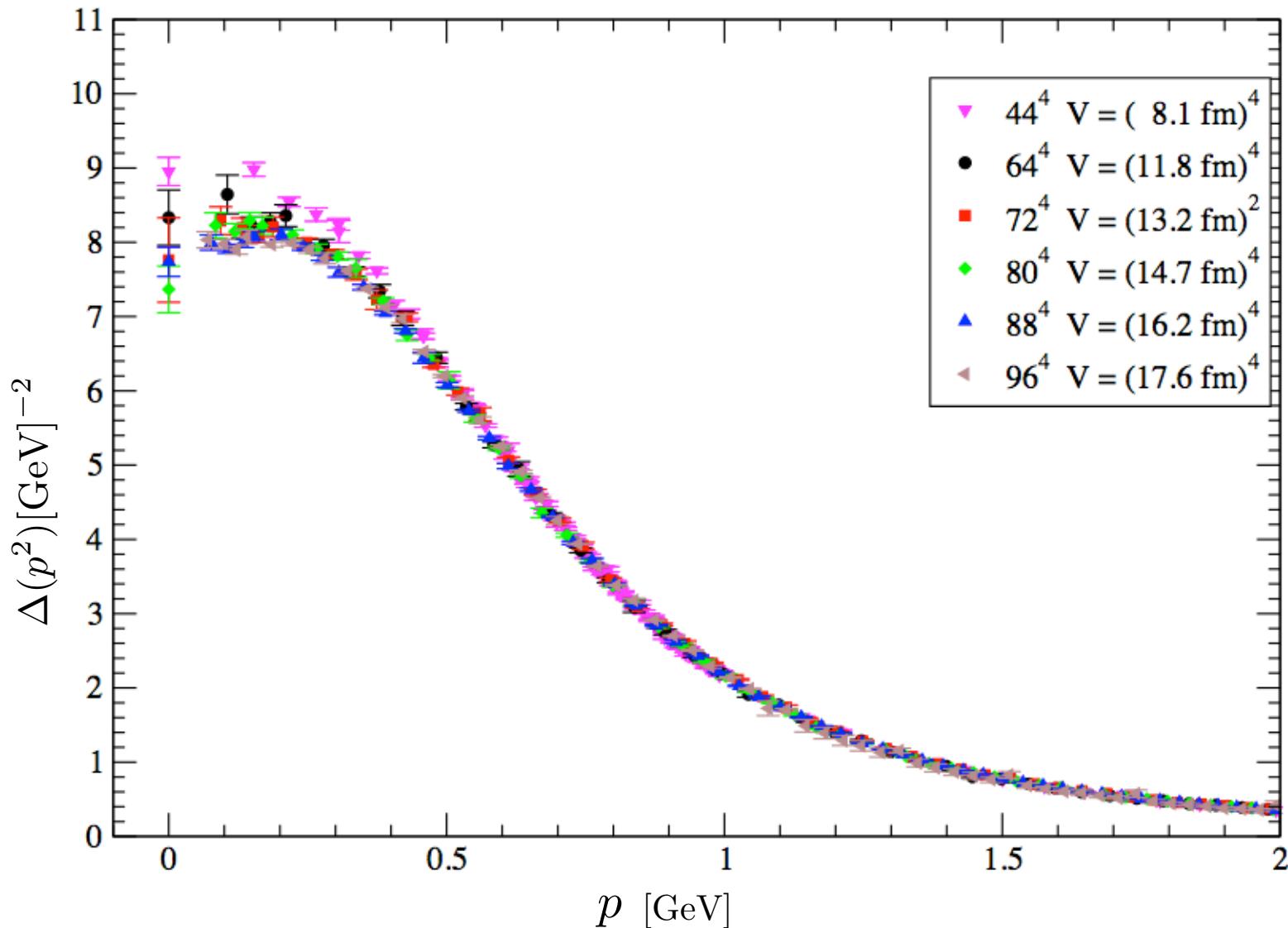
Quark constituent masses and chiral symmetry breaking

Bound state formation: mesons, hadrons, glueballs, hybrids, exotics ...

Signals of Confinement

Large volume lattice simulations

*The gluon propagator **saturates** in the deep infrared*



I. Bogolubsky, E. Ilgenfritz, M. Müller-Preussker, and A. Sternbeck, Phys. Lett. B676, 69 (2009).

Emergent mass in the gauge sector

J. M. Cornwall, Phys. Rev. D26, 1453 (1982)

A.C. Aguilar, D. Binosi, J.P. (various works)

- Saturation of $\Delta(0) \longleftrightarrow$ *unequivocal* signal of gluon mass generation
- A dynamical and nonperturbative mechanism is needed to accomplish this
- A mass term $m^2 A^2$ in the YM Lagrangian is forbidden by gauge invariance
- No quadratic divergences are allowed !
- All symmetries must be explicitly preserved.
In particular, no violation of the STIs !



Schwinger-Dyson eqs. in the PT-BFM scheme

Pinch Technique

Background Field Method

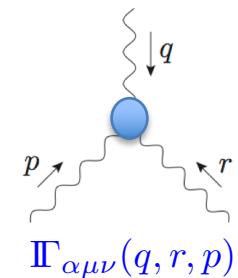
$$\tilde{\Pi}_{\mu\nu}(q) = \boxed{(a_1) + (a_2)} + \boxed{(a_3) + (a_4)} + \boxed{(a_5) + (a_6)} + \dots$$

Beautiful truncation properties !

Symmetries manifest: all sorts of “alarms” go off if one tries “forbidden” things

Crucial dynamical ingredient:

Existence of “massive” solution requires the presence of massless poles inside the three-gluon vertex





Schwinger mechanism in Yang-Mills theories

$$\begin{aligned} \text{Diagram: } & \text{A wavy line labeled } \alpha \text{ with a downward arrow } q \text{ meets a blue circle at a vertex. From the blue circle, two wavy lines labeled } p \text{ and } r \text{ emerge, labeled } \nu \text{ and } \mu \text{ respectively.} \\ & = \quad \text{Diagram: } \text{The same setup as above, but the blue circle is replaced by a red circle.} \\ & + \quad \text{Diagram: } \text{The same setup as above, but the blue circle is replaced by a green circle. A black dot is connected to the green circle by a vertical line. A horizontal line connects the black dot to the green circle. A blue arrow points from the green circle towards the black dot. The label } i/q^2 \text{ is placed near the black dot.} \\ & \text{Labels: } \mathbb{I}_{\alpha\mu\nu}(q, r, p) \quad \Gamma_{\alpha\mu\nu}^{\text{np}}(q, r, p) \quad \Gamma_{\alpha\mu\nu}^{\text{P}}(q, r, p) \\ & \text{Text: } \text{Dynamically generated massless \& colored excitations} \end{aligned}$$

A.C.Aguilar, D. Ibanez, V. Mathieu, and J. P., Phys. Rev. D 85, 014018 (2012)

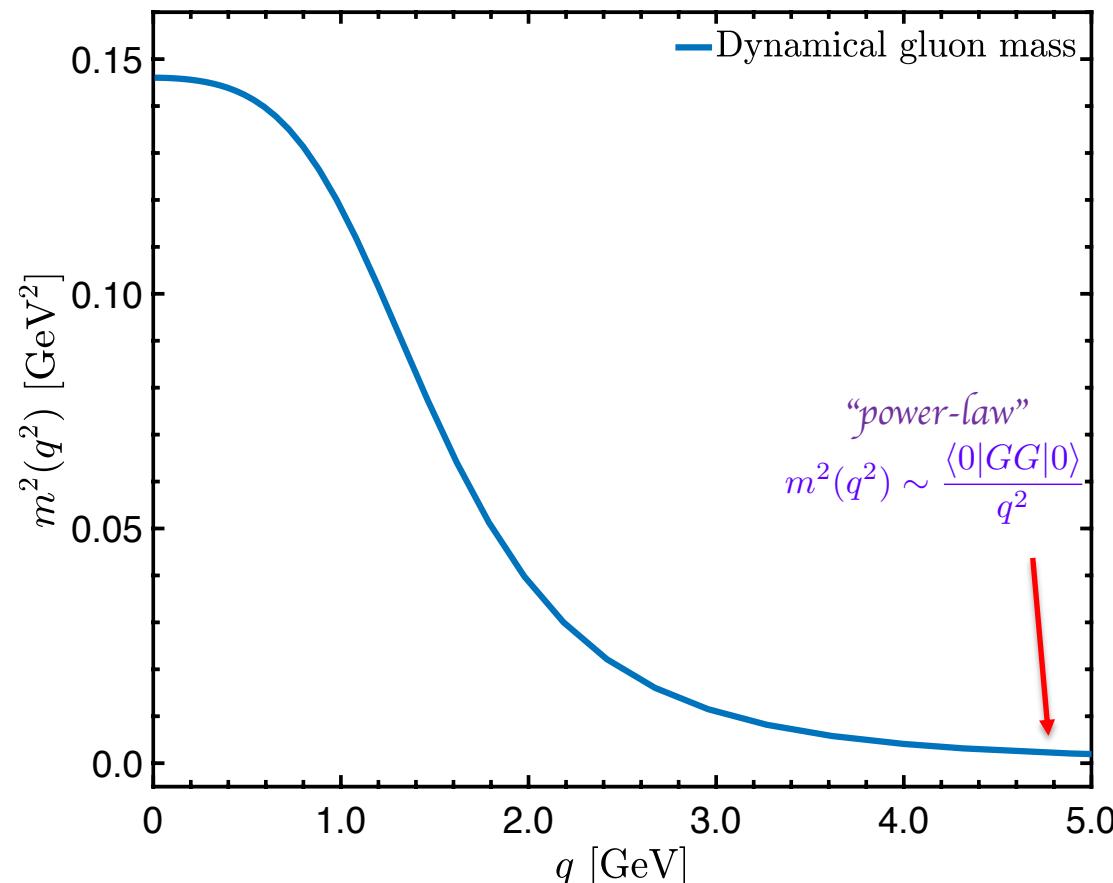
$$\left. \begin{aligned} \text{Text: } & \text{Triggers the "Schwinger mechanism"} \\ \text{Diagram: } & \text{A wavy line meets a chain of four circles. The first and last circles are light blue. The middle two are dark green. A horizontal line connects the second and third circles. A blue arrow points from the third circle to the fourth. The label } i/q^2 \text{ is placed near the horizontal line.} \\ \text{Label: } & \Gamma_{\alpha\mu\nu}^{\text{P}}(q, r, p) \end{aligned} \right\} \quad \begin{aligned} \text{Text: } & \text{J.S. Schwinger, Phys. Rev. 125, 397 (1962); Phys. Rev. 128, 2425 (1962)} \\ \text{Text: } & \text{Makes possible } \Delta^{-1}(0) \neq 0 \\ \text{Equation: } & P_{\alpha\alpha'}(q) P_{\mu\mu'}(r) P_{\nu\nu'}(p) \Gamma_{\alpha\mu\nu}^{\text{P}}(q, r, p) = 0 \\ \text{Text: } & \text{"Longitudinally coupled"} \quad \longrightarrow \quad \text{Text: } \text{Drops out from "lattice observables" and transversely projected Green's functions} \end{aligned}$$



Natural parametrization

$$\Delta^{-1}(q) = q^2 J(q) + m^2(q)$$

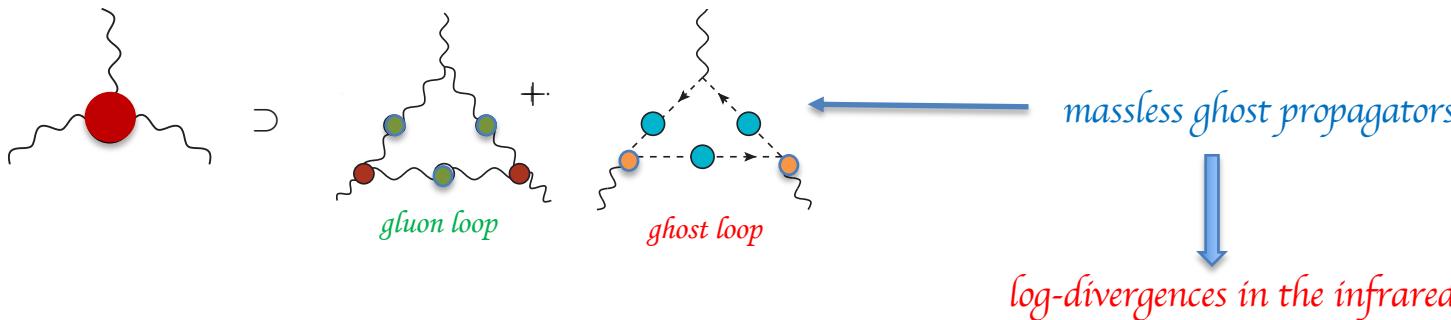
kinetic term running mass



$m(0) \sim 375$ MeV (Landau gauge)

• Infrared suppression of the three-gluon vertex: intriguing nonperturbative feature

A.C.Aguilar, D.Binosi, D.Ibañez, J.P., Phys. Rev. D 89, no. 8, 085008 (2014)



$$\Gamma_{\alpha\mu\nu}^{\text{NP}} = f(q, r, p) \Gamma_{\alpha\mu\nu}^{(0)}$$

symmetric point: $q^2 = p^2 = r^2$

$$f(q^2) = a \left[1 + b \ln \frac{q^2 + m^2}{\mu^2} + c \ln \frac{q^2}{\mu^2} \right]$$

↑ ↑
"protected" "unprotected"

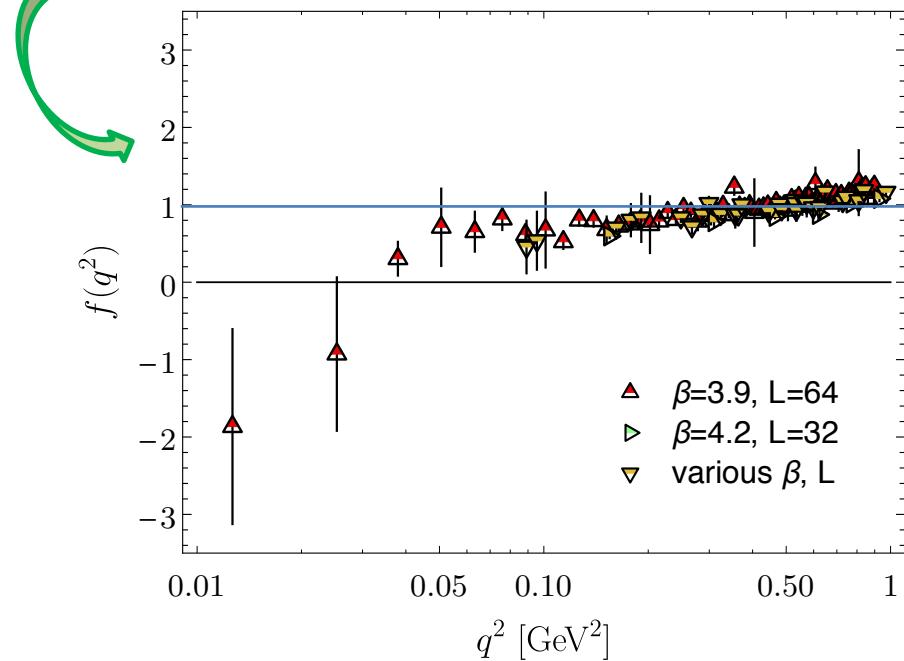
$f(0) \rightarrow -\infty$

• Dramatic confirmation that all pieces fit together and are tightly interlocked!

• Phenomenological implication for bound state formation (glueballs, hybrids, EIC physics, etc)

E.-V.-Souza et al, Eur. Phys. J. A 56, no.1, 25 (2020)

S.S.Xu et al, Eur. Phys. J. A 55, no.7, 113 (2019)



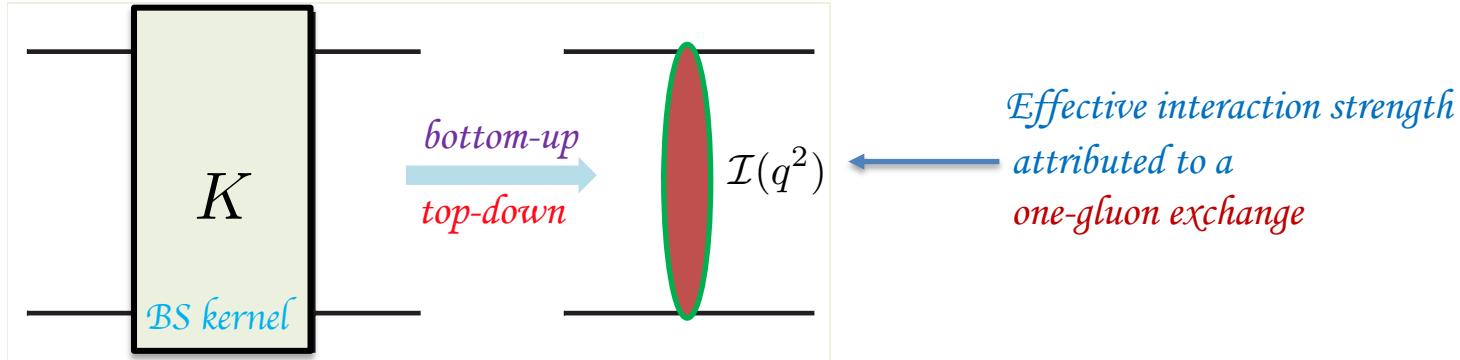
A.Athenodorou et al, Phys. Lett. B761, 444 (2016)

A.G.Duarte, O.Oliveira, and P.J.Silva,
Phys. Rev. D 94 (2016) no.7, 074502

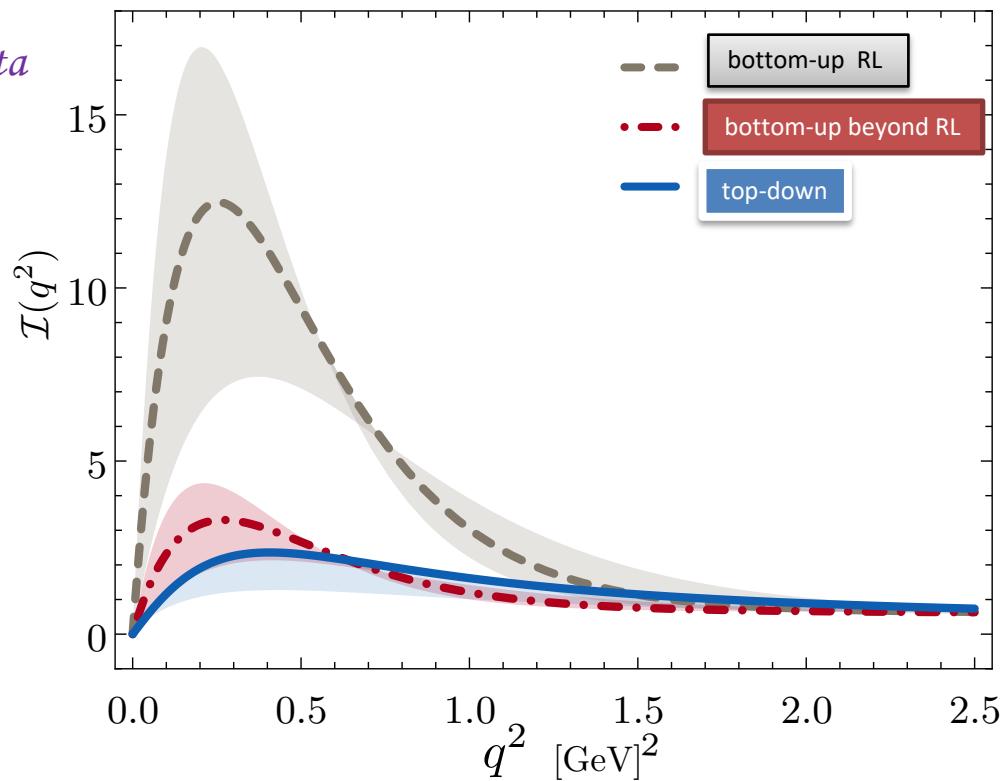
A.C.Aguilar et al, Eur. Phys. J. C 80, no.2, 154 (2020)

Bridging a gap between continuum QCD and ab initio predictions of hadron observables

D. Binosi, L. Chang, J.P. and C.D. Roberts, Phys. Lett. B742, 183 (2015)



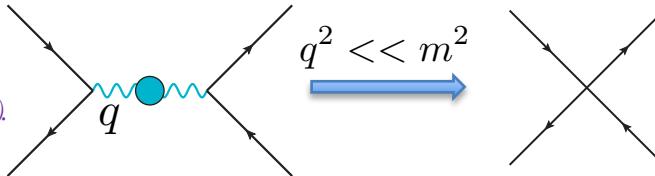
- bottom-up scheme: infer interaction by fitting data within a well-defined truncation of the matter sector SDEs that are relevant to bound state properties.
- top down approach: ab initio computation of the interaction via direct analysis of the gauge sector gap equations
- Significant step toward parameter-free predictions of hadron properties



Conclusions

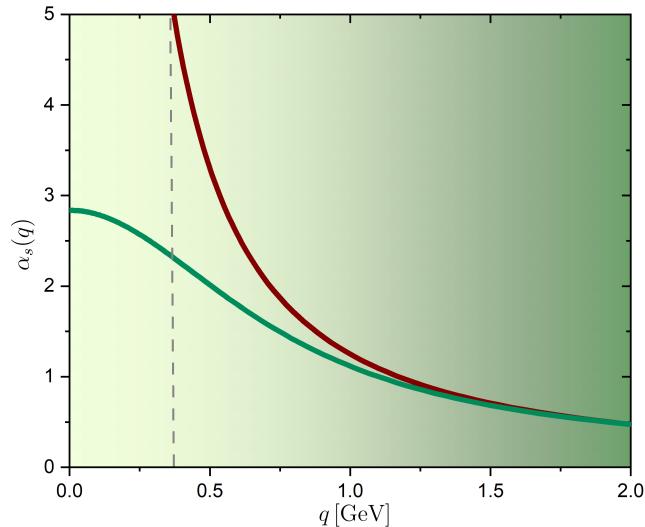
- The gluon self-interactions generate a dynamical mass scale in the gauge sector of QCD
- Important theoretical and phenomenological implications
- “Contact interactions” from first principles

S.-X. Qin, L. Chang, Y.-X. Liu, C. D. Roberts and D. J. Wilson, Phys. Rev. C 84, 042202 (2011).



- Tames the Landau pole; allows for the QCD generalization of the process-independent Gell-Mann – Low effective charge

D.Binosi, C.Mezrag, J.P., C.D.Roberts, and J.Rodriguez-Quintero, Phys. Rev. D 96, no.5, 054026 (2017)



- The dynamical generation of a running gluon mass may alone be sufficient to remove the Gribov ambiguity.

F.Gao, S.X.Qin, C.D.Roberts, and J.Rodriguez-Quintero, Phys. Rev. D 97, no.3, 034010 (2018)