

SMEFT@NLO

Automated one-loop
computations in the SMEFT

arXiv:2008.11743

Ken Mimasu

King's College London

LHC EW WG general meeting, 7th October 2020

*on behalf of: Gauthier Durieux, Céline Degrande,
Fabio Maltoni, KM, Cen Zhang & Eleni Vryonidou*

<http://feynrules.irmp.ucl.ac.be/wiki/SMEFTatNLO>

SMEFT is...

$$\mathcal{L}_{\text{EFT}} = \mathcal{L}_{\text{SM}} + \sum_i \frac{c_i^{(6)}}{\Lambda^2} O_i^{(6)} + \mathcal{O}(\Lambda^{-4})$$

Model independent

- Underlying assumptions

Heavy new physics: $M > E_{\text{exp}}$

SM field content & gauge symmetries

Linear EWSB: Higgs = doublet

Systematically improvable

- Double expansion *higher dim.* $\frac{E^2}{\Lambda^2}$ & $\{g_s, g, g'\}$ *more loops*

Global

- Model independence: we don't know what operators NP will generate
- **Patterns & correlations** among observables are key
- Ultimate goal: complete likelihood for SMEFT confronted with HEP data

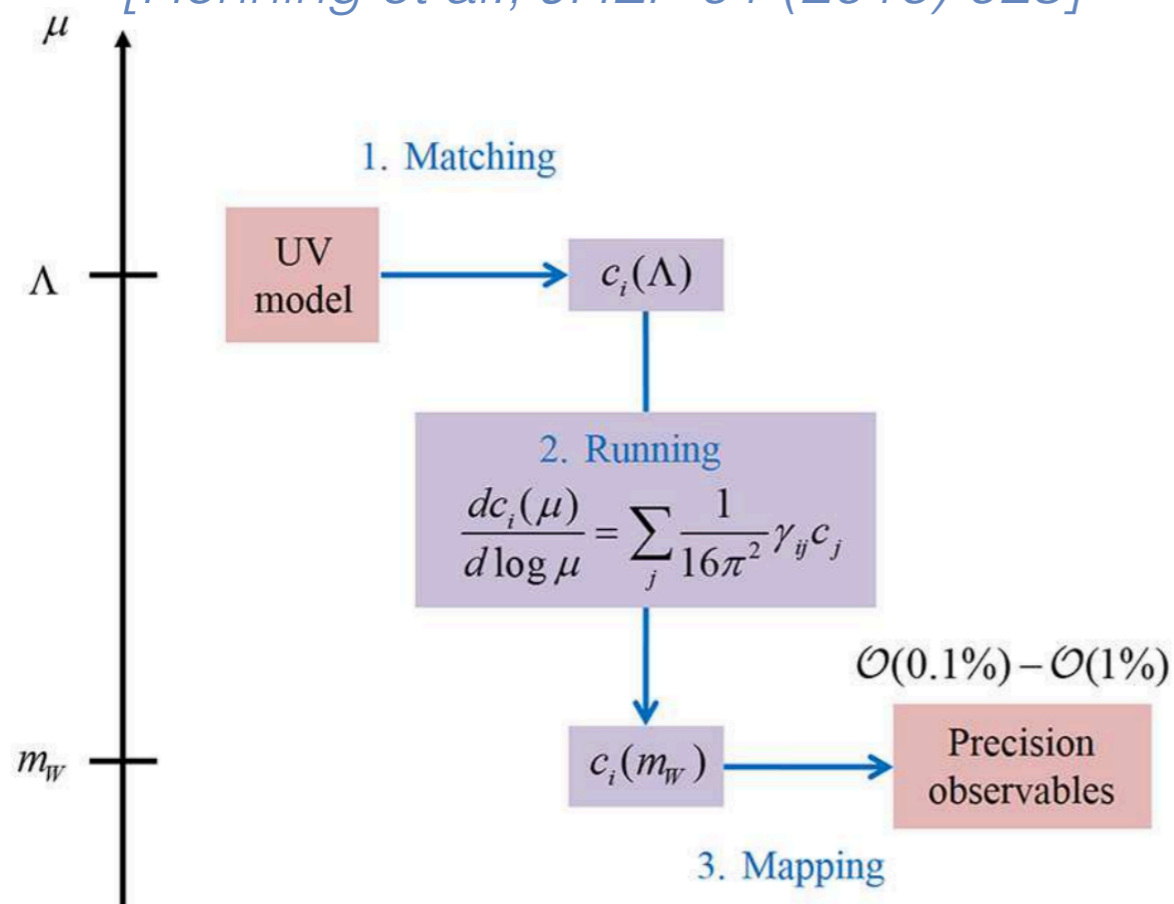
EWPO, Higgs, multiboson, top, DY, flavor, ...

Established part of LHC programme

Higher orders

$$\mathcal{L}_{\text{EFT}} = \mathcal{L}_{\text{SM}} + \sum_i \frac{c_i^{(6)}}{\Lambda^2} O_i^{(6)} + \mathcal{O}(\Lambda^{-4})$$

[Henning et al.; JHEP 01 (2016) 023]



Dimension 7,8,9,...

[Lehman; PRD 90 (2014) 12, 125023]

[Lehman & Martin; JHEP 02 (2016) 081]

[Henning et al.; JHEP 08 (2017) 016]

[Liao, Ma & Wang; JHEP 08 (2020) 162]

[Li et al.; 2005.00008]

[Murphy; arXiv: 2005.00059]

[Liao & Ma.; 2007.08125]

[Li et al.; 2007.07899]

Increasing # of explicit studies

One-loop (QCD, EW)

Too many works to cite...

We can improve in Λ & g for all stages 1-3

- Bottom-up: mapping Wilson coefficients to observables (stage 3.)
- LHC priority: dimension-6 & QCD loops

Precision interpretations

Want to improve...

$$\Delta o_n = o_n^{\text{EXP}} - o_n^{\text{SM}} = \sum_i \frac{a_{n,i}^{(6)}(\mu) c_i^{(6)}(\mu)}{\Lambda^2} + \mathcal{O}\left(\frac{1}{\Lambda^3}\right)$$

Precision interpretations

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Global nature

As many observables
as possible

Identify patterns &
correlations in fits

Exploit energy-growth

Precision interpretations

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Sensitivity

Experiment:

Best measurements & understanding of uncertainties and correlations

Theory:

Best available predictions for observables (NLO, NNLO, N3LO,...)

Precision interpretations

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Interpretation

Relies on accurate knowledge of the size & correlation among a_i

Determining $c_i^{(6)}$ requires most precise available SMEFT predictions

Why higher orders

Higher orders in SMEFT improve...

Accuracy (better central value)

- No deviation: better representation of new physics **reach**
- Yes deviation: better **pinpointing** of new physics origin

Precision (better error bars)

- Control over **scale uncertainty** (must include running & mixing)

Sensitivity

- Knowledge of the **patterns & correlations**
- **Differential** predictions - key for, e.g., multivariate & ME based analyses
- New **loop-induced** sensitivity (e.g., top loop in ggF)

SMEFT@NLO

NLO computations for SMEFT: very active field

- Many results & analyses have appeared in the last few years
- **Non-universal K-factors** in EFT space → **new information at NLO**
- Experimental interest in including one-loop for SMEFT analyses/interpretations

Many processes x **many operators**

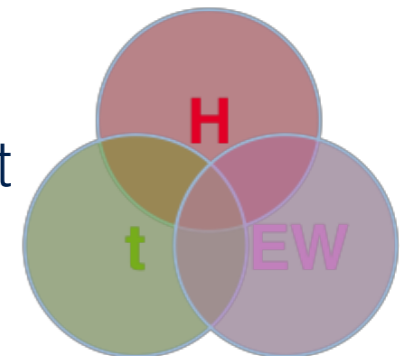
- NLO generally complicates picture: more cross-talk, more operators
- Automated tools for Fixed Order/NLO+PS are essential

SMEFT@NLO

[Degrande et al.; arXiv:2008.11743]

<http://feynrules.irmp.ucl.ac.be/wiki/SMEFTatNLO>


- NLO UFO model for MadGraph5_aMC@NLO
- Process independent SMEFT implementation: **top-specific** flavor limit
- Suitable for LO/NLO computations of EW/Higgs/Top processes



Standard Model Effective Theory at One-Loop in QCD

Céline Degrande, Gauthier Durieux, Fabio Maltoni, Ken Mimasu, Eleni Vryonidou & Cen Zhang, [arXiv:2008.11743](#)

The implementation is based on the Warsaw basis of dimension-six SMEFT operators, after canonical normalization. Electroweak input parameters are taken to be G_F , M_Z , M_W . The CKM matrix is approximated as a unit matrix, and a $U(2)_q \times U(2)_u \times U(3)_d \times (U(1)_l \times U(1)_e)^3$ flavor symmetry is enforced. It forbids all fermion masses and Yukawa couplings except that only of the top quark. The model therefore implements the five-flavor scheme for PDFs.

A new coupling order, `NP=2`, is assigned to SMEFT interactions. The cutoff scale `Lambda` takes a default value of 1 TeV^{-2} and can be modified along with the Wilson coefficients in the `param_card`. Operators definitions, normalisations and coefficient names in the UFO model are specified in [definitions.pdf](#) . The notations and normalizations of top-quark operator coefficients comply with the LHC TOP WG standards of [1802.07237](#). Note however that the flavor symmetry enforced here is slightly more restrictive than the baseline assumption there (see the [dim6top page](#) for more information). This model has been validated at tree level against the `dim6top` implementation (see [1906.12310](#) and the [comparison details](#)).

Current implementation

UFO model: [SMEFTatNLO_v1.0.tar.gz](#) 

The current implementation imposes CP conservation. In the quark sector, it focuses primarily on top-quark interactions. The light-quark current operator, qqHDH, uuHDH, ddHDH, with coefficients `cpq3i`, `cpqMi`, `cpu`, `cpd` are however included. The triple-gluon operator, with coefficient `cG`, is currently not available (see the loop-capable [GGG](#) implementation). Vertices including more than four scalars or four leptons are not included. Scalar and tensor `QQ11` operators, with coefficients `ct1S3`, `ct1T3`, and `cb1S3`, break our flavor symmetry assumption and are not available for one-loop computations. Top-quark flavor-changing interactions, not compatible with the imposed flavor symmetry, are not included (see the loop-capable [TopFCNC](#) implementation).

Unlike prescribed by the LHC TOP WG, the top quark chromomagnetic-dipole operator coefficient `ctG` is normalized with a factor of the strong coupling, g_s . This normalization factor temporarily ensures compatibility with the 2.X.X series of MadGraph5_aMC@NLO but may be dropped in the future. As with every other appearance of this coupling in MadGraph5_aMC@NLO, its value is renormalisation-group evolved to the QCD renormalization scale (set in the `run_card`).

```
MG5_aMC>import model SMEFTatNLO
MG5_aMC>generate p p > t t~ NP=2 [QCD]
MG5_aMC>output
MG5_aMC>launch
```

What's in there?

'Warsaw' basis

not 2499 operators!

[Grzadkowski et al.; JHEP 1010 (2010) 085]

X^3		φ^6 and $\varphi^4 D^2$		$\psi^2 \varphi^3$		$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
Q_G	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	Q_φ	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$	Q_{ll}	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	Q_{ee}	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	Q_{le}	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi\Box}$	$(\varphi^\dagger \varphi)\Box(\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$	$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{uu}	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{lu}	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
Q_W	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$	$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{dd}	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	Q_{ld}	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{\tilde{W}}$	$\varepsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$					$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	Q_{eu}	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	Q_{qe}	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
						$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	Q_{ed}	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
								$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
								$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
										$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$		$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		B-violating			
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_{\mu\nu}^A G^{A\mu\nu}$	Q_{eW}	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$	Q_{ledq}	$(\bar{l}_p^j e_r)(\bar{d}_s q_t^j)$	Q_{duq}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^\gamma)^T C l_t^k]$		
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	Q_{eB}	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$	$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	Q_{qqu}	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$		
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$	Q_{uG}	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$	$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	$Q_{qqq}^{(1)}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} \varepsilon_{mn} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^\gamma)^T C l_t^m]$		
$Q_{\varphi \tilde{W}}$	$\varphi^\dagger \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	Q_{uW}	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu q_r)$	$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{qqq}^{(3)}$	$\varepsilon^{\alpha\beta\gamma} (\tau^I \varepsilon)_{jk} (\tau^I \varepsilon)_{mn} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^\gamma)^T C l_t^m]$		
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	Q_{uB}	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{q}_p \tau^I \gamma^\mu q_r)$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$	Q_{dqu}	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$		
$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	Q_{dG}	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_p \gamma^\mu u_r)$						
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	Q_{dW}	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$						
$Q_{\varphi \tilde{W}B}$	$\varphi^\dagger \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	Q_{dB}	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$						

Some symmetries imposed to control parameter space

- CP, B and flavor conservation
- Top-specific flavour structure of 2 & 4 fermion operators

Flavor symmetry

Approximate flavor symmetry in the SM

- Broken by Yukawa interactions
- In the SMEFT, broken by: $\psi^2 X \varphi$, $\psi^2 \varphi^3$, $(\bar{L}R)(\bar{L}R)$, $(\bar{L}R)(\bar{R}L)$ & $\mathcal{O}_{\varphi ud}$
- Any off-diagonal or non-universal entries of other 2F operators

SMEFTatNLO: minimal extension to single out top quark

universal $U(3)_L \times U(3)_e \times U(3)_Q \times U(3)_u \times U(3)_d$
 top $U(3)_L \times U(3)_e \times U(2)_Q \times U(2)_u \times U(3)_d$ *cf. Minimal flavor violation*

Yukawa	$\psi^2 H^3 : (\varphi^\dagger \varphi)^2 (\bar{Q} t \tilde{\varphi})$
Dipoles	$\psi^2 X H : (\bar{Q} \sigma^{\mu\nu} t \tilde{\varphi}) B_{\mu\nu} [W_{\mu\nu}^I, G_{\mu\nu}^a]$
3rd gen. currents	$\psi^2 H^2 D : (\varphi^\dagger \overleftrightarrow{D}_\mu \varphi) (\bar{Q} \gamma^\mu Q) [(\bar{Q} \gamma^\mu \tau^I Q), (\bar{t} \gamma^\mu t), \dots]$
3rd gen. 4F	$\psi^4 : (\bar{Q} \gamma^\mu Q) (\bar{q} \gamma_\mu q), (\bar{Q} \gamma^\mu Q) (\bar{Q} \gamma_\mu Q), \dots$

See Dim6top

[Aguilar-Saavedra et al.; arXiv:1802.07237]

What's in there?

Bosonic operators of the Warsaw basis

Top-specific flavour structures

- Chirality-flipping interactions involving Q_3 & t_R
- Bottom quark chirality-flipping interactions not present (b_R)
- Chirality-conserving interactions: universal gen. 1 & 2 + 3rd gen

$$[\mathcal{O}_{\varphi q}^{(3)}] \rightarrow [\mathcal{O}_{\varphi q}^{(3)}]^{j,j} \text{ and } [\mathcal{O}_{\varphi q}^{(3)}]^{3,3} = \{ \mathcal{O}_{\varphi q_i}^{(3)}, \mathcal{O}_{\varphi Q}^{(3)} \}$$

$$[\mathcal{O}_{\varphi u}] \rightarrow [\mathcal{O}_{\varphi u}]^{j,j} \text{ and } [\mathcal{O}_{\varphi u}]^{3,3} = \{ \mathcal{O}_{\varphi u_i}, \mathcal{O}_{\varphi t} \}$$

- four-fermions: 2-heavy-2-light & 4-heavy (no 4-light)

Lepton sector: $[U(1)_L \times U(1)_e]^3$, flavor diagonal (e, μ, τ)

Conventions match [dim6top](#), where relevant

See [definitions.pdf](#) on webpage for more details

[CMS-PAS-TOP-001]

ttH, ttZ, ttW,
tW, tZ, tH

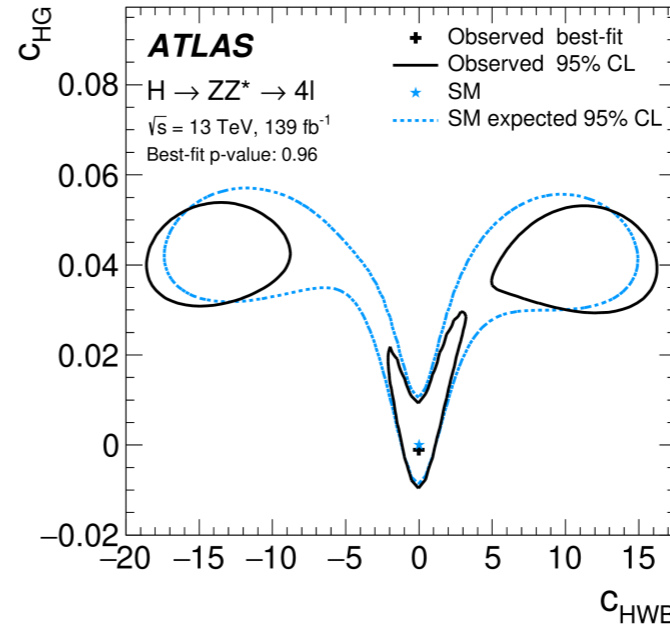
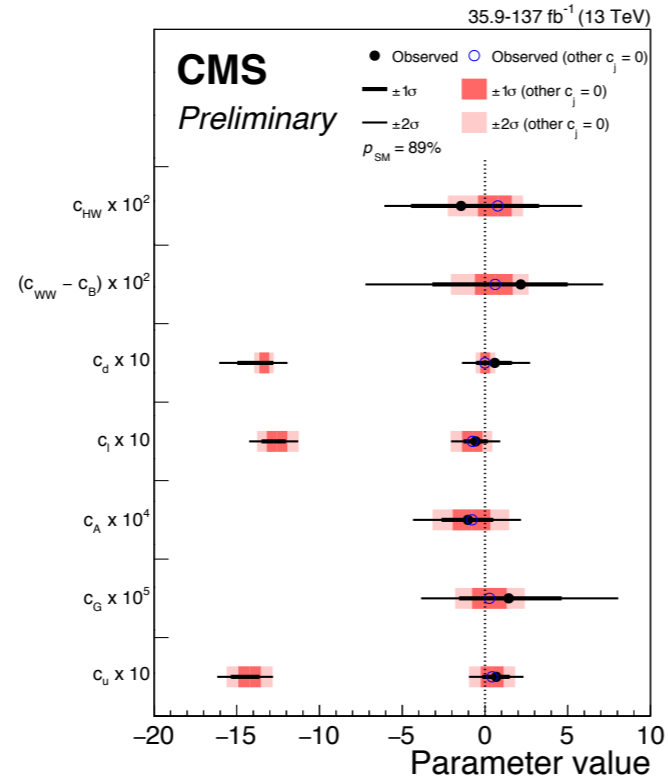
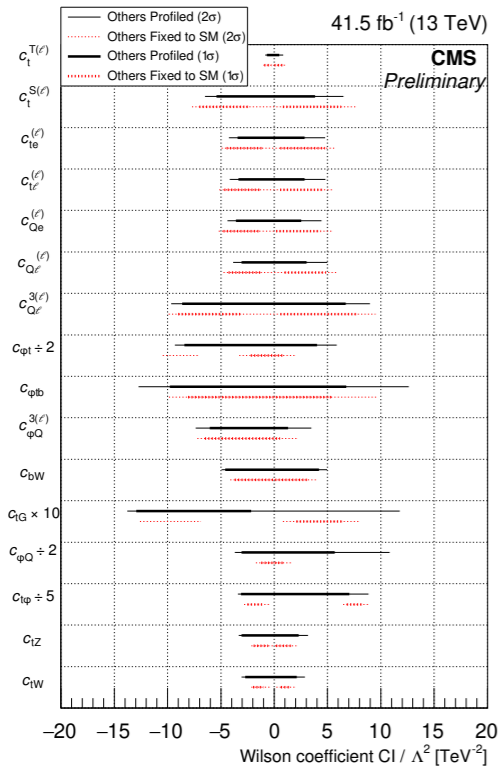
[CMS-PAS-HIG-19-005]

Higgs combination

[CERN-EP-2020-034]

$H \rightarrow 4l$

NLO QCD
OK ✓



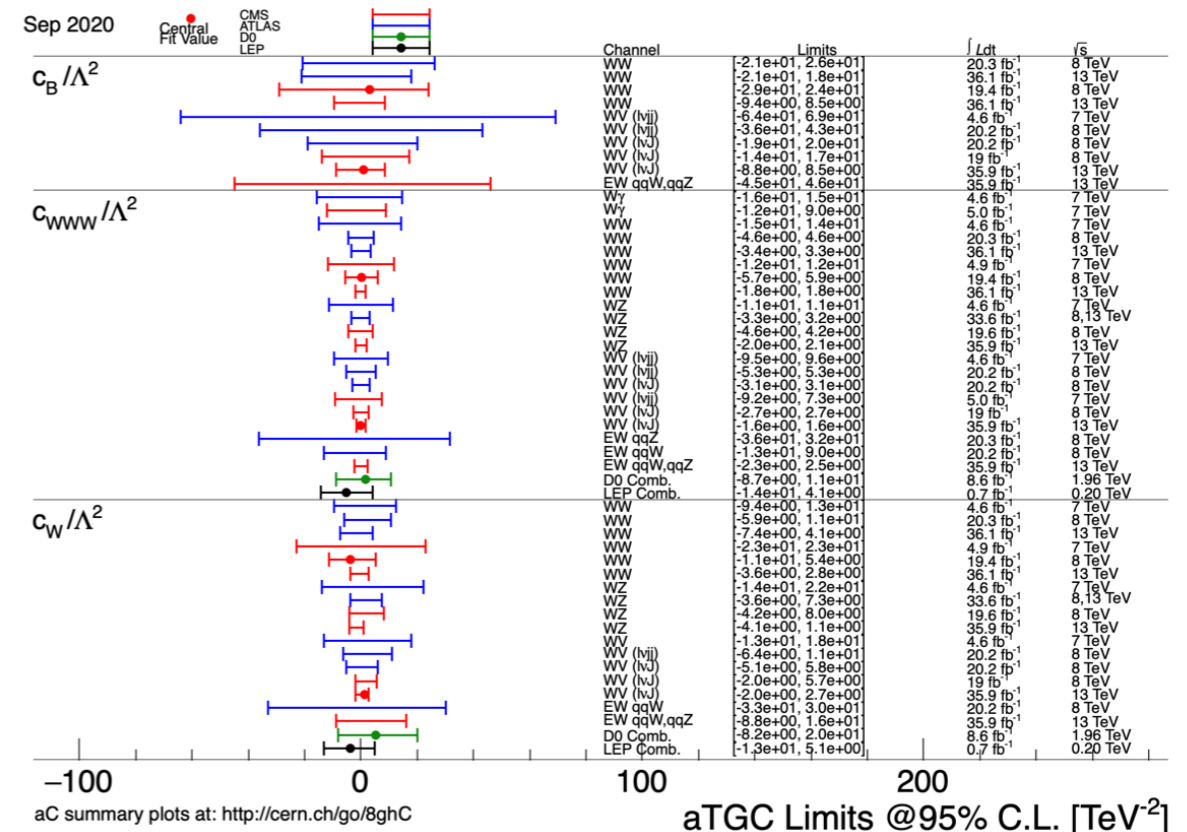
hh (LO),
VVV,
VBS,
tt,
4top,
...

WW & WZ

[ATLAS; PRD 99 (2017) 072009]

ttV

Coefficients	$C_{\phi Q}^{(3)}/\Lambda^2$	$C_{\phi t}/\Lambda^2$	C_{tB}/Λ^2	C_{tW}/Λ^2
Previous indirect constraints at 68% CL	[-4.7, 0.7]	[-0.1, 3.7]	[-0.5, 10]	[-1.6, 0.8]
Previous direct constraints at 95% CL	[-1.3, 1.3]	[-9.7, 8.3]	[-6.9, 4.6]	[-0.2, 0.7]
Expected limit at 68% CL	[-2.1, 1.9]	[-3.8, 2.7]	[-2.9, 3.0]	[-1.8, 1.9]
Expected limit at 95% CL	[-4.5, 3.6]	[-23, 4.9]	[-4.2, 4.3]	[-2.6, 2.6]
Observed limit at 68% CL	[-1.0, 2.7]	[-2.0, 3.5]	[-3.7, 3.5]	[-2.2, 2.1]
Observed limit at 95% CL	[-3.3, 4.2]	[-25, 5.5]	[-5.0, 5.0]	[-2.9, 2.9]
Expected limit at 68% CL (linear)	[-1.9, 2.0]	[-3.0, 3.2]	-	-
Expected limit at 95% CL (linear)	[-3.7, 4.0]	[-5.8, 6.3]	-	-
Observed limit at 68% CL (linear)	[-1.0, 2.9]	[-1.8, 4.4]	-	-
Observed limit at 95% CL (linear)	[-2.9, 4.9]	[-4.8, 7.5]	-	-



Selected results

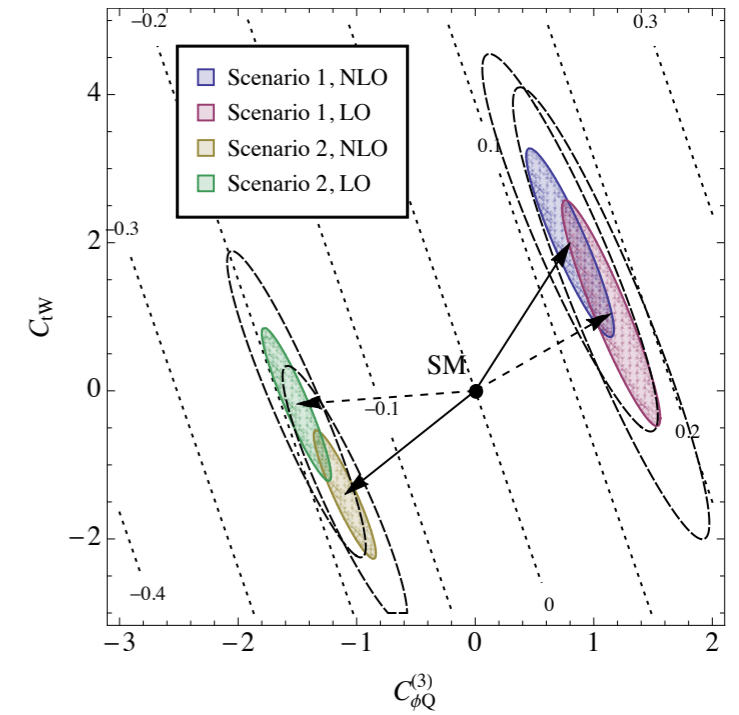
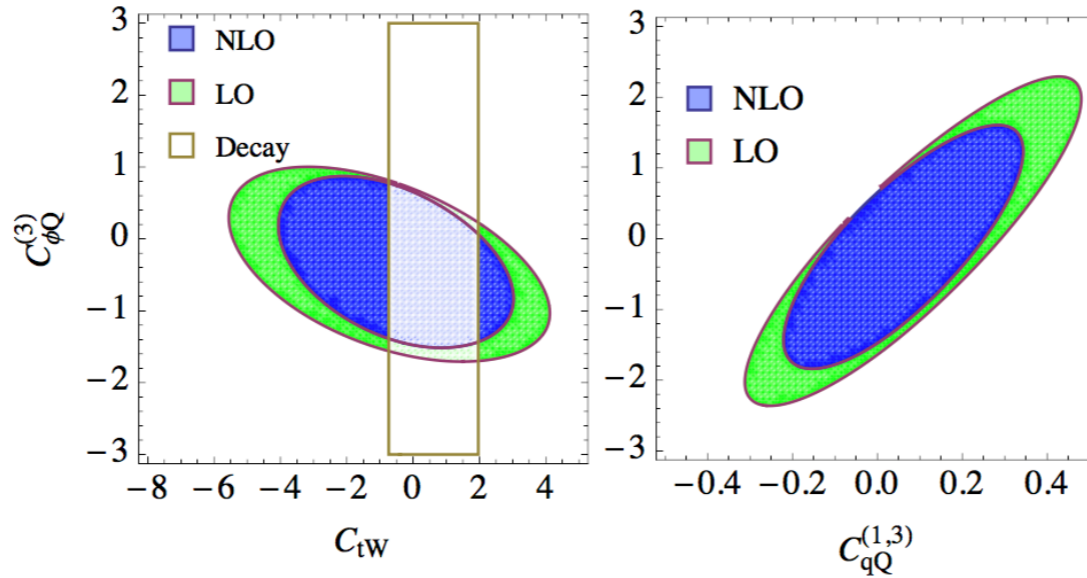
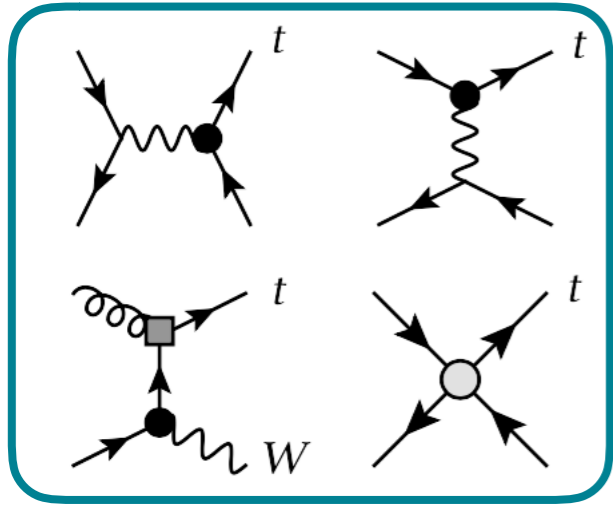
Some from previous works, superseded by SMEFT@NLO
A few, simple new results presented in 2008.11743

Single top

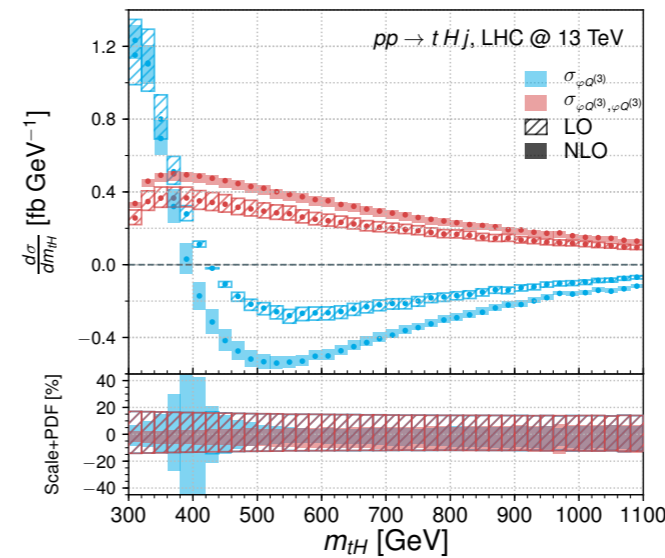
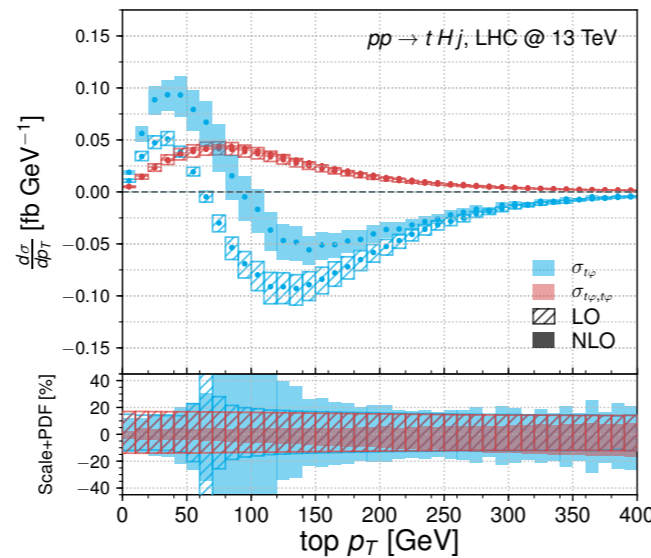
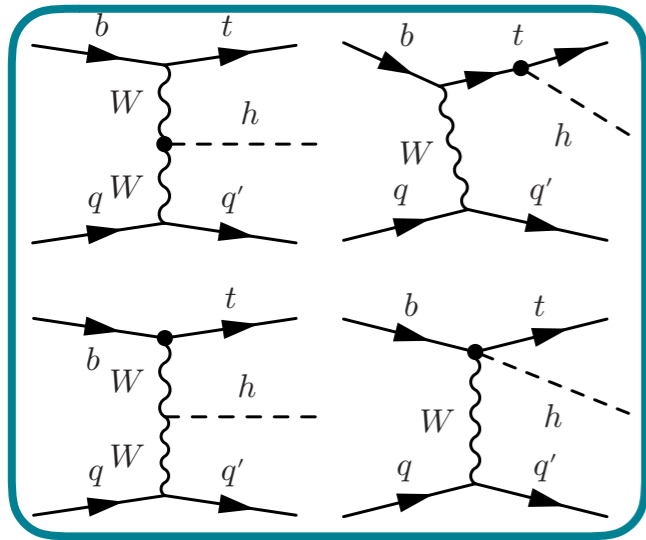
[Zhang; PRL 116 (2016) 162002]

Fit without deviation

Fit with a (hypothetical) deviation



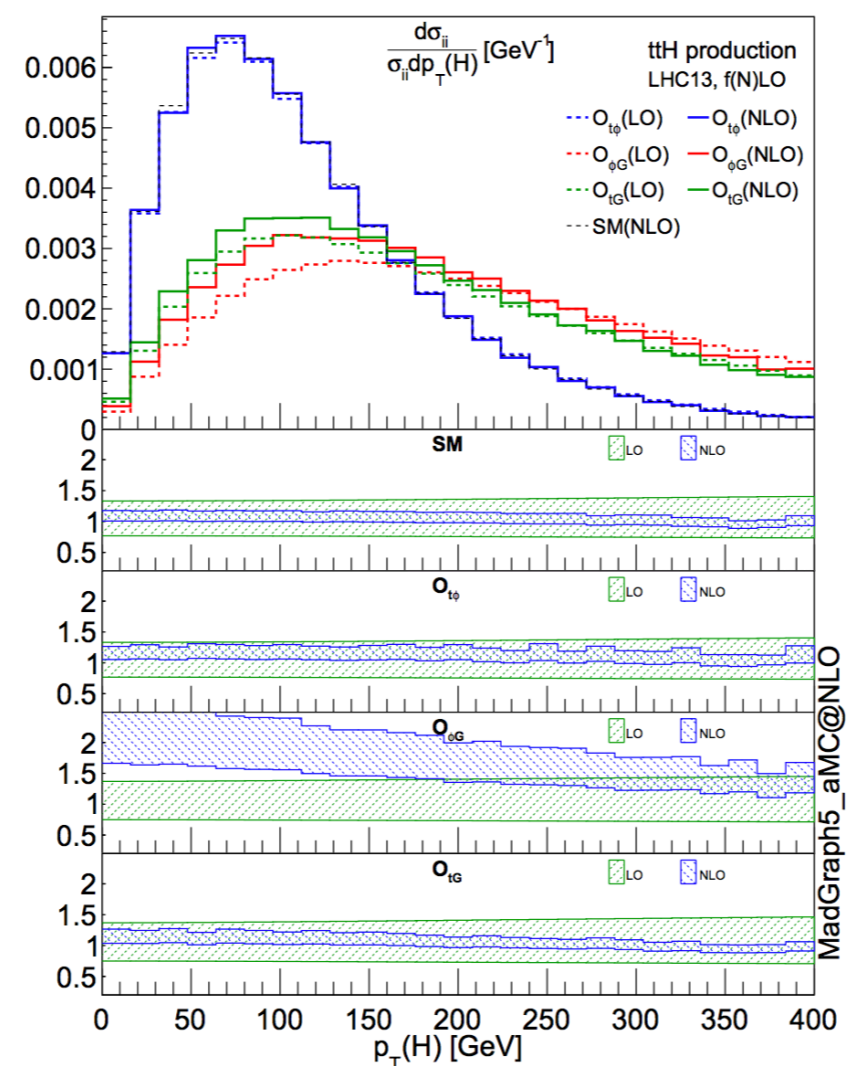
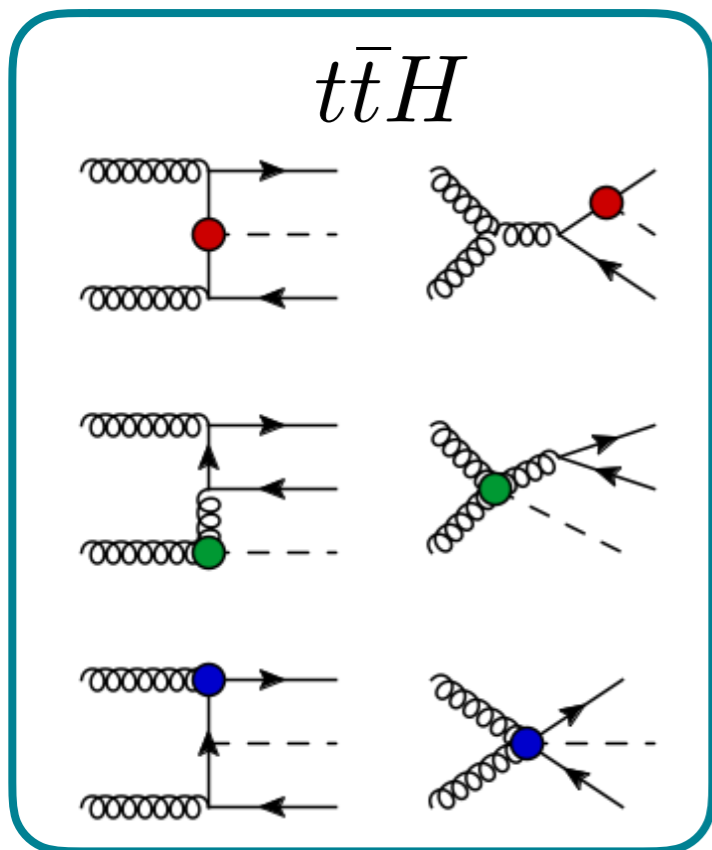
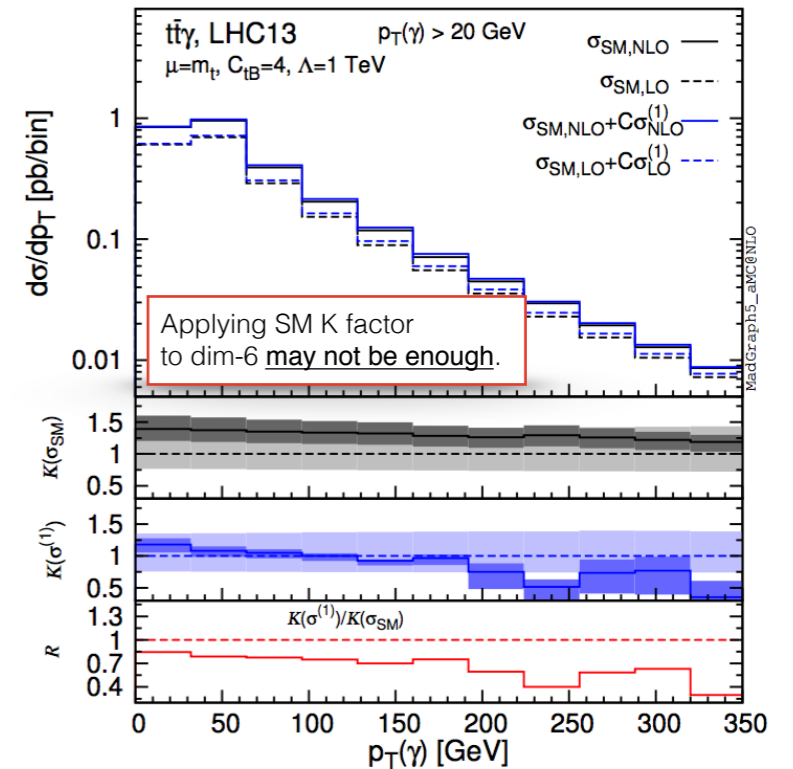
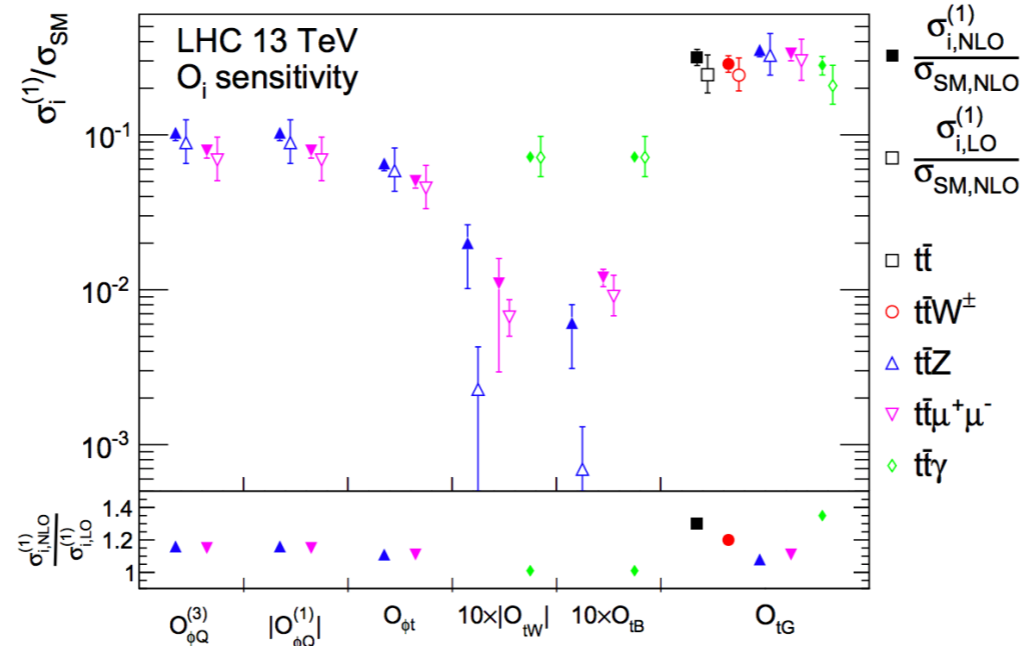
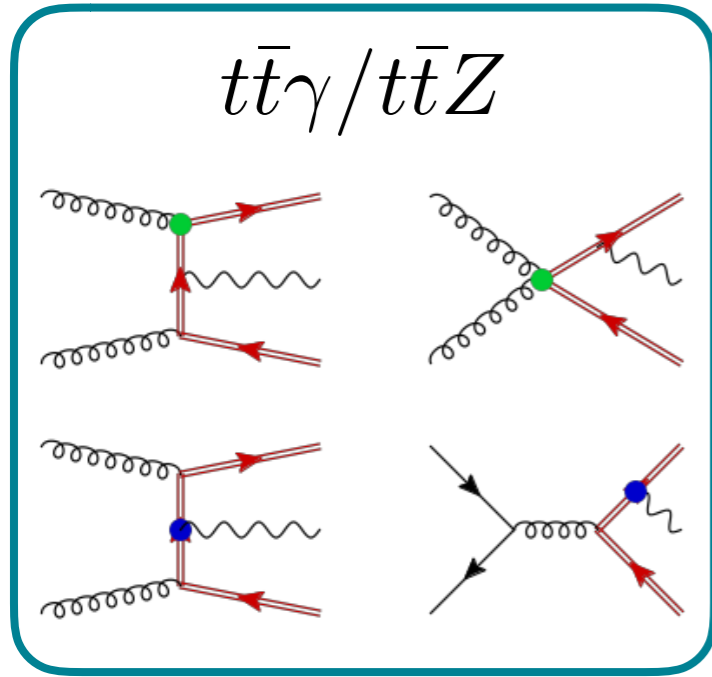
[Degrande et al.; JHEP 10 (2018) 005]



tZj & tHj

Different patterns of phase-space cancellations at LO/NLO lead to non-trivial & strange K factors

σ [fb]	K-factor
σ_{SM}	1.32
$\sigma_{\phi W}$	0.96
$\sigma_{\phi W, \phi W}$	1.20
$\sigma_{t\phi}$	0.20
$\sigma_{t\phi, t\phi}$	1.09
σ_{tW}	1.14
$\sigma_{tW, tW}$	1.54
$\sigma_{\phi Q^{(3)}}$	3.31
$\sigma_{\phi Q^{(3)}, \phi Q^{(3)}}$	1.36



13 TeV	σ LO	σ NLO	K
σ _{SM}	0.464 ^{+0.161} _{-0.111}	0.507 ^{+0.03} _{-0.04}	1.09
σ _{tϕ}	-0.055 ^{+0.0} _{-0.0}	-0.062 ^{+0.0} _{-0.0}	1.13
σ _{ϕG}	0.627 ^{+0.228} _{-0.153}	0.872 ^{+0.13} _{-0.12}	1.39
σ _{tG}	0.470 ^{+0.167} _{-0.114}	0.503 ^{+0.02} _{-0.04}	1.07
σ _{tϕ,tϕ}	0.0016 ^{+0.00} _{-0.00}	0.0019 ^{+0.0} _{-0.0}	1.17
σ _{ϕG,ϕG}	0.646 ^{+0.274} _{-0.178}	1.021 ^{+0.20} _{-0.17}	1.58
σ _{tG,tG}	0.645 ^{+0.276} _{-0.178}	0.674 ^{+0.03} _{-0.06}	1.04
σ _{tϕ,ϕG}	-0.037 ^{+0.0} _{-0.0}	-0.053 ^{+0.0} _{-0.0}	1.42
σ _{tϕ,tG}	-0.028 ^{+0.0} _{-0.0}	-0.031 ^{+0.0} _{-0.0}	1.10
σ _{ϕG,tG}	0.627 ^{+0.252} _{-0.166}	0.859 ^{+0.12} _{-0.12}	1.37

Non-universal K-factors in rates & distributions

4F in top pair

LHC 13 TeV, SM = 744 pb, K-factor = 1.46

color-octet $qqtt$:

dominant operators in $t\bar{t}$

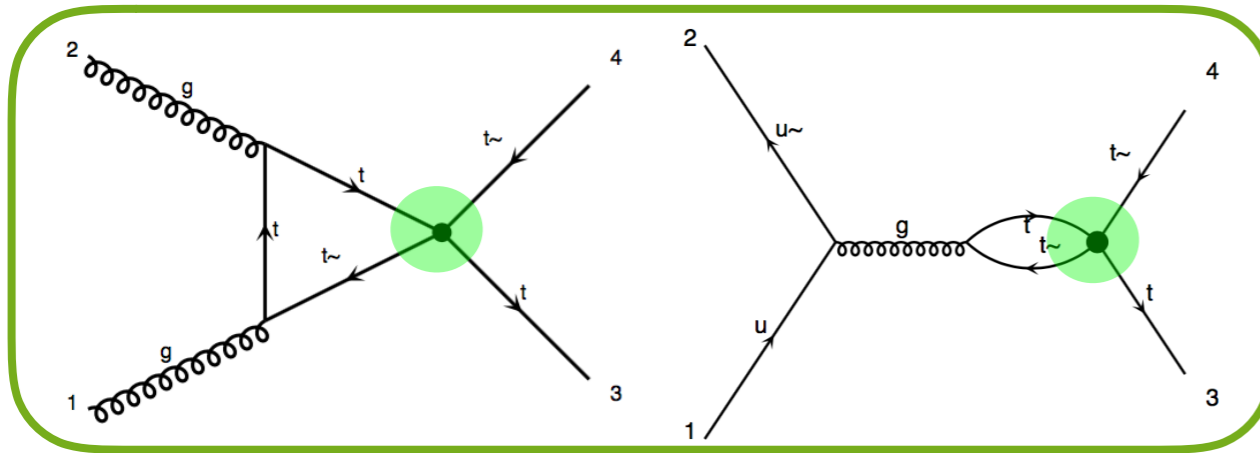
NLO corrections can break degeneracies

color-singlet $qqtt$:

interference with QCD $t\bar{t}$ at NLO

[x] interference with EW $t\bar{t}$

4-top operators: loop-induced sensitivity



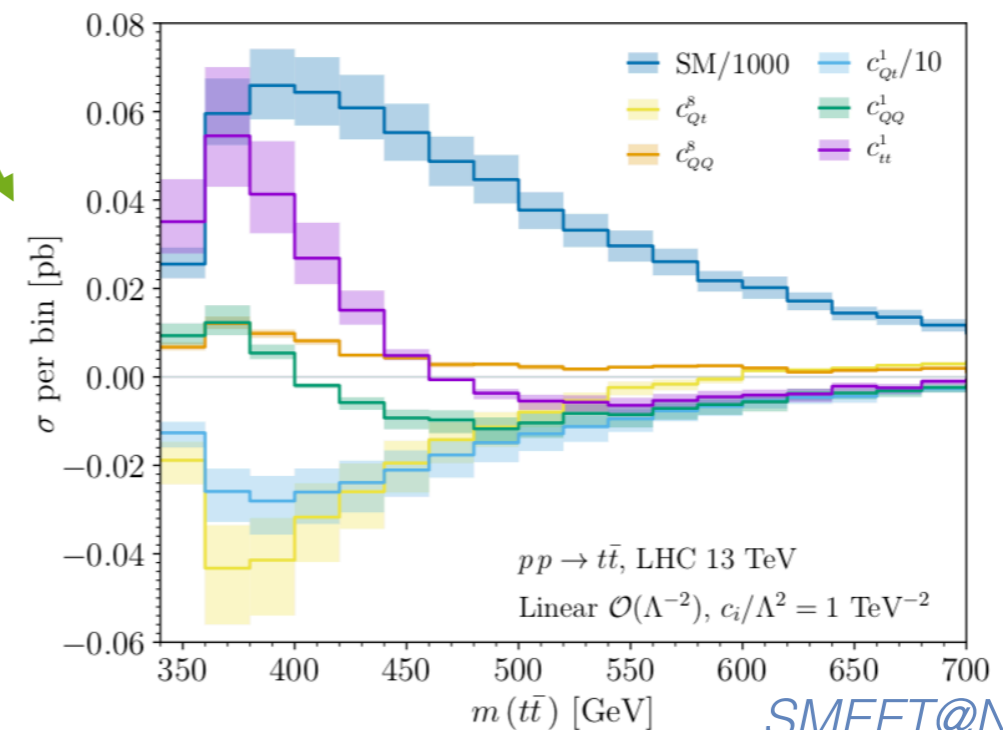
some operators (Q) have a bb -initiated contribution

4-top interference in $t\bar{t}$:

pattern of cancellations at differential level

competition between phase space & gg, bb

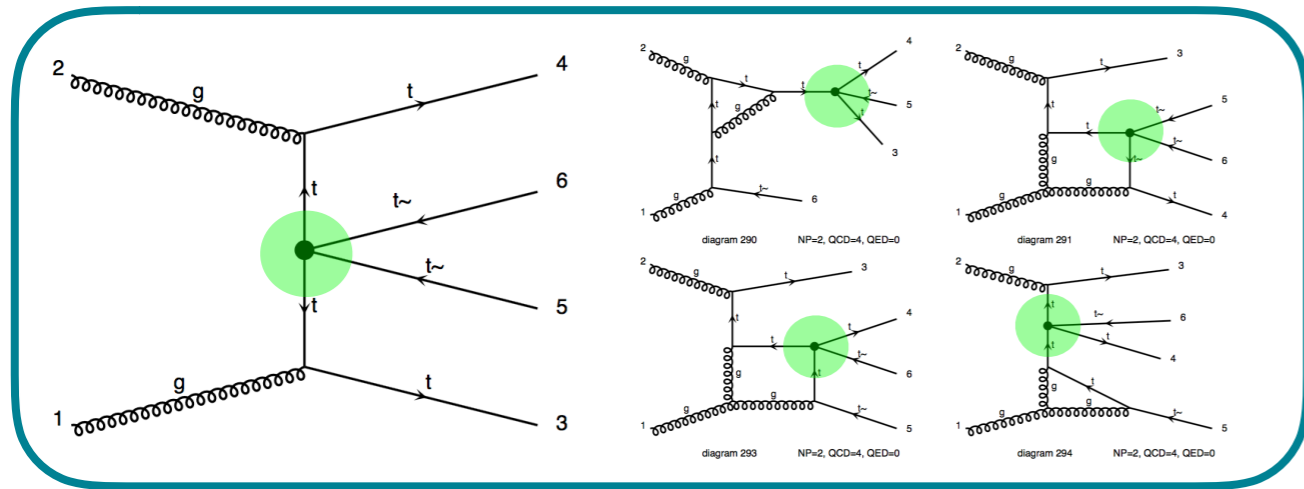
c_i	$\mathcal{O}(\Lambda^{-2})$		$\mathcal{O}(\Lambda^{-4})$	
	LO	NLO	LO	NLO
c_{tu}^8	$4.27^{+11\%}_{-9\%}$	$4.06^{+1\%}_{-3\%}$	$1.04^{+6\%}_{-5\%}$	$1.03^{+2\%}_{-2\%}$
c_{td}^8	$2.79^{+11\%}_{-9\%}$	$2.77^{+1\%}_{-3\%}$	$0.577^{+6\%}_{-5\%}$	$0.611^{+3\%}_{-2\%}$
c_{tq}^8	$6.99^{+11\%}_{-9\%}$	$6.67^{+1\%}_{-3\%}$	$1.61^{+6\%}_{-5\%}$	$1.29^{+3\%}_{-2\%}$
c_{Qu}^8	$4.26^{+11\%}_{-9\%}$	$3.93^{+1\%}_{-4\%}$	$1.04^{+6\%}_{-5\%}$	$0.798^{+3\%}_{-3\%}$
c_{Qd}^8	$2.79^{+11\%}_{-9\%}$	$2.93^{+0\%}_{-1\%}$	$0.58^{+6\%}_{-5\%}$	$0.485^{+2\%}_{-2\%}$
$c_{Qq}^{8,1}$	$6.99^{+11\%}_{-9\%}$	$6.82^{+1\%}_{-3\%}$	$1.61^{+6\%}_{-5\%}$	$1.69^{+3\%}_{-3\%}$
$c_{Qq}^{8,3}$	$1.50^{+10\%}_{-9\%}$	$1.32^{+1\%}_{-3\%}$	$1.61^{+6\%}_{-5\%}$	$1.57^{+2\%}_{-2\%}$
c_{tu}^1	$[0.67^{+1\%}_{-1\%}]$	$-0.078(7)^{+31\%}_{-23\%}$	$[0.41^{+13\%}_{-17\%}]$	$4.66^{+6\%}_{-5\%}$
c_{td}^1	$[-0.21^{+1\%}_{-2\%}]$	$-0.306^{+30\%}_{-22\%}$	$[-0.15^{+10\%}_{-13\%}]$	$2.62^{+6\%}_{-5\%}$
c_{tq}^1	$[0.39^{+0\%}_{-1\%}]$	$-0.47^{+24\%}_{-18\%}$	$[0.50^{+3\%}_{-2\%}]$	$7.25^{+6\%}_{-5\%}$
c_{Qu}^1	$[0.33^{+0\%}_{-0\%}]$	$-0.359^{+23\%}_{-17\%}$	$[0.57^{+6\%}_{-5\%}]$	$4.68^{+6\%}_{-5\%}$
c_{Qd}^1	$[-0.11^{+0\%}_{-1\%}]$	$0.023(6)^{+114\%}_{-75\%}$	$[-0.19^{+6\%}_{-5\%}]$	$2.61^{+6\%}_{-5\%}$
$c_{Qq}^{1,1}$	$[0.57^{+0\%}_{-1\%}]$	$-0.24^{+30\%}_{-22\%}$	$[0.39^{+9\%}_{-12\%}]$	$7.25^{+6\%}_{-5\%}$
$c_{Qq}^{1,3}$	$[1.92^{+1\%}_{-1\%}]$	$0.088(7)^{+28\%}_{-20\%}$	$[1.05^{+17\%}_{-22\%}]$	$7.25^{+6\%}_{-5\%}$
c_{QQ}^8	$0.0586^{+27\%}_{-25\%}$	$0.125^{+10\%}_{-11\%}$	$0.00628^{+13\%}_{-16\%}$	$0.0133^{+7\%}_{-5\%}$
c_{Qt}^8	$0.0583^{+27\%}_{-25\%}$	$-0.107(6)^{+40\%}_{-33\%}$	$0.00619^{+13\%}_{-16\%}$	$0.0118^{+8\%}_{-5\%}$
c_{QQ}^1	$[-0.11^{+15\%}_{-18\%}]$	$-0.039(4)^{+51\%}_{-33\%}$	$[-0.12^{+7\%}_{-5\%}]$	$0.0282^{+13\%}_{-16\%}$
c_{Qt}^1	$[-0.068^{+16\%}_{-18\%}]$	$-2.51^{+29\%}_{-21\%}$	$[-0.12^{+3\%}_{-6\%}]$	$0.0651^{+5\%}_{-6\%}$
c_{tt}^1	\times	$0.215^{+23\%}_{-18\%}$	\times	\times



4-top

[SMEFT@NLO; arXiv:2008.11743]

! computation time warning !



c_i	$\mathcal{O}(\Lambda^{-2})$			$\mathcal{O}(\Lambda^{-4})$		
	LO	NLO	K	LO	NLO	K
c_{QQ}^8	$0.126^{+61\%}_{-35\%}$	$0.089^{+8\%}_{-66\%}$	0.71	$0.170^{+53\%}_{-32\%}$	$0.165^{+3\%}_{-26\%}$	0.97
c_{Qt}^8	$0.421^{+63\%}_{-35\%}$	$0.295^{+9\%}_{-69\%}$	0.70	$0.498^{+52\%}_{-32\%}$	$0.333^{+15\%}_{-75\%}$	0.67
c_{QQ}^1	$0.373^{+62\%}_{-35\%}$	$0.20(1)^{+23\%}_{-115\%}$	0.53	$1.513^{+53\%}_{-32\%}$	$1.40^{+3\%}_{-32\%}$	0.93
c_{Qt}^1	$-0.007(1)^{+88\%}_{-84\%}$	$-0.14(3)^{+83\%}_{-40\%}$	21	$2.061^{+53\%}_{-32\%}$	$1.89^{+3\%}_{-33\%}$	0.92
c_{tt}^1	$0.741^{+61\%}_{-35\%}$	$0.42(3)^{+18\%}_{-101\%}$	0.57	$6.08^{+53\%}_{-32\%}$	$5.65^{+3\%}_{-30\%}$	0.93

LHC 13 TeV, SM = 13.9 pb, K-factor = 1.37

Interference K-factors mainly $\ll 1$

Quadratic < 1

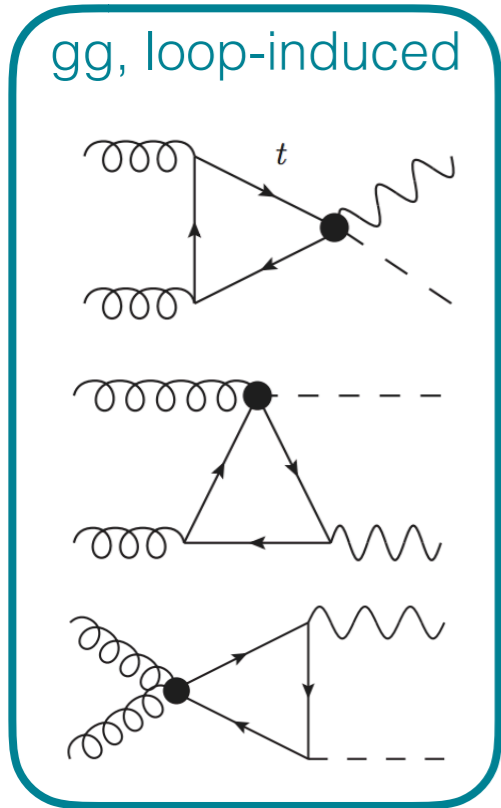
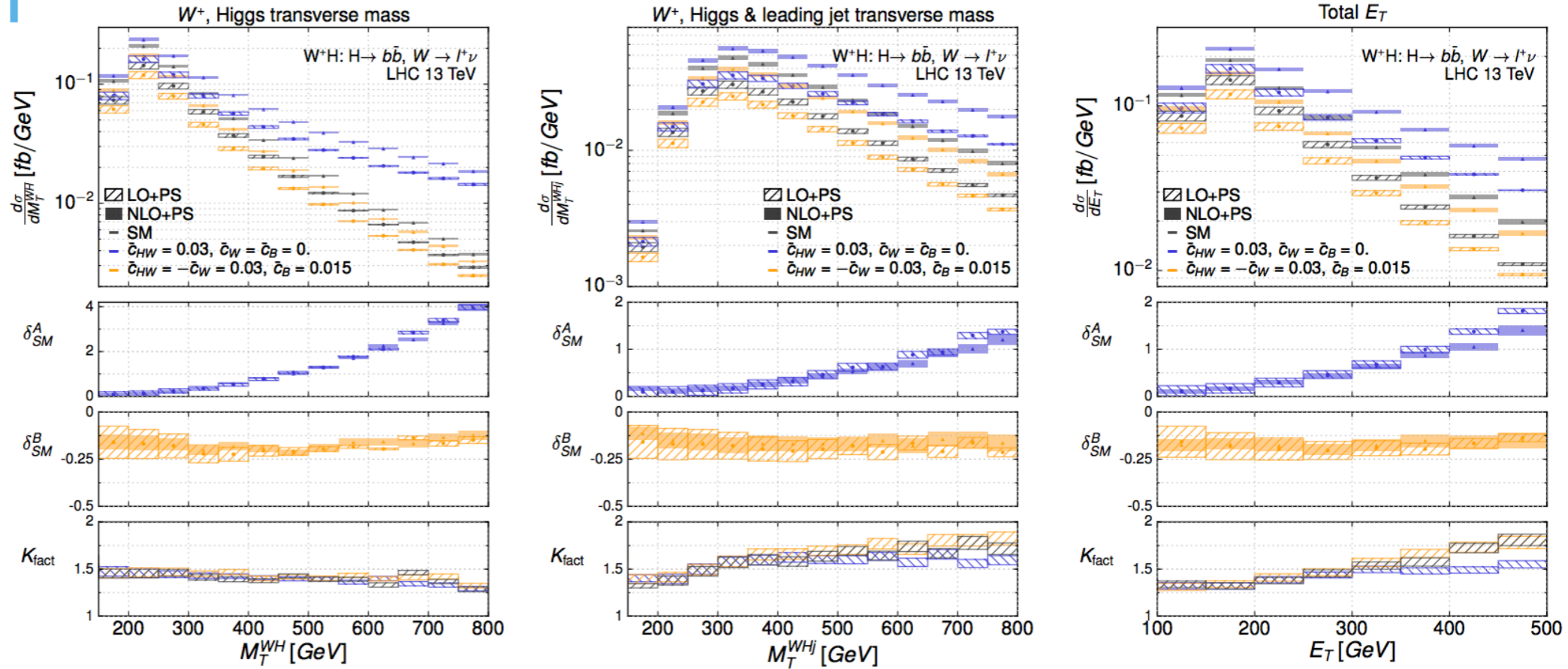
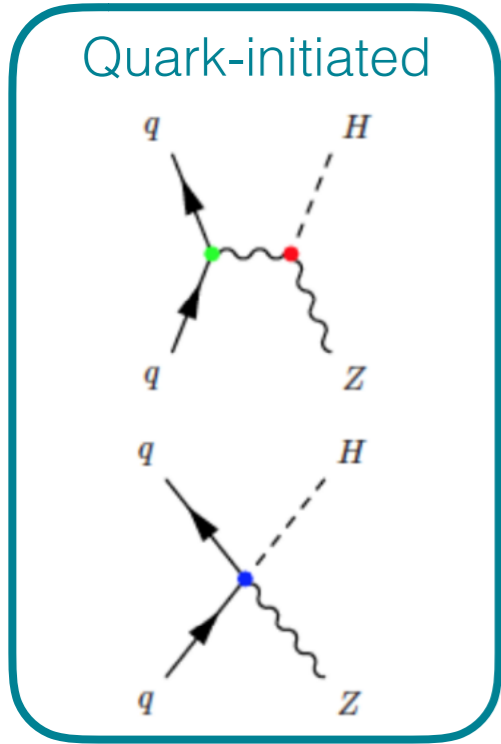
Recent 4.3(2.6) sigma evidence reported by ATLAS(CMS)

- Actually an excess, $\mu \sim 2$ [ATLAS-CONF-2020-013] [CMS; EPJC 80 (2020) 2, 75]
- Current limits on 4-top operators $\sim |C| < 2-5 (1 \text{ TeV})^2/\Lambda^2$ [CMS; JHEP 11 (2019) 082]
- Dominated by EFT² quadratic term
- Room for complementarity from loop-induced top pair effects

Operator	Expected C_k/Λ^2 (TeV ⁻²)	Observed (TeV ⁻²)
\mathcal{O}_{tt}^1	[-2.0, 1.9]	[-2.2, 2.1]
\mathcal{O}_{QQ}^1	[-2.0, 1.9]	[-2.2, 2.0]
\mathcal{O}_{Qt}^1	[-3.4, 3.3]	[-3.7, 3.5]
\mathcal{O}_{Qt}^8	[-7.4, 6.3]	[-8.0, 6.8]

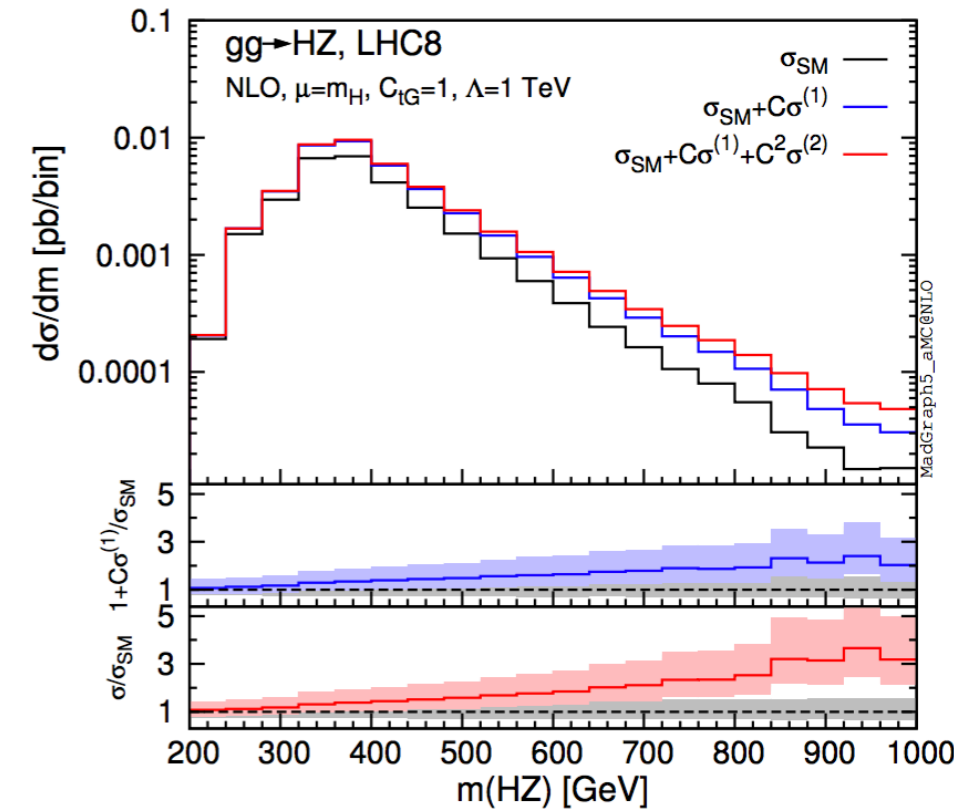
pp → ZH

[Degrande, et al.; EPJC 77 (2017) 4, 262]

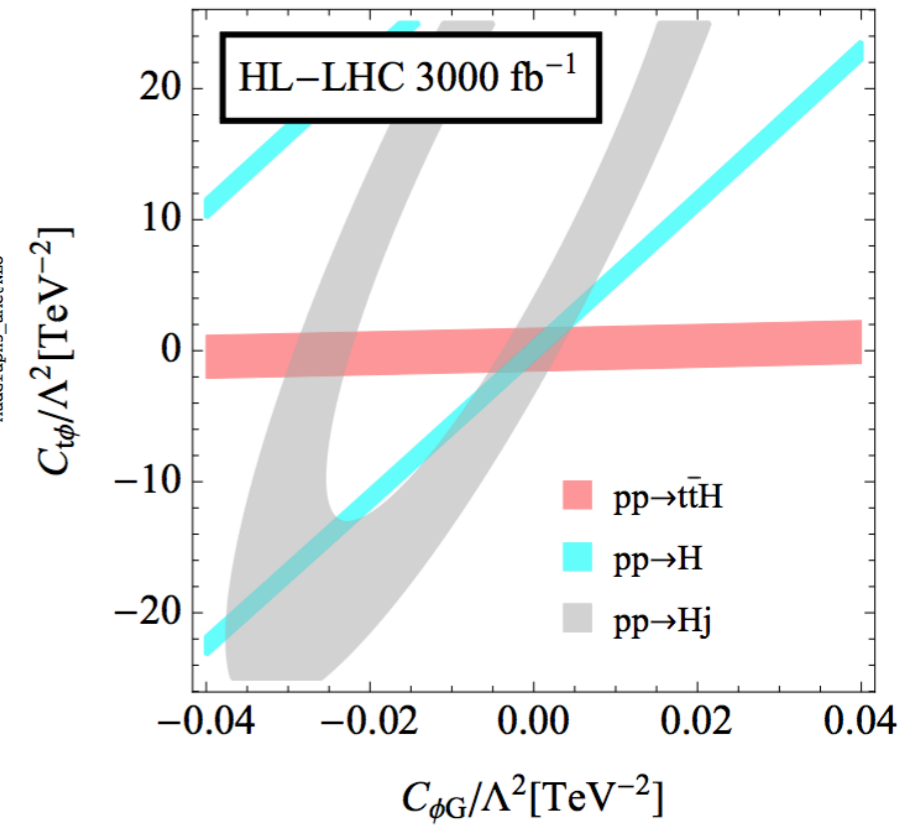
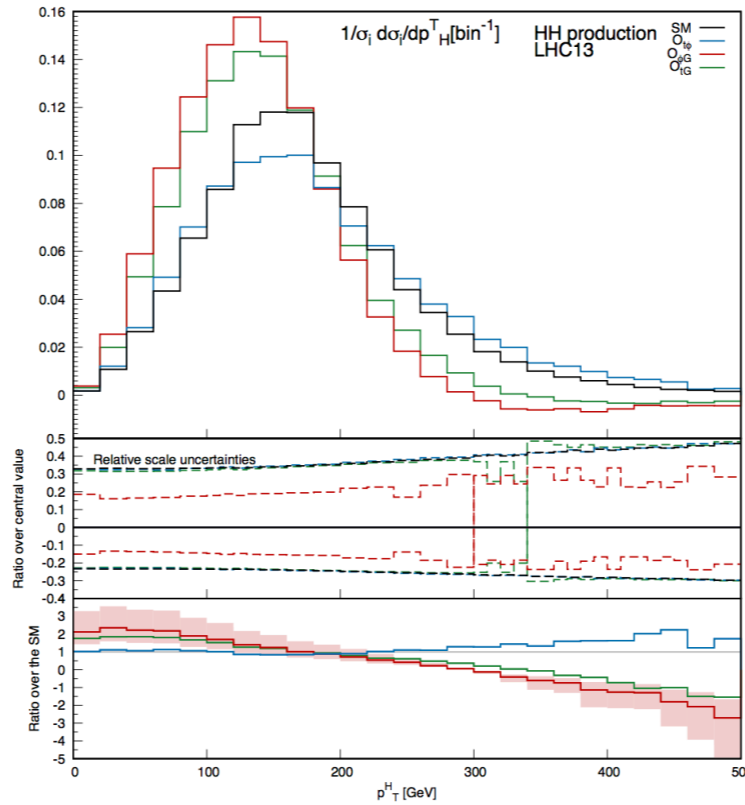
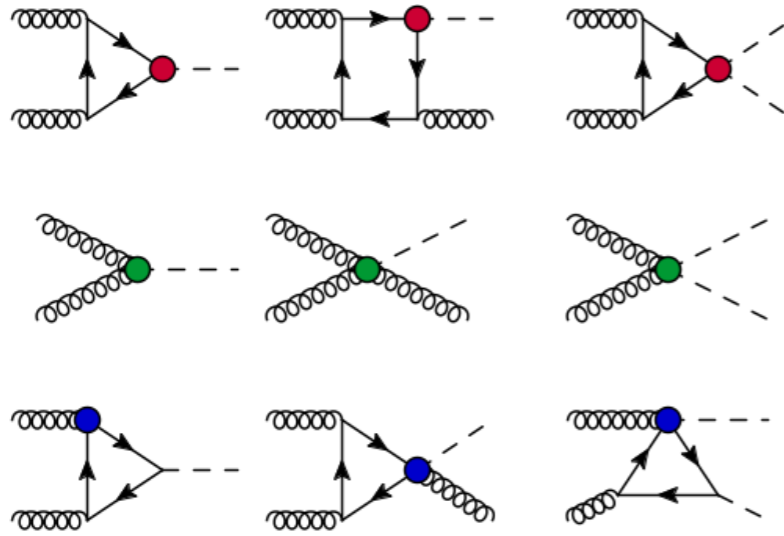


[Bylund et al.; JHEP 1605 (2016) 052]

[fb]	SM		\mathcal{O}_{tG}	$\mathcal{O}_{\phi Q}^{(1)}$
8TeV	$29.15^{+40.0\%}_{-26.6\%}$	$\sigma_i^{(1)}$	$10.37^{+41.3\%}_{-27.2\%}$	$1.719^{+42.5\%}_{-27.6\%}$
		$\sigma_i^{(2)}$	$1.621^{+45.1\%}_{-28.7\%}$	$0.0469^{+46.5\%}_{-29.2\%}$
		$\sigma_i^{(1)}/\sigma_{SM}$	$0.356^{+0.9\%}_{-0.8\%}$	$0.0590^{+1.8\%}_{-1.4\%}$
		$\sigma_i^{(2)}/\sigma_i^{(1)}$	$0.156^{+2.6\%}_{-2.0\%}$	$0.0273^{+2.8\%}_{-2.3\%}$
		13TeV	$93.6^{+34.3\%}_{-23.8\%}$	$\sigma_i^{(1)}$
$\sigma_i^{(2)}$	$6.09^{+39.2\%}_{-26.1\%}$			$0.182^{+40.2\%}_{-26.6\%}$
$\sigma_i^{(1)}/\sigma_{SM}$	$0.370^{+0.7\%}_{-0.9\%}$			$0.0631^{+1.6\%}_{-1.5\%}$
$\sigma_i^{(2)}/\sigma_i^{(1)}$	$0.176^{+2.9\%}_{-2.1\%}$			$0.0309^{+2.8\%}_{-2.2\%}$

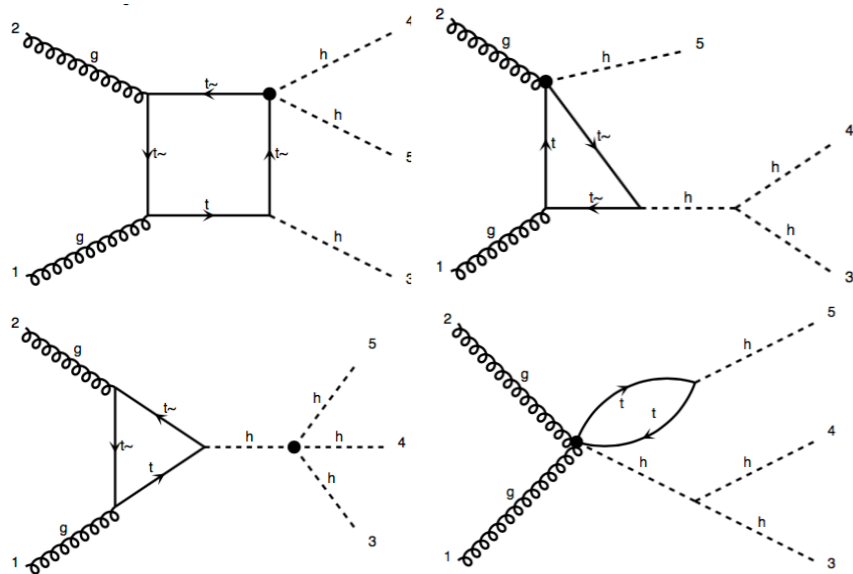


loop-sensitivity, $gg \rightarrow H/Hj/HH$

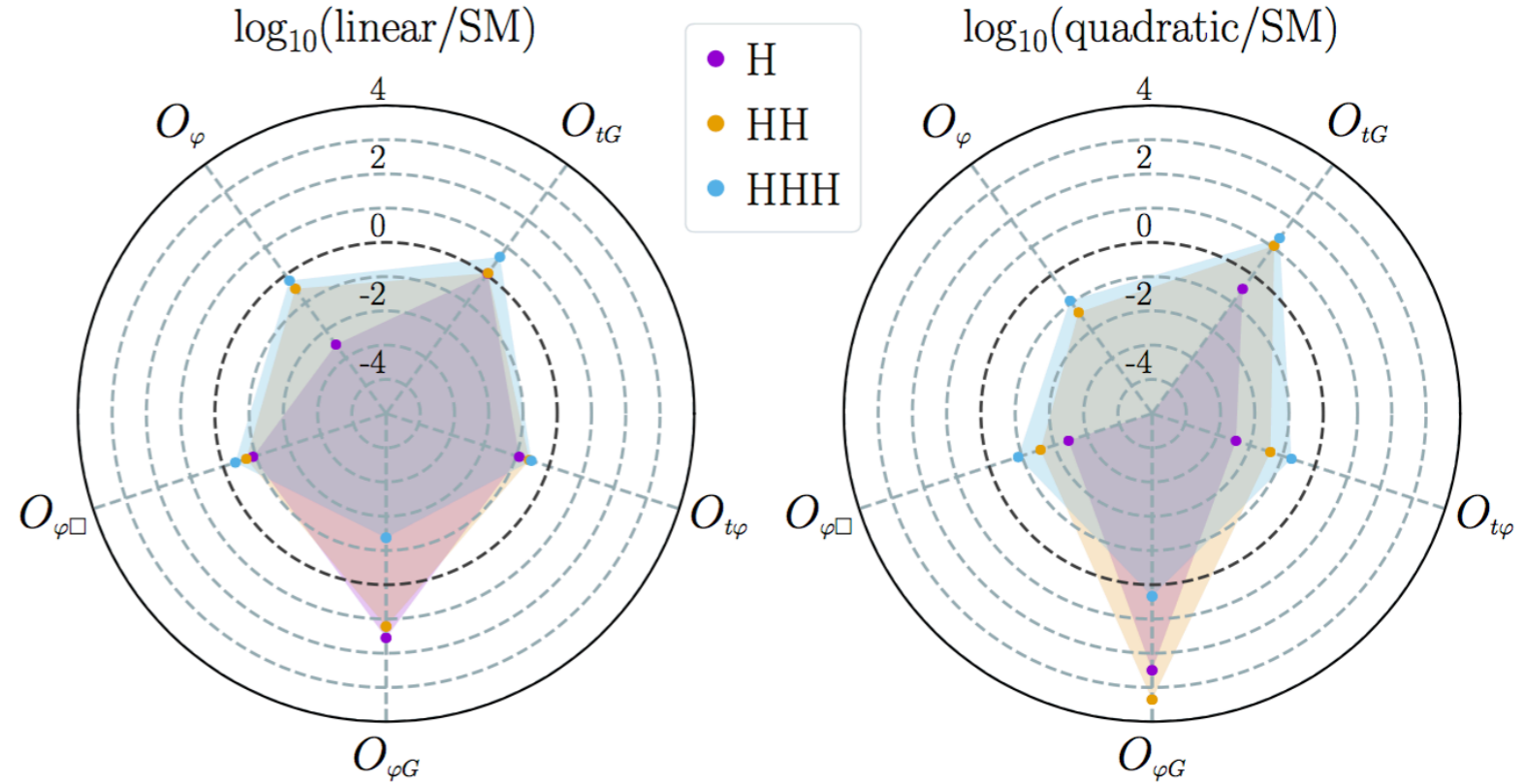


[Maltoni, Vryonidou & Zhang; JHEP 1610 (2016) 123]

$gg \rightarrow H/HH/HHH$ (100 TeV)



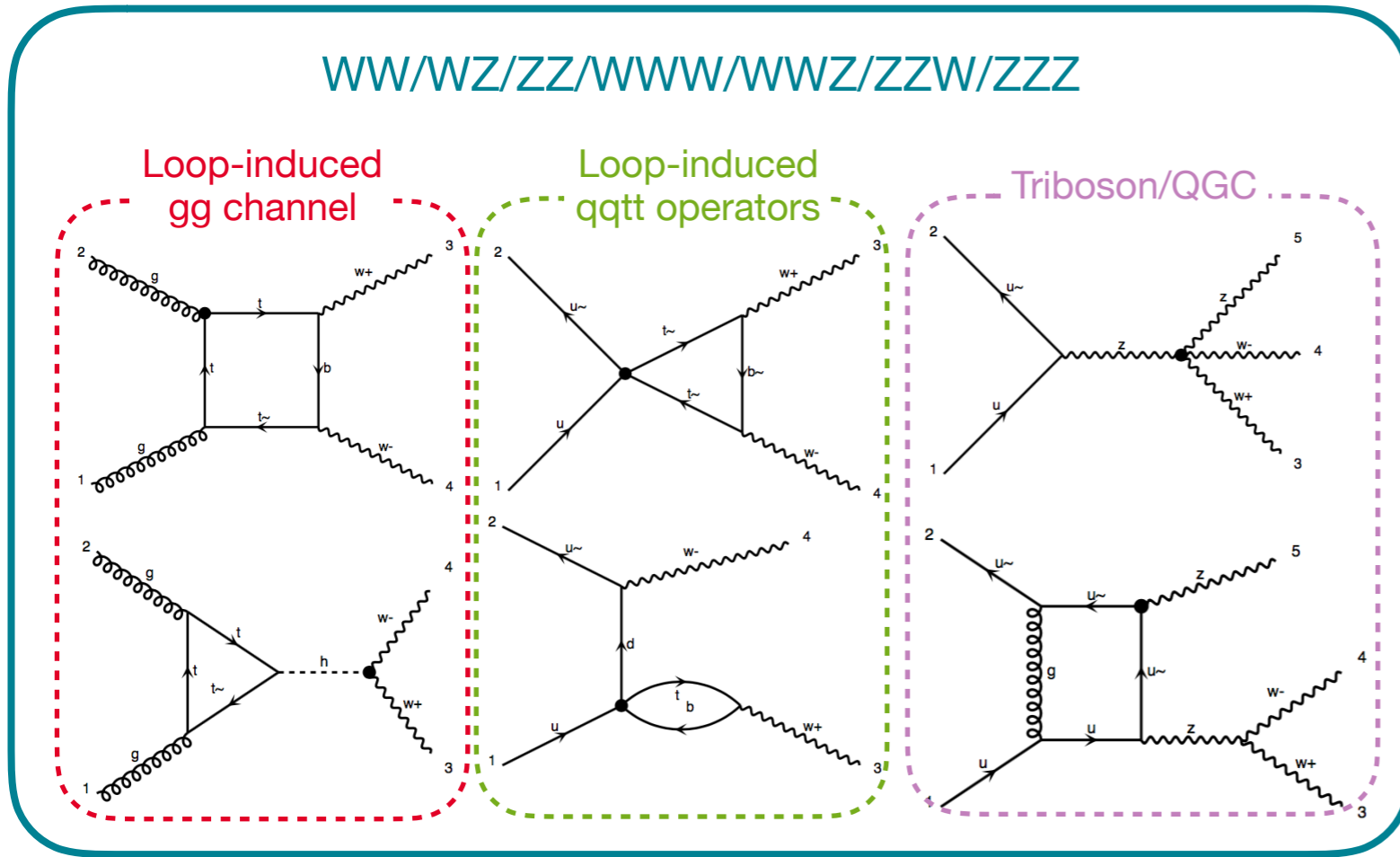
[SMEFT@NLO; arXiv:2008.11743]



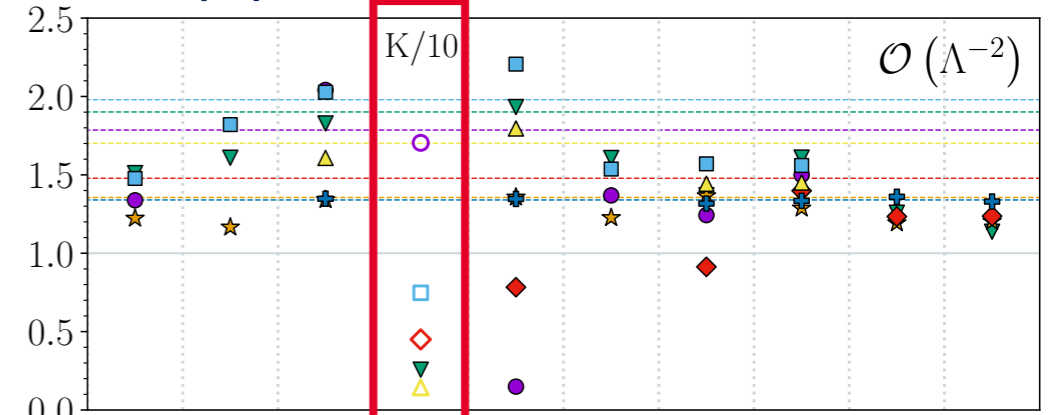
Projected FCC-hh reach: 1%, 5% and 50% on H, HH and HHH

Multiboson

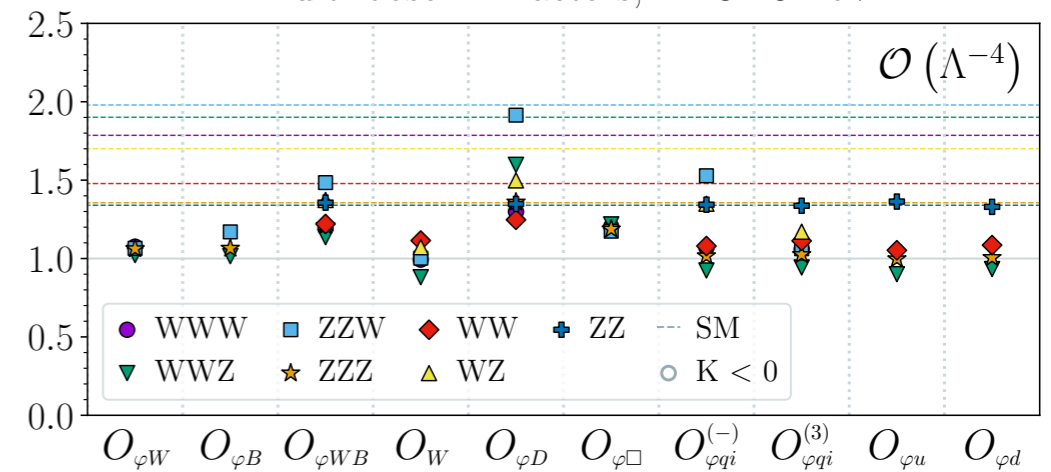
[SMEFT@NLO; arXiv:2008.11743]



qq-initiated K-factors



Multi-boson K-factors, LHC 13 TeV



[CMS; arXiv:2006.11191]

Non-universal NLO corrections, different from SM

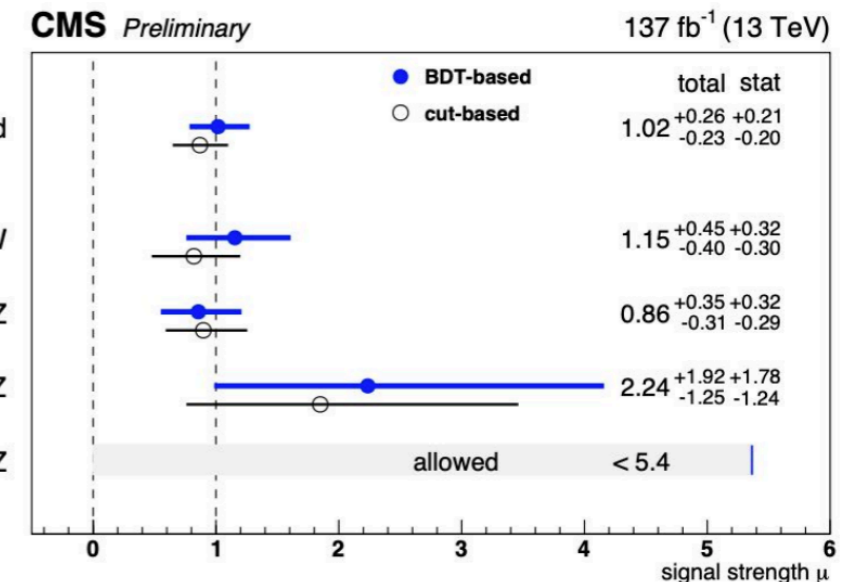
Large, negative K-factors for triple gauge operator, c_W

Non-interference/cancellation at LO broken at NLO

First triboson observation by CMS this year

- Also strong evidence from ATLAS

- New window into SMEFT? [ATLAS; PLB 798 (2019) 134913]

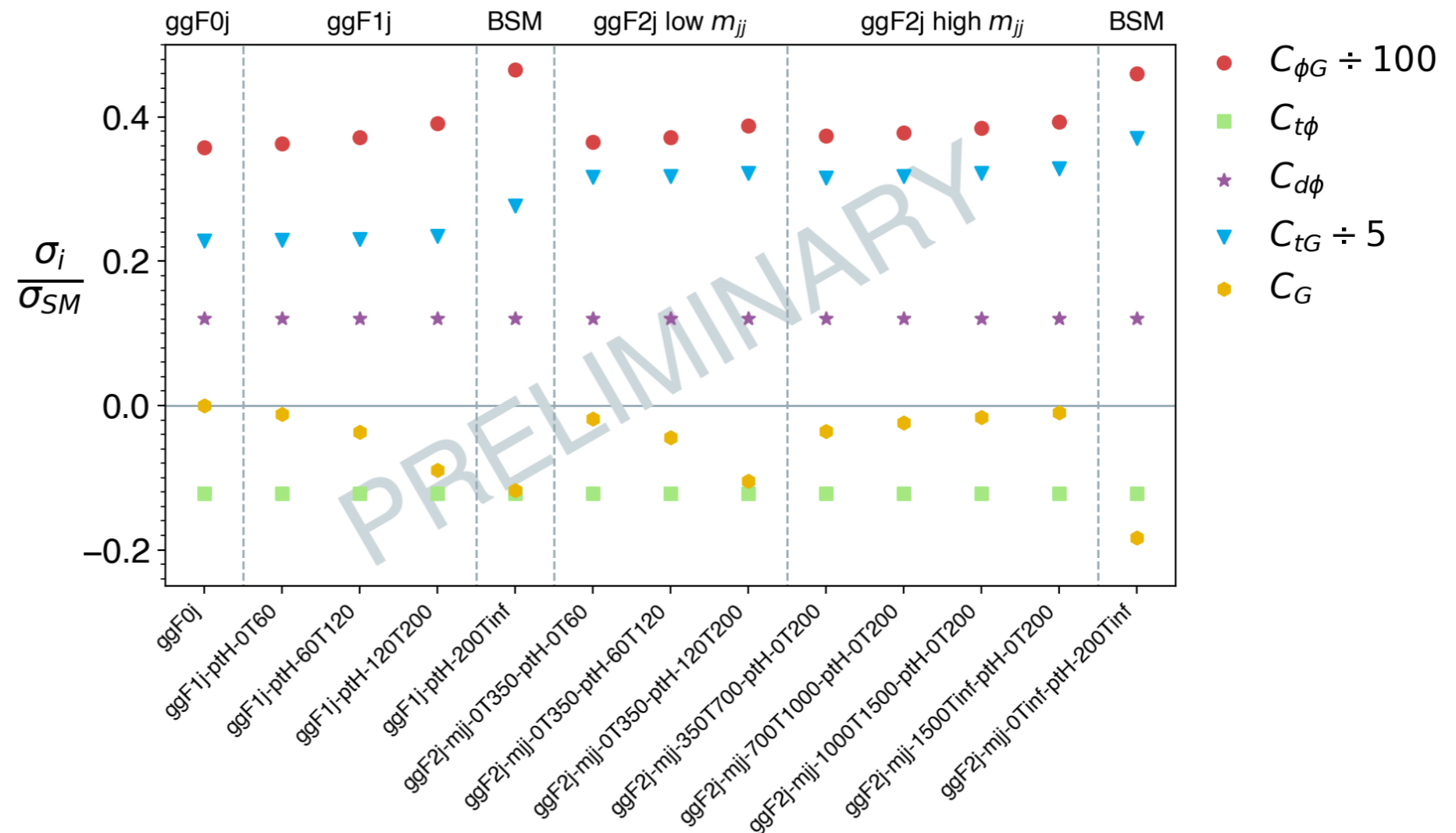
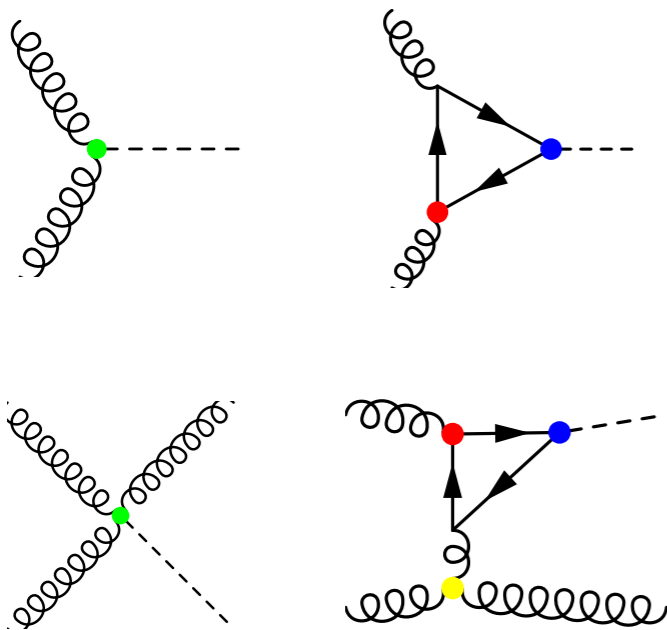


Improving fits

[Ellis, Madigan, KM, Sanz, You; in preparation]

STXS for ggF: one-loop is LO for the SM

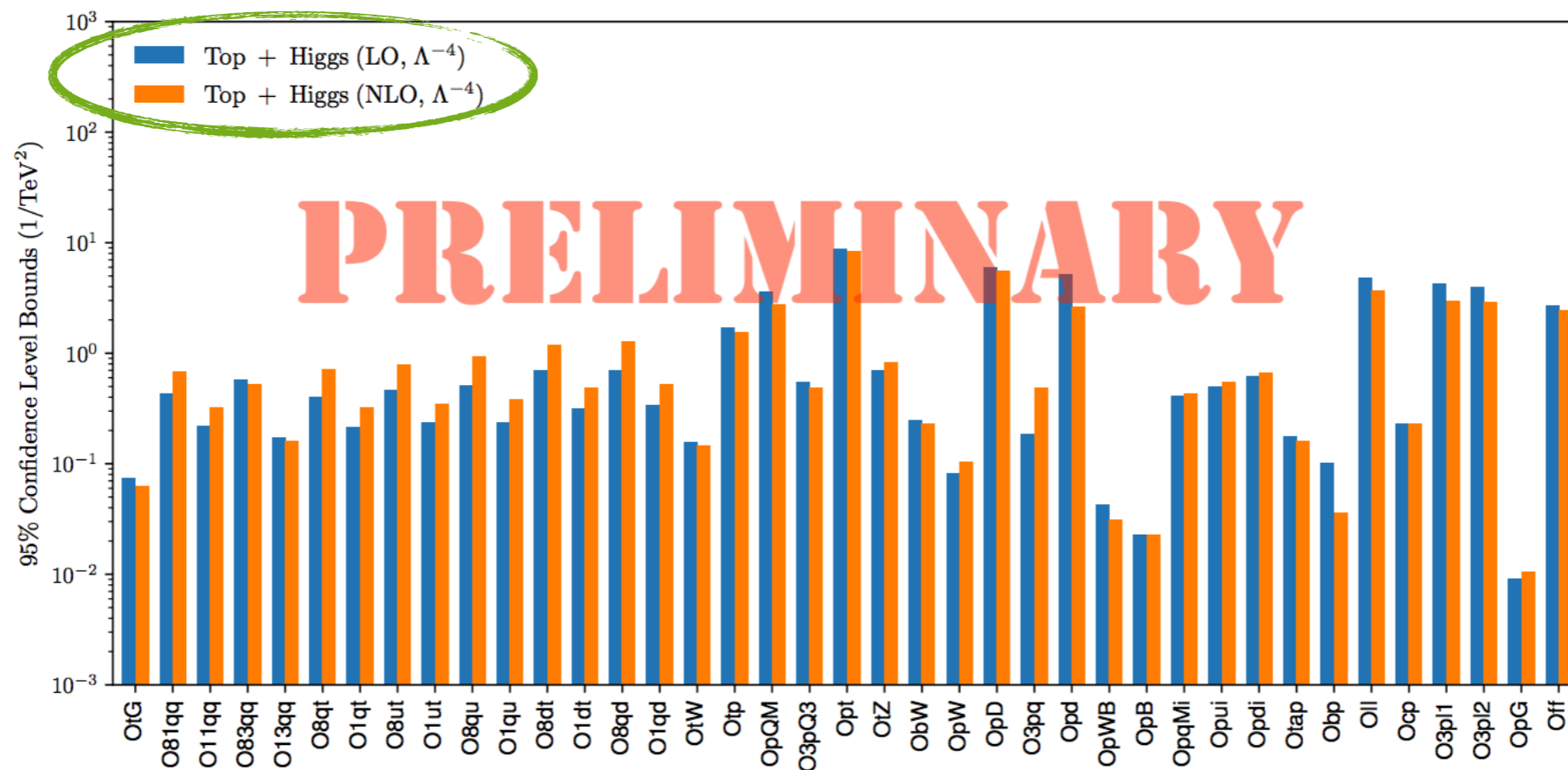
- Tree-EFT x loop-SM and loop-EFT x loop-SM interference terms
- Heavy top limit OK for 0-jet, breaks down for high- p_T



Improving fits

Impact of NLO corrections in combined Top + Higgs fit

- Update from SMEFiT collaboration adding diboson & Higgs



[Ethier et al.; in preparation]

Conclusion & future plans

SMEFT@NLO is a milestone in tools for SMEFT predictions

- Automated, fully differential computations up to one-loop
- NLO+PS, loop-induced, tree-loop interference (see backup)
- Visit & contact us for more info <http://feynrules.irmp.ucl.ac.be/wiki/SMEFTatNLO>

Many extensions planned

- CP-violation
 - Extended flavor structure: $U(2)^5$ (b chirality-flipping ops)
 - c_G @ NLO
 - 4 light fermions operators (qqqq & qqll)
 - **Open to suggestions!**
- 'add-on' for b-Yukawa operator at LO (see website)*

Work in progress for *running* of Wilson coefficients in MG5

Long term: *EW loops*, already possible for the SM in MG5

Backup

Technical details

5-flavor scheme (massless b) & CKM=1

EW input scheme: $\{G_F, M_Z, M_W\}$

- Relevant field redefinitions & EW parameter shifts performed

EFT renormalisation scale **mu_{EFT}**

- Separate, fixed scale for the running of the Wilson coefficients
- MG5 does not run the Wilson coefficients (yet)
- Usual **mu_R** & **mu_F** are kept for α_s & PDFs

Everything available for NLO/loop calculations, except...

- Triple gluon operator, **c_G** <http://feynrules.irmp.ucl.ac.be/wiki/GGG> *Dedicated model*
- Scalar & tensor 2-quark-2-lepton operators: **ct_{1S3}**, **ct_{1T3}**, **cb_{1S3}**

Validated at LO against dim6top & SMEFTsim

v2 or v3

MG5 uses coupling orders for command → diagrams

- **QCD, QED & NP** : $NP(1/\Lambda)=1$
 - v2: cannot mix QCD orders among diagrams in NLO computations
 - 4F operators have only NP=2, cannot interfere with SM QCD using v2
- Reason for g_s normalisation of top chromo-dipole operator ctG*

Recommend v3 for full access to SMEFT@NLO features

<https://code.launchpad.net/~maddevelopers/mg5amcnlo/3.0.3-neworders>

- Dev. branch that works with SMEFT@NLO, merged to trunk soon
- ! Fixed Order only ! NLO+PS in preparation (out by end of the year)

v2.X.Y

coupling order matters

no SM x four-fermion

v3.0.3-neworders

split interference & square

no events (yet)

Always specify QCD, QED & NP orders when generating

Tree-loop interference

MG5 supports LO, NLO & loop-induced modes

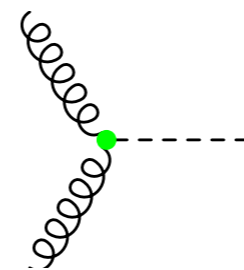
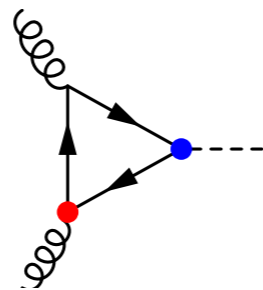
- Loop-induced is a relatively new feature
- Directly computing *interference of tree & loop diagrams* not implemented

Example: $g g \rightarrow H (+ X)$ in SMEFT

- SM is loop-induced but SMEFT has a tree-level contribution:

$$\text{SM, } C_{t\varphi} |\varphi|^2 (\bar{Q} t) \tilde{\varphi},$$

$$\& C_{tG} (\bar{Q} \sigma_{\mu\nu} T^A t) \tilde{\varphi} G_A^{\mu\nu}$$



$$C_{\varphi G} |\varphi|^2 G_A^{\mu\nu} G_{\mu\nu}^A$$

- Relevant for $g g \rightarrow H j, H j j, H H, H H H$

Can be obtained using reweighting feature of MG5

- Alternative method at FO NLO in v3
- See backup for H+j reweighting recipe

*Dedicated recipes on the
webpage soon*

Example commands

QCD

```
> p p > j j          QED=0 QCD=2 NP=2 [QCD]
```

Drell Yan [†]

```
> p p > mu+ mu-      QCD=0 QED=2 NP=2 [QCD]
> p p > mu+ nu        QCD=0 QED=2 NP=2 [QCD]
> p p > W+ j $$ t     QCD=1 QED=1 NP=2 [QCD]
> p p > W- j $$ t~    QCD=1 QED=1 NP=2 [QCD]
> p p > Z j           QCD=1 QED=1 NP=2 [QCD]
```

Multi-boson production

quark-initiated

```
> p p > W+ W-        QED=2 QCD=0 NP=2 [QCD]
> p p > W+ Z          QED=2 QCD=0 NP=2 [QCD]
> p p > Z Z           QED=2 QCD=0 NP=2 [QCD]
```

loop-induced

```
> g g > W+ W-        QED=2 QCD=2 NP=2 [QCD]
> g g > Z Z           QED=2 QCD=2 NP=2 [QCD]
> g g > W+ W- Z       QED=3 QCD=2 NP=2 [QCD]
> g g > Z Z Z         QED=3 QCD=2 NP=2 [QCD]
```

Higgs production

loop-induced

```
> g g > H            QED=1 QCD=2 NP=2 [QCD]
> g g > H H          QED=2 QCD=2 NP=2 [QCD]
> g g > H H H        QED=3 QCD=2 NP=2 [QCD]
> g g > H j           QED=1 QCD=3 NP=2 [QCD]
```

Top quark production

```
> e+ e- > t t~       QED=2 QCD=0 NP=2 [QCD]
> p p > t t~         QED=0 QCD=2 NP=2 [QCD]
> p p > t t~ h       QED=1 QCD=2 NP=2 [QCD]
> p p > t t~ Z       QED=1 QCD=2 NP=2 [QCD]
> p p > t t~ W+      QED=1 QCD=2 NP=2 [QCD]
> p p > t W- $$ t~   QED=1 QCD=1 NP=2 [QCD]
> p p > t W- j $$ t~ QED=1 QCD=2 NP=2 [QCD]
> p p > t j          $$ W- QED=2 QCD=0 NP=2 [QCD]
> p p > t h j        $$ W- QED=3 QCD=0 NP=2 [QCD]
> p p > t Z j        $$ W- QED=3 QCD=0 NP=2 [QCD]
> p p > t a j        $$ W- QED=3 QCD=0 NP=2 [QCD]
```

**set widths to zero to ensure gauge invariance*

Supported processes passing gauge & pole checks

- Some amplitudes have been cross-checked analytically
- NLO can be costly, we are available to contact about 'feasibility' of processes

g g > h j in SMEFT@NLO

MG5_aMC draw diagrams based on coupling orders

- Loop-induced mode is triggered when no born diagrams are found
- Technical issue when you want to compute EFT-tree x SM-loop interference

Ingredients: 2 restriction cards, one with $cpG=0$ (restrict_opt.dat), one with $cpG\neq 0$ (restrict_opG.dat)

1) `MG5_aMC>import model ./SMEFTatNLO_U2_2_U3_3_cG_4F_LO_UFO` `-opt` switch off cpG

`MG5_aMC>generate g g > h j QCD=1 NP=0 QED=1 [QCD]` SM only

`MG5_aMC>output ...`

2) `MG5_aMC>generate g g > h j QCD=1 NP=2 NP^2==2 QED=1 [QCD]` Yukawa interference

`MG5_aMC>output ...`

3a) `MG5_aMC>import model ./SMEFTatNLO_U2_2_U3_3_cG_4F_LO_UFO` `-opG` switch on cpG

`MG5_aMC>generate g g > h j NP=2 QCD=1 QED=1 NP^2==4` Tree-level

`MG5_aMC>output gg_hg`

3b) Create & modify `reweight_card.dat`

`change process g g > h j NP=2 QCD=1 QED=1 NP^2==2 [QCD]`

`change output 2.0`

`launch`