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# GEANT4 MicroElec module 2020 update

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## MICROELEC :

- Low energy transport module
- [ $\sim$ eV,  $\sim$ keV] electrons
- $>$   $\sim$ 50 keV/amu protons & ions
- Based on complex dielectric function (OELF),
- Extended Drude model
- Silicon material
- low energy limit : 16 eV

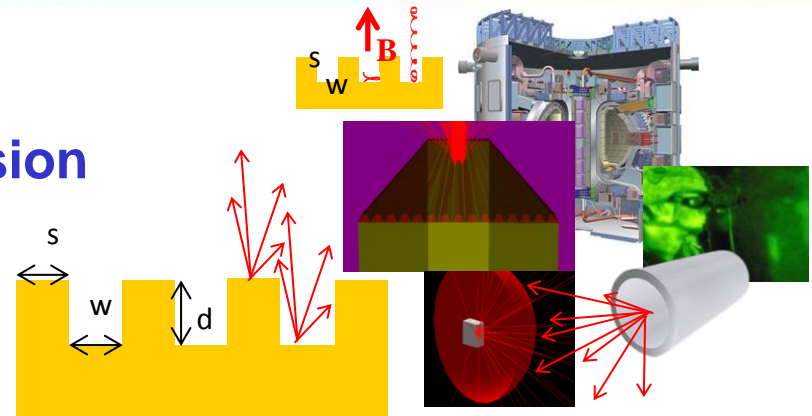
## NEEDs :

- Extending to other materials
- Extending to other applications ( $\neq$  microelectronics)
- Improving the reliability specially for protons & ions



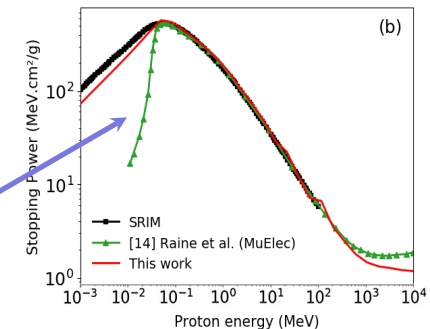
# GEANT4 MicroElec : GOALs & main issues

**Ex :** modelling the  
**Secondary Electron Emission**  
is necessary for many  
applications



## Scientific problem :

- Modelling material/material interfaces (Workfunction solid/vacuum)
- Dielectric materials
  - large gap,
  - importance of phonons,
  - trapping effect,
  - electric field,
- Stopping power for protons not good at low energy with the Drude model



# New developments (1)

- Mermin complex dielectric function

$$\epsilon_M(k, \omega; E_p, \gamma) = 1 + \frac{\left(1 + \frac{i\gamma}{\hbar\omega}\right) (\epsilon_L(k, \omega + i\gamma) - 1)}{1 + \frac{\left(\frac{i\gamma}{\hbar\omega}\right) (\epsilon_L(k, \omega + i\gamma) - 1)}{\epsilon_L(k, 0) - 1}}$$

- Dependence on the wave vector

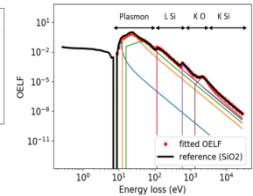
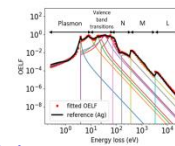
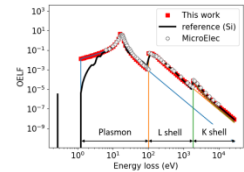
$$\epsilon_L(k, \omega; E_p) = 1 + \frac{\chi^2}{z^2} (f_1(u, z) + if_2(u, z))$$

- Dispersion relation of the Drude model REMOVED

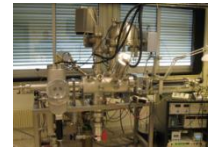
$$z = k/2k_F$$

- Principle remains the same

- Fit of OELF function according to the energy of the different shells
- Weakly bound electrons treated analogously to core electrons
  - Plasmon Damping : systematic production of a secondary electron
  - introduction of a « mean » initial energy for electrons (valence & cond. bands)
- Interband transition taken into account
- Decay : G4 Auger cascade
- Optimisation of the fitting procedure:



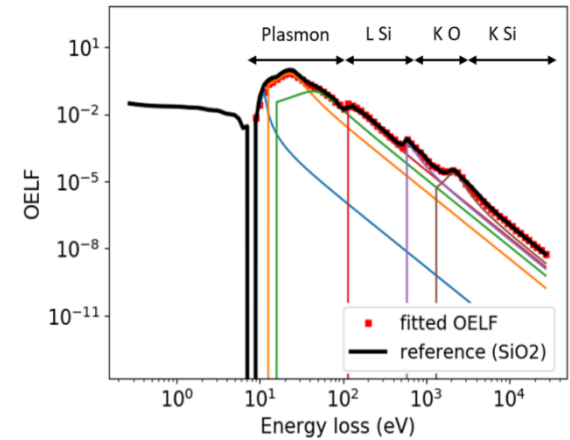
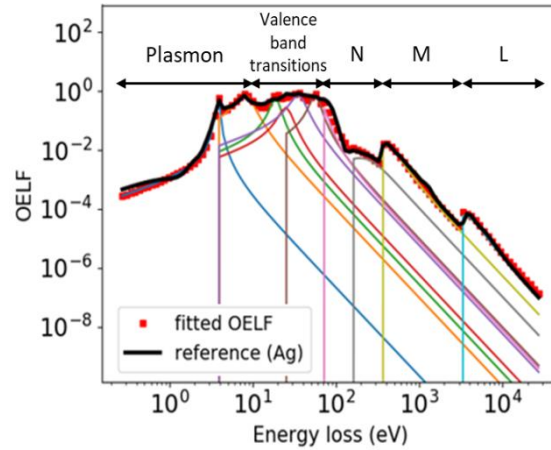
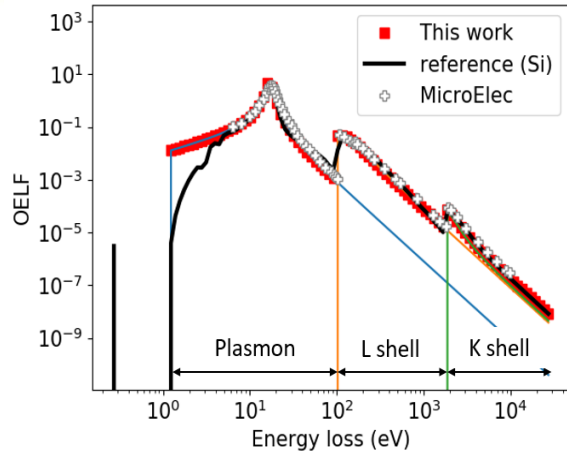
Trade off  
 Sum rules (mean ionizing potential + valence)  
 vs.  
 Secondary electron emission yield  
 experimental data  
 ONERA measurements )



I.M. Bronshtein, B.S. Fraiman,  
 VTORICHNAYA ELEKTRONNAYA  
 EMISSIYA. (Secondary Electron Emission),  
 1969, 1969.



# New developments (2)



## - 11 materials

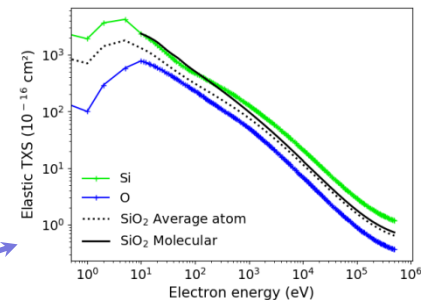
C, Al, Si, Ti, Ni, Cu, Ge, Ag, W, Kapton and SiO<sub>2</sub>

## - 2 dielectrics

Kapton and SiO<sub>2</sub>

## - Low energy limit extended to the work function ~5 eV

## - ELECTRONS : Elastic cross sections re-calculated following PW formalism using ELSEPA (1 eV to 500keV)



F. Salvat, A. Jablonski, C.J. Powell, ELSEPA—Dirac partial-wave calculation of elastic scattering of electrons and positrons by atoms, positive ions and molecules, Computer Physics Communications. 165 (2005) 157–190.

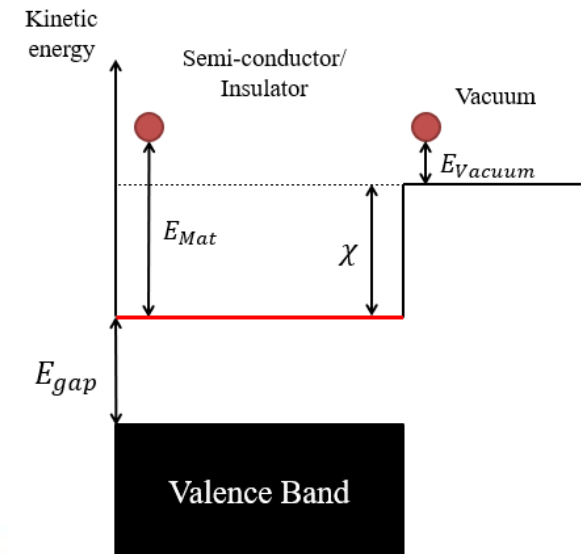
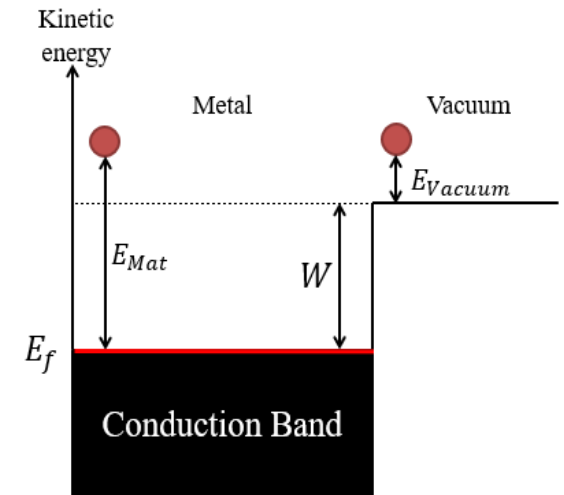
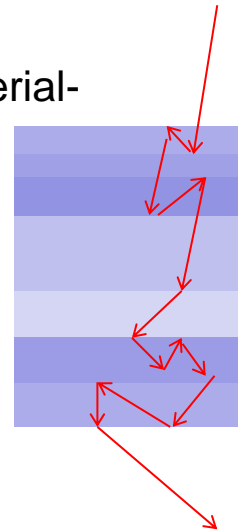
# Material interface potential barrier

- Exponential potential barrier with an height  $W$  or  $\chi$  and a transmission probability

$$T(\theta, E) = 1 - \frac{\sinh^2(\pi a(k_i - k_f))}{\sinh^2(\pi a(k_i + k_f))}$$

- Low energy electrons or high incidence angles may be reflected by the surface
- Model usable for vacuum-material and material-material interfaces
  - Simulation of Multilayers
- Handled by the new discrete process

**G4MicroElecSurface**



# Electron-phonon interactions in SiO<sub>2</sub>

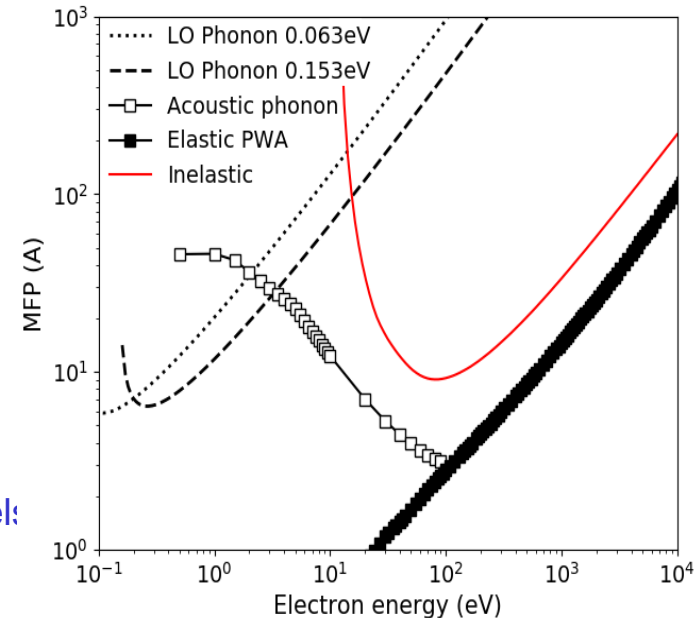
## New discrete process: G4LOPhononModel

### Optical phonons

- Fröhlich theory [1]
- Energy loss for incident electrons below the band gap (9eV)
- Monoenergetic loss of the phonon mode  $\hbar\omega_{LO}$ , 2 modes for SiO<sub>2</sub>: 63 and 153meV

### Acoustic phonons

- Bradford screened model [2]
- Isotropic angular distribution
- Substitute to the partial wave cross sections below 100eV
- Transition between the 2 models handled in G4MicroElecElasticModel



[1] J. Llacer, E.L. Garwin, Electron-Phonon Interaction in Alkali Halides. I. The Transport of Secondary Electrons with Energies between 0.25 and 7.5 eV, Journal of Applied Physics. 40 (1969) 2766–2775. <https://doi.org/10.1063/1.1658075>.

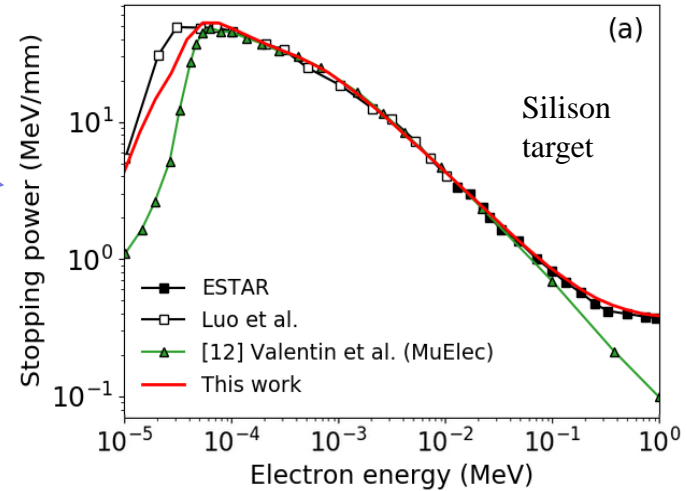
[2] J.N. Bradford, S. Woolf, Electron-acoustic phonon scattering in SiO<sub>2</sub> determined from a pseudo-potential for energies of  $E \geq E_{bz}$ , Journal of Applied Physics. 70 (1991) 490–492. <https://doi.org/10.1063/1.350254>.



# Validations : Stopping powers

Improvement of the Mermin approach compared to former Drude treatment

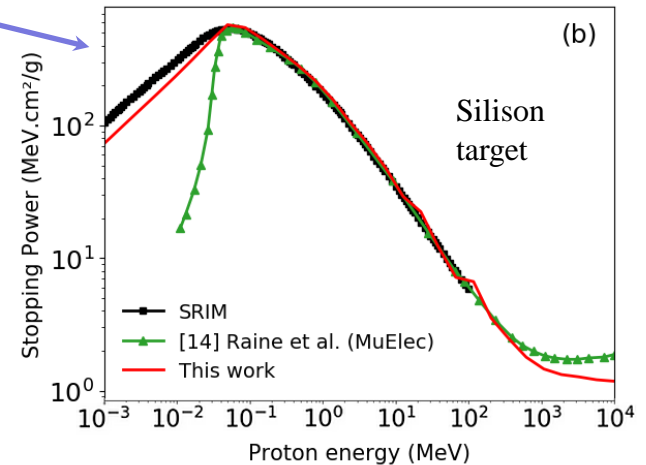
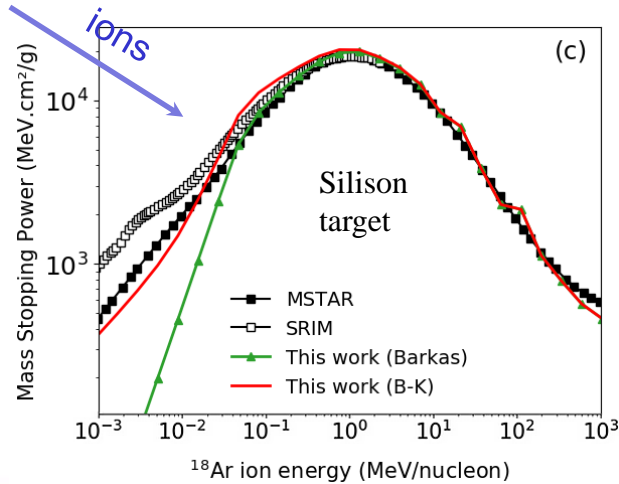
Electrons



Good agreement with the stopping power of SRIM for both protons

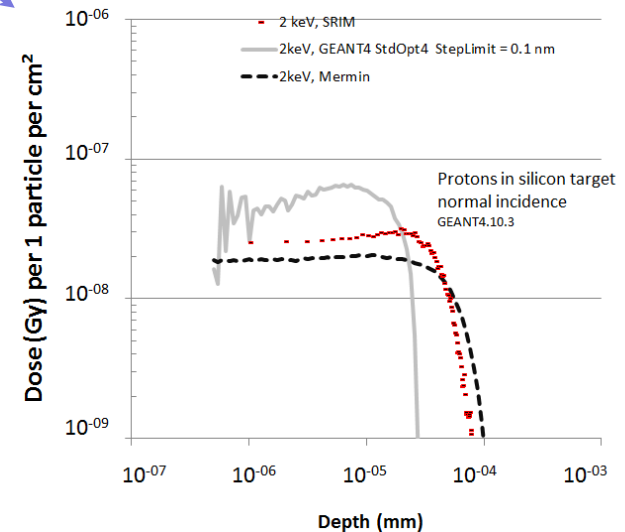
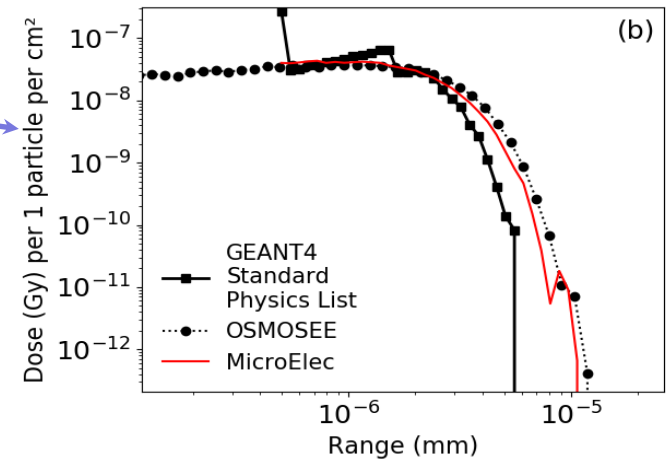
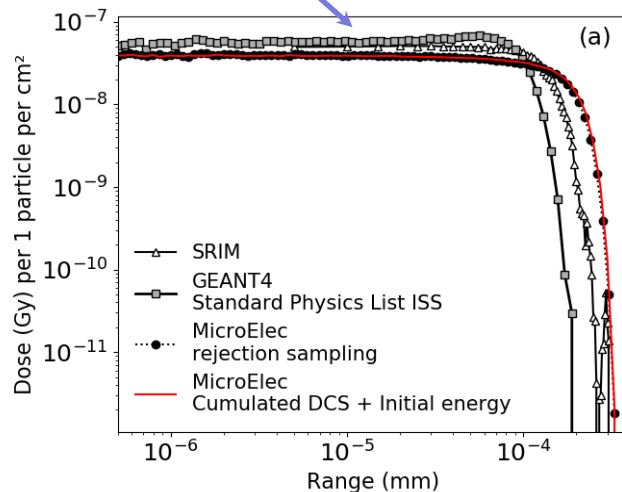
Protons

And heavy ions improvement of the Kaneko approach



# Validation : Silicon dose-depth profile

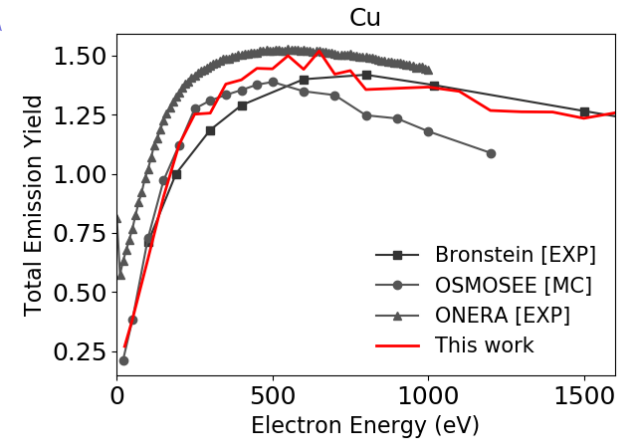
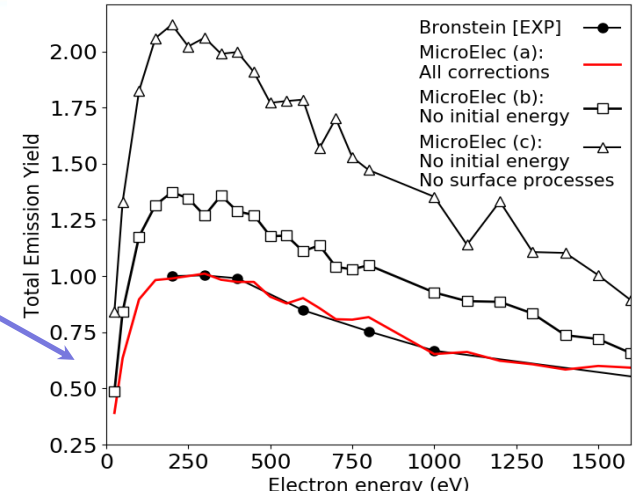
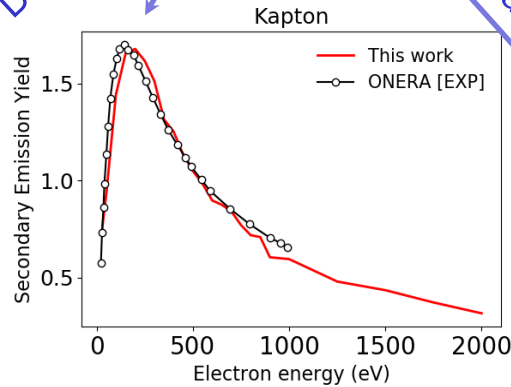
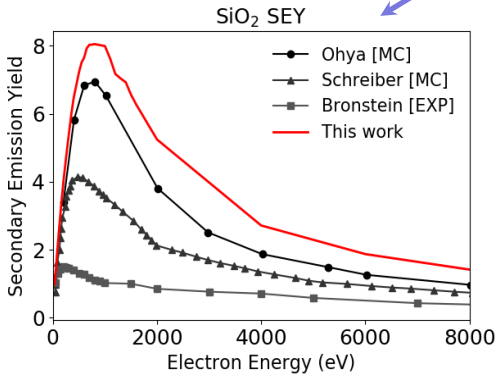
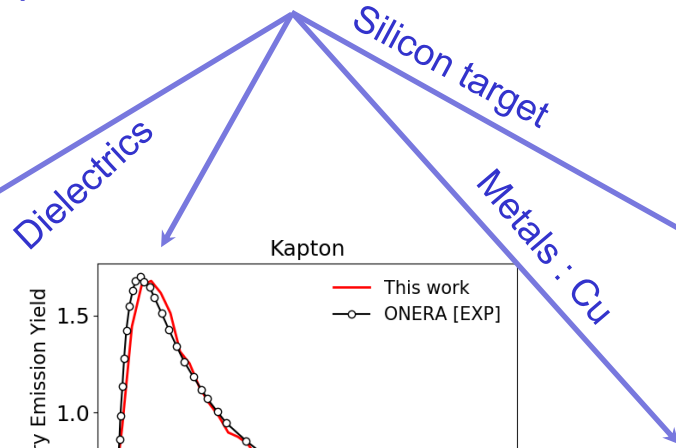
- ELECTRONS (200 eV): Good agreement between OSMOSEE\* and  $\mu$ ELEC
- PROTONS (2 keV) : 25 % difference with SRIM (formerly valid > 50keV)
- PROTONS (10 keV) : satisfying when compared to both SRIM & Std ISS physics



\* J. Pierron, C. Inguibert, M. Belhaj, T. Gineste, J. Puech, Electron emission yield for low energy electrons: Monte Carlo simulation and experimental comparison for Al, Ag, and Si Electron emission yield for low energy electrons: Monte Carlo simulation and experimental comparison for, Journal of Applied Physics. 121 (2017) 215107. <https://doi.org/10.1063/1.4984761>.

# Electron emission yield calculations

Good agreement with experimental data for most materials



Very low energy production threshold for secondary electrons (4-5eV, 9eV for SiO<sub>2</sub> due to the band gap)

Difference for SiO<sub>2</sub> probably due to charging effect (electric field establishing)

# Undergoing developments

- Trapping and charge effects to be added to get accurate SEY calculations for insulators
- Generalized Oscillator Strength (GOS) formalism to improve deep shells for certain materials for which Lorentzian fits of OELF fail.
- Improving cross sections for low energy ions
- Extending the list of materials :
  - $\text{Al}_2\text{O}_3$
  - BN,
  - Au
  - Etc...
- Publication submitted to Nucl. Instr. Method. This work will be available in G4 Dec 2020 release.