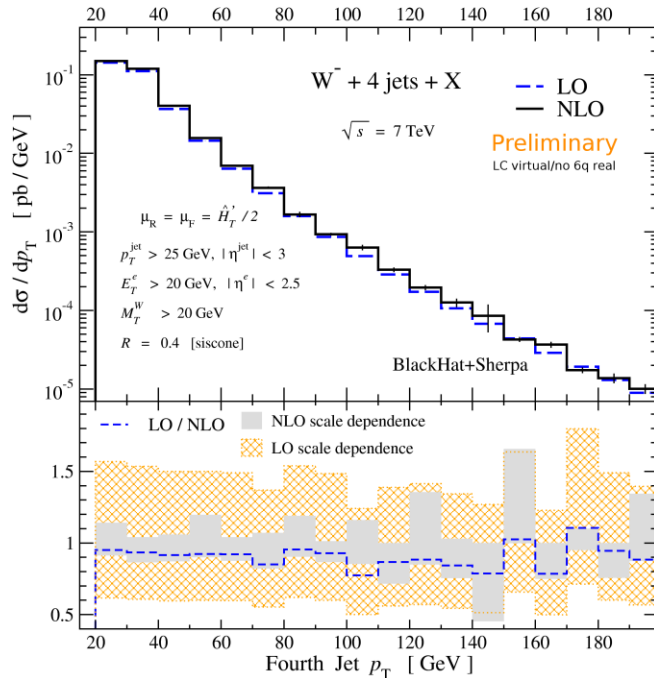


Recent Advances in NLO QCD (V-boson+jets)



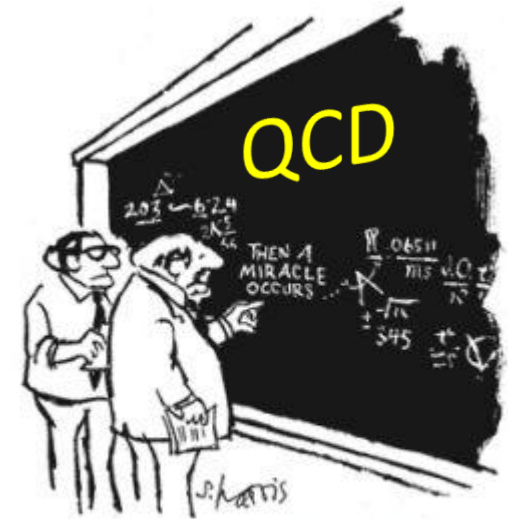
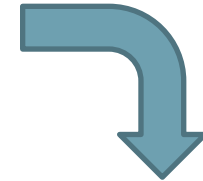
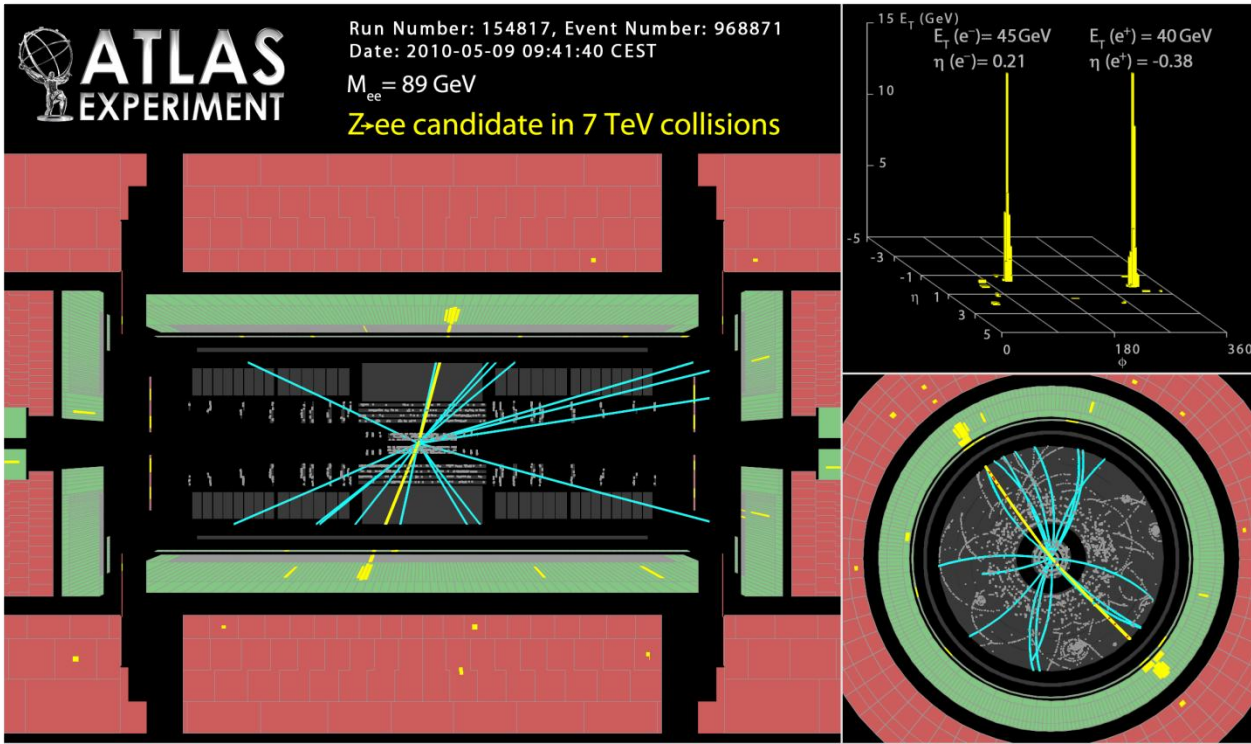
In collaboration with BlackHat: C.F.Berger,
 Z.Bern, L.J.Dixon, F.Febres Cordero,
 D.Forde, D.A.Kosower, D.Maitre;
 +Sherpa: T.Gleisberg

Harald Ita, (UCLA+NSF TI-fellow)

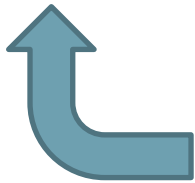
US ATLAS Hadronic Final State Forum

SLAC, Aug 23rd 2010

QCD omnipresent @ the LHC



"I THINK YOU SHOULD BE MORE EXPLICIT HERE IN STEP TWO."

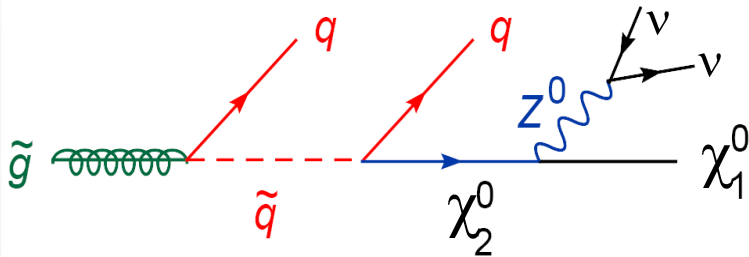


Fundamental stuff:
masses, couplings, fields,
strategies, theories ...



Signals in multi-jet final states

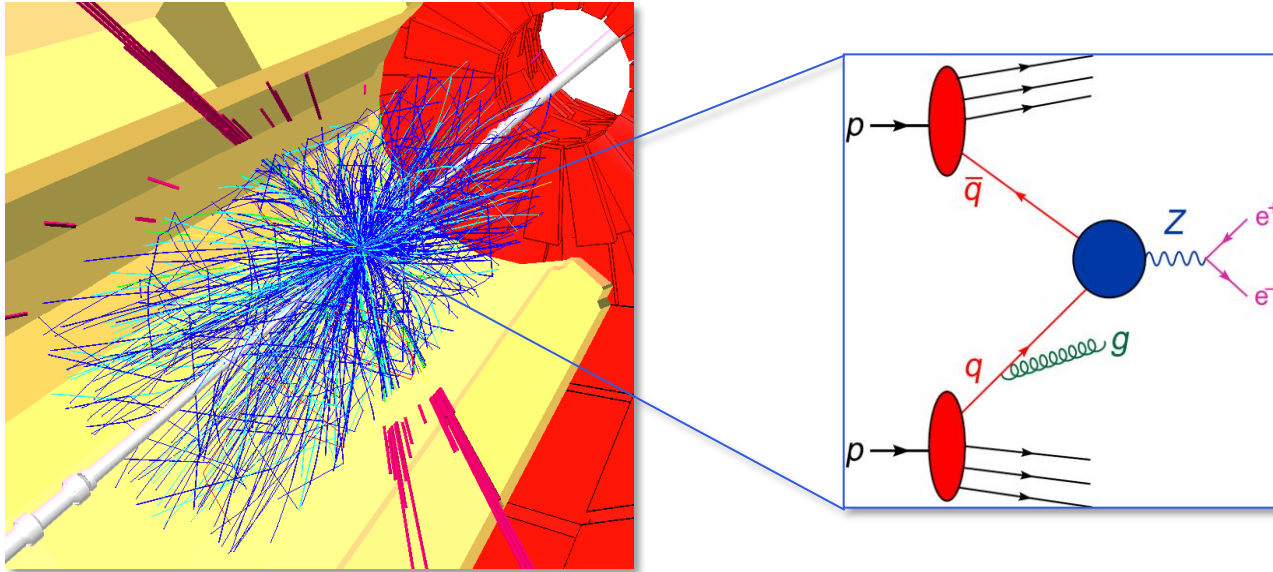
Example: SUSY gluino cascade



- New particles, e.g. supersymmetry, Higgs boson(s) typically decay through cascades into multi-jet final states
- Kinematic signatures not always clean (e.g. mass bumps) if dark matter, neutrinos, or other escaping particles present

Need **precise Standard Model backgrounds** for a variety of processes with multiple jets, to maximize potential for new physics discoveries.

QCD factorization & parton model



Heavy fundamental particles produced in high energy interactions

→ Factorization:

- **Protons** appear as clouds of point-like **partons** (quarks + gluons).
- **Asymptotic freedom** guarantees that hard interactions between **partons** well described by **perturbative QCD**.

Quantitative first principle predictions.

How best to control SM backgrounds?

Increasing availability →

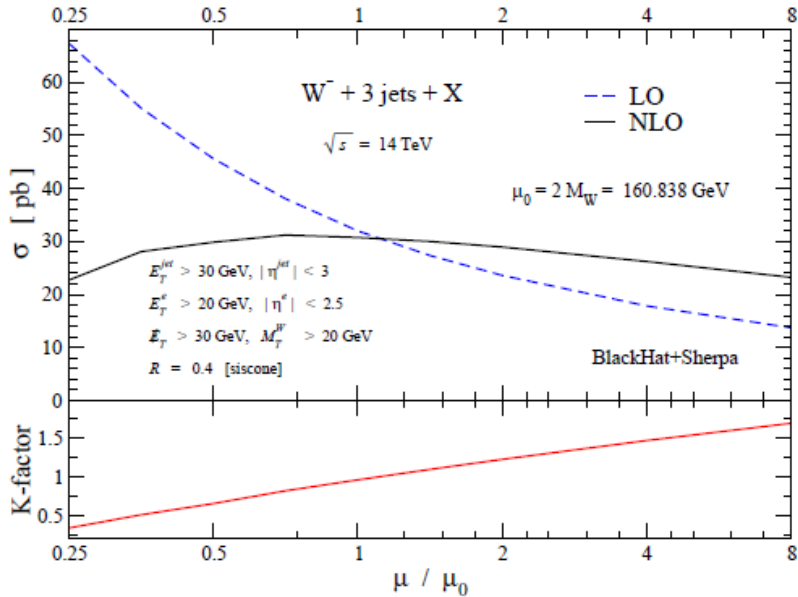
Increasing accuracy →

1. Get the **best theoretical prediction** you can, whether
 - Basic Monte Carlo [PYTHIA, HERWIG, Sherpa, ...]
 - LO QCD parton level
 - LO QCD matched to parton showers [MadGraph/MadEvent, ALPGEN/PYTHIA, Sherpa, ...]
 - NLO QCD at parton level
 - NLO matched to parton showers [MC@NLO, POWHEG, ...]
 - NNLO inclusive at parton level
 - NNLO with flexible cuts at parton level

2. Take **ratios** whenever possible
 - QCD effects cancel when event kinematics are similar
 - Closely related to “data driven” strategies

Want NLO for multi-jets

[BlackHat,0907.1984]



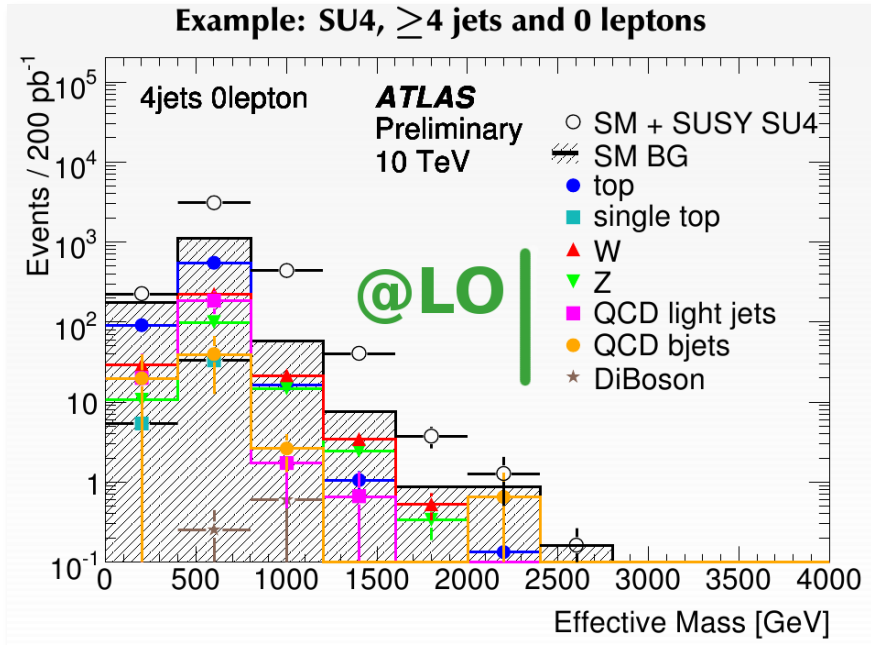
Typical scale variation W+n jets

Number of Jets	LO	NLO
1	16 %	7 %
2	30 %	10 %
3	42 %	12 %

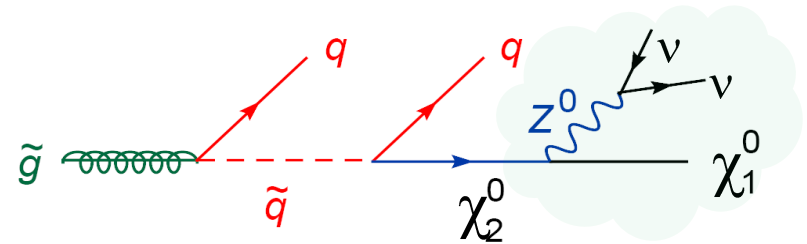
- Reduced dependence on unphysical **renormalization** and **factorization scales**.
- NLO importance for scale dependence grows with increasing number of jets.
- NLO captures more physics:
 - multiple partons merged to **jets**
 - initial state **radiation**
 - more types of **initial state partons** included
- Shape changes

NLO required for quantitative control of multi-jet final states

NLO motivation from SUSY search



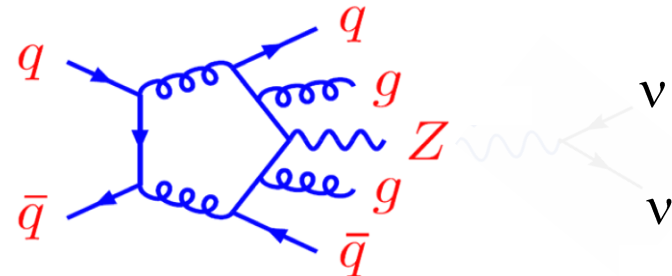
- Signature: **multijet** + **Missing E_T** + X



- Irreducible background:
Z (\rightarrow neutrinos) + 4 jets

- Signal excess over **LO background** with normalization still quite uncertain

Aim for NLO background:
Z (\rightarrow neutrinos) + 4 jets



The Les Houches Wish List (2001)

Run II Monte Carlo Workshop, April 2001

Single boson	Diboson	Triboson	Heavy flavour
$W + \leq 5j$	$WW + \leq 5j$	$WWW + \leq 3j$	$t\bar{t} + \leq 3j$
$W + b\bar{b} + \leq 3j$	$WW + b\bar{b} + \leq 3j$	$WWW + b\bar{b} + \leq 3j$	$t\bar{t} + \gamma + \leq 2j$
$W + c\bar{c} + \leq 3j$	$WW + c\bar{c} + \leq 3j$	$WWW + \gamma\gamma + \leq 3j$	$t\bar{t} + W + \leq 2j$
$Z + \leq 5j$	$ZZ + \leq 5j$	$Z\gamma\gamma + \leq 3j$	$t\bar{t} + Z + \leq 2j$
$Z + b\bar{b} + \leq 3j$	$ZZ + b\bar{b} + \leq 3j$	$WZZ + \leq 3j$	$t\bar{t} + H + \leq 2j$
$Z + c\bar{c} + \leq 3j$	$ZZ + c\bar{c} + \leq 3j$	$ZZZ + \leq 3j$	$t\bar{b} + \leq 2j$
$\gamma + \leq 5j$	$\gamma\gamma + \leq 5j$		$b\bar{b} + \leq 3j$
$\gamma + b\bar{b} + \leq 3j$	$\gamma\gamma + b\bar{b} + \leq 3j$		
$\gamma + c\bar{c} + \leq 3j$	$\gamma\gamma + c\bar{c} + \leq 3j$		
	$WZ + \leq 5j$		
	$WZ + b\bar{b} + \leq 3j$		
	$WZ + c\bar{c} + \leq 3j$		
	$W\gamma + \leq 3j$		
	$Z\gamma + \leq 3j$		

- Five-particle processes under good control with Feynman diagram based approaches.
- Problem posed for over 10 years. **Solution clear only recently!**

Les Houches Wish List (2005)

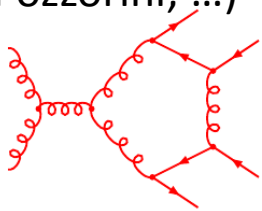
Descope!

Les Houches 2005

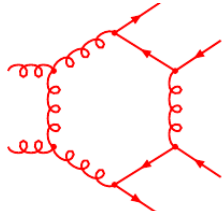
process wanted at NLO ($V \in \{Z, W, \gamma\}$)	background to
1. $pp \rightarrow VV + \text{jet}$	$t\bar{t}H$, new physics
2. $pp \rightarrow H + 2 \text{ jets}$	H production by vector boson fusion (VBF)
3. $pp \rightarrow t\bar{t}b\bar{b}$	$t\bar{t}H$
4. $pp \rightarrow t\bar{t} + 2 \text{ jets}$	$t\bar{t}H$
5. $pp \rightarrow VV b\bar{b}$	VBF $\rightarrow H \rightarrow VV$, $t\bar{t}H$, new physics
6. $pp \rightarrow VV + 2 \text{ jets}$	VBF $\rightarrow H \rightarrow VV$
7. $pp \rightarrow V + 3 \text{ jets}$	new physics
8. $pp \rightarrow VVV$	SUSY trilepton

NLO bottleneck: loops

state of the art: $pp \rightarrow t\bar{t}b\bar{b} + X$
(Bredenstein, Denner, Dittmaier,
Pozzorini; ...)



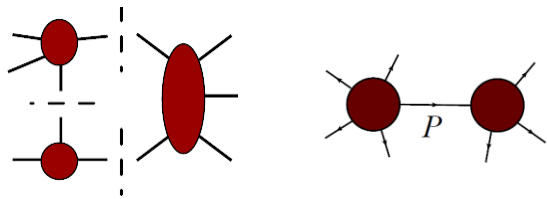
114 pentagons



40 hexagons

Factorial growth of number of diagrams with multiplicity.
Intricate tensor reductions.

Bern, Dixon & Kosower
Britto, Cachazo & Feng
Ossola, Pittau & Papadopoulos
Giele, Kunszt & Melnikov



Efficiently drops unphysical parts (ghosts,...).
Automatable for many processes.

- **Traditional methods:**
Simplify loop-level Feynman diagrams analytically.
Reduce tensor integrals.

- **Recursive & on-shell/unitarity methods:**
Use unitarity and factorization properties to assemble amplitudes from (on-shell) tree amplitudes numerically.

Example: new insights

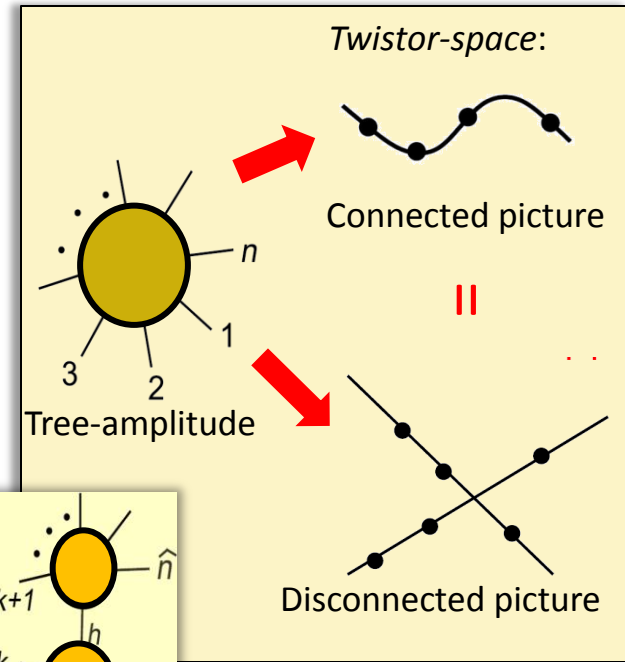
twistor string [Witten 03']:

- Remarkable simplicity: Tree amplitudes supported on lines in twistor space.
Obscure from *Feynman diagrams*!

- Tree recursions: [Britto, Cachazo, Feng, Witten 05']
Fast QCD tree amplitudes from lower point on-shell amplitudes.

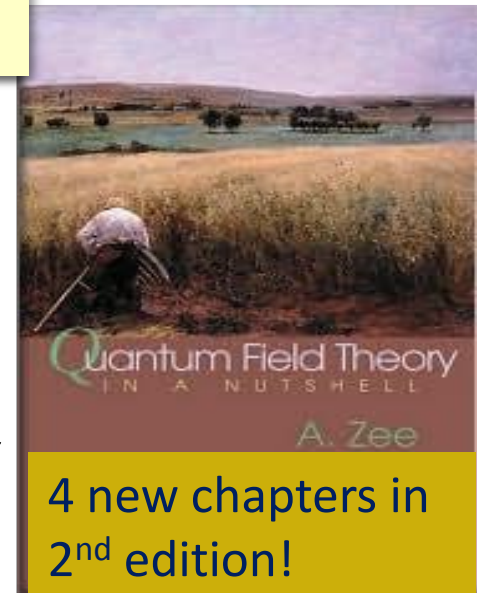
- Loop recursions: [Bern, Dixon, Kosower 05']
Most efficient for parts of loop amplitudes (rational terms).

Leads to *rewriting* of and *rethinking* about perturbative QFT.



The equation shows a tree amplitude with n external lines (labeled 1, 2, 3, ..., n) equal to a sum over h, k of two diagrams. The top diagram has $k+1$ external lines (labeled 1, 2, 3, ..., $k+1$) and \hat{n} external lines. The bottom diagram has k external lines (labeled 1, 2, 3, ..., k) and $\hat{1}$ external lines.

New textbook QFT



05' Wishlist 2→4 processes

- **pp → t⁻tb⁻b:**
 - 09' Bredenstein, Denner, Dittmaier and Possorini [traditional]
 - 09' Bevilacqua, Czakon, Papadopoulos, Pittau and Worek [unitarity]
- **pp → W+3 jets:**
 - 09' Ellis, Melnikov and Zanderighi (leading color approx) [unitarity]
 - 09' BlackHat [unitarity]
- **pp → Z+3 jets:**
 - 10' BlackHat [unitarity]
- **pp → b⁻bb⁻b** (q⁻q-channel):
 - 09' Binoth, Greiner, Guffanti, Reuter, Guillet and Reiter [traditional]
- **pp → t⁻tjj:**
 - 10' Bevilacqua, Czakon, Papadopoulos and Worek [unitarity]
- **pp → W⁺W⁺+2 jets:**
 - 10' Melia, Melnikov, Rontsch, Zanderighi [unitarity]

Selected recent NLO

- **pp → WWW, WWZ, ... ZZZ:**
 - 08' Binotha, Ossola, Papadopoulos, Pittau [unitarity]
- **pp → H+2 jets:**
 - 09'+10' Campbell, Ellis, Zanderighi, Badger, Williams; Dixon, Sofianatos [unitarity]
- **pp → tt̄+1 jet:**
 - 07' Dittmaier, Uwer, Weinzierl [traditional]
 - 10' Melnikov, Schulze [unitarity]

The Les Houches Wish List (2010)

2010

process wanted at NLO	background to
1. $pp \rightarrow VV + \text{jet}$	$t\bar{t}H$, new physics Dittmaier, Kallweit, Uwer; Campbell, Ellis, Zanderighi
2. $pp \rightarrow H + 2 \text{ jets}$	H in VBF Campbell, Ellis, Zanderighi; Ciccolini, Denner Dittmaier
3. $pp \rightarrow t\bar{t}b\bar{b}$	$t\bar{t}H$ Bredenstein, Denner Dittmaier, Pozzorini; Bevilacqua, Czakon, Papadopoulos, Pittau, Worek
4. $pp \rightarrow t\bar{t} + 2 \text{ jets}$	$t\bar{t}H$ Bevilacqua, Czakon, Papadopoulos, Worek
5. $pp \rightarrow VVb\bar{b}$	VBF $\rightarrow H \rightarrow VV$, $t\bar{t}H$, new physics
6. $pp \rightarrow VV + 2 \text{ jets}$	VBF $\rightarrow H \rightarrow VV$ Melia, Melnikov, Rontsch, Zanderighi VBF: Bozzi, Jäger, Oleari, Zeppenfeld
7. $pp \rightarrow V + 3 \text{ jets}$	new physics Berger, Bern, Dixon, Febres Cordero, Forde, Gleisberg, Ita, Kosower, Maitre; Ellis, Melnikov, Zanderighi
8. $pp \rightarrow VVV$	SUSY trilepton Lazopoulos, Melnikov, Petriello; Hankele, Zeppenfeld; Binoth, Ossola, Papadopoulos, Pittau
9. $pp \rightarrow b\bar{b}b\bar{b}$	Higgs, new physics GOLEM

Feynman
diagram
methods

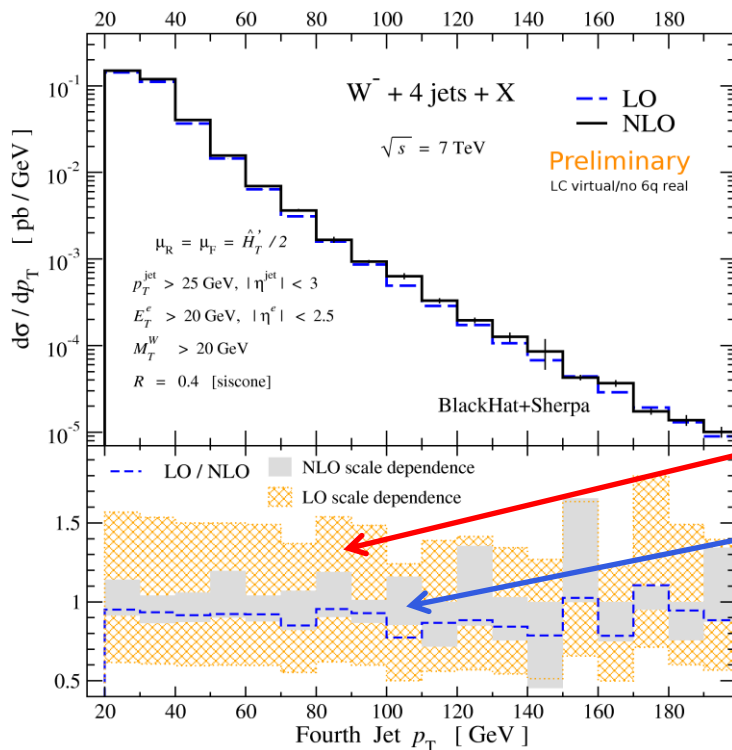
now joined
by

unitarity
based
methods

First 2→5 process

- **pp → W+4 jets:**

- 10' BlackHat (leading color, preliminary) [unitarity]



- First 2→5 NLO computation as needed for SUSY background
- Background to top quark studies

LO uncertainty

NLO uncertainty

Back on the earlier 2001 wishlist!

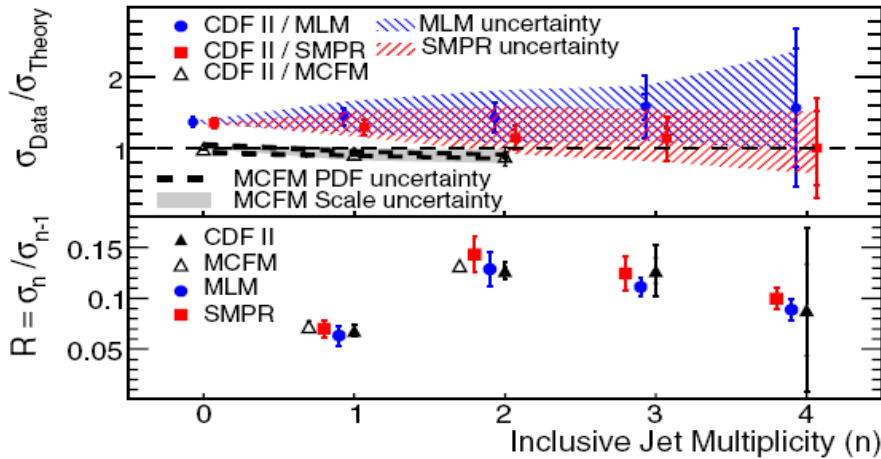
The Les Houches Wish List (2001)

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$W + c\bar{c} + \leq 3j$	$WW + c\bar{c} + \leq 3j$	$WWW + \gamma\gamma + \leq 3j$	$t\bar{t} + W + \leq 2j$
$Z + \leq 5j$	$ZZ + \leq 5j$	$Z\gamma\gamma + \leq 3j$	$t\bar{t} + Z + \leq 2j$
$Z + b\bar{b} + \leq 3j$	$ZZ + b\bar{b} + \leq 3j$	$WZZ + \leq 3j$	$t\bar{t} + H + \leq 2j$
$Z + c\bar{c} + \leq 3j$	$ZZ + c\bar{c} + \leq 3j$	$ZZZ + \leq 3j$	$t\bar{b} + \leq 2j$
$\gamma + \leq 5j$	$\gamma\gamma + \leq 5j$		$b\bar{b} + \leq 3j$
$\gamma + b\bar{b} + \leq 3j$	$\gamma\gamma + b\bar{b} + \leq 3j$		
$\gamma + c\bar{c} + \leq 3j$	$\gamma\gamma + c\bar{c} + \leq 3j$		
	$WZ + \leq 5j$		
	$WZ + b\bar{b} + \leq 3j$		
	$WZ + c\bar{c} + \leq 3j$		
	$W\gamma + \leq 3j$		
	$Z\gamma + \leq 3j$		

Comparing tools

T. Aaltonen et al. [CDF Collaboration], data: 320 pb⁻¹
 arXiv:0711.4044



LO+shower:

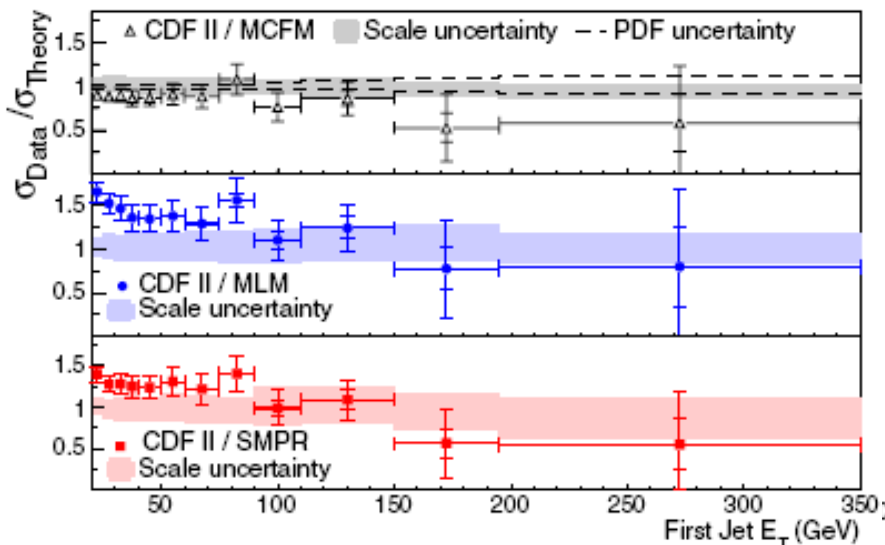
- **SMPR-model: Madgraph+Pythia**
- **MLM-model: Alpgen+Herwig**

NLO-parton level (MCFM)

CDF: JETCLU R=0.4, f=0.75 (IR unsafe)

NLO: SIScone: R=0.4, f=0.5

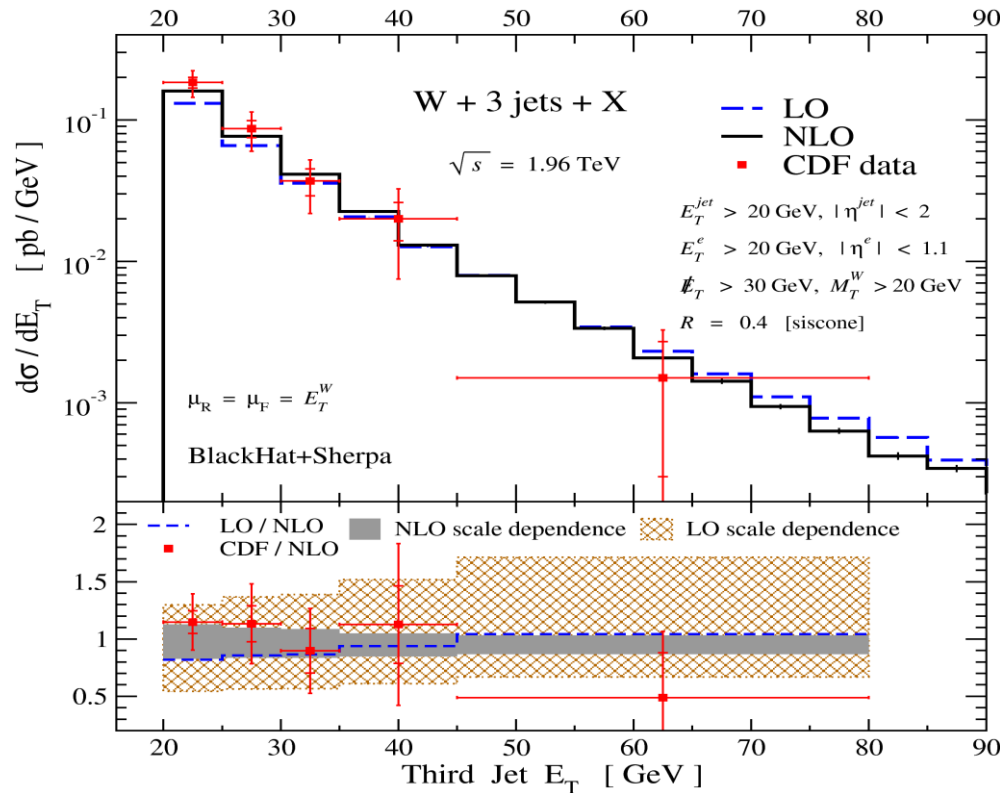
Second jet in W+2 jets



NLO has smallest uncertainties on distributions.

NLO deviation of Data/Theory smaller than other calculations.

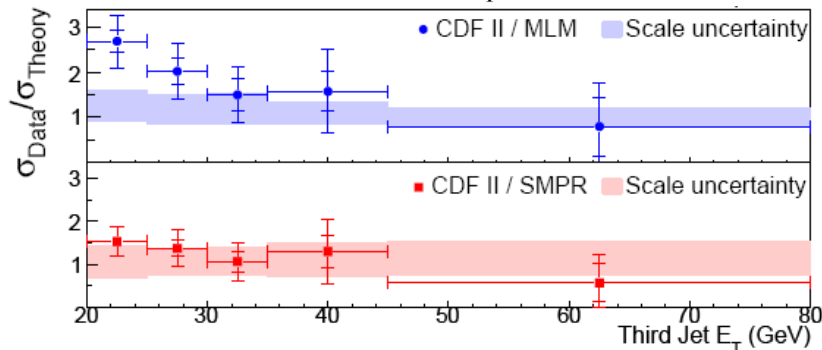
Comparing tools



Third jet in W+3 jets

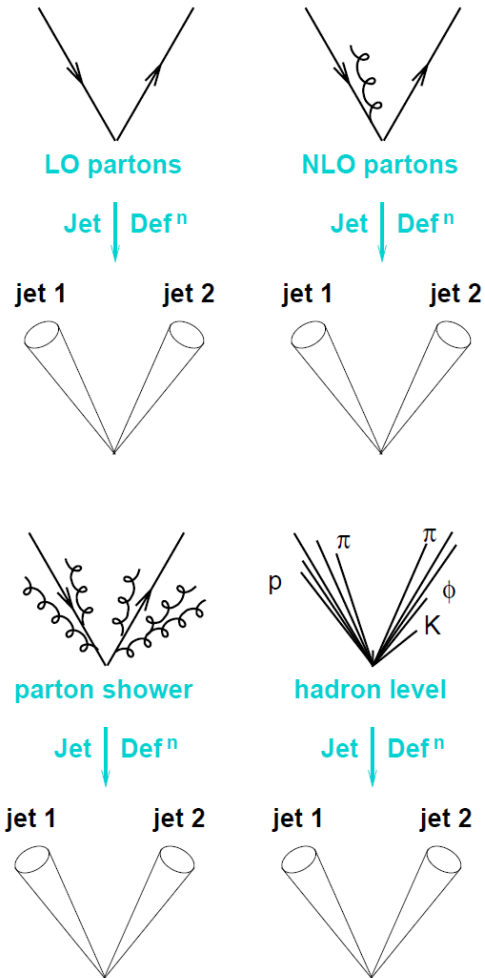
[BlackHat,0907.1984]

- Reduced scale dependence at NLO
- Shape change small compared to LO scale variation



NLO + Shower MCs

Projection to jets provides “universal” view of event



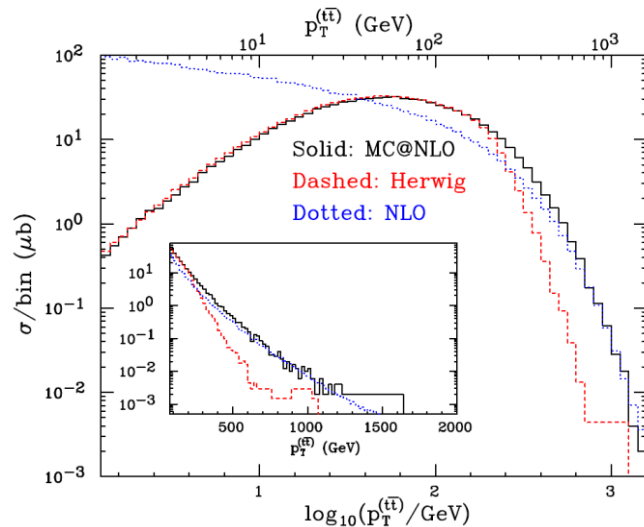
- Recent NLO progress ($2 \rightarrow 4,5$) at **parton level**:
 - no parton shower, no hadronization, no underlying event.
- Methods for matching NLO parton-level results to parton showers:
 - **MC@NLO** [Frixione, Webber 02', ...]
 - **POWHEG** [Nason 04'; Frixione, Nason, Oleari 07'; ...]
 - **GenEvA** [Bauer, Tackmann, Thaler 08']
 - **ME NLO PS** [Gehrmann, Höche, Krauss, Schönherr; Hamilton, Nason; Alioli, Nason, Oleari, Re 10']
- Technical status:
 - no complex multi-jet NLO included yet
 - E.g.: **NLO: Z**, **LO: Z+1/2/3/...** + parton shower
Hamilton & Nason '10; SHERPA, prelim;
 - NLO: Z & Z+j** + parton shower, Alioli et al, prelim

Meanwhile:

- NLO parton-level gives **best normalizations** away from shower-dominated regions.
- Ratios** will be considerably less sensitive to shower + nonperturbative effects.

NLO + Shower MCs: samples

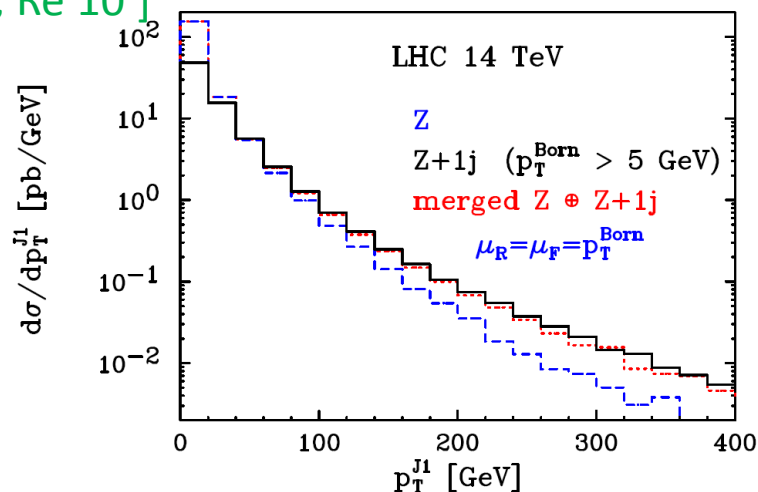
MC@NLO [Frixione, Webber 02']



Some LHC processes available, but see above references more complete account.

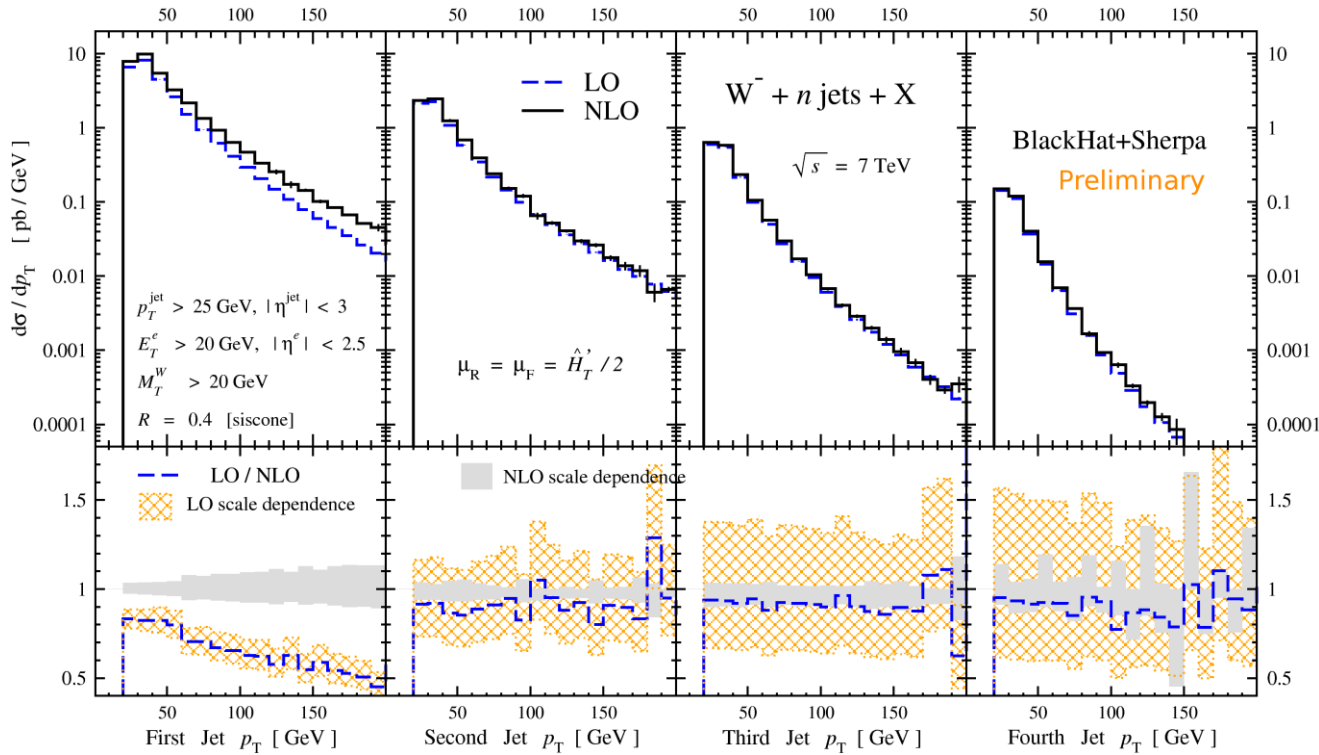
- *W/Z production*
- Higgs production
- *Z + 1 jet*
- vector boson pairs
- heavy quark pairs
- single top
- lepton pairs
- Higgs bosons in association with a W or Z

Merged Z and Z + 1 jet events [Alioli, Nason, Oleari, Re 10']



Multi-jet systematics: $W+n$ jets.

W^-+n jet+X softest jet p_T spectrum
 [BlackHat, preliminary]



- Reduction of cross-section by power of strong coupling for each added jet.

- Jets prefer lowest p_T .

- Growth of LO scale variation and NLO reduction.

- Complete input for MC@NLO approaches for $W+4$ jets

Multi-jet systematics: jet-algorithms Z+n jets.

CDF: Phys. Rev. Lett. 100, 102001 (2008)
 [BlackHat: 0912.4927, 1004.1659]

See also talk by J. Huston

σ in [fb]

# of jets	LO parton SISCONE	NLO parton SISCONE	LO parton anti- k_T	NLO parton anti- k_T	Non-pert correction
1	$4635(2)^{+928}_{-715}$	$6080(12)^{+354}_{-402}$	$4635(2)^{+928}_{-715}$	$5783(12)^{+257}_{-334}$	~ 1.1
2	$429.8(0.3)^{+171.7}_{-111.4}$	$564(2)^{+59}_{-70}$	$481.2(0.4)^{+191}_{-124}$	$567(2)^{+31}_{-57}$	~ 1.2
3	$24.6(0.03)^{+14.5}_{-8.2}$	$35.9(0.9)^{+7.8}_{-7.2}$	$37.88(0.04)^{+22.2}_{-12.6}$	$44.9(0.3)^{+4.7}_{-7.1}$	~ 1.4

σ (stat) \pm scale var

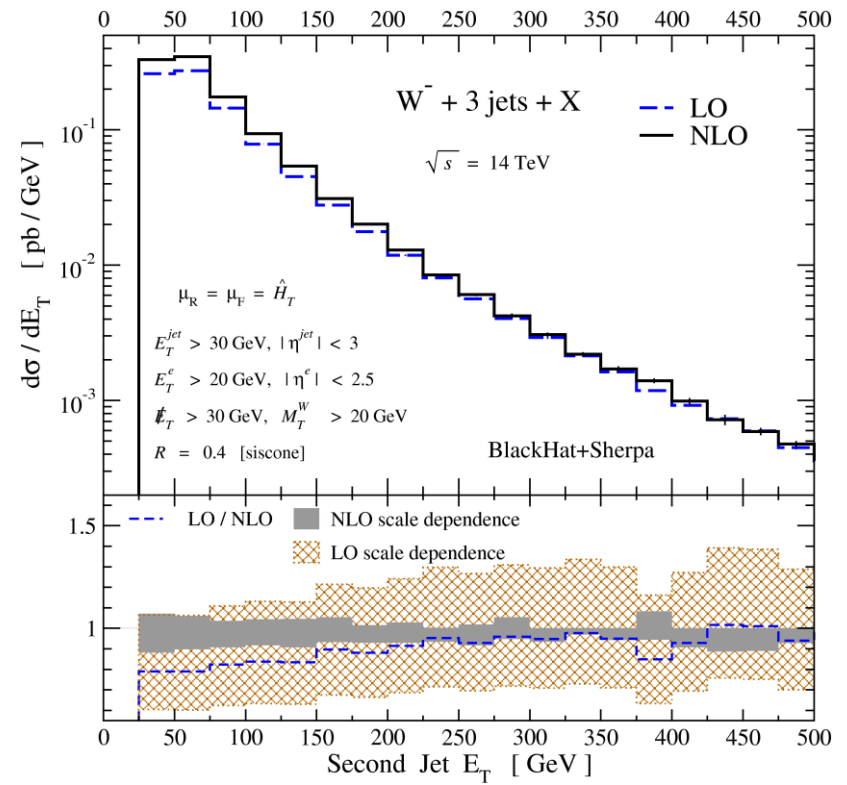
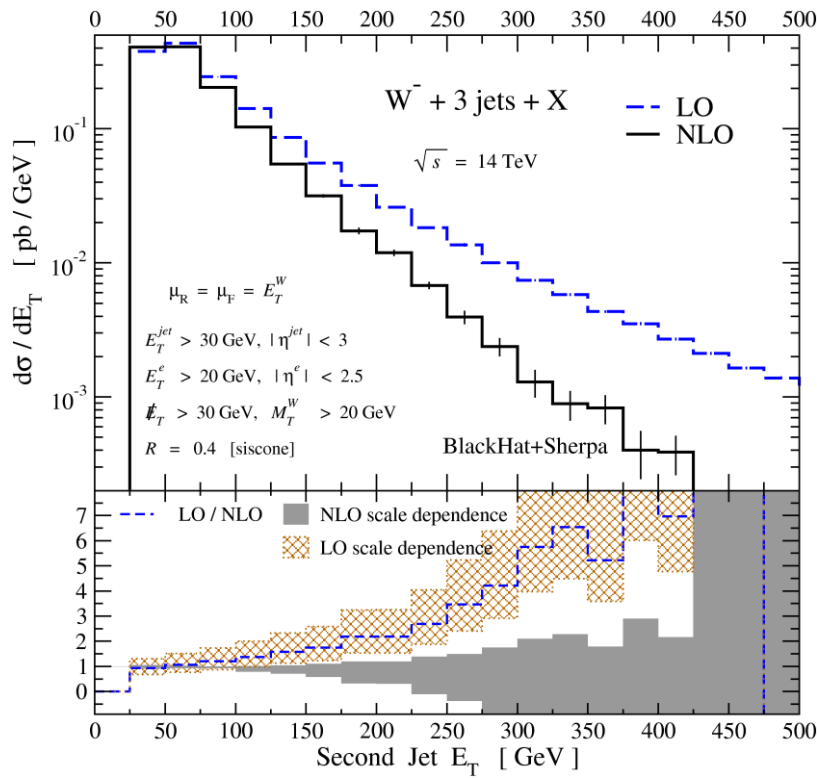
# of jets	CDF	Need non-perturbative corrections to		
		Is there a best value for R?		
1	7003 \pm study	Jet alg R	Non-pert corr	
2	695 \pm study	CDF: W+n jets	R=0.4	<10%
3	60 \pm study	CDF: Z+n jets	R=0.7	10-40%

$\sigma \pm$ stat \pm sys \pm lum

Scale Choices

- Need to choose scales **event-by-event**
- Functional form of scale choice is also important

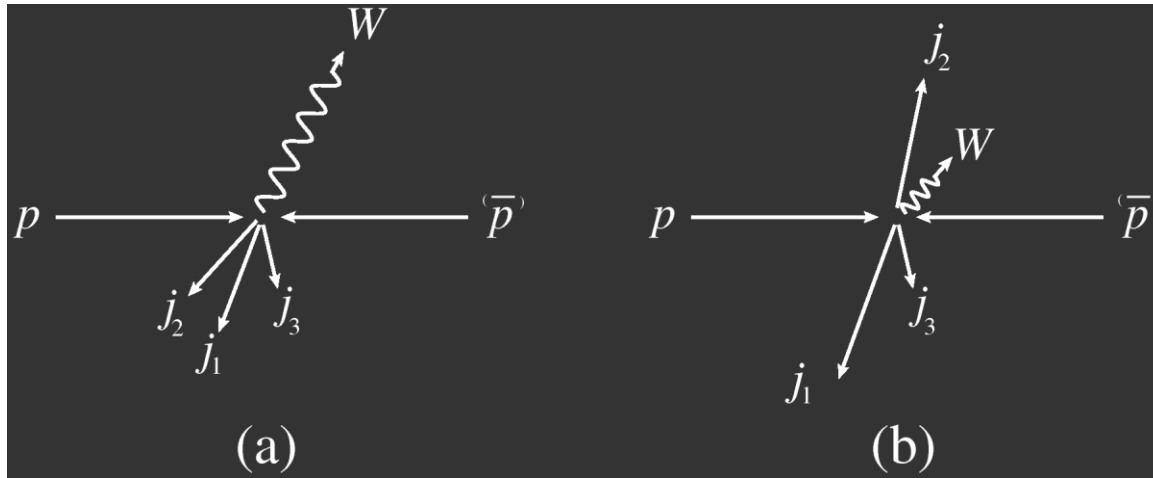
Bauer, Lange 09';
BlackHat 09'



- E_T^W is not suitable; \hat{H}_T is

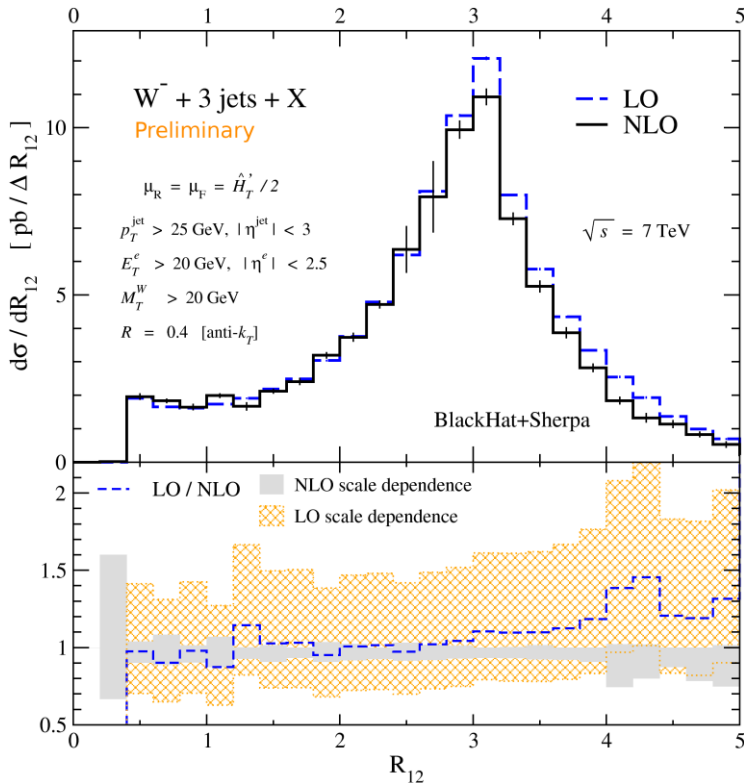
Scale Choices

- E_T^W is not suitable; \hat{H}_T is



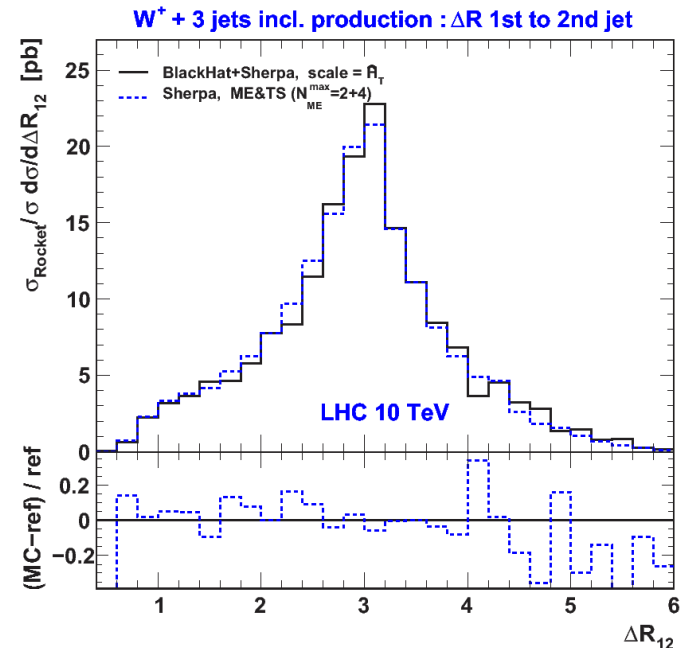
- NLO calculation is **self-diagnosing**, LO isn't
- In the absence of an NLO calculation, should **use a scale like \hat{H}_T**

Shape change: **W+3jets**.



- $\Delta R(1^{\text{st}}, 2^{\text{nd}})$ jet
- Physics of leading jets not modeled well at LO: additional radiation allows jets to move closer
 \Rightarrow Shapes can change!

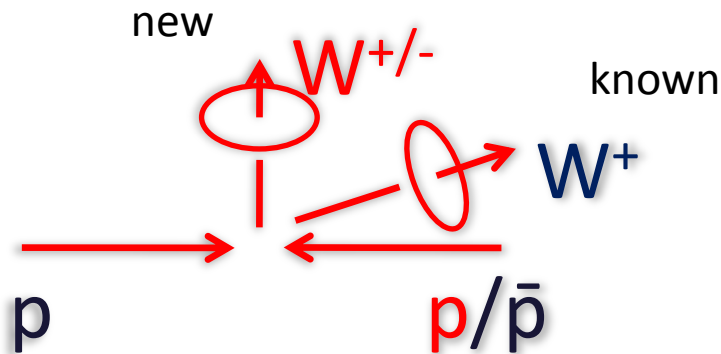
- compare: Les Houches study [Hoche, Huston, Maitre, Winter, Zanderighi, 10'] comparing to SHERPA with ME matching & showering



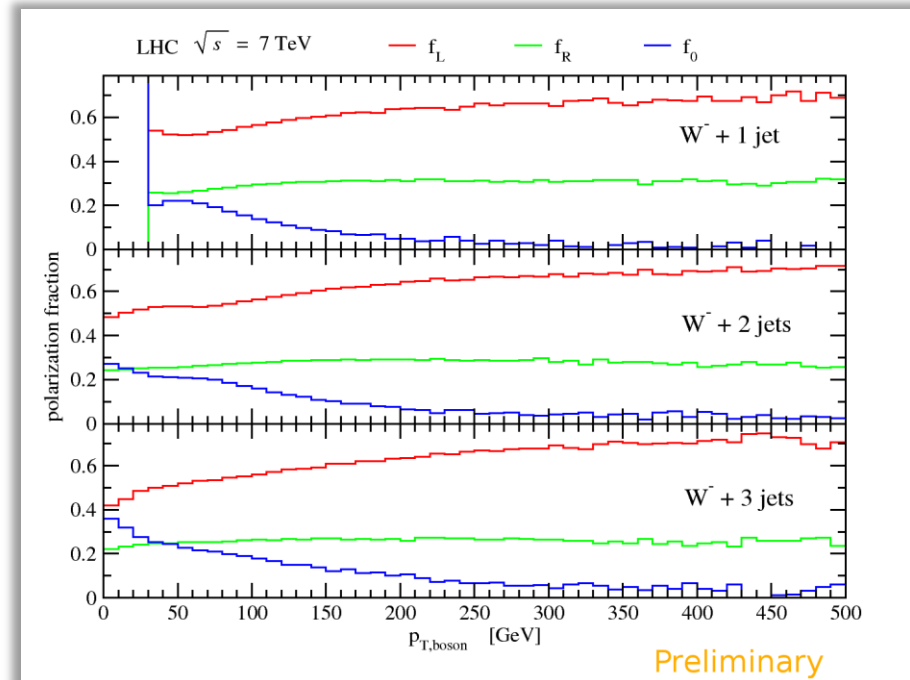
High- E_T W Polarization

- Polarization of *low- p_T* , longitudinal, W s is textbook material [Ellis, Stirling & Webber] \Rightarrow dilution in charged-lepton rapidity distribution asymmetry at Tevatron

- This is a *different* effect! W s are also polarized at *high p_T*
- **Universal:**
 - Present at LO
 - Present for fewer jets too

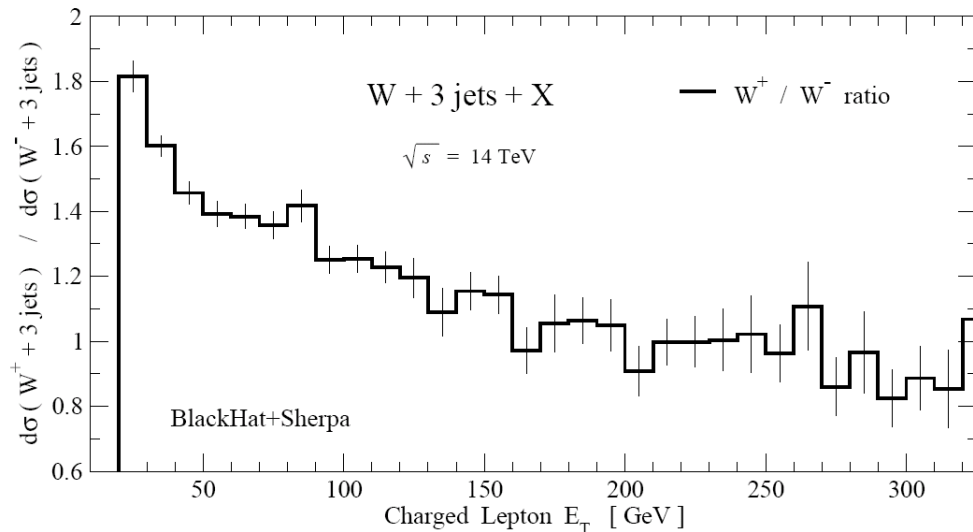


[BlackHat 09',10']

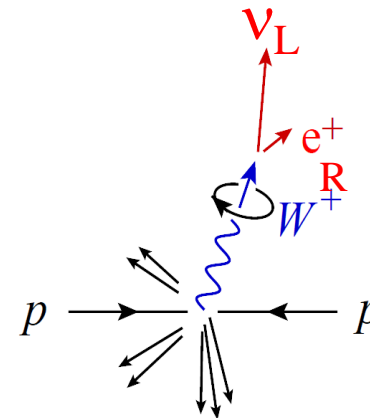


High- E_T W Polarization: analyzed by leptons

Ratio: E_T of e^+ over E_T of e^- [BlackHat 09']



- W Polarization analyzed by leptons:

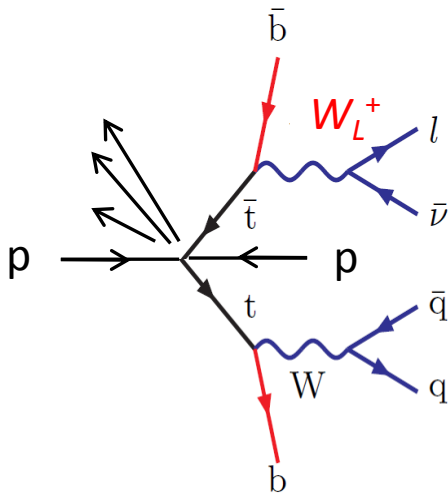


$\Rightarrow E_T$ dependence of e^+/e^- ratio
and missing E_T in W^+/W^- at LHC.

- Useful for distinguishing “prompt” W s from daughter W s in top decay (or new heavy-particle decays)!

High- E_T W Polarization

Semi-leptonic $t\bar{t}$ -decay



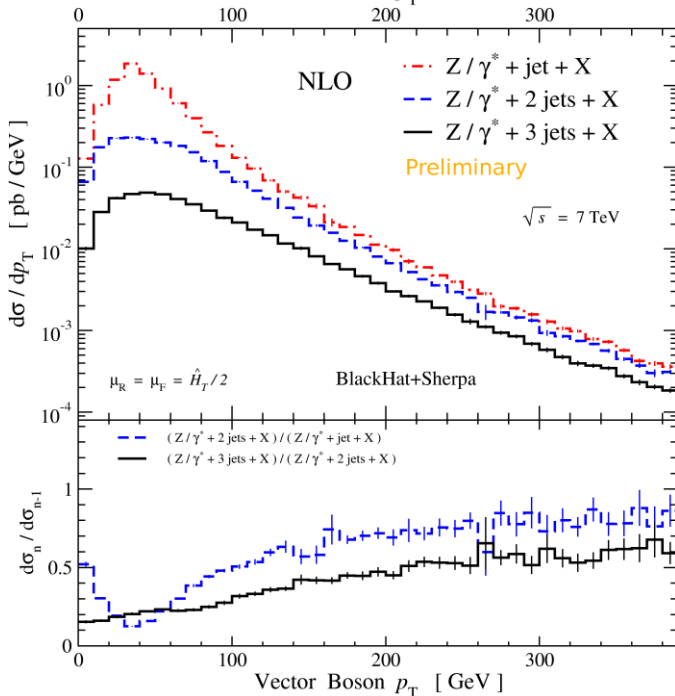
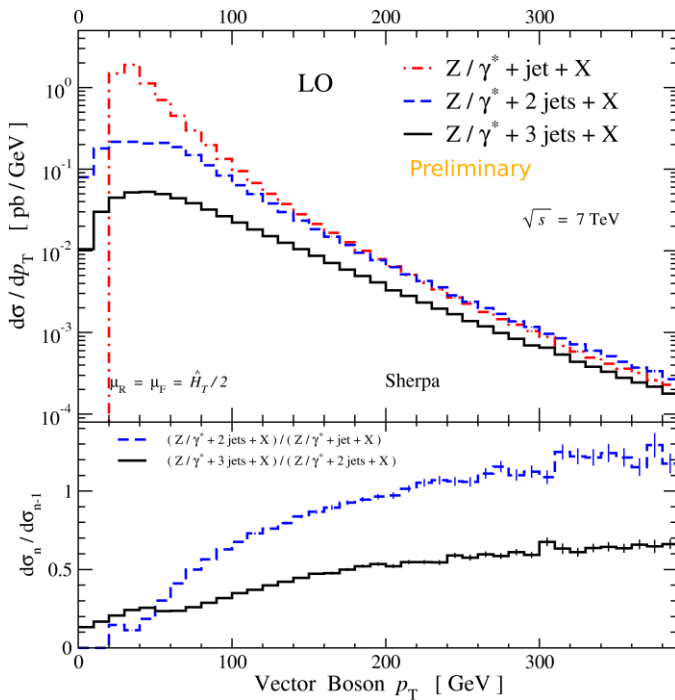
+ charge conjugate decay

- Semi-leptonic **top** decay involves **left-handed** W^+
- But charge conjugate **top** decay involves **right-handed** W^-

\Rightarrow Electron and positron have **almost identical** p_T distributions.

Nice handle on separating W + jets from semi-leptonic **top** pairs.

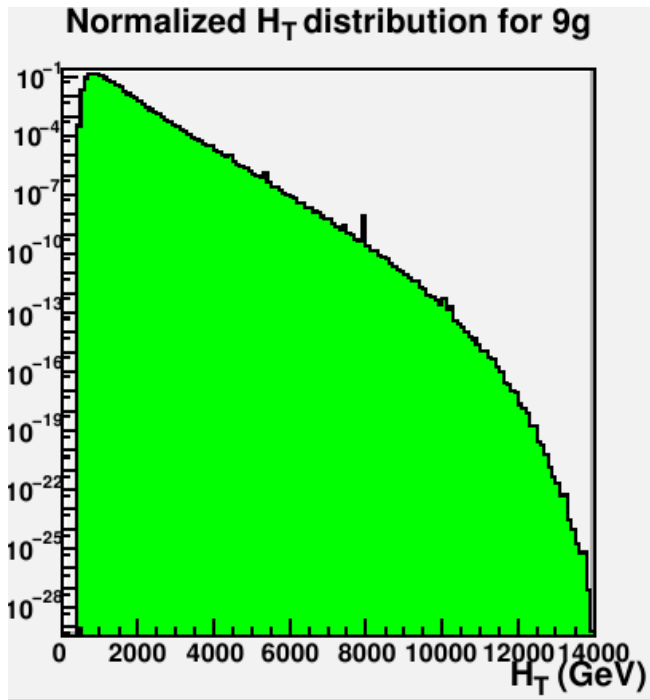
Jet-Production Ratios: Z+jets.



- Ratios of jet cross sections should be less sensitive **jet energy scale** and **non-pert corrections**
- Ratios are stable LO→NLO
- But hide a lot of structure in differential distributions:
 - Kinematic constraints at low p_T in 2/1
 - Factorization & IR $\ln(p_T/\rho_{T \min})$ s at intermediate p_T
 - Phase-space & pdf suppression at higher p_T .

Interesting developments

J. Winter and W. Giele 09';
Here LO; total NLO in progress



Multi-jet computation time-consuming:

- need to integrate over multi particle phase space
- amplitudes themselves take longer to evaluate

Or get efficiency gain from graphics cards?

[Hagiwara et al '09, Giele, Stavenga & Winter '09-10]

Generation of ROOT tuples: [Huston,...; BlackHat in progress]

- Re-analysis possible
- Distribute distributions
- Flexibility for studying scale variations
- Flexibility for computing error estimates associated with PDFs

Conclusions

- NLO calculations required for reliable QCD predictions at the Tevatron and LHC
- **New efficient computational approaches** to one-loop QCD amplitudes, exploiting **unitarity & factorization properties**, are now method of choice for important LHC backgrounds.
- Many new processes: $W/Z + 1,2,3,4$ jets, $tt + 1,2$ jets, $VV+1,2$ jets,... now known at NLO!
- Most complex NLO results are still at **parton level** and not embedded in **a full Monte Carlo**. **Best use** of these results may sometimes be via **ratios** – as aids to data-driven analysis of backgrounds. Interesting recent progress from **NLO parton-shower** approaches.
- Discussed some new understanding from multi-jet NLO for $V+n$ jets: **scale choices, jet-algorithms**,...
- Left-handed **W polarization** large and universal and allows to, leading to further charge-asymmetric effects in $W + n$ jets.

Thanks.