

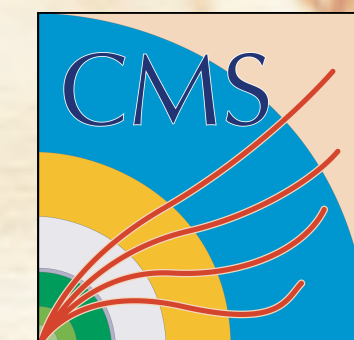
BTTB9  
10/02/2021

# Electromagnetic performance of CMS HGCAL in beam tests

**Matteo Bonanomi**

(LLR, Ecole Polytechnique, CNRS)

On behalf of the HGCAL Beam Tests group





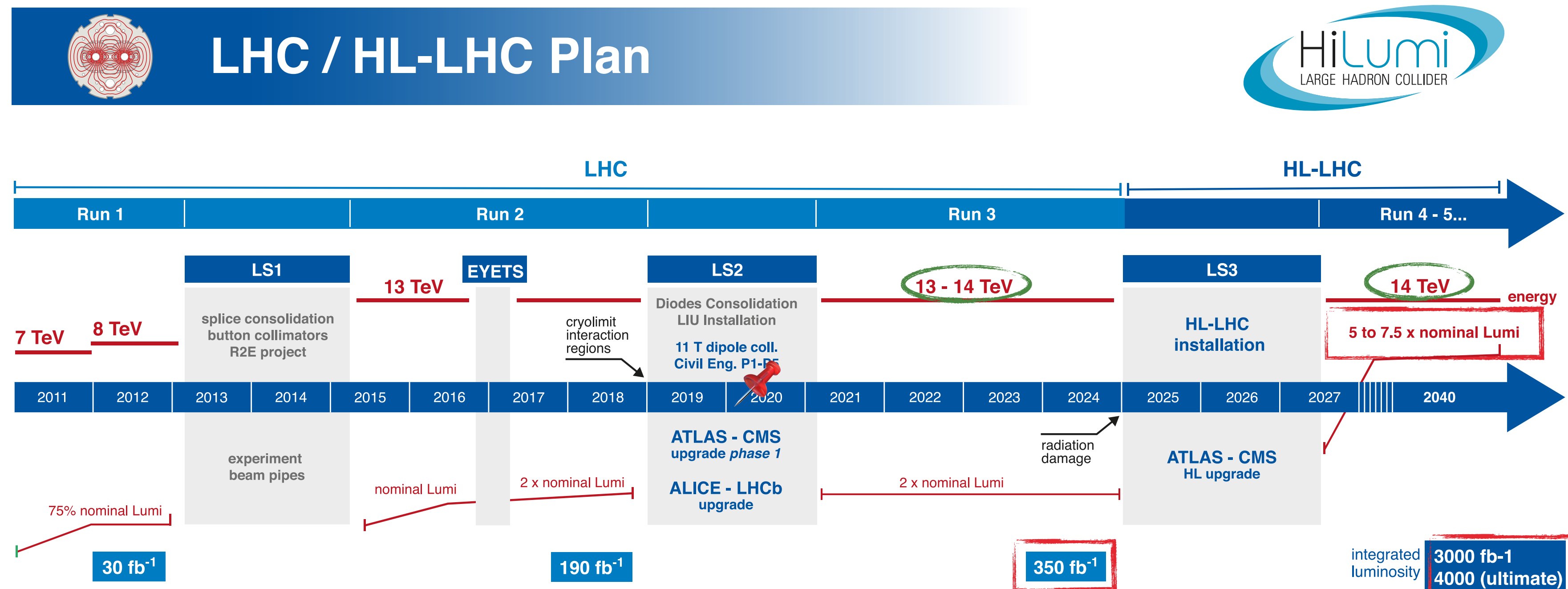
# The High-Luminosity LHC



- In 2027 CERN is intended to start the **High-Luminosity LHC** program:
- **HL-LHC** will integrate **5 (10) times the instantaneous** (integrated) **luminosity** of LHC:

**UP!** **High pile-up rate:** evts/bunch-crossing from  $\sim 70$  in LHC to  $O(140/200)$  in HL-LHC!

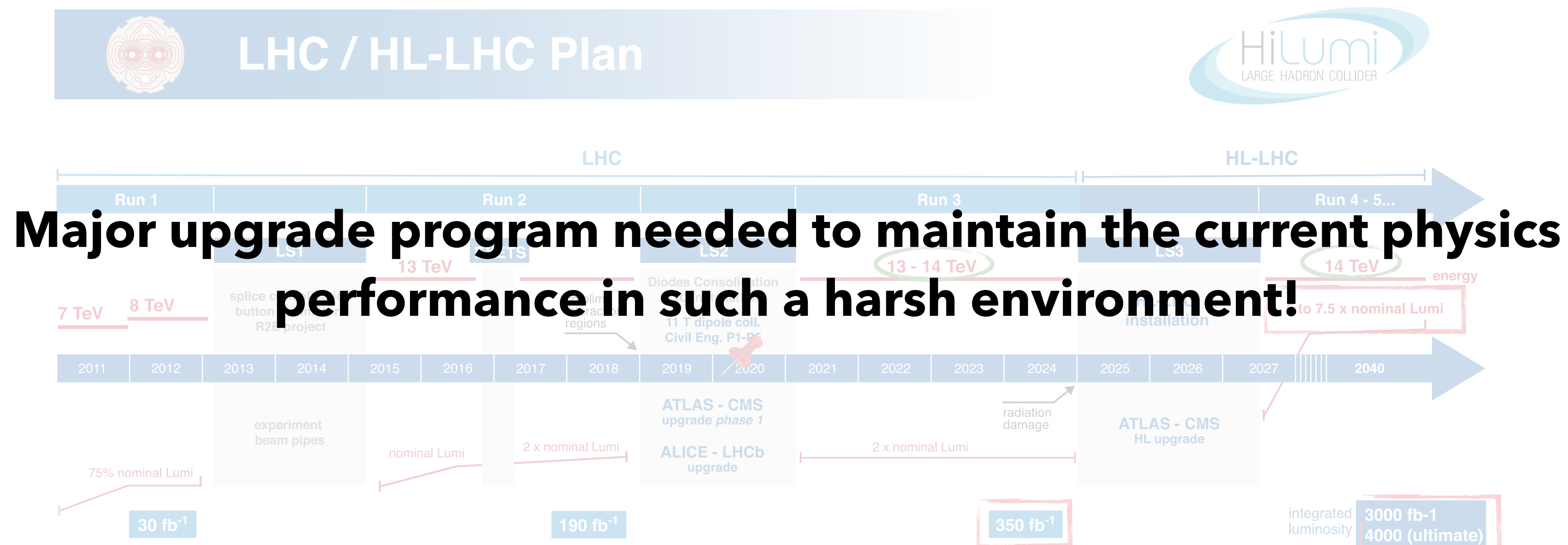
**☢** **Unprecedented radiation levels:** doses up to 2 MGy and fluences up to  $10^{16}$   $n_{eq}/cm^2$



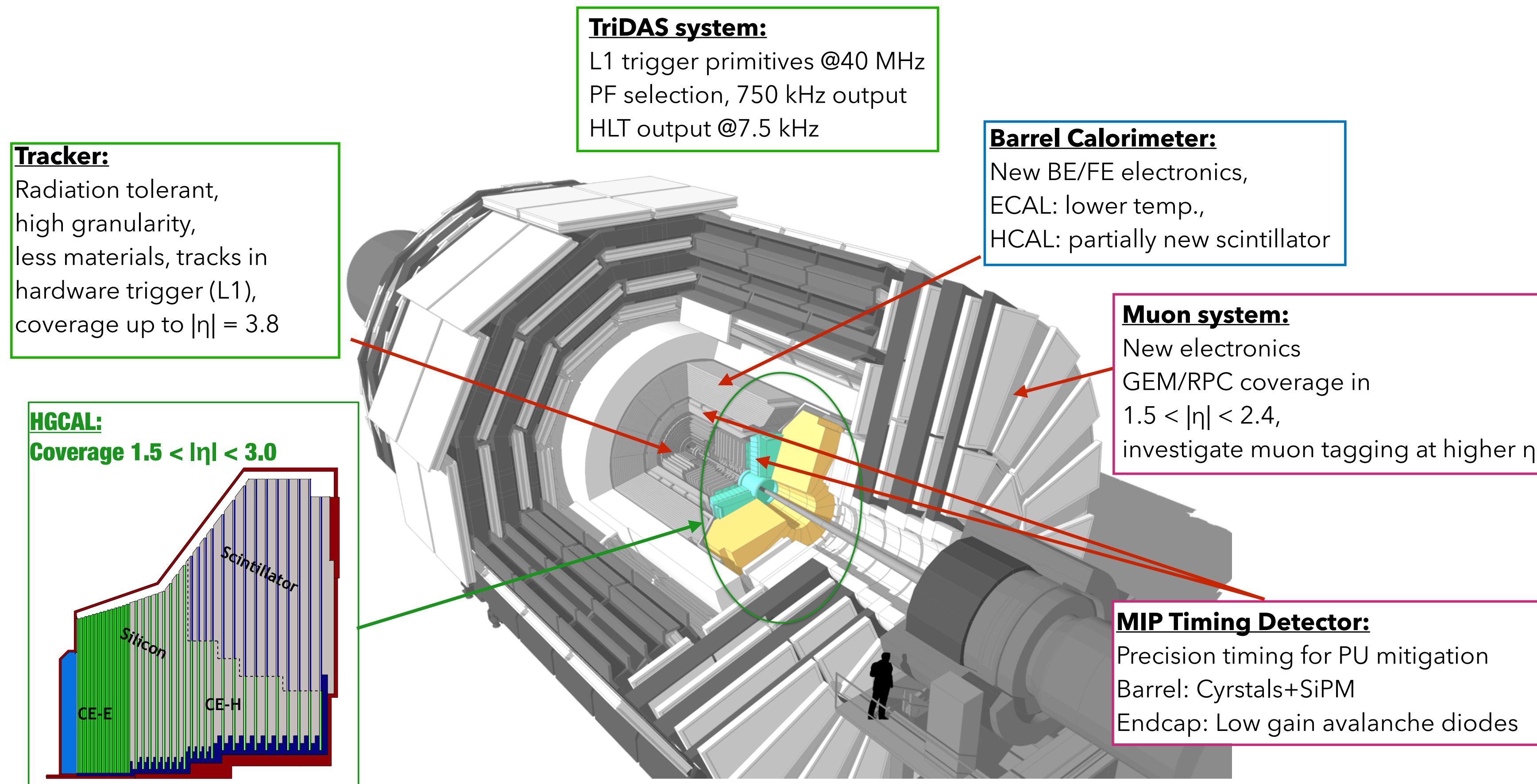
# The High-Luminosity LHC



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  - ☢ **Unprecedented radiation levels:** doses up to 2 MGy and fluences up to  $10^{16} \text{ n}_{\text{eq}}/\text{cm}^2$



# The CMS Upgrades for HL-LHC



**UP!** High granularity and precise timing to mitigate pile-up

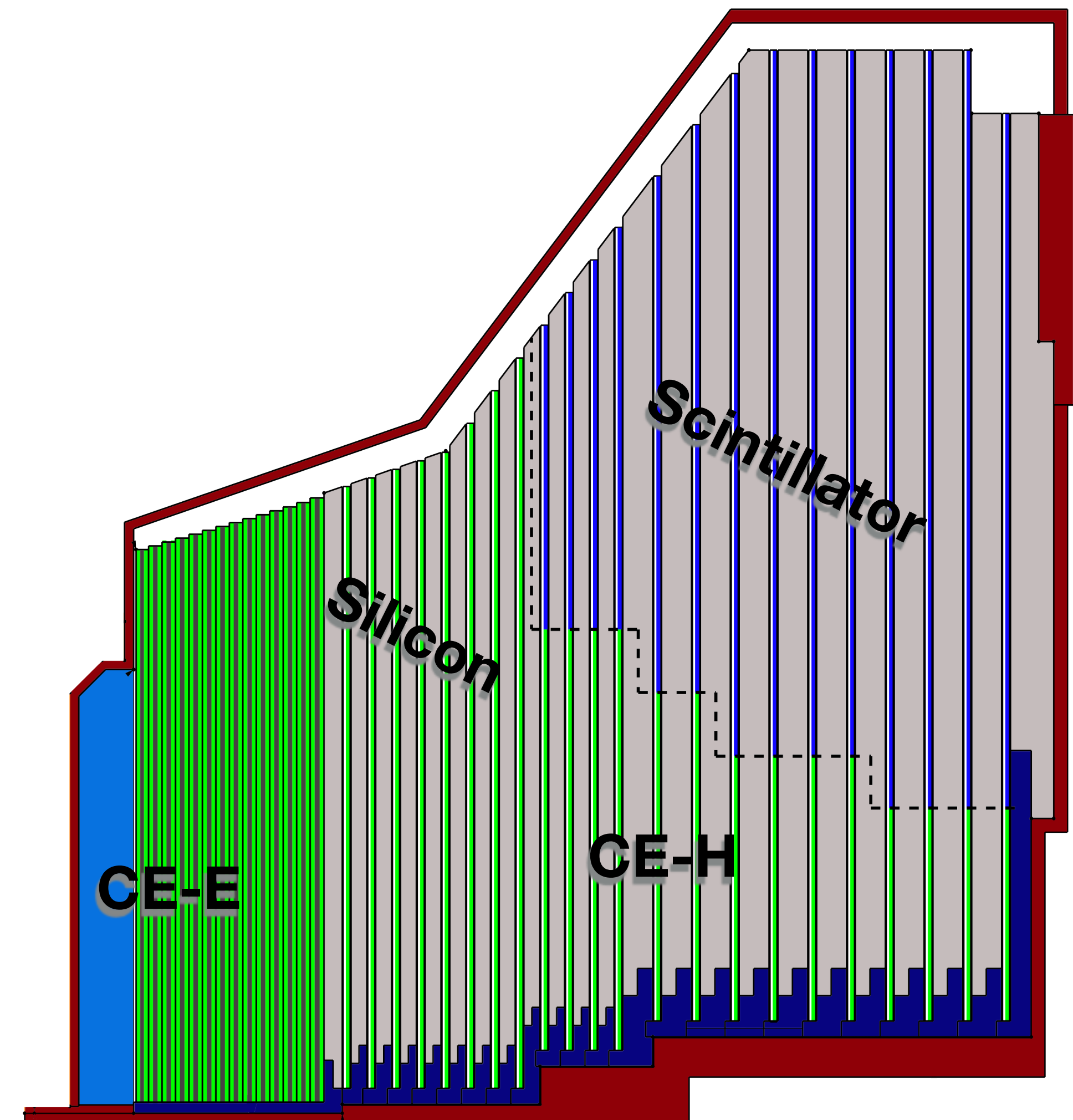
**Radiation hard detector material to cope with large dose**



# HGCAL: a novelty in calorimetry



- New **endcap calorimeter** of CMS:
  - ▶ Need to replace **ECAL** crystals and **HCAL** scintillators as they were **designed for 500 fb<sup>-1</sup>**
- **High precision energy measurements:**
  - ▶ Missing energy/precision resolution;
- **Ideal detector for Particle Flow;**
- Fully utilise **timing\*** (real novelty in calorimetry!);
- **5D (imaging) calorimeter:**
  - ▶ Energy, time, x, y, z



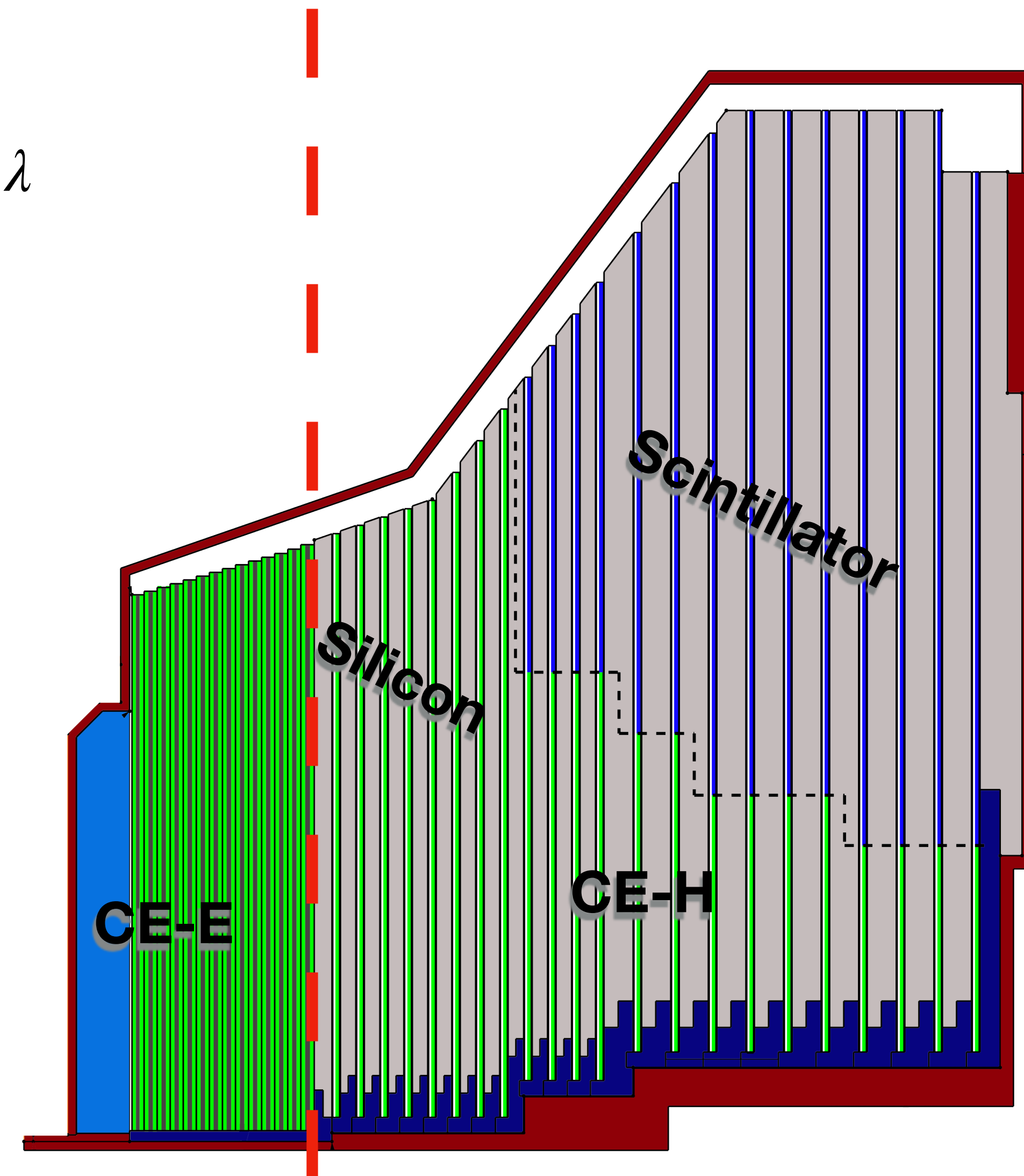
\* See Rohith talk for results on timing performance in TB



# HGCAL in numbers

Sampling calorimeter consisting of:

- 28 layers **Si-based** EM compartment (CE-E),  $\sim 25X_0$  and  $\sim 1.3\lambda$
- 22 layers hadronic compartment (CE-H):  
**Si-based** + Scintillator tiles,  $\sim 8.5\lambda$





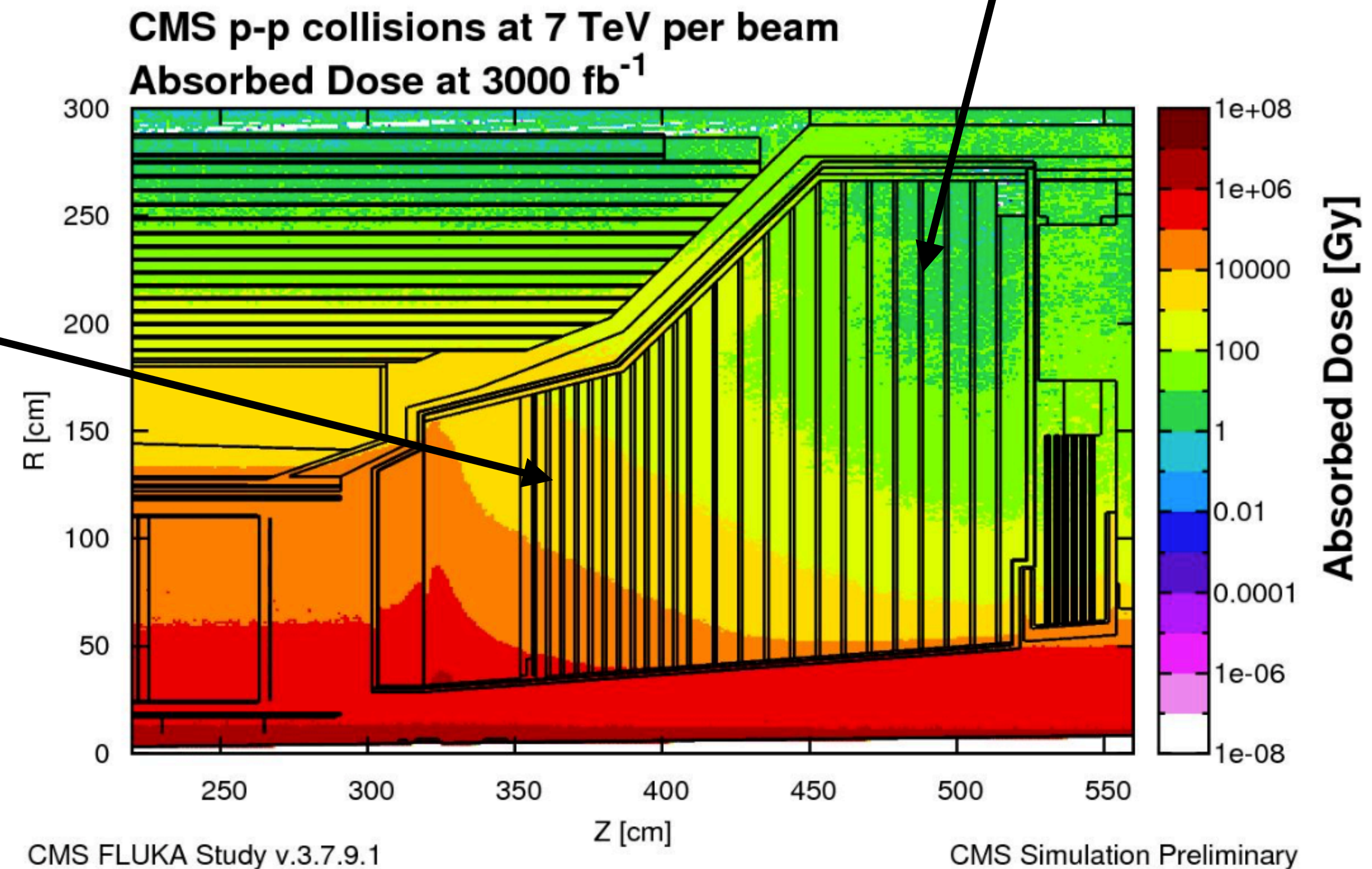
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**Si-based** + Scintillator tiles,  $\sim 8.5\lambda$

**Si is radiation hard!**

**SiPM tiles\***



\* See Malinda talk for results with SiPM tiles



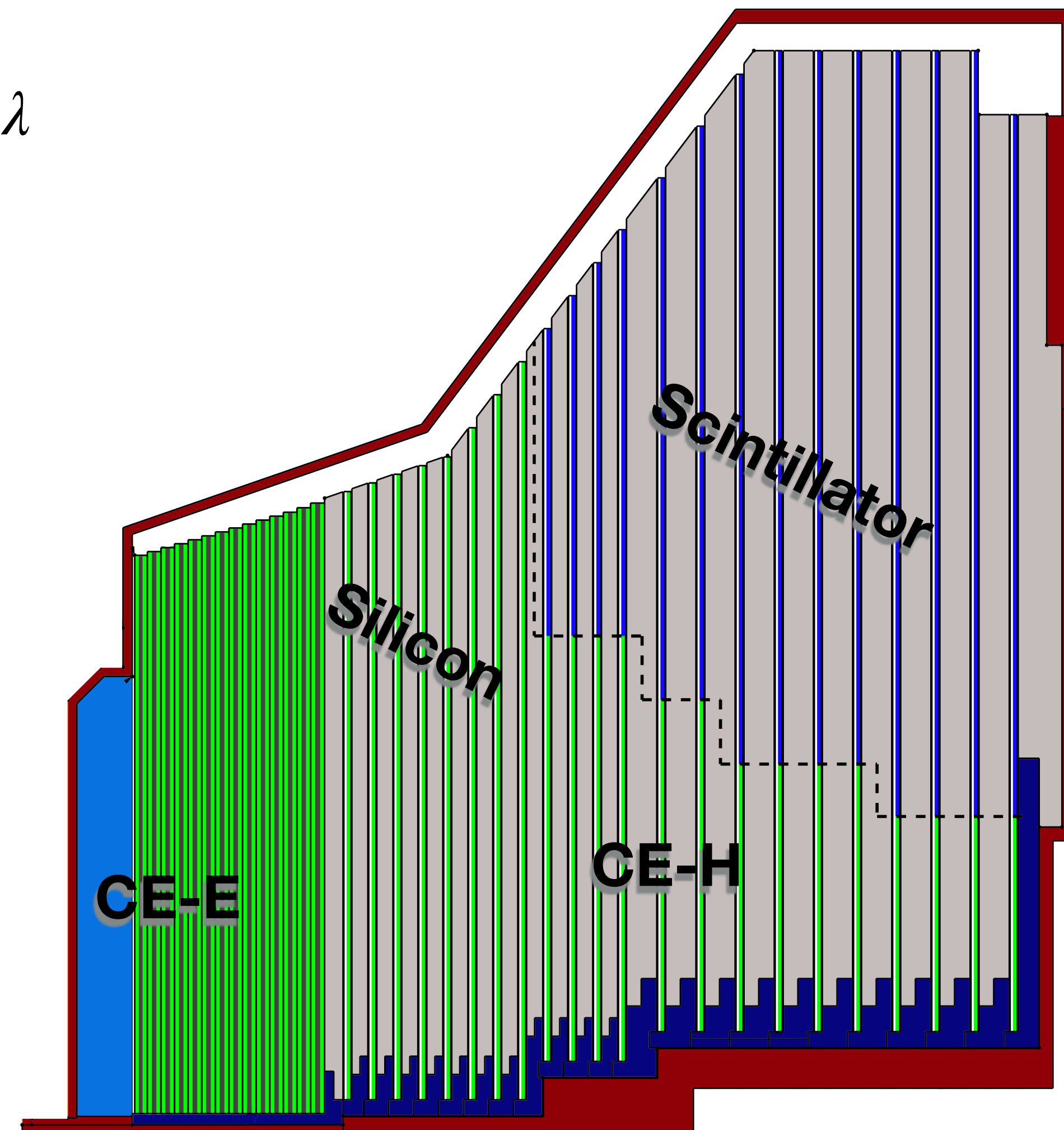
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- 22 layers hadronic compartment (CE-H):  
**Si-based** + Scintillator tiles,  $\sim 8.5\lambda$

- Coverage:  $1.5 < |\eta| < 3.0$
- **$\sim 620 \text{ m}^2$  Si** sensors in  $\sim 30\text{k}$  channels;
- **6M Si channels** of  $0.5/1 \text{ cm}^2$  cell size;
- **$\sim 400 \text{ m}^2$  of scintillators** in 4k boards;
- $\sim 240\text{k}$  scintillators channels,  $4\text{-}30 \text{ cm}^2$  cell size;

 Operating temperature:  $-35 \text{ }^\circ\text{C}$





A hand-drawn sketch in brown ink on a light background. The central focus is a circular structure with a complex internal layout of rectangular and square sections, possibly representing a particle accelerator or a large-scale testing facility. Several rectangular, box-like structures are arranged around the perimeter of this central area. In the background, a range of jagged mountains is sketched with fine lines. The overall style is that of a technical or conceptual drawing.

# BEAM TESTS

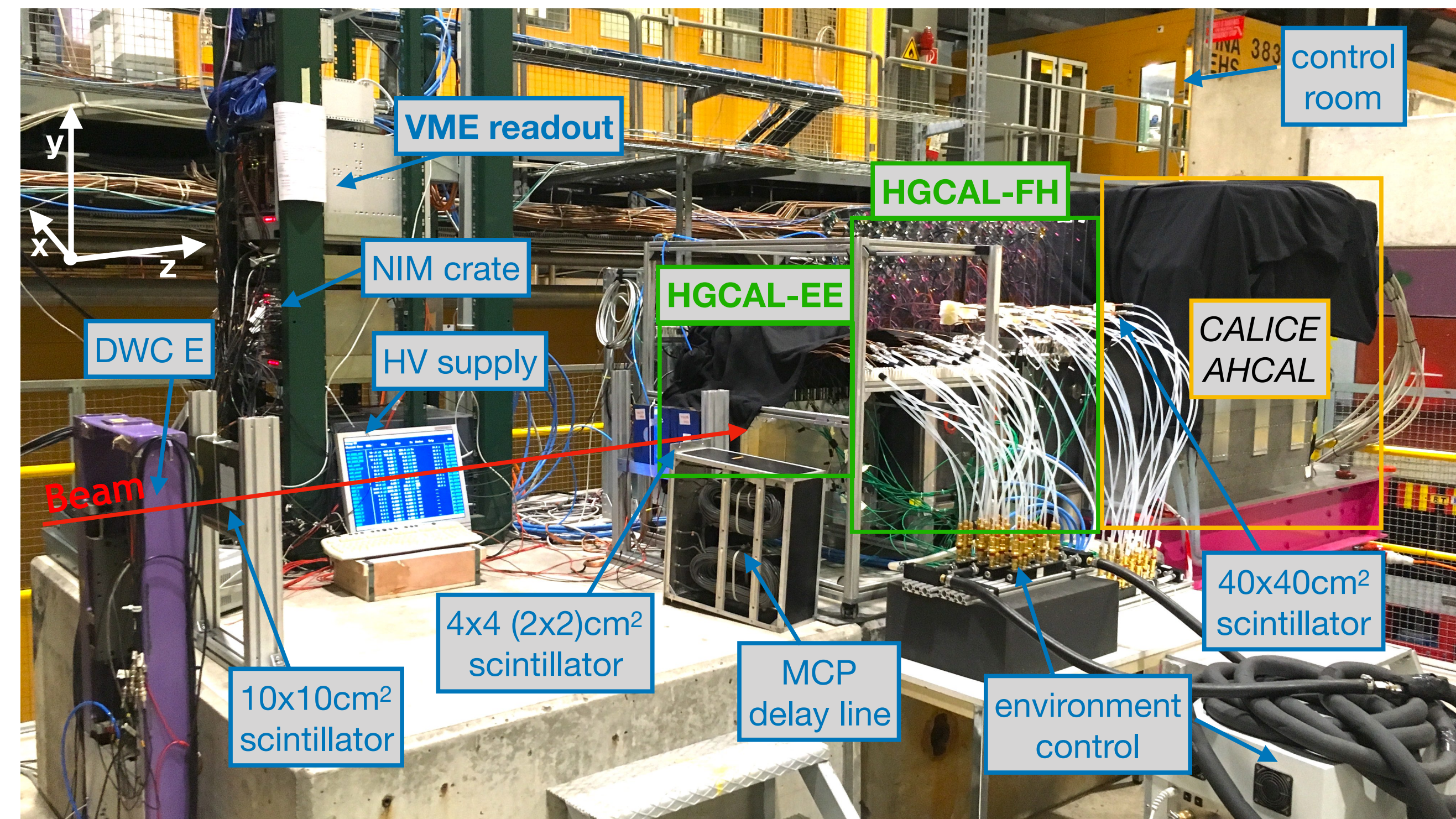


# October 2018: beam test @CERN-SPS



**Validation** of the **detector design** and assessment of **HGCAL performance**

- **First large scale prototype**
  - ▶ 28 layers CE-E
  - ▶ 12 layers CE-H
  - ▶ 39 layers CALICE AHCAL
- **Calibration with MIPs** and showers;
- **Physics performance** :  $e^+$  and  $\pi^-$  over a wide energy range (20-300 GeV);
- **Timing performance** from TOA.



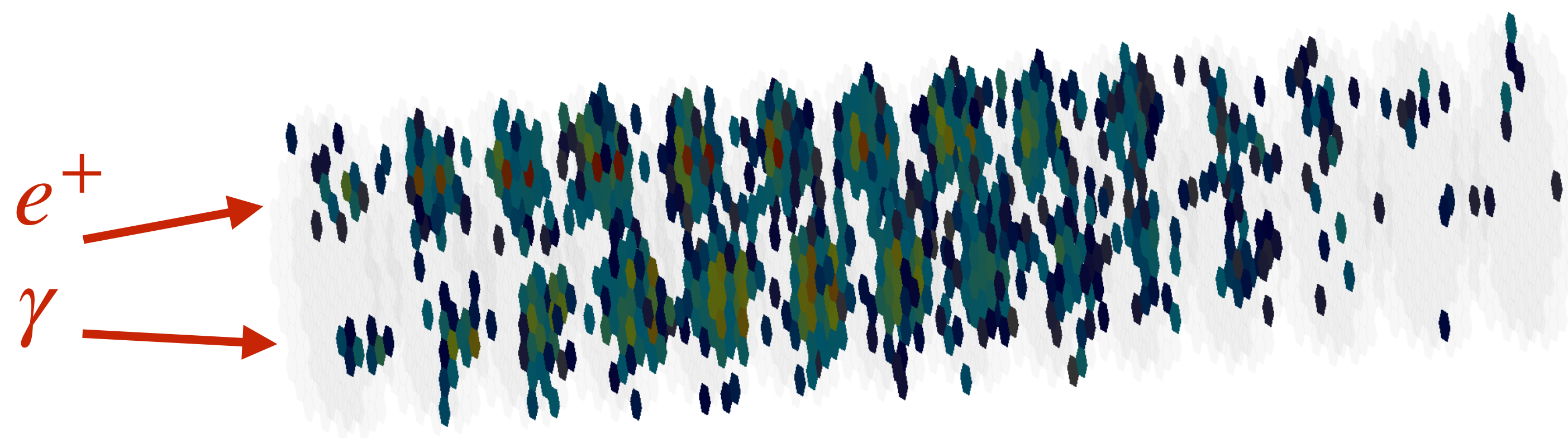
**$O(10^6)$  events collected!**



# Electrons performance in CE-E

Fine longitudinal and transverse granularities: **HGCAL is an *imaging* calorimeter**

June 2018 run 407 - event 1  
150 GeV/c  $e^+$  (poor beam)





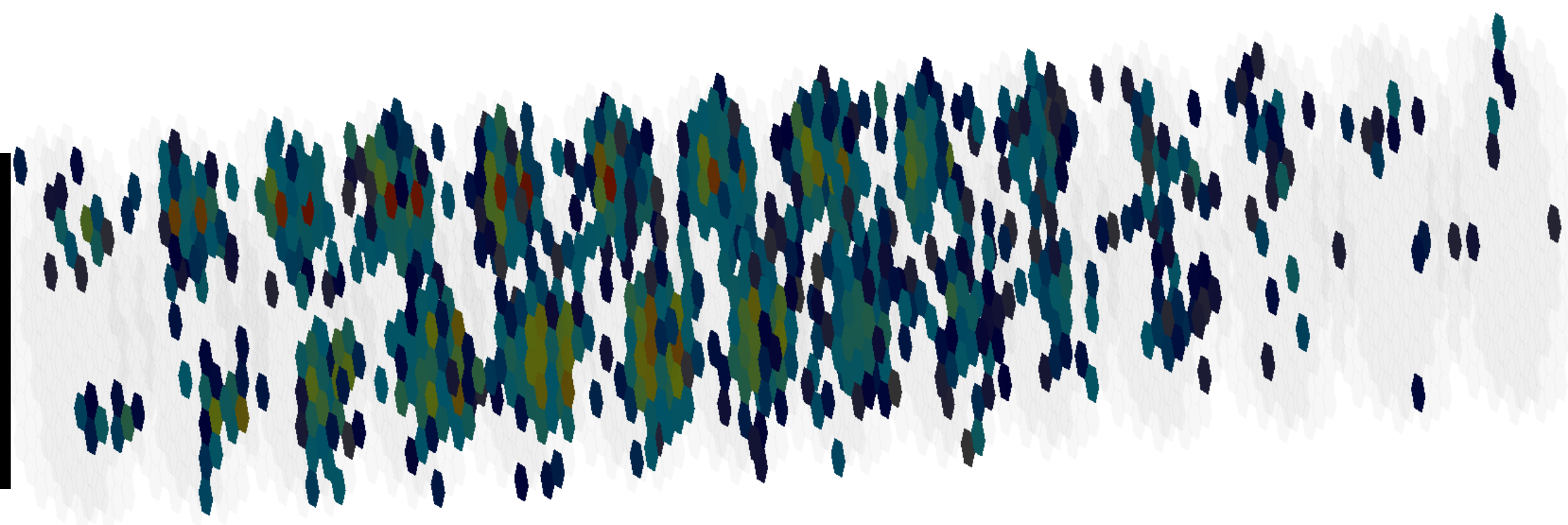
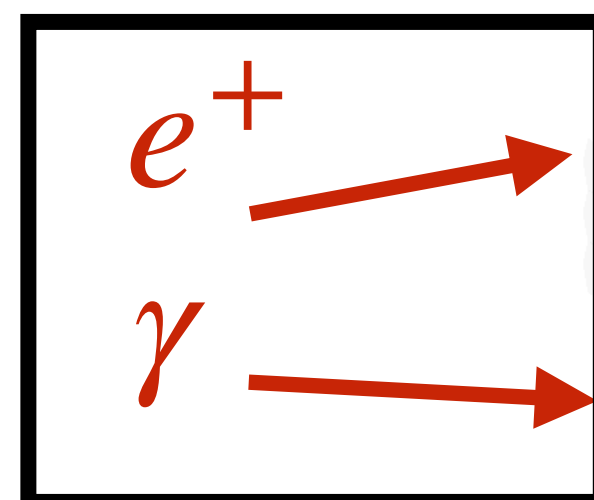
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Particle ID  
&  
Energy reco





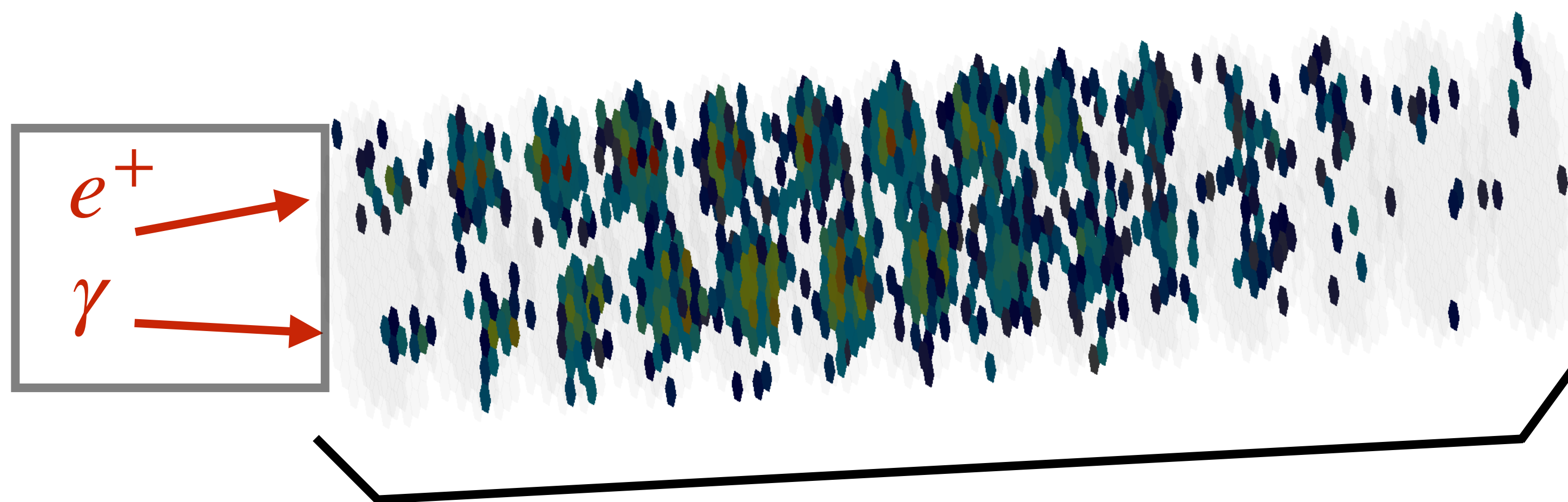
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Particle ID  
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Energy reco



Longitudinal shower shapes



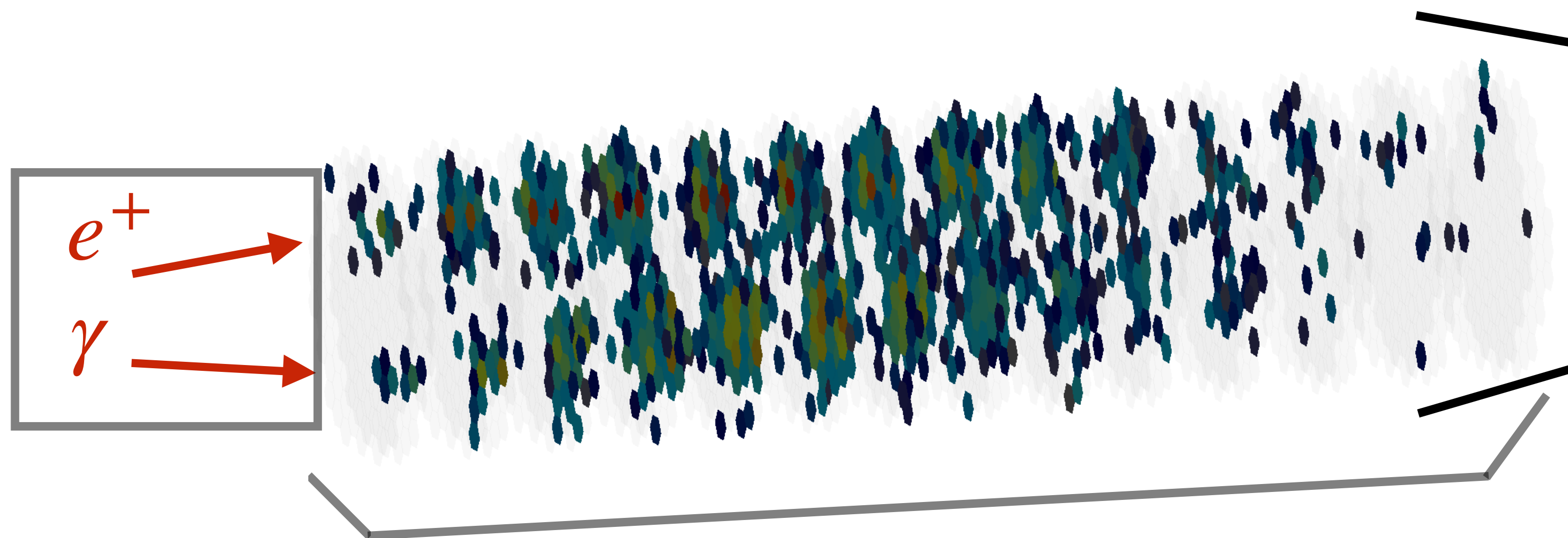
# Electrons performance in CE-E

Fine longitudinal and transverse granularities: **HGCAL is an *imaging* calorimeter**

June 2018 run 407 - event 1

150 GeV/c  $e^+$  (poor beam)

Particle ID  
&  
Energy reco



Transverse  
shower shapes

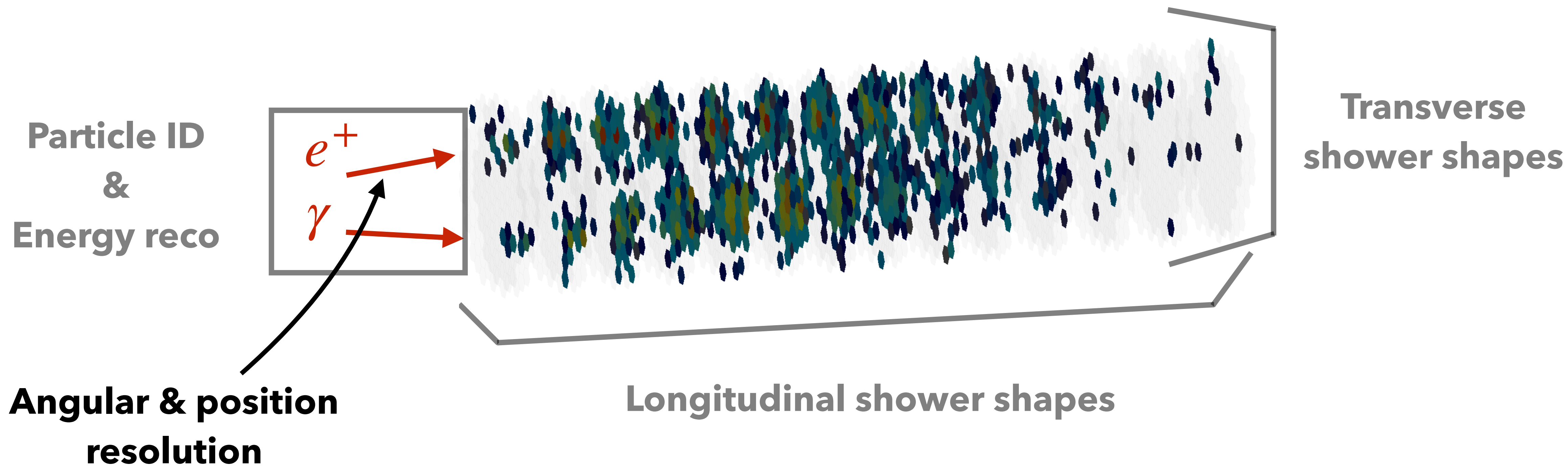
Longitudinal shower shapes



# Electrons performance in CE-E

Fine longitudinal and transverse granularities: **HGCAL is an *imaging* calorimeter**

June 2018 run 407 - event 1  
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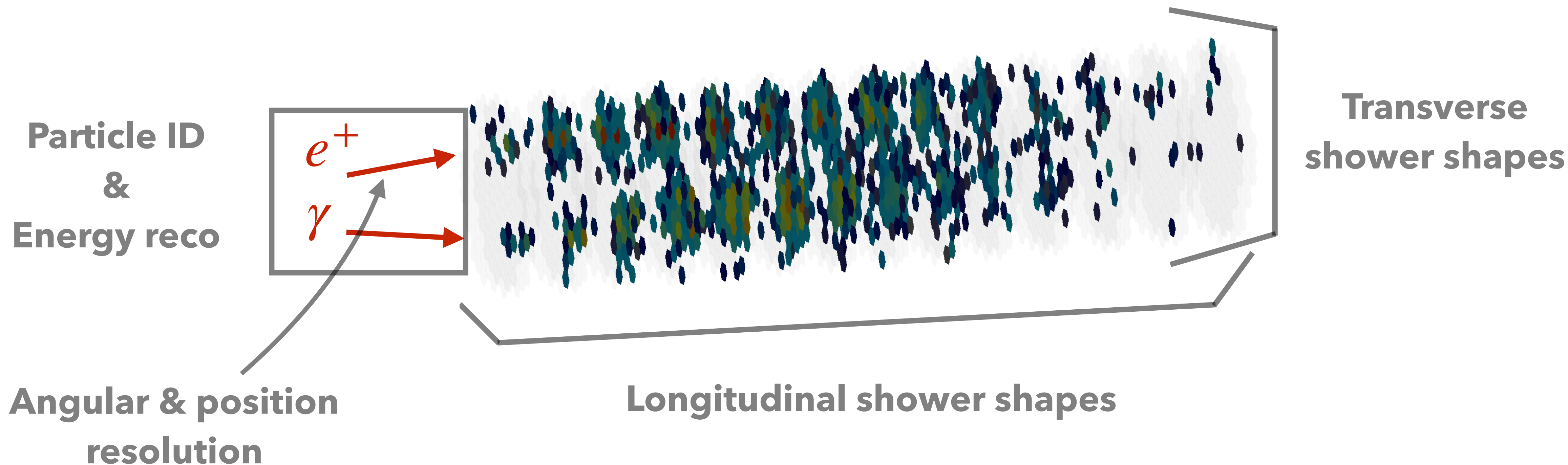




# Electrons performance in CE-E

Fine longitudinal and transverse granularities: **HGCAL is an *imaging* calorimeter**

June 2018 run 407 - event 1  
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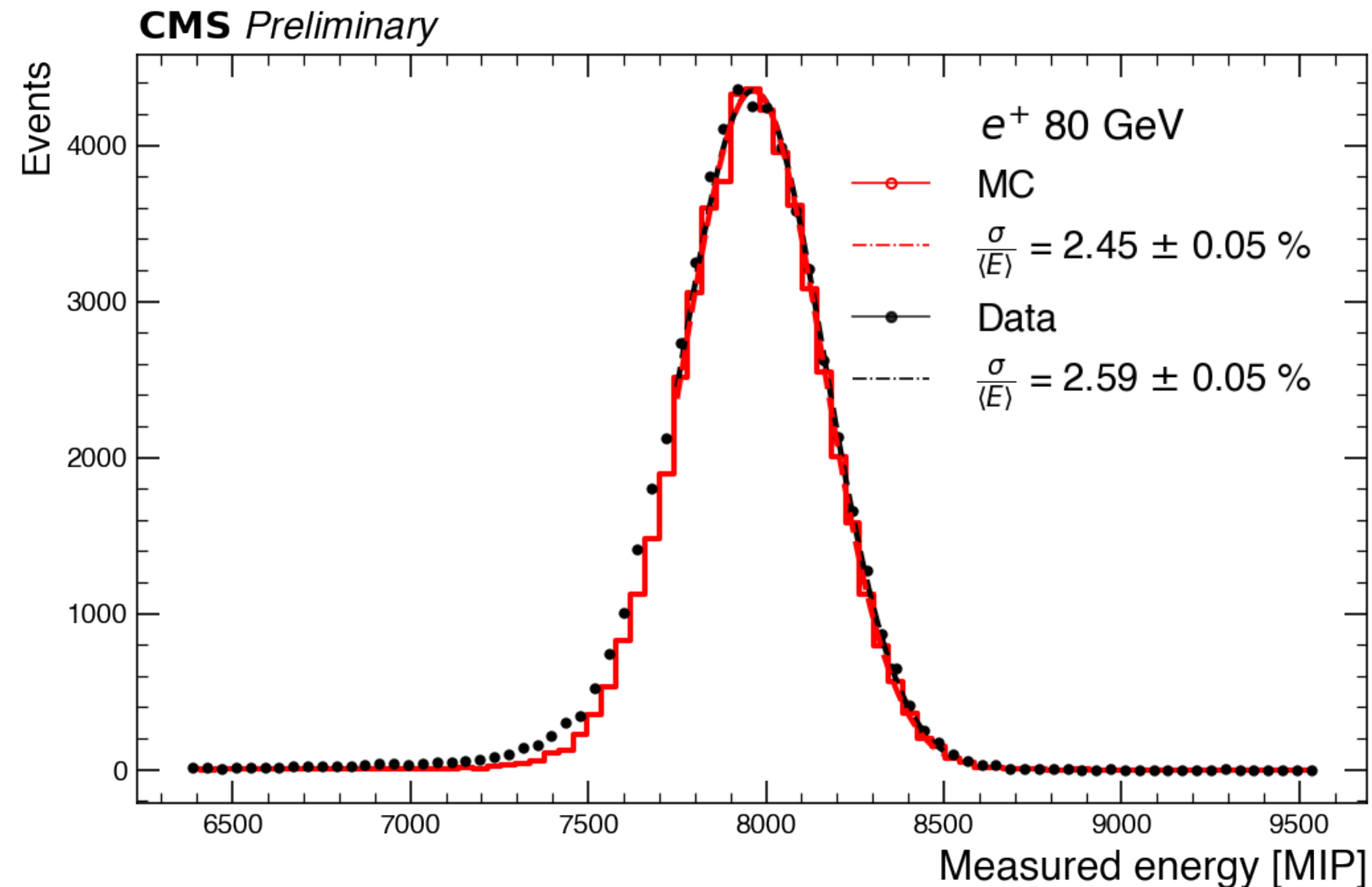
**Ideal detector for Particle Flow!**



# Electrons energy reconstruction



- **Different reconstructions** studied:  
**MIP** calibration, **dE/dx weights**,  
sampling fraction method (**SF**);
- **Energy distribution:** unclustered **energy sum** of the deposit **in all Si-pads**;
- **Gaussian fit** around the core region **to determine the energy resolution**  $\sigma_E/\langle E \rangle$
- **Good Data/MC agreement** throughout the full energy range;





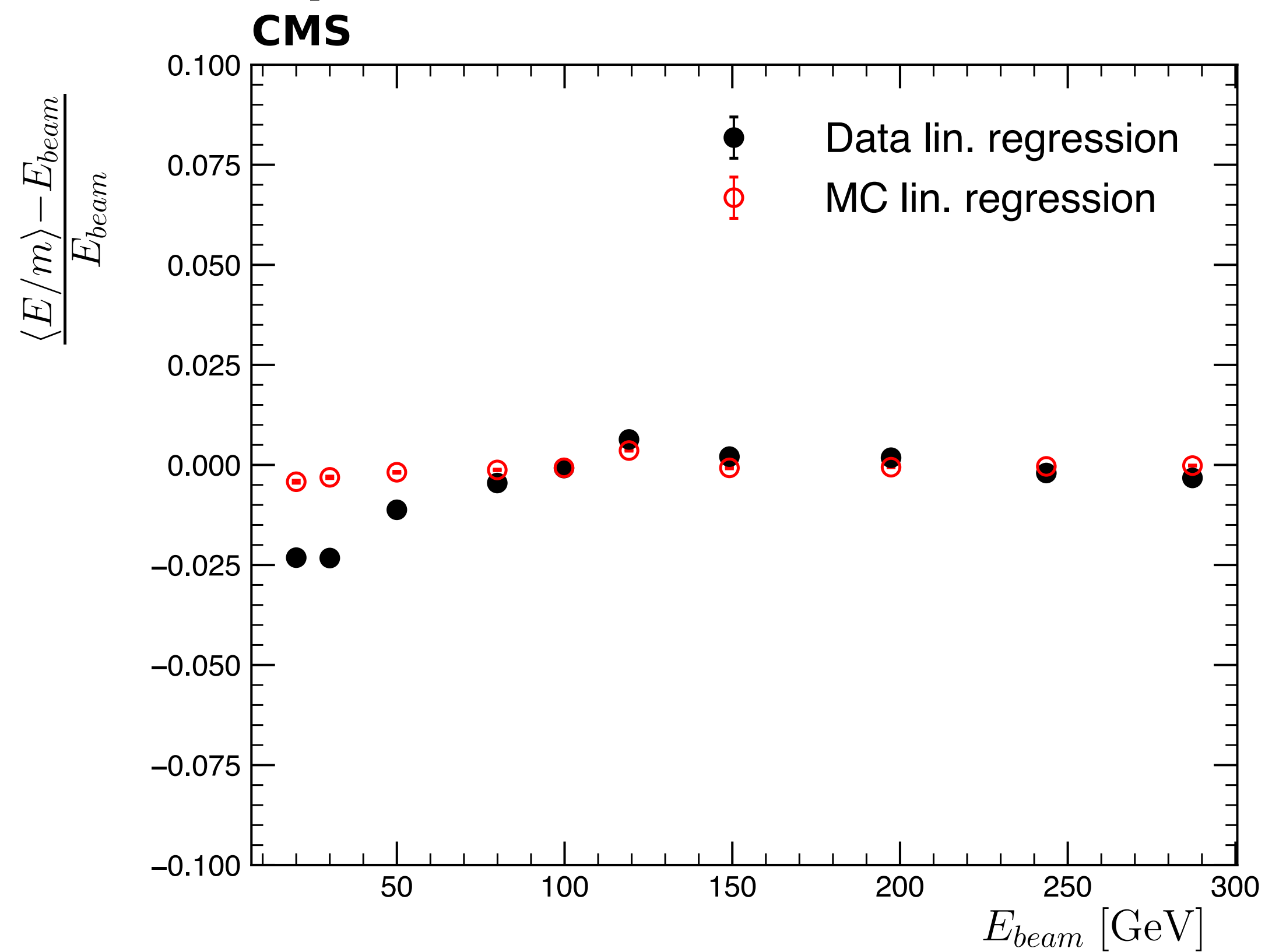
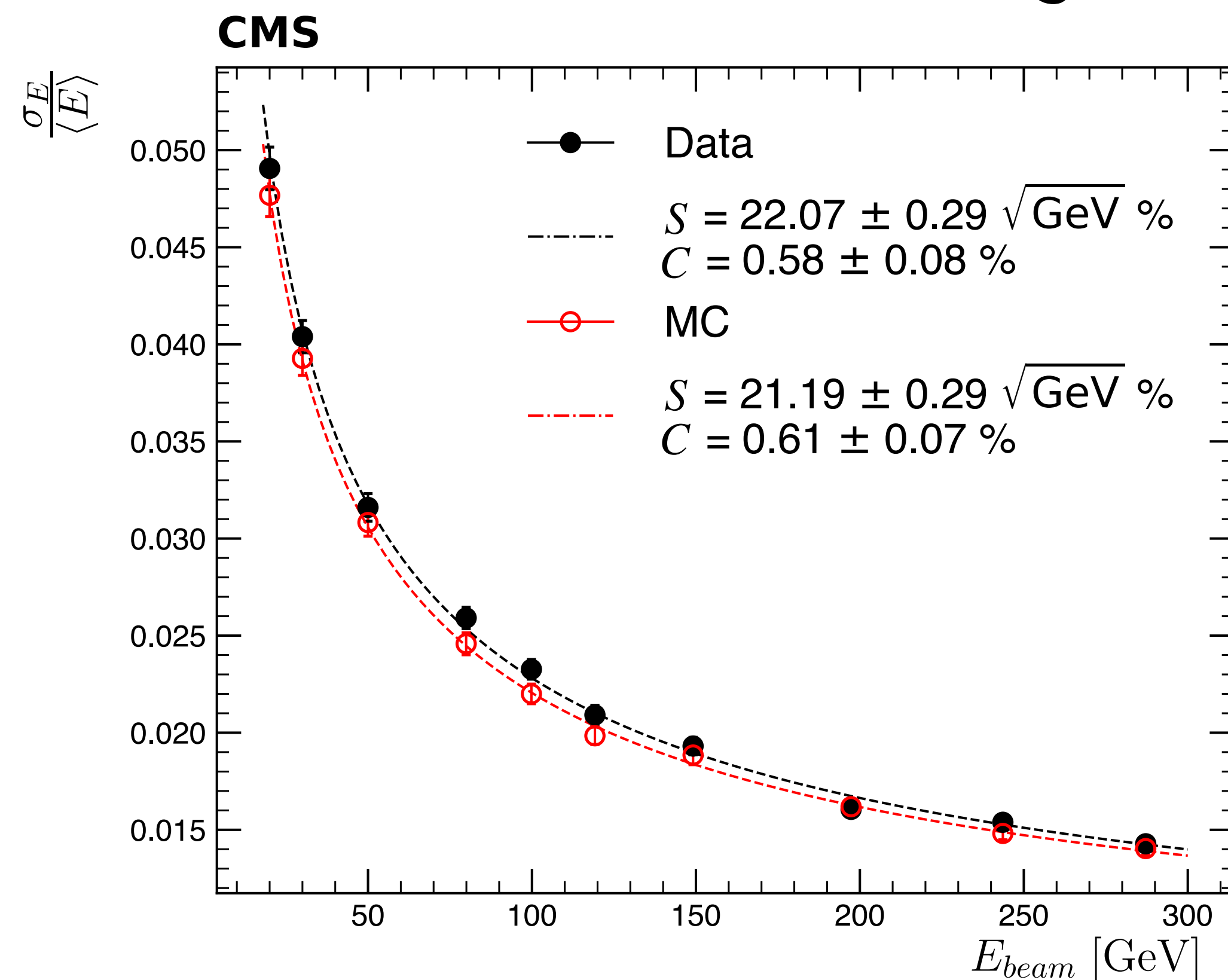
# Energy resolution and linearity



Good Data/MC agreement across the entire energy range

Small non-linearity  $O(2\%)$  at low energies, but optimal linearity for  $E > 50$  GeV

Values in agreement with TDR expectation!



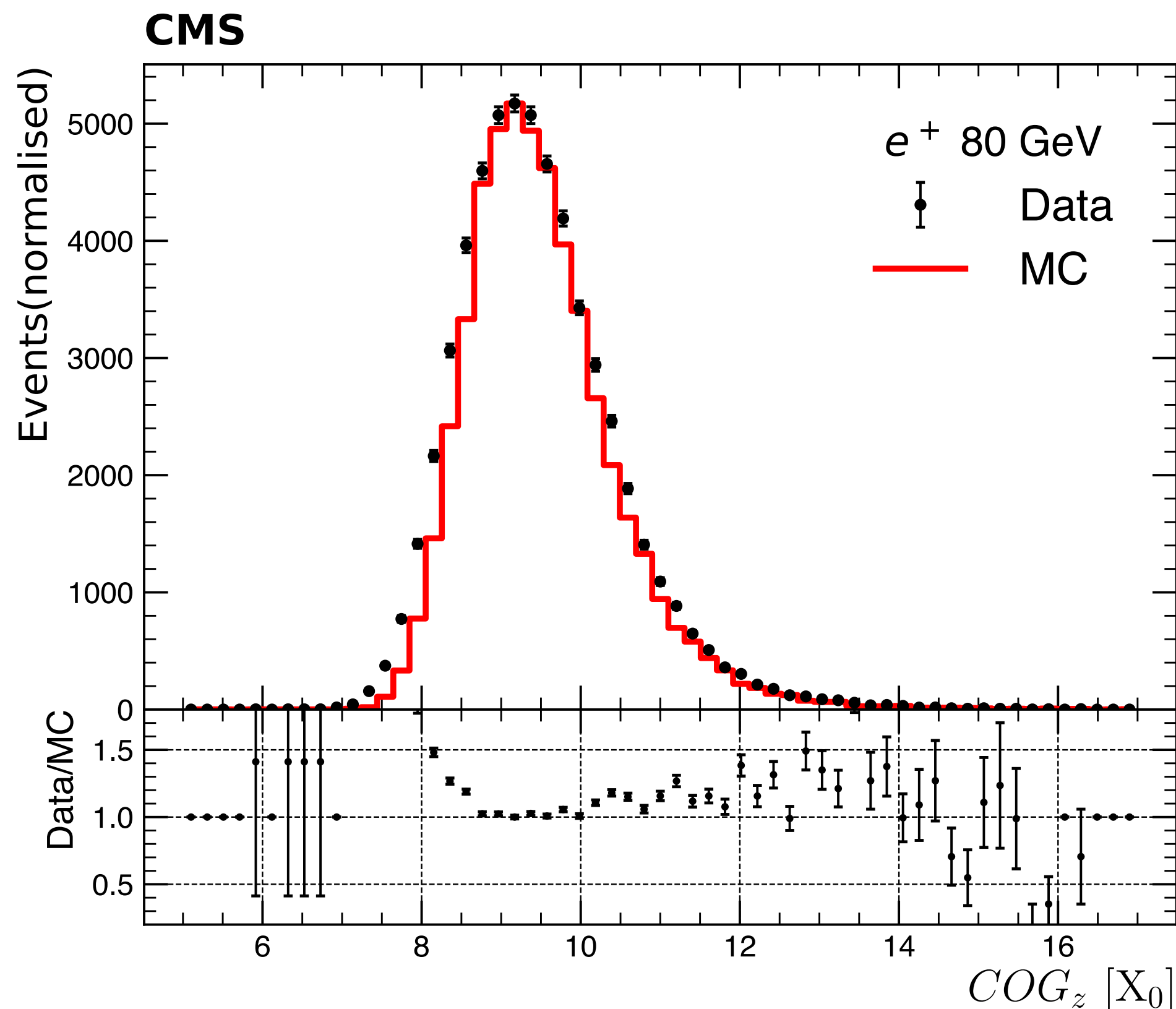


# Longitudinal center of gravity

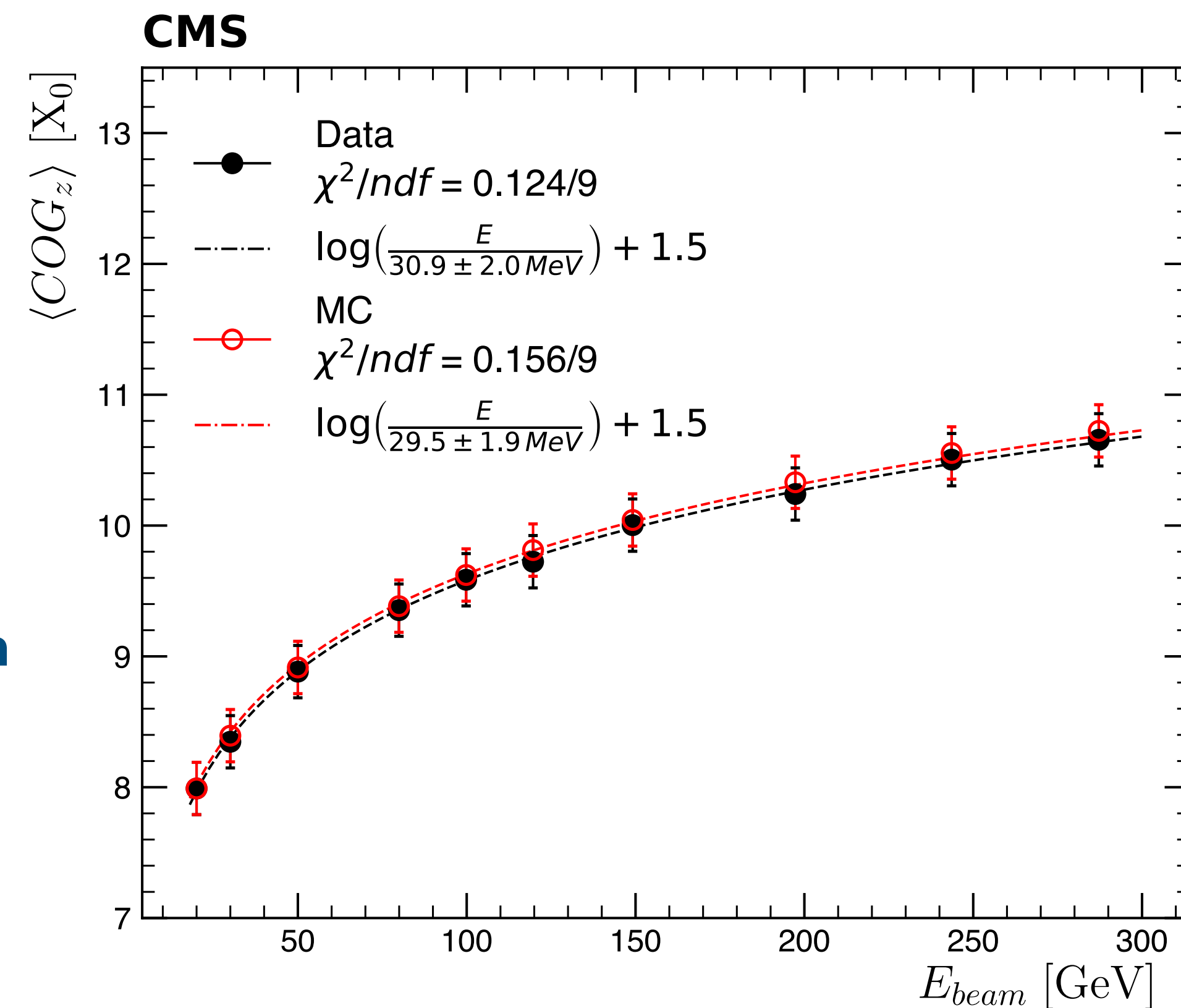
Assessment of longitudinal shower evolution studying **center of gravity**:

$$COG_z = \frac{\sum_{i=1}^{28} E_i^{Si} \cdot z_i[X_0]}{\sum_{i=1}^{28} E_i^{Si}}$$

**Validation of dependence on the beam energy and measurement of CE-E critical energy**



Average  $COG_z$  from  
  
 reconstructed distribution





# Showower shapes: longitudinal profiles



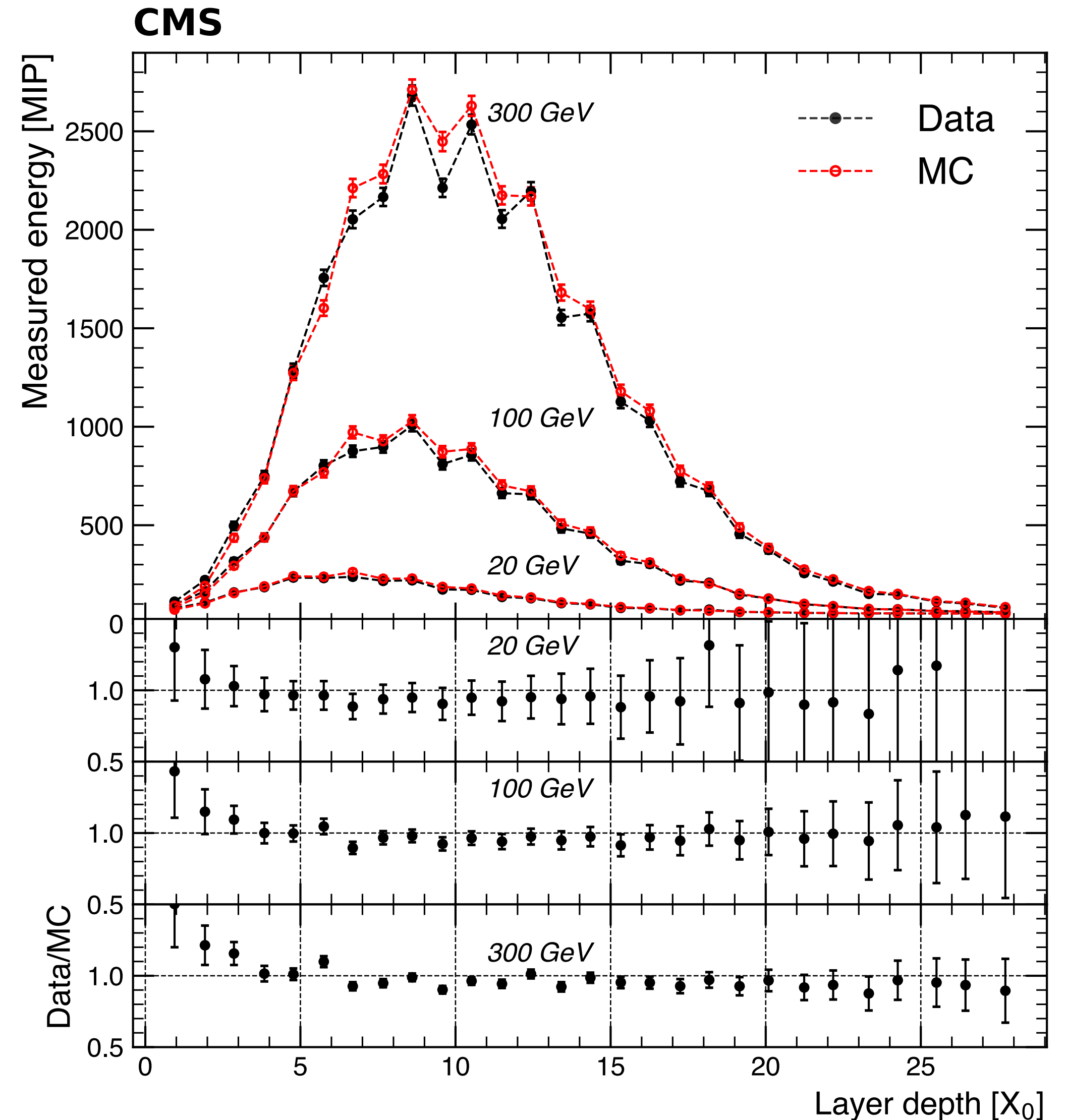
Longo's parametrisation:

$$\left\langle \frac{dE(t)}{dt} \right\rangle = E_0 \frac{(\beta t)^{\alpha-1} \beta \exp(-\beta t)}{\Gamma(\alpha)},$$

**Longitudinal center of gravity and shower maximum:**

$$\langle COG_z \rangle = \frac{\alpha}{\beta}, \quad t_{\max} = \frac{\alpha - 1}{\beta}$$

- Validation of  $\langle COG_z \rangle$ ,  $t_{\max} \propto \ln(E/E_C)$
- **Measurement of the CE-E critical energy**
- Sampling calorimeter: reconstruction of the longitudinal profiles





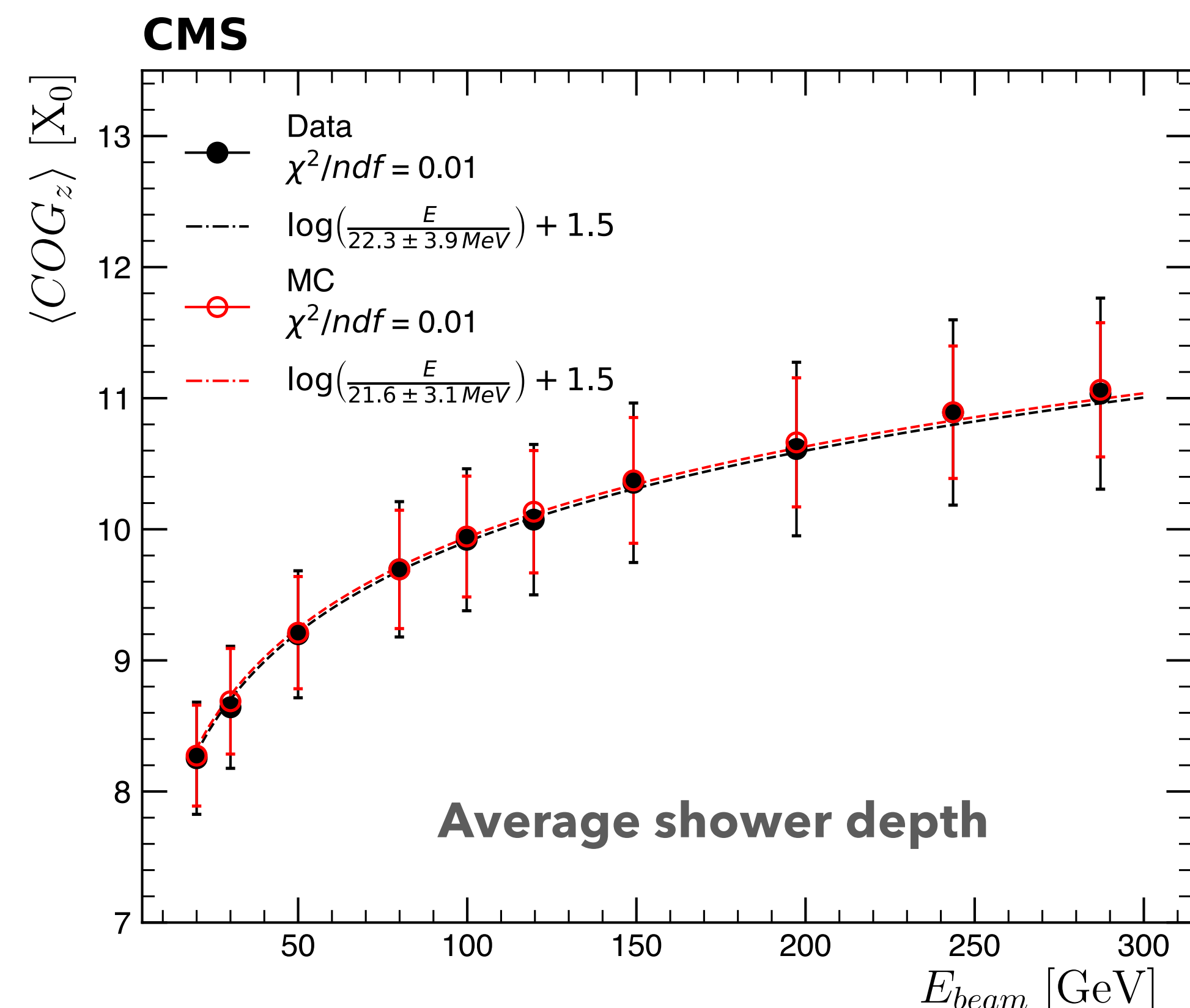
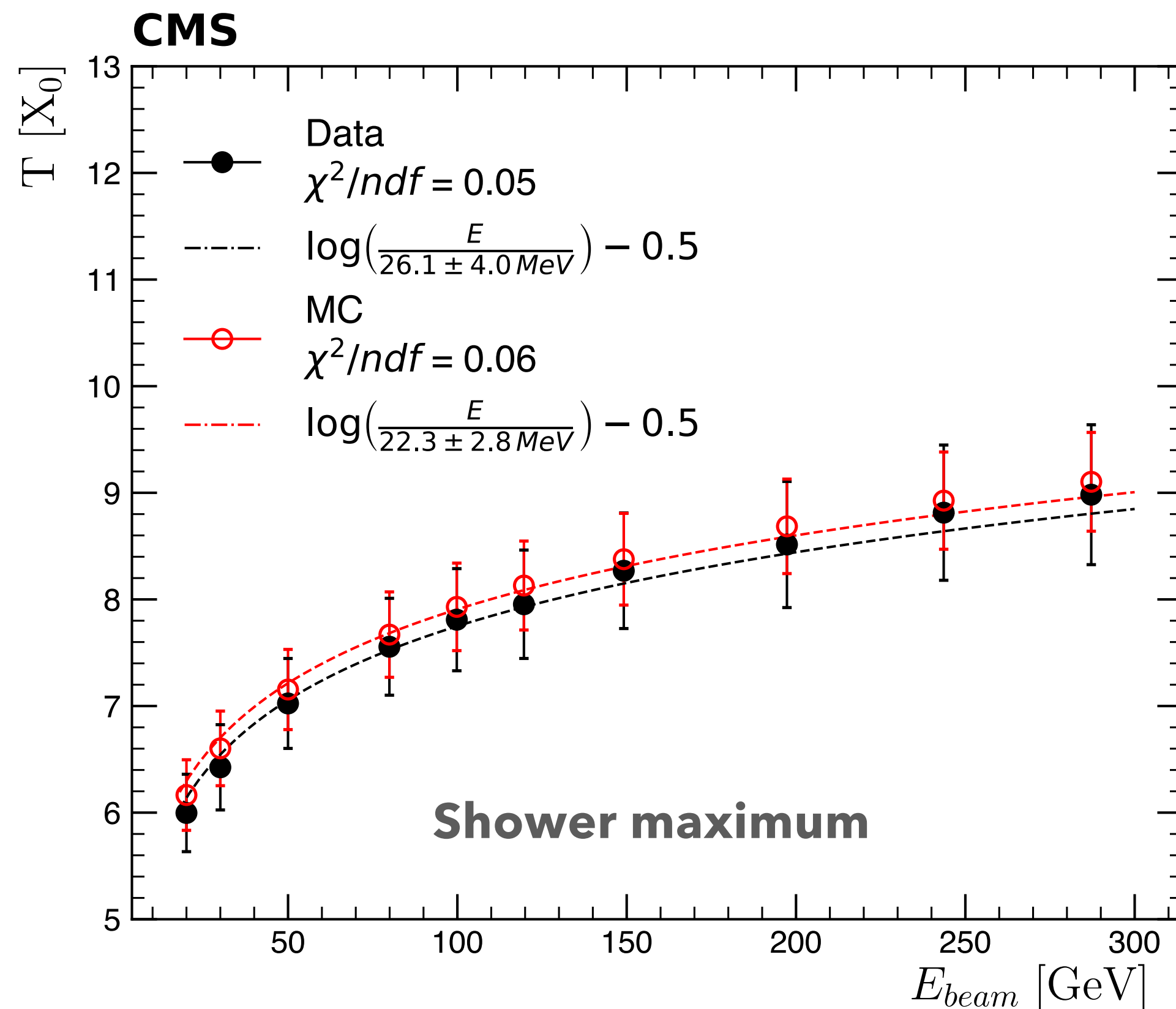
# From the fit to CE-E critical energy



Measurement of the CE-E Critical Energy from  $T$  and  $\langle COG_z \rangle$  vs  $E_{beam}$

Complete reconstruction of longitudinal showers profile

Good Data/MC agreement over a wide energy range





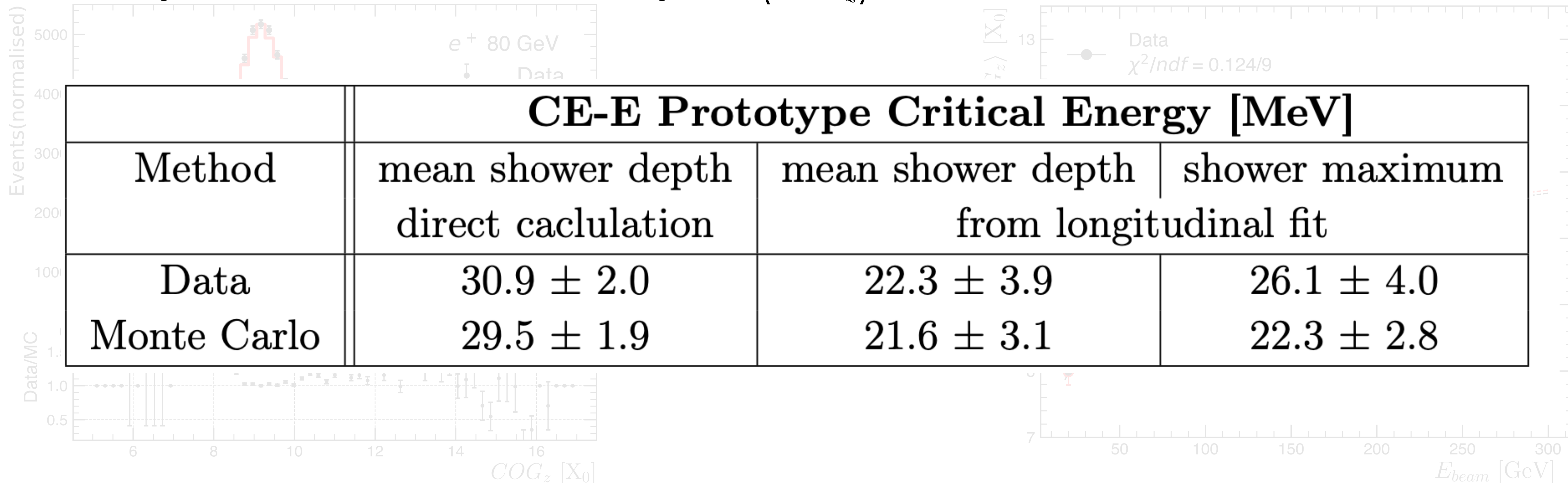
# CE-E critical energy in a nutshell



Three complementary measurements of CE-E Critical Energy ( $E_C$ )

Overall qualitative agreement within  $2\sigma$

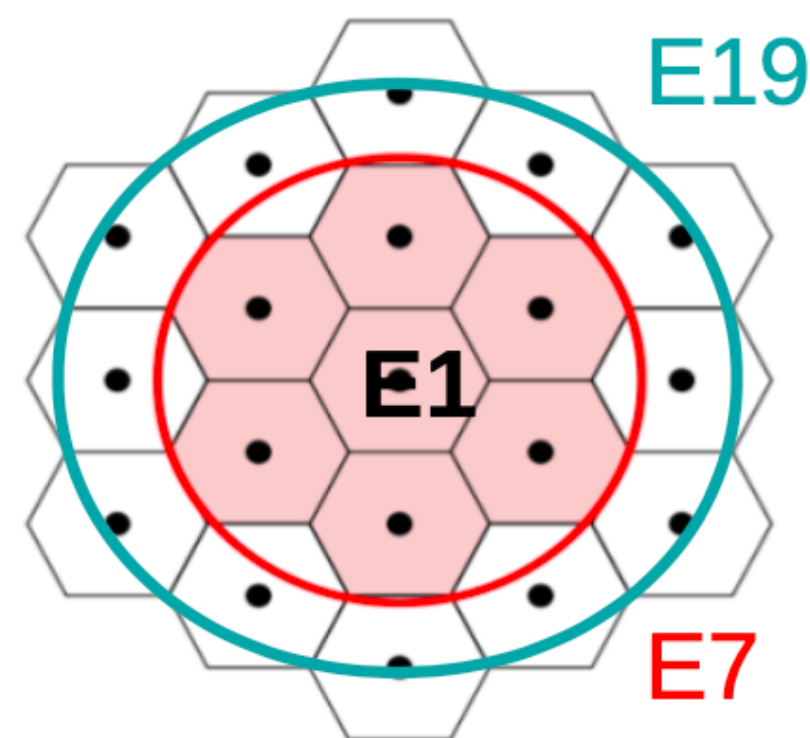
CMS  $E_C$  from longitudinal fit lower than  $E_C$  from  $\langle COG_z \rangle$  definition, being the latter more precise



CE-E Prototype Critical Energy [MeV]			
Method	mean shower depth direct calculation	mean shower depth from longitudinal fit	shower maximum
Data	$30.9 \pm 2.0$	$22.3 \pm 3.9$	$26.1 \pm 4.0$
Monte Carlo	$29.5 \pm 1.9$	$21.6 \pm 3.1$	$22.3 \pm 2.8$

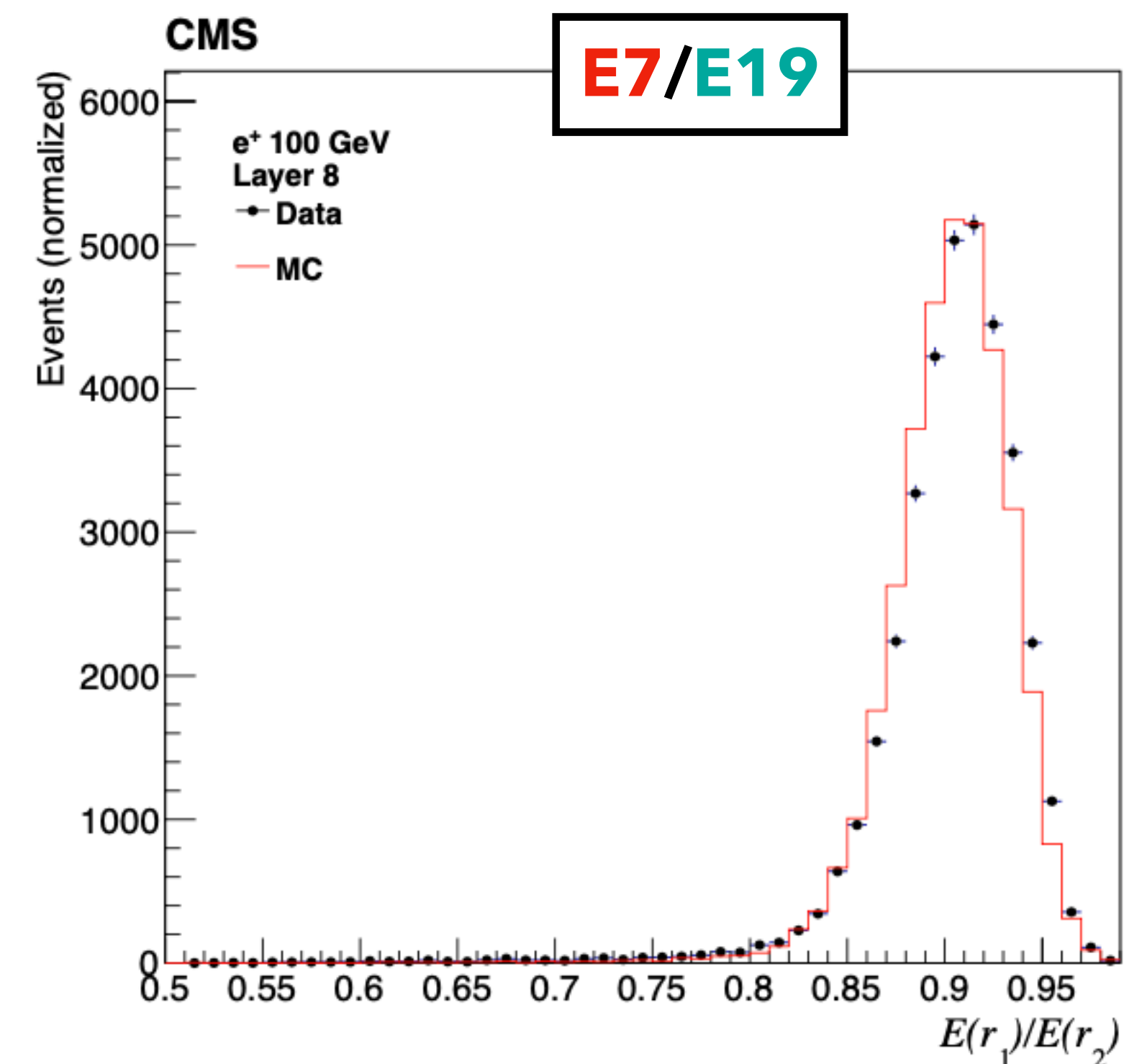
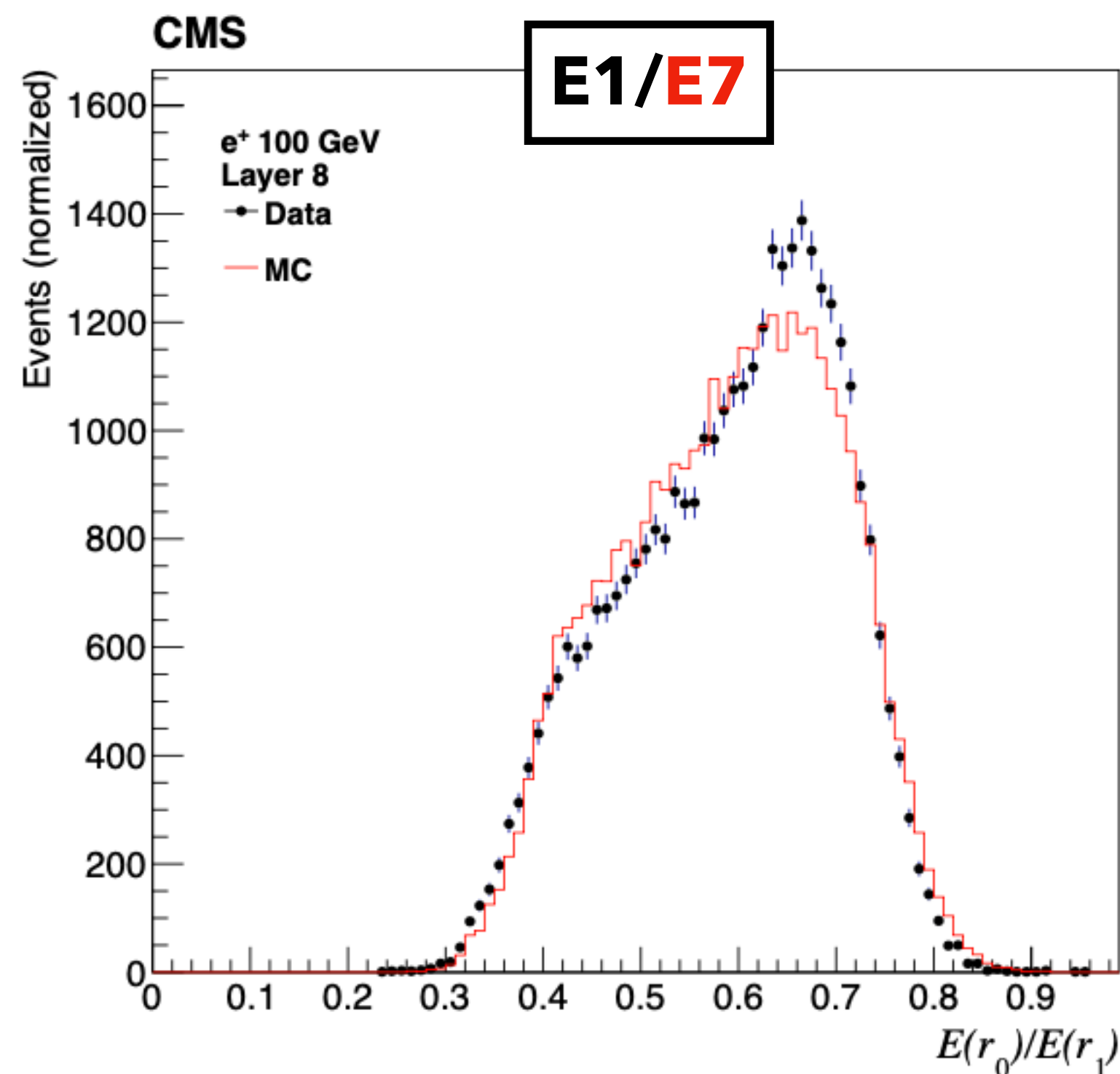
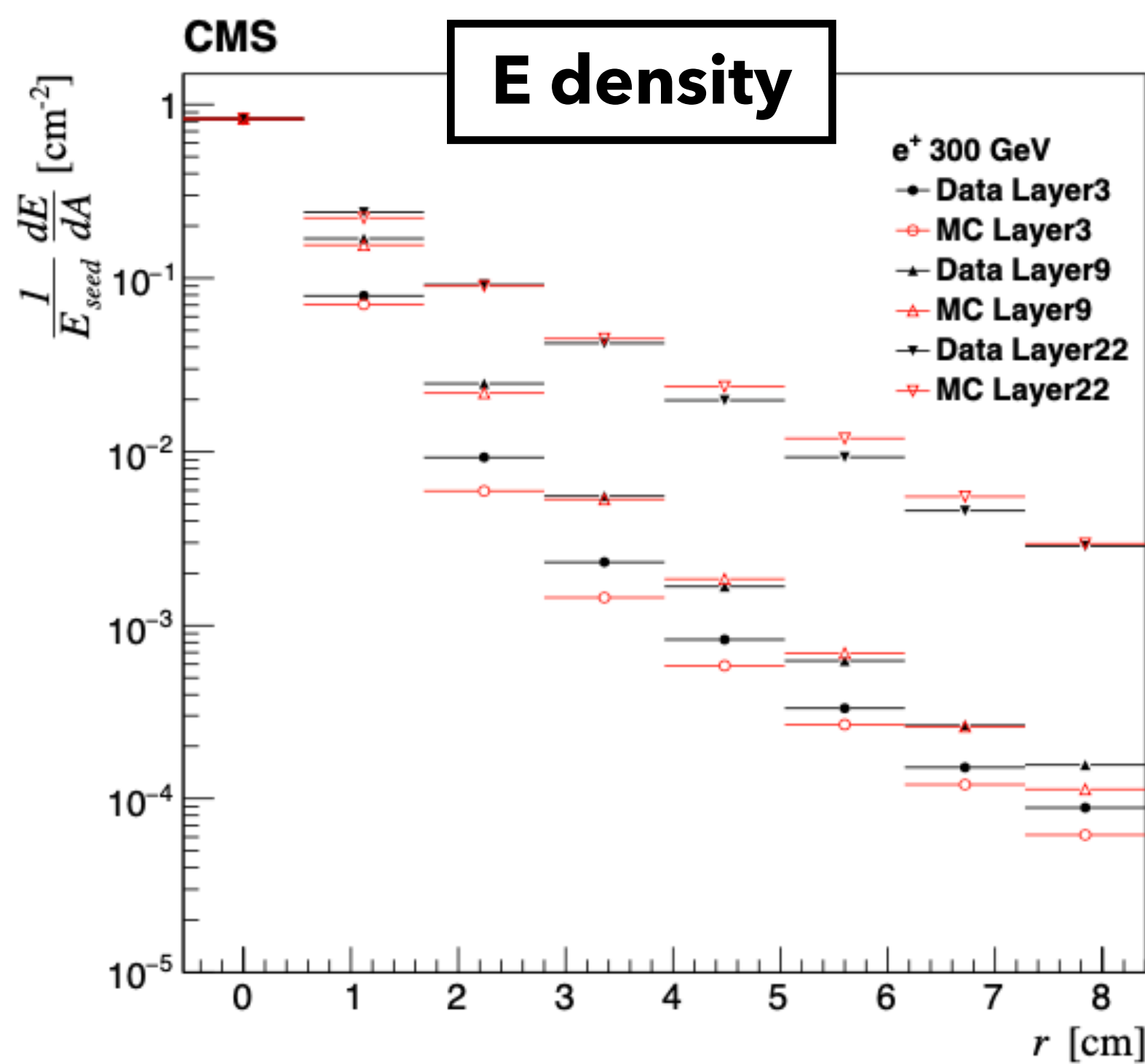


# Transversal shower shapes



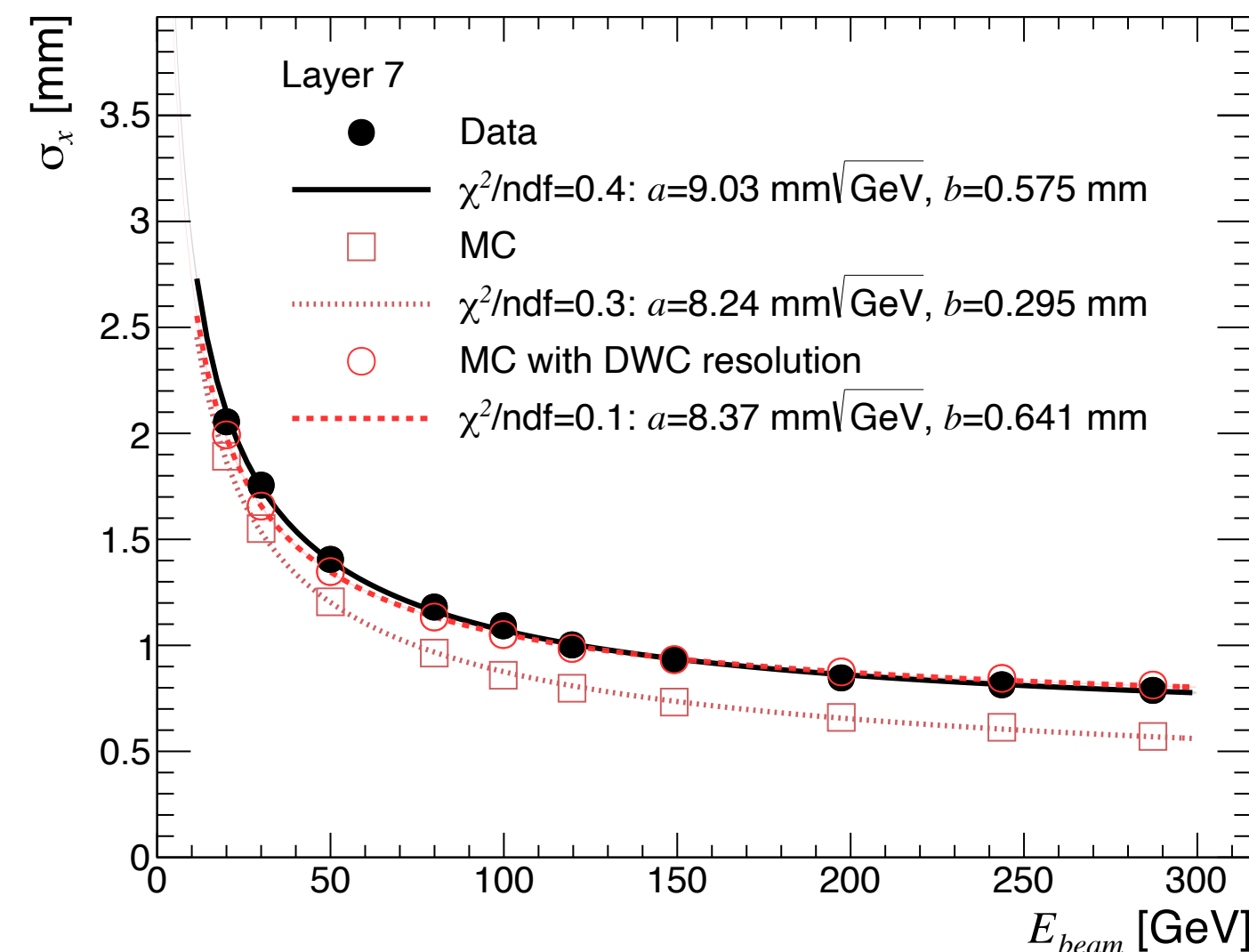
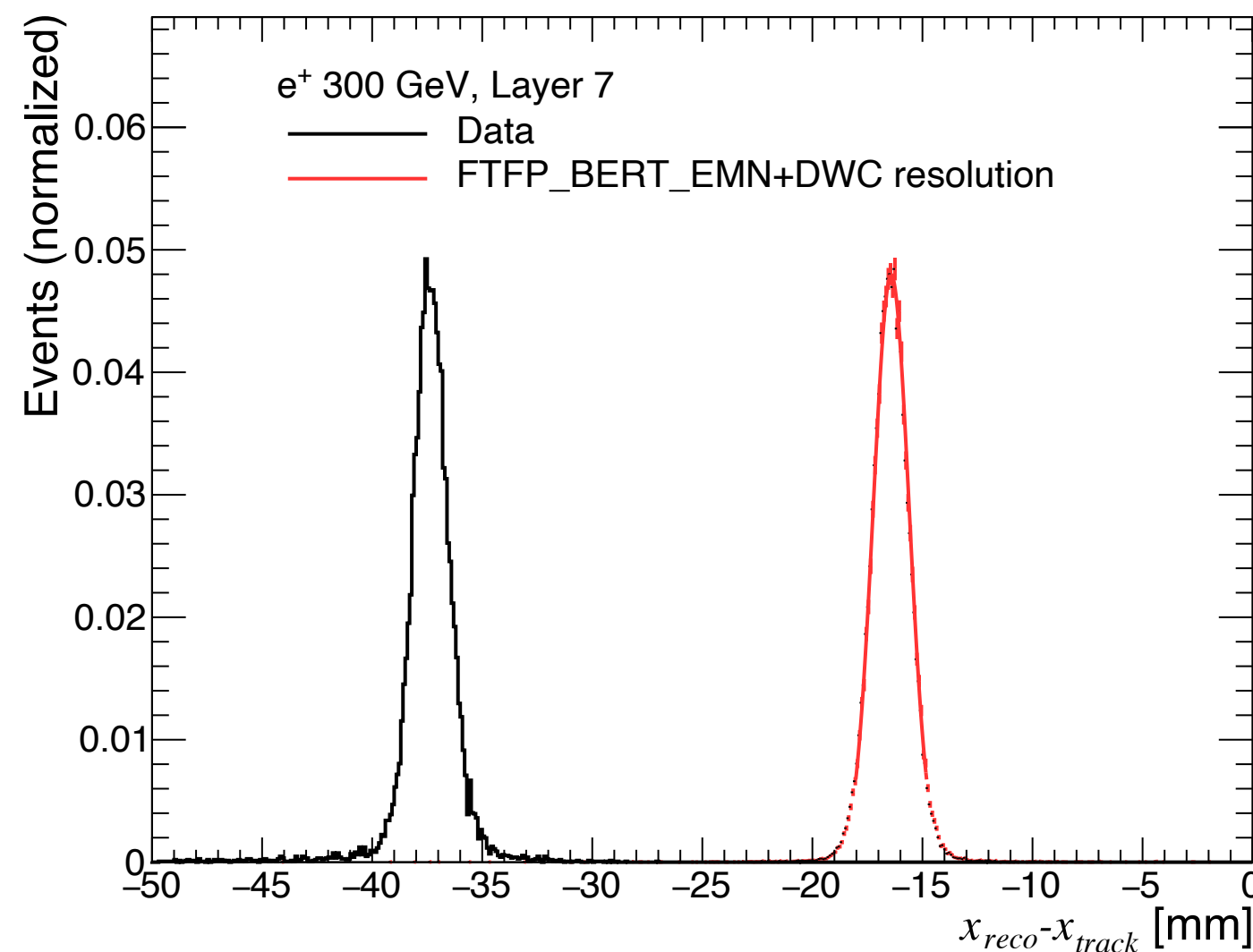
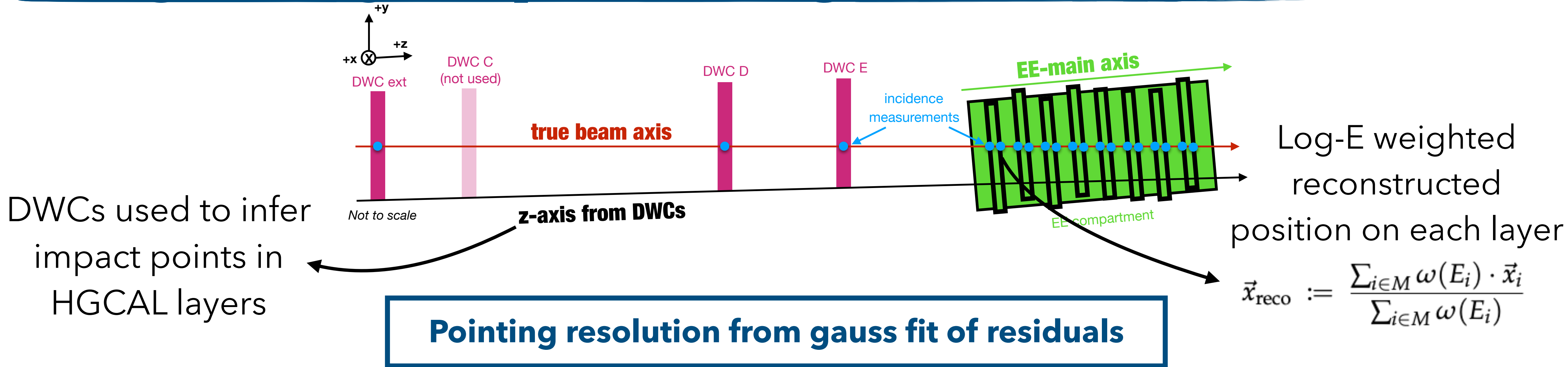
Transverse shower **containment** assessed looking at:

- **Layer energy density w.r.t central pad** (*seed*)
- **Ratio** between **central pad** and **one (two) ring(s)** around it





# Single layer pointing resolution





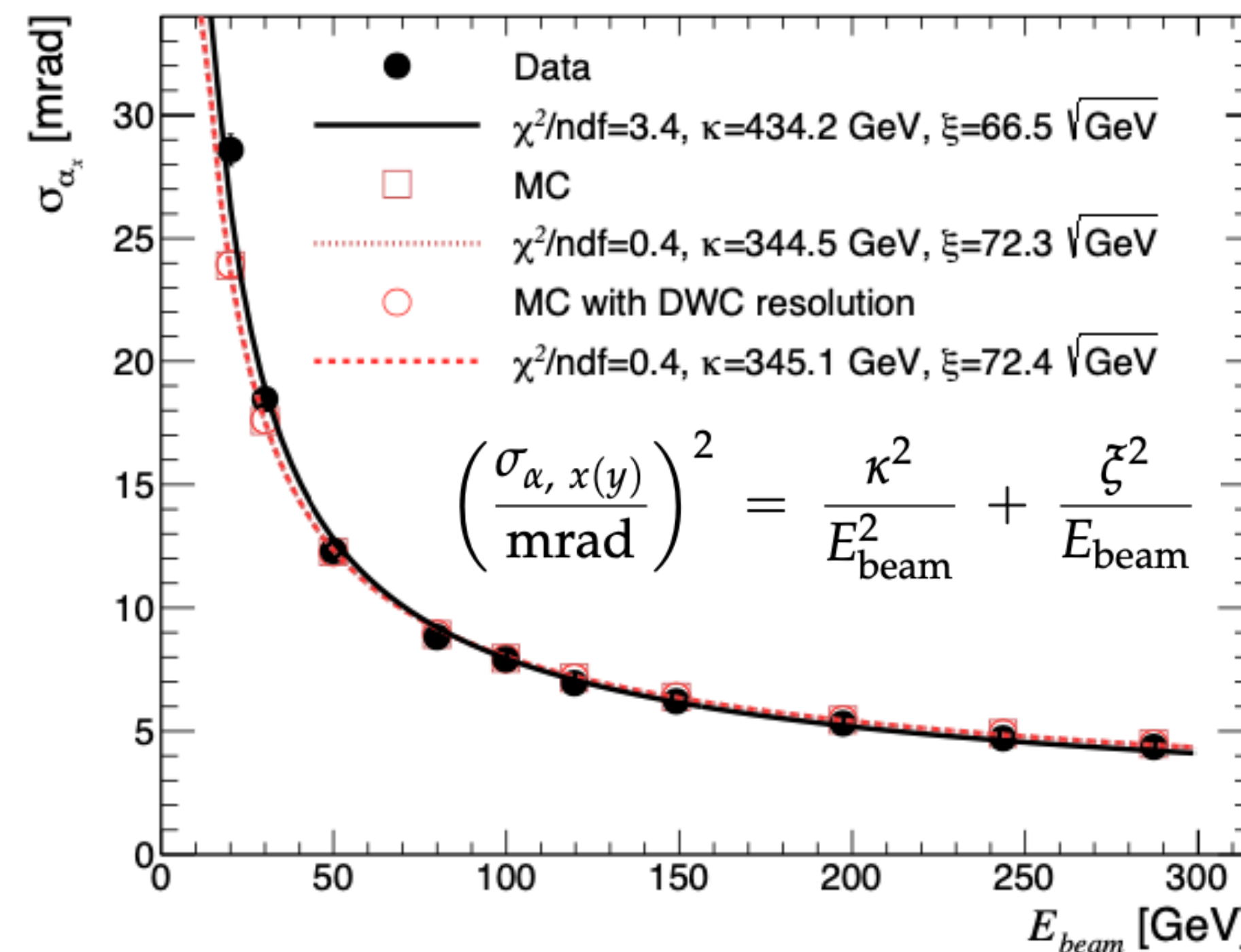
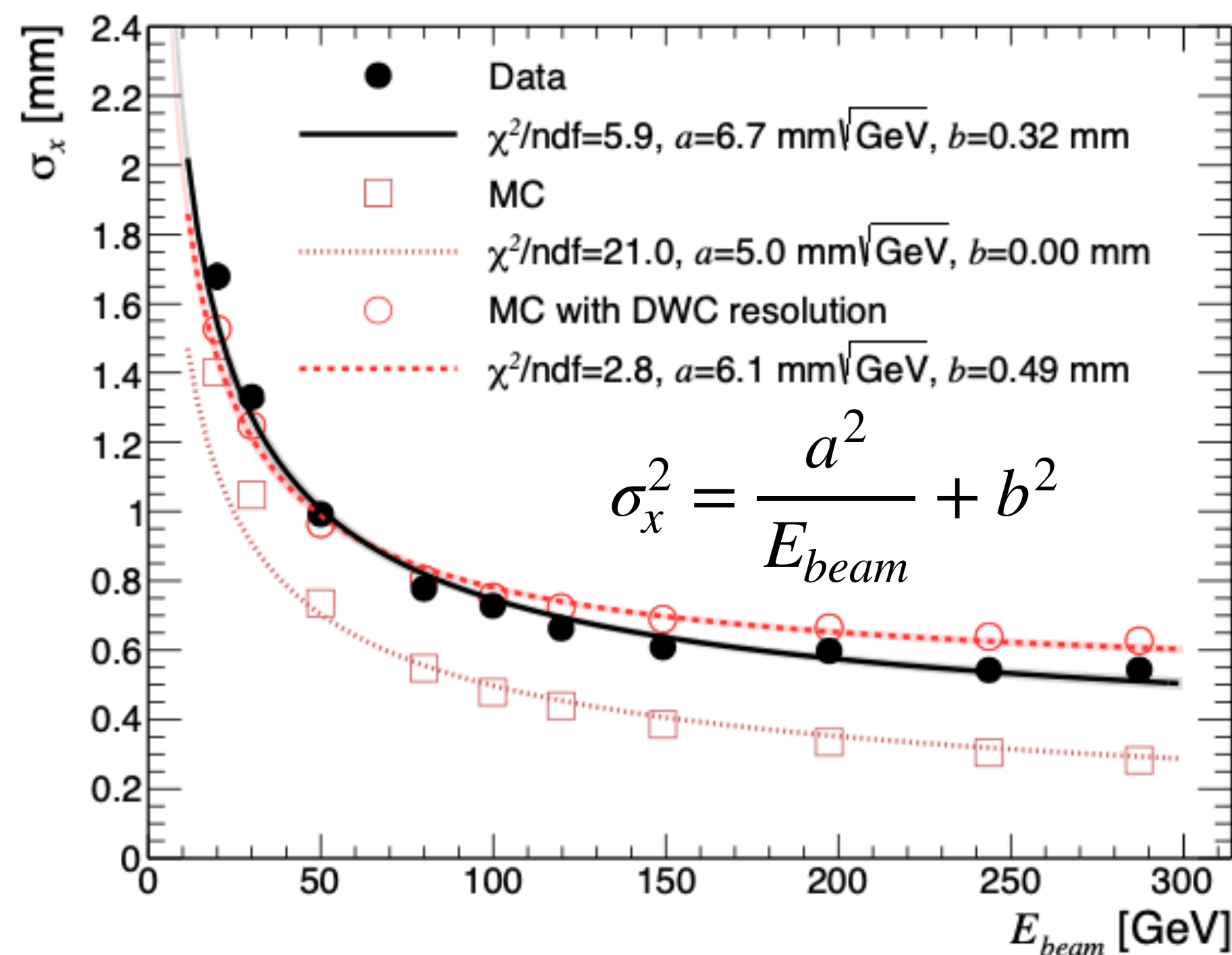
# Position & angular resolution

## CE-E prototype with 28 layers: shower axis reconstruction

Straight line fit on single layer positions for layers with 1% to 95% energy deposit

DWC and HGCAL systems alignment → **residuals** as a **function of longitudinal center of gravity**

### Pointing and angular resolutions of the HGCAL CE-E prototype





# Conclusions



The **HGCAL** will **replace CMS endcap** calorimeters for **HL-LHC programme**

**28-layer CE-E HGCAL prototype studied in beam tests:**

- **Validation of dedicated GEANT4 simulation** shows good agreement
- **Energy resolution:**  $S \simeq 22\%$ , and  $C \simeq 0.6\%$  **in agreement with TDR expectation**
- Complete shower characterisation: **longitudinal** and **transverse** shower **shapes**
- **Imaging calorimeter:** reconstruction of **shower axis**
- **Position** and **angular resolutions** at the level of 0.3 mm and 5 mrad

**Validation of the HGCAL design and complete characterisation of electromagnetic showers!**



# CMS High Granularity Calorimeter Prototype at CERN Timing Analysis

Test Beams 2018

Rohith Saradhy

(University of Minnesota)

On behalf of the HGCAL Beam Tests group



10th February, 2021



# Motivation Recap

- High Granularity Calorimeter will replace CMS End-Caps as part of the HL-LHC upgrade
- Two of the many challenges that HL-LHC poses are:
  - ◆ Higher Levels of Pileup
  - ◆ Higher Dose of Radiation
- HGCAL prototype was designed keeping these constraints in mind, and the prototypes was tested at various beam facilities over the past few year.
- Si detectors are radiation tolerant compared to the Lead Tungstate Crystals currently used, these are used in the CE-E and CE-H-Si parts of the HGCAL (placed in high radiation zones) to provide radiation tolerance.
- One of the goals of the 2018 Test Beam was to characterize the timing of the HGCAL Prototype.
  - ◆ The 2018 HGCAL prototype uses SKIROC2\_CMS ASIC with a precision as low as 50ps
  - ◆ The final version with HGCROC ASIC will have a precision of  $\geq 20$ ps (for Si)
- These tests were essential to validate the Monte Carlo simulation of the prototype and readout.
  - ◆ The same Monte Carlo will be used in the design of the final version of the detector and readout



# October 2018 Test Beam Configuration

Delay Wire Chamber

Threshold Cherenkov Counter

CALICE - AHCAL

*e, μ, hadrons upto 300 GeV*

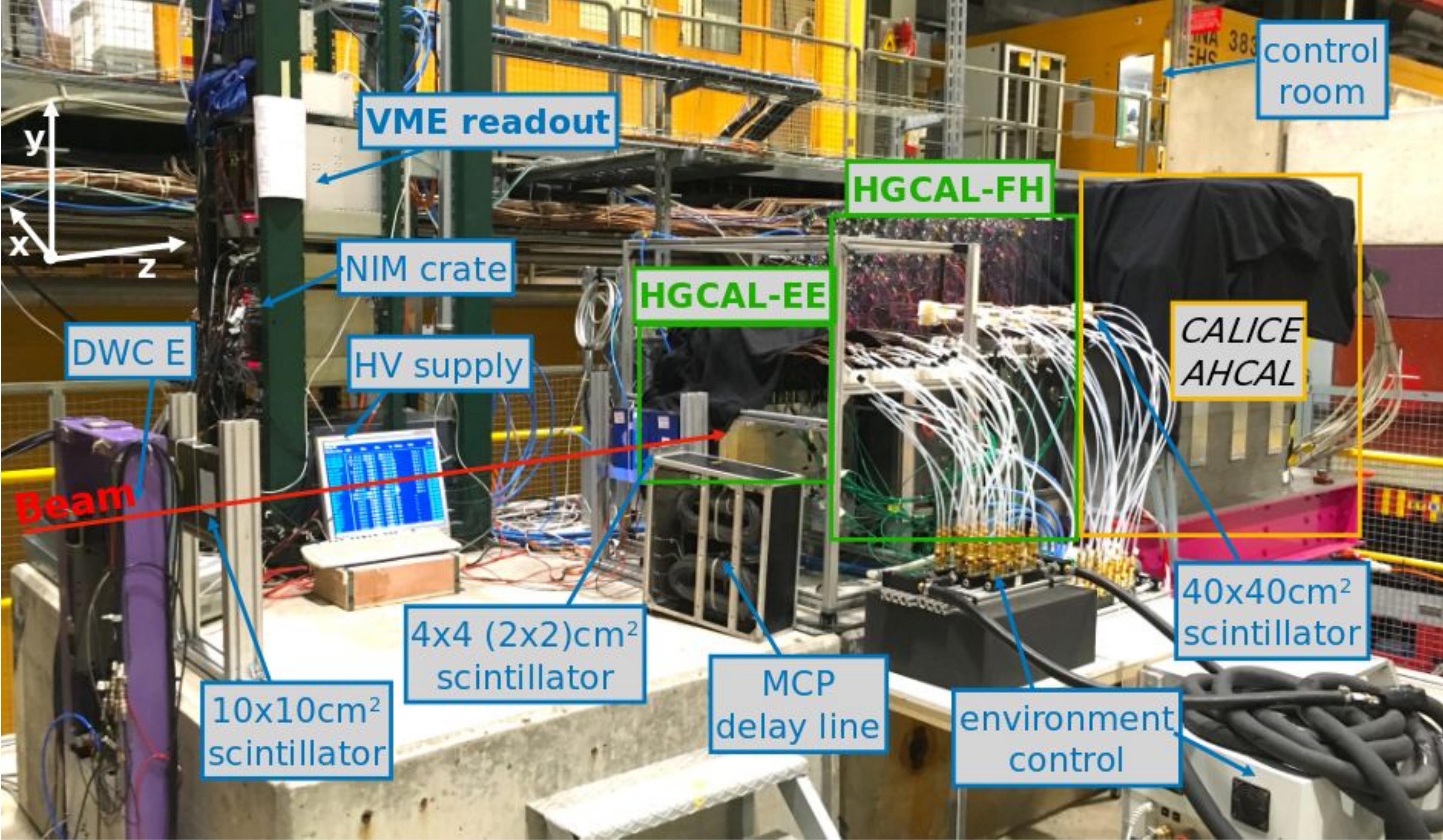
Trigger:

2x Scintillators in front of CE-E

1x Veto Behind CE-H-Si

Two MCP Detectors  
(Micro Channel Plate)

- Used as a reference time-stamp
- In-front of CE-E
- Orthogonal to the beam



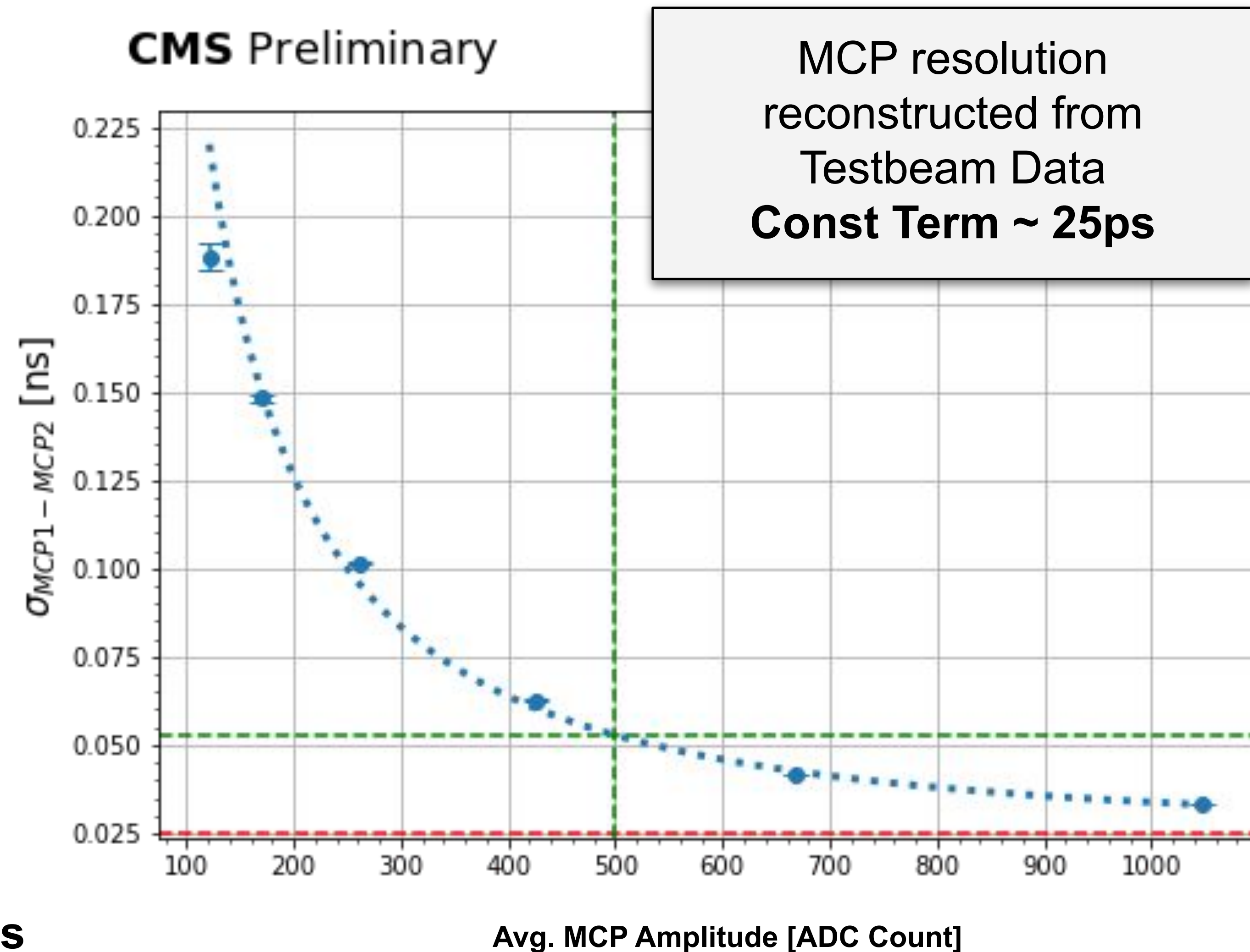


# MCP Characteristics

- 2x MCP Detectors
  - ◆ Operated in PMT-MCP mode
  - ◆ Provides high-precision timing, used as a time-reference
  - ◆ For ease of calibration and characterisation

**Assuming identical performance between the two MCPs:**

**→ Time Resolution (single MCP) ~18 ps**



**Note**  
Green dotted lines represents combined resolution of MCP at 500 MCP Ampl



# Available Timing Information

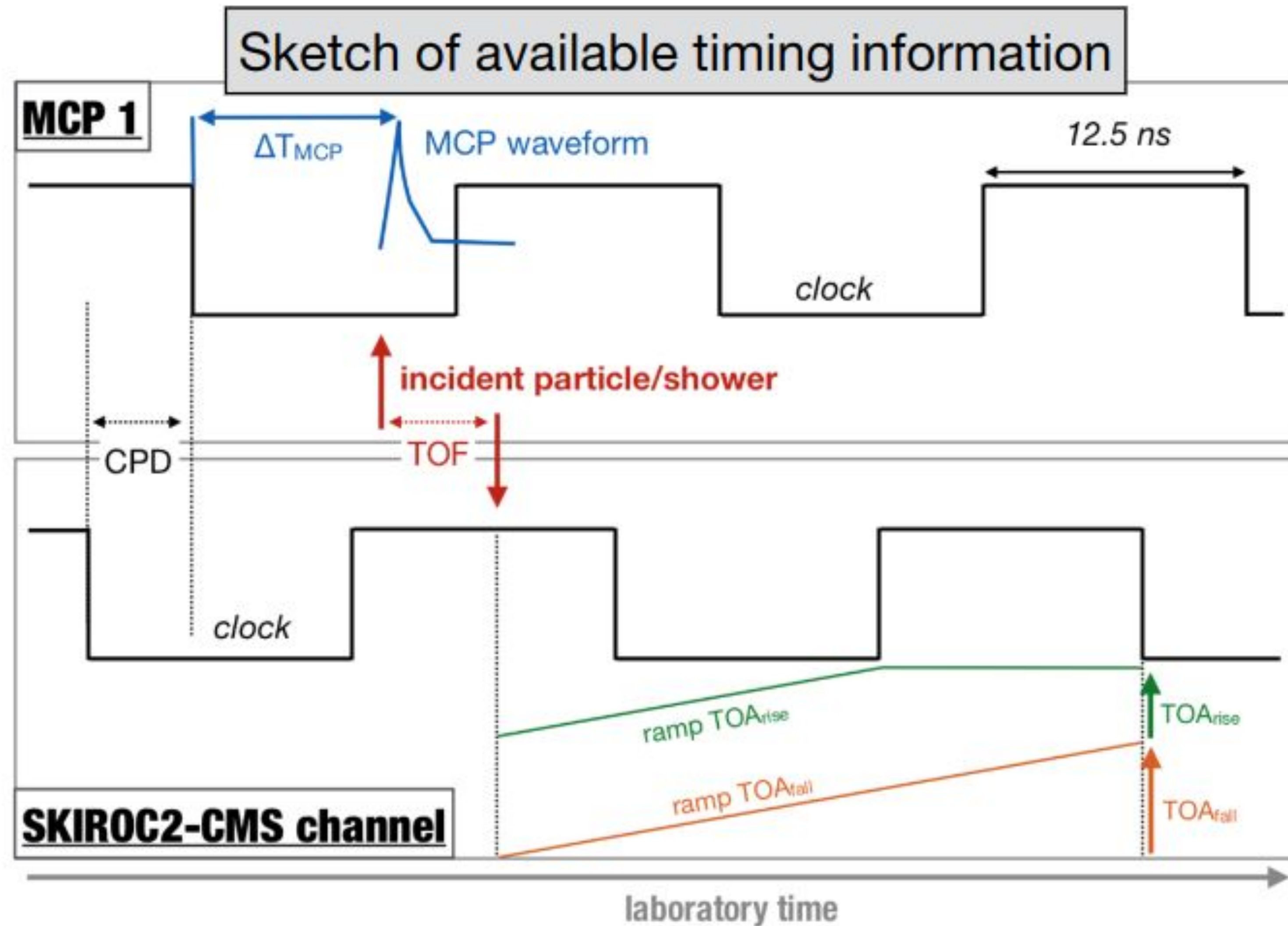
## MCP Time Stamp:

- Time recorded with respect to the falling edge of the global clock
- Tighter cuts on MCP amplitudes were used for better timing performance

## Time-of-Arrival (TOA) Time Stamp:

- TOA circuit starts a voltage ramp when threshold of  $\sim 10$ MIPs is exceeded
- Stops the timing circuit at Rising/Falling edge of the global clock
  - ◆ This corresponds to TOA-Rise / TOA-Fall

*MCP was used as a reference to calibrate TOA and calculate the Time of Flight*



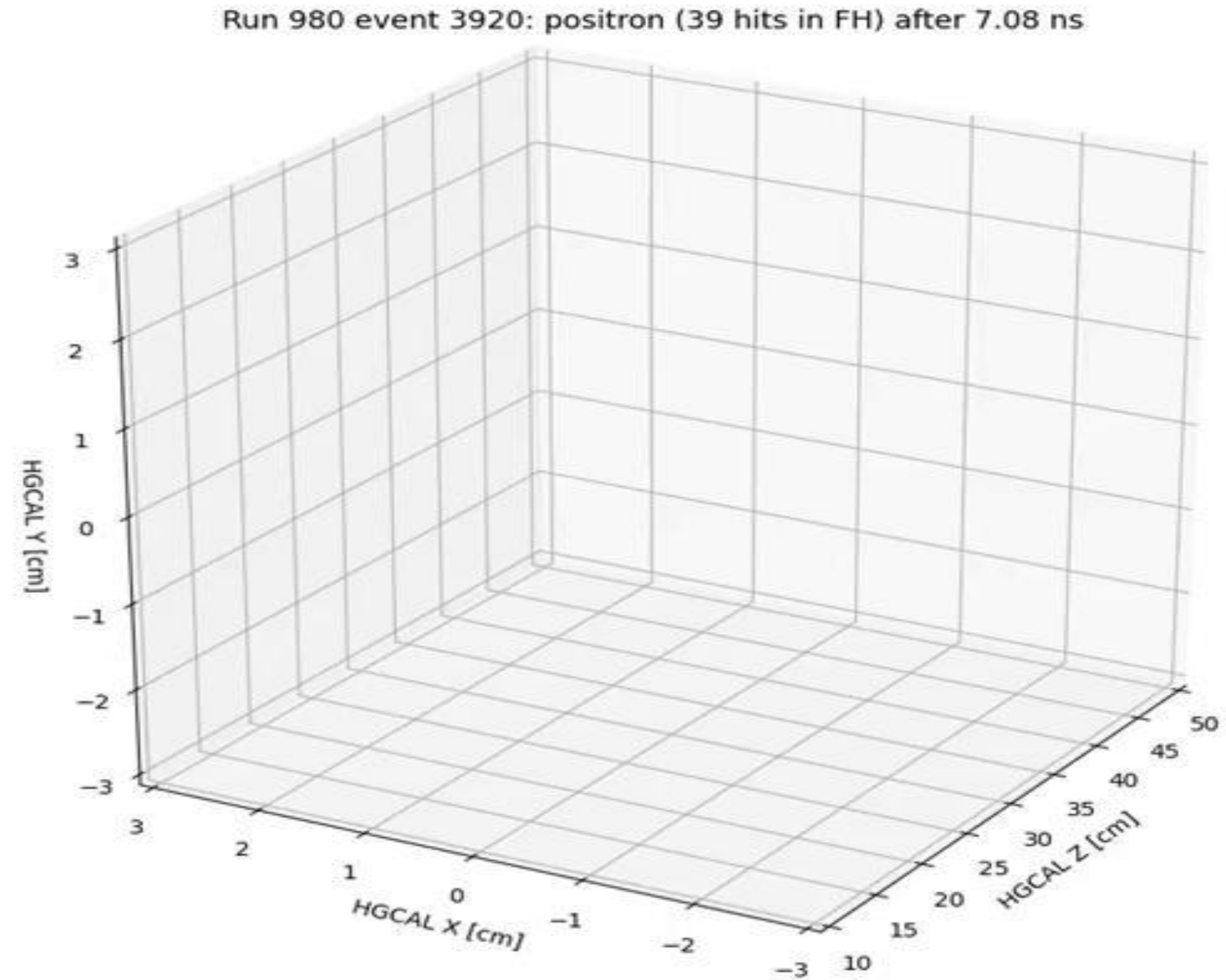


# Electron Shower

Animation of a single event focussing on timing:

- Hits > 50 MIPs considered
- Size of the point correlates to amount of energy deposited
- Colour encodes hit timestamp w.r.t current frame

*We observe the shower depositing energy in the central cells and the cells immediately around it in most of the layers*





# Timing Calibration

## Linearisation:

- Non-Linearity caused by ramp saturation
- Two independent calibration techniques were implemented
  1. TOA data-driven method exploiting the asynchronous nature of the beam particles.
  2. TOA calibration using the full MCP time-stamp

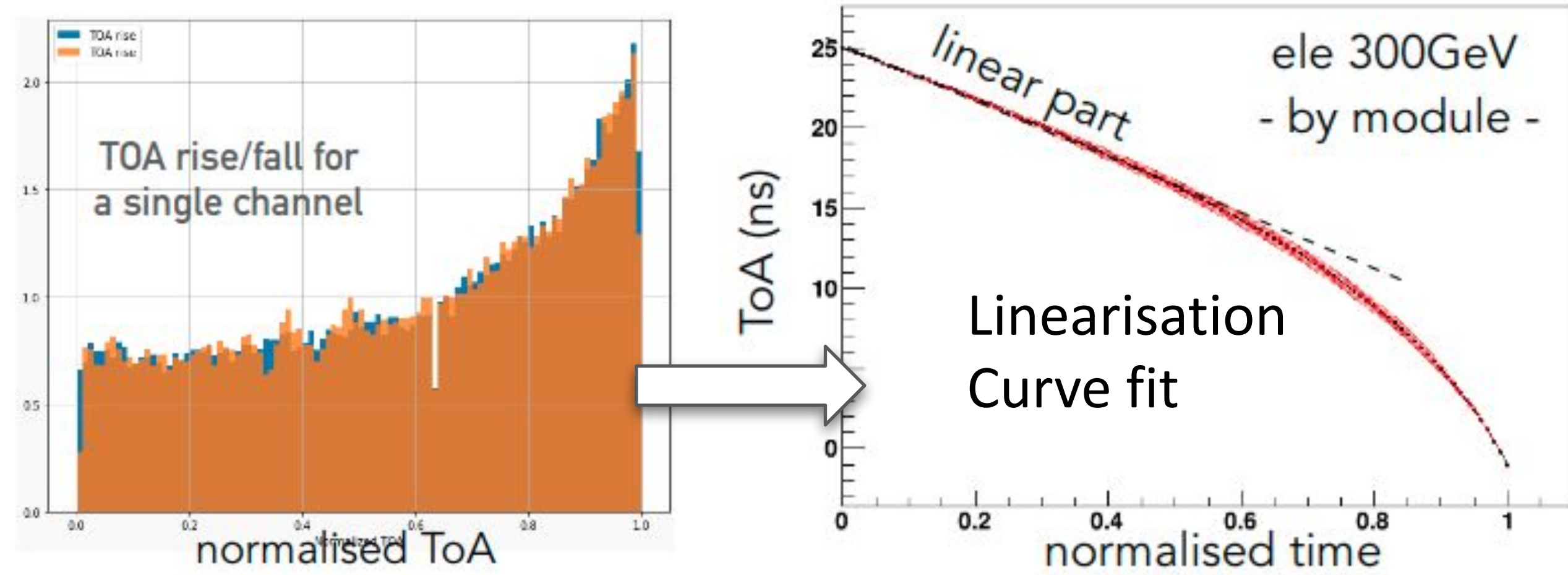
**Consistent results were derived from both techniques**

Calibration

- Reasonably stable over
  - ◆ Beam Energies
  - ◆ Rise and Fall
- Calibration applied on the smallest level of granularity (per channel)

## METHOD 1

Cumulative TOA is linearised with a parametric equation



**Linearisation:**  
Fit using a parametric equation and corrected by inverting it

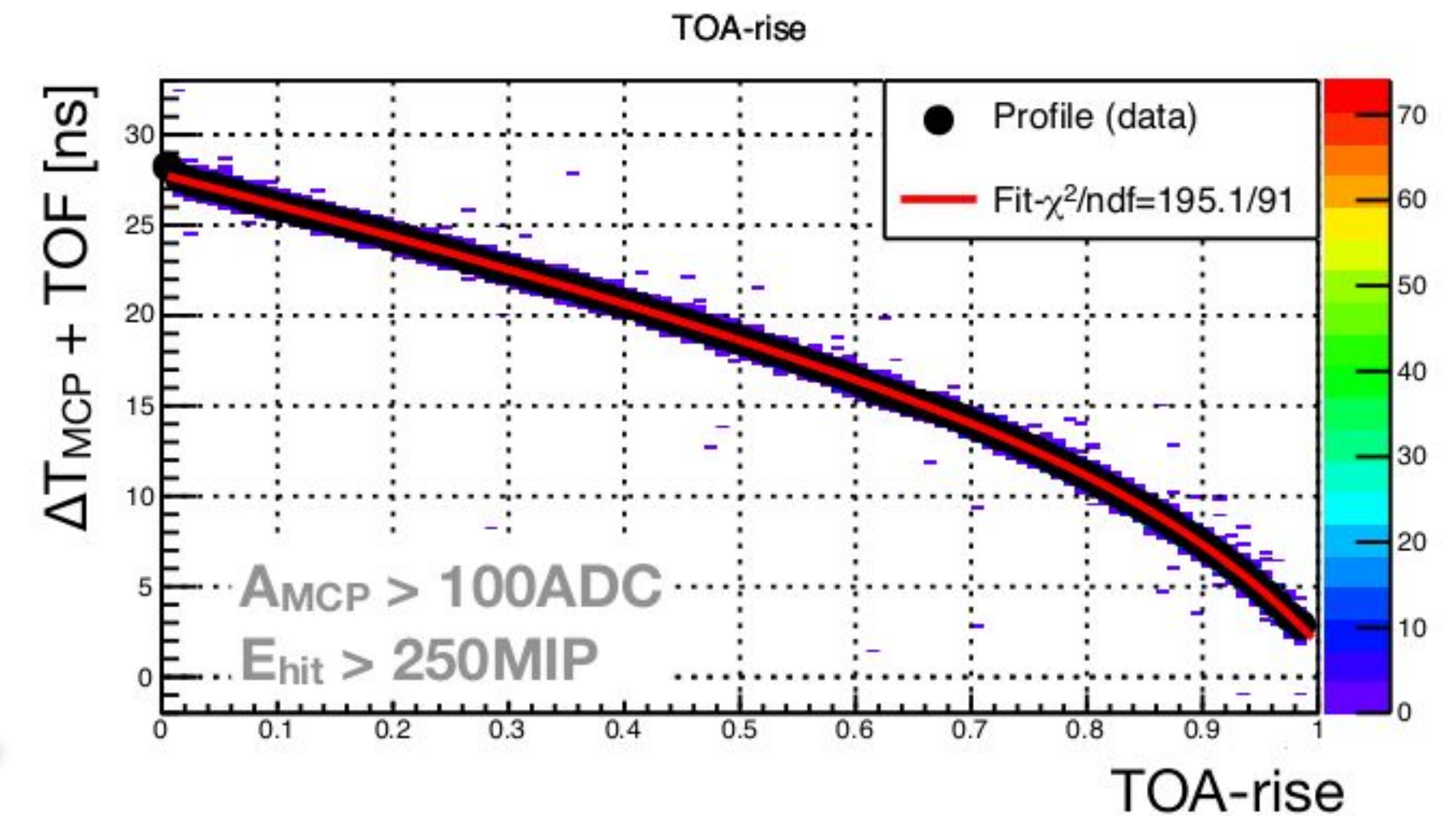
$$\rightarrow [0] * x + 25 + [1] * \left( \frac{1}{x - 1.25} + 0.8 \right)$$

## METHOD 2

Normalized TOA is plotted against MCP time-stamp and linearised

**Linearisation:**  
Fit using a parametric equation and corrected by inverting it

$$f_{\text{TOA}}(x) := a_{\text{TOA}} \cdot x + b_{\text{TOA}} + \frac{c_{\text{TOA}}}{x - d_{\text{TOA}}}$$





# Timing Calibration

## Time Walk:

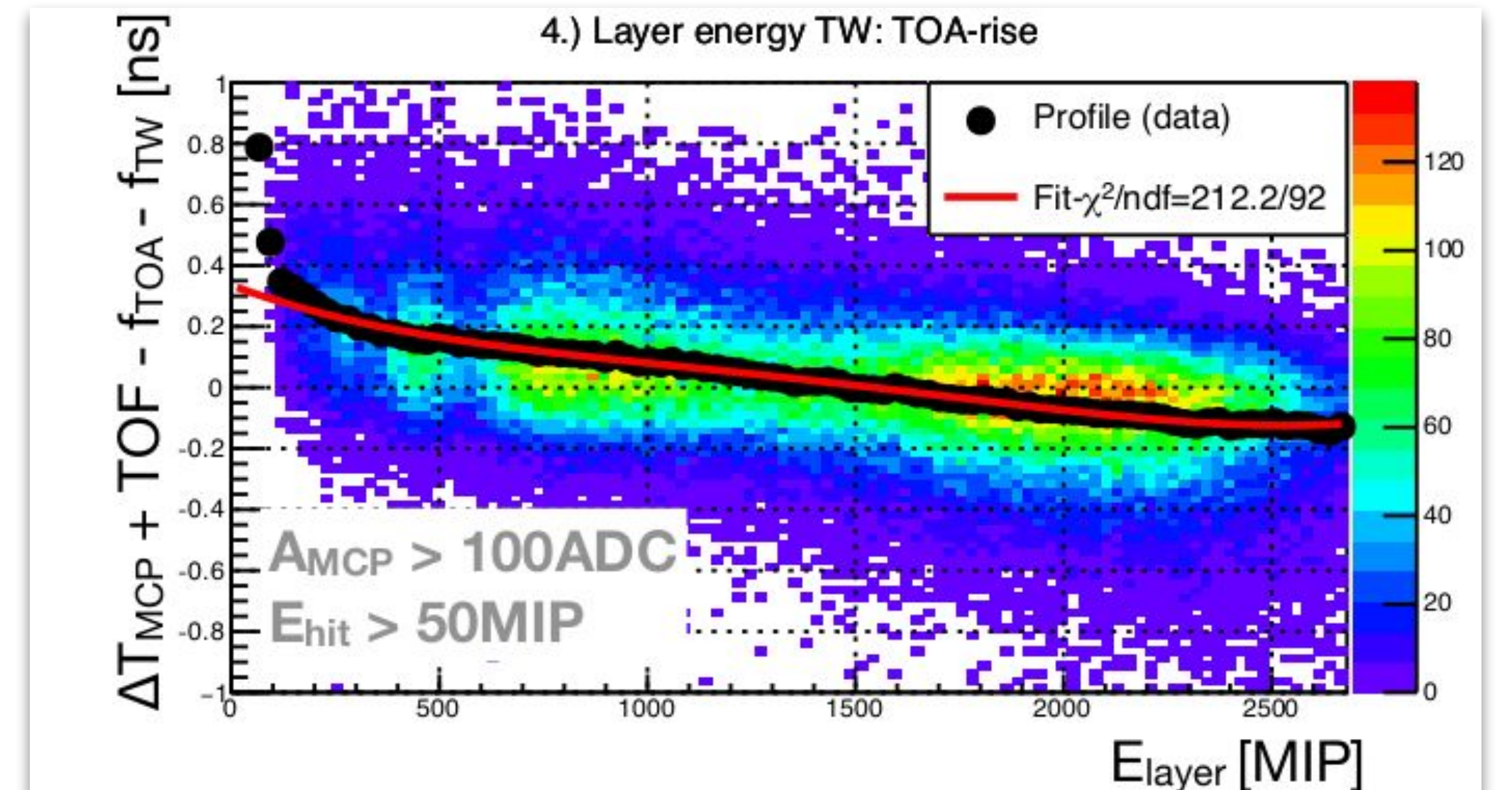
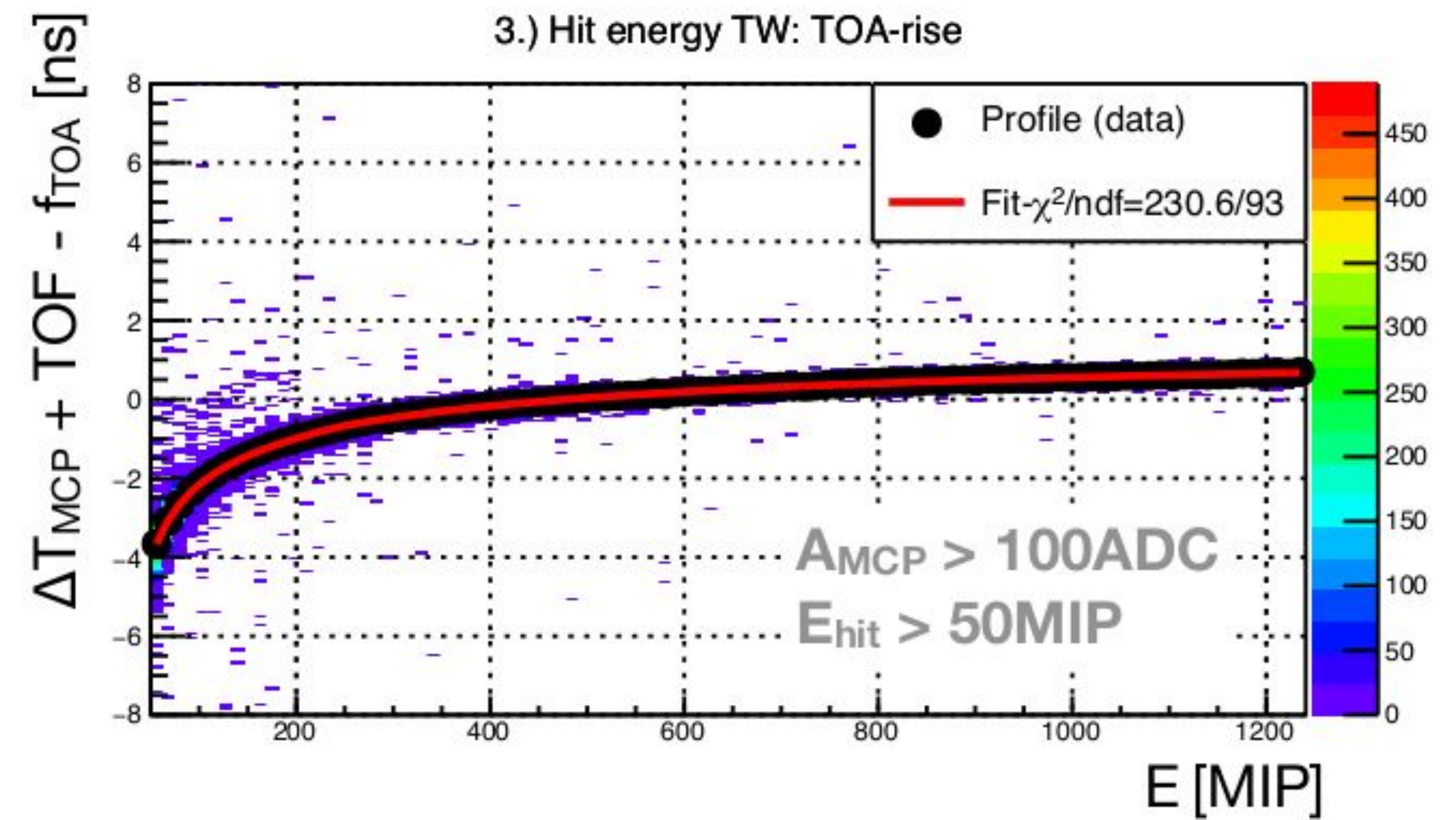
- Phenomenon where the time-stamp depends on the energy deposited in the detector
- Corrected by inverting Time Walk parametric equation

$$f_{\text{TW}}(E) := a_{\text{TW}} \cdot E + b_{\text{TW}} + \frac{c_{\text{TW}}}{E - d_{\text{TW}}}$$

## Correction for Baseline Shift:

- It was observed that there was a systematic shift in timing of the channel with respect to the energy deposited in the layer
- This was corrected using the parametric form below

$$f_{\hat{B}}(E_{\text{module}}) = a_B + b_B \cdot E_{\text{module}} + c_B \cdot E_{\text{module}}^2 + d_B \cdot E_{\text{module}}^3 + e_B \cdot E_{\text{module}}^4$$





# Single Si Channel Resolution (MCP reference)

Layer 8 Single Cell, 300 GeV Electrons

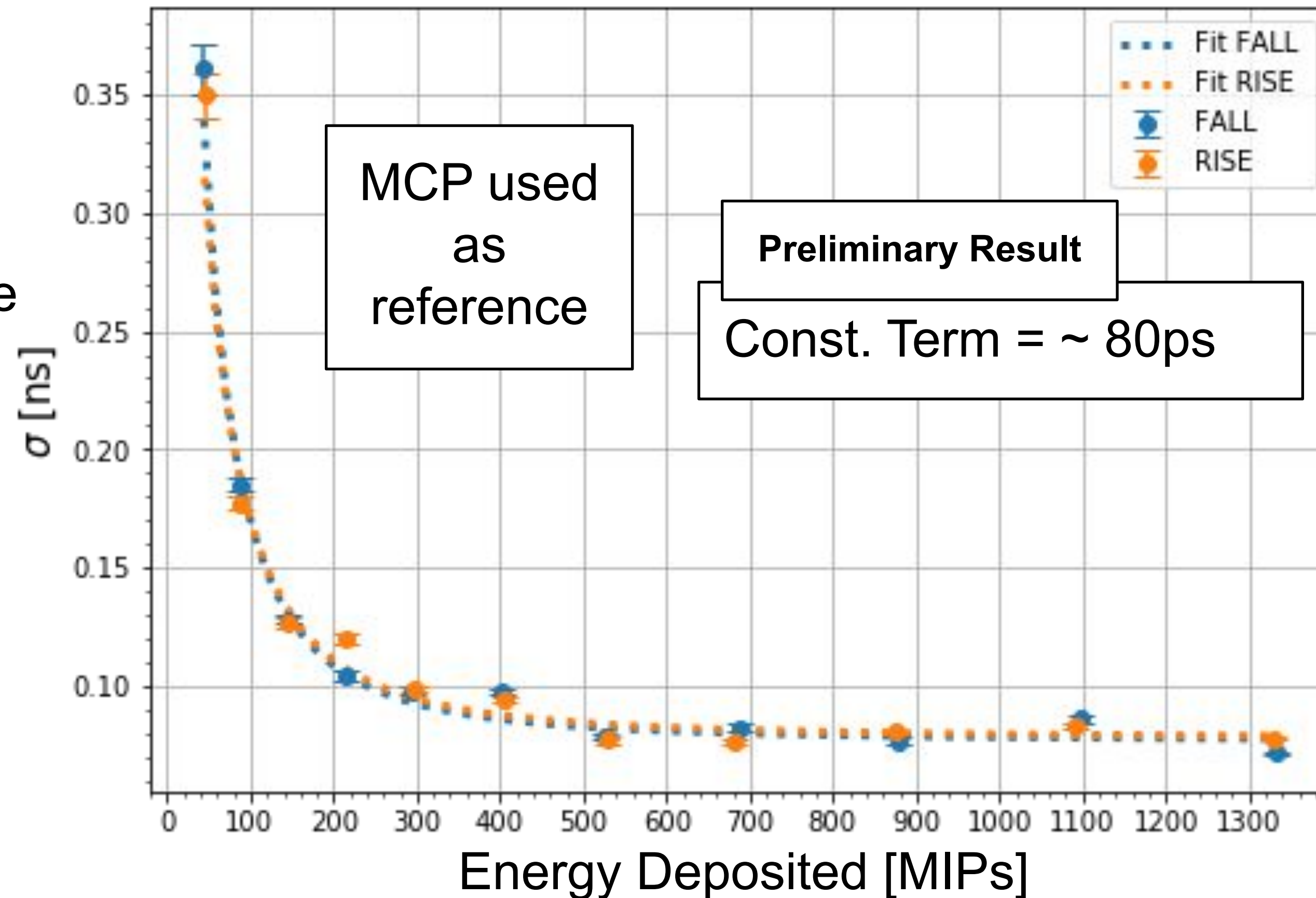
METHOD 1

CMS Preliminary

MCP Ampl > 500 ADC

## Single Channel Resolution:

- 300 GeV Electrons
- Binned in energy deposited in the channel fit against a gaussian distribution
- Consistent results between fall and rise TOA



$$\text{RISE} = \sqrt{\left(\frac{A}{E-B}\right)^2 + C^2}$$

$A = 16.473 \pm 0.49$   
 $B = -8.972 \pm 2.742$   
 $C = 0.078 \pm 0.0$   
 $\chi^2_\nu = 20.312$

$$\text{FALL} = \sqrt{\left(\frac{A}{E-B}\right)^2 + C^2}$$

$A = 15.609 \pm 0.448$   
 $B = -3.309 \pm 2.487$   
 $C = 0.077 \pm 0.001$   
 $\chi^2_\nu = 20.605$

MCP Resolution is estimated to be between 18-35ps

**Note: Result includes the time resolution of the MCP**



# Timing characterization of the full shower

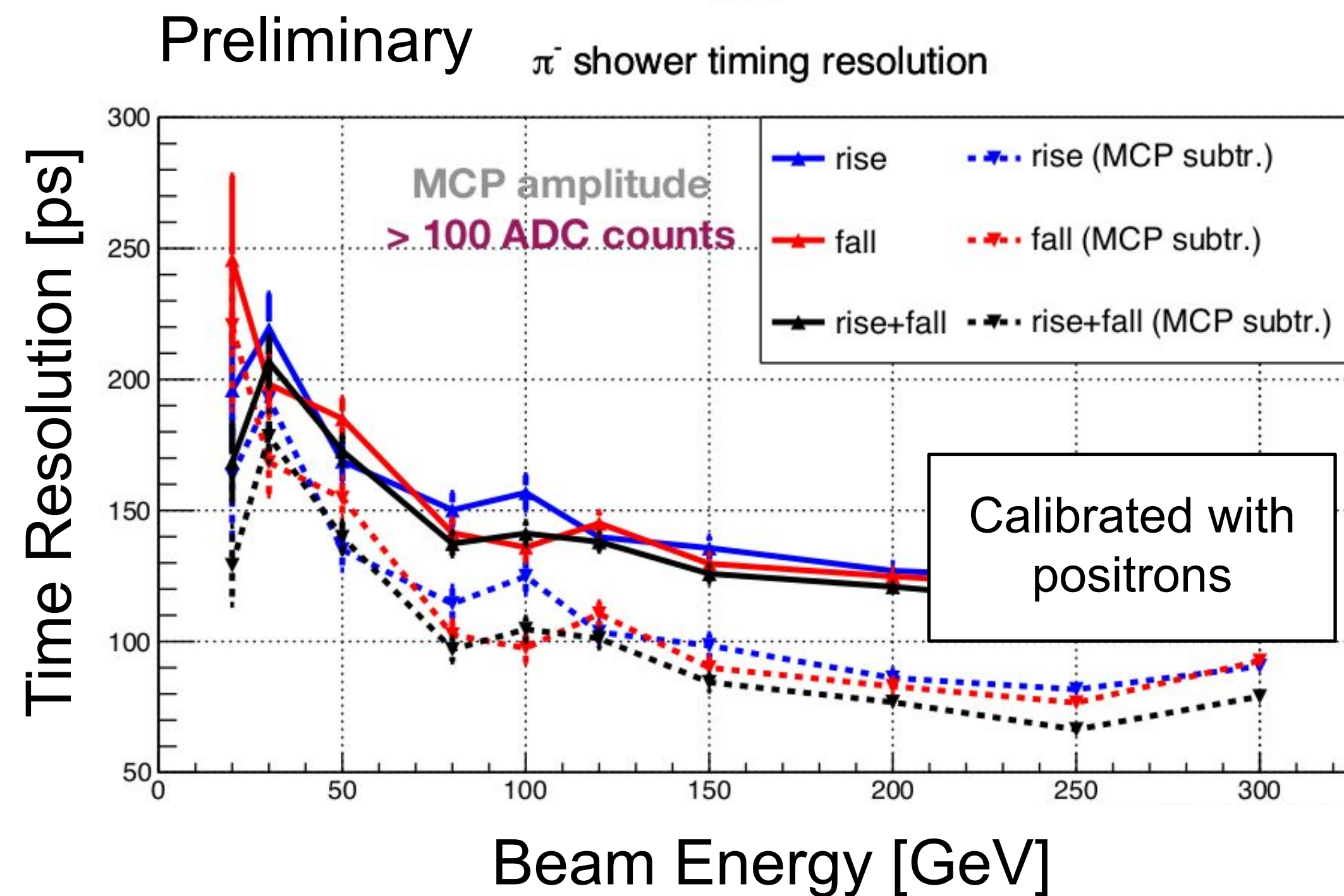
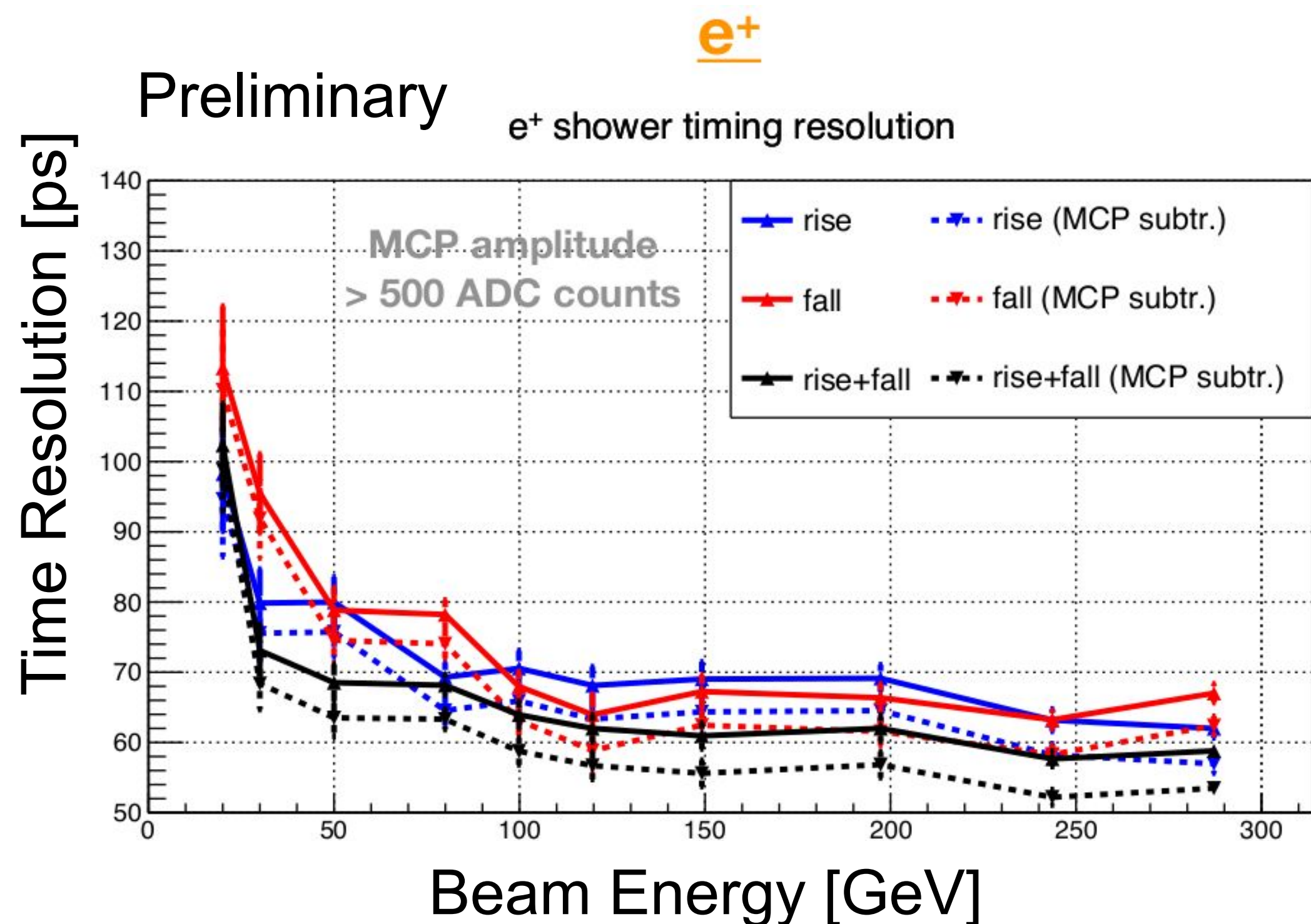
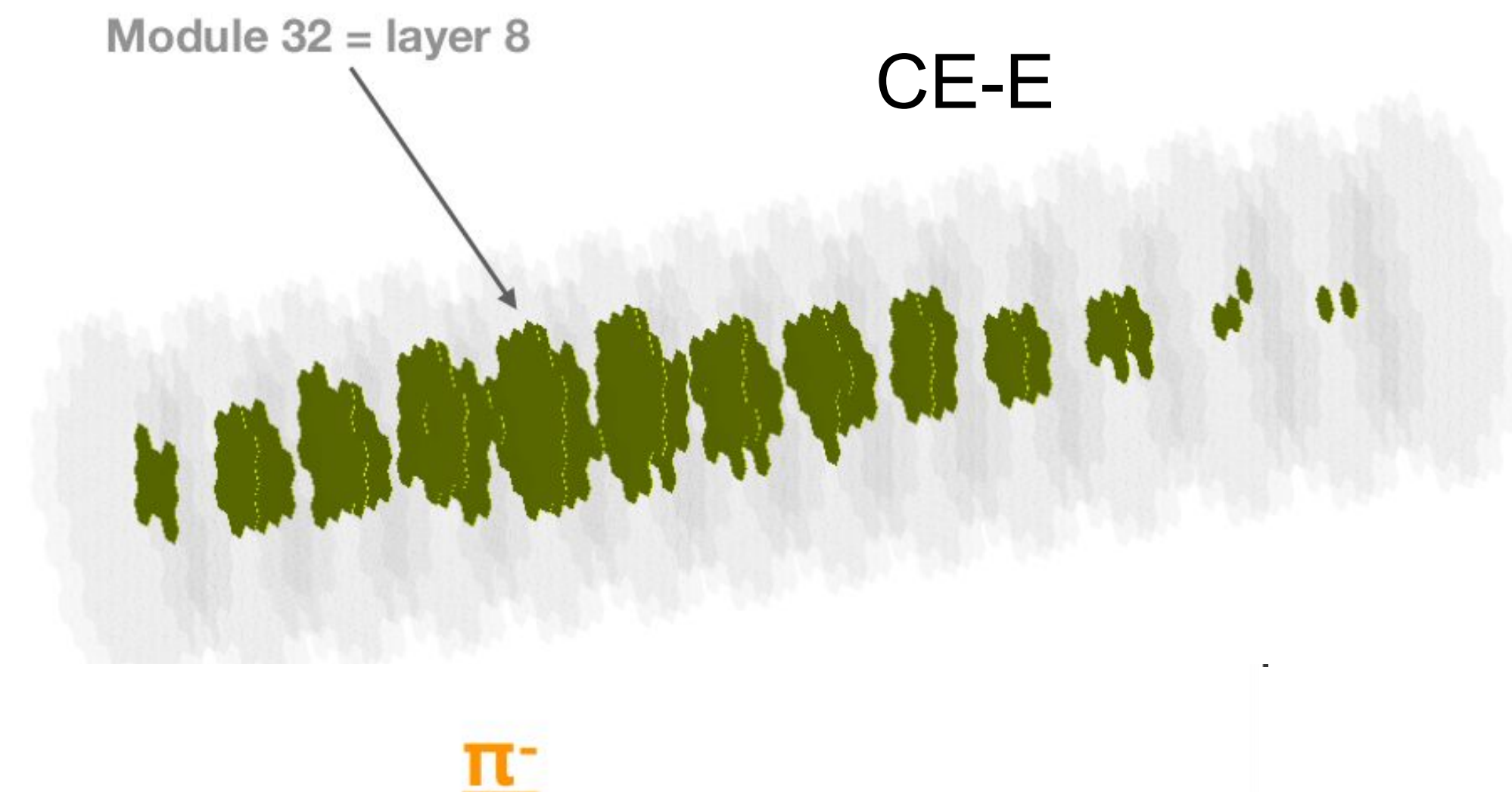
METHOD 2

Hits with > 50 MIPs contributions were selected

Observations:

- Electrons in CE-E
  - ◆ Const. term ~ 60 ps
- Pions in CE-E
  - ◆ Const. term < 100ps

$$T_{\text{shower}} = \frac{\sum_i^{E_i \geq 50 \text{ MIP}} E_i \cdot (T_i - \text{TOF}_i)}{\sum_i^{E_i \geq 50 \text{ MIP}} E_i}$$

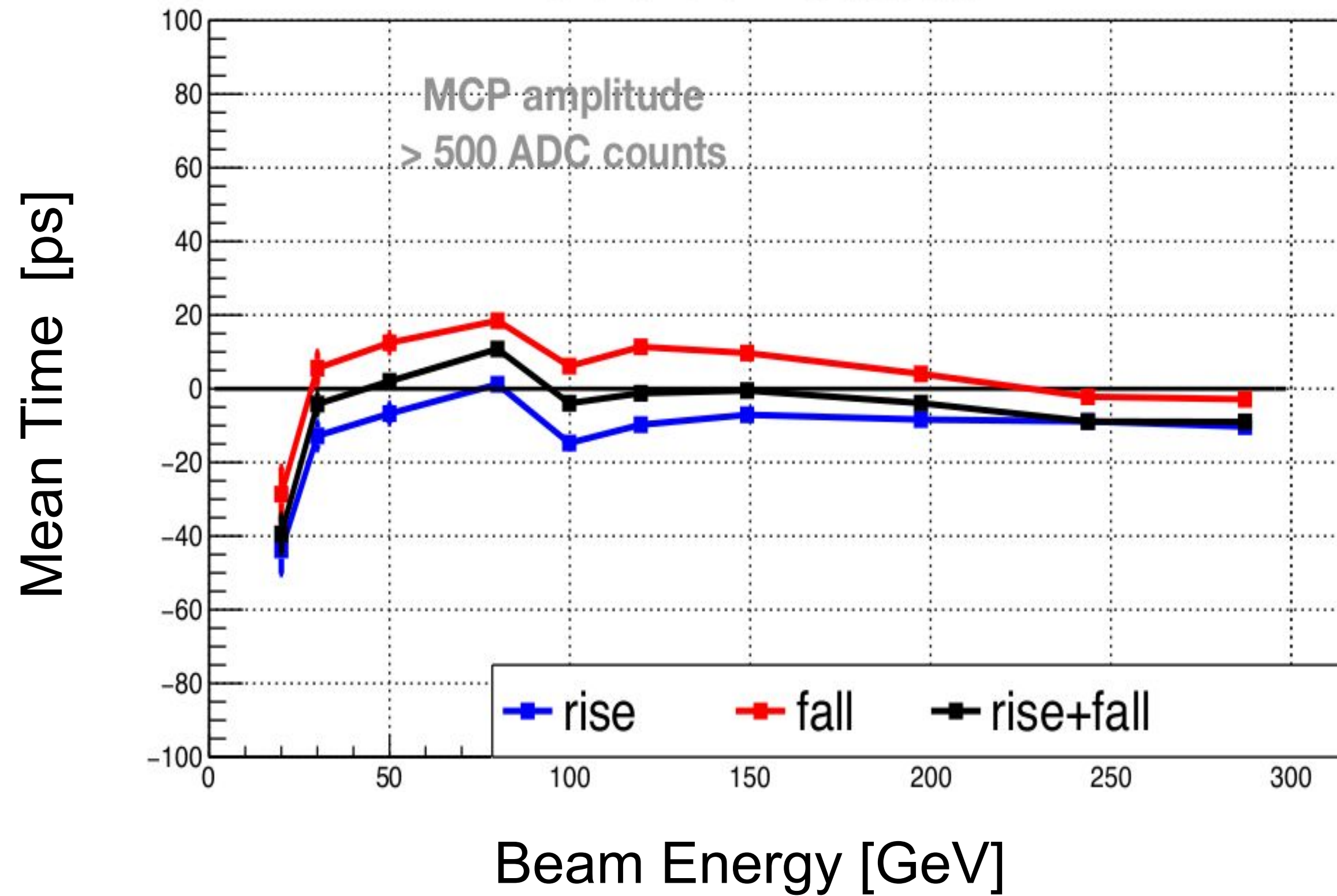




# Stability of the shower timing with respect to beam energy

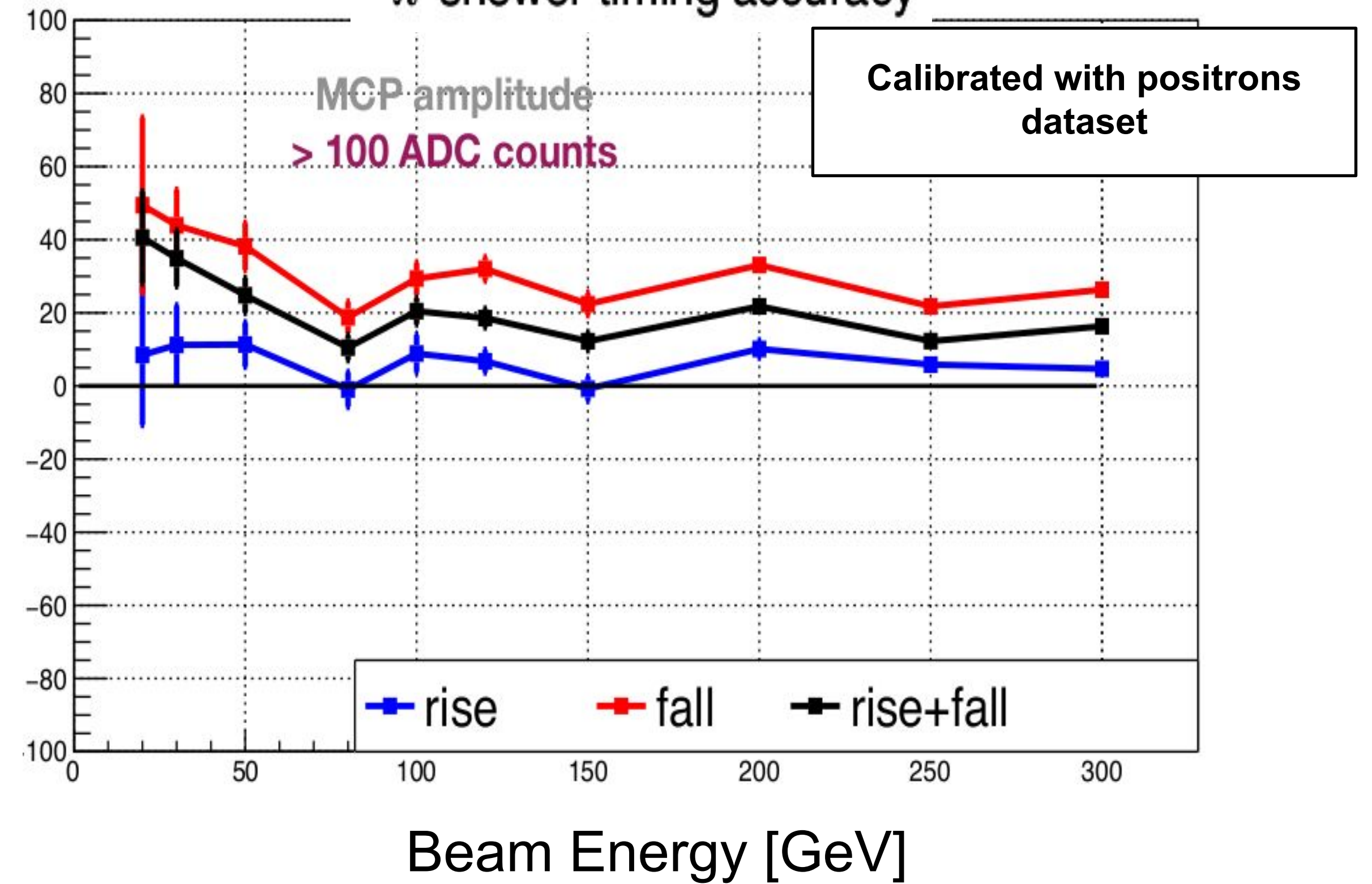
$e^+$

$e^+$  shower timing accuracy



$\pi^-$

$\pi^-$  shower timing accuracy





# Monte Carlo Simulation of HGCAL Prototype

## Algorithm to measure time:

- Electron Beams (20-300 GeV)
- Selection Implicitly requires > 15MIPs (simulating voltage threshold)
- CE-E Channels Considered:
  - ◆ All Cells
  - ◆ 7-Cells (1 (max hit) + 6 (neighbour))
  - ◆ 19-Cells (1 + 18(neighbours))
- Shower timing is *truncated*
  - ◆ Keep only the hits from the smallest interval containing **68% the timing distribution**

## We observe:

- Differences in 7-cell and 19-cell clusters
  - ◆ Hits are dispersed laterally
- At low beam energy, we expect bigger average times, if any, not smaller as seen in Fig 2 (7,9 cell cluster)

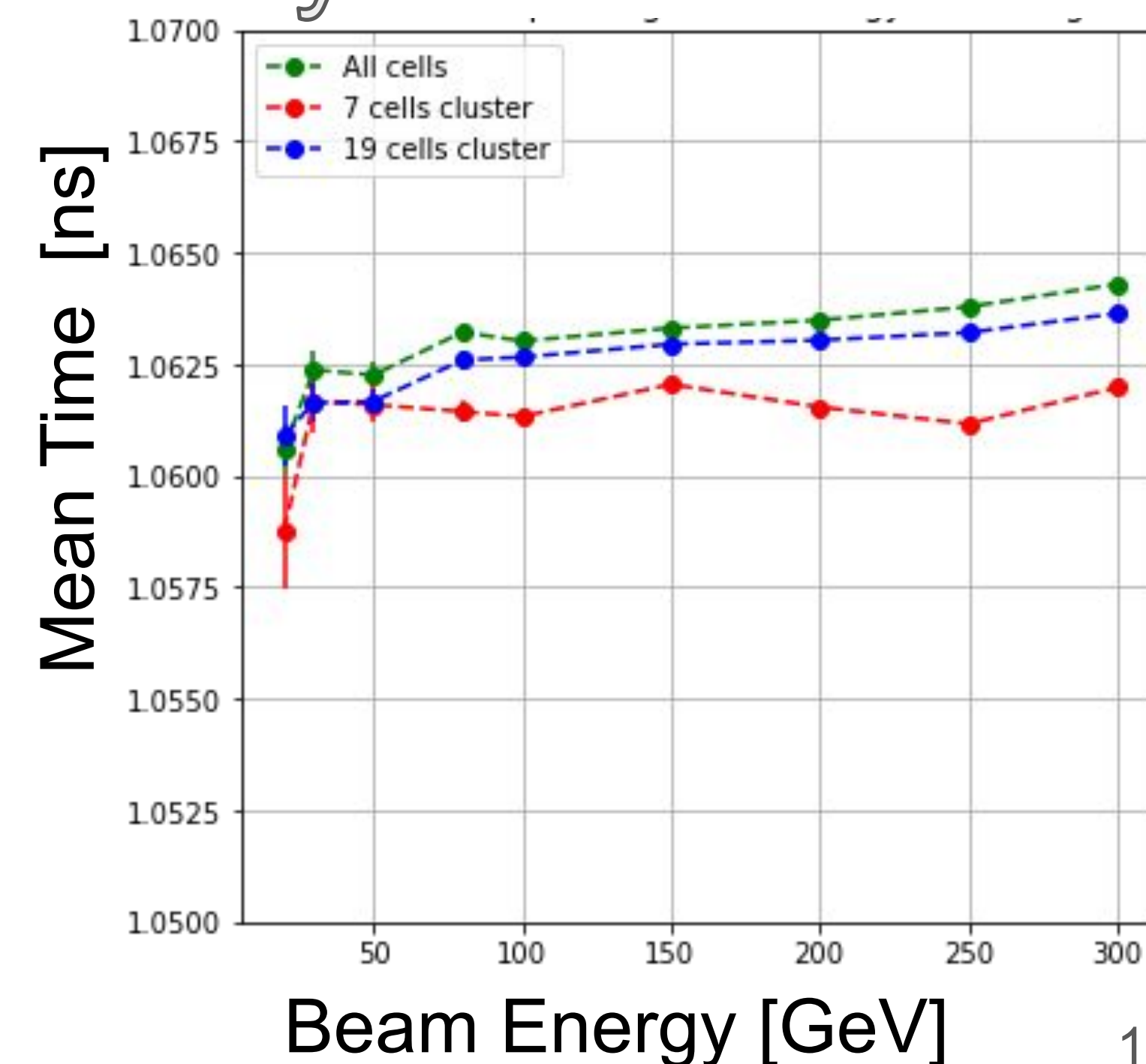
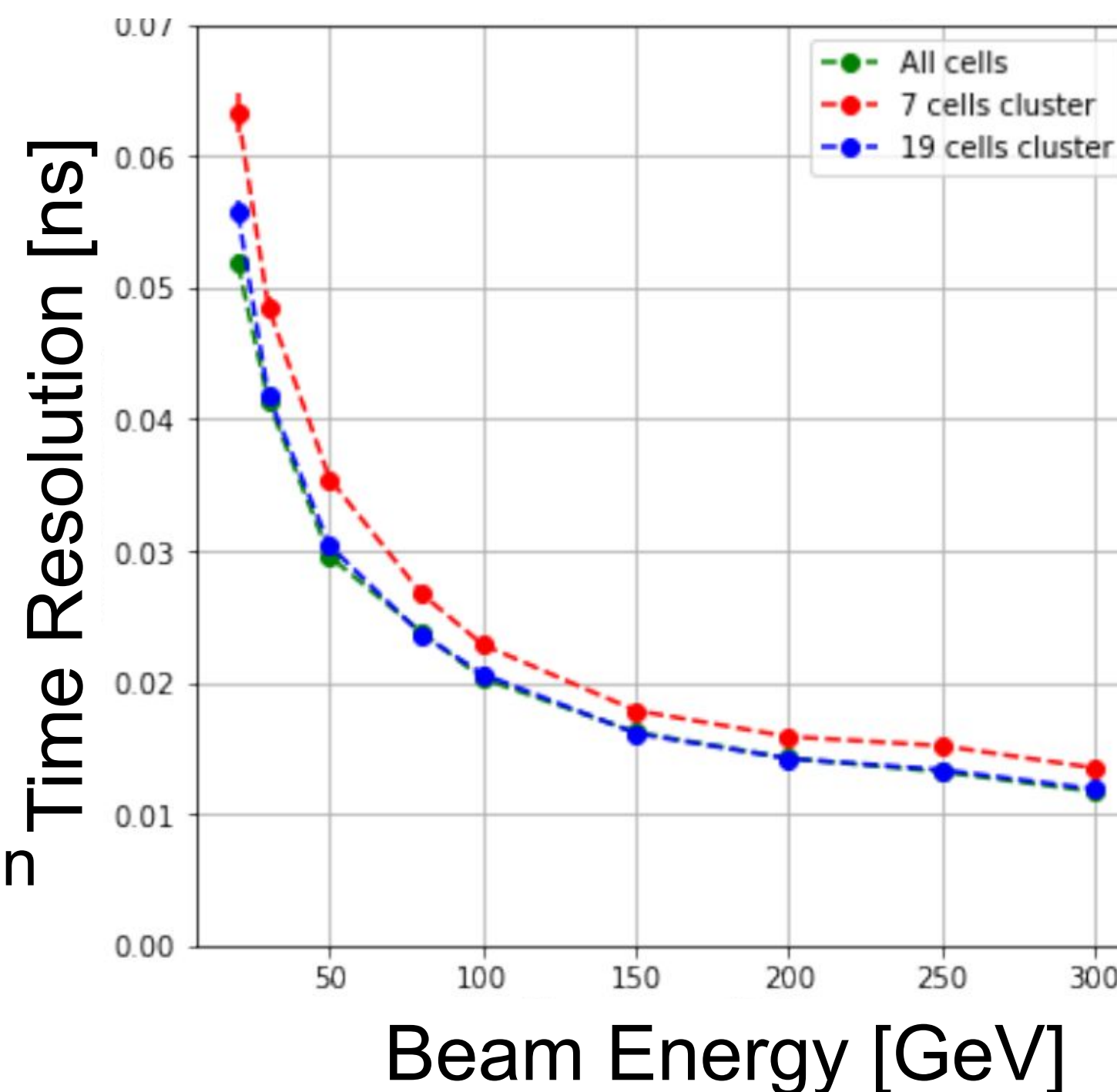
Time was smeared using parameters derived from data

$$y = \frac{A}{Energy} \oplus C$$

Derived from Si-channel compared to another Si-channel test beam data

Const Term (C) = 50ps ; Stochastic Term (A) = 10 MIP.ns

Preliminary





# Conclusion

HGCAL prototype was designed with radiation hardness and superior time-resolution in mind

## Test Beam 2018:

- We observe a constant term of  $\sim 60\text{ps}$  for electrons and  $< 100\text{ps}$  for pions in the CE-E
  - ◆ *Combined using simple energy weighting between channels*
  - ◆ *Expected to improve with resolution weighting and improved reconstruction algorithms*
  - ◆ ***Preliminary results appears to be consistent with specification of the SKIROC2\_CMS ASIC***
- Timing studies were carried out on full statistics
- Geant4 Simulation yields insightful results
  - ◆ *Timing performance for electrons in the CE-E was studied*
  - ◆ *MC data was smeared using results derived from data*

## Next Steps:

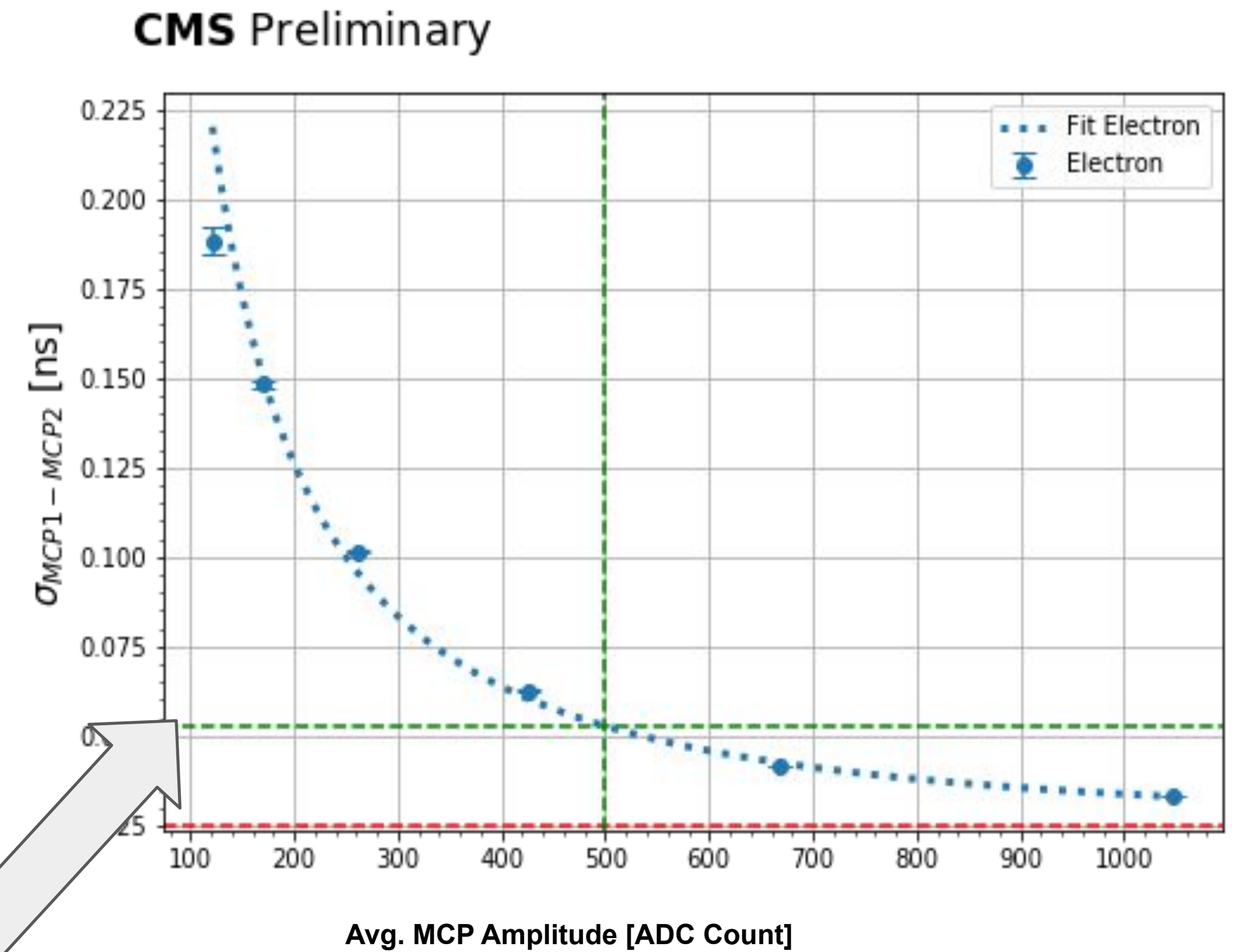
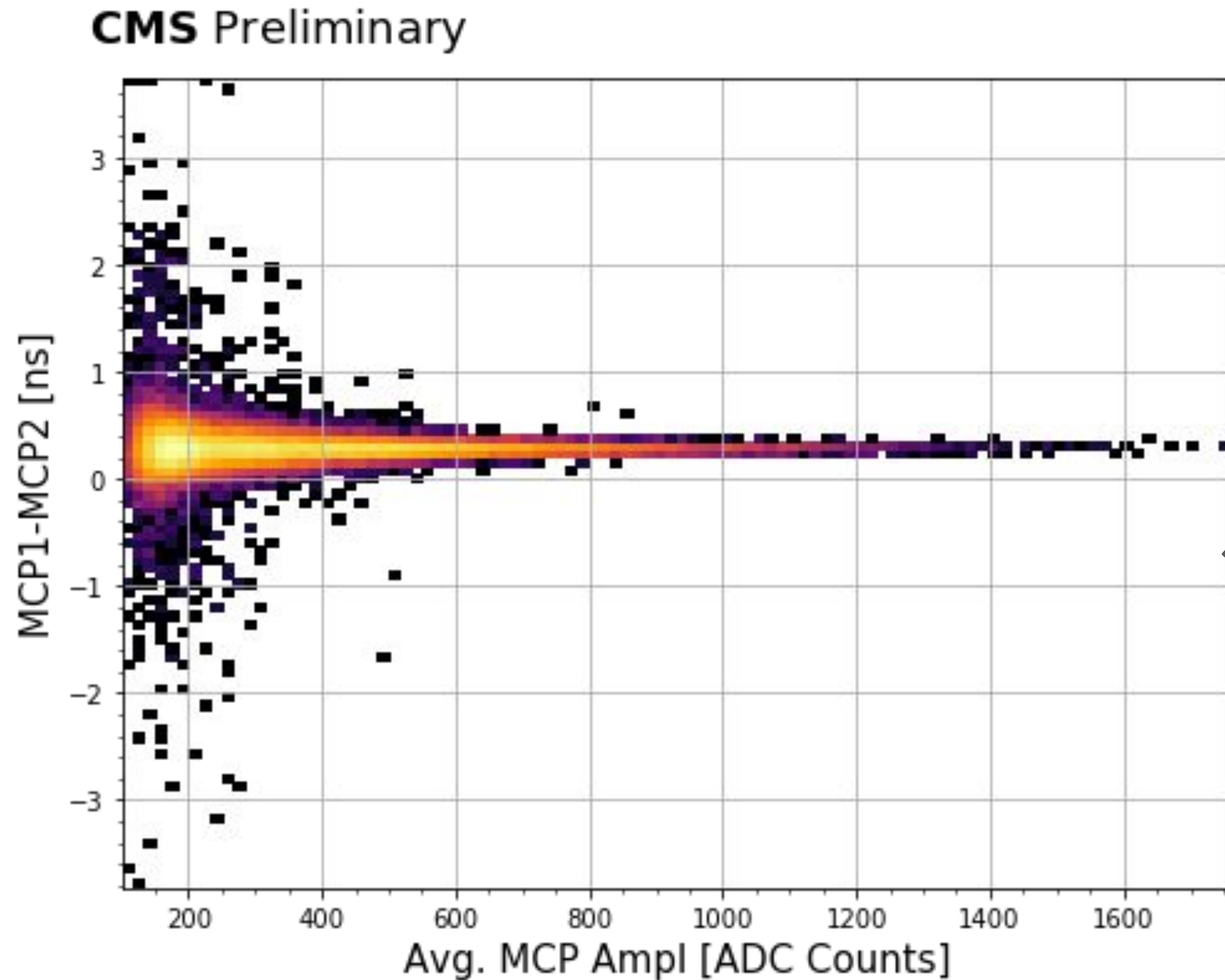
- Comparison of MC result to data
- Extending the study to CE-H-Si for Hadronic Showers



# Backup of Timing Analysis



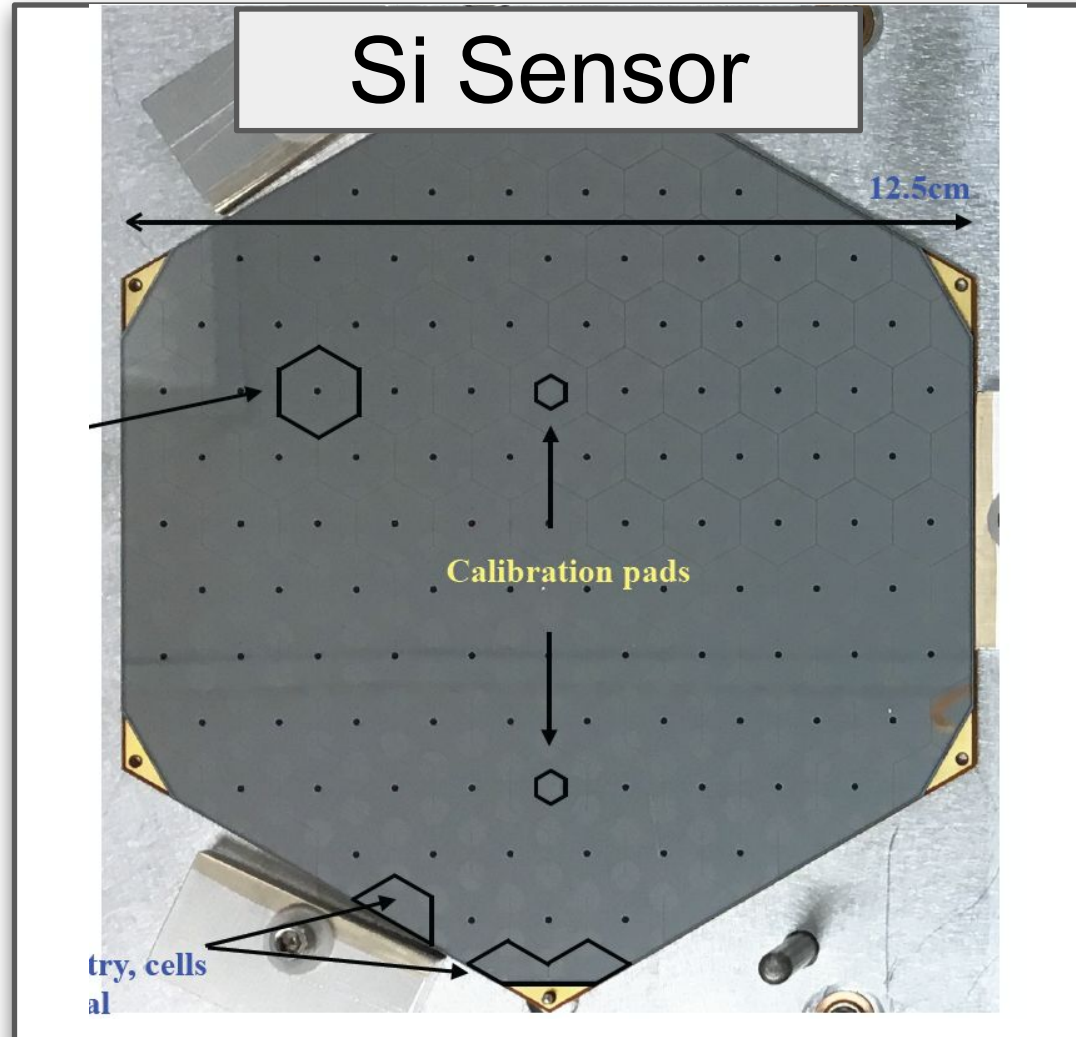
# MCP Detector 2D Histogram



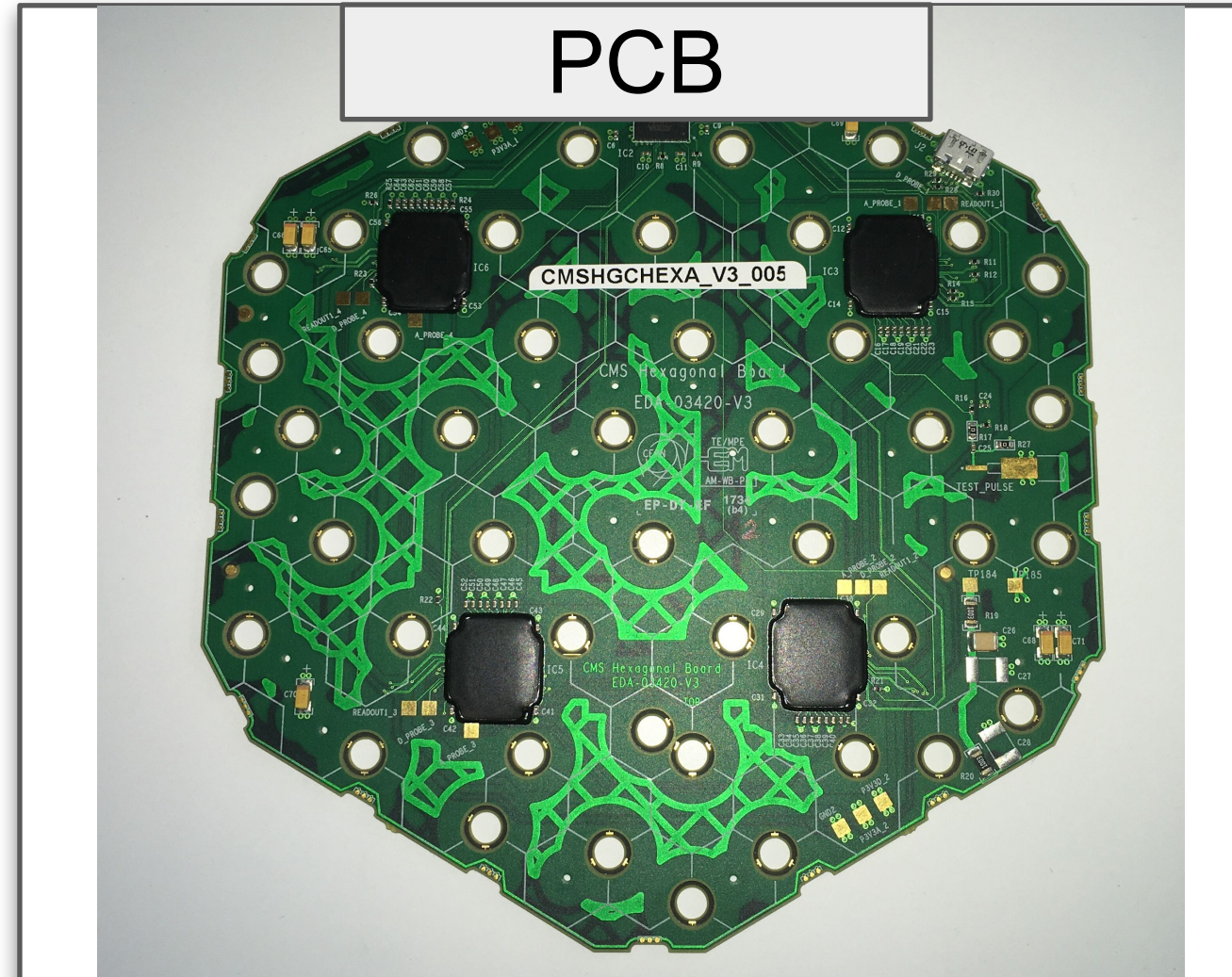


# HGCAL Prototype Modules

## Active Materials

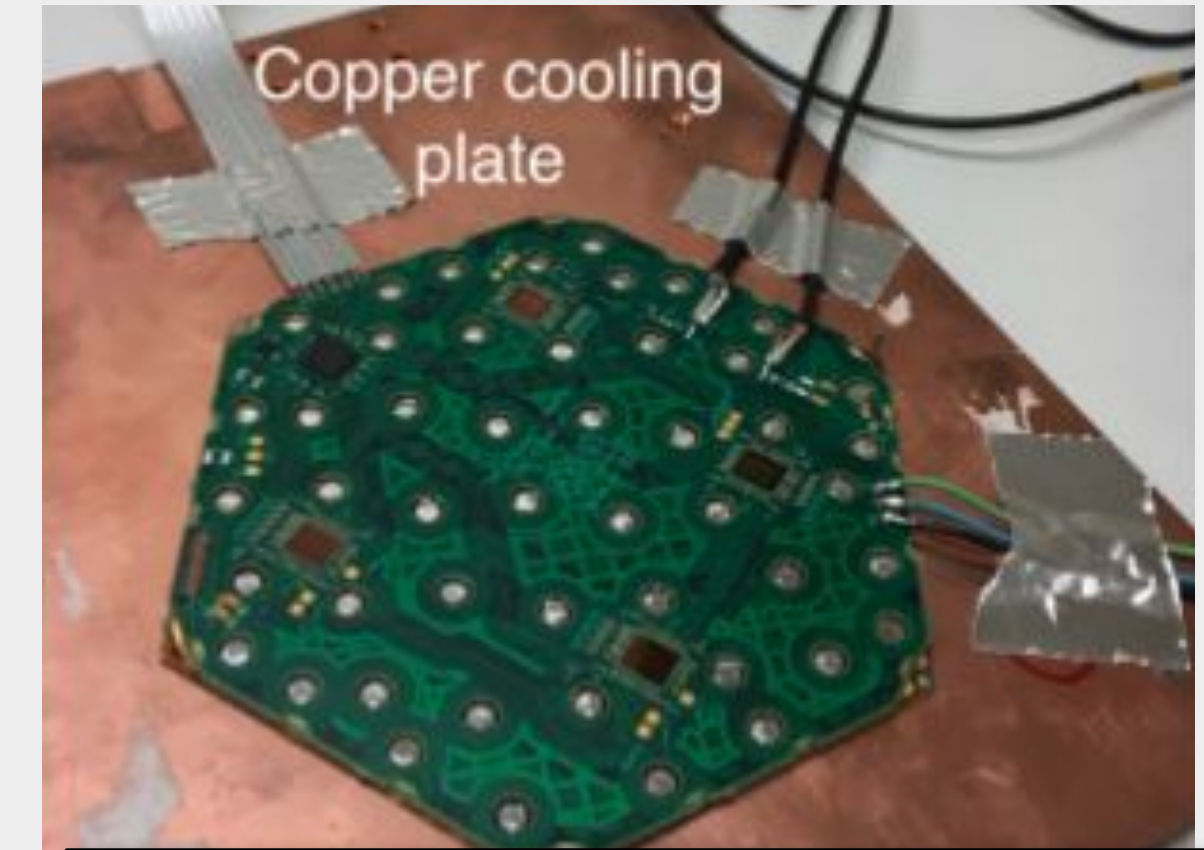
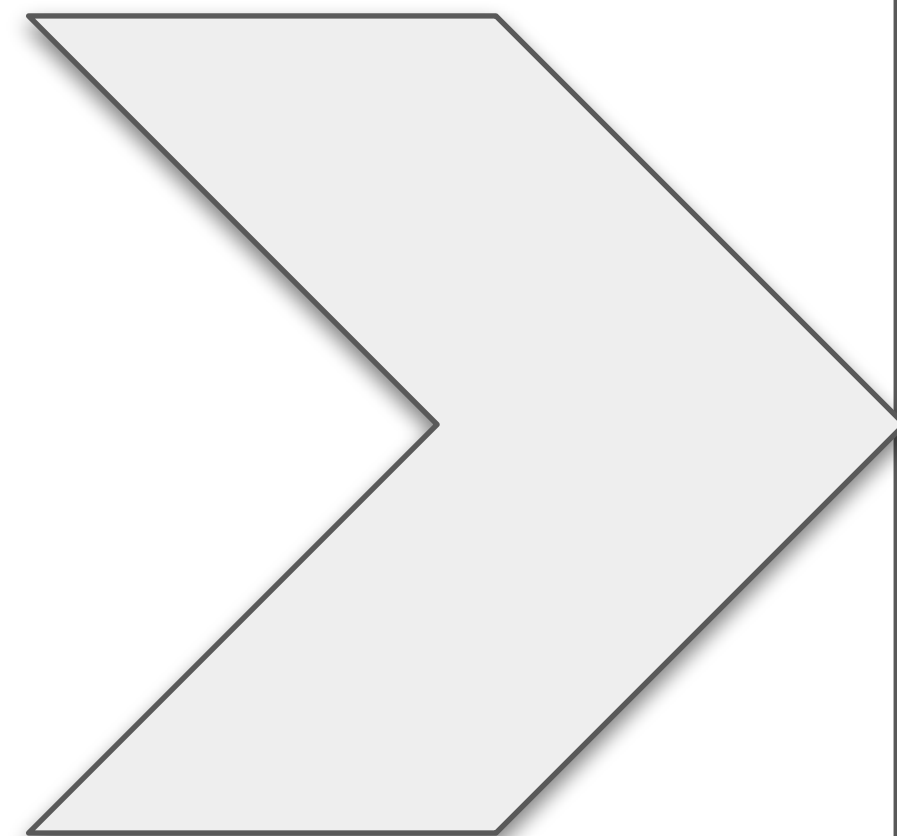


**6" Si Sensors**  
 n-type, 128 cells  
 1 cm<sup>2</sup> cell size  
 depletion: 200 & 300μm



**SKIROC2 CMS ASIC**  
 - 64 Ch., 4 Chips/Module  
 Developed for CALICE (SKIROC2)  
 & adjusted for HGCal

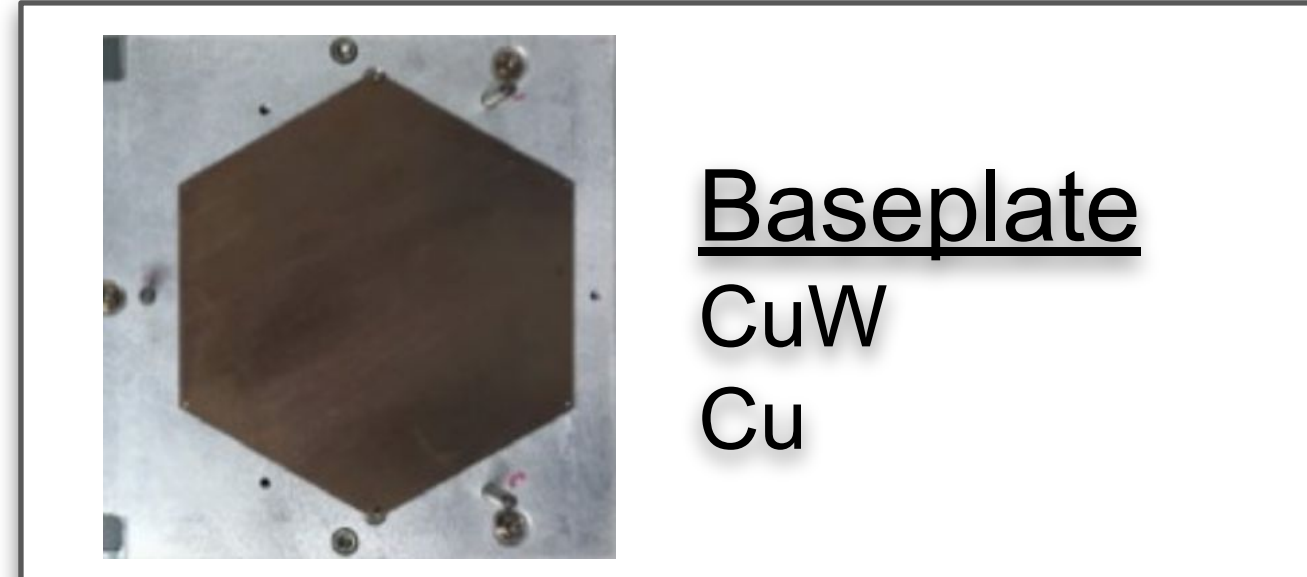
Wire-bonded and  
 glued together



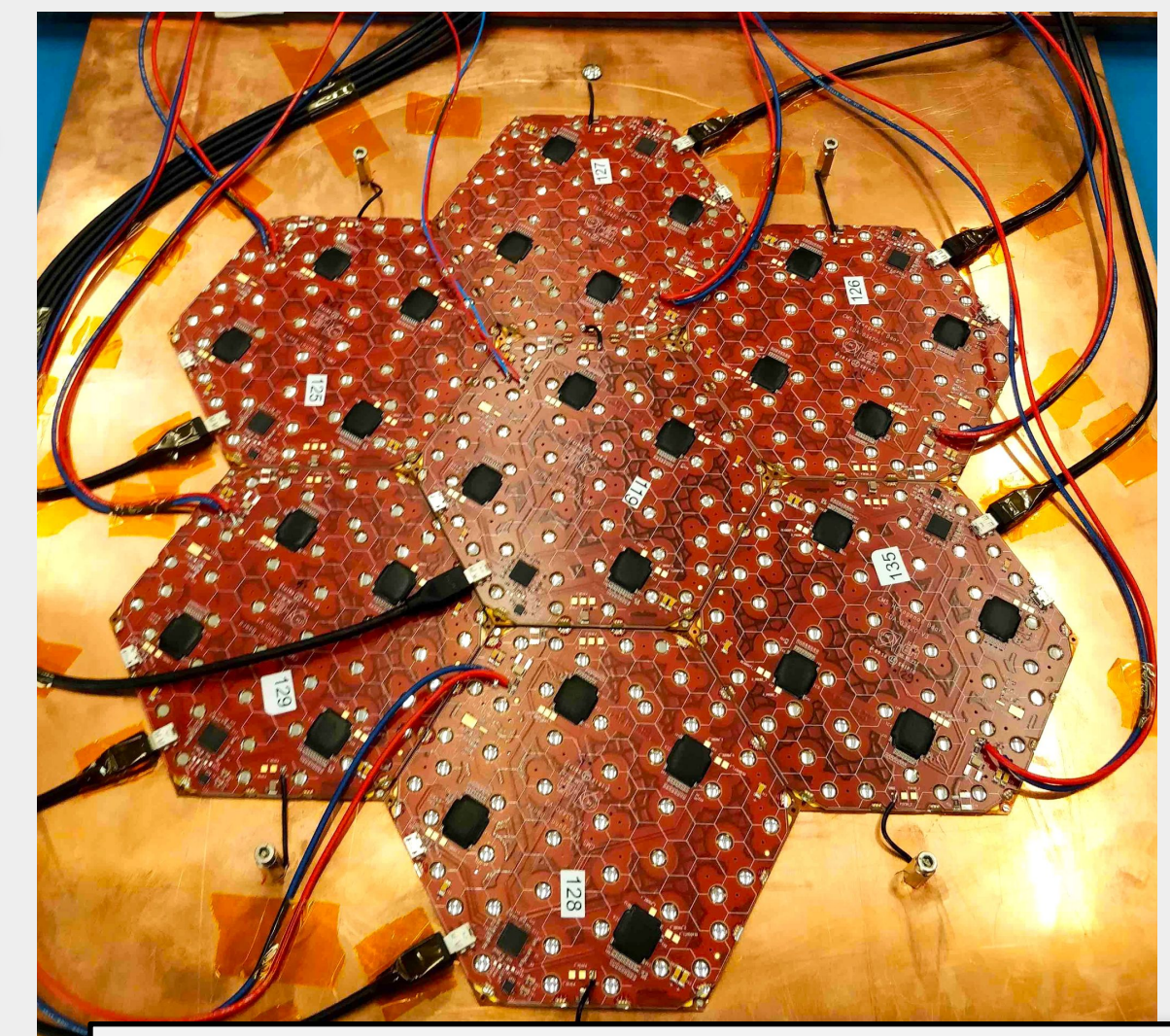
**CE-E Single Module Layer**



**Kapton<sup>®</sup>**  
 Gold Plated



**Baseplate**  
 CuW  
 Cu



**CE-H Seven Module Layer**



# Testbeam Configurations

## PASSIVE MATERIAL

### CE-E:

- Pb, W, Cu
- 5-6 mm thickness

### CE-H-Si:

- Fe
- 4 cm thickness
- O(1000Kg) weight

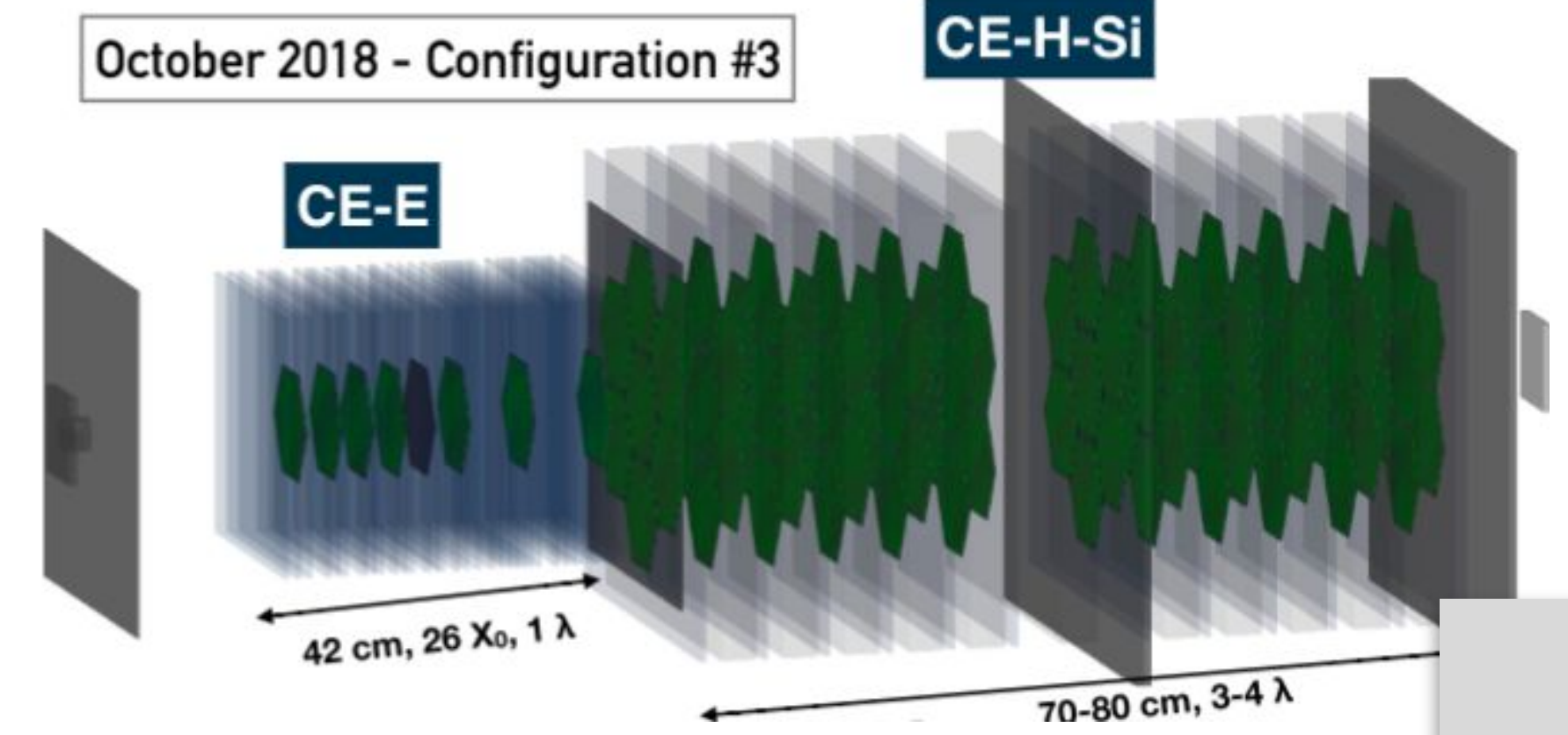


Fig 1

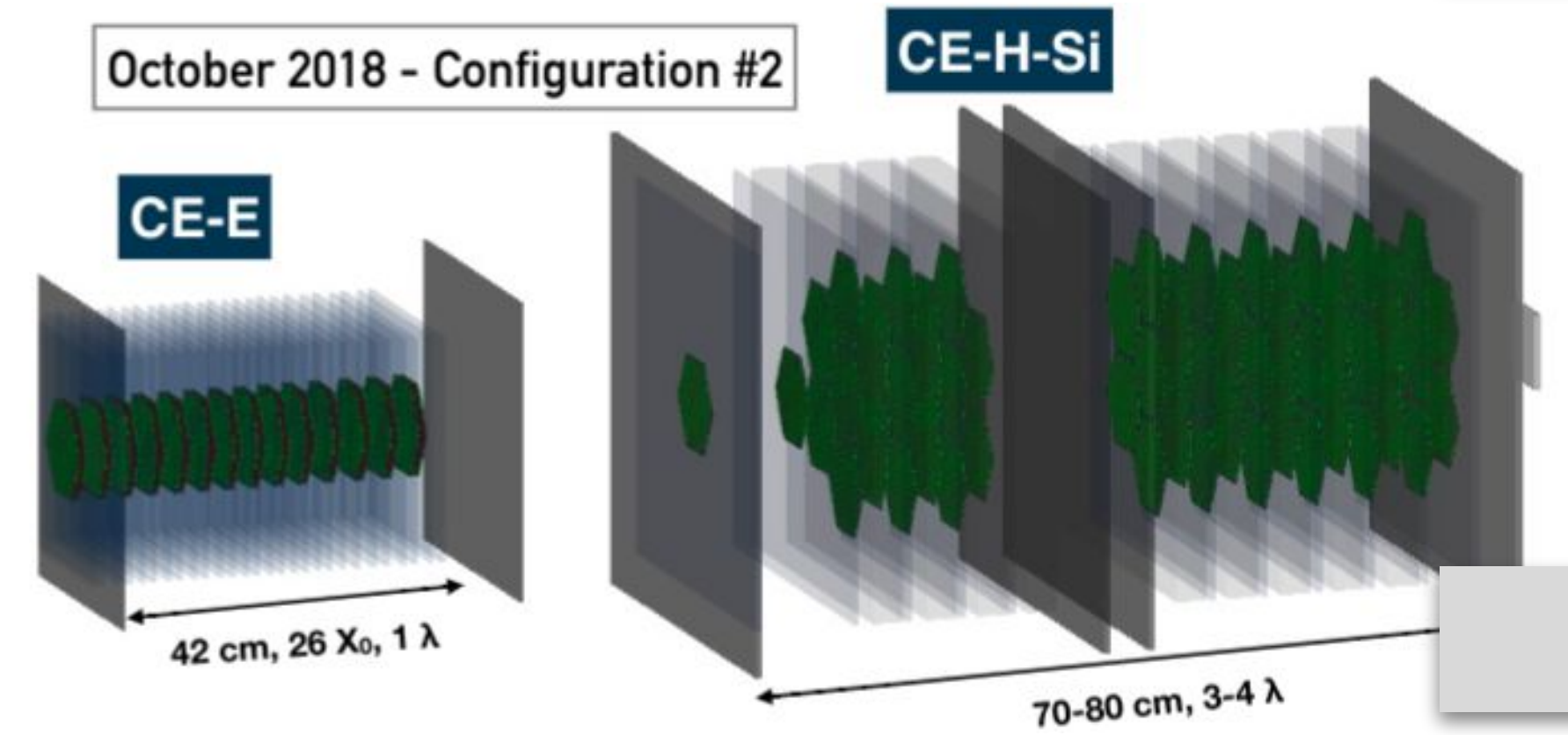
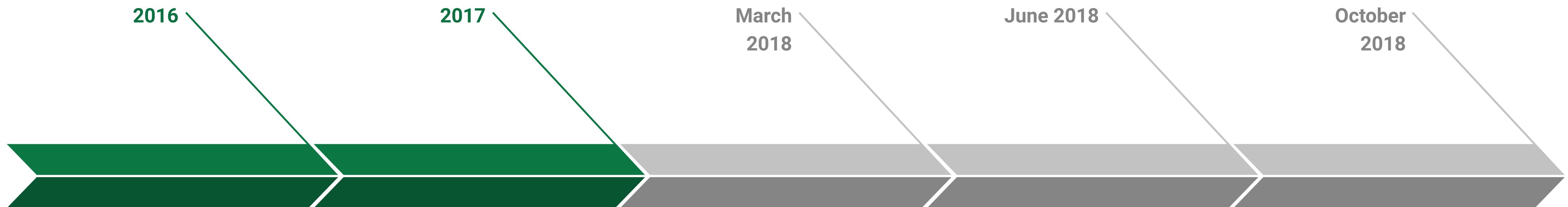


Fig 2



N Akchurin et al.  
2018 JINST 13 P10023

First Tests with  
SKIROC2-CMS ASIC

Tests @DESY

3 Modules

Tests @SPS CERN

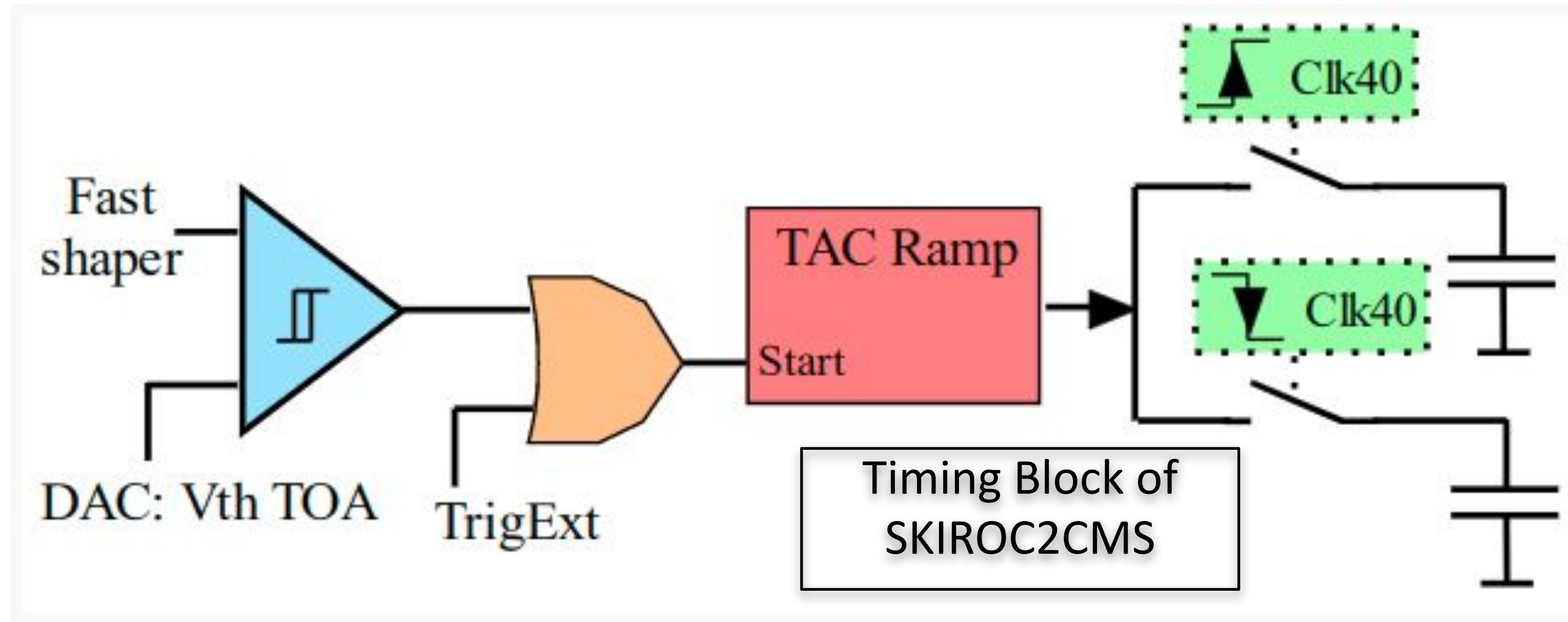
Full CE-E:  
28 modules

Tests @SPS CERN

Full Prototype:  
94 Modules



# HGCAL Prototype Timing Circuit



- SKIROC2\_CMS Timing Circuit



5ns Shaping Time

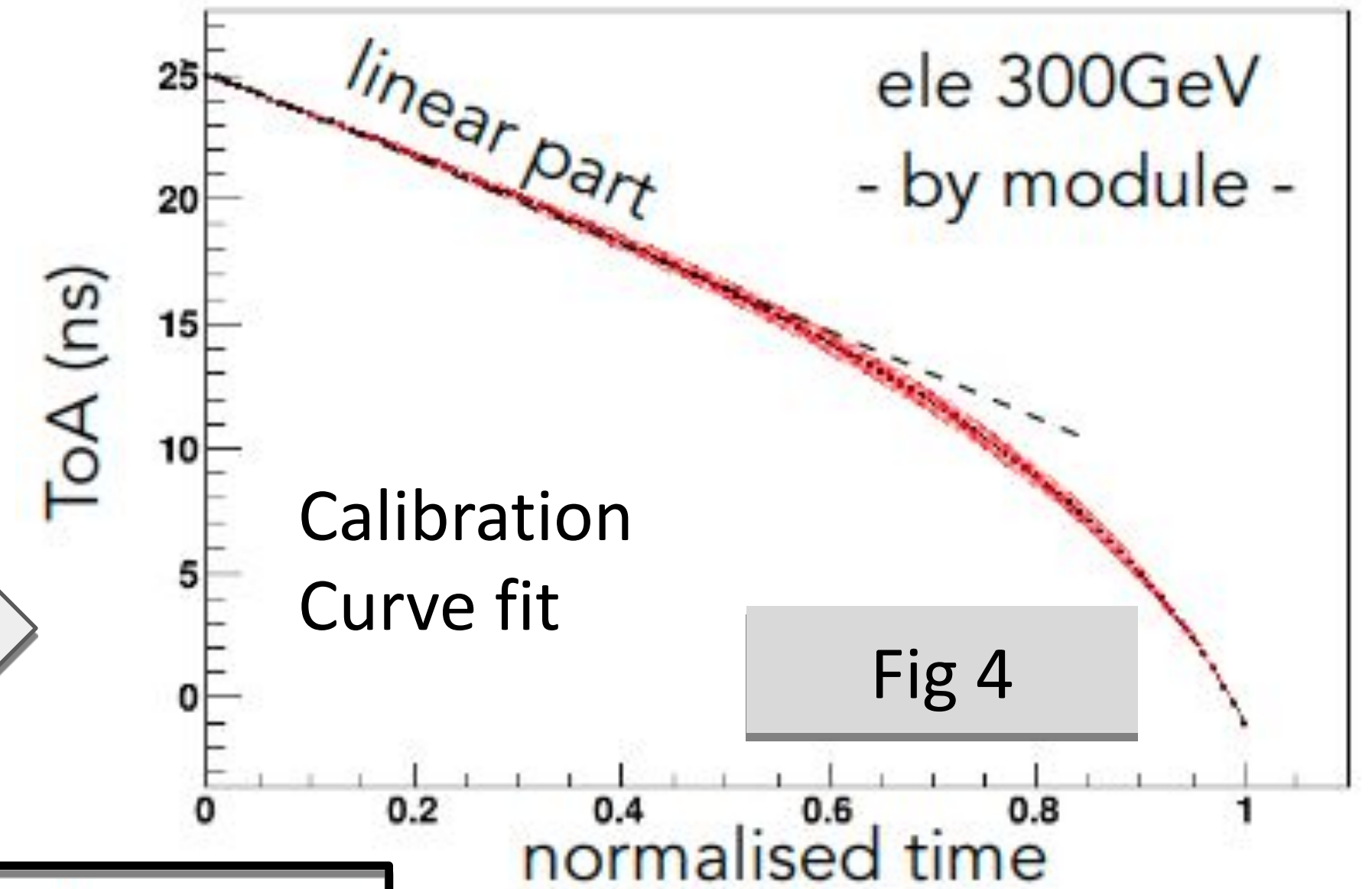
Voltage threshold set  
to >15 MIPs  
equivalent

Clocks the  
signal w.r.t  
Rising and  
Falling Edge of  
the Clock



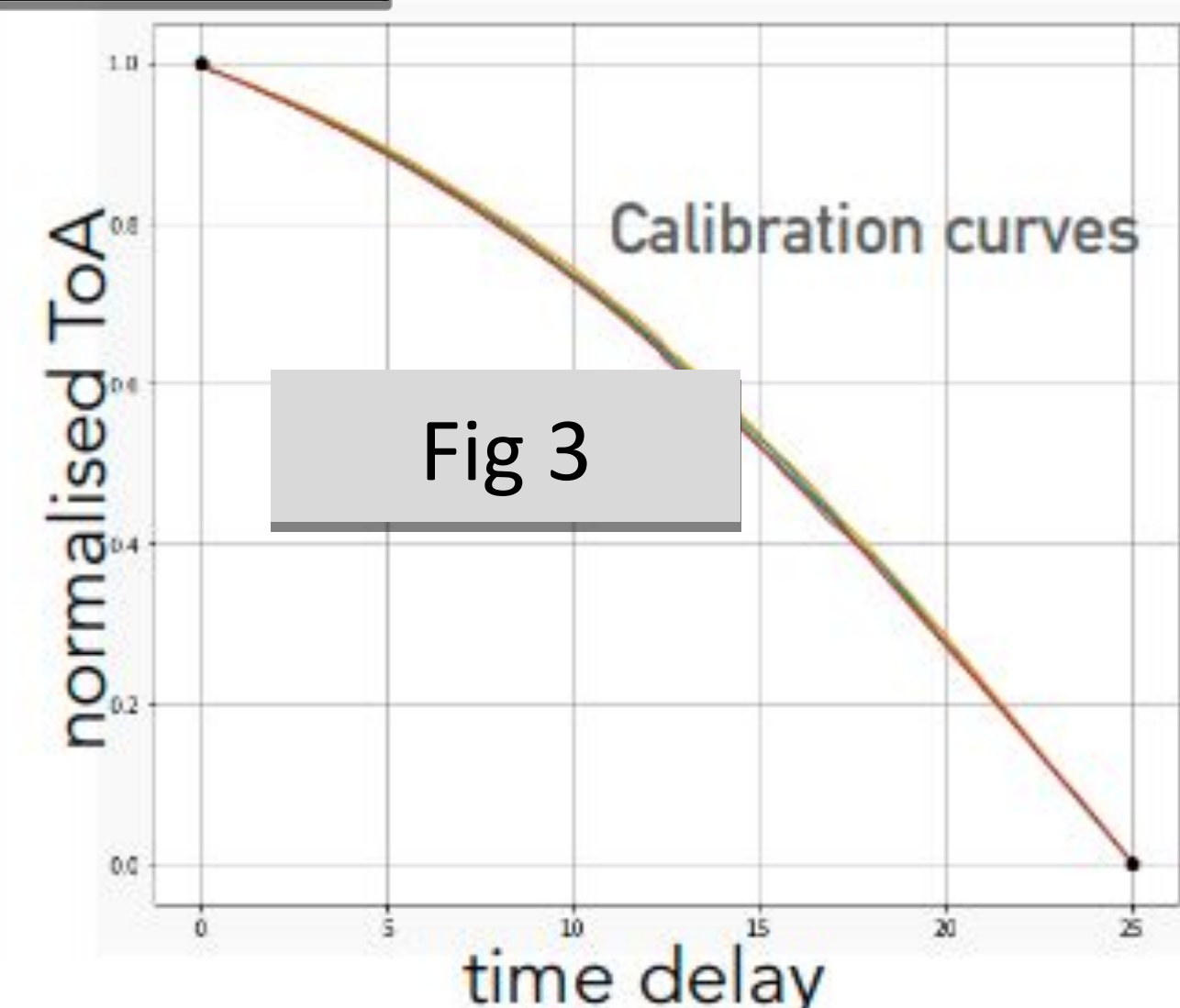
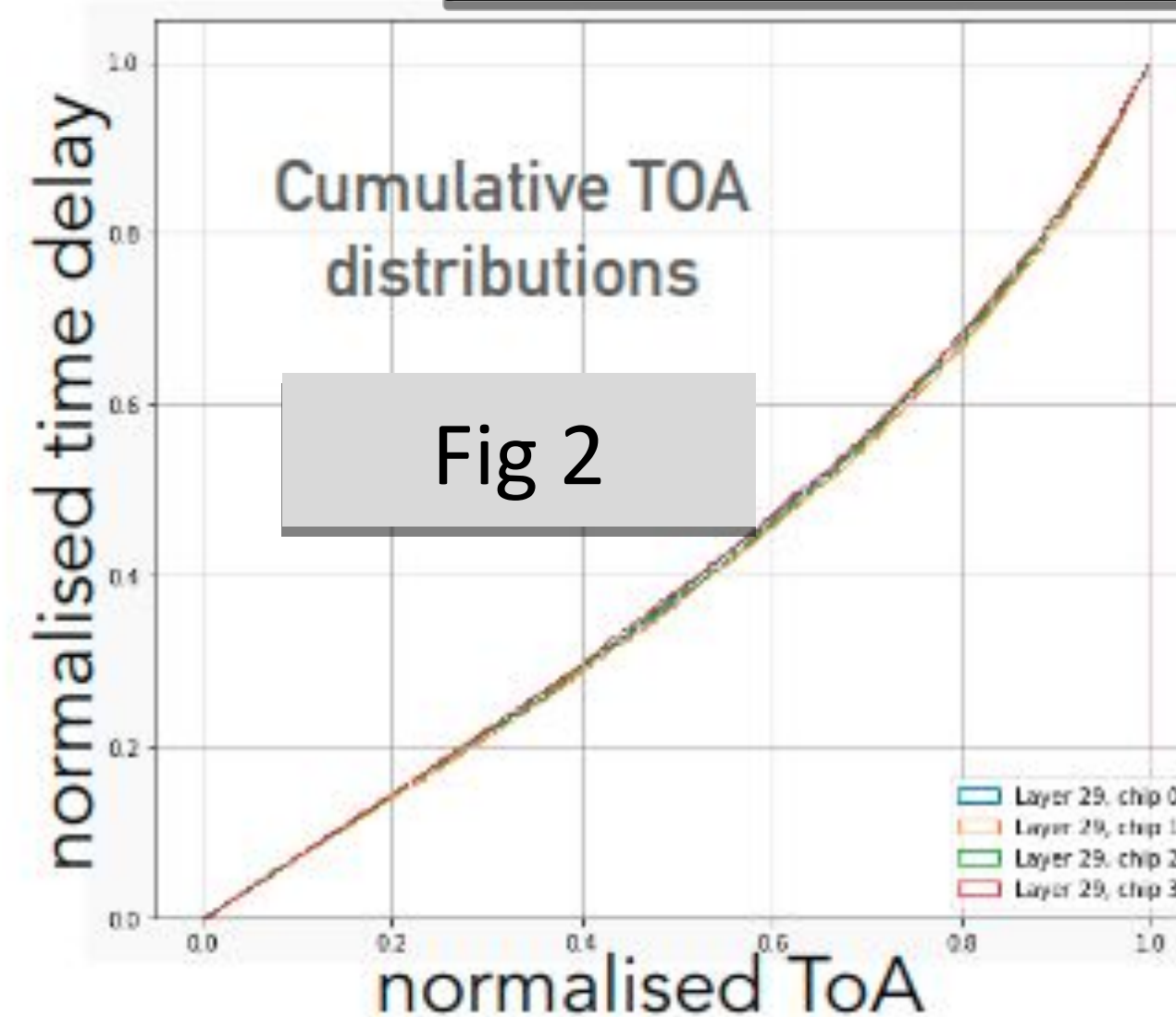
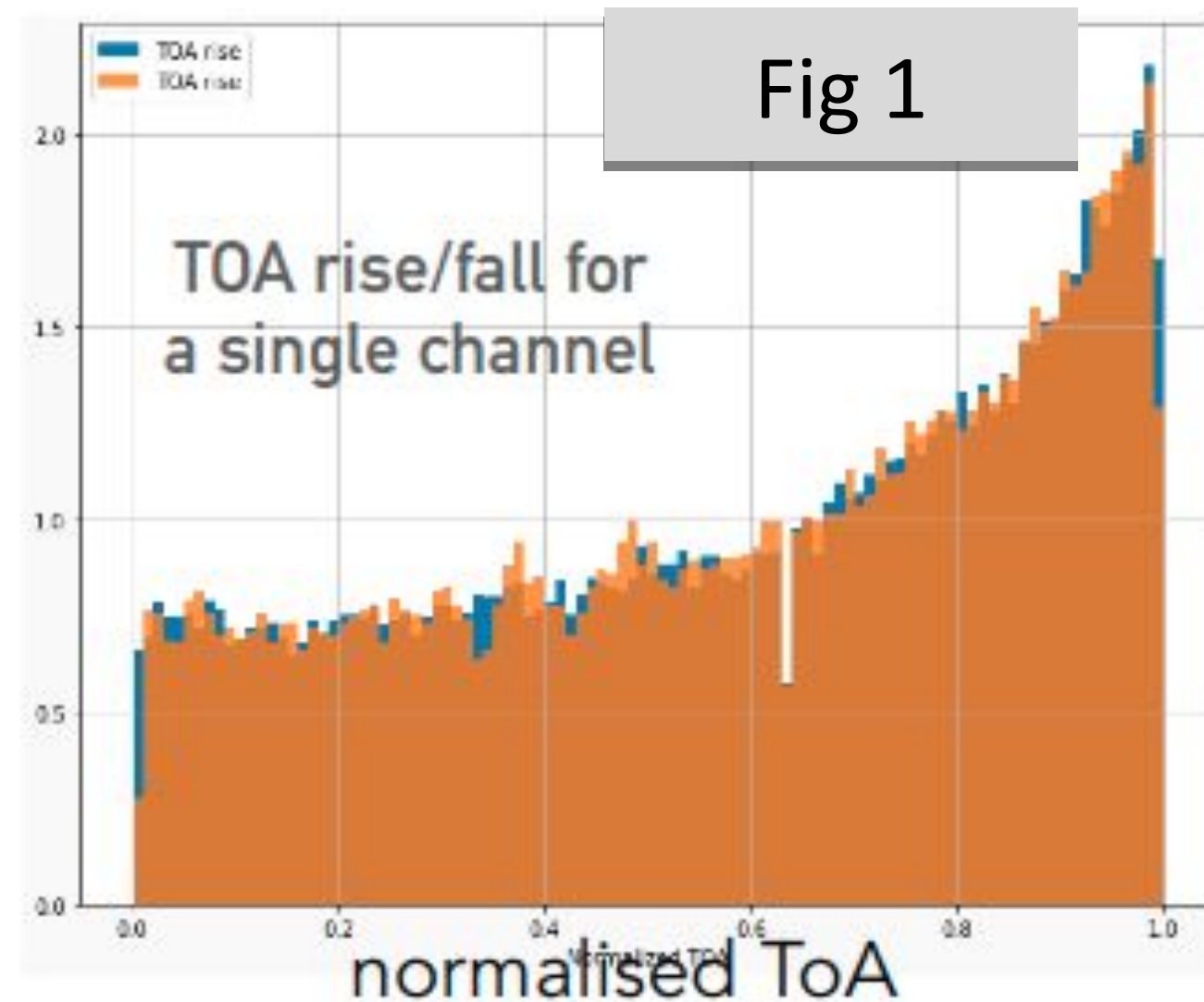
# Calibration -- Linearisation

- The ramp saturation causes non-linearity in the TOA
- This was calibrated using a data driven method which exploits the asynchronous nature of the internal clock and the beam.
- Sampled with a uniformly distributed beam delay from which we derived the time calibration curves [[more info](#)]



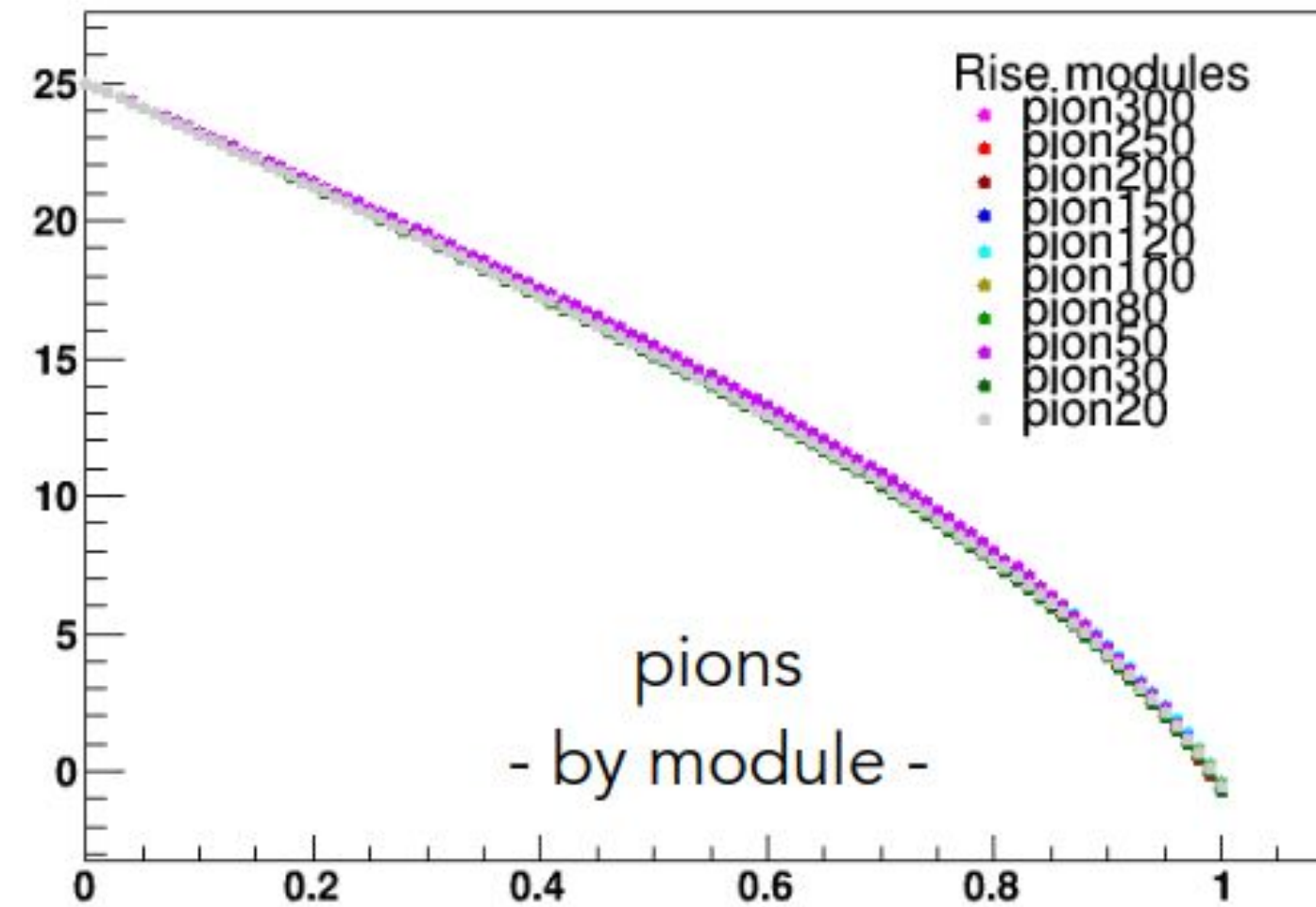
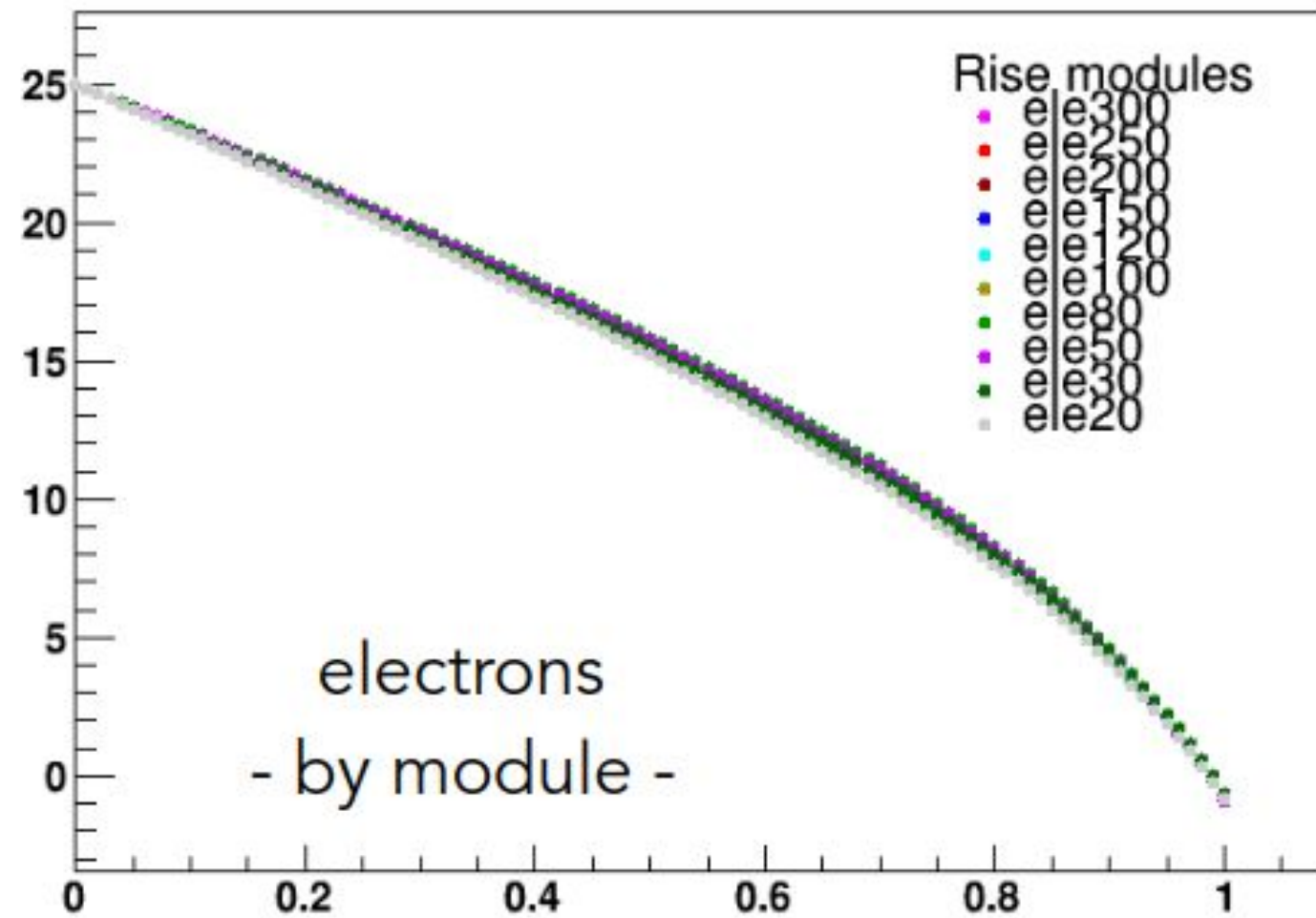
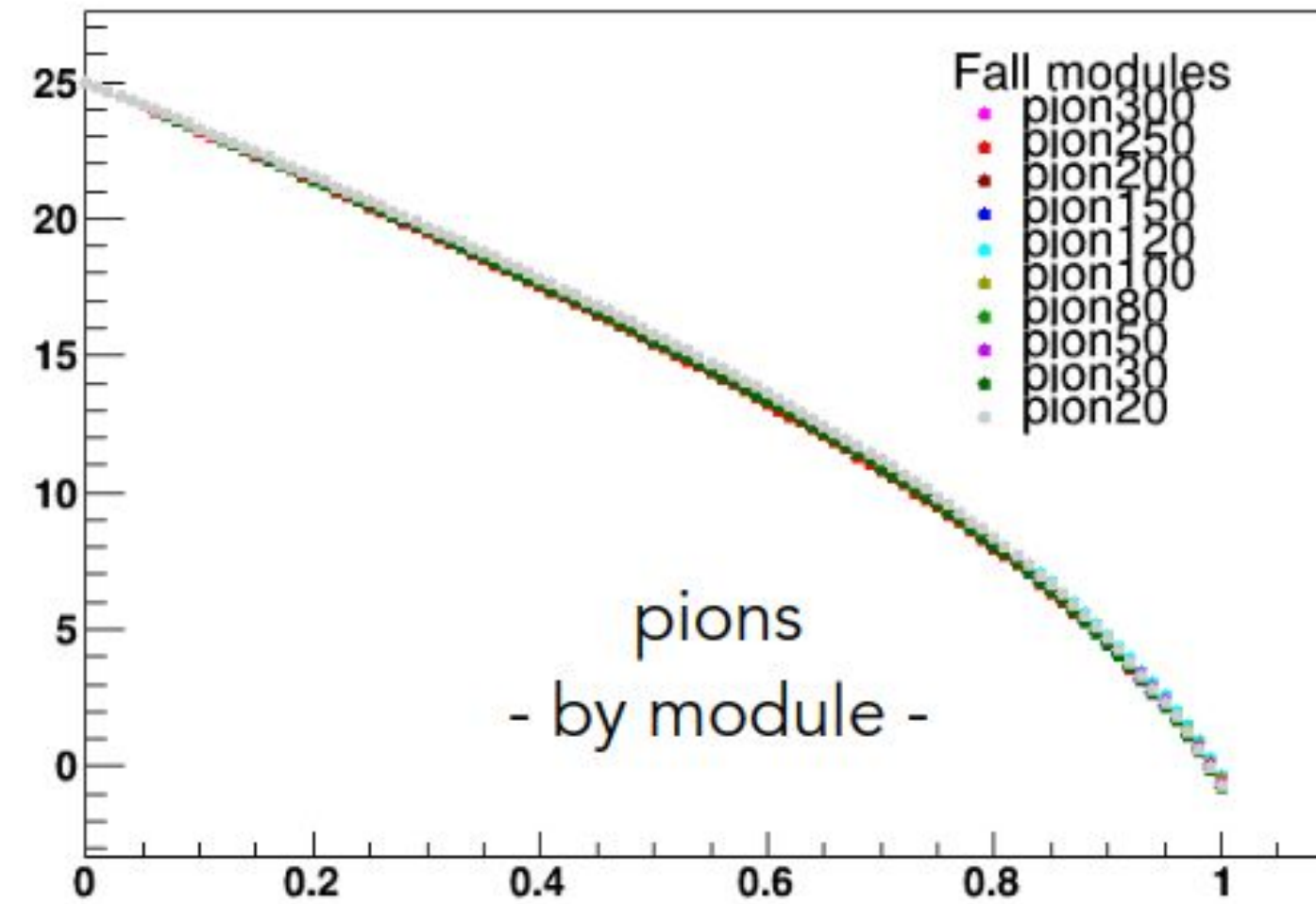
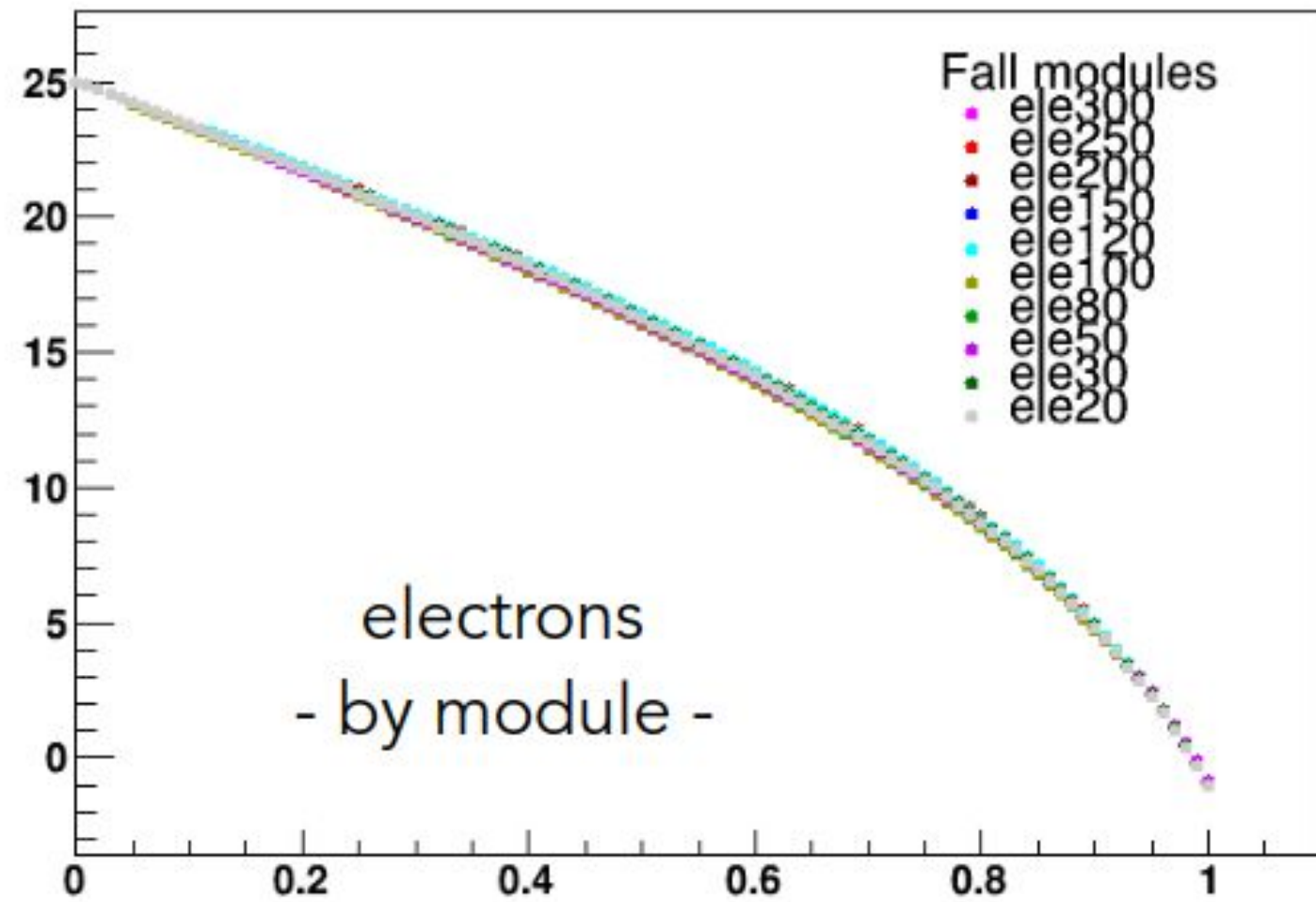
$$[0] * x + 25 + [1] * \left( \frac{1}{x - 1.25} + 0.8 \right)$$

Equation 1: Fit curve for 300 GeV Electron





# TOA Linearisation (Performance)



→ Reasonably stable over

- ◆ Beam Energies
- ◆ Rise and Fall

→ Calibration applied on the smallest level of granularity (per channel)

- ◆ If the channel doesn't have stats the following preference is applied



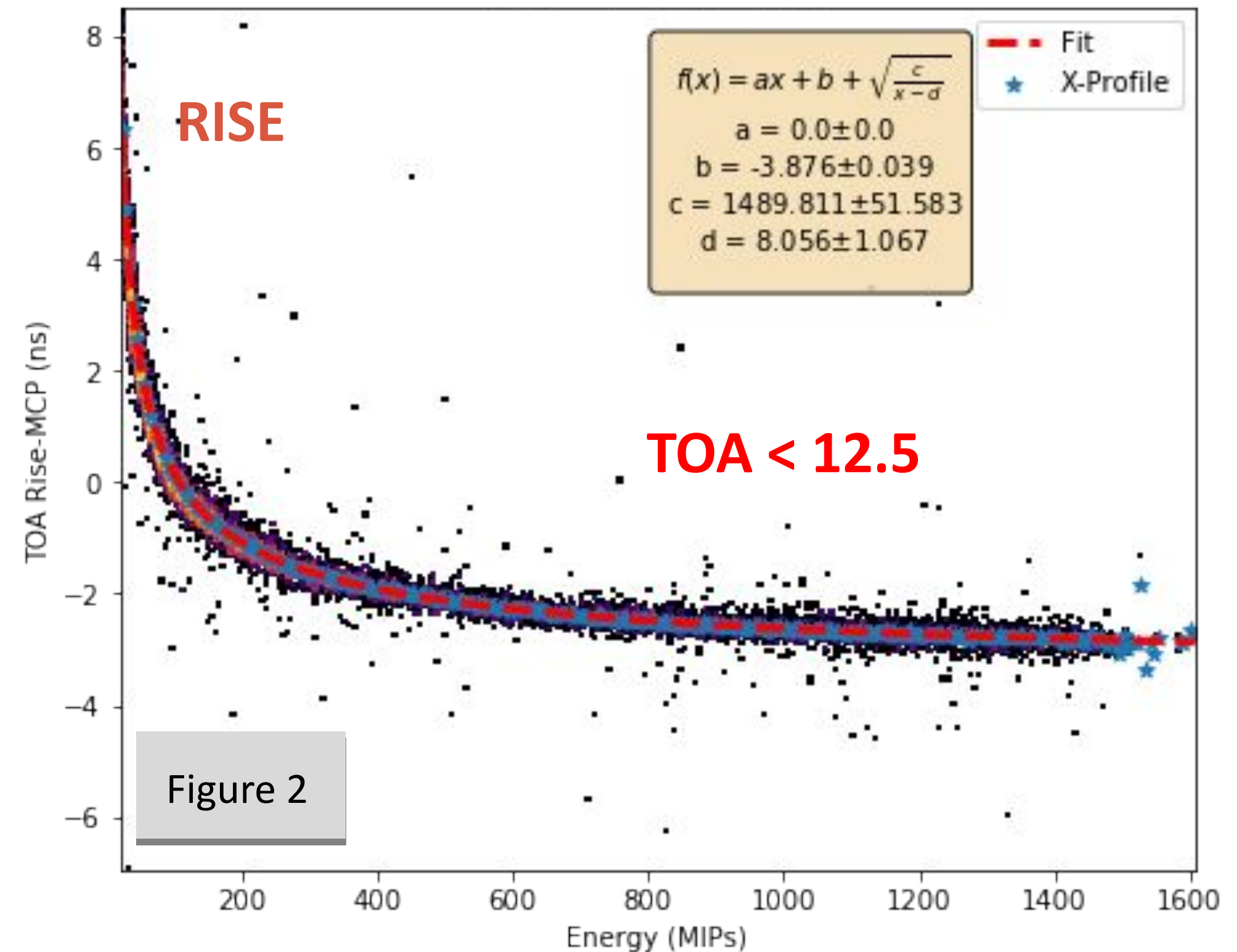
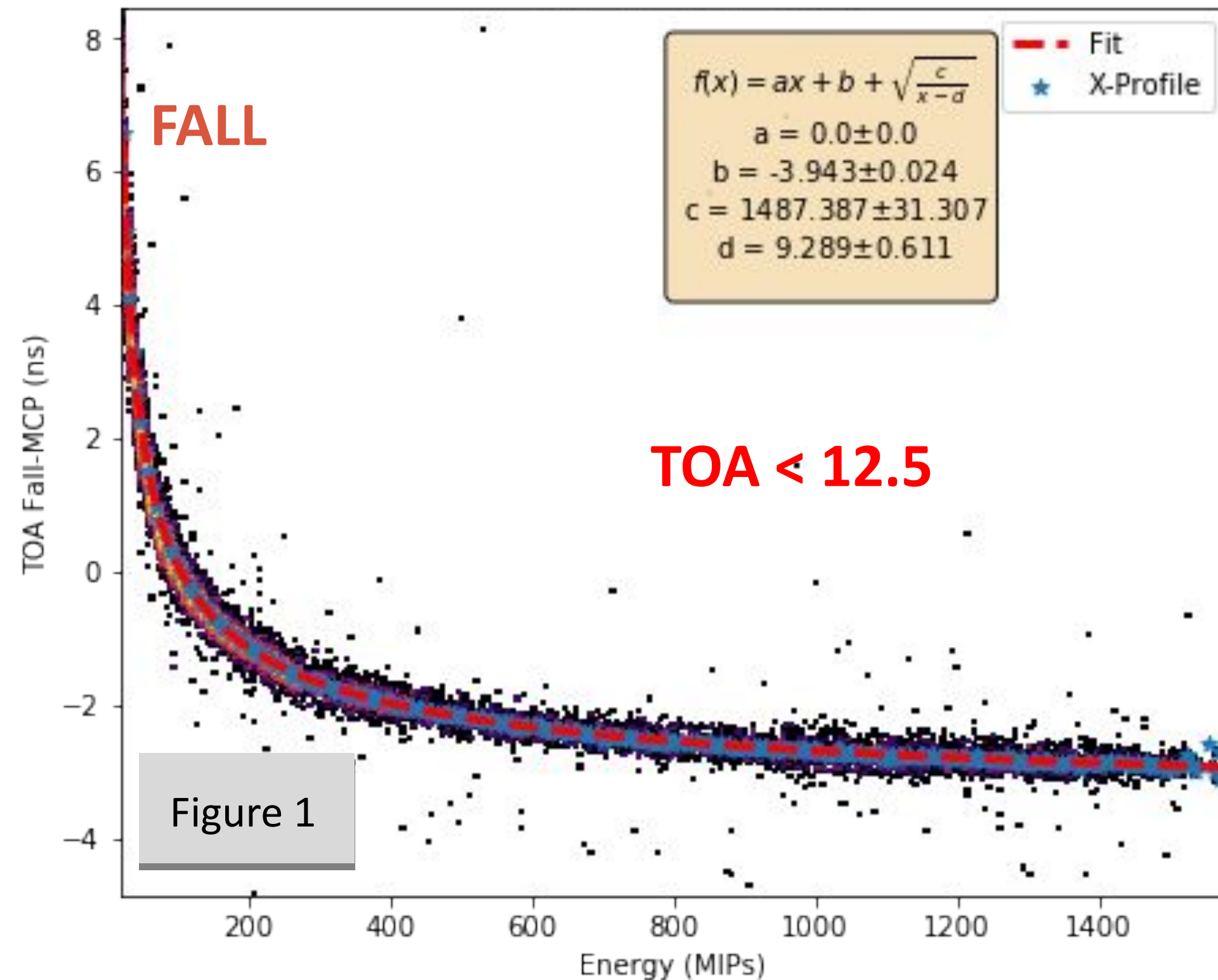
$$[0] * x + 25 + [1] * \left( \frac{1}{x - 1.25} + 0.8 \right)$$

Equation 1: Shows the fit curve for 300 GeV Electron



# Calibration -- Time Walk Correction

Layer 8 Single Cell, 300 GeV Electrons



We apply a phase selection cut, TOA < 12.5ns , to remove residual non-linearity.  
We fit the Time Walk Curve with  $f(x)$  (given in the figure), and correct for it by inverting the equation.

**Fit parameters are consistent between Fall and Rise**



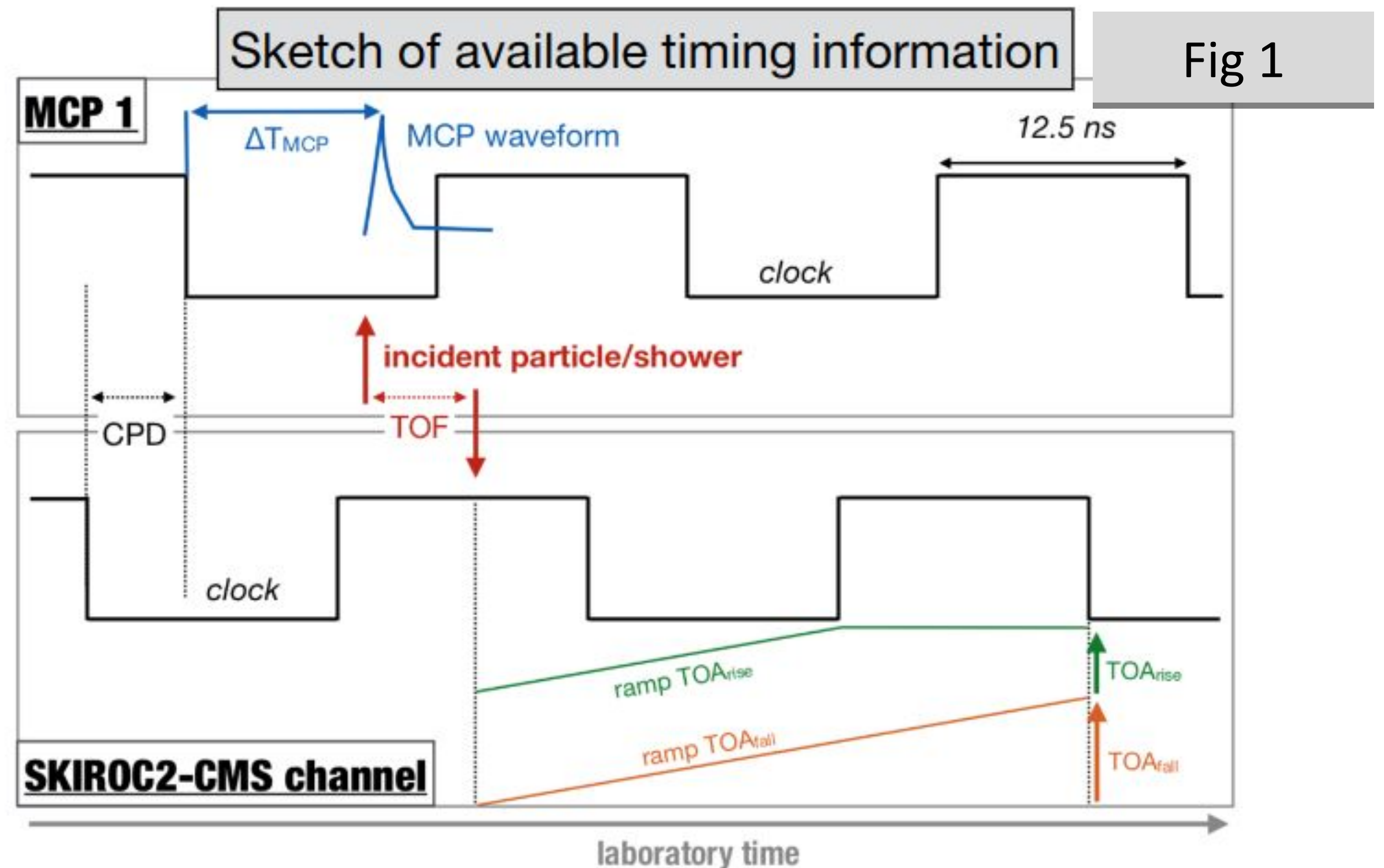
# Timing Characterization using full MCP time-stamp

## Goals:

- Reconstruction of MCP timestamp for calibration of the per-channel TOA-rise/fall
- Resolution + accuracy for single channels and channels combined

## Key differences to other studies:

- Full usage of MCP timestamp
- No strict dependence on random beam incidence
- Per-channel time offsets, due to path lengths or TOF are not considered here



Calibrated hit-timestamp

$$T = T(TOA, E, E_{\text{module}}) = f_{\text{TOA}} \left( \frac{TOA - TOA^{\text{min}}}{TOA^{\text{max}} - TOA^{\text{min}}} \right) + f_{\text{TW}}(E) + f_{\text{B}}(E_{\text{module}}) + \Delta l_0$$

TOA-non linearity
hit energy timewalk
Signal trace lengths,

per-event baseline shift



# Si-MCP: Single Channel Resolution

Layer 8 Single Cell, 300 GeV Electrons

## Calibration Steps:

- Linearisation:
  - ◆ Non-Linearity caused by ramp saturation
  - ◆ Calibrated using a data driven method which exploits the asynchronous nature of the internal clock and the beam.
- Time Walk Correction:
  - ◆ Phenomenon where the timing depends on the energy deposited in the detector
  - ◆ Corrected by inverting Time Walk parametric equation

## Single Channel Resolution:

- ◆ 300 GeV Electrons
- ◆ Binned in energy deposited in the channel fit against a gaussian distribution
- ◆ Consistent results between fall and rise TOA

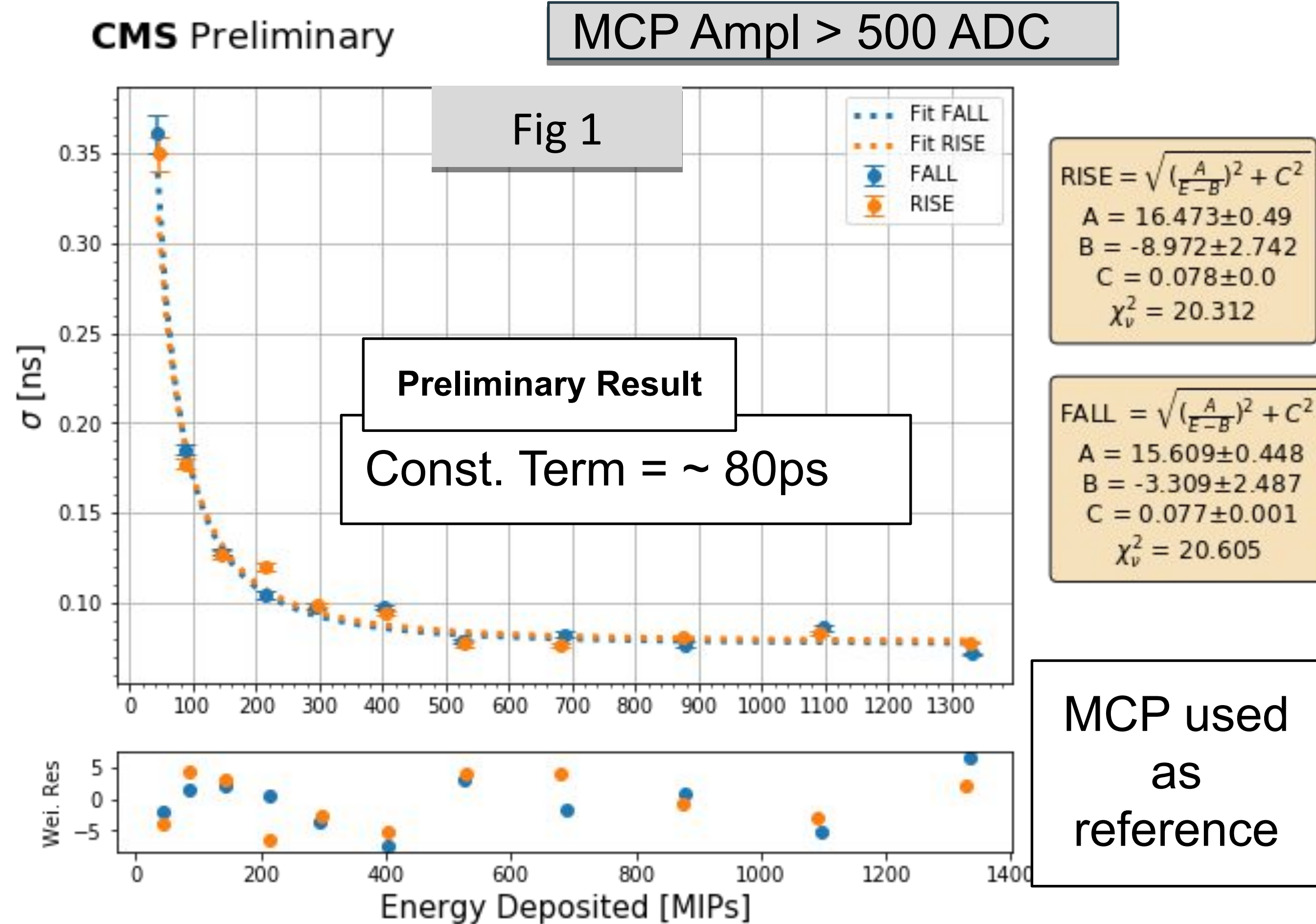
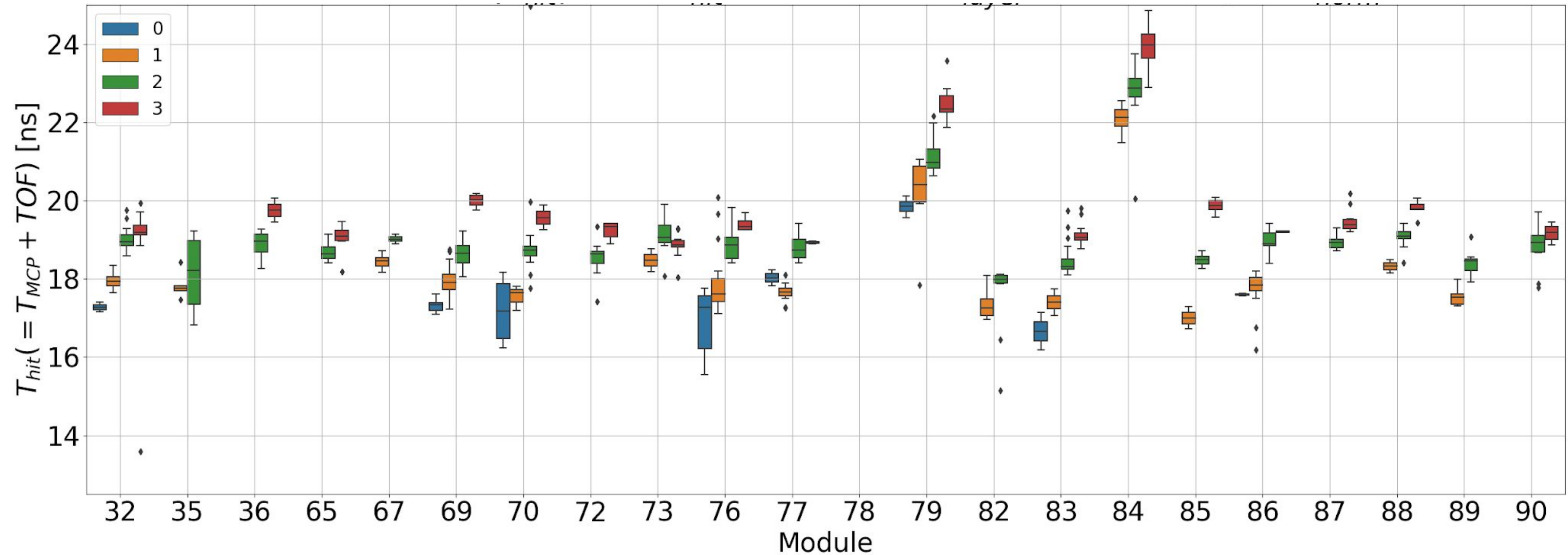


Figure 1: Time-Resolution as a function of Energy Deposited



# Mean, median, and spread of the calibrated hit time



Shows the box plot of

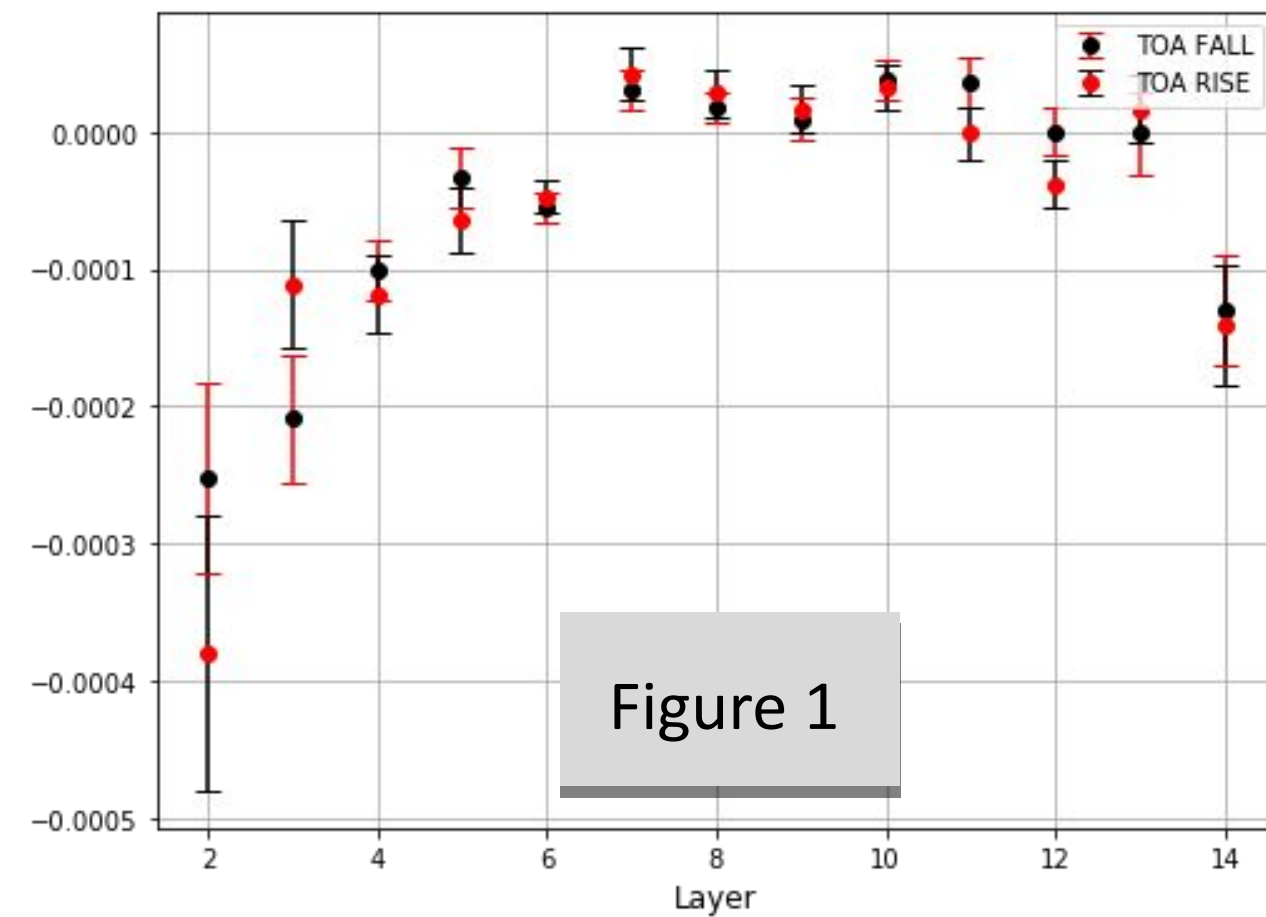
Calibrated Hit Time ( $T_{hit}$ ):

- $E_{hit} = 500$  MIPs
- $E_{layer} = 600$  MIPs

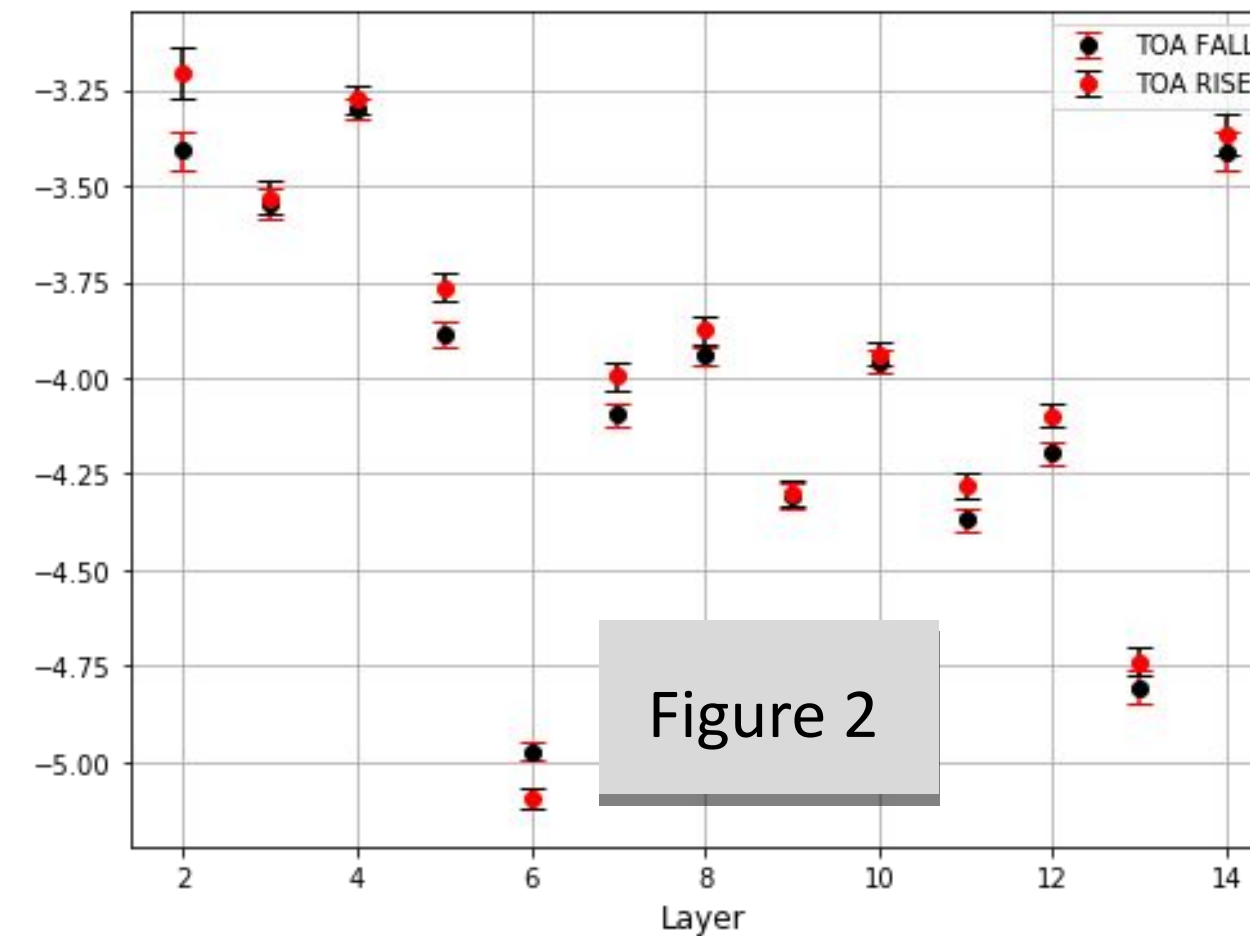


# Stability Across Layers

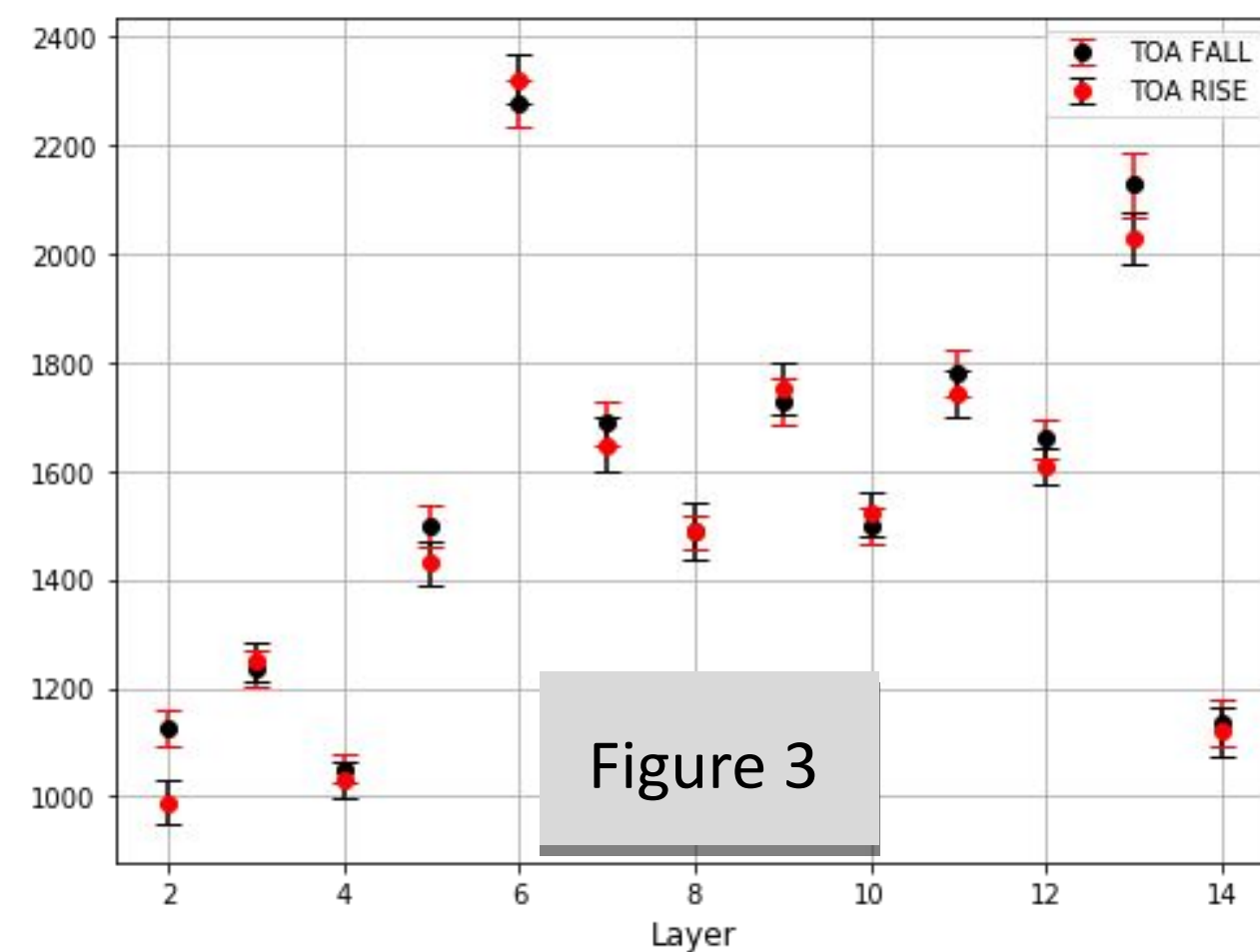
Fit Parameter A [ns/MIP]



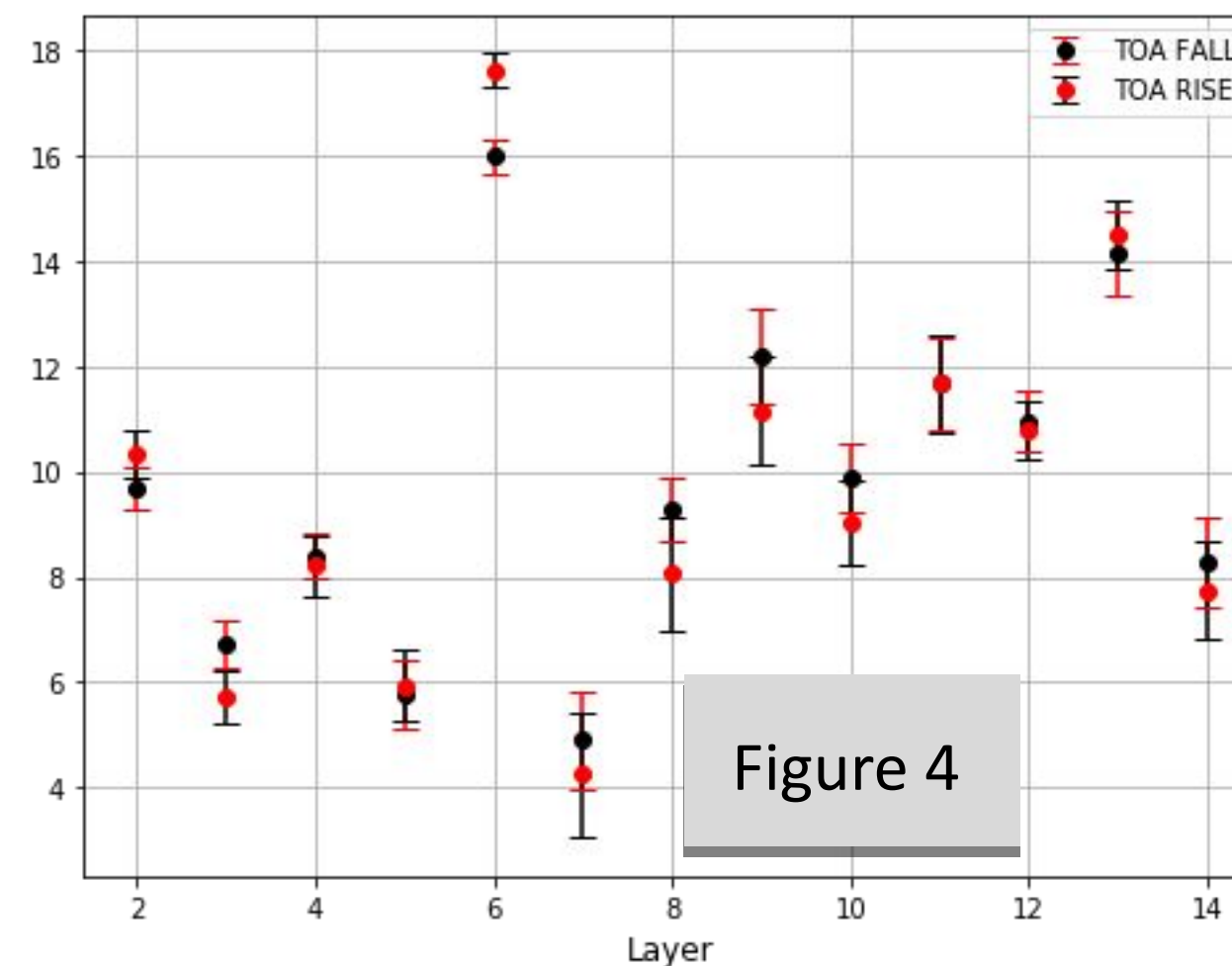
Fit Parameter B [ns]



Fit Parameter C [ns-MIP]



Fit Parameter D [MIPS]



$$y = A.x + B + \sqrt{\frac{C}{x - D}}$$

Consistent results  
between TOA Fall and  
TOA Rise



# Effects of Variation in Smearing

