
Early Electroweak Measurements at the LHC

1. Motivation
2. W/Z production: on and off the resonance
3. Di-boson production
4. Conclusions

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1 – Introduction

- I will concentrate on two topics:
 - ☞ W/Z production on and off the resonance
 - ☞ di-boson production: probing gauge boson self-couplings
- W/Z production:
 - ☞ Standard candles
 - ☞ W mass measurement (maybe not in the first year or so...)
 - ☞ constraining PDF's
 - ☞ search for W' and Z' resonances

- di-boson production:
 - ☞ probe WWV , $V = \gamma, Z$, vertex in $W\gamma$, WZ and WW production
 - ☞ probe $ZZ\gamma$ and $Z\gamma\gamma$ vertices in $Z\gamma$ production
 - ☞ probe $ZZ\gamma$ and ZZZ couplings in ZZ production
- I will concentrate on how higher order QCD and electroweak (EW) corrections affect measurements
- most numerical results are for $\sqrt{s} = 14$ TeV, but hold *mutatis mutandis* for $\sqrt{s} = 7$ TeV

2 – W/Z production: on- and off-shell

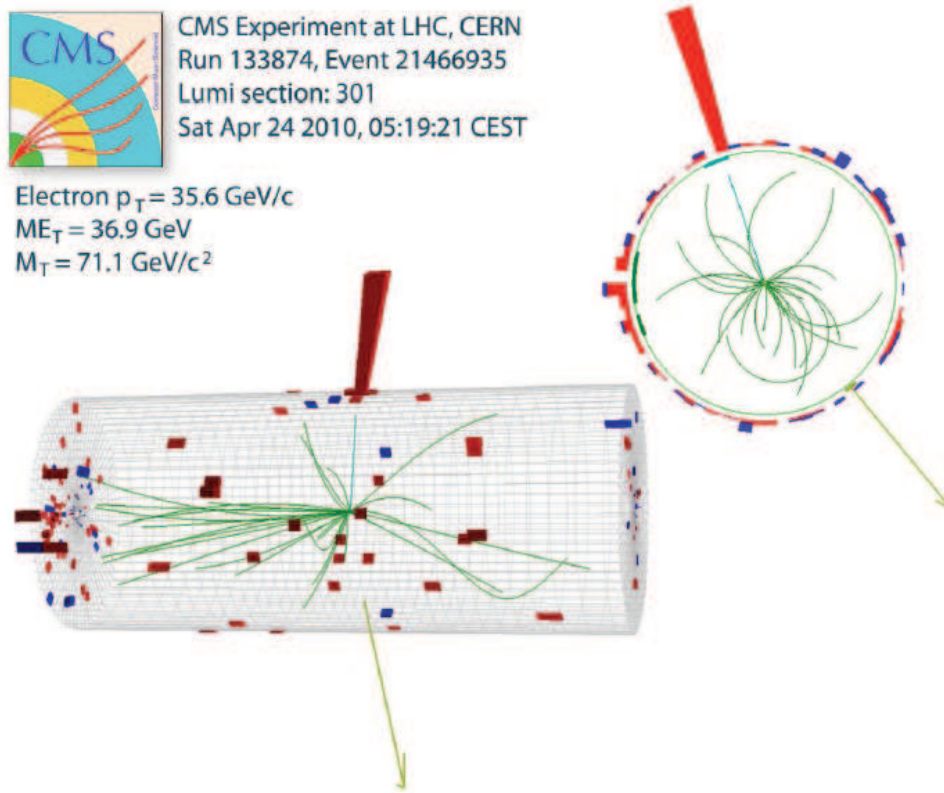
- W and Z Production has been observed at the LHC

$W \rightarrow e\nu$ candidate



CMS Experiment at LHC, CERN
Run 133874, Event 21466935
Lumi section: 301
Sat Apr 24 2010, 05:19:21 CEST

Electron $p_T = 35.6$ GeV/c
 $ME_T = 36.9$ GeV
 $M_T = 71.1$ GeV/c²



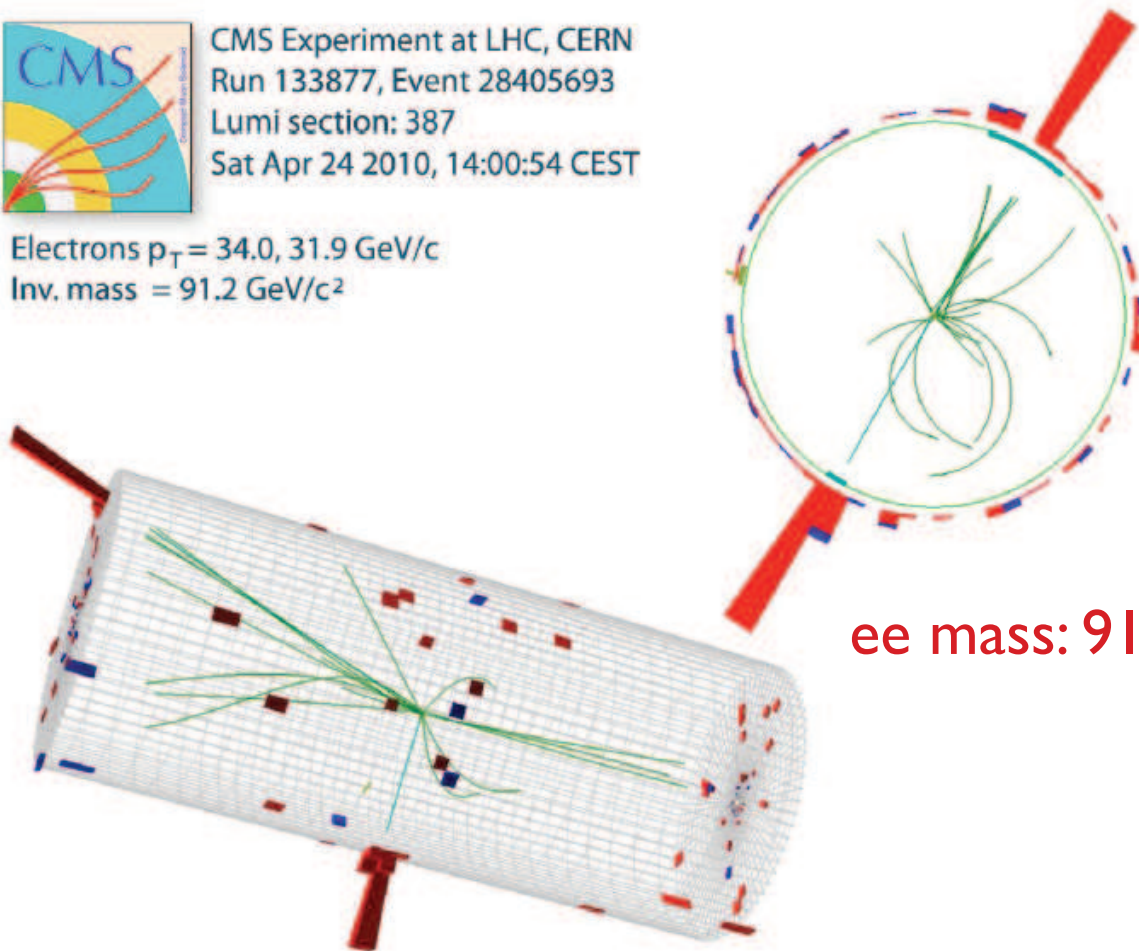
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Z → ee candidate



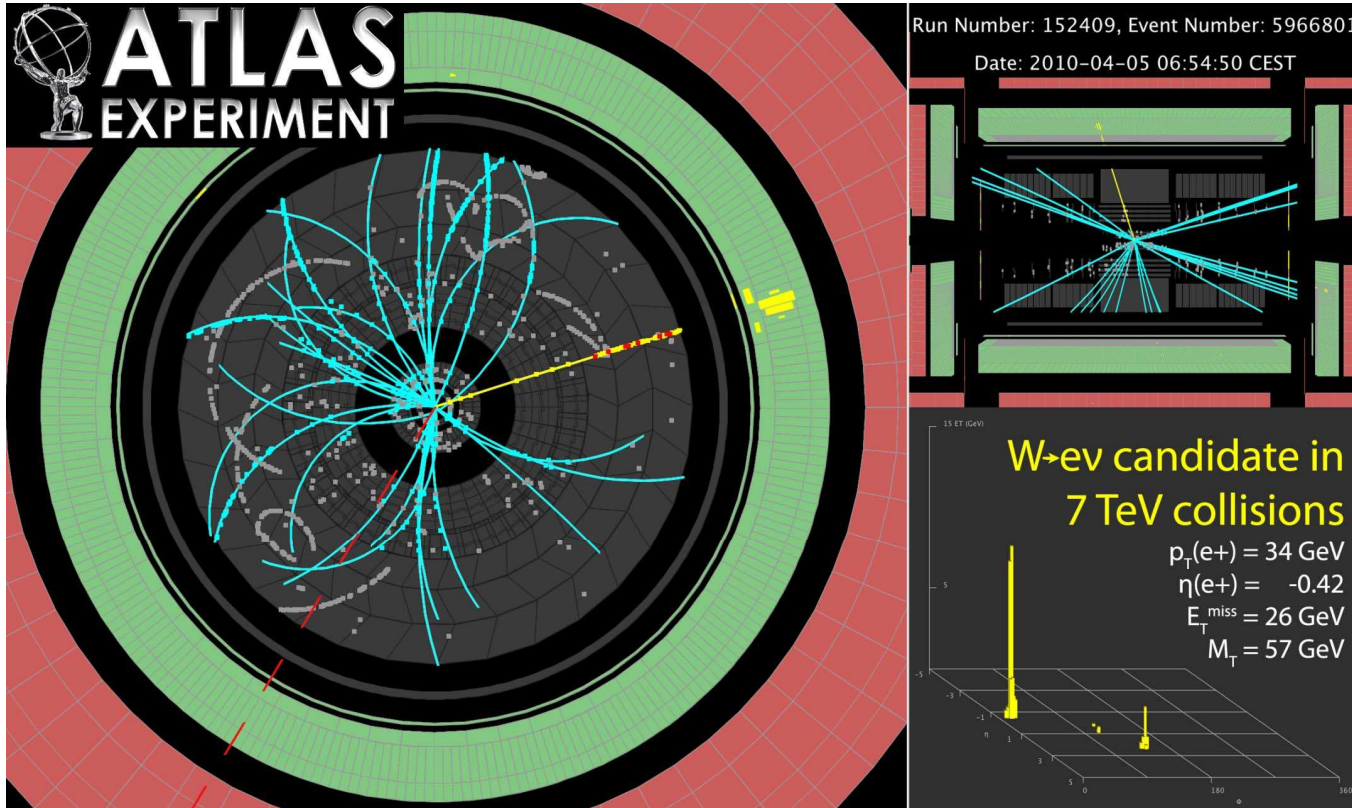
CMS Experiment at LHC, CERN
Run 133877, Event 28405693
Lumi section: 387
Sat Apr 24 2010, 14:00:54 CEST

Electrons $p_T = 34.0, 31.9$ GeV/c
Inv. mass = 91.2 GeV/c²



ee mass: 91.2 GeV

$W \rightarrow e\nu$ Candidate



Pheno 2010 Symposium, Madison, Wisconsin, May 10-12, 2010

Jianming Qian (University of Michigan) 17

- expect a torrent of W 's and Z 's at the LHC in the near future
- for $\sqrt{s} = 7$ TeV:
 - $\sigma(W^\pm \rightarrow l\nu) \approx 10.5$ nb
 - $\sigma(Z \rightarrow l^+l^-) \approx 0.96$ nb
- cross section approximately doubles for $\sqrt{s} = 14$ TeV
- Status of theory calculations for W/Z production:
 - ➔ the NNLO QCD corrections to W/Z production are known in fully differential form (**Melnikov, Petriello**) and are available in form of a parton level MC program (**FEWZ**)
 - ➔ resummed NLL QCD corrections (soft gluon resummation) are known (**RESBOS**)
 - ➔ NLO QCD corrections have been merged with HERWIG in **MC@NLO** and **POWHEG**

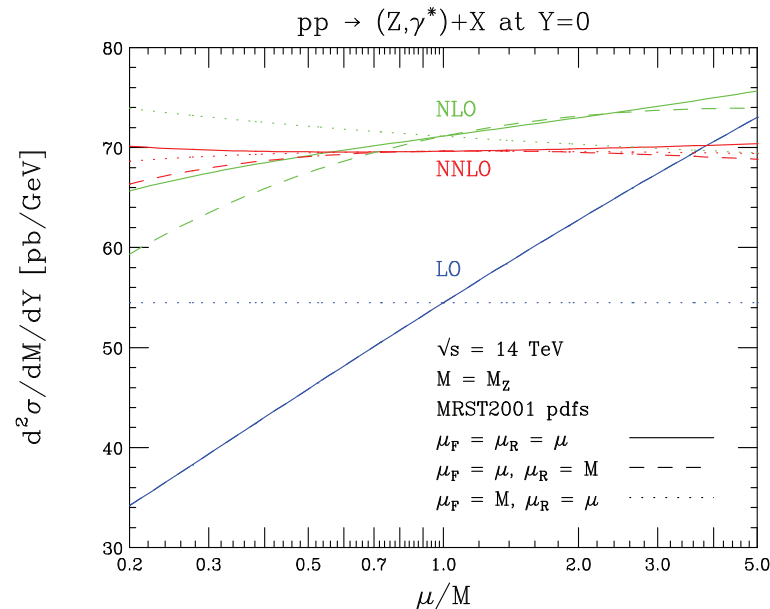
- Status of theory calculations for W/Z production (continued...)
 - ☞ several calculations of the full $\mathcal{O}(\alpha)$ EWK corrections to W/Z production exist (UB, Wackerath [WGRAD, ZGRAD]; Bardin *et al.* [SANC]; Carloni Calame *et al.* [HORACE]; Dittmaier, Denner; Jadach *et al.* [WINHAC])
- Why do we need higher order QCD corrections?
 - ☞ LO cross sections strongly depend on the renormalization and factorization scales, μ_R and μ_F , used
 - ☞ this dependence is an artificial byproduct of truncating the perturbation series
 - ☞ the scale dependence is (usually) reduced when higher order QCD corrections are included, and NLO theory predictions tend to agree much better with actual data

- **Example:** $W + n$ jet production at the Tevatron
(C. Berger et al., arXiv:0907.1984)

# of jets	CDF	LO	NLO
1	53.5 ± 5.6	$41.40(0.02)^{+7.59}_{-5.94}$	$57.83(0.12)^{+4.36}_{-4.00}$
2	6.8 ± 1.1	$6.159(0.004)^{+2.41}_{-1.58}$	$7.62(0.04)^{+0.62}_{-0.86}$
3	0.84 ± 0.24	$0.796(0.001)^{+0.488}_{-0.276}$	$0.882(0.005)^{+0.057}_{-0.138}$

- in some cases (eg. $W + 1$ jet production) NLO is not enough...

- when do we need NNLO corrections?
 - ☞ When NLO corrections are large and NNLO is needed to check expansion ($gg \rightarrow H$)
 - ☞ for benchmark processes where high precision is needed ($pp \rightarrow jj, W/Z$ production)
- Example: (Anastasiu et al.)



The NNLO residual scale uncertainty is $< 1\%$

- $\mathcal{O}(\alpha)$ electroweak (EWK) corrections to W/Z production

- ➡ 1-loop: naively of $\mathcal{O}(\alpha) \leq 1\%$

- ➡ why bother?

- ➡ EWK corrections may be enhanced by large

- ➔ collinear logs: $\log(\hat{s}/m_f^2)$, relevant near the W/Z peak

- ➔ Sudakov logs: $\log(\hat{s}/M_{W/Z}^2)$, relevant at large di-lepton masses

- ➡ QCD corrections may be small (example: QCD corrections largely cancel in W/Z cross section ratio)

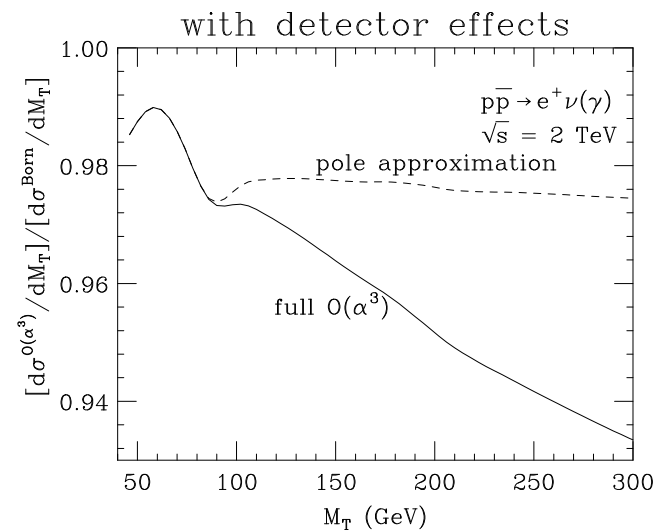
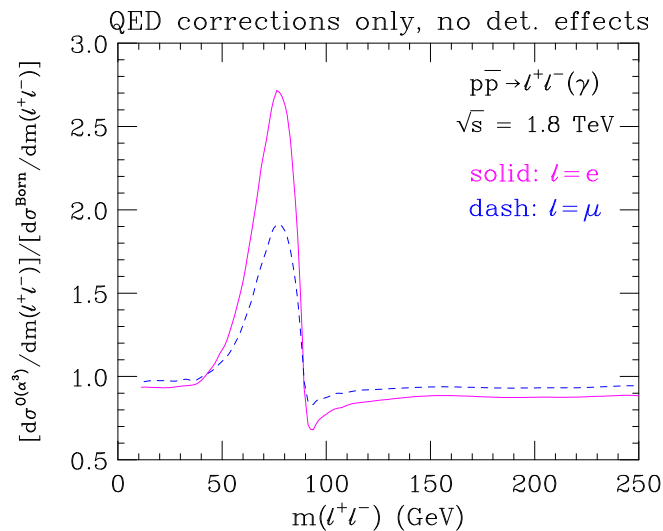
- ➡ for consistent treatment need PDF's which include QED corrections. These are available in **MRSTQED04** set (eventually will need an update to these ...)

Anatomy of the EWK $\mathcal{O}(\alpha)$ Corrections

- 1-loop EWK corrections shift W and Z masses by $\mathcal{O}(100 \text{ MeV})$
 - ☞ most of the effect comes from final state photon radiation
 - ☞ proportional to

$$\frac{\alpha}{\pi} \log \left(\frac{\hat{s}}{m_\ell^2} \right)$$

→ these terms together with the Sudakov logs significantly influence the $\ell^+\ell^-$ inv. mass distribution and $\ell\nu$ transverse mass distribution (pole approximation: no Sudakov logs are present)



Sidebar: W mass measurement at the LHC

- need

$$\delta M_W \approx 7 \times 10^{-3} \cdot \delta m_{top}$$

for equal contribution to M_H uncertainty from m_{top} and M_W

☞ Tevatron: $\delta m_t = 1.1 \text{ GeV}$ (NEW!!)

☞ expect $\delta m_t \approx 1 \text{ GeV}$ at LHC

☞ limited by non-perturbative QCD effects, which introduce theoretical uncertainty $\delta m_t = \mathcal{O}(\Lambda_{QCD})$ (renormalon uncertainty)

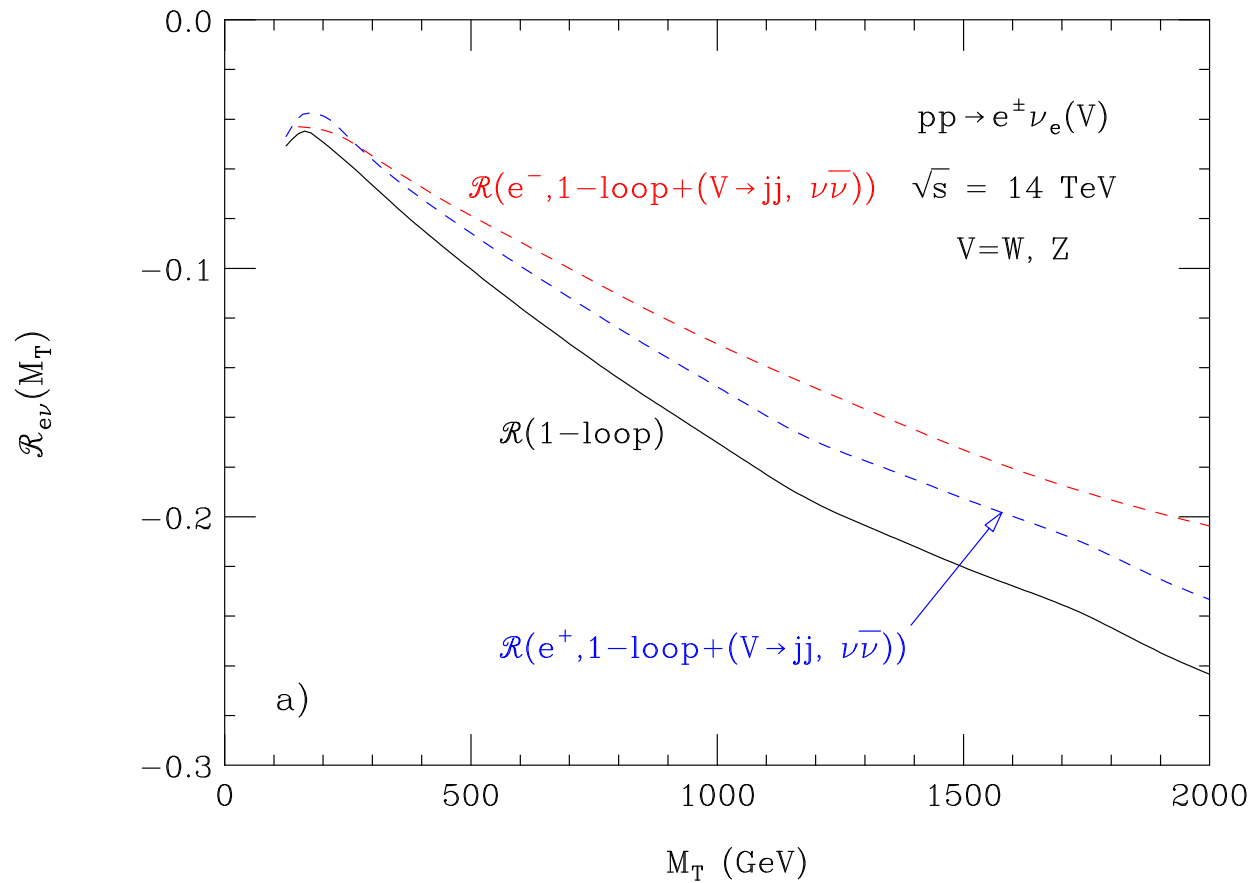
→ $\delta M_W < 10 \text{ MeV}$ should be goal for LHC

- LHC expectations (for $\sqrt{s} = 14$ TeV):
 - ☞ ATLAS: $\delta M_W = 7$ MeV for 10 fb^{-1} per lepton channel using the M_T and $p_T(\ell)$ distributions ([arXiv:0805.2093](#))
 - need excellent understanding of detector (lepton scale and resolution, p_T resolution) to achieve this
 - assumes that PDF uncertainties can be controlled such that they contribute only 1 MeV to δM_W
 - assumes that needed theoretical tools will be available to achieve a 1 MeV uncertainty from unknown higher order corrections
 - ☞ CMS: $\delta M_W = 40$ MeV (20 MeV) for 1 fb^{-1} (10 fb^{-1}) using the scaled observable method and the so-called morphing method ([J. Phys. G 34 \(2007\), N193](#))
 - CMS makes less aggressive assumptions on PDF and theoretical uncertainties

Electroweak Sudakov Logs

- for $\hat{s} \gg M_{W/Z}^2$, the weak corrections become **large and negative**
- relevant for new physics searches in $\ell\nu$ and $\ell^+\ell^-$ production (eg. W' , Z' searches)
- **However**, EW corrections do **not** include real EW corrections, eg. $WW \rightarrow \ell\nu jj$ which may partially cancel the large, negative EW one-loop corrections (**UB**)
- answer depends on whether one looks at **exclusive** or **inclusive** Drell-Yan production

$\mathcal{R}_{e\nu}$: relative correction to LO cross section



Combining QCD and EW corrections

- QCD and EW corrections tend to cancel in the high mass region
- for accurate predictions need a calculation which combines QCD and EW corrections, preferably interfaced with PYTHIA or HERWIG
- such a calculation is also needed to achieve $\delta M_W \approx 10$ MeV or better
- The **HORACE** team has interfaced HORACE (EW corrections) with MC@NLO (NLO QCD corrections consistently interfaced with HERWIG)
([arXiv:0907.0276](https://arxiv.org/abs/0907.0276))

☞ the procedure for doing this is **not unique**

☞ additive approach:

$$\left[\frac{d\sigma}{d\mathcal{O}} \right]_{QCD\&EW} = \left\{ \frac{d\sigma}{d\mathcal{O}} \right\}_{MC@NLO} + \left\{ \left[\frac{d\sigma}{d\mathcal{O}} \right]_{EW} - \left[\frac{d\sigma}{d\mathcal{O}} \right]_{LO} \right\}_{HERWIG\ PS}$$

☞ factorized approach:

$$\left[\frac{d\sigma}{d\mathcal{O}} \right]_{QCD\&EW} = \left(1 + \frac{[d\sigma/d\mathcal{O}]_{MC@NLO} - [d\sigma/d\mathcal{O}]_{HERWIG\ PS}}{[d\sigma/d\mathcal{O}]_{LO/NLO}} \right) \times \left\{ \frac{d\sigma}{d\mathcal{O}_{EW}} \right\}_{HERWIG\ PS}$$

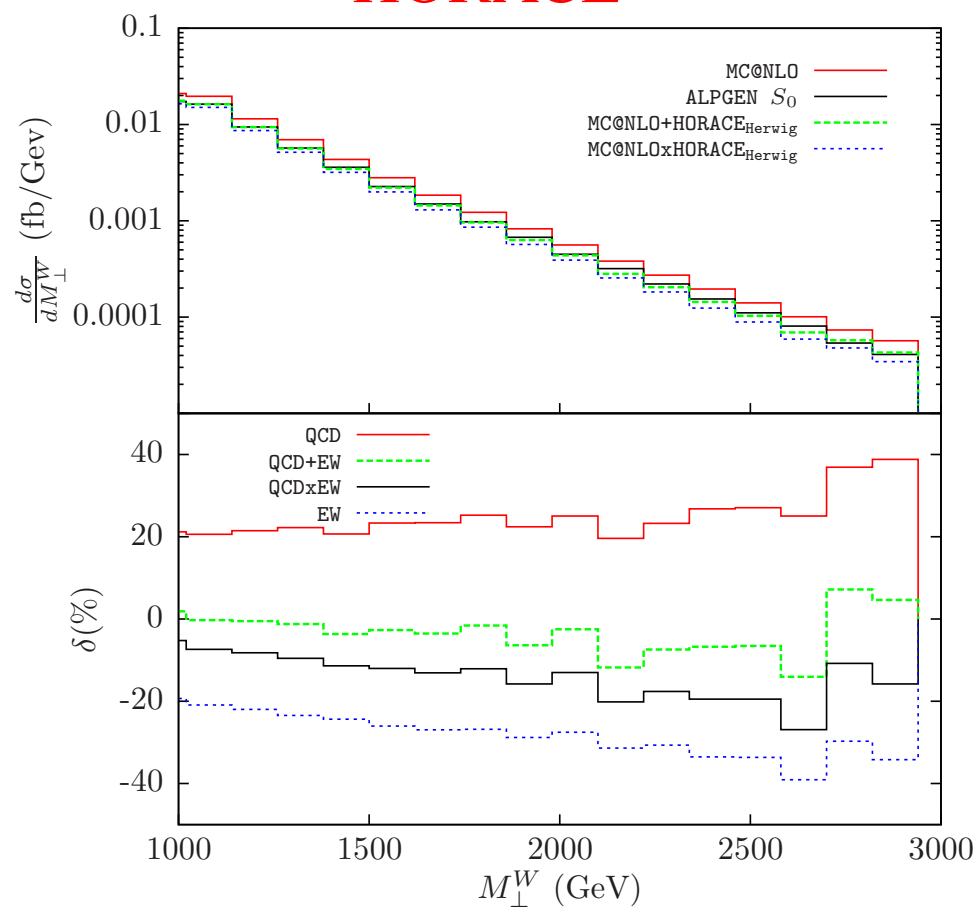
⇒ defined either in terms of LO or NLO cross section

⇒ differ at $\mathcal{O}(\alpha_s^2)$ by non-leading contributions

☞ the residual uncertainties resulting from the ambiguity between the additive and factorized approach are of $\mathcal{O}(\alpha\alpha_s)$

👉 they are numerically significant

HORACE



→ need full $\mathcal{O}(\alpha\alpha_s)$ corrections to quantify

3 – Di-boson production

- Physics interest:
 - ☞ background to new physics searches (WW and ZZ production background to SM Higgs search)
 - ☞ probing weak boson self-interactions
- concentrate on the latter
- qualitative overview of three gauge boson couplings in the Standard Model:
 - ☞ $WW\gamma$ and WWZ couplings are non-zero
 - ☞ there are no tree level couplings with neutral gauge bosons, ie. $Z\gamma\gamma$, $ZZ\gamma$ and ZZZ couplings all vanish

General $WW\gamma$ and WWZ Couplings

- If we want to test the $SU(2)\times U(1)$ gauge theory, we have to go beyond and generalize the WWV ($V = \gamma, Z$) couplings
- The most general effective Lagrangian consistent with **electromagnetic** gauge invariance and Lorentz invariance is

$$\begin{aligned}
 i\mathcal{L}_{eff}^{WWWV} = & g_{WWV} \left[g_1^V \left(W_{\mu\nu}^\dagger W^\mu - W^{\dagger\mu} W_{\mu\nu} \right) V^\nu + \kappa_V W_\mu^\dagger W_\nu V^{\mu\nu} \right. \\
 & + \frac{\lambda_V}{m_W^2} W_{\rho\mu}^\dagger W^\mu{}_\nu V^{\nu\rho} - g_4^V W_\mu^\dagger W_\nu (\partial^\mu V^\nu + \partial^\nu V^\mu) \\
 & + i g_5^V \varepsilon_{\mu\nu\rho\sigma} \left((\partial^\rho W^{\dagger\mu}) W^\nu - W^{\dagger\mu} (\partial^\rho W^\nu) \right) V^\sigma \\
 & \left. + i\tilde{\kappa}_V W_\mu^\dagger W_\nu \tilde{V}^{\mu\nu} + i \frac{\tilde{\lambda}_V}{m_W^2} W_{\rho\mu}^\dagger W^\mu{}_\nu \tilde{V}^{\nu\rho} \right].
 \end{aligned}$$

$$\begin{aligned}
 W_{\mu\nu} &= \partial_\mu W_\nu - \partial_\nu W_\mu; \text{ same for } V_{\mu\nu}; \tilde{V}_{\mu\nu} = (1/2)\varepsilon_{\mu\nu\rho\sigma} V^{\rho\sigma} \\
 g_{WW\gamma} &= e; g_{WWZ} = e \cot \theta_W
 \end{aligned}$$

- In the SM:

$$g_1^Z = g_1^\gamma = \kappa_Z = \kappa_\gamma = 1,$$

$$\lambda_Z = \lambda_\gamma = g_4^V = g_5^Z = g_5^\gamma = \tilde{\kappa}_V = \tilde{\lambda}_V = 0$$

- g_1^V , κ_V and λ_V respect charge conjugation (C) and parity (P)
- g_4^V and g_5^V violate C invariance
- g_4^V , $\tilde{\kappa}_V$ and $\tilde{\lambda}_V$ violate CP invariance
- for on-shell photons: $g_1^\gamma = 1$ (electric charge of W), $g_4^\gamma = g_5^\gamma = 0$ (em gauge invariance)
- higher dimensional operators do not lead to a new Lorentz structure
- they can be taken into account by allowing the couplings g_1^V , κ_V etc. to be energy dependent so-called **form factors**

- the $WW\gamma$ couplings are related to the **static moments** of the W (μ_W (d_W): (magnetic (electric) dipole moment; q_W (\tilde{q}_W) electric (magnetic) quadrupole moment)

$$\begin{aligned}\mu_W &= \frac{e}{2m_W} (g_1^\gamma + \kappa_\gamma + \lambda_\gamma) , & d_W &= \frac{e}{2m_W} (\tilde{\kappa}_\gamma + \tilde{\lambda}_\gamma) , \\ q_W &= -\frac{e}{m_W^2} (\kappa_\gamma - \lambda_\gamma) & \tilde{q}_W &= -\frac{e}{m_W^2} (\tilde{\kappa}_\gamma - \tilde{\lambda}_\gamma) .\end{aligned}$$

- S -matrix unitarity requires weak boson self-couplings to be of SM form at high energies
- anomalous weak boson couplings need to have a form factor behaviour such as

$$\frac{1}{\left(1 + \frac{\hat{s}}{\Lambda^2}\right)^n}$$

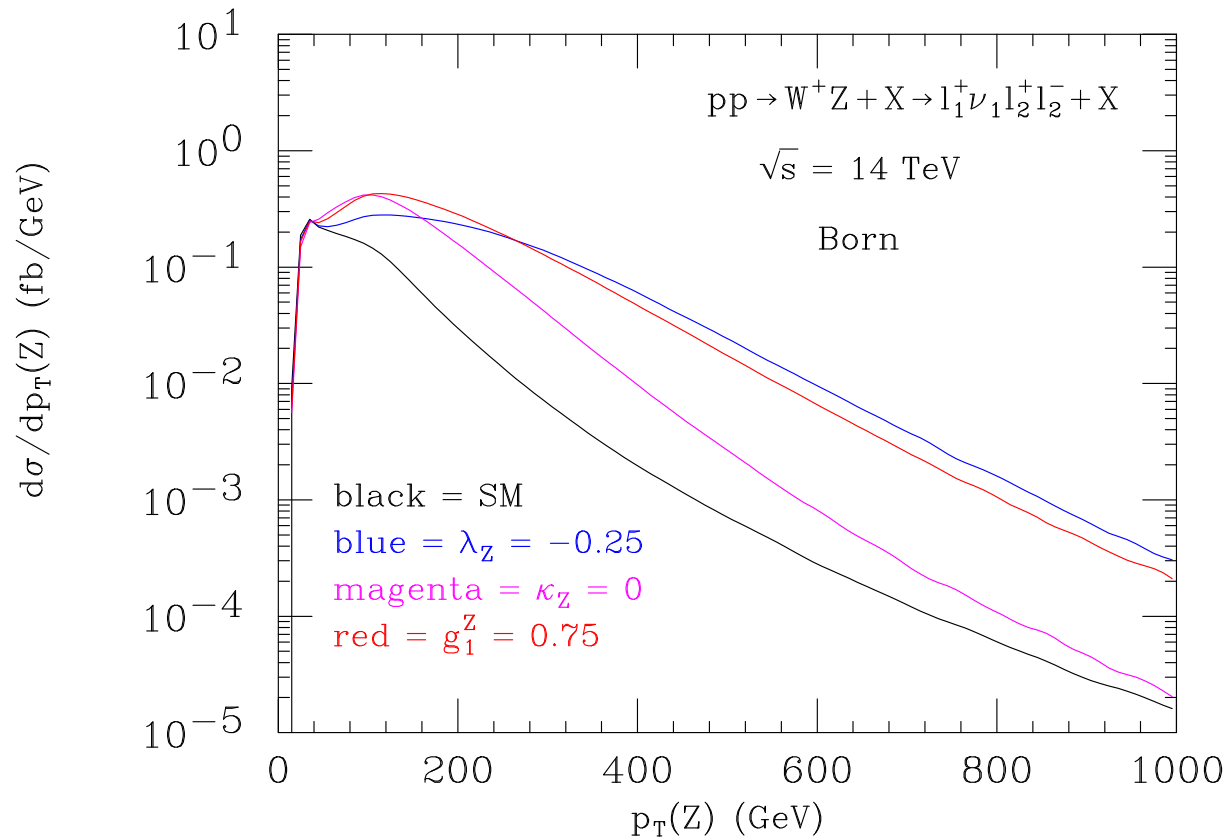
where Λ is the scale of new physics responsible for the non-standard couplings ($n = 2$ is often used)

Neutral Weak Boson Couplings

- appear in $Z\gamma$ and ZZ production
- there are 4 $ZZ\gamma$, h_i^Z ($i = 1, \dots, 4$), and 4 $Z\gamma\gamma$ couplings, h_i^γ , which contribute to $q\bar{q} \rightarrow Z\gamma$
- $h_{1,3}$ ($h_{2,4}$) correspond to dimension 6 (8) terms in the Lagrangian
- $h_{1,2}$ ($h_{3,4}$) violate (conserve) CP
- the $Z\gamma\gamma$ vertex function vanishes if **both** photons are on-shell (**Yang's theorem**)
- there are also 2 ZZZ ($f_{4,5}^Z$) and 2 $ZZ\gamma$ couplings ($f_{4,5}^\gamma$) contributing to $q\bar{q} \rightarrow ZZ$
- all these couplings have to be form factors which $\rightarrow 0$ for $\hat{s} \rightarrow \infty$ to avoid violation of unitarity

- thus, non-standard gauge boson self-couplings lead to an enhanced cross section at large gauge boson transverse momenta

example (form factor scale $\Lambda = 1$ TeV):



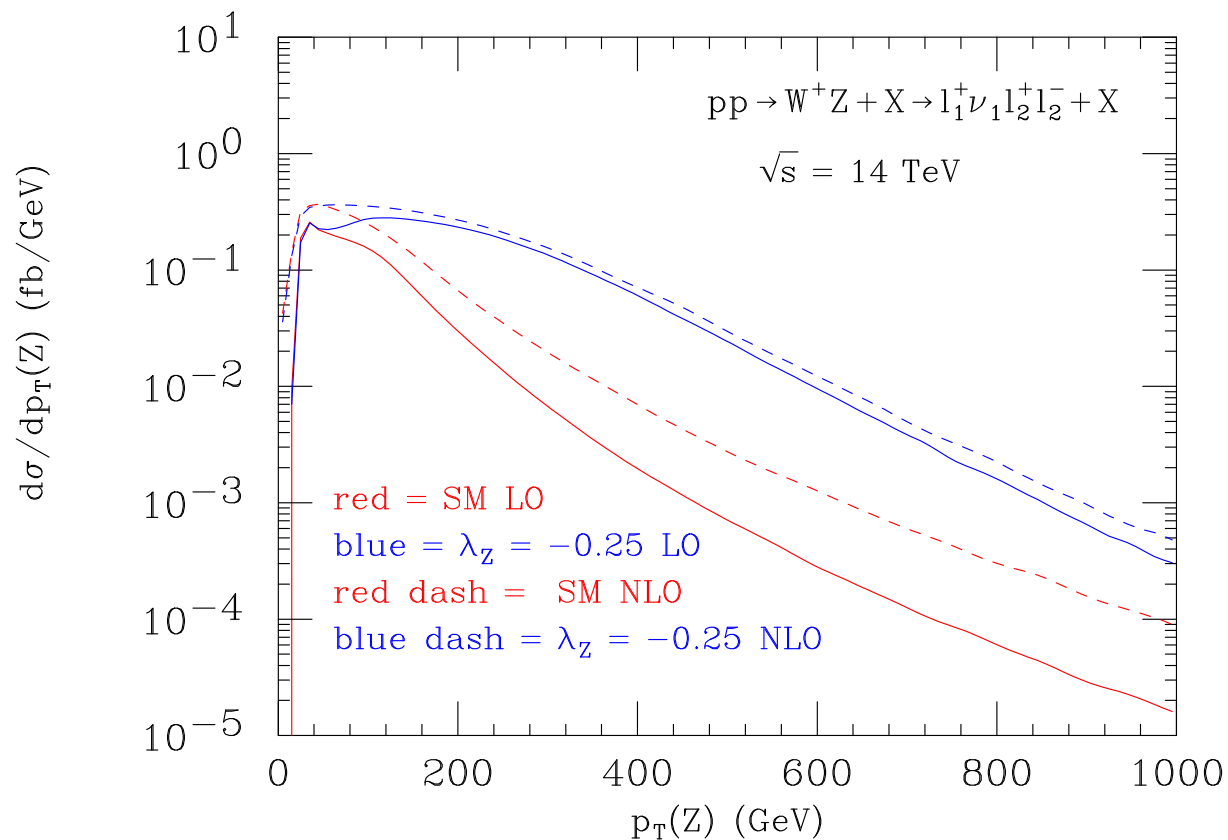
QCD corrections to Di-boson Production

- QCD corrections to di-boson production become very large at high energies
- Reason: there is a logarithmic enhancement factor, eg, for $W\gamma$ production, the $qg \rightarrow W\gamma q'$ cross section can be written at high photon transverse momenta $p_T(\gamma)$:

$$d\hat{\sigma}(q_1 g \rightarrow W\gamma q_{1,2}) = d\hat{\sigma}(q_1 g \rightarrow \gamma q_1) \frac{\alpha}{4\pi \sin^2 \theta_W} \log^2 \left(\frac{p_T^2(\gamma)}{M_W^2} \right)$$

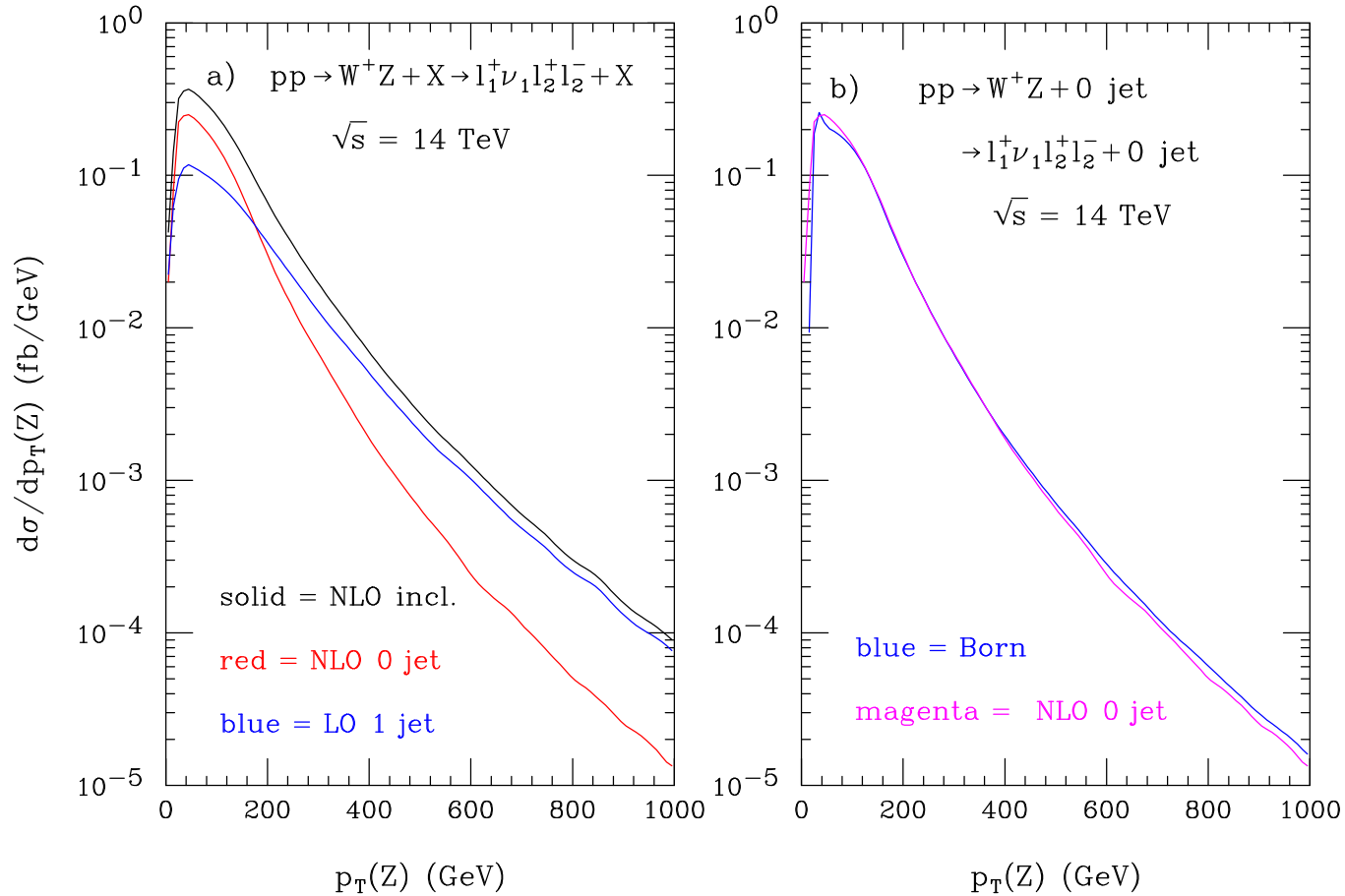
- similar expressions hold in WZ production and other processes

- the log enhancement is not present in diagrams with the $WW\gamma/WWZ$ vertex
- QCD corrections substantially reduce sensitivity to anomalous couplings (UB, J. Ohnemus, T. Han)



- **however:** at high p_T , most events have a hard jet
 → a jet veto helps to get the QCD under control and restore sensitivity to anomalous couplings

example: no jets with $p_T(j) > 50$ GeV



- Scale dependence:

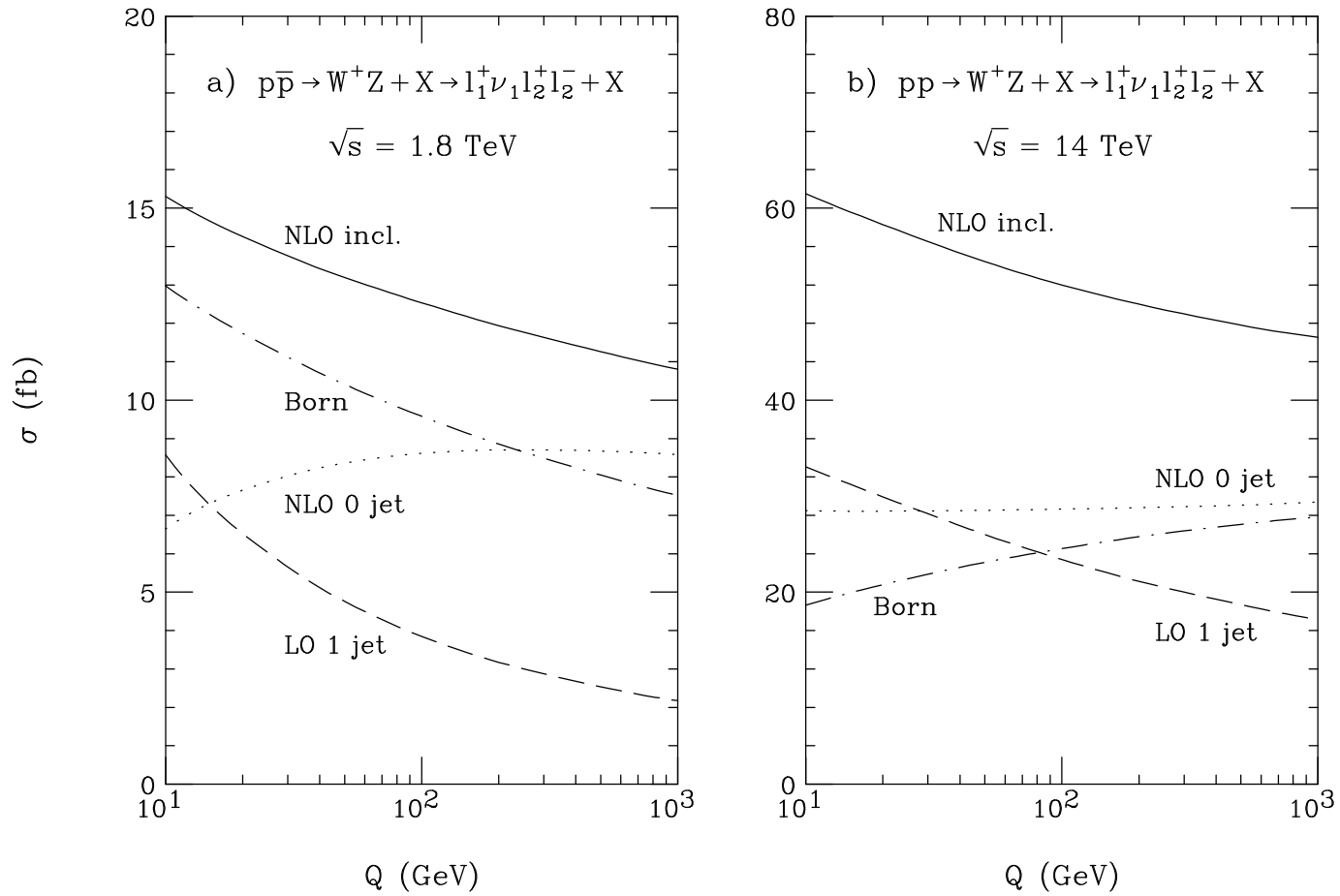
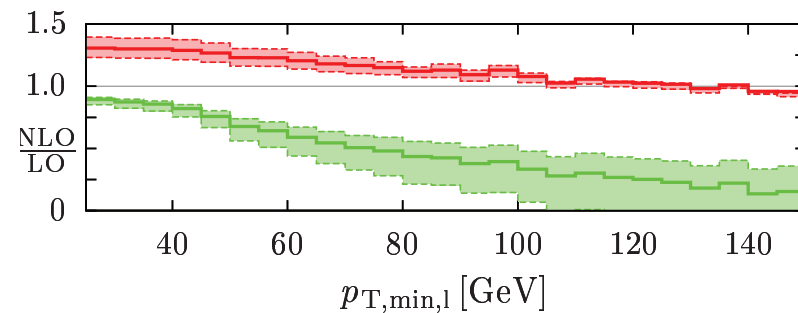


Figure 13

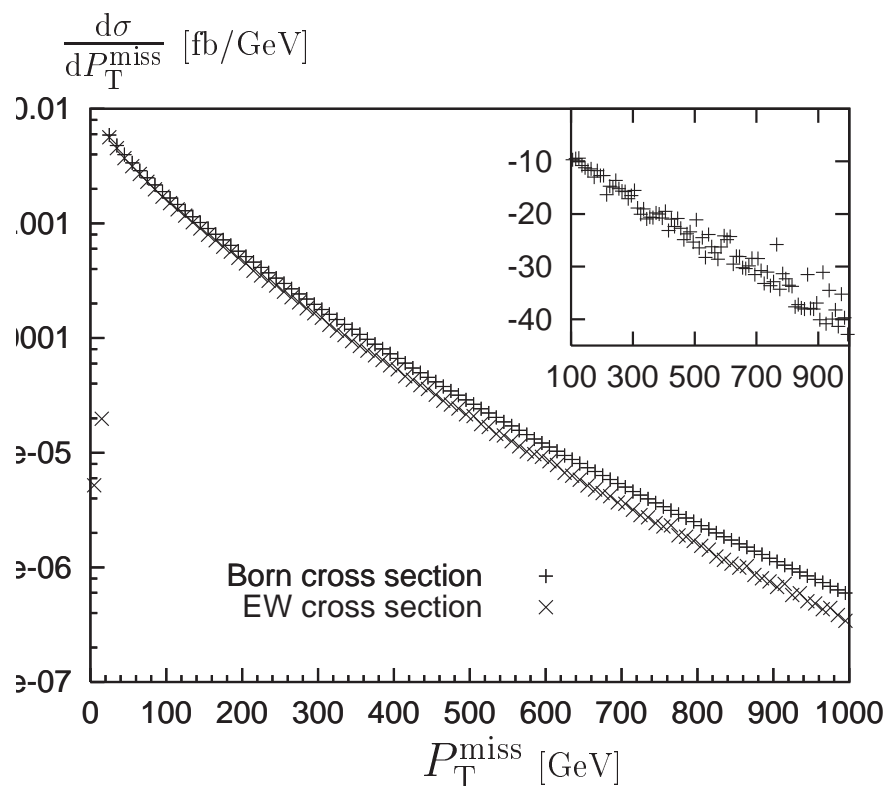
- ☞ Since the (LO) $WZ + 1$ jet cross section dominates, the scale dependence is not reduced in the **inclusive** NLO cross section
- ☞ Need $WZ + 1$ jet production at NLO QCD for that
- ☞ However, once a jet veto is imposed, the scale dependence in $WZ + 0$ jet production appears to be very small
- ☞ **This could be very misleading!**
- ☞ NLO QCD corrections to $WZ + 1$ jet production (**Campanario et al.**, arXiv:1006.0390) (**red**: inclusive NLO; **green**: exclusive NLO [no 2nd hard jet])



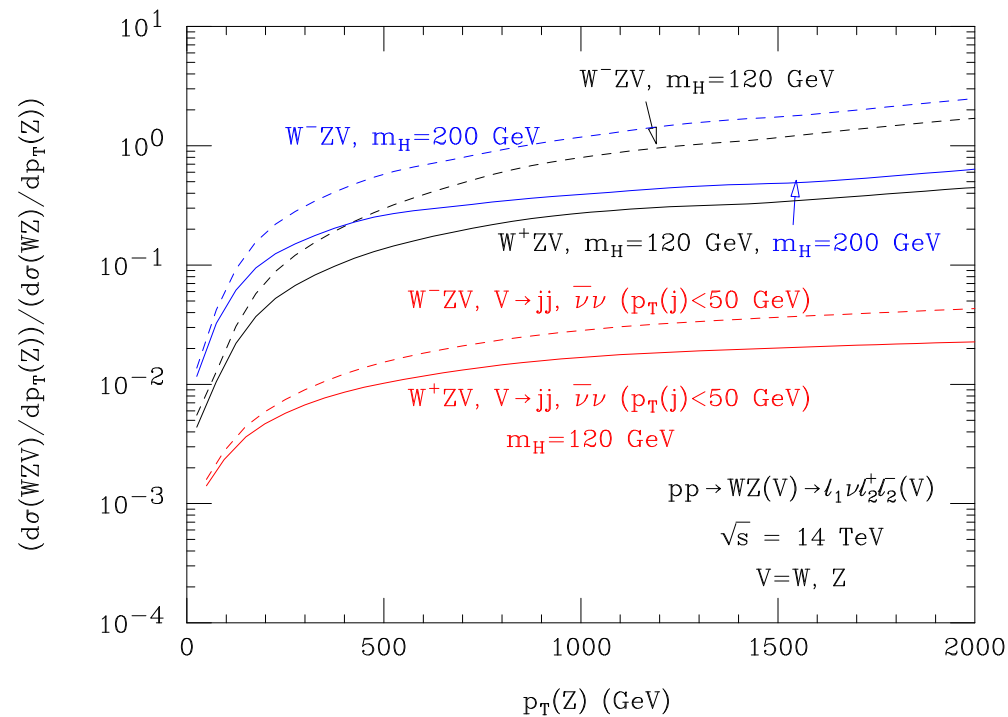
- 👉 scale dependence (μ is varied by a factor 2 up or down) is small at low minimum $p_T(l)$, and thus in the total cross section, it is **large** at higher p_T
- 👉 need to check for WZ and other diboson production processes

EWK Corrections to WZ Production

- As in single W/Z production, large Sudakov logs appear in EWK radiative corrections to di-boson production at large p_T
- Example: WZ production ([Accomando, Denner, Kaiser](#))



- EWK corrections to WZ production are substantial (but smaller than the inclusive NLO QCD corrections) and **negative**
- **but**, for inclusive $WZ + X$ production, weak boson emission processes (WZV , $V = W, Z$ production) may largely compensate the 1-loop corrections (**UB**)



Scrutinizing the WWZ vertex at 7 TeV

- recent study by **Eboli et al.**, arXiv:1006.3562
- consider WW and WZ production
- current bounds (from $e^+e^- \rightarrow WW$ and WZ production at the Tevatron) and expected bounds from the LHC @ 7 TeV with 1 fb^{-1}

☞ C and P conserving couplings

coupling	PDG bounds	WZ 2σ limits	WW 2σ limits
Δg_1^Z	$-0.016^{+0.022}_{-0.019}$	$[-0.055, 0.094]$	$[-0.33, 0.56]$
$\Delta \kappa_Z$	$-0.076^{+0.059}_{-0.056}$	$[-0.27, 0.55]$	$[-0.088, 0.11]$
λ_Z	$-0.088^{+0.060}_{-0.057}$	$[-0.051, 0.054]$	$[-0.055, 0.056]$

👉 C and/or P violating couplings

coupling	PDG bounds	WZ 2σ limits	WW 2σ limits
g_5^Z	-0.07 ± 0.09	$[-0.18, 0.19]$	$[-0.53, 0.51]$
g_4^Z	-0.30 ± 0.17	$[-0.08, 0.08]$	$[-0.48, 0.48]$
$\tilde{\kappa}_Z$	$-0.12^{+0.06}_{-0.04}$	$[-0.40, 0.40]$	$[-0.38, 0.38]$
$\tilde{\lambda}_Z$	-0.09 ± 0.07	$[-0.053, 0.053]$	$[-0.055, 0.055]$

- form factor effects are still quite small at 7 TeV, but **not** at 14 TeV
- can improve current bounds on λ_Z , g_4^Z and $\tilde{\lambda}_Z$ (λ_Z and $\tilde{\lambda}_Z$) in WZ (WW) production with early LHC data
- further significant improvements (factor of 4 or more) at 14 TeV with 100 fb^{-1}

4 – Conclusions

- Early LHC data provide an opportunity to calibrate detectors with well understood processes such as W and Z production
- These are theoretically fairly well understood, although there are open questions on how to combine QCD and EWK corrections
- EWK radiative corrections may become large at high p_T
- Early LHC data offer an opportunity to improve bounds on weak boson couplings in di-boson production
- NLO QCD and EWK corrections in di-boson processes may be large, but this depends on whether one does an exclusive or inclusive analysis (ie. jet veto yes, or no)

This talk was prepared in a 100% Microsoft free environment