

# Quantum Circuit Optimization for Scientific Applications

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# HEP and Quantum Computing

- Particle Physics directly probing quantum properties of fundamental building blocks in nature
- Needs of large computing resources in HEP experiments

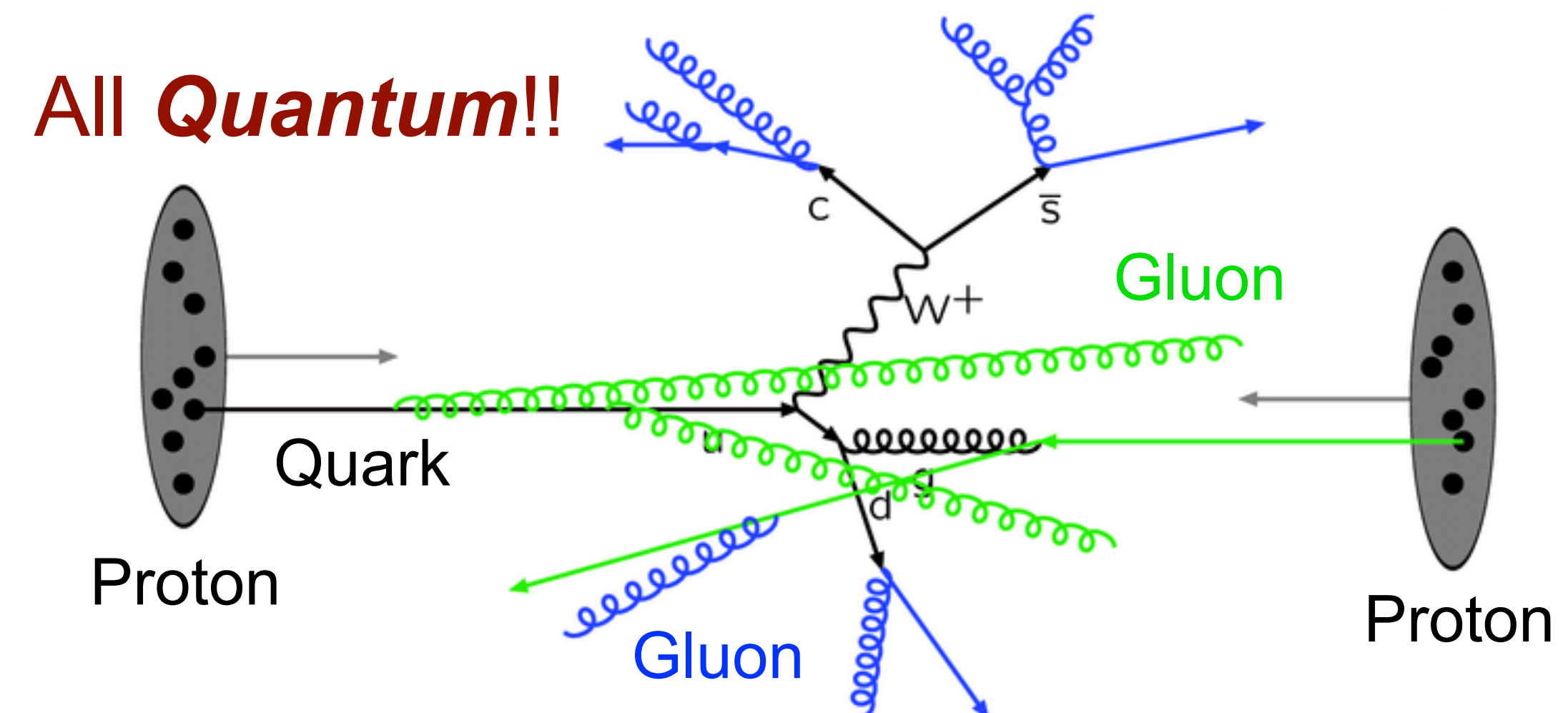
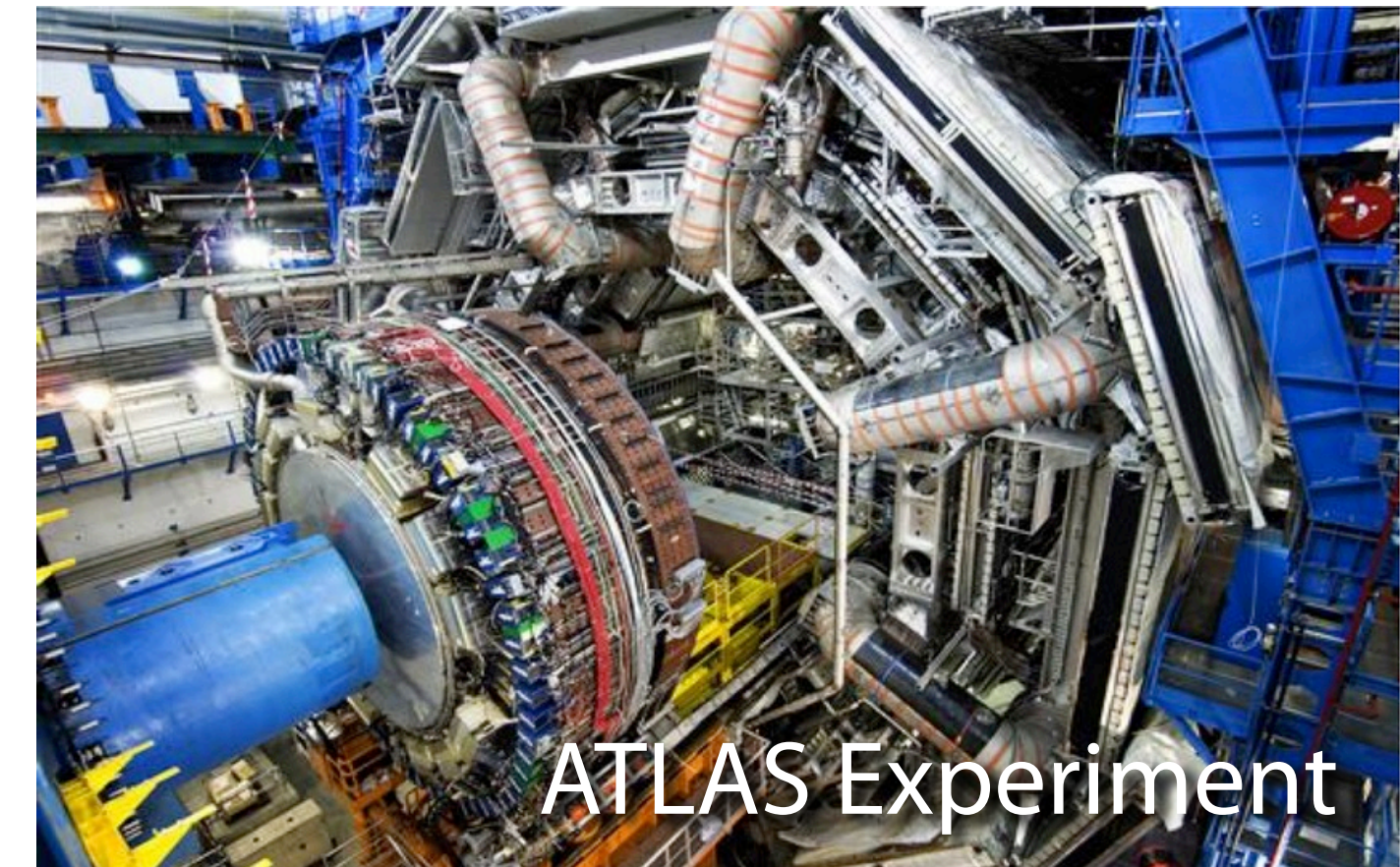
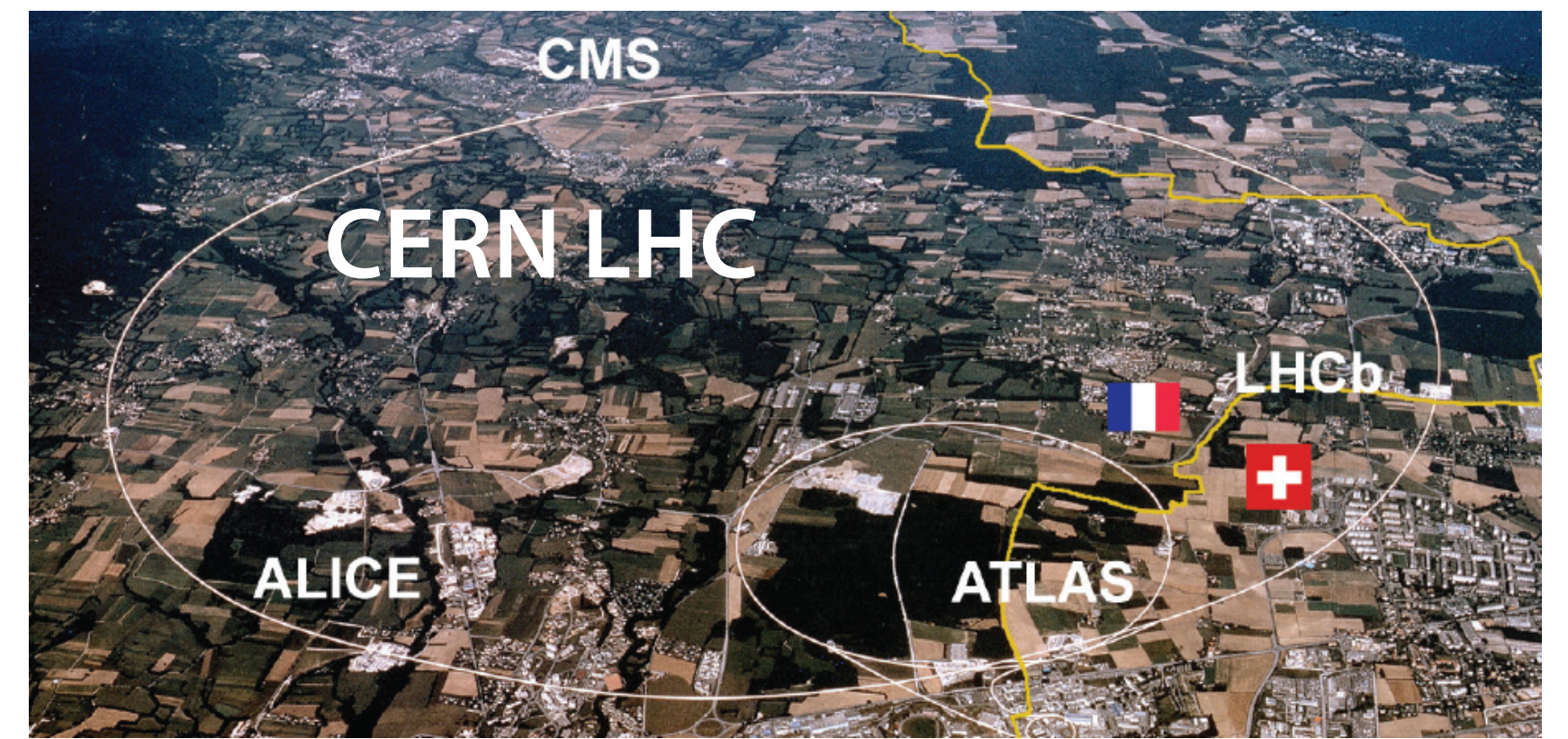
➔ Natural to explore quantum computing in particle physics

- Present quantum computer, called *NISQ* (noisy intermediate-scale quantum device), still at early stage for general use...

➔ Need 1) quantum applications with advantage over classical method, and 2) optimizations suitable for NISQ device

International Center for Elementary Particle Physics (ICEPP), University of Tokyo

- ▶ Working on LHC-ATLAS (CERN), MEG (PSI), ILC, ...
- ▶ International collaboration with CERN & LBNL



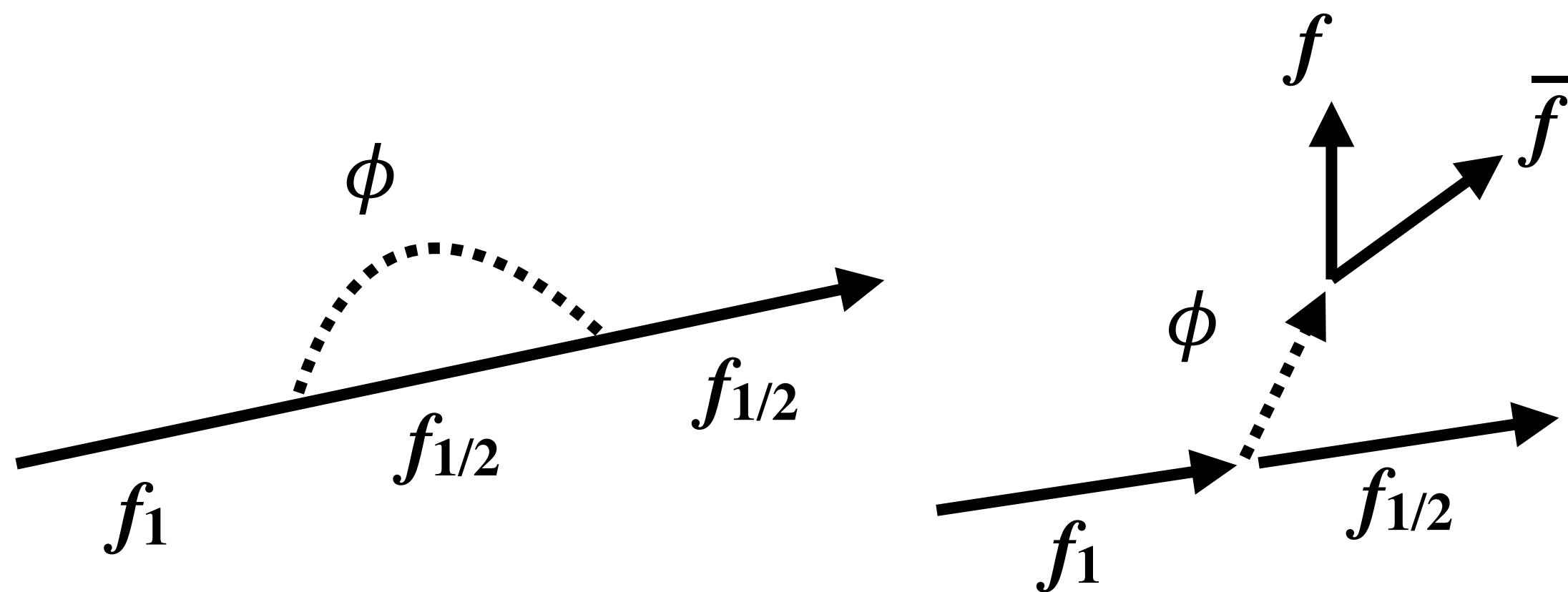
# Quantum Algorithm for HEP Simulation

Parton shower processes typically simulated using probabilistic classical calculations (e.g., Markov-Chain MC)  
➔ Impossible to include all amplitudes of contributing processes when the number of emissions grows

C. W. Bauer, B. Nachman *et al.*  
[Phys. Rev. Lett. 126, 062001 \(2021\)](#)

## Quantum parton shower model:

- Consider a system composed of boson  $\phi$  and fermion  $f$
- Emission of  $\phi$ -boson ( $f \rightarrow f\phi$ ) and splitting ( $\phi \rightarrow f\bar{f}$ )
- Interference due to two fermion flavors  $\{f_1, f_2\}$  in the intermediate states



- Many quantum gates required to calculate amplitudes at each emission step for every particles
- Algorithm designed to be generic to be able to simulate processes with different initial states

➔ **Reduction of # of gates crucial for NISQ machine**

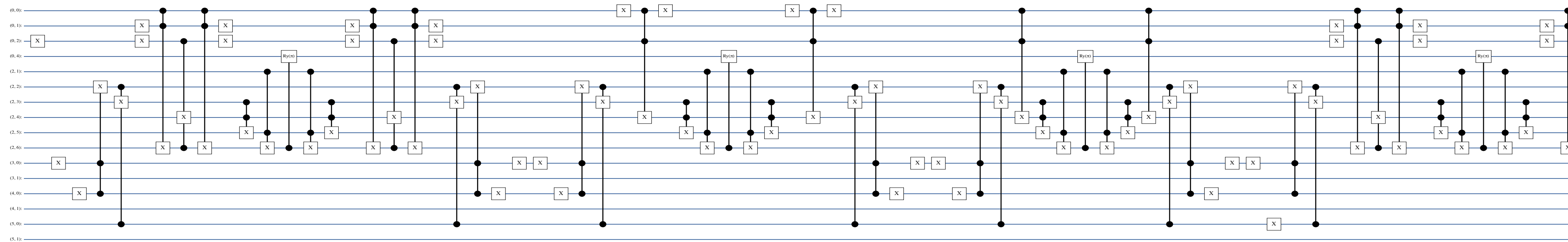
➔ Feasible to do that when focusing on specific initial states at run time

➔ Developed a novel, generic *run-time* optimization protocol called **AQCEL**

**AQCEL** = **A**dvancing **Q**uantum **C**ircuit  
by **ICEPP** and **LB**NL

# Quantum Circuit for Parton Shower Simulation

Only a small fraction of representative circuit for quantum parton shower simulation



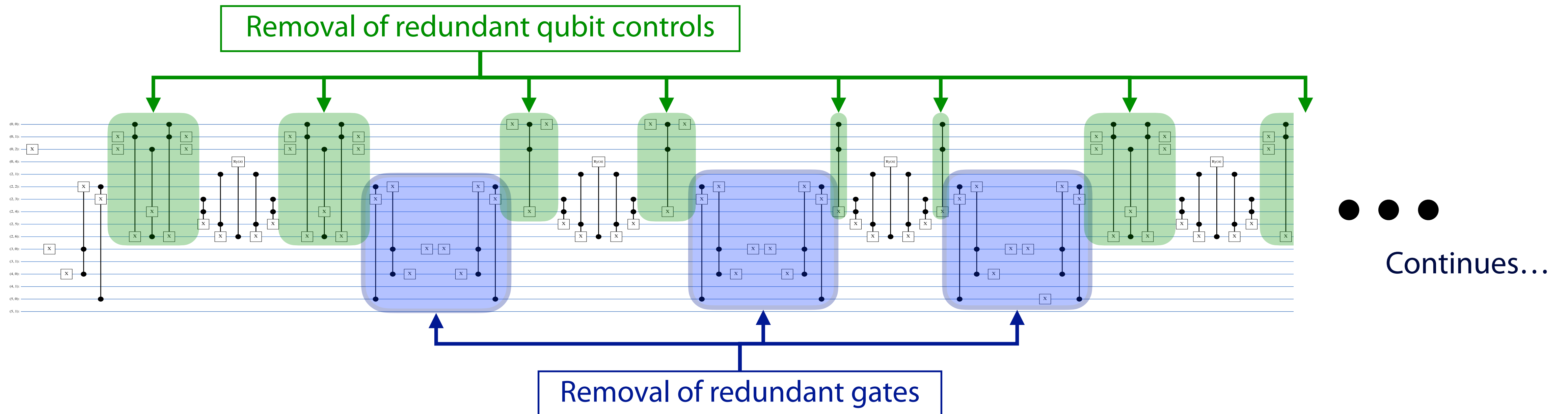
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Actual circuit contains  $>1200$  gates (after compiling to hardware native gates) just for 2 branching steps in showering...

# Quantum Circuit Optimization

Developed a novel optimization protocol called **AQCEL** :

- ▶ Removal of redundant qubit controls by identifying zero- or low-amplitude basis states
- ▶ Removal of redundant gates

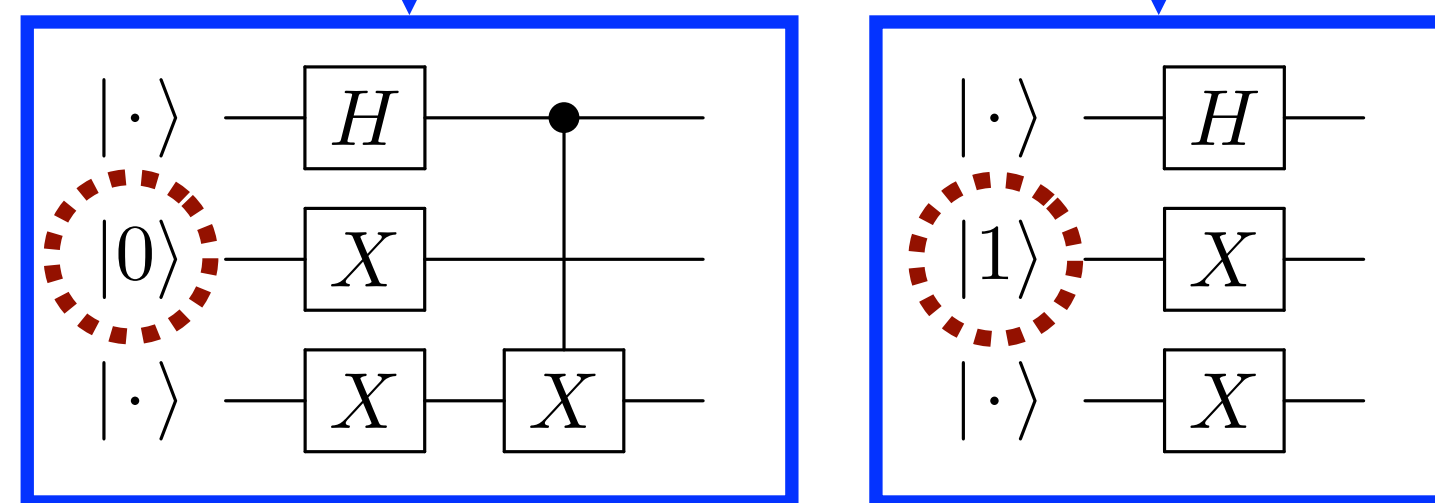
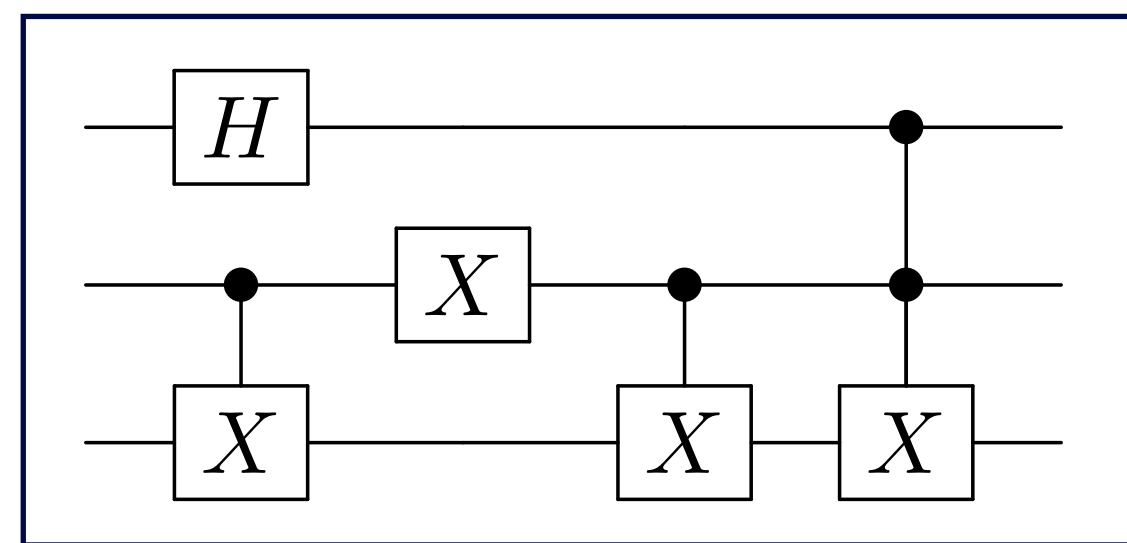


# AQCEL Optimization Protocol

2 main ingredients for gate reduction:

① **Remove redundant qubit controls/gates with identified basis states**

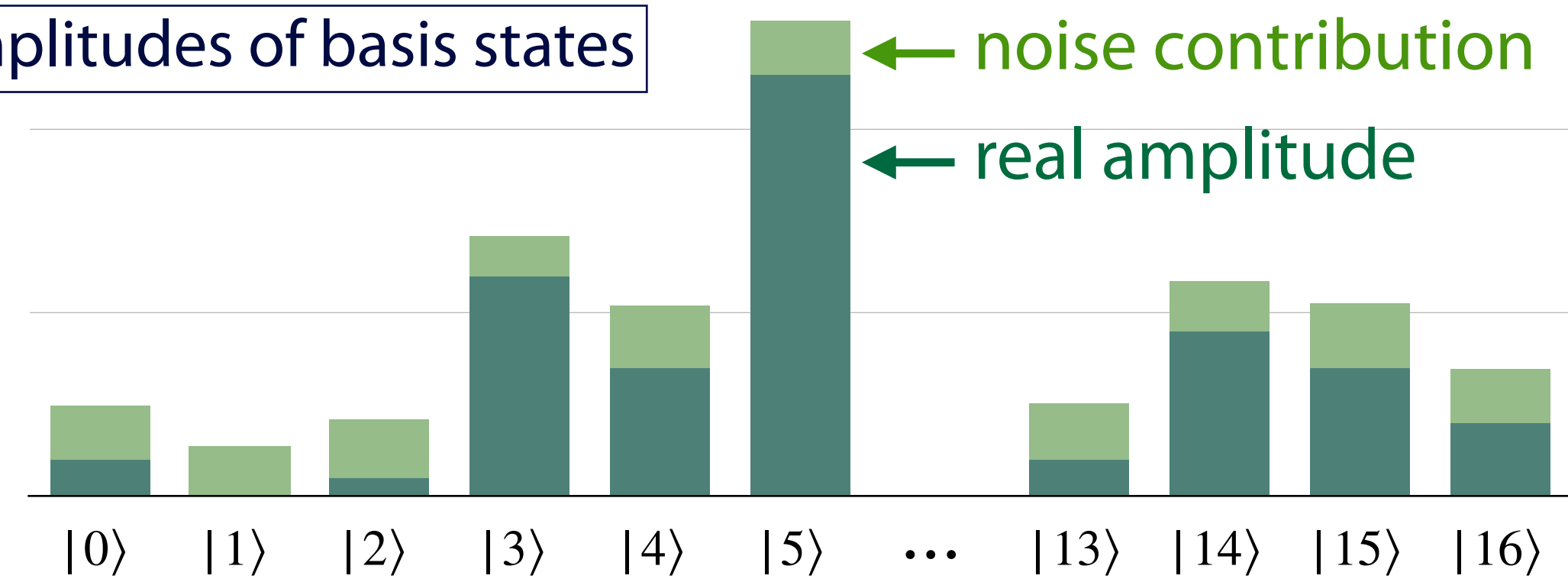
Example circuit



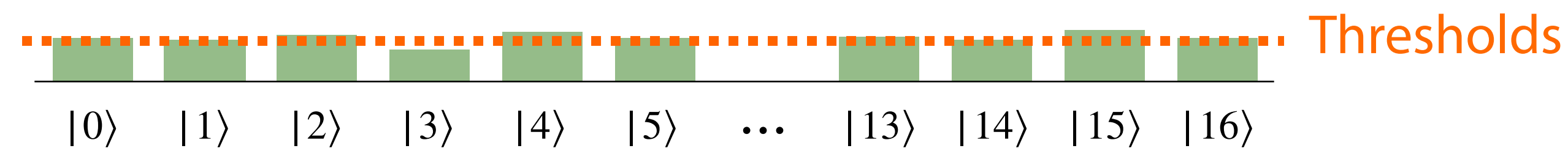
Circuit designed to work with different initial states (*a la* parton shower algorithm) can be simplified when running on specific initial state

② **Identify basis states with polynomial resources using quantum measurements**

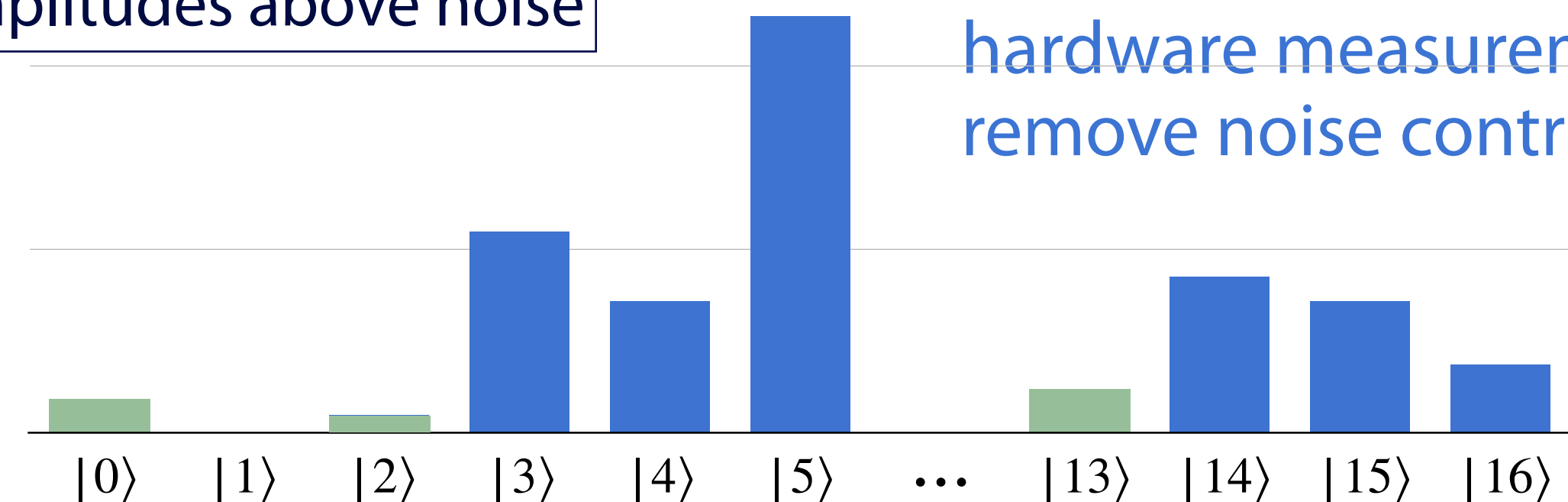
Amplitudes of basis states



Noise-only amplitudes



Amplitudes above noise

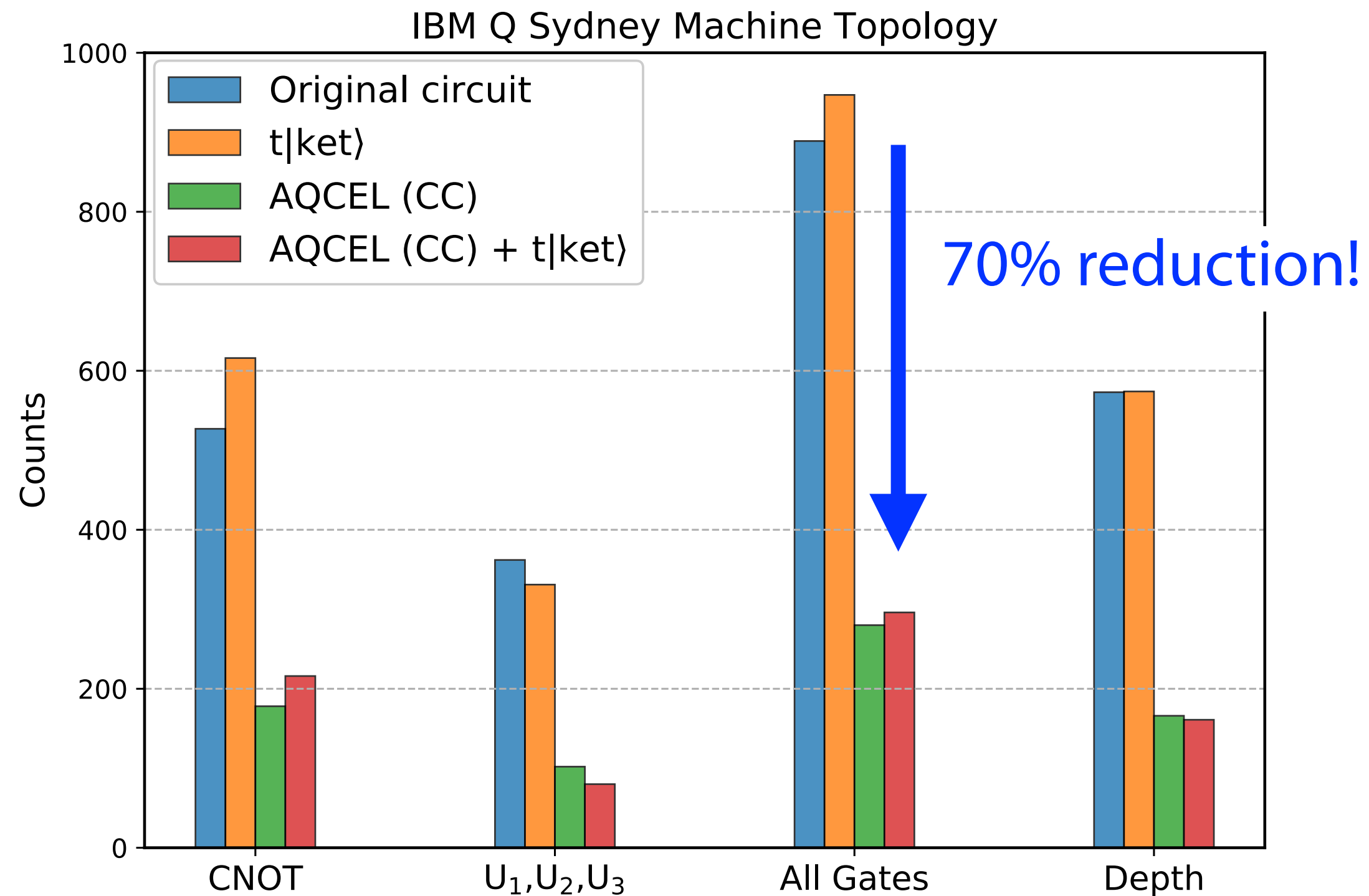


Thresholds determined with hardware measurements can remove noise contribution

➔ **Generic approach; Applicable to other algorithms**

# Circuit Optimization for Parton Shower Simulation

Compared the optimization performance between AQCEL and  $t|\text{ket}\rangle$  from [Cambridge Quantum Computing](#)



Number of native gates in quantum parton shower circuit\*

#Gates	Original	$t \text{ket}\rangle$	AQCEL (Classical)	AQCEL (Quantum)
CNOT	527	616	178 (34%)	64 (12%)
$U_{1,2,3}$	362	331	102 (28%)	24 (7%)
All	889	947	280 (31%)	88 (10%)

\* 1 splitting step only

- ▶ Significant gate reduction achieved for parton shower simulation by AQCEL
- ▶ Further gate reduction possible by AQCEL if circuit optimized using hardware measurements

→ Accuracy??

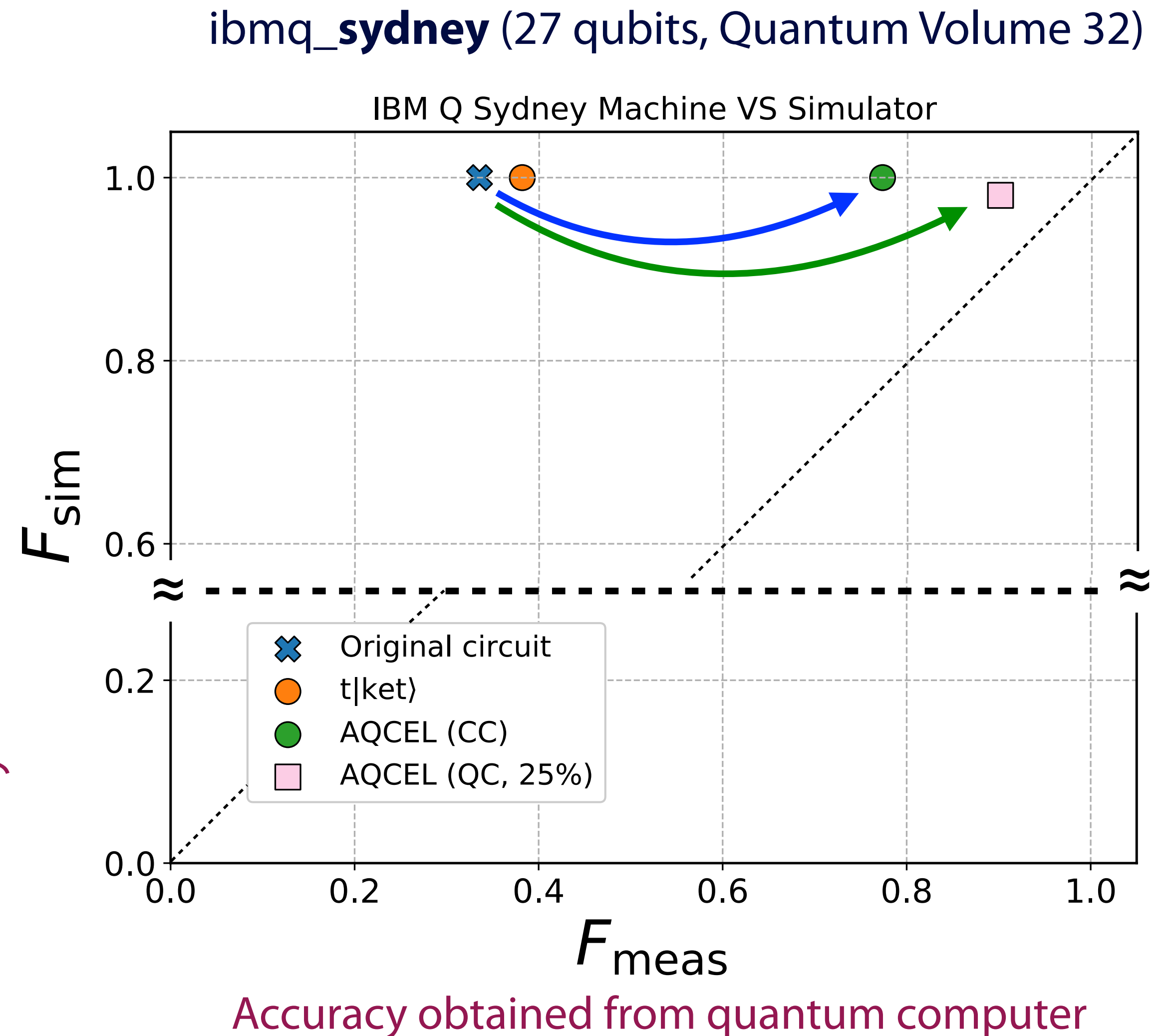
# Circuit Optimization for Parton Shower Simulation

Computational accuracy quantified using probability distributions of measured output bit-strings:

$$F = \sum_k \sqrt{p_k^{\text{orig}} p_k^{\text{opt}}} \quad (\text{Classical Fidelity})$$

$p_k^{\text{orig (opt)}}$  = Probability of  $k$  computational basis state before (after) optimization

Accuracy obtained from classical simulation



- ▶ AQCEL circuit maintains computational accuracy if circuit optimized classically
- ▶ Algorithm performance further improved on quantum computer by AQCEL due to noise suppression if circuit optimized using hardware measurements

➡ More details in [arXiv:2102.10008](https://arxiv.org/abs/2102.10008)



# Summary

- ▶ Working towards quantum computing applications to high-energy physics
- ▶ Working on application-specific circuit design/optimization (quantum parton shower simulation in HEP as a benchmark) for NISQ applications

**AQCEL** optimization protocol documented in [arXiv:2102.10008](https://arxiv.org/abs/2102.10008)

The screenshot shows the arXiv.org interface for the paper 'Quantum Gate Pattern Recognition and Circuit Optimization for Scientific Applications'. The breadcrumb trail is 'arXiv.org > quant-ph > arXiv:2102.10008'. The page title is 'Quantum Physics' with a submission date of '19 Feb 2021'. The authors listed are Wonho Jang, Koji Terashi, Masahiko Saito, Christian W. Bauer, Benjamin Nachman, Yutaro Iiyama, Tomoe Kishimoto, Ryunosuke Okubo, Ryu Sawada, and Junichi Tanaka. The abstract discusses the AQCEL optimization protocol for quantum circuits. On the right, there are options to download the paper in PDF or other formats, and a list of references including INSPIRE HEP, NASA ADS, Google Scholar, and Semantic Scholar.

Code is made public at [Github](#)



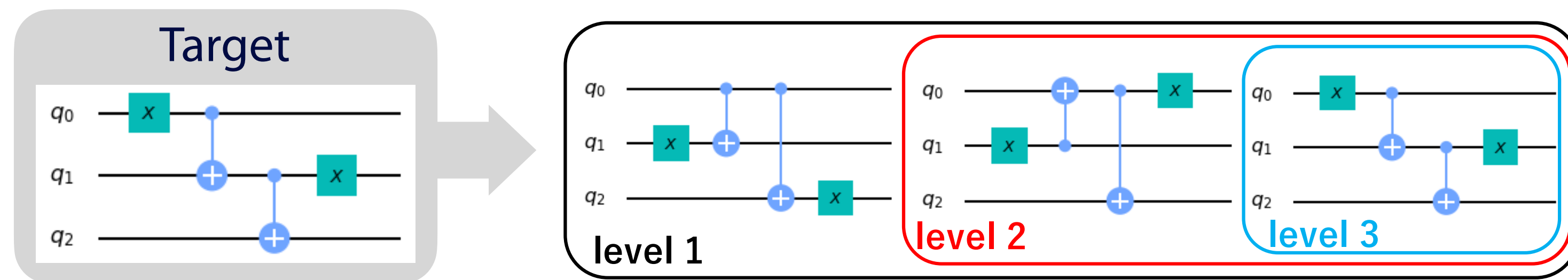
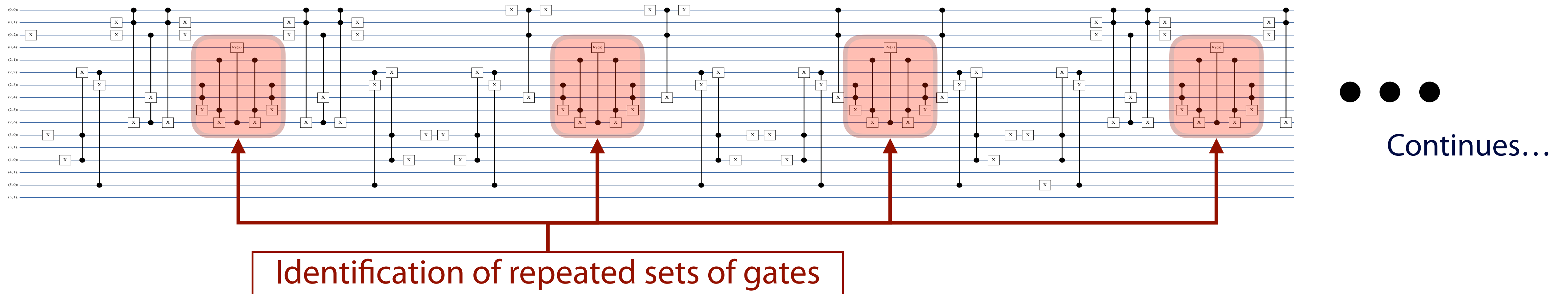
*Feedback appreciated!*

# Backup

# Quantum Gate Pattern Recognition

Developed a novel optimization protocol called **AQCEL** :

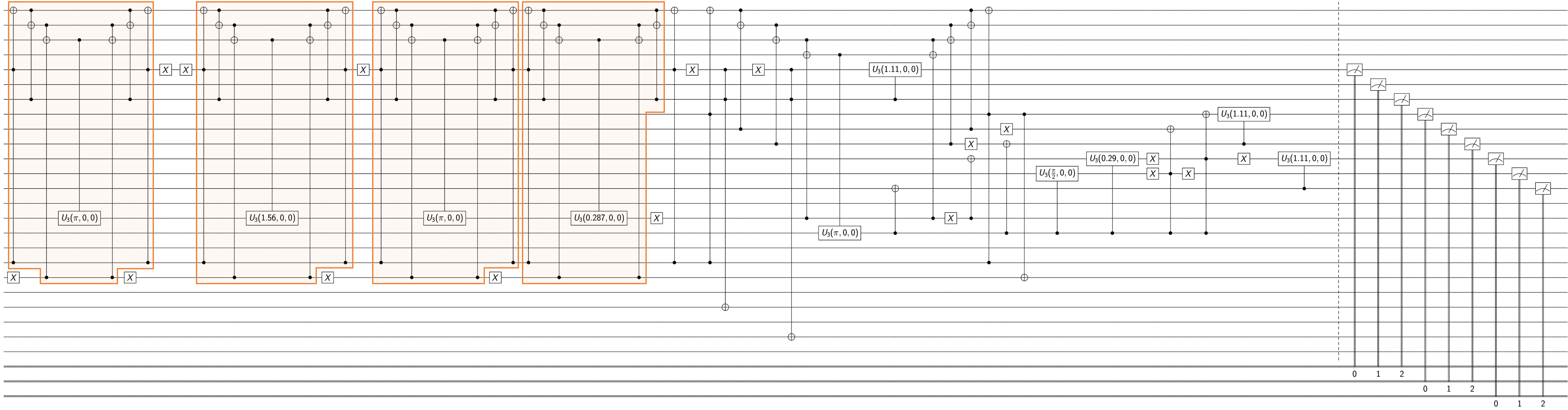
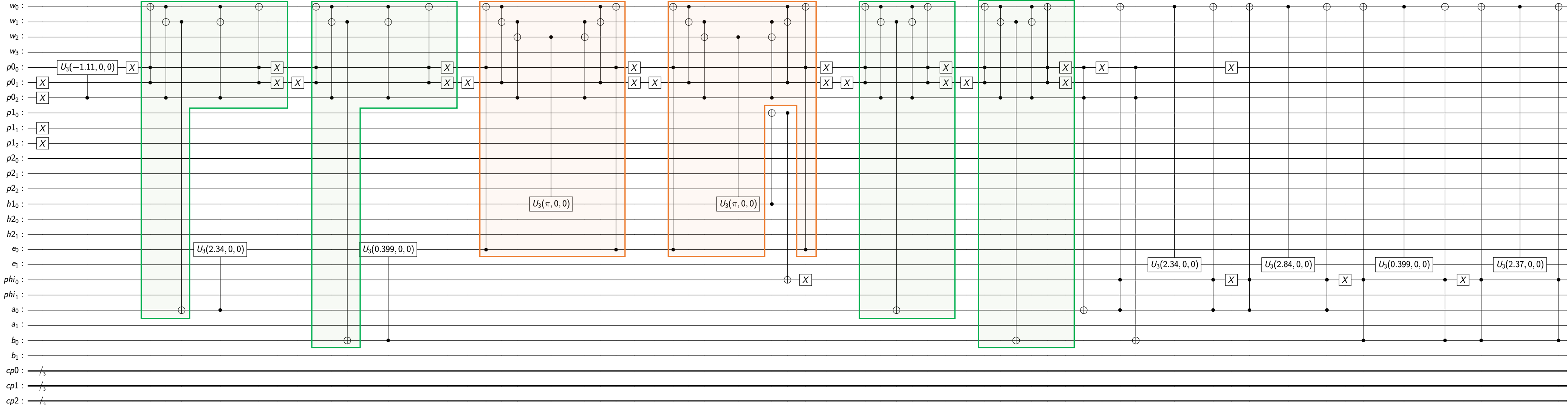
- Identification of repeated sets of gates for application-specific gates/hardware control



- Analyze circuit structure using directed acyclic graph
- 3-level pattern matching to identify repeated gates

# Recognized Gate Sets for Parton Shower Simulation

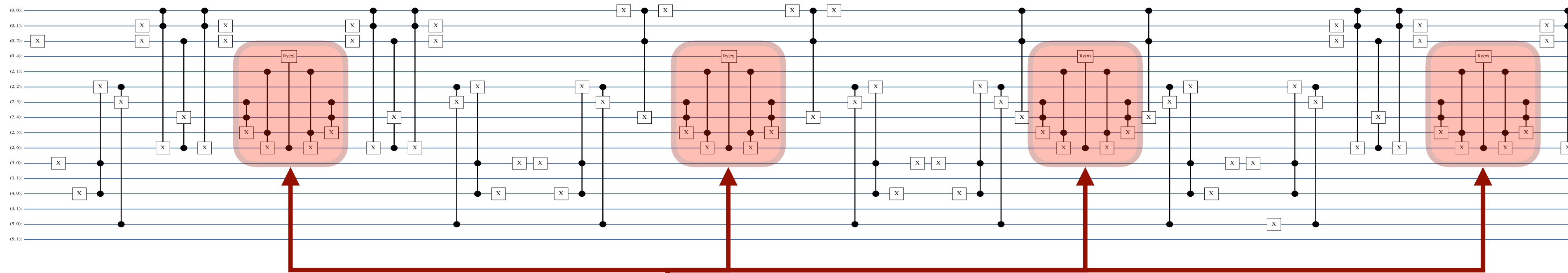
Level-2 matching



# Quantum Gate Pattern Recognition

Developed a novel optimization protocol called **AQCEL** :

- Identification of repeated sets of gates for application-specific gates/hardware control



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Identification of repeated sets of gates

