

Study of the process
 $e^+e^- \rightarrow K_S K^\pm \pi^\mp$
with CMD-3 detector

Channels contribution to HVP

$$\text{had.} = \int \frac{ds}{\pi(s-q^2)} \text{Im} \text{had.}$$

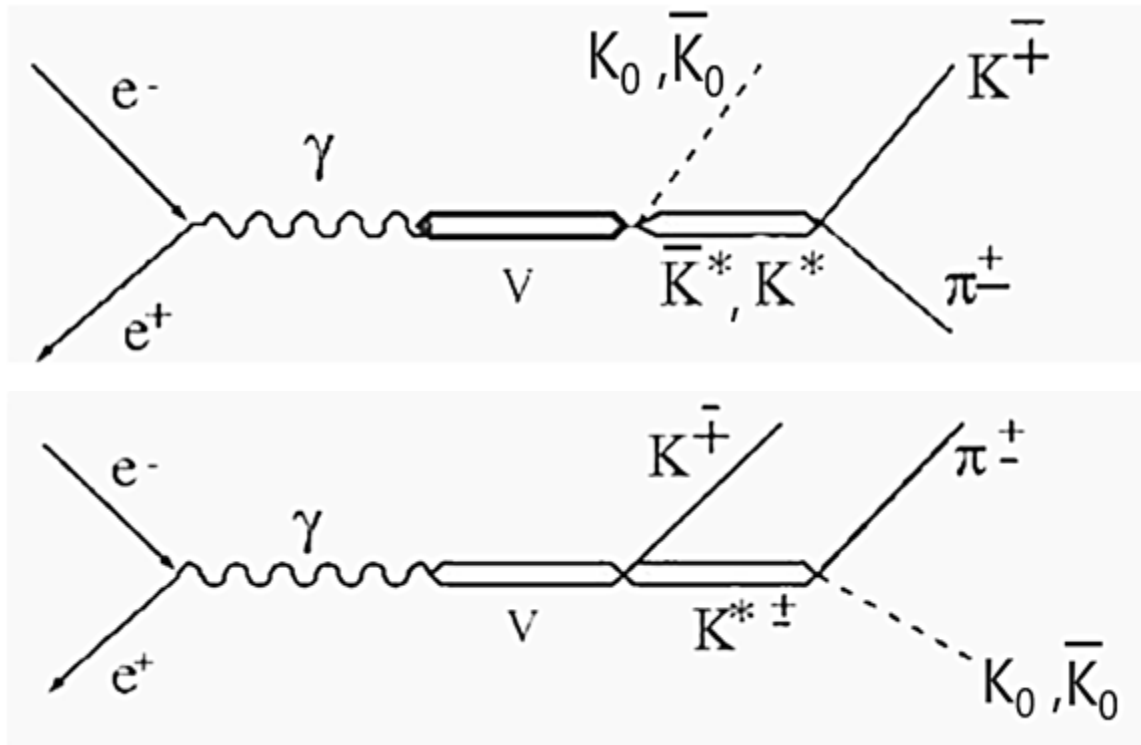
$$2 \text{Im} \text{had.} = \sum_{\text{had.}} \int d\Phi \left| \text{had.} \right|^2$$

$$a_{\mu}^{\text{had,LO}} = \frac{m_{\mu}^2}{12\pi^3} \int_{s_{\text{th}}}^{\infty} ds \frac{1}{s} \hat{K}(s) \sigma_{\text{had}}(s)$$

$\eta\pi^+\pi^-$	0.88 ± 0.10	$K\bar{K}\pi$	2.77 ± 0.15
K^+K^-	22.09 ± 0.46	$K\bar{K}2\pi$	3.31 ± 0.58
$K_S^0 K_L^0$	13.32 ± 0.16	$K\bar{K}3\pi$	0.08 ± 0.04
$\omega\pi^0$	0.76 ± 0.03	$\omega(\rightarrow\pi^0\gamma)K\bar{K}$	0.01 ± 0.00
$\pi^+\pi^-$	505.65 ± 3.09	$2\pi^+2\pi^-\pi^0(\text{no } \eta)$	1.20 ± 0.10
$2\pi^+2\pi^-$	13.50 ± 0.44	$\pi^+\pi^-3\pi^0(\text{no } \eta)$	0.60 ± 0.05
$3\pi^+3\pi^-$	0.11 ± 0.01	$\omega(\rightarrow\pi^0\gamma)2\pi$	0.11 ± 0.02
$\pi^+\pi^-\pi^0$	47.38 ± 0.99	$2\pi^+2\pi^-2\pi^0(\text{no } \eta)$	1.80 ± 0.24
$\pi^+\pi^-2\pi^0$	18.62 ± 1.15	$\pi^+\pi^-4\pi^0(\text{no } \eta)$	0.28 ± 0.28
$\pi^0\gamma$	4.54 ± 0.14	$\omega(\rightarrow\pi^0\gamma)3\pi$	0.22 ± 0.04
$\eta\gamma$	0.69 ± 0.02	$\eta\pi^+\pi^-(\text{data})$	0.98 ± 0.24
$\eta2\pi^+2\pi^-$	0.02 ± 0.00	$\eta\omega(\text{data})$	0.42 ± 0.07
$\eta\omega$	0.38 ± 0.06	$\eta\phi(\text{data})$	0.46 ± 0.03
$\eta\phi$	0.33 ± 0.03	$\eta2\pi^+2\pi^-(\text{data})$	0.11 ± 0.02
$\phi(\rightarrow \text{unaccounted})$	0.04 ± 0.04	$\eta\pi^+\pi^-2\pi^0$	0.11 ± 0.06

Motivation

- ◆ Study the mechanism of final state birth in the reaction $e^+e^- \rightarrow K_S K \pi$
- ◆ Determine the cross section vs energy of the process $e^+e^- \rightarrow K_S K \pi$
- ◆ Find the parameters of $\varphi(1680)$, $\rho(1450)$ (mass, width, branching)
- ◆ Improve calculation accuracy of the hadronic contribution in $(g-2)_\mu$



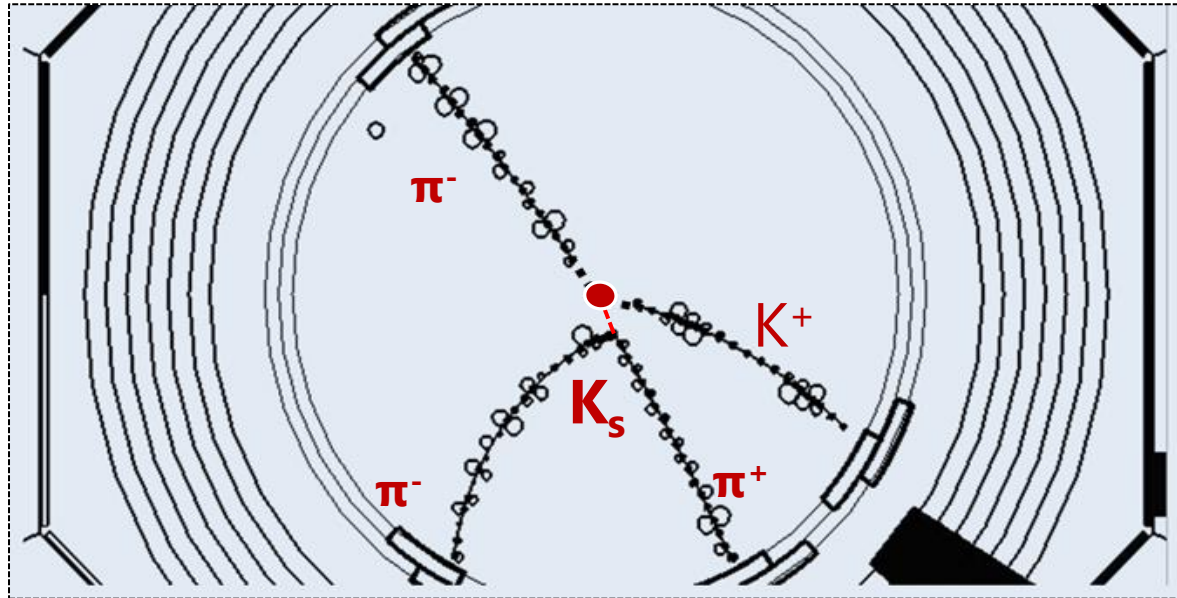
= $K_S K \pi$

Work content:

- ◆ Develop optimal criteria to select events of $e^+e^- \rightarrow KK^* \rightarrow K_s K \pi$ (signal events).
- ◆ Study background processes that mimic signal events.
- ◆ Assess efficiency of registration by simulation with radiative corrections.
- ◆ The systematic errors are included in analysis.
- ◆ Obtained parameters $\varphi(1680)$, $\rho(1450)$ (mass, width, branching) using Vector Model of Dominance.

Events in CMD3

A single signal event of $K_S K^\pm \pi^\mp$ shown on CMD-3 visualization



● - beam axis,

--- - K_S decay length

Event:

One K_S : found by kinematic fit (= *kinfit*), energy-momentum conservation required

Two opposite charged tracks from interaction point (= *IP*)

Two opposite charged tracks from K_S decay

Tracks:

Polar track angle $1 < \Theta_{tr} < \pi - 1$

Number of hits per track ≥ 10

Track momentum from **60** to **800** MeV/c

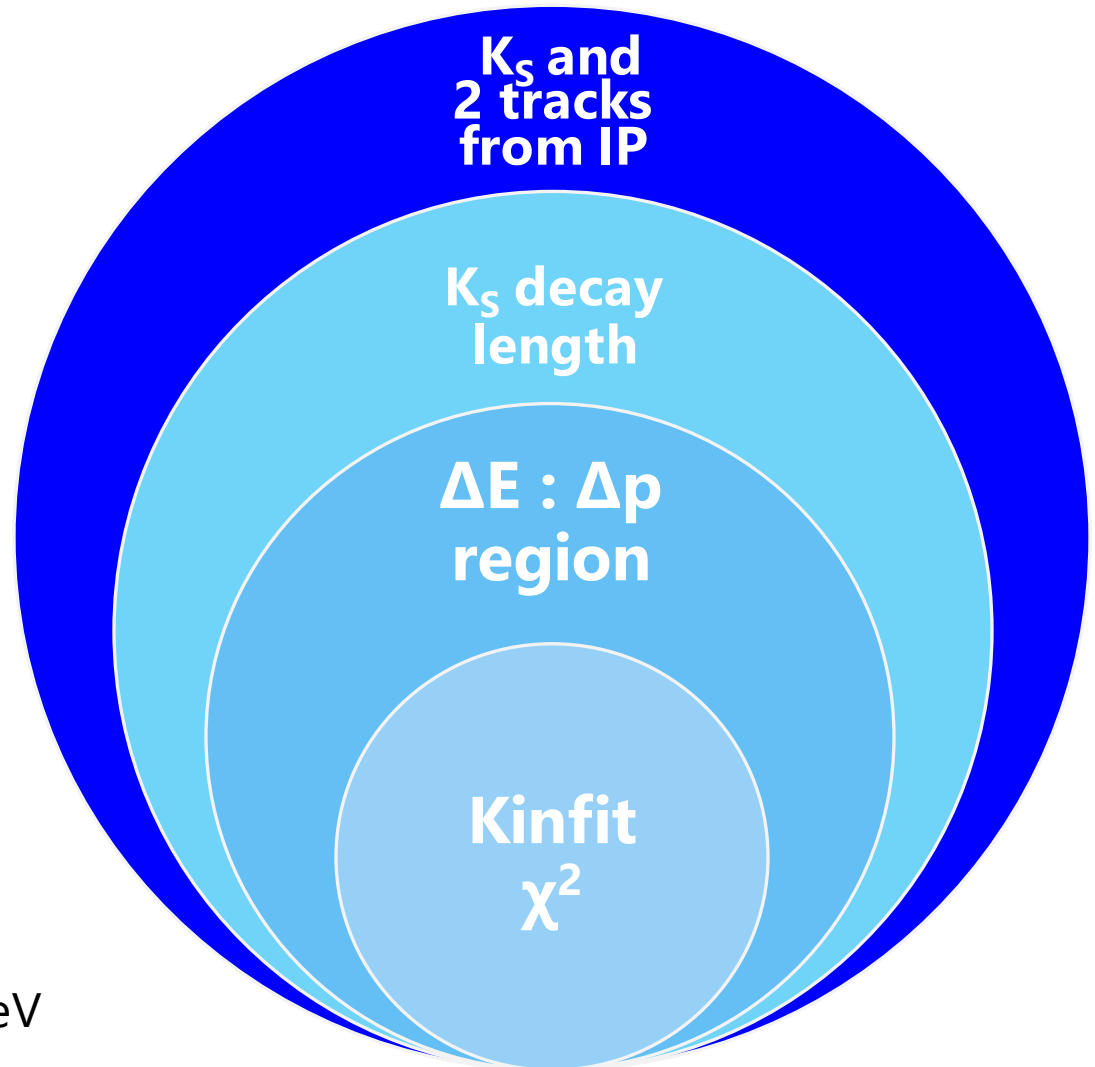
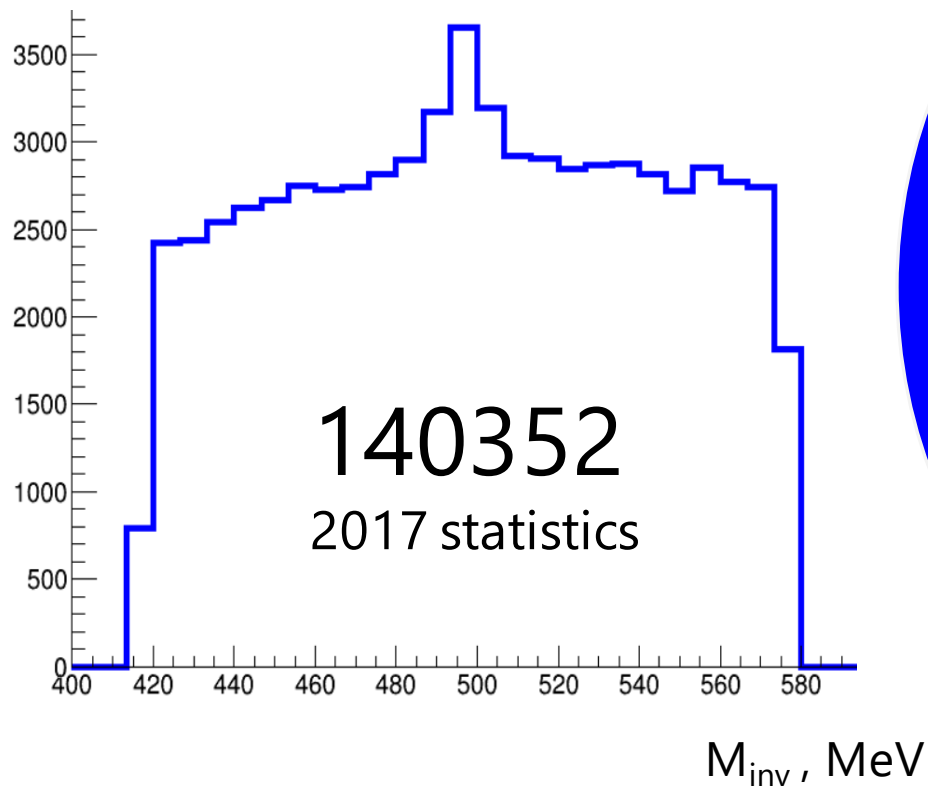
Track z along the beam axis < 12 cm

Track (not from K_S) impact parameter < 0.1 cm

The K_S invariant mass after pre-selection

All pairs of tracks with opposite signs are searched.
They are ascribed a mass of pions and an invariant mass is constructed.

The K_S invariant mass

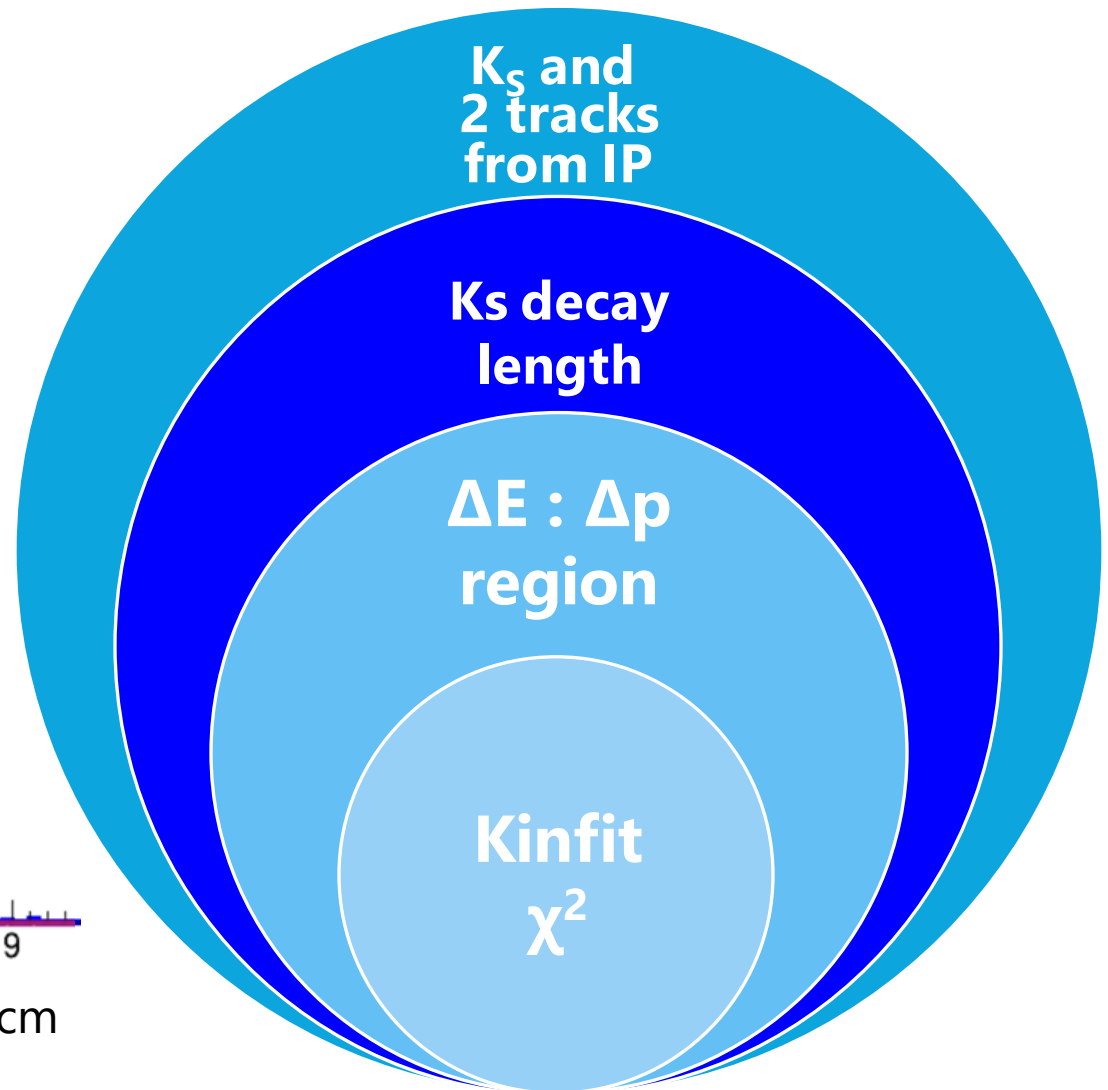
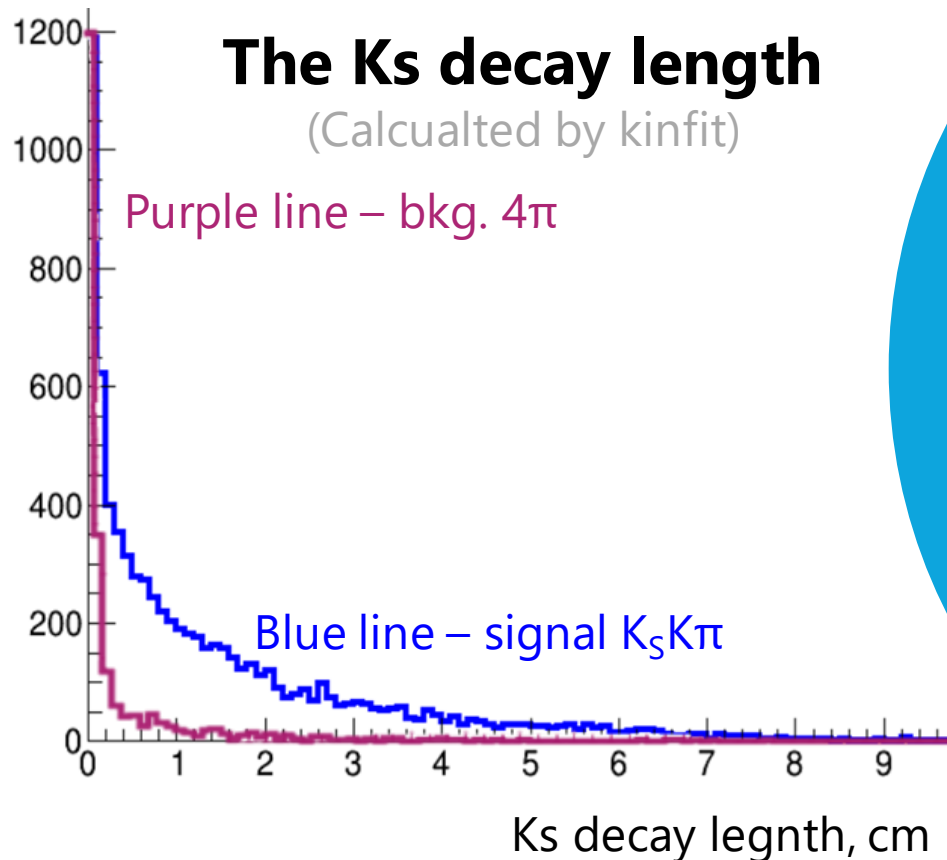


The invariant mass of K_S after the second selection

The K_S decay length is more than 0.2 cm from the beam.

Signal events \downarrow **1.2** times

Background \downarrow **10** times



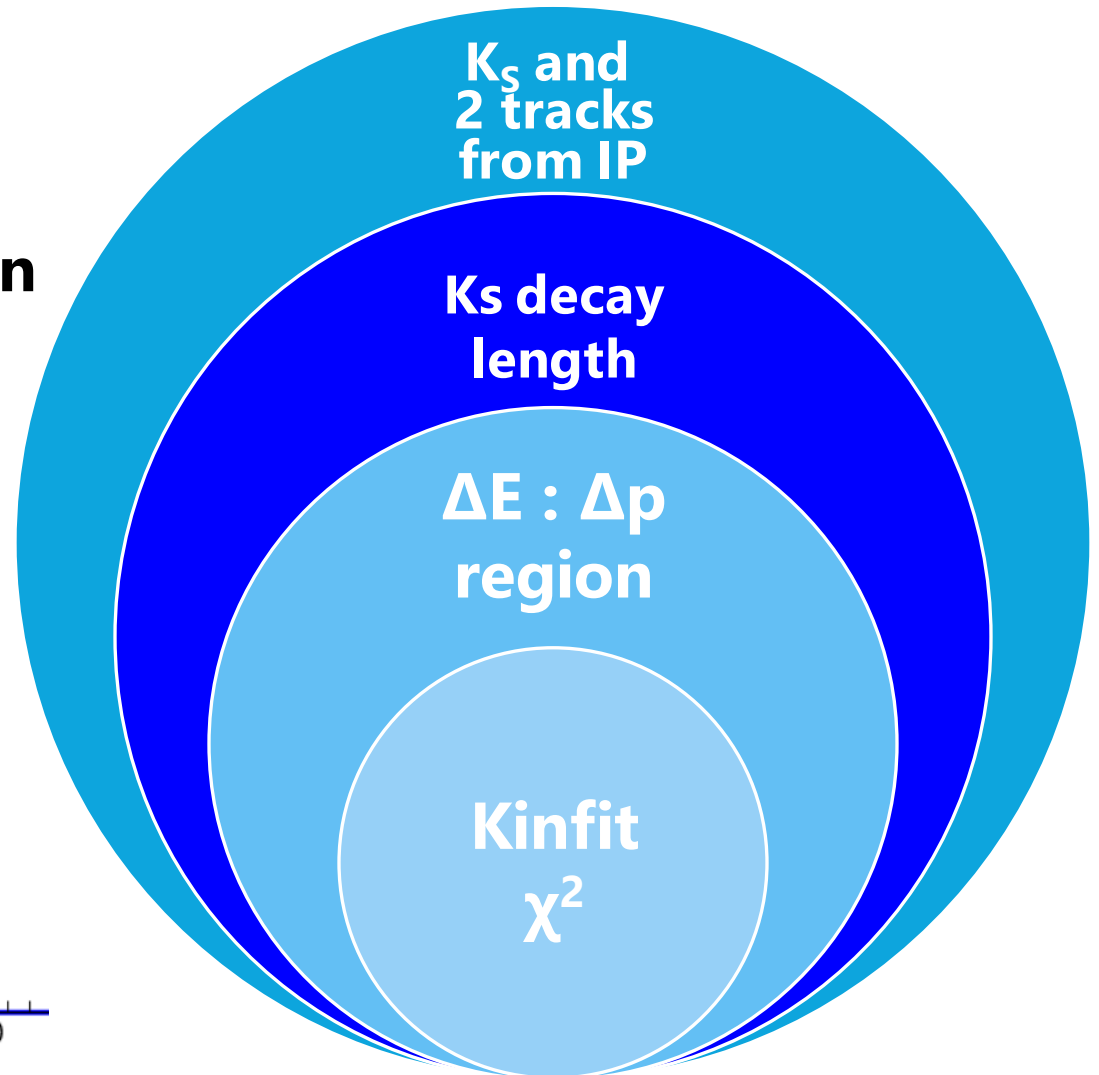
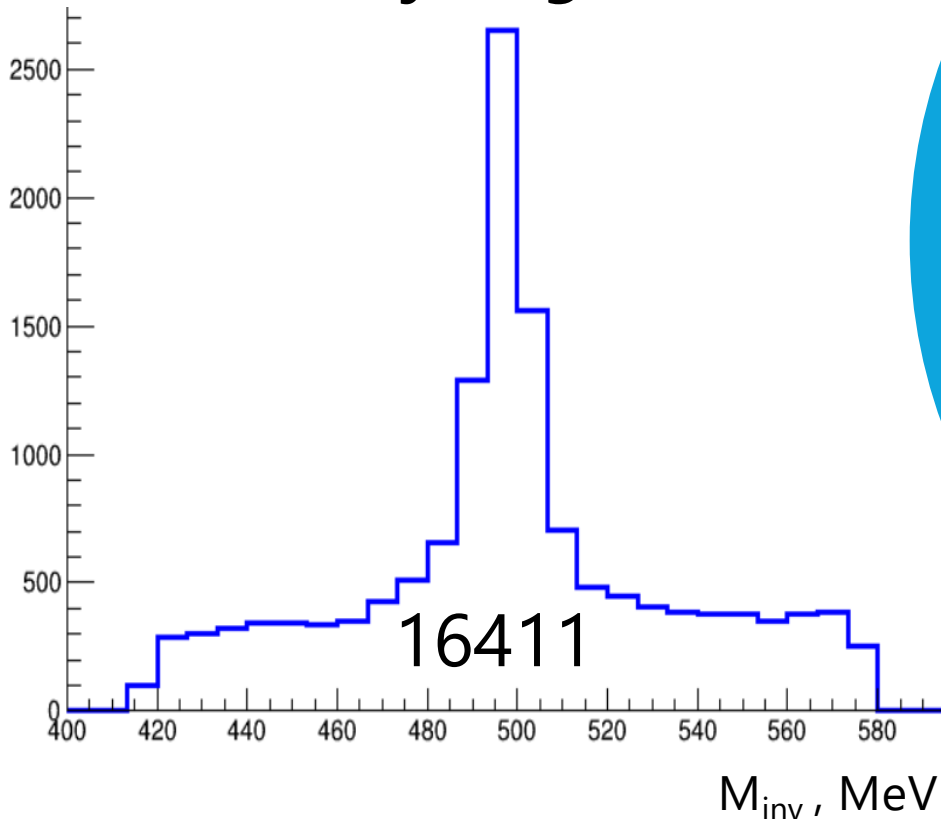
The invariant mass of K_s after the second selection

The K_s decay length is more than 0.2 cm from the beam.

Signal events \downarrow 1.2 times

Background \downarrow 10 times

The K_s invariant mass after decay length selection



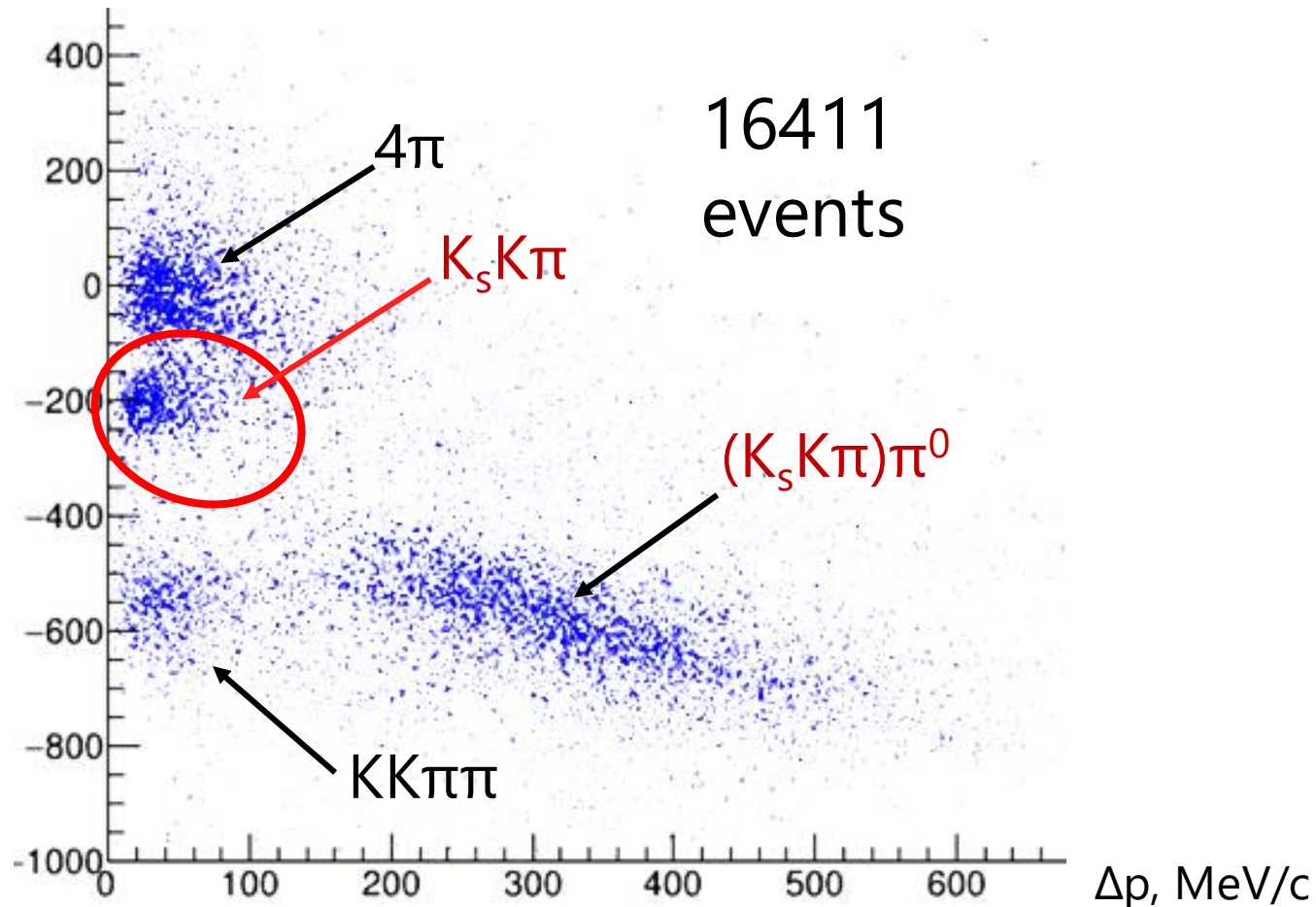
Highlight the events of $K_S K \pi$ process

All four tracks are assigned a mass of π

$$\Delta E = E_1 + E_2 + E_3 + E_4 - 2E_{beam}$$

$$\Delta p = \|\vec{p}_1 + \vec{p}_2 + \vec{p}_3 + \vec{p}_4\|$$

ΔE , MeV

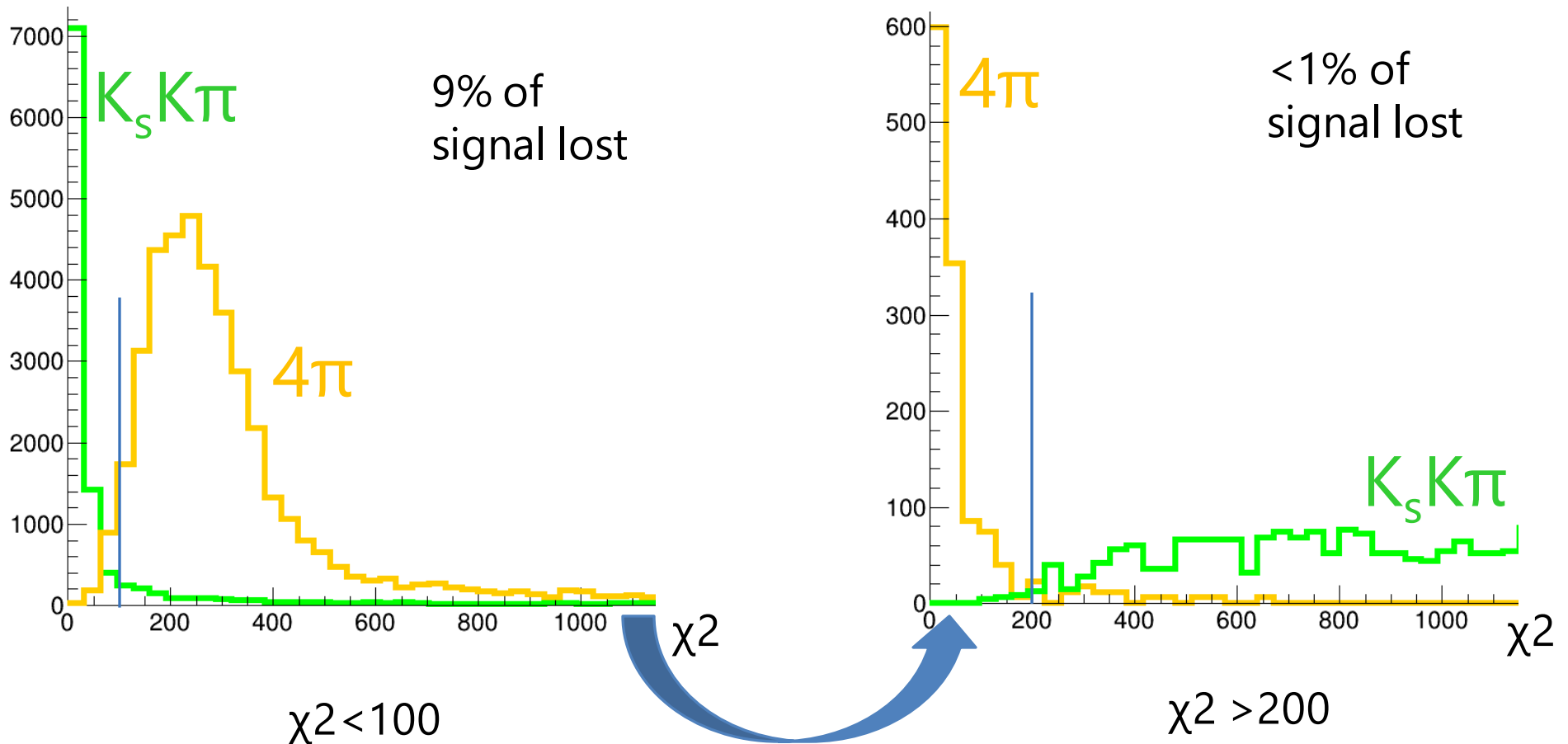


Kinematic reconstruction is carried out in 2 stages

χ^2 of the kinematic reconstruction simulation (760 MeV)

Hypothesis $K_S K\pi$

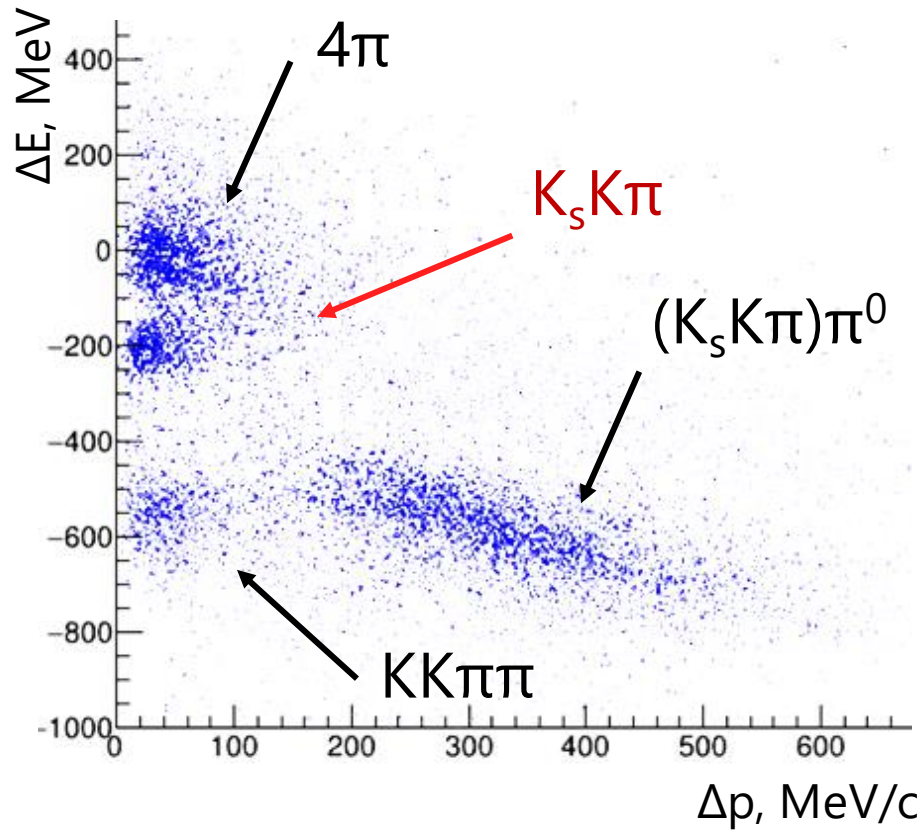
Hypothesis 4π



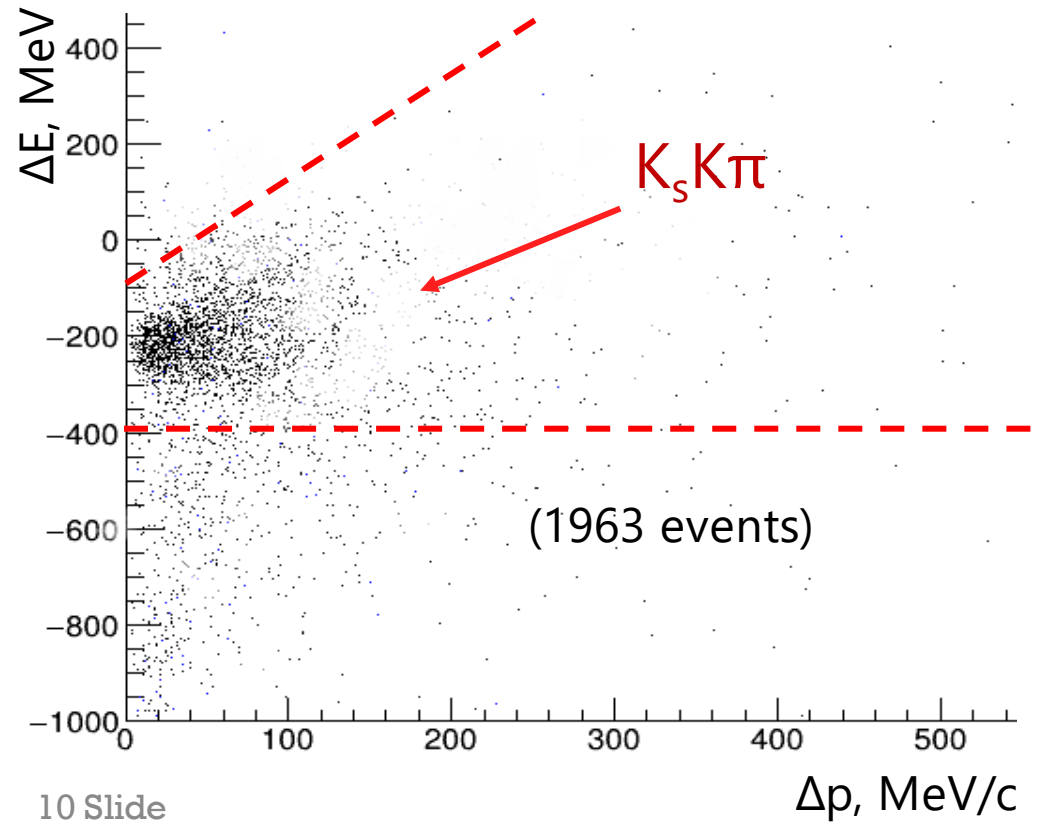
Physical background suppressed x5

Kinematic reconstruction with χ^2 cut suppressed background

Before kinematic reconstruction χ^2 cut
(16411 events)

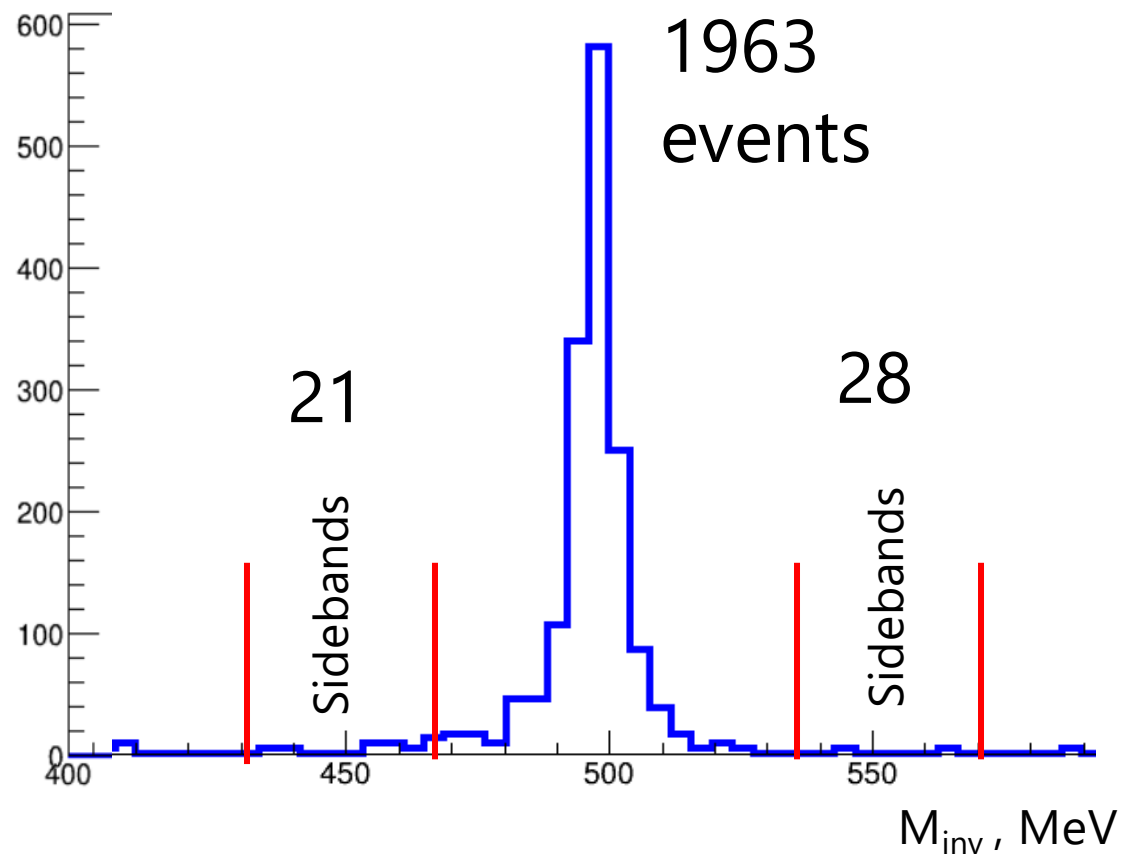


After kinematic reconstruction χ^2 cut



Count events. Subtract background.

The invariant mass of Ks



Dynamics of the process $K_S K \pi$

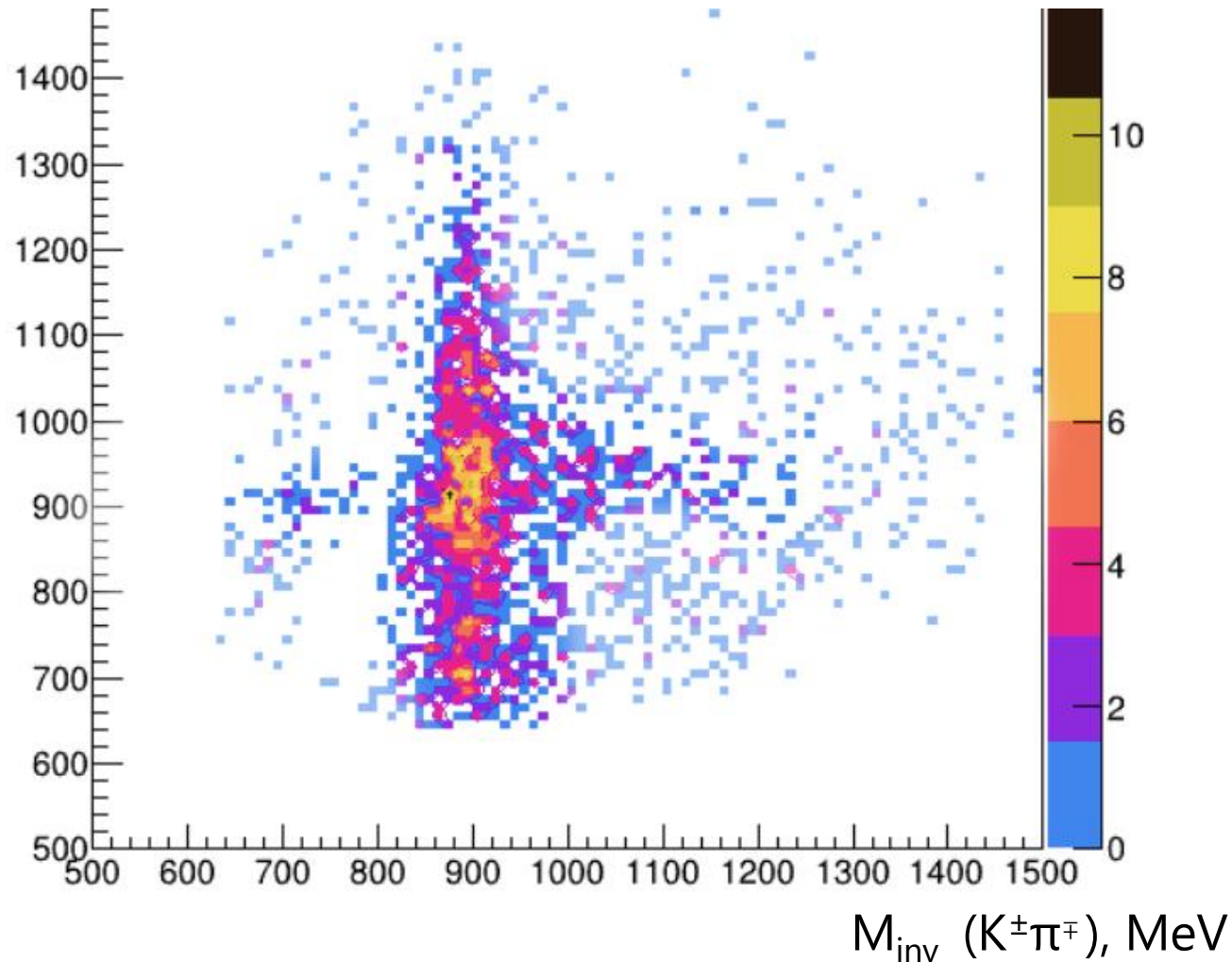
D_{K^*0} – neutral K^* propagator, depends on $M_{inv} (K^\pm \pi^\mp)$

$D_{K^*\pm}$ – charged K^* propagator, depends on $M_{inv} (K_S \pi^\mp)$

Isopin-1/2 \longrightarrow D_{K^*0} enters the amplitude with $A_0 + A_1$,

$D_{K^*\pm}$ enters the amplitude with $A_0 - A_1$, A_0 and A_1 are amplitudes for **isospin** 0 and 1

$M_{inv} (K_S \pi^\mp)$, MeV

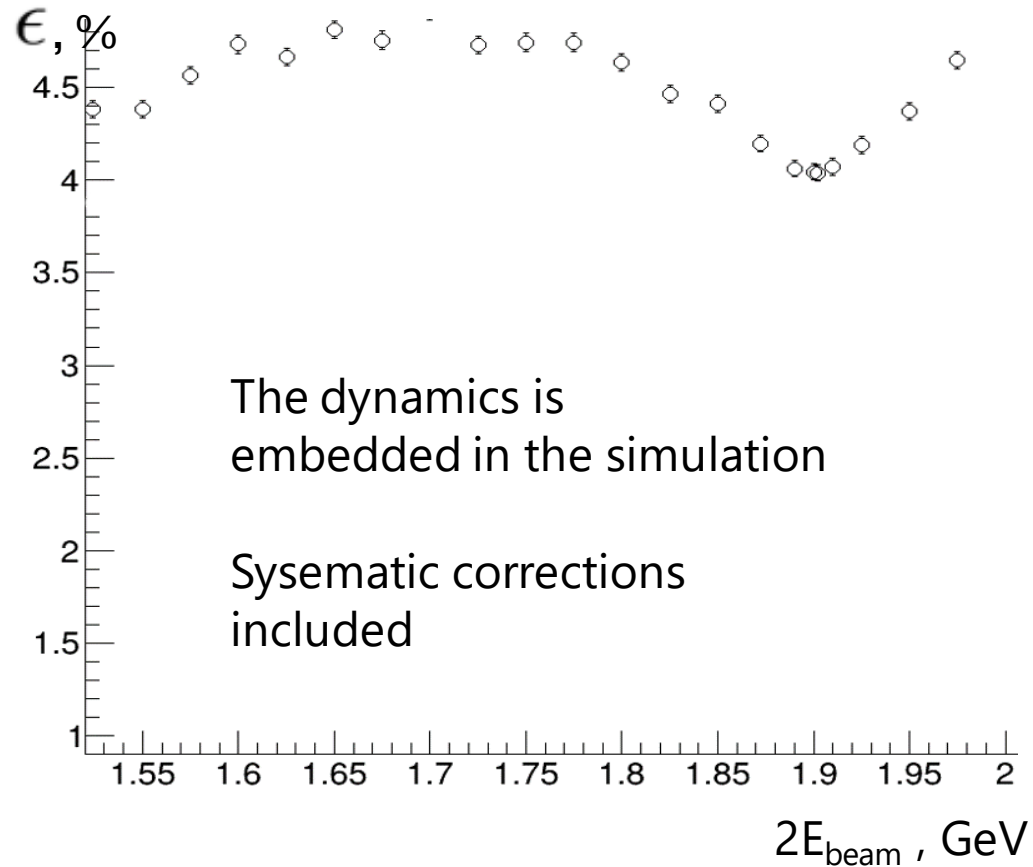
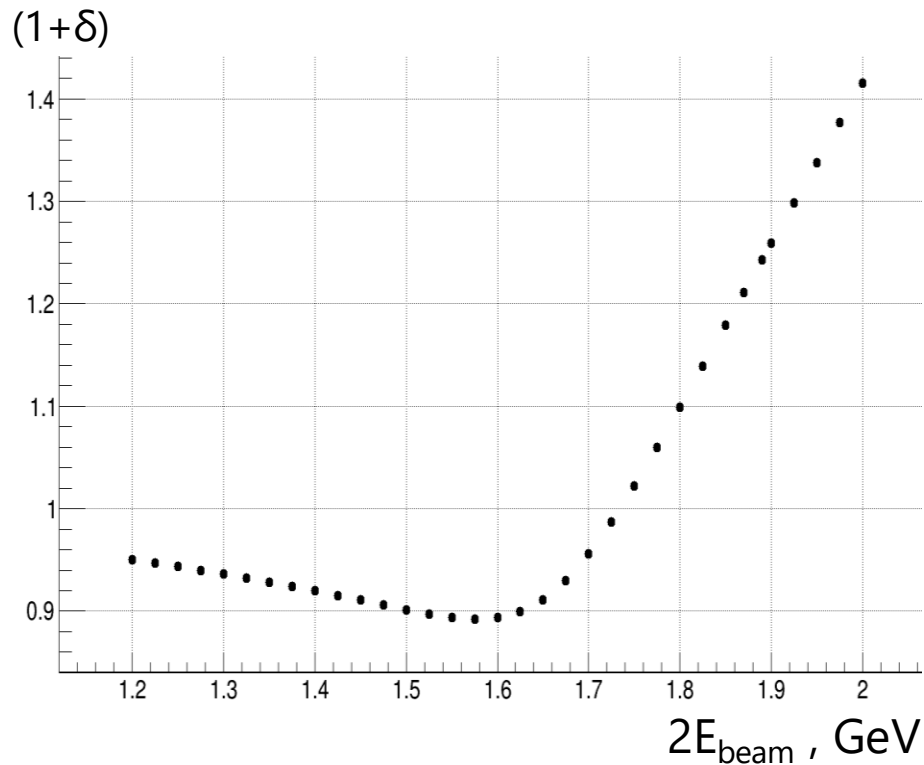


Registration Efficiency and Radiative Correction

$$\sigma_{visible} = \frac{N_{signal}}{L * \epsilon}$$

$$\sigma_{born} = \sigma_{vis} / (1 + \delta)$$

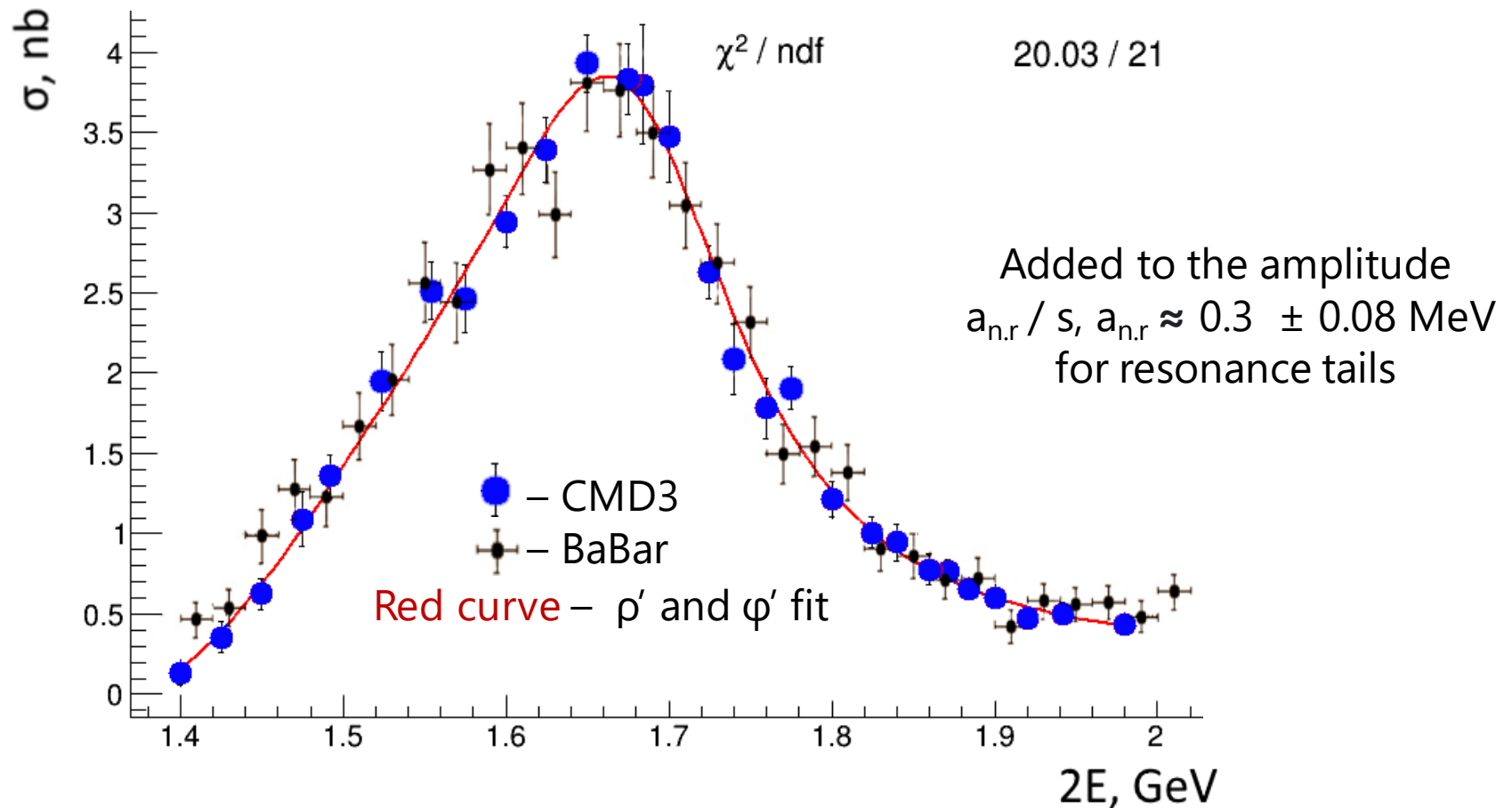
$$\sigma_{visible}(s) = \int_0^{\epsilon} dx \sigma_{born}(s(1-x)) F(x, s)$$



Cross section of the process $e^+e^- \rightarrow K_s K \pi$

Approximation with two resonances $\rho'(1450)$ and $\varphi'(1680)$
plus resonance tail below threshold (red curve)

- The analysis is based on an integral luminosity of 127 pb^{-1} **6019** events selected
- Points less than 5 MeV apart in energy were combined according to luminosity weights



Systematic Uncertainties and Corrections

Accuracy of luminosity measurements, difference of simulation and experiment, model assumptions – all contribute to systematic errors.

We applied corrections, and then estimated errors by varying parameters.

Table 1: Systematic errors of cross-section measurement.

Source	Value, %
Polar angle variation	1.3
Variation of the upper dotted line on dE:dP	1.1
Variation of the bottom dotted line	1.3
Variation of K_S decay vertex distance	1.5
Correction to the reconstruction of tracks in the DC	1.3
Correction to events selection by χ^2	1.1
Background Subtraction	1.2
Luminosity	1.5
Total	3.7

Contributions from uncertainties: branching of K_S to $\pi^+\pi^-$, energy spread, trigger efficiency, radiative correction – are negligible.

Results: mass, width, and lepton branchings

ϕ'

	$\Gamma_{ee}^{\phi'} Br_{KK^*(892)}^{\phi'} (eV)$	$M_{\phi'} (MeV)$	$\Gamma_{\phi'} (MeV)$
This paper 10.1088/1402-4896/abb694	$374 \pm 80 \pm 29$	$1699 \pm 7 \pm 11$	$207 \pm 26 \pm 15$
CMD-3 10.1016/j.physletb.2019.134946	—	$1667 \pm 5 \pm 11$	$176 \pm 23 \pm 38$
BaBar	367 ± 50	1709 ± 19	325 ± 68
PDG	—	1680 ± 20	150 ± 50

ρ'

	$\Gamma_{ee}^{\rho'} Br_{KK^*(892)}^{\rho'} (eV)$	$M_{\rho'} (MeV)$	$\Gamma_{\rho'} (MeV)$
This paper	$105 \pm 17 \pm 13$	$1495 \pm 26 \pm 15$	$361 \pm 29 \pm 18$
CMD-3 10.1007/JHEP01(2020)112	—	1502 ± 11	315 ± 27
BaBar	129 ± 15	1508 ± 19	418 ± 26
PDG	—	1465 ± 25	400 ± 60

Systematic errors include uncertainties of:
cross-section, branchings in $\mathbf{\Gamma(s)}$, resonance tails $\mathbf{a_{n,r}}$

Summary

- ◆ Developed selection criteria for the processes $e^+e^- \rightarrow K_S K^\pm \pi^\mp$ and $e^+e^- \rightarrow K_S K^\pm \pi^\mp \pi^0$
- ◆ Confirmed the dominance of the neutral channel $K^0 K^{*0}(892)$
- ◆ Measured the cross section of the process $e^+e^- \rightarrow K_S K^\pm \pi^\mp$ with a systematic accuracy better than 4%
- ◆ Approximated cross section of the process $e^+e^- \rightarrow K_S K^\pm \pi^\mp$ with two resonances $\phi(1680)$, $\rho(1450)$. Measured parameters of these resonances with the world average accuracy.