



Istituto Nazionale di Fisica Nucleare  
SEZIONE DI TORINO

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# *Spectroscopy: experimental review*

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*Lepton-Photon 2021*  
*January 13<sup>th</sup> 2022*

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*INFN – Sezione di Torino*

# Interplay with theory



Non-perturbative QCD

Hadroquarkonium

Lattice

NRQCD

Di-quarks

Molecules

Light cone

Experiments

**Spectroscopy = Non perturbative QCD**

→ Can't do direct calculation, rely on models approximating QCD

→ Understand (solve?) QCD in the NP regime

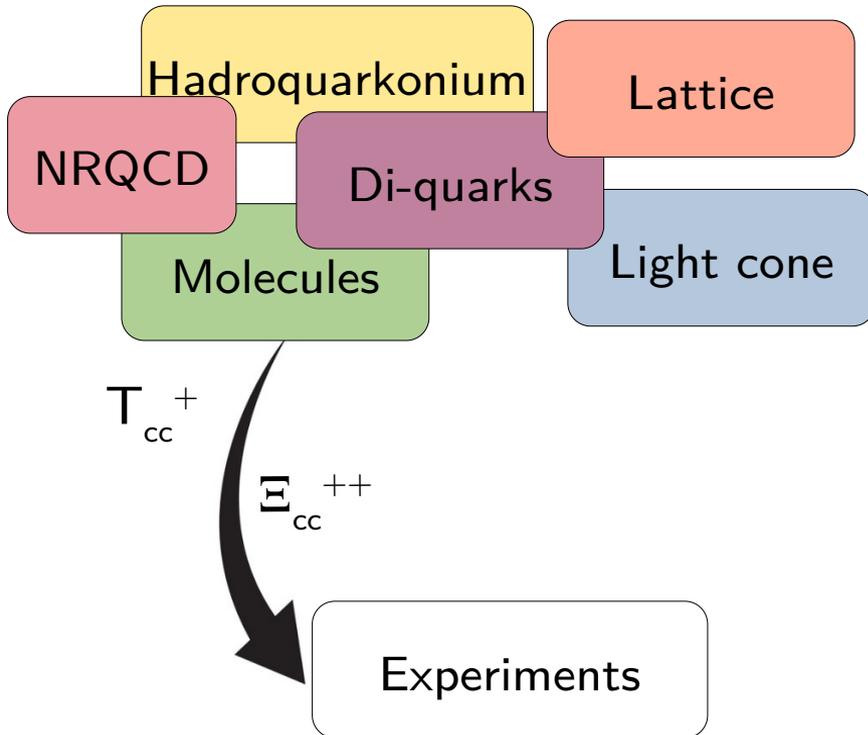
# Interplay with theory



Non-perturbative QCD

## Peculiar features

→ Huge number of theoretical predictions



# Interplay with theory



Non-perturbative QCD

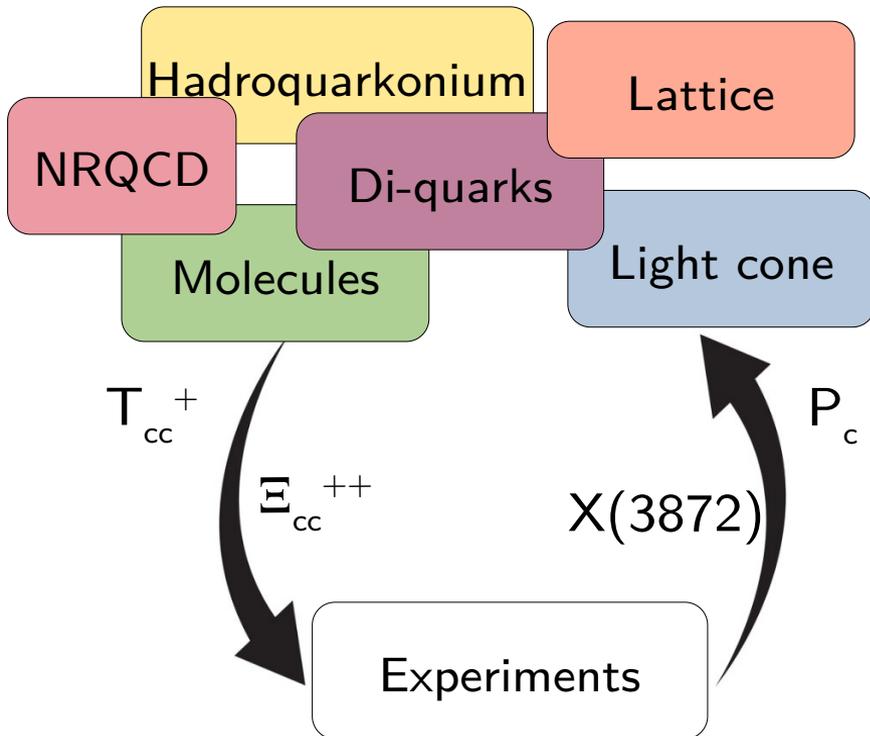
## Peculiar features

→ Huge number of theoretical predictions

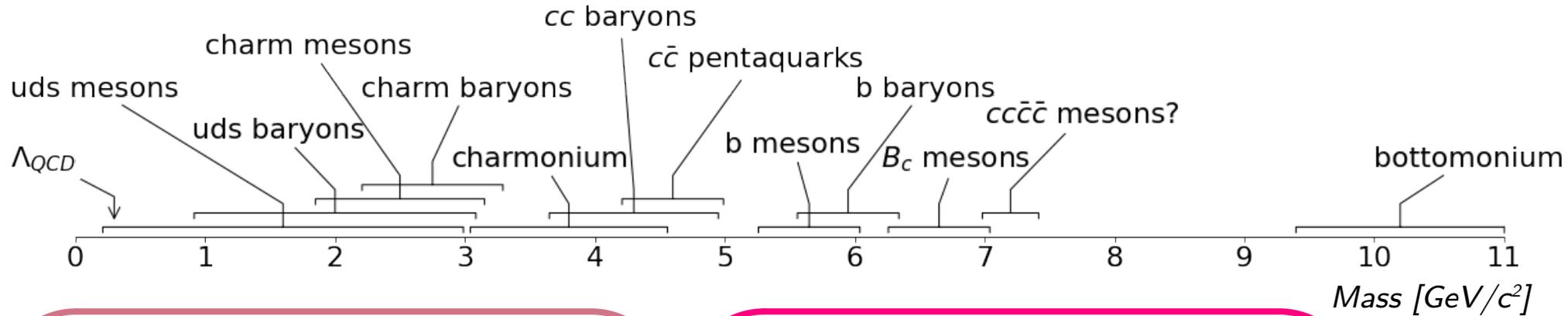
→ feedback loop

→ **We often discover unpredicted features**

→ New knowledge feeds back to theory



# Heavy or light hadrons?



## Light hadrons

Large mixing by  $SU(3)_f$

$$M(q) \sim E_{\text{binding}}$$

- Relativistic
- L not good quantum number

## Heavy hadrons

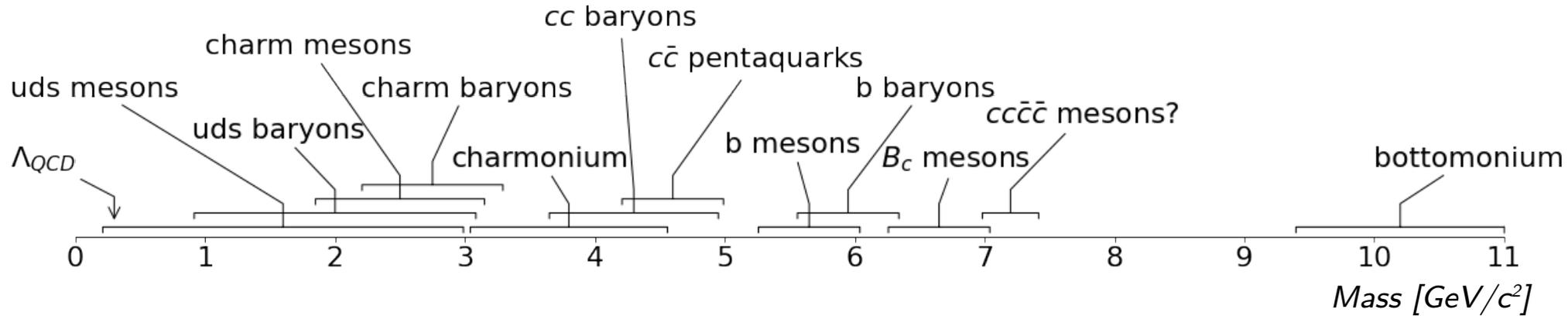
$SU(n)_f$  broken

- c and b hadron don't mix
- tag flavor by decay products

$$M(c,b) \gg E_{\text{binding}}$$

- non-relativistic
- L is good quantum number
- heavy quark spin symmetry

# Heavy or light hadrons?



$\gamma N, \pi N$  scattering



CLAS, COMPASS ...

$D, \Lambda_c$  decays



Belle II, BESIII, LHCb ...

$B, \Lambda_b$  decays



Belle II, LHCb, CMS ...

$e^+e^-$  direct production



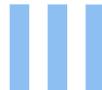
CMD-3, Belle II, BESIII

$pp/HI$  prompt production



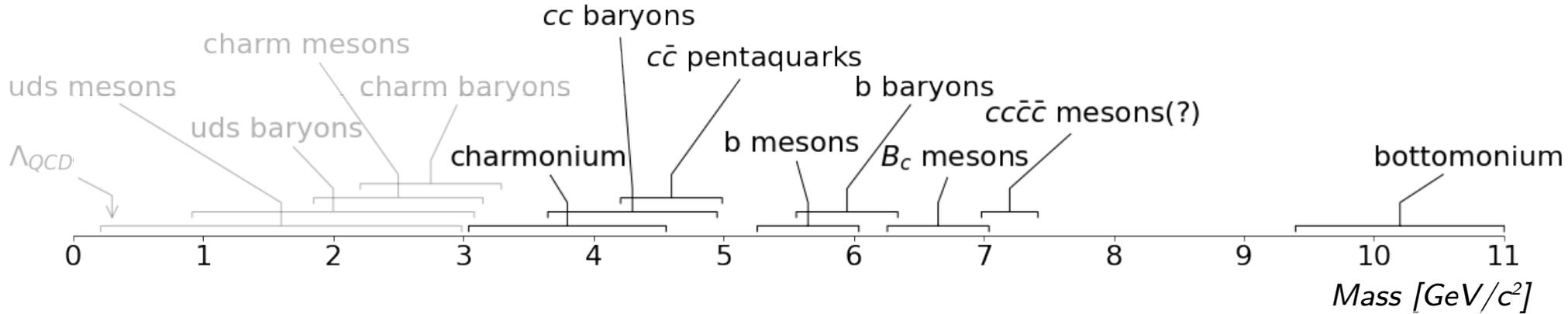
LHCb, CMS ...

Quarkonia decay



Belle II, BESIII, LHCb, CMS ...

# Heavy or light hadrons?



$\gamma N, \pi N$  scattering

$D, \Lambda_c$  decays

$B, \Lambda_b$  decays

$e^+e^-$  direct production

$pp/HI$  prompt production

Quarkonia decay

**This talk will be focused on  
charmonium and above**



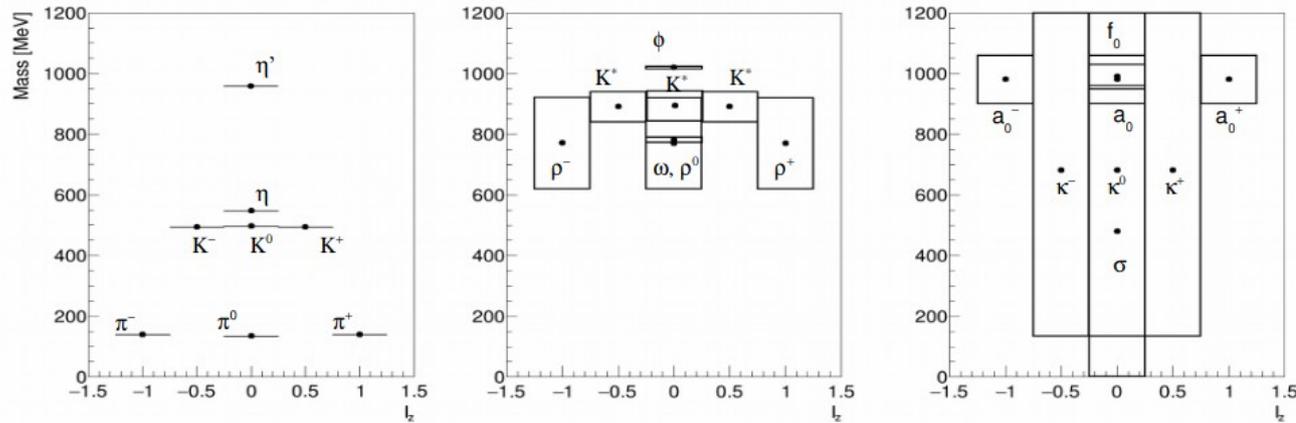
# Why heavy mesons

**Multi-quark systems are possible at any energy** [Jaffe, Wilke, *PRL* 91 232003 (2003)]

- proposed to describe  $a_0(980)$  and  $f_0(980)$  [Baru et al. *PLB* 586 53-61 (2004)]

- can explain inverted hierarchy in scalar mesons [Maiani et al. *PRL* 93 212002 (2004)]

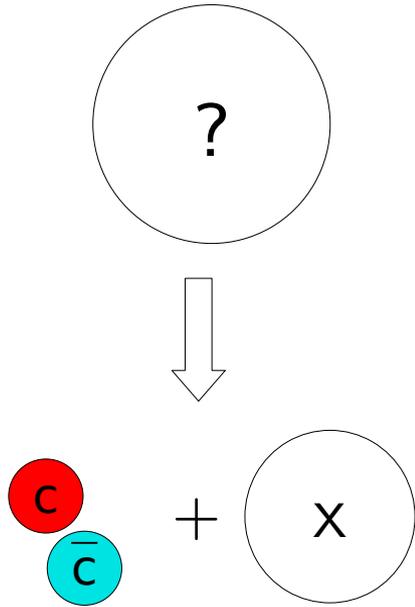
[t Hooft et al. *PLB* 662 424-430 (2008)]



However, no smoking gun to distinguish  $q\bar{q}$  and  $qq\bar{q}\bar{q}$  in the light sector

# Why heavy mesons

With Heavy mesons separating conventional and exotics is much simpler



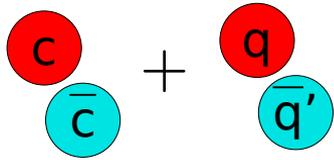
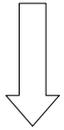
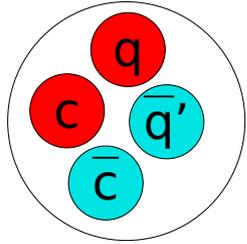
If a state has:

- Mass  $> 3 \text{ GeV}/c^2$
- Narrow ( $\Gamma/M < 0.1$ )
- Decaying strongly into  $J/\psi$  (or  $D\bar{D}$ ) + something

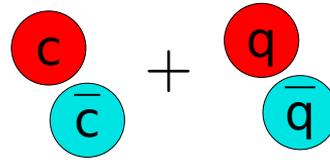
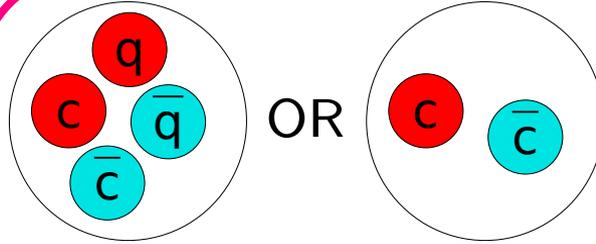
**It must contain a  $c\bar{c}$  pair**

# Why heavy mesons

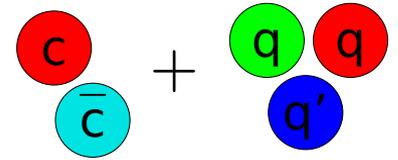
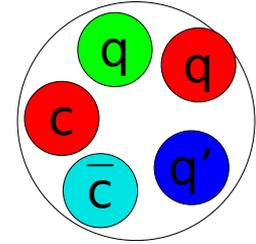
With Heavy mesons separating conventional and exotics is much simpler



Charged/flavoured  $c\bar{c}$ -like  
- must have 4 quarks



Neutral  $c\bar{c}$ -like  
- 2 or 4 quarks  
- check  $c\bar{c}$  spectrum



Baryonic  $c\bar{c}$ -like  
- 5 quarks

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*Part I: The news*

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# The first charmed-strange tetraquark

First strange charmonium-like tetraquark ...

BESIII [*PRL* 126, 102001 (2021)]

$e^+e^- \rightarrow K^+ Z_{cs}(3985)^- \rightarrow K^+ (D^*D_s^- \text{ and } D^-D_s^*)$



# The first charmed-strange tetraquark

... Soon after followed by other 2

BESIII [PRL 126, 102001 (2021)]

$e^+e^- \rightarrow K^+ Z_{cs}(3985)^- \rightarrow K^+ (D^*D_s^- \text{ and } D^-D_s^*)$



LHCb [PRL 127, 082001 (2021)]

$B^+ \rightarrow \Phi Z_{cs}(4220)^+ \rightarrow \Phi (K^+J/\psi)$



LHCb [PRL 127, 082001 (2021)]

$B^+ \rightarrow \Phi Z_{cs}(4000)^+ \rightarrow \Phi (K^+J/\psi)$



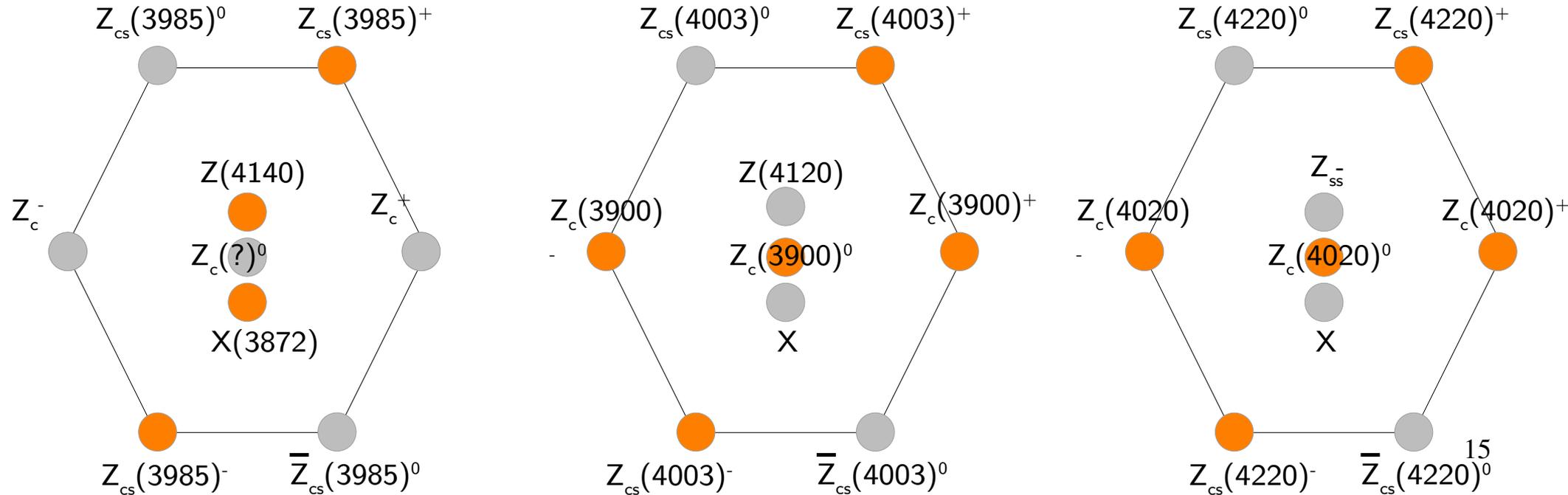
# The first charmed-strange tetraquark

Maiani et al, J. SCI.B. 2021 04 040 (2021)

## Di-quarks arrange to produce 3 S-wave nonets

- predictions about the mass of missing states is possible now
- Are we filling up the compact tetraquark nonets?

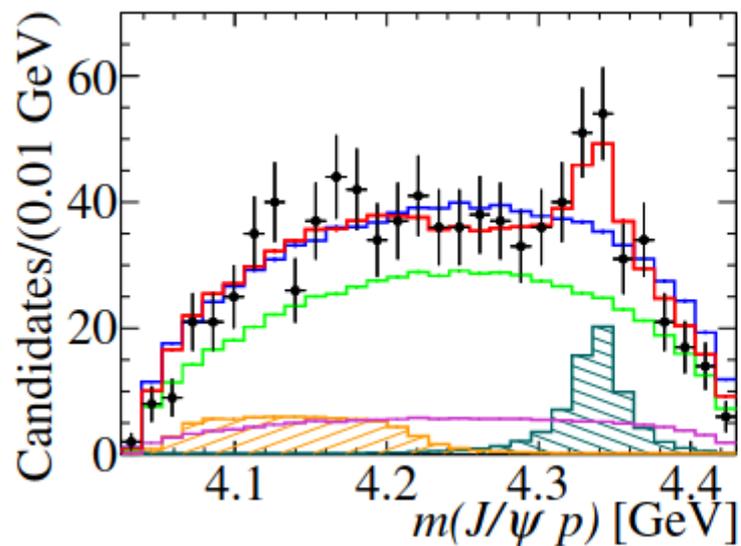
More on this later



# New pentaquarks (now with strangeness)

$$B_s \rightarrow J/\psi p p \bar{p}$$

[arXiv:2108.04720]

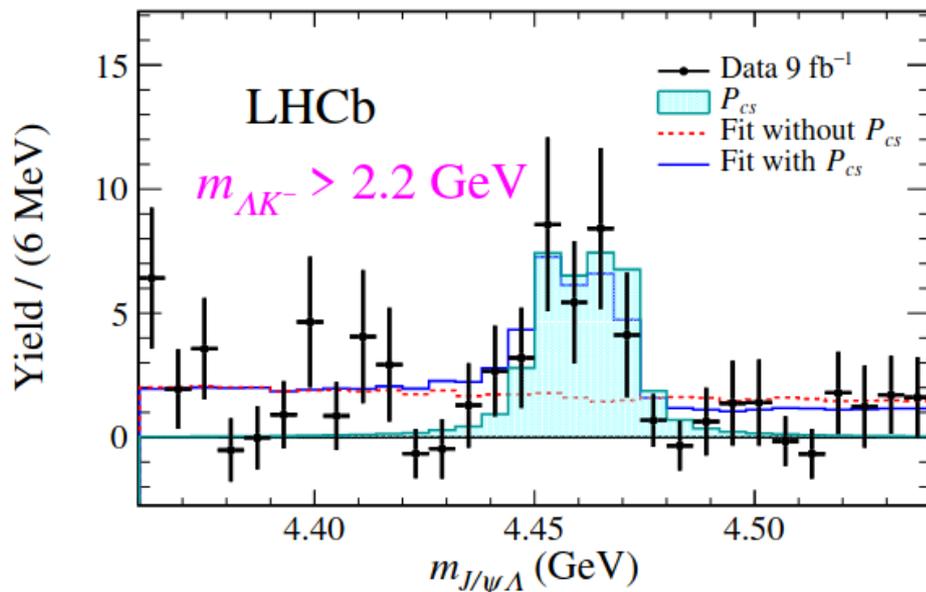


$P_c(4337)$

$J^{PC} = 1/2^+$  (probably)

$$\Xi_b \rightarrow J/\psi \Lambda K$$

[Sci.Bull. 66 (2021) 1278-1287]



$P_{cs}(4459)$

$J^{PC} = \text{unknown}$

# Fully-heavy states: $X(3900)$

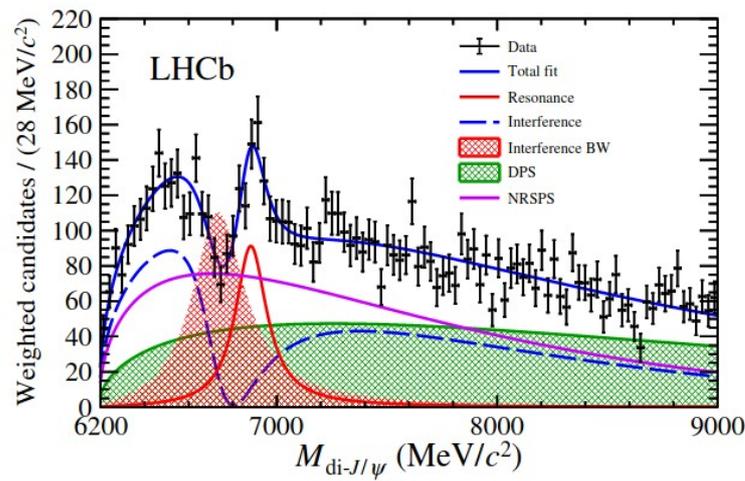
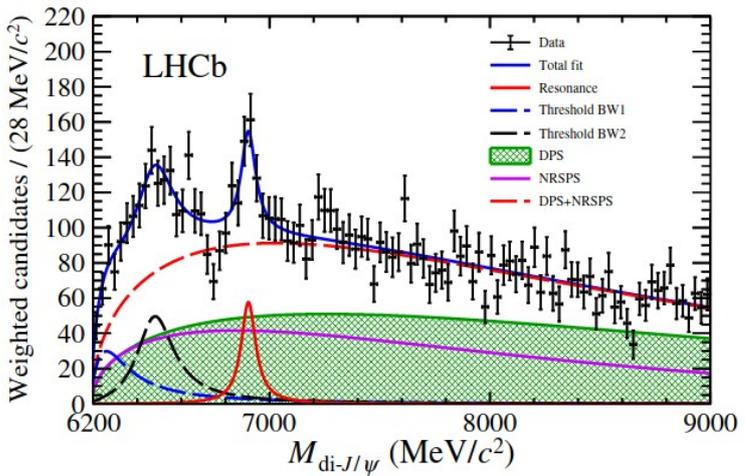
$$pp \rightarrow J/\psi J/\psi + X$$

[Sci. Bull. 65 1983 (2020)]

## Two structures in $M(J/\psi J/\psi)$

- Narrow  $X(6900)$
- Broad enhancement @ threshold

70+ theoretical interpretations



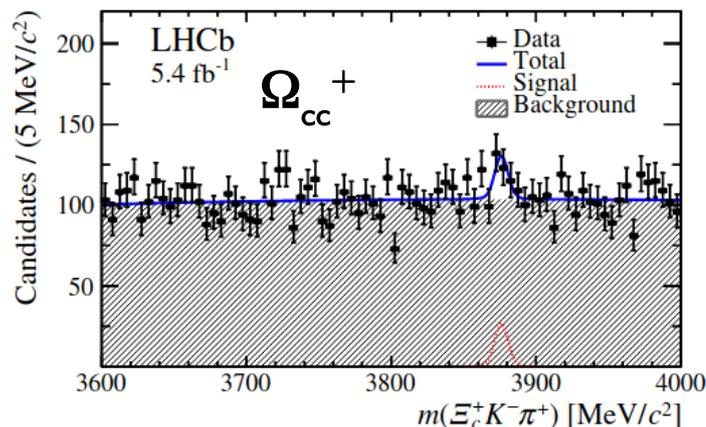
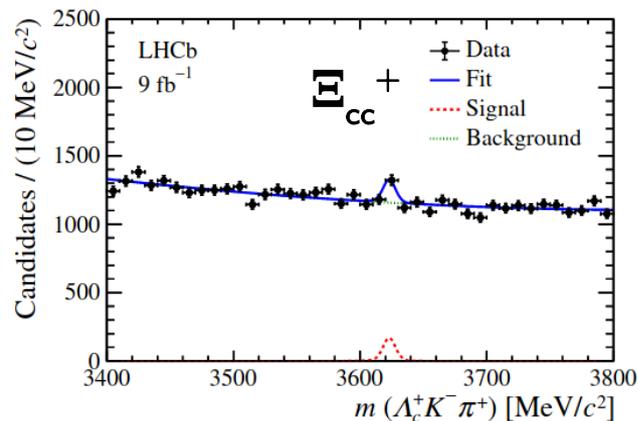
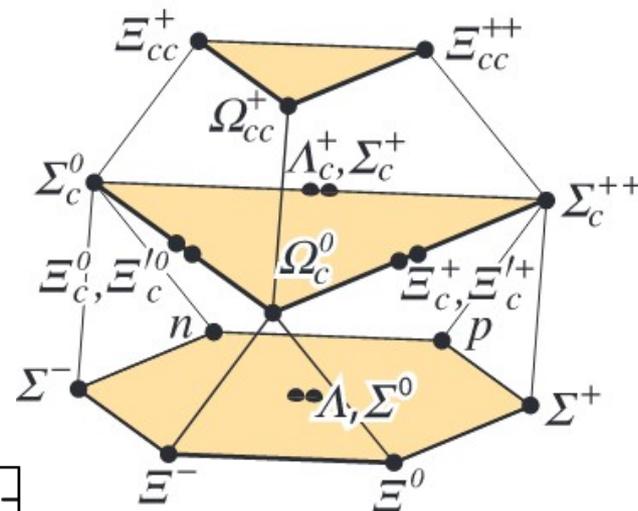
# Doubly-charmed objects

$\Xi_{cc}^{++}$  Observed in 2017

2021: First hints of  $\Omega_{cc}^+$  and  $\Xi_{cc}^+$

[Sci. China-Phys. Mech. Astron. 64, 101062 (2021)]

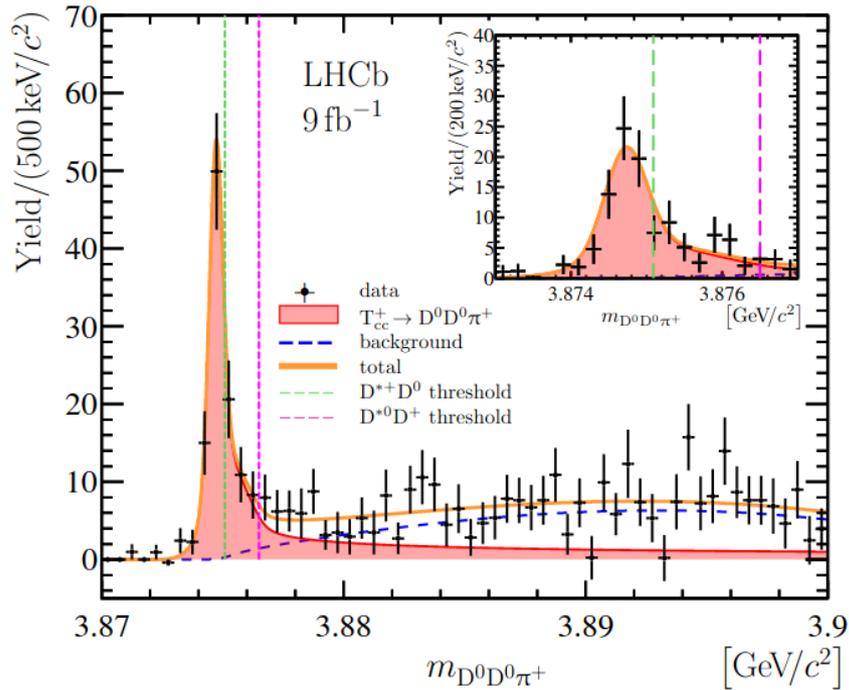
[arXiv:2109.07292]



More on this later

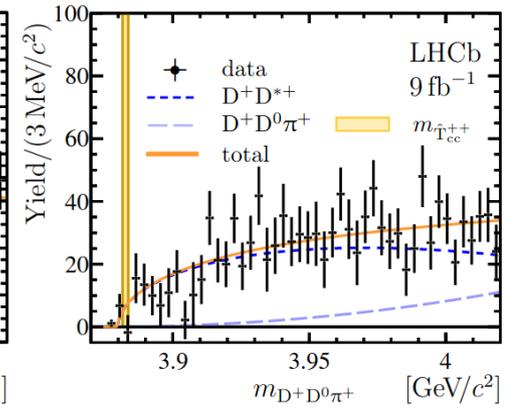
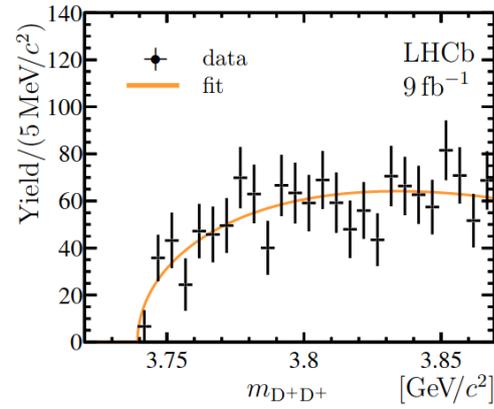
Prompt production of something decaying into  $(DD^*)^+$

[arXiv:2109:01038 and arXiv:2109:01056]



$J^{PC} = 1^+$  (probably)

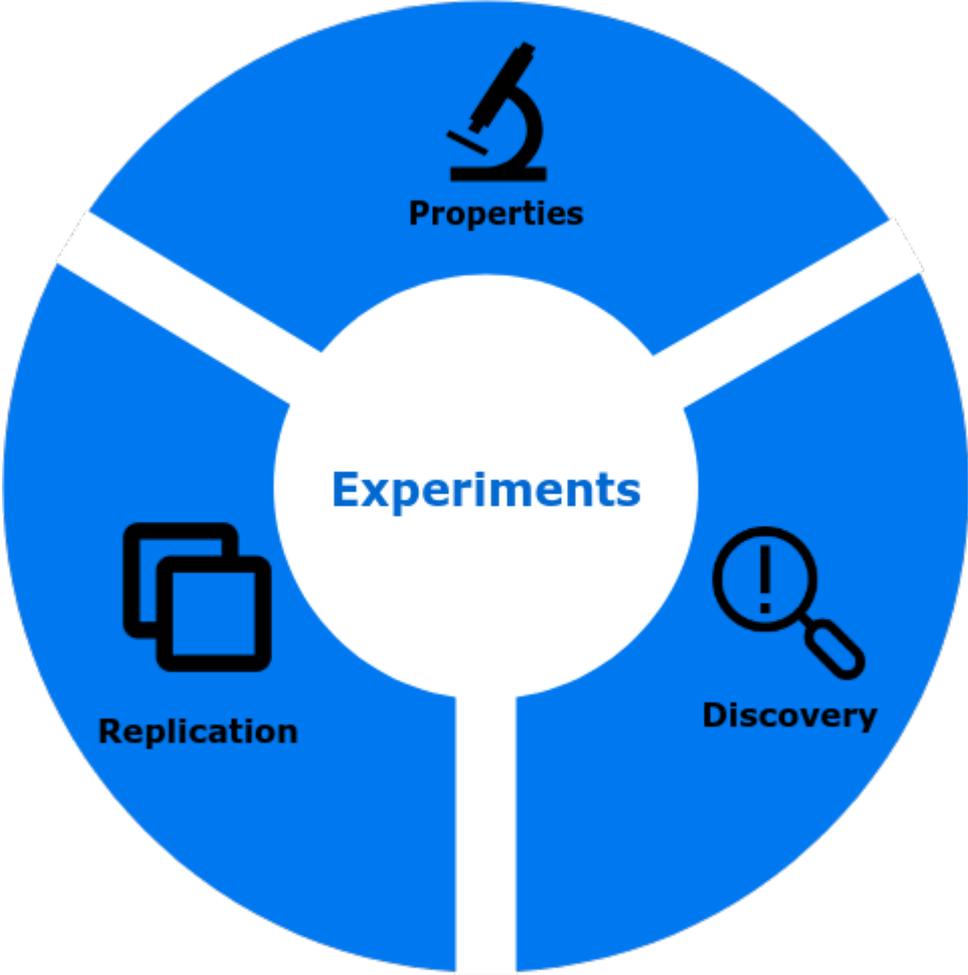
Nothing in the  $D^+D^+$  channel



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*Part II: The path forward*

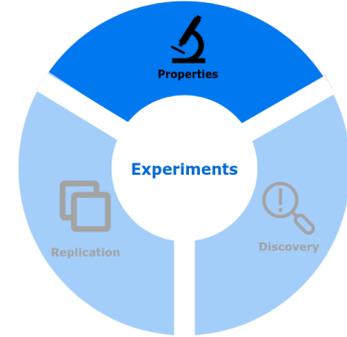
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# Mapping properties: $J^{PC}$

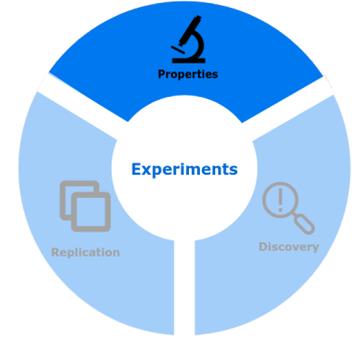
$J^{PC}$  is not directly measured for several of the most recent states

- pentaquarks: 0/5
- charmonium-like: 30/42 (inc. quark model assignments)
- heavy baryons: 28/52 (5/52 excl. quark model assignments)
- heavy mesons: 31/42 (inc. quark model assignments)
- bottomonium-like: 22/22 (inc. quark model assignments)



## Task

Determine  $J^{PC}$  for all  
known states

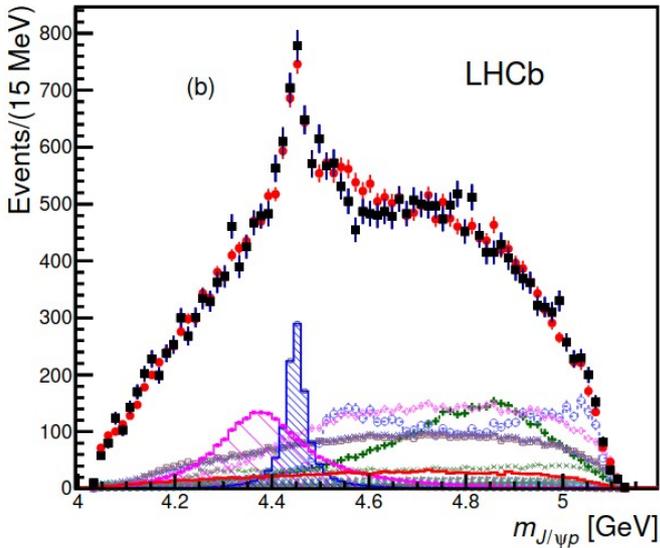


# $J^PC$ analysis: the pentaquark example

Amplitude analysis is challenging with narrow states

- Cannot neglect the resolution
- Fit computationally very demanding

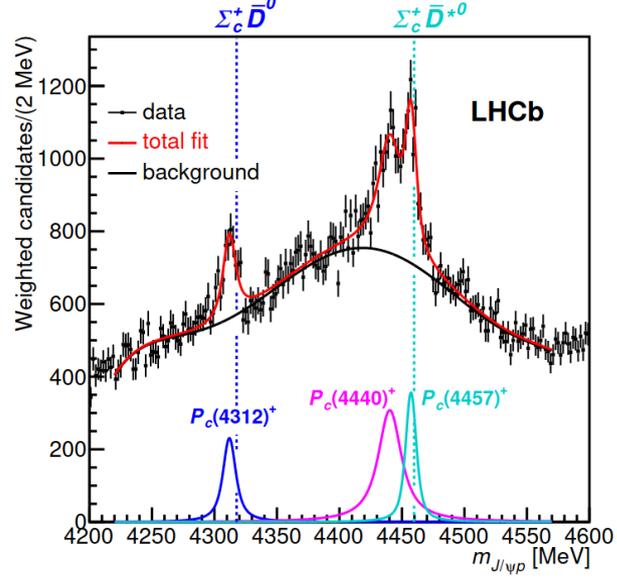
2015: two **broad** states



Assume  $\Gamma \gg$  resolution

- full fit in the first paper

2019: three **narrow** states



$\Gamma \sim$  resolution

- full fit still ongoing

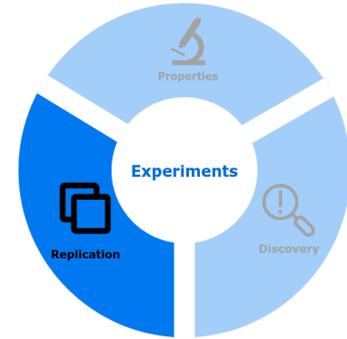
Same issues in Belle II!  
Common shared tools?

# Look for new states

Many states have been seen in either

- 1 decay mode only
- 1 production mode only
- 1 experiment only

Examples: all pentaquarks,  $T_{cc}$ ,  $Z_c(3900)$ ,  $\Xi_{cc}^{++} \dots$



## Task

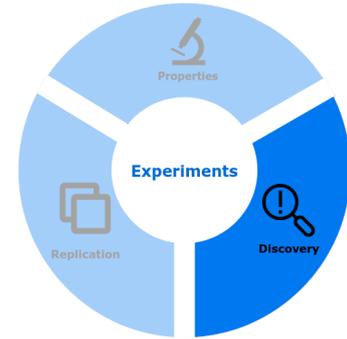
Look for known states where we have not seen them

(more or less) recent ideas to explore:

- Prompt production of exotica (4q/molecule)  
[EPJ C81, 669 (2021)]
- Photo-production of pentaquarks  
[PRD 101, 074010 (2020)]
- 4q in HI peripheral collisions  
[PRD 104, 114029 (2021)]

# Look for new states

Broad-band, serendipitous searches have been extremely rewarding



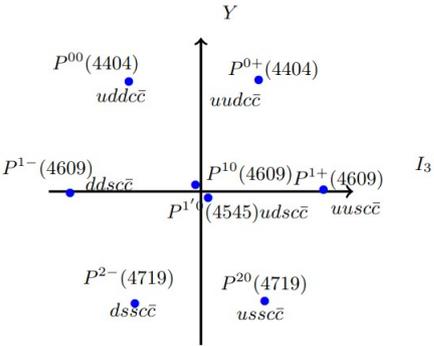
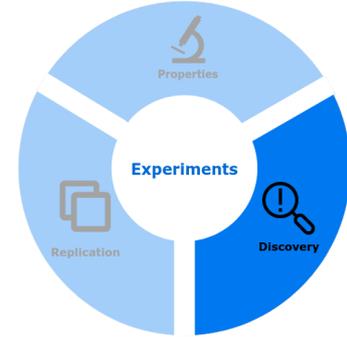
## Task

Keep up the good bump hunting!

# Look forward to: new pentaquarks

In di-quark models pentaquarks form octets and a decuplet

[PRD 96, 014014 (2017)], [PLB 749, 289-291 (2015)]



Possible discovery modes:

$$\Xi_b(5794) \rightarrow K (J/\Psi \Sigma(1385))$$

$$\Omega_b^-(6049) \rightarrow \phi (J/\Psi \Omega^-(1672))$$

$$\Omega_b^-(6049) \rightarrow K (J/\Psi \Xi(1387))$$

Molecular models also predict several states

[PRL 115, 122001 (2015)]

Channel	Minimum isospin	Minimal quark content <sup>a,b</sup>	Threshold (MeV) <sup>c</sup>	S-wave $J^P$	Example of decay mode
$\Sigma_c \bar{D}^*$	1/2	$c\bar{c}qqq'$	4462.4	$1/2^-, 3/2^-$	$J/\psi p$
$\Sigma_c B^*$	1/2	$c\bar{b}qqq'$	7779.5	$1/2^-, 3/2^-$	$B_c^+ p$
$\Sigma_b \bar{D}^*$	1/2	$b\bar{c}qqq'$	7823.0	$1/2^-, 3/2^-$	$B_c^- p$
$\Sigma_b B^*$	1/2	$b\bar{b}qqq'$	11139.6	$1/2^-, 3/2^-$	$\Upsilon(nS)p$

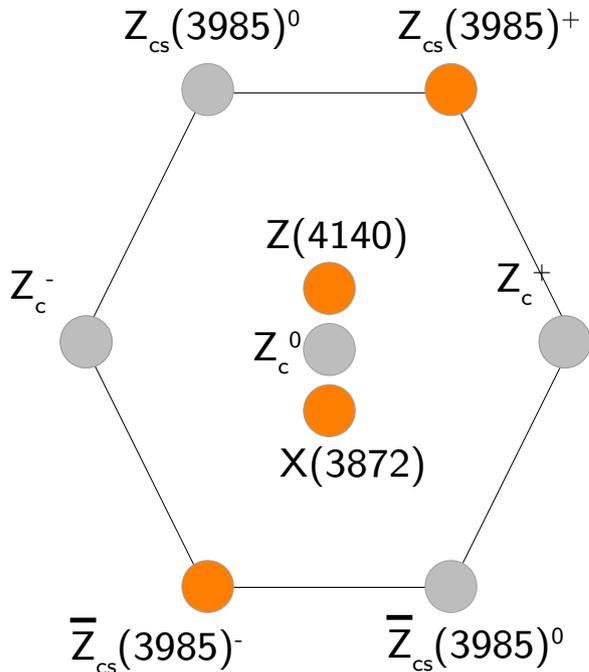
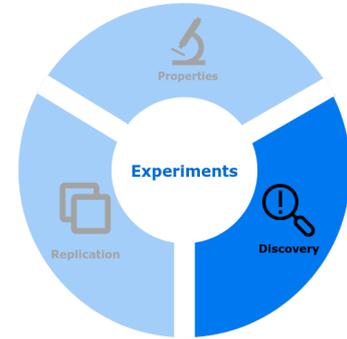
**Task**

Explore all  $J/\psi +$  baryon,  
 $B_c +$  baryon and  
 $\Upsilon(nS) +$  baryon spectra

# Look forward to: the $\bar{c}c\bar{q}q$ multiplets

## Unique prediction of the compact tetraquark model

[J. SCI.B. 2021 04 040 (2021)]



**WANTED**

*X(3872) isospin triplet*

*Z<sub>c</sub>(3900) isospin singlet*

*Neutral Z<sub>cs</sub>*

***Predictions on production rates needed***

# Look forward to: doubly-charmed objects

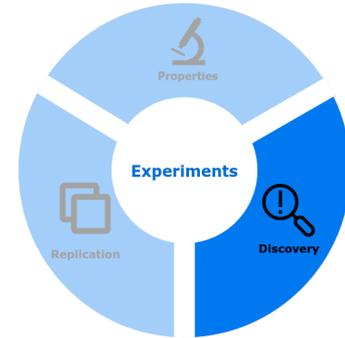
The  $\Xi_{cc}^{++}$  is a (simple) benchmark to understand the  $c$ - $c$  interaction

→ Can generalize to other  $cc+q$ ,  $qq$  hadrons (predict  $T_{cc}$  mass!)

[Karlner, Rosner, PRL 119, 202001 (2017)]

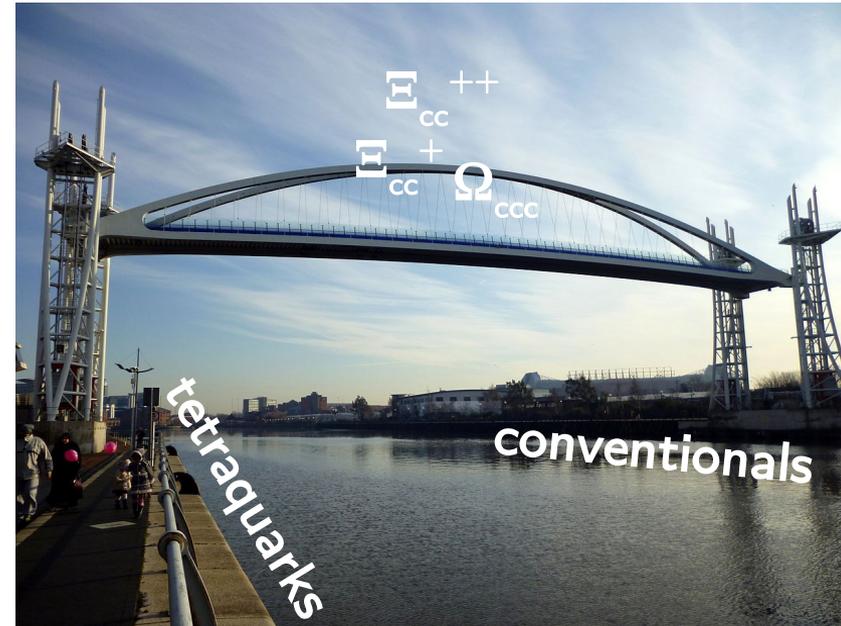
→ Successful history of predictions

[Karlner, Rosner, PRD 90, 094007 (2014)]



## Task

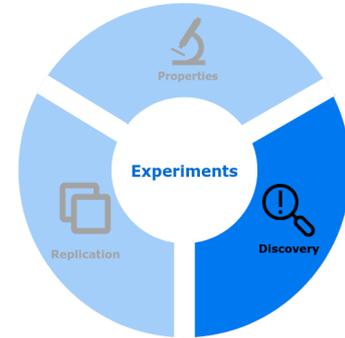
Complete the double-charmed baryons spectra and multiplets, look for more  $T_{cc}$



# Look forward to: hadrons with beauty

## Patterns seen with charm should repeat with b-quark

- Smaller relativistic corrections
- Stronger selection rules (Heavy quark spin symmetry...)



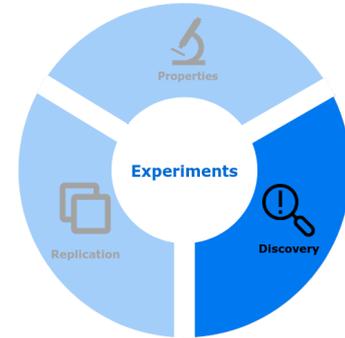
## Experimentally challenging

- Only prompt production at LHC
  - but  $\sigma_{\text{prompt}}[pp \rightarrow Y(1S)] \sim 0.0003 \times \sigma_{\text{prompt}}[pp \rightarrow J/\psi]$
- Can produce  $Y(nS) 1^-$  states at  $e^+e^-$ 
  - Strongly depend on the the BF for the  $Y(nS)$  to your state
  - $E_{\text{cm}}$  @ Belle II limited to  $\sim 11$  GeV ( threshold for  $T_{bb} \sim 19\text{-}20$  GeV)

# Look forward to: hadrons with beauty

Patterns seen with charm should repeat with b-quark

- Smaller relativistic corrections
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Experimentally ch

**B-hadrons are much less known  
than their charmed counterparts**

- Only prom
- but  $\sigma_{\text{prod}}$

- Can produce  $Y(nS) 1^-$  states at  $e^+e^-$ 
  - Strongly depend on the the BF for the  $Y(nS)$  to your state
  - $E_{\text{cm}}$  @ Belle II limited to  $\sim 11$  GeV ( threshold for  $T_{bb} \sim 19-20$  GeV)

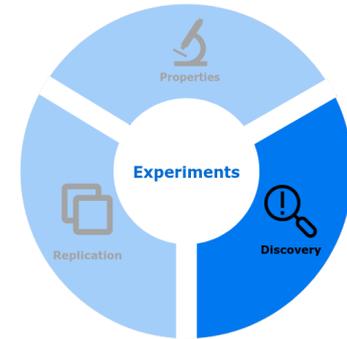
# Look forward to: hadrons with beauty

## For LHC(b) (run 3?)

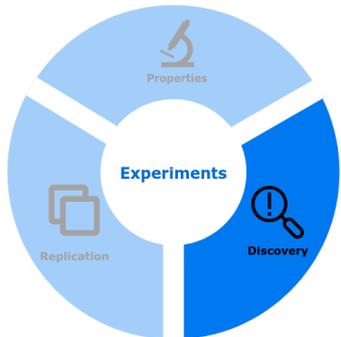
→ The  $T_{bb}^+$  could be stable against strong and EM decays!

*[PRL 119, 202001 (2017)] [PRL 119, 202002 (2017)]*

→ Doubly-b baryons, 4-b tetraquarks ...



# Look forward to: hadrons with beauty



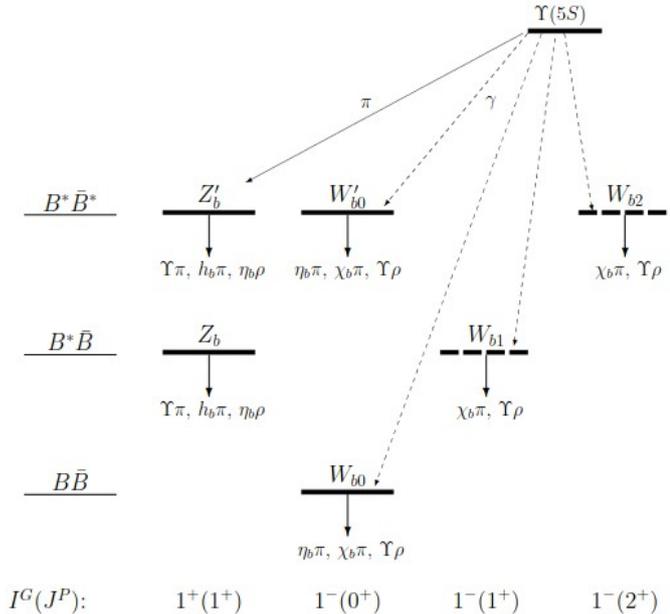
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 [PRL 119, 202001 (2017)] [PRL 119, 202002 (2017)]

→ Doubly-b baryons, 4-b tetraquarks ...

## For Belle II

→ 4-q states in  $Y(5S)$  radiative decays (2024+)  
 [PRD 84 031502], [Mod.Phys.Let.A 32, 1750025 (2017)]



# Look forward to: hadrons with beauty

## For LHC(b) (run 3?)

→ The  $T_{bb}^+$  could be stable against strong and EM decays!

[PRL 119, 202001 (2017)] [PRL 119, 202002 (2017)]

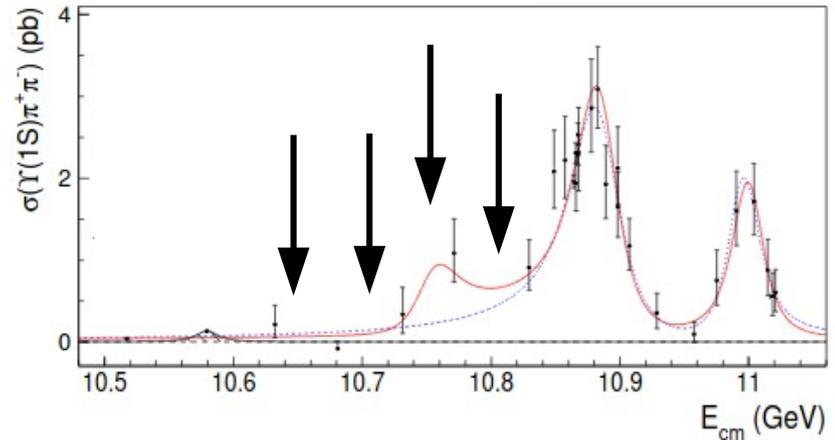
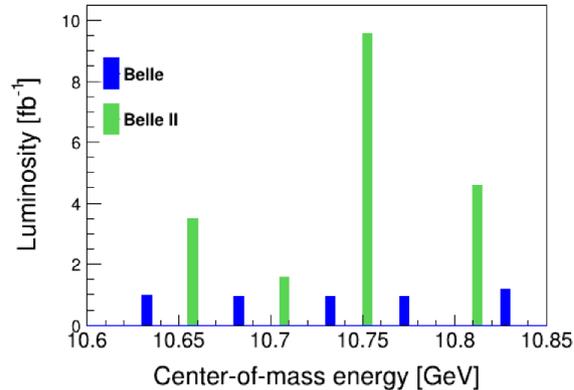
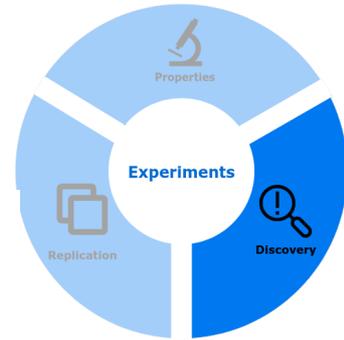
→ Doubly-b baryons, 4-b tetraquarks ...

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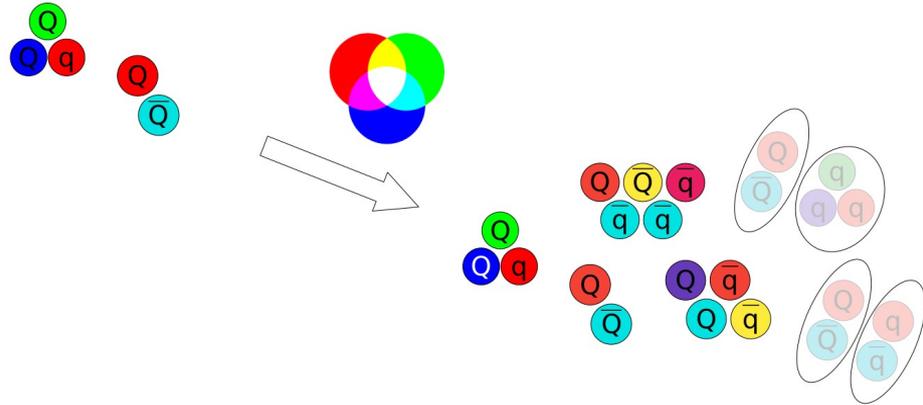
→ results of the scan at 10.750 GeV (2022!)



# Conclusions

The heavy hadrons gave us solid experimental evidences of exotic states

- $b\bar{b}$ ,  $c\bar{c}$ , and  $cc$  4-quark states
- $cc$ , pentaquarks



3(+) experiments are taking data

- LHCb, Belle II, BES III (CMS, CLAS...)

With more data we can (hopefully!) start constraining the theoretical models

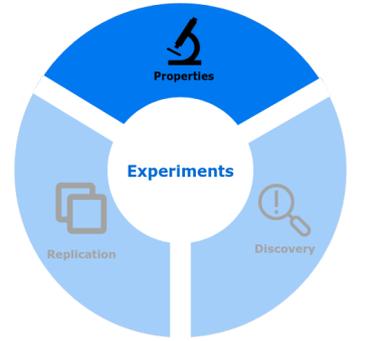
- Quantum numbers for all known states
- Doubly-heavy baryons and missing tetraquarks
- Beauty counterparts of charmed hadrons

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# *Backup*

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# Mapping properties: absolute BFs



$Z_c(3900)$  Decay Modes

When we observe a new state  $S$  we access

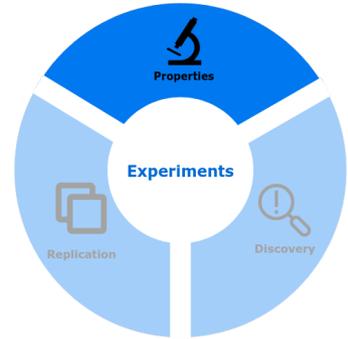
$$\text{Rate} = \sigma_{\text{production}}(S) \times \text{BF}(S \rightarrow \text{final state})$$

↑ Poorly (or not) constrained by theory

↙ Some (pre, post)dictions usually available

	Mode	Fraction ( $\Gamma_i / \Gamma$ )
$\Gamma_1$	$J/\psi\pi$	seen
$\Gamma_2$	$h_c\pi^\pm$	not seen
$\Gamma_3$	$\eta_c\pi^+\pi^-$	not seen
$\Gamma_4$	$\eta_c(1S)\rho(770)^\pm$	
$\Gamma_5$	$(D\bar{D}^*)^{+-}$	seen
$\Gamma_6$	$D^0D^{*-} + \text{c.c.}$	seen
$\Gamma_7$	$D^-D^{*0} + \text{c.c.}$	seen
$\Gamma_8$	$\omega\pi^\pm$	not seen
$\Gamma_9$	$J/\psi\eta$	not seen
$\Gamma_{10}$	$D^+D^{*-} + \text{c.c.}$	seen
$\Gamma_{11}$	$D^0\bar{D}^{*0} + \text{c.c.}$	seen

# Mapping properties: absolute BFs

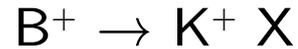
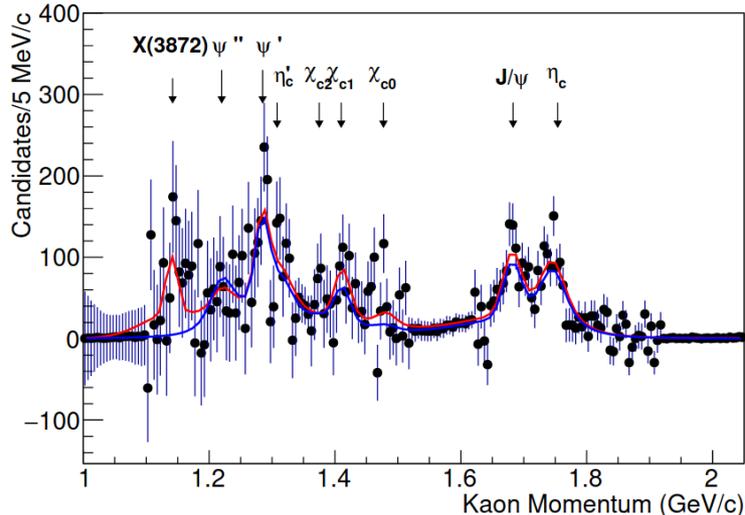


When we observe a new state  $S$  we access

$$\text{Rate} = \sigma_{\text{production}}(S) \times \text{BF}(S \rightarrow \text{final state})$$

Workaround: measure inclusive production BF from B mesons

[BaBar, PRL 124, 152001 (2020)]



- $X$  not reconstructed. Use  $K^+$  recoil
- Measure production BF

Next generation b-factories: use this method as much as possible

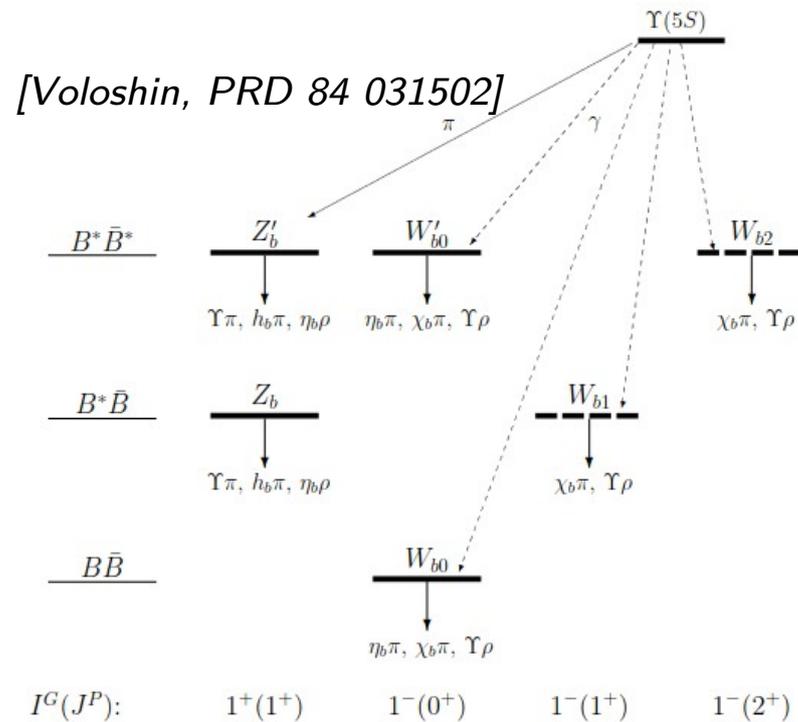
# Future challenges: hadrons with beauty

Exotic search with  $E_{cm} < 12$  GeV are challenging

→ rely on rare, soft EM transitions

[Ali et. Al., Prog. Part. Nucl. Phys. 97 (2017) 123-198]

Label	$J^{PC}$	charmonium-like		bottomonium-like	
		State	Mass [MeV]	State	Mass [MeV]
$X_0$	$0^{++}$	—	3756	—	10562
$X'_0$	$0^{++}$	—	4024	—	10652
$X_1$	$1^{++}$	$X(3872)$	3890	—	10607
$Z$	$1^{+-}$	$Z_c^+(3900)$	3890	$Z_b^{+,0}(10610)$	10607
$Z'$	$1^{+-}$	$Z_c^+(4020)$	4024	$Z_b^+(10650)$	10652
$X_2$	$2^{++}$	—	4024	—	10652
$Y_1$	$1^{--}$	$Y(4008)$	4024	$Y_b(10890)$	10891
$Y_2$	$1^{--}$	$Y(4260)$	4263	$\Upsilon(11020)$	10987
$Y_3$	$1^{--}$	$Y(4290)$ (or $Y(4220)$ )	4292	—	10981
$Y_4$	$1^{--}$	$Y(4630)$	4607	—	11135
$Y_5$	$1^{--}$	—	6472	—	13036

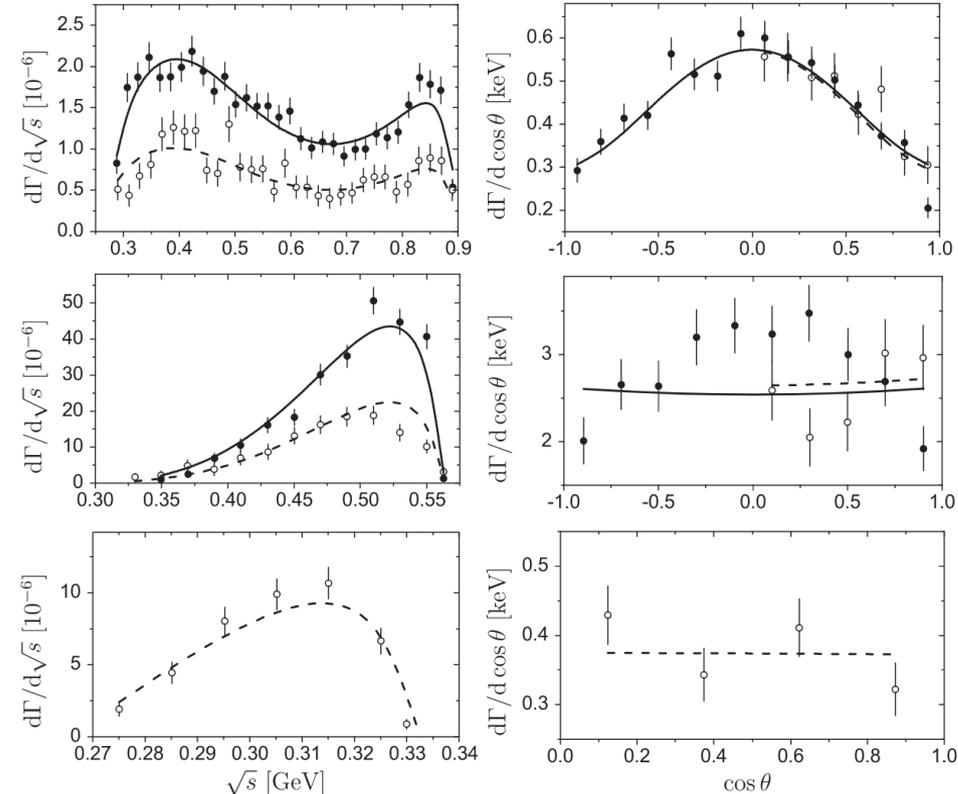
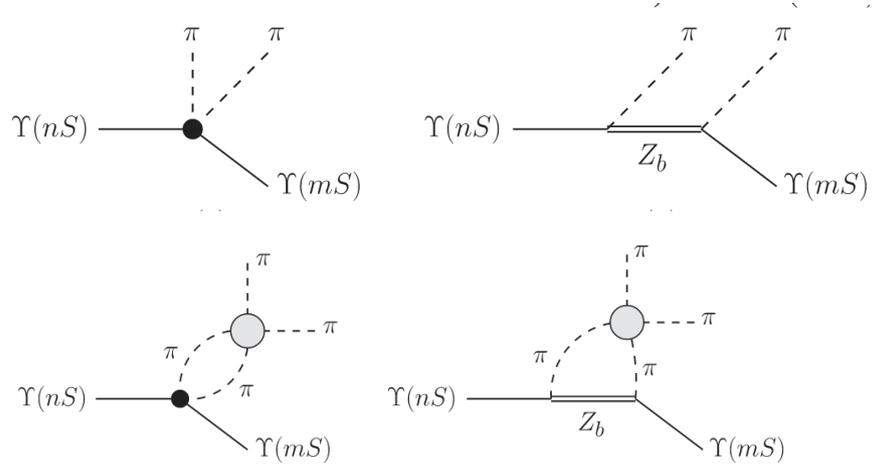


# Bottomonium: alternative approaches

Exotic stats contribute to the transitions from narrow quarkonia?

→ new (?) approach to heavy spectroscopy

Y.H. Chen et al, PRD93 (2016) 034030



# Why is bottomonium so special?

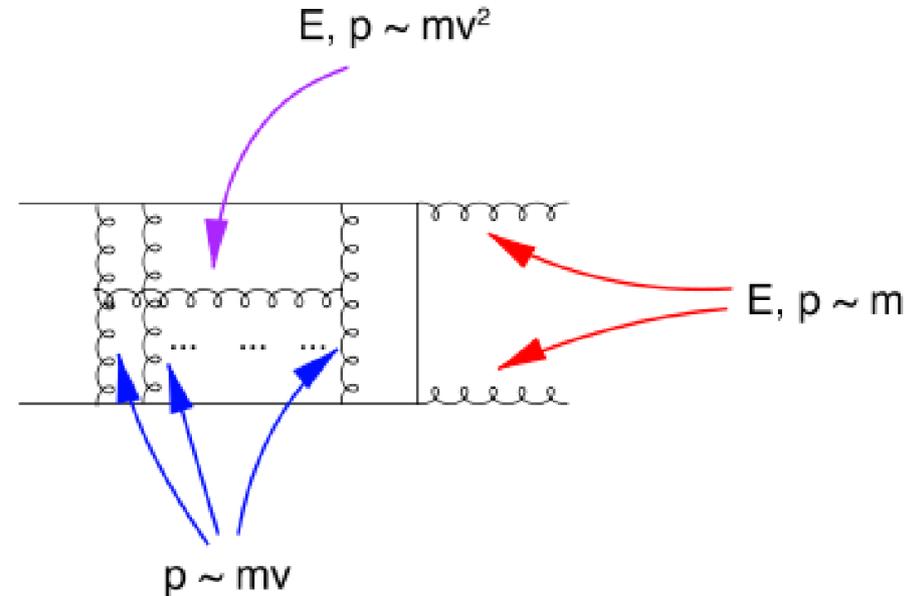
A clean spectrum is not the only distinctive feature

## → A QCD multi-scale system

- each feature is controlled by a different scale
- From perturbative to non-perturbative in one system!

## → A lepton-pair factory

- $BF(Y \rightarrow \ell\ell) \sim 2.5\%$
- (almost) purely EM process



# Charmonium at experiments

Charmonium is experimentally easy and accessible

→ Direct production in  $e^+e^-$  collisions  

→ Production in  $B \rightarrow K c\bar{c}$   

→ Photon-photon scattering  $\gamma\gamma^* \rightarrow (c\bar{c})$  

→ Double Charmonium  $e^+e^- \rightarrow (c\bar{c})(c\bar{c})$  

→ Prompt production    

→ Direct production in  $pp$   (???)

Bottom line: Charmonium will still be fully covered in the next 15 yrs.

# Bottomonium at experiments

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Bottomonium is much less accessible

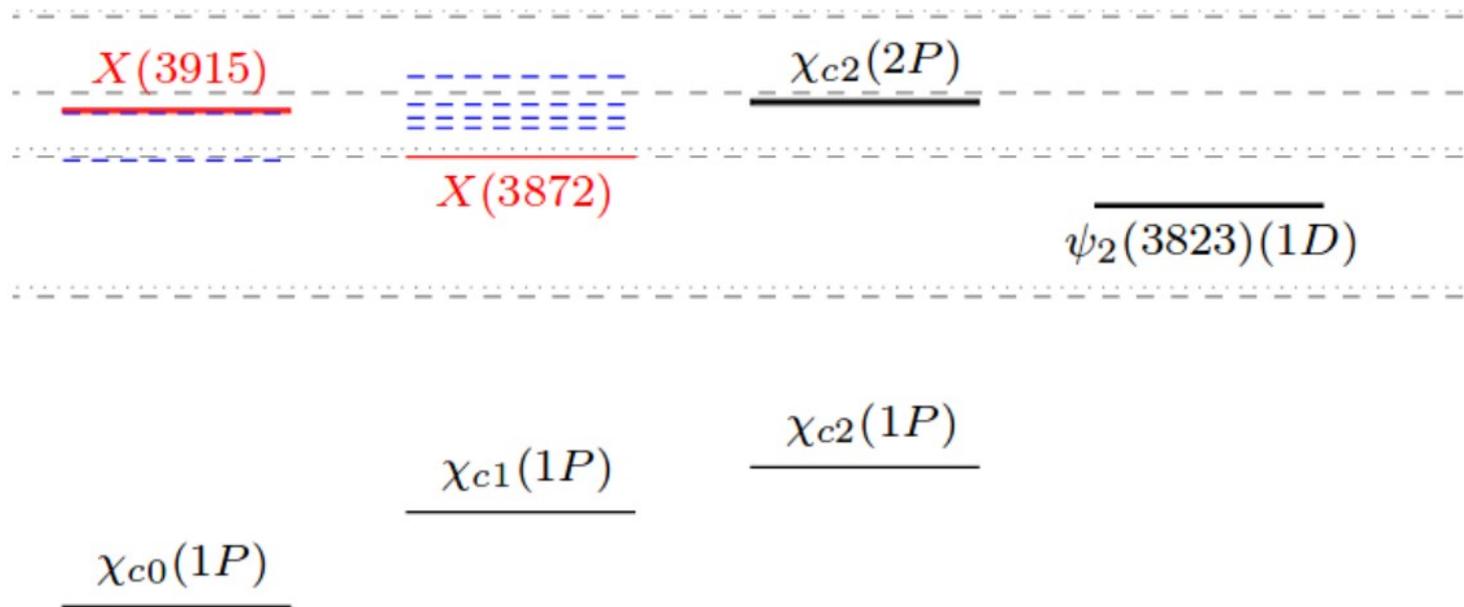
→ Direct production in  $e^+e^-$  collisions 

→ Prompt production    

Bottom line: after Belle II, bottomonium studies will have strong limitations

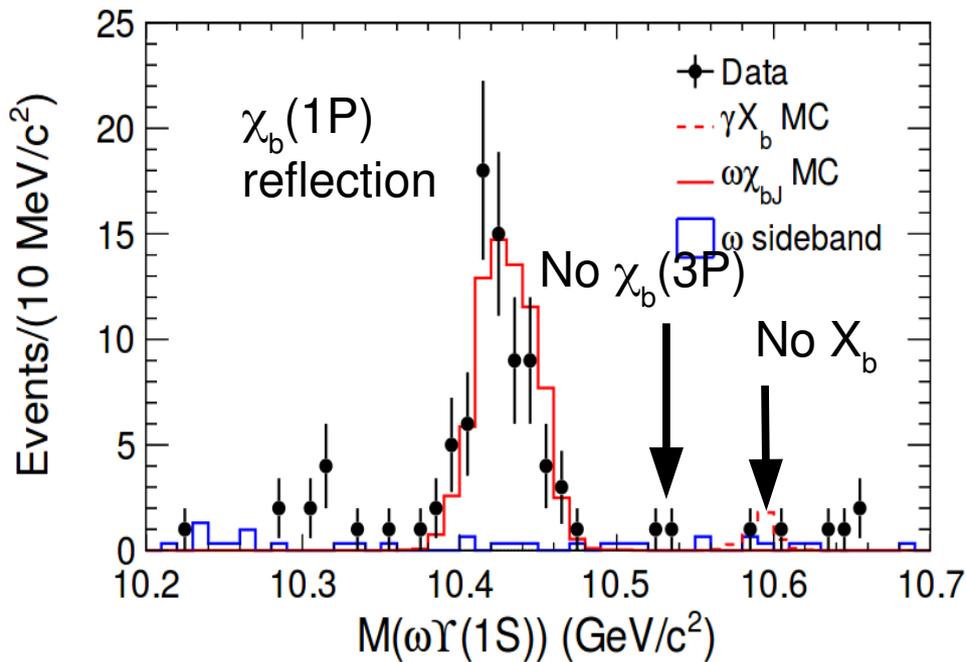
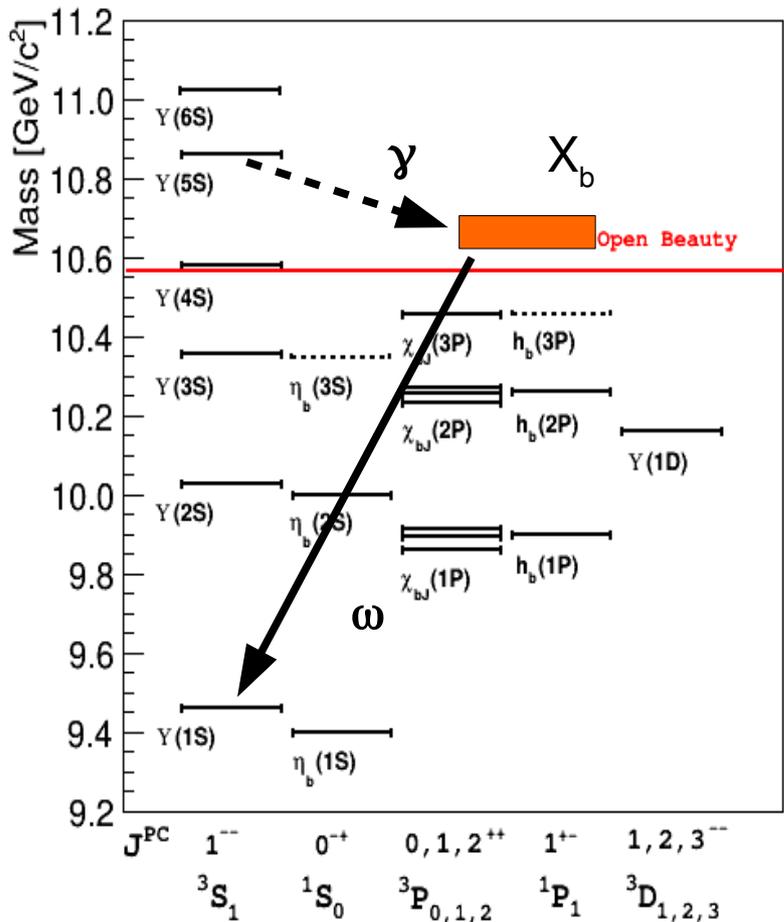
# Look for more patterns: the $X(3872)$

- The only exotica to have been observed in several different conditions
- A narrow peak  $\sim$  at the  $DD^*$  threshold
- Same quantum numbers as a  $\chi_{c1}(2P)$ , completely different properties



# Is there an $X(3872)$ counterpart?

Both tetraquark and pure molecule predict a counterpart ( $X_b$ )

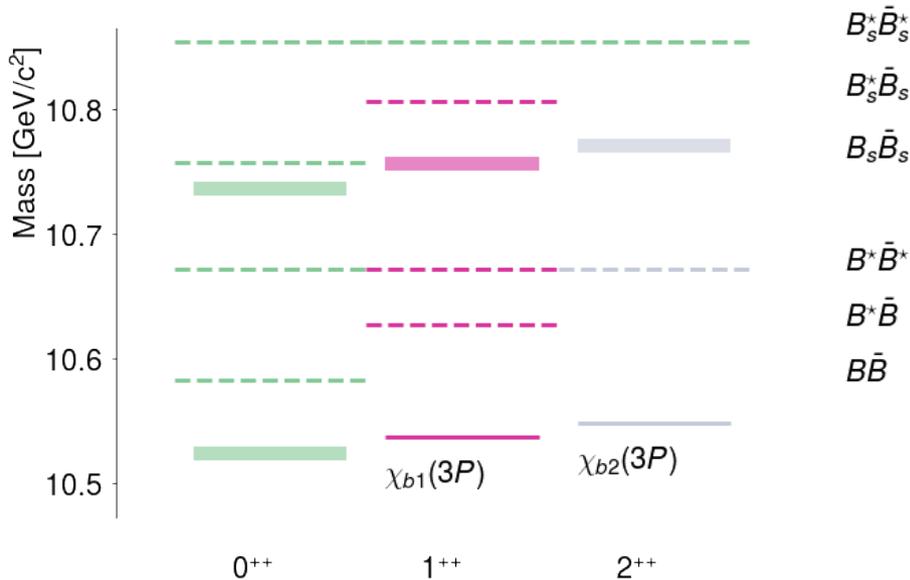
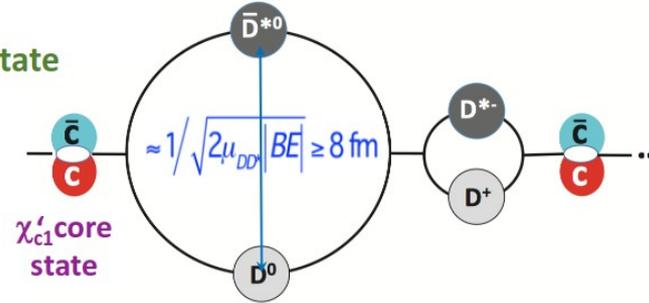


# Why no $X_b$ ?

The  $X(3872)$  may generated by a peculiar coincidence

$D\bar{D}^* \oplus \chi_{c1}'$  coupled channel state

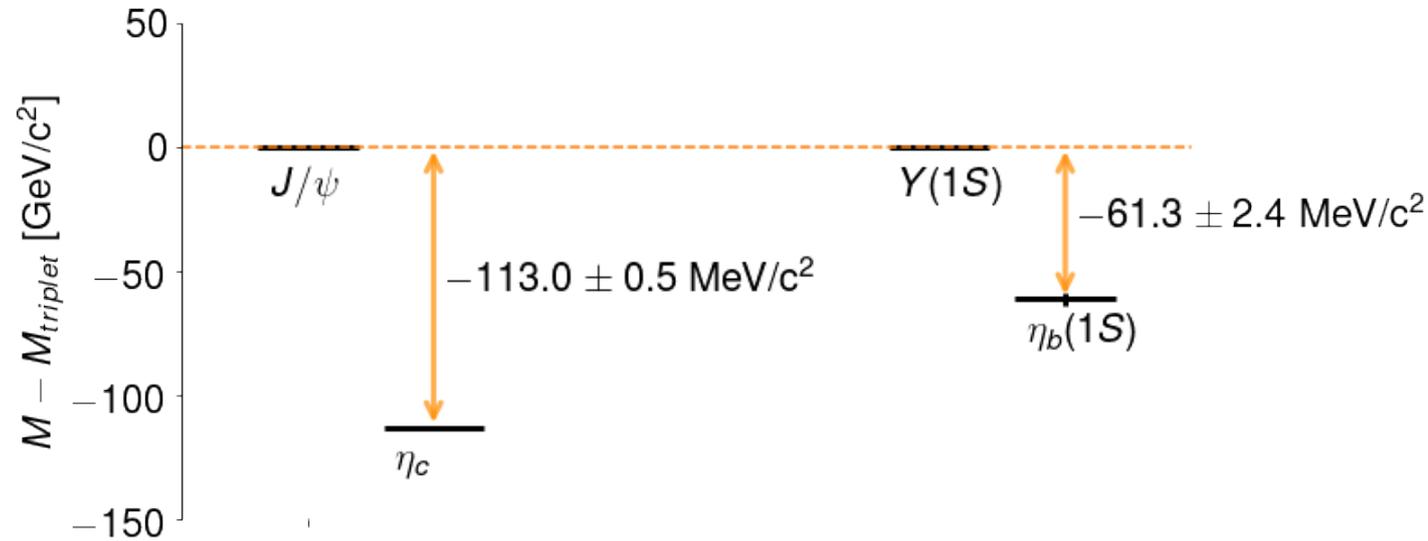
Specific model by  
Takizawa & Takeuchi, PTEP 9, 093D01



No  $\chi_b$  is near the  $BB^*$  threshold, no  $X_b$

Statistics in bottomonium is still too limited. **Need to set a stronger UL to rule out the  $X_b$  tetraquark hypothesis**

# The ground states

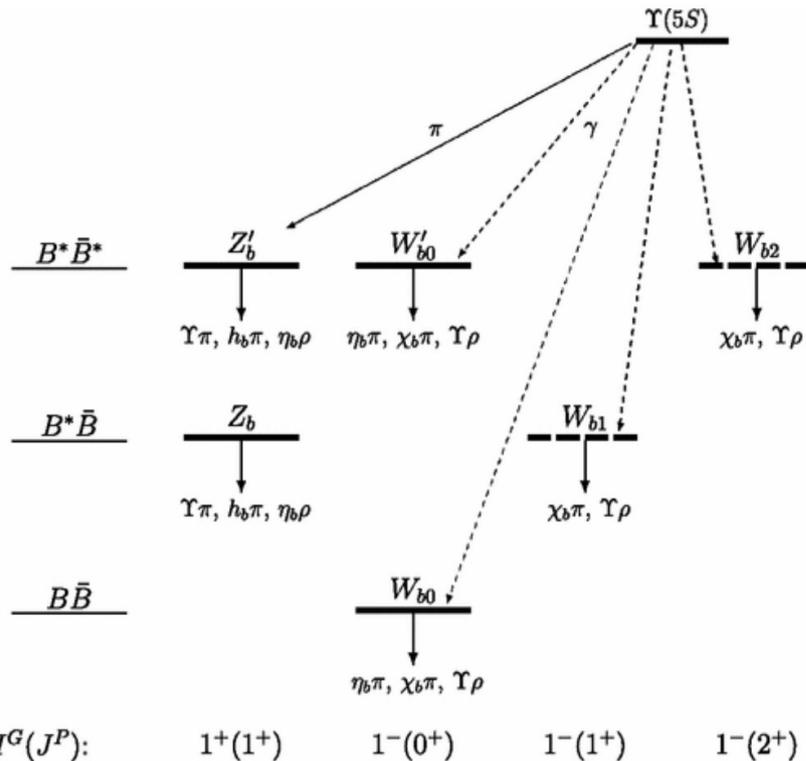


$$\begin{aligned}
 V_{spin}(r) = & \left( \frac{1}{2m_1^2} \vec{L} \cdot \vec{S}_1 + \frac{1}{2m_2^2} \vec{L} \cdot \vec{S}_2 \right) \frac{1}{r} \frac{d}{dr} (V(r) + 2V_1(r)) \\
 & + \frac{1}{m_1 m_2} \vec{L} \cdot (\vec{S}_1 + \vec{S}_2) \frac{1}{r} \frac{dV_2(r)}{dr} \\
 & + \frac{1}{m_1 m_2} (\hat{r} \cdot \vec{S}_1 \hat{r} \cdot \vec{S}_2 - \frac{1}{3} \vec{S}_1 \cdot \vec{S}_2) V_3(r) + \frac{1}{3m_1 m_2} \vec{S}_1 \cdot \vec{S}_2 V_4(r)
 \end{aligned}$$

# $Y(5S)$ and $Y(6S)$ : new exotica

→ If the  $Z_b$  is a loosely bound state, then several other molecules must appear

→ No predictions on the production rates



*Mod. Phys. Lett. A 32, 1750025 (2017)*

$I^G(J^P)$	Name	Composition	Co-produced particles [Threshold, GeV/ $c^2$ ]	Decay channels
$1^+(1^+)$	$Z_b$	$B\bar{B}^*$	$\pi$ [10.75]	$\Upsilon(nS)\pi, h_b(nP)\pi, \eta_b(nS)\rho$
$1^+(1^+)$	$Z'_b$	$B^*\bar{B}^*$	$\pi$ [10.79]	$\Upsilon(nS)\pi, h_b(nP)\pi, \eta_b(nS)\rho$
$1^-(0^+)$	$W_{b0}$	$B\bar{B}$	$\rho$ [11.34], $\gamma$ [10.56]	$\Upsilon(nS)\rho, \eta_b(nS)\pi$
$1^-(0^+)$	$W'_{b0}$	$B^*\bar{B}^*$	$\rho$ [11.43], $\gamma$ [10.65]	$\Upsilon(nS)\rho, \eta_b(nS)\pi$
$1^-(1^+)$	$W_{b1}$	$B\bar{B}^*$	$\rho$ [11.38], $\gamma$ [10.61]	$\Upsilon(nS)\rho$
$1^-(2^+)$	$W_{b2}$	$B^*\bar{B}^*$	$\rho$ [11.43], $\gamma$ [10.65]	$\Upsilon(nS)\rho$
$0^-(1^+)$	$X_{b1}$	$B\bar{B}^*$	$\eta$ [11.15]	$\Upsilon(nS)\eta, \eta_b(nS)\omega$
$0^-(1^+)$	$X'_{b1}$	$B^*\bar{B}^*$	$\eta$ [11.20]	$\Upsilon(nS)\eta, \eta_b(nS)\omega$
$0^+(0^+)$	$X_{b0}$	$B\bar{B}$	$\omega$ [11.34], $\gamma$ [10.56]	$\Upsilon(nS)\omega, \eta_b(nS)\eta$
$0^+(0^+)$	$X'_{b0}$	$B^*\bar{B}^*$	$\omega$ [11.43], $\gamma$ [10.65]	$\Upsilon(nS)\omega, \eta_b(nS)\eta$
$0^+(1^+)$	$X_b$	$B\bar{B}^*$	$\omega$ [11.39], $\gamma$ [10.61]	$\Upsilon(nS)\omega$
$0^+(2^+)$	$X_{b2}$	$B^*\bar{B}^*$	$\omega$ [11.43], $\gamma$ [10.65]	$\Upsilon(nS)\omega$

# Charmonium in bottomonium

Lots of observation of exotica, but quite few completely independent confirmations

→ Only X(3872) has been seen in prompt production ( in  $p\bar{p}$  and  $pp$  collisions)

Based on *Phys. Rev. D* 93, 112013 [Belle]

