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Polarized PDFs and Higher Twist in the Light of the Recent CLAS and COMPASS Data

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OUTLINE

- Method of analysis – **higher twist** corrections are taken into account
- Two **new** sets of very precise data on **inclusive** polarized DIS are included in the analysis

- **low Q^2** CLAS data

- COMPASS data mainly at **large Q^2**

*Very different
kinematic regions*



- Impact of the **new** data on **LSS'05 polarized PD** and **HT**
- The sign of the gluon polarization
- Summary

*LSS: hep-ph/0612360
(PR D75, 2007)*

Theory

In QCD

$$g_1(x, Q^2) = g_1(x, Q^2)_{LT} + g_1(x, Q^2)_{HT}$$

$$g_1(x, Q^2)_{LT} = g_1(x, Q^2)_{pQCD} + \frac{M^2}{Q^2} h^{TMC}(x, Q^2) + O\left(\frac{M^4}{Q^4}\right)$$

$$g_1(x, Q^2)_{HT} = h(x, Q^2) / Q^2 + O\left(\frac{\Lambda^4}{Q^4}\right)$$

dynamical HT power in Λ^2/Q^2 corrections ($\tau=3,4$)
 \Rightarrow non-perturbative effects (model dependent)

target mass corrections
which are calculable
A. Piccione, G. Ridolfi

In NLO pQCD

$$g_1(x, Q^2)_{pQCD} = \frac{1}{2} \sum_q^{N_f} e_q^2 [(\Delta q + \Delta \bar{q}) \otimes (1 + \frac{\alpha_s(Q^2)}{2\pi} \delta C_q) + \frac{\alpha_s(Q^2)}{2\pi} \Delta G \otimes \frac{\delta C_G}{N_f}]$$

$\delta C_q, \delta C_G$ – Wilson coefficient functions

polarized PD evolve in Q^2

according to **NLO DGLAP** eqs.

$N_f (=3)$ - the number of flavors

- An important difference between the kinematic regions of the unpolarized and **polarized** data sets
- A lot of the present data are at **moderate** Q^2 and W^2 :

$$Q^2 \approx 1-5 \text{ GeV}^2, \quad 4 < W^2 < 10 \text{ GeV}^2$$

*preasymptotic
region*

While in the determination of the PD in the unpolarized case we can cut the low Q^2 and W^2 data in order to eliminate the less known non-perturbative HT effects, it is **impossible** to perform such a procedure for the present data on the spin-dependent structure functions without losing too much information.

$$\alpha(\Lambda^2/Q^2)$$

➡ HT corrections have to be **accounted for**
in **polarized** DIS !

Method of analysis

$$\left[\frac{g_1(x, Q^2)}{F_1(x, Q^2)} \right]_{\text{exp}} \xleftrightarrow{\chi^2} \frac{g_1(x, Q^2)_{\text{LT}} + h^{g_1}(x)/Q^2}{F_1(x, Q^2)_{\text{exp}}}$$

$F_2^{\text{NMC}}, R_{1998}(\text{SLAC})$

in model independent way

Input PD

$$\Delta f_i(x, Q_0^2) = A_i x^{\alpha_i} f_i^{\text{MRST}}(x, Q_0^2) \quad Q_0^2 = 1 \text{ GeV}^2, A_i, \alpha_i - \text{free par.}$$

$h^p(x_i), h^n(x_i) - 10 \text{ parameters } (i = 1, 2, \dots, 5) \text{ to be determined from a fit to the data}$

8-2(SR) = 6 par. associated with PD; positivity bounds imposed by **MRST'02** unpol. PD

SUM



RULES

$$a_3 = g_A = (\Delta u + \Delta \bar{u})(Q^2) - (\Delta d + \Delta \bar{d})(Q^2) = F - D = 1.2670 \pm 0.0035$$

$$a_8 = (\Delta u + \Delta \bar{u})(Q^2) + (\Delta d + \Delta \bar{d})(Q^2) - 2(\Delta s + \Delta \bar{s})(Q^2) = 3F - D = 0.585 \pm 0.025$$

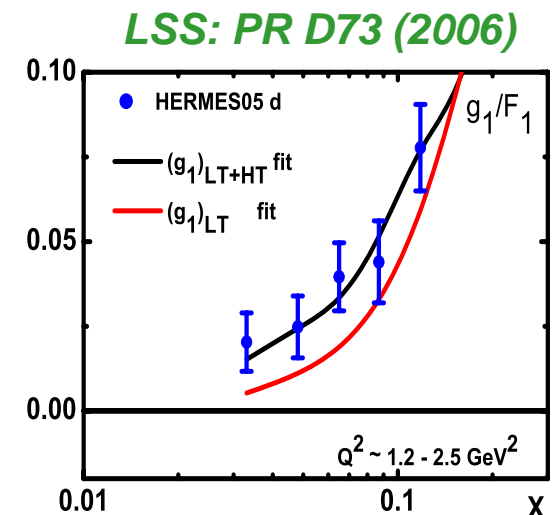
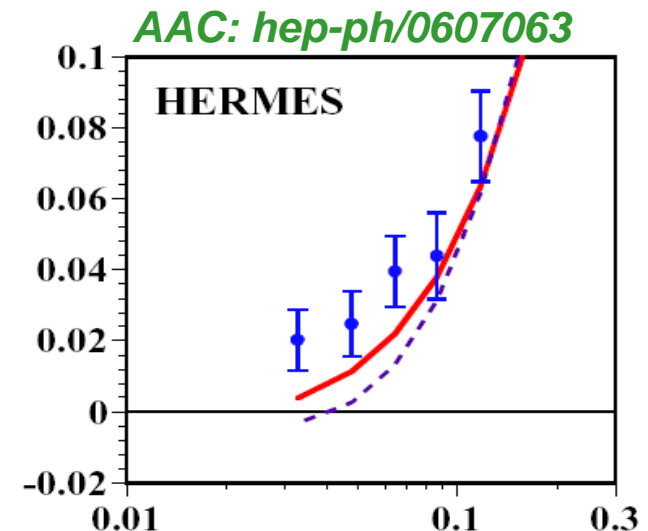
Flavor symmetric sea convention: $\Delta u_{\text{sea}} = \Delta \bar{u} = \Delta d_{\text{sea}} = \Delta \bar{d} = \Delta s = \Delta \bar{s}$

Higher twist effects

(CLAS'06 and COMPASS'06 not included)

$$g_1 = (g_1)_{LT} + h^{g_1}(x)/Q^2$$

- The low x and low Q^2 (**1.2 ~ 2.5 GeV²**) HERMES/d data (*PR D71, 2005*) can **not** be described by the **LT** (logarithmic in Q^2) term in $g_1 \Rightarrow$ **red curves**
- Excellent agreement with the data if the **HT corrections** to g_1 are taken into account in the analysis



DATA
(old set)

CERN **EMC** - A_1^p **SMC** - A_1^p, A_1^d **COMPASS'05** - A_1^d

DESY **HERMES** - $\frac{g_1^p}{F_1^p}, \frac{g_1^d}{F_1^d}$

SLAC **E142, E154** - A_1^n **E143, E155** - $\frac{g_1^p}{F_1^p}, \frac{g_1^d}{F_1^d}$

JLab **Hall A** - $\frac{g_1^n}{F_1^n}$

$$A_1^N \approx (1 + \gamma^2) \frac{g_1^N}{F_1^N}$$

$\gamma^2 = 4M^2 x^2 / Q^2$ - kinematic factor

Number of exp. points: **190**



LSS'05 polarized PD and HT (*PR D73, 2006*)

DATA

CERN **EMC** - A_1^p **SMC** - A_1^p, A_1^d **COMPASS'05** - A_1^d

DESY **HERMES** - $\frac{g_1^p}{F_1^p}, \frac{g_1^d}{F_1^d}$

SLAC **E142, E154** - A_1^n **E143, E155** - $\frac{g_1^p}{F_1^p}, \frac{g_1^d}{F_1^d}$

JLab **Hall A** - $\frac{g_1^n}{F_1^n}$ **CLAS'06** - $\frac{g_1^p}{F_1^p}, \frac{g_1^d}{F_1^d}$

$$A_1^N \approx (1 + \gamma^2) \frac{g_1^N}{F_1^N}$$

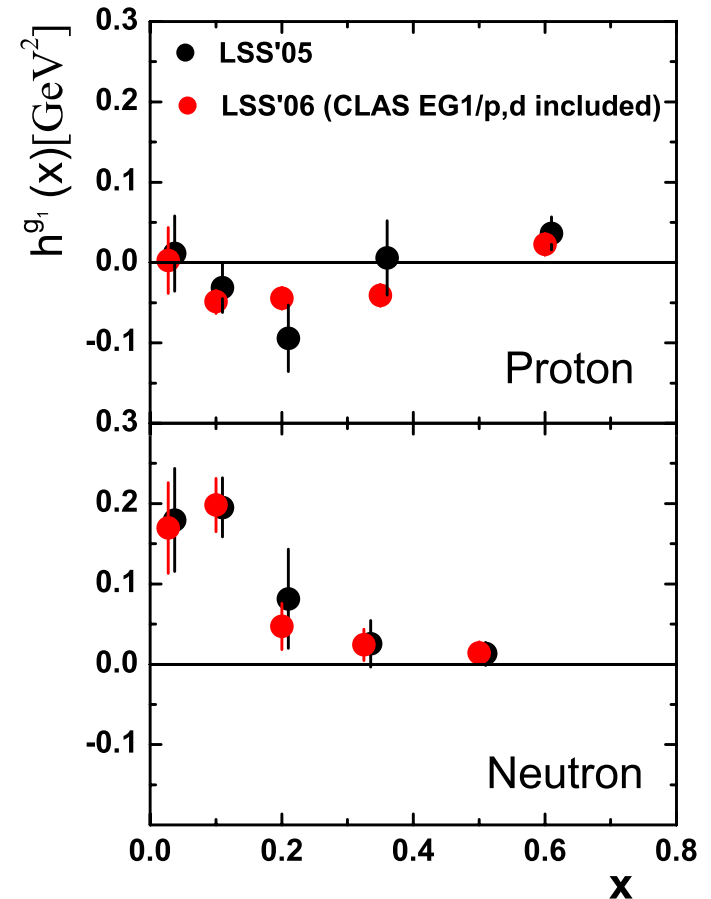
$\gamma^2 = 4M^2 x^2 / Q^2$ - kinematic factor

Number of exp. points: **190**  **823**

Effect of CLAS'06 p and d data (*PL B641, 11, 2006*) on polarized PD and HT

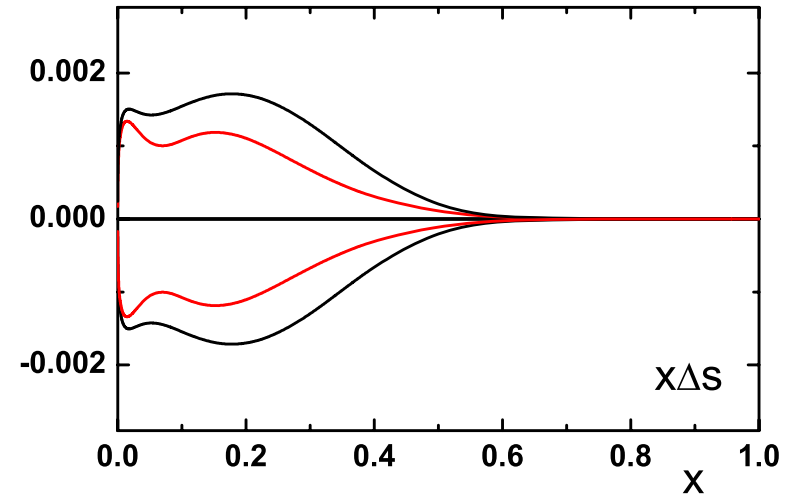
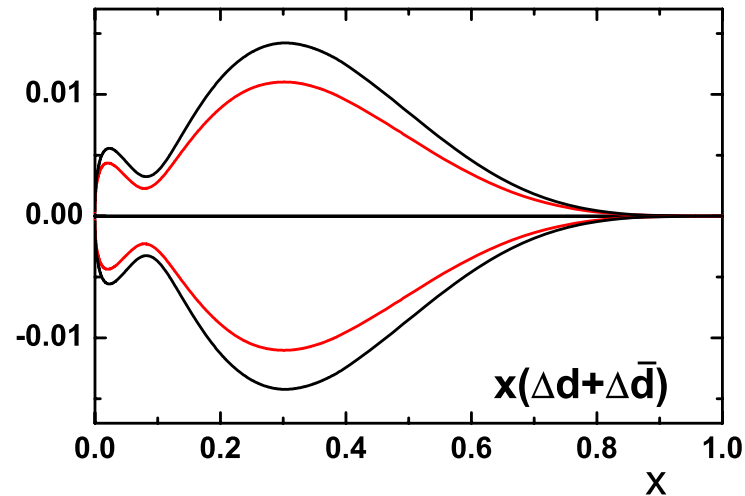
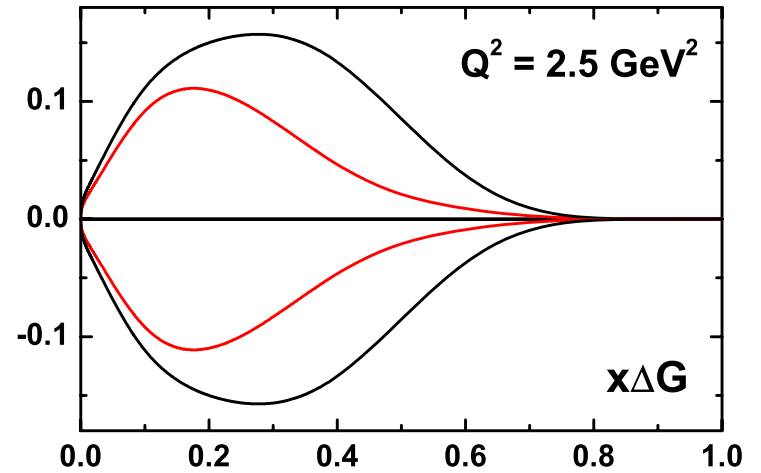
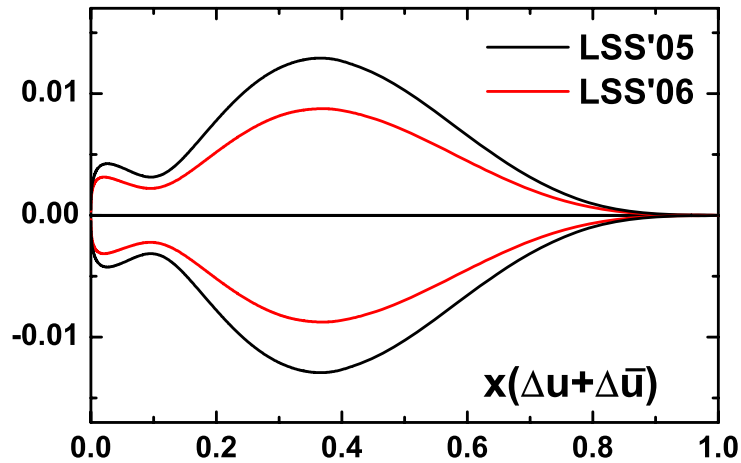
- Very accurate data on g_1^p and g_1^d at **low** Q^2 : **1~4 GeV²** for **$x \sim 0.1 - 0.6$** (**$W > 2$ GeV**)
- The determination of HT/p and HT/n is **significantly improved** in the *CLAS* x region compared to HT(LSS'05)
- As expected, the central values of PPD are practically **not** affected by *CLAS* data, **BUT** the accuracy of its determination is **essentially improved** (**a consequence** of much better determination of HT corrections to g_1)

LSS'05: PR D73 (2006)

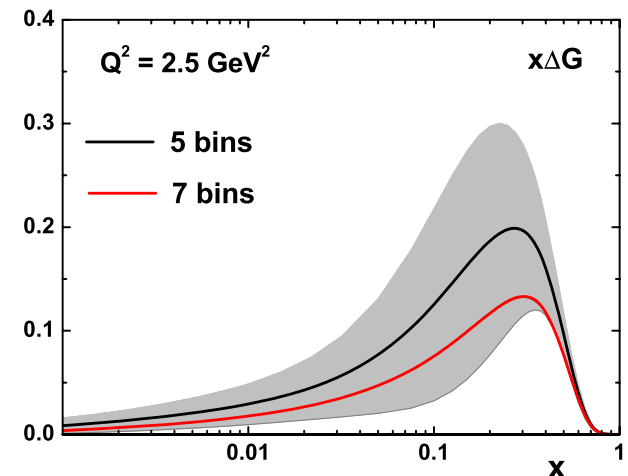
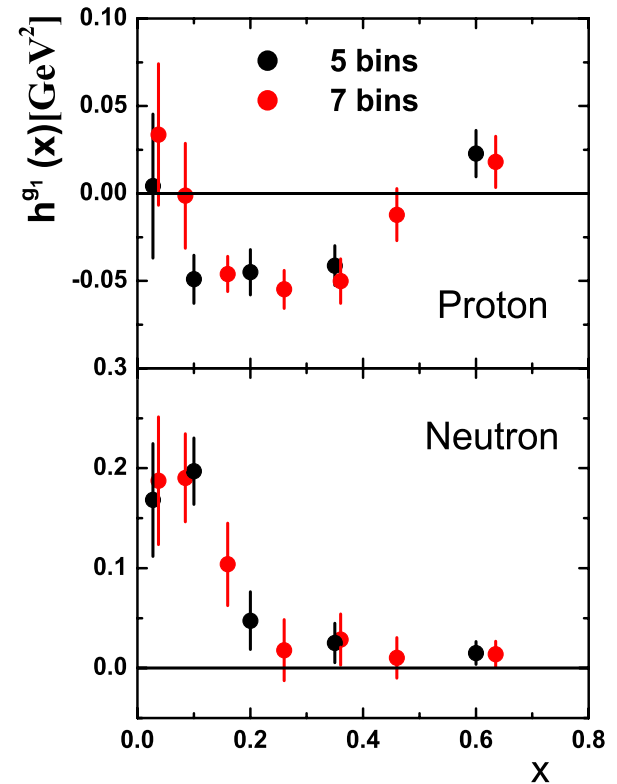


$$g_1 = (g_1)_{LT} + h^{g_1}(x)/Q^2$$

Impact of CLAS'06 data on the uncertainties for NLO(MS) polarized PD



- Due to the good accuracy of the *CLAS* data, one can split the measured x region of the *world+CLAS* data set into 7 bins instead of 5, and to determine more precisely the x -dependence of HT
- The corresponding PPD are practically identical with those of LSS'06 (5 bins)
- The only exception is $x\Delta G$, but it lies within the error band of $x\Delta G$ (5 bins) \rightarrow small correlation between gluons and HT



DATA

CERN **EMC** - A_1^p **SMC** - A_1^p, A_1^d **COMPASS'06** - A_1^d

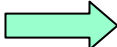
DESY **HERMES** - $\frac{g_1^p}{F_1^p}, \frac{g_1^d}{F_1^d}$

SLAC **E142, E154** - A_1^n **E143, E155** - $\frac{g_1^p}{F_1^p}, \frac{g_1^d}{F_1^d}$

JLab **Hall A** - $\frac{g_1^n}{F_1^n}$ **CLAS'06** - $\frac{g_1^p}{F_1^p}, \frac{g_1^d}{F_1^d}$

$$A_1^N \approx (1 + \gamma^2) \frac{g_1^N}{F_1^N}$$

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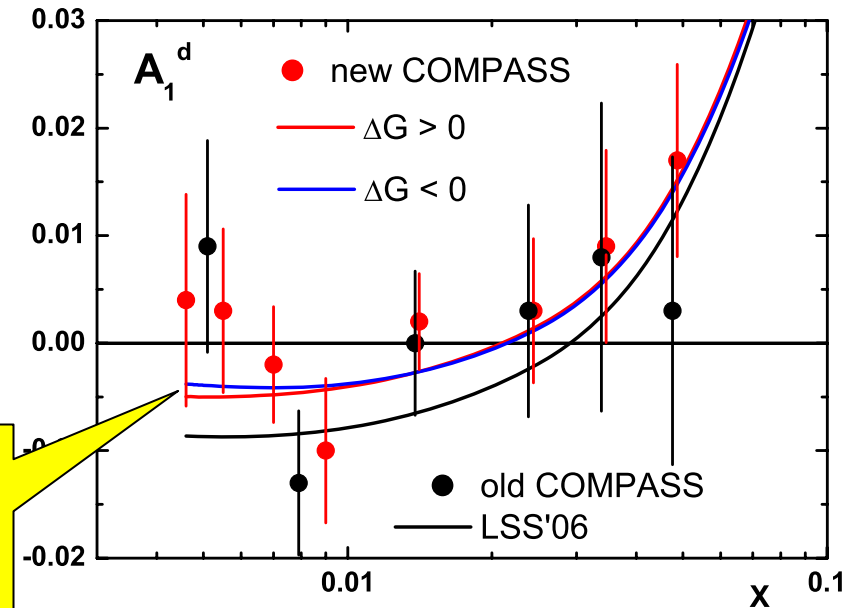
COMPASS'05  **COMPASS'06**

Number of exp. points: 823  826

Effect of COMPASS'06 A_1^d data (hep-ex/0609038) on polarized PD and HT

In contrast to the *CLAS* data, the *COMPASS* data are mainly at **large Q^2** and the **only precise** data at small x : **$0.004 < x < 0.02$** . The new data are based on **2.5 times** larger statistics than those of *COMPASS'05*

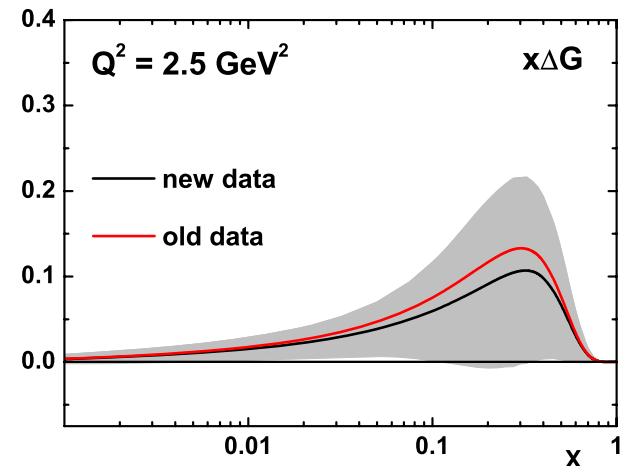
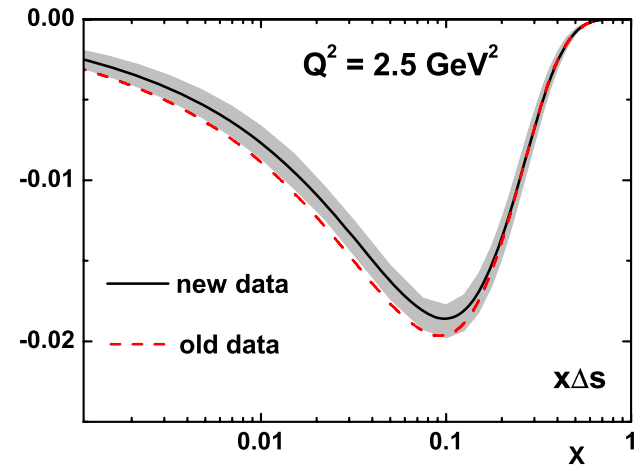
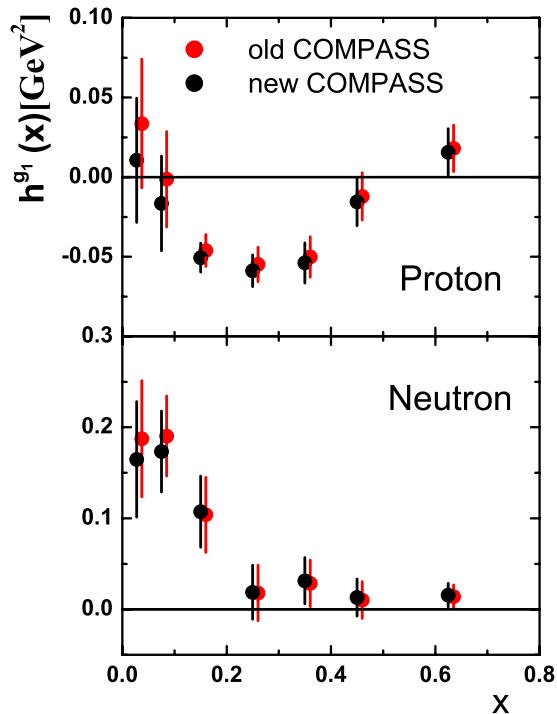
The **new** QCD curves corresponding to the best fits **lie above** the old one at **$x < 0.1$**



- $(\Delta u + \Delta \bar{u}), (\Delta d + \Delta \bar{d})$ do **NOT** change
- **$x|\Delta s(x)|$** and **$x\Delta G(x)$** and their first moments **Δs** and **ΔG** slightly **decrease**

$$Q^2 = 1 \text{ GeV}^2$$

<i>COMPASS</i>	Δs	ΔG	$a_0 = \Delta \Sigma_{MS}$
old	-0.070 ± 0.006	0.173 ± 0.184	0.165 ± 0.044
new	-0.063 ± 0.005	0.129 ± 0.166	0.207 ± 0.040



The values of HT are practically **NOT** affected by *COMPASS* data excepting the **small x** where Q^2 are also **small**

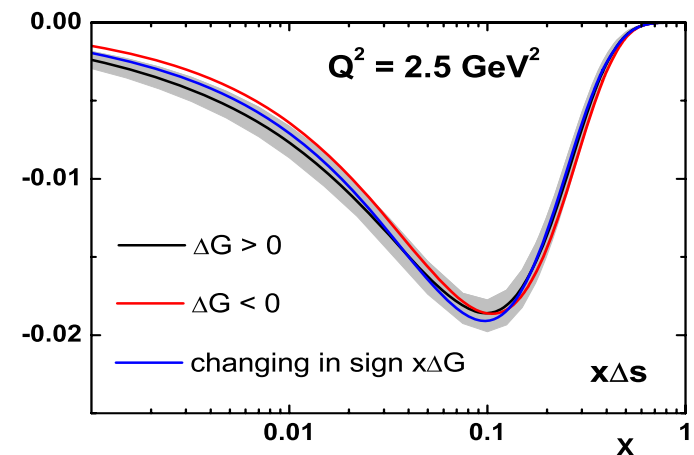
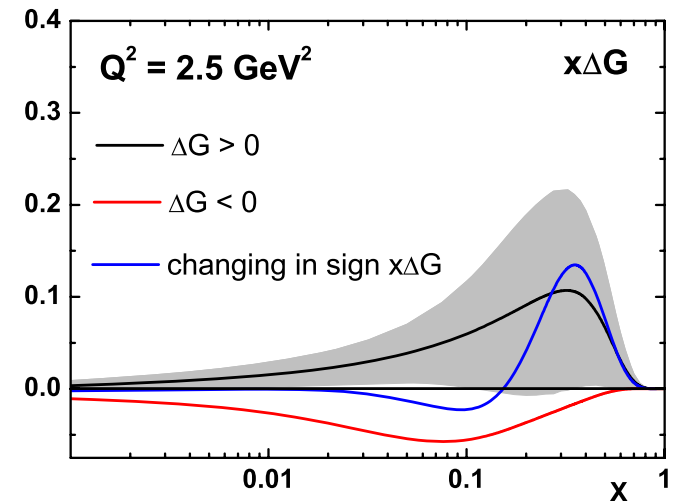
The sign of gluon polarization

- The present **inclusive** DIS data **cannot rule out** the solutions with negative and changing in sign gluon polarizations

$$\chi_{DF}^2(\Delta G > 0) = 0.895$$

$$\chi_{DF}^2(\Delta G < 0) = 0.897, \chi_{DF}^2(x\Delta G / \text{chsign}) = 0.895$$

- The shape of the negative gluon density **differs** from that of positive one
- In all the cases the magnitude of ΔG is small: $|\Delta G| \leq 0.2$
- The corresponding polarized quark densities are **very close** to each other



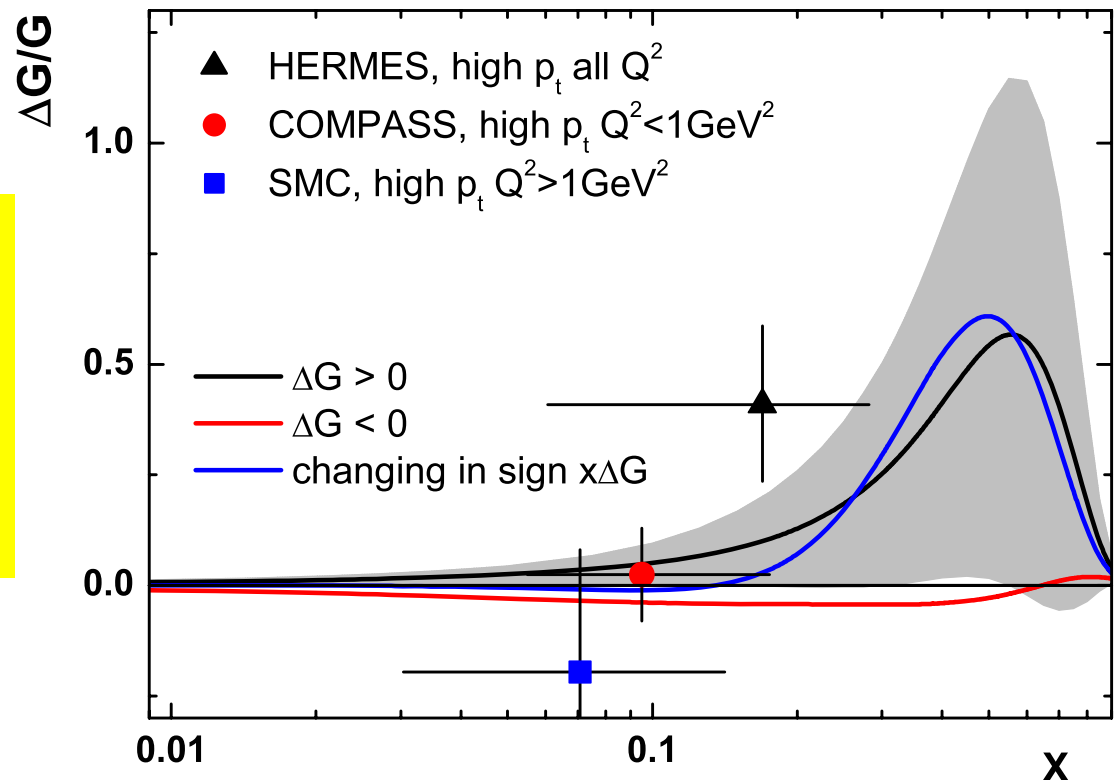
Comparison with directly measured $\Delta G/G$ at $Q^2 = 3 \text{ GeV}^2$

MRST'02 unpolarized gluon density is used for $G(x)$

The error band corresponds to statistic and systematic errors of ΔG

The error bars of the experimental points represent the **total errors**

The most precise value of $\Delta G/G$, the **COMPASS** one, is **well consistent** with any of the polarized gluon densities determined in our analysis



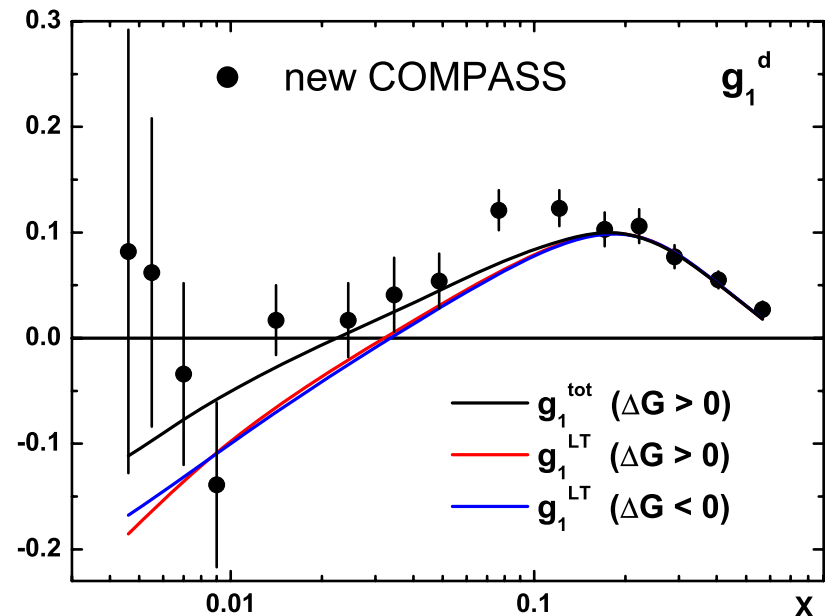
LSS'06 ν vs COMPASS'06

- At small x : **0.004 – 0.02** ($Q^2 \sim 1\text{-}3 \text{ GeV}^2$)
our results differ from those of *COMPASS*
- COMPASS* \rightarrow **significant** difference
between $(g_1)_{\text{th}}$ corresponding to the
best fits for $\Delta G > 0$ and $\Delta G < 0$
- LSS'06* \rightarrow the theoretical curves
for both cases are **very close** to
each other
- The reason \rightarrow HT effects (**40% at
small x**) which are NOT taken into
account by *COMPASS*

$$(g_1)_{\text{exp}} \leftrightarrow$$

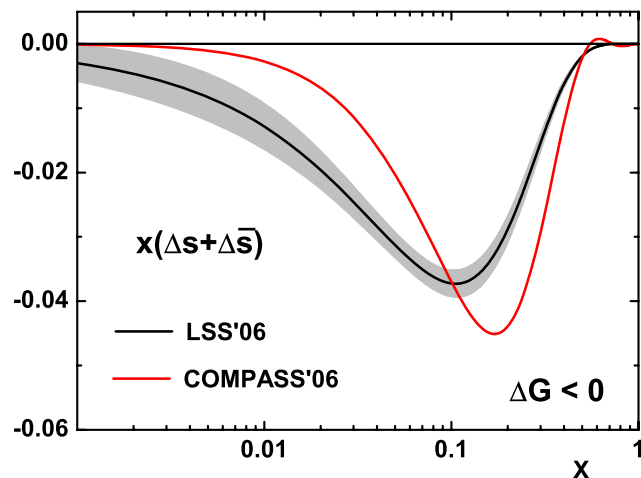
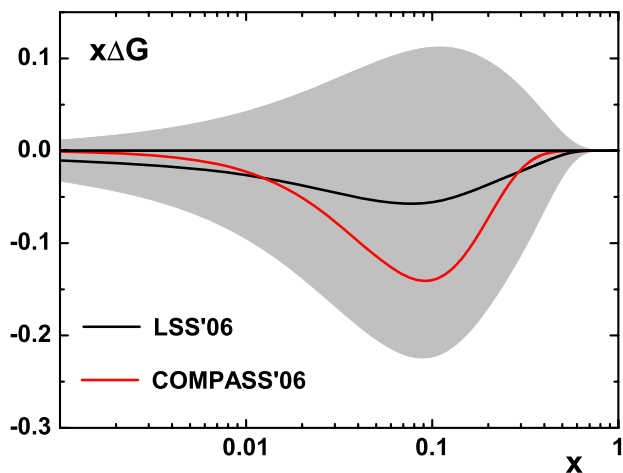
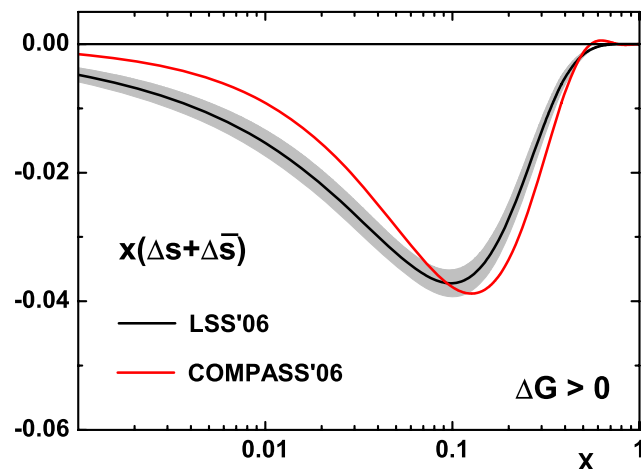
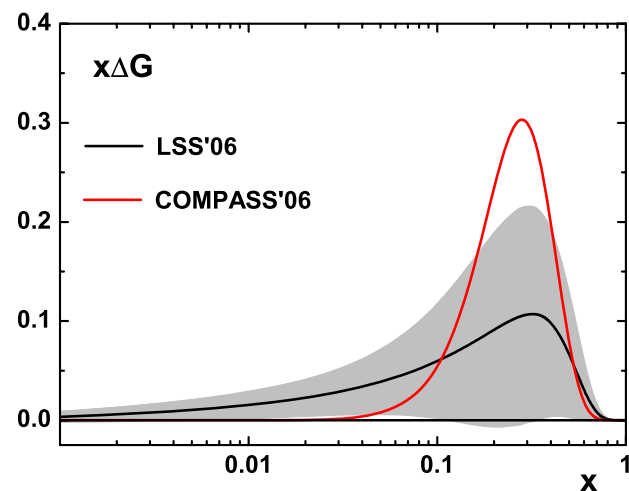
$$(g_1)_{\text{LT}}(\text{COMPASS}) \approx$$

$$(g_1)_{\text{LT}}(\text{LSS}) + h^d(x)/Q^2$$



- $x\Delta s$ are different, especially in the case of $\Delta G < 0$
- $x\Delta G$ obtained by COMPASS in both fits are more peaked than ours

$Q^2 = 3 \text{ GeV}^2$



SUMMARY

- The **low Q^2** *CLAS* data improve **essentially** our knowledge of **higher twist** corrections to g_1 structure function
- The central values of polarized PD are **NOT affected**, but the accuracy of its determination is **essentially improved**
- The *COMPASS* data (mainly at **large Q^2**) influence $|\Delta s|$ and ΔG which slightly **decrease**, but practically do **NOT** change HT



Strong support of the QCD framework

- **Large (40%)** contribution of HT to $(g_1)^d$ at small x (**low Q^2**)
- The present **inclusive** DIS data **cannot rule out** the negative and changing in sign gluon densities
- **Good agreement** with the directly measured $\Delta G/G$