

Dijet azimuthal correlations in QCD hard processes

Yazid Delenda¹

University of Manchester

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¹In collaboration with Andrea Banfi and Mrinal Dasgupta

Introduction

Motivation

Studies of **soft gluon radiation** and **non-perturbative effects** are vital for current and future colliders:

- ▶ Predictions for future colliders [LHC] (e.g. Higgs Q_t spectrum).
- ▶ All-orders analytical resummations.
- ▶ Separating non-perturbative effects and underlying event from perturbative physics.
- ▶ Extracting non-perturbative parameters (coupling, pdfs).
- ▶ (Correct) tuning of Monte Carlos (HERWIG, PYTHIA, etc).

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Examples of where we could go wrong

1. **Non-global logs:** numerically resummed for **two-jet** observables in the **large N_c limit** to **single-log** accuracy:

M. Dasgupta and G.P. Salam, 2001, 2002

- ▶ $\mathcal{O}(1/N_c^2)$ neglected. Could be vital in some cases.
- ▶ Three and four-jet observables unaccounted for.

2. Use of a jet algorithm affects resummation of non-global observables:

- ▶ Reduces non-global logs.

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Dijet azimuthal correlation is a valuable observable for these studies:

- ▶ Sensitive to jet algorithm and recombination scheme.
- ▶ Sensitive to soft and/or collinear gluon radiation and non-perturbative effects.
- ▶ Involves three or more jets (challenges our understanding of power corrections, resummation, clustering algorithm effects and non-global logs).
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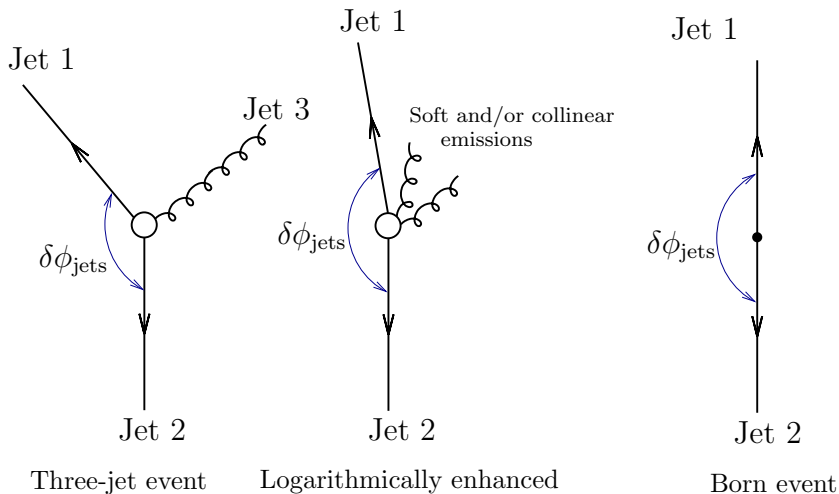
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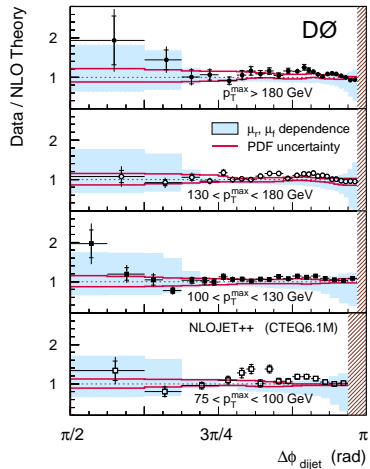
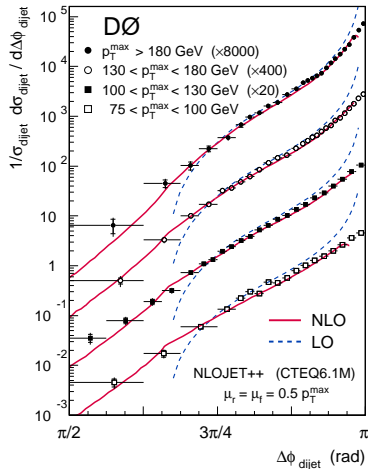
Dijet azimuthal correlation



Introduction

Dijet azimuthal correlation at DØ

Dijet azimuthal correlation recently measured by DØ



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Comparison to NLOJET++

- ▶ **NLO** description is good when $\pi - \delta\phi_{\text{jets}}$ is **large**.
- ▶ Close to Born configuration ($\pi - \delta\phi_{\text{jets}} \rightarrow 0$) NLO results diverge.
- ▶ Soft and/or collinear logs + non-perturbative effects become enhanced.
- ▶ \implies Needs resummation, power corrections and NLO matching.
- ▶ Same story in DIS. M. Hansson and L. Joensson , DIS 2006

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Resummation

- ▶ Resummation has been successful for many observables (e.g. **event-shape variables**) **M. Dasgupta and G.P. Salam, 2002**
- ▶ Dijet azimuthal correlation not yet resummed [difficult since jet-type observable].
- ▶ Now we have the technology to resum it.

Y. Delenda et al, 2006

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The observable

In the soft and/or collinear regime

$$\Delta = \pi - \delta\phi_{\text{jets}},$$

$\delta\phi_{\text{jets}}$: difference in azimuth of outgoing jets.

Depends on jet recombination method:

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Depends on jet recombination method:

- **4-momentum addition** - used at DØ :

$$p_{\text{jet}}^{\mu} = \sum_{i \in \text{jet}} p_i^{\mu}$$

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$$p_{\text{jet}}^{\mu} = \sum_{i \in \text{jet}} p_i^{\mu}$$

$$\Delta \simeq \frac{1}{p_t} \left| \sum_{i \notin \text{outgoing jets}} k_{t,i} \sin \phi_i \right|,$$

p_t : transverse momentum of outgoing jets.

$k_{t,i}$: transverse momentum of i^{th} gluon.

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⇒ **non-global observable.**

The observable

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$$\Delta = \pi - \delta\phi_{\text{jets}},$$

$\delta\phi_{\text{jets}}$: difference in azimuth of outgoing jets.

Depends on jet recombination method:

- Average E_t -weighted azimuth - used at HERA:

$$\phi_{\text{jet}} = \sum_{i \in \text{jet}} E_{t,i} \phi_i / \sum_{i \in \text{jet}} E_{t,i}$$

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$\theta_{ij} = 1$ if particle i belongs to jet j .

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⇒ **Continuously global observable.**

Dijet azimuthal correlation in DIS

The resummed result

- ▶ Use **average E_t -weighted azimuth** method.
- ▶ Measure Δ between outgoing legs in hadronic CoM.

$$\sigma(\Delta) = \int \sigma_B d\mathcal{B} \frac{2}{\pi} \int_0^\infty \frac{db}{b} \sin(b \Delta) e^{-R(b)},$$

σ_B : Born weight.

$R(b)$: Radiator, $R(b) = l g_1(\alpha_s l) + g_2(\alpha_s l)$.

$l = \ln(b e^{\gamma_E})$.

- ▶ $l g_1(\alpha_s l)$ resums leading logs. Originate from soft-collinear emissions to all legs.
- ▶ $g_2(\alpha_s l)$ resums next-to-leading logs. Originate from soft wide-angle or hard-collinear emissions to all the legs.

Dijet azimuthal correlation in DIS

The resummed result

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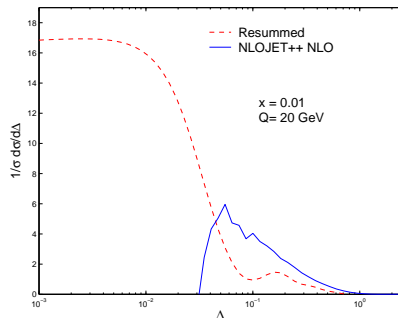
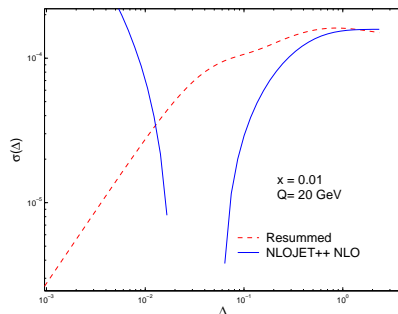
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Dijet azimuthal correlation in DIS

The resummed result (preliminary)



Comparison to NLOJET++

MC vs resummation at $\mathcal{O}(\alpha_s)$

Expansion of resummed result to $\mathcal{O}(\alpha_s)$:

$$\frac{d\sigma^{(1)}(\Delta)}{dL} = h_{11} + 2h_{12}L,$$

$L = \ln(1/\Delta)$, h_{ij} : constants.

All logs controllable. Must fully agree with NLOJET++ in the logarithmically enhanced region.

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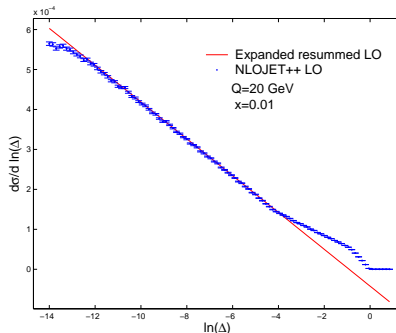
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Comparison to NLOJET++

MC vs resummation at $\mathcal{O}(\alpha_s^2)$

Expansion of resummed result to $\mathcal{O}(\alpha_s^2)$:

$$\frac{d\sigma^{(2)}(\Delta)}{dL} = 2h'_{22}L + 3h_{23}L^2 + 4h_{24}L^3,$$

NLOJET++ result at $\mathcal{O}(\alpha_s^2)$:

$$\frac{d\sigma_{\text{MC}}^{(2)}(\Delta)}{dL} = h_{21} + 2h_{22}L + 3h_{23}L^2 + 4h_{24}L^3 + \mathcal{O}(\Delta).$$

h'_{22} and h_{22} not the same (contain uncontrollable sub-leading logs).

$(d\sigma^{(2)}/dL)/L$ should give agreement for large values of L .

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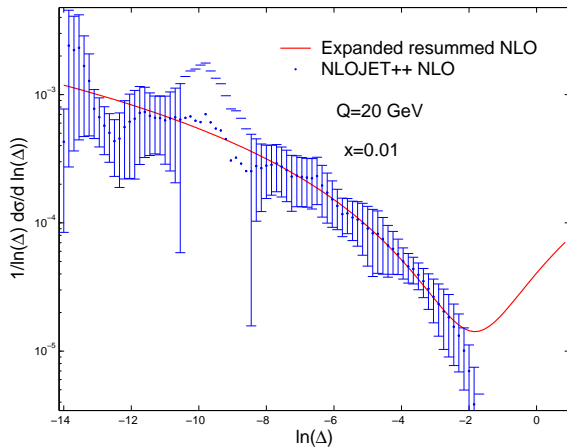
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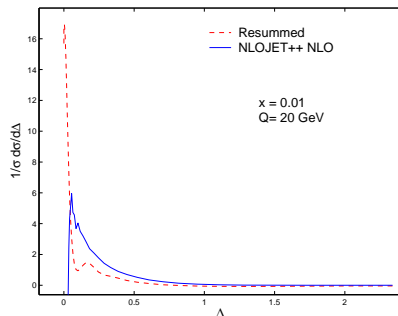
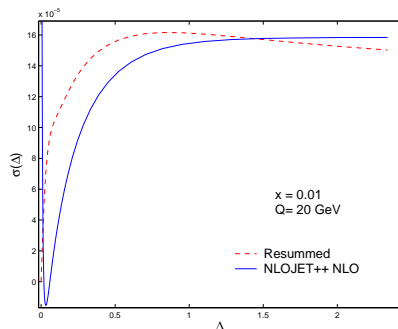
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MC vs resummation at $\mathcal{O}(\alpha_s^2)$



Matching

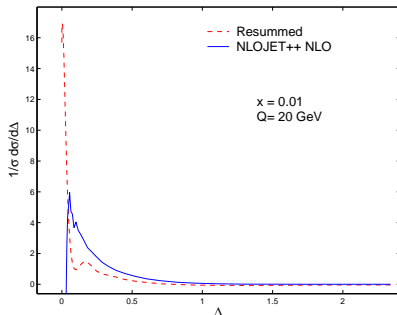
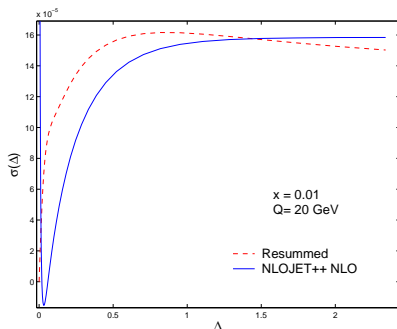
Back to the resummed result:



Need to combine NLO result with resummed result and remove double counted terms so as to achieve NLL+NLO accuracy.
IN PROGRESS!

Matching

Back to the resummed result:

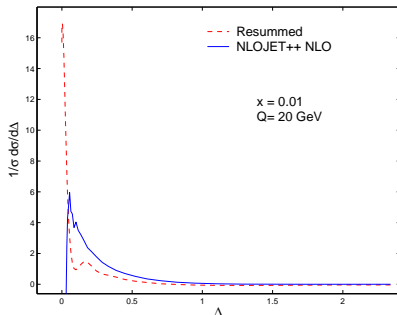
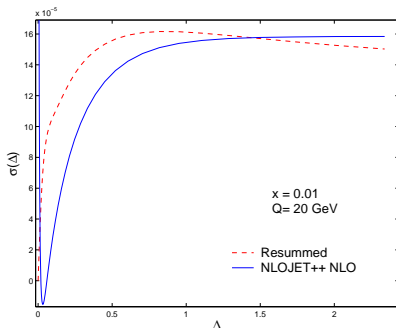


Need to **combine** NLO result with resummed result and **remove** double counted terms so as to achieve **NLL+NLO** accuracy.

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Non-perturbative effects (hadronisation) enter the distribution through running of α_s below some scale μ_I ($\sim 2\text{GeV}$):

- ▶ Replace α_s with α_{eff} below μ .

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$$\frac{1}{\mu} \int_0^\mu \alpha_{\text{eff}}(k_t) dk_t = \alpha_0(\mu),$$

α_0 : non-perturbative parameter. $\alpha_0(2\text{GeV}) \approx 0.52 \pm 0.04$

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Future directions and conclusions

- ▶ Perform a **NLO matching** to NLOJET++ and calculate **power corrections**.
- ▶ Study the hadron-hadron case ($D\bar{D}$) [Result analytically available for E_t -weighted recombination scheme].
- ▶ 4-momentum addition recombination scheme.
- ▶ Estimate the effects of non-global logs [may be insignificant] and clustering algorithm in the hadron-hadron case.
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