

# Future of DIS: PDF studies at LHC

April 18<sup>th</sup> DIS 2007

A M Cooper-Sarkar, Oxford

At the LHC high precision (SM and BSM) cross section predictions require precision Parton Distribution Functions (PDFs)

How do PDF Uncertainties affect SM physics

W/Z production, Higgs production

How do PDF uncertainties affect BSM physics?

- sometimes it will only affect precision e.g.  $Z'$  in high-mass Drell-Yan
- sometimes it will compromise discovery e.g, contact interactions in highET jet production

What measurements can we make at LHC to improve the PDF uncertainty?

# So when is it all going to happen?

- First pp collisions in **Nov 2007**  $\sqrt{s} = 0.9 \text{ TeV}$
- **Summer '08**  $\sqrt{s} = 14 \text{ TeV}$  at Low luminosity
- $L = 1 \text{ fb}^{-1}/\text{year}$  ( $\approx 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$ )
- **End '08**  $\sqrt{s} = 14 \text{ TeV}$  at High luminosity
- $L = 10 \text{ fb}^{-1}/\text{year}$  ( $\approx 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$ )

**LHC is W, Z, top ... factory**

Process	$\sigma(\text{nb})$	Ev./10fb <sup>-1</sup>
$W \rightarrow e \nu$	15	$\sim 10^8$
$Z \rightarrow e^+ e^-$	1.5	$\sim 10^7$
$t \bar{t}$	0.8	$\sim 10^7$
jets ( $p_T > 200 \text{ GeV}$ )	100	$\sim 10^9$

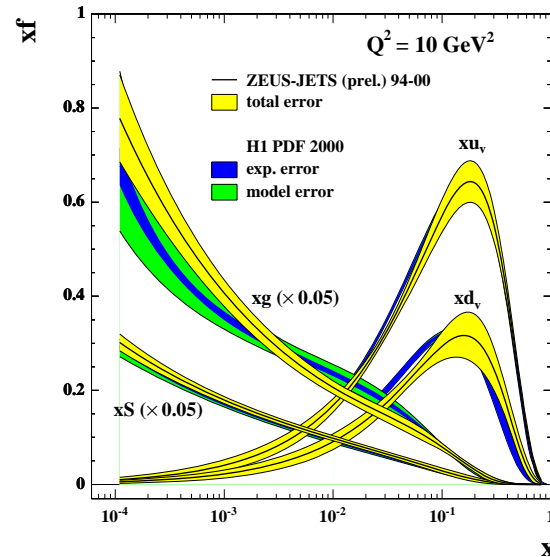
**Large statistics for SM processes  $\Rightarrow$**

- SM precision physics (EW, top-, b-physics, multijets...)
- Big potential for new physics (Higgs, Extra Dimensions, SUSY...)

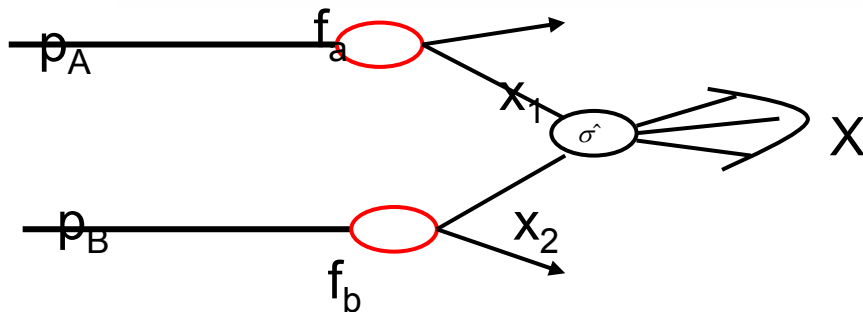
# The Standard Model is not as well known as you might think

particularly in the QCD sector  
and particularly in the non-perturbative part of  
the QCD sector

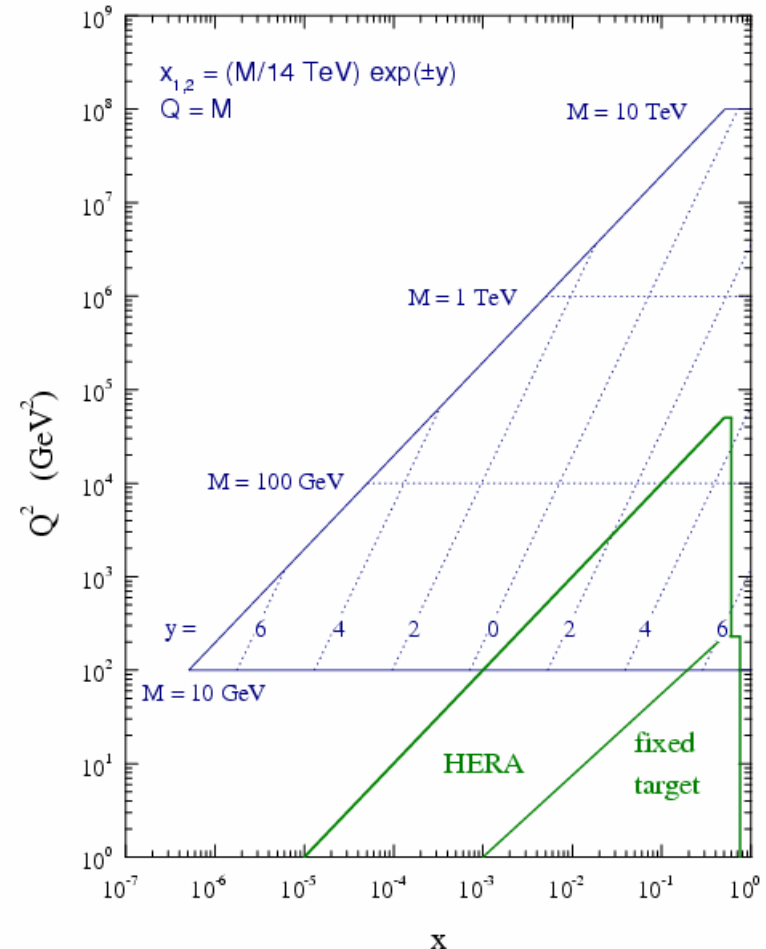
At the LHC high  
precision (SM and  
BSM) cross section  
predictions require  
precision Parton  
Distribution  
Functions (PDFs



$$\sigma_X = \sum_{a,b} \int_0^1 dx_1 dx_2 f_a(x_1, \mu_F^2) f_b(x_2, \mu_F^2) \times \hat{\sigma}_{ab \rightarrow X} \left( x_1, x_2, \{p_i^\mu\}; \alpha_S(\mu_R^2), \alpha(\mu_R^2), \frac{Q^2}{\mu_R^2}, \frac{Q^2}{\mu_F^2} \right)$$



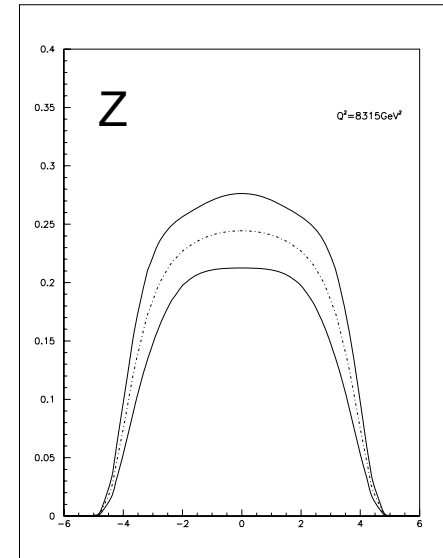
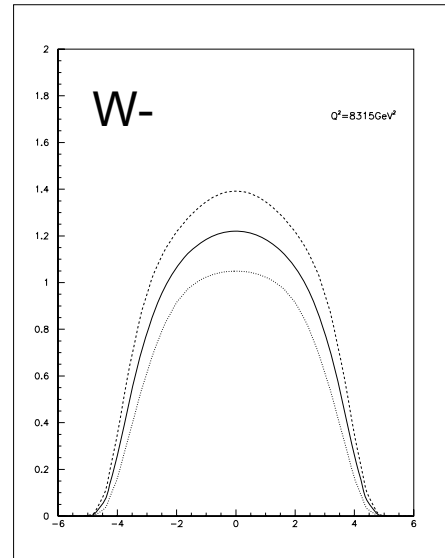
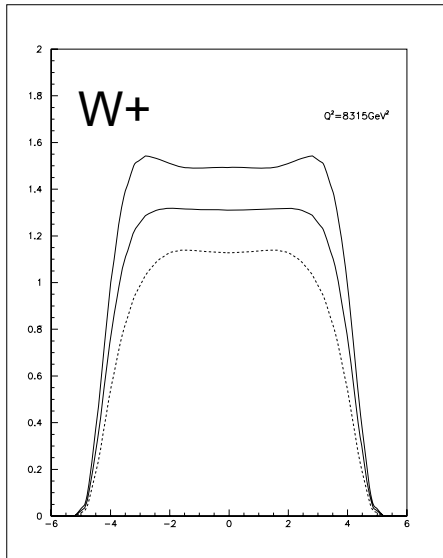
LHC parton kinematics



The central rapidity range for W/Z  
production AT LHC is at low-x

( $5 \times 10^{-4}$  to  $5 \times 10^{-2}$ )

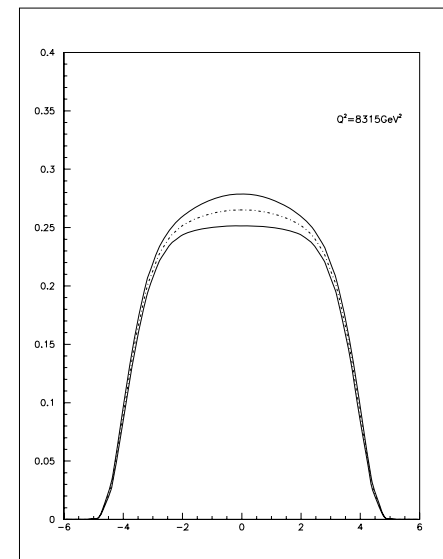
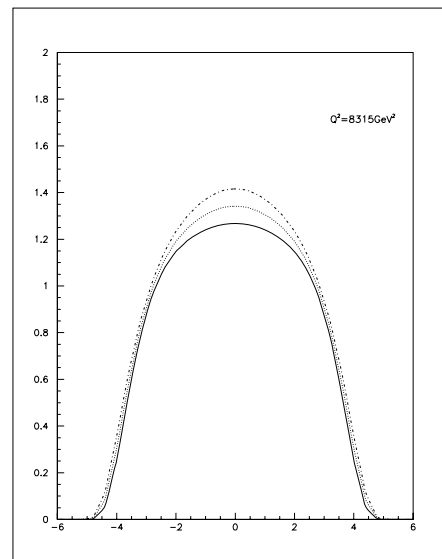
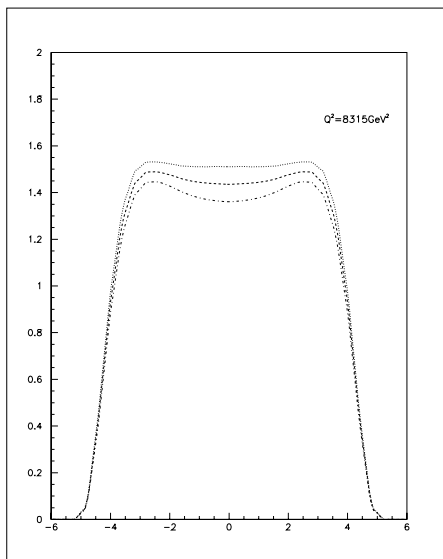
## What has HERA data ever done for us?



Pre-HERA W+/W-/Z rapidity spectra  $\sim \pm 15\%$  uncertainties become!

NO WAY to use these cross-sections as a good luminosity monitor

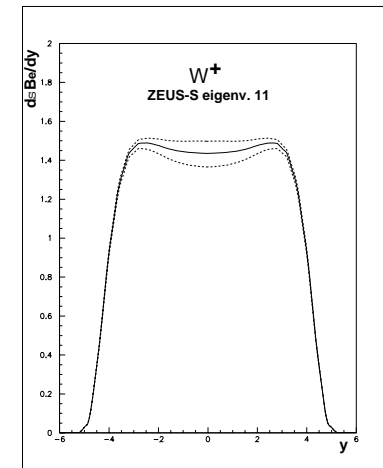
Post-HERA W+/W-/Z rapidity spectra  $\sim \pm 5\%$  uncertainties



Where did the improvement come from? There has been a tremendous improvement in our knowledge of the low-x glue and thus of the low-x sea

The uncertainty on the W/Z rapidity distributions is dominated by — **gluon PDF dominated eigenvectors**

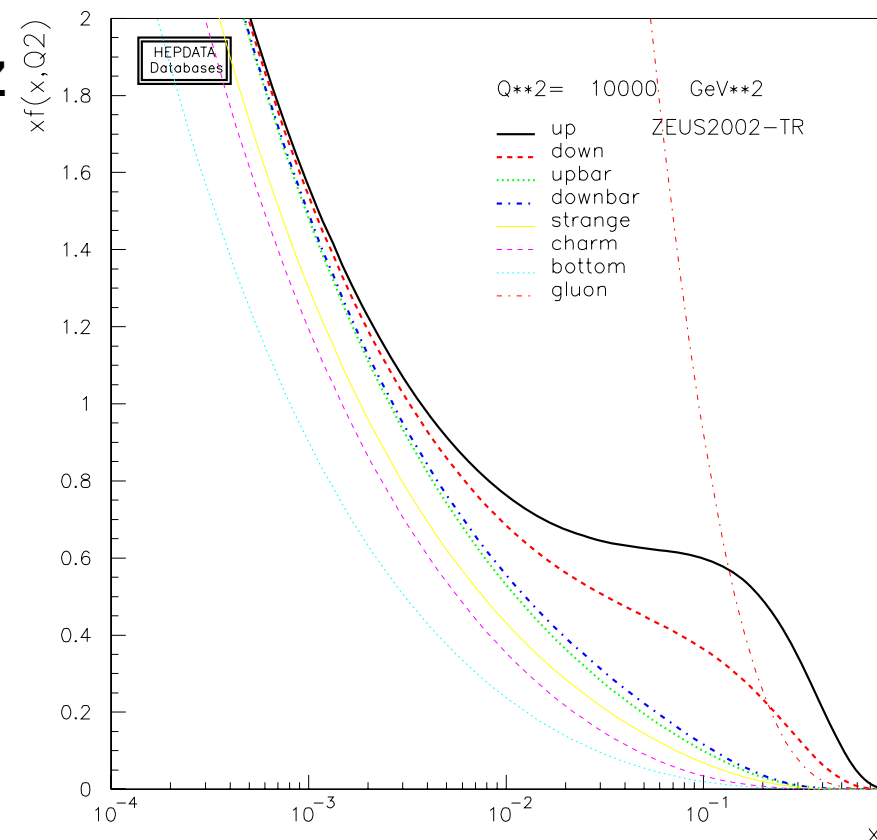
Both low-x and high-x gluon



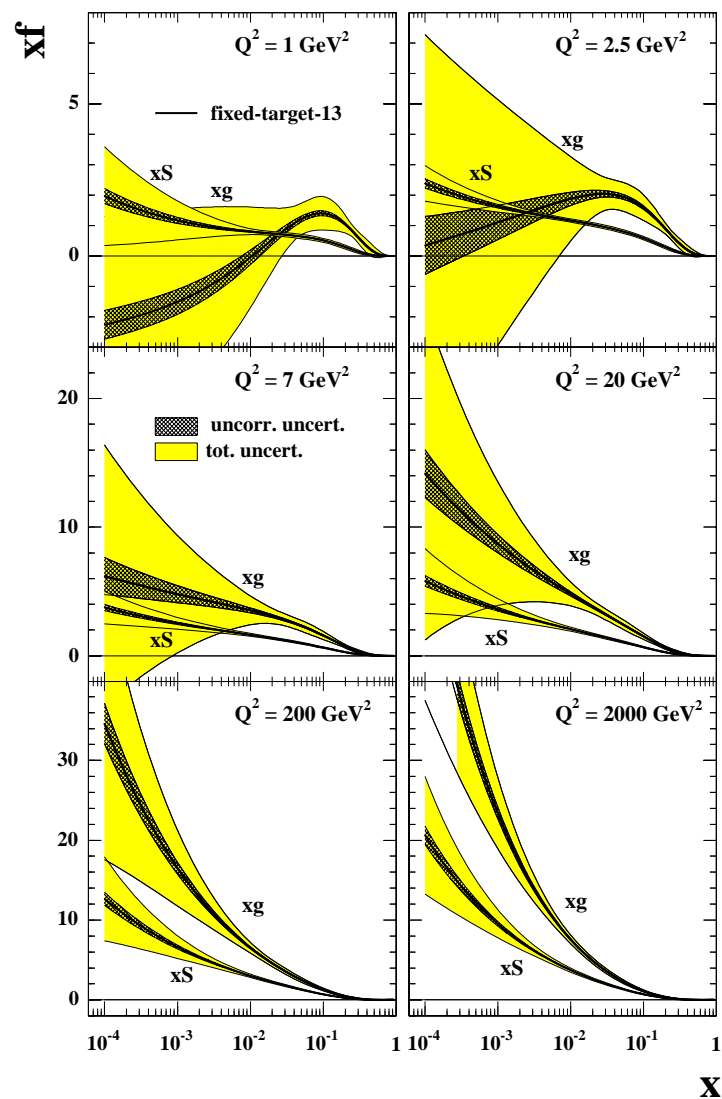
High-x gluon eigenvector

It may at first sight be surprising that **W/Z distns are sensitive to gluon parameters** BUT our experience is based on the Tevatron where Drell-Yan processes can involve valence-valence parton interactions.

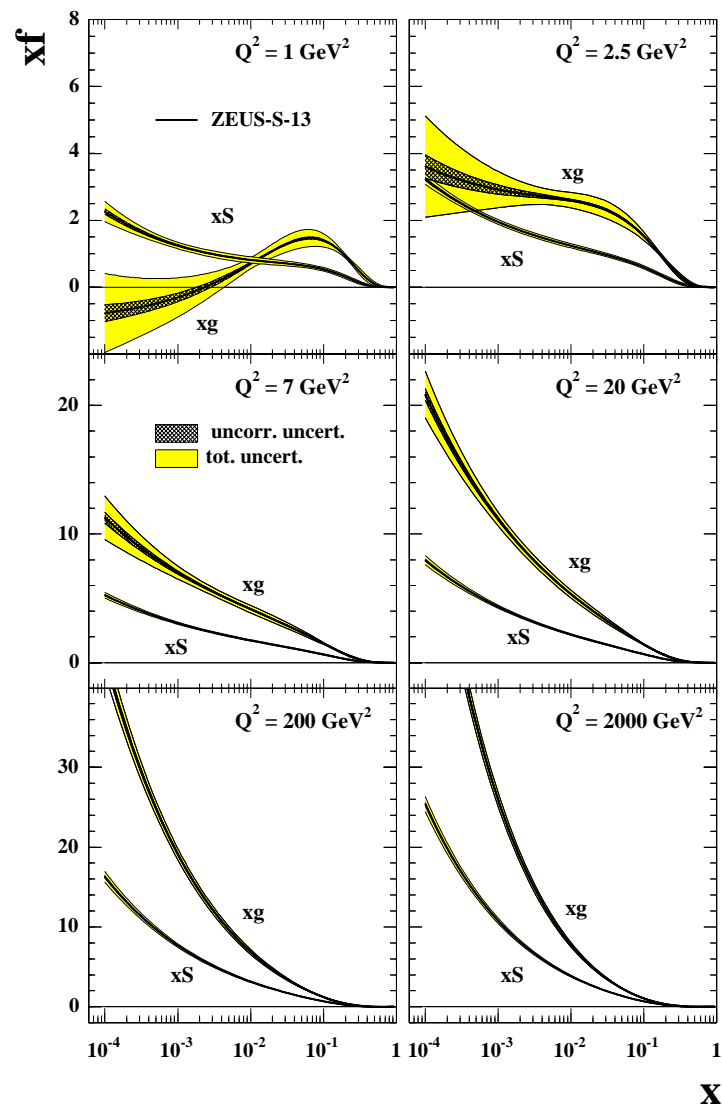
**At the LHC we will have dominantly sea-sea parton interactions at low-x**  
**And at  $Q^2 \sim M_Z^2$  the sea is driven by the gluon-** which is far less precisely determined for all x values



**Where did the improvement come from?** There has been a tremendous improvement in our knowledge of the low-x glue and thus of the low-x sea



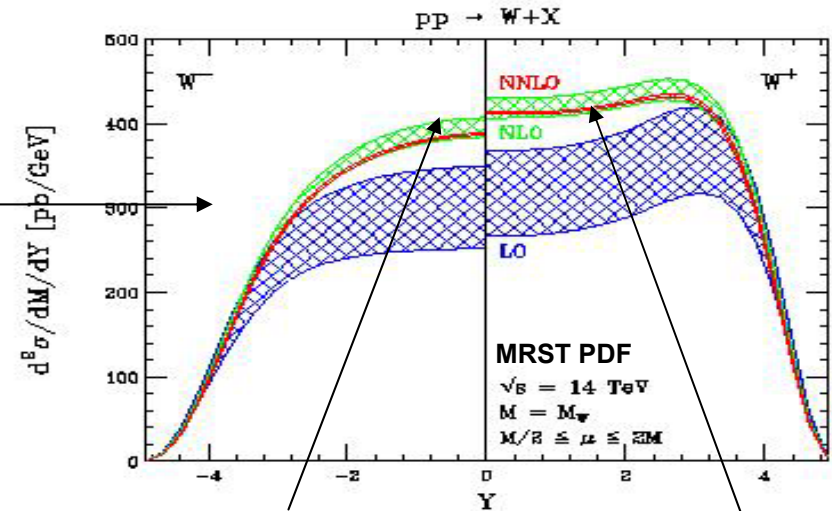
Pre-HERA sea and glue distributions



Post HERA sea and glue distributions

W/Z production have been considered as good standard candle processes with small theoretical uncertainty.

PDF uncertainty is a dominant contribution and most PDF groups quote uncertainties  $< \sim 5\%$

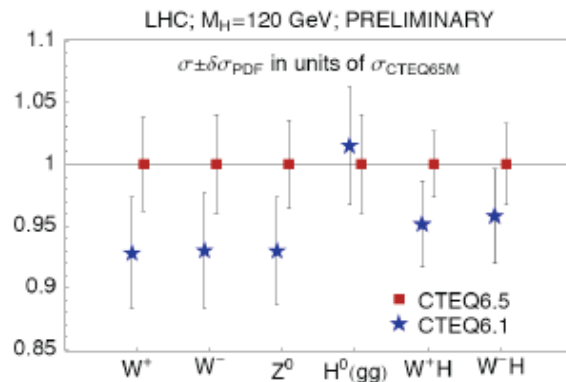


NNLO corrections small  $\sim$  few%  
 NNLO residual scale dependence  $< 1\%$

PDF Set	$\sigma_{W^+} \cdot B_{W \rightarrow \ell \nu}$ (nb)	$\sigma_{W^-} \cdot B_{W \rightarrow \ell \nu}$ (nb)	$\sigma_Z \cdot B_{Z \rightarrow \ell \ell}$ (nb)
ZEUS-S	$12.07 \pm 0.41$	$8.76 \pm 0.30$	$1.89 \pm 0.06$
CTEQ6.1	$11.66 \pm 0.56$	$8.58 \pm 0.43$	$1.92 \pm 0.08$
MRST01	$11.72 \pm 0.23$	$8.72 \pm 0.16$	$1.96 \pm 0.03$

BUT the central values differ by more than some of the uncertainty estimates.

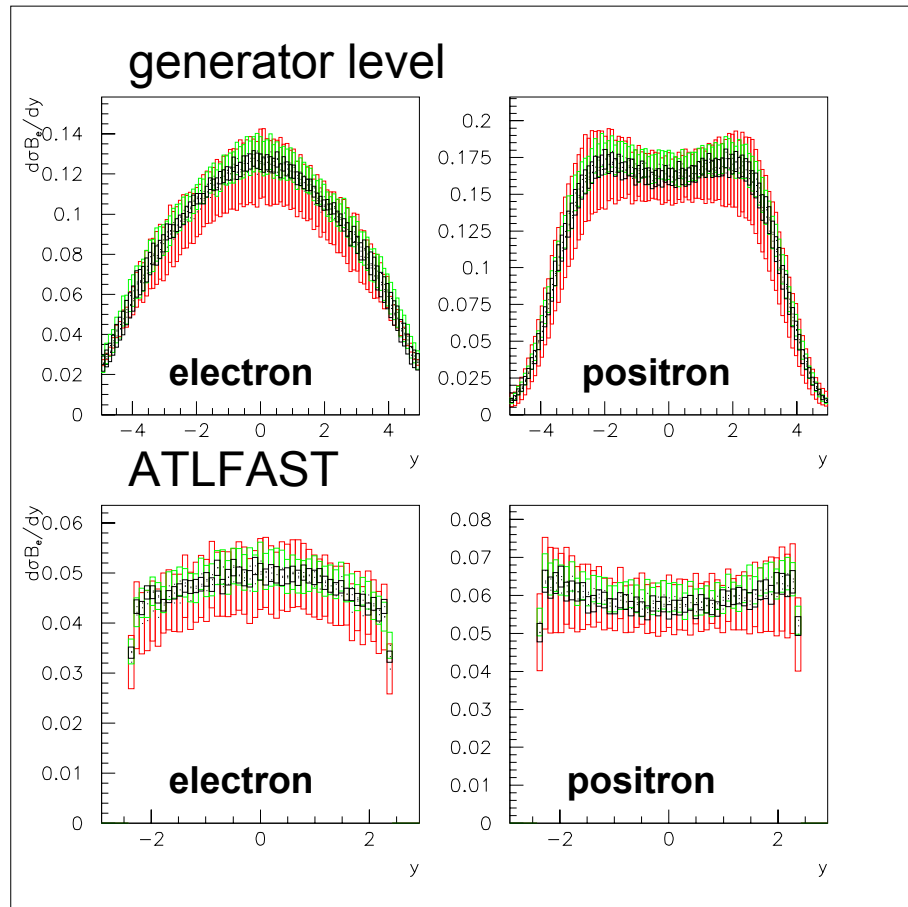
AND the situation just got dramatically worse. The new CTEQ6.5 estimate is 8% higher



→ Not so well known

Not such a precise luminosity monitor

# Can we improve our knowledge of PDFs using ATLAS data itself?



## We actually measure the decay lepton spectra

Generate 1000000  $W \rightarrow e\nu$  events ( $100\text{pb}^{-1}$ ) with HERWIG+k-factors (checked against MC@NLO) using CTEQ6.1M ZEUS\_S MRST2001 PDFs with full uncertainties from LHAPDF eigenvectors

At  $y=0$  the total uncertainty is

~  $\pm 6\%$  from ZEUS

~  $\pm 4\%$  from MRST01E

~  $\pm 8\%$  from CTEQ6.1

To improve the situation we NEED to be more accurate than this:  $\sim 4\%$

Statistics are no problem there will be millions of  $W$ 's

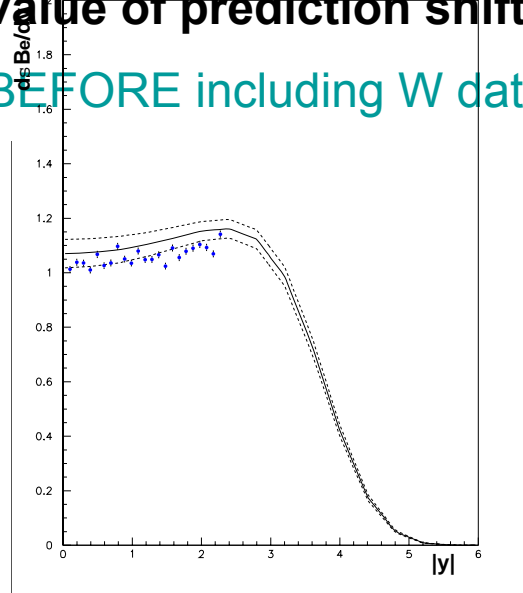
We need to control the systematic uncertainty



Study of the effect of including the LHC W Rapidity distributions in global PDF fits  
**by how much can we reduce the PDF errors with early LHC data?**

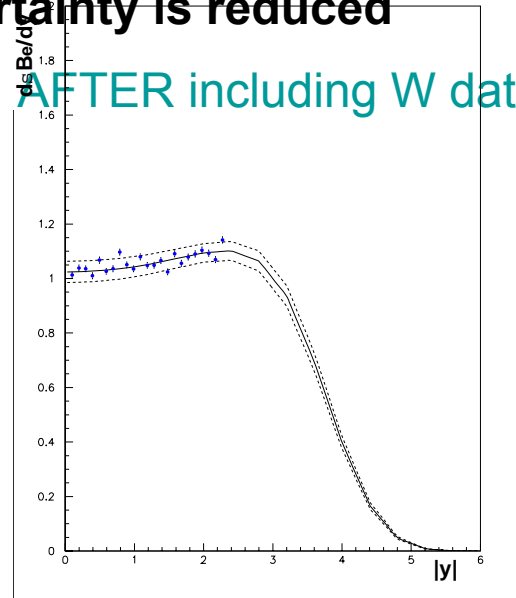
Generate data with 4% error using CTEQ6.1 PDF, pass through ATLFAST detector simulation and then include this pseudo-data in the global ZEUS PDF fit **Central value of prediction shifts and uncertainty is reduced**

BEFORE including W data



Lepton+ rapidity spectrum  
data generated with CTEQ6.1  
PDF compared to predictions  
from ZEUS PDF

AFTER including W data



Lepton+ rapidity spectrum  
data generated with CTEQ6.1  
PDF compared to predictions  
from ZEUS PDF **AFTER these  
data are included in the fit**

Specifically the low-x gluon shape parameter  $\lambda$ ,  $xg(x) = x^{-\lambda}$ , was  
 $\lambda = -.199 \pm .046$  for the ZEUS PDF before including this pseudo-data  
It becomes  $\lambda = -.181 \pm .030$  after including the pseudodata

The **uncertainty on the  $W^+ W^-$  and  $Z$  rapidity distributions** are all dominated by **gluon PDF uncertainty** and there is **cancellation of this uncertainty** in the ratio

$$Z_W = Z/(W^+ + W^-)$$

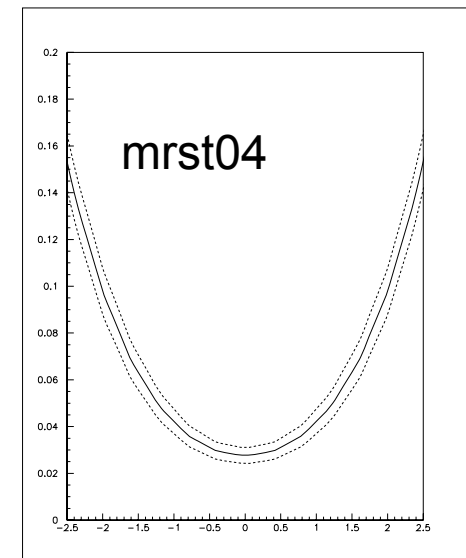
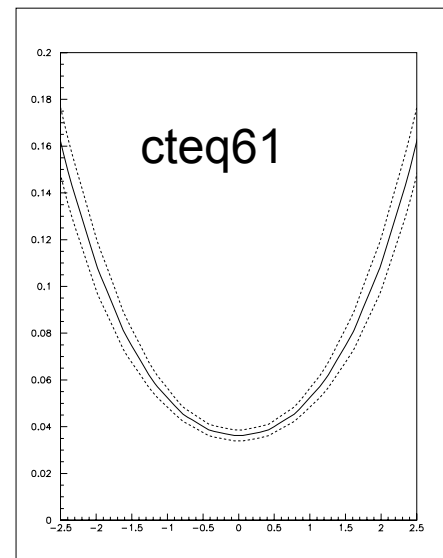
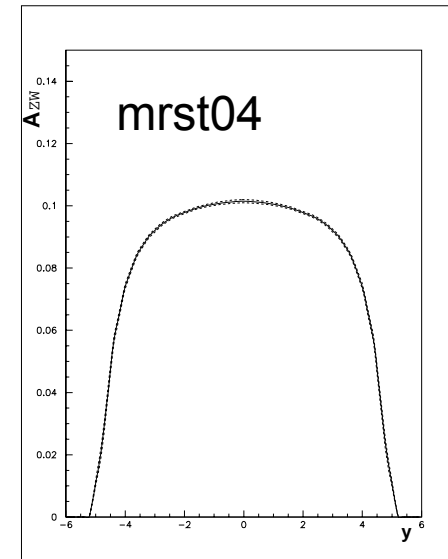
the PDF uncertainty on this ratio is  $\sim 1\%$  and there is agreement between PDFsets

**But the same is not true for the  $W$  asymmetry**

$$A_W = (W^+ - W^-)/(W^+ + W^-)$$

the PDF uncertainty on this ratio is reduced compared to that on the  $W$  rapidity spectra within any one PDF set

BUT there is not good agreement between PDF sets- **a difference in valence PDFs is revealed**



Dominantly, at LO  $A_W = \frac{(u \bar{d} - d \bar{u})}{(u \bar{d} + d \bar{u})}$

And  $\bar{u} = \bar{d} = \bar{q}$  at small x

So  $A_W \sim \frac{(u - d)}{(u + d)} = \frac{(u_v - d_v)}{(u_v + d_v + 2q)}$

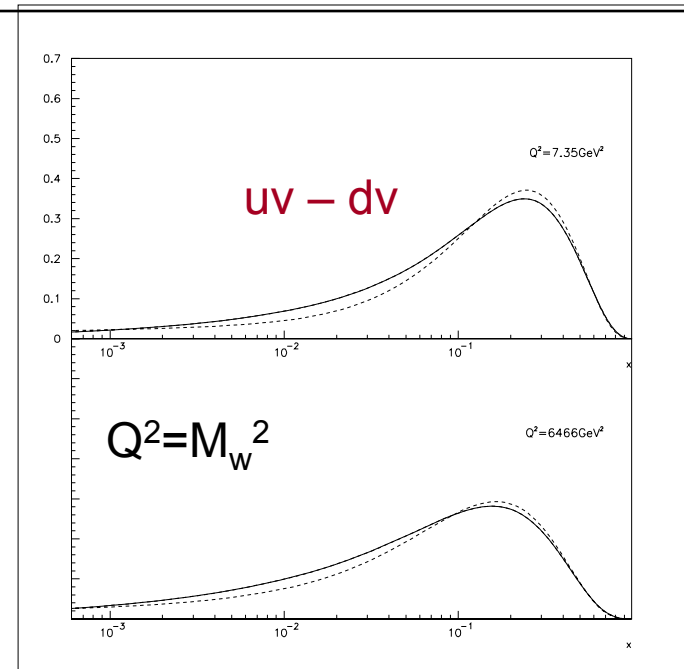
Actually this pretty good even quantitatively

The difference in valence PDFs you see here  
does explain the difference in  $A_W$

**Of course we will actually measure the  
lepton asymmetry**

MRST04

CTEQ6.1

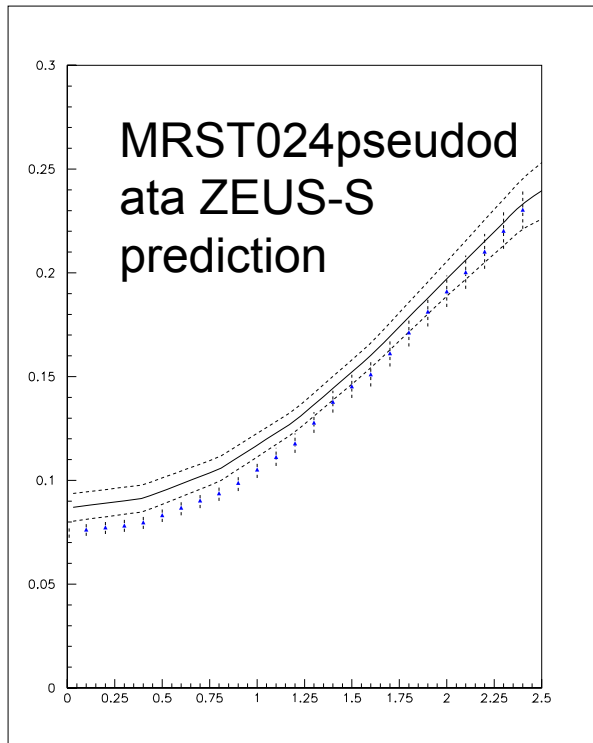


x- range affecting W asymmetry in the  
measurable rapidity range

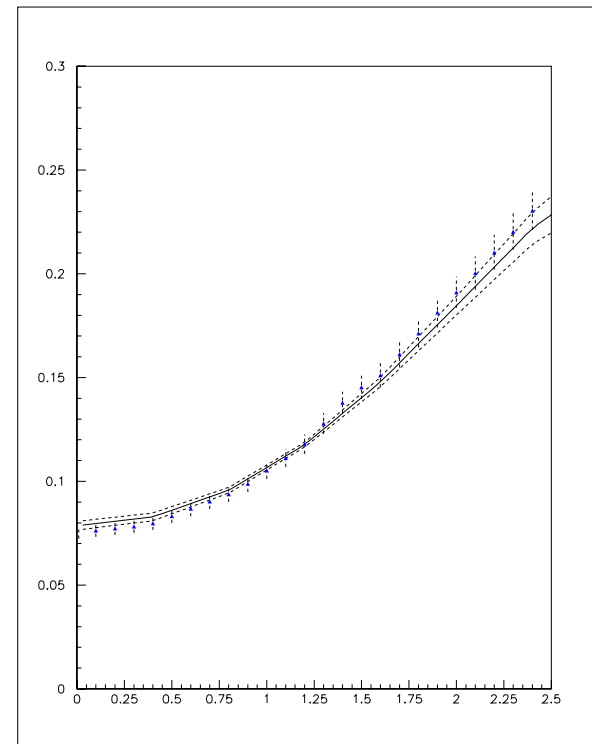
Generate data with 4% error using MRST04 PDF and then include this pseudo-data in the global ZEUS PDF fit

The PDF uncertainty is improved by the input of such data and the fit is only able to describe the MRST pseudodata if the valence parametrizations at  $Q^2_0$  are extended to become  $xV(x) = A x^a (1-x)^b (1+d \sqrt{x} + c x)$ .

BEFORE including  $A_W$   
pseudo-data



AFTER including  $A_W$   
pseudo-data



Conclusion we have valence PDF discrimination, and will be able to measure valence distributions at  $x \sim 0.005$  on proton targets for the first time

# But what about valence PDFs at high-x?

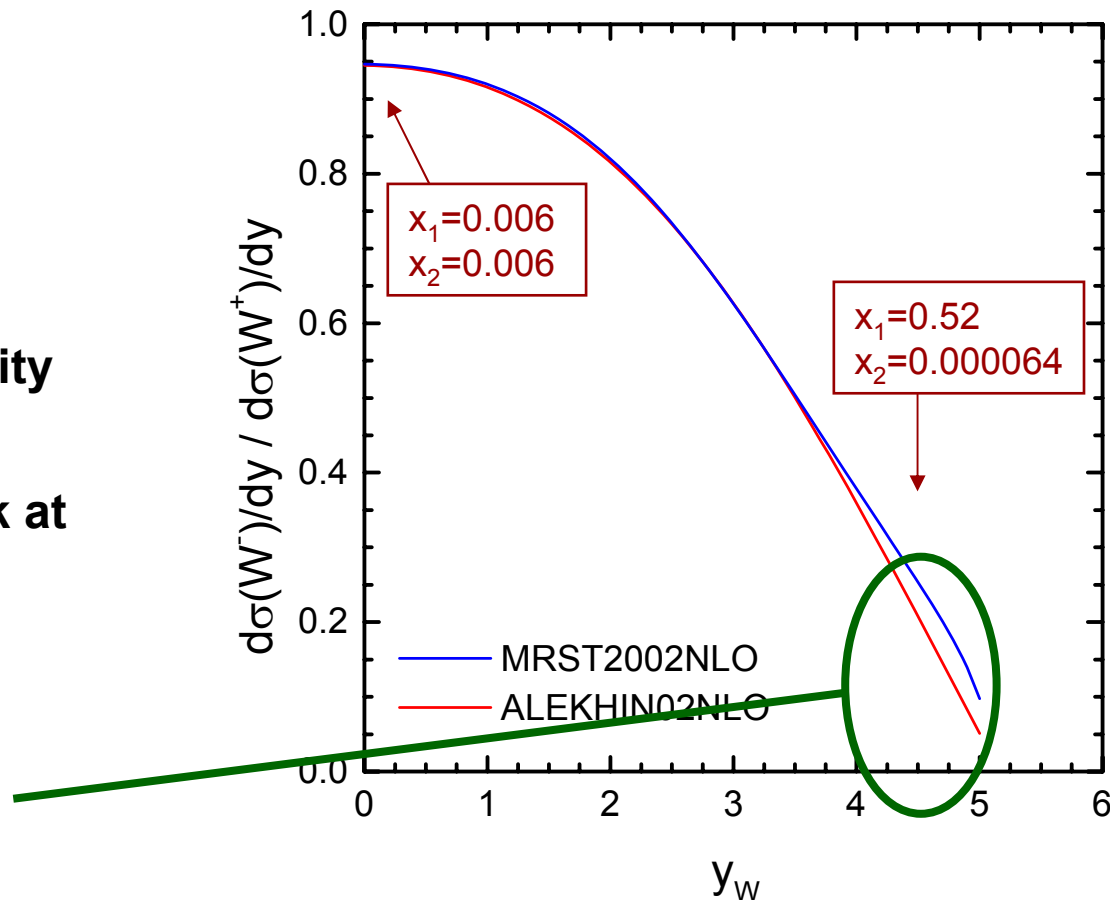
Look at W-/W+ ratio at large rapidity

$$\frac{W^-}{W^+} = \frac{u \bar{d}}{d \bar{u}}$$

Not possible for main LHC detectors BUT LHCb rapidity range 1.9 to 4.9

There is a proposal to look at this in LHCb

sensitive to large-x d/u



**Further thoughts on W production: LHC will be a low-x machine  
(at least for the early years of running)**

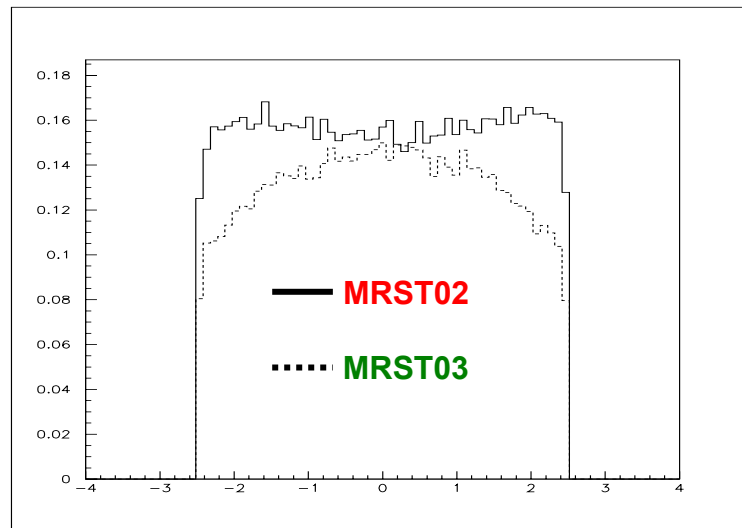
Is NLO (or even NNLO) DGLAP good enough?

The QCD formalism may need extending at small-x

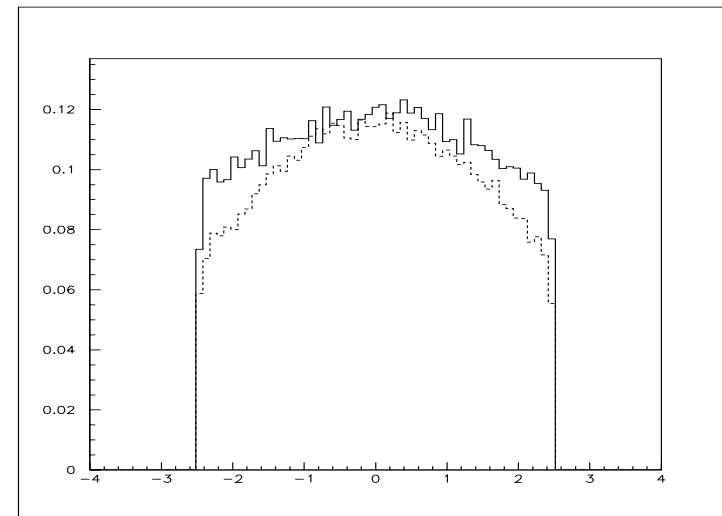
MRST03 is a toy PDF set produced without low-x data

200k events of  $W^{+-} \rightarrow e^{+-}$  generated with MC@NLO using MRST03 and MRST02

**Reconstructed Electron Pseudo-Rapidity Distributions (ATLAS fast simulation)**



Reconstructed  $e^+$



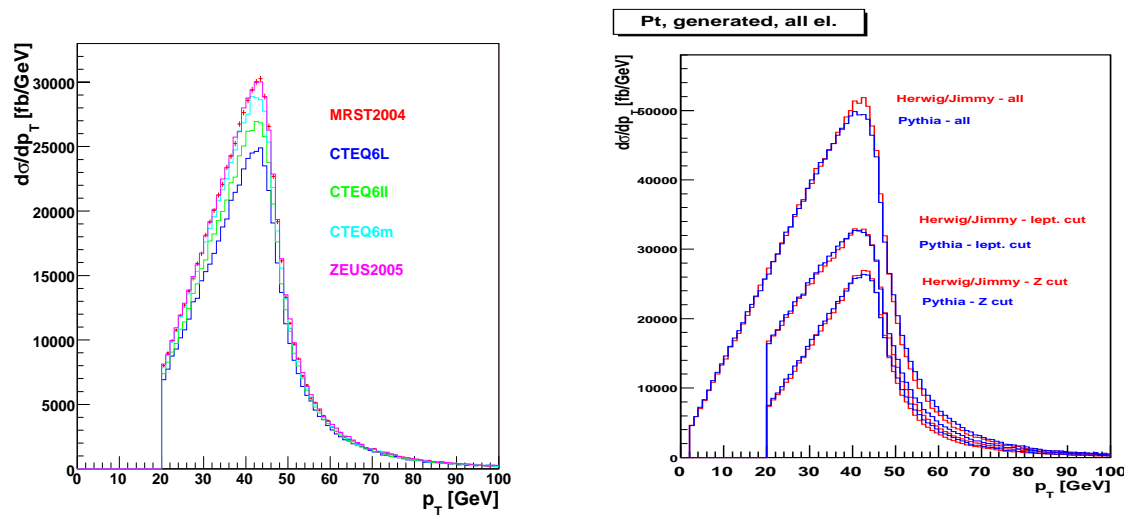
Reconstructed  $e^-$

6 hours  
running

**If something is very different about low-x behaviour it will show up in the  
our measurable rapidity range**

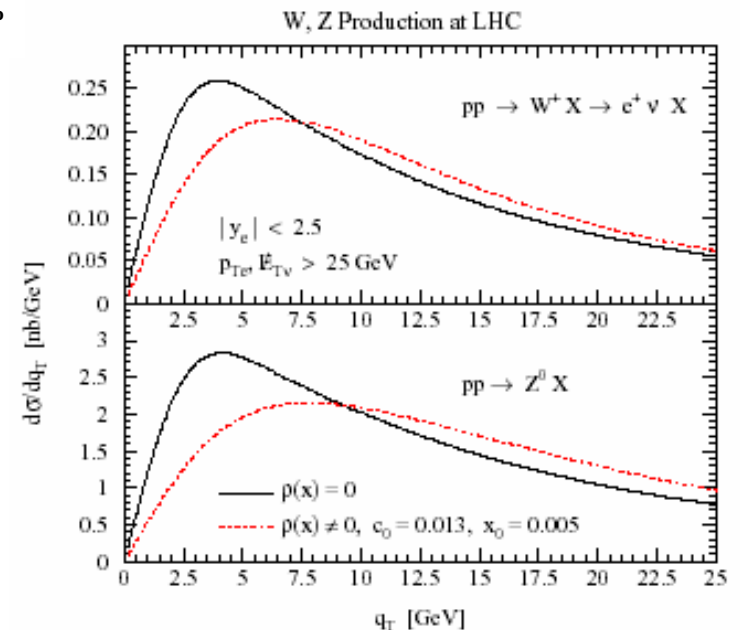
But the TOY PDF is unlikely to be realistic - a better way could be to look at  $p_T$  spectra for W and Z production

**$p_T$  spectra show PDF differences, but also show differences in modelling – e.g. PYTHIA/HERWIG differences**



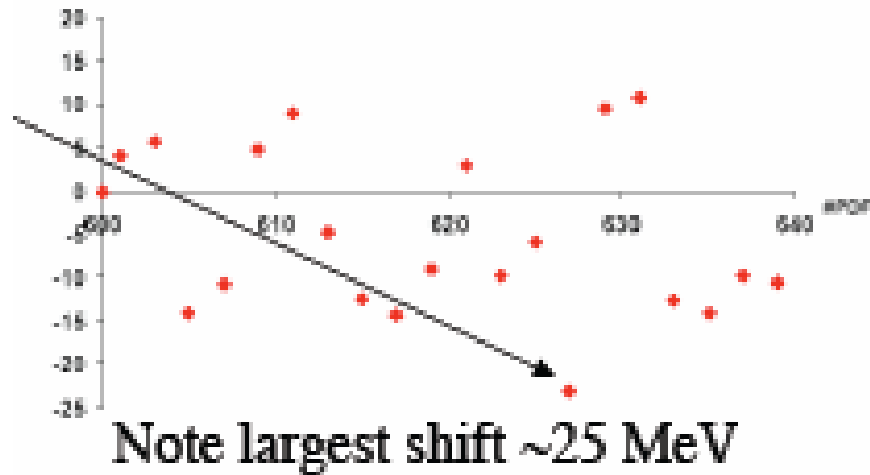
Probably needs more sophisticated treatment e.g. RESBOS.

There has been an interesting recent calculation of how lack of  $p_T$  ordering at low- $x$  may affect the  $p_T$  spectra for W and Z production at the LHC (See hep-ph/0508215)



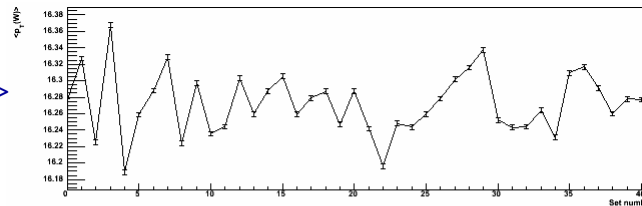
## Pt spectra are also used to measure MW

Raw  $dM_W$  from PDF uncertainties as of today, when using pt(e), is  $\sim 20$  MeV

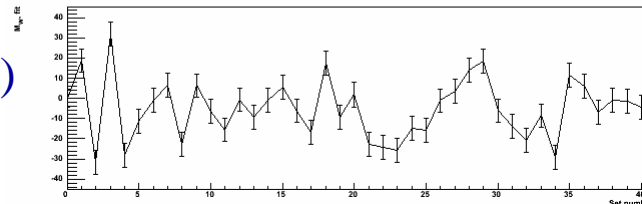


So we'd better be sure we've got the calculations for Pt spectra right

$\langle p_T(W) \rangle$



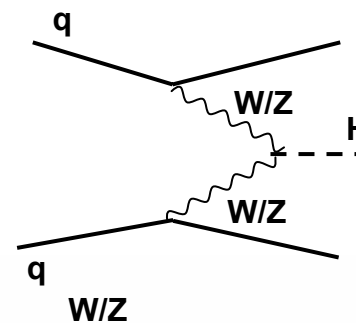
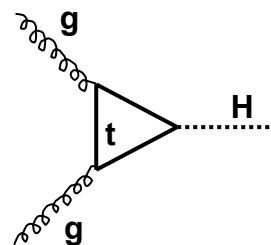
$\delta M_W(\text{fit})$



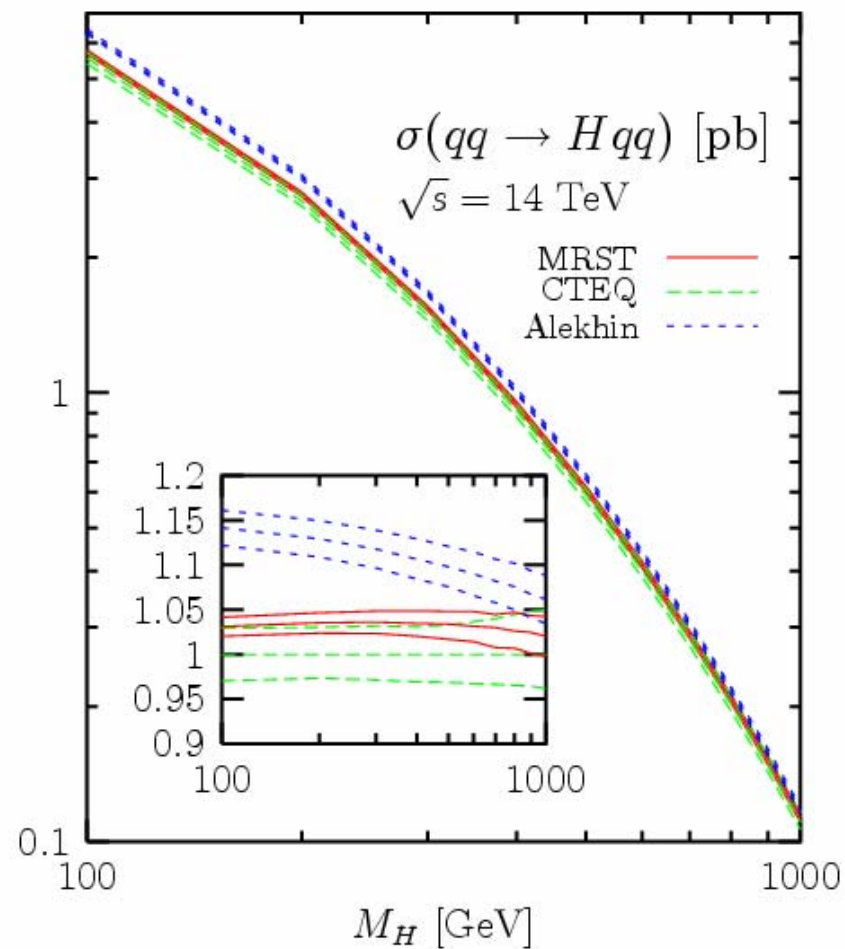
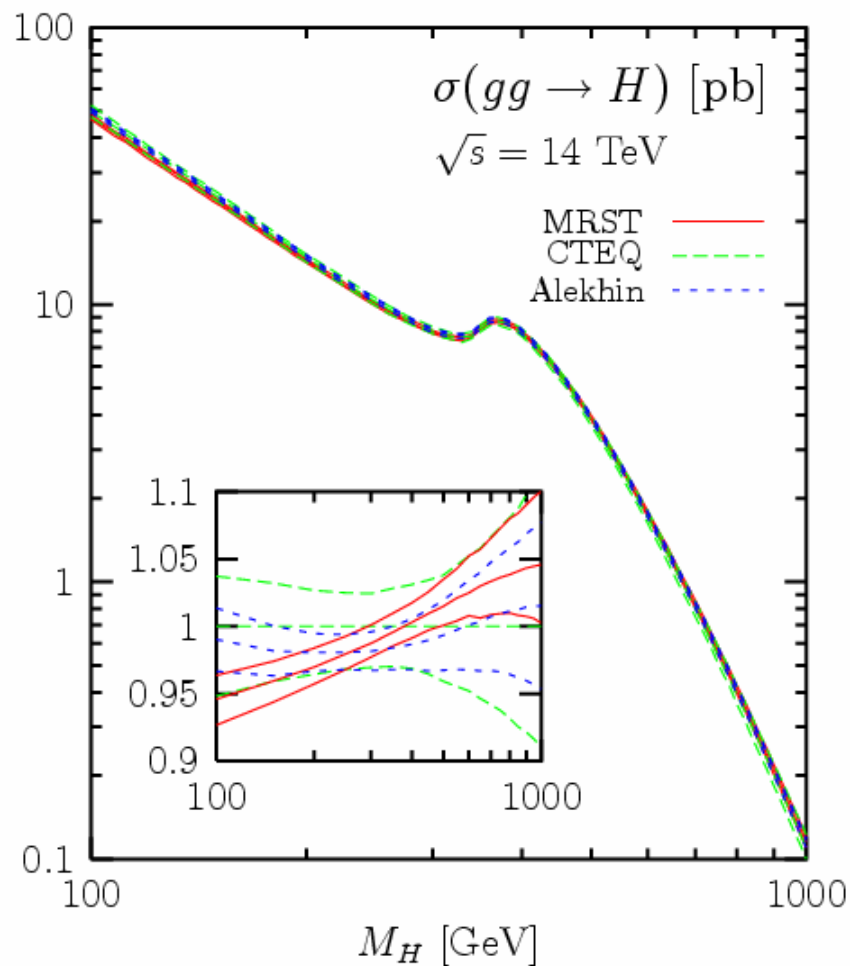
Same pattern



And how do PDF uncertainties affect the Higgs discovery potential?  
not too badly

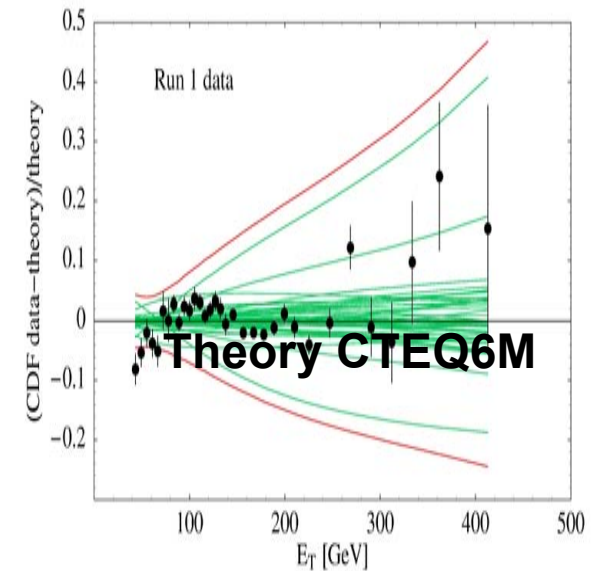
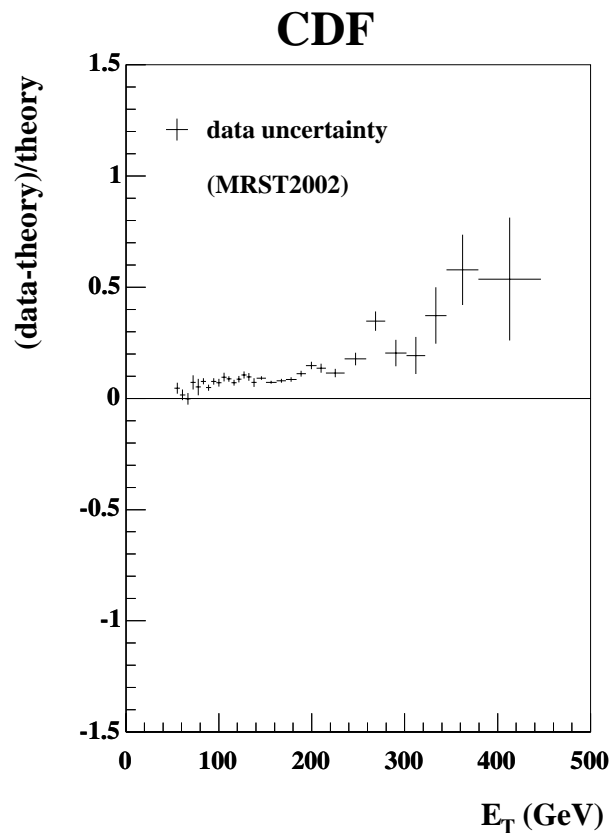


S Ferrag



## Moving on to BSM physics

Tevatron jet data were originally taken as evidence for new physics--



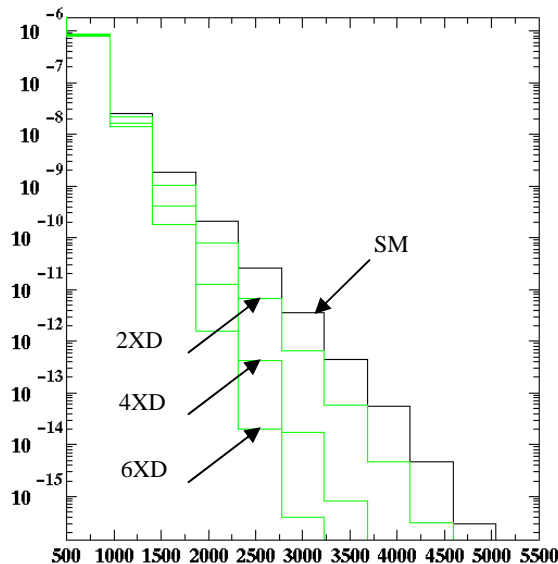
These figures show inclusive jet cross-sections compared to predictions in the form  $(\text{data} - \text{theory})/\text{theory}$

Today Tevatron jet data are considered to lie within PDF uncertainties  
And the largest uncertainty comes from the uncertainty on the high  $x$  gluon

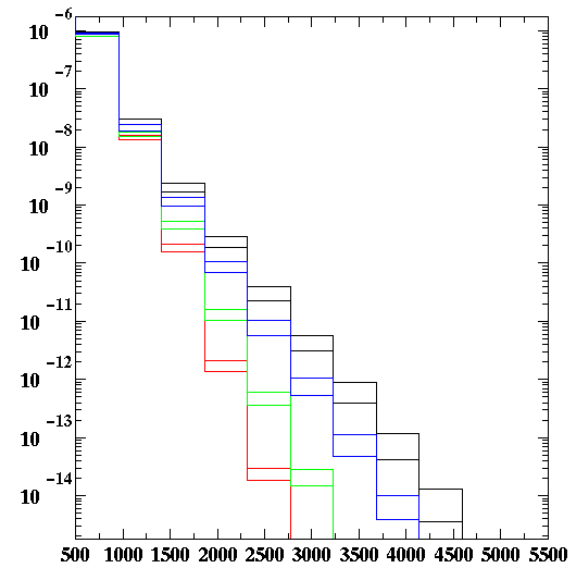
Such PDF uncertainties the jet cross sections compromise the LHC potential for discovery of physics effects which can be written as a contact interaction

E.G. Dijet cross section potential sensitivity to compactification scale of extra dimensions ( $M_c$ ) reduced from  $\sim 6$  TeV to 2 TeV. (Ferrag et al)

$M_c = 2$  TeV,  
no PDF error



$M_c = 2$  TeV,  
with PDF error

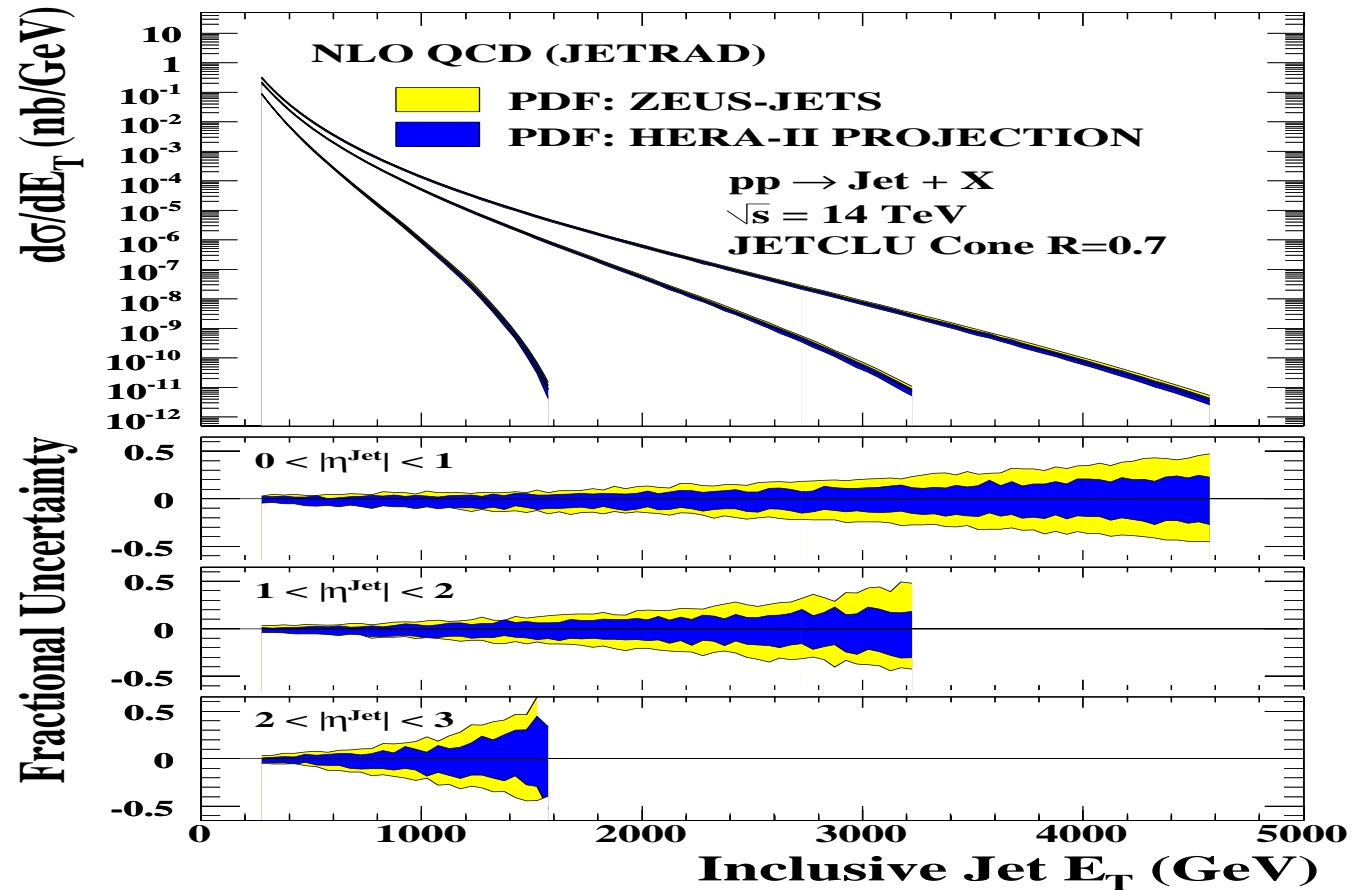


Can we know the high- $x$  gluon better?

And how might this impact on LHC high- $E_T$  jet cross-sections?

HERA now in second stage of operation (HERA-II)

HERA-II projection shows significant improvement to high- $x$  PDF uncertainties



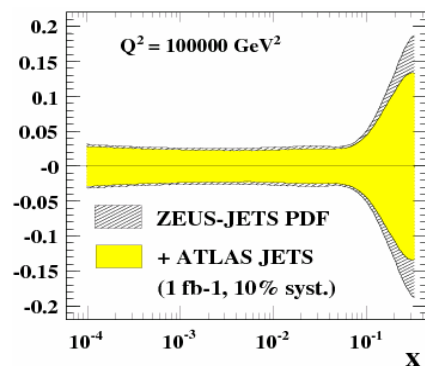
## And will we be able to use LHC data itself to improve the situation?

Recently grid techniques have been developed to NLO cross-sections in PDF fits (e.g ZEUS-JETs fit)

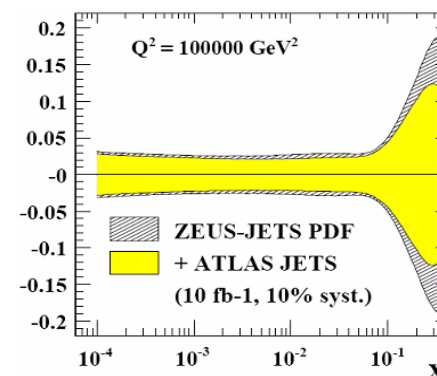
This technique can be used for LHC high-ET jet cross-sections

Use data at lower  $p_T$  and higher  $\eta$ -where new physics is not expected

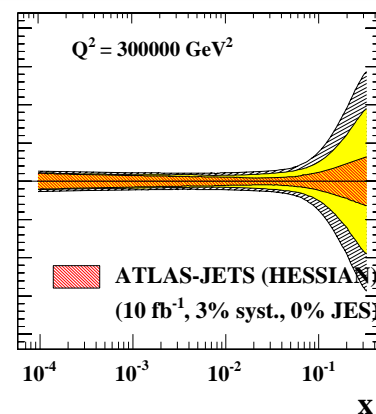
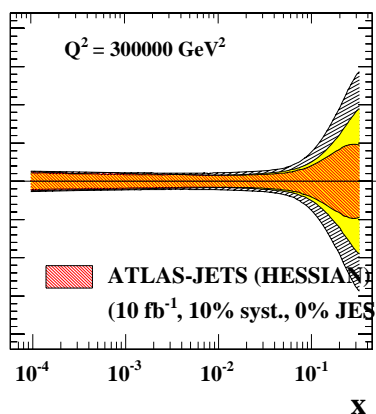
- Grids were generated for the inclusive jet cross-section at ATLAS in the pseudorapidity ranges  $0 < \eta < 1$ ,  $1 < \eta < 2$ , and  $2 < \eta < 3$  up to  $p_T = 3 \text{ TeV}$  (NLOJET).
- In addition pseudodata for the same process was generated using JETRAD [4].
- The pseudo-data was then used in a global fit to assess the impact of ATLAS data on constraining PDFs:



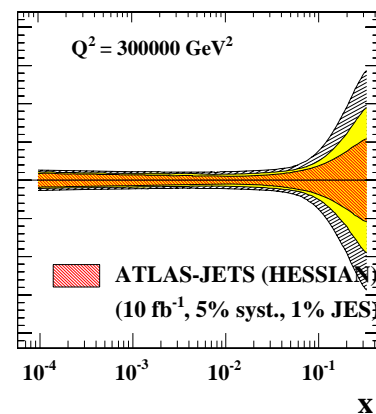
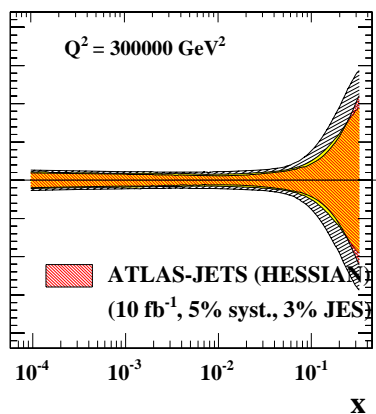
**Impact of increasing statistics**



**Impact of decreasing experimental systematic uncertainty**



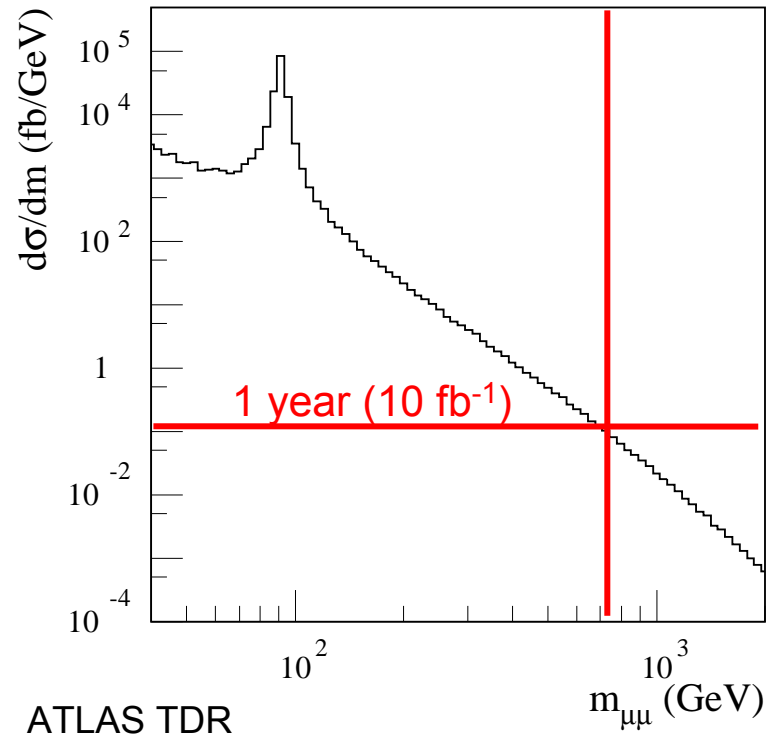
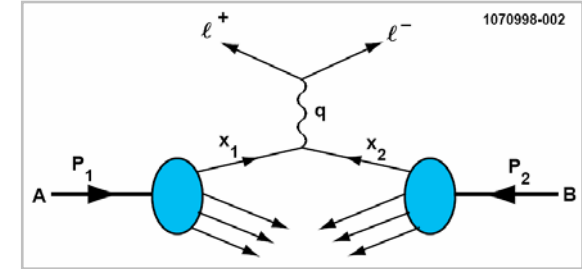
**Impact of decreasing experimental correlated systematic uncertainty**



**Challenging!**

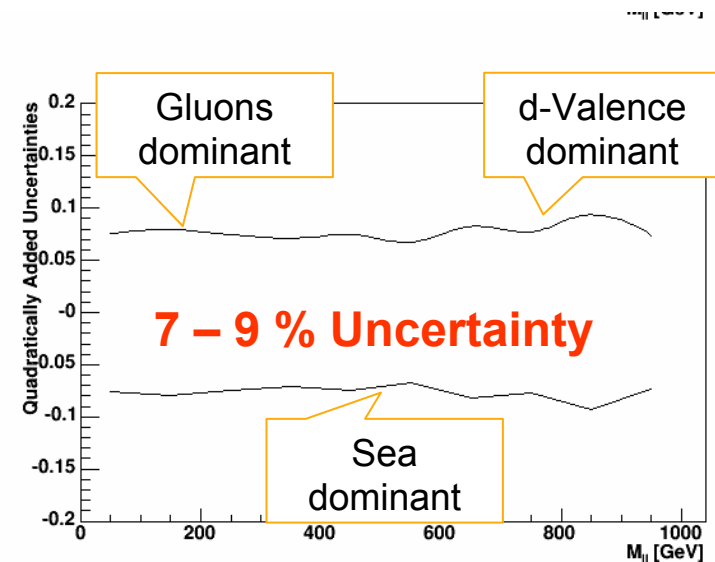
**Can we decrease Jet Energy Scale systematic to 1%?**

**But not all BSM physics is strongly compromised: e.g PDF Uncertainty in High-mass Drell-Yan- won't stop us seeing Z's**



dominant

**Different mass ranges have different contributions to the PDF uncertainty**



# Summary

**PDF uncertainties impact significantly on**

Precise  $W/Z$  cross-sections, **hence on use of these as luminosity monitor**  
(however  $Z/W$  ratio is a golden calibration measurement)

High  $E_t$  jet cross-sections, **hence on discovery of new physics which can be written in terms of contact interactions**

**PDF uncertainties will not obscure discovery of**

Higgs **in mass range 100-1000 GeV**

High mass  $Z'$  **in mass range 150-2500 GeV**

**Measurements from LHC itself may improve knowledge of**

Gluon PDF at low- $x$  ( $W$  prodn) and high- $x$  (high  $E_t$  jets)

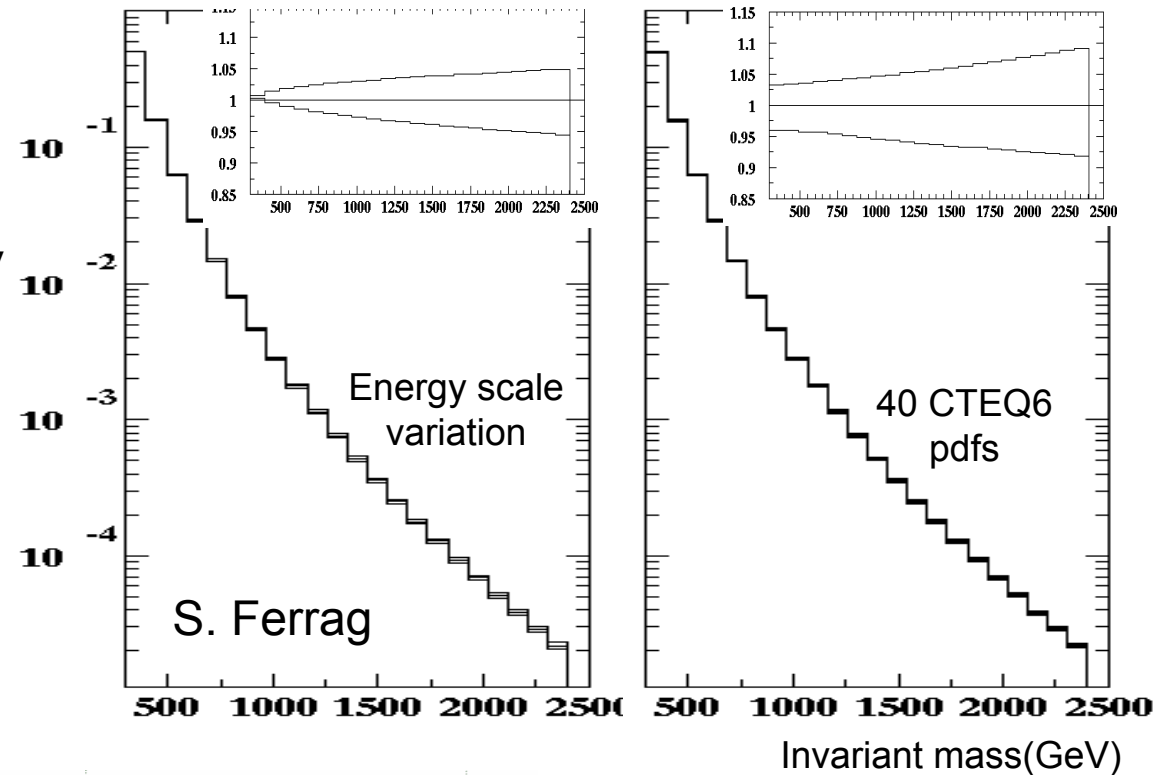
Low- $x$  valence PDFs (and maybe higher- $x$ )  $W$  asymmetry



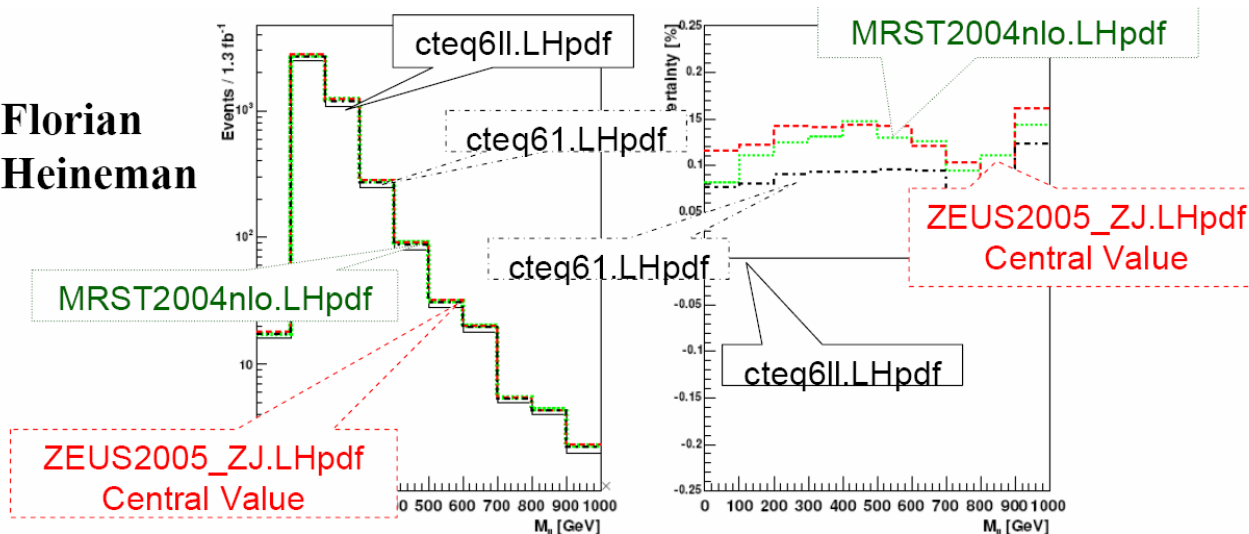
extras

# Standard Model side: Theoretical Uncertainties

- Generator level MC@NLO:  
 $\sigma$  computed by 100 GeV bin  
 $200 \text{ GeV} < \text{invMass} < 2500 \text{ GeV}$
- Sources of uncertainties:
  - Factorisation and Renormalisation scales  
 $1/\pi * m_t < \mu < \pi * m_t$
  - PDFs: CTEQ6



Florian  
Heineman



- Fully simulation level:  
 Sample Zee  $M > 150$ : 5114



## Top vs W cross section



- Plot predictions for 40 error pdf's (CTEQ6.1) for top and W cross sections at the Tevatron and LHC
- Not much correlation at Tevatron
  - ◆ big excursions caused by eigenvector 15; high x gluon
- Anti-correlation at LHC; more momentum for gluons, less for sea quarks (at lower x) that produce W's

