

Astrophysical Signatures of Dense Axion Clumps

Ani Prabhu (Stanford University)

10/27/2020



Based on work:

[arXiv:2006.10231](https://arxiv.org/abs/2006.10231)

[arXiv:2005.03700](https://arxiv.org/abs/2005.03700) (with Nicholas Rapidis)

Follow-up work in
progress with:

Harikrishnan Ramani (Stanford)
Ryan Janish (Fermilab)

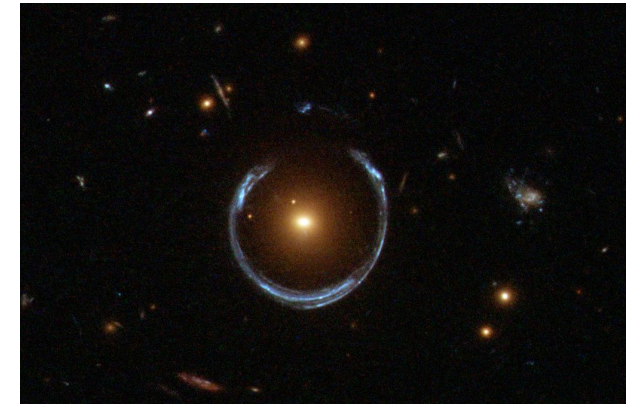
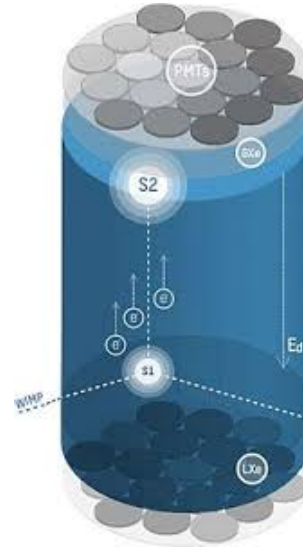
Overview

- I. Axions as DM Candidates
- II. Formation of Axion Clumps
- III. Non-gravitational Lensing Effects of Axion Clumps
- IV. Resonant Conversion of Axion Clumps Around NSs.
- V. Summary & Conclusions

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Dark Matter Candidates



Ultralight bosons

Axions, ALPs, Dilatons, Dark Photons

QCD Axion



Thermal DM

WIMPs



Non-thermal DM

PBHs

WIMPZILLAs



10^{-20}

10^{-10}

1

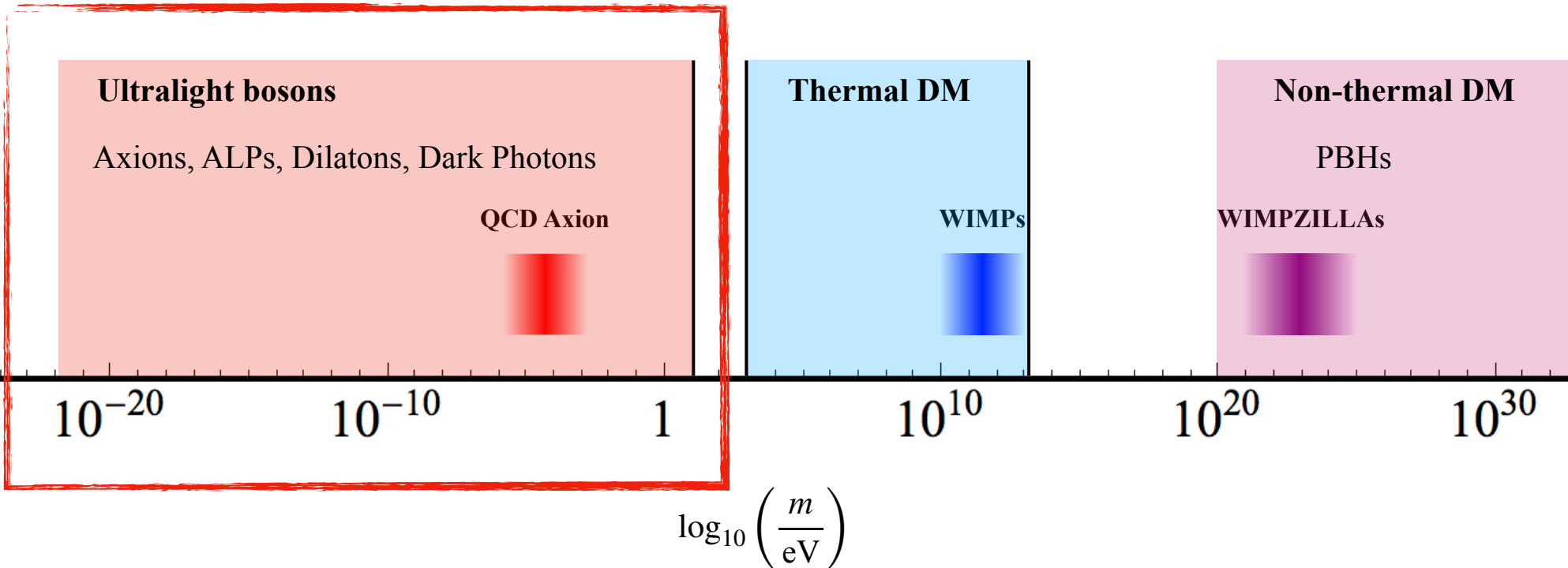
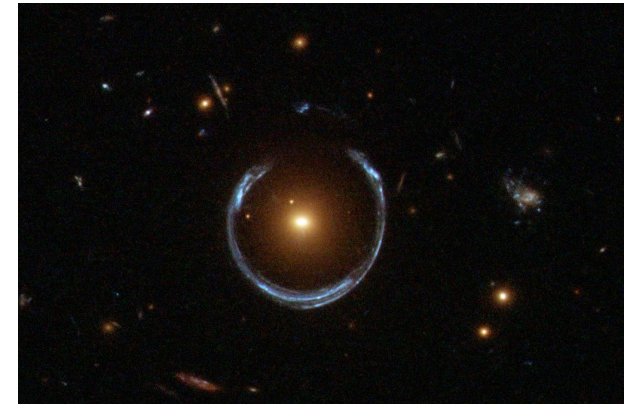
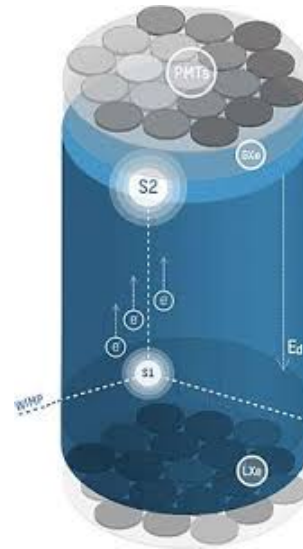
10^{10}

10^{20}

10^{30}

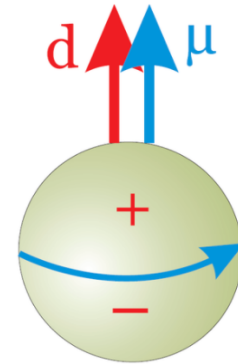
$$\log_{10} \left(\frac{m}{\text{eV}} \right)$$

Dark Matter Candidates



Strong- CP Problem & Axions

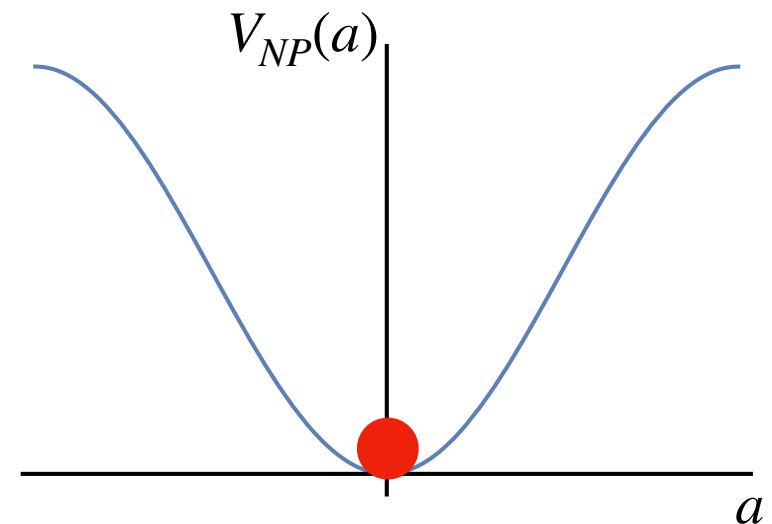
$$\mathcal{L}_{\text{QCD}} \supset \frac{\theta}{32\pi^2} \text{Tr} G_{\mu\nu} \tilde{G}^{\mu\nu}$$



- Upper bound on nEDM $\implies \theta_0 + \arg \det M_u M_d \lesssim 10^{-10}$.

- Peccei-Quinn Solution: $\theta \rightarrow a(x)/f_a$.

- Instantons generate potential, axion dynamically relaxes to CP -conserving value. Vafa & Witten (1984)



- Ubiquitous in String Theory. Svrček, Witten (2006)

Axions in String Theory

Arvanitaki, Dimopoulos, Dubovsky, Kaloper, March-Russell (2009)

p -Forms (A_p)

B_{MN} (NS), C_p (Ramond-Ramond), ...

+

Extra Dimensions

$$M = 0, 1, 2, 3, 4, \dots, D - 1$$

+

Compact Extra Dimensions

Non-trivial Topology



||

CP -odd scalars (axions)

$$A_p = \sum_{i=1}^{b_p} a_i(x) \omega_{p,i}(y)$$

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$$A_p = \sum_{i=1}^{b_p} a_i(x) \omega_{p,i}(y)$$

Misalignment Production

$$n_{DM} \lambda_a^3 \gg 1$$

$$(m_a \lesssim 1 \text{ eV})$$



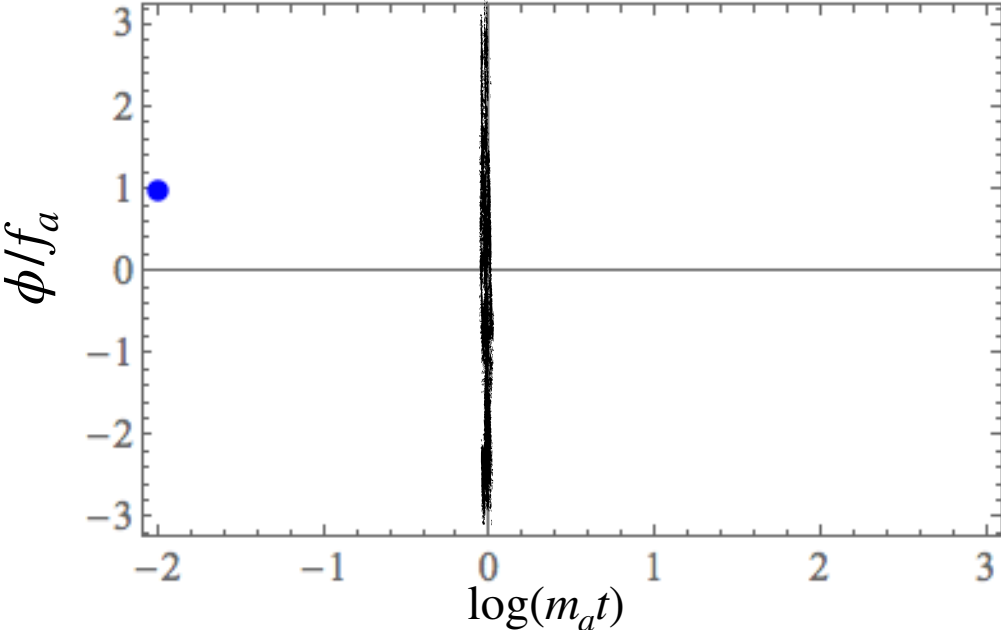
Axion: coherently oscillating field

$$\phi = \phi_0 \cos(m_a t + \varphi)$$

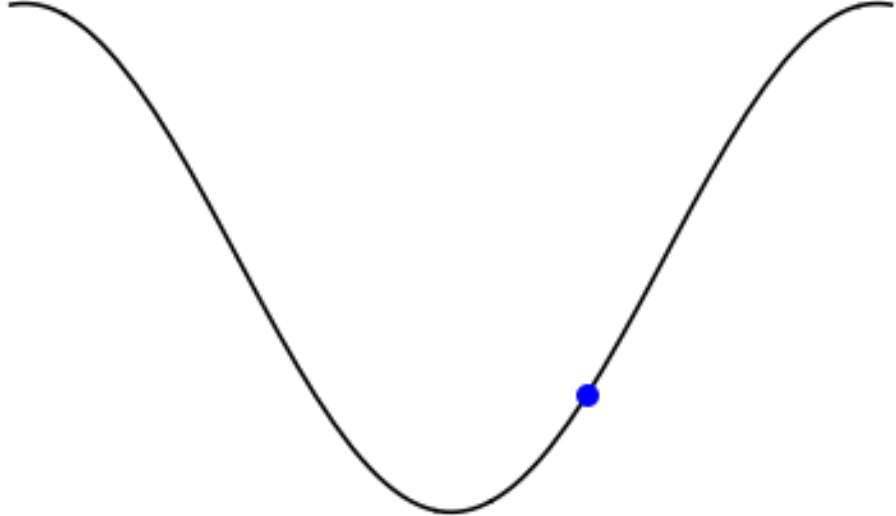


$$\ddot{\phi} + 3H\dot{\phi} + m_a^2\phi = 0$$

$$(\ddot{x} + \gamma\dot{x} + \omega^2x = 0)$$



Early time: $\rho_a \propto \text{constant}$
Dark Energy



Late time: $\rho_a \propto a^{-3}$
Dark Matter

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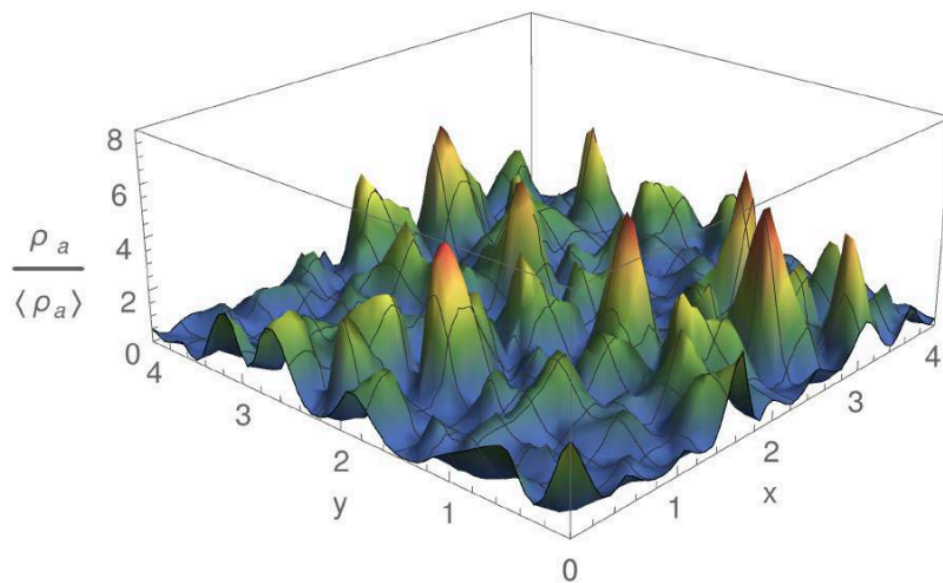
III. Non-gravitational Lensing Effects of Axion Clumps

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Axion Miniclusters

- Post-inflationary PQ SSB ($f_{PQ} < H_I/2\pi$).
- θ_{PQ} is drawn from $\mathcal{U}[-\pi, \pi]$ in each Hubble volume, uncorrelated across different volumes.
- $\mathcal{O}(1)$ fluctuations on horizon scale at symmetry breaking collapse to form **axion miniclusters (MCs)**.



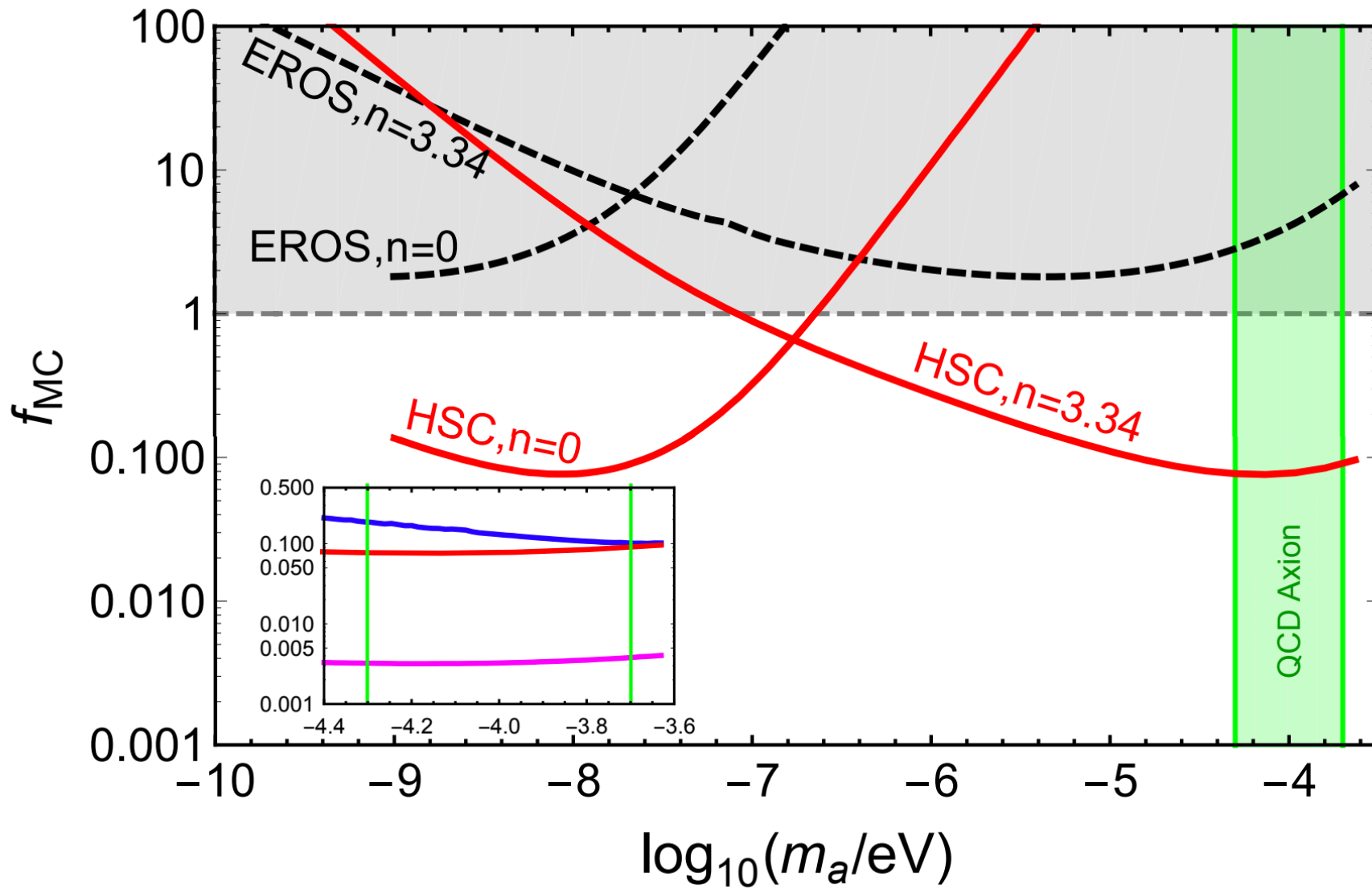
Hardy (2016)

- Present-day abundance of MCs with mass

$$M_{MC} = \frac{4\pi}{3} \left(\frac{\pi}{\mathcal{H}(t_0)} \right)^3 \rho_{0,a} \simeq 2 \times 10^{-13} M_{\odot} \left(\frac{m_a}{10^{-6} \text{ eV}} \right)^{-3/2}$$

$$T_{\text{coll}} = T_{\text{eq}}(1 + \Phi)$$

$$\rho_{MC} \simeq 7 \times 10^6 \Phi^3 (1 + \Phi) \text{ GeV/cm}^3 \quad \bar{\rho}_{CDM} \simeq 0.3 \text{ GeV/cm}^3$$



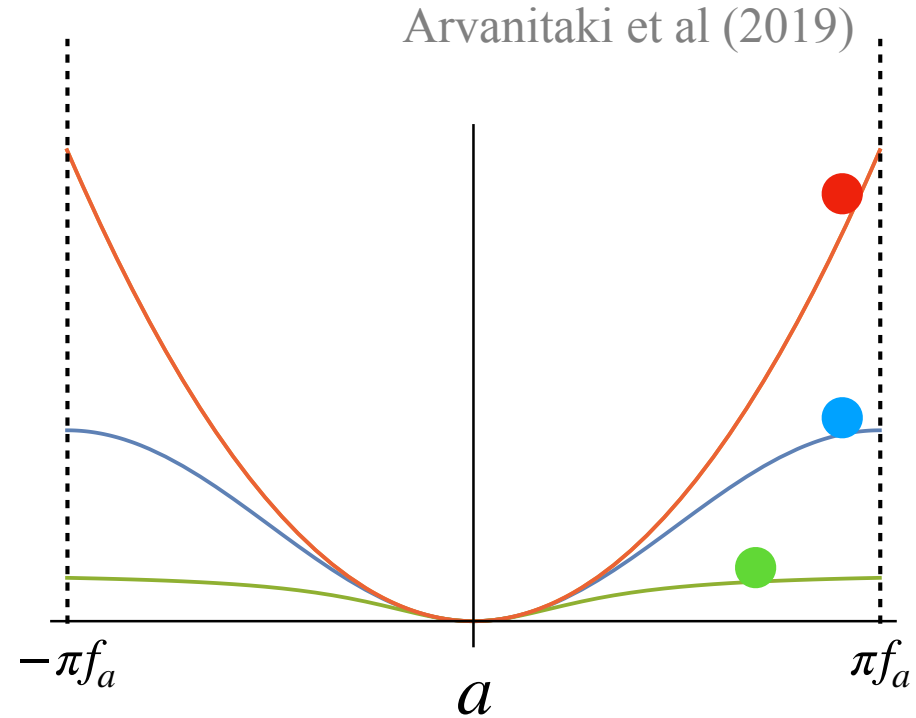
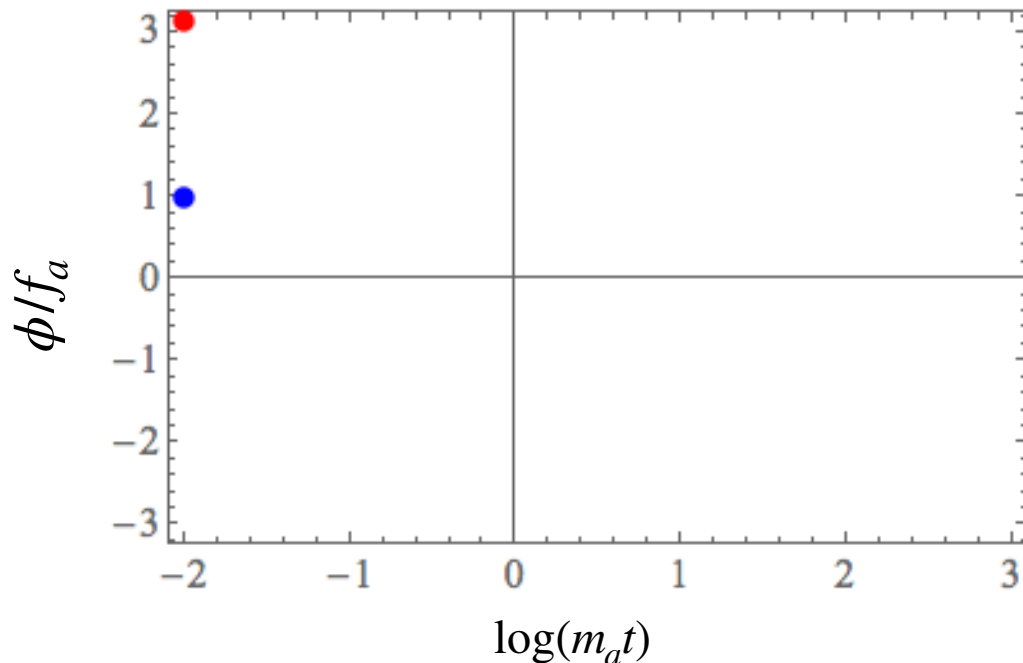
Fairbairn, Marsh, Quevillon & Rozier (2017)

Large Misalignment Mechanism

- At high ϕ_i dynamics probe the full, non-harmonic potential.

$$\ddot{\phi} + 3H\dot{\phi} + V'(\phi) = 0$$

- Delay in the onset of oscillations.



Parametric resonant growth of modes with wavelength $\lambda \sim 2\pi/m_a$ at time oscillations begin.

$$M \simeq 5 \times 10^{-15} M_{\odot} \left(\frac{m_a}{10^{-6} \text{ eV}} \right)^{-3/2}$$

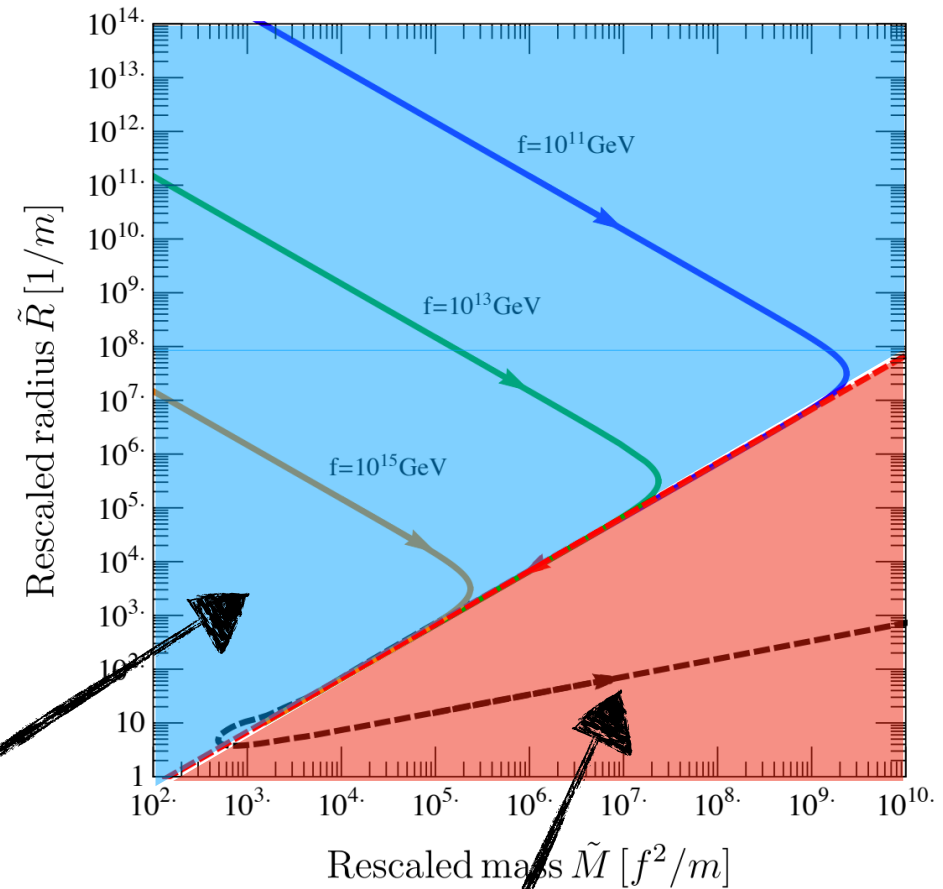
$$\rho \sim 10^3 - 10^7 \rho_{\text{CDM}}$$

Femtohalos

Solitons and Oscillons

- At very high misalignment ($\phi_i/f_a - \pi \ll 1$), collapse may take place deep into RD, giving ultradense structures.
- At small scales, scalar field dynamics become important.

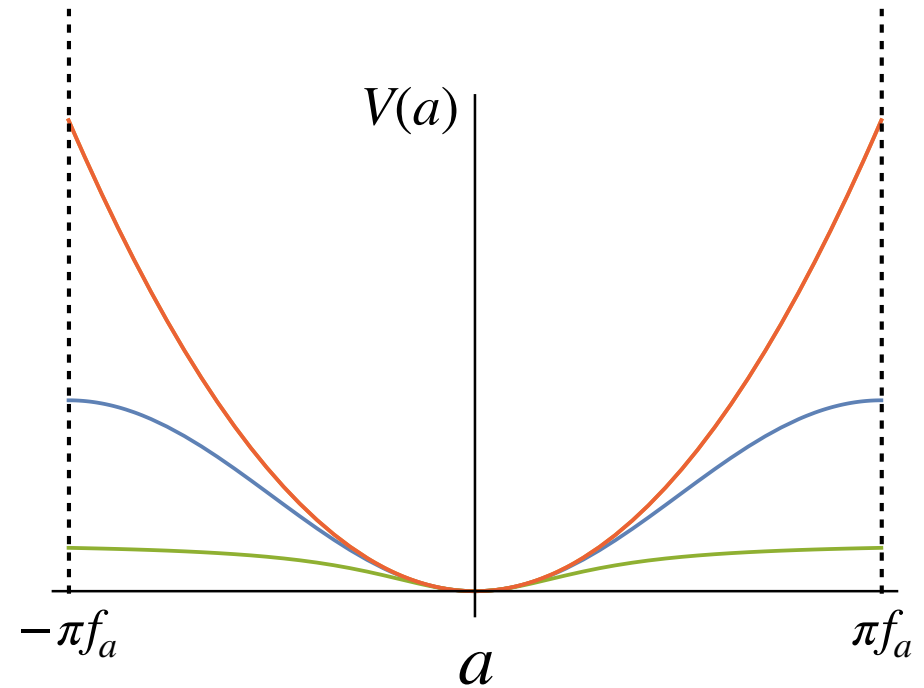
Hydrostatic equilibrium of **quantum pressure + gravity = solitons**



Hydrostatic equilibrium of **quantum pressure + attractive self-interactions = oscillons**

Oscillon Phenomenology

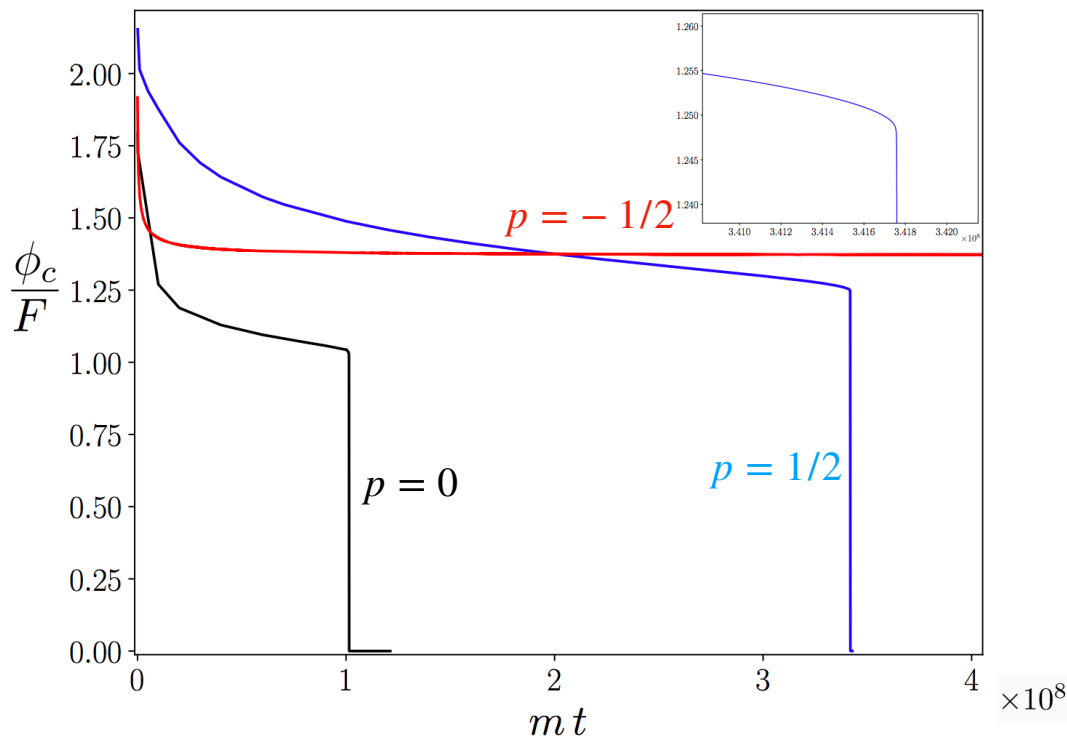
- Central axion amplitude $a_0 \gtrsim f_a$, central density $\rho_0 \sim m_a^2 f_a^2$.
- Metastable**, QCD axion lifetime $\tau_{QCD} \lesssim 10^3/m_{a'}$ decay before matter-radiation equality.



$$V(a) = \frac{1}{2} m_a^2 a^2$$

$$V(a) = m_a^2 f_a^2 \left[1 - \cos\left(\frac{a}{f_a}\right) \right]$$

$$V(a) = \frac{m_a^2 f_a^2}{2p} \left[\left(1 + \frac{a^2}{f_a^2} \right)^p - 1 \right]$$



Ollé, Pujolàs & Rompineve (2019)

Summary of Axion Clumps

$$m_a = 10^{-6} \text{ eV}, f_a = 10^{12} \text{ GeV}$$

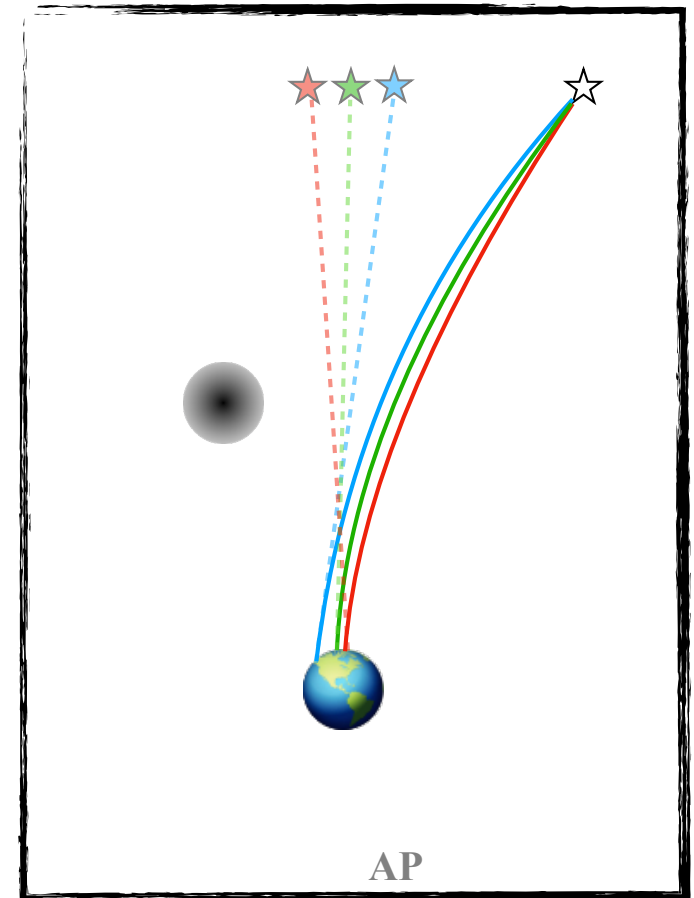
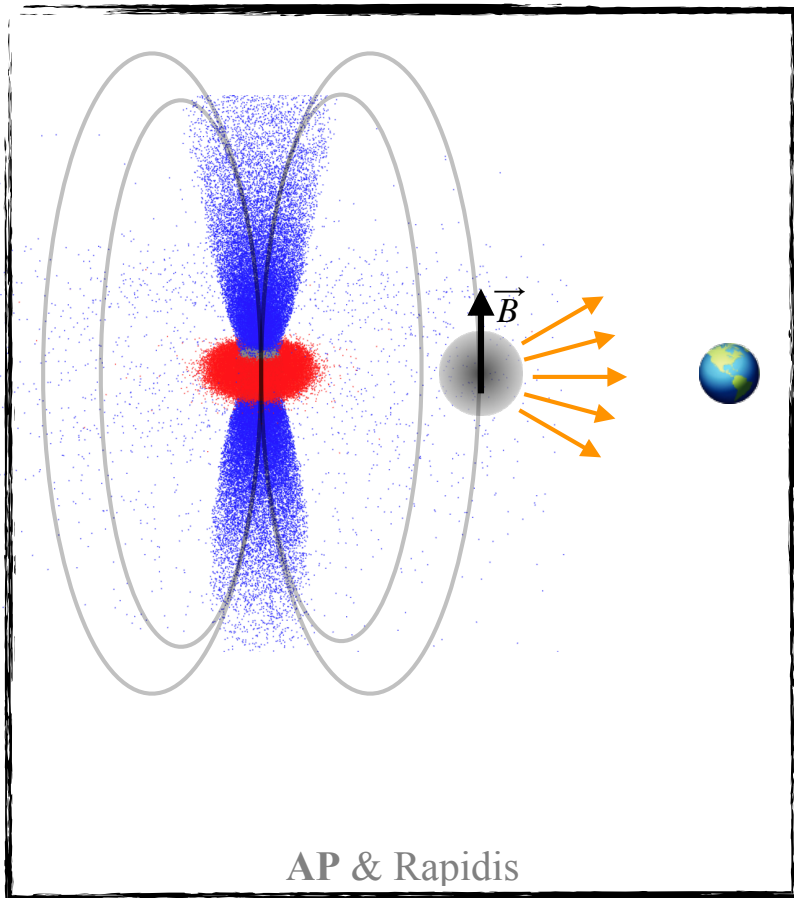
Density



Clump	Mass	Density
CDM Halo	$\sim 10^{12} M_\odot$	0.3 GeV/cm^3
Femtohalo	$\sim 5 \times 10^{-15} M_\odot$	$(10^3 - 10^7) \bar{\rho}_{CDM}$
Minicluster	$\sim 2 \times 10^{-13} M_\odot$	$(10^8 - 10^{12}) \bar{\rho}_{CDM}$
Soliton	$\lesssim 6 \times 10^{-11} M_\odot$	$\lesssim 10^{29} \bar{\rho}_{CDM}$
Oscillon	$\sim 10^{-15} M_\odot$	$\sim 10^{36} \bar{\rho}_{CDM}$

Non-Gravitational Signatures of Axion Clumps

$$\mathcal{L} \supset -\frac{g_{a\gamma\gamma}}{4} a \tilde{F}^{\mu\nu} F_{\mu\nu} = -g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B}$$



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Axion Electrodynamics

$$\nabla \cdot \mathbf{E} = 0$$

$$\nabla \times \mathbf{E} = - \frac{\partial \mathbf{B}}{\partial t}$$

$$\nabla \cdot \mathbf{B} = 0$$

$$\nabla \times \mathbf{B} = \frac{\partial \mathbf{E}}{\partial t}$$

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$$\nabla \times \mathbf{B} = \frac{\partial \mathbf{E}}{\partial t} + g_{a\gamma\gamma} (\dot{\mathbf{a}} \mathbf{B} + \nabla a \times \mathbf{E})$$

- Modification to photon dispersion relation: refraction, spectral distortions, group delays, etc.

$$\omega(\mathbf{k}, \sigma) = |\mathbf{k}| + \sigma \frac{g_{a\gamma\gamma}}{2} \left[\dot{a} + \hat{\mathbf{k}} \cdot \nabla a \right] + \frac{g_{a\gamma\gamma}^2}{16|\mathbf{k}|} \left[\dot{a}^2 - 2(\nabla a)^2 + (\hat{\mathbf{k}} \cdot \nabla a)^2 \right] + \mathcal{O} \left((g_{a\gamma\gamma} a)^3 \right)$$

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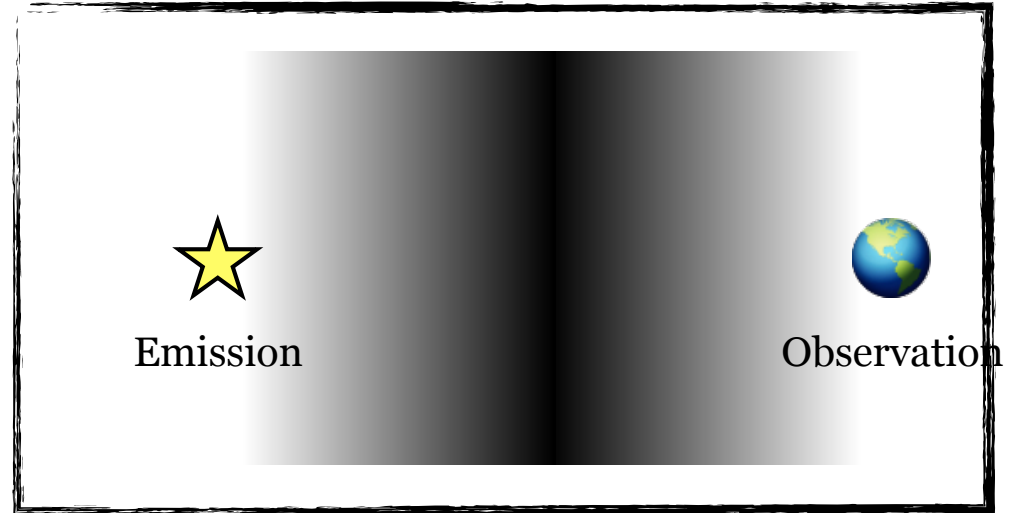
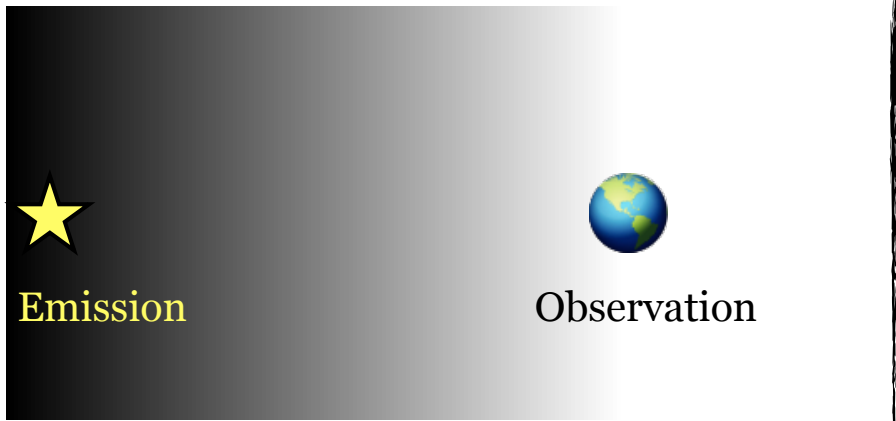
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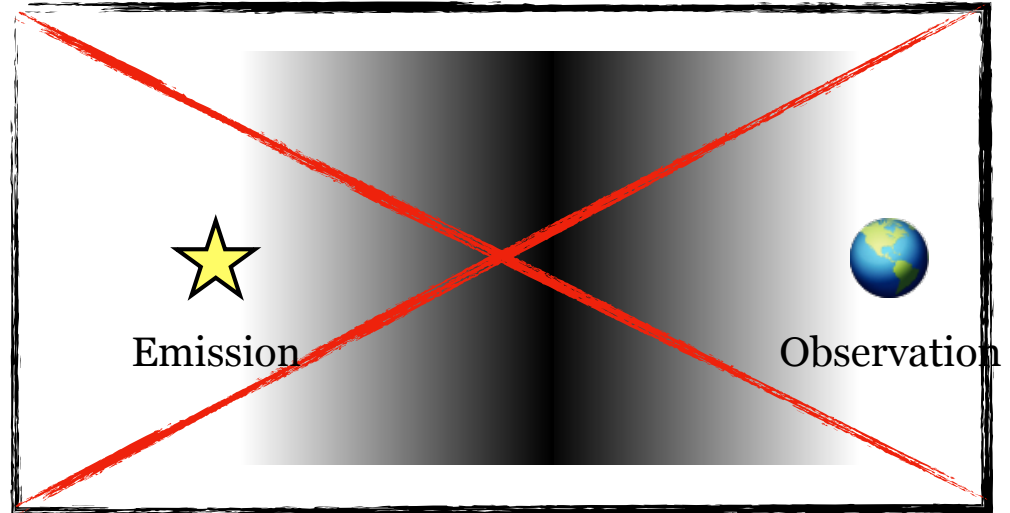
Optical Effects at $\mathcal{O}(g_{\alpha\gamma})$

- Linear-order term is a total derivative and only contributes through boundary terms.



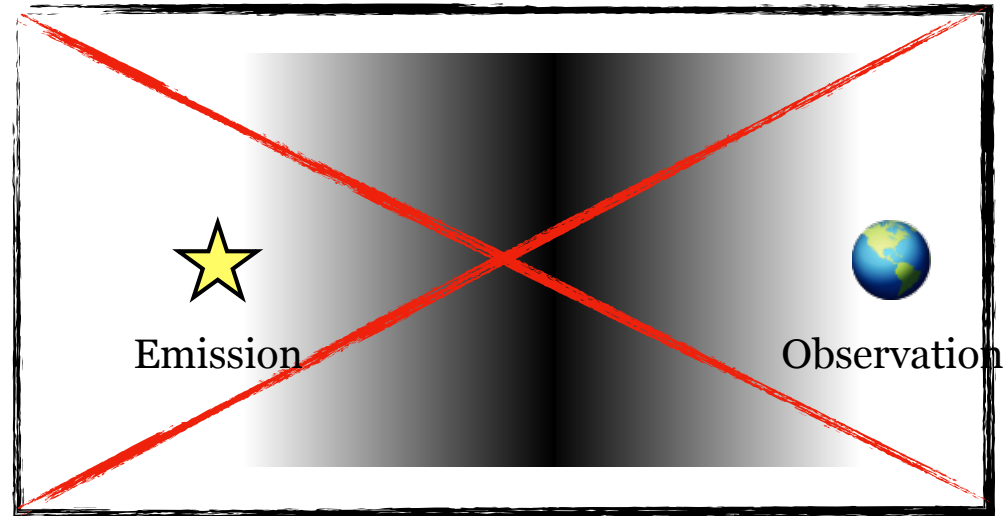
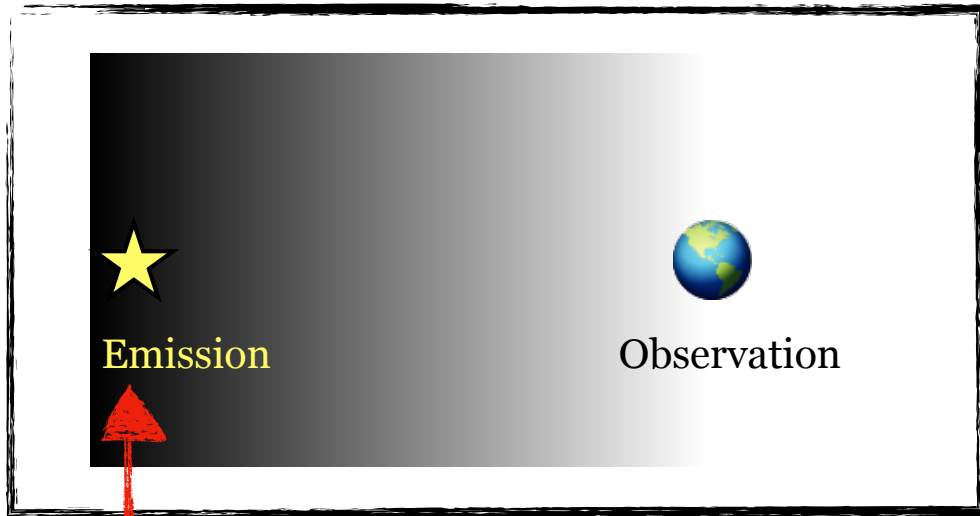
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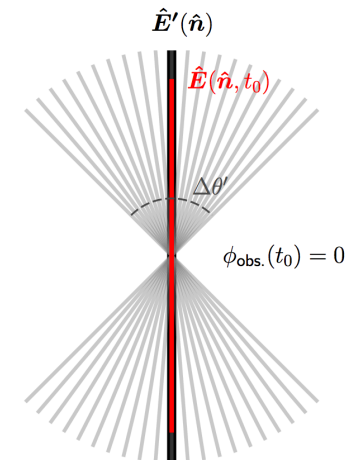
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CMB

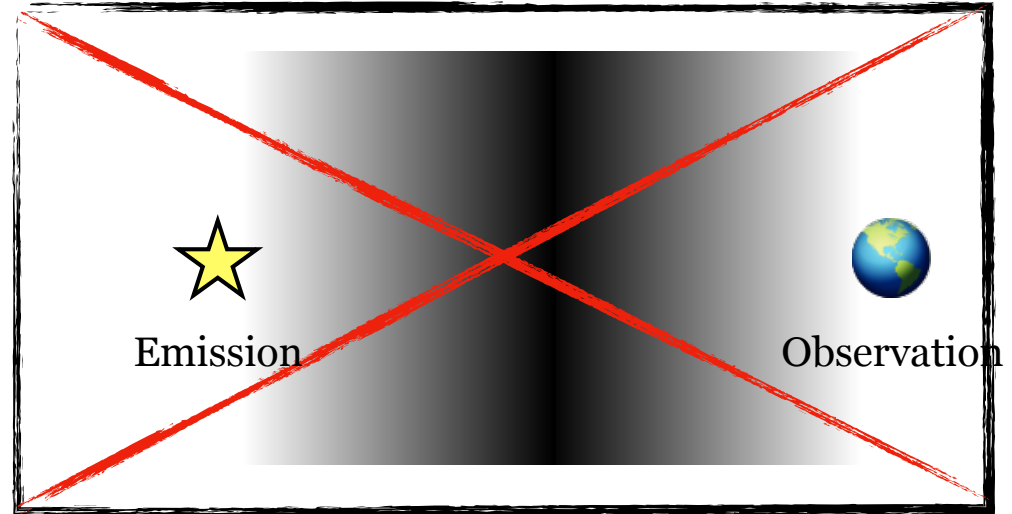
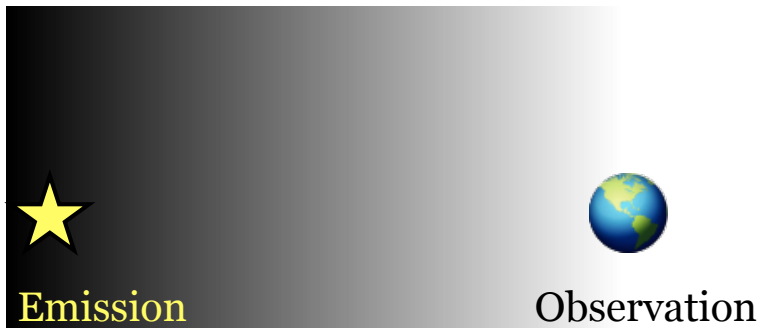
Relative phase shift
between LHCP, RHCP light

$$\delta\phi \sim g_{\alpha\gamma} [a(t_{em}, \mathbf{x}_{em}) - a(t_{obs}, \mathbf{x}_{obs})]$$



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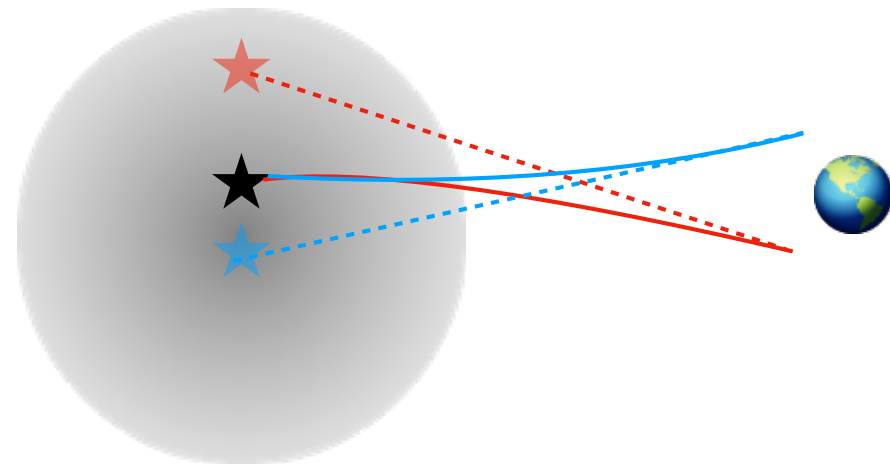
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Birefringent refraction

$$\frac{\delta \mathbf{k}}{k} \sim g_{\alpha\gamma} \left[\nabla_{\perp} a(t_{em}, \mathbf{x}_{em}) - \nabla_{\perp} a(t_{obs}, \mathbf{x}_{obs}) \right]$$

∇_{\perp} : Transverse gradient



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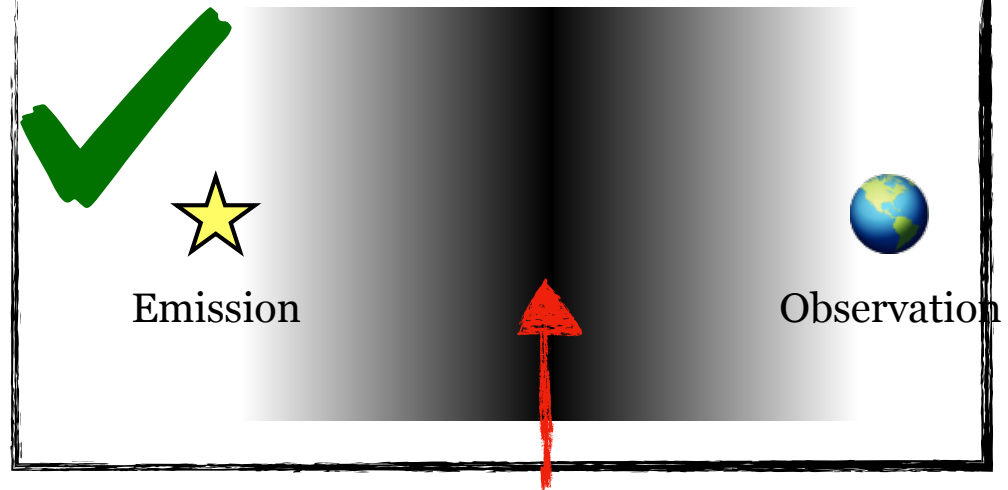
Refraction at $\mathcal{O}(g_{a\gamma\gamma}^2)$

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Bending Angle

$$\delta\theta = \frac{g_{a\gamma\gamma}^2}{8|\mathbf{k}_0|^2} \int_{t_{\text{em}}}^{t_{\text{obs}}} \nabla_{\perp} \dot{a}^2(t', \mathbf{x}_0(t'; \xi)) dt'$$

Gaussian Profile

$$\delta\theta \sim \frac{g_{a\gamma\gamma}^2 a_0^2}{|\mathbf{k}_0|^2} \left(\frac{b}{R_a} \right) e^{-b^2/R_a^2}$$

b : Impact parameter

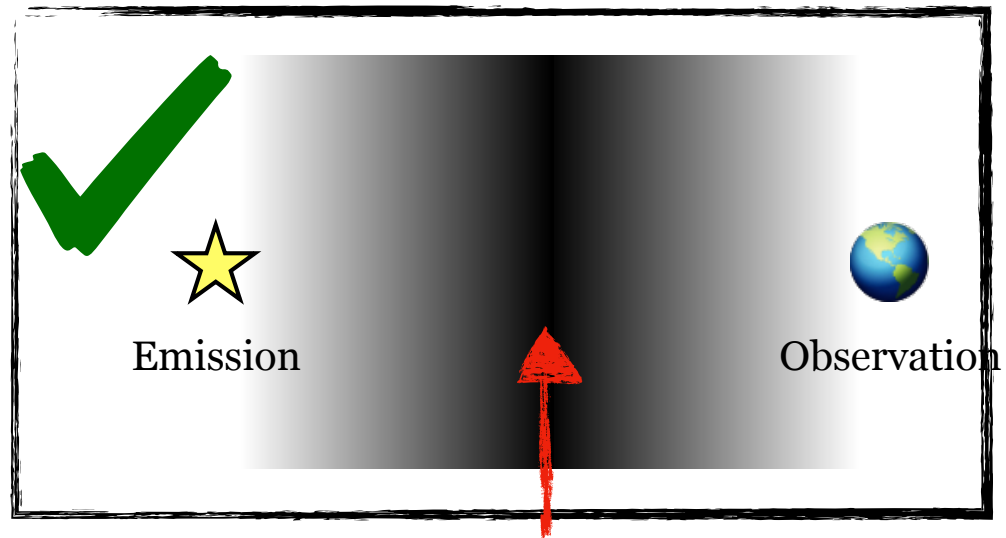
R_a : Axion star radius

a_0 : Central axion density

Axions Stars, Halos

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Effects stronger at low frequency \implies **radio** observations

Axions Stars, Halos

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Lensing Effects: **Axions** vs. **Gravity**

Magnitude (Oscillons)

$$\delta\theta_a(b = R_a) \approx 10^{-6} \text{ rad} \left(\frac{\phi_0}{f_a} \right)^2 \left(\frac{m_a}{\omega} \right)^2 \quad (\text{Axions})$$

$$\delta\theta_G(b = R_a) \approx 10^{-10} \text{ rad} \left(\frac{f_a}{10^{12} \text{ GeV}} \right)^2 \left(\frac{m_a R_a}{10} \right)^2 \quad (\text{Gravity})$$

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Dispersion

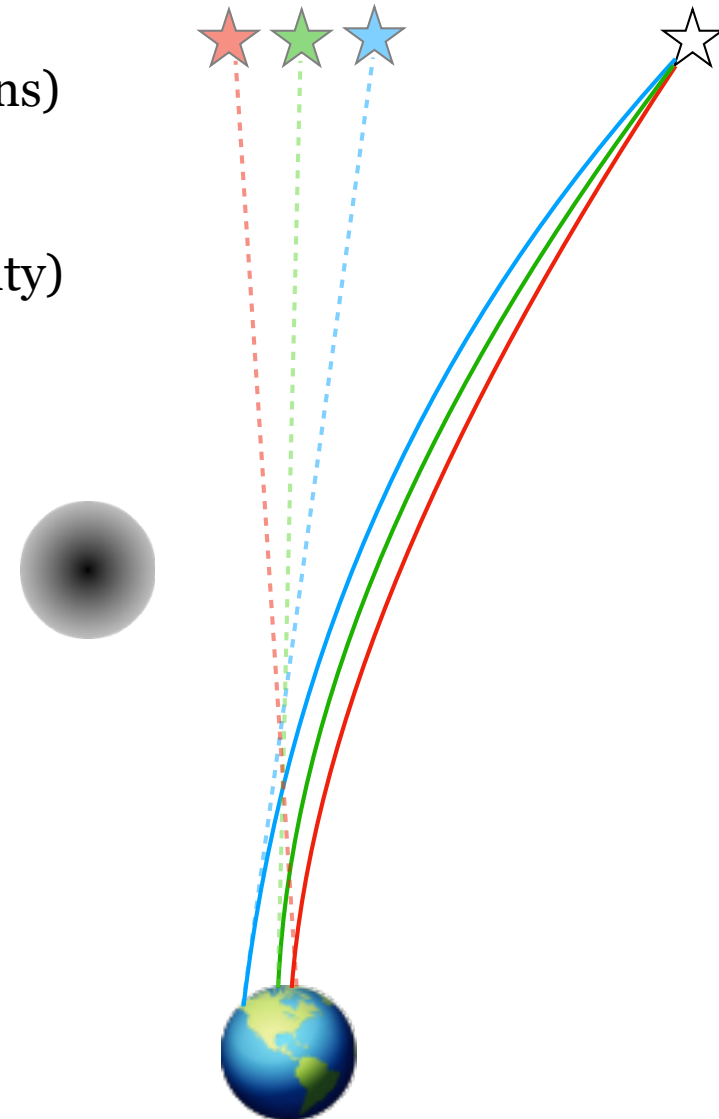
Axion: Dispersive

Gravity: Achromatic



Can be differentiated by multi-wavelength observations.

We can search for such lensing signatures with high-precision astrometric missions (SKA).



Observation with SKA

- Lensing of background radio sources by axion stars leads to apparent positional shifts.
- SKA can make astrometric measurements of background radio sources reaching $\sim \mu\text{as}$ precision.

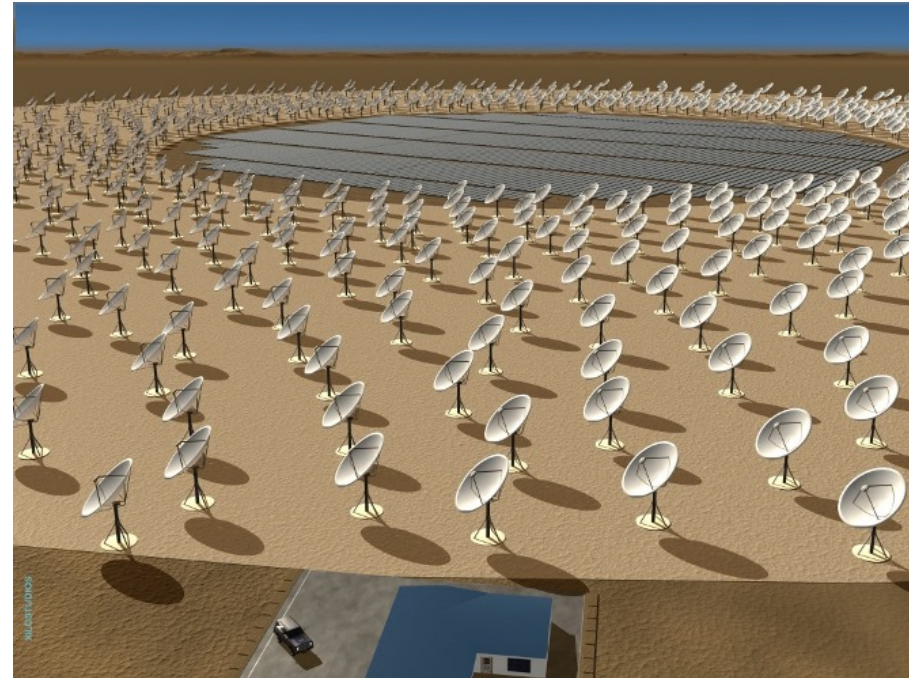


Figure: NAOC

- High-cadence monitoring of background radio source positions can give information about dark matter subhalos.

van Tilburg et al (2018)

Observables

- Candidate signals: close approach between AS and one (mono-blip) or multiple (multi-blip) background radio sources.

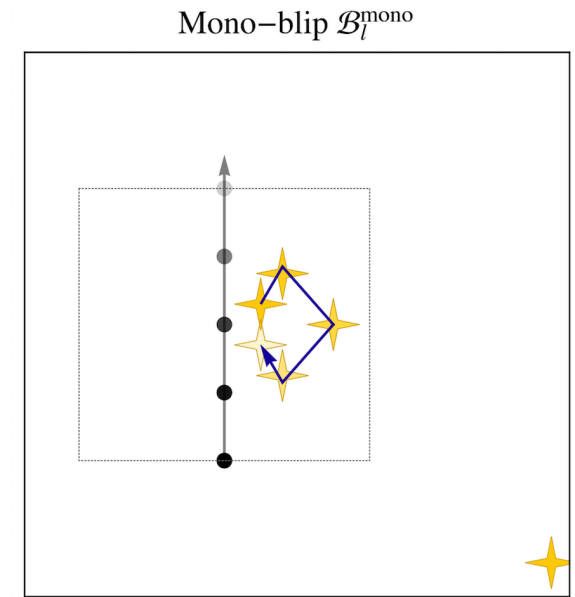
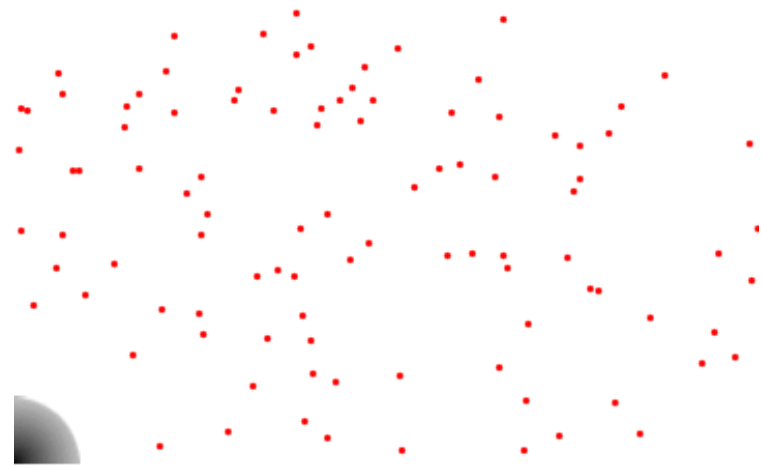


Figure: van Tilburg et al (2018)



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Mono-blip Statistic

$$\mathcal{B}_{mono}[\mathbf{x}_\ell(t)] = \frac{1}{\sigma_{\delta\theta}^2} \sum_n \delta\theta_a(\mathbf{x}_\ell(t_n)) \cdot \Delta\theta(t_n)$$

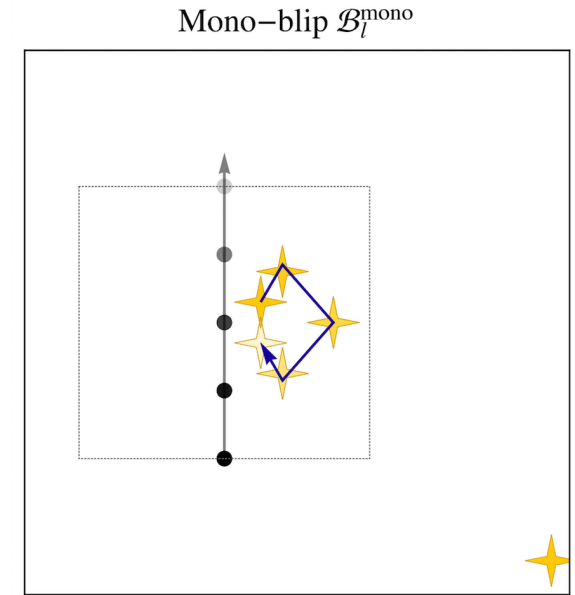
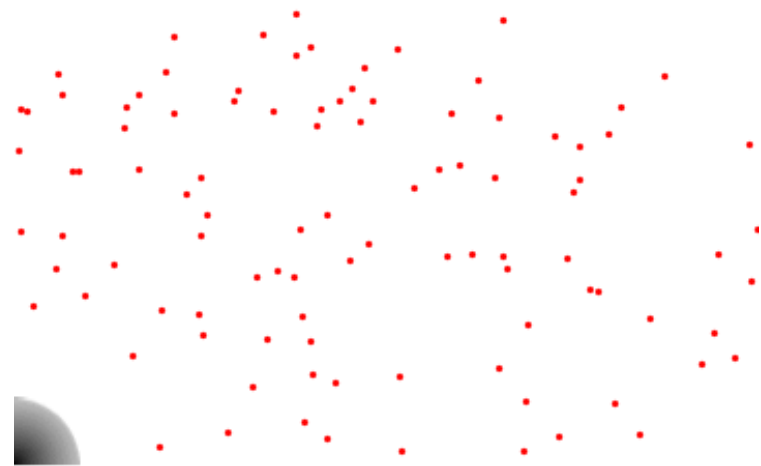


Figure: van Tilburg et al (2018)

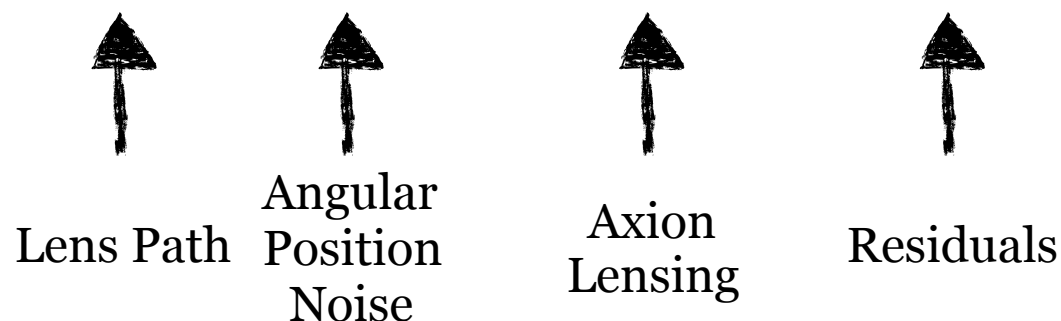


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- $\text{SNR} \propto \langle \mathcal{B}[\mathbf{x}_\ell(t)] \rangle^{1/2}$.

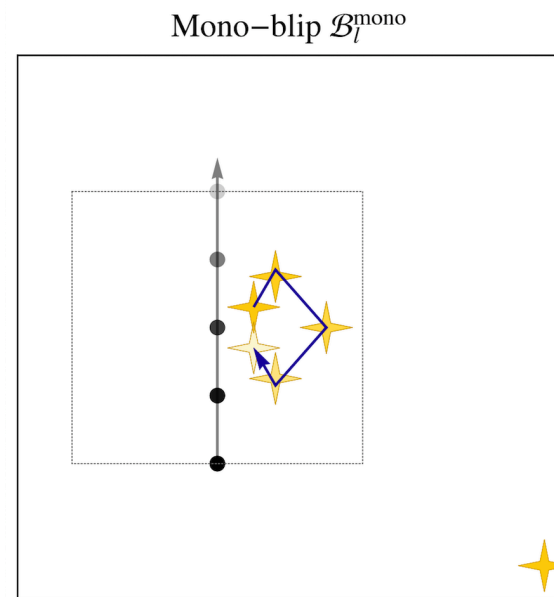
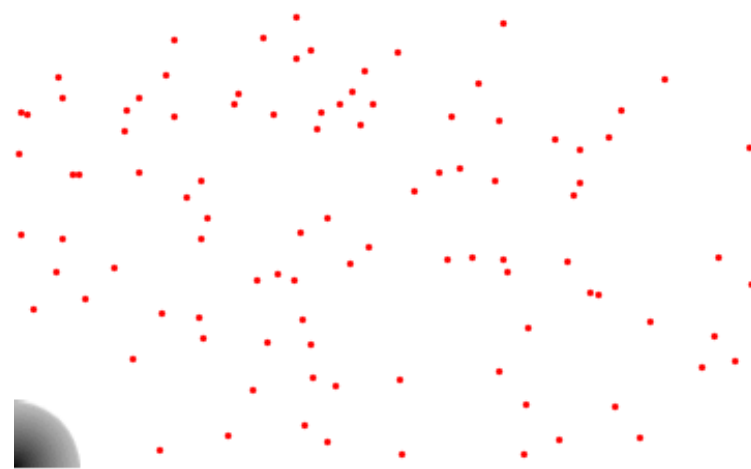
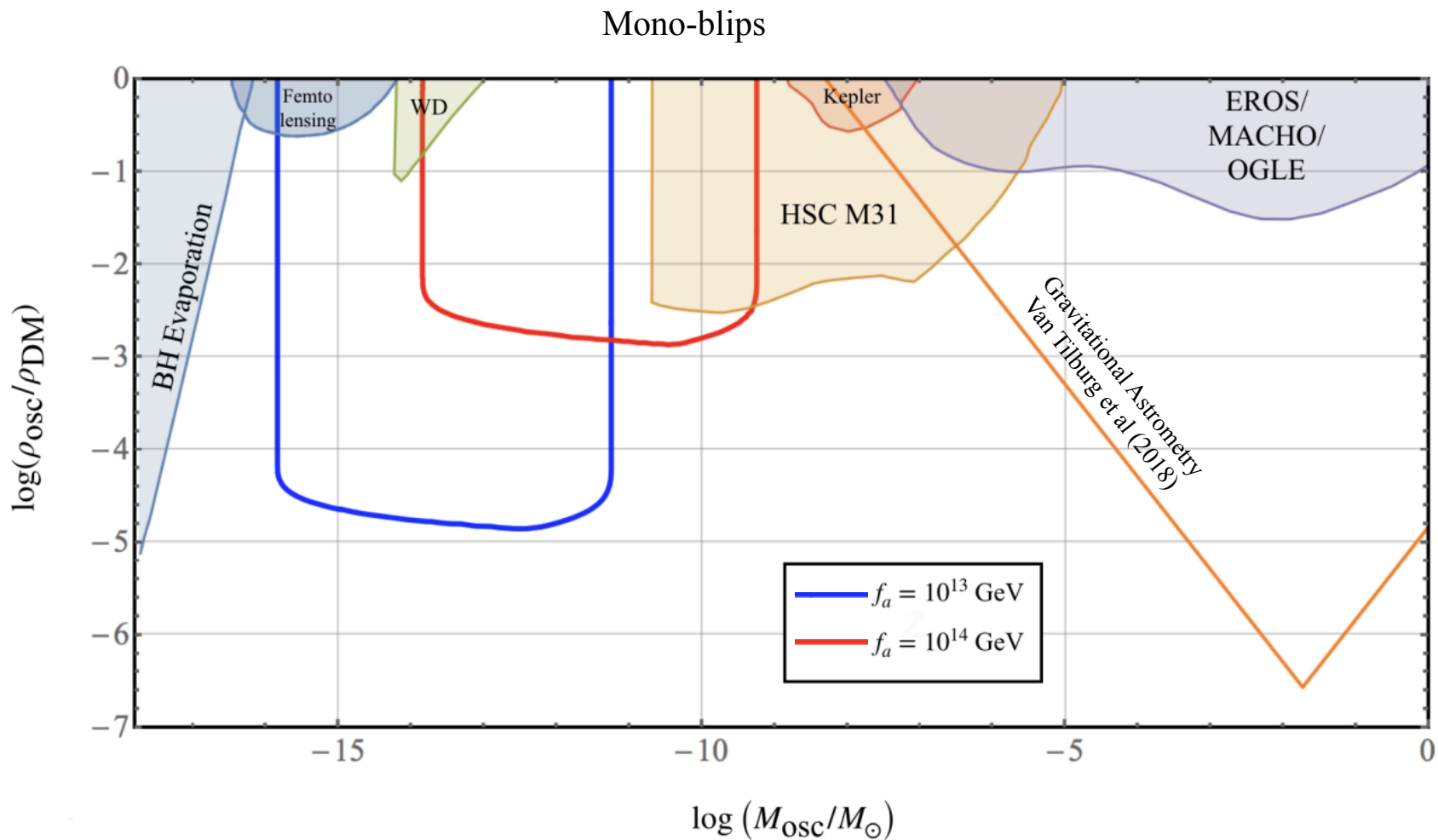


Figure: van Tilburg et al (2018)



Oscillon Sensitivity

- Daily measurements of 10^8 radio sources with angular precision $\sigma_{\delta\theta} = 10 \mu\text{as}$.

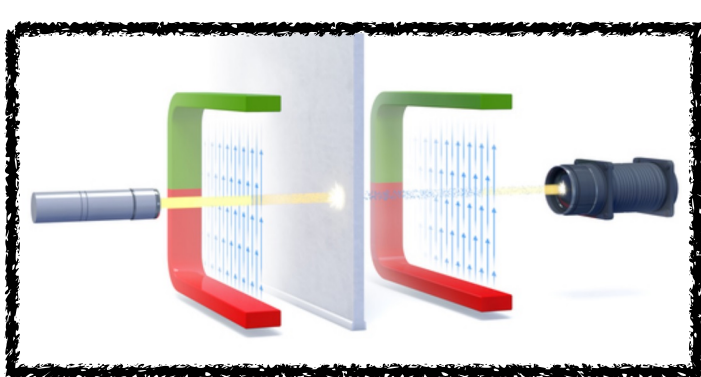
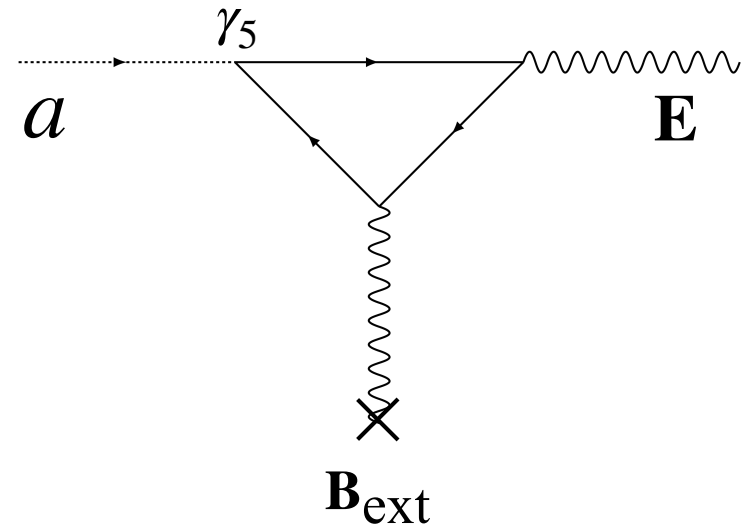


Overview

- I. Axions as DM Candidates
- II. Formation of Axion Clumps
- III. Non-gravitational Lensing Effects of Axion Clumps
- IV. Resonant Conversion of Axion Clumps Around NSs.
- V. Summary & Conclusions

Axion-Photon Coupling

$$\mathcal{L} \supset -\frac{g_{a\gamma\gamma}}{4} a \tilde{F}^{\mu\nu} F_{\mu\nu} = -g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B}$$



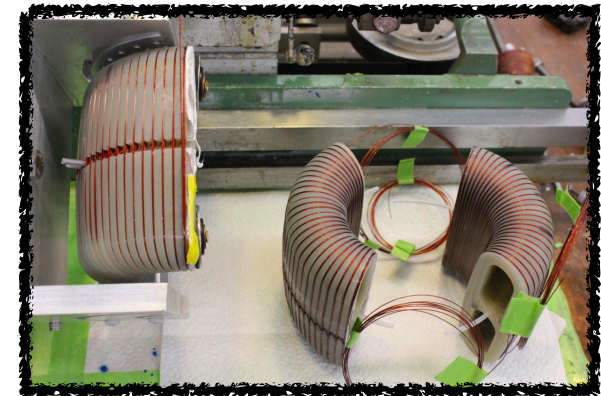
Light Shining Through Walls

Figure: DESY



ADMX

Figure: Scientific American



ABRACADABRA

Kahn, Safdi, Thaler (2016)

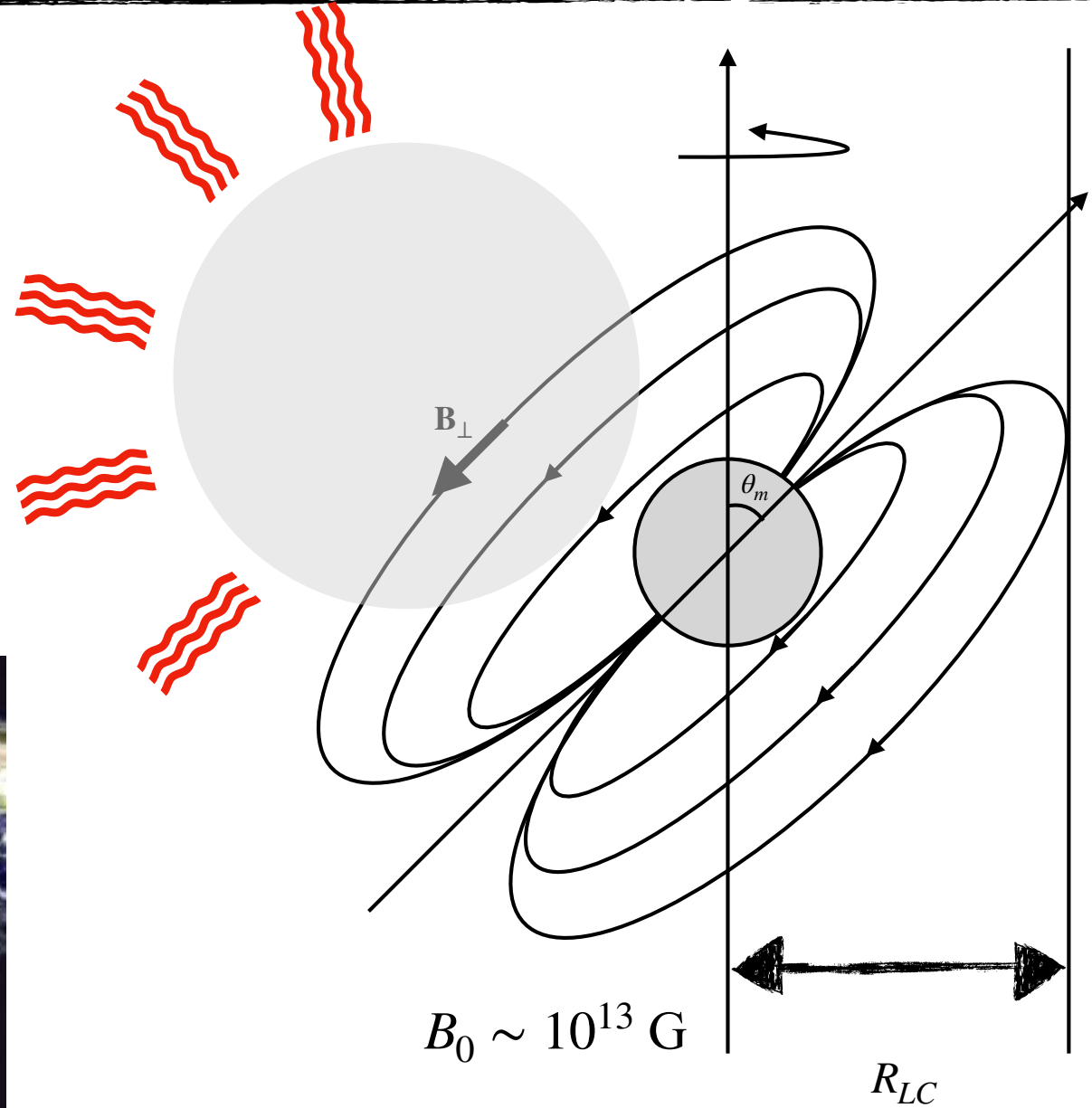
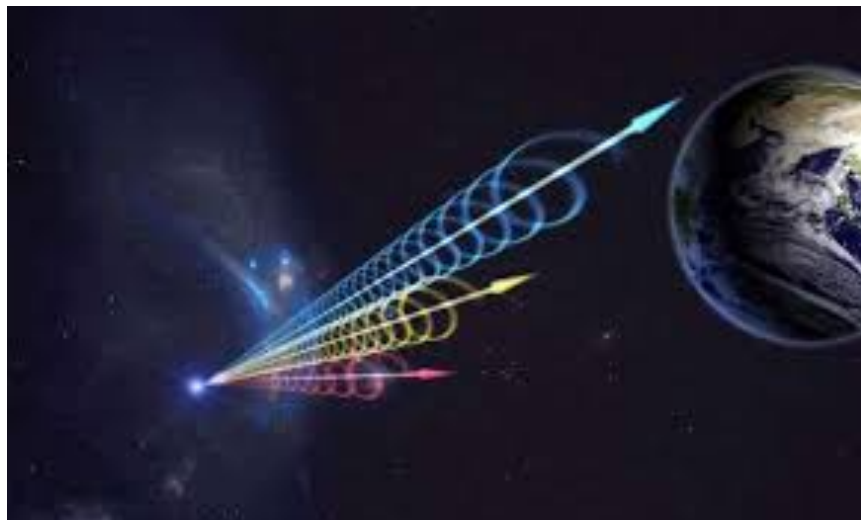
AS-NS Collisions

Axion Miniclusters
Tkachev (2014)

Solitons
Iwazaki (2014)



Fast Radio Bursts?



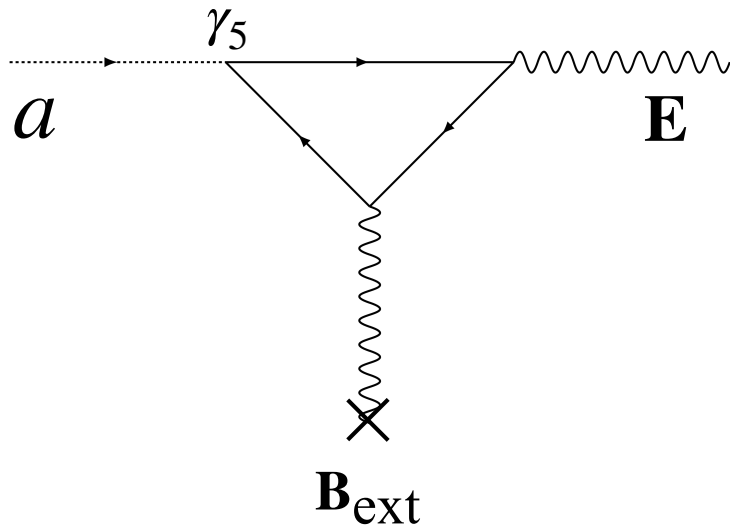
Non-Resonant Conversion

Axion-Photon Conversion

$$\mathcal{L} = g_{a\gamma\gamma} a \mathbf{E} \cdot \mathbf{B}_{ext}$$



CAST: Wikipedia



$$m_a = \omega, \quad p_a \neq p_\gamma$$

Non-resonant Conversion

$$P_{a \rightarrow \gamma} = \left(g_{a\gamma\gamma} |\mathbf{B}_{ext}| L \right)^2 \begin{cases} L_{app} & \Delta k L_{app} \ll 1 \\ \frac{\omega}{m_a^2} & \Delta k L_{app} \gg 1 \end{cases}$$

Resonant Conversion

Raffelt, Stodolsky (1988)
Hook, Kahn, Safdi, Sun (2018)

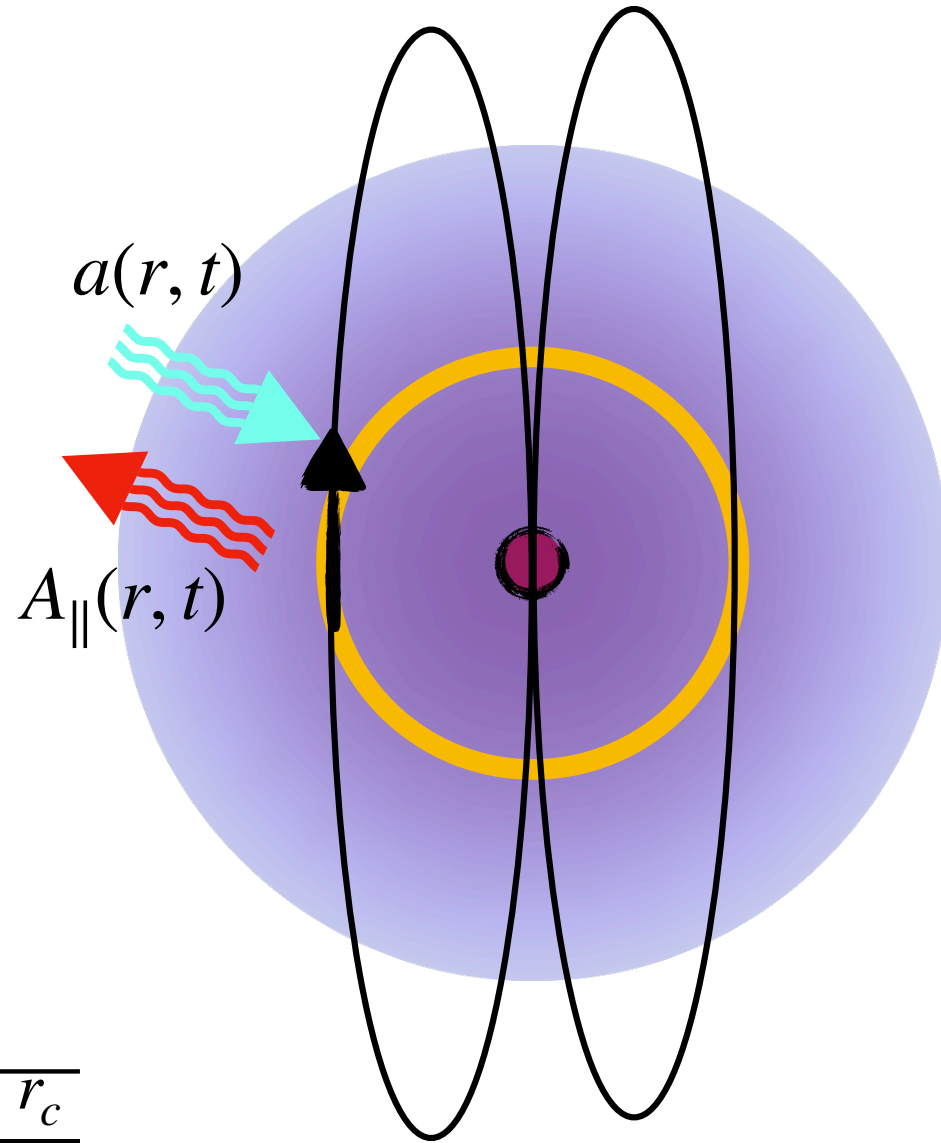
- Pulsars possess large \vec{B} -fields and a spatially varying plasma density.

Goldreich-Julian Model

$$\omega_p(r) \sim 20 \mu\text{eV} \left(\frac{B_0}{10^{13} \text{ G}} \right)^{1/2} \left(\frac{r}{r_{NS}} \right)^{-3/2}$$

- At some "critical" radius r_c , $\omega_p(r_c) = m_a$ and axions may resonantly convert to photons.

$$P_{a \rightarrow \gamma} \approx g_{a\gamma\gamma}^2 B(r_c)^2 L_{eff}^2 \quad L_{eff} = \sqrt{\frac{r_c}{m_a}}$$



Resonant Conversion of Oscillons

- In order for resonant conversion to take place, the axion star must remain tidally stable until it reaches r_c .

Resonant Conversion of Oscillons

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Femtohalo



Minicluster



Soliton



Oscillon



Resonant Conversion of Oscillons

- In order for resonant conversion to take place, the axion star must remain tidally stable until it reaches r_c .

Femtohalo



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Soliton



Oscillon



$$\Phi = \frac{P}{4\pi d^2 (m_a/2\pi)} = 8.2 \times 10^4 \text{ Jy} \left(\frac{B_0}{10^{14} \text{ G}} \right)^{1/6} \left(\frac{m_a}{10^{-6} \text{ eV}} \right)^{5/3} \left(\frac{d}{1 \text{ kpc}} \right)^{-2}$$

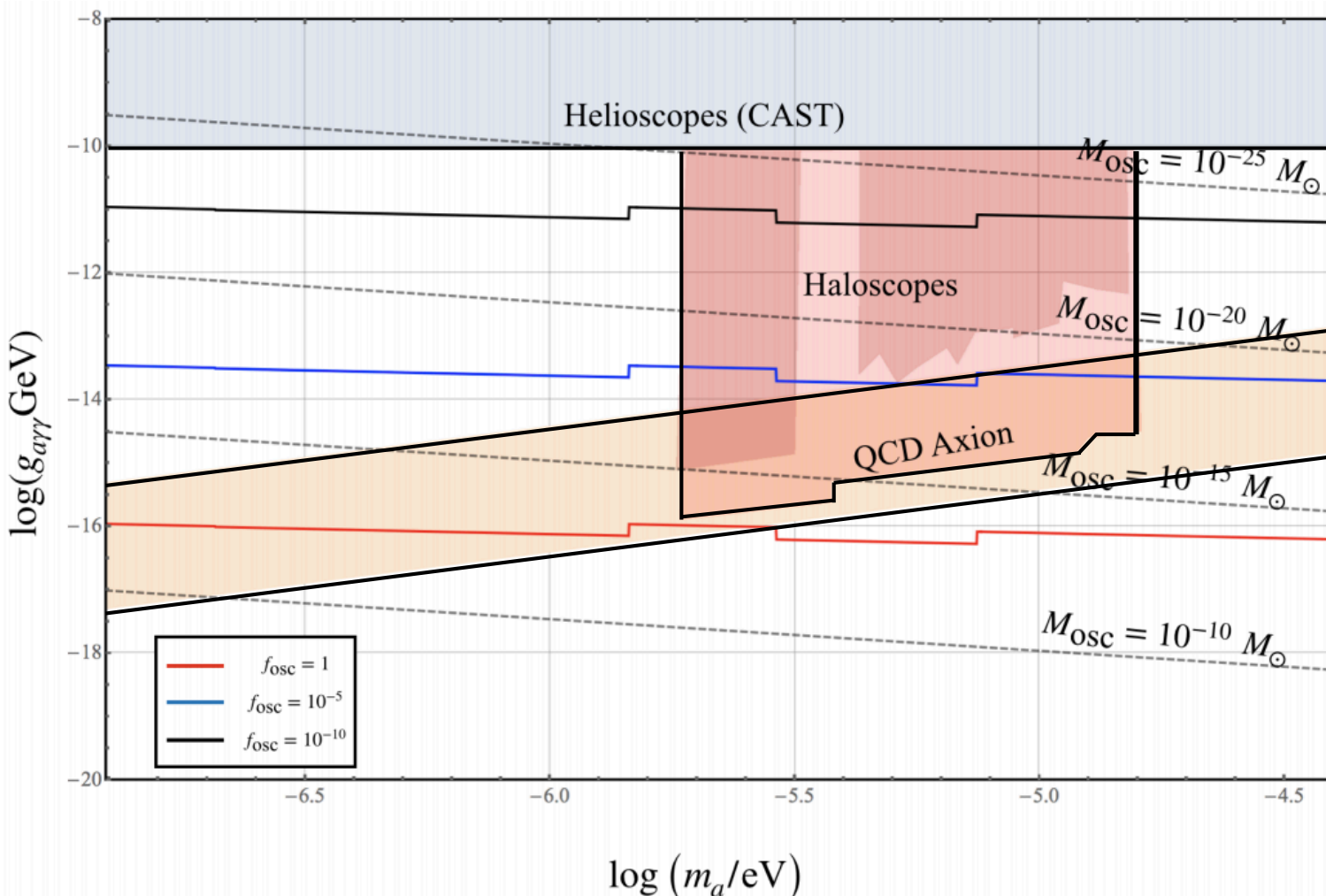
$$\Gamma_{\text{GC}} \approx 200 \text{ yr}^{-1} \left(\frac{m_a}{10^{-6} \text{ eV}} \right)^{1/3} \left(\frac{f_a}{10^{12} \text{ GeV}} \right)^{-2} \left(\frac{B_0}{10^{14} \text{ G}} \right)^{1/3} \left(\frac{N_{\text{bulge}}}{6 \times 10^8} \right) \left(\frac{P}{1 \text{ sec}} \right)^{-1/3}$$

Flux of Sun on Earth: $\Phi = 1.6 \times 10^6 \text{ Jy}$ (at 1.4 GHz)

Projected Sensitivity

- Observation of the GC ($T = 1$ year), with current and planned radio telescopes, optimized for field-of-view.

$$g_{a\gamma\gamma} = \alpha/(2\pi f_a), P_{NS} = 1 \text{ sec}, B_0 = 10^{13} \text{ Gauss}$$



Outlook

So FRBs?

- Many axion clumps will be tidally destroyed before converting significantly (still potentially detectable EM signatures).
- Oscillons are the most promising candidate among axion clumps.
- FRBs have been observed over a range of frequencies
~ 328 MHz – 8 GHz . Cannot be explained by a single axion.

Summary

- Several cosmological scenarios lead to the formation of dense axion clumps
- These clumps may be detected by their non-gravitational lensing signature or by photons produced when they collide with NSs.
- Collisions with NSs may be responsible for some FRBs.
- Electromagnetic signatures may reach parameter space inaccessible to gravitational searches.

Thank you for your attention!

Questions?

Supplemental Slides

Plasma Lensing

- Degeneracy with plasma inhomogeneities?

$$n_p(\mathbf{r}) = 1 - \frac{\omega_p^2(\mathbf{r})}{\omega^2}$$

c.t.

$$n_a(\mathbf{r}) = 1 - \frac{g_{a\gamma\gamma}^2 \dot{a}(\mathbf{r}, t)^2}{16\omega^2}$$

- Time dependence of axion field imprints spectral distortions at frequency $2m_a$.

