

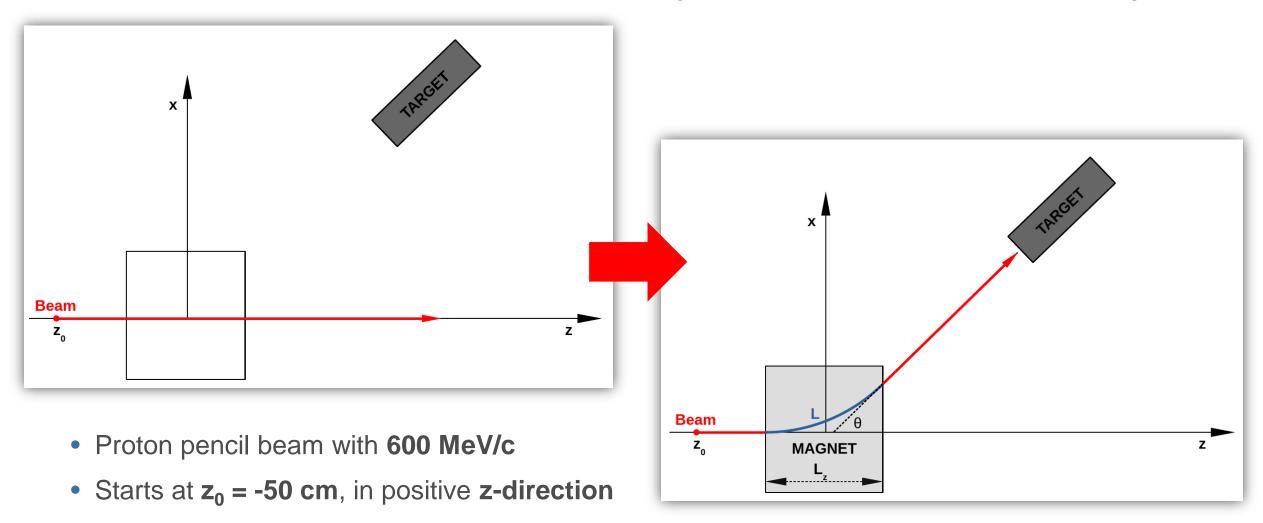
Exercise: Magnetic Field

Aim of the exercise:

- Define a dipole field which deviates the beam on a target
- Plot the field
- Visualize the effect of the field on the beam trajectory

Goal of the exercise

Introduce a dipole field in order to deflect a given beam on a pre-defined target



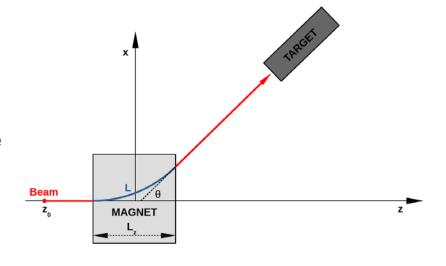


Steps

- The beam, regions and scoring is pre-defined
 - Note that all regions except the target are set to VACUUM (including the magnet)



- Activate a magnetic field in the pre-defined region called MAGNET (ASSIGNMA card)
- 2. Introduce a MGNFIELD card and define a B field such that:
 - a. the beam is deflected in the **x-z plane** as illustrated in the figure (hint: the B field direction can be determined from the Lorentz force).
 - b. the deflection angle θ is **25 deg**; use the formula on slide 5 to determine the required |B|. Note that the magnet is L_z =**50 cm** long in z-direction.
- 3. Verify that the field is correctly activated by plotting the field intensity and field vectors:
 - a. see lecture slides for instructions how to plot a field
 - b. make sure to chose an appropriate plotting plane which contains the field vectors
- 4. Run one cycle (1 primary) and plot the particle fluence in the x-z plane
 - a. use the *pre-defined* **usrbin** scoring in the Plot tab of Flair



For simplicity, let's keep the default transport settings

Did you manage to hit the target?



Lorentz force

• Use following expression to determine which B field component needs to be set on the MGNFIELD card in order to deflect the beam on the target:

$$\begin{pmatrix} F_{\mathcal{X}} \\ F_{\mathcal{Y}} \\ F_{\mathcal{Z}} \end{pmatrix} = q \begin{pmatrix} v_{\mathcal{X}} \\ v_{\mathcal{Y}} \\ v_{\mathcal{Z}} \end{pmatrix} \times \begin{pmatrix} B_{\mathcal{X}} \\ B_{\mathcal{Y}} \\ B_{\mathcal{Z}} \end{pmatrix} = q \begin{pmatrix} v_{\mathcal{Y}} B_{\mathcal{Z}} - v_{\mathcal{Z}} B_{\mathcal{Y}} \\ v_{\mathcal{Z}} B_{\mathcal{X}} - v_{\mathcal{X}} B_{\mathcal{Z}} \\ v_{\mathcal{X}} B_{\mathcal{Y}} - v_{\mathcal{Y}} B_{\mathcal{X}} \end{pmatrix}$$

- $(F_x, F_y, F_z) = \text{Lorentz force}$
- q = Particle charge
- (v_x, v_y, v_z) = Particle velocity
- (B_x, B_y, B_z) = Magnetic field (magnetic flux density) components

Required |B|

• Use the following expression to determine the required |B| in order to deviate the beam on the target:

$$\frac{p \left[\frac{GeV/c}{c} \right]}{0.299792 Q \left[\frac{e}{e} \right]} = \frac{|B| \left[\frac{T}{c} \right] L_z \left[\frac{m}{c} \right]}{\sin \theta}$$

- p = Particle momentum in GeV/c
- Q = Particle charge (as multiple of elementary charges)
- $|B| = \sqrt{B_x^2 + B_y^2 + B_z^2}$ in Tesla
- L_z = Length of the magnetic field in z-direction (i.e. in the original beam direction)
- θ = Deflection angle in rad

Note: this formula can be simply derived from the Lorentz force and applies for a homogenous dipole field with $L_z < R$, where R is the bending radius.

