

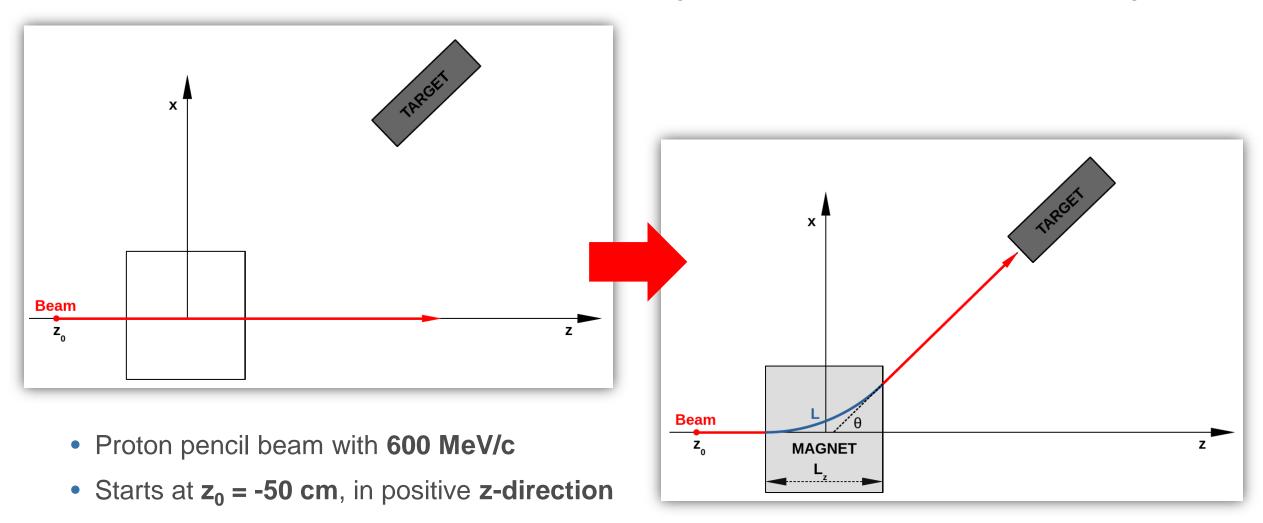
### **Exercise: Magnetic Field - Solution**

Aim of the exercise:

- Define a dipole field which deviates the beam on a target
- Plot the field
- Visualize the effect of the field on the beam trajectory

#### **Exercise**

Introduce a dipole field in order to deflect a given beam on a pre-defined target



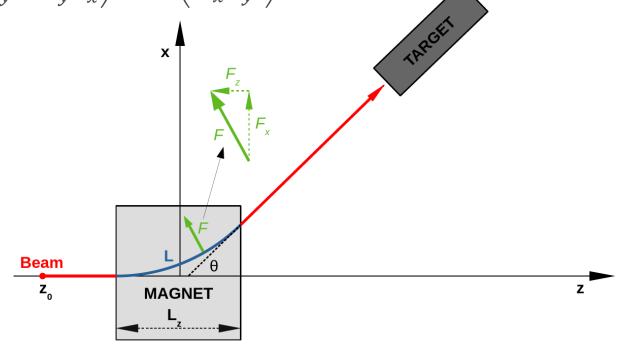


#### **B** field direction

• The B field is perpendicular to the plane of movement - hence only  $B_y$  can be non-zero if the particle shall move in the x-z plane:

$$\begin{pmatrix} F_{x} \\ 0 \\ F_{z} \end{pmatrix} = q \begin{pmatrix} v_{x} \\ v_{y} \\ v_{z} \end{pmatrix} \times \begin{pmatrix} B_{x} \\ B_{y} \\ B_{z} \end{pmatrix} = q \begin{pmatrix} v_{y}B_{z} - v_{z}B_{y} \\ v_{z}B_{x} - v_{x}B_{z} \\ v_{x}B_{y} - v_{y}B_{x} \end{pmatrix} = q \begin{pmatrix} -v_{z}B_{y} \\ 0 \\ v_{x}B_{y} \end{pmatrix}$$

- $(F_x, F_y, F_z) = \text{Lorentz force}$
- q = Particle charge
- $(v_x, v_y, v_z)$  = Particle velocity
- $(B_x, B_y, B_z)$  = Magnetic field components
- Protons are positively charged (q>0):
  - As shown in the figure:  $F_x > 0$  and  $F_z \le 0$
  - Since  $v_z > 0$ ,  $v_x \ge 0$ ,  $B_v$  must be negative



# Required |B|

 Required B field strength of a 50 cm long dipole to deviate a 600 MeV/c proton beam by 25 deg:

$$|B|[T] = \frac{0.6 [GeV/c]}{0.299792 * 1 [e] * 0.5 [m]} \sin\left(\frac{25}{180} * \pi\right) = 1.69164 [T]$$

#### The cards

• ASSIGNMA (under "Media"):

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Step: Field Magnetic ▼

Mat(Decay): ▼ Reg: MAGNET ▼ to Reg: ▼

Mat(Decay): ▼ Step: Field Magnetic ▼
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• MGNFIELD (under "Transport"):

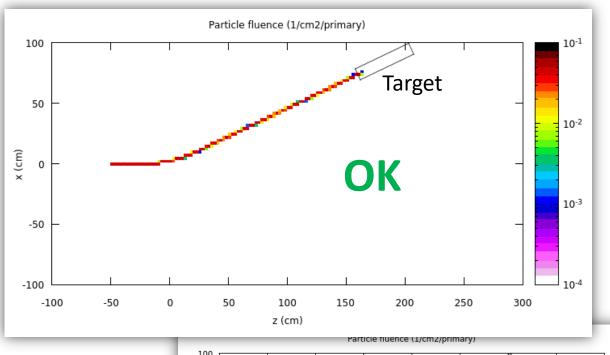
### Plotting the field

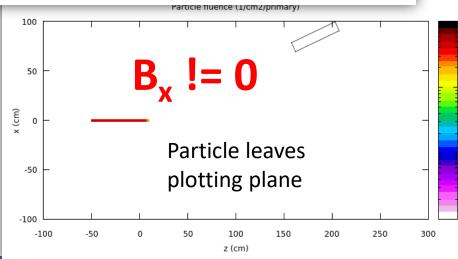
• Since the B-field only has a y component, let's for example chose the x-y plane

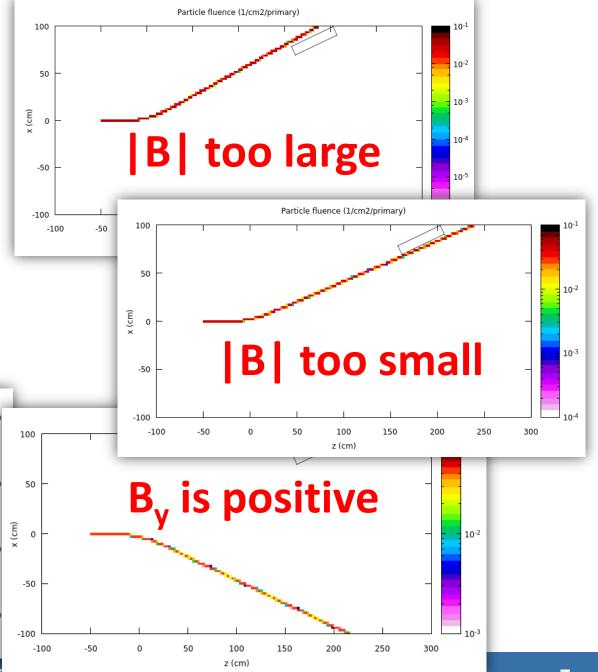
for plotting: ₩ Flair Winput Geometry & Run Diot ■ Output ▼ Paste □Copy Add ▼ Oz •Rename Clean Plot Clone ☑ Notes Plot Fluence Title: Magnetic field in x-y plane Display: 0 Magnetic Field Axes Min Max ▼ Label Log x: x (cm) y: y (cm) cb: B (T) Center Basis Extends X:Y Tyre: Field x: 0. Axes ▼ Δu: 50.0 y: 0. x-y y-z -u Δv: 50.0 Run: <uerault> z: 0. x-z swap -v Get Advanced **V** Magnetic field in x-y plane -Grid -Options Nu: 100 Vector Scale: boundaries 1.6 Nv: 100 Plot Coordinates: X-Y ▼ 🗷 labels 1.4 20 1.2 0.8 0.6 -20 0.4 0.2 -40 20 x (cm) Fluka: ex magfield.flair Plot completed



### Particle fluence in x-z plane









Magnetic field exercise

# Tracking accuracy (boundary crossing)

