



High RR Lecture Heidelberg

How Neutron EDM-Experiments Really Work III

Outline of the nEDM lecture

Motivation & History

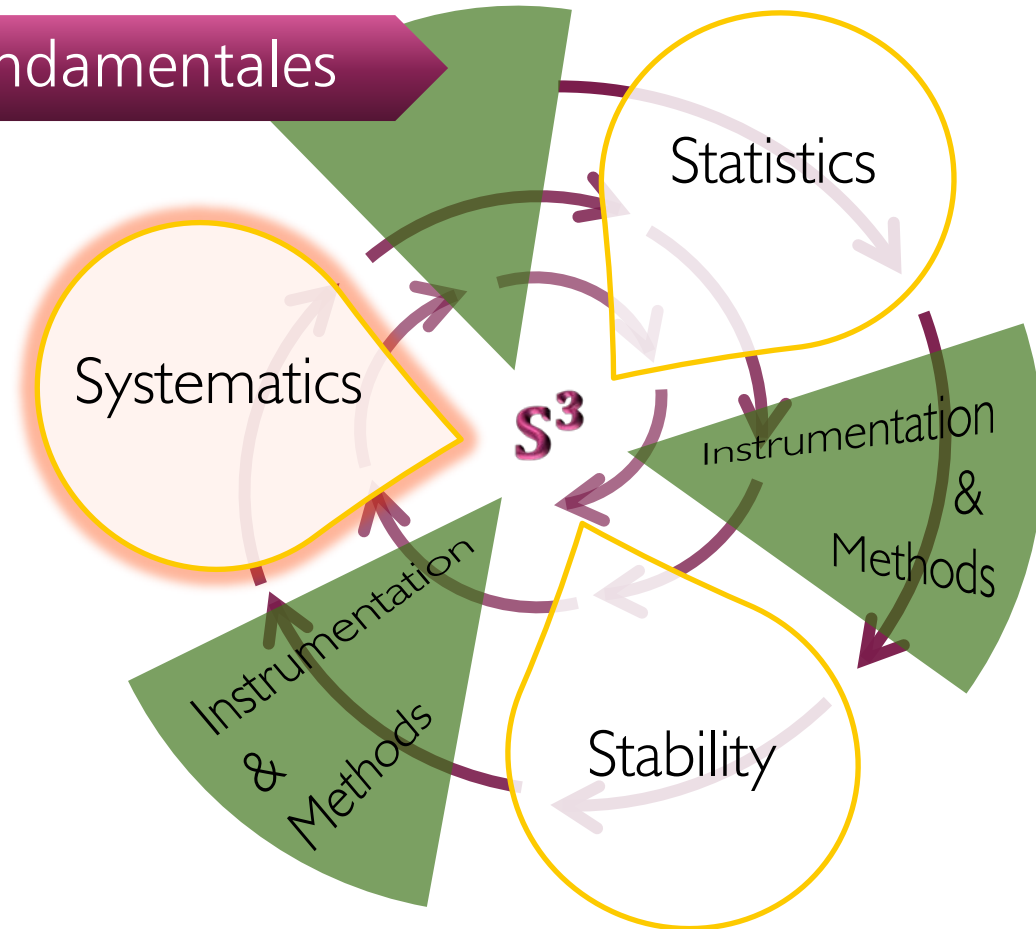
Fundamentales

Lecture I:

Motivation & Fundamentales

Lecture II&III:

The spiral to ultimate sensitivity



Express EDM with ratios:

$$d_n = \frac{\hbar \langle \omega_{\text{Hg}} \rangle}{4E} (R_+ - R_-)$$

$$R_{\pm} = \frac{f_n}{f_{\text{Hg}}} = \left| \frac{\gamma_n}{\gamma_{\text{Hg}}} \right| \left(1 \pm \delta_{\text{EDM}} \pm \delta_{\text{EDM}}^{\text{false}} + \delta_Q + \underbrace{+\delta_G + \delta_T}_{\text{B-field}} + \underbrace{+\delta_E + \delta_{\text{LS}} + \delta_I + \delta_P + \delta_{\text{AC}}}_{\text{Secondary effects}} \right)$$

- nEDM
- HgEDM

Linear effect ($v \times E$)

- “geometric phase”
- Ordered motion

Quadratic effect (neutron and Hg, random motion)

secondary effects cancel unless correlated with E-field.

$v \times E$ the dominant systematic

- Motional magnetic field from $B_m = -\frac{v \times E}{c^2}$
- Naively no contribution as $\bar{v} = 0$ for UCN?
- In non-uniform B-field and E-field:

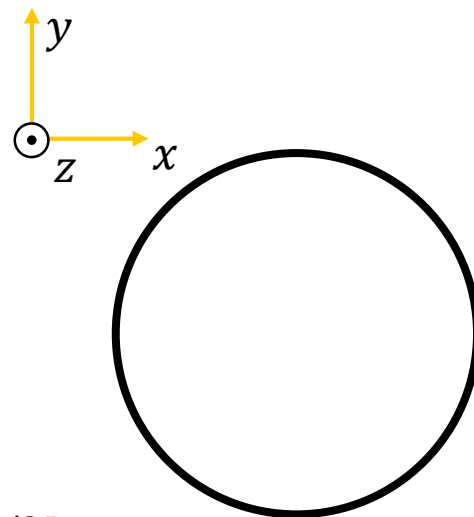
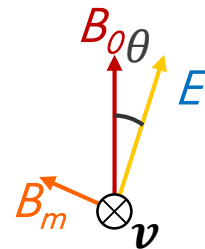
Rabi: Spin rotation due to oscillating horizontal field.
This leads to a shift (Ramsey, Bloch, Siegert) of the resonance frequency by

$$\Delta\omega = \frac{(\gamma_n B_\perp)^2}{2(\gamma_n B_0 - \omega_r)}$$

with

$$B_\perp = \frac{\partial B_z}{\partial z} \frac{r}{2} + \frac{v_r E}{c^2}$$

and the oscillation ω_r is a result of rapidly changing trajectories, e.g. $\omega_r = v_r/2R$



$v \times E$ the dominant systematic

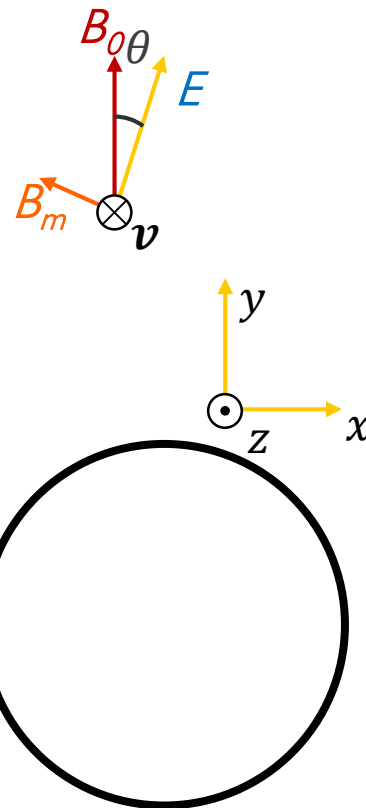
- Motional magnetic field from $B_m = -\frac{v \times E}{c^2}$
- In non-uniform B-field and E-field:

$$B_{\perp}(r)^2 = \left(\frac{\partial B_z}{\partial z} \frac{r}{2} \right)^2 + r \frac{\partial B_z}{\partial z} \frac{v_{\perp} E}{c^2} + \left(\frac{v_{\perp} E}{c^2} \right)^2$$

- The term linear in E will lead to a electric field induced shift of precession frequency, **an EDM like signal.**

$$\Delta\omega_f = \gamma^2 r \frac{\partial B_z}{\partial z} \frac{v_{\perp} E}{2c^2(\gamma_n B_0 - \omega_r)}$$

Different for neutrons (adiabatic), and mercury (ballistic/non-adiabatic)



- Typical B-field gradients: ~ 10 pT/cm
- Dominant effect from mercury transferred to neutron by correction

$$\Delta\omega_f^{\text{adiabtic}} \approx \frac{\pi v_{\perp}^2}{48c^2 B^2} \frac{\partial B_z}{\partial z} E$$

$$\Delta\omega_f^{\text{n-adiabtic}} \approx \frac{\gamma^2 R^2}{8\pi c^2} \frac{\partial B_z}{\partial z} E$$

$$d_n^{\text{false}} / \frac{\text{pT}}{\text{cm}} = 1.5 \times 10^{-28} \text{ ecm}$$

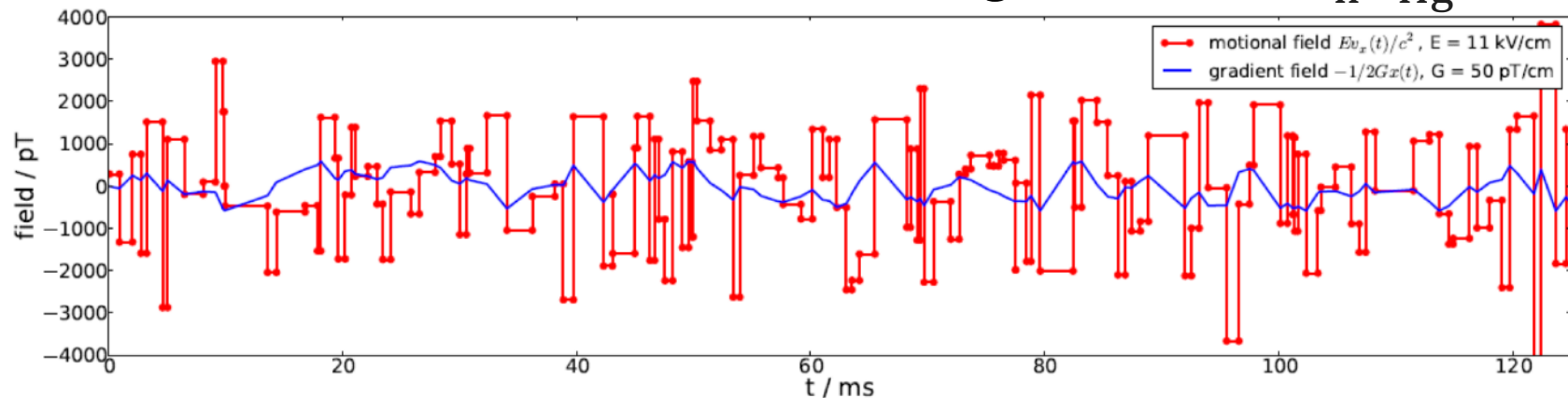
$$d_n^{\text{false}} / \frac{\text{pT}}{\text{cm}} = 1.15 \times 10^{-27} \text{ ecm}$$

$$d_{\text{Hg} \rightarrow \text{n}}^{\text{false}} / \frac{\text{pT}}{\text{cm}} = -4.4 \times 10^{-27} \text{ ecm}$$

nEDM strategy

Measure nEDM as function of B-Field gradient

The dominant effect is transferred from ^{199}Hg to neutron: $d_{n\leftarrow\text{Hg}}^{\text{false}}$



$$d_{n\leftarrow\text{Hg}}^{\text{false}} = \frac{\hbar\gamma_n\gamma_{\text{Hg}}}{2c^2} \langle xB_x + yB_y \rangle$$

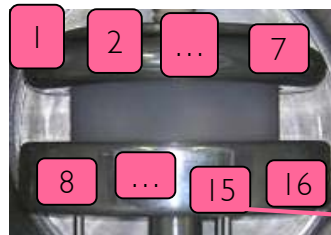
$$= \frac{\hbar\gamma_n\gamma_{\text{Hg}}}{32c^2} D^2 G_{1,0}$$

with
D = 47cm

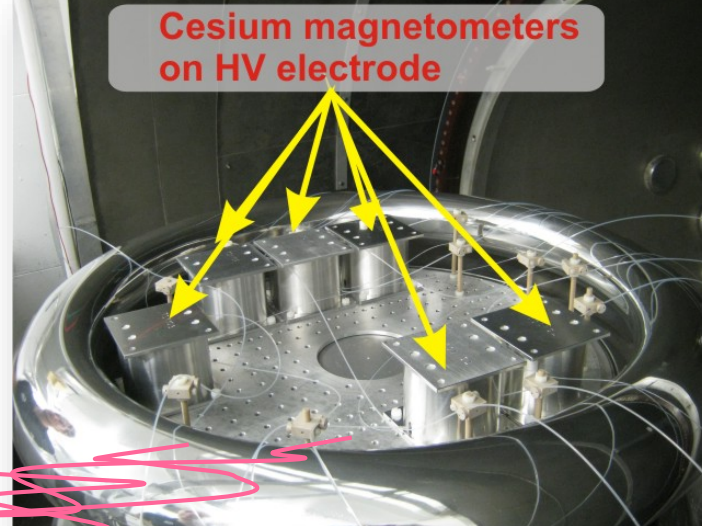
$$d_{n\leftarrow\text{Hg}}^{\text{false}} = -G_{1,0} 4.4 \times 10^{-27} e \frac{\text{cm}^2}{\text{pT}}$$

Monitoring of vertical magnetic gradients

$\pm 132\text{kV}$

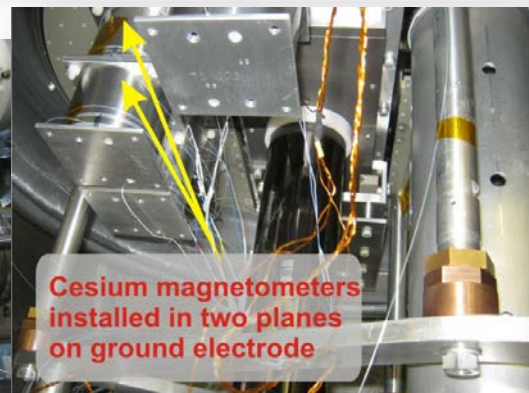


- 7 HV CsM
- 9 ground CsM
- Stabilized laser
- PID phase locked DAO

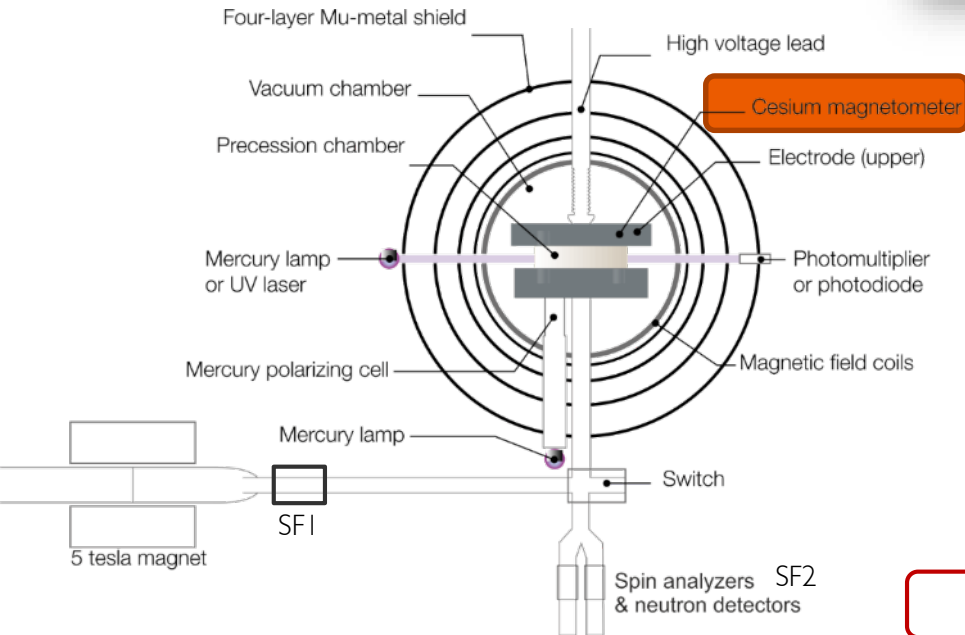


Accuracy:

$$\sigma(g_z) \approx 10\text{pT/cm}$$



- Cesium magnetometer array for field gradients



Use polynomial decomposition to calculate non-uniform field

$$\vec{B}(\vec{r}) = \sum_{l,m} G_{l,m} \begin{pmatrix} \Pi_{x,l,m}(\vec{r}) \\ \Pi_{y,l,m}(\vec{r}) \\ \Pi_{z,l,m}(\vec{r}) \end{pmatrix}$$



$$\sigma(G_{1,0}) \approx 8 \text{ pT/cm}$$

Not sufficient to correct for systematic

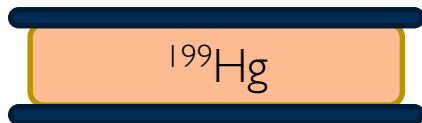
Use R-value as proxy for $G_{1,0}$

- Center of mass offset

- Non-adiabaticity

$$R_{\pm} = \frac{f_n}{f_{\text{Hg}}} = \left| \frac{\gamma_n}{\gamma_{\text{Hg}}} \right| (1 \pm \delta_{\text{EDM}} \pm \delta_{\text{EDM}}^{\text{false}} + \delta_Q + \delta_G + \delta_T + \delta_E + \delta_{\text{LS}} + \delta_I + \delta_P + \delta_{\text{AC}})$$

$$\frac{\gamma_{\text{Hg}}}{2\pi} \approx 8 \text{ Hz}/\mu\text{T}$$



$$\frac{\gamma_n}{2\pi} \approx 30 \text{ Hz}/\mu\text{T}$$

$$\overline{v}_{\text{Hg}} \approx 160 \text{ m/s vs. } \overline{v}_{\text{UCN}} \approx 3 \text{ m/s}$$

$$R \cdot \left| \frac{\gamma_n}{\gamma_{\text{Hg}}} \right| - 1 = \delta_G = \pm \frac{\langle z \rangle G_{1,0}}{B_0}$$

Effect of higher order gradients

$$R_{\pm} = \frac{f_n}{f_{\text{Hg}}} = \left| \frac{\gamma_n}{\gamma_{\text{Hg}}} \right| \left(1 \pm \delta_{\text{EDM}} \pm \delta_{\text{EDM}}^{\text{false}} + \delta_Q \pm \delta_G \mp \delta_T + \delta_E + \delta_{\text{LS}} + \delta_I + \delta_P + \delta_{\text{AC}} \right)$$

$$\delta_G = \pm \frac{\langle z \rangle G_{1,0}}{|B_0|}$$

and

$$d_{n \leftarrow \text{Hg}}^{\text{false}} = \frac{\hbar \gamma_n \gamma_{\text{Hg}}}{32c^2} D^2 G_{1,0}$$

is not the full story, but...

... neither.

But instead:

$$\delta_G = \frac{\langle z \rangle G_g}{|B_0|}$$

with

$$G_g = G_{10} + G_{30} \left(\frac{3H^2}{20} - \frac{3D^2}{16} \right) + \dots$$

$$\begin{aligned} d_{n \leftarrow \text{Hg}}^{\text{false}} &= -\frac{\hbar \gamma_n \gamma_{\text{Hg}}}{32c^2} \sum_{l \text{ odd}} G_{l0} \langle \rho \Pi_{\rho l m} \rangle \\ &= \frac{\hbar \gamma_n \gamma_{\text{Hg}}}{32c^2} D^2 \left[G_{10} - G_{30} \left(\frac{D^2}{8} - \frac{H^2}{4} \right) \right] \end{aligned}$$

Correcting systematic by G_g and \hat{G}

The crossing point analysis takes care of a large part of the motional false EDM:

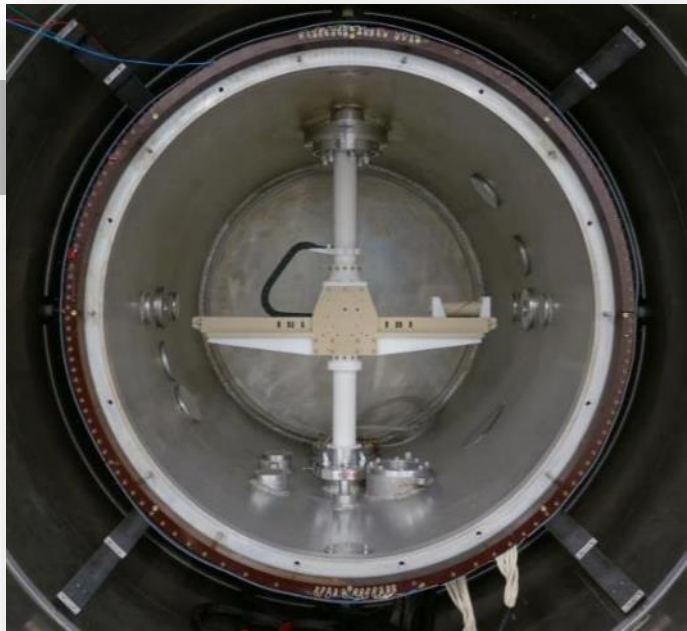
$$d_{n \leftarrow \text{Hg}}^{\text{false}} = \frac{\hbar \gamma_n \gamma_{\text{Hg}}}{32c^2} D^2 \left[G_g + G_{30} \left(\frac{D^2}{16} + \frac{H^2}{10} \right) + G_{50} \left(\frac{H^4}{28} - \frac{D^2 H^2}{96} - \frac{5D^4}{256} \right) \right]$$

Corrected by
crossing point fit

$$\hat{G} := \hat{G}_{30} + \hat{G}_{50}$$

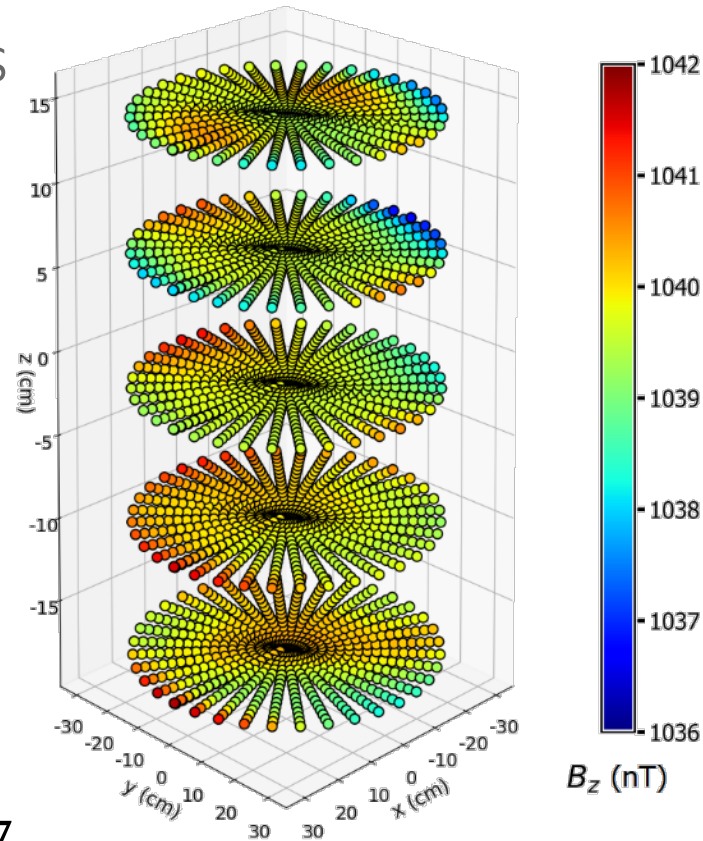
Corrected set for set using map analysis

Magnetic field maps



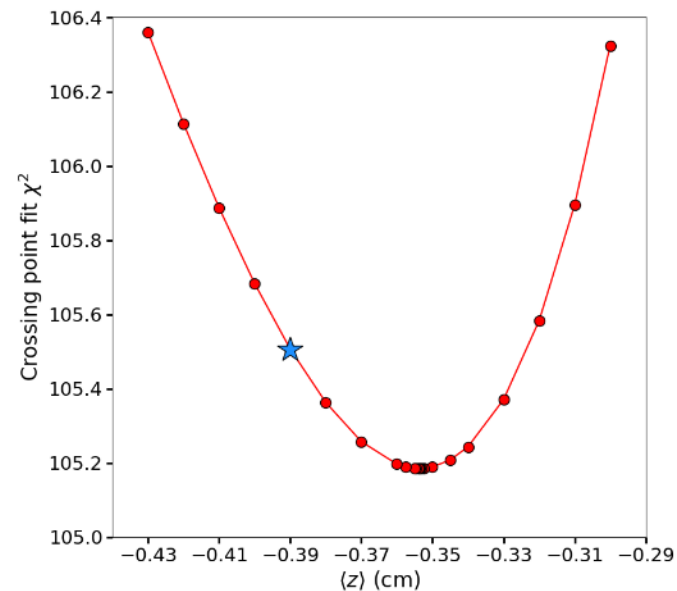
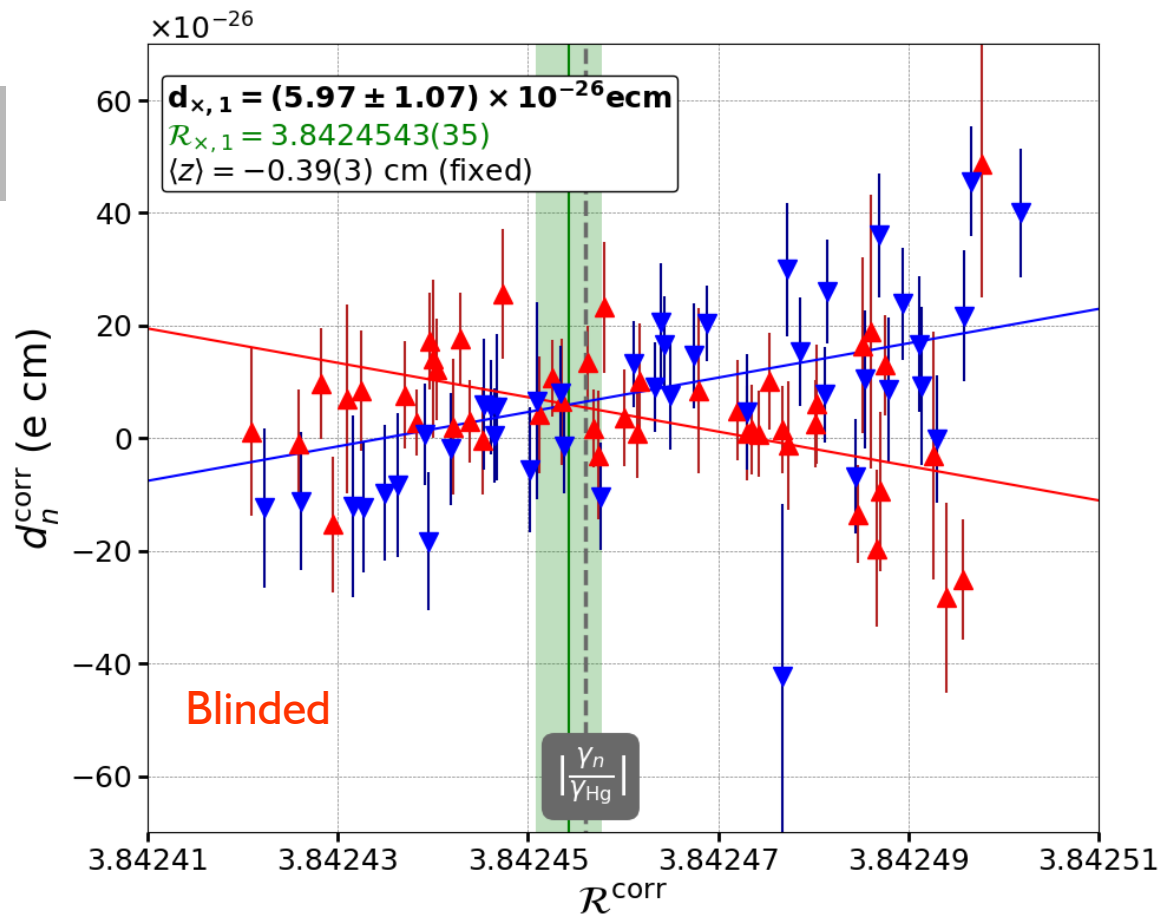
Mapping with fluxgate

- $-20 < z < 20$,
- $-10 < r < 30$,
- $\Delta\phi = 5^\circ$



- Fit to order $l = 7$
- Extract $\langle B_T^2 \rangle$ for each base configuration
- Extract $\delta_G(\hat{G})$ for each base configuration

Crossing point analysis



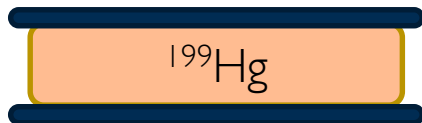
Use R-value as proxy for $G_{1,0}$

- Center of mass offset

- Non-adiabaticity

$$R_{\pm} = \frac{f_n}{f_{\text{Hg}}} = \left| \frac{\gamma_n}{\gamma_{\text{Hg}}} \right| (1 \pm \delta_{\text{EDM}} \pm \delta_{\text{EDM}}^{\text{false}} + \delta_Q + \delta_G + \delta_T + \delta_E + \delta_{\text{LS}} + \delta_I + \delta_P + \delta_{\text{AC}})$$

$$\frac{\gamma_{\text{Hg}}}{2\pi} \approx 8 \text{ Hz}/\mu\text{T}$$



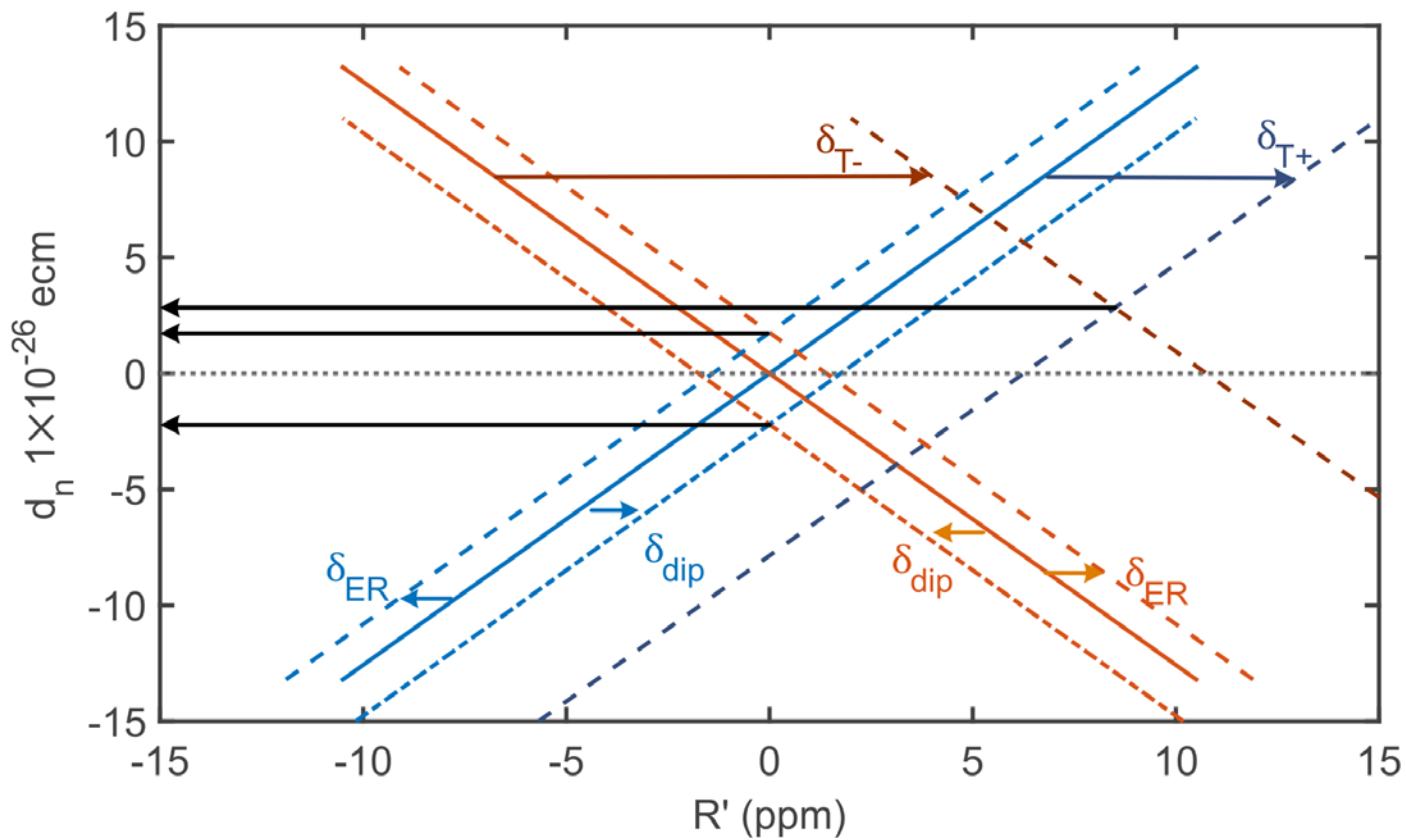
$$\frac{\gamma_n}{2\pi} \approx 30 \text{ Hz}/\mu\text{T}$$

$$\overline{v_{\text{Hg}}} \approx 160 \text{ m/s vs. } \overline{v_{\text{UCN}}} \approx 3 \text{ m/s}$$

$$R \cdot \left| \frac{\gamma_n}{\gamma_{\text{Hg}}} \right| - 1 - \delta_G = +\delta_T = \frac{\langle B_T^2 \rangle}{2B_0^2}$$

Needs to be known for
each sequence

Crossing point analysis



Systematic effects

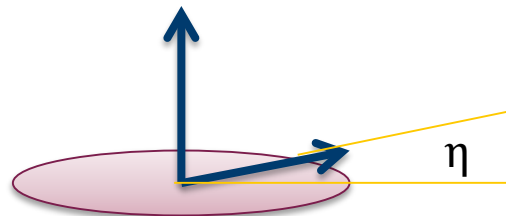
Table I: Summary of systematic effects in 10^{-28} ecm. The first three effects are treated within the crossing-point fit and are included in d_x . The additional effects below the line are considered separately.

		Effect	shift error	
False Hg EDM	}	Error on $\langle z \rangle$	-	7
		Higher order gradients \hat{G}	69	10
		Transverse field correction $\langle B_T^2 \rangle$	0	5
Other effects	}	Hg EDM[8]	-0.1	0.1
		Local dipole fields	-	4
		$v \times E$ UCN net motion	-	2
		Quadratic $v \times E$	-	0.1
		Uncompensated G drift	-	7.5
		Mercury light shift	-	0.4
		Inc. scattering ^{199}Hg	-	7
		TOTAL		

Field mapping

Pseudo magnetic field from incoherent scattering length

$$B^* = -\frac{4\pi\hbar}{m_n\gamma_n} nb_i P \sqrt{\frac{I}{I+1}}$$

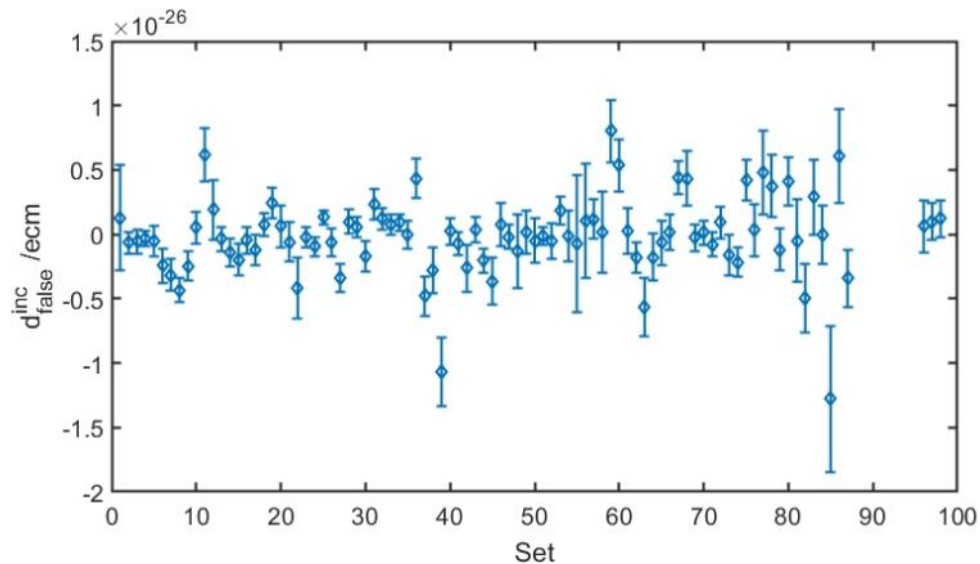


$$\delta\eta = \eta(+E) - \eta(-E)$$

- $b_i = \pm 15.5$ fm
- nP (^{199}Hg × polarization) extracted from data cycle by cycle

$$d_n^{\text{false}} = \hbar \frac{\gamma_n}{4E} B^* \cdot \delta\eta$$

$$< 7 \times 10^{-28} \text{ ecm}$$



Outline of the nEDM lecture

Motivation & History

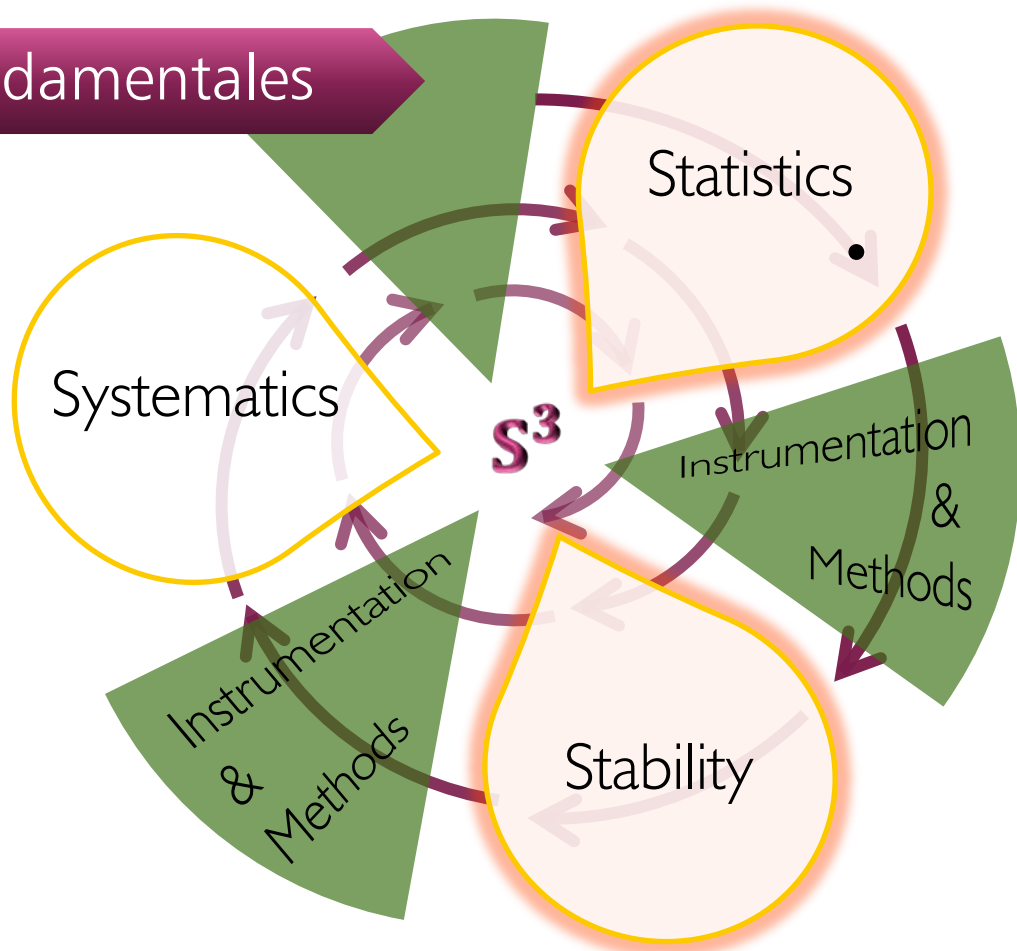
Fundamentales

Lecture I:

Motivation & Fundamentales

Lecture II&III:

The spiral to ultimate sensitivity



What seems possible in a single shot?

Number of neutrons N:

Higher density and/or larger volume → more neutrons

New UCN sources:

- superthermal sources based on D₂ or sfHe
- Transport losses/dilution
- Ramsey cell = source

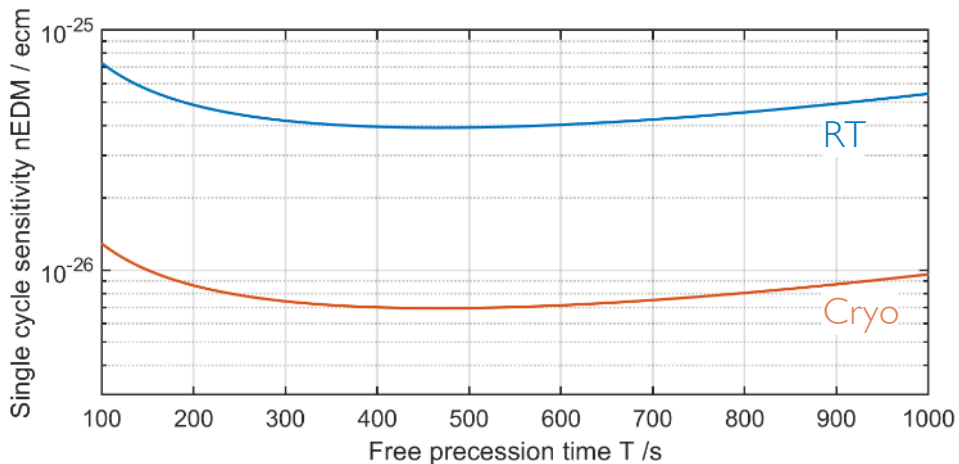
Needs matching of source volume to experiment volume, other wise too strong dilution.

Neutron spin coherence function of cell radius → good control of gradients:

$$\frac{1}{T_{2,\text{mag}}} = \frac{8R^3\gamma_n^2}{9\pi v} (G_{1,-1}^2 + G_{1,1}^2) + \frac{\mathcal{H}^3\gamma_n^2}{16v} G_{1,0}^2$$

What seems possible in a single shot?

Number of neutrons	N:	10^7	← 100 times larger (SuperSun, TRIUMF, SNS)
Electric field	RT:	20 kV/cm	Cryogenic: 80kV/cm
Coherence time	T_2 :	3000 s	
Storage times	t_s, t_f :	(100, 300) s	← 8 times larger (SNS, former CryoEDM)



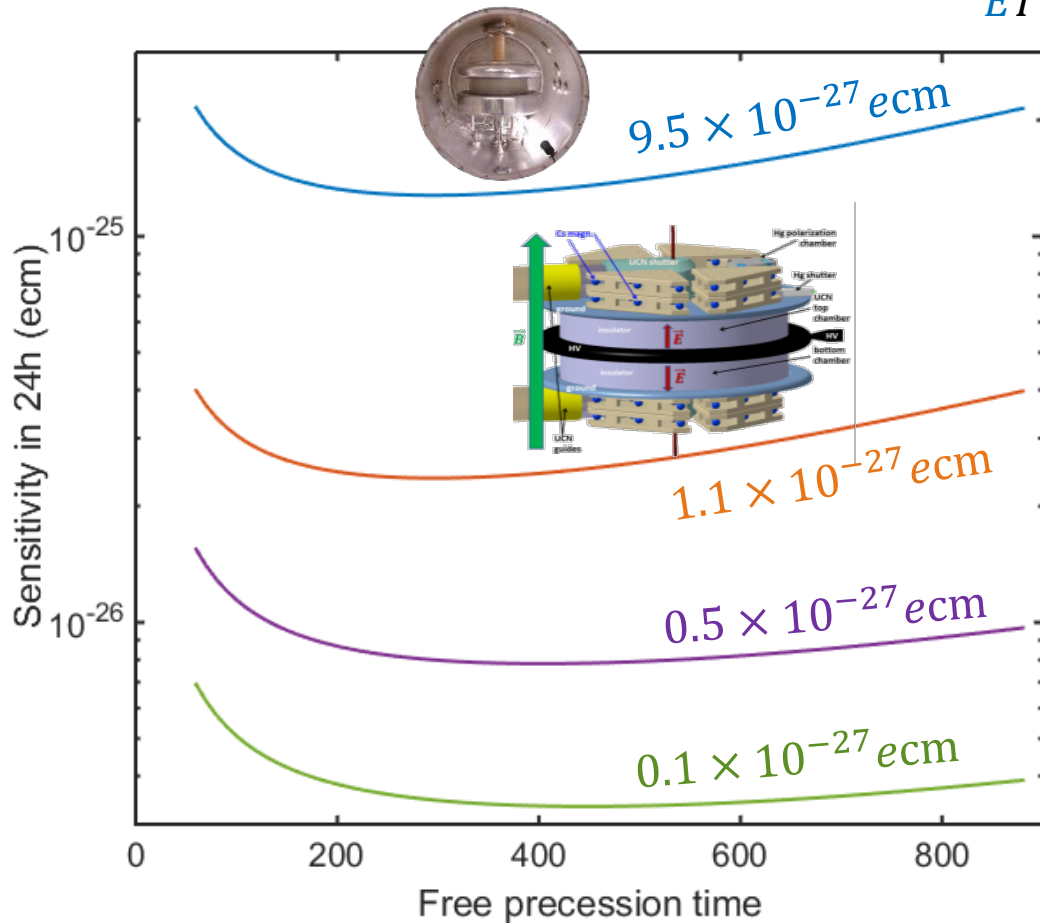
After 4 years with
200 days each:

$$\sigma_{RT} \approx 1 \times 10^{-28} \text{ ecm}$$

$$\sigma_{Cryo} \approx 0.2 \times 10^{-28} \text{ ecm}$$

Sensitivity at PSI:

$$\sigma(d_n) = \frac{\hbar}{ET\alpha_0 e^{-T/T_2} \sqrt{2N_0(e^{-T/\tau_s} + e^{-T/\tau_f})}}$$



Performance in 2015/2016

Prospect TDR (start 2021)

$E = 15 \text{ kV/cm}, N = 8 \times N_{2016}$

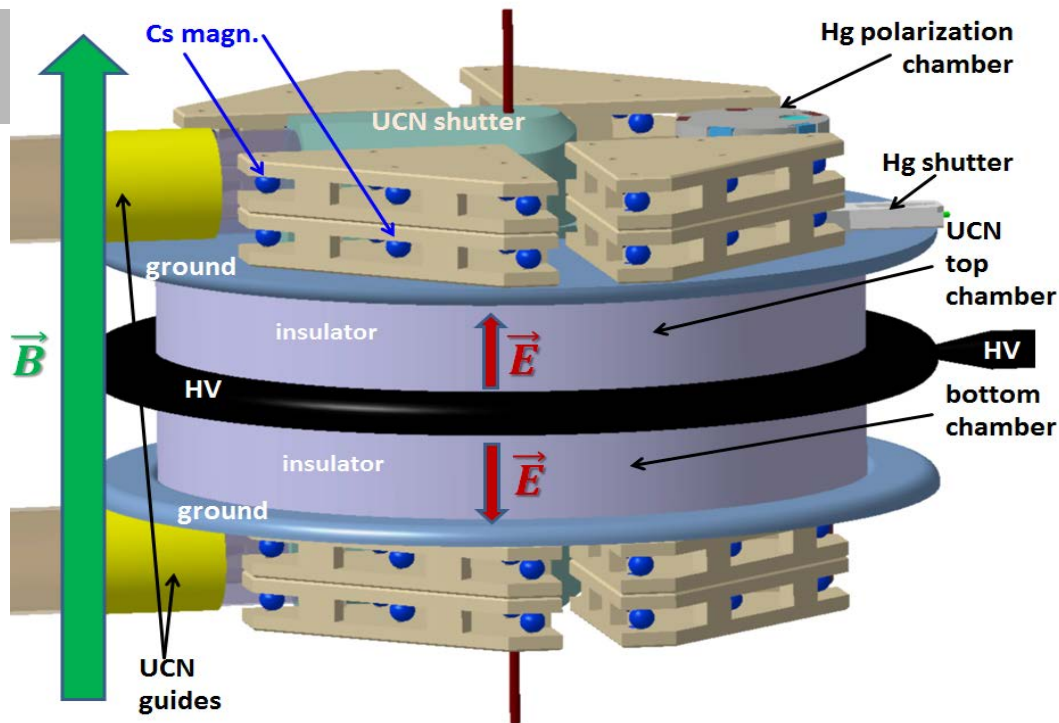
Possible final performance at PSI

$E = 18 \text{ kV/cm}$, improved UCN source, optimal magnetic field tuning

New source? At ESS?

$E = 20 \text{ kV/cm}, N = 128 \times N_{2016}$

Main features of the new instrument

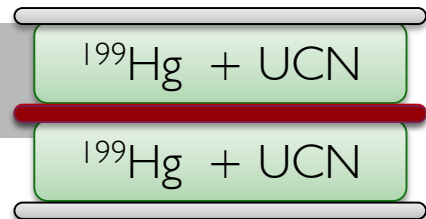


$$\sigma(d_n) \approx 1 \times 10^{-27} \text{ ecm}$$

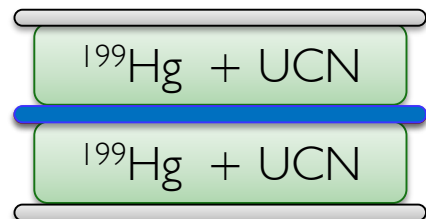
Inspired by Gatchina double-chamber setup
I. Altarev et al. JETP Lett. 44(1986)460
 and based on years of experience with our
 own operating experiment:

- 2 neutron precession chambers
- Hg co-magnetometer in both chambers with laser read out
- Baseline scenario: UCN chamber with materials and coatings as present chamber, but larger diameter of storage volume - upgrades in development
- Surrounded by calibrated Cs arrays on ground potential (~ 100 sensors)
- large NiMo ($^{58}\text{NiMo}$) coated UCN guides

Analysis: Frequency ratio $R = f_n/f_{\text{Hg}}$



double chamber - linear $\partial B/\partial z$ is almost perfectly compensated
but due to different h_t and h_b gradient fluctuations still cause an error on a lower level though

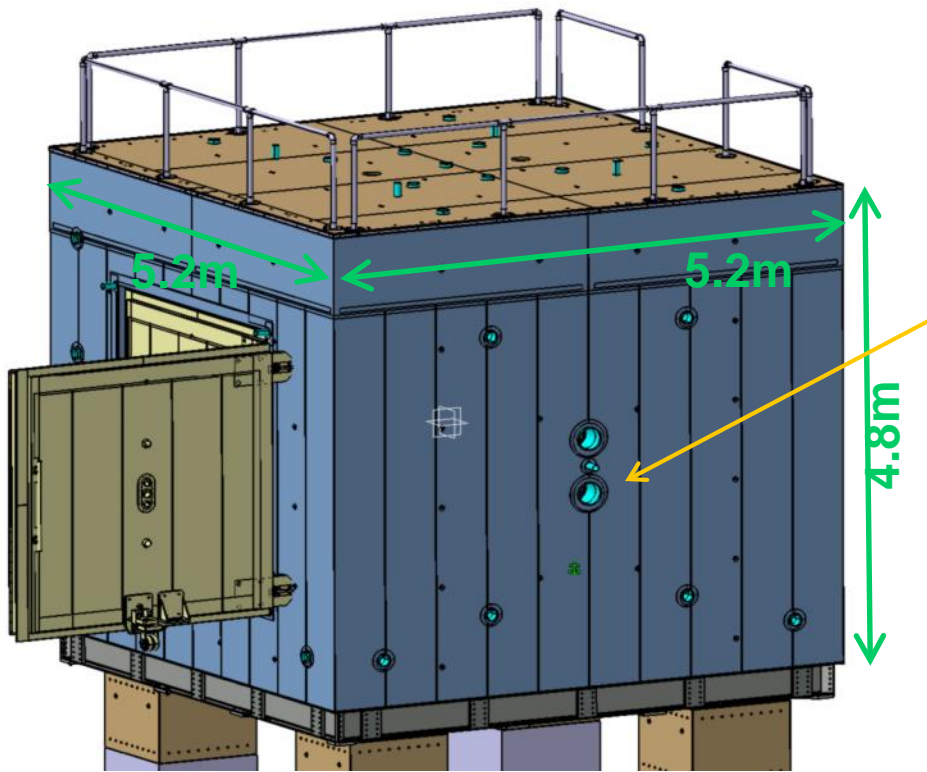


$$R^{+T} - R^{+B} = \frac{\gamma_n}{\gamma_{\text{Hg}}} \left(2\delta_{\text{EDM}} + (\langle z \rangle_T - \langle z \rangle_B) \frac{g^+}{B_0} + \dots \right)$$

$$R^{-T} - R^{-B} = \frac{\gamma_n}{\gamma_{\text{Hg}}} \left(-2\delta_{\text{EDM}} + (\langle z \rangle_T - \langle z \rangle_B) \frac{g^-}{B_0} + \dots \right)$$

Analysis: based on $(R^T - R^B)$ as function of dB/dz extrapolate to 0

Magnetically Shielded Room



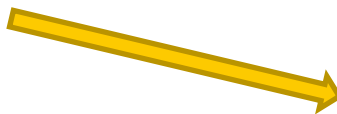
setup features:

- (2 + 4) layers mu-metal
- Al eddy current shield
- 78 openings for experiment use
- largest openings
ID=220mm
for 2 UCN guides
for 2 main pumping ports

expected performance:

- quasi-static shielding factor
guaranteed > 70'000
(expected > 100'000)
- central B-field < 0.5nT
- central gradient < 0.3 nT/m

Fundamental
Neutron Physics
Beamline (SNS)



EB-1

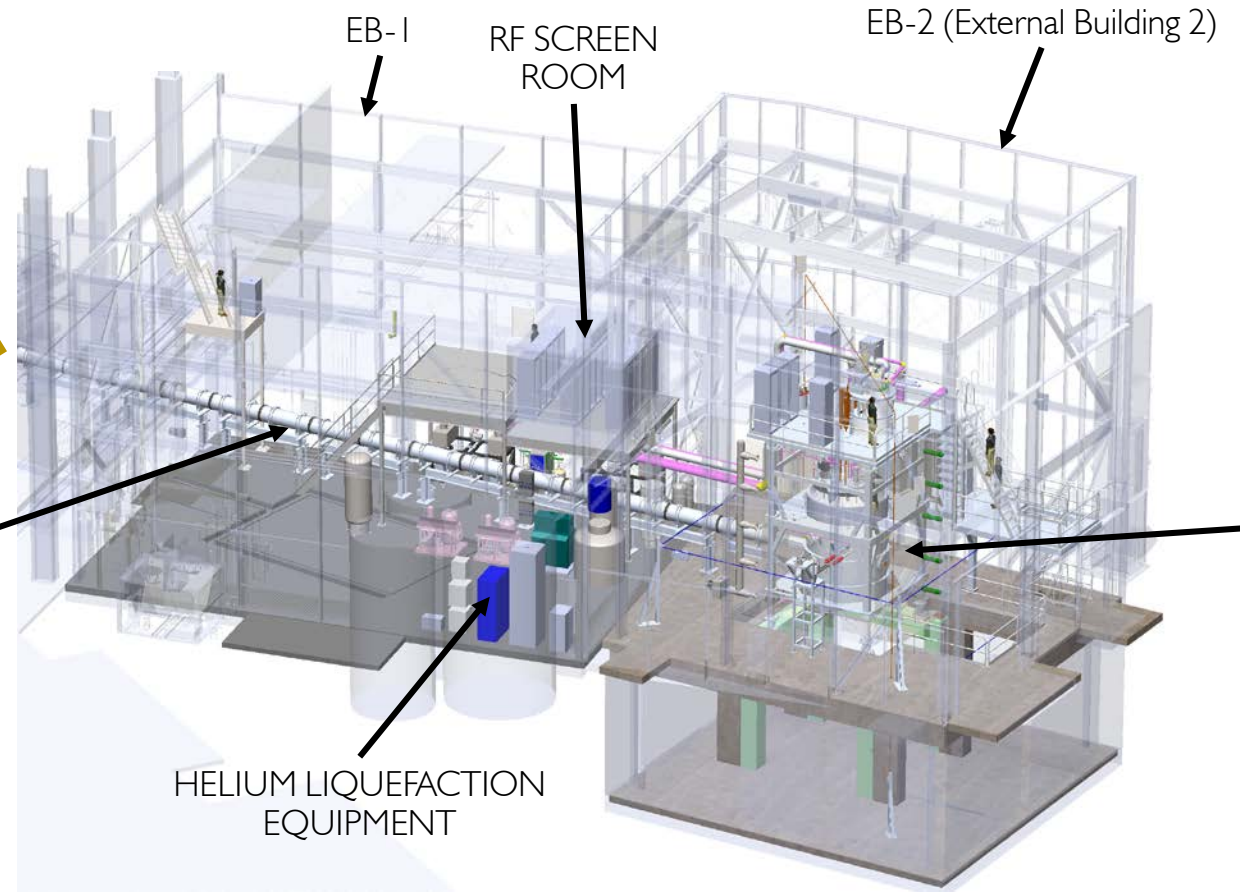
RF SCREEN
ROOM

EB-2 (External Building 2)

NEUTRON
GUIDE

nEDM
APPARATUS

HELIUM LIQUEFACTION
EQUIPMENT

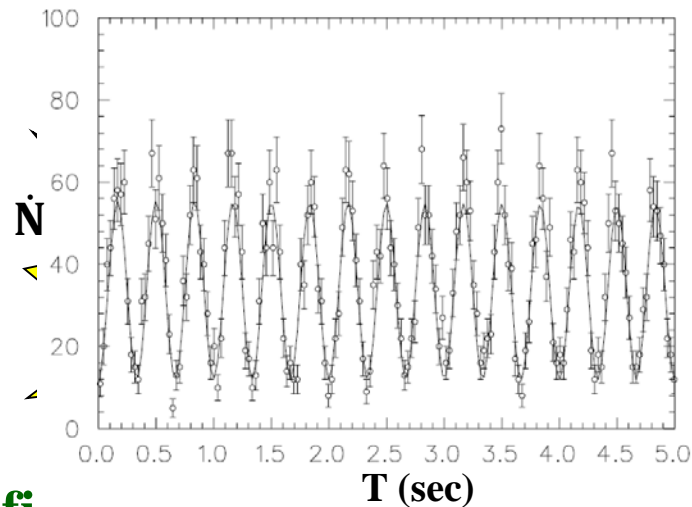
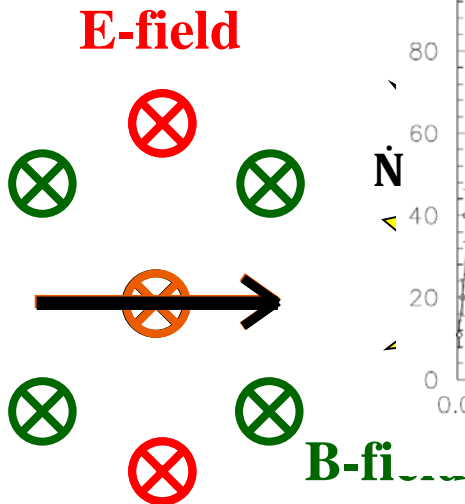


But ... New Techniques = New Challenges

- Cryogenic system introduces challenges
 - Cold vacuum leaks & SFHe leaks are tough to find
 - AC spin dressing field virtually forbids metals/conductors in central volume due to eddy-current heating
 - Superconducting components distort B-fields
- Magnetic field gradients must be minimized
 - Components near central volume must use *really* non-magnetic material (316 SS, brass, ... don't count)
 - Measurement cells must be free of “magnetic” dust
- Because of above most components near central volume are made from G10, PMMA, PEEK, Torlon, ...
 - Challenging materials for machining, vacuum, thermal contraction, ...
- Little previous work on large scale HV in superfluid
 - Requires significant R&D (past, present & future)

New Technique for n-EDM

1. Inject polarized neutron & polarized ^3He
2. Rotate both spins by 90°
3. Measure $n+^3\text{He}$ capture vs. time
(note: $\sigma_{\downarrow\uparrow} \gg \sigma_{\uparrow\uparrow}$)
4. Flip E-field direction



$$\omega_{\text{rel}} = (\gamma_3 - \gamma_n)B_0 + 2d_n E / \hbar.$$

^3He functions as “co-magnetometer”

Since ^3He EDM shielded by atomic electrons

Dressed spin of polarized ^3He in a cell

P.-H. Chu,^{1,*} A. M. Esler,¹ J. C. Peng,¹ D. H. Beck,¹ D. E. Chandler,¹ S. Clayton,¹ B.-Z. Hu,³ S. Y. Ngan,² C. H. Sham,²
L. H. So,^{1,2} S. Williamson,¹ and J. Yoder¹

¹Department of Physics, University of Illinois at Urbana-Champaign, Urbana, Illinois 61801, USA

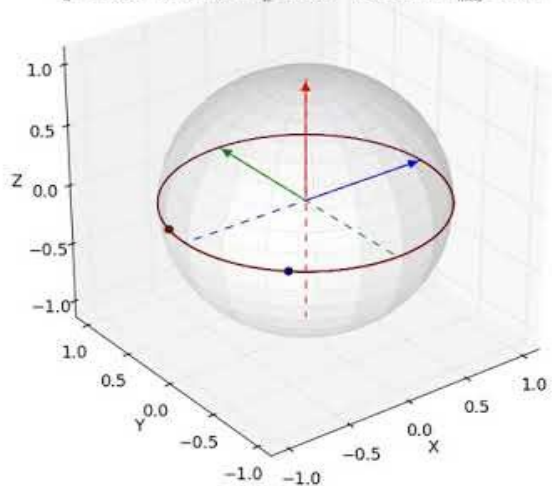
²Department of Physics, The Chinese University of Hong Kong, Hong Kong, China

³Department of Physics, Soochow University, Taipei, Taiwan

(Received 25 April 2011; revised manuscript received 22 July 2011; published 19 August 2011)

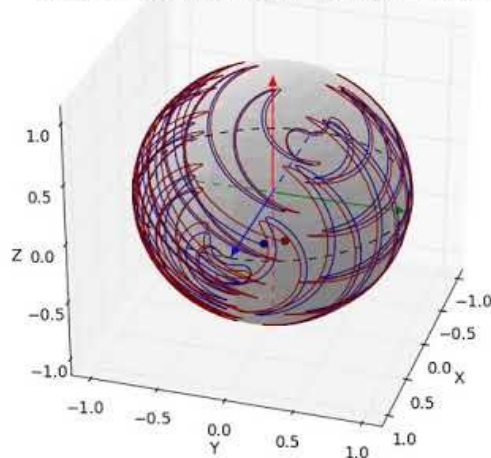
Without “dressing”

- Neutron
 - ^3He
- Dressing Parameters**
 $Y_n=0.1$ $X_n=0.0$, $Y_3=0.112$ $X_3=0.0$
 $f_d=1000$ Neutron $f_L=100$ Neutron $f_{mod}=100$



With dressing

- Neutron
 - ^3He
- Dressing Parameters**
 $Y_n=0.1$ $X_n=1.18$, $Y_3=0.112$ $X_3=1.31$
 $f_d=1000$ Neutron $f_L=100$ Neutron $f_{mod}=68$



$$\omega_{\text{rel}} = (\gamma_3 - \gamma_n) B_0 + 2d_n E / \hbar.$$

^3He SERVICES
MODULE

POLARIZED ^3He
SOURCE

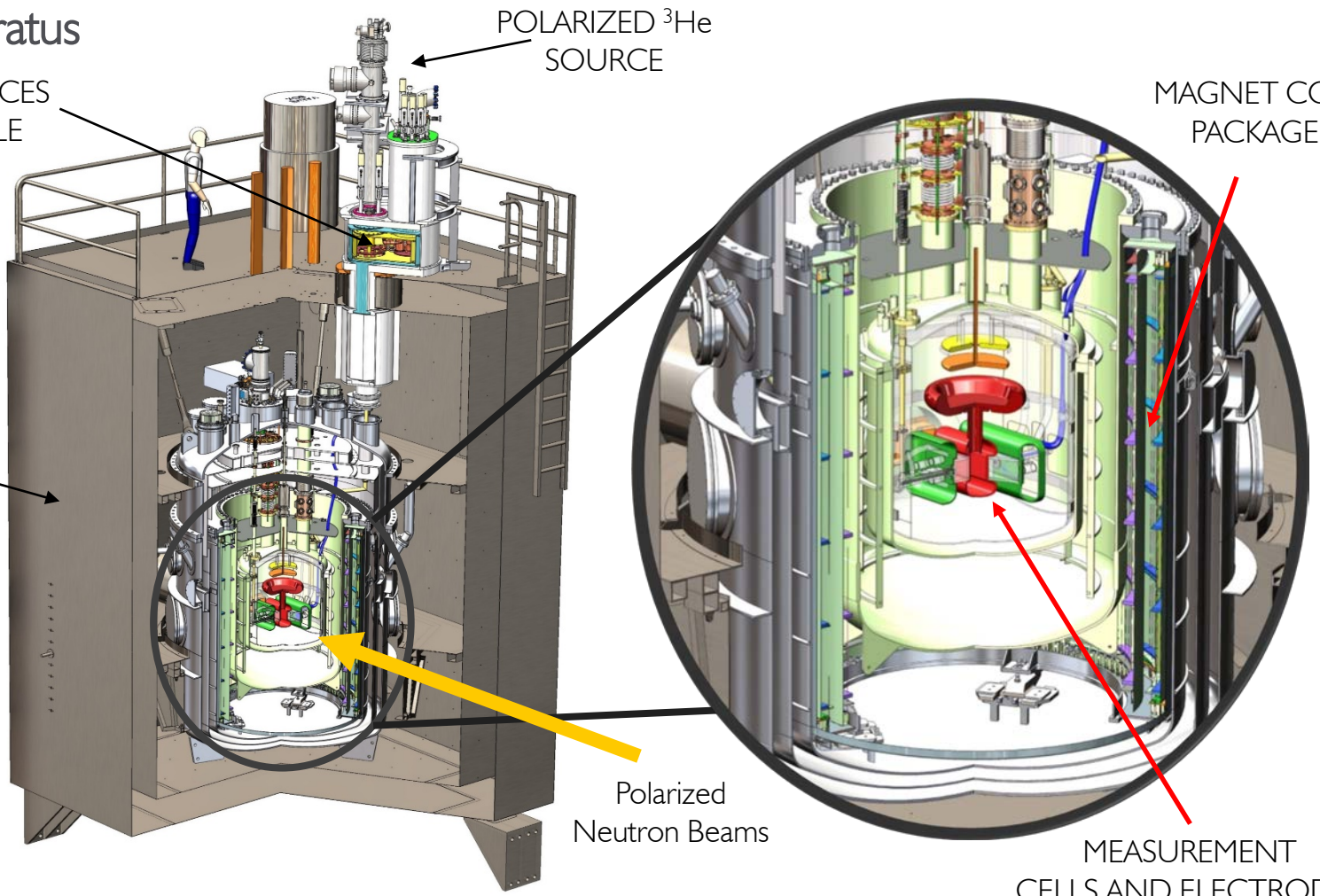
MAGNET COIL
PACKAGE

MAGNETICALLY
SHIELDED ROOM

Polarized
Neutron Beams

MEASUREMENT
CELLS AND ELECTRODES

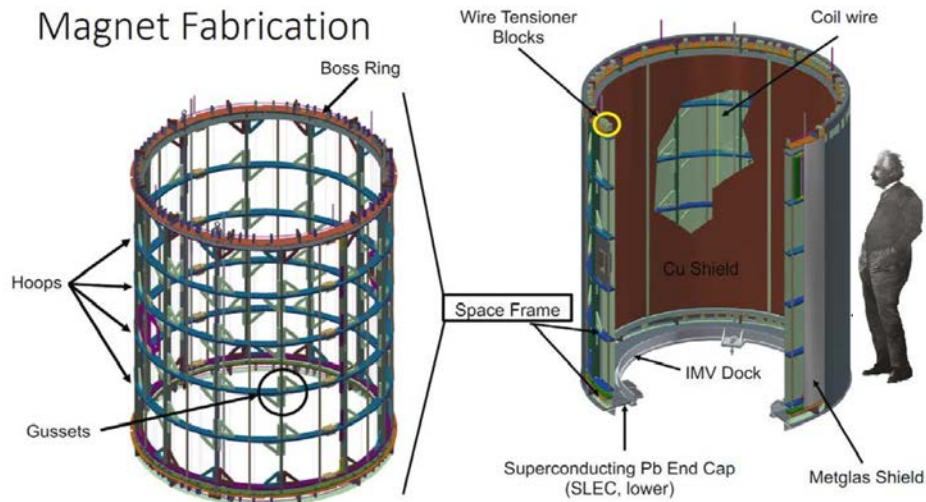
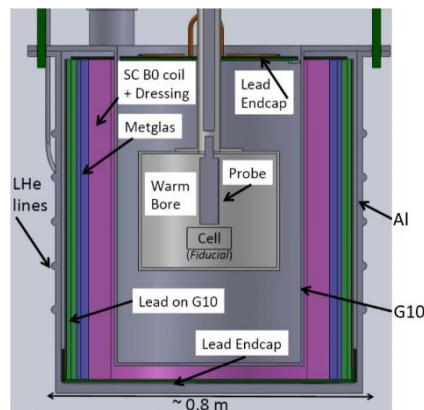
Slide from B. Filippone, SNS EDM



- Achieved required specs for uniformity, heat load and maximum temperature in 1/3 Scale prototype

- Achieved full-scale spec for fractional B-field uniformity for B_0 : $3 \times 10^{-6}/\text{cm}$ and spin dressing B_{SD} : $9 \times 10^{-5}/\text{cm}$
- Achieved acceptable heat load while maintaining temperature of $< 6.2\text{K}$

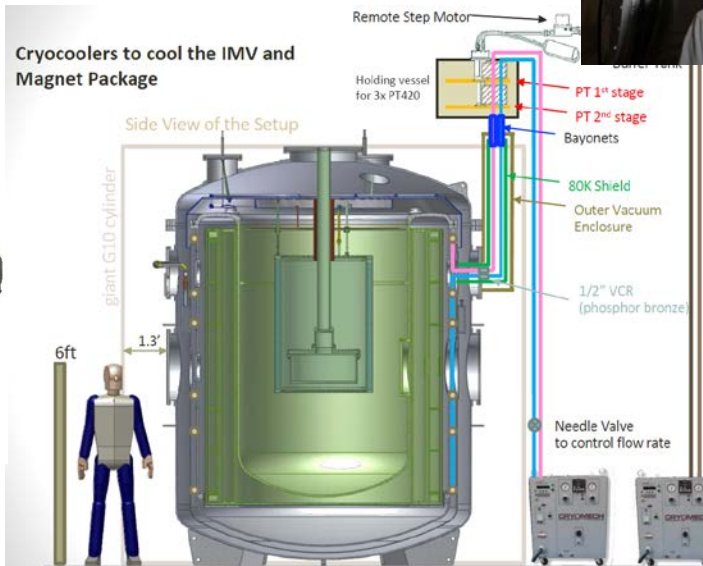
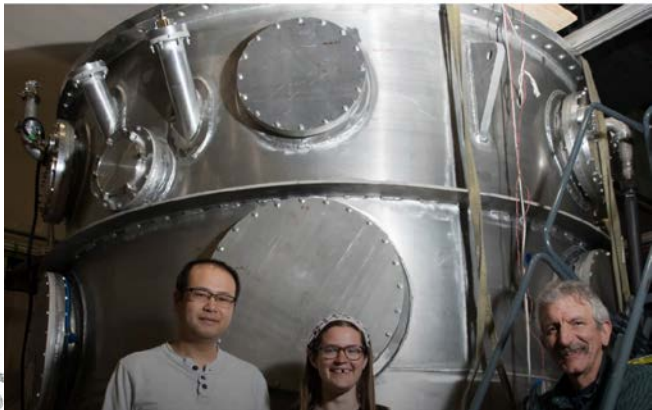
- Full-scale Magnet Design



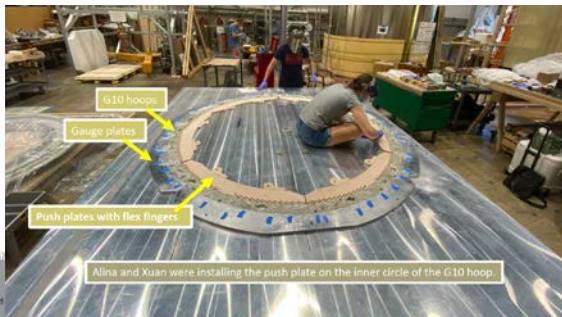
Outer Vacuum Vessel Tested to 80K

Construction of full-scale Magnet System underway

Inner Magnet Volume ready to ship



G10 Magnet Components being Vacuum Laminated

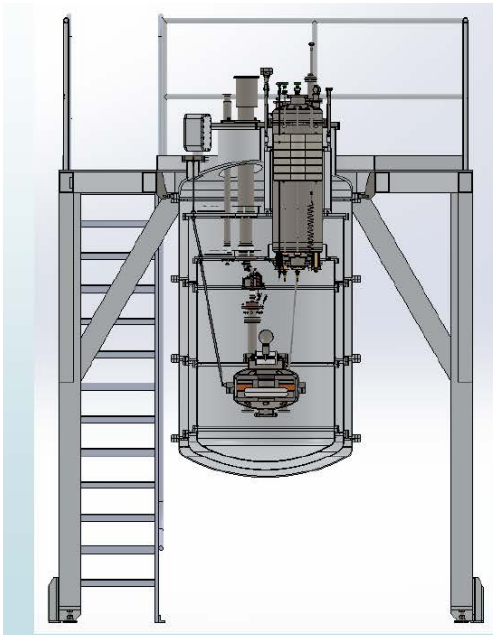


Central Detector System (CDS)

- Small-scale HV system provides info on breakdown field geometric scaling
- Medium-scale HV (1/5 full-scale) system achieved 85 kV/cm
 - Goal is 75 kV/cm in full-scale
- Half-scale HV system under construction
 - Two acrylic measurement cells with central HV electrode to optimize electrode design and study candidate materials
- Many CDS subsystems have achieved near required performance
 - Low noise SQUID system developed
 - Acrylic measurement cell tested with 1800 s ultra-cold neutron wall-loss lifetime
 - Cryogenic Si photomultiplier system achieved > 20 photo-electrons equiv.
 - Superfluid tight non-conducting, non-magnetic valves tested
 - Cryogenic HV multiplier under construction

Central Detector System (CDS)

Half-Scale High Voltage System assemble & beginning testing

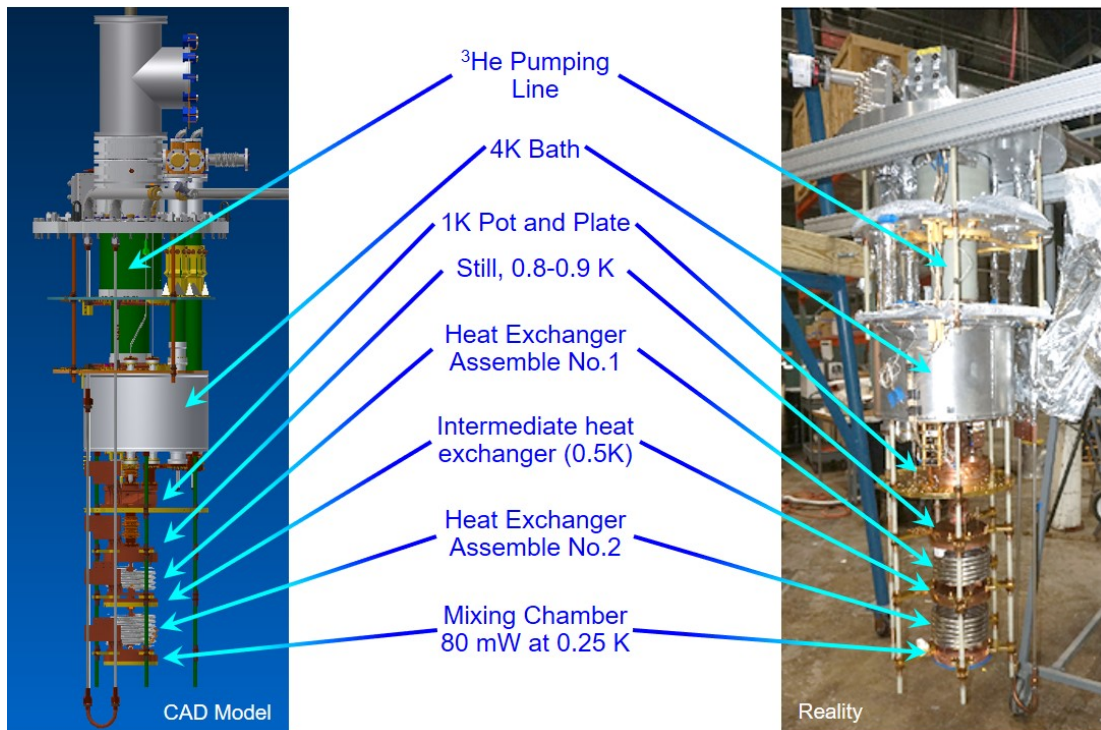


Polarized ^3He System

- Produce highly polarized ($>97\%$) ^3He and delivers it into purified L^4He
 - Atomic Beam Source built; testing & optimization underway
 - Developed working Superfluid film burner
- Transport polarized ^3He via phonon wind (aka heat flush) to measurement cells
 - Small scale heat flush system successfully tested
 - Large volume heat flush tests underdevelopment
- Empty measurement cells of reduced polarization ^3He and re-purify to 10^{-12} fractional ^3He density
- Design, build & test non-magnetic high-cooling-power dilution refrigerator (DR)

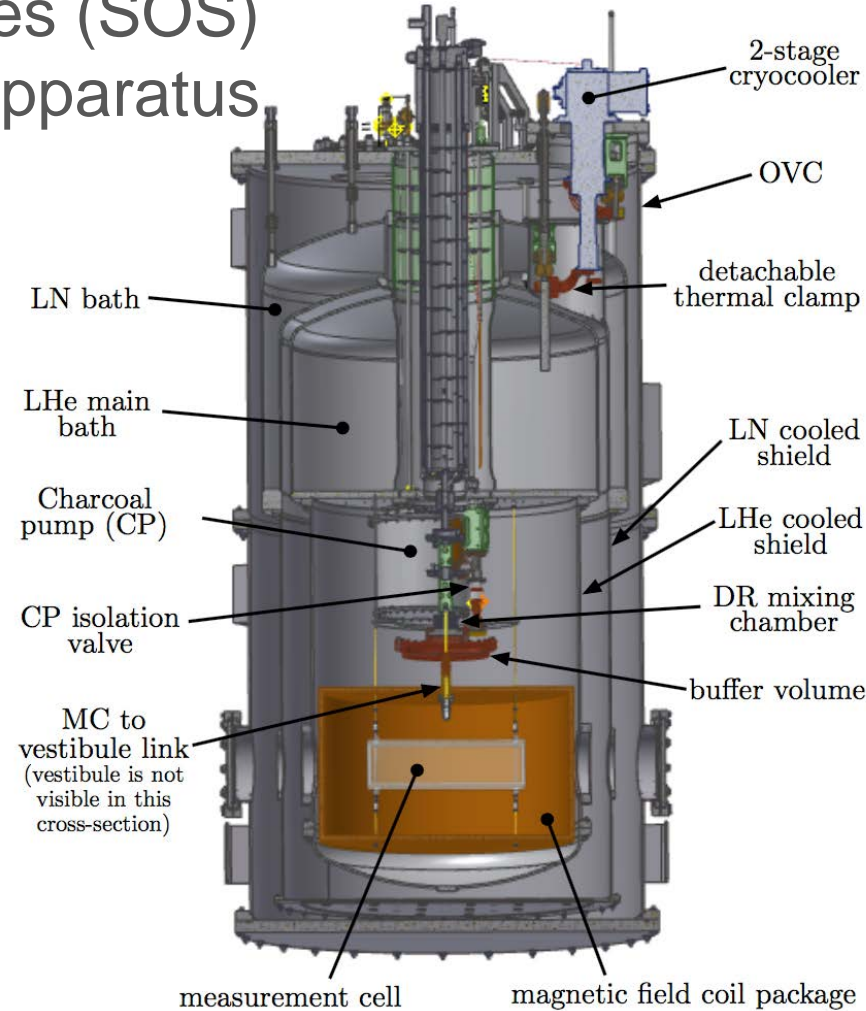
Dilution Refrigerators (DR)

- First DR (for ^3He system) complete and being tested
 - Measured 75mW at .25K
- 2nd DR for (CDS) being constructed



Systematics & Operational Studies (SOS) Apparatus

- Located at PULSTAR → teaching reactor at NCSU
- Mini-nEDM@SNS
 - One full-size measurement cell
 - No electric field
 - Full magnetic field capability
 - Relaxed ^3He polarization requirements
 - Relatively small size → rapid thermal cycling
- Goals:
 - validate production measurement cells
 - Develop spin manipulation techniques
 - Characterize geometric phase effect



nEDM@SNS Sensitivity

- Free Precession Measurement (SQUIDs)

–Sensitivity : 3.3×10^{-28} e-cm

–90% CL : 5.4×10^{-28} e-cm



300 live-days ~ 3 yrs

- Dressed Spin Measurement (AC Field)

–Sensitivity : 1.6×10^{-28} e-cm

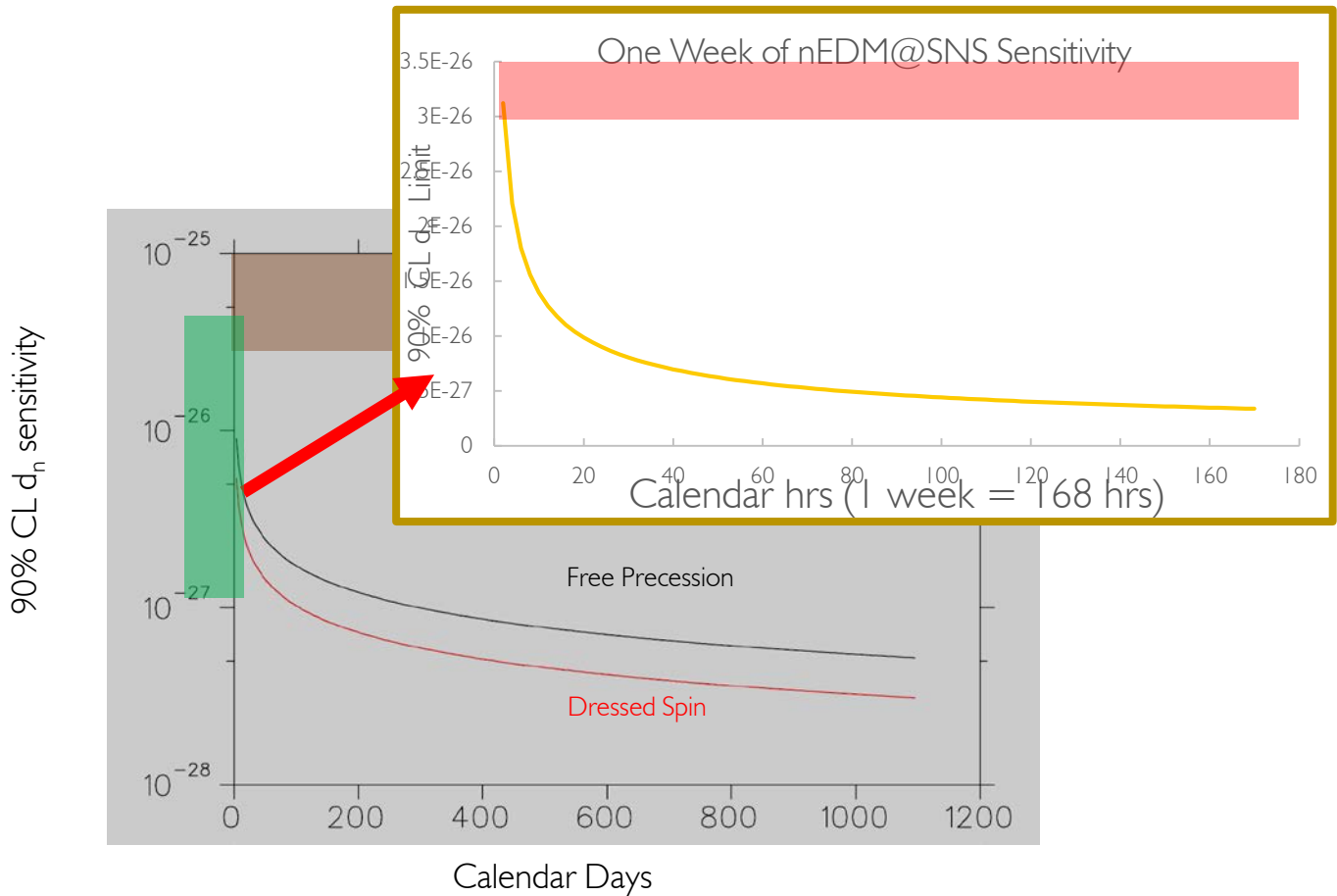
–90% CL : 2.6×10^{-28} e-cm



300 live-days ~ 3 yrs

Systematic Uncertainties $< 1.5 \times 10^{-28}$ e-cm

Time to 90% CL Sensitivity





Systematic Uncertainties

Uncertainty Source	Systematic uncertainty (e-cm)	Comments	Key Parameters
Linear (E x v)	$< 1 \times 10^{-28}$	Uniformity of B_0 field	B field gradient Temperature
Quadratic (E x v)	$< 0.5 \times 10^{-28}$	E field reversal accuracy $< 1\%$	
Pseudomagnetic field effects	$< 1 \times 10^{-28}$	Modulation, comparing two cells	^3He density, $\pi/2$ pulse, modulation
Gravitational Offset	$< 0.2 \times 10^{-28}$	with 1 nA leakage current	
^3He inhomogeneity due to leakage current heating	$< 1.5 \times 10^{-28}$	leakage $< 1\text{pA}$	Temperature B field gradient