

ANTI-PROTON PRODUCTION

- Production mechanism: pair production

$$\begin{array}{cccccc}
 p + p & \rightarrow & p + p + & \boxed{p + \bar{p}} & & \\
 E & m & m & m & m & \text{energy} \\
 p & 0 & 0 & 0 & 0 & \text{momentum}
 \end{array}$$

- Threshold energy in laboratory:

- Relativistic invariant: length of 4-vector $P^\mu = (E, p)$

- Energy and momentum conservation: $P_\mu P^\mu = p^2 - E^2$

- After: $E_{\text{tot}} = 4 m_p, \quad p_{\text{tot}} = 0: P_\mu P^\mu = -16 m_p^2$

- Before: $E_{\text{tot}} = E + m_p, \quad p_{\text{tot}}^2 = E^2 - m_p^2: E^2 - m_p^2 - (E + m_p)^2$

- $E^2 - m_p^2 - (E + m_p)^2 = -2m_p^2 - 2m_p E = -16 m_p^2$

- $E = 7 m_p = T + m_p : T = 6 m_p = 5.63 \text{ GeV}$

Bound protons: Fermi momentum \rightarrow threshold lowers to 4.3 GeV

