



CLIC physics potential for DM searches at 3 TeV using mono-photons and polarised beams

On behalf of
J-J. Blaising, P. Roloff, U. Schnoor, A. Wulzer



Outline

- Introduction.
- Background cross-section calculation, event simulation and systematic errors.
- $\sigma(95\%)$ calculation for different polarisation conditions and exclusion limits for Simplified DM models.
- Simplified DM model discrimination and DM mass determination.
- Summary



Introduction

For the CLICdp Yellow report and for the contributions prepared for Granada, the DM exclusion limits were computed by Ulrike using simplified DM models provided by Andrea. The limits were derived using $\sigma(95\%)$ computed using backgrounds without polarisation.

(PeL,PeR) polarised e^- beams change significantly the main SM background rate, $\nu \bar{\nu} \gamma$.

This study shows that using the B cross-section ratio $\sigma(L)/\sigma(R)$:

- improves significantly, $\sigma(95\%)$
- allows DM model discrimination and DM mass determination.



Background cross-section calculation and event simulation

Background cross-sections calculated at 3 TeV without/with e^- beam polarisation for $10^\circ < \theta_\gamma < 170^\circ$ and $P_{T\gamma}/\sqrt{s} > 0.02$.

Cross-section calculation and event generation done using Whizard with beam spectrum, isr function and n(1...3) matrix element photons.

Events with Isr γ 's overlapping ME γ 's were rejected using the merging procedure (Note: CLICdp-2020-004, Filip, Pawel ...).

Fast simulation used to take into account γ energy resolution and efficiency and $e^+ e^- \gamma$ veto efficiency.

The 3 TeV fast simulation based on extrapolation of full simulation.



Luminosity and Background Cross-sections 3TeV

	Polarisation		
	No	PeL= Pe ⁻ :-80%	PeR= Pe ⁻ :+80%
Integrated luminosity [ab ⁻¹]	5	4	1
Process	$\sigma[\text{fb}]$	$\sigma[\text{fb}]$	$\sigma[\text{fb}]$
$e^+ e^- \rightarrow \nu \bar{\nu} \gamma + \nu \bar{\nu} \gamma \gamma + \nu \bar{\nu} \gamma \gamma \gamma (\gamma)$	1058	1880	235
$e^+ e^- \rightarrow e^+ e^- \gamma + e^+ e^- \gamma \gamma + e^+ e^- \gamma \gamma \gamma (\gamma)$	1925	1960	1890

The luminosity sharing assumptions for different polarisation conditions.
Background σ values for $e^+ e^- \rightarrow \nu \bar{\nu} \gamma$ and $e^+ e^- \rightarrow e^+ e^- \gamma$ processes.
For PeR, $\sigma(\nu, \bar{\nu}, \gamma)$ is a factor 4.5 lower w.r.t. no polarisation and by a factor 8 w.r.t. PeL. $\sigma(e^+ e^- \gamma)$ has very little dependence on the beam polarisation.



Experimental systematic errors

Systematic error	Value
Event selection $\nu \bar{\nu} \gamma$	0.002
Event selection $e^+ e^- \gamma$	0.01 *
Luminosity	0.002
Polarisation	0.0025

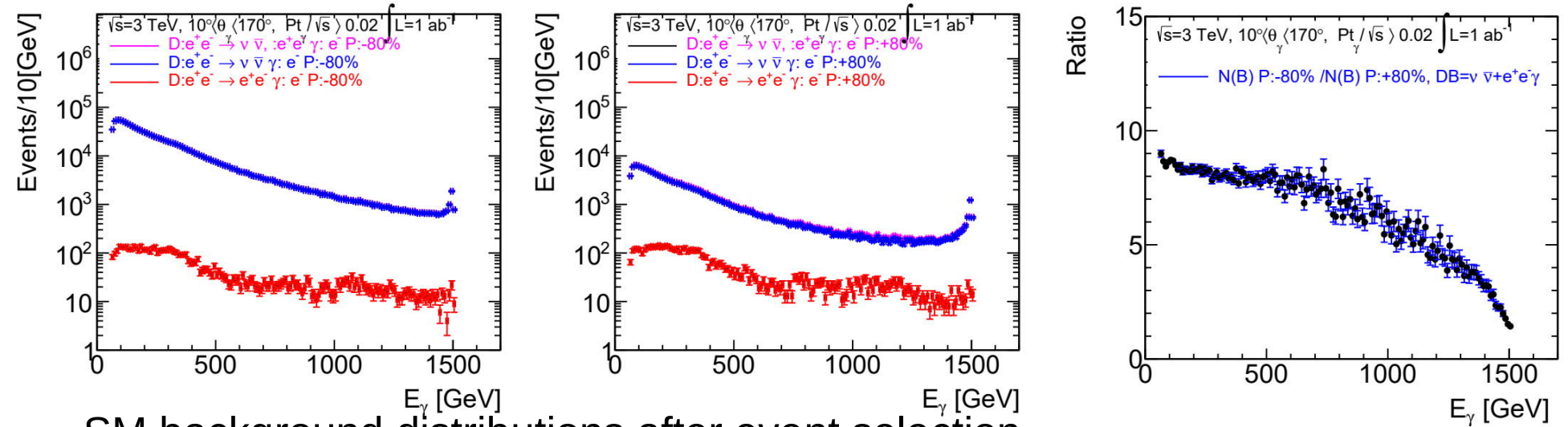
The values are those listed in the ILC paper arXiv:2001.03011v1.

* ILC does not assign a systematic error on the $e^+ e^- \gamma$ veto.

Assuming the sign of the polarisation can be reversed at each bunch train, experimental uncertainties will be strongly correlated and cancel out in cross section ratios.



SM backgrounds, $\int L = 1 \text{ ab}^{-1}$



SM background distributions after event selection.

Left : dN/dE_γ (PeL) for $\nu \bar{\nu} \gamma$, $e^+ e^- \gamma$ events and $\sum N(e^+ e^- \gamma) / N(\nu \bar{\nu} \gamma) = 0.005$

Middle: dN/dE_γ (PeR) for $\nu \bar{\nu} \gamma$, $e^+ e^- \gamma$ events and $\sum N(e^+ e^- \gamma) / N(\nu \bar{\nu} \gamma) = 0.04$

Right : $dN/dE_\gamma(B, \text{PeL}) / dN/dE_\gamma(B, \text{PeR})$, the shape of dR/dE_γ is due to the $\nu \bar{\nu} \gamma$ s and t-channel contributions changing with E_γ .

These 3 distributions are used to compute the 95%CL cross-section $\sigma(95\%)$.



$\sigma(95\%)$ and Z Calculation

To compute $\sigma(95\%)$ the likelihood ratio test statistic probability is computed using F1:

b = number of background events.

$b+s$ = number of background + signal events.

N_{obs} = number of background events

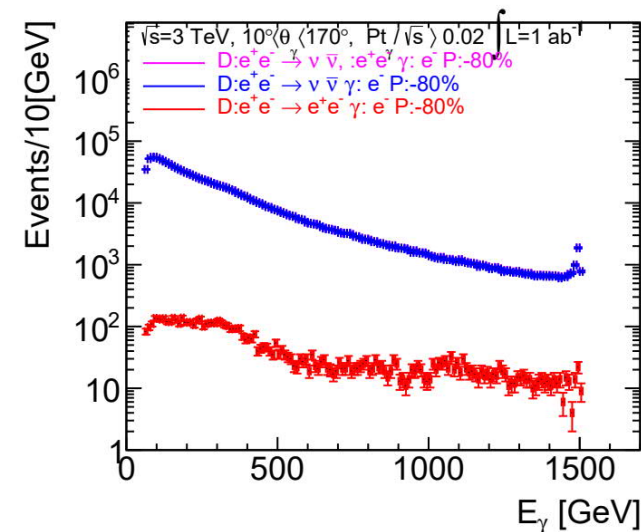
Significance $Z = \sqrt{2} \cdot \text{Erf}^{-1}(1-2P)$ (F2)

A 1 sided 95% CL upper limit corresponds to $P \geq 0.025$ and $Z \leq 2$.

$$P = \frac{\sum_{n=0}^{N_{obs}} (b+s)^n \frac{e^{-(b+s)}}{n!}}{\sum_{n=0}^{N_{obs}} (b)^n \frac{e^{-b}}{n!}} \quad (\text{F1})$$



$\sigma(95\%)$ calculation for $\text{PeL}=\text{Pe}^-:-80\%$



For a DM mass m_{XD} , $E_{\gamma\max} = \sqrt{s}/2 - 2m_{XD}^2/\sqrt{s}$.

The number of background events b is computed for $50 \text{ GeV} < E_{\gamma} < E_{\gamma\max}$ using F1.

For each m_{XD} the s excluded at 95%CL is computed using F2.
 $\sigma(95\%) = s/\text{Lumi}$.

$\sigma(95\%)$ is computed for m_{XD} masses in the range:

$200 \text{ GeV} < m_{XD} < 1400 \text{ GeV}$

with systematic errors.

Same procedure for PeR and PeL/PeR

$$b = \int_{E_{\gamma\min}}^{E_{\gamma\max}} dN/dE_{\gamma} \quad (\text{F1})$$

$$\frac{\sum_{n=0}^{N_{\text{obs}}} (b+s)^n \frac{e^{-(b+s)}}{n!}}{\sum_{n=0}^{N_{\text{obs}}} (b)^n \frac{e^{-b}}{n!}} \geq 0.025 \quad (\text{F2})$$



$d\sigma(95\%)/dm_{XD}$ results

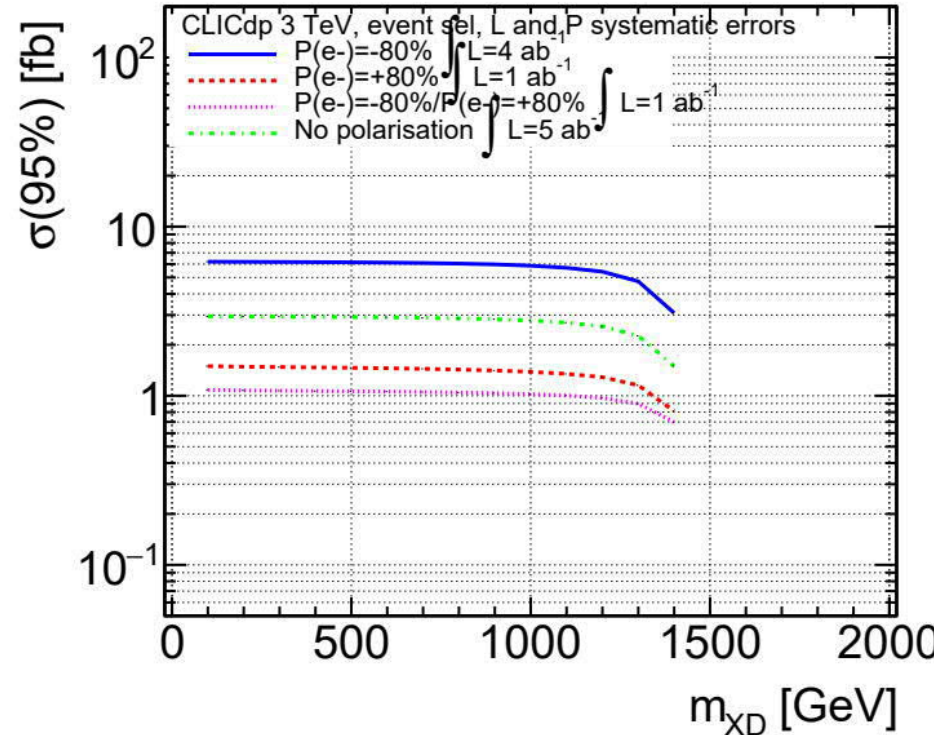
$d\sigma(95\%)/dm_{XD}$ for different polarisation and luminosity conditions with systematic errors (event selection+ luminosity+polarisation)

Polarisation	Luminosity ab^{-1}	$\sigma(95\%)$ fb
PeL	4	6
PeR	1	1.5
PeL/PeR	1	1
No	5	3

The lowest $\sigma(95\%)$ values are obtained using the ratio $dN/dE_{\gamma}(PeL)/dN/dE_{\gamma}(PeR)$ in which systematic errors cancel out.

October 2020

J-J Blaising/IN2P3/LAPP



10



Simplified DM models and exclusion limits calculation

Simplified DM models with interface to Whizard provided by Andrea Wulzer or made available by the Dmsimp authors at :

<http://feynrules.irmp.ucl.ac.be/wiki/DMSimp>

The parameters are

- DM mediator type YD, vector (v) or axial-vector(a-v) or scalar(s)
- Mediator mass m_{YD} and electron-YD coupling g_{e-Y}
- DM mass m_{XD} , mediator-XD coupling g_{Y-X}

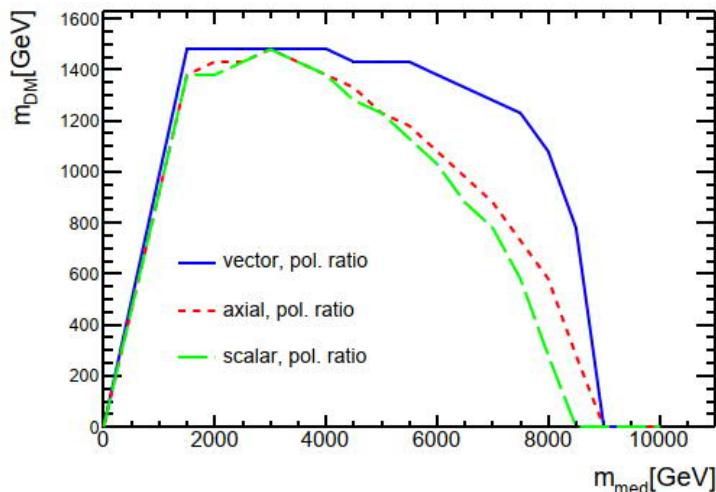
Limits were derived in the m_{XD} - m_{YD} plane by Ulrike using $\sigma(95\%)$ computed with the cross-section ratio $\sigma(\text{PeL})/\sigma(\text{PeR})$.

In the plane m_{XD} - m_{YD} , in many points, a scan over the cross-sections is performed. For each mediator mass m_{YD} , the limit in m_{XD} is the point where the cross-section $\sigma(m_{XD}, m_{YD}) \geq \sigma(95\%)$.



Simplified DM model limits

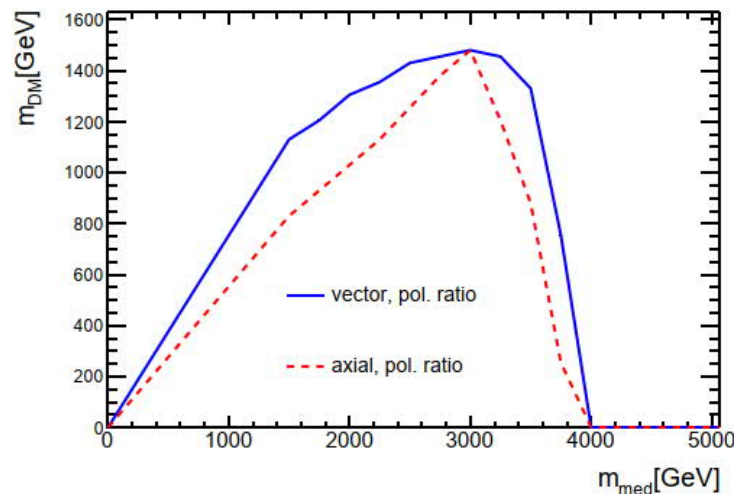
exclusion limits $g_{DM}=g_{lep}=1$ for CLIC-3000



compared to ESU limits from last year at $m(DM)=1$ GeV for 3 TeV with systematics:

- ▶ vector & axial-vector: 4800 GeV
- ▶ scalar: 4600 GeV

exclusion limits $g_{DM}=1, g_{lep}=0.1$ for CLIC-3000



compared to ESU limits from last year at $m(DM)=1$ GeV for 3 TeV with systematics:

- ▶ vector & axial-vector: 3200 GeV

scalar case only available for $g_{lep}=1$

$g_e Y=1$, large σ , w.r.t.2019, gain: 1.9

$g_e Y=0.1$, small σ , gain 1.25

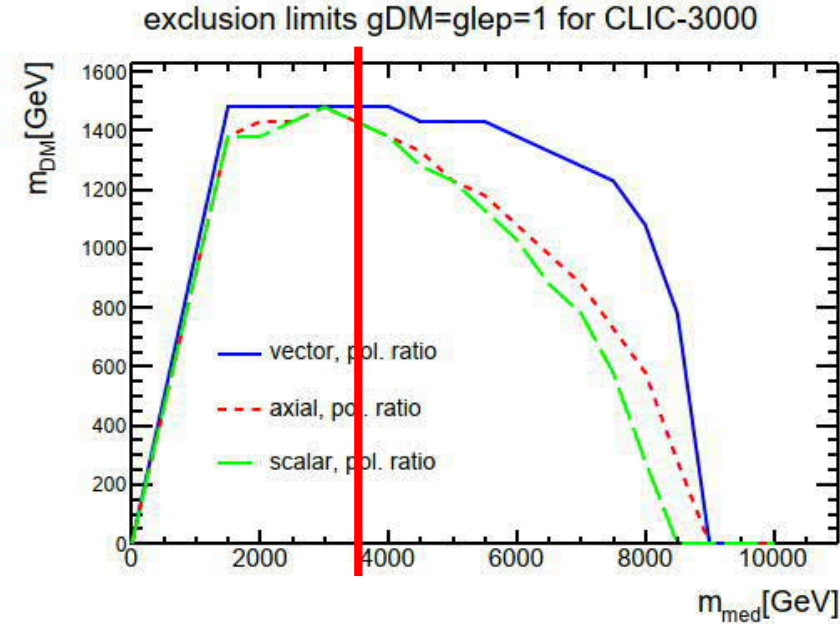
2019 limits determined with $\sigma(95)$ computed without polarized beams.



Model discrimination and mass determination

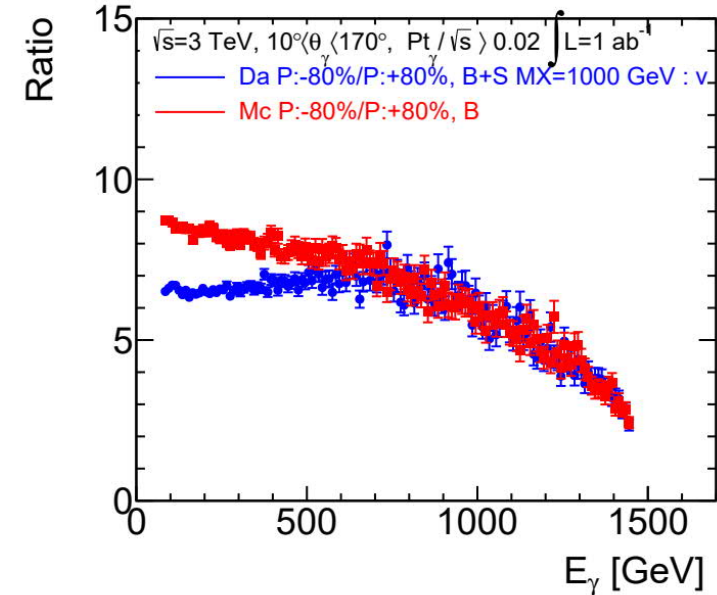
The Study done using the simplified DM models with the following conditions:

- DM mediator, v or $a-v$, $m_{YD}=3.5$ TeV
- Coupling $g_{e-Y}=1$ or 0.5
- DM mass m_{XD} from 200 GeV to 1.4 TeV (along the red line in the exclusion plot)
- Coupling $g_{Y-X}=1$





Expected Signal and Z calculation



$RBM(E_{\gamma}) = [dNB/dE_{\gamma}(PeL)]/[dNB/dE_{\gamma}(PeR)]$ (B only, red)
computed for $50 \text{ GeV} < E_{\gamma} < 1400 \text{ GeV}$

In presence of signal: e.g Data: YD- ν , mXD=1000 GeV

$RBPS(E_{\gamma}) = [dNBPS/dE_{\gamma}(PeL)]/[dNBPS/dE_{\gamma}(PeR)]$

(B+S, blue)

$\Rightarrow NSD(E_{\gamma}) = NBM(PeR) * (RBM - RBPSD) / (RBPSD - 1)$

For the templates (T), for ν , a- ν models the ratio:

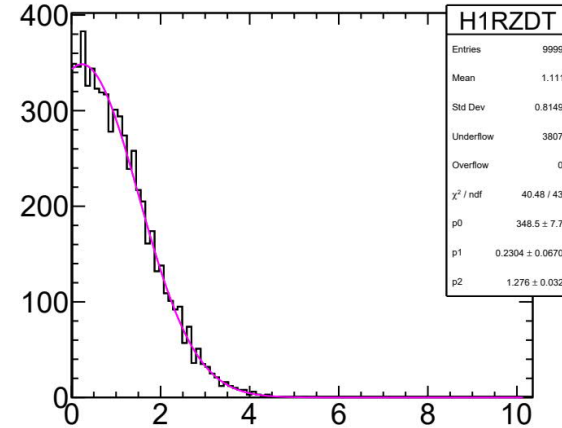
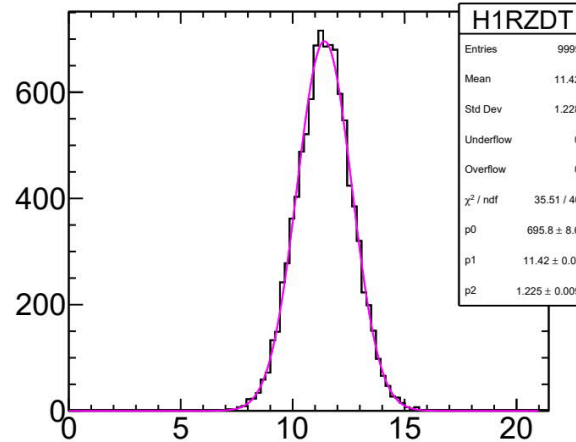
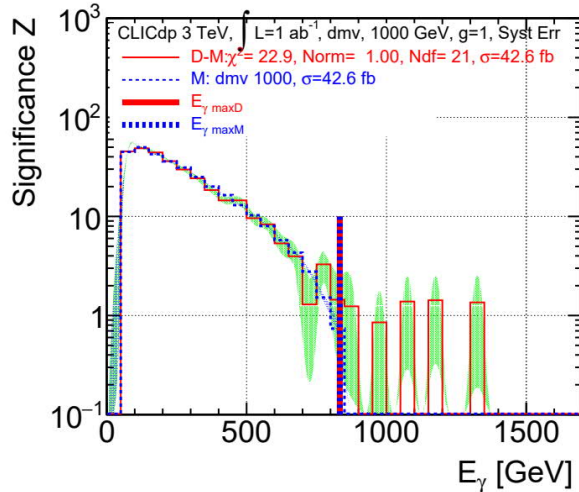
$RBPST(E_{\gamma}) = [dNBPS/dE_{\gamma}(PeL)]/[dNBPS/dE_{\gamma}(PeR)]$

$\Rightarrow NST(E_{\gamma}) = NBM(PeR) * (RBM - RBPST) / (RBPST - 1)$

$NSD(E_{\gamma})$ and $NST(E_{\gamma})$ are used to compute the significance $Z(E_{\gamma})$ of data and templates using the Roostat implementation of F2 slide 8.



dZ/dE γ , δZ calculation data-template χ^2 fit



dZ/dE γ Data: mXD=1000 GeV (red), dZ/dE γ Tmp : mXD=1000 GeV (blue).

in each E γ bin, δZ obtained using Toy MC events and a fit of dN/dZ

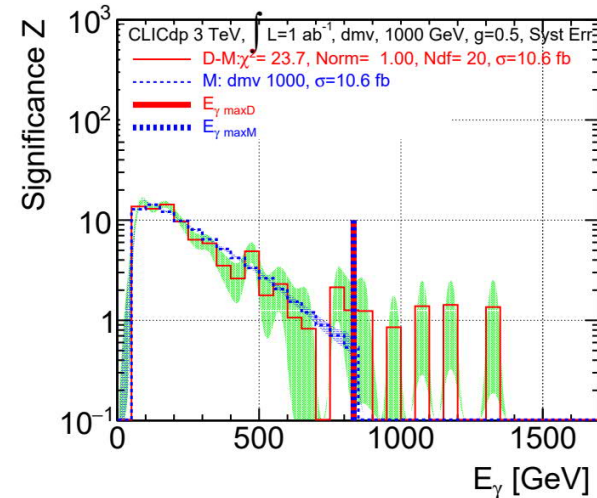
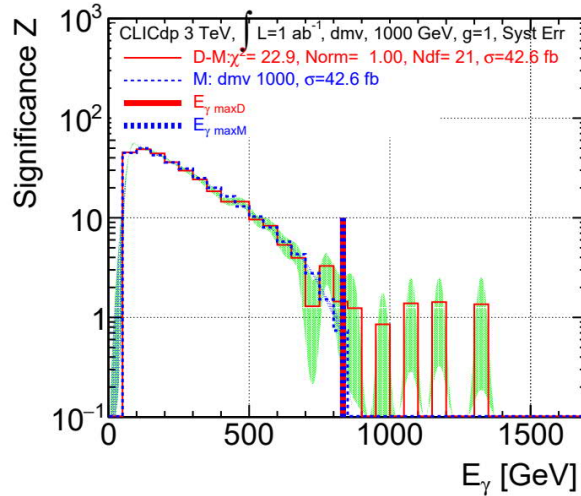
(plots for bin2 and bin14), green band is ZData $\pm 1 \sigma$.

For Tmp, B statistics 10x larger, to reduce B fluctuations, dN/dE γ hists are weighted.

Data-Tmp fit using: $\chi^2 = \sum [(Z\text{Data}(E\gamma) - Z\text{Tmp}(E\gamma))^2 / \delta Z(\text{Data}(E\gamma))^2]$, normalisation free.

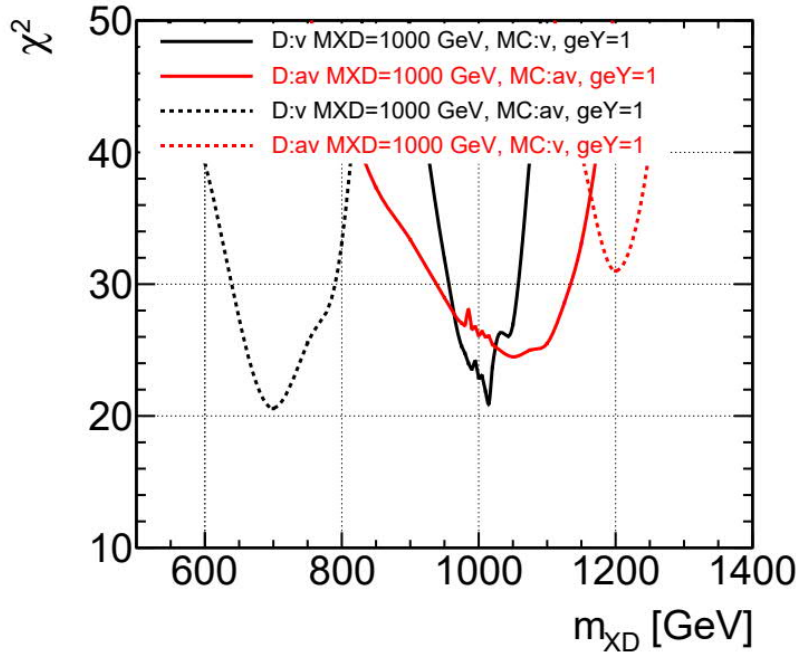


data-template χ^2 fit check



Left: dZ/dE_γ Data: Yv, $g_e - Y = 1.0$, $m_{XD} = 1000$ GeV, Tmp: Yv, $g_e - y = 1.0$, $m_{XD} = 1000$ GeV
 The plots shows also χ^2 , normalisation, Ndf and σ values and expected end-points.
 The data bins beyond end-point are due to data background fluctuations.

Right: dZ/dE_γ Data: Yv, $g_e - Y = 0.5$, $m_{XD} = 1000$ GeV, Tmp: Yv, $g_e - Y = 0.5$ $m_{XD} = 1000$ GeV
 $g_e - Y = 0.5 \Rightarrow \sigma$ four times lower, significance is lower, nevertheless $\chi^2 / Ndf \sim 1$

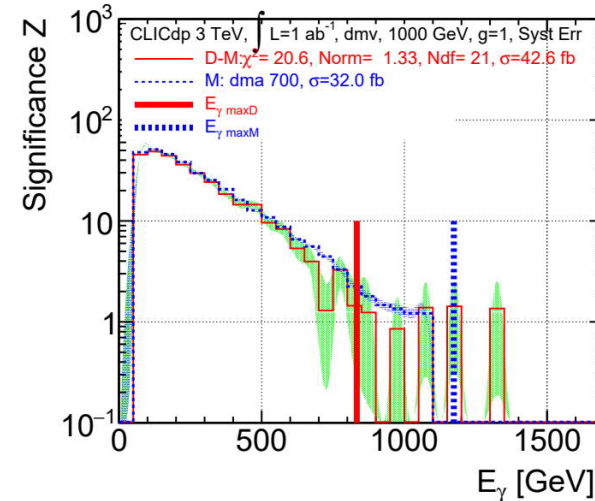
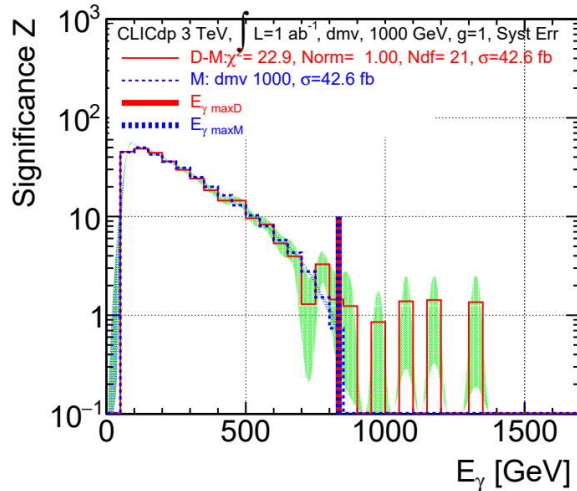


χ^2 fit for different data-tmp assumptions

χ^2 distributions as a function of m_{XD} for Data-Tmp fits (normalisation free) for $ge-Y=1$.
 For (Data-v,Tmp-v) fit (black) the min of χ^2 is 1015 GeV, the true mass is 1 TeV.
 For (Data-a-v, Tmp-a-v) fit (red) the min of χ^2 is 1050 GeV, the true mass is 1 TeV.
 For (Data-v,Tmp-a-v) fit (black dotted) the min of χ^2 is ~ 700 GeV, the true mass is 1 TeV.
 For (Data-a-v,Tmp-v) fit (red dotted) the min of χ^2 is ~ 1.2 TeV, the true mass is 1 TeV.
 How discriminate (v,v) from (v,a-v) and (a-v,a-v) from (a-v,v) ?



dZ/dE γ :data-template χ^2 fit v, a-v model discrimination



dZ/dE γ Data:Y-v, ge-y=1.0, mXD=1000 GeV, Tmp:Y-v , ge-y=1.0, mXD=1000 GeV

dZ/dE γ Data:Y-v, ge-y=1.0, mXD=1000 GeV, Tmp:Ya-v, ge-y=1.0, mXD= 700 GeV

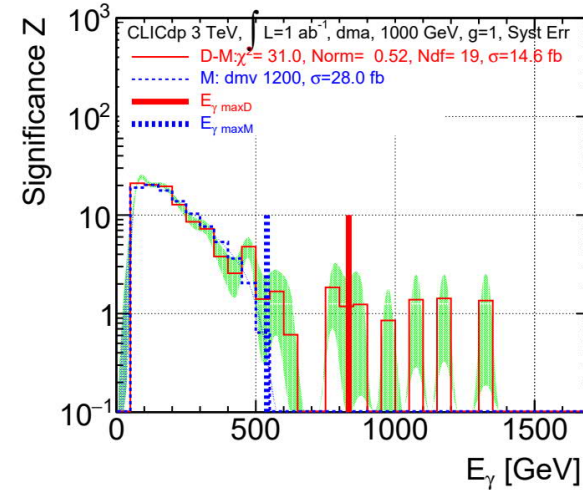
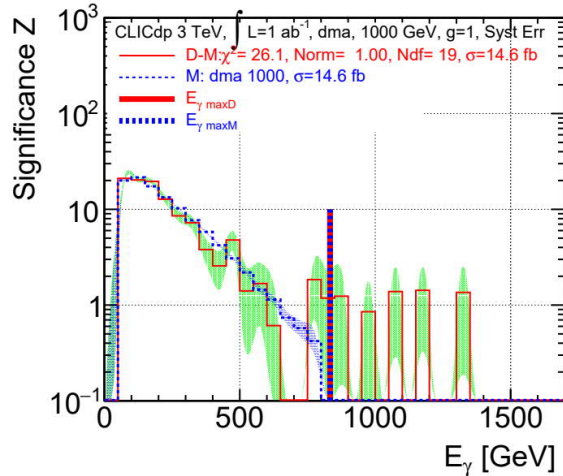
$\chi^2(v,v)=22.9 > \chi^2(v,a-v)=20.6$, *cannot discriminate using shape only.*

Norm(v,v)=1.0 and Norm(v,a-v)=1.33

Use normalisation to discriminate models.



dZ/dE γ , data-template χ^2 fit a-v, v model discrimination



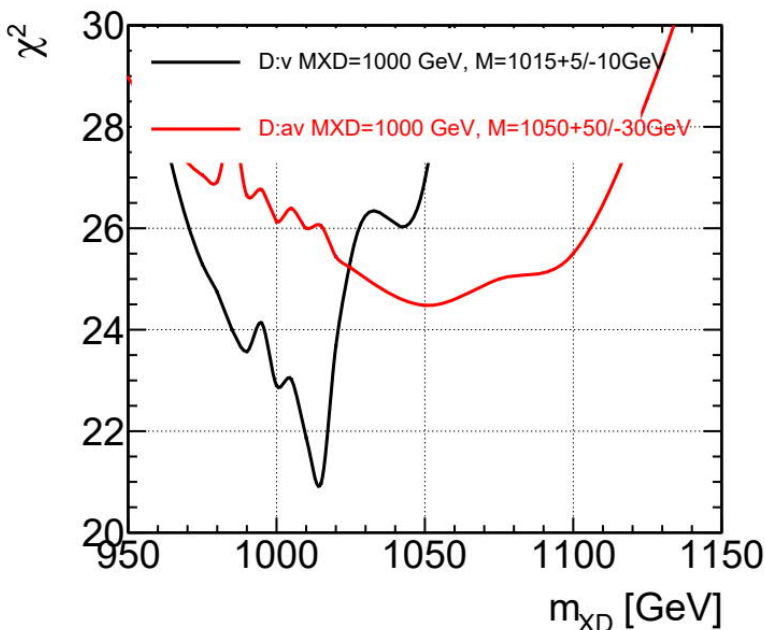
dZ/dE γ Data:Y-a-v, ge-y=1.0, mXD=1000 GeV, Tmp:Y-a-v, ge-y=1.0, mXD=1000 GeV

dZ/dE γ Data:Y-a-v, ge-y=1.0, mXD=1000 GeV, Tmp:Y-v, ge-y=1.0, mXD=1200 GeV

$\chi^2(\text{a-v, a-v})=26.1 < \chi^2(\text{a-v,v})=31$, can use shape to discriminate, but not alone, $\delta\chi^2=4.9$.

Norm(a-v,a-v)=1.0 and Norm(a-v,v)=0.52

Use shape and normalisation to discriminate models.



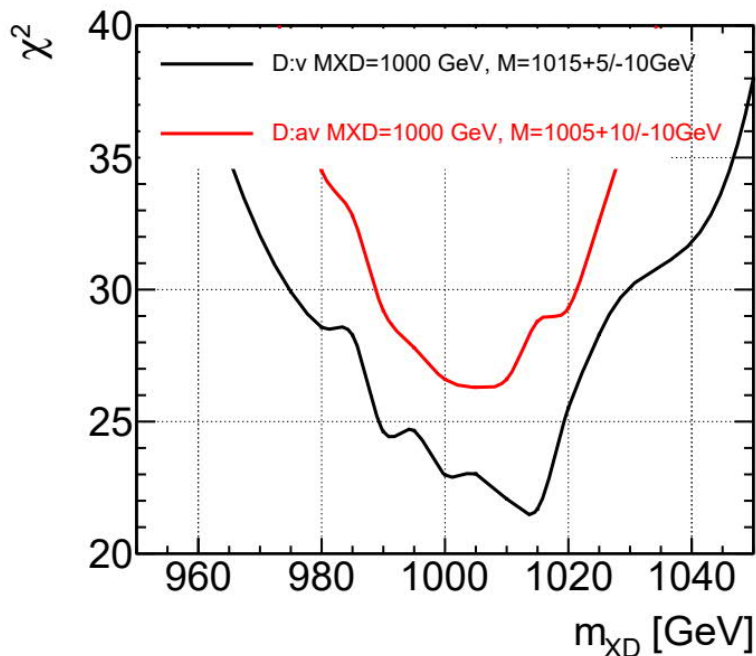
χ^2 fit, m_{XD} and δM determination

χ^2 distributions as a function of MXD for Data-Tmp fits (normalisation free) for $g_e\text{-}Y=1$.
Zoom into the region of the minimum.

m_{XD} is the value where χ^2 is minimum, δM corresponds to χ^2 variation of 1.

For (v,v) fit (black) $m_{XD}=1015 +5/-10$ GeV

For (a-v,a-v) fit (red) $m_{XD}=1050+50/-30$ GeV (lower $\sigma \Rightarrow$ larger δM)



χ^2 fit with normalisation =1

χ^2 distributions as a function of m_{XD} for Data-Tmp fits (normalisation=1) for $g_e\text{-}Y=1$.
For (v,v) fit (black) $m_{XD}=1015 +5/-10$ GeV
For (a-v,a-v) fit (red) $m_{XD}=1005+10/-10$ GeV
For $m_{XD}=1$ TeV, and normalisation fixed to 1, $\delta m_{XD}=1\%$.



Summary

Using $[d\sigma/dE\gamma(\text{PeL})] / [d\sigma/dE\gamma(\text{PeR})]$ allows computing $d\sigma(95\%)/dm_{\text{XD}}$ with reduced systematic errors, it improves significantly the exclusion limits.

Data-Temp χ^2 fits of $dZ/dE\gamma$ with normalisation free allow discriminating between ν and $a-\nu$ models, it requires taking into account the normalisation values.

It allows also the determination of the DM mass and error, the error δm_{XD} , depends on the cross section value.

For $m_{\text{XD}}=1$ TeV, and normalisation=1, $\delta m_{\text{XD}}=1\%$.



Thank You



Additional slides



Radiative Neutrinos Diagrams

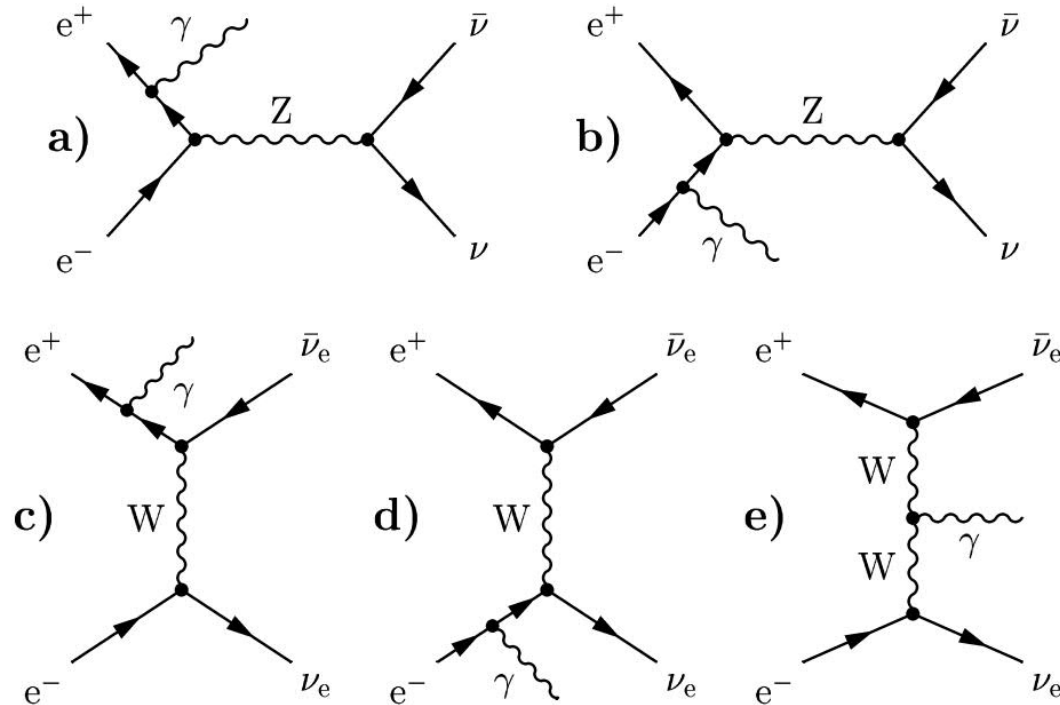
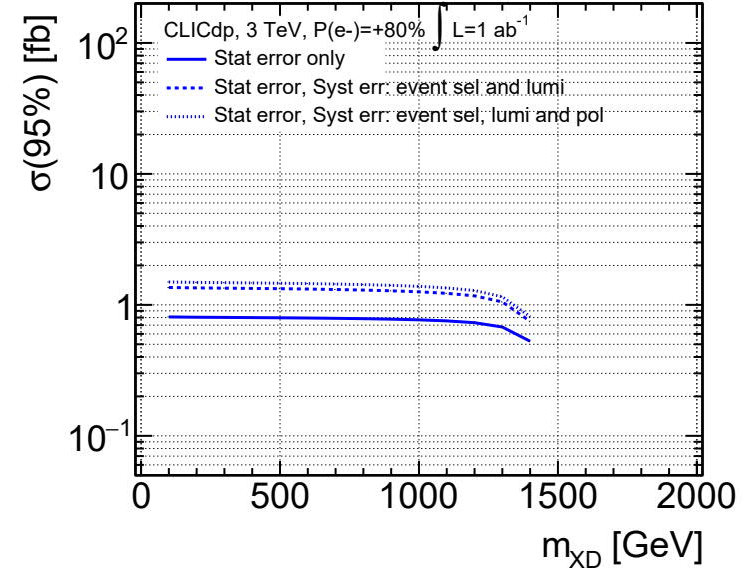
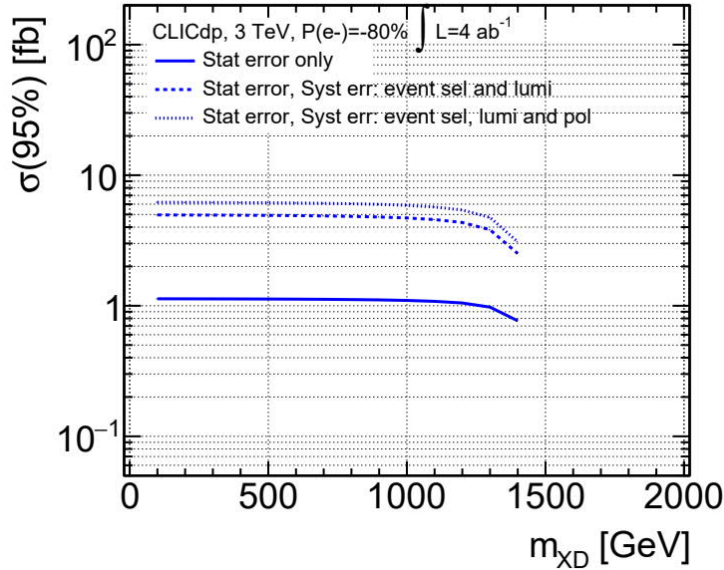


Figure 2.6: Lowest-order Feynman diagrams for the reaction $e^+e^- \rightarrow \nu\bar{\nu}\gamma$.



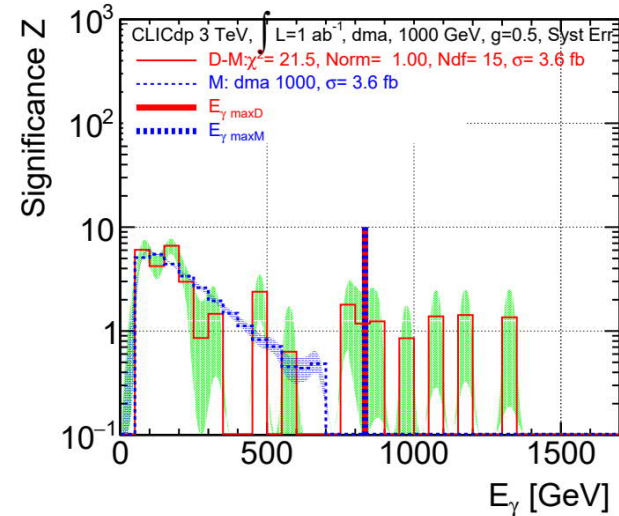
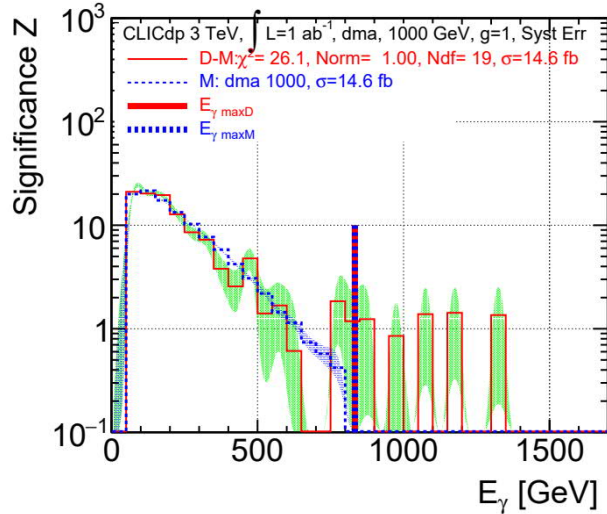
$d\sigma(95\%)/dm_{XD}$ for PeL and PeR



Polarisation	$\int L$ ab^{-1}	$\sigma(95\%) \text{ [fb]}$ No syst err	$\sigma(95\%) \text{ [fb]}$ with syst err
PeL	4	1.1	6
PeR	1	0.8	1.5



$dZ/dE_\gamma: Y_{a-v}$, data-template χ^2 fit



dZ/dE_γ Data: Y_{a-v} , $g_e Y = 1.0$, $m_{XD} = 1000$ GeV, Tmp: Y_{a-v} , $g_e Y = 1.0$, $m_{XD} = 1000$ GeV
 The plots show χ^2 , normalisation, Ndf and σ values, $\sigma(a-v)/\sigma(v) = 0.34 \Rightarrow$ lower Z.
 dZ/dE_γ Data: Y_{a-v} , $g_e Y = 0.5$, $m_{XD} = 1000$ GeV, Tmp: Y_{a-v} , $g_e Y = 0.5$, $m_{XD} = 1000$ GeV
 $g_e Y = 0.5 \Rightarrow \sigma$ four times lower, Z much lower.