

Measuring the polarization of boosted hadronic W bosons with jet substructure observables

presented by
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Objectives

- 1 To measure the longitudinal and transverse polarization fractions of hadronic decays of boosted W bosons

Motivation

- 1 In order to test unitarity in vector boson scattering (VBS), it will be ideal to measure the polarization fraction of both the outgoing weak bosons in a scattering process
- 2 The branching fraction of W boson decaying to hadrons is approximately 68%. It would greatly increase our statistical grasp of the polarization fractions, if we were able to measure the polarization of hadronic W bosons

Parton level angular distributions

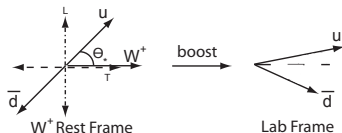


Figure: LEFT: The polar angle θ of the decay products of the W^+ as defined in W^+ rest-frame. RIGHT: Upon boosting to the lab-frame, the up and anti-down quarks can display an asymmetry in energy.

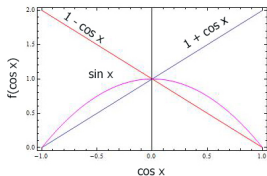


Figure: Distribution of amplitude in terms of $\cos\theta_*$

For transverse polarization of W-boson,

$$\mathcal{M}_{\pm} \propto \frac{1 \mp \cos\theta_*}{\sqrt{2}} \quad (1)$$

For longitudinal polarization of W-boson,

$$\mathcal{M}_0 \propto \frac{-\sin\theta_*}{\sqrt{2}} \quad (2)$$

Energy Difference

Potential observable in the lab frame at parton-level that can distinguish between longitudinal and transverse W^+ bosons,

$$\boxed{\cos\theta_* = \frac{\Delta E}{p_w}} \quad (3)$$

The distribution of the W^+ decay rate as a function of its decay polar angle,

$$\boxed{\frac{1}{\sigma} \frac{d\sigma}{d|\cos\theta_*|} = f_T \frac{3}{4} (1 + |\cos\theta_*|^2) + f_L \frac{3}{2} (1 - |\cos\theta_*|^2)} \quad (4)$$

where, the transverse polarization fraction f_T and the longitudinal polarization fraction f_L are related by, $f_T + f_L = 1$

Construction of proxy variable

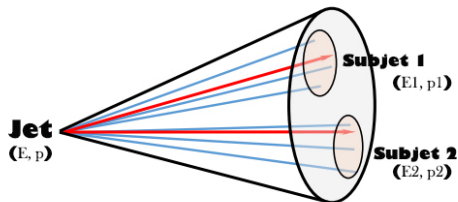
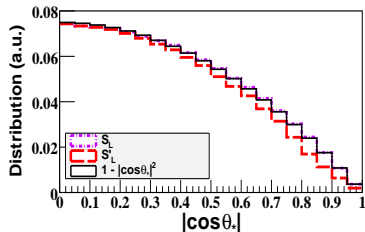


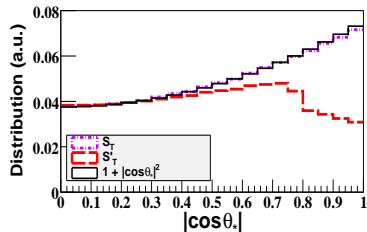
Figure: 2 subjets inside a jet (Courtesy: Nick Amin's presentation on Jet Substructure)

$$p_{\theta} = \frac{|\Delta E^{\text{reco}}|}{p_W^{\text{reco}}} \quad (5)$$

$|\cos\theta_*|$ distribution



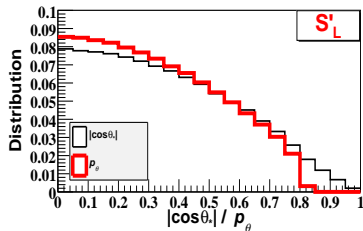
(a)



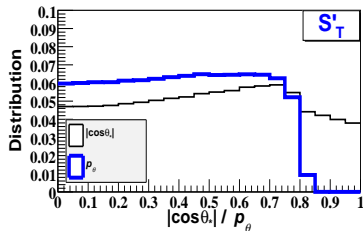
(b)

Figure: (a) Parton level truth information for the distributions of $|\cos\theta_*$ for longitudinal W bosons in the untagged longitudinal W^+ sample, S_L and the tagged sample S'_L . Also shown is the theoretically expected $(1 - |\cos\theta_*|^2)$ distribution which agrees very well with the S_L distribution. (b) Same as the left panel, but with transverse W bosons. Here, the theoretically expected distribution is $(1 + |\cos\theta_*|^2)$.

Distribution of the proxy variable



(a)



(b)

Figure: (a) Comparison of the distribution of p_θ with that of $|\cos\theta_*|$ for the S'_L event sample.
 (b) Same comparison for the S'_T sample.

Polarization Reconstruction in semi-leptonic VBS

The semi-leptonic VBS channel, $pp \rightarrow W^- W^+ jj \rightarrow \ell^- \nu_{\ell} jjjj$, where the W^+ boson decays hadronically and the W^- decays leptonically

1 Basic selection cuts

- 1 p_T of the lepton: $p_T^{\ell} > 25$ GeV
- 2 η of the lepton: $|\eta^{\ell}| < 2.5$
- 3 p_T of the jets: $p_T^j > 30$ GeV

2 Associated jet cuts

- 1 Pseudo-rapidity gap between the associated forward jets: $|\Delta\eta_{jj}| > 4.0$
- 2 Invariant mass of the associated jets: $M_{jj} > 200$ GeV
- 3 η of the forward jets: $2 < |\eta_j| < 4.7$

3 Hadronic W^+ tagging and selection cuts

- 1 Fat jet mass cut: $60 \text{ GeV} < M_j < 100 \text{ GeV}$
- 2 Mass-drop cut: $\mu^{\text{cut}} < 0.25, y^{\text{cut}} < 0.09$
- 3 N -Subjettiness Ratio: $\tau_2/\tau_1 < 0.3$
- 4 p_T of the tagged jet: $p_T^j > 400$ GeV

Polarization Reconstruction in semi-leptonic VBS

If the longitudinal polarization fraction in a sample is denoted as f_L *before* the tagging cuts are applied, then the polarization fraction *after* tagging cuts are applied (which we denote as f'_L) will be given by,

$$f'_L = \frac{\epsilon_L f_L}{\epsilon_L f_L + \epsilon_T (1 - f_L)}. \quad (6)$$

Here, ϵ_L and ϵ_T are the tagging efficiencies for longitudinal and transverse W bosons respectively.

Using this procedure, we find the expected longitudinal polarization fraction after tagging cuts are applied as $f'_L = 0.15$

**Monte-Carlo
Truth Information**

Polarization Reconstruction in semi-leptonic VBS

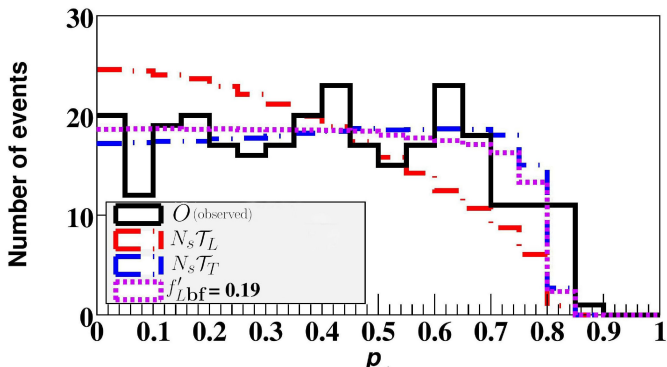


Figure: p_θ distribution for a benchmark sample of $N_s = 288$ VBS events, corresponding to $\sim 3 \text{ ab}^{-1}$ of luminosity, and after all selection and tagging cuts are applied (black curve). The best-fit linear combination of templates with longitudinal W fraction $f'_{Lbf} = 0.19$ is shown with the magenta dotted curve. Also shown are the longitudinal and transverse templates (\mathcal{T}_L and \mathcal{T}_T) rescaled to N_s events.

Polarization Reconstruction in semi-leptonic VBS

The χ^2 test-statistic with one parameter f'_L is given by,

$$\chi^2(f'_L) = \sum_{i=1}^B \frac{(O_i - N_s(f'_L \mathcal{T}_{Li} + (1 - f'_L) \mathcal{T}_{Ti}))^2}{\sigma_i^2} \quad (7)$$

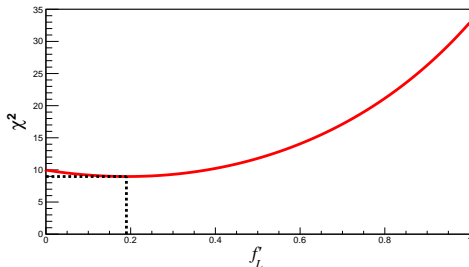


Figure: χ^2 distribution as a function of the longitudinal polarization fraction f'_L for fits to the pseudo-experiment data. We obtain a best-fit value of $f'_{L\text{bf}} = 0.19$ with a 1- σ range between $[0.00, 0.38]$. The fit is quite good at the minimum with a χ^2 per degree of freedom of 0.6. Values of $f'_L > 0.88$ can be ruled out at the 95% confidence level.

Conclusion

- 1 At the parton level, the distribution of the decay polar angle $|\cos\theta_*|$ allows us to extract the longitudinal vs transverse polarization fraction
- 2 We found our hadron level proxy variable p_θ to track the $|\cos\theta_*|$ extremely well
- 3 For semi-leptonic WW scattering, we showed that with 3 ab^{-1} of integrated luminosity at the HL-LHC, we potentially reconstruct the observed longitudinal polarization fraction to within a ± 0.15 uncertainty at the $1\text{-}\sigma$ level

**THANK
YOU!**



Backup slides

N-Subjettiness Definition

The N -subjettiness technique can be used to identify the number of hard centres of energy within a fat-jet. For each N candidate subjets, we construct the following variable,

$$\tau_N = \min_{\hat{n}_1, \hat{n}_2, \dots, \hat{n}_N} \tilde{\tau}_N, \text{ where,}$$

$$\tilde{\tau}_N = \frac{1}{d_0} \sum_k p_{T,k} \min\{(\Delta R_{1,k}), (\Delta R_{2,k}), \dots, (\Delta R_{N,k})\} \quad (8)$$

- 1 $\tau_N \approx 0 \Rightarrow$ there are N or fewer subjets & $\tau_N \gg 0 \Rightarrow$ there are at least N+1 subjets
- 2 The ratio τ_2/τ_1 is preferred as a discriminating variable to discriminate between W boson and the QCD background

Construction of templates

Generated 1 million events:
 $pp \rightarrow \phi \rightarrow W^+W \rightarrow jjjj$ at $\sqrt{s} = 13$ TeV in MadGraph.
At the generator level, $800 \text{ GeV} < p_T^W < 1000 \text{ GeV}$

Showered & hadronized in Pythia

Clustered using the CA algorithm in FastJet with a jet radius $R_0 = 1.0$. Also, implemented pruning to remove soft tracks

- 1 Mass cut: $60 \text{ GeV} < M_J < 100 \text{ GeV}$,
- 2 Mass-drop cut: $\mu^{\text{cut}} < 0.25$ and $y^{\text{cut}} < 0.09$,
- 3 N -subjettiness cut: $\tau_2/\tau_1 < 0.3$

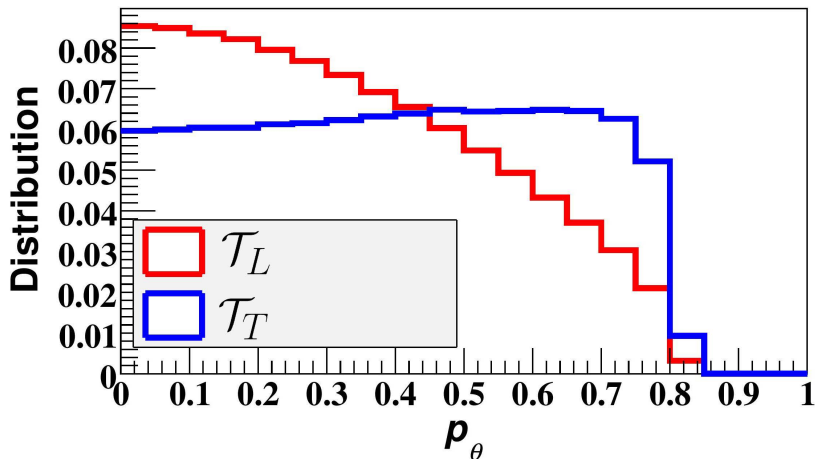


Figure: We now define universal templates \mathcal{T}_L and \mathcal{T}_T for the proxy variable distributions, as shown in the figure. These templates can be used to extract W boson polarization in a mixed sample.