

# Phenomenology of the minimal inverse-seesaw with Abelian flavour symmetries

Filipe R. Joaquim

Departamento de Física and CFTP, Instituto Superior Técnico, Lisboa



Based on work in collaboration with **Henrique Câmara** & R.G. Felipe

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# Inverse-seesaw (ISS) mechanism

## INVERSE SEESAW

### ISS( $n_R, n_s$ )

Mohapatra; Mohapatra & Valle'86;  
Gonzalez-Garcia & Valle'89

$$(3 + n_R + n_s) \times (3 + n_R + n_s)$$

$$\mathcal{M} = \begin{pmatrix} 0 & \mathbf{M}_D^* & 0 \\ \mathbf{M}_D^\dagger & 0 & \mathbf{M}_R \\ 0 & \mathbf{M}_R^T & \mathbf{M}_s \end{pmatrix}$$

- Sterile neutrino fields:  $\nu_{Ri}$  ( $i = 1, \dots, n_R$ ),  $s_i$  ( $i = 1, \dots, n_s$ )

$$-\mathcal{L}_{\text{mass}}^{\text{ISS}} = \bar{e}_L \mathbf{M}_\ell e_R + \bar{\nu}_L \mathbf{M}_D \nu_R + \bar{\nu}_R \mathbf{M}_R s + \frac{1}{2} \bar{s}^c \mathbf{M}_s s + \text{H.c.}$$

- Effective neutrino mass matrix ( $m_D, \mu_s \ll M$ ):

$$\mathbf{M}_{\text{eff}} = -\mathbf{M}_D^* (\mathbf{M}_R^T)^{-1} \mathbf{M}_s \mathbf{M}_R \mathbf{M}_D^\dagger \longrightarrow m_\nu \sim \mu_s \frac{m_D^2}{M^2}$$

- Active-sterile mixing:

$$\mathbf{U}_{\text{Hl}} \simeq \mathbf{V}_L^\dagger (0, \mathbf{M}_D (\mathbf{M}_R^\dagger)^{-1}) \mathbf{U}_s \longrightarrow U_{\text{Hl}} \sim \frac{m_D}{M} \sim \sqrt{\frac{m_\nu}{\mu_s}}$$

$$\text{Type-I seesaw: } m_\nu \sim \frac{m_D^2}{M}, U_{\text{Hl}} \sim \frac{m_D}{M} \sim \sqrt{\frac{m_\nu}{M}}$$

The ISS provides a natural template for (active) neutrino mass suppression with sizeable active-sterile mixing

### Minimal Inverse Seesaw:

$$\text{ISS}(n_R, n_s) \longrightarrow \text{ISS}(2, 2)$$

Abada & Lucente'14

- One massless neutrino
- Neutrino data can be accommodated
- Still 17 parameters (in the  $\mathbf{M}_s$  diagonal basis)

# Neutrino oscillation data

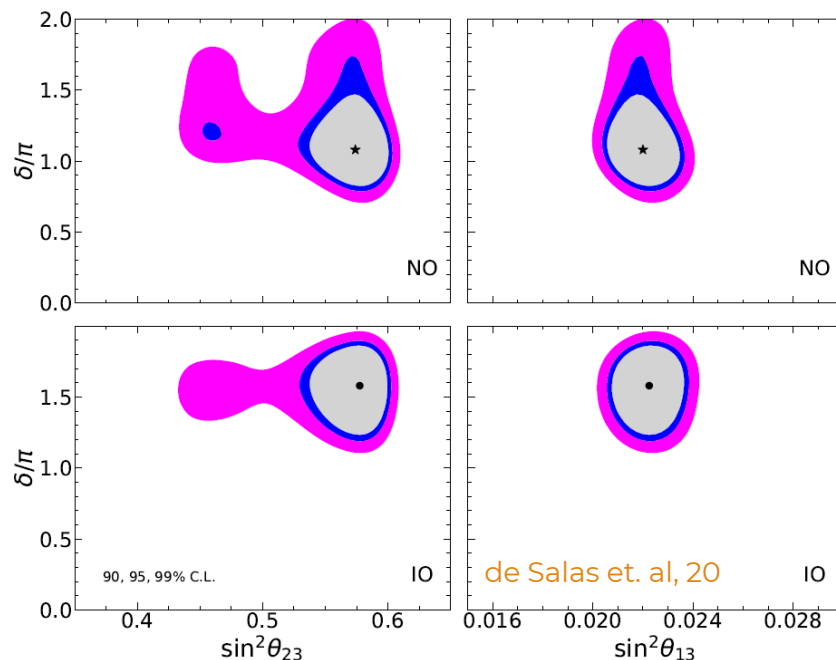
## Minimal Inverse Seesaw ISS(2,2):

17 parameters vs 7 observables

$$\theta_{12}, \theta_{23}, \theta_{13}, \Delta m_{21,31}^2, \delta, \alpha$$

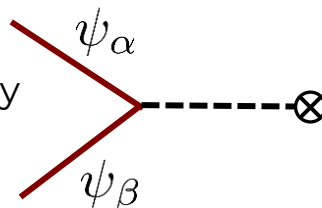
Parameter	Best Fit $\pm 1\sigma$	$3\sigma$ range
$\theta_{12}(\circ)$	$34.3 \pm 1.0$	$31.4 \rightarrow 37.4$
$\theta_{23}(\circ)$ [NO]	$48.79_{-1.25}^{+0.93}$	$41.63 \rightarrow 51.32$
$\theta_{23}(\circ)$ [IO]	$48.79_{-1.30}^{+1.04}$	$41.88 \rightarrow 51.30$
$\theta_{13}(\circ)$ [NO]	$8.58_{-0.15}^{+0.11}$	$8.16 \rightarrow 8.94$
$\theta_{13}(\circ)$ [IO]	$8.63_{-0.15}^{+0.11}$	$8.21 \rightarrow 8.99$
$\delta(\circ)$ [NO]	$216_{-25}^{+41}$	$144 \rightarrow 360$
$\delta(\circ)$ [IO]	$277_{-24}^{+23}$	$205 \rightarrow 342$
$\Delta m_{21}^2 (\times 10^{-5} \text{ eV}^2)$	$7.50_{-0.20}^{+0.22}$	$6.94 \rightarrow 8.14$
$ \Delta m_{31}^2  (\times 10^{-3} \text{ eV}^2)$ [NO]	$2.56_{-0.04}^{+0.03}$	$2.46 \rightarrow 2.65$
$ \Delta m_{31}^2  (\times 10^{-3} \text{ eV}^2)$ [IO]	$2.46 \pm 0.03$	$2.37 \rightarrow 2.55$

de Salas et. al, 20; Capozzi et. al'20; Esteban et. al'20



## ABELIAN FLAVOUR SYMMETRIES

- All mass terms generated dynamically
- CPV from vacuum phases (SCPV)



$$\langle \phi_a^0 \rangle = v_a e^{i\theta_a}$$

$$\langle S_a \rangle = u_a e^{i\xi_a}$$

Mass matrices

$$\mathbf{M}_\ell, \mathbf{M}_D$$

$$\mathbf{M}_R, \mathbf{M}_s$$

# Scalar content and Yukawa Lagrangian

- Need to add a **second Higgs doublet** to be able to realise the charged-lepton mass matrix textures.
- Add **two neutral complex scalar singlets** to dynamically generate  $\mathbf{M}_S$  and  $\mathbf{M}_R$ .

$$\Phi_{1,2} = \begin{pmatrix} \phi_{1,2}^+ \\ \phi_{1,2}^0 \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} \sqrt{2}\phi_{1,2}^+ \\ v_{1,2}e^{i\theta_{1,2}} + \rho_{1,2} + i\eta_{1,2} \end{pmatrix}, \quad S_{1,2} = \frac{1}{\sqrt{2}} (u_{1,2}e^{i\xi_{1,2}} + \rho_{3,4} + i\eta_{3,4})$$

## Yukawa Lagrangian

$$-\mathcal{L}_{\text{Yuk.}} = \bar{\ell}_L (\mathbf{Y}_\ell^1 \Phi_1 + \mathbf{Y}_\ell^2 \Phi_2) e_R + \bar{\ell}_L (\mathbf{Y}_D^1 \tilde{\Phi}_1 + \mathbf{Y}_D^2 \tilde{\Phi}_2) \nu_R \\ + \frac{1}{2} \bar{s}^c (\mathbf{Y}_s^1 S_1 + \mathbf{Y}_s^2 S_1^*) s + \bar{\nu}_R (\mathbf{Y}_R^1 S_2 + \mathbf{Y}_R^2 S_2^*) s + \text{H.c.}$$

## SCALAR POTENTIAL

$$V(\Phi_a, S_a) = V_{\text{sym.}} + V_{\text{soft}}(\Phi_a, S_a)$$

$$V_{\text{soft}}(\Phi_a, S_a) = \mu_{12}^2 \Phi_1^\dagger \Phi_2 + \mu_3^2 S_1^2 + \mu_4 |S_1|^2 S_1 \\ + \mu_5 |S_2|^2 S_2 + \text{H.c.}$$

$$\text{SCPV IS ACHIEVED WITH: } \theta, \xi_2 = 0, \xi_1 = \arctan \left( \frac{\sqrt{32\mu_3^4 - \mu_4^2 u_1^2}}{\mu_4 u_1} \right)$$

# Abelian flavour symmetries

- Maximally-restrictive sets compatible with neutrino oscillation data that are **realizable** by Abelian symmetries:

$$\mathbf{G}_F = \mathrm{U}(1) \times \mathbb{Z}_n \times \mathrm{U}(1)_F, \quad n = 2, 4$$

Fields	U(1)	$(5_{1,I}^\ell, T_{45})$	$(4_3^\ell, T_{124})$	$(4_3^\ell, T_{456})$	$(4_3^\ell, T_{136,I})$	$(4_3^\ell, T_{146,I})$
		$\mathbb{Z}_2 \times \mathrm{U}(1)_F$	$\mathbb{Z}_2 \times \mathrm{U}(1)_F$	$\mathbb{Z}_2 \times \mathrm{U}(1)_F$	$\mathbb{Z}_4 \times \mathrm{U}(1)_F$	$\mathbb{Z}_4 \times \mathrm{U}(1)_F$
$\Phi_1$	0	(1, 1)	(0, -5)	(1, 1)	(1, 2)	(0, 1)
$\Phi_2$	0	(0, -1)	(1, -3)	(0, -1)	(0, 1)	(3, 0)
$S_1$	0	(0, 2)	(0, -2)	(0, -2)	(0, -2)	(0, -2)
$S_2$	1	(0, 0)	(0, 0)	(1, 0)	(0, 0)	(0, 0)
$\ell_{eL}$	1	(1, 0)	(0, 0)	(0, 0)	(2, 0)	(2, 0)
$\ell_{\mu L}$	1	(0, 2)	(1, 2)	(1, -2)	(1, -1)	(1, -1)
$\ell_{\tau L}$	1	(0, -2)	(0, 4)	(0, -4)	(0, -2)	(0, -2)
$e_R$	1	(1, -3)	(0, 9)	(1, -5)	(3, -4)	(0, -3)
$\mu_R$	1	(0, 3)	(1, 7)	(0, -3)	(0, -3)	(1, -2)
$\tau_R$	1	(0, -1)	(0, 5)	(1, -1)	(1, -2)	(2, -1)
$\nu_{R_1}$	1	(0, 1)	(0, -1)	(0, -1)	(0, -1)	(0, -1)
$\nu_{R_2}$	1	(1, -1)	(1, 1)	(1, 1)	(2, 1)	(2, 1)
$s_1$	0	(1, -1)	(1, 1)	(0, 1)	(2, 1)	(2, 1)
$s_2$	0	(0, 1)	(0, -1)	(1, -1)	(0, -1)	(0, -1)

# Abelian flavour symmetries

## ONLY INTERESTING CASE

Fields	U(1)	$(5_{1,I}^\ell, T_{45})$ $\mathbb{Z}_2 \times U(1)_F$
$\Phi_1$	0	(1, 1)
$\Phi_2$	0	(0, -1)
$S_1$	0	(0, 2)
$S_2$	1	(0, 0)
$\ell_{eL}$	1	(1, 0)
$\ell_{\mu L}$	1	(0, 2)
$\ell_{\tau L}$	1	(0, -2)
$e_R$	1	(1, -3)
$\mu_R$	1	(0, 3)
$\tau_R$	1	(0, -1)
$\nu_{R1}$	1	(0, 1)
$\nu_{R2}$	1	(1, -1)
$s_1$	0	(1, -1)
$s_2$	0	(0, 1)

$$-\mathcal{L}_{\text{Yuk.}} = \bar{\ell}_L (\mathbf{Y}_\ell^1 \Phi_1 + \mathbf{Y}_\ell^2 \Phi_2) e_R + \bar{\ell}_L (\mathbf{Y}_D^1 \tilde{\Phi}_1 + \mathbf{Y}_D^2 \tilde{\Phi}_2) \nu_R + \frac{1}{2} \bar{s}^c (\mathbf{Y}_s^1 S_1 + \mathbf{Y}_s^2 S_1^*) s + \bar{\nu}_R (\mathbf{Y}_R^1 S_2 + \mathbf{Y}_R^2 S_2^*) s + \text{H.c.}$$

## Mass matrices Yukawa decompositions

$\mathbf{M}_\ell$	$\mathbf{Y}_\ell^1$	$\mathbf{Y}_\ell^2$
$5_{1,I}^\ell$	$\begin{pmatrix} 0 & 0 & \times \\ 0 & 0 & 0 \\ \times & 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 0 & 0 \\ 0 & \times & 0 \\ 0 & 0 & \times \end{pmatrix}$

$\mathbf{M}_R$	$\mathbf{Y}_R$
$T_{14}$	$\begin{pmatrix} 0 & \times \\ \times & 0 \end{pmatrix}$

$\mathbf{M}_D$	$\mathbf{Y}_D^1$	$\mathbf{Y}_D^2$
$T_{45}$	$\begin{pmatrix} \times & 0 \\ 0 & 0 \\ 0 & \times \end{pmatrix}$	$\begin{pmatrix} 0 & \times \\ \times & 0 \\ 0 & 0 \end{pmatrix}$

$\mathbf{M}_s$	$\mathbf{Y}_s^1$	$\mathbf{Y}_s^2$
$T_{23}$	$\begin{pmatrix} \times & 0 \\ 0 & 0 \end{pmatrix}$	$\begin{pmatrix} 0 & 0 \\ 0 & \times \end{pmatrix}$

# A common origin for Leptonic CPV

- Parameterisation of the charged lepton-mass matrix:

$$5_1^\ell : \mathbf{M}_\ell = \begin{pmatrix} 0 & 0 & a_1 \\ 0 & m_{\ell_1}^2 & 0 \\ a_2 & 0 & a_4 \end{pmatrix}, \quad \mathbf{H}_\ell = \begin{pmatrix} a_1^2 & 0 & a_1 a_4 \\ 0 & a_3^2 & 0 \\ a_1 a_4 & 0 & a_2^2 + a_4^2 \end{pmatrix}, \quad \mathbf{V}'_L = \begin{pmatrix} c_L & 0 & s_L \\ 0 & 1 & 0 \\ -s_L & 0 & c_L \end{pmatrix} \theta_L$$

$$5_1^e : \mathbf{V}_{L,R} = \mathbf{V}'_{L,R} \mathbf{P}_{12}, \quad 5_1^\mu : \mathbf{V}_{L,R} = \mathbf{V}'_{L,R}, \quad 5_1^\tau : \mathbf{V}_{L,R} = \mathbf{V}'_{L,R} \mathbf{P}_{23},$$

NO<sub>e,μ,τ</sub>, IO<sub>e,μ,τ</sub> → 6 distinct cases to be analysed

REAL YUKAWAS (CP is conserved @ the Lagrangian level)

$$\mathbf{Y}_D^1 = \begin{pmatrix} b_1 & 0 \\ 0 & 0 \\ 0 & b_2 \end{pmatrix}, \quad \mathbf{Y}_D^2 = \begin{pmatrix} 0 & b_3 \\ b_4 & 0 \\ 0 & 0 \end{pmatrix}, \quad \mathbf{Y}_R = \begin{pmatrix} 0 & d_2 \\ d_1 & 0 \end{pmatrix}, \quad \mathbf{Y}_s^1 = \begin{pmatrix} f_2 & 0 \\ 0 & 0 \end{pmatrix}, \quad \mathbf{Y}_s^2 = \begin{pmatrix} 0 & 0 \\ 0 & f_1 \end{pmatrix}$$

VEV configuration:

$$\langle \phi_1^0 \rangle = v \cos \beta$$

$$\langle \phi_2^0 \rangle = v \sin \beta$$

$$\langle S_1 \rangle = u_1 e^{i\xi}, \quad \langle S_2 \rangle = u_2$$

$$\mathbf{M}_D = \begin{pmatrix} m_{D_1} & m_{D_3} \\ m_{D_4} & 0 \\ 0 & m_{D_2} \end{pmatrix}, \quad \mathbf{M}_R = \begin{pmatrix} 0 & M \\ qM & 0 \end{pmatrix}, \quad \mathbf{M}_s = \begin{pmatrix} p \mu_s e^{i\xi} & 0 \\ 0 & \mu_s e^{-i\xi} \end{pmatrix}$$

# Correlation between low-energy observables

- EFFECTIVE NEUTRINO MASS MATRIX:  $\mathbf{V}_L^\dagger \mathbf{M}_{\text{eff}} \mathbf{V}_L$

$$\mathbf{M}_{\text{eff}} = e^{-i\xi} \begin{pmatrix} \frac{y^2}{x} + \frac{z^2}{w} e^{2i\xi} & y & ze^{2i\xi} \\ y & x & 0 \\ ze^{2i\xi} & 0 & we^{2i\xi} \end{pmatrix}, \quad \mathbf{V}_L = \begin{pmatrix} \cos \theta_L & 0 & \sin \theta_L \\ 0 & 1 & 0 \\ -\sin \theta_L & 0 & \cos \theta_L \end{pmatrix}$$

$$5_1^e : \mathbf{V}_{L,R} = \mathbf{V}'_{L,R} \mathbf{P}_{12}$$

$$5_1^\mu : \mathbf{V}_{L,R} = \mathbf{V}'_{L,R}$$

$$5_1^\tau : \mathbf{V}_{L,R} = \mathbf{V}'_{L,R} \mathbf{P}_{23}$$

$$z = \mu_s \frac{m_{D_2} m_{D_3}}{M^2} \frac{p}{q^2}, \quad w = \mu_s \frac{m_{D_2}^2}{M^2} \frac{p}{q^2}, \quad x = \mu_s \frac{m_{D_4}^2}{M^2}, \quad y = \mu_s \frac{m_{D_1} m_{D_4}}{M^2}$$

- The effective light neutrino mass matrix is written solely in terms of **6 effective parameters**:

$$(x, y, z, w, \theta_L, \xi) \longrightarrow \mathcal{O}_i \equiv (\Delta m_{21}^2, \Delta m_{31}^2, \theta_{ij}, \delta, \alpha)$$

$$\text{NO} : M_{ij} = \left[ \mathbf{U}'^* \text{diag} \left( 0, \sqrt{\Delta m_{21}^2}, \sqrt{\Delta m_{31}^2} \right) \mathbf{U}'^\dagger \right]_{ij}$$

$$\text{IO} : M_{ij} = \left[ \mathbf{U}'^* \text{diag} \left( \sqrt{\Delta m_{31}^2}, \sqrt{\Delta m_{21}^2 + \Delta m_{31}^2}, 0 \right) \mathbf{U}'^\dagger \right]_{ij}$$

$$D_{ij} = M_{ii} M_{jj} - M_{ij}^2$$

Low-energy relations:

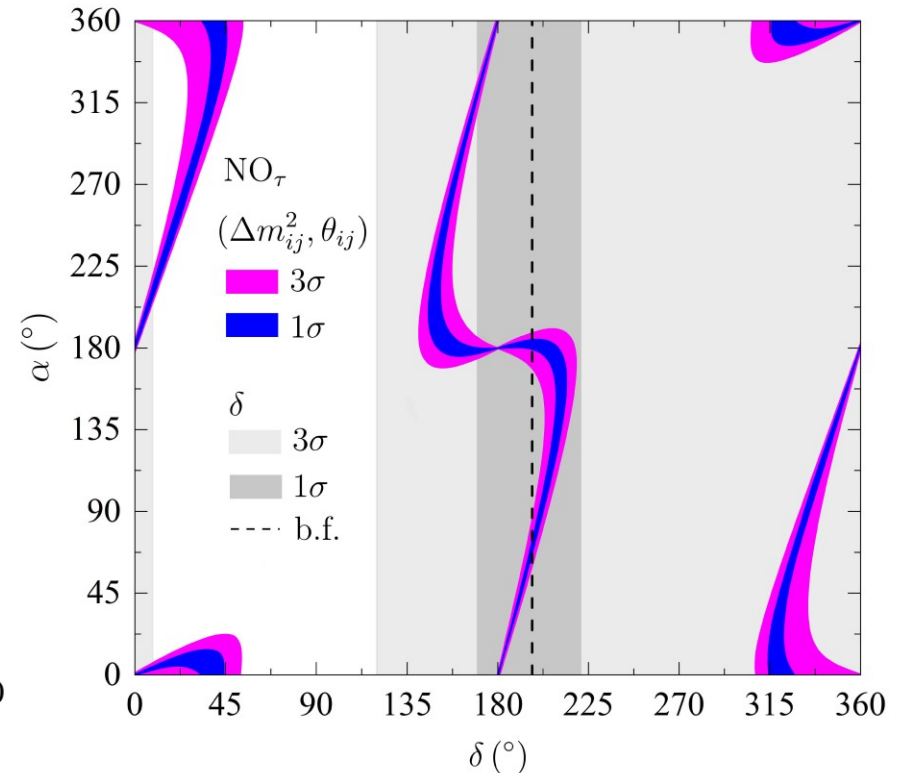
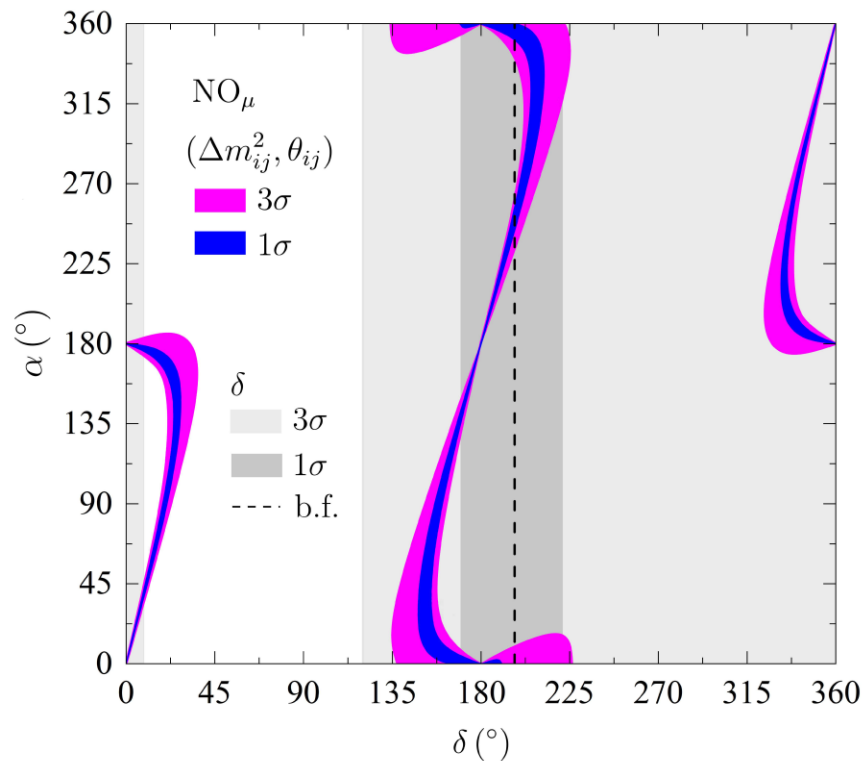
$$5_1^e : \arg \left[ M_{11}^{*2} M_{13}^2 \frac{D_{12}}{D_{23}} \right] = 0$$

$$5_1^\mu : \arg \left[ M_{12}^{*2} M_{23}^2 \frac{D_{12}}{D_{23}} \right] = 0$$

$$5_1^\tau : \arg \left[ M_{13}^{*2} M_{33}^2 \frac{D_{12}}{D_{23}} \right] = 0$$



# Leptonic CP violation



- Strong correlation between  $\alpha$  and  $\delta$
- Approximate symmetry  $\delta \rightarrow \delta + \pi$
- No Dirac CPV implies no Majorana CPV
- A measurement of  $\delta$  in the intervals  $[45^\circ, 135^\circ]$  and  $[225^\circ, 315^\circ]$  would exclude the NO<sub>μ</sub> and NO<sub>τ</sub> cases

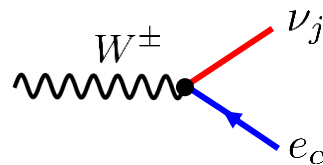
$$\langle S_1 \rangle = u_1 e^{i\xi}$$

$$\mathcal{J}_{\text{Dirac}}^{\text{CP}}, \mathcal{J}_{\text{Maj}}^{\text{CP}} \propto \sin(2\xi)$$

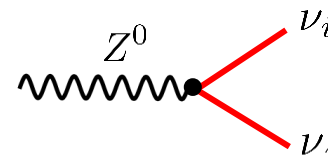
as in Branco, Felipe, FRJ, Serôdio (2012)

# Heavy-light mixing relations

$$\mathcal{L}_{W^\pm} = \frac{g}{\sqrt{2}} W_\mu^\pm \sum_{\alpha=1}^3 \sum_{j=1}^{n_f} \mathbf{B}_{\alpha j} \bar{e}_\alpha \gamma^\mu P_L \nu_j + \text{H.c.}$$



$$\mathcal{L}_Z = \frac{g}{4c_W} Z_\mu \sum_{i,j=1}^{n_f} \bar{\nu}_i \gamma^\mu (\mathbf{C}_{ij} P_L - \mathbf{C}_{ij}^* P_R) \nu_j, \quad \mathbf{C}_{ij} = \sum_{\alpha=1}^3 \mathbf{B}_{\alpha i}^* \mathbf{B}_{\alpha j}$$



$$\frac{\mathbf{B}_{e4}}{\mathbf{B}_{\mu4}} \simeq \frac{\mathbf{B}_{e5}}{\mathbf{B}_{\mu5}} \simeq \frac{x}{y c_L}, \quad \frac{\mathbf{B}_{\tau4}}{\mathbf{B}_{\mu4}} \simeq \frac{\mathbf{B}_{\tau5}}{\mathbf{B}_{\mu5}} \simeq \tan \theta_L, \quad \frac{\mathbf{B}_{\mu6}}{\mathbf{B}_{\tau6}} \simeq \frac{\mathbf{B}_{\mu7}}{\mathbf{B}_{\tau7}} \simeq \frac{z - w \tan \theta_L}{w + z \tan \theta_L}, \quad \mathbf{B}_{e6} \simeq \mathbf{B}_{e7} \simeq 0$$

## NUMERICAL ESTIMATES

	NO <sub>e</sub>	NO <sub>μ</sub>	NO <sub>τ</sub>	IO <sub>e</sub>	IO <sub>μ</sub>	IO <sub>τ</sub>
$\mathbf{B}_{e4}/\mathbf{B}_{\mu4} \simeq \mathbf{B}_{e5}/\mathbf{B}_{\mu5}$	0.21	0.17	0.17	2.73	0.21	0.41
$\mathbf{B}_{\tau4}/\mathbf{B}_{\mu4} \simeq \mathbf{B}_{\tau5}/\mathbf{B}_{\mu5}$	0.27	0.88	0.87	0.51	1.09	1.24
$\mathbf{B}_{\tau4}/\mathbf{B}_{e4} \simeq \mathbf{B}_{\tau5}/\mathbf{B}_{e5}$	1.27	5.07	5.24	0.19	5.33	5.02
$\mathbf{B}_{e6}/\mathbf{B}_{\mu6} \simeq \mathbf{B}_{e7}/\mathbf{B}_{\mu7}$	0	–	0.36	0	–	4.96
$\mathbf{B}_{\tau6}/\mathbf{B}_{\mu6} \simeq \mathbf{B}_{\tau7}/\mathbf{B}_{\mu7}$	0.61	–	0	1.14	–	0
$\mathbf{B}_{\tau6}/\mathbf{B}_{e6} \simeq \mathbf{B}_{\tau7}/\mathbf{B}_{e7}$	–	1.64	0	–	0.23	0

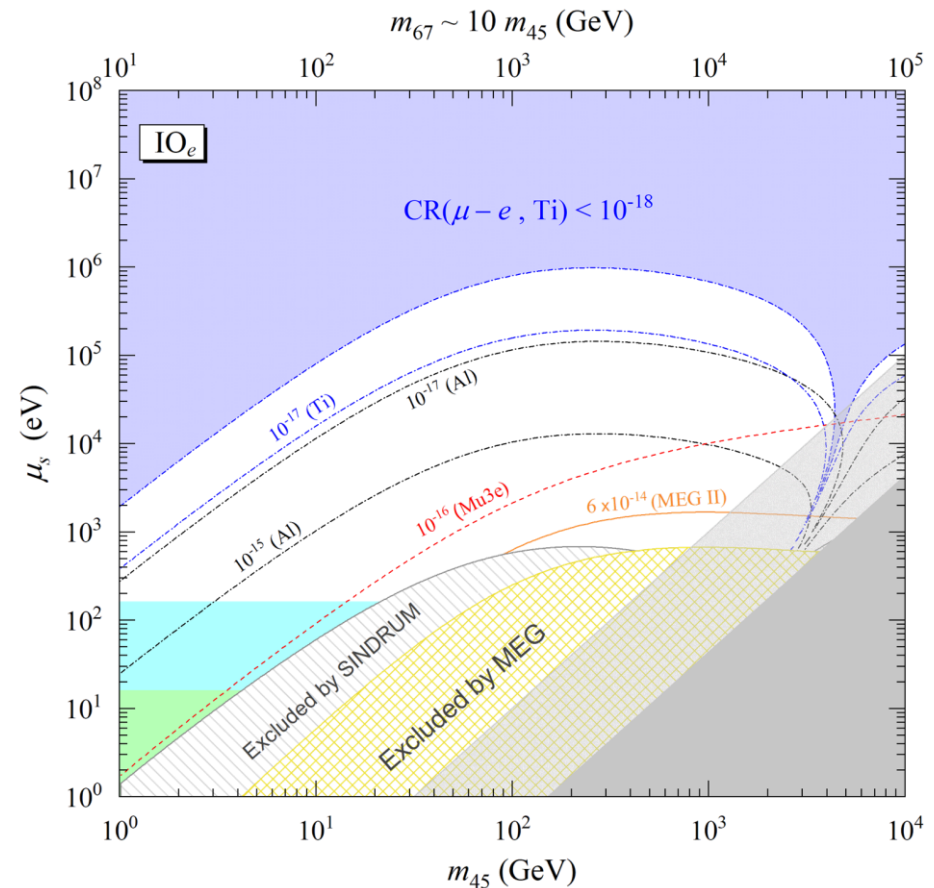
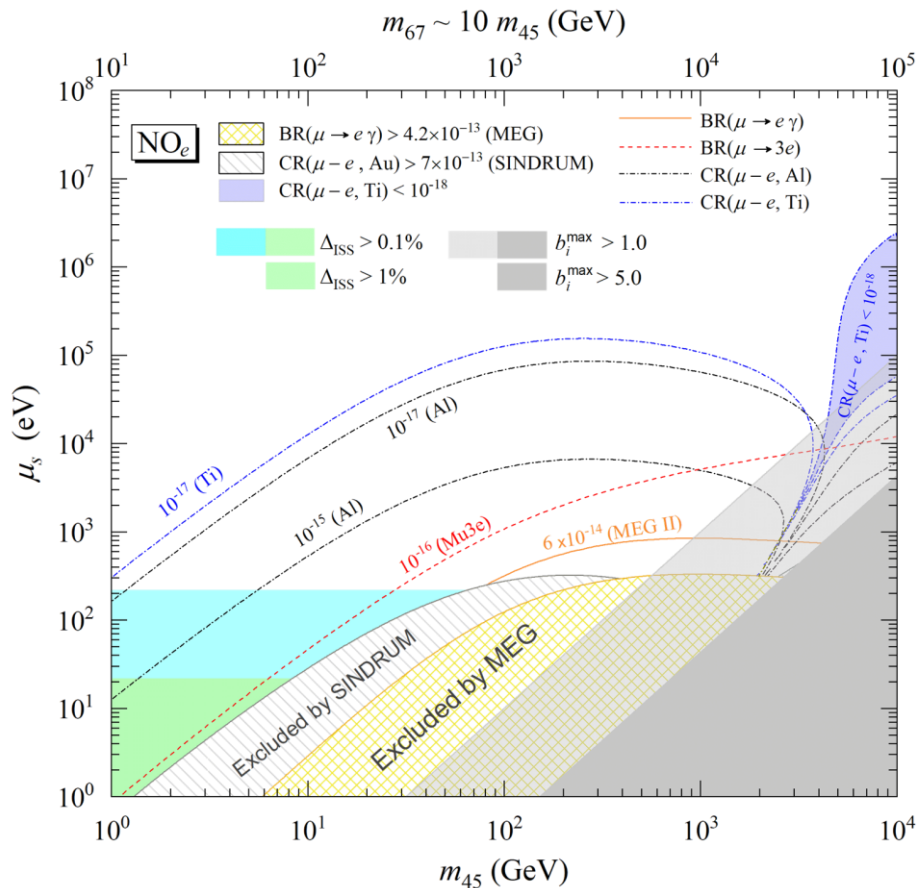
- The  $\mathbf{B}_{\alpha i}$  ( $\alpha = e, \mu, \tau$ ) ( $i = 4, \dots, 7$ ) are related to each other,
- The relations are expressed solely in terms of the low-energy neutrino observables,
- Due to the flavour symmetries the heavy-light mixing parameters are not independent,

This establishes relations among cLFV processes (no time to discuss here)

# Charged lepton flavour violation (cLFV)

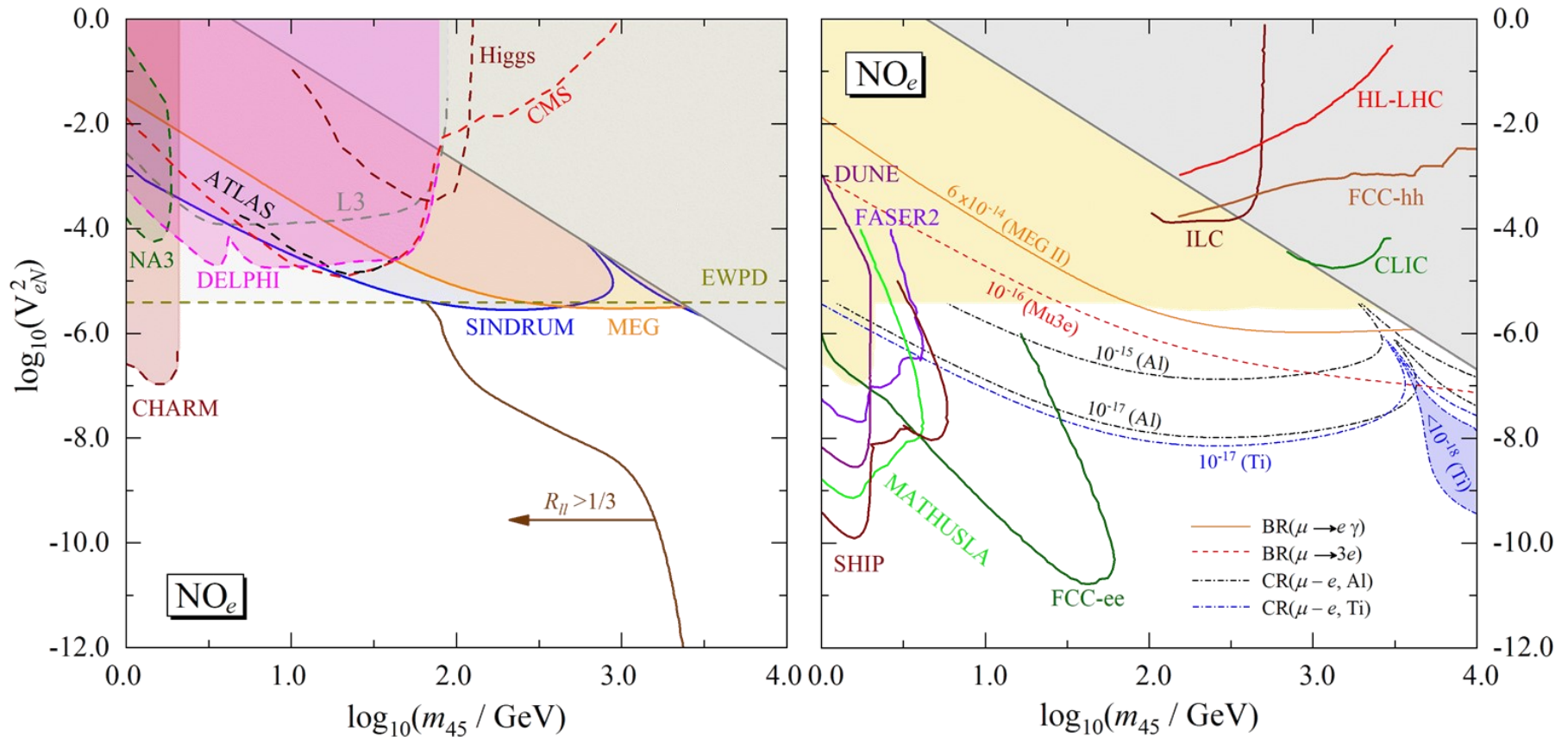
cLFV process	Present limit (90% CL)	Future sensitivity
$\text{BR}(\mu \rightarrow e\gamma)$	$4.2 \times 10^{-13}$ (MEG)	$6 \times 10^{-14}$ (MEG II)
$\text{BR}(\tau \rightarrow e\gamma)$	$3.3 \times 10^{-8}$ (BaBar)	$3 \times 10^{-9}$ (Belle II)
$\text{BR}(\tau \rightarrow \mu\gamma)$	$4.4 \times 10^{-8}$ (BaBar)	$10^{-9}$ (Belle II)
$\text{BR}(\mu^- \rightarrow e^- e^+ e^-)$	$1.0 \times 10^{-12}$ (SINDRUM)	$10^{-16}$ (Mu3e)
$\text{BR}(\tau^- \rightarrow e^- e^+ e^-)$	$2.7 \times 10^{-8}$ (Belle)	$5 \times 10^{-10}$ (Belle II)
$\text{BR}(\tau^- \rightarrow e^- \mu^+ \mu^-)$	$2.7 \times 10^{-8}$ (Belle)	$5 \times 10^{-10}$ (Belle II)
$\text{BR}(\tau^- \rightarrow e^+ \mu^- \mu^-)$	$1.7 \times 10^{-8}$ (Belle)	$3 \times 10^{-10}$ (Belle II)
$\text{BR}(\tau^- \rightarrow \mu^- e^+ e^-)$	$1.8 \times 10^{-8}$ (Belle)	$3 \times 10^{-10}$ (Belle II)
$\text{BR}(\tau^- \rightarrow \mu^+ e^- e^-)$	$1.5 \times 10^{-8}$ (Belle)	$3 \times 10^{-10}$ (Belle II)
$\text{BR}(\tau^- \rightarrow \mu^- \mu^+ \mu^-)$	$2.1 \times 10^{-8}$ (Belle)	$4 \times 10^{-10}$ (Belle II)
$\text{CR}(\mu - e, \text{Al})$	–	$3 \times 10^{-17}$ (Mu2e) $10^{-15} - 10^{-17}$ (COMET I-II)
$\text{CR}(\mu - e, \text{Ti})$	$4.3 \times 10^{-12}$ (SINDRUM II)	$10^{-18}$ (PRISM/PRIME)
$\text{CR}(\mu - e, \text{Au})$	$7 \times 10^{-13}$ (SINDRUM II)	–
$\text{CR}(\mu - e, \text{Pb})$	$4.6 \times 10^{-11}$ (SINDRUM II)	–

# cLFV in the ISS(2,2) with Abelian symmetries



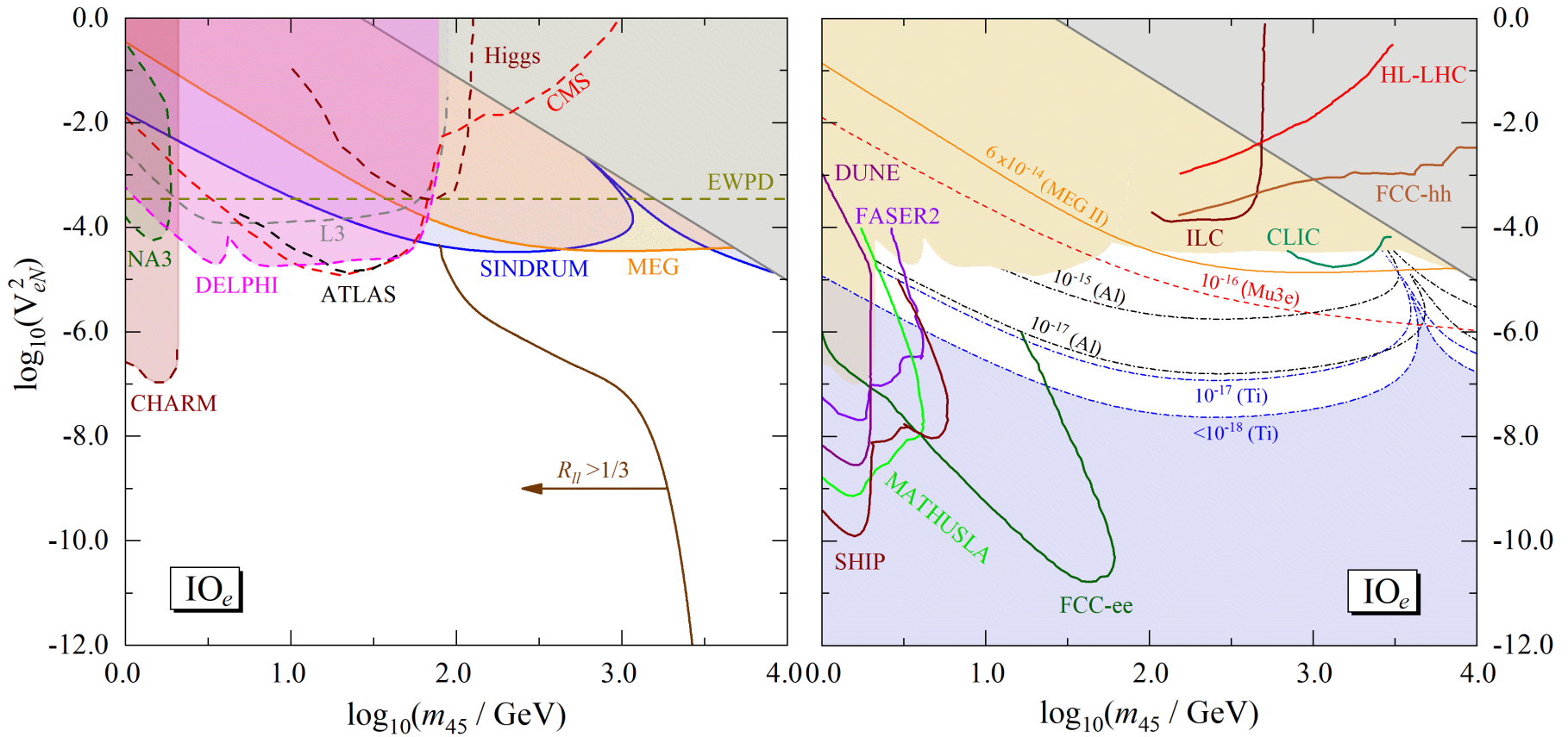
- (Almost) the whole parameter space will be scrutinized by future  $\mu$ - $e$  conversion experiments (Mu2e, COMET, PRISM/PRIME) for normal neutrino mass ordering;
- For inverted ordering the prospects are less optimistic.

# Constraints on heavy sterile neutrinos



- Current data implies an upper bound  $V_{eN}^2 \sim 10^{-6} - 10^{-5}$ ;
- Future probes will be sensitive to much smaller mixings. LFV complementary to other searches.

# Constraints on heavy sterile neutrinos



- EWPD is less constraining in the IO case;
- Future CLV probes will be sensitive to  $V_{eN}^2 \sim 10^{-7}$



# Concluding Remarks

- Minimal inverse seesaw mechanism constrained by Abelian flavour symmetries with all mass terms generated via SSB;
- Majorana and Dirac-type CP violation are related;
- Relations among LFV parameters in our framework provide a very constrained setup for phenomenological studies;
- Constraining power of cLFV processes in the model's parameter space;
- Alternative probes such as beam-dump, hadron-collider, linear-collider, displaced-vertex experiments as well as EWPD.

Impact of radiative correction on neutrino masses, neutrinoless double beta decay, relations among tau and mu decays,...

Thanks!