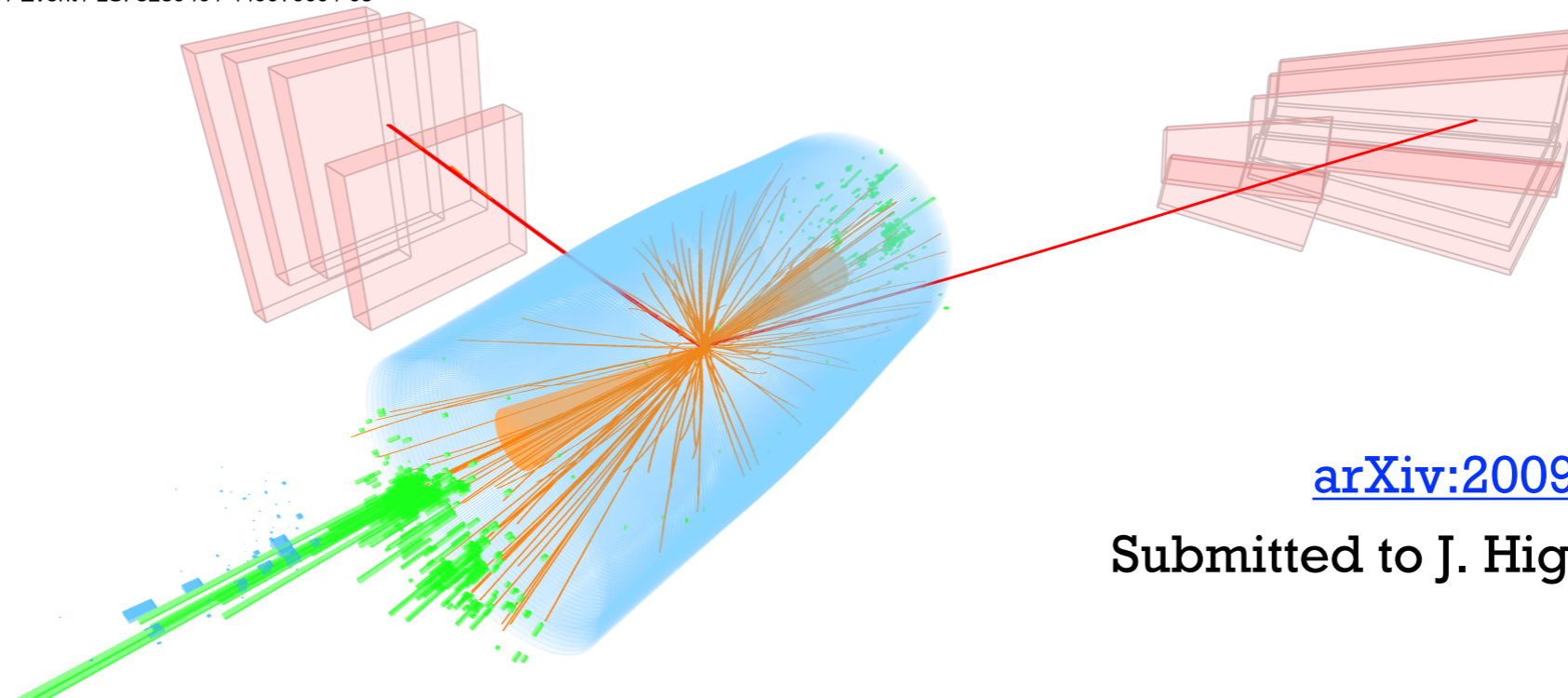


# First evidence for Higgs boson decay to muons



CMS Experiment at the LHC, CERN  
Data recorded: 2018-Oct-03 01:19:17.320393 GMT  
Run / Event / LS: 323940 / 44997009 / 65



[arXiv:2009.04363](https://arxiv.org/abs/2009.04363)

Submitted to J. High Energy Phys.



Stephane Cooperstein (UC San Diego)

*LPHE Seminar, EPFL*

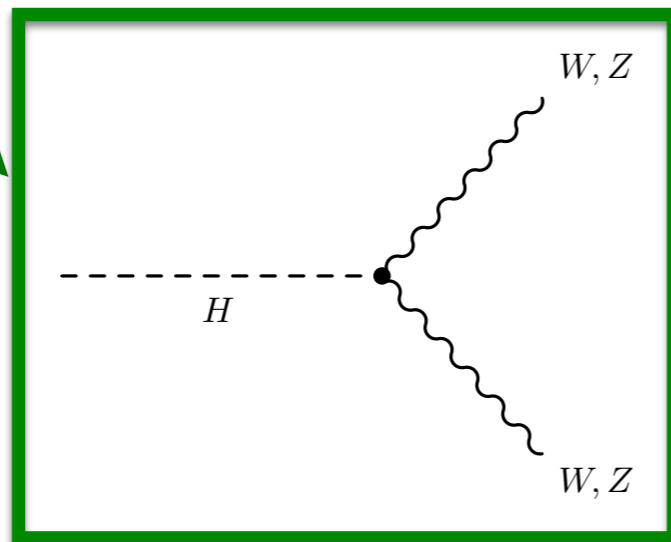
*October 12, 2020*



$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i \bar{\Psi} \not{D} \Psi + h.c. + \bar{\Psi}_i y_{ij} \Psi_j \phi + h.c. + \underbrace{|\mathcal{D}_\mu \phi|^2}_{\text{Bosonic Couplings}} - V(\phi)$$

- Mass generation for and Higgs interactions with gauge bosons is a direct consequence of electroweak symmetry breaking.

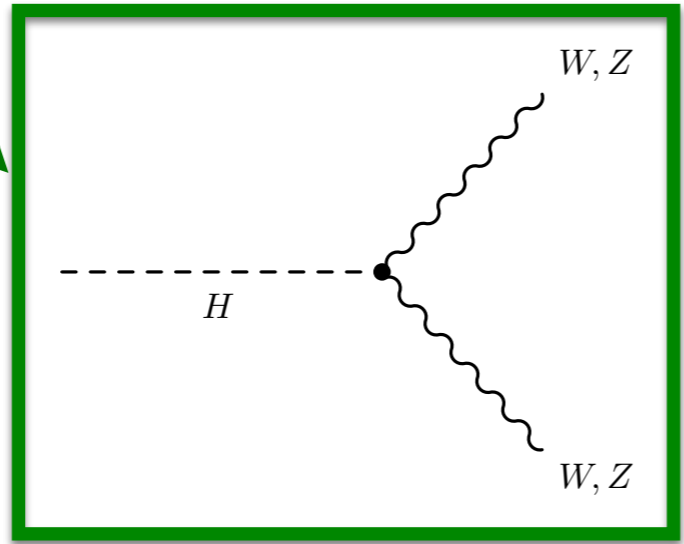
**Bosonic Couplings**



$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} + i \bar{\Psi} \not{D} \Psi + h.c. + \bar{\Psi}_i y_{ij} \Psi_j \phi + h.c. + |D_\mu \phi|^2 - V(\phi)$$

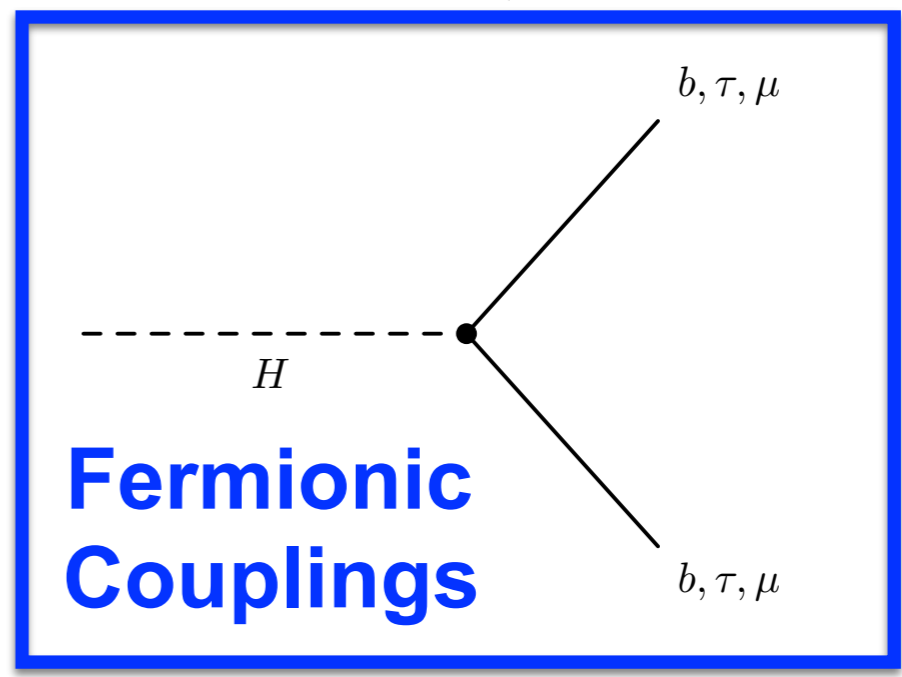
- Mass generation for and Higgs interactions with gauge bosons is a direct consequence of electroweak symmetry breaking.
- Yukawa interactions: fermion masses proportional to Higgs-fermion interaction strength.
- Each Yukawa coupling  $Y_f$  is a free parameter of the SM.

**Bosonic Couplings**

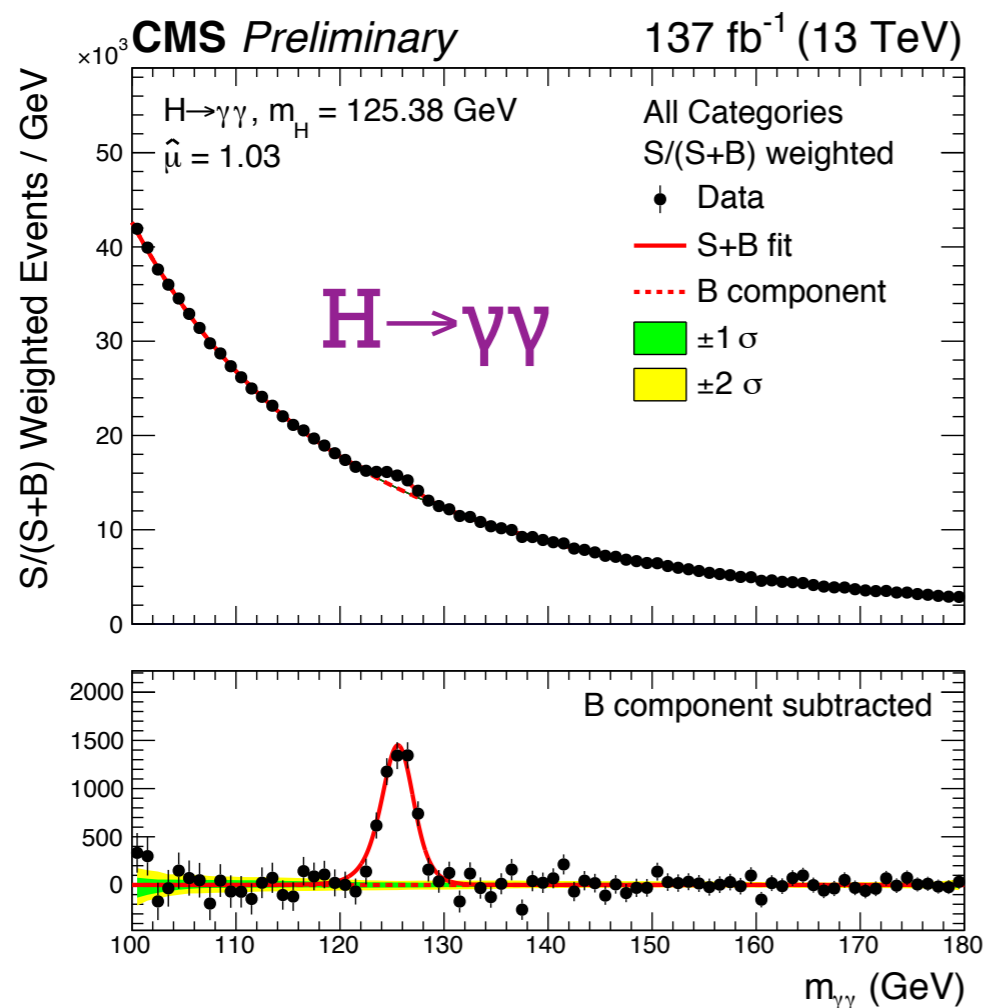


$$L_{\text{Yuk}} = (1 + \frac{H}{v}) m_f \bar{f}_L f_R$$

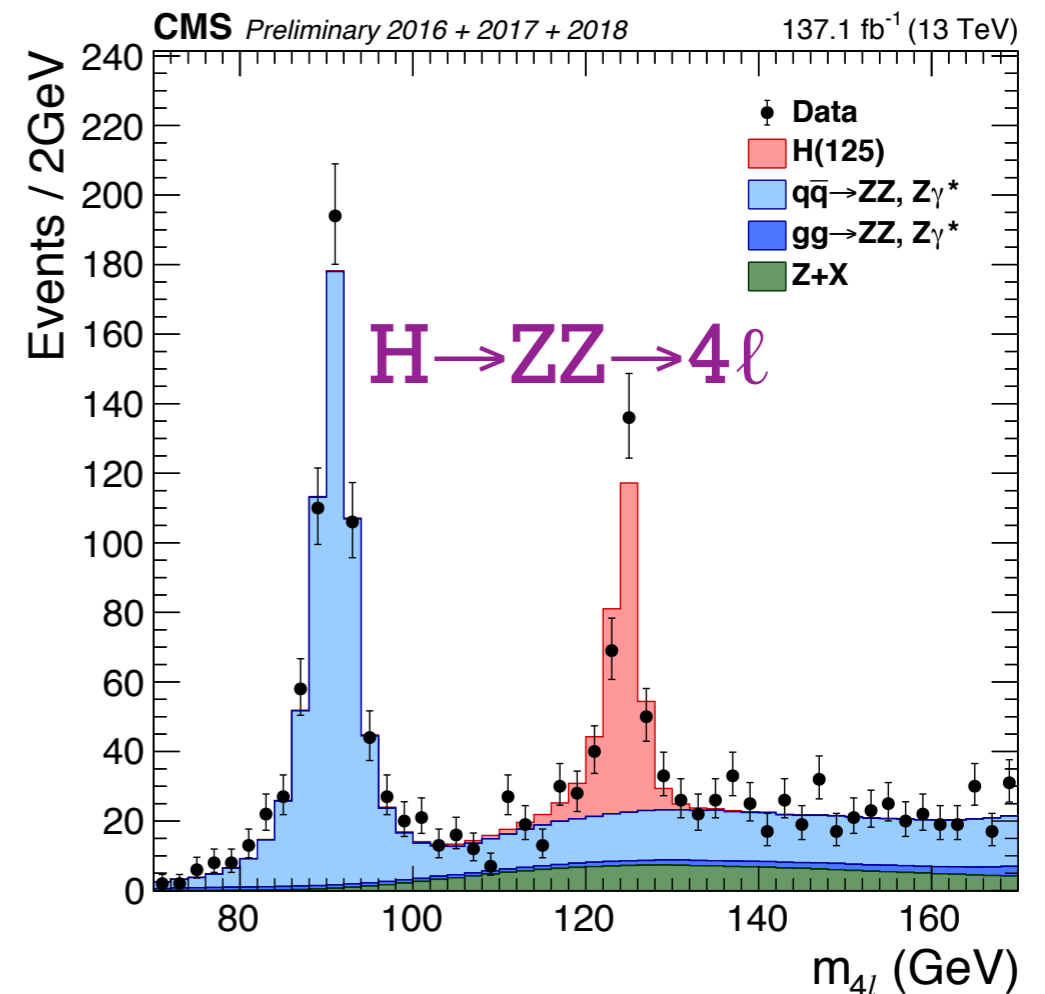
**Fermionic Couplings**



- *We have come a long way in studying the properties of the Higgs boson in the eight years since its discovery.*
- All measured properties (production rate, spin, CP, ...) consistent with SM.
- Mass measured at nearly per-mille level:  $m_H = 125.38 \pm 0.14$  GeV ([Phys. Lett. B 805 \(2020\) 135425](#)).



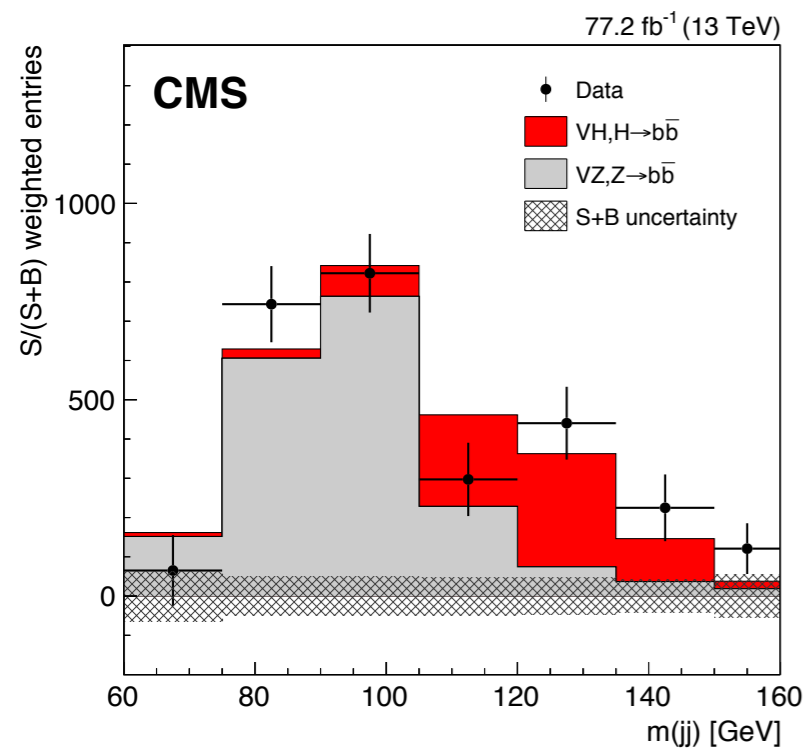
[CMS-PAS-HIG-19-015](#)



[CMS-PAS-HIG-19-001](#)

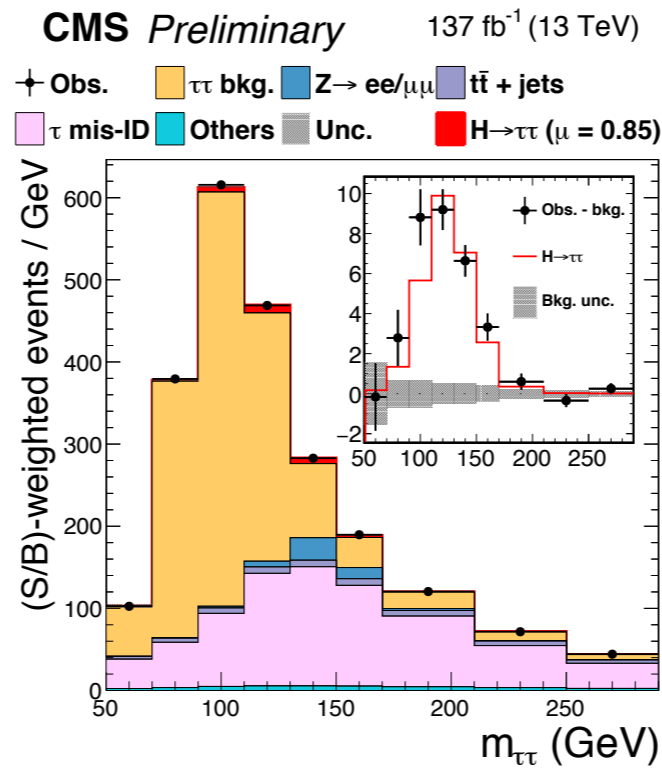
- In addition to gauge boson couplings, Higgs boson couplings to third generation fermions (t,  $\tau$ , b) firmly established and consistent with SM.
- Yukawa interactions for third generation are clearly SM-like within the current experimental 10-20% precision.

## $H \rightarrow b\bar{b}$



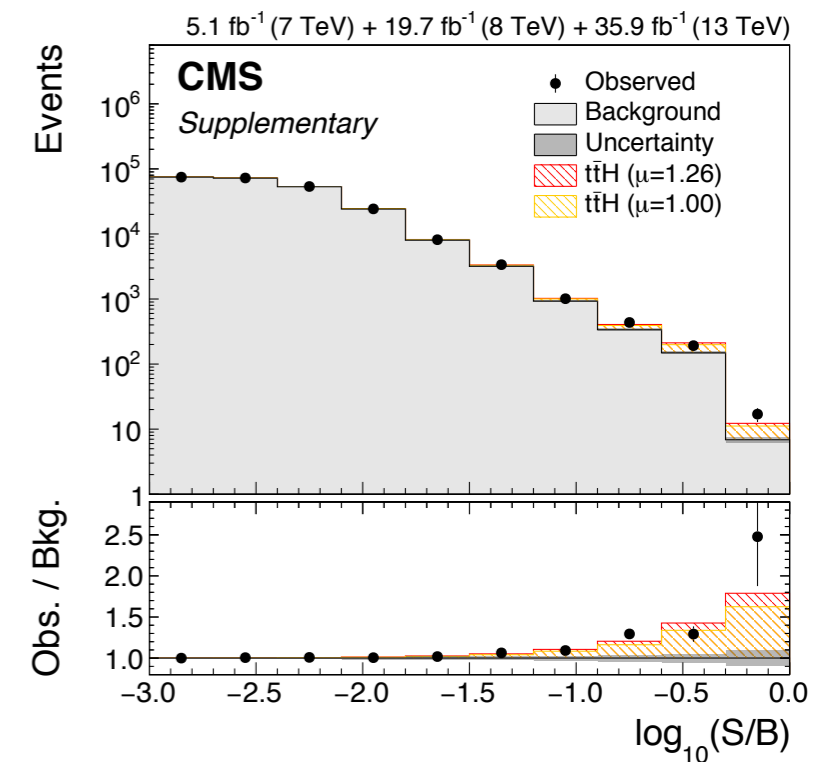
[Phys. Rev. Lett. 121 \(2018\) 121801](#)

## $H \rightarrow \tau\tau$



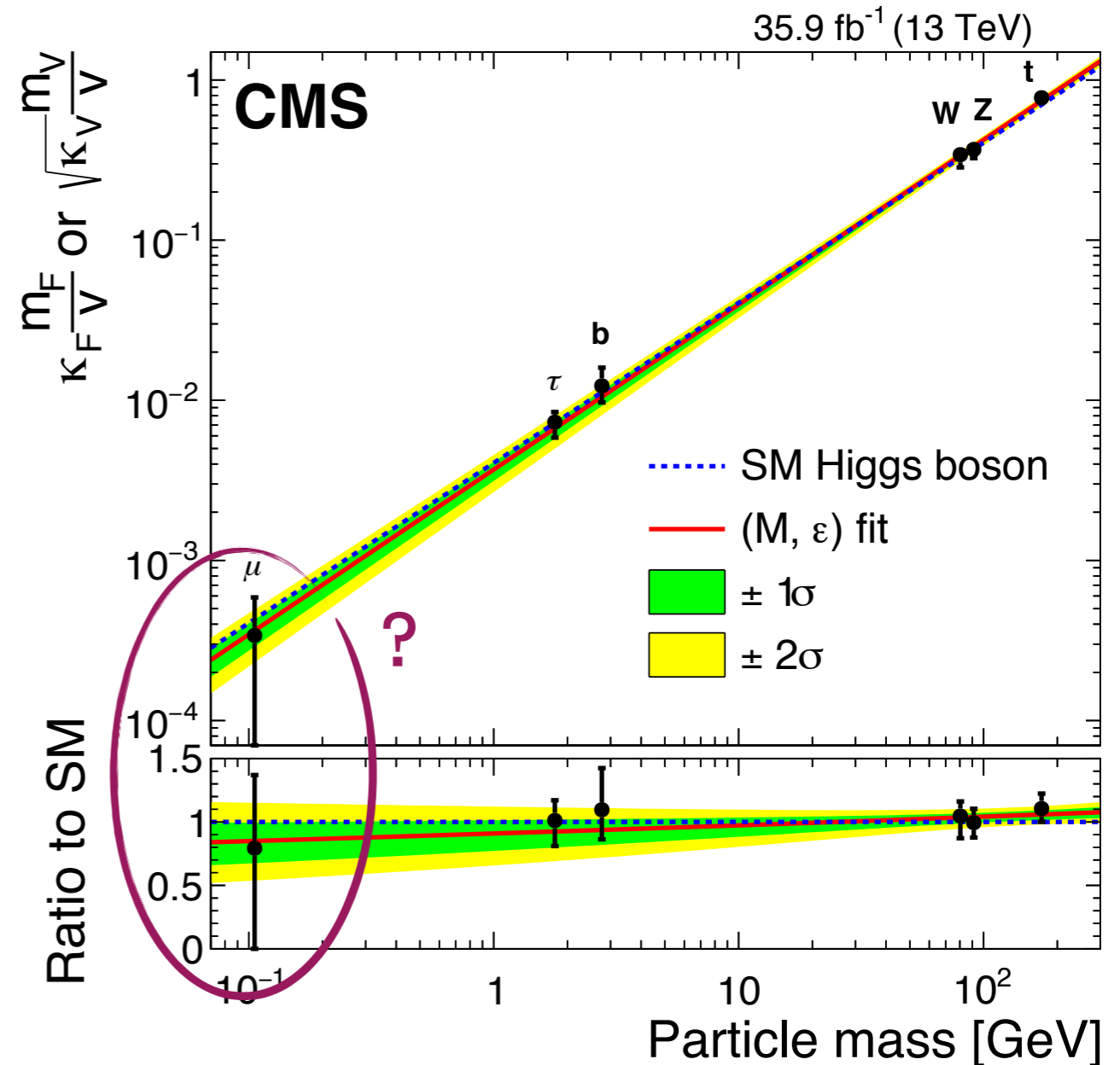
[CMS-PAS-HIG-19-010](#)

## ttH



[Phys. Rev. Lett. 120 \(2018\) 231801](#)

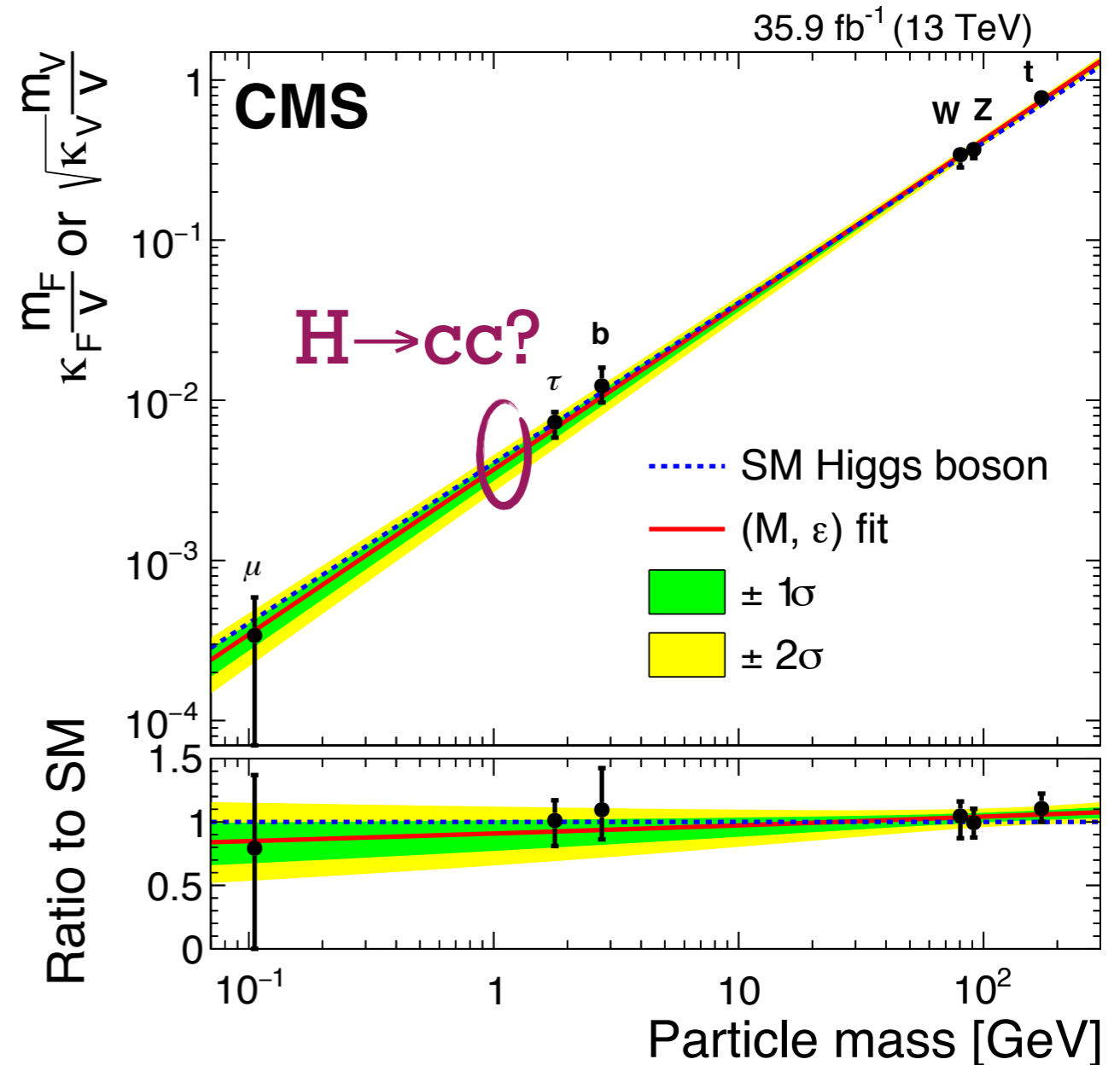
- *Next frontier: Higgs boson couplings to second generation fermions*
- **$H \rightarrow \mu\mu$  is likely the only accessible probe of first or second generation couplings at the LHC.**
- Extend probe of Higgs interactions by more than an order of magnitude in mass scale.



(from latest CMS Higgs couplings combination)

[Eur. Phys. J. C 79 \(2019\) 421](#)

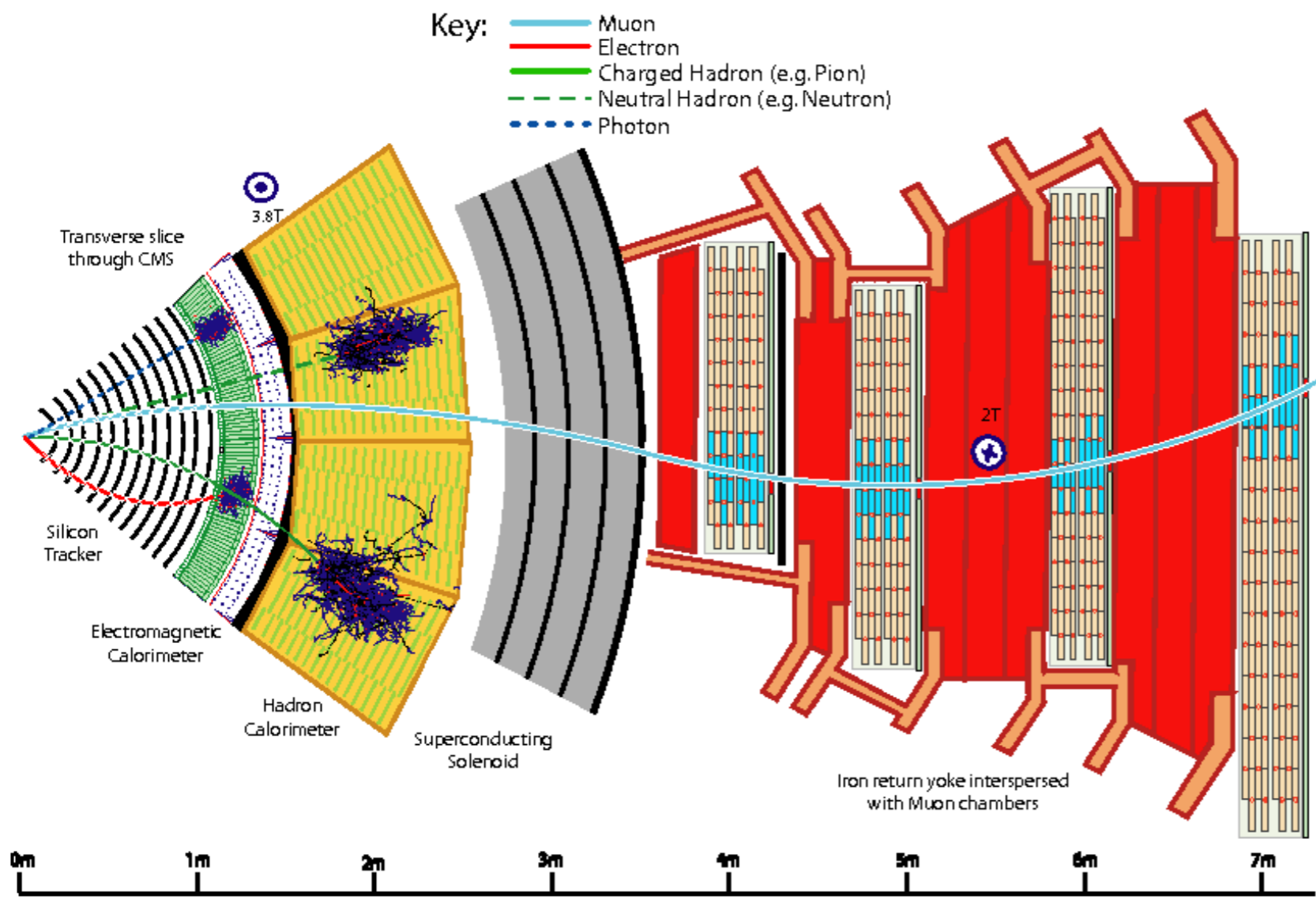
- *What about  $H \rightarrow cc$ ?*
- $\text{BR}(H \rightarrow cc) = 2.9\%$ !
- Significant branching fraction, but very large backgrounds and difficult to isolate jets originating from charm quarks.
- Current limits are factor  $\sim 40$  higher than SM with partial Run-2 data set [1].
- ***Measuring  $H \rightarrow cc$  will be very difficult, even with  $3\text{-}4 \text{ ab}^{-1}$  from HL-LHC.***



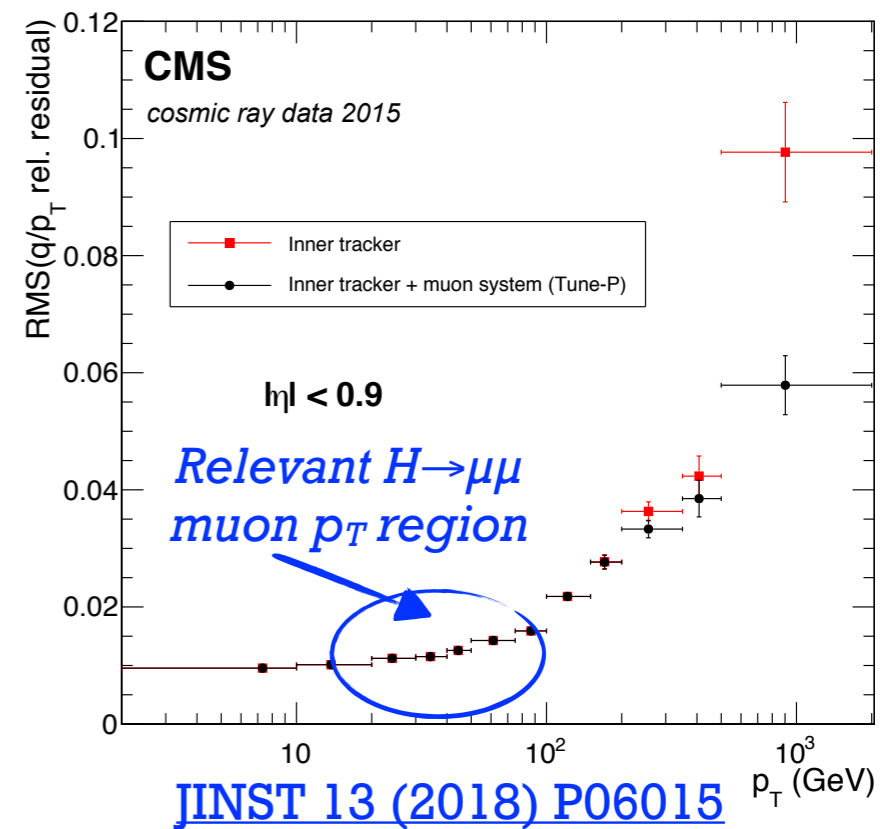
(from latest CMS Higgs couplings combination)

[Eur. Phys. J. C 79 \(2019\) 421](#)

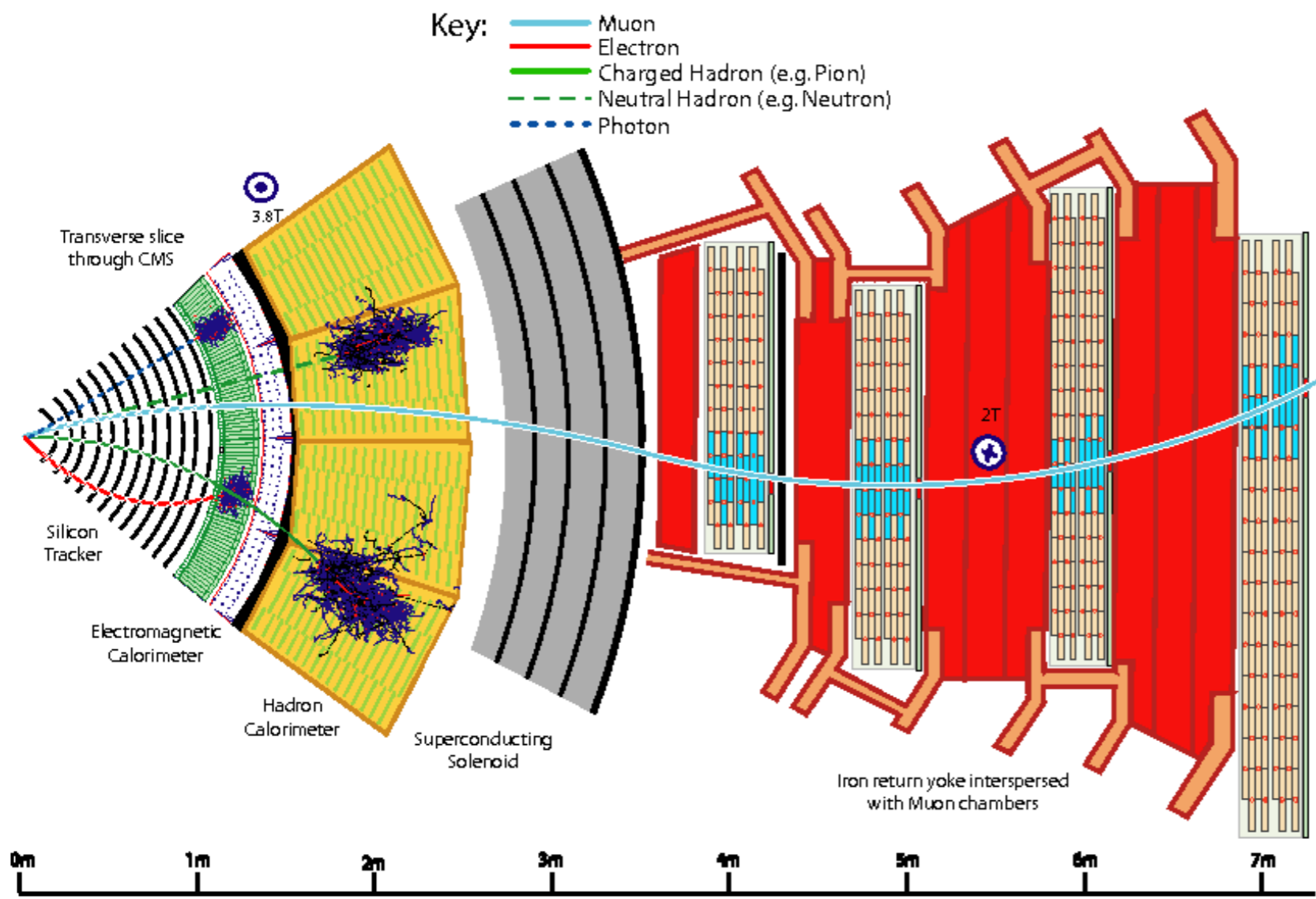
[1] [JHEP 03 \(2020\) 131](#)



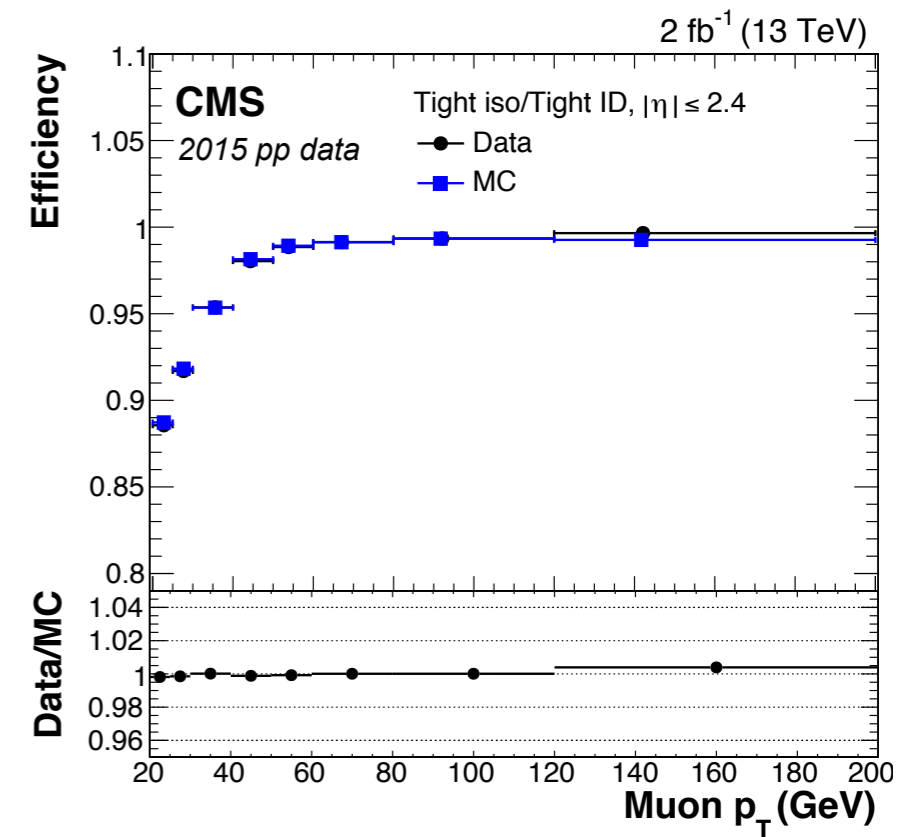
## Muon momentum resolution vs $p_T(\mu)$





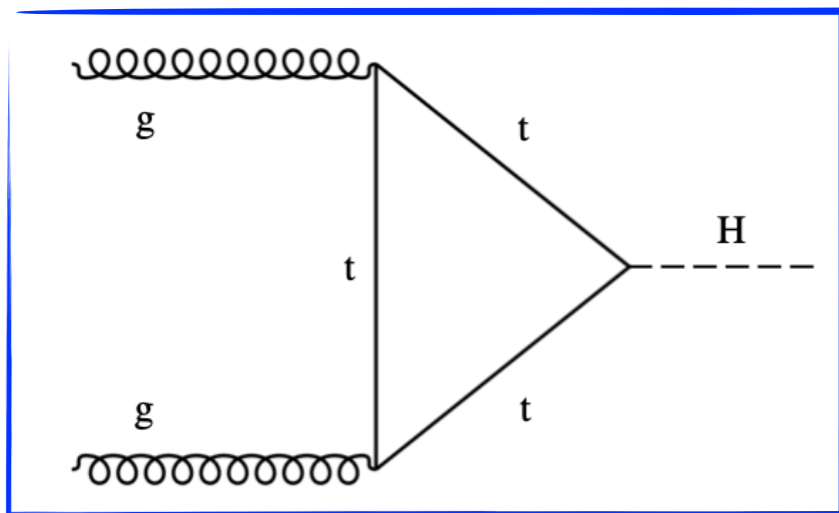


## Muon reconstruction efficiency vs $p_T(\mu)$



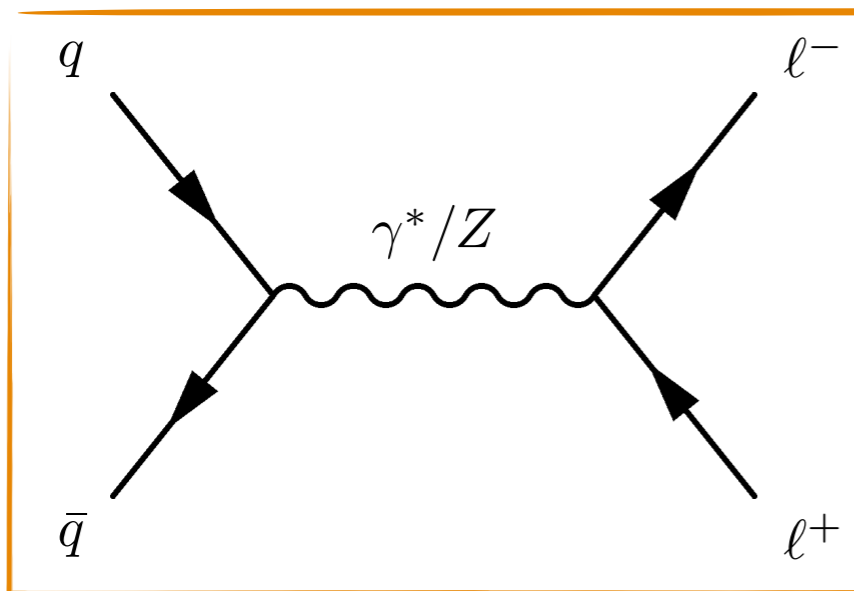
*~95% selection efficiency for muons from  $H \rightarrow \mu\mu$  decays.*

**Gluon-gluon fusion production (ggH)**  
dominant Higgs boson production  
mode at the LHC



- Inclusive Higgs boson production cross section at 13 TeV:  $\sigma_H \sim 50$  pb.
- Expected  $H \rightarrow \mu\mu$  branching fraction for  $m_H$  near 125 GeV:  **$\text{BR}(H \rightarrow \mu\mu) \sim 2.2 \cdot 10^{-4}$** .
- $\Rightarrow \sigma_{\text{eff}}(H \rightarrow \mu\mu) \sim 0.01$  pb
- **Roughly 1k total signal events in Run-2 ( $137 \text{ fb}^{-1}$ ) dataset.**

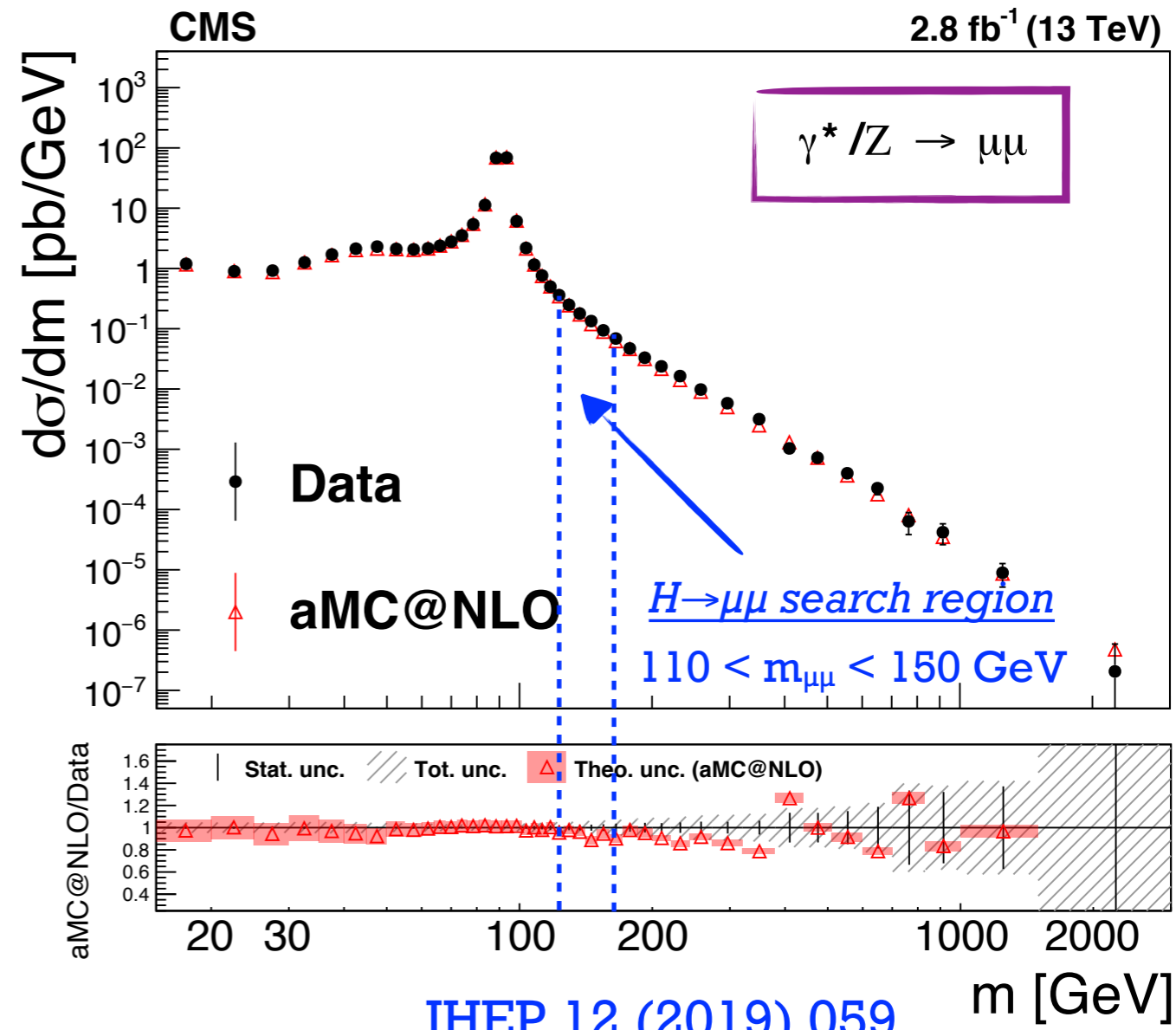
## Drell-Yan (DY) production



Total effective cross section in  $H \rightarrow \mu\mu$  search region with  $110 < m_{\mu\mu} < 150$  GeV:

$$\sigma_{\text{eff}}(\text{DY}) \sim 15 \text{ pb}$$

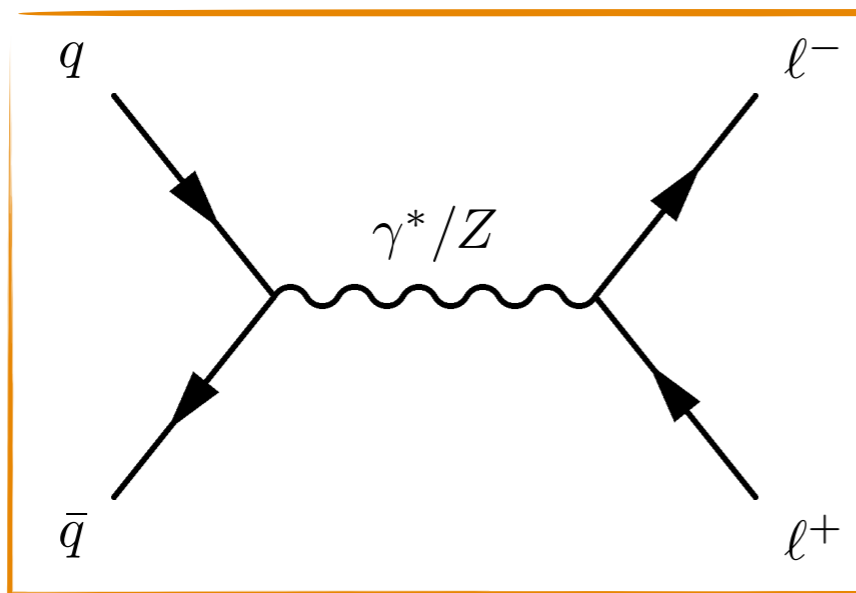
*i.e. ~two million DY background events in  $H \rightarrow \mu\mu$  preselected 13 TeV data sample with  $m_{\mu\mu}$  near 125 GeV.*



[JHEP 12 \(2019\) 059](#)

## Drell-Yan (DY) production

$$\sigma_{\text{eff}}(\text{DY}) \sim 15 \text{ pb}$$

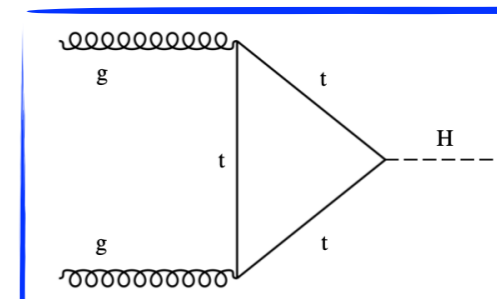


- S/B ~ one per mille with  $m_{\mu\mu}$  near 125 GeV
- Large additional background rejection necessary to measure  $H \rightarrow \mu\mu$  signal.

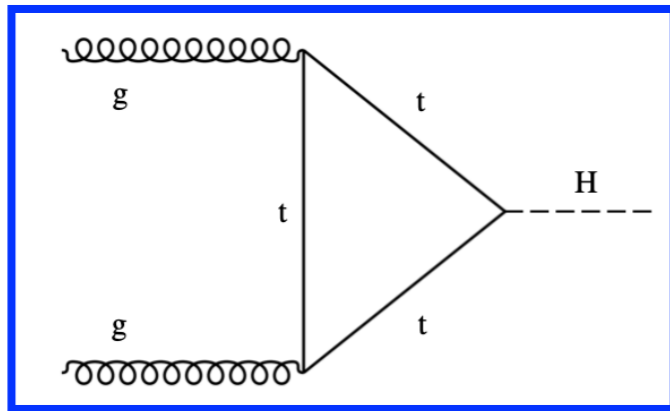
Effective cross section

*Three orders of magnitude more DY background than  $H \rightarrow \mu\mu$  signal in preselected search region.*

**$H \rightarrow \mu\mu$  signal**  
 $\sigma_{\text{eff}}(H \rightarrow \mu\mu) \sim 0.01 \text{ pb}$

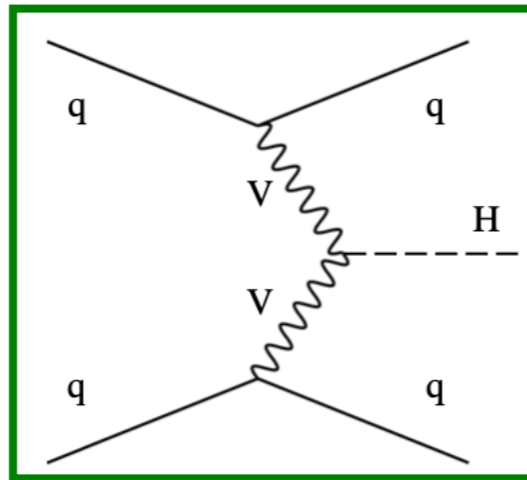


## Gluon-gluon fusion ( $ggH$ )

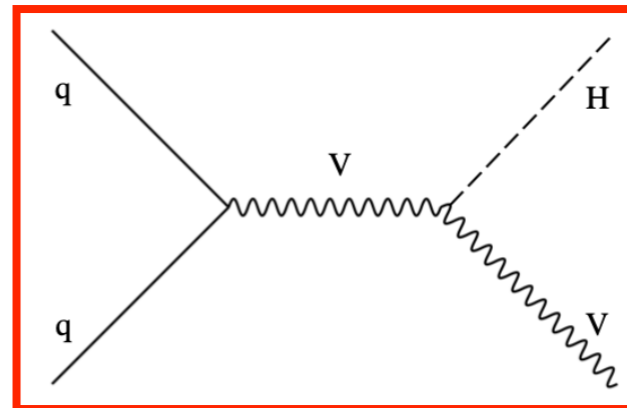


Improve signal-to-background separation by *splitting events into exclusive categories, each targeting a particular Higgs boson production mode.*

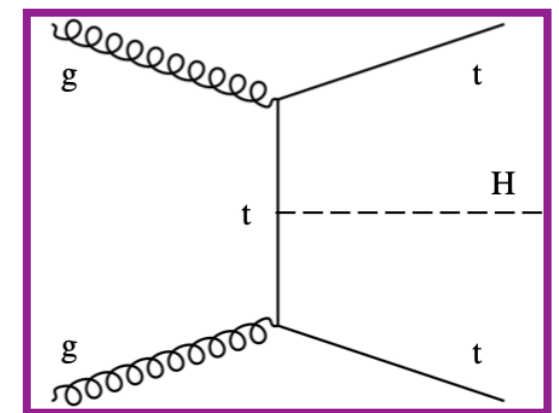
## Vector boson fusion (VBF)



*Associated production with W or Z (VH)*



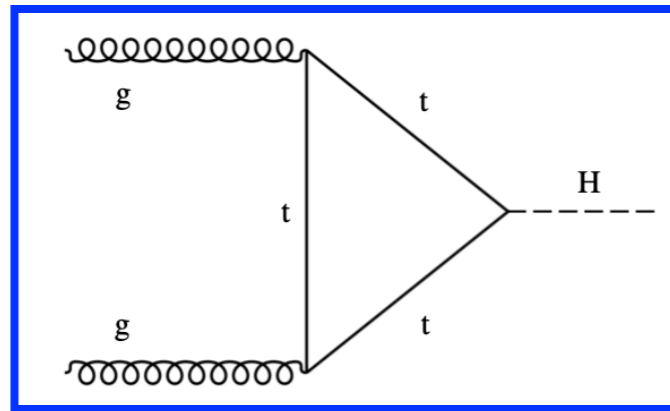
*Associated production with top quarks ( $ttH$ )*



**Effective cross section (rate)**

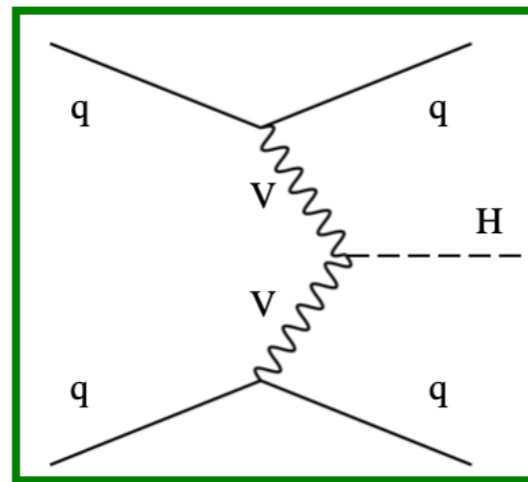
**Level of achievable signal purity**

## Gluon-gluon fusion (ggH)



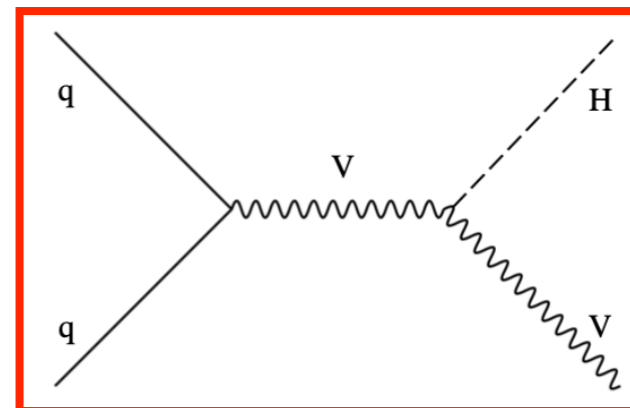
Significant improvements of existing strategy

## Vector boson fusion (VBF)



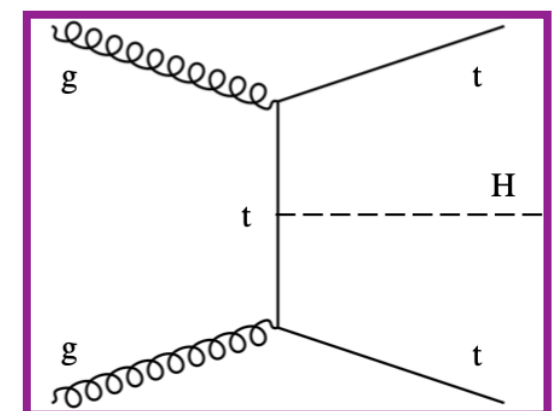
Completely redesigned strategy

## Associated production with W or Z (VH)



New categories

## Associated production with top quarks (ttH)



Effective cross section (rate)

Level of achievable signal purity

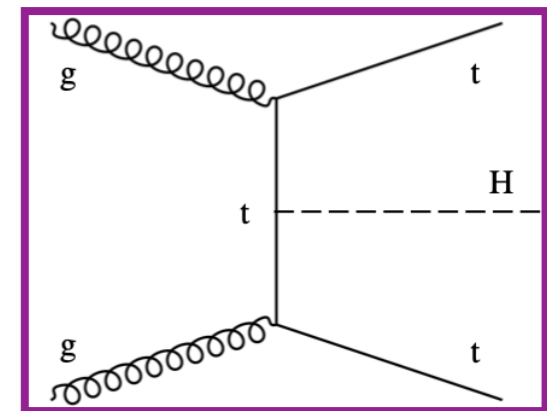
$\mu^+\mu^-$  pair with mass near 125 GeV

Presence of b-tagged jets?

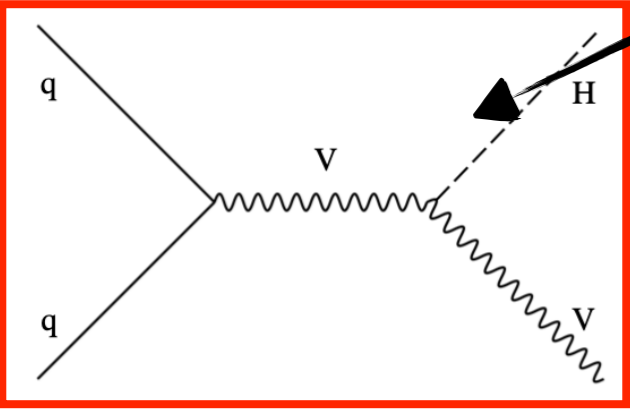
Additional electron(s) or muon(s)?

Two jets with large  $m_{jj}$ ,  $\Delta\eta(jj)$ ?

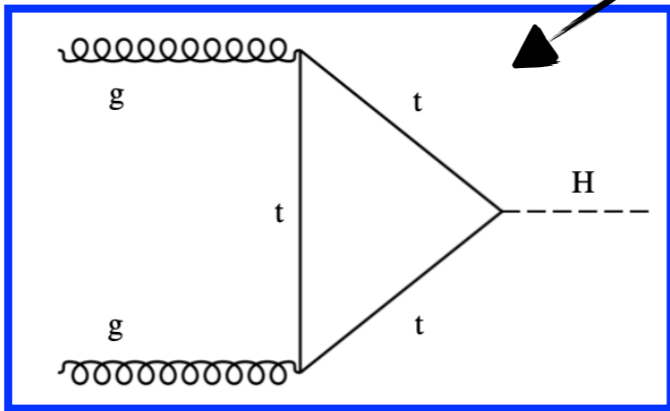
*ttH category*



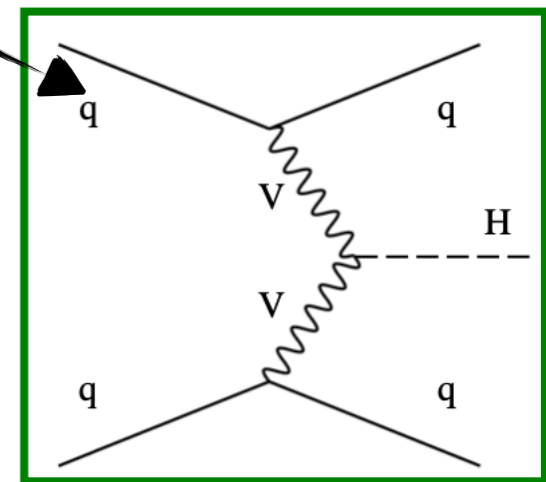
*VH category*



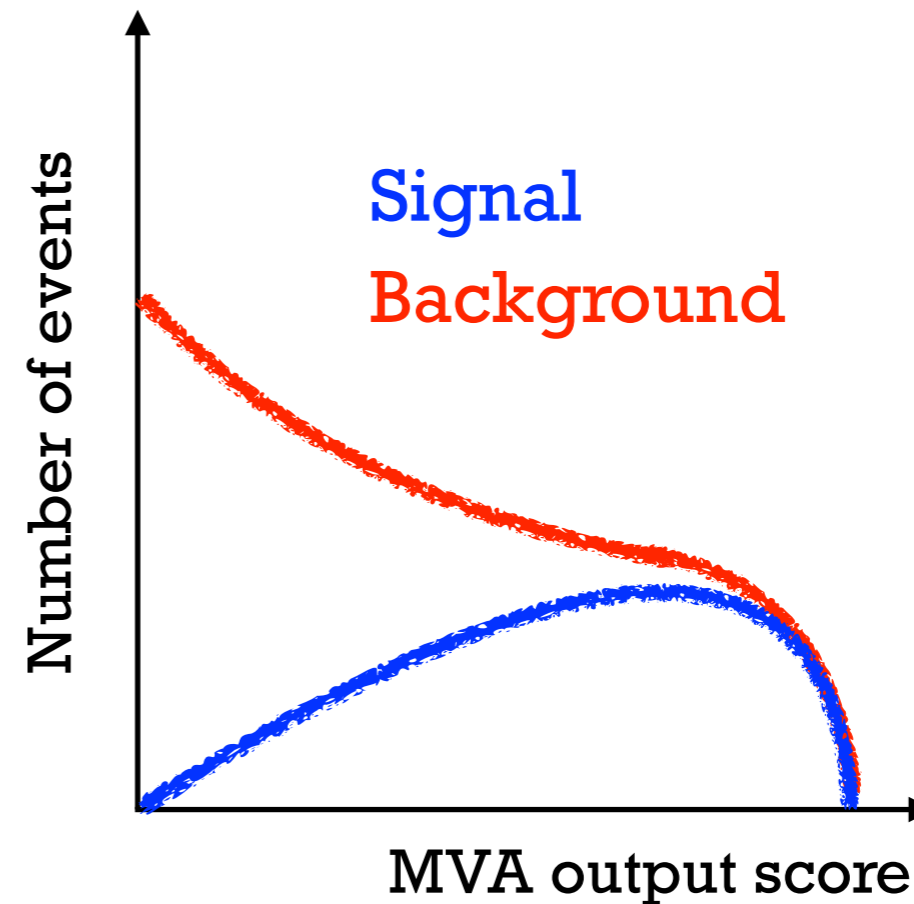
*ggH category*



*VBF category*

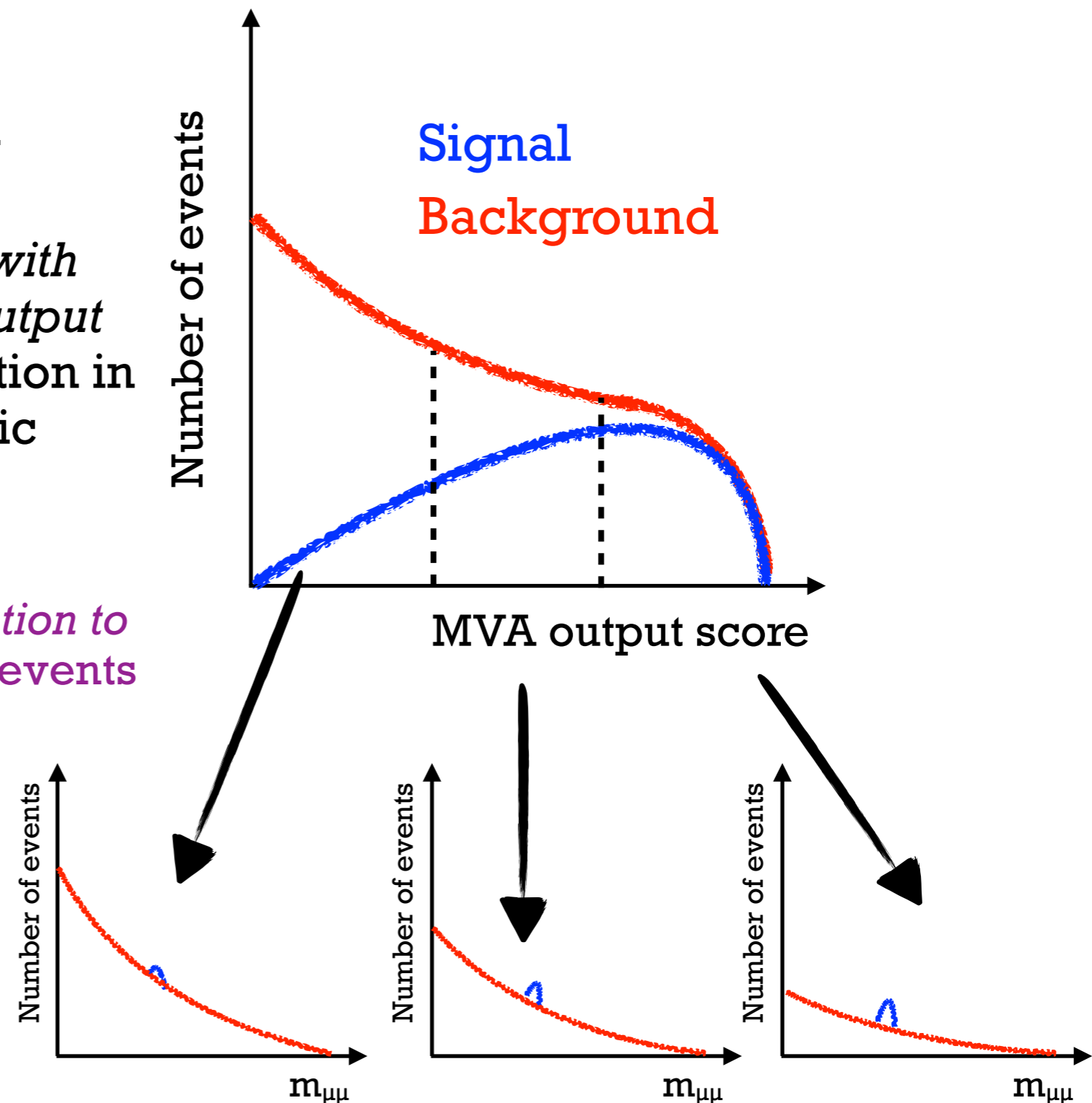


- *Train a multivariate (MVA) classifier to separate signal from background*
- Using kinematic input variables uncorrelated with H candidate mass.

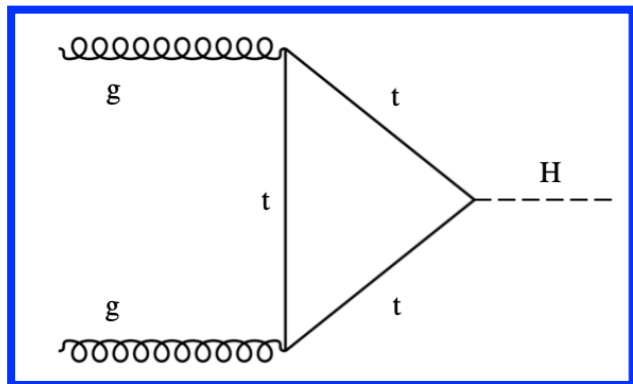




- Train a multivariate (MVA) classifier to separate signal from background
- Using kinematic input variables uncorrelated with H candidate mass.
- **Divide** events into subcategories with varying signal purity using MVA output **and fit** the dimuon mass distribution in each subcategory with parametric functions.
- Promote events with best mass resolution to high BDT score by weighting signal events by  $1/\sigma_m$  in BDT training.

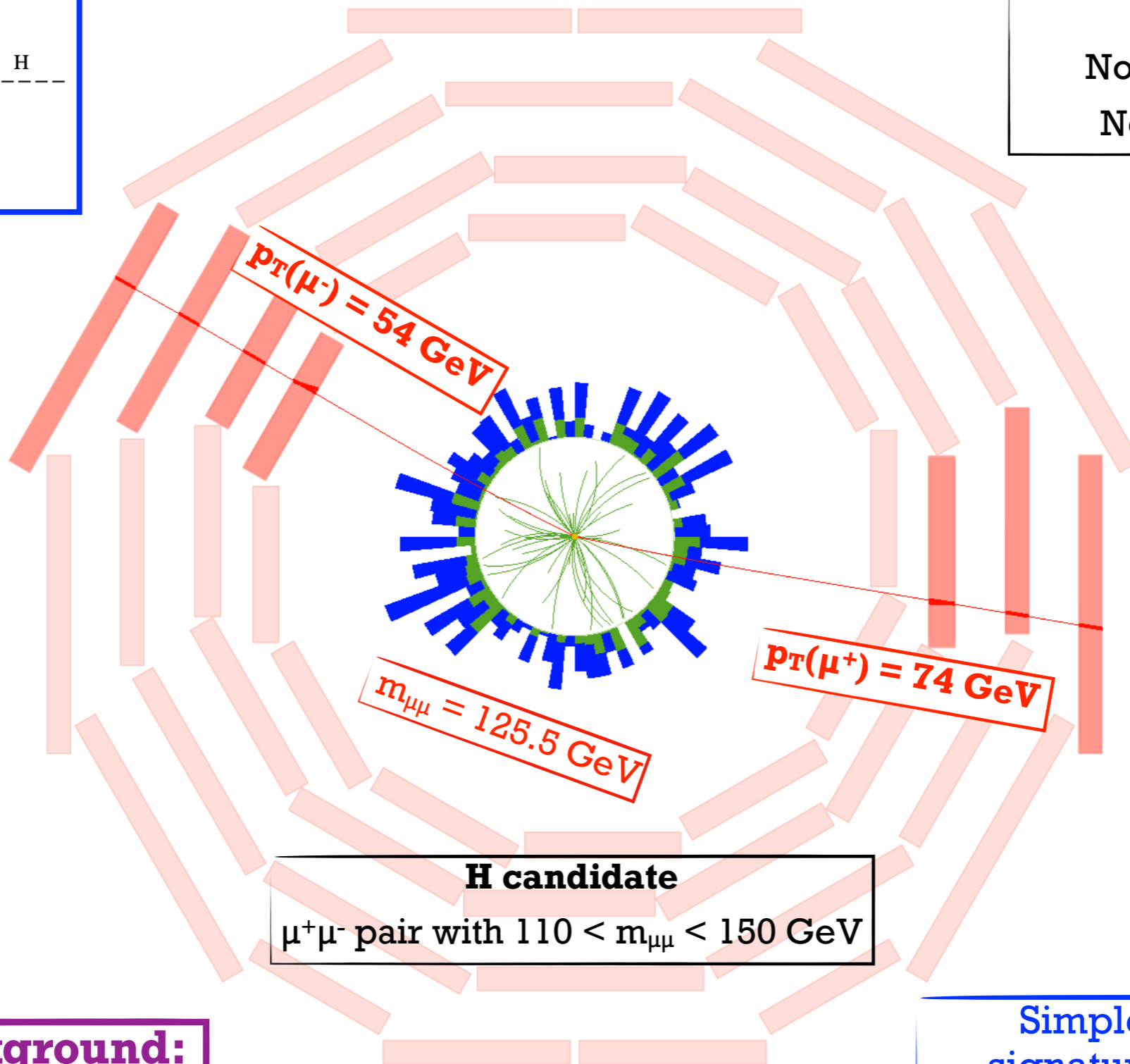


MVA subcategories with varying signal purity



**Veto exclusive categories:**

- No b jets
- No additional leptons
- No VBF-like jet pair



**Dominant background:**  
Drell-Yan (DY)

Simple experimental signature, but difficult to distinguish from background.

- Train a Boosted Decision Tree (BDT) to discriminate signal from backgrounds.
- H candidate kinematic variables:
  - Dimuon  $p_T$  and rapidity, decay angles  $\phi_{CS}$ ,  $\cos\theta_{CS}$
  - $\eta(\mu)$ ,  $p_T(\mu)/m_{\mu\mu}$ , ...
- Potential signature of initial state radiation:
  - Leading jet  $p_T$  and  $\eta$ .
  - Minimum angular separation between H candidate and jet.

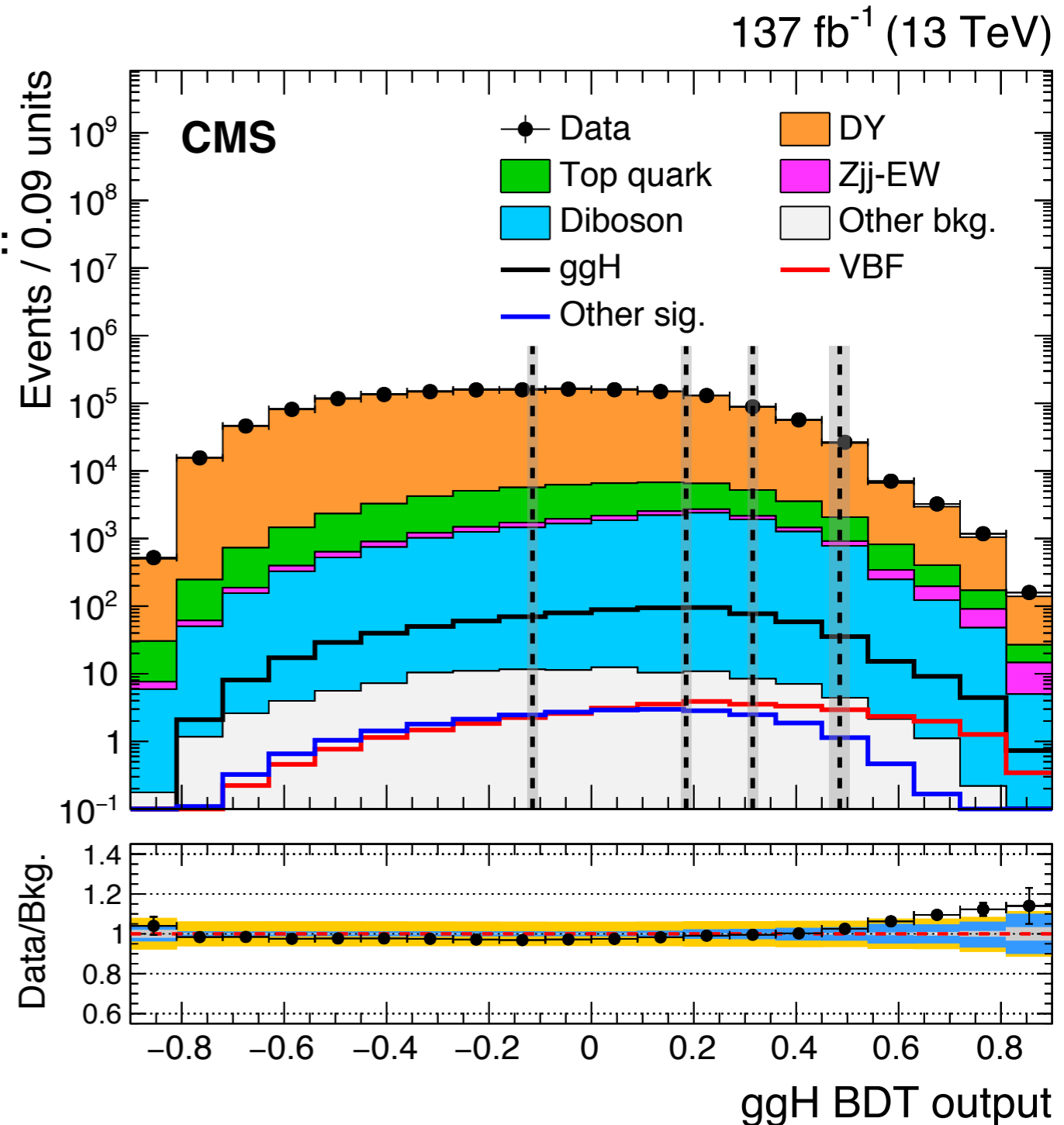
### Mass resolution per ggH subcategory

Event category	HWHM (GeV)
ggH-cat1	2.12
ggH-cat2	1.75
ggH-cat3	1.60
ggH-cat4	1.47
ggH-cat5	1.50

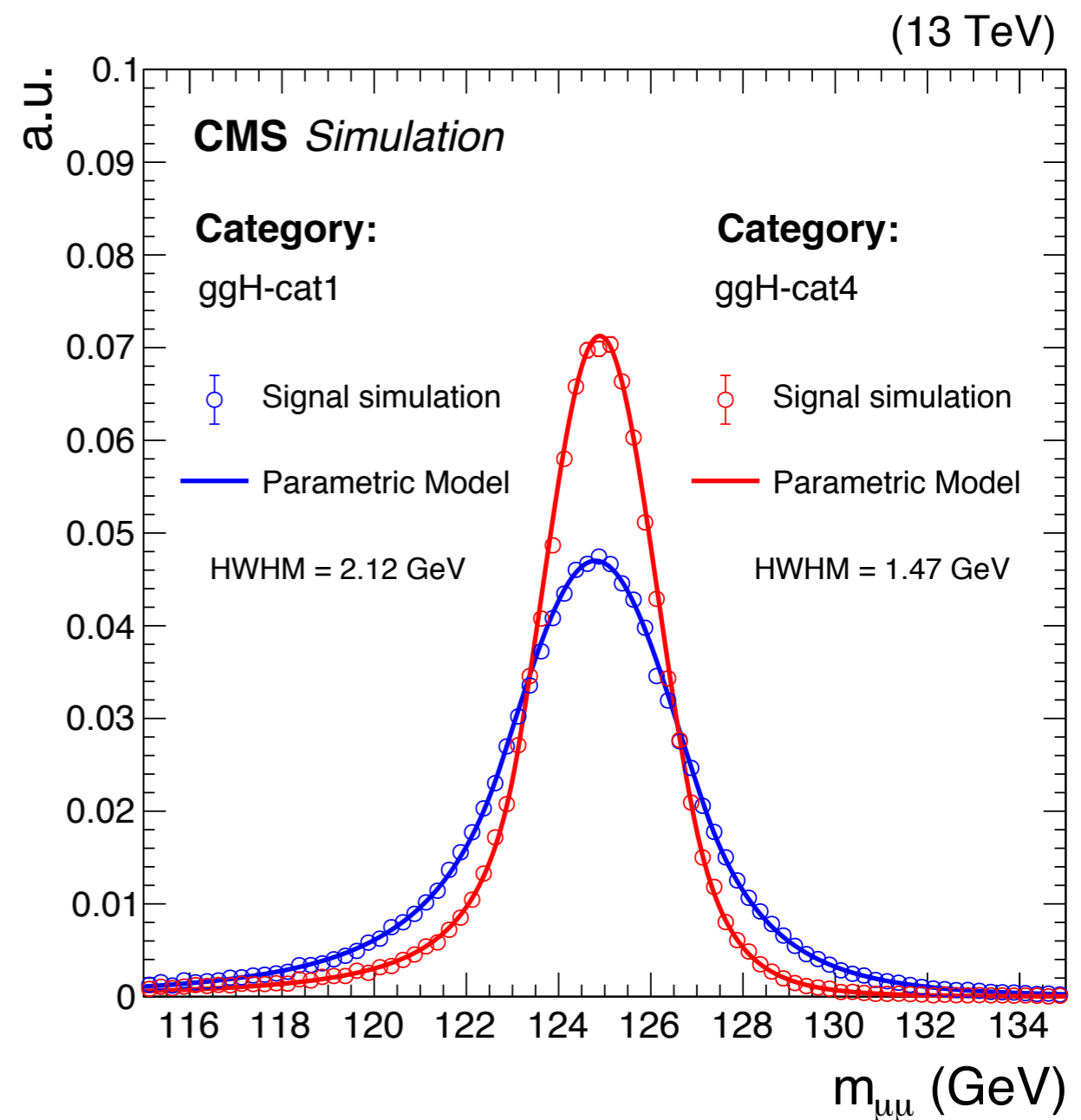
signal purity



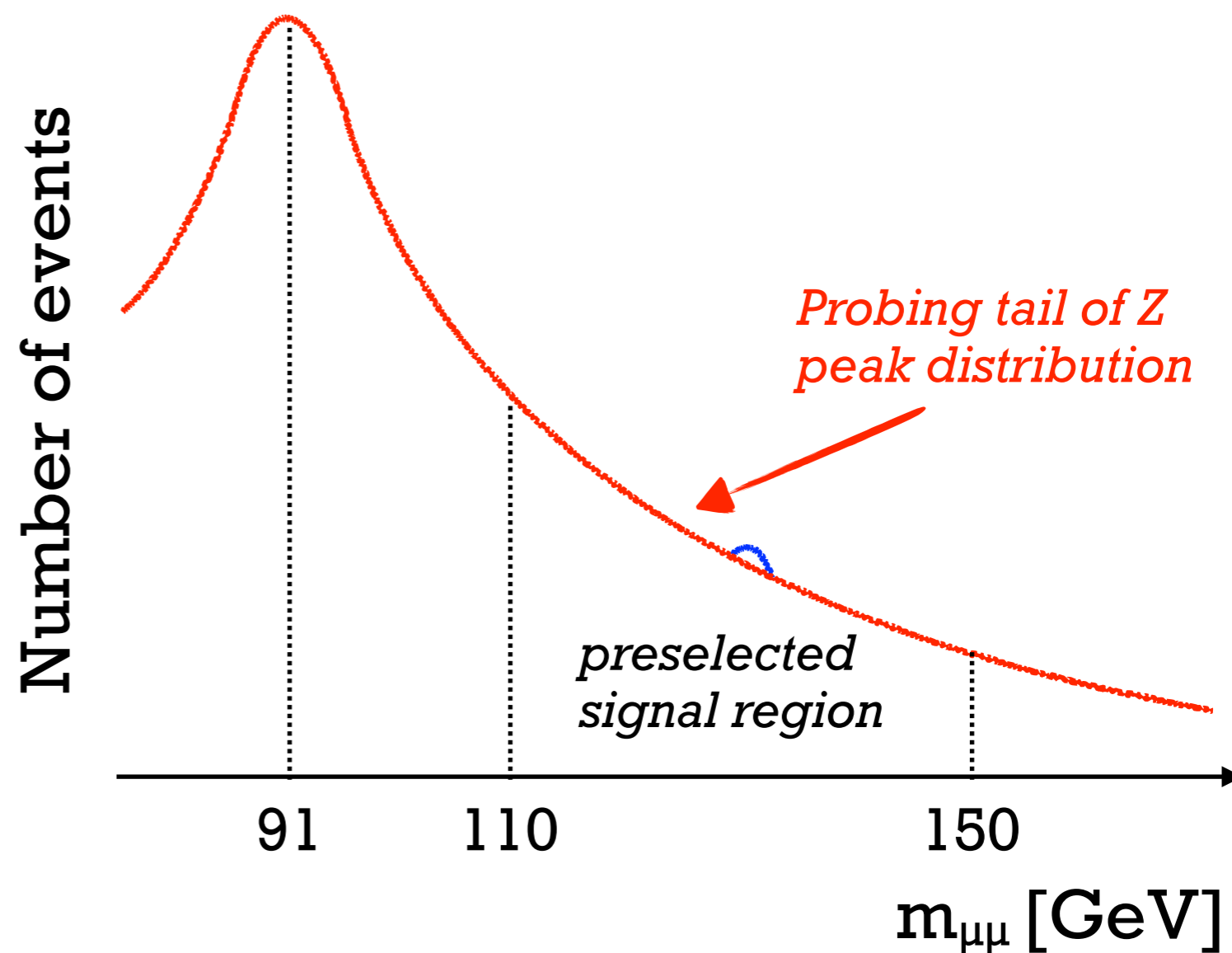
### ggH category BDT score distribution



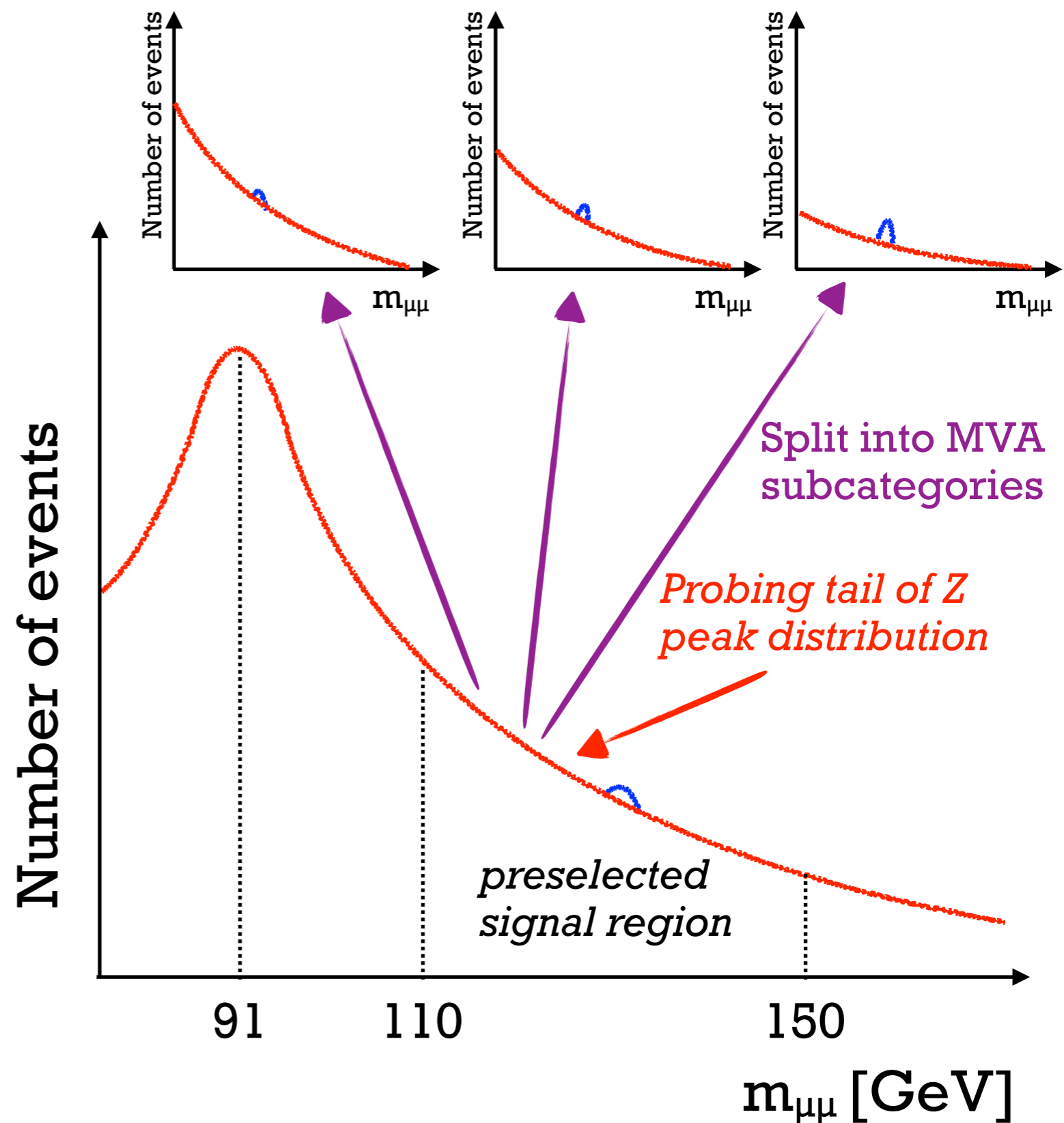
- Dimuon mass resolution ranges from 1 to 2% across subcategories, depending on muon  $p_T$  and  $\eta$ .
- Mass resolution further improved by:
  - recovery of photons from final state radiation ( $\sim 3\%$ )
  - constraining muon track to originate from interaction point ( $\sim 4\%$ )

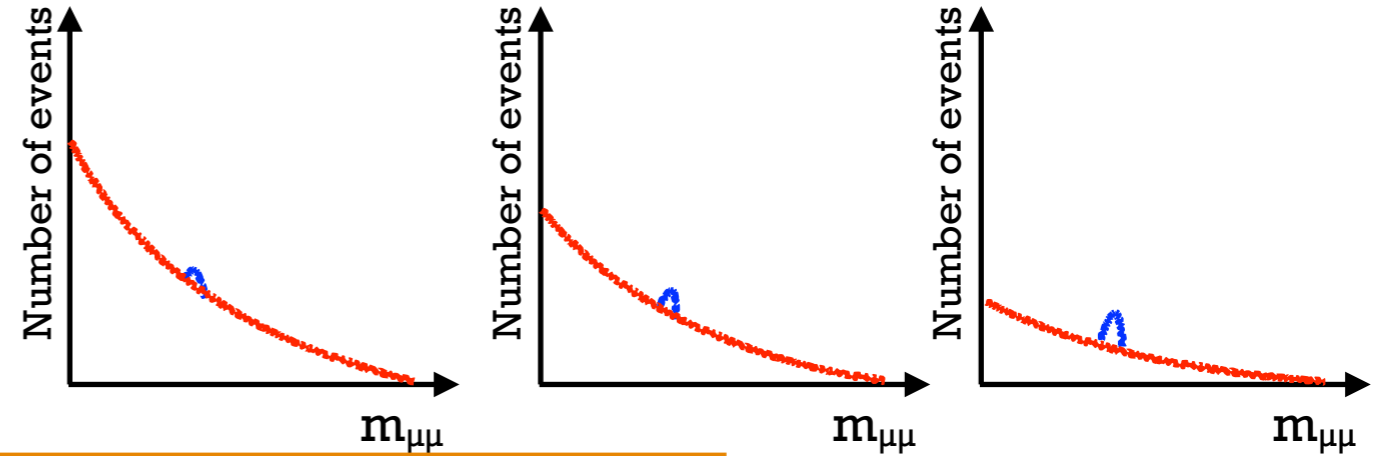


- Looking for small resonant peak over large smoothly falling DY background.



- Looking for small resonant peak over large smoothly falling DY background.
- Background shape expected to be similar across subcategories, with minor variations from differing muon kinematics.*



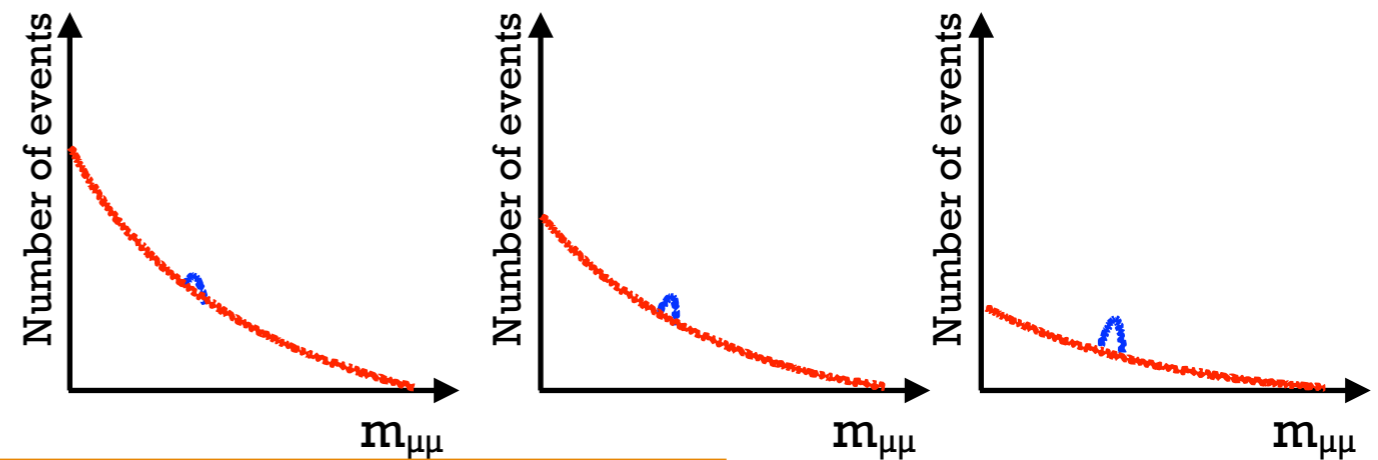


## The "Core-PDF" method

$$B_{cat}(m_{\mu\mu}, \vec{\alpha}, \vec{\beta}) = N_B \times F_{core}(m_{\mu\mu}, \vec{\alpha}) \times T_{SMF}(m_{\mu\mu}, \vec{\beta})$$

Number of  
bkg. events

"Core" function with **parameters correlated across subcategories.**



## The "Core-PDF" method

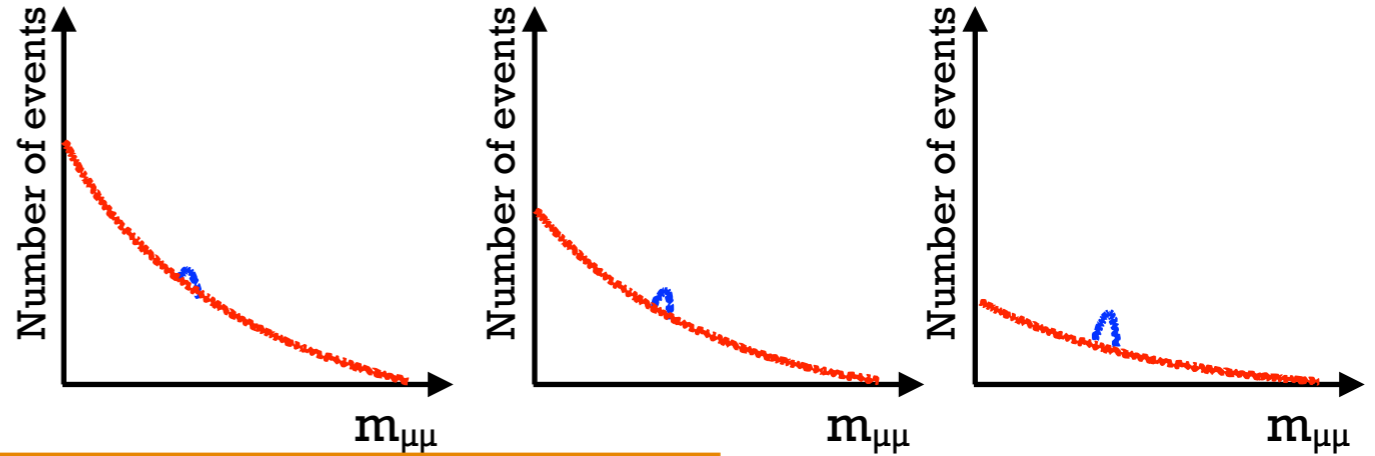
$$B_{cat}(m_{\mu\mu}, \vec{\alpha}, \vec{\beta}) = N_B \times F_{core}(m_{\mu\mu}, \vec{\alpha}) \times T_{SMF}(m_{\mu\mu}, \vec{\beta})$$

Number of  
bkg. events

"Core" function with **parameters correlated across subcategories.**

**Per-category polynomial shape modifier** to adjust for kinematic differences.





## The "Core-PDF" method

$$B_{cat}(m_{\mu\mu}, \vec{\alpha}, \vec{\beta}) = N_B \times F_{core}(m_{\mu\mu}, \vec{\alpha}) \times T_{SMF}(m_{\mu\mu}, \vec{\beta})$$

Number of  
bkg. events

"Core" function with **parameters correlated across subcategories.**

**Per-category polynomial shape modifier** to adjust for kinematic differences.

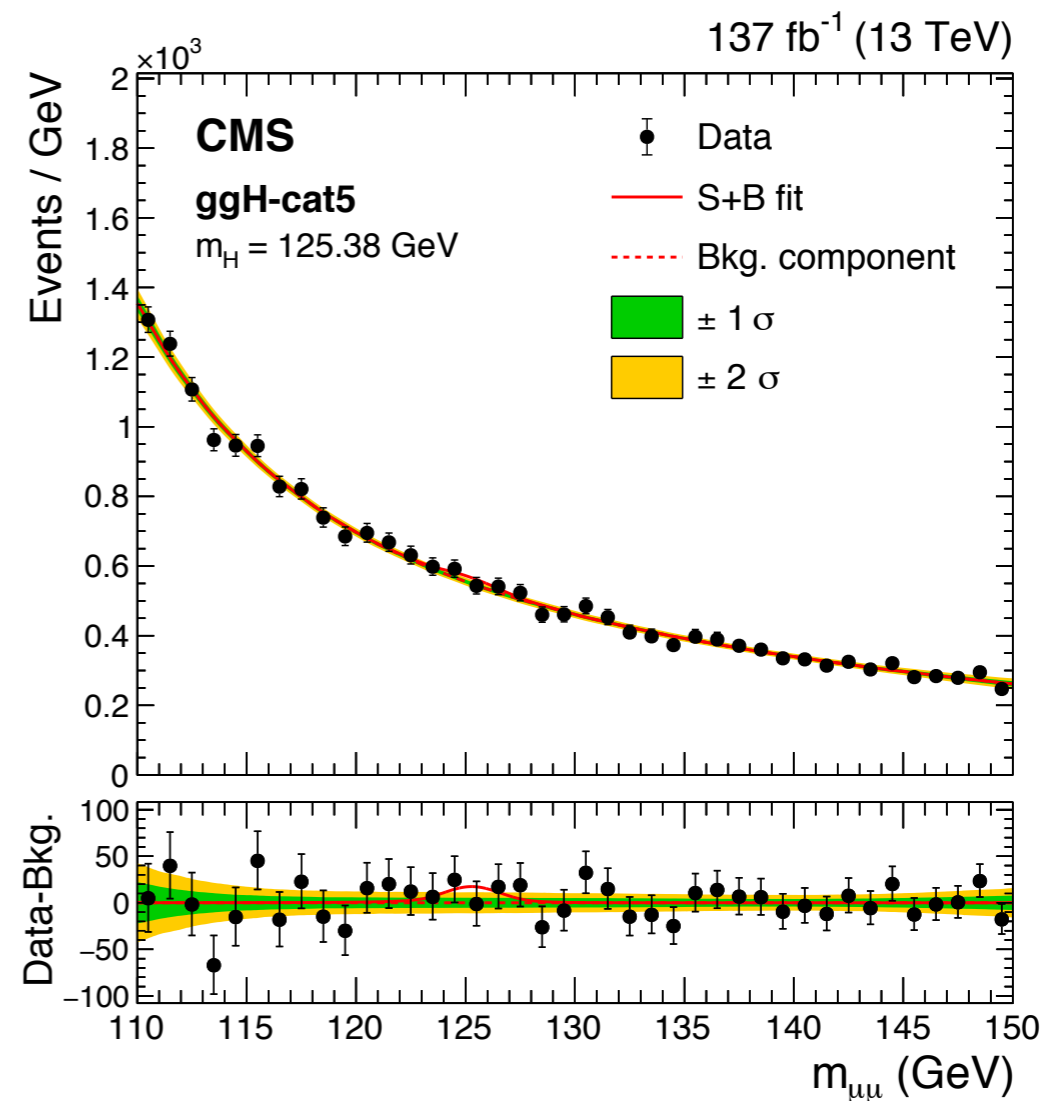
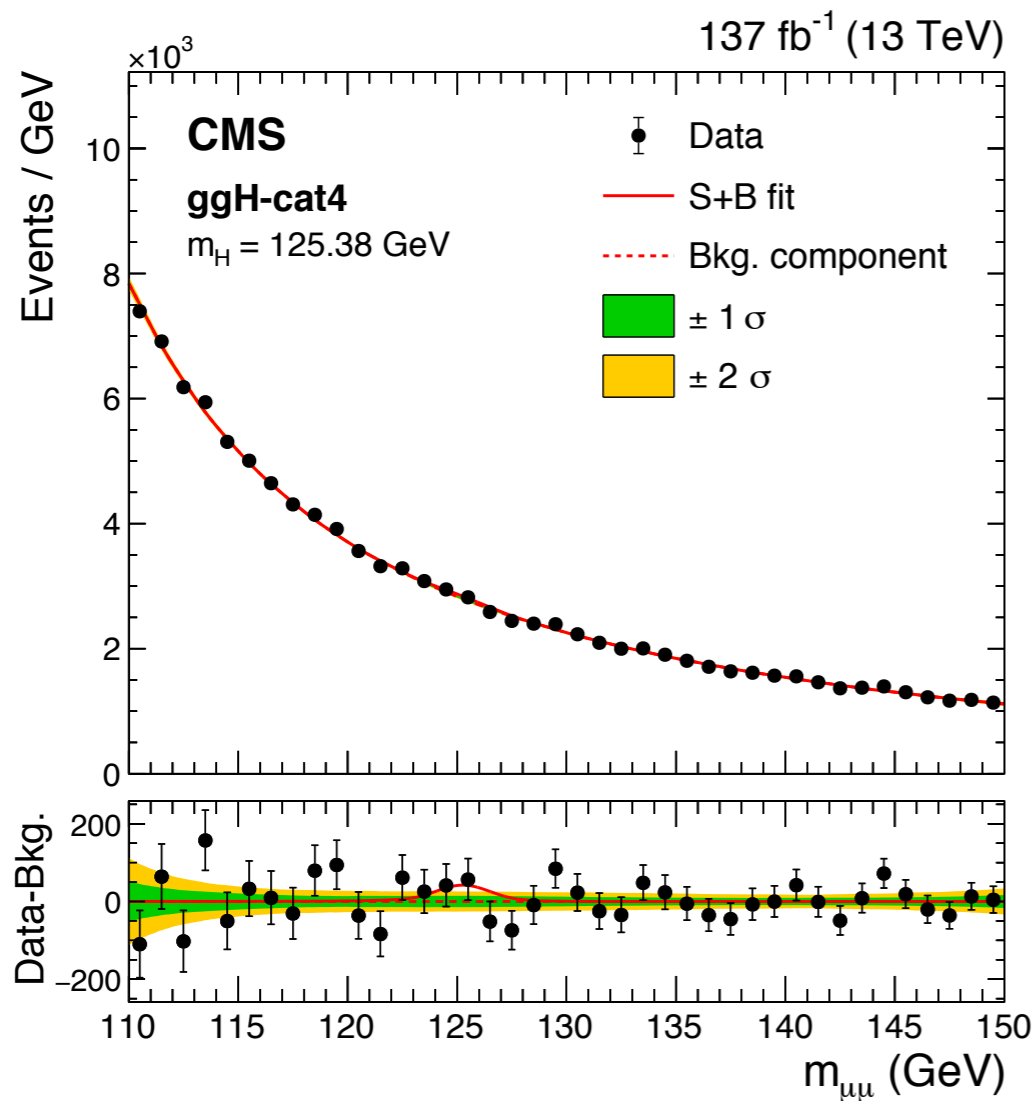
*10% performance improvement and fewer total degrees of freedom with respect to previous strategy, while retaining negligible bias.*

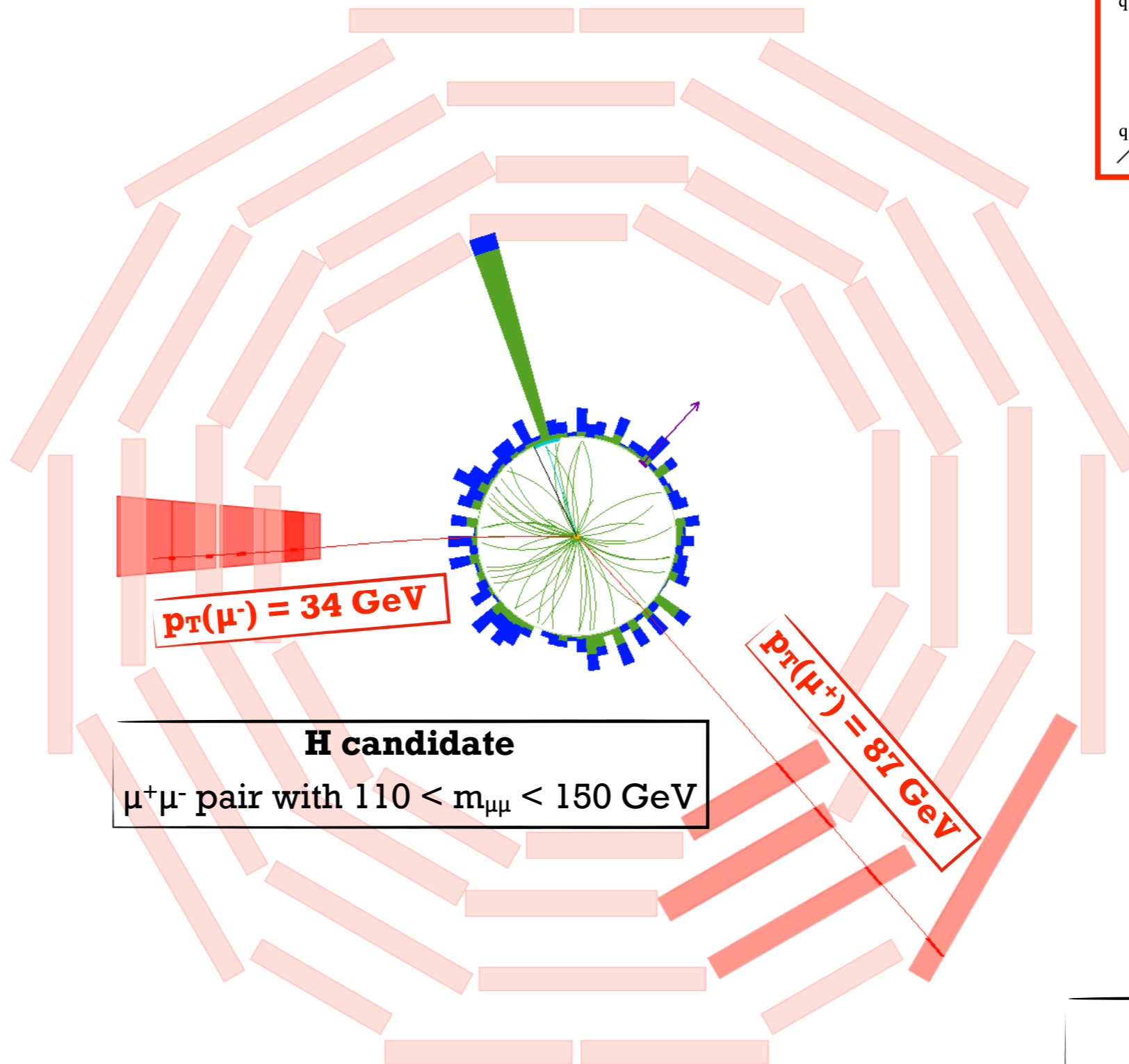
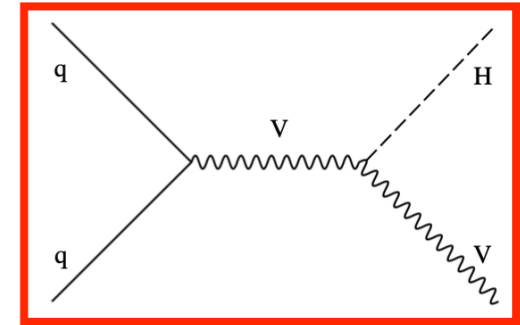
***ggH category result***

Observed (expected) significance:  $1.0\sigma$  ( $1.6\sigma$ )

$$\mu = \frac{\sigma_H \cdot \text{BR}(H \rightarrow \mu\mu)}{\sigma_H \cdot \text{BR}(H \rightarrow \mu\mu)_{\text{SM}}} = 0.63^{+0.65}_{-0.65}$$

*$m_{\mu\mu}$  distribution in the highest purity ggH subcategories*

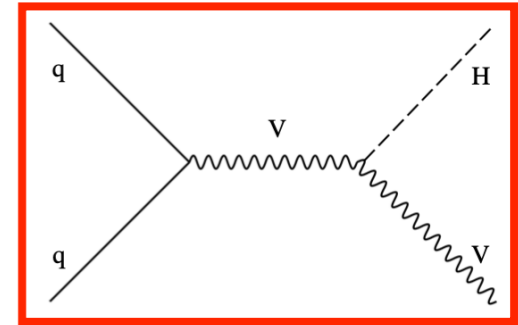




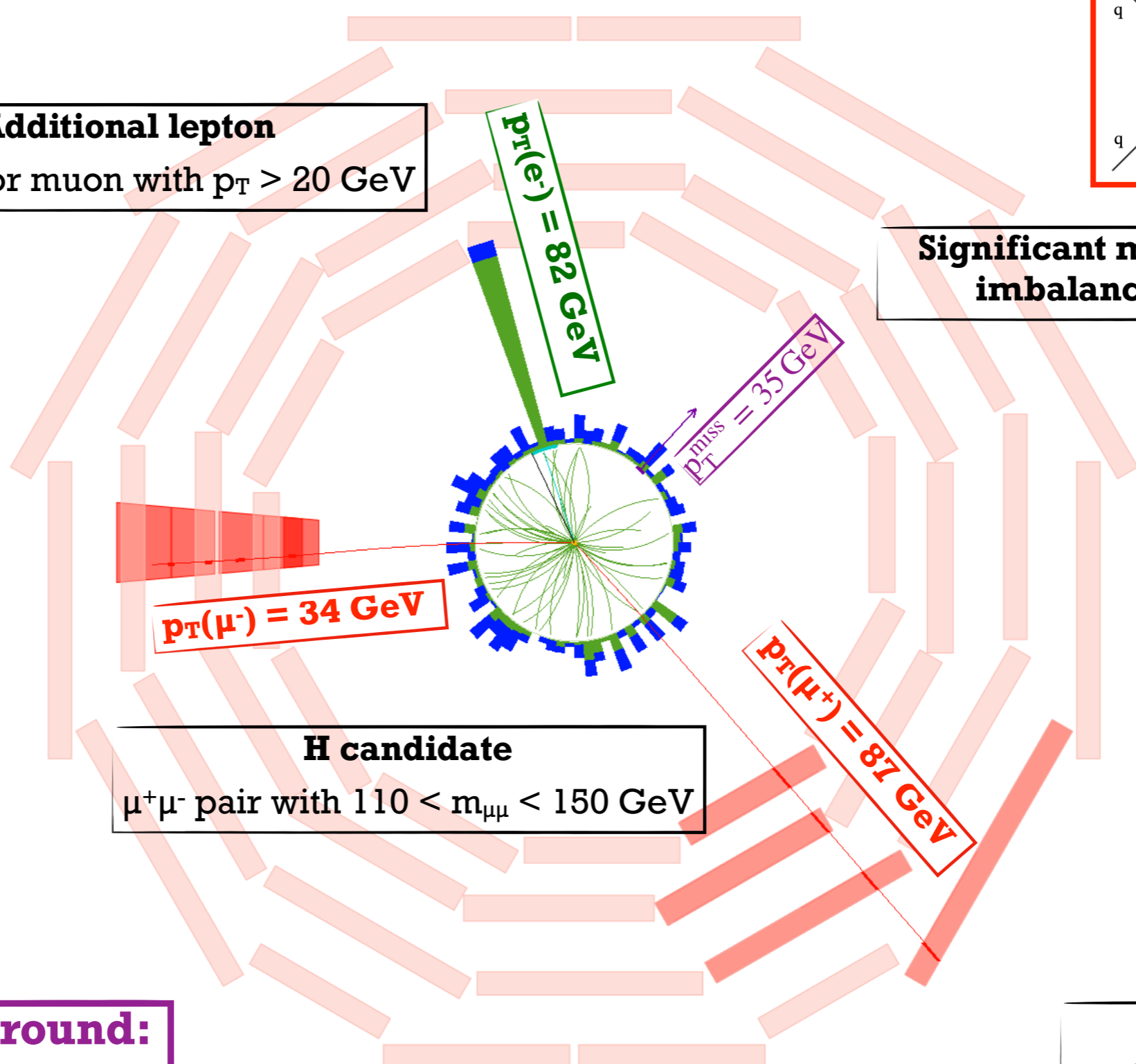
**H candidate**  
 $\mu^+\mu^-$  pair with  $110 < m_{\mu\mu} < 150$  GeV

**b-jet veto**  
 No jets in event  
 passing b-tagging

**Additional lepton**  
Electron or muon with  $p_T > 20$  GeV



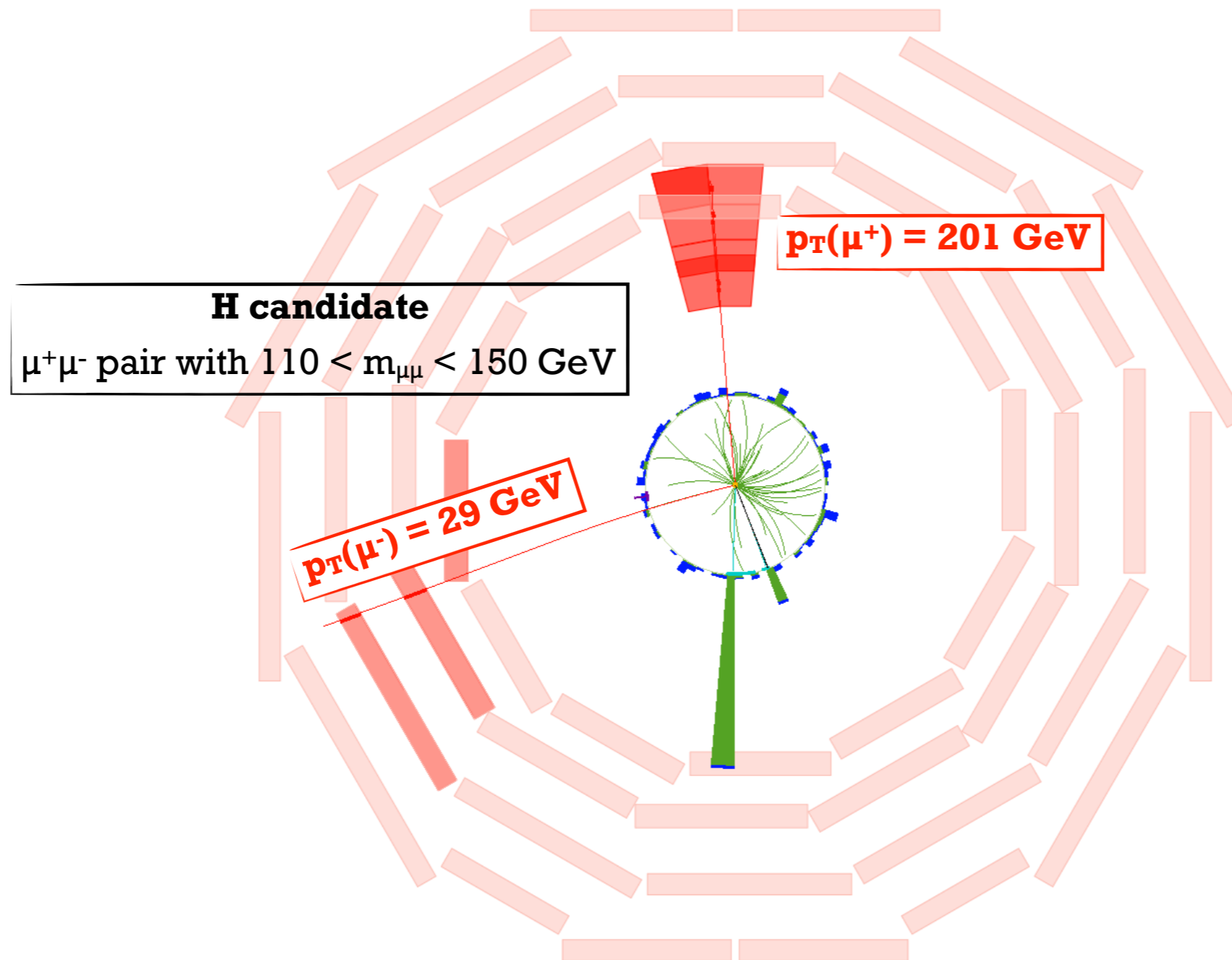
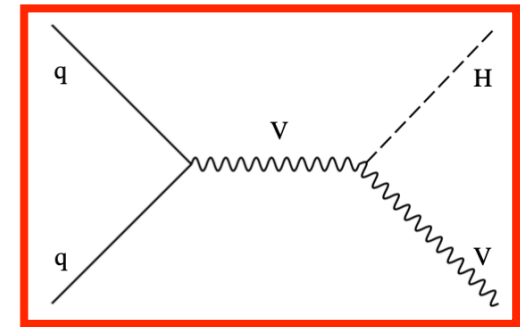
**Significant momentum imbalance**  
 $p_T^{\text{miss}}$



**H candidate**  
 $\mu^+\mu^-$  pair with  $110 < m_{\mu\mu} < 150$  GeV

**Dominant background:**  
 $WZ \rightarrow \ell \nu 2\mu$

**b-jet veto**  
No jets in event passing b-tagging

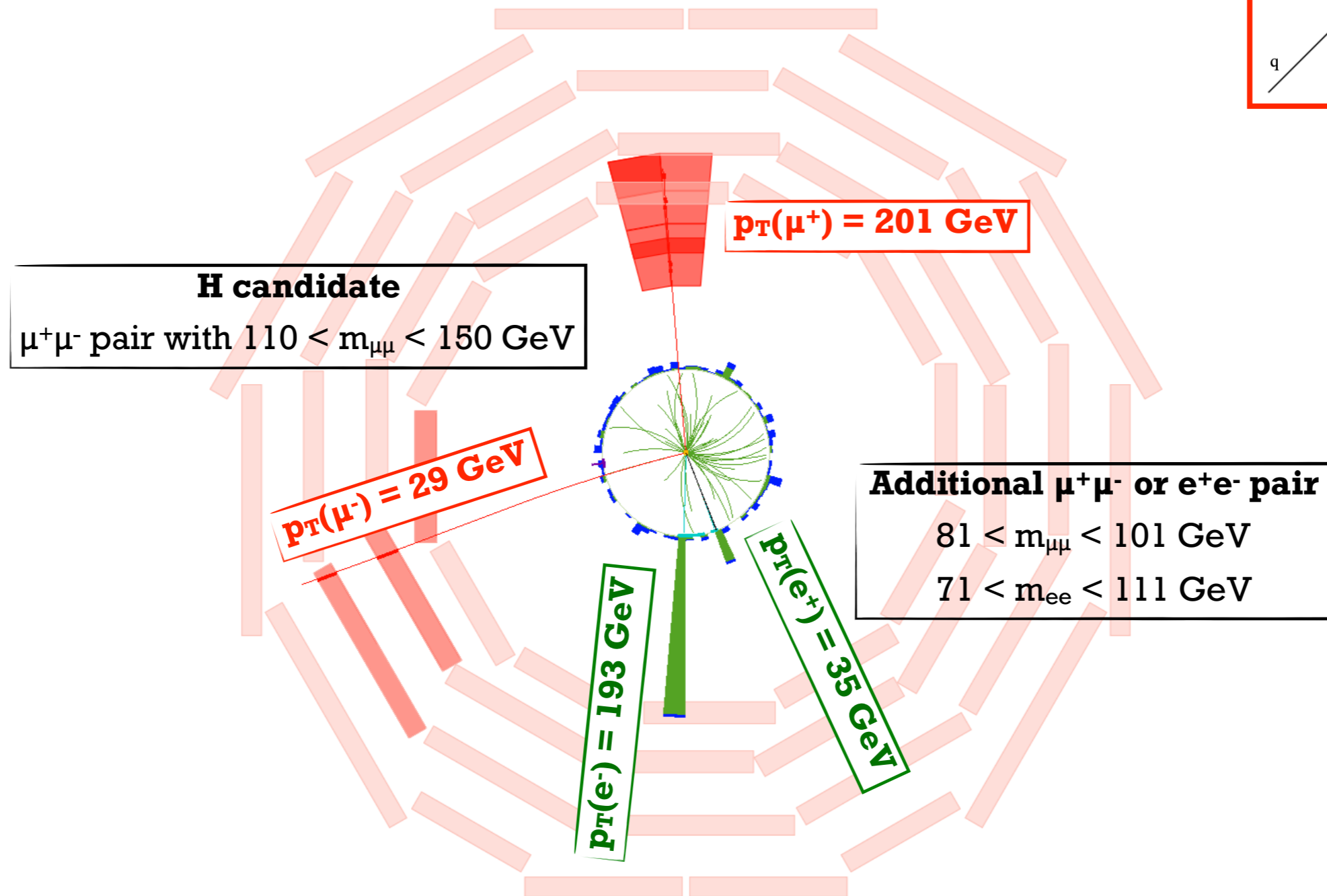
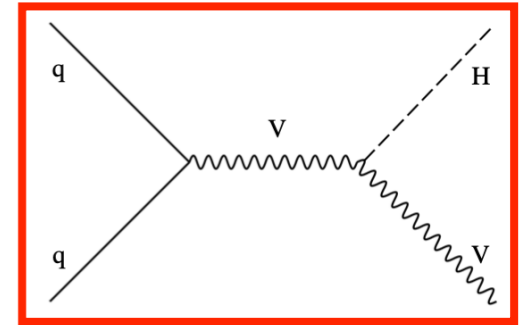


**H candidate**  
 $\mu^+\mu^-$  pair with  $110 < m_{\mu\mu} < 150$  GeV

$p_T(\mu^+) = 201$  GeV

$p_T(\mu^-) = 29$  GeV

**b-jet veto**  
 No jets in event  
 passing b-tagging

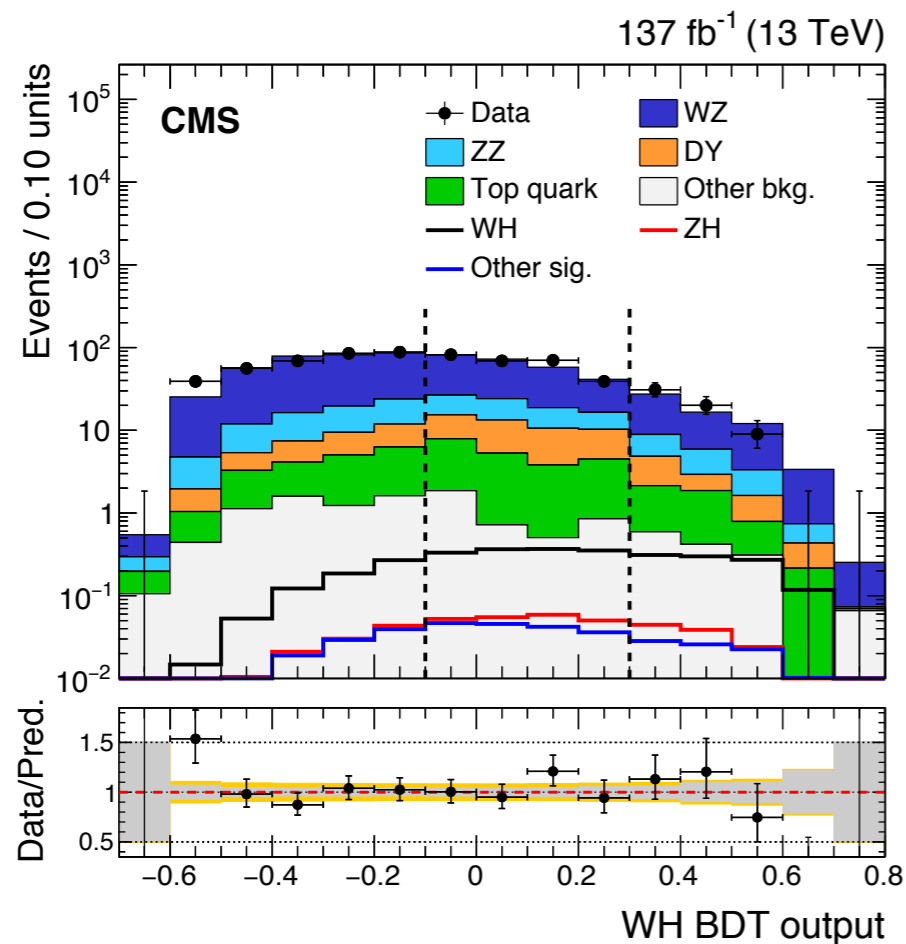


**Dominant background:**  
 $ZZ \rightarrow 2\ell 2\mu$

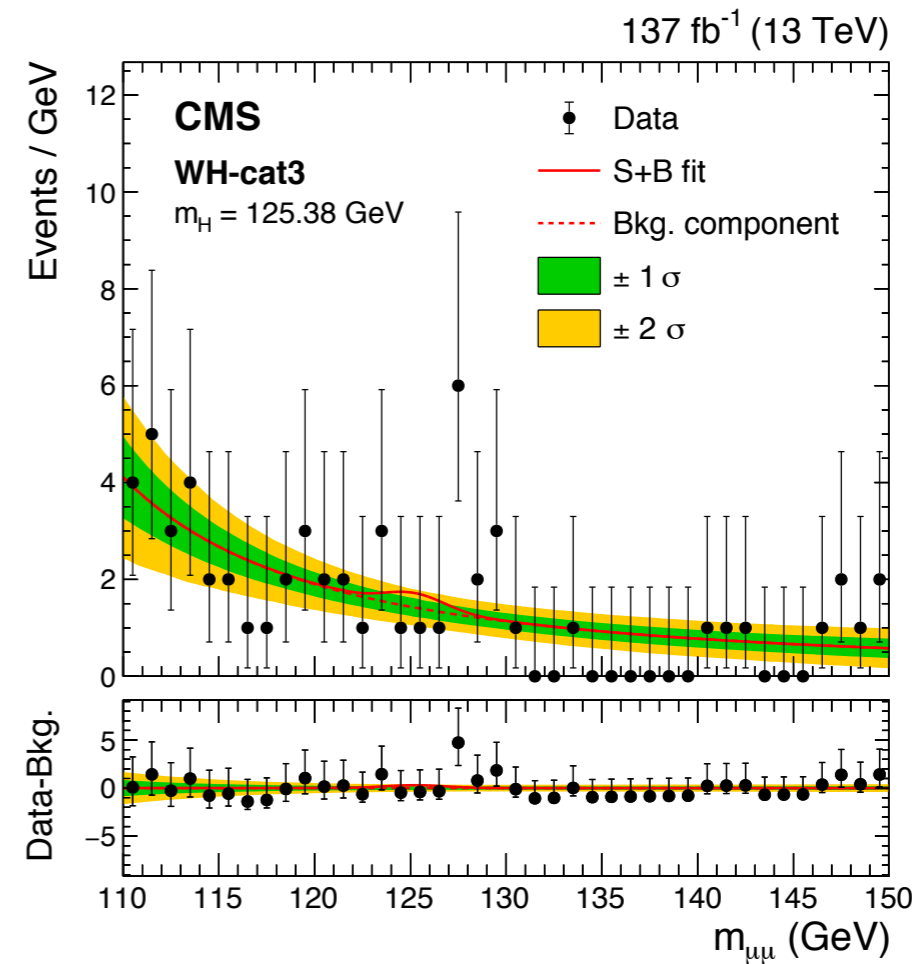
**b-jet veto**  
 No jets in event  
 passing b-tagging

- Inputs to WH and ZH BDT classifiers:
  - H candidate kinematic variables:  $p_T(\mu\mu)$ ,  $\Delta\phi(\mu\mu)$ , ...
  - WH system:  $p_T(\ell_W)$ ,  $\Delta\eta(\ell_W, H)$ ,  $\Delta\phi(\ell_W, H)$ ,  $m_T(\ell_W, p_T^{\text{miss}})$ , ...
  - ZH system:  $p_T(Z)$ ,  $\eta(Z)$ ,  $m_Z$ ,  $\Delta\eta(Z, H)$ ,  $\Delta\phi(Z, H)$ ,  $\cos\theta^*(Z, H)$ , ...

*WH category BDT score*

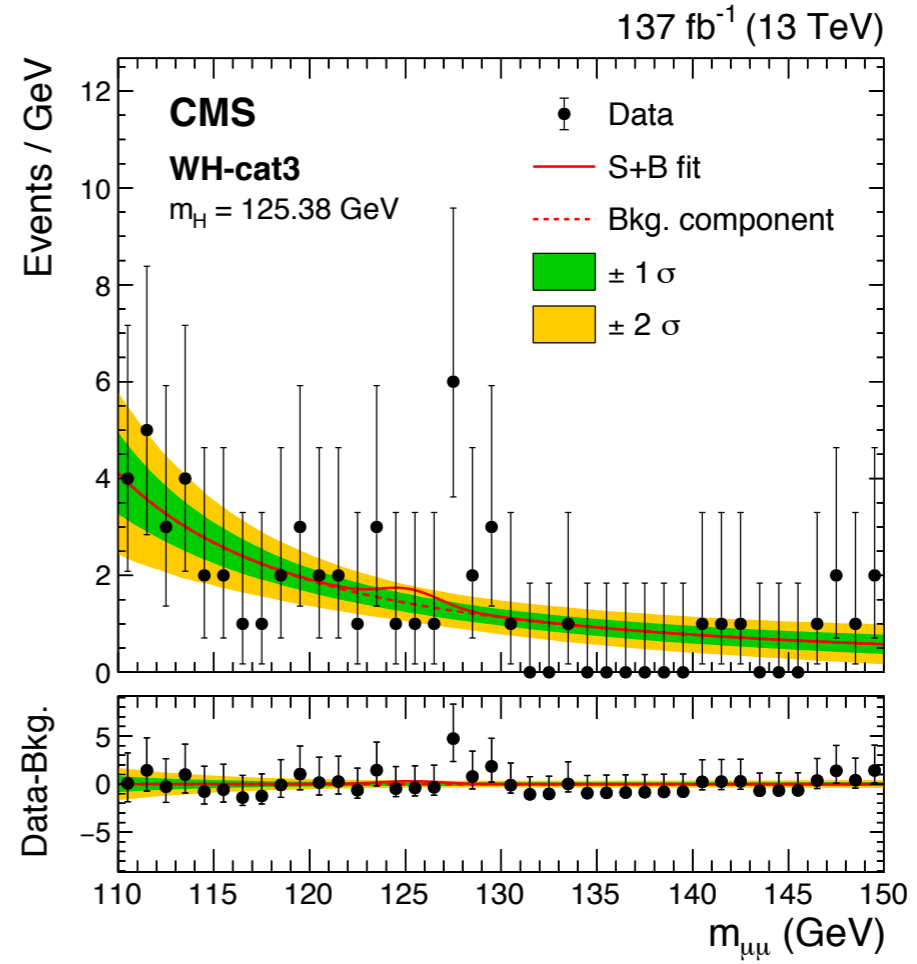
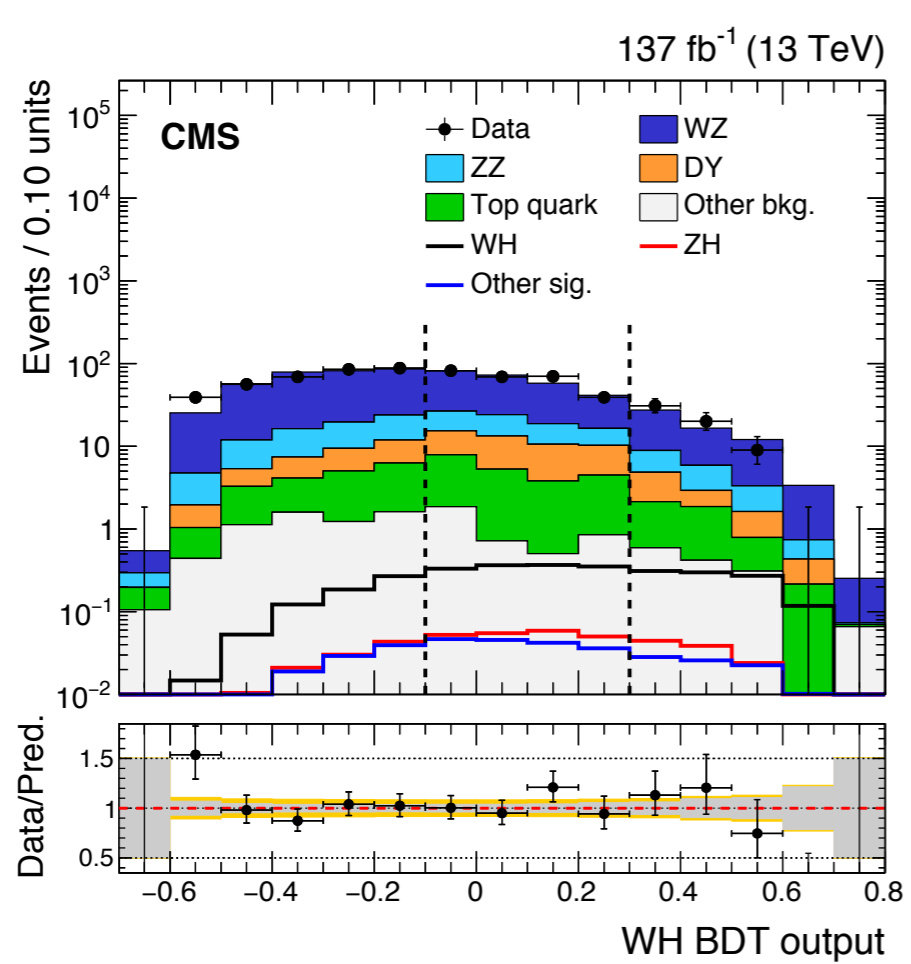


*$m_{\mu\mu}$  distribution in the highest purity WH subcategory*

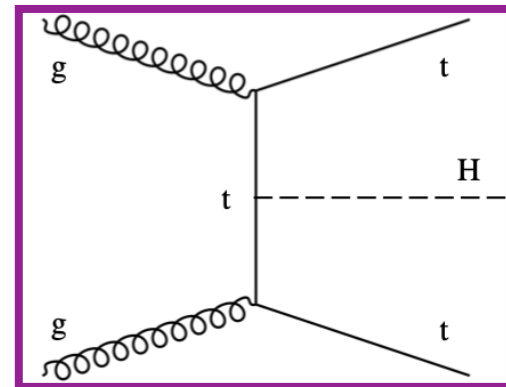
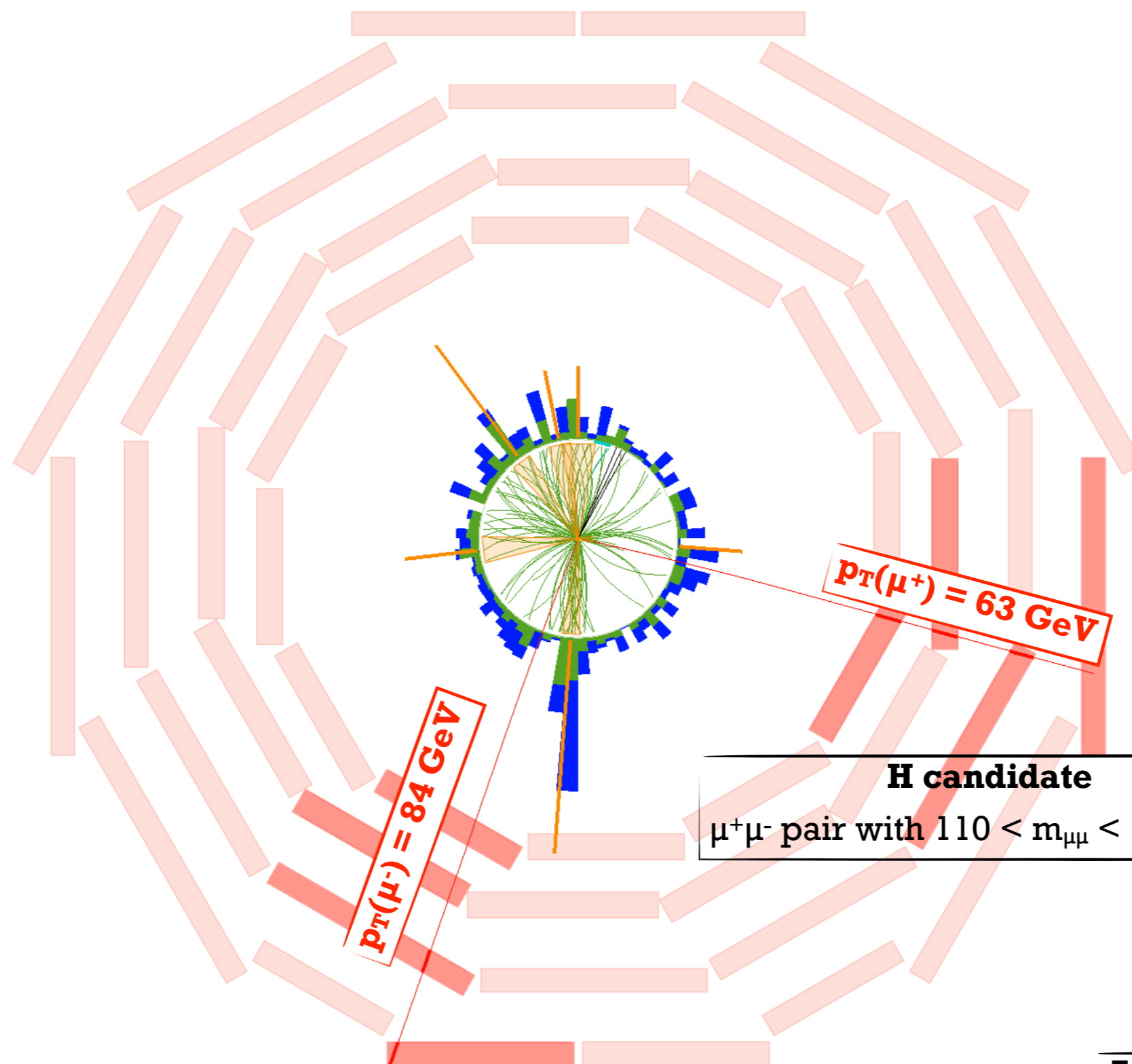


- Inputs to WH and ZH BDT classifiers:
  - H candidate kinematic variables:  $p_T(\mu\mu)$ ,  $\Delta\phi(\mu\mu)$ , ...
  - WH system:  $p_T(\ell_W)$ ,  $\Delta\eta(\ell_W, H)$ ,  $\Delta\phi(\ell_W, H)$ ,  $m_T(\ell_W, p_T^{\text{miss}})$ , ...
  - ZH system:  $p_T(Z)$ ,  $\eta(Z)$ ,  $m_Z$ ,  $\Delta\eta(Z, H)$ ,  $\Delta\phi(Z, H)$ ,  $\cos\theta^*(Z, H)$ , ...

**Combined WH and ZH category result**  
 Observed (expected) significance:  $2.0\sigma$  ( $0.4\sigma$ )

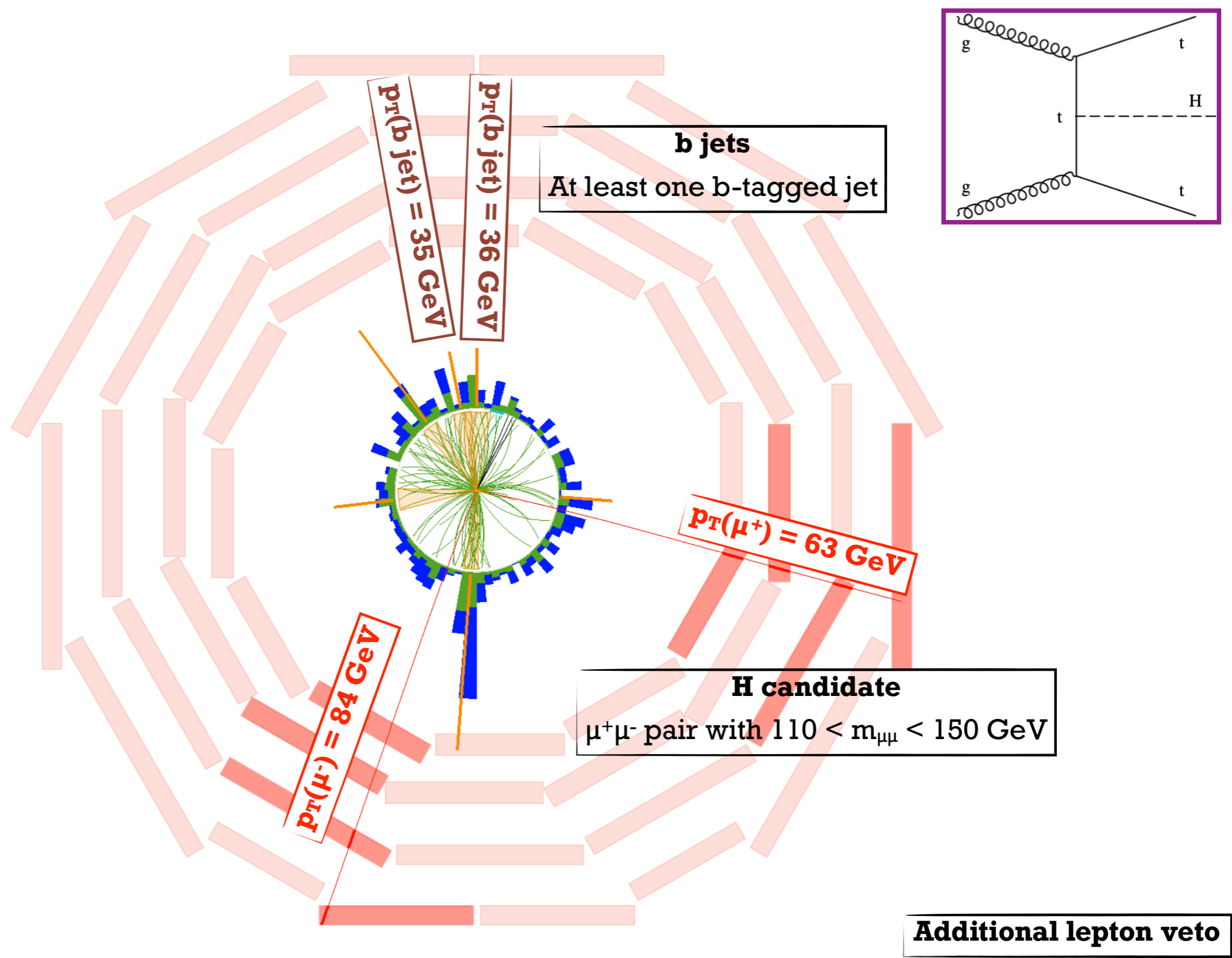
$$\mu = \frac{\sigma_H \cdot \text{BR}(H \rightarrow \mu\mu)}{\sigma_H \cdot \text{BR}(H \rightarrow \mu\mu)_{\text{SM}}} = 5.48^{+3.10}_{-2.83}$$






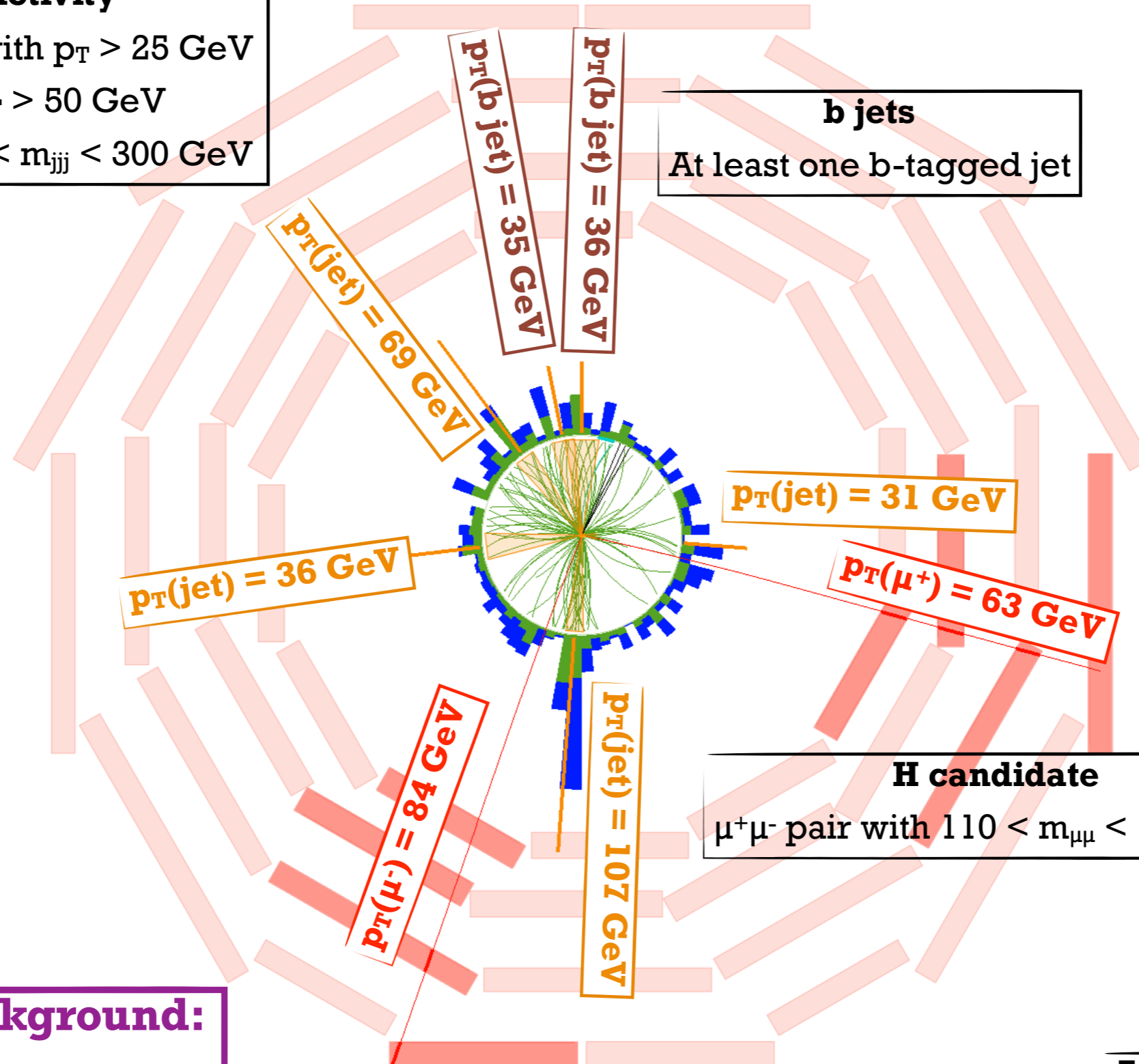
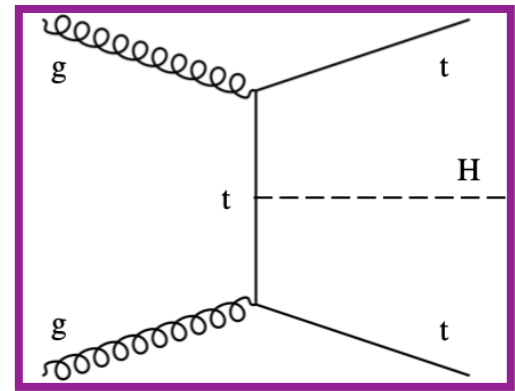
**H candidate**  
 $\mu^+\mu^-$  pair with  $110 < m_{\mu\mu} < 150$  GeV

**Additional lepton veto**



**Hadronic activity**  
 At least three jets with  $p_T > 25$  GeV  
 Leading jet  $p_T > 50$  GeV  
 Jet triplet with  $100 < m_{jjj} < 300$  GeV

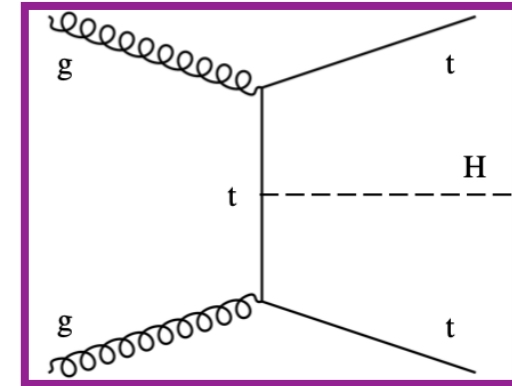
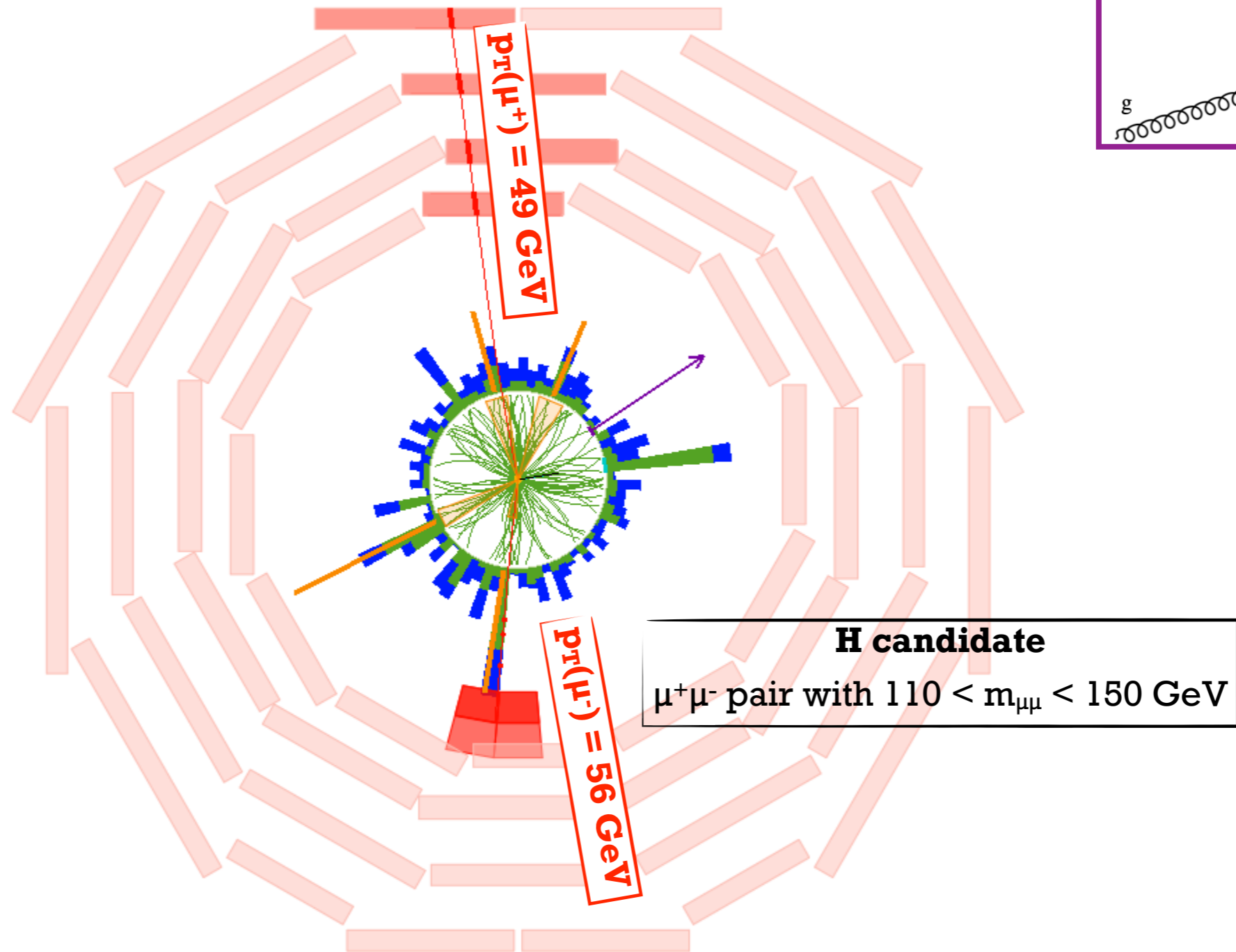
**b jets**  
 At least one b-tagged jet



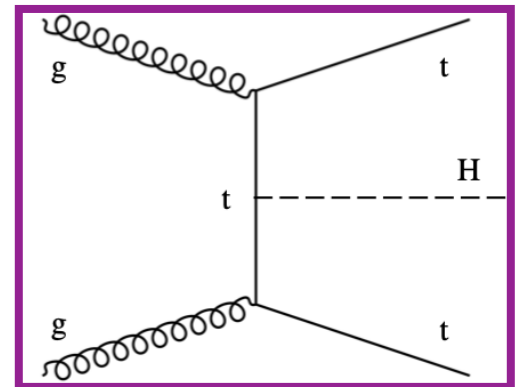
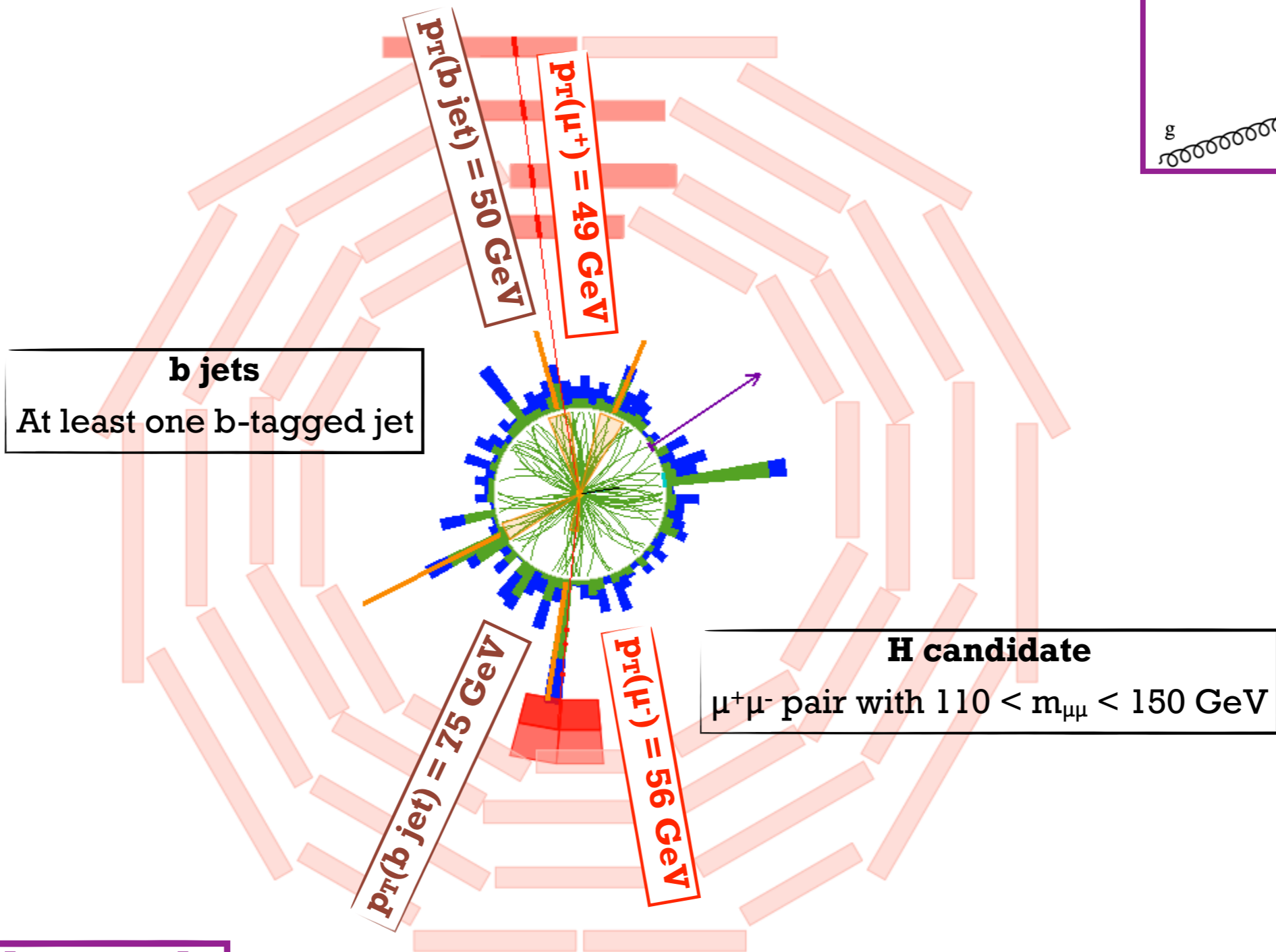
**H candidate**  
 $\mu^+\mu^-$  pair with  $110 < m_{\mu\mu} < 150$  GeV

**Dominant background:**  
 tt+jets

**Additional lepton veto**

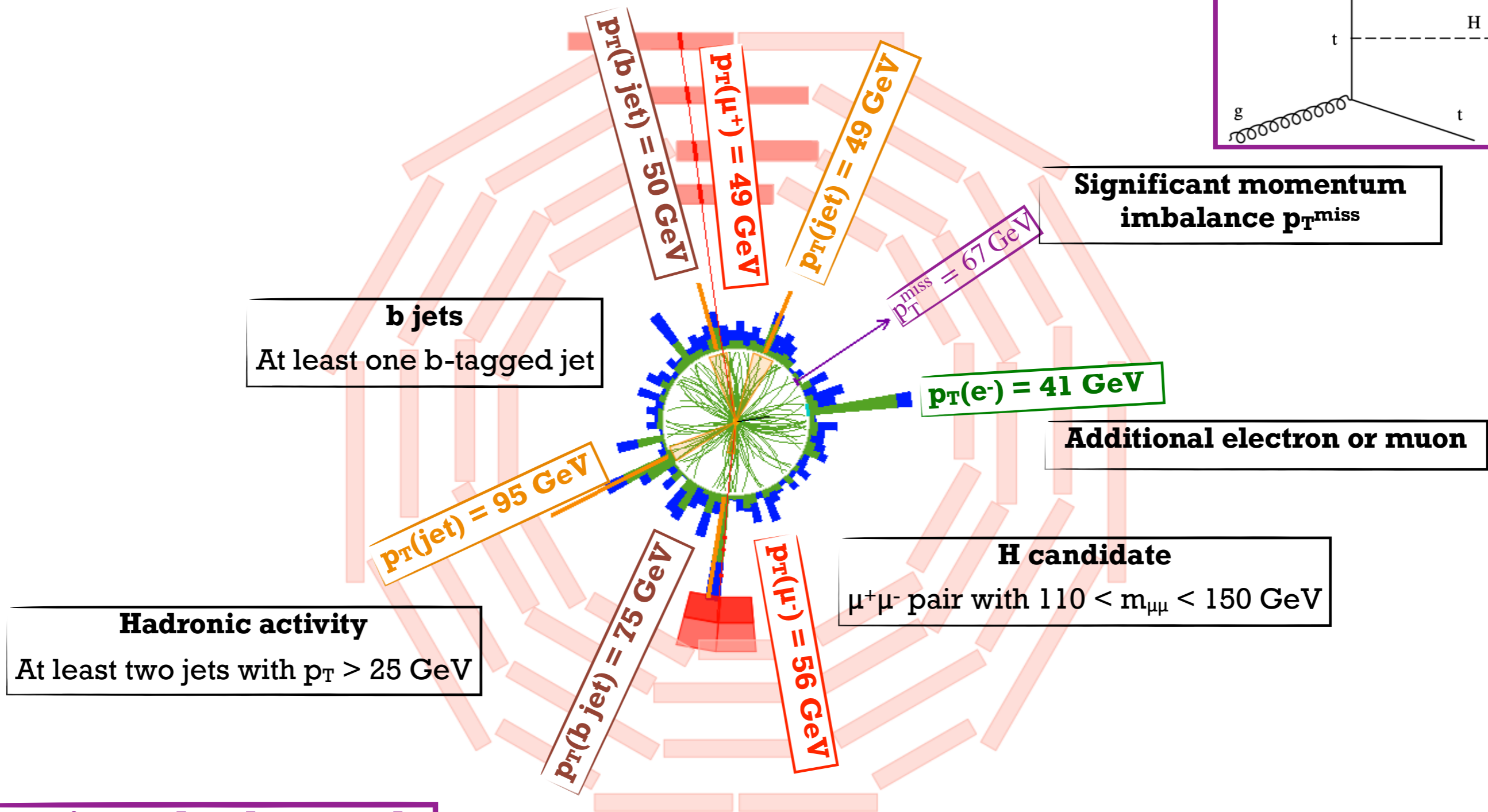
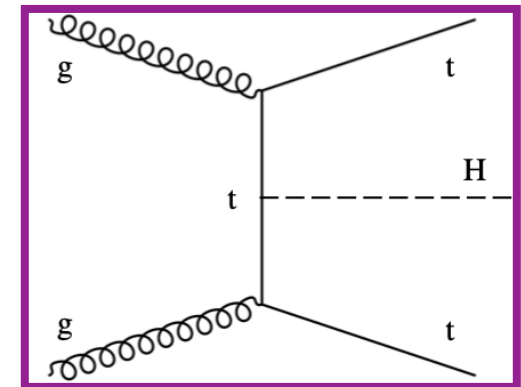


*\*Dileptonic ttH events also considered*



**Dominant background:**  
tt, ttZ

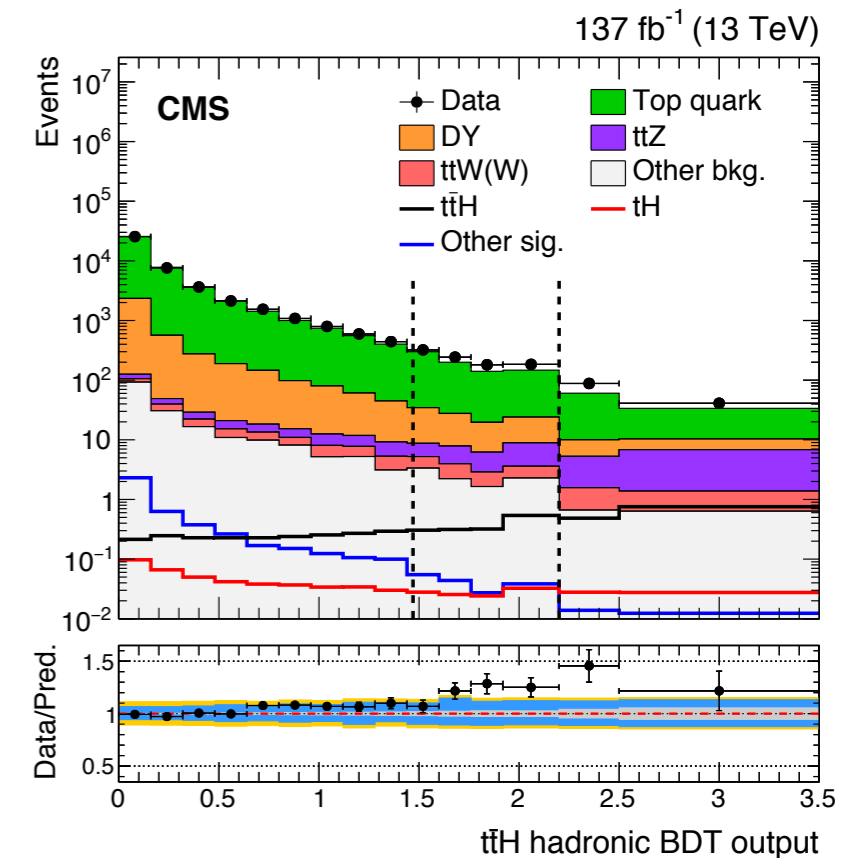
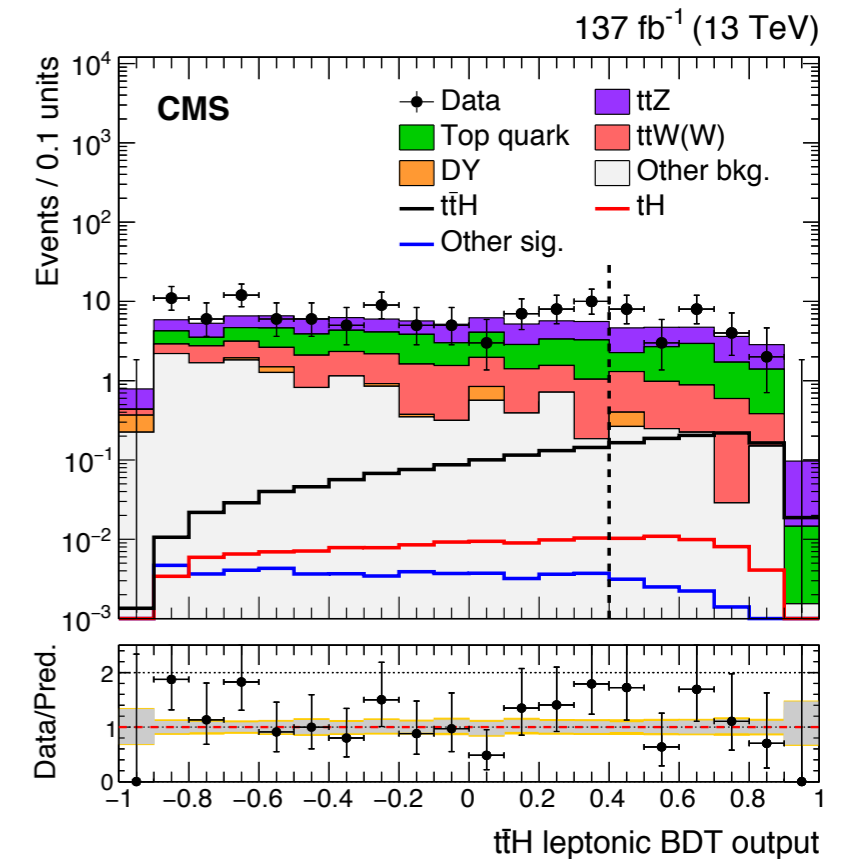
*\*Dileptonic ttH events also considered*



**Dominant background:**  
tt, ttZ

*\*Dileptonic ttH events also considered*

- **Common ttH BDT inputs:**
  - Dimuon  $p_T$  and rapidity, decay angles  $\phi_{CS}$ ,  $\cos\theta_{CS}$ , ...
  - $p_T^{\text{miss}}$ ,  $H_T$ , jet multiplicity, ...
- **Specific inputs for hadronic category:**
  - $p_T$ ,  $\eta$  of the three leading jets
  - top quark candidate: jet triplet with maximum Resolved Hadronic Top Tagger (RHTT) score
    - $p_T(\text{jjj})$ , RHTT score,  $p_T\text{-balance}(H, \text{jjj})$
- **Specific inputs for leptonic category:**
  - $\ell^T$ : highest- $p_T$  additional lepton
  - $\Delta\phi(\ell^T, H)$ ,  $\text{mass}(\text{b jet}, \ell^T)$ ,  $m_T(p_T^{\text{miss}}, \ell^T)$

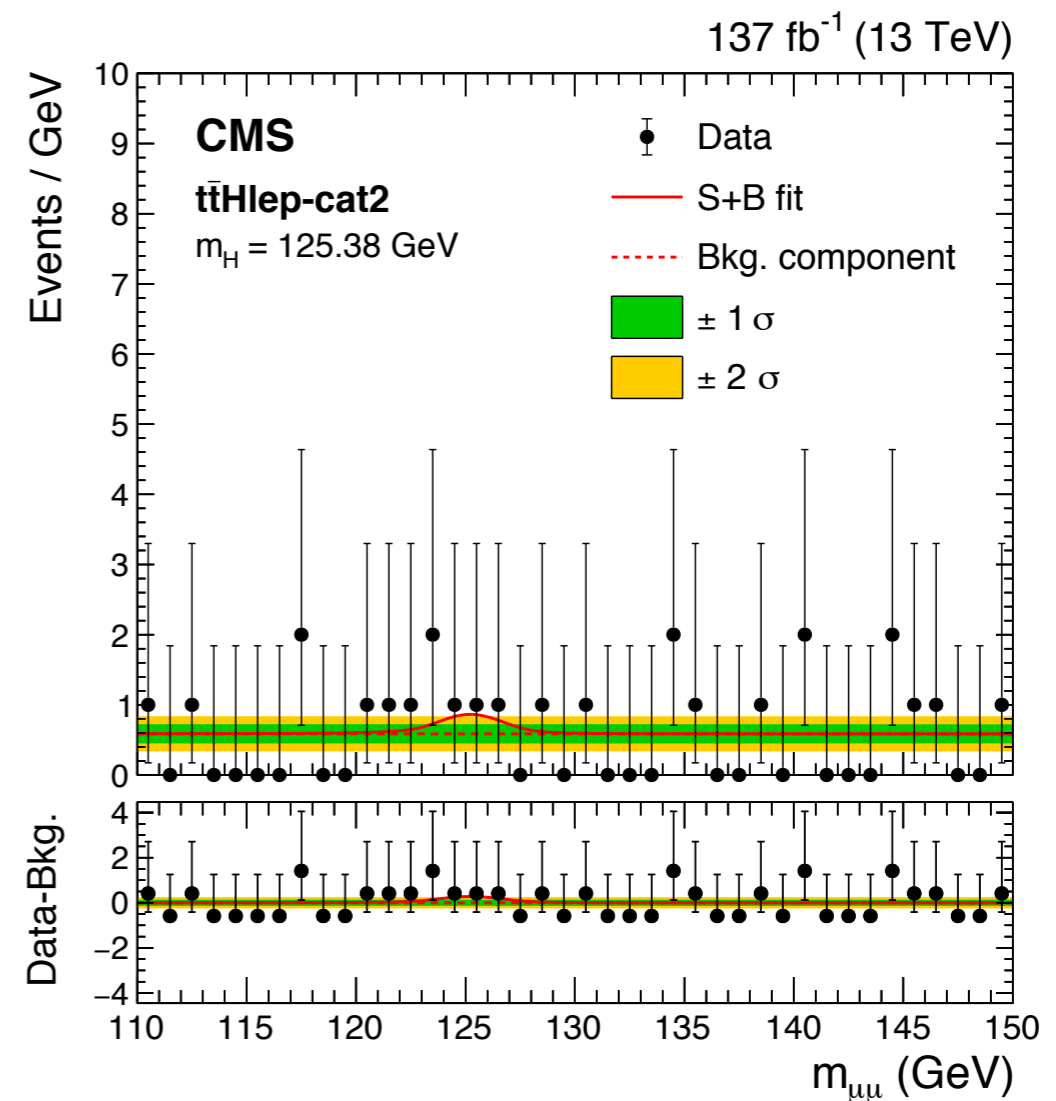
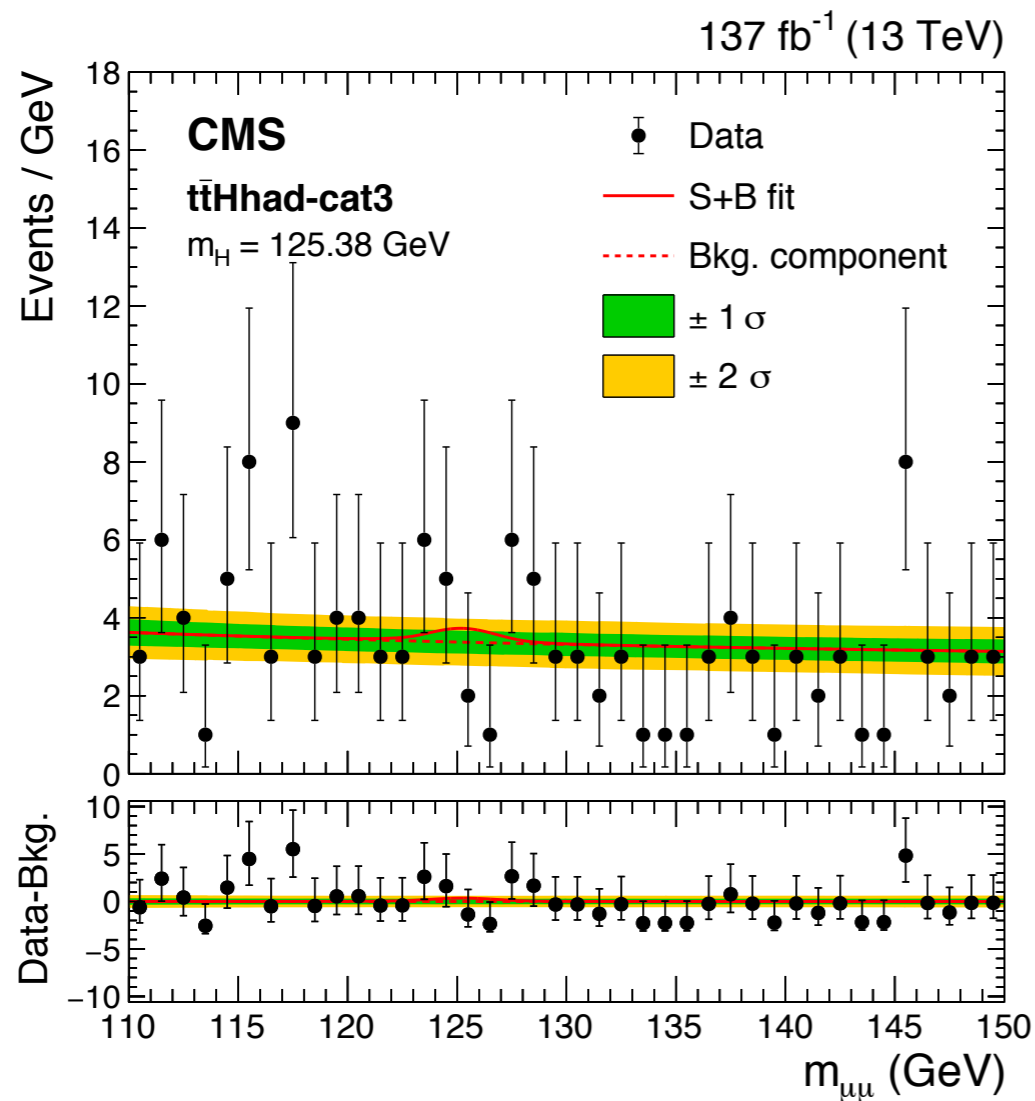


## Combined ttH (hadronic + leptonic) category result

Observed (expected) significance:  $1.2\sigma$  ( $0.5\sigma$ )

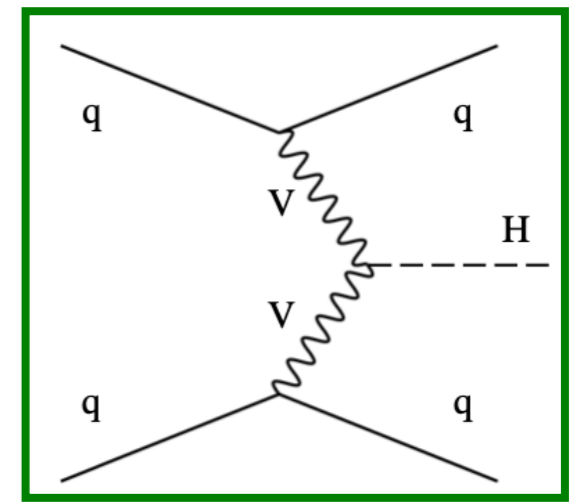
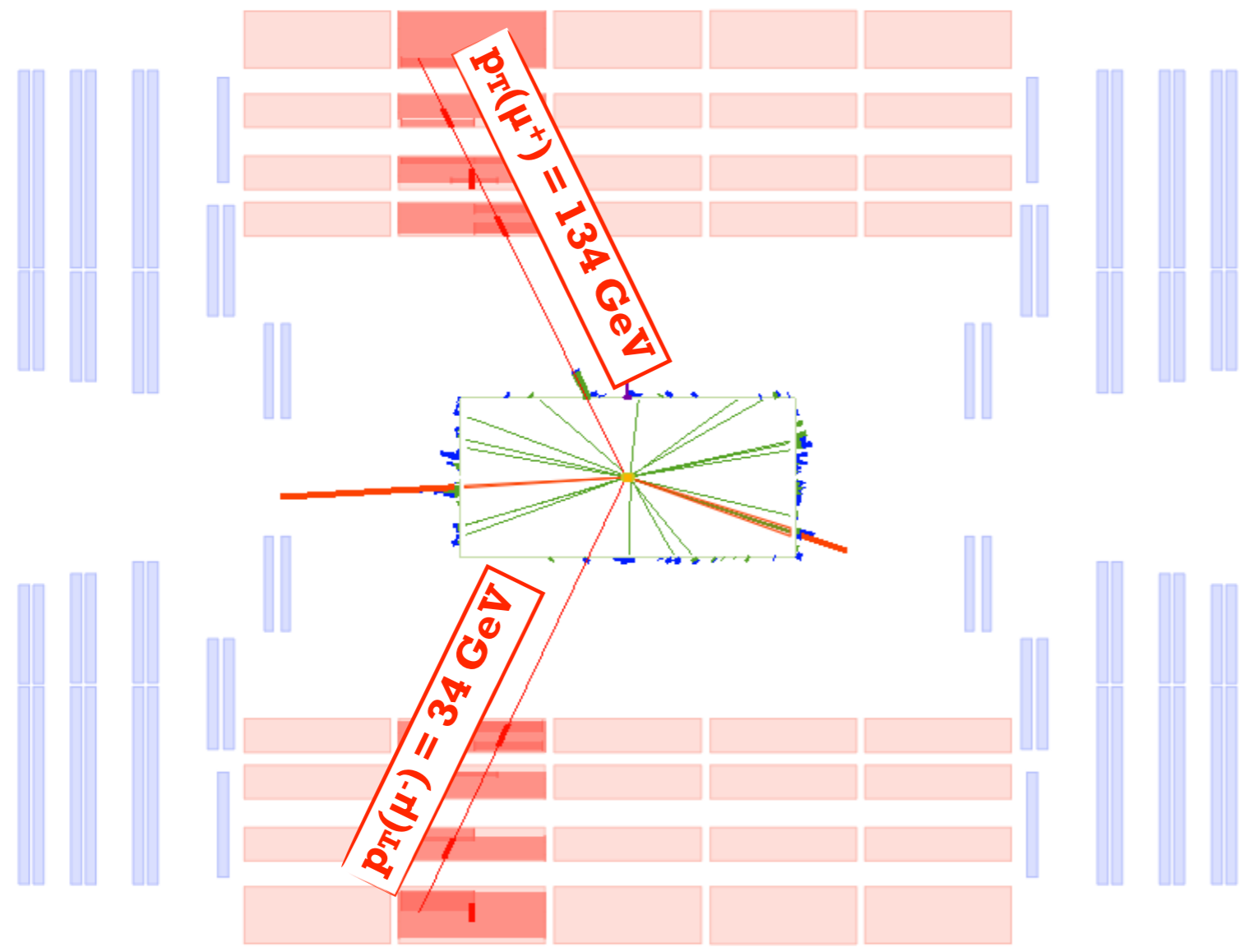
$$\mu = \frac{\sigma_H \cdot \text{BR}(H \rightarrow \mu\mu)}{\sigma_H \cdot \text{BR}(H \rightarrow \mu\mu)_{\text{SM}}} = 2.32^{+2.27}_{-1.95}$$

## $m_{\mu\mu}$ distribution in the highest purity ttH subcategories



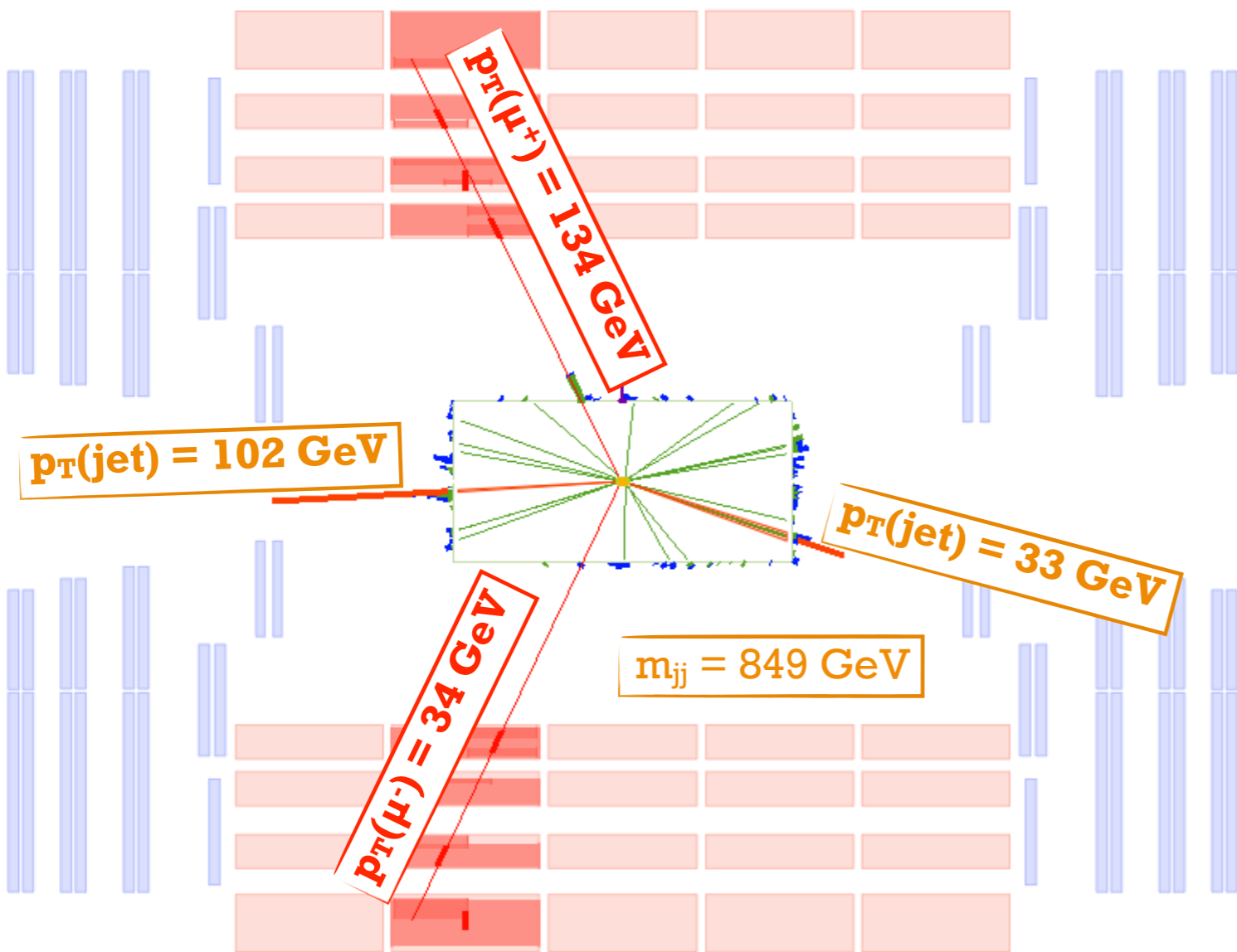
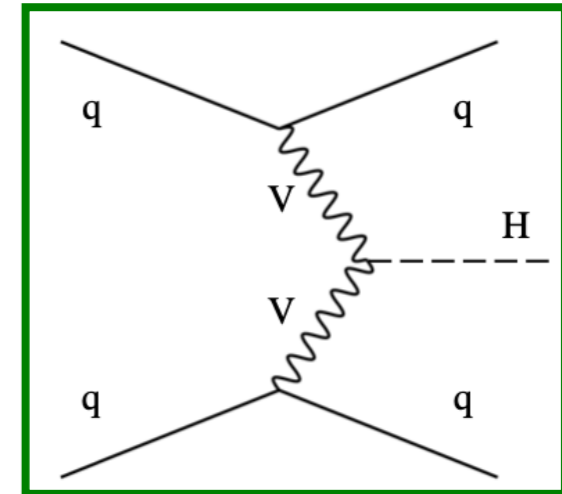


**H candidate**  
 $\mu^+\mu^-$  pair with  $110 < m_{\mu\mu} < 150$  GeV



**No additional leptons, no b jets.**

**H candidate**  
 $\mu^+\mu^-$  pair with  $110 < m_{\mu\mu} < 150$  GeV

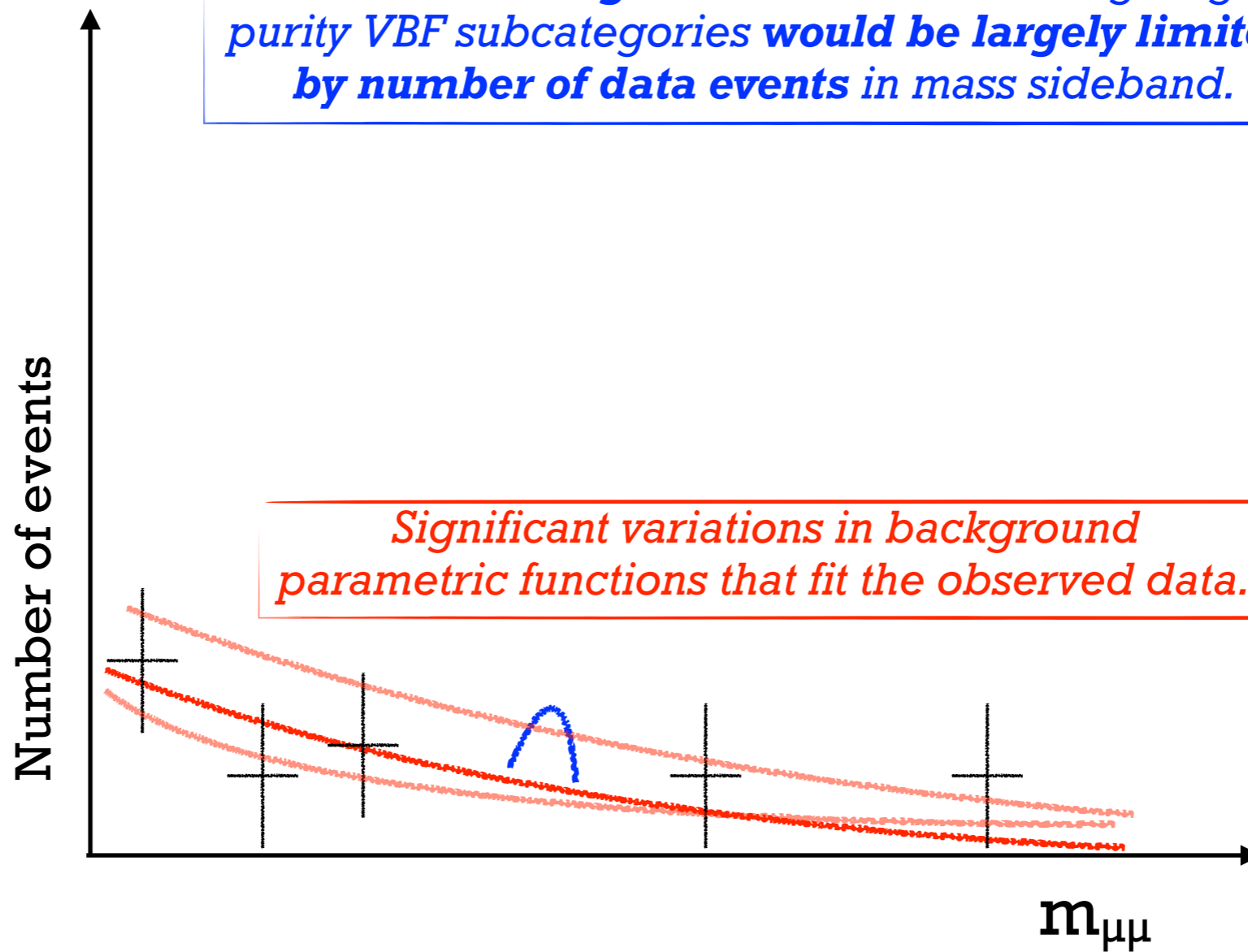


**VBF selections:**  
 At least two jets with  $p_T > 25$  GeV and  $|\eta| < 4.7$ ,  
 leading jet  $p_T > 35$  GeV,  
 $m_{jj} > 400$  GeV and  $|\Delta\eta(jj)| > 2.5$

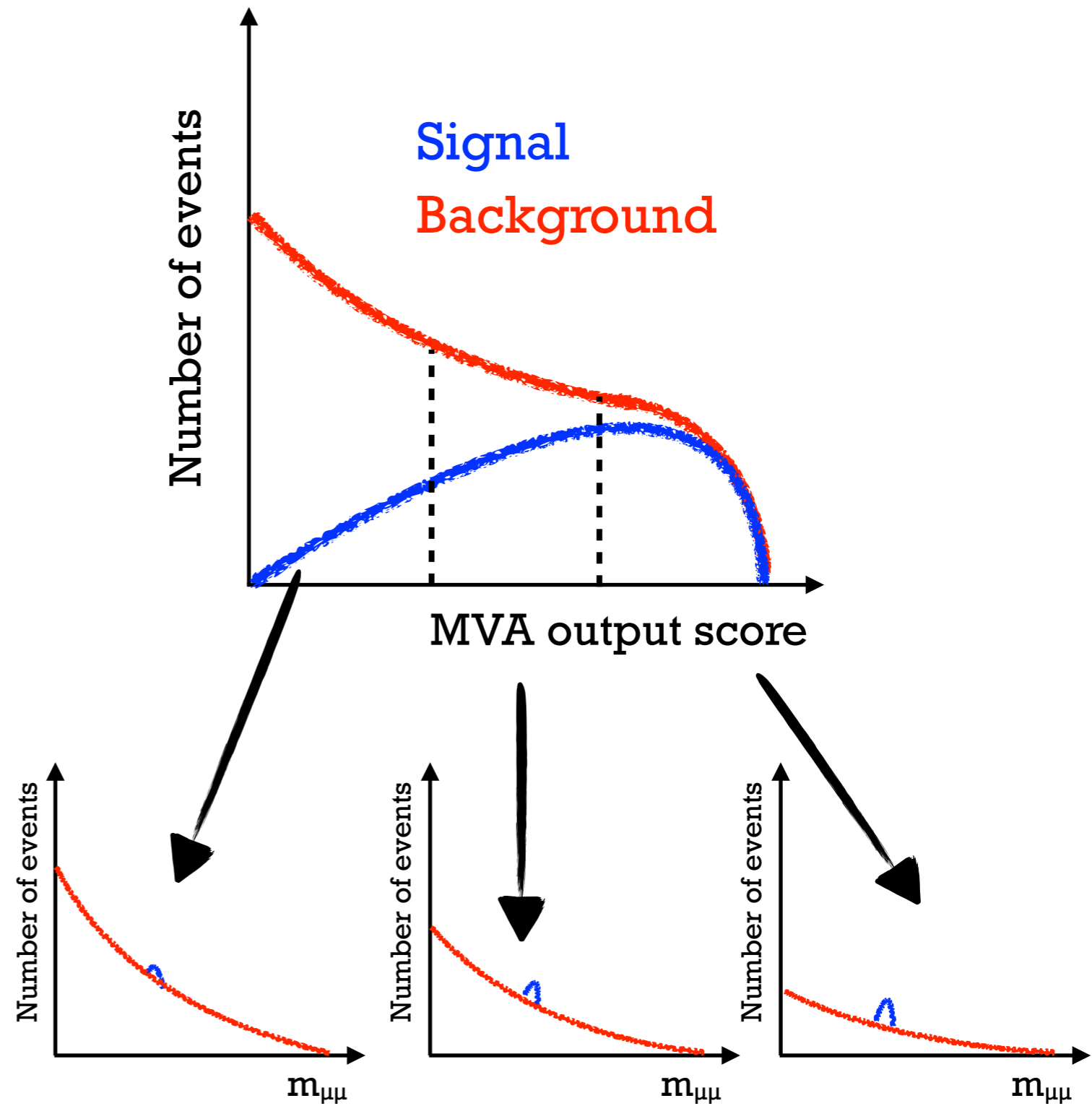
**Dominant backgrounds:**  
 Drell-Yan (DY), EW  $Z_{jj}$

**No additional leptons, no b jets.**

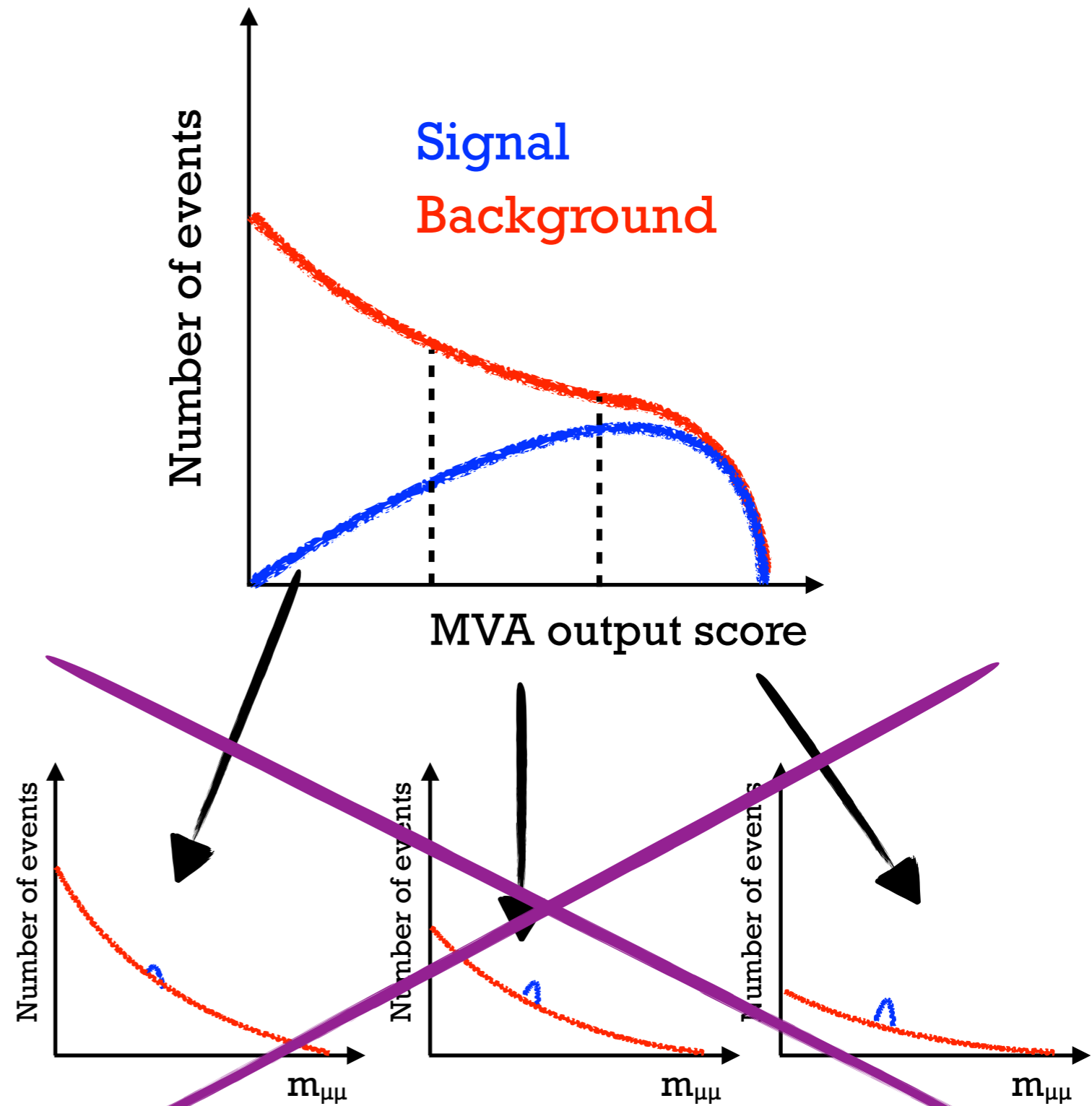
*Data-driven background estimation in high signal purity VBF subcategories would be largely limited by number of data events in mass sideband.*



(representation of high purity VBF subcategory)

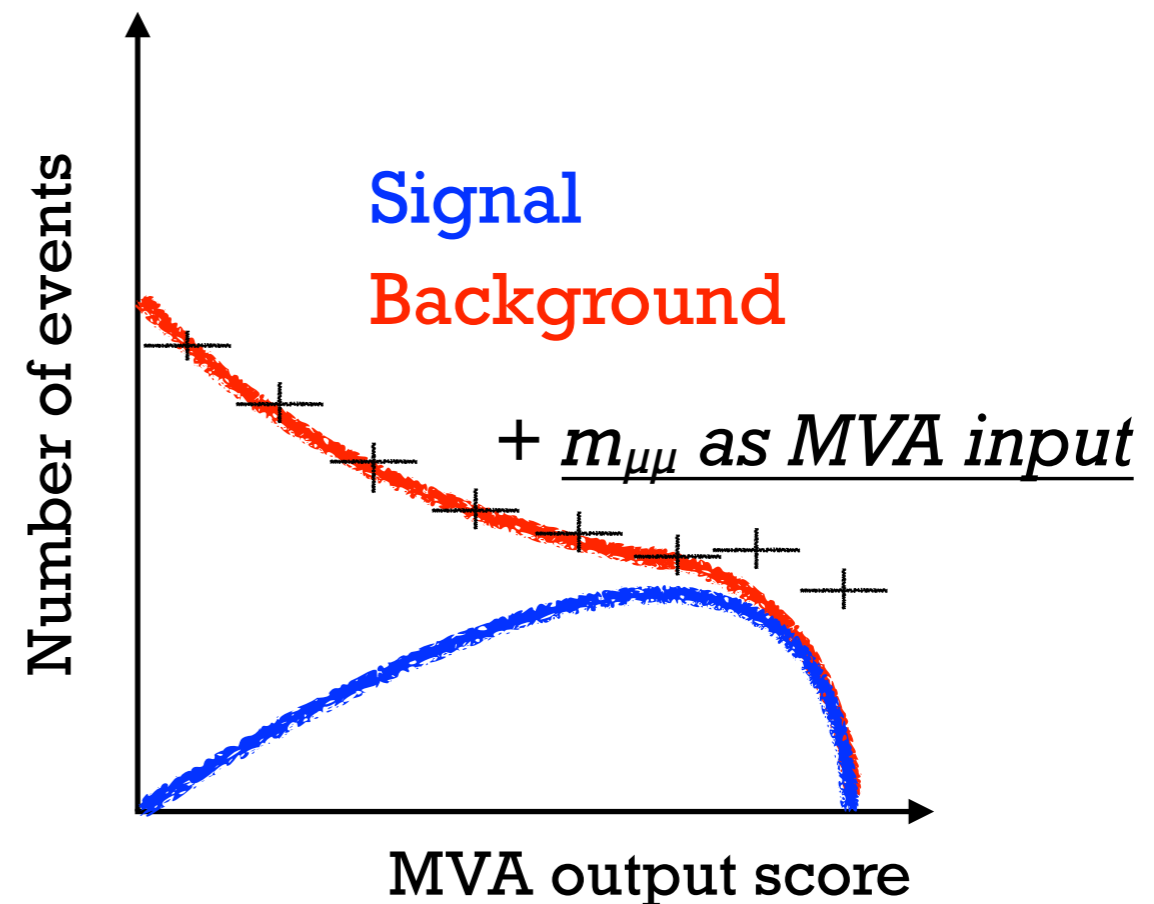


MVA subcategories with varying signal purity



MVA subcategories with varying signal purity

- *New approach for the VBF category:*
  - Include  $m_{\mu\mu}$  as **MVA input** variable.
  - **Fit MVA output directly** to extract  $H \rightarrow \mu\mu$  signal.
  - Take **background prediction from simulated samples**.
- Trading limited number of data events in mass sideband for systematic uncertainties in simulation.
- Following strategy similar to CMS EW  $Z_{jj}$  measurement [1] and  $H \rightarrow bb$  observation [2].



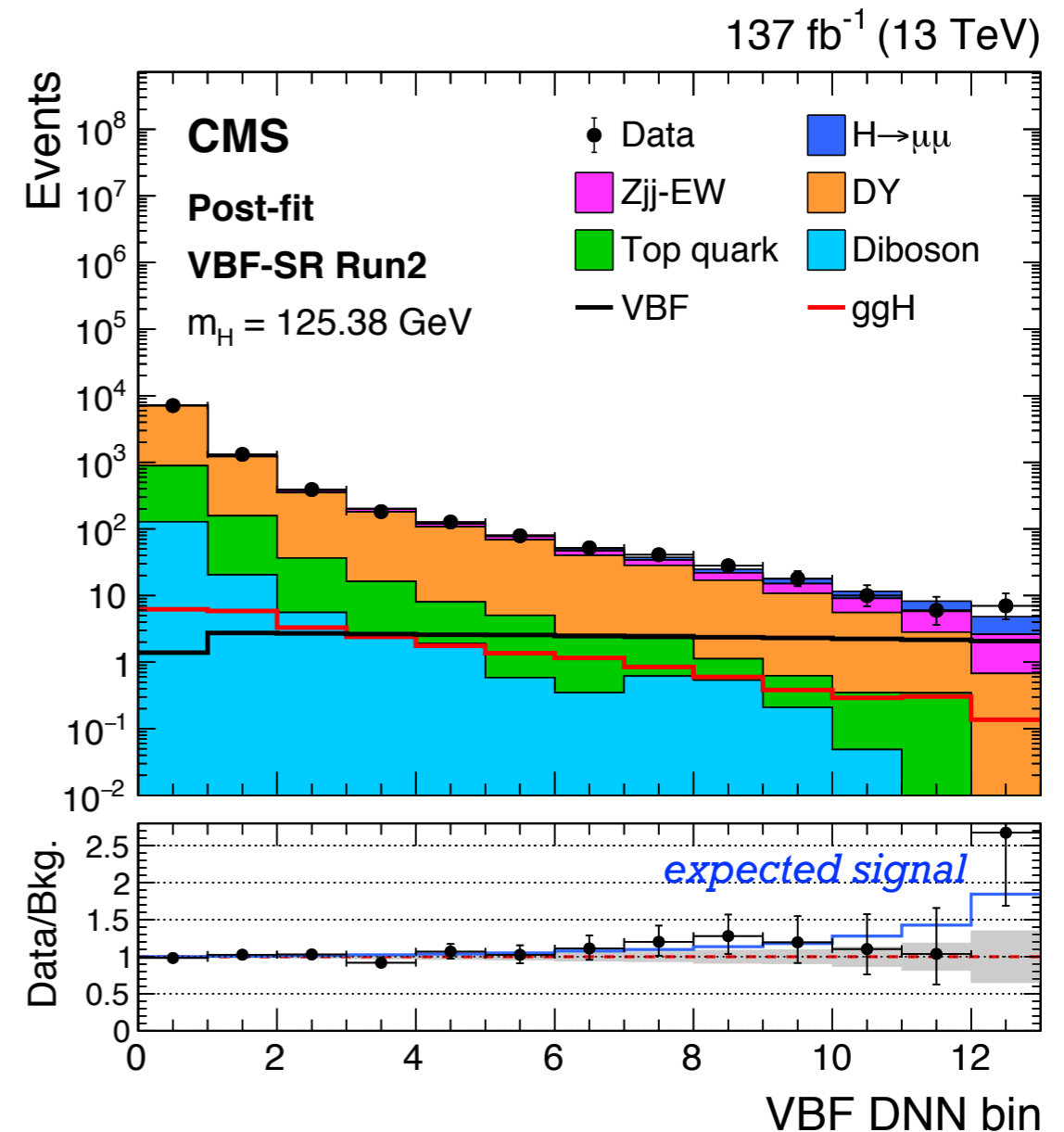
$\Rightarrow$  20% improvement in performance in VBF category

[1] [Eur. Phys. J. C 78 \(2018\) 589](#)

[2] [Phys. Rev. Lett. 121 \(2018\) 121801](#)

- Train a deep neural network (DNN) including the  $H$  candidate mass  $m_{\mu\mu}$  as an input.
- DNN inputs targeting VBF  $H$  signal:
  - $m_{jj}$ ,  $\Delta\eta(jj)$ ,  $\Delta\phi(jj)$ ,  $\min\text{-}\Delta\eta(H,j)$ ,  $\min\text{-}\Delta\phi(H,j)$ ,  $p_T\text{-balance}(H,jj)$ ,  $H$  centrality, ...
  - Suppressed hadronic activity in jet rapidity gap expected for VBF signal  $\Rightarrow$  track-jet multiplicity and  $H_T$  in jet rapidity gap.

*VBF category DNN score in signal region*

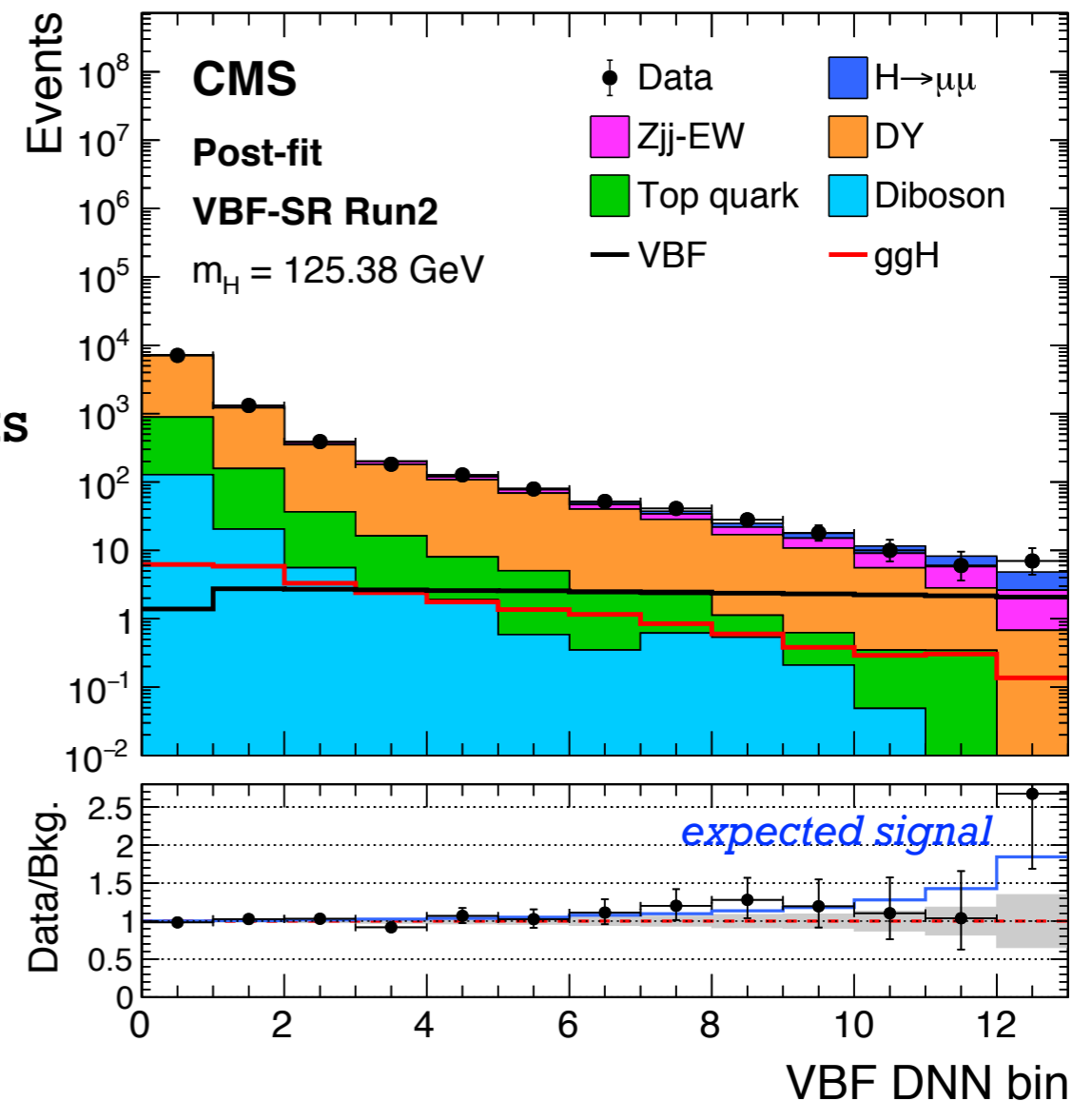


*Total systematic uncertainty impact <5%*

*VBF category DNN score in signal region*

137 fb<sup>-1</sup> (13 TeV)

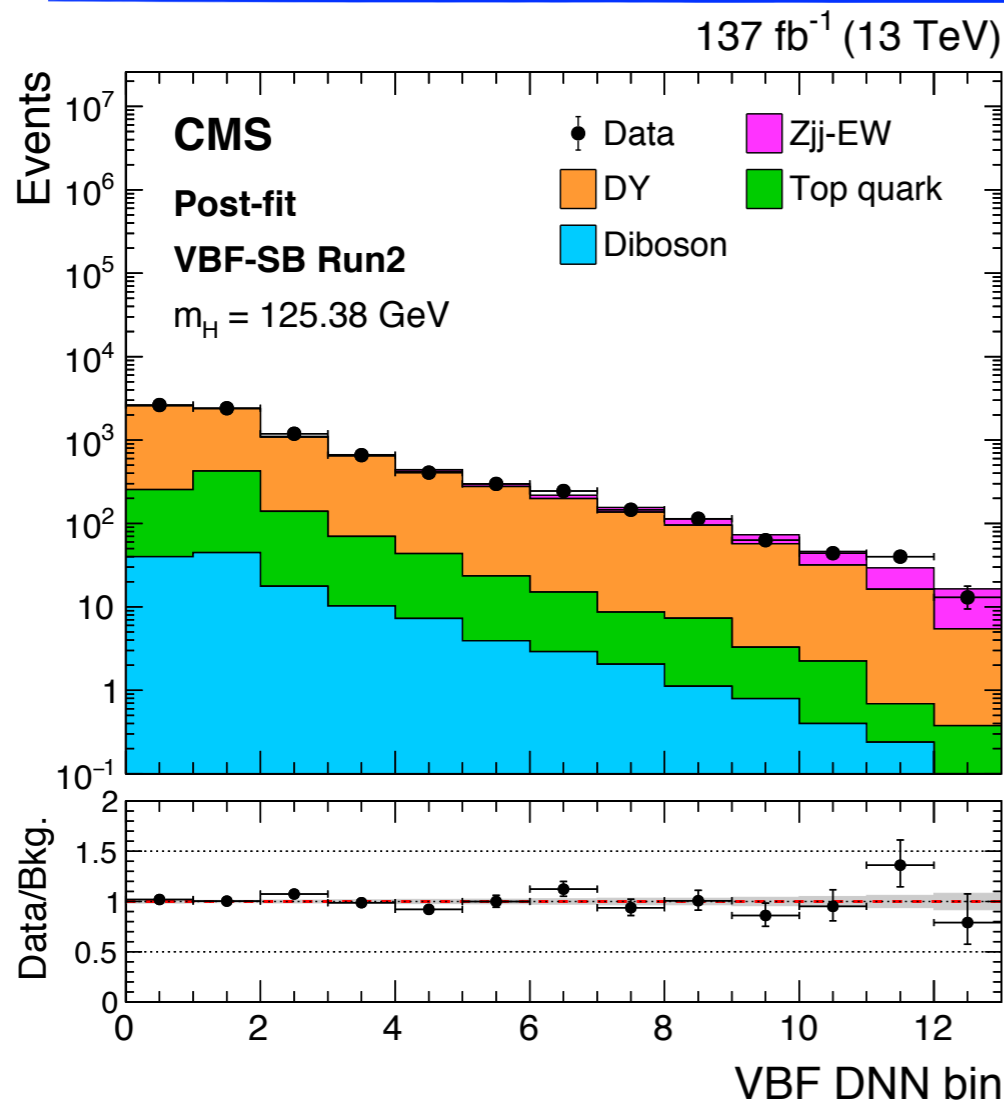
- **Largest systematic uncertainties:**
  - VBF (H signal and Z background) parton shower modeling
  - Jet energy scale and resolution
  - DY contribution with one or more pileup jets
  - Statistical precision of simulated events
  - Theory uncertainties: missing higher order corrections, etc.



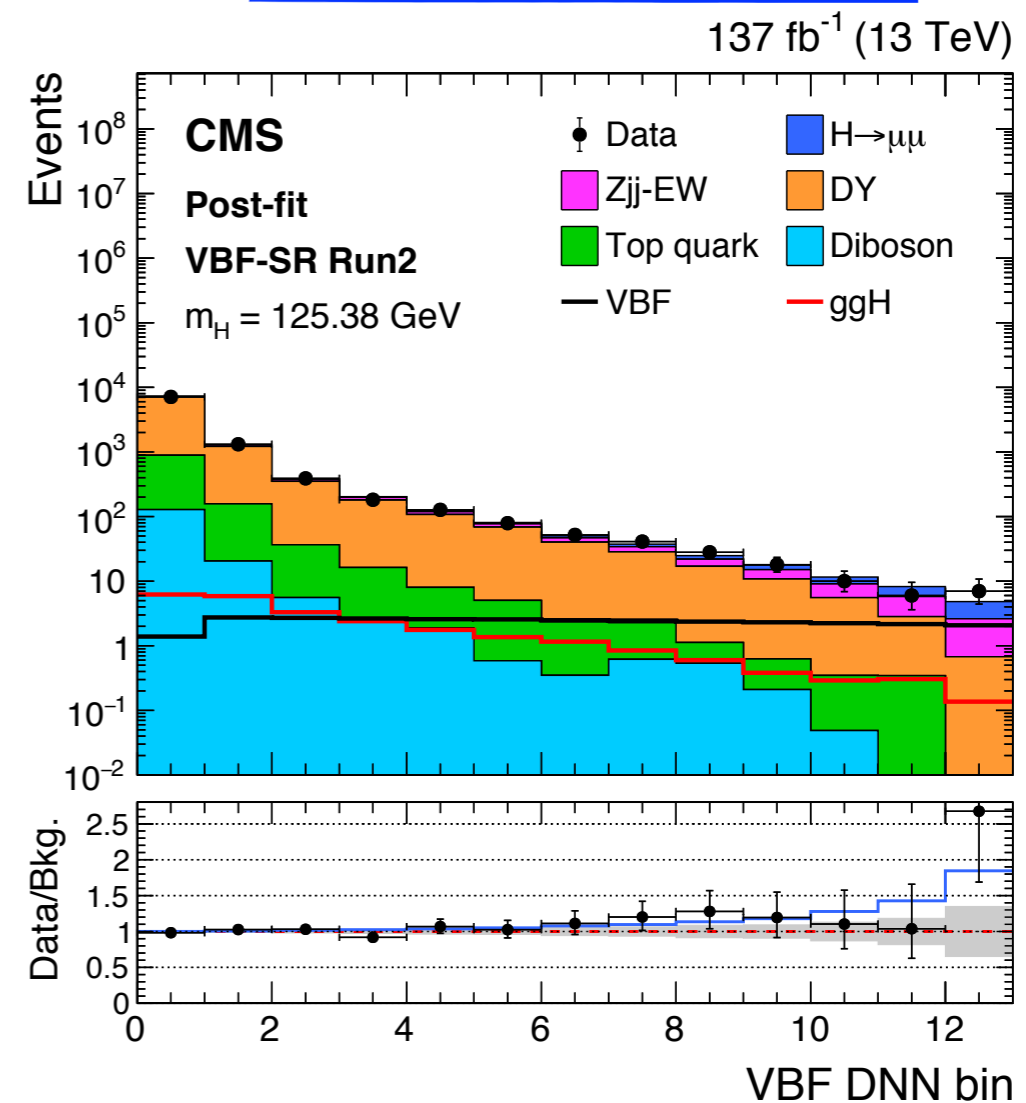


- Binned maximum-likelihood fit to DNN score simultaneously in the *signal region* and the *mass sideband region* to better constrain uncertainties.

Mass sideband region:  
 $m_{\mu\mu}$  in  $[105, 115] + [135, 150]$  GeV



Signal region:  
 $115 < m_{\mu\mu} < 135$  GeV



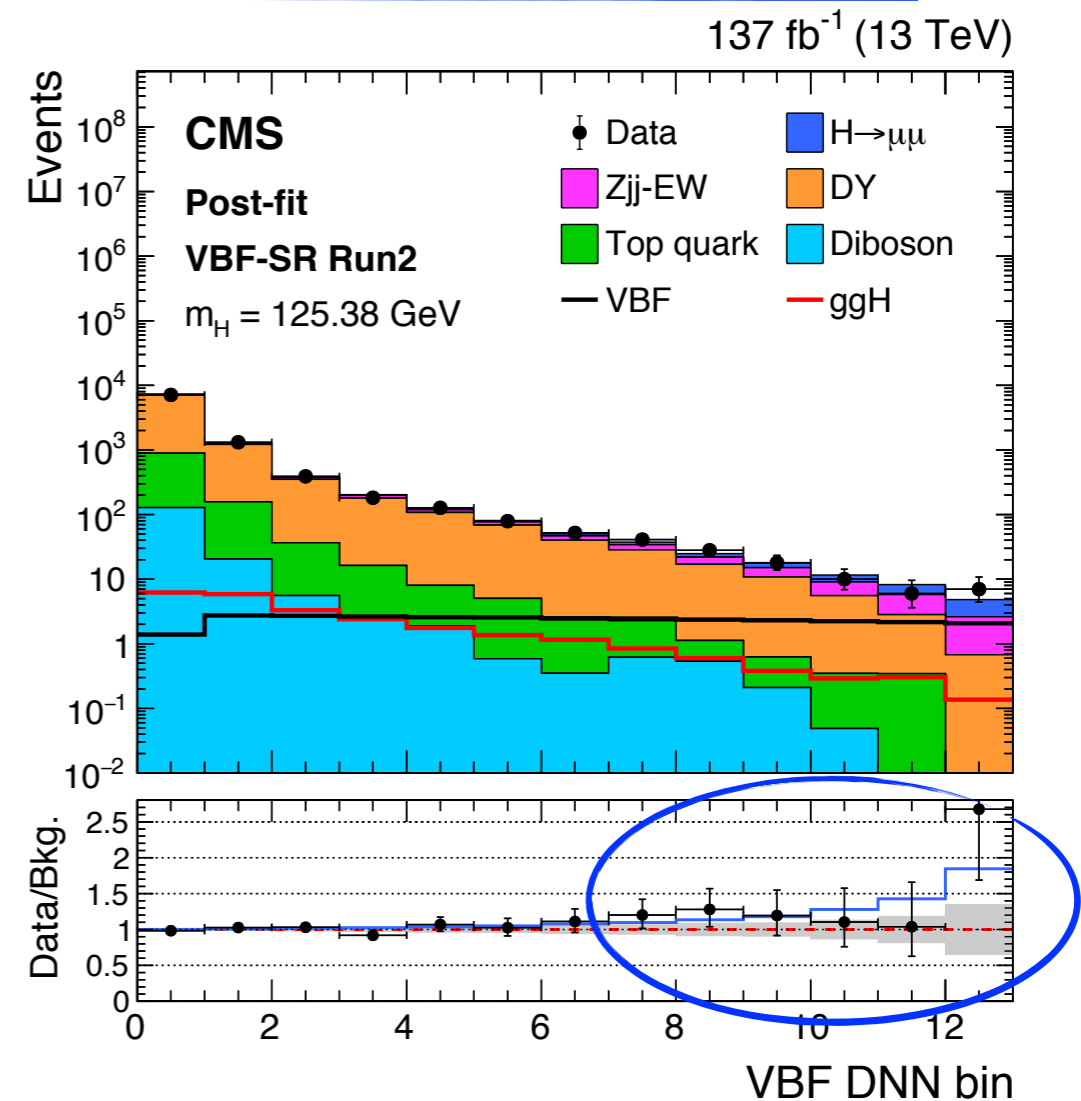
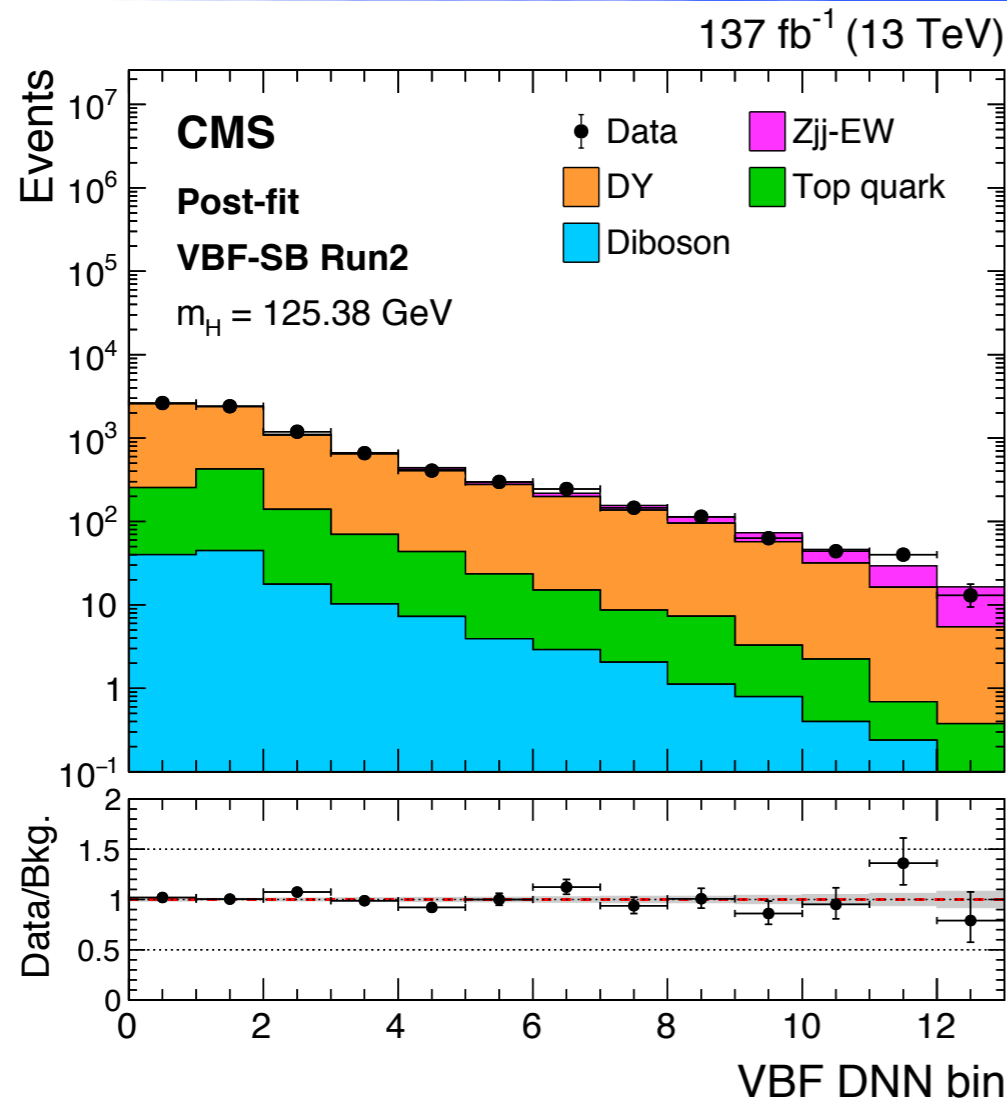
***VBF category result***

Observed (expected) significance:  $2.4\sigma$  ( $1.8\sigma$ )

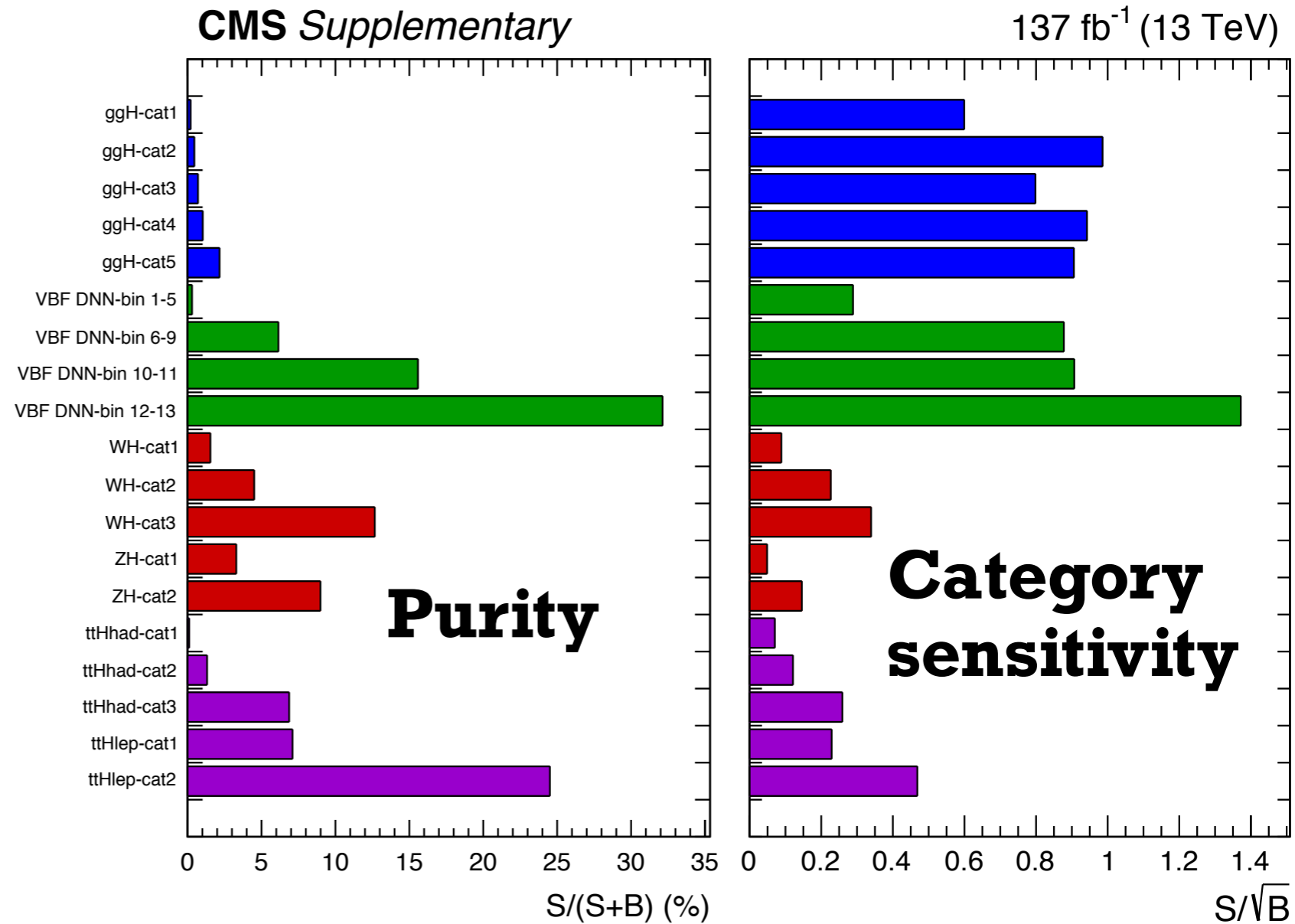
$$\mu = \frac{\sigma_H \cdot \text{BR}(H \rightarrow \mu\mu)}{\sigma_H \cdot \text{BR}(H \rightarrow \mu\mu)_{\text{SM}}} = 1.36^{+0.69}_{-0.61}$$

Mass sideband region:  
 $m_{\mu\mu}$  in  $[105, 115] + [135, 150]$  GeV

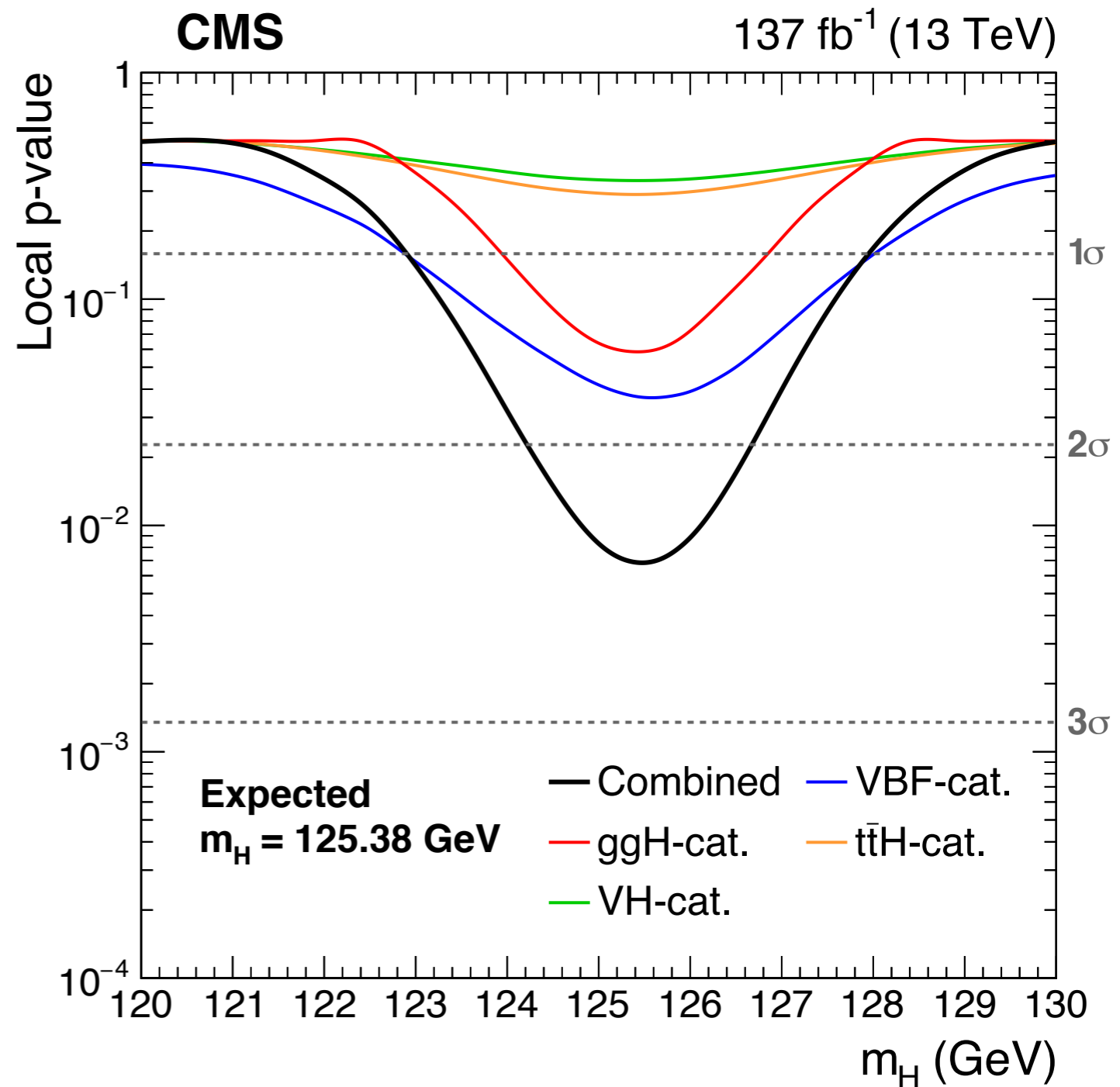
Signal region:  
 $115 < m_{\mu\mu} < 135$  GeV



- Sensitivity of each category is a balance between purity and signal yield.
- ggH and VBF category sensitivities are comparable, with VBF slightly better.
- ttH and VH categories are strongly limited by small signal yield.

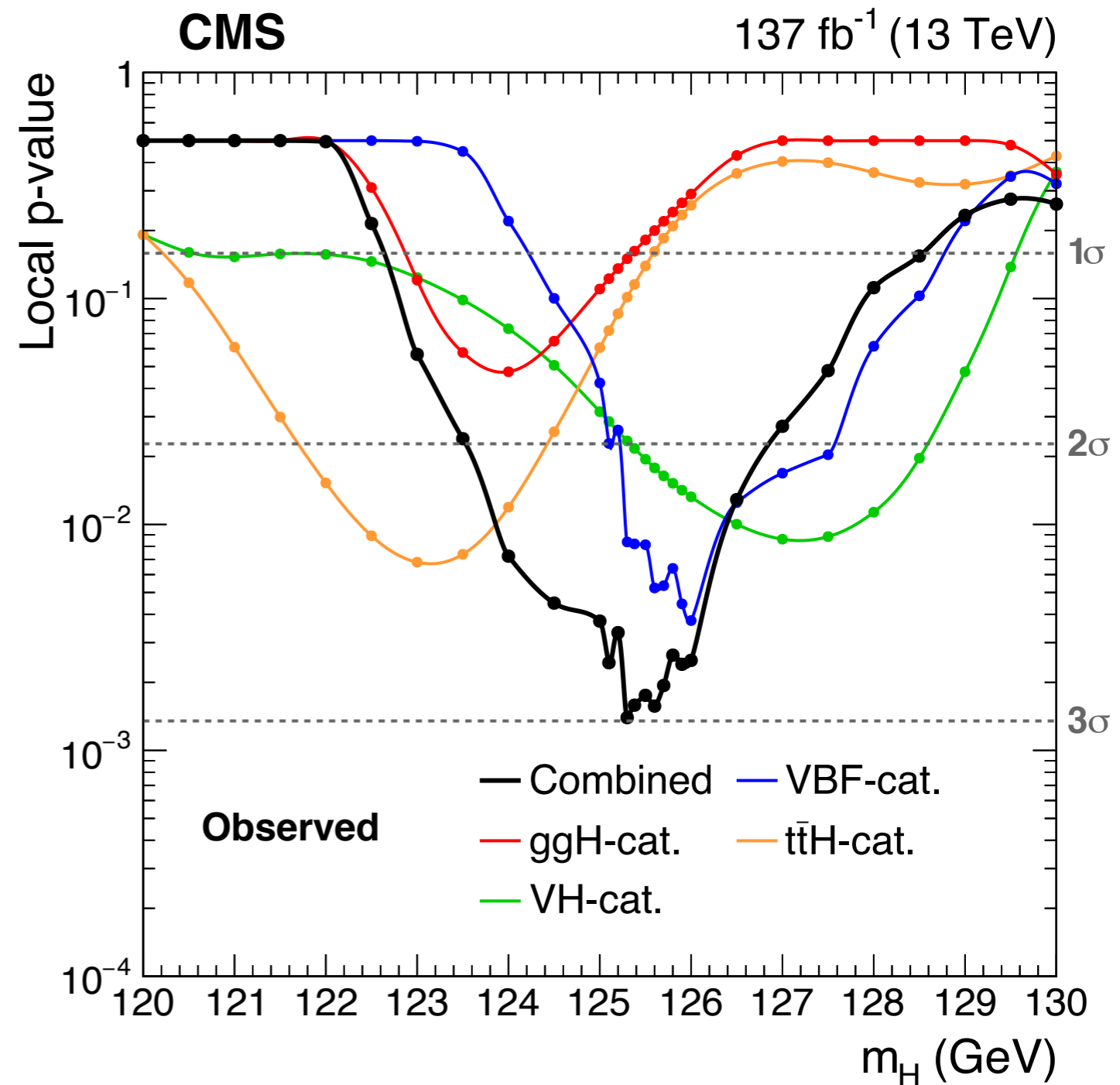


- Simultaneous fit of all categories to extract combined  $H \rightarrow \mu\mu$  signal.
- *VBF category* has the best expected sensitivity, followed by the *ggH category*.



Expected ( $m_H = 125.38$  GeV)  
combined significance:  $2.5\sigma$

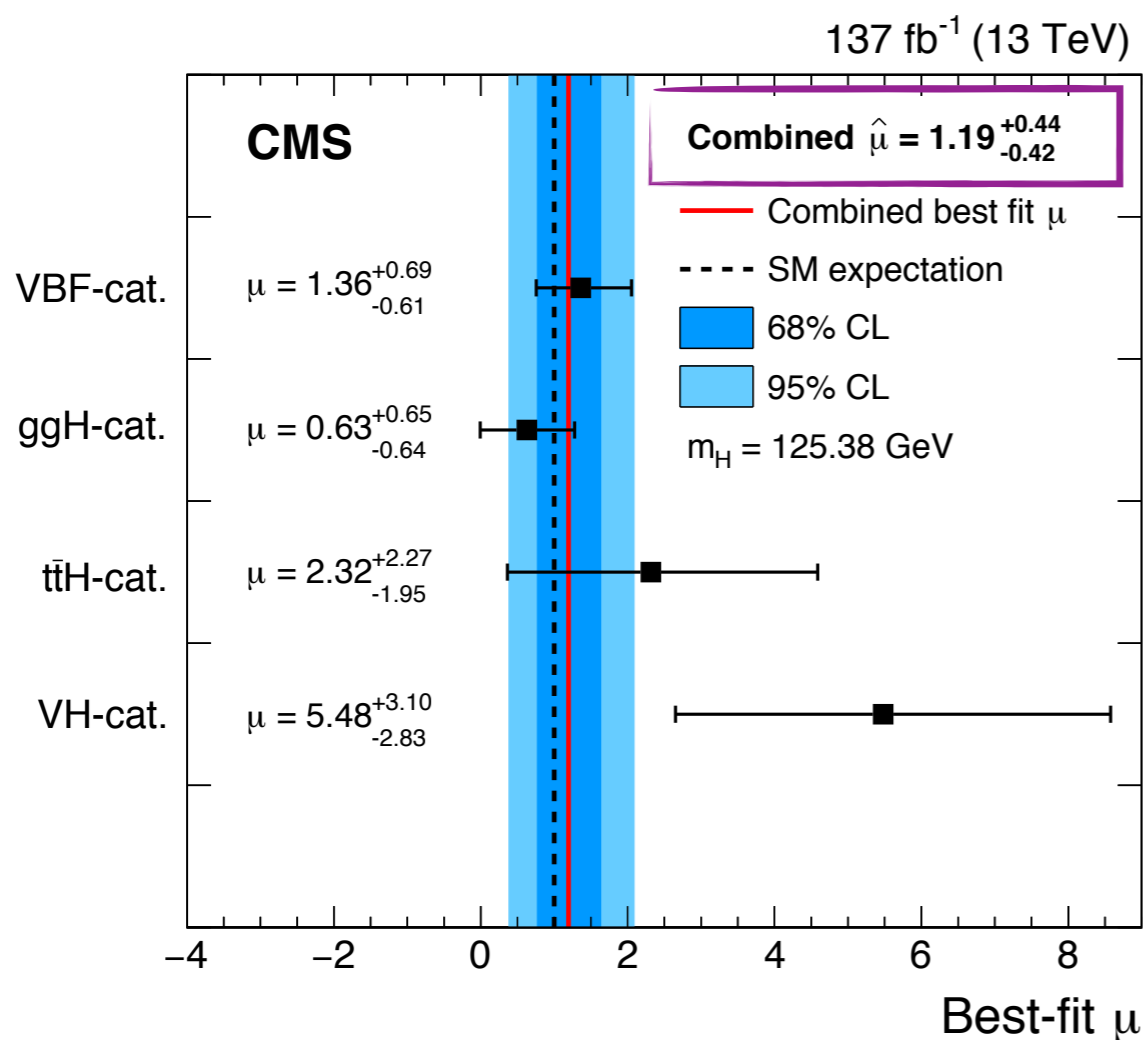
- Excess over background-only prediction observed at  $m_H = 125.38$  GeV with a statistical significance of  $3.0\sigma$ .
- *This constitutes the first evidence for the  $H \rightarrow \mu\mu$  decay.*
- Fluctuations in the observed p-value arising from discrete nature of the mass profiling in the VBF category.



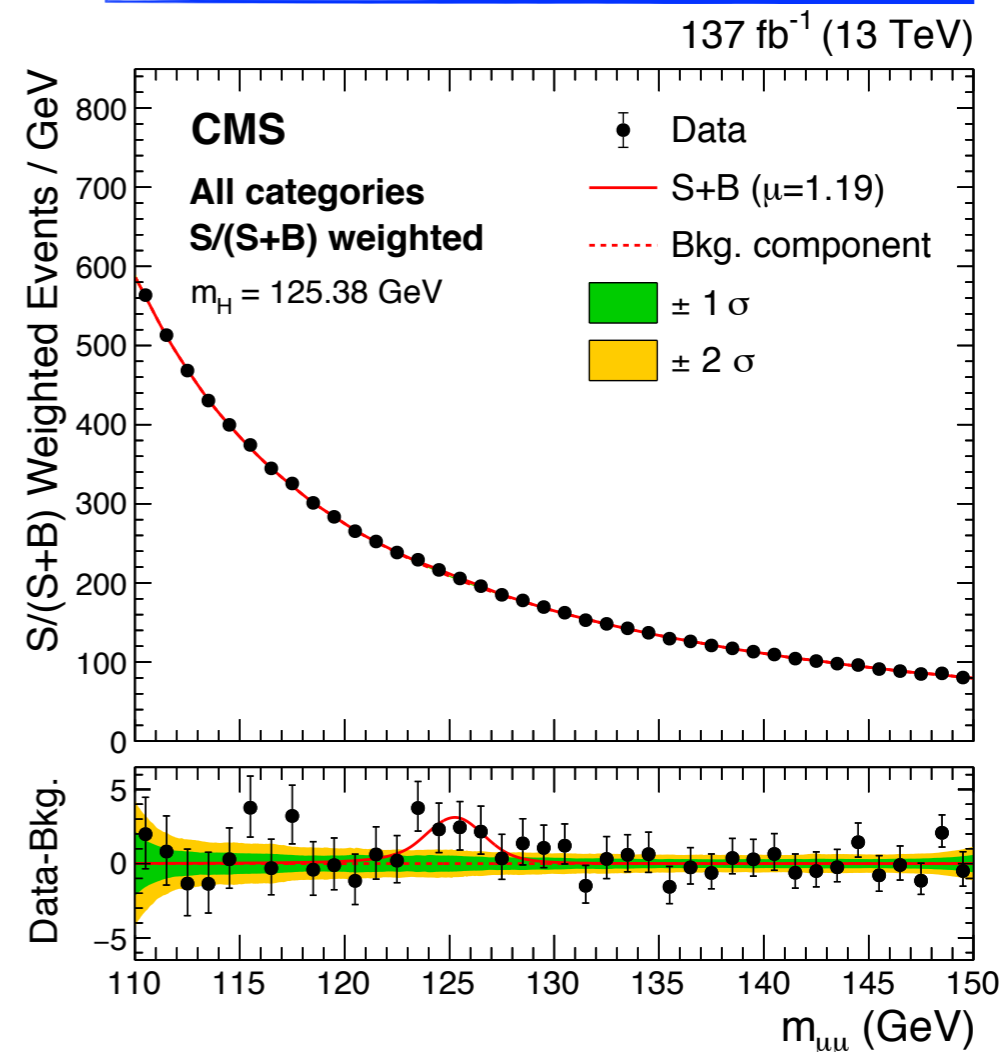
**Observed ( $m_H = 125.38$  GeV)  
combined significance:  $3.0\sigma$**

- *The observed signal is well compatible, within uncertainties, with the SM expectation for the Higgs boson interaction with the muon.*
- Dominant uncertainties are statistical  $\Rightarrow$  with more data, we will more precisely test this interaction.

Signal strength per category



Visualization of the observed excess vs.  $m_{\mu\mu}$



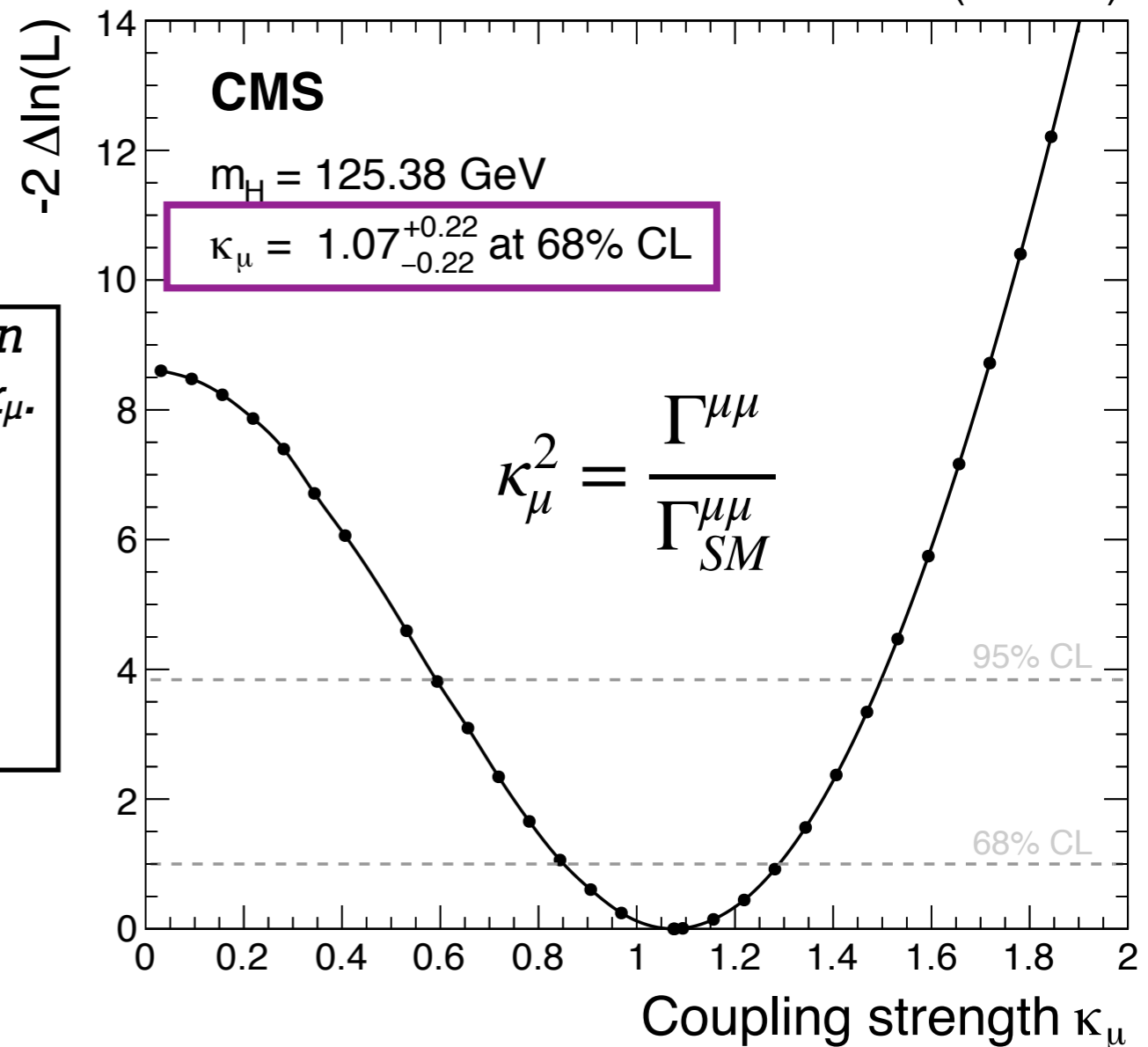
Direct access to H- $\mu$  interaction

$$\mu = \sigma_H \cdot \text{BR}(H \rightarrow \mu\mu)$$

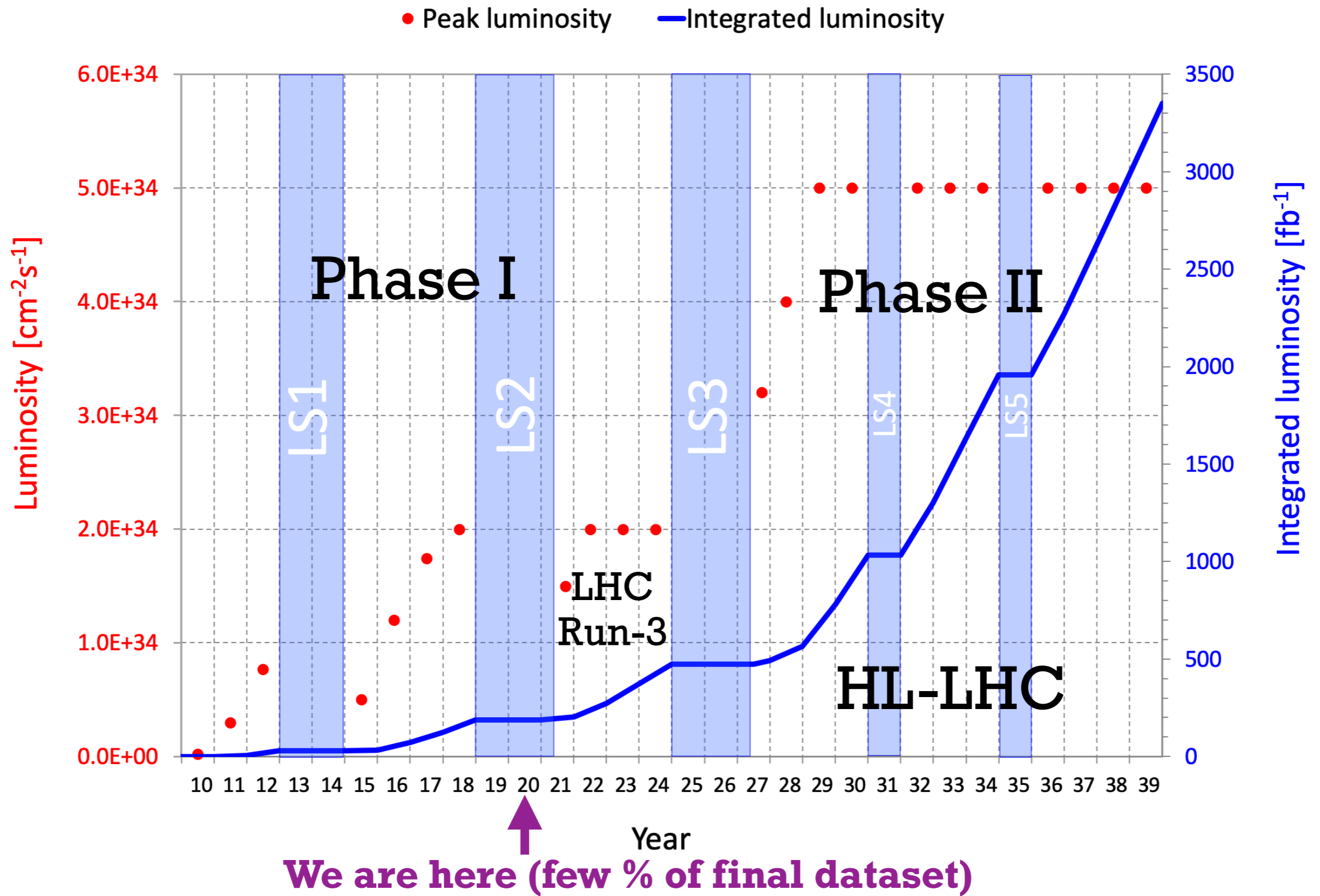
Depends on Higgs boson interaction strength with t, W, Z, ...

*H- $\mu$  coupling strength from combination with measurements of other Higgs channels (EPJC 79 (2019) 421)*

35.9-137 fb<sup>-1</sup> (13 TeV)



- *Combine with other Higgs channels to obtain direct constraints on H- $\mu$  coupling strength  $\kappa_\mu$ .*
- *Coupling strength of Higgs boson to muon measured with nearly 20% precision at 68% confidence level.*





[CMS-PAS-FTR-18-011](#)

(based on previous  $H \rightarrow \mu\mu$  published analysis)

300 fb<sup>-1</sup> (13 TeV)

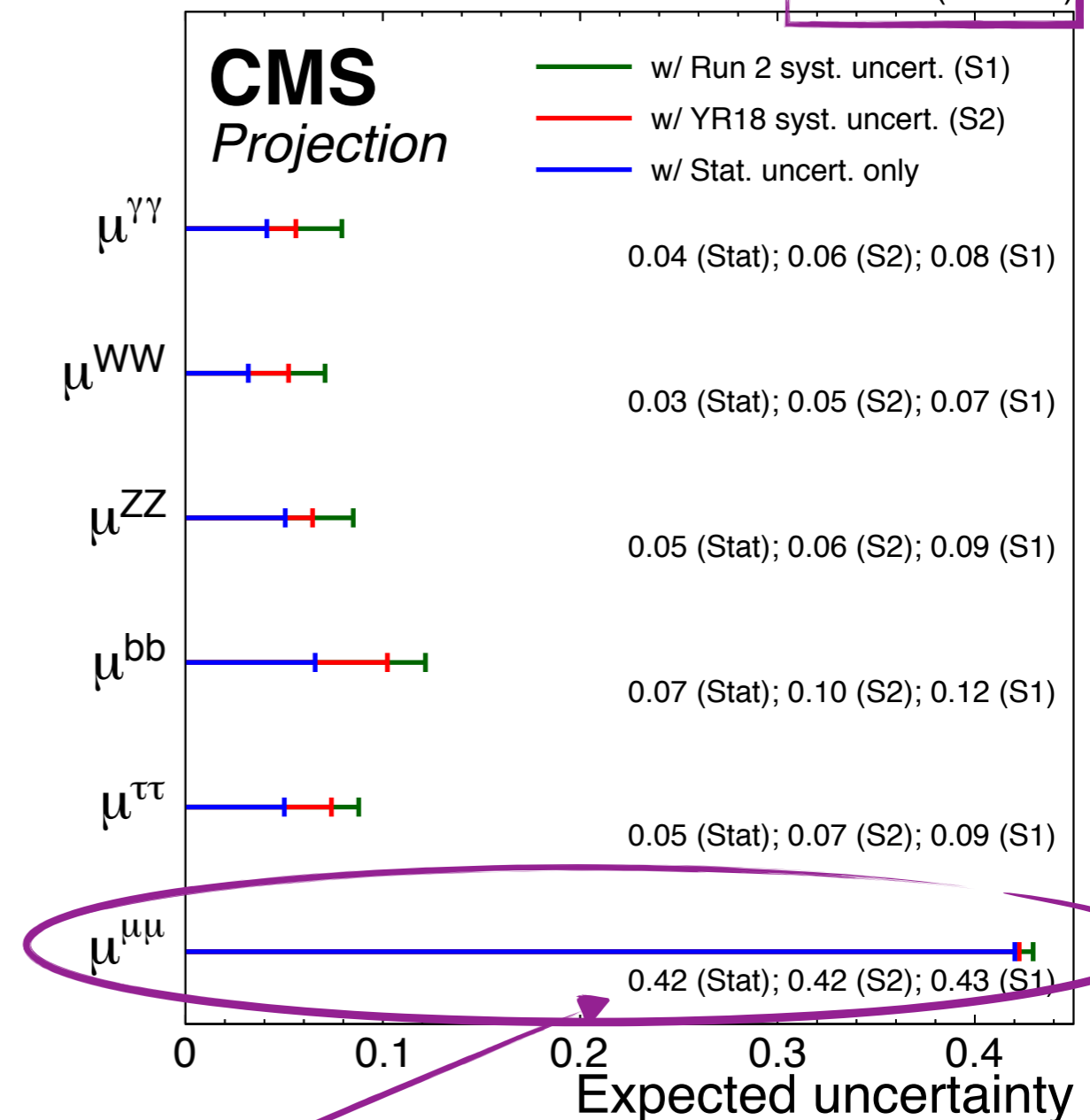
- CMS has released projections of expected precision of Higgs measurements up to end of HL-LHC.

- Including  $H \rightarrow \mu\mu$ , based on projections from previous CMS  $H \rightarrow \mu\mu$  publication [1].

- *The future is hard to predict!*

- Cannot extrapolate ingenuity, new ideas, new methods, precise performance and usage of new technologies, etc.

- So please keep this in mind...



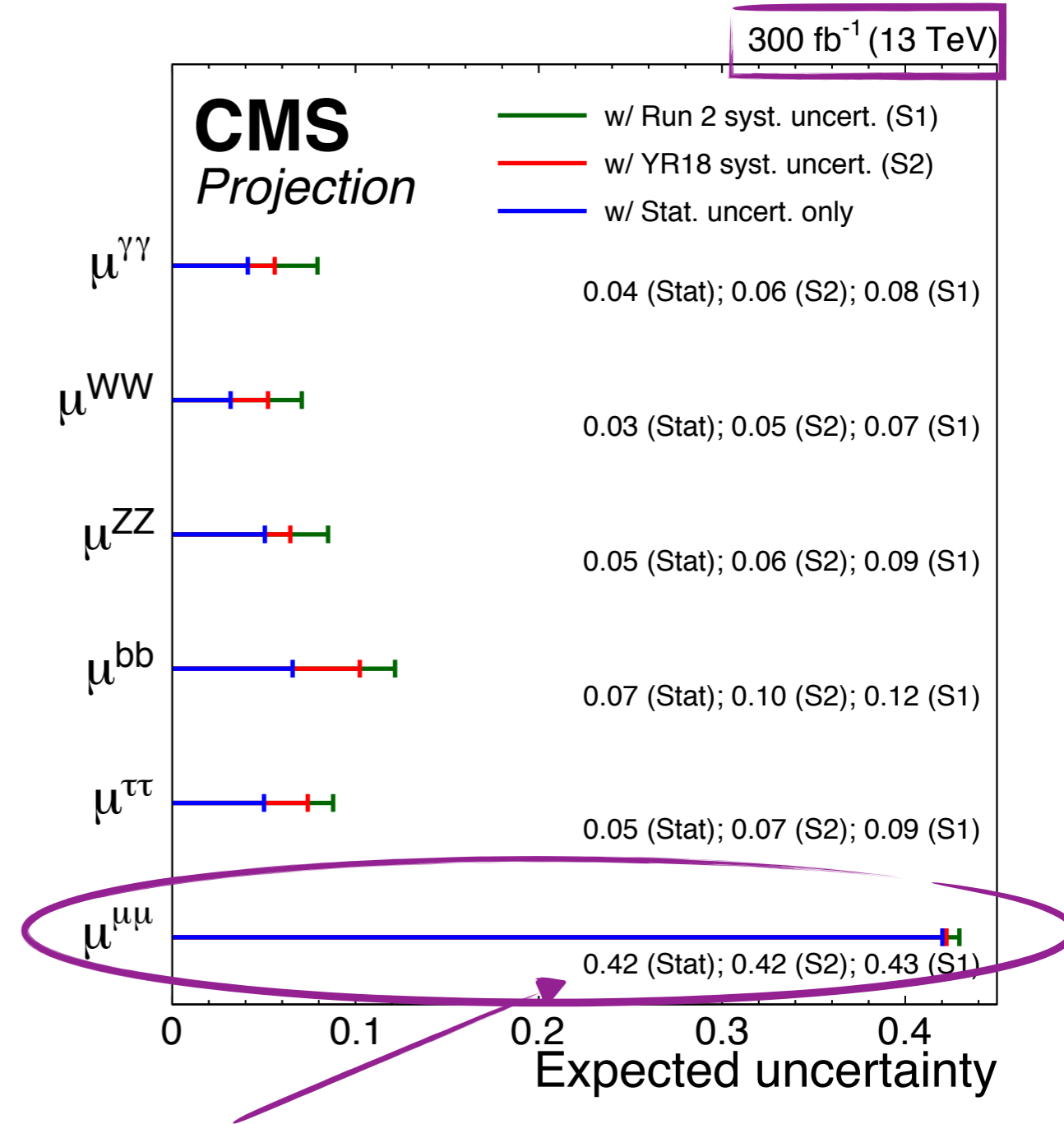
**We are already here with 137 fb<sup>-1</sup> !**

[1] [Phys. Rev. Lett. 122 \(2019\) 021801](#)

- LHC Run-3 (2022-2024) expected to deliver about 200 fb<sup>-1</sup> of 13 or 14 TeV data.
- Data conditions similar to those at end of Run-2.
- Some small upgrades to CMS detector, but similar performance expected overall.
- Assuming no significant improvements to the analysis, expect *roughly 4σ* sensitivity to H → μμ including Run-3 data.

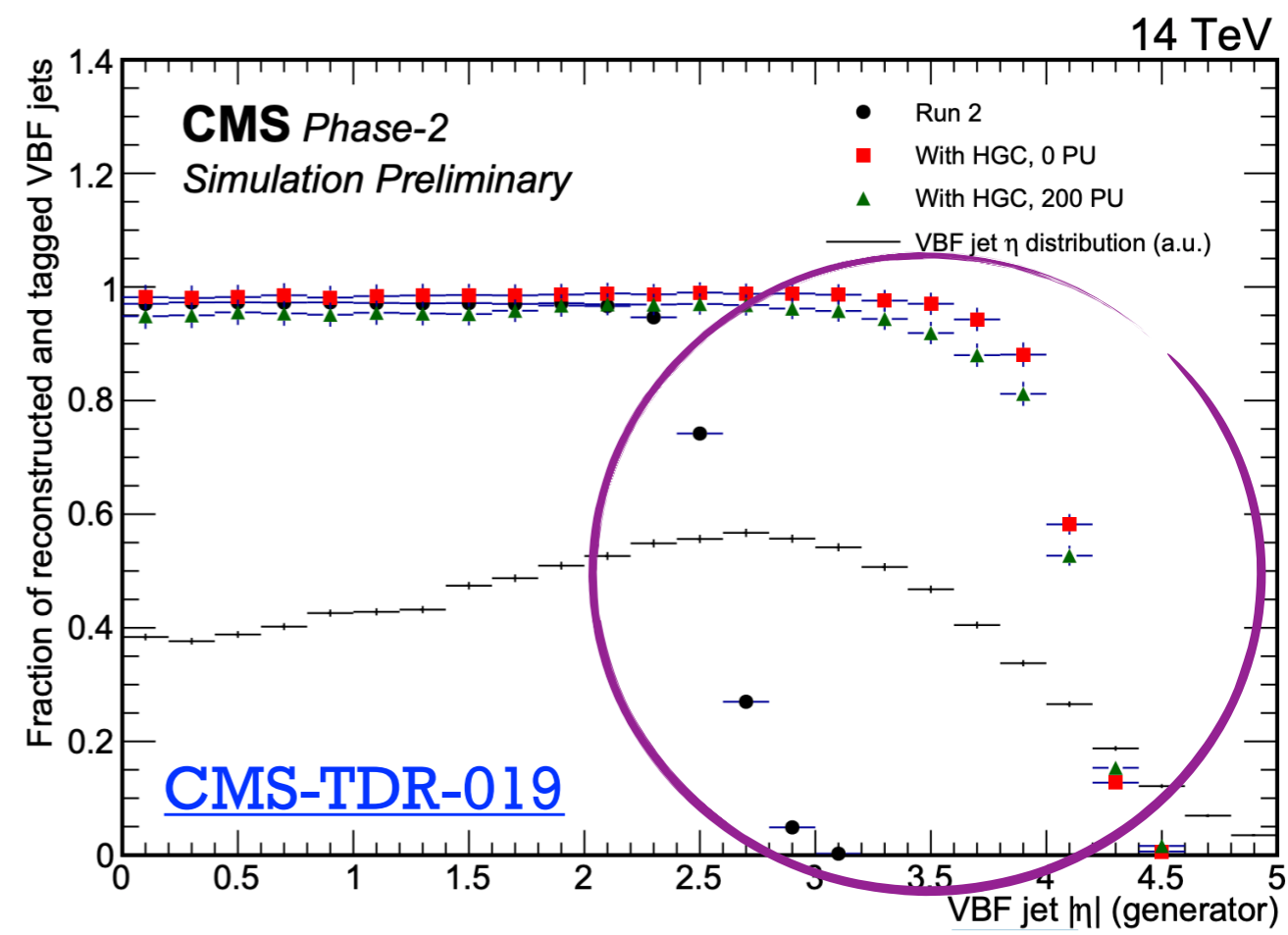
[CMS-PAS-FTR-18-011](#)

(based on previous H → μμ published analysis)



**We are already here with 137 fb<sup>-1</sup> !**

- CMS detector will largely be fully redesigned, improved.
- Tracking coverage extended in  $\eta$  from 2.4 to 4.0.
- High-granularity forward calorimetry with improved resolution.
- Improved muon resolution and efficiency,  $\eta(\mu)$  extended from 2.4 to 2.8.



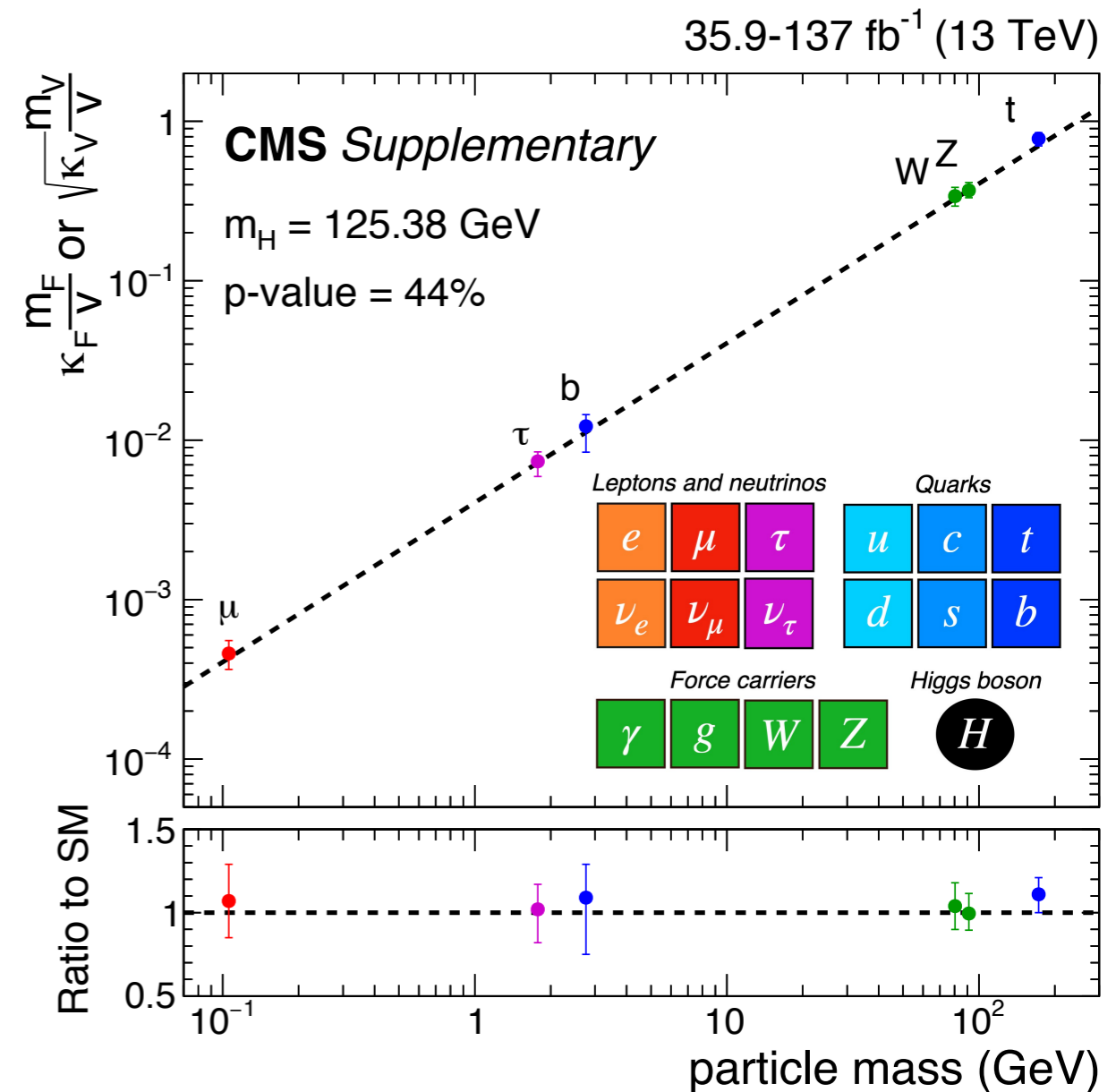
- Currently projecting  $\sim 10\%$  uncertainty on  $H \rightarrow \mu\mu$ , i.e.  $\sim 5\%$  precision on  $\kappa_\mu$ .
- Note that projection only considers increased dataset and improved mass resolution.

### Projections: 3 ab<sup>-1</sup> of HL-LHC data

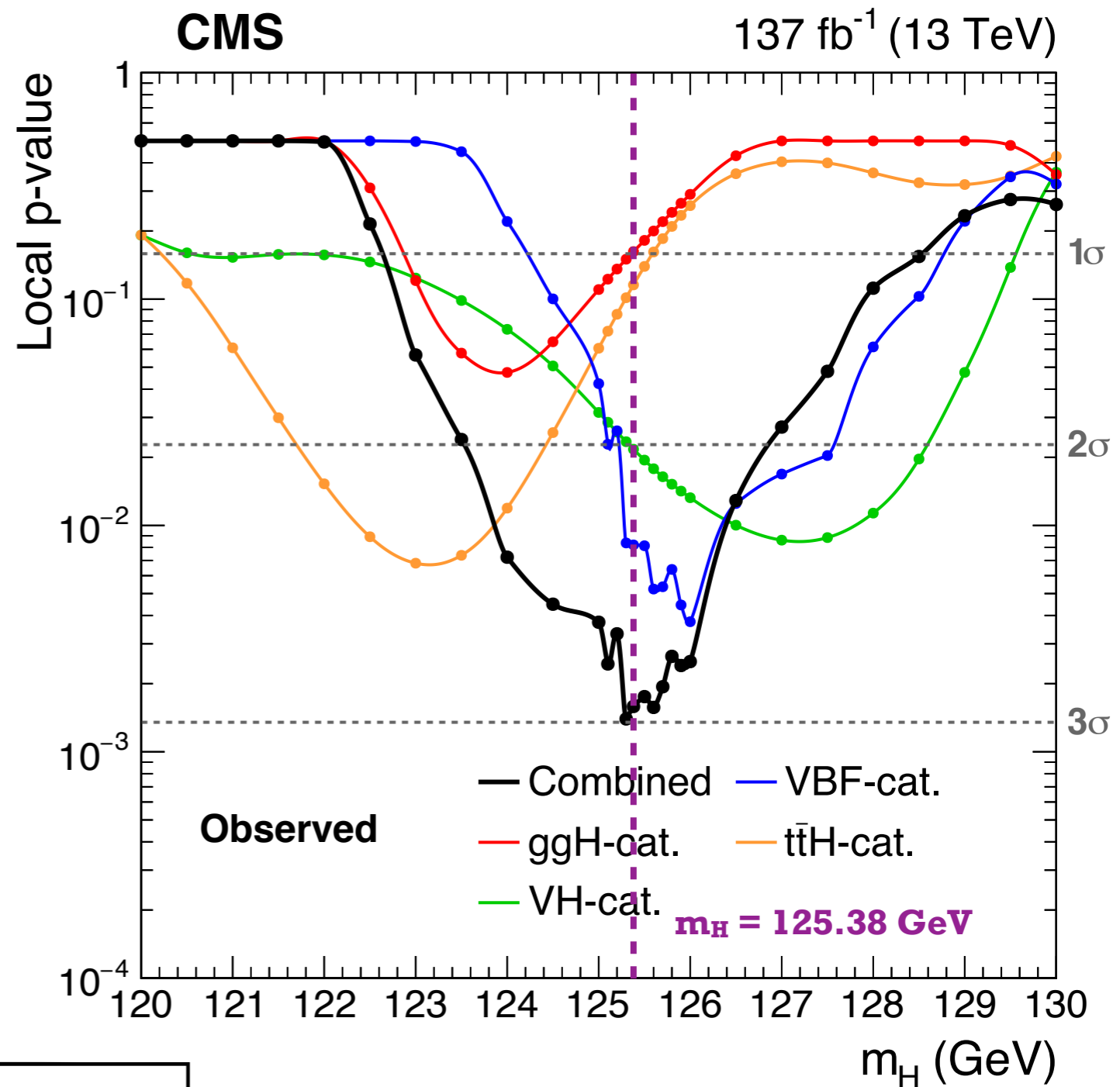
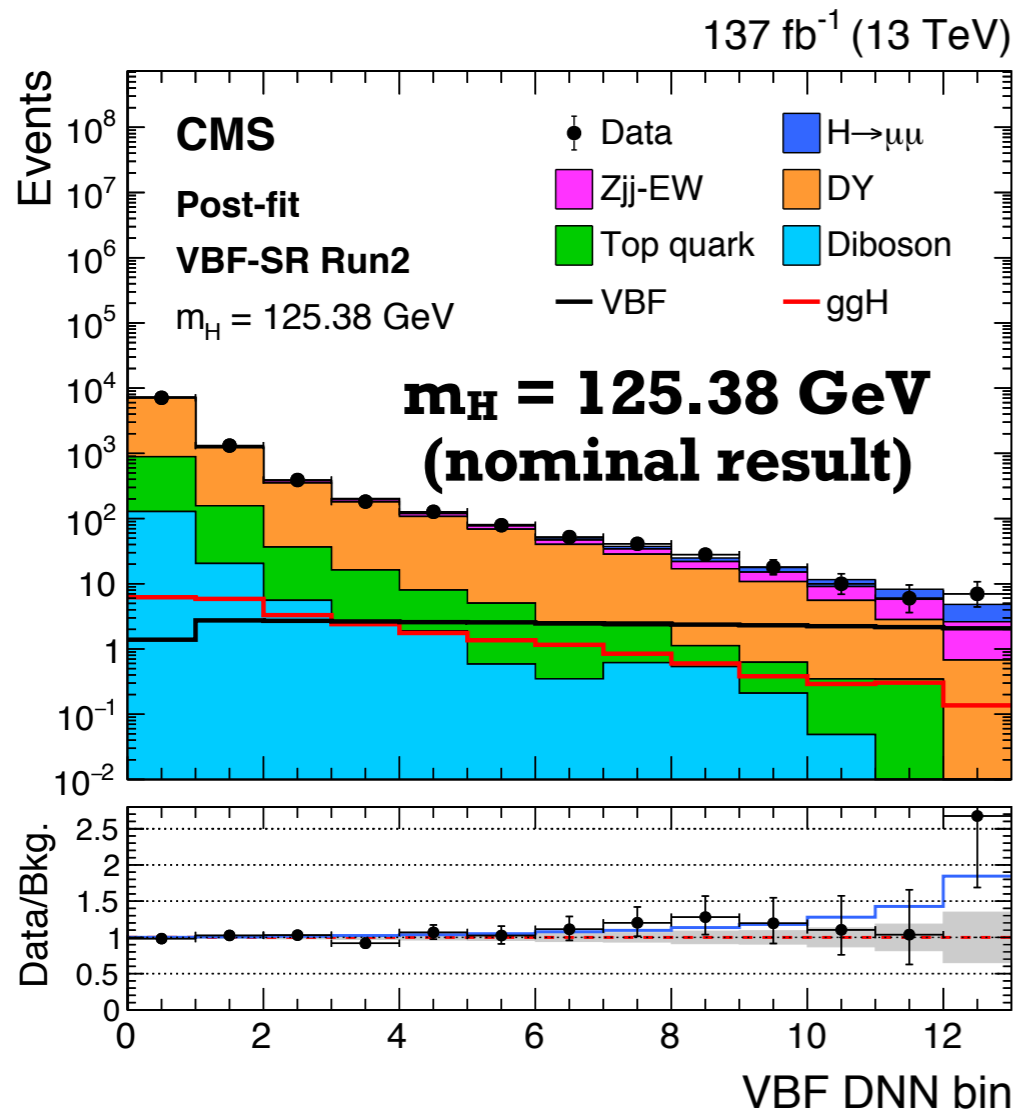
Experiment	CMS	
Process	Combination	
Scenario	S1	S2
Total uncertainty	13%	10%
Statistical uncert.	9%	9%
Experimental uncert.	8%	2%
Theory uncer.	5%	3%

[arXiv:1902.00134](https://arxiv.org/abs/1902.00134)

- Measurement of  $H \rightarrow \mu\mu$  performed by CMS with  $137 \text{ fb}^{-1}$  of 13 TeV Run-2 data.
- Observed (expected) significance:  $3.0$  ( $2.5$ ) $\sigma$ .
- First evidence for  $H \rightarrow \mu\mu$  decay.
- First evidence of Higgs boson interaction with second generation fermions.
- *Remarkable success of the standard model (unfortunately) continues!*

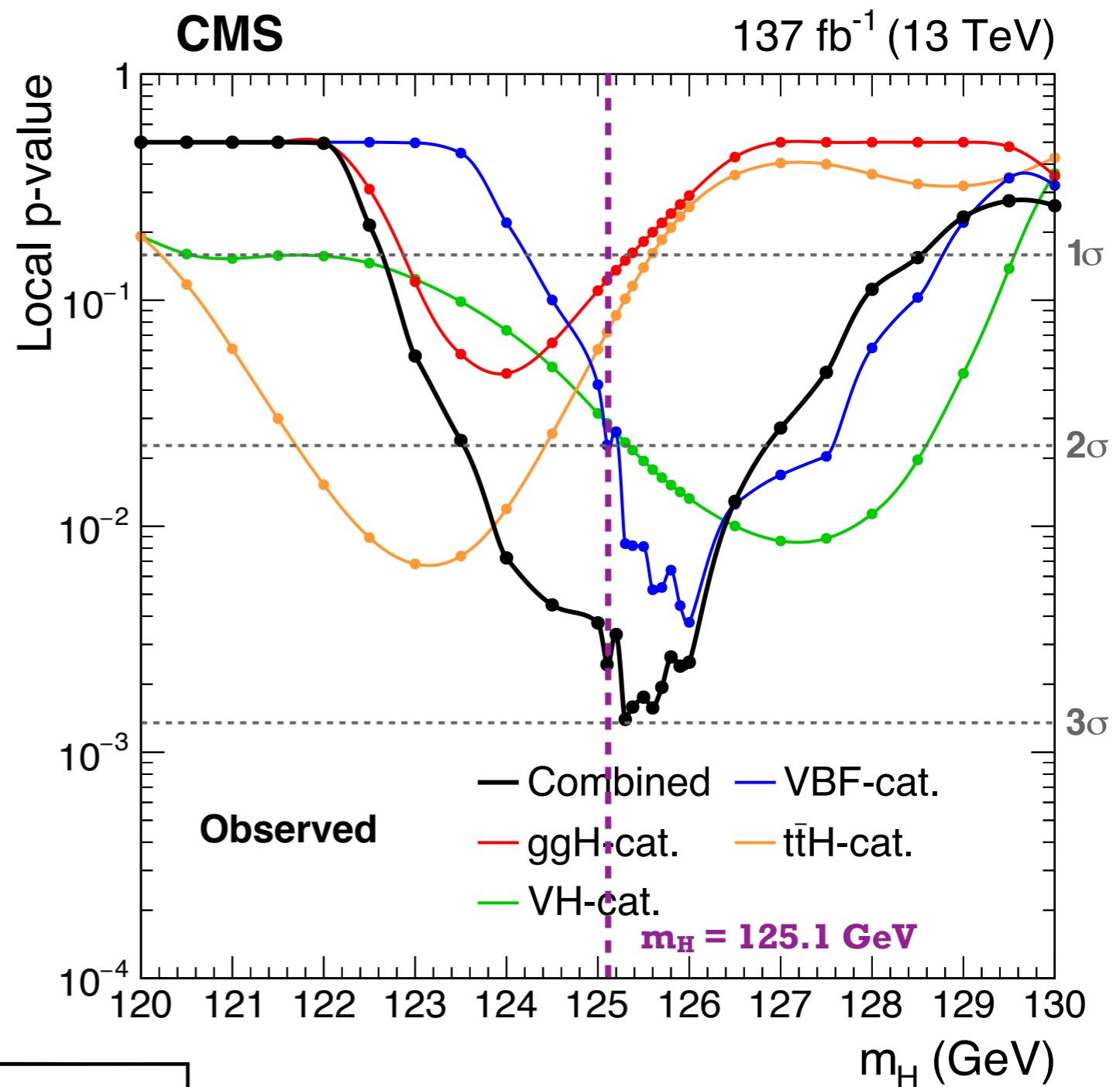
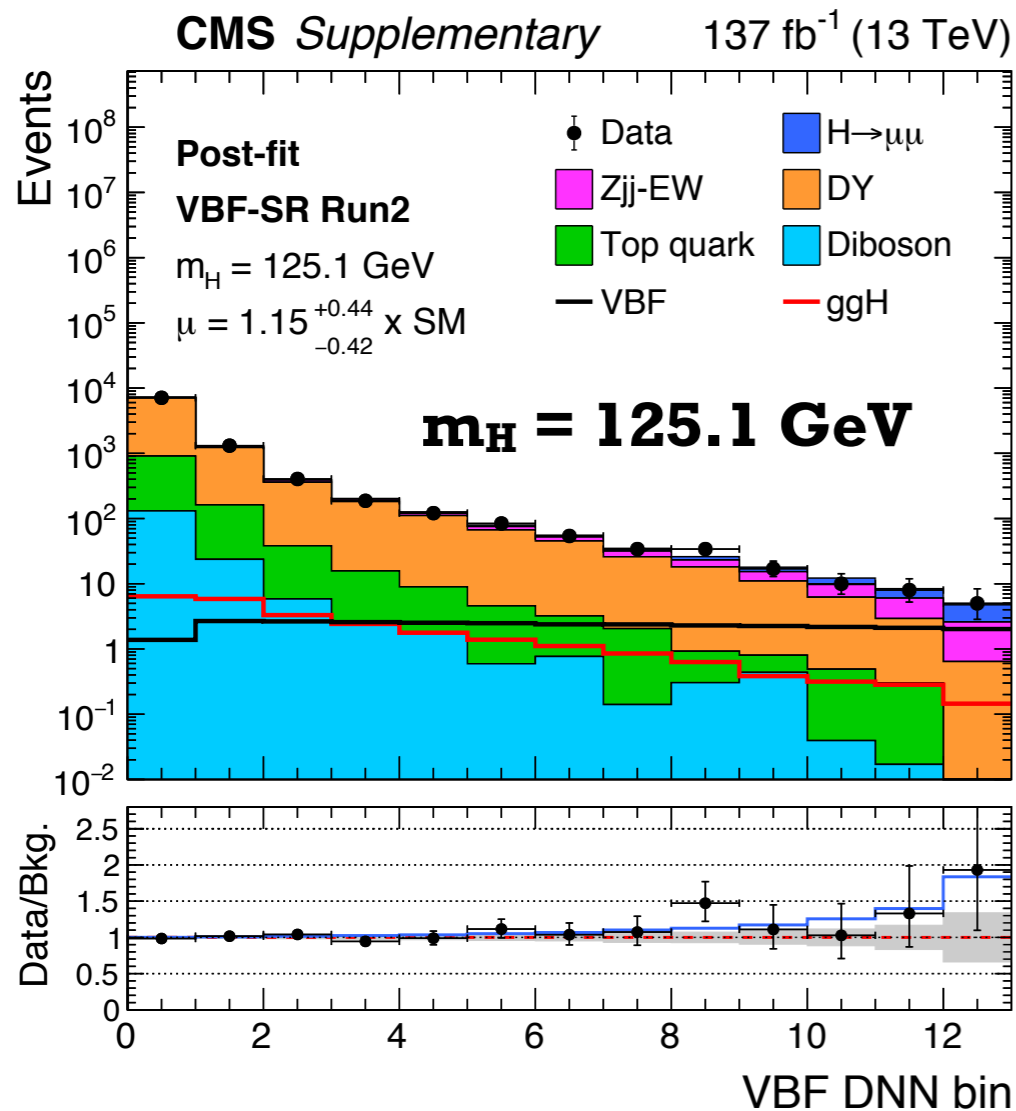


# **Additional Material**



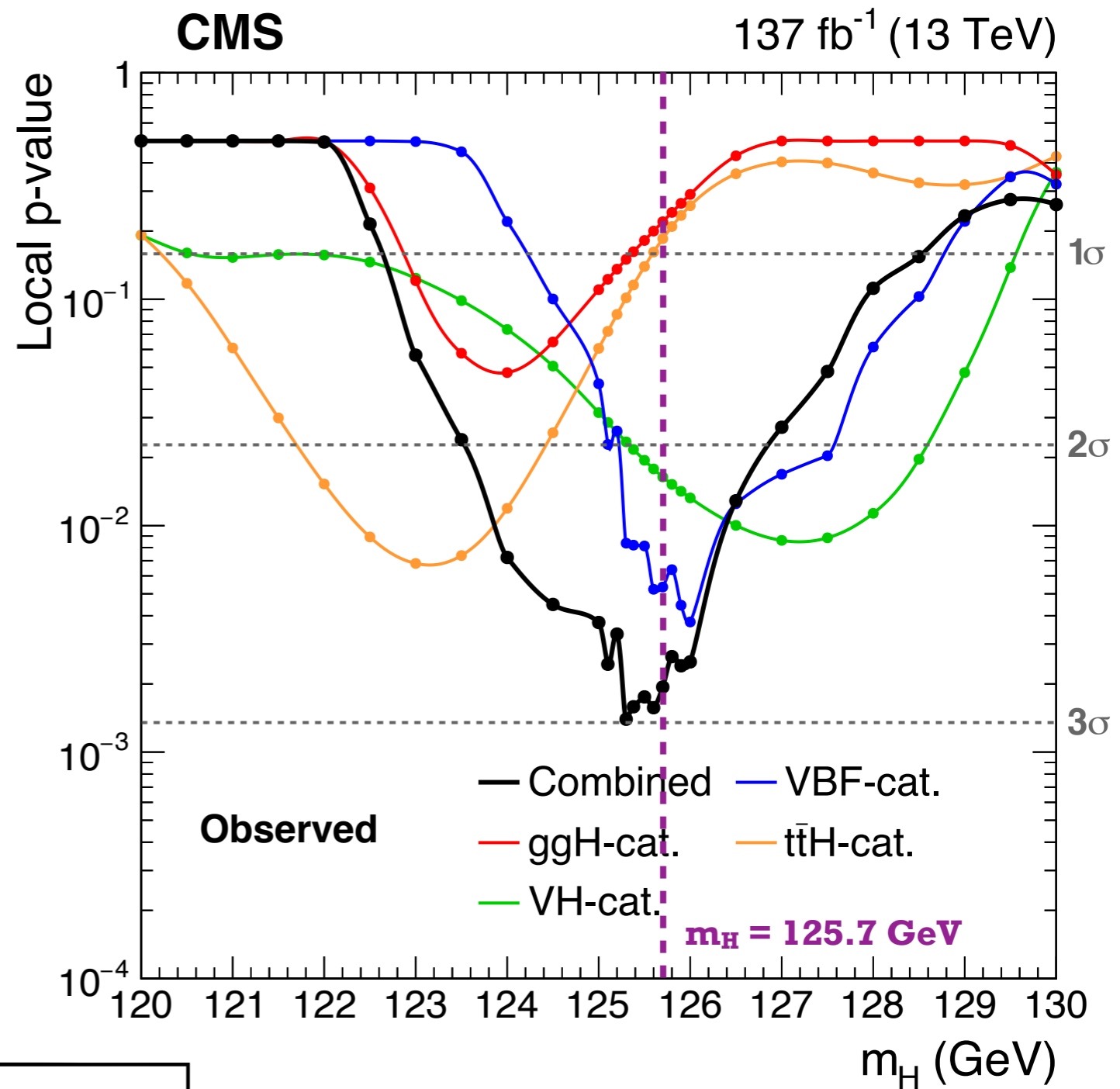
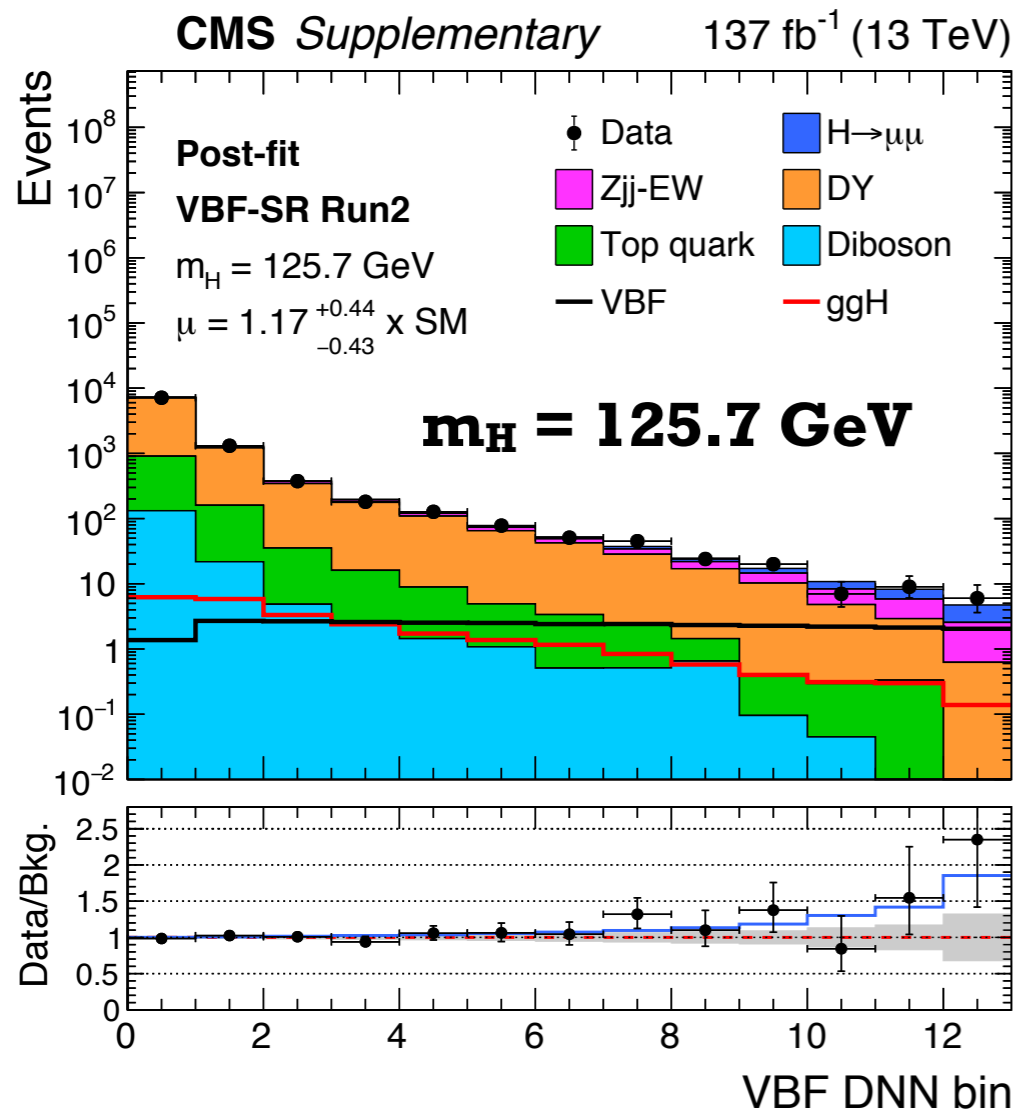
**Small change in  $m_H$  hypothesis leads to:**

- $\Rightarrow$  **shuffling of a few data events at high DNN score.**
- $\Rightarrow$  **discrete jumps in observed p-value at few percent level.**



**Small change in  $m_H$  hypothesis leads to:**

- ⇒ **shuffling of a few data events at high DNN score.**
- ⇒ **discrete jumps in observed p-value at few percent level.**



**Small change in  $m_H$  hypothesis leads to:**

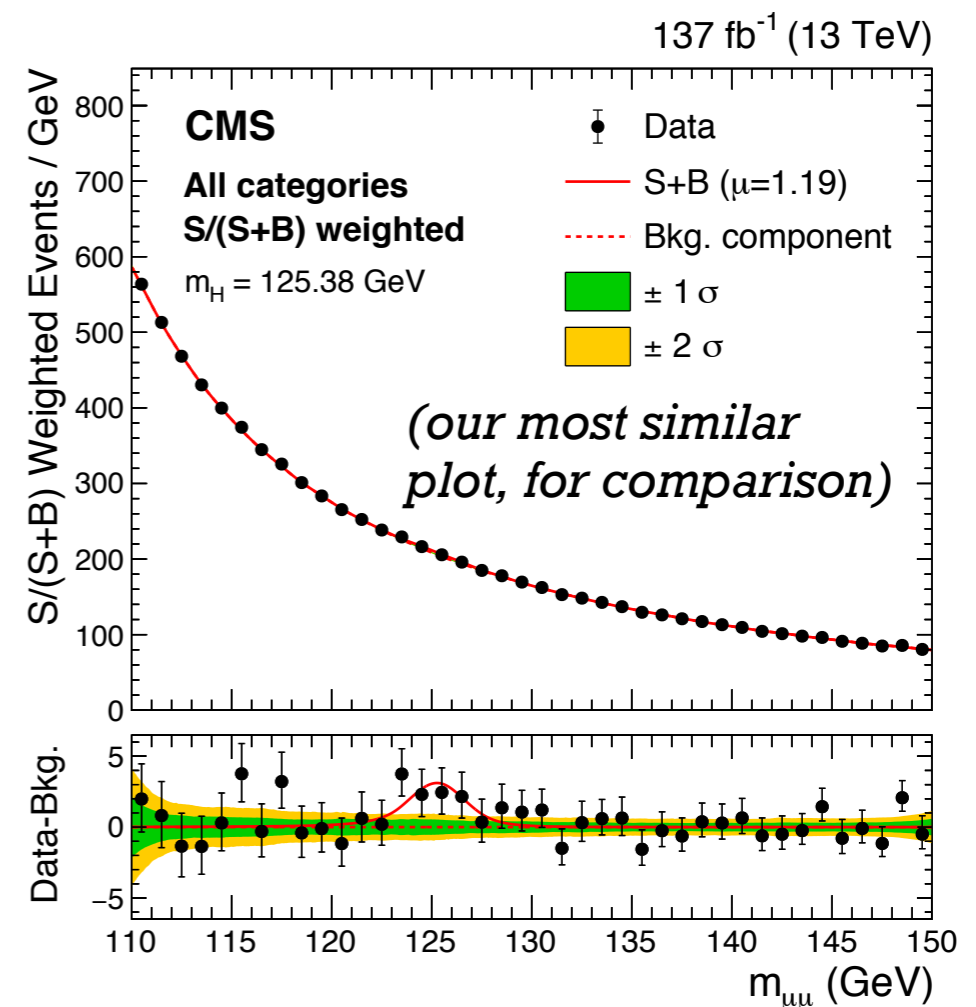
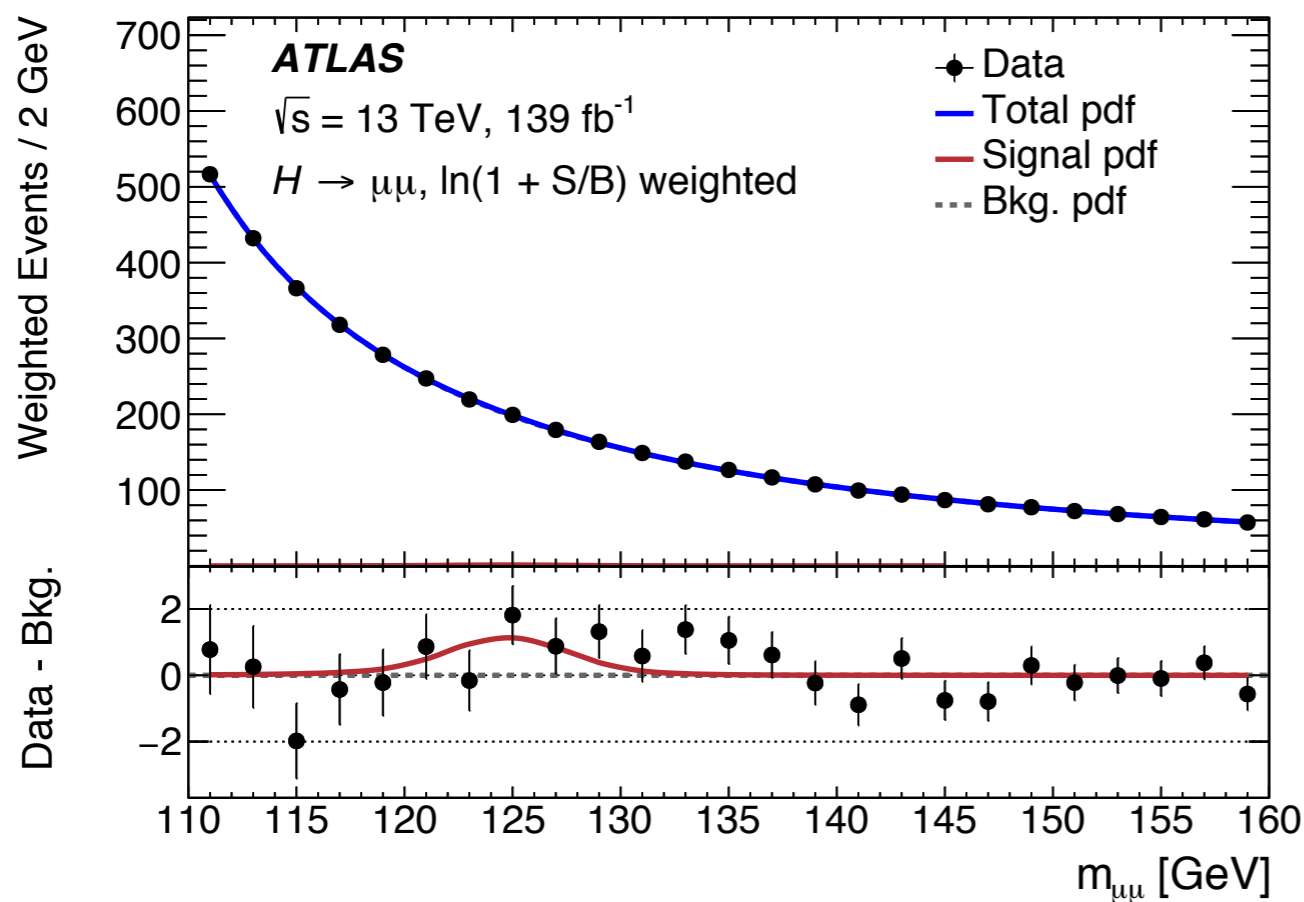
- ⇒ **shuffling of a few data events at high DNN score.**
- ⇒ **discrete jumps in observed p-value at few percent level.**



- Both CMS and ATLAS results include exclusive ttH and VH categories, as well as VBF-targeted region.
- However, many details are sufficiently different to make a direct comparison of these two new results quite complicated.

Obs. (exp.) significance: 2.0 (1.7) s.d.  
Signal strength  $\mu = 1.2 \pm 0.6$

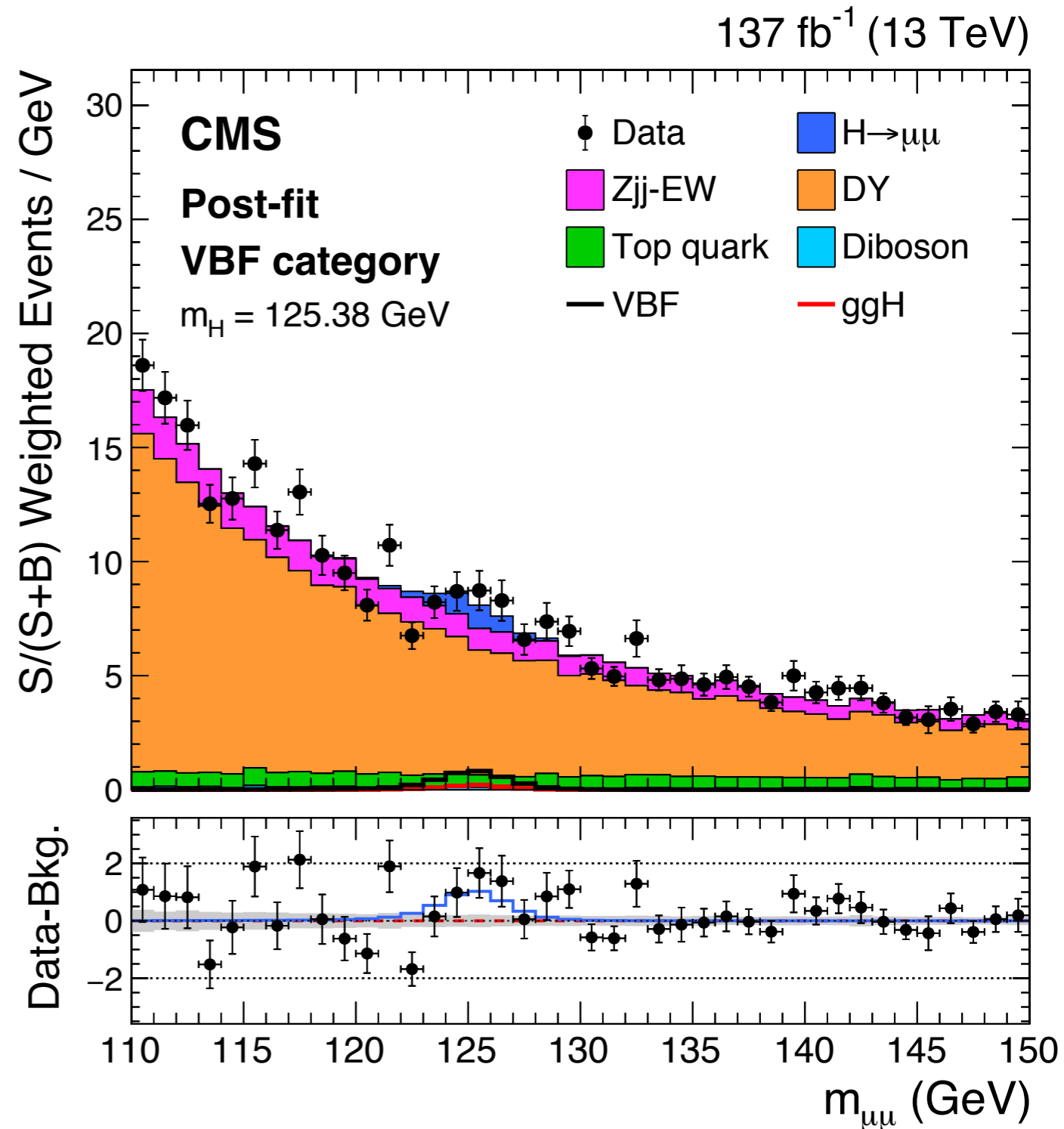
Obs. (exp.) significance: 3.0 (2.5) s.d.  
Signal strength  $\mu = 1.2 \pm 0.4$



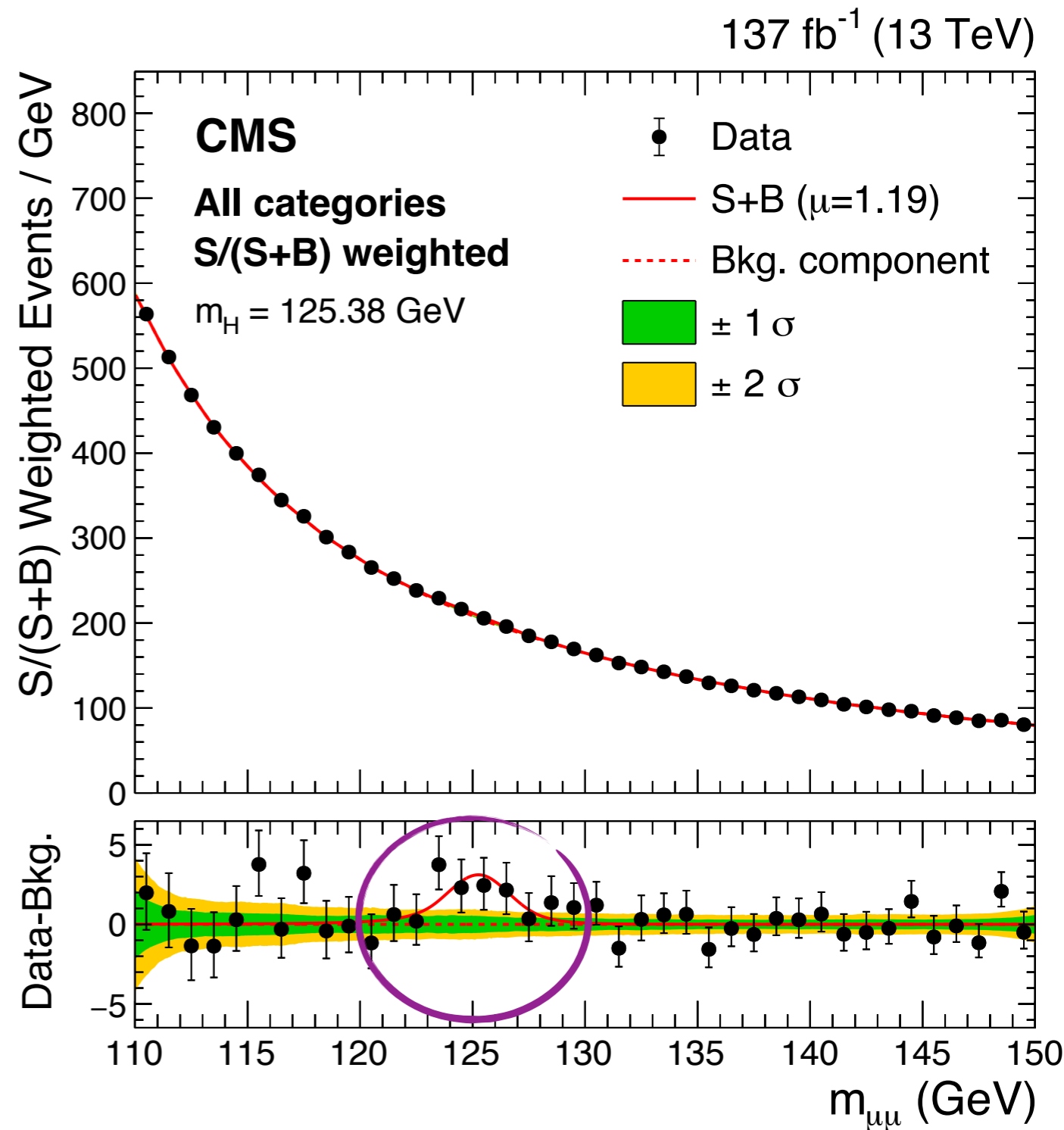
[1] [arXiv:2007.07830](https://arxiv.org/abs/2007.07830), submitted to PLB

Category	Data	$S_{\text{SM}}$	$S$	$B$	$S/\sqrt{B}$	$S/B$ [%]	$\sigma$ [GeV]
VBF Very High	15	$2.81 \pm 0.27$	$3.3 \pm 1.7$	$14.5 \pm 2.1$	0.86	22.6	3.0
VBF High	39	$3.46 \pm 0.36$	$4.0 \pm 2.1$	$32.5 \pm 2.9$	0.71	12.4	3.0
VBF Medium	112	$4.8 \pm 0.5$	$5.6 \pm 2.8$	$85 \pm 4$	0.61	6.6	2.9
VBF Low	284	$7.5 \pm 0.9$	$9 \pm 4$	$273 \pm 8$	0.53	3.2	3.0
2-jet Very High	1030	$17.6 \pm 3.3$	$21 \pm 10$	$1024 \pm 22$	0.63	2.0	3.1
2-jet High	5433	$50 \pm 8$	$58 \pm 30$	$5440 \pm 50$	0.77	1.0	2.9
2-jet Medium	18 311	$79 \pm 15$	$90 \pm 50$	$18\,320 \pm 90$	0.66	0.5	2.9
2-jet Low	36 409	$63 \pm 17$	$70 \pm 40$	$36\,340 \pm 140$	0.37	0.2	2.9
1-jet Very High	1097	$16.5 \pm 2.4$	$19 \pm 10$	$1071 \pm 22$	0.59	1.8	2.9
1-jet High	6413	$46 \pm 7$	$54 \pm 28$	$6320 \pm 50$	0.69	0.9	2.8
1-jet Medium	24 576	$90 \pm 11$	$100 \pm 50$	$24\,290 \pm 100$	0.67	0.4	2.7
1-jet Low	73 459	$125 \pm 17$	$150 \pm 70$	$73\,480 \pm 190$	0.53	0.2	2.8
0-jet Very High	15 986	$59 \pm 11$	$70 \pm 40$	$16\,090 \pm 90$	0.55	0.4	2.6
0-jet High	46 523	$99 \pm 13$	$120 \pm 60$	$46\,190 \pm 150$	0.54	0.3	2.6
0-jet Medium	91 392	$119 \pm 14$	$140 \pm 70$	$91\,310 \pm 210$	0.46	0.2	2.7
0-jet Low	121 354	$79 \pm 10$	$90 \pm 50$	$121\,310 \pm 280$	0.26	0.1	2.7
VH4L	34	$0.53 \pm 0.05$	$0.6 \pm 0.3$	$24 \pm 4$	0.13	2.6	2.9
VH3LH	41	$1.45 \pm 0.14$	$1.7 \pm 0.9$	$41 \pm 5$	0.27	4.2	3.1
VH3LM	358	$2.76 \pm 0.24$	$3.2 \pm 1.6$	$347 \pm 15$	0.17	0.9	3.0
$t\bar{t}H$	17	$1.19 \pm 0.13$	$1.4 \pm 0.7$	$15.1 \pm 2.2$	0.36	9.2	3.2

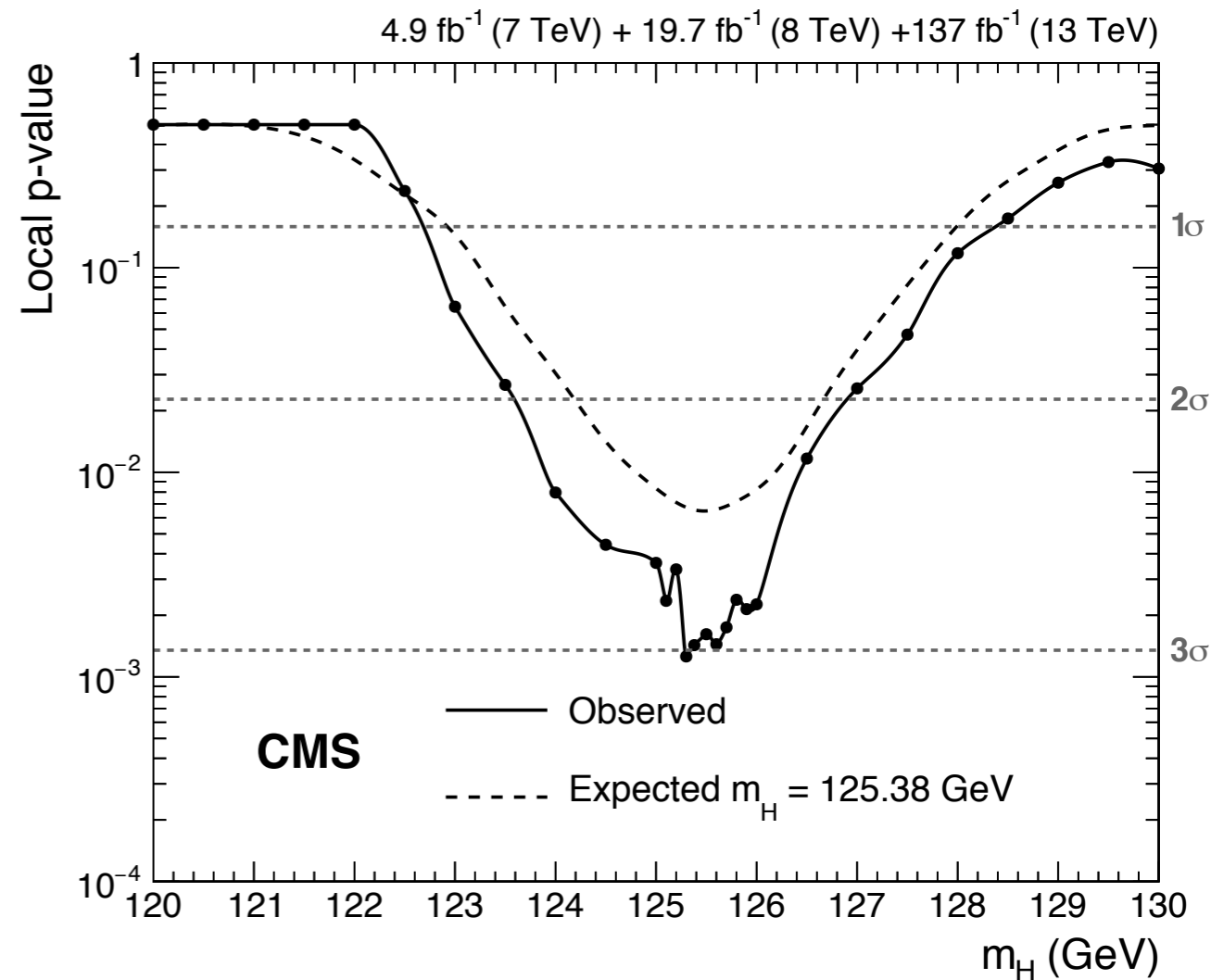
- For VBF channel, assign per-event S/S+B calculated as a function of mass-decorrelated ( $m_H$  fixed to 125 GeV) DNN score
- This binned  $m_{\mu\mu}$  histogram is interpolated with a spline and merged with the other channels for the combined mass plot.
- *Note that this is just a way to visualize the observed excess, not the fit result itself.*



- Weight  $m_{\mu\mu}$  distribution in each ggH, VH, and ttH category by S/S+B within signal HWHM.
- Interpolate binned VBF category  $m_{\mu\mu}$  histogram (see previous slide) with spline and merge with other categories.
- *Note that this is just a way to visualize the observed excess, not the fit result itself.*



- Combination performed with CMS Run-1  $H \rightarrow \mu\mu$  search.
- Full p-value scan vs.  $m_H$ .
- Run-1 adjusted to  $m_H = 125.38$  GeV signal hypothesis.
- **Observed (expected) significance  $2.98\sigma$  ( $2.48\sigma$ ).**
- *Local minimum at  $m_H = 125.3$  GeV is  $3.02\sigma$ .*

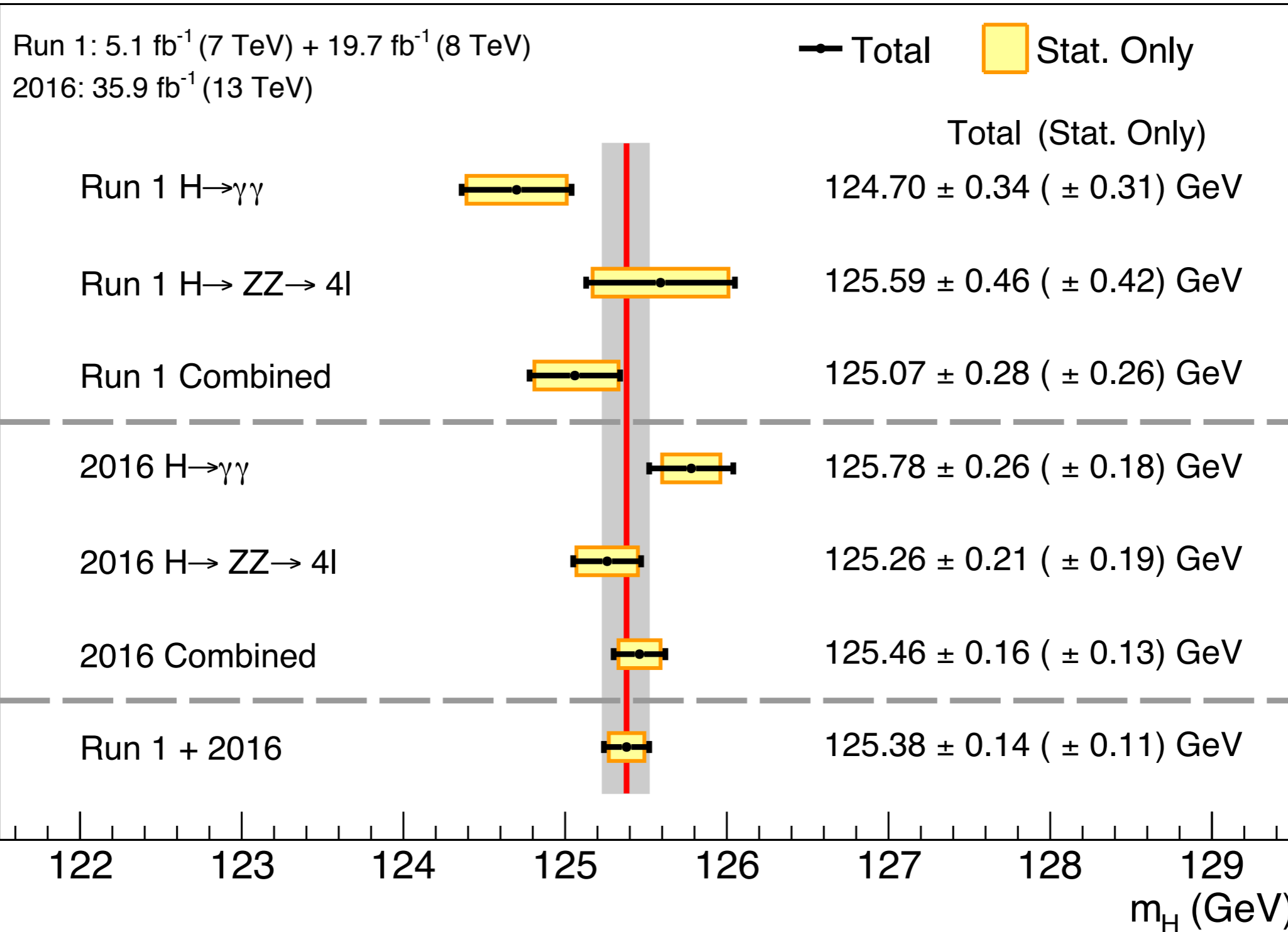


Production category	Observed (expected) signif.	Observed (expected) UL on $\mu$
VBF	2.40 (1.77)	2.57 (1.22)
ggH	0.99 (1.56)	1.77 (1.28)
$t\bar{t}H$	1.20 (0.54)	6.48 (4.20)
VH	2.02 (0.42)	10.8 (5.13)
Combined $\sqrt{s} = 13$ TeV	2.95 (2.46)	1.94 (0.82)
Combined $\sqrt{s} = 7, 8, 13$ TeV	2.98 (2.48)	1.93 (0.81)

- Precision in all channels dominated by limited amount of data.
  - Largest impact from systematics in VBF category (<5%).
- Largest systematic uncertainty impacts from limited MC statistics in VBF category and VBF (signal and EW Zjj) parton shower modeling.

Uncertainty source	$\Delta\mu$	
Post-fit uncertainty	+0.44	-0.42
Statistical uncertainty	+0.41	-0.40
Systematic uncertainty	+0.17	-0.16
Experimental uncertainty	+0.12	-0.11
Theoretical uncertainty	+0.10	-0.11
Size of simulated samples	+0.07	-0.06

## CMS



[Phys. Lett. B 805 \(2020\) 135425](#)

- Background composition is quite stable across categories and dominated by DY (>90%).
- Core background function built as discrete profile of two physics-inspired (Breit-Wigner, FEWZ) and an agnostic (sum of exponentials) function.
- Bias studied against multiple physics-inspired and agnostic background functions and always < 20% (negligible impact on result).
- No prior assumption on background shape or normalization

$$B_{cat}(m_{\mu\mu}, \vec{\alpha}, \vec{\beta}) = N_B \times F_{core}(m_{\mu\mu}, \vec{\alpha}) \times T_{SMF}(m_{\mu\mu}, \vec{\beta})$$

Number of bkg. events



**Core-PDF**, defined as a **discrete profile** of three functions. Associated **parameters** are **correlated across categories**



Per-category **polynomial shape modifier** use to “morph” the core component

\*method in ggH channel only

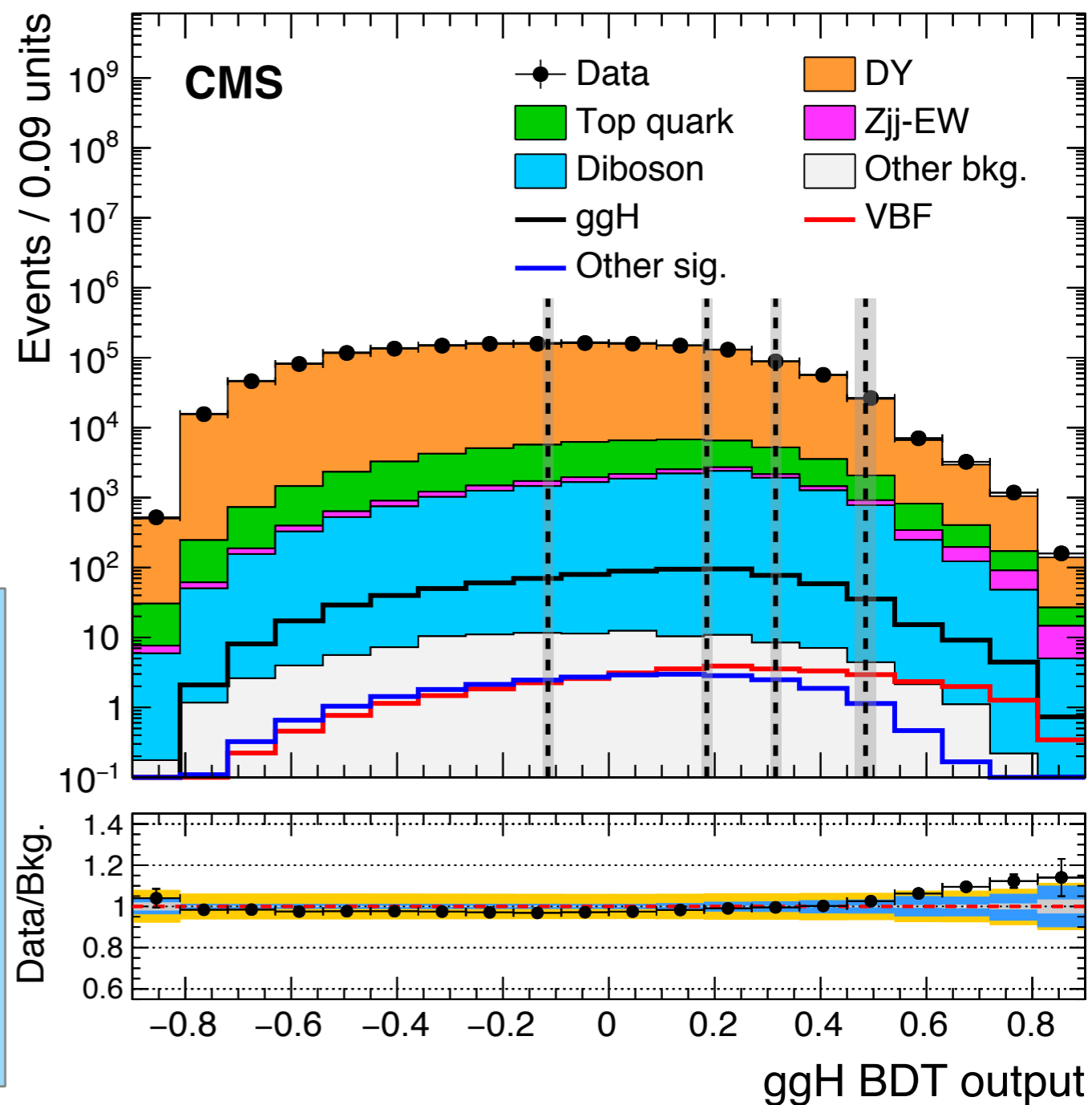


- Consider all events not selected by exclusive categories.
- About 96% of total inclusive events selected in ggH category.
- Largest signal yield, but smallest S/B  $\sim 0.1\%$ .
- Train mass-decorrelated BDT based on muon kinematics + possible jet kinematics (to pick up also ggH+X, residual VBF, hadronic VH)

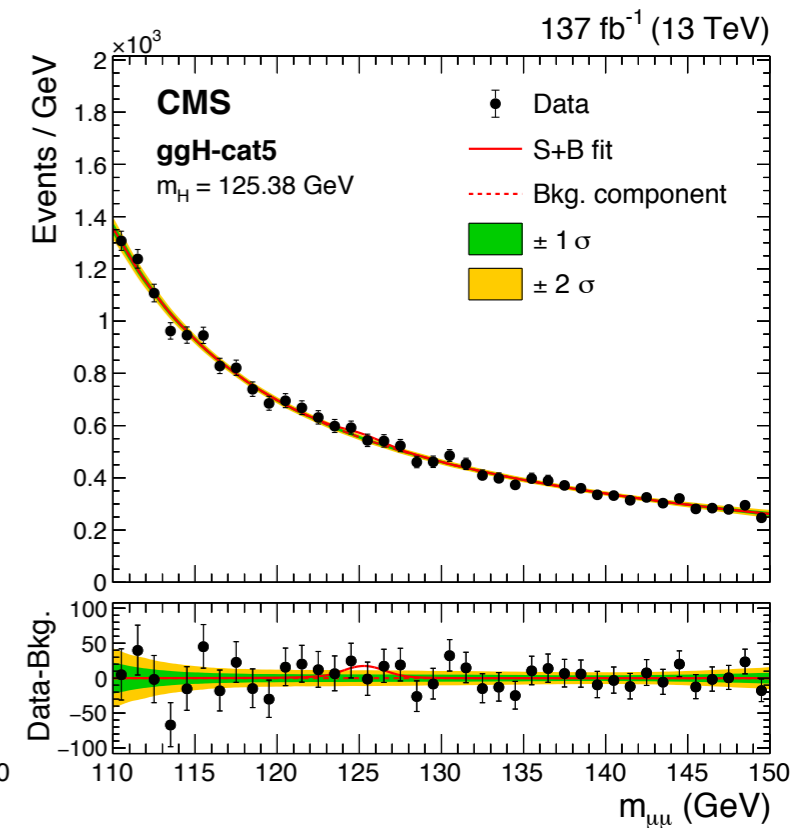
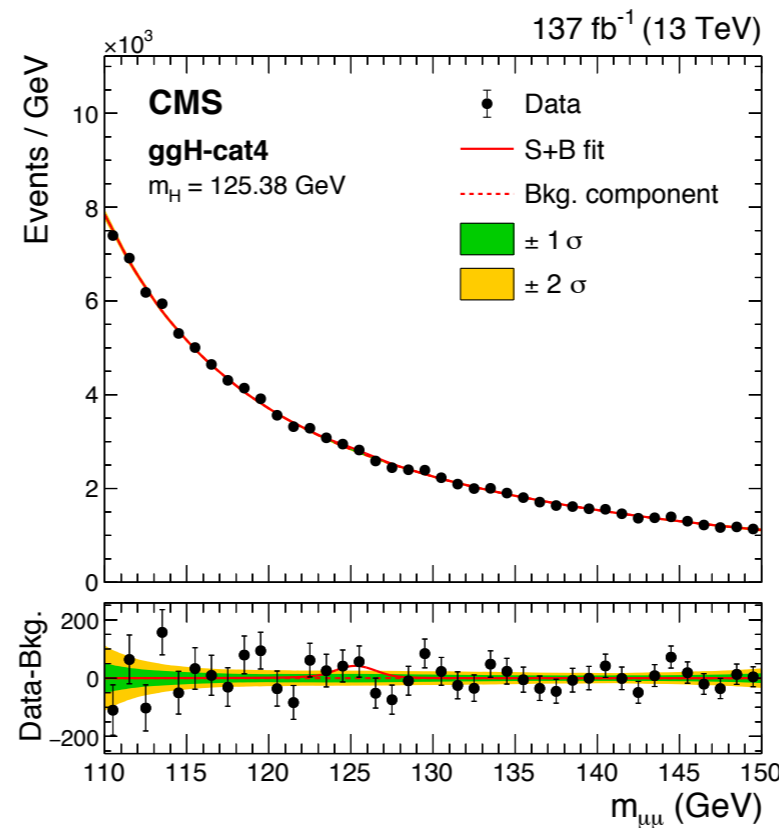
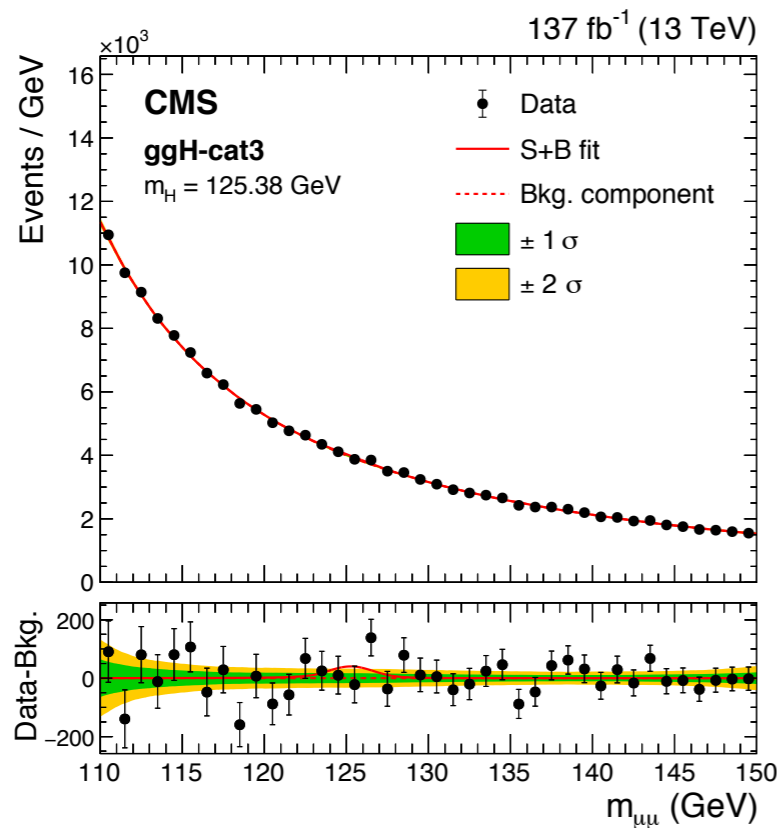
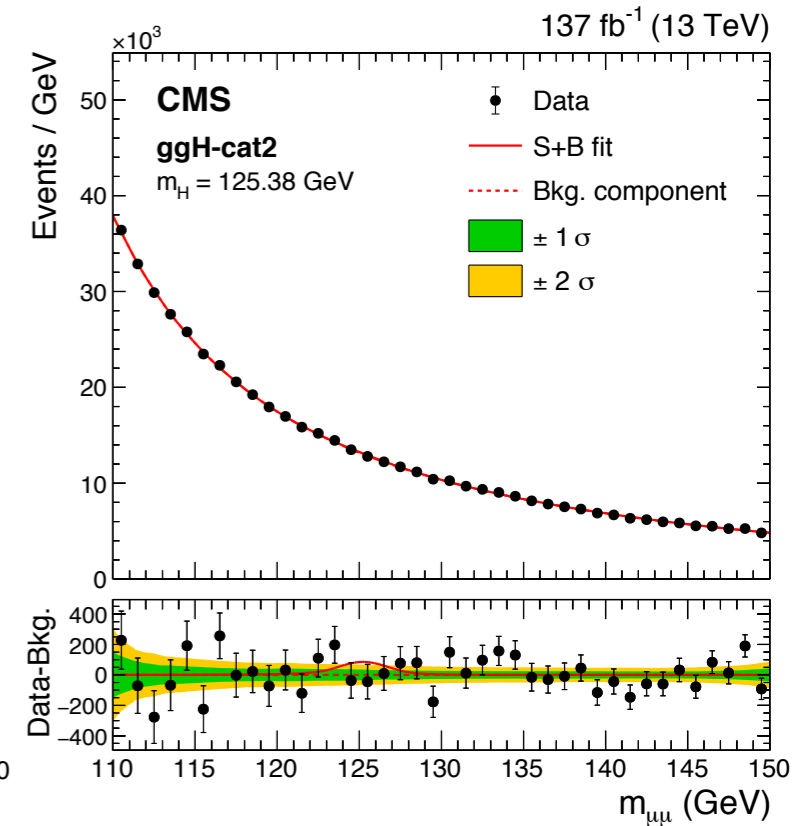
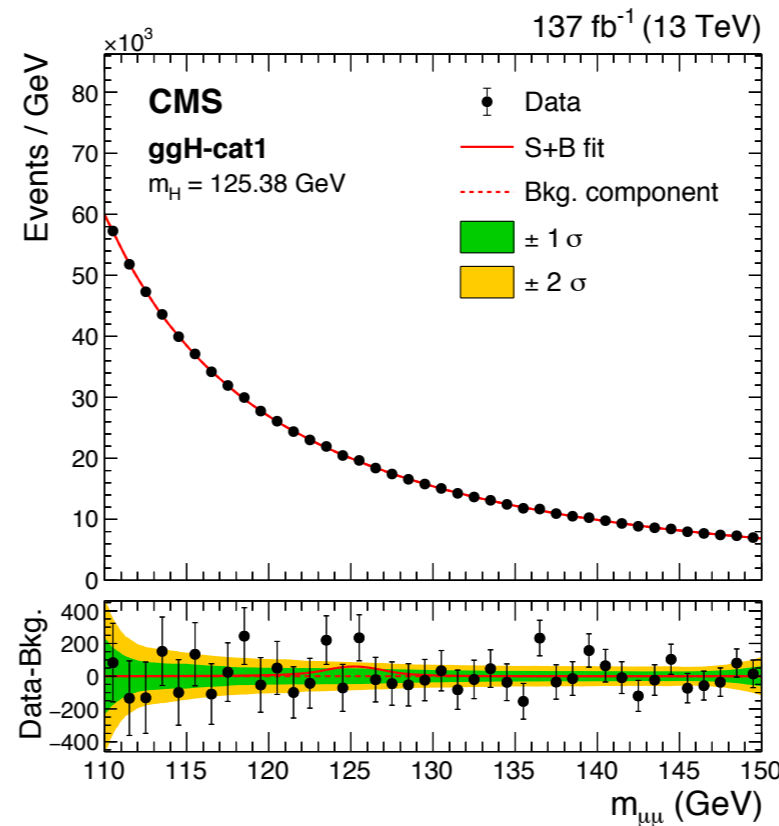
BDT subcategory boundaries optimized iteratively based on significance from full fit to MC.

137 fb<sup>-1</sup> (13 TeV)

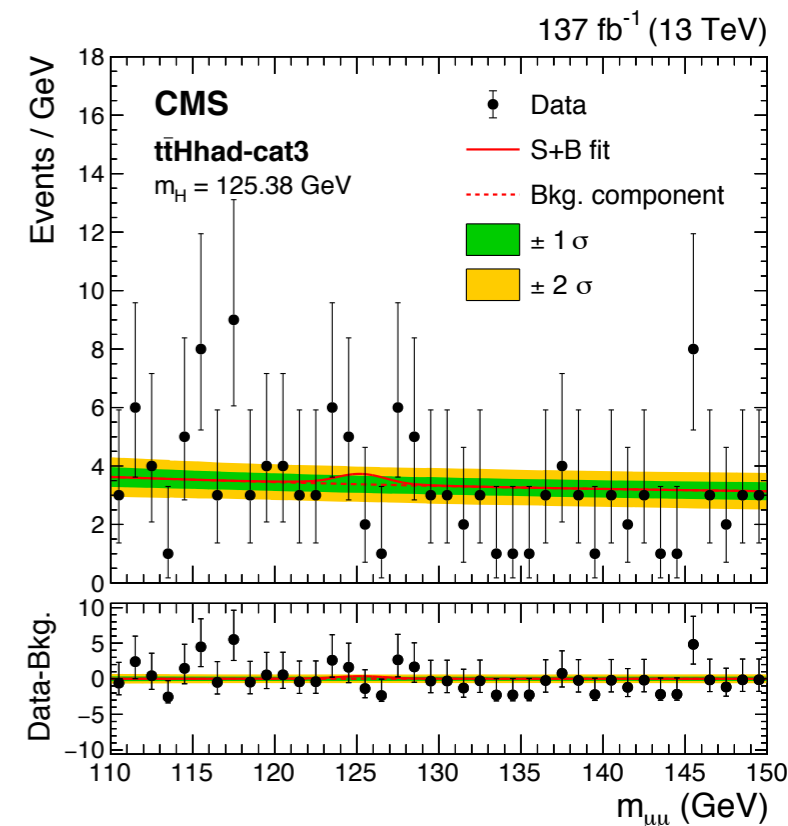
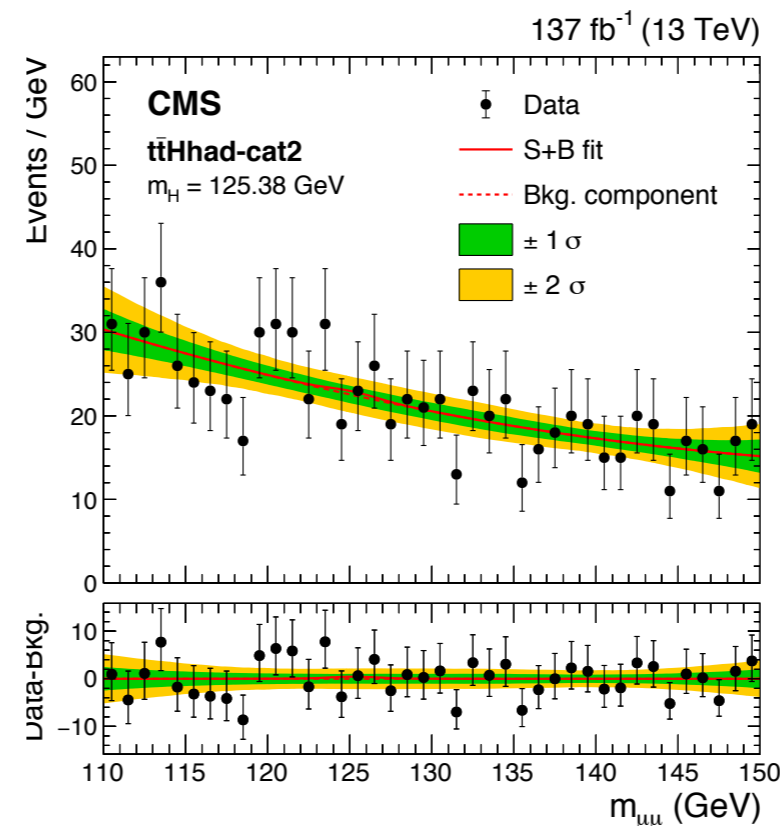
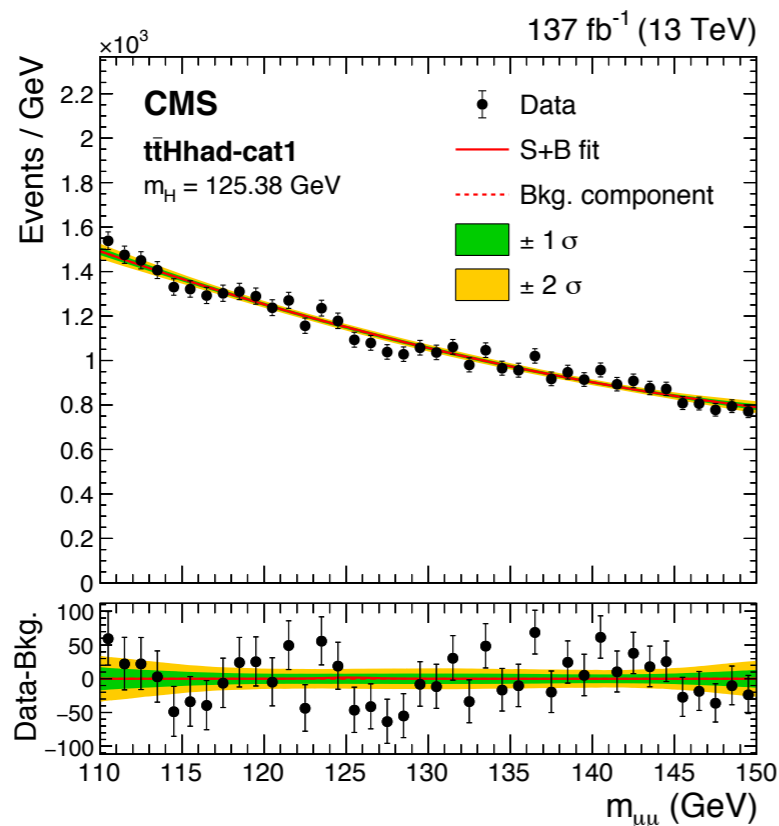
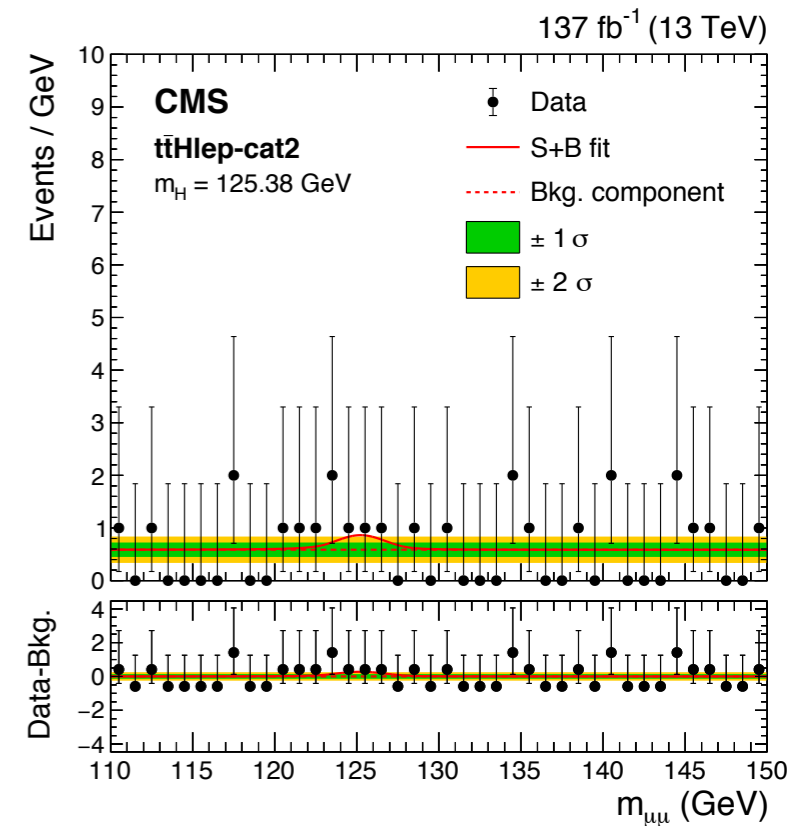
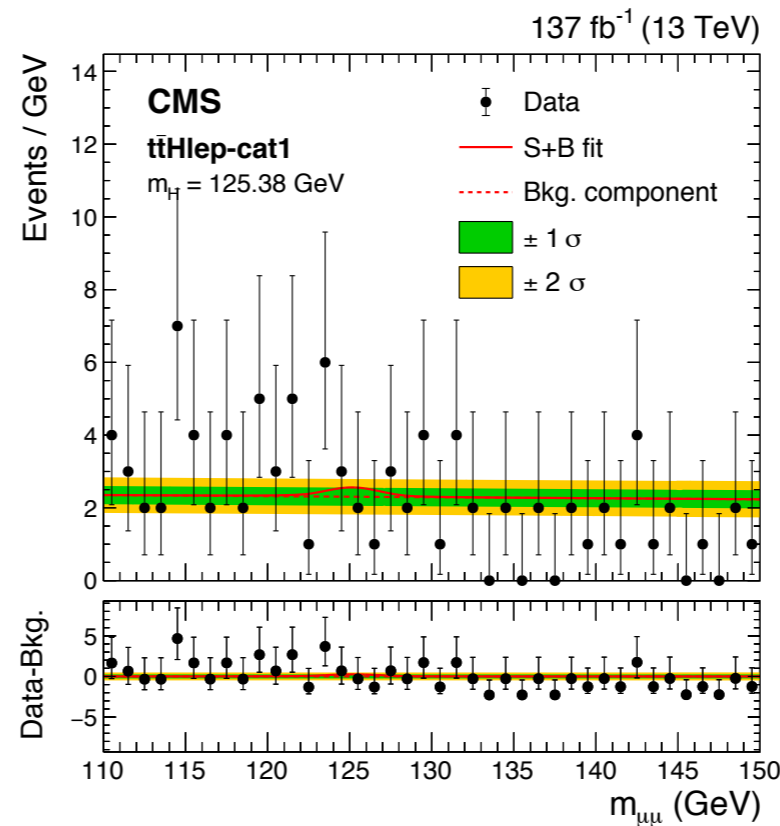
<b>Dimuon system</b> <ul style="list-style-type: none"> <li>• <math>p_T(\mu\mu)</math></li> <li>• <math>y(\mu\mu)</math></li> <li>• Colin-Soper angles</li> </ul>	<b>Leading jet</b> <ul style="list-style-type: none"> <li>• <math>p_T(j_1)</math></li> <li>• <math>\eta(j_1)</math></li> <li>• <math>\Delta\eta(\mu\mu, j_1)</math></li> <li>• <math>\Delta\phi(\mu\mu, j_2)</math></li> </ul>	<b>Dijet system</b> <ul style="list-style-type: none"> <li>• <math>m(jj)</math></li> <li>• <math>\Delta\eta(jj)</math></li> <li>• <math>\Delta\phi(jj)</math></li> <li>• Zeppenfeld</li> <li>• <math>p_T(j_2)</math></li> <li>• <math>\min\text{-}\Delta\eta(\mu\mu, j)</math></li> <li>• <math>\min\text{-}\Delta\phi(\mu\mu, j)</math></li> </ul>
<b>Single muon</b> <ul style="list-style-type: none"> <li>• <math>p_T(\mu)/m(\mu\mu)</math></li> <li>• <math>\eta(\mu)</math></li> </ul>	<b>Event variables</b> <ul style="list-style-type: none"> <li>• <math>N_{\text{jets}}</math></li> </ul>	



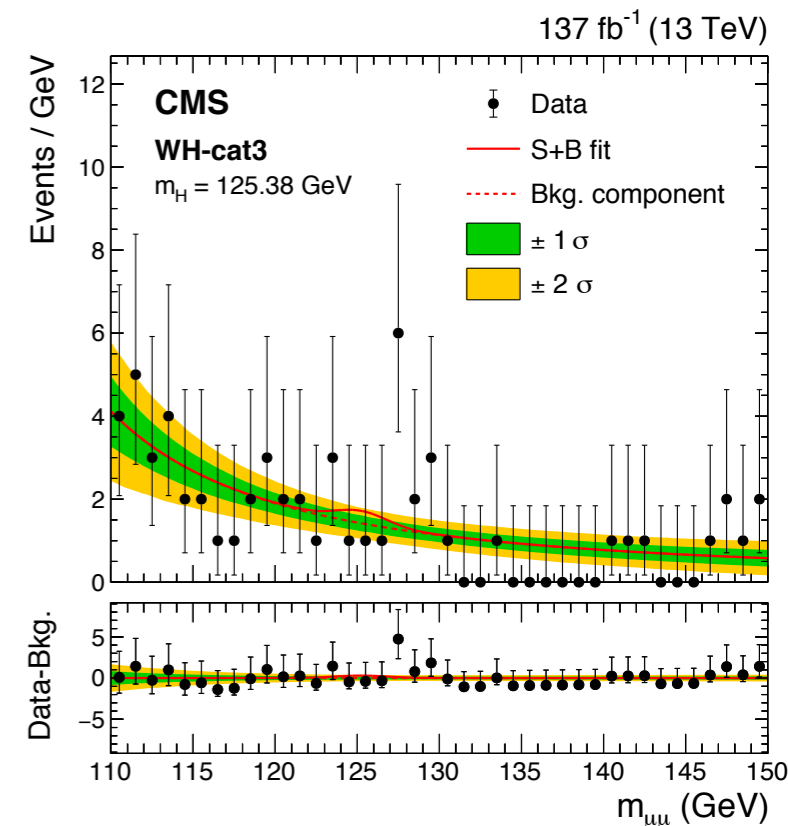
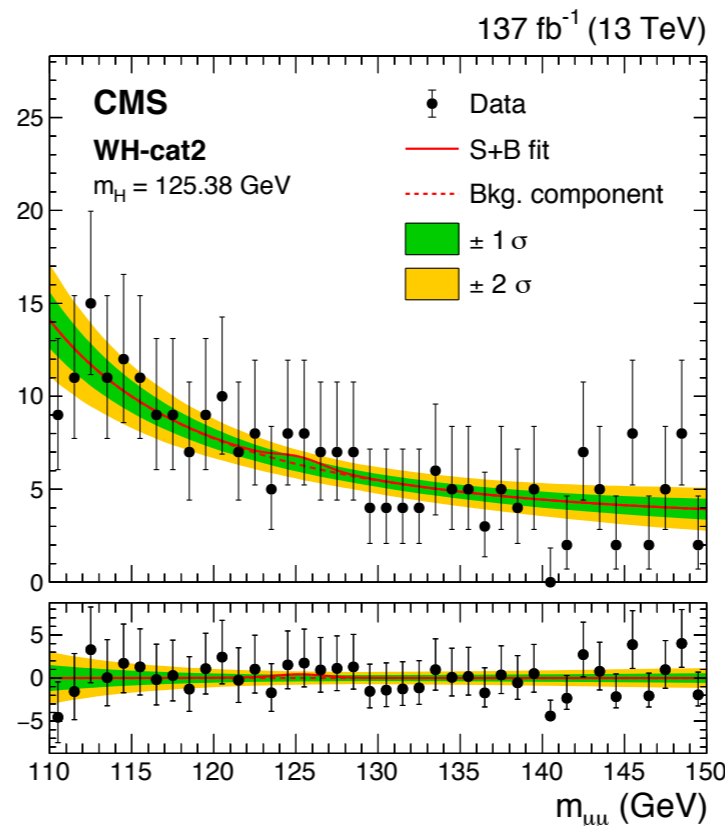
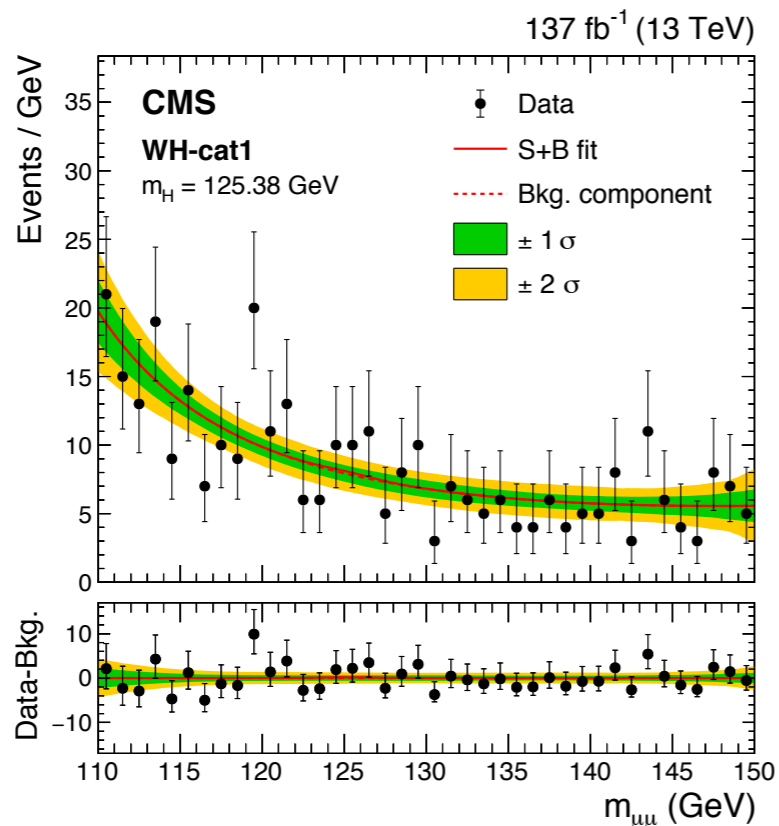
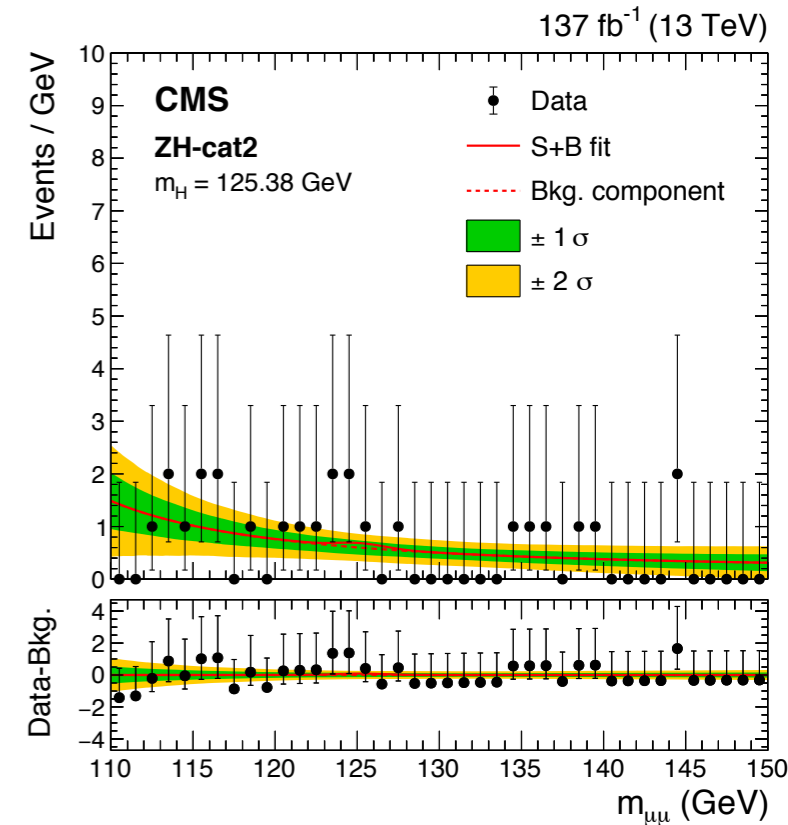
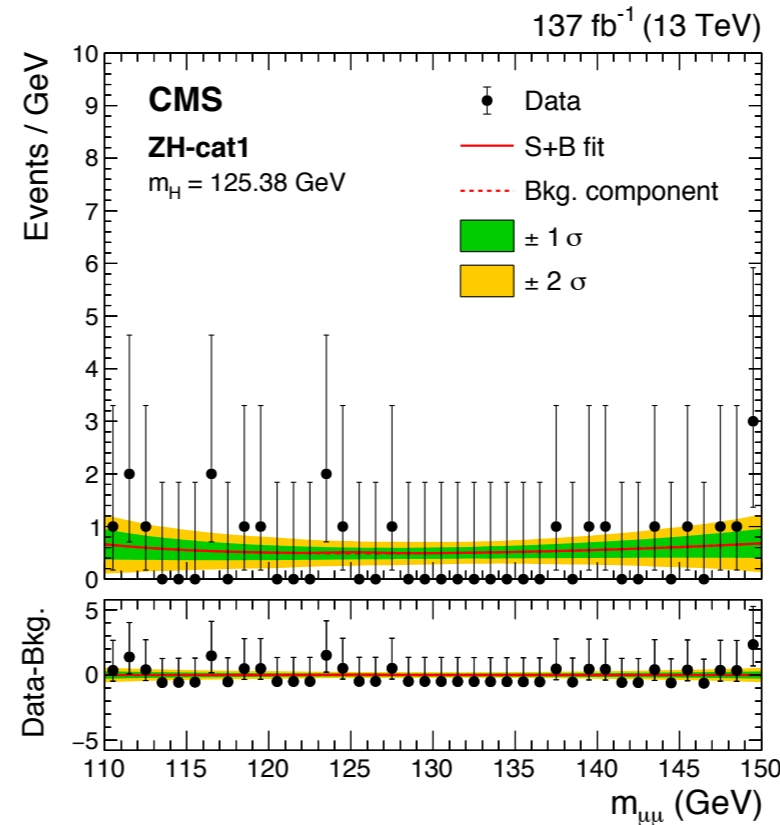
- S+B background fit describes the data well throughout the  $m_{\mu\mu}$  spectrum in all categories.

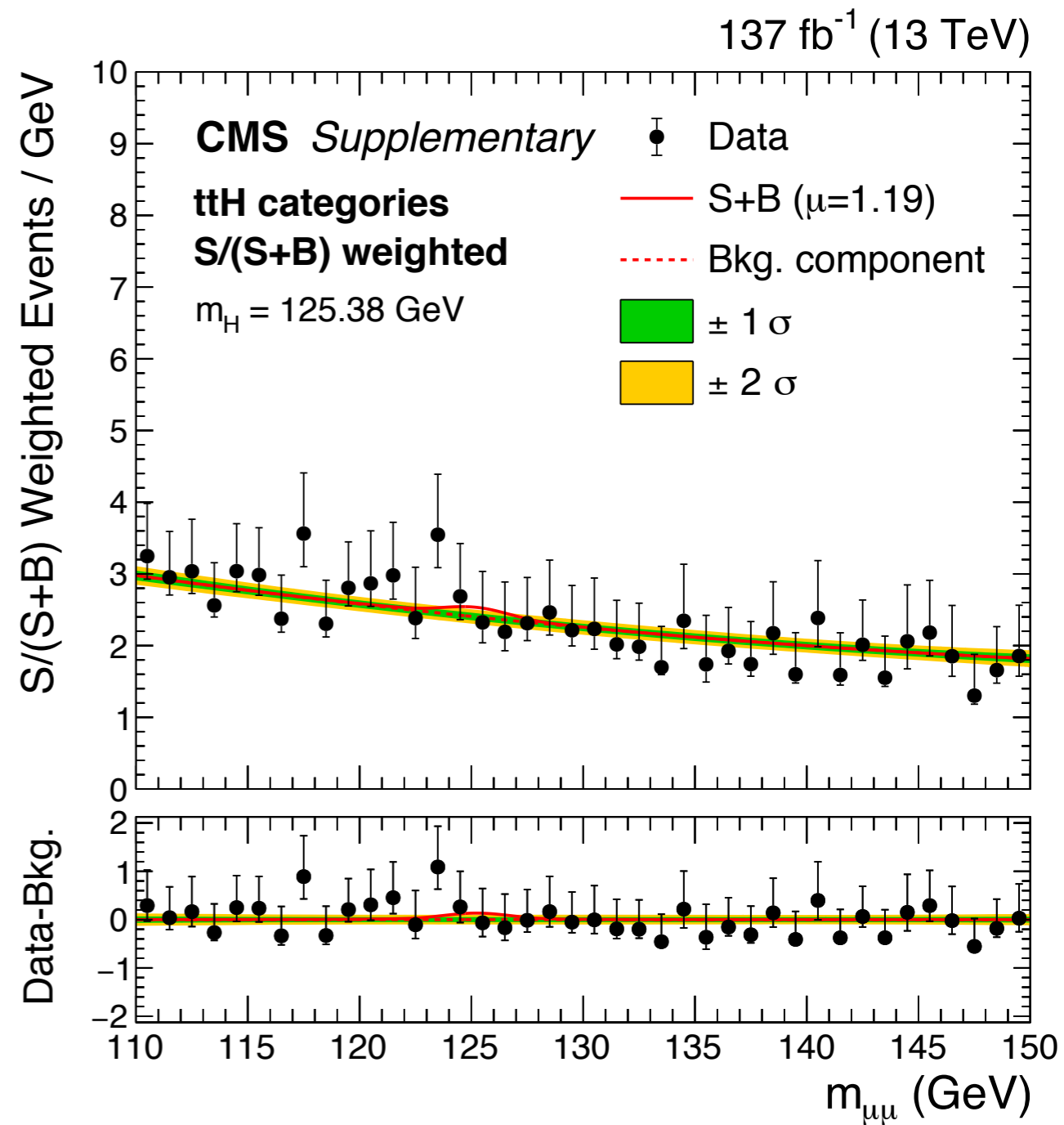
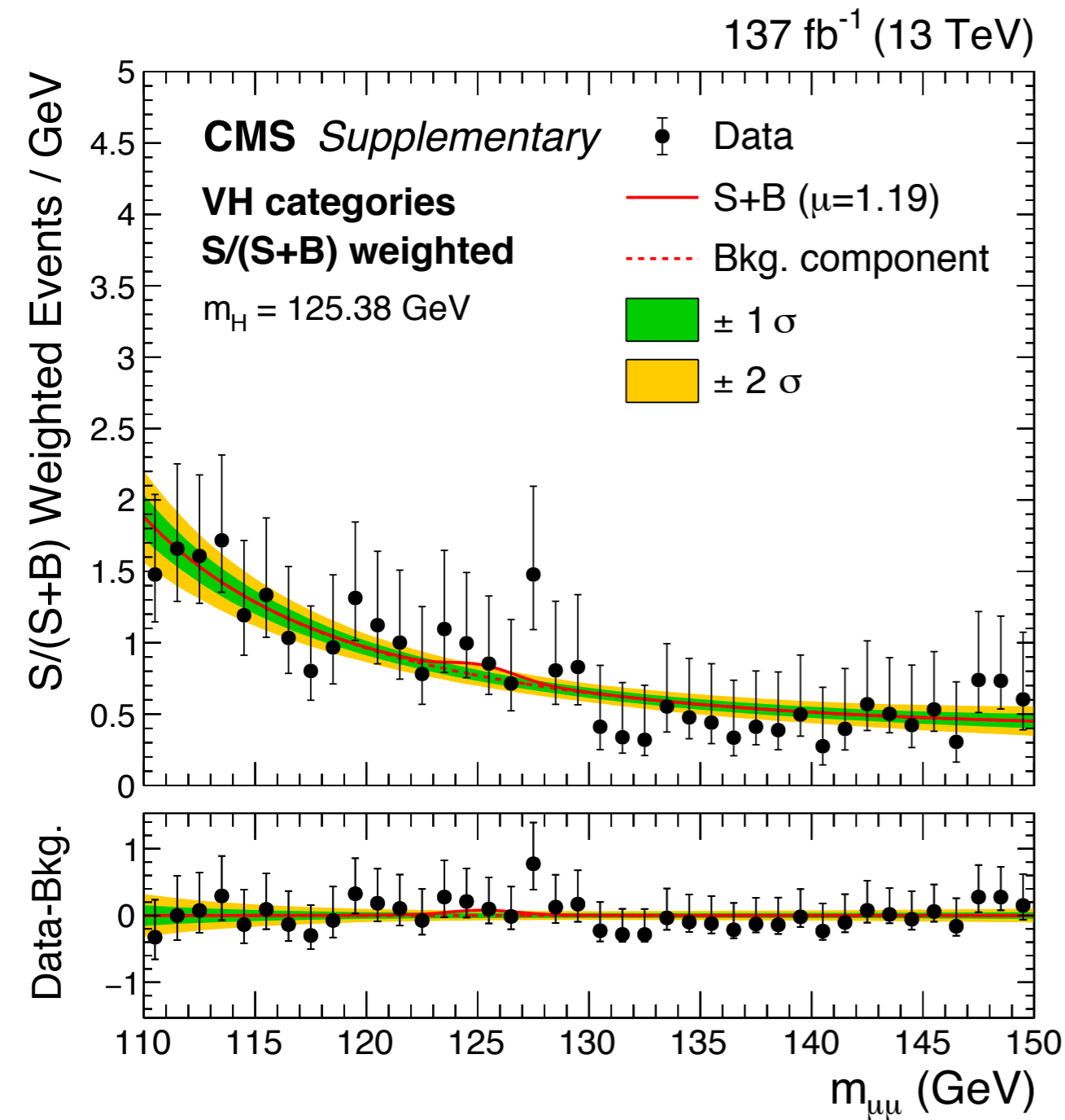


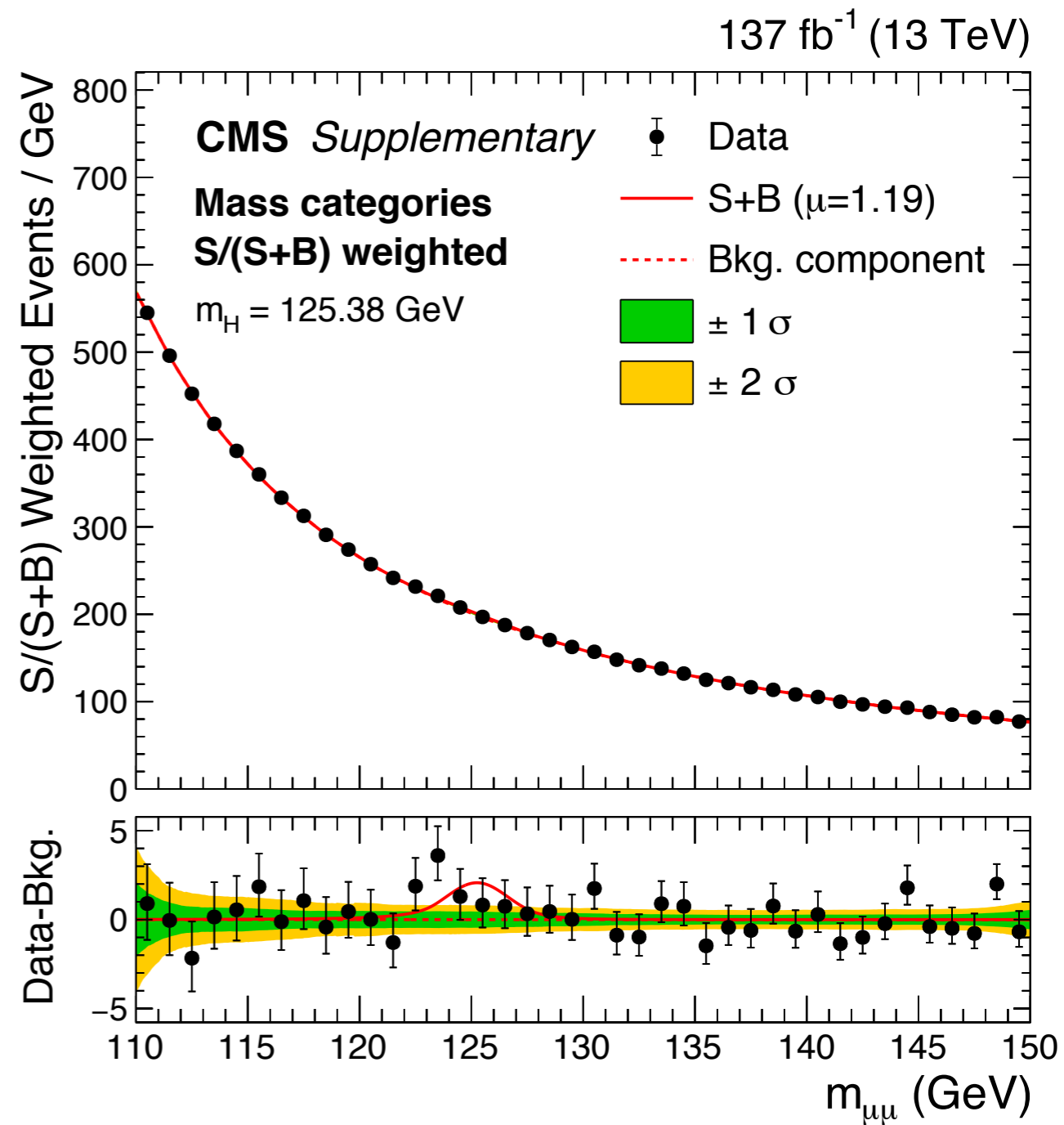
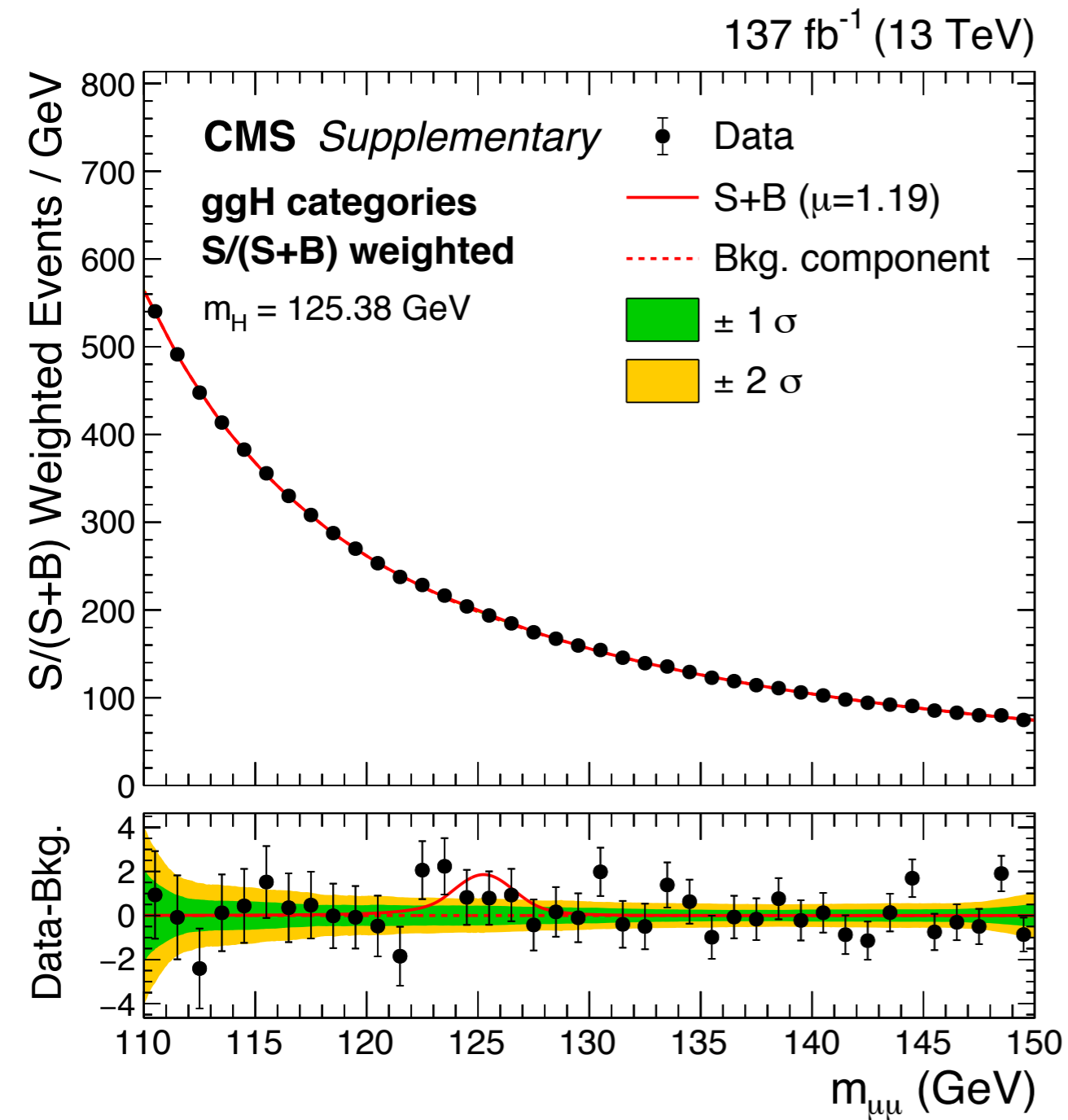
- Background fit with simple exponential (ttH-lep) or polynomial (ttH-had).
- Bias checked following similar procedure as in ggH channel.
- Categories optimized following same strategy as ggH channel.



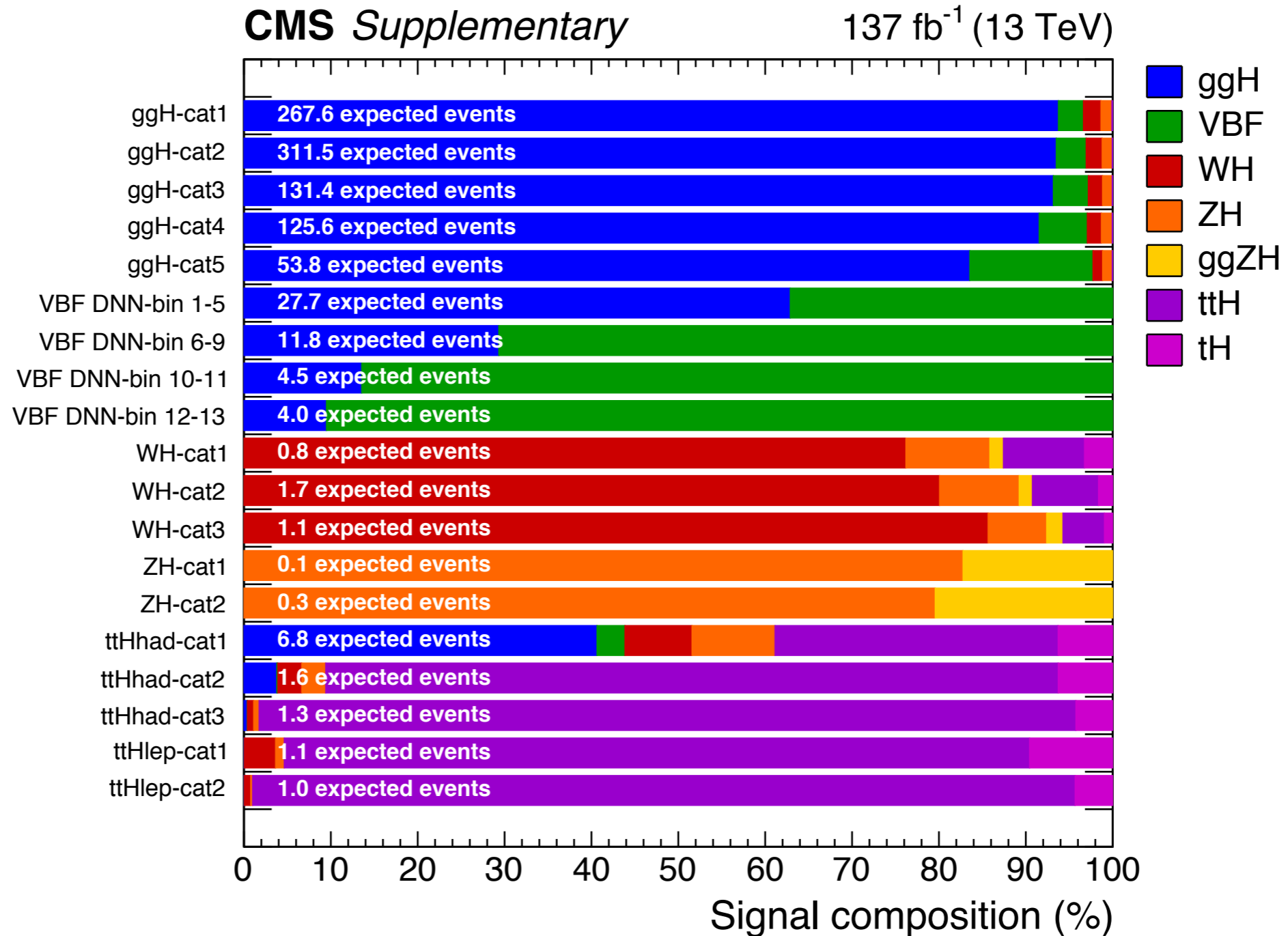
- Background fit with BWZ function.
- Choice of functions and bias studies similar to other channels.
- Small excesses in data near 125 GeV, but consistent with expectation within (large) statistical uncertainties.



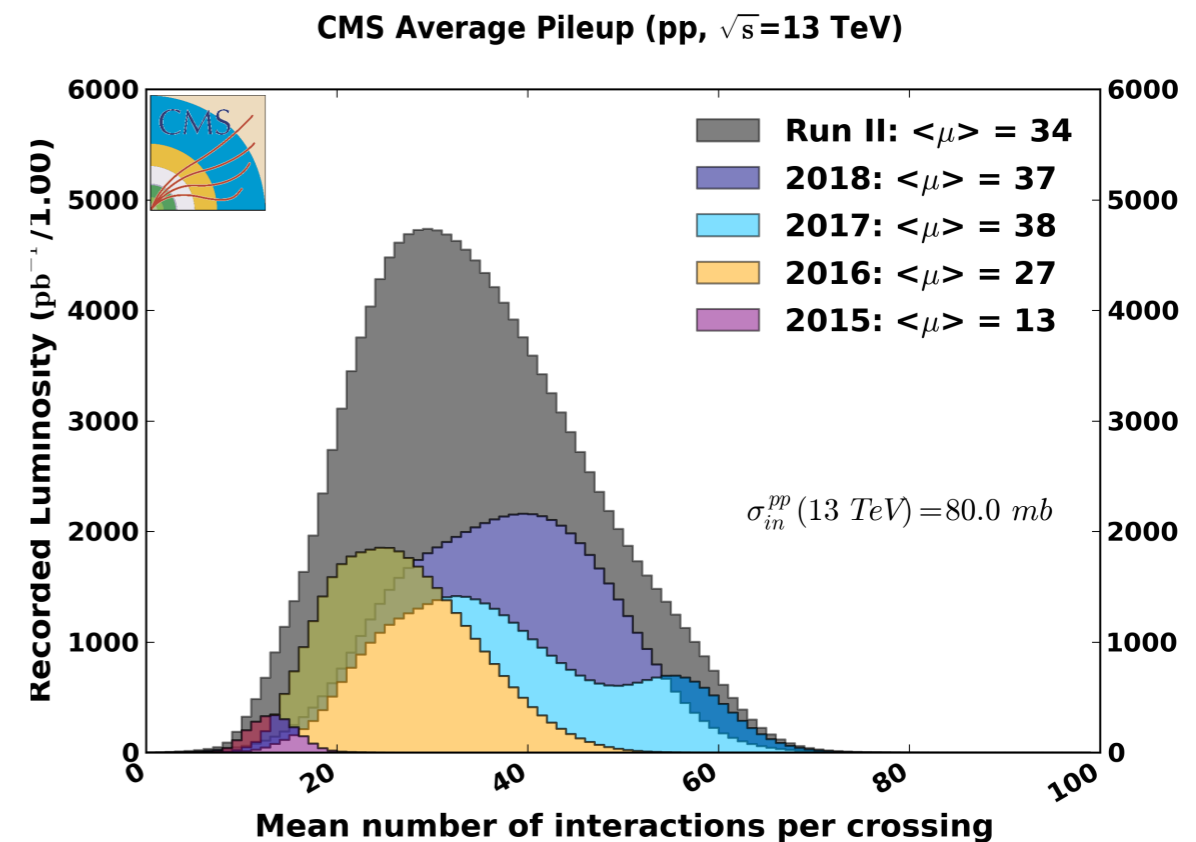
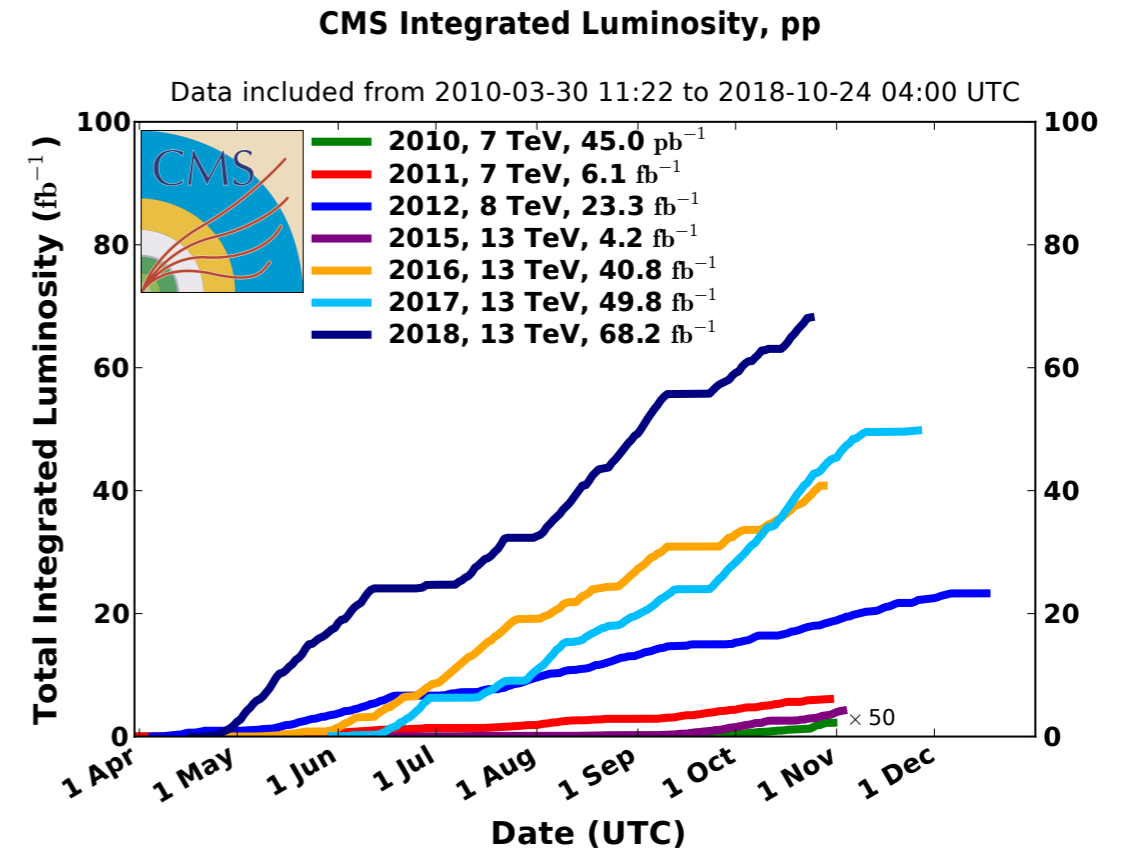




- Relatively high purity in targeted Higgs boson production mode achieved in each category.



- *This result focuses on  $137 \text{ fb}^{-1}$  of  $13 \text{ TeV}$  data collected by CMS from 2016 to 2018.*
- Including new analysis of recalibrated 2016 data, which had been used for previous CMS  $H \rightarrow \mu\mu$  search.
- With excellent LHC performance comes the challenge of high rates and many simultaneous collisions (pileup).





- 3.8T superconducting solenoidal magnet with 6m diameter.

- **Tracker System:** silicon strip+ pixel system which reconstructs the trajectories of charged particles.

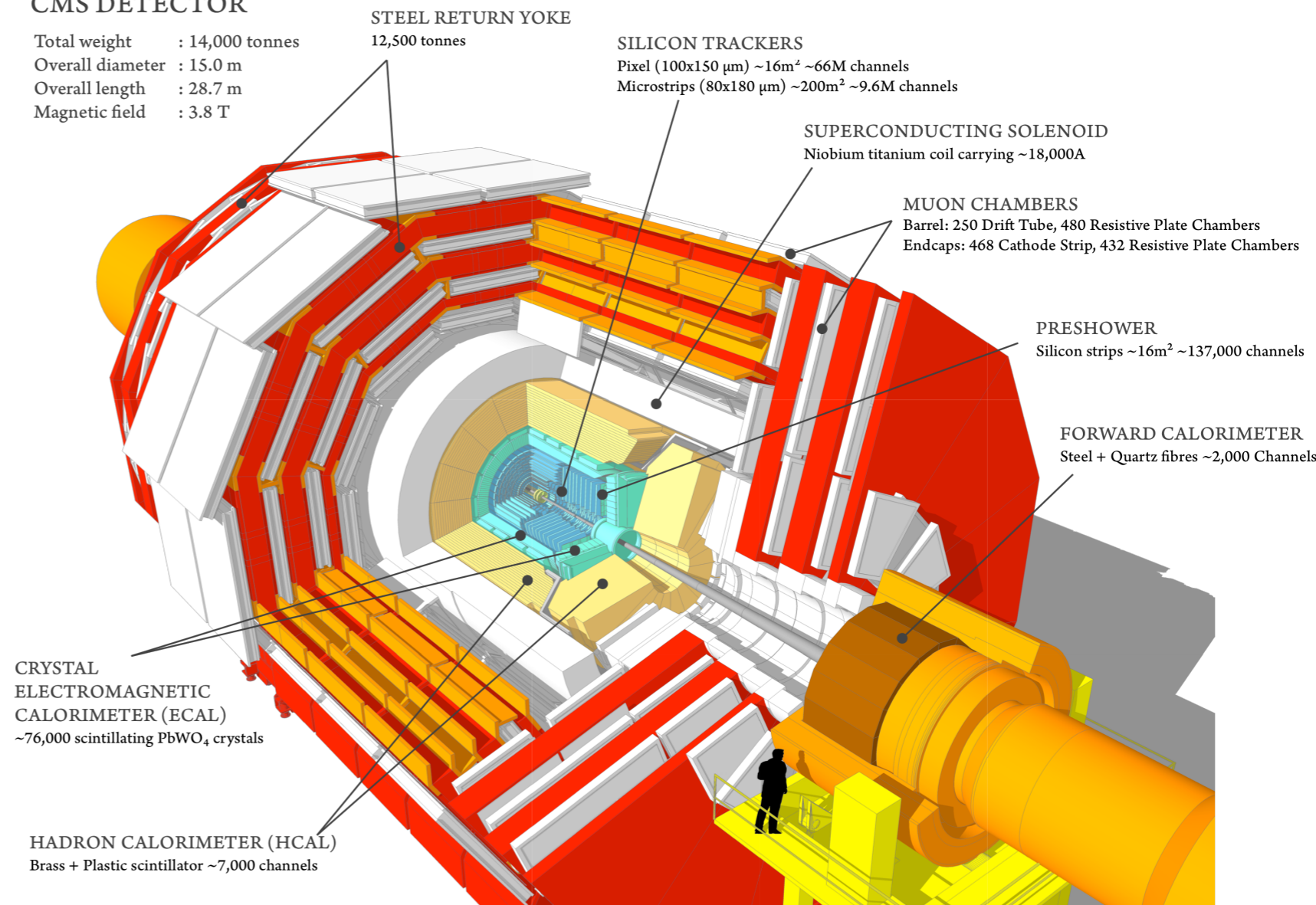
- **Electromagnetic calorimeter (ECAL):** scintillator made from lead tungstate crystals sensitive to energy deposits from electrons and photons.

- **Hadronic calorimeter (HCAL):** brass scintillator sensitive to energy deposits from hadrons, mainly pions and kaons.

- Gas ionization chambers for **muon detection**.

## CMS DETECTOR

Total weight : 14,000 tonnes  
 Overall diameter : 15.0 m  
 Overall length : 28.7 m  
 Magnetic field : 3.8 T



Observable	VBF-SB	VBF-SR
Number of loose (medium) b-tagged jets		$\leq 1$ (0)
Number of selected muons		$= 2$
Number of selected electrons		$= 0$
Jet multiplicity ( $p_T > 25$ GeV, $ \eta  < 4.7$ )		$\geq 2$
Leading jet $p_T$		$\geq 35$ GeV
Dijet mass ( $m_{jj}$ )		$\geq 400$ GeV
Pseudorapidity separation ( $ \Delta\eta_{jj} $ )		$\geq 2.5$
Dimuon invariant mass	$110 < m_{\mu\mu} < 115$ GeV or $135 < m_{\mu\mu} < 150$ GeV	$115 < m_{\mu\mu} < 135$ GeV

DNN bin	Total signal	VBF (%)	ggH (%)	Bkg. $\pm \Delta B$	Data	S/(S+B) (%)	$S/\sqrt{B}$
1-3	19.5	30	70	$8890 \pm 67$	8815	0.22	0.21
4-6	11.6	57	43	$394 \pm 8$	388	2.86	0.58
7-9	8.43	73	27	$103 \pm 4$	121	7.56	0.83
10	2.30	85	15	$15.1 \pm 1.4$	18	13.2	0.59
11	2.15	88	12	$9.1 \pm 1.2$	10	19.1	0.71
12	2.10	87	13	$5.8 \pm 1.1$	6	26.6	0.87
13	1.87	94	6	$2.6 \pm 0.9$	7	41.8	1.16

Observable	Selection
Number of loose (medium) b-tagged jets	$\leq 1$ (0)
Number of selected muons	$= 2$
Number of selected electrons	$= 0$
VBF selection veto	if $N_{\text{jets}} \geq 2$ $m_{jj} < 400 \text{ GeV}$ or $ \Delta\eta_{jj}  < 2.5$ or $p_T(j_1) < 35 \text{ GeV}$

Event category	Total signal	ggH (%)	VBF (%)	Other (%)	HWHM (GeV)	Bkg. @HWHM	Data @HWHM	S/(S+B) (%) @HWHM	S/ $\sqrt{B}$ @HWHM
ggH-cat1	268	93.7	2.9	3.4	2.12	86 360	86 632	0.20	0.60
ggH-cat2	312	93.5	3.4	3.1	1.75	46 350	46 393	0.46	0.98
ggH-cat3	131	93.2	4.0	2.8	1.60	12 660	12 738	0.70	0.80
ggH-cat4	126	91.5	5.5	3.0	1.47	8260	8377	1.03	0.96
ggH-cat5	53.8	83.5	14.3	2.2	1.50	1680	1711	2.16	0.91

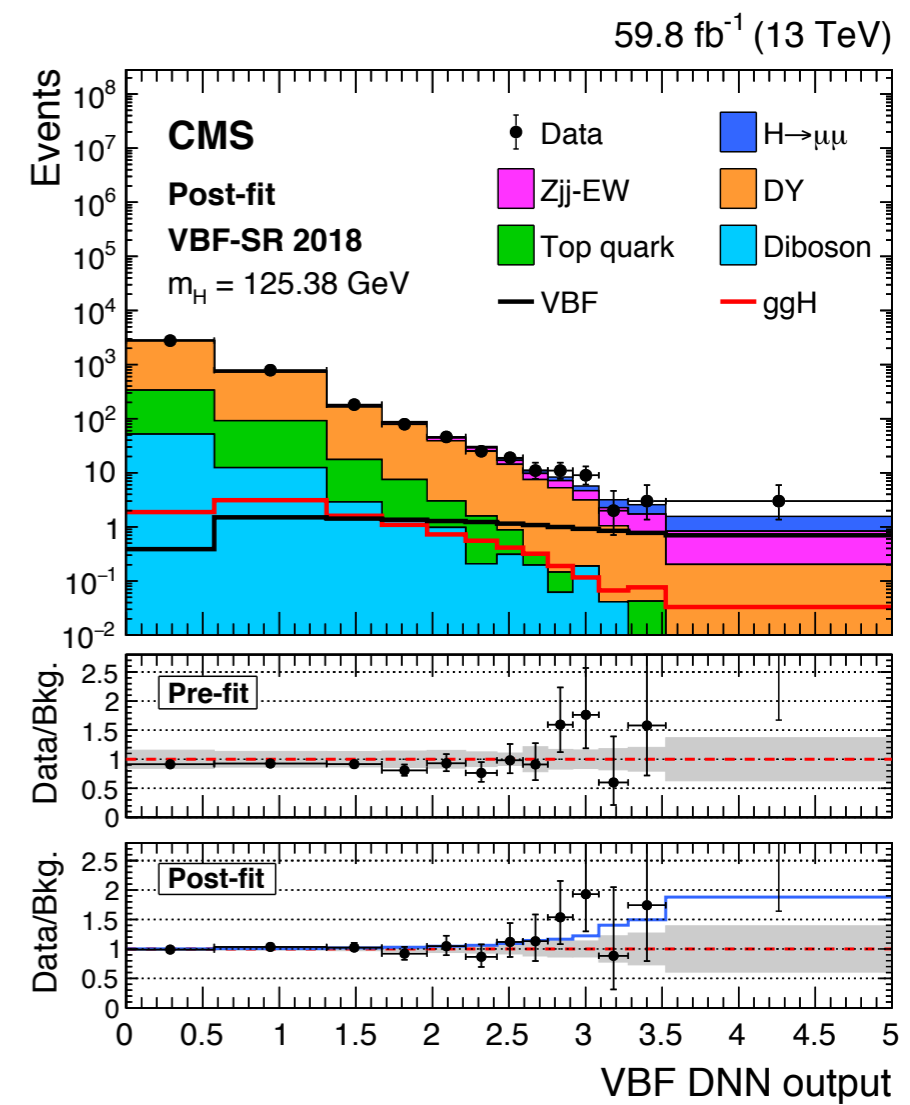
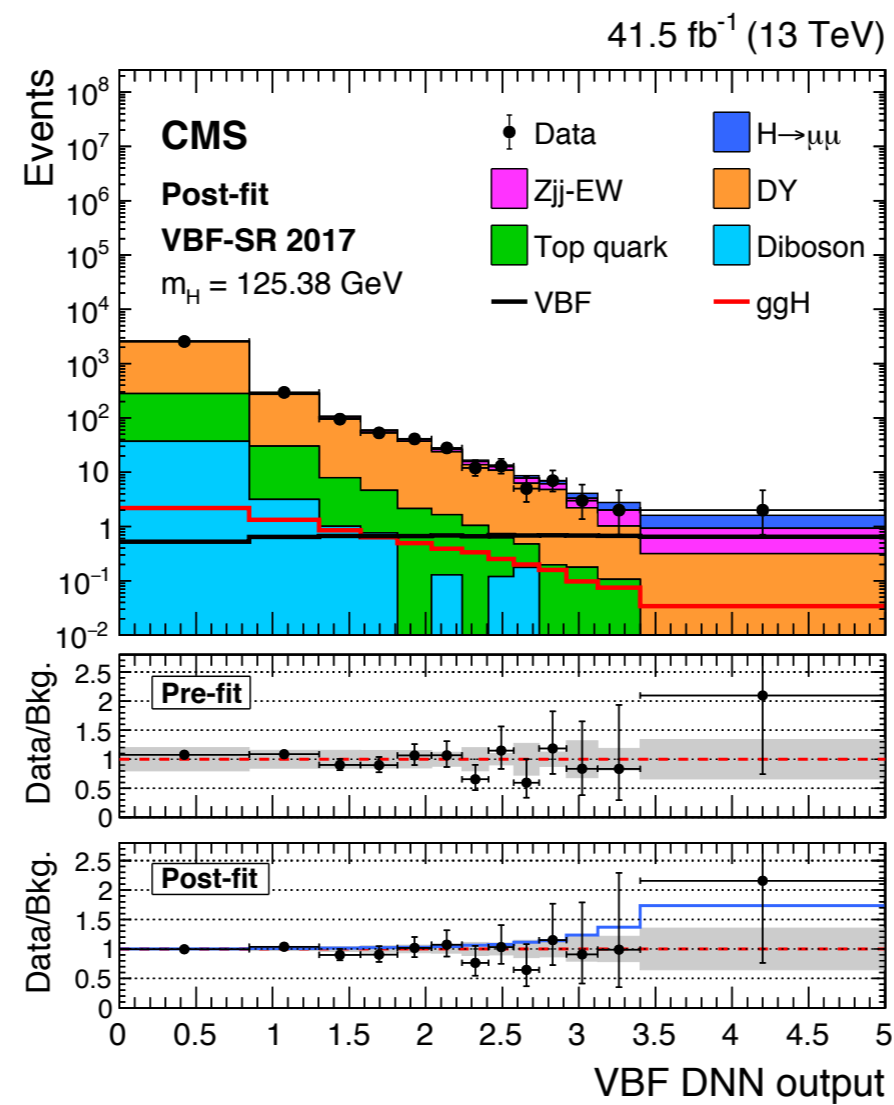
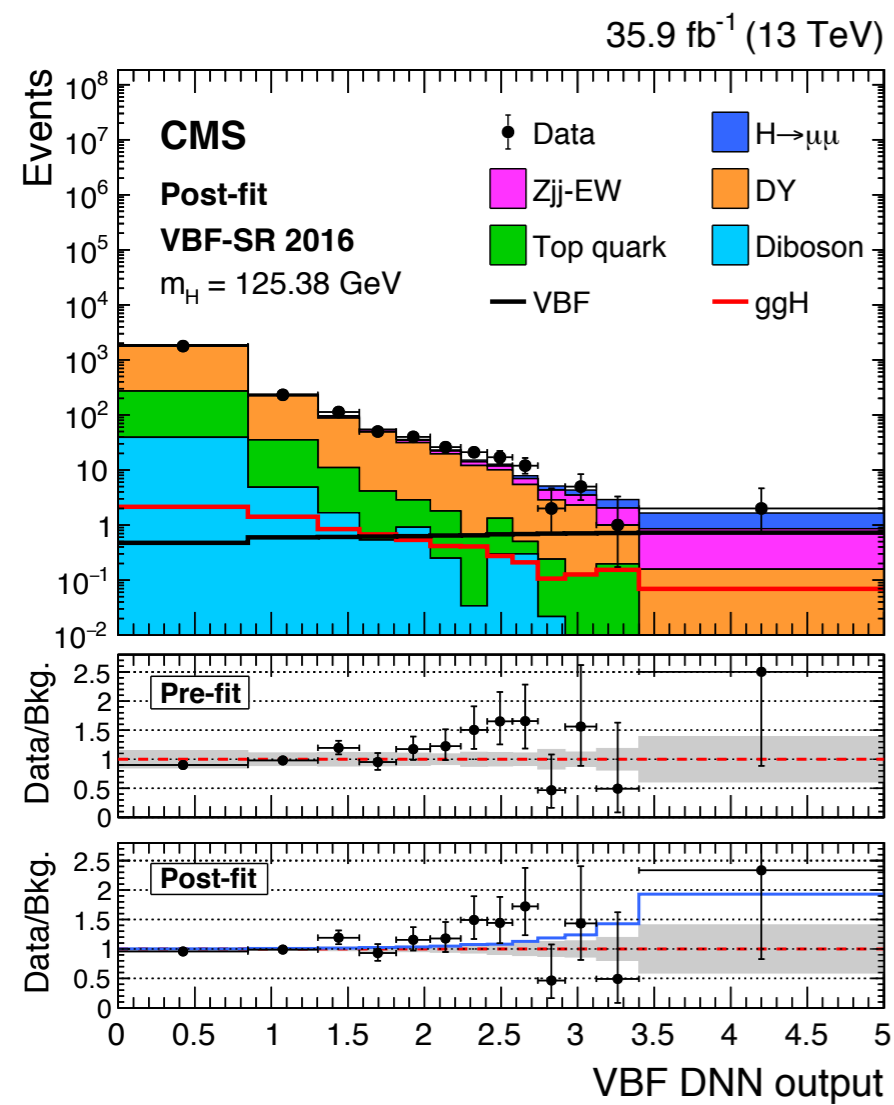
Observable	ttH hadronic	ttH leptonic
Number of b quark jets	>0 medium or >1 loose b-tagged jets	
Number of leptons ( $N(\ell = \mu, e)$ )	=2	=3 or 4
Lepton charge ( $q(\ell)$ )	$\sum q(\ell) = 0$	$N(\ell) = 3 (4) \rightarrow \sum q(\ell) = \pm 1 (0)$
Jet multiplicity ( $p_T > 25 \text{ GeV},  \eta  < 4.7$ )	$\geq 3$	$\geq 2$
Leading jet $p_T$	>50 GeV	>35 GeV
Z boson veto	—	$ m_{\ell\ell} - m_Z  > 10 \text{ GeV}$
Low-mass resonance veto	—	$m_{\ell\ell} > 12 \text{ GeV}$
Jet triplet mass	$100 < m_{jjj} < 300 \text{ GeV}$	—

Event category	Total signal	ttH (%)	ggH (%)	VH (%)	Other (%)	HWHM (GeV)	Bkg. fit function	Bkg. @HWHM	Data @HWHM	S/(S+B) (%) @HWHM	$S/\sqrt{B}$ @HWHM
ttHhad-cat1	6.87	32.3	40.3	17.2	10.2	1.85	Bern(2)	4298	4251	1.07	0.07
ttHhad-cat2	1.62	84.3	3.8	5.6	6.2	1.81	Bern(2)	82.0	89	1.32	0.12
ttHhad-cat3	1.33	94.0	0.3	1.3	4.4	1.80	S-Exp	12.3	12	6.87	0.26
ttHlep-cat1	1.06	85.8	—	4.7	9.5	1.92	Exp	9.00	13	7.09	0.22
ttHlep-cat2	0.99	94.7	—	1.0	4.3	1.75	Exp	2.08	4	24.5	0.47

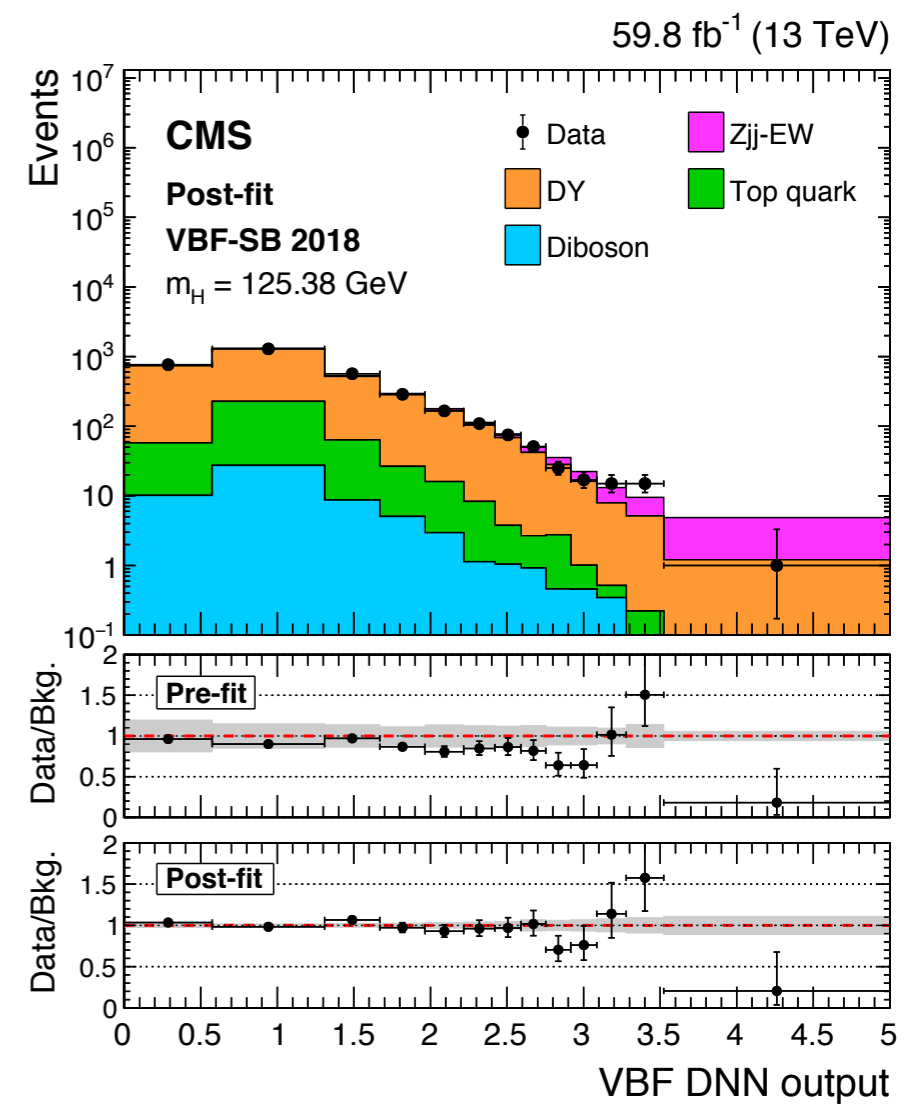
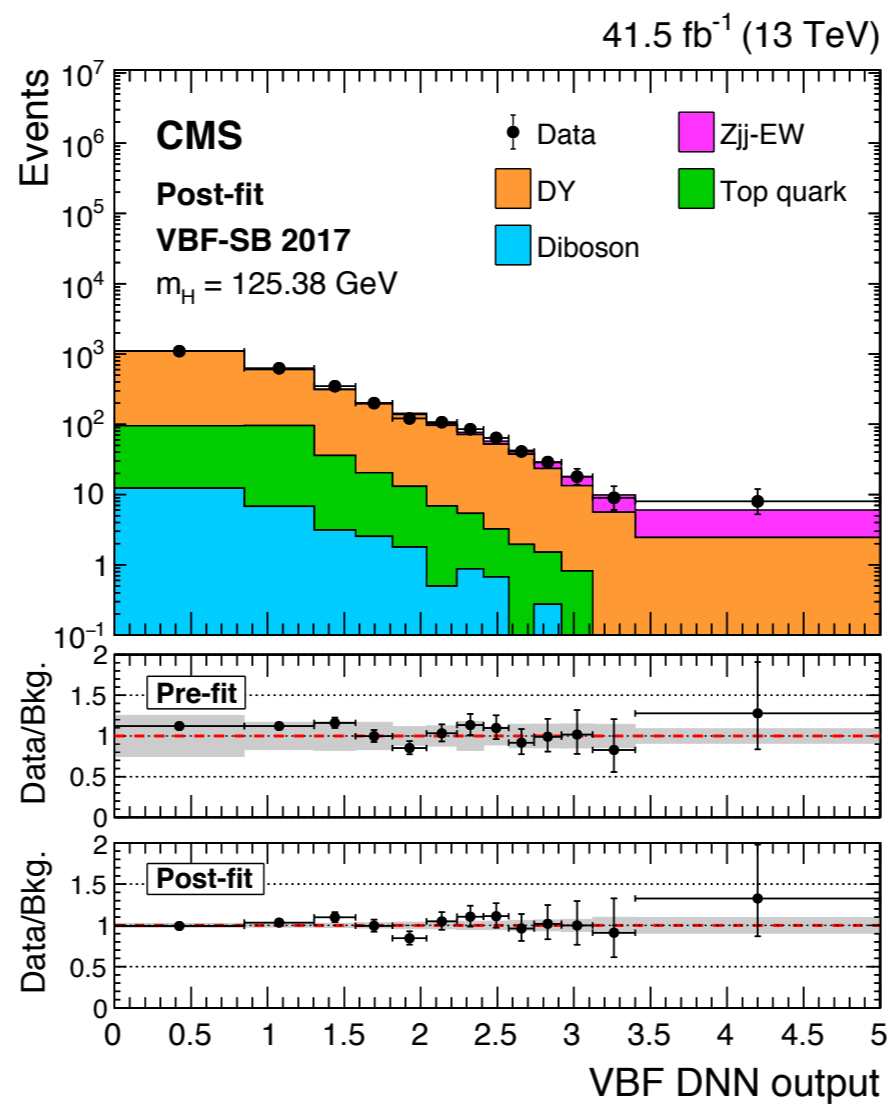
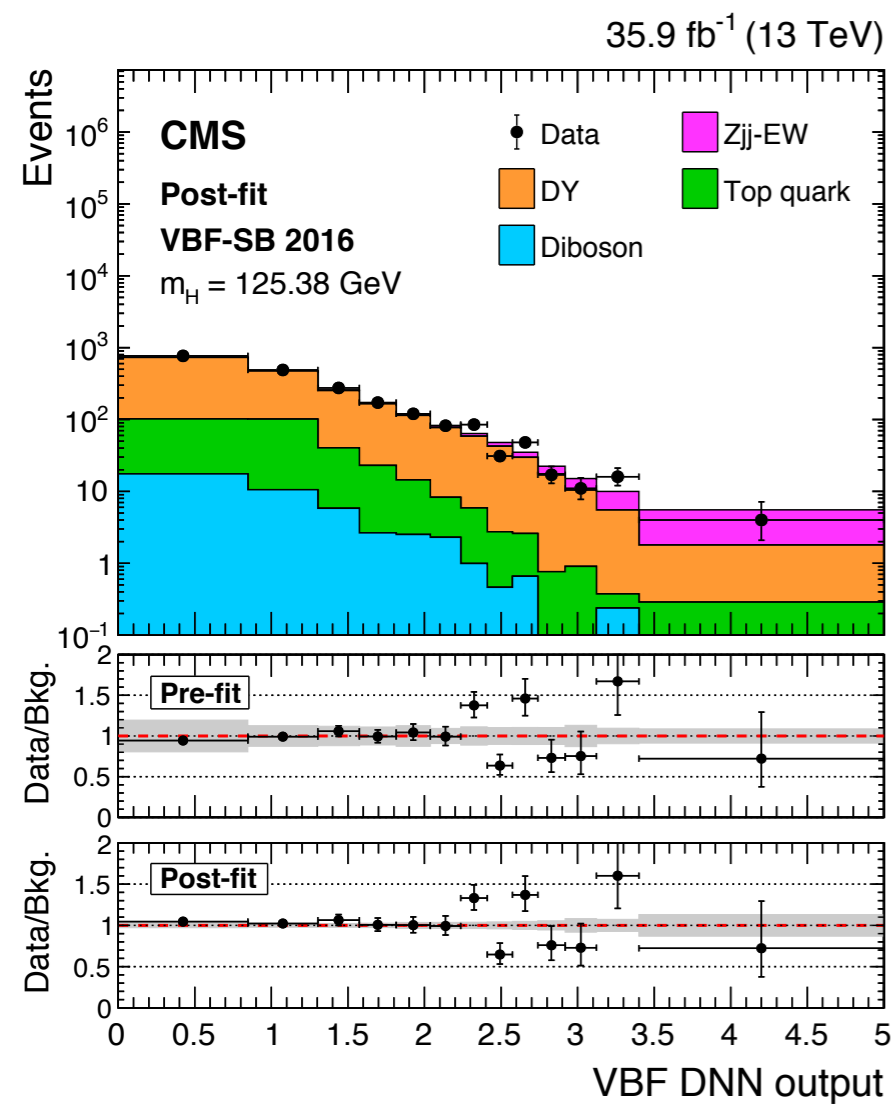
Observable	WH leptonic		ZH leptonic	
	$\mu\mu\mu$	$\mu\mu e$	$4\mu$	$2\mu 2e$
Number of loose (medium) b-tagged jets	$\leq 1$ (0)	$\leq 1$ (0)	$\leq 1$ (0)	$\leq 1$ (0)
Number of selected muons	$= 3$	$= 2$	$= 4$	$= 2$
Number of selected electrons	$= 0$	$= 1$	$= 0$	$= 2$
Lepton charge ( $q(\ell)$ )	$\sum q(\ell) = \pm 1$		$\sum q(\ell) = 0$	
Low-mass resonance veto	$m_{\ell\ell} > 12 \text{ GeV}$			
$N(\mu^+ \mu^-)$ pairs with $110 < m_{\mu\mu} < 150 \text{ GeV}$	$\geq 1$	$= 1$	$\geq 1$	$= 1$
$N(\mu^+ \mu^-)$ pairs with $ m_{\mu\mu} - m_Z  < 10 \text{ GeV}$	$= 0$	$= 0$	$= 1$	$= 0$
$N(e^+ e^-)$ pairs with $ m_{ee} - m_Z  < 20 \text{ GeV}$	$= 0$	$= 0$	$= 1$	$= 1$

Event category	Total signal	WH (%)	qqZH (%)	ggZH (%)	$t\bar{t}H+tH$ (%)	HWHM (GeV)	Bkg. fit function	Bkg. @HWHM	Data @HWHM	S/(S+B) (%) @HWHM	S/ $\sqrt{B}$ @HWHM
WH-cat1	0.82	76.2	9.6	1.6	12.6	2.00	BWZ $\gamma$	32.0	34	1.54	0.09
WH-cat2	1.72	80.1	9.1	1.5	9.3	1.80	BWZ	23.1	27	4.50	0.23
WH-cat3	1.14	85.7	6.7	1.8	4.8	1.90	BWZ	5.48	4	12.6	0.35
ZH-cat1	0.11	—	82.8	17.2	—	2.07	BWZ	2.05	4	3.29	0.05
ZH-cat2	0.31	—	79.6	20.4	—	1.80	BWZ	2.19	4	8.98	0.14

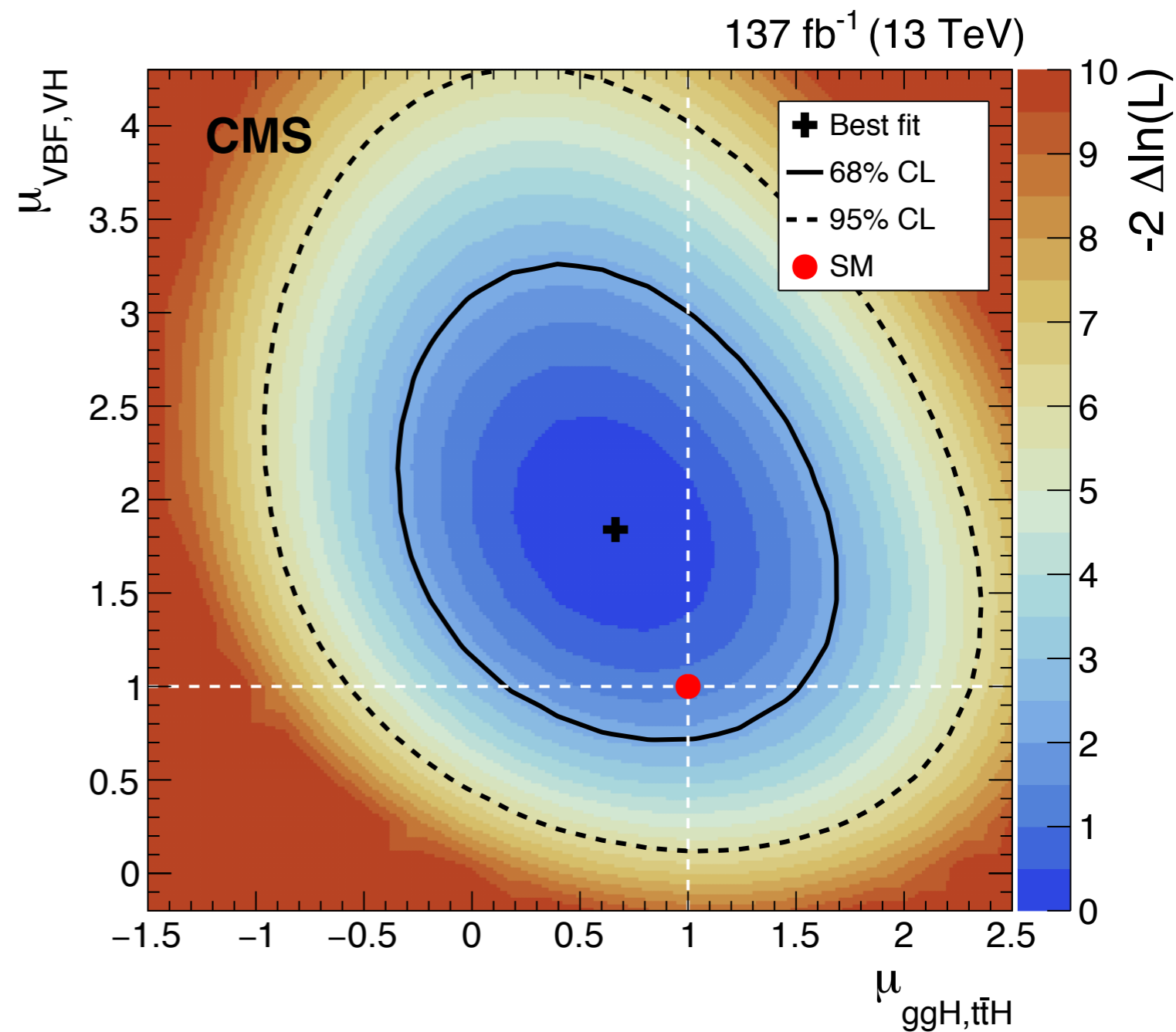
VBF signal region,  
 $115 < m(\mu\mu) < 135 \text{ GeV}$



VBF mass sideband,  
 $110 < m(\mu\mu) < 115 \text{ GeV}$ ,  
 $135 < m(\mu\mu) < 150 \text{ GeV}$

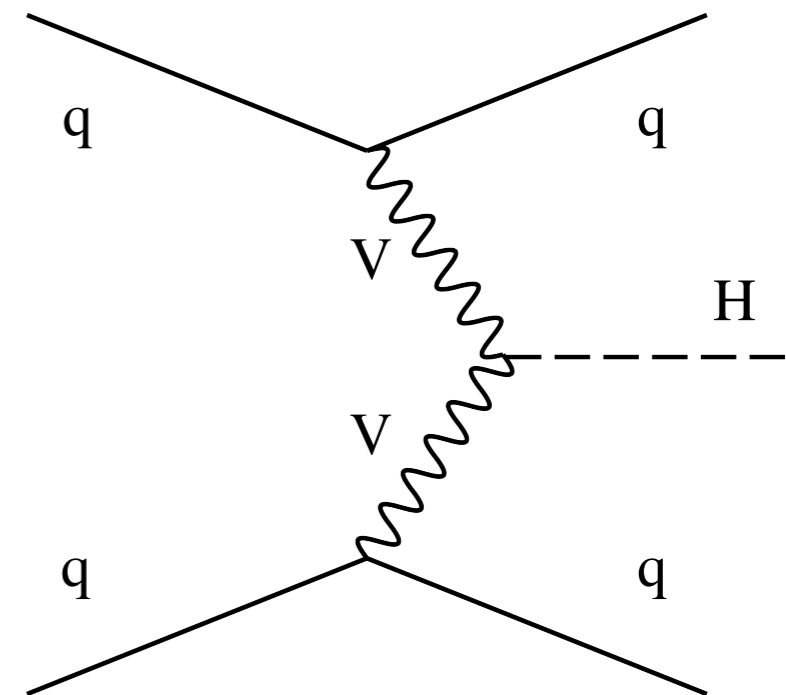


- Independent fit for Higgs boson production channels sensitive to vector boson couplings (VBF, VH) and top quark coupling (ggH, ttH).
- Result well consistent with SM within uncertainties.



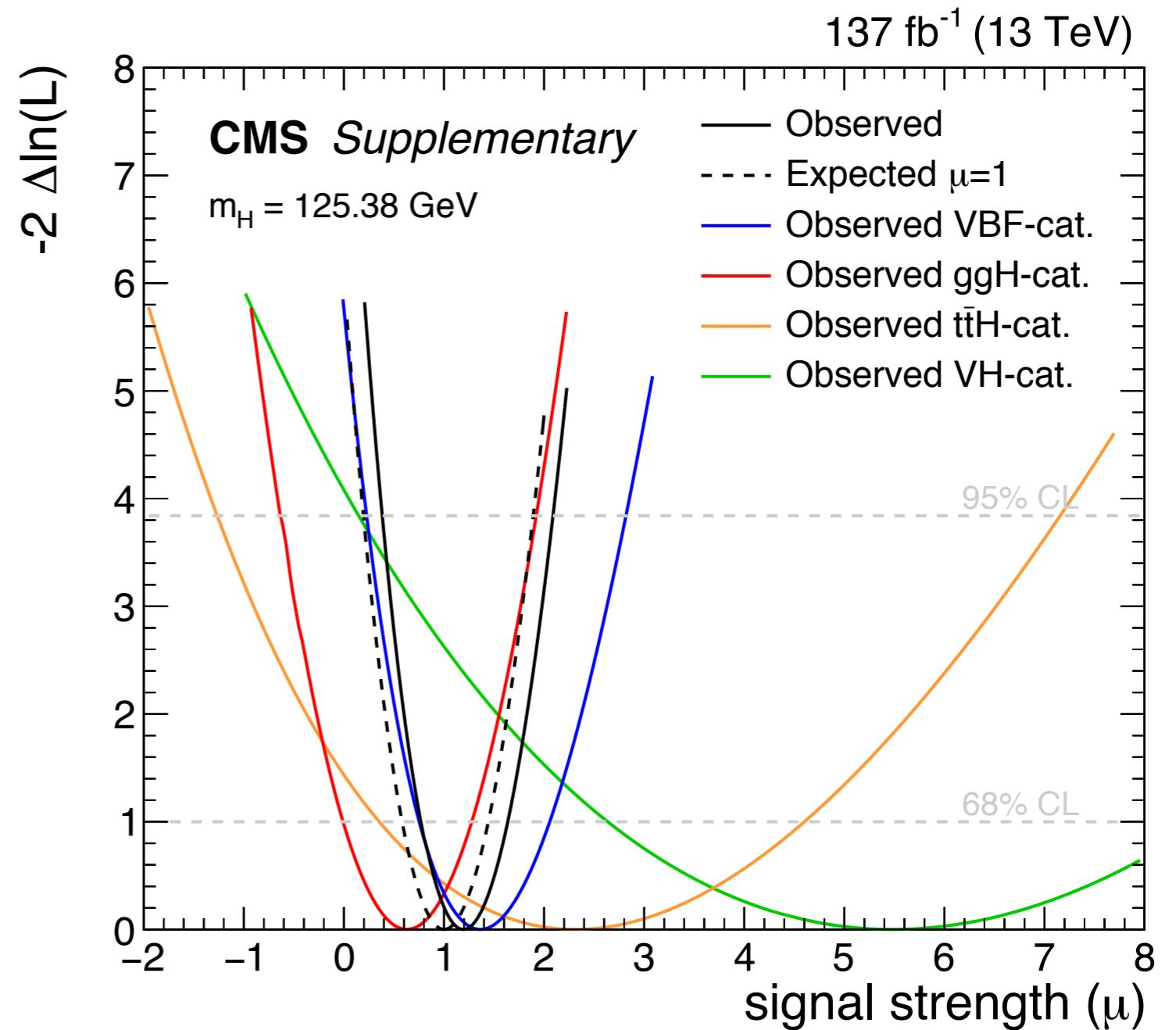


- VBF process incoming and outgoing quark lines are color-connected (pure EW exchange).
- Until recently, PYTHIA did not account for this effect (default “global recoil” scheme).
  - “Dipole recoil” scheme recently implemented into PYTHIA that takes this effect into account.
  - Herwig7 default angular-ordered shower considers effect similar to PYTHIA with dipole recoil.
- Private VBF  $H \rightarrow \mu\mu$  signal samples generated with PYTHIA dipole recoil (nominal prediction) and HERWIG7 (to assess systematic uncertainty).

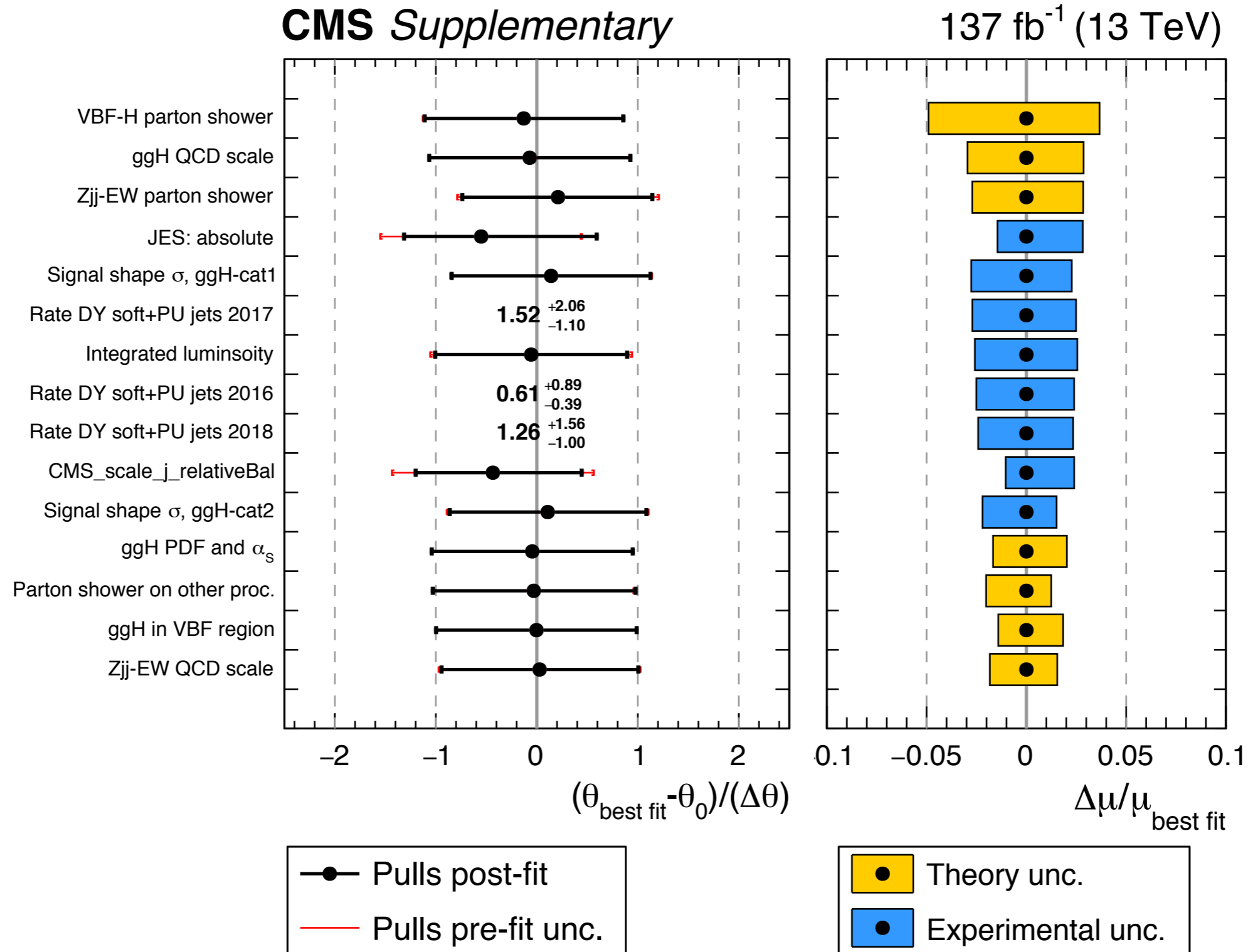


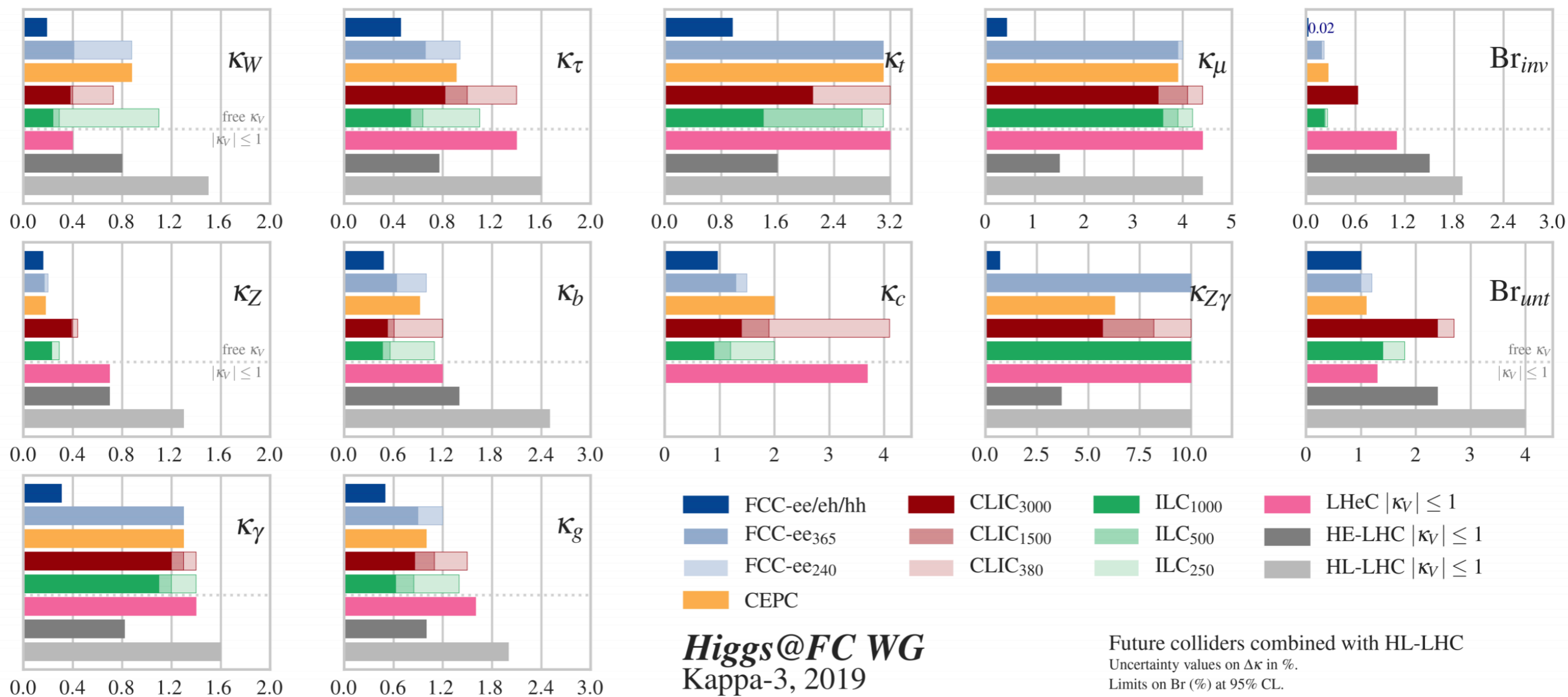
\*discussed within VBF HXSWG and recent dedicated theory paper [arXiv:2003.12435](https://arxiv.org/abs/2003.12435)

- Observed log-likelihood ratios as a function of signal strength for the combined result as well as the individual channels.
- For the combination, also the expected likelihood shape with  $\mu = 1$  signal injected.



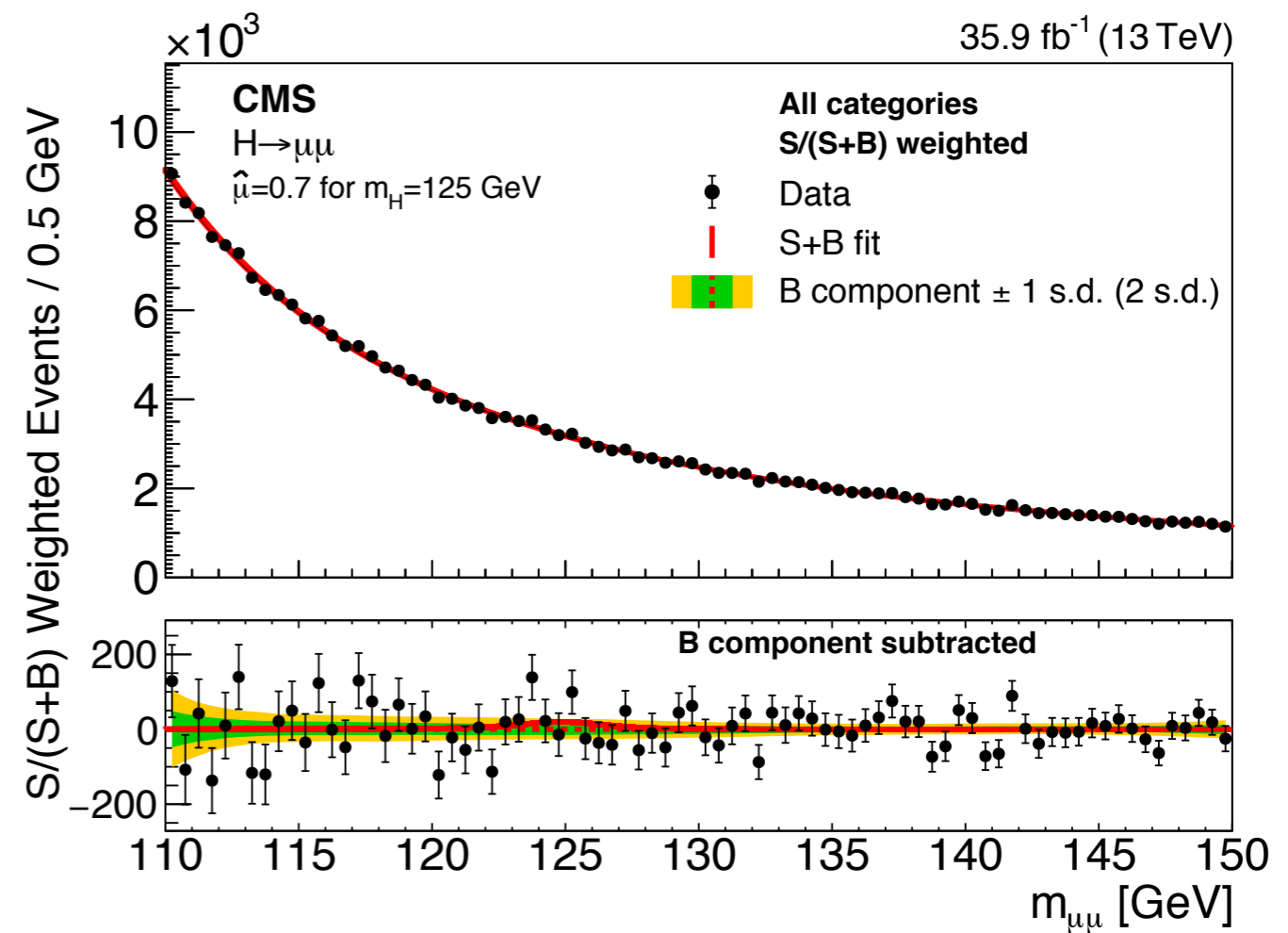
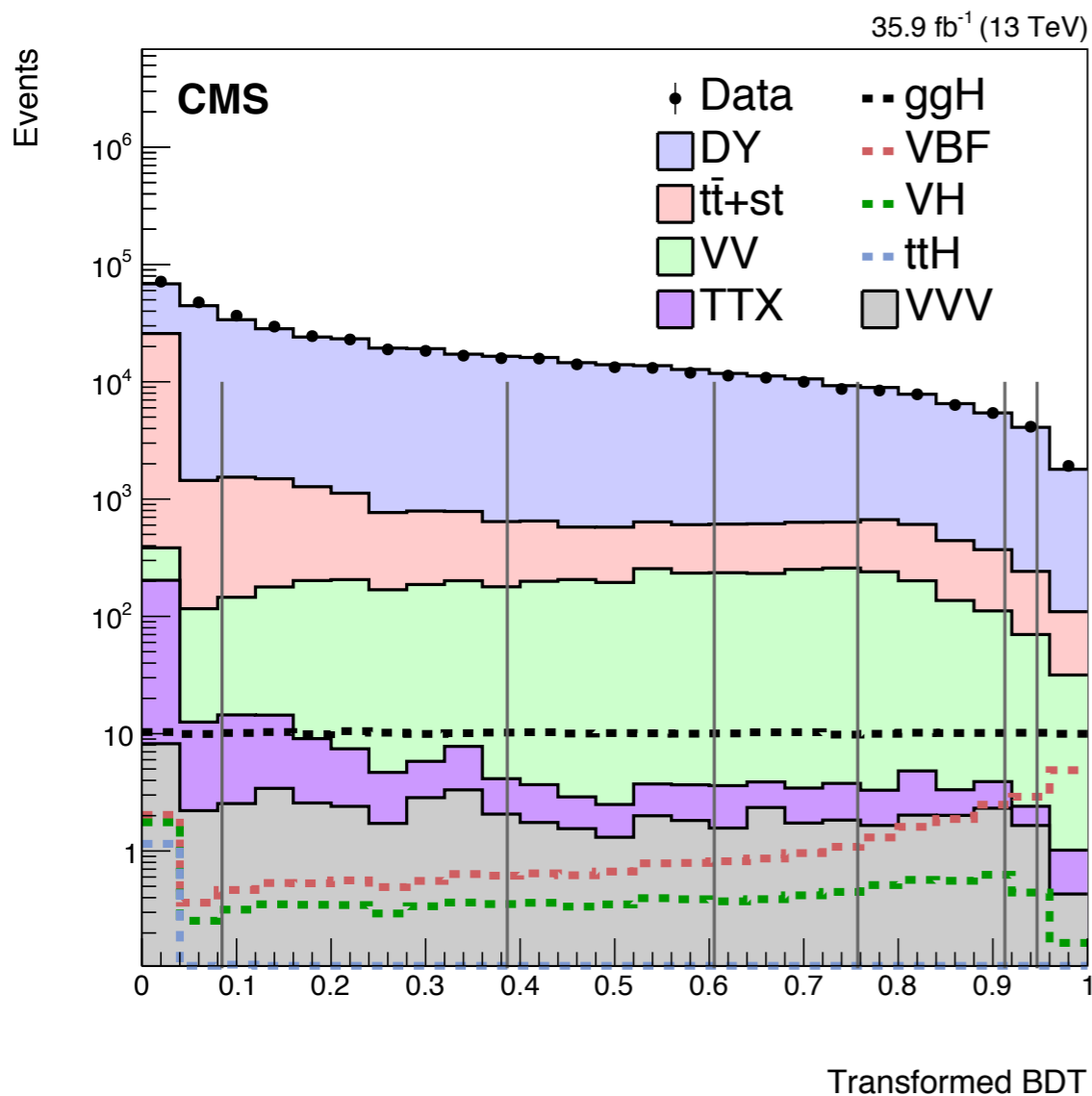
*Overall impact of systematics uncertainties on measurement is a few percent.*





[From Physics Briefing Book](#)

- With 35.9 fb<sup>-1</sup> 13 TeV data:
  - Observed (expected) significance 0.6 (0.9) $\sigma$ , signal strength  $\mu = 0.7 \pm 1.0$
- Combined with 7 and 8 TeV data:
  - Observed (expected) significance 0.9 (1.0) $\sigma$ , signal strength  $\mu = 1.0 \pm 1.0$



- SingleMuon primary data sets used by all channels.
- Background simulation (specifically requested for  $H \rightarrow \mu\mu$ ):
  - DY Madgraph samples at NLO with  $m(\mu\mu)$  [105,160] GeV filter, including set of VBF-enriched ( $m_{jj,GEN} > 350$  GeV) samples.
  - VBF Z Madgraph samples at LO with Herwig PS\* and  $m(\mu\mu)$  [105,160] GeV filter.
    - Detailed studies of stability of prediction vs. Madgraph version and  $p_T(j)$  minimum threshold.
- Signal simulation:
  - ggH signal: MG\_aMC at NLO with up to two partons in final state at ME level
  - VBF signal: POWHEG interfaced with PYTHIA parton shower with dipole recoil shower (more details in backup)
  - VH, ttH signal: POWHEG + PYTHIA PS

\*as studied extensively in CMS VBF Z measurement:

[Eur. Phys. J. C 78 \(2018\) 589](#)

\*highlighting just the most relevant MC samples used

## Muons

- Muons passing medium ID and loose PF isolation.
- $p_T > 26-29$  (20) GeV,  $|\eta| < 2.4$
- Momentum scale and resolution calibration with Rochester corrections.
- FSR recovery: strategy inspired by H(4l) and optimized for  $H \rightarrow \mu\mu$ .
  - Negligible  $H \rightarrow Z\gamma$
- GeoFit correction: using beam spot as additional track constraint to improve resolution.
  - 3-10% improvement in  $\sigma(m_{\mu\mu})$ .

## Jets

- AK4 CHS jets with  $p_T > 25$  GeV and  $|\eta| < 4.7$
- Loose (tight) jet ID in 2016 (2017/2018).
- Loose pileup jet ID for jets with  $p_T < 50$  GeV.
- Dedicated 2017 pileup jet ID training  $\Rightarrow$  15% improvement in 2017 signal efficiency.
- Latest JEC applied, JER not applied but used for systematic uncertainty.

## Electrons

- $p_T > 20$  GeV and  $|\eta| < 2.5$
- Passing MVA ID WP90

## B-tagging

- $p_T > 25$  GeV and  $|\eta| < 2.5$
- Passing DeepCSV loose or medium WPs.

### Pileup re-weight

- Applied taking the certified pileup profile in data
- **Uncertainty** estimated by varying the minimum bias cross section

### L1 prefiring

- In 2016/17, **mis-timed ECAL TPs** lead to inefficiency in the L1 trigger
- **Corrections** measured from a set of **unpreferable events** by JetMET
- **Corrections applied** in the analysis and **only relevant for VBF channel**

### DY $p_T(Z)$ spectrum

- DY MC poorly describe the data for  $p_T(\mu\mu) < 40$  GeV
- This is due to **missing resummation** effects [[10.1007/JHEP12\(2019\)061](https://arxiv.org/abs/10.1007/JHEP12(2019)061)]
- **Reweighting** performed using **data** with **70**  $< m(\mu\mu) < 110$  GeV, as a function of  $p_T(\mu\mu)$  and  $N_{\text{jets}}$

### ggH $p_T(H)$ spectrum

- **Reweighed to NNLOPS** in bins of  $N_{\text{jets}}$  at the generator level