

Estimate of the uncertainties

$$\begin{aligned} \frac{d\sigma}{dq_T} &\propto H(M_{\ell\ell}, \mu_R) && : \text{Hard factor} \\ &\times \exp[S_{\text{PT}+\text{NP}}(\mu_R, \mu_b)] && : \text{Evolution} \\ &\times C_{1,2}(\mu_b) f_{\text{NP}}^{(1,2)}(\mu_b) && : \text{Matching onto collinear} \\ &\times \underbrace{\Gamma_{1,2}^{\text{DGLAP}}(\mu_b, \mu_F) f_1(\mu_F) f_2(\mu_F)}_{f_1(\mu_b) f_2(\mu_b)} && : \text{Collinear PDFs} \end{aligned}$$

🍏 Theoretical uncertainty estimate on **N³LL**:


- 🍏 variations of μ_R by a factor 2 up and down w.r.t. M_U ,
- 🍏 variations of μ_F by a factor 2 up and down w.r.t. M_U ,
- 🍏 estimate of the of the subleading logarithmic corrections by including N⁴LL corrections in the Sudakov (mimicking **resummation scale variations**),
[G. Das, S.-O. Moch, A. Vogt, arXiv:1912.12920]
- 🍏 inclusion of non-perturbative effects as determined in the **PV19** fit.
[A. Bacchetta et al., arXiv:1912.07550]

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 **N⁴LL corrections** to the Sudakov: [G. Das, S.-O. Moch, A. Vogt, arXiv:1912.12920]

$$A_5 = (1.7 \pm 0.5, 1.1 \pm 0.5, 0.7 \pm 0.5) \cdot 10^5 \quad \text{for } n_f = 3, 4, 5.$$

$$B_4^{\text{DIS}} \Big|_{\text{appr}} = (10.68 \pm 0.01) \cdot 10^4 + (-2.025 \pm 0.032) \cdot 10^4 n_f + 798.0698 n_f^2 - 12.08488 n_f^3$$

 we used the configuration that gave the largest difference w.r.t. N³LL (and finally multiplied it by two both in the plus and minus directions).

 **Non-perturbative corrections** determined by a fit to data at N³LL (PV19): [A. Bacchetta et al., arXiv:1912.07550]

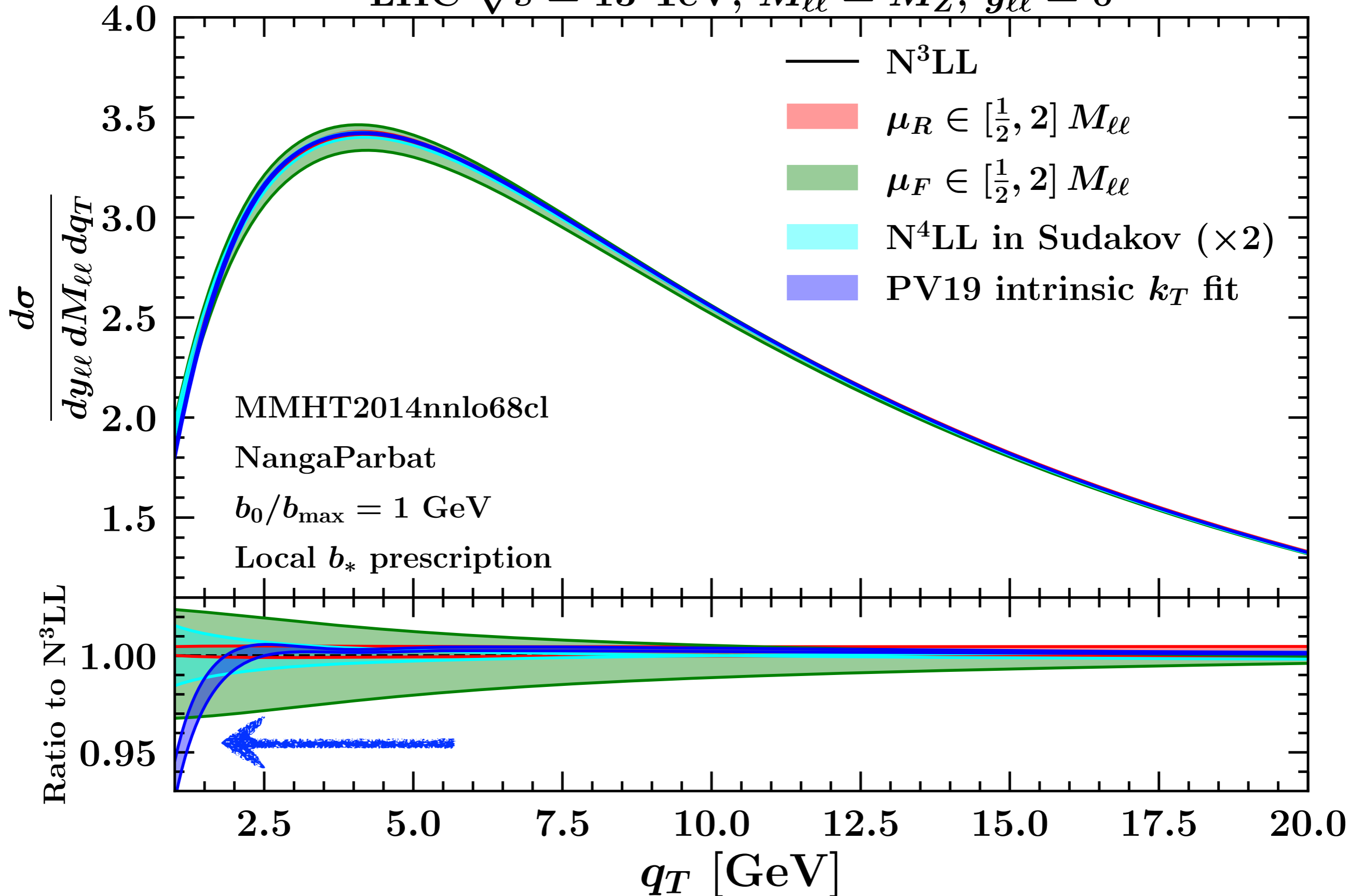
 Parameterisation used:

$$f_{\text{NP}}(x, \mu_b) \exp[S_{\text{NP}}(Q, \mu_b)] = \left[\frac{1 - \lambda}{1 + g_1(x) \frac{b^2}{4}} + \lambda \exp\left(-g_{1B}(x) \frac{b^2}{4}\right) \right] \times \exp\left[-(g_2 + g_{2B} b^2) \ln\left(\frac{Q^2}{Q_0^2}\right) \frac{b^2}{4}\right]$$

$$g_1(x) = \frac{N_1}{x\sigma} \exp\left[-\frac{1}{2\sigma^2} \ln^2\left(\frac{x}{\alpha}\right)\right] \quad g_{1B}(x) = \frac{N_{1B}}{x\sigma_B} \exp\left[-\frac{1}{2\sigma_B^2} \ln^2\left(\frac{x}{\alpha_B}\right)\right]$$

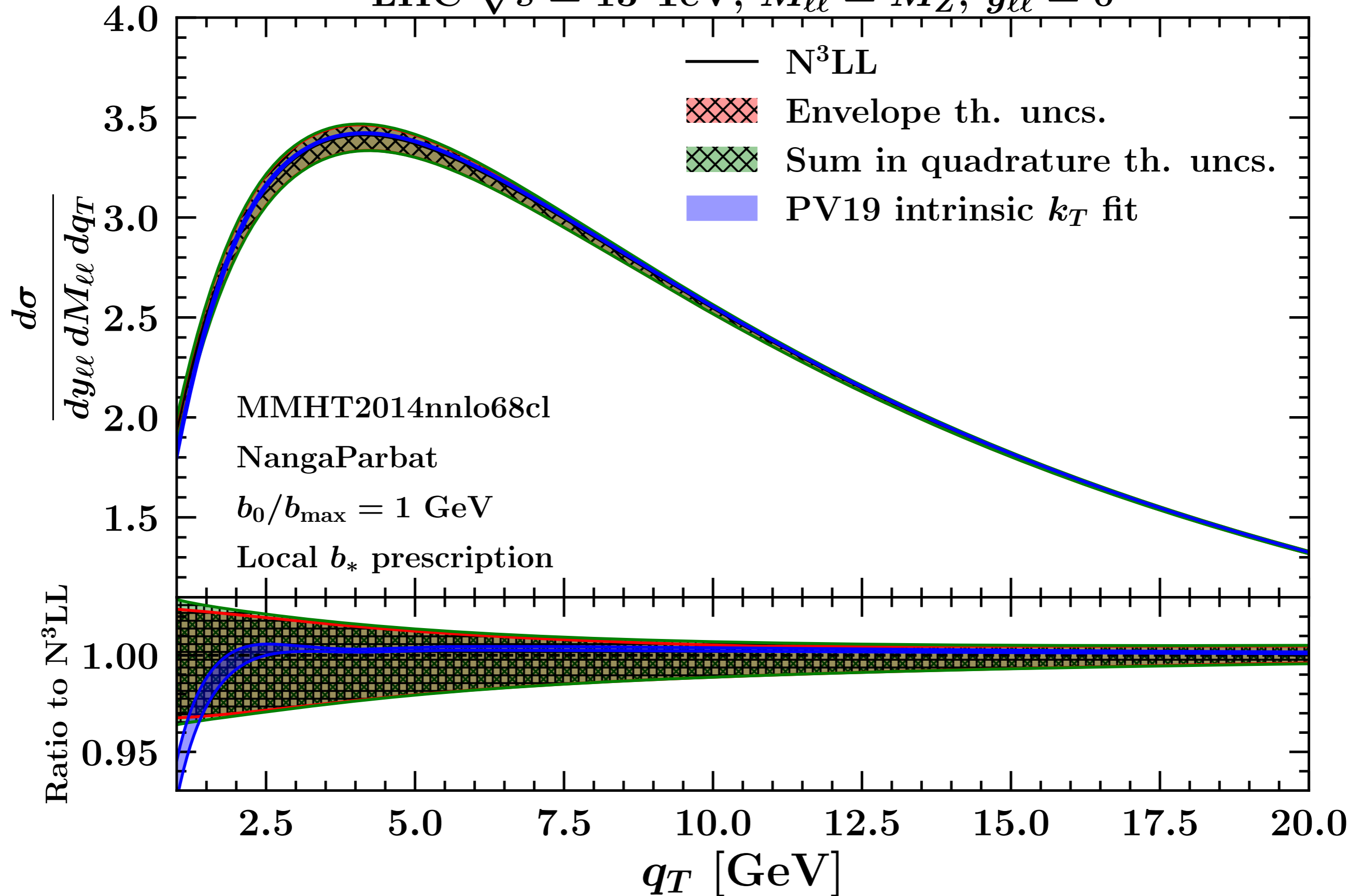
Estimate of the uncertainties

LHC $\sqrt{s} = 13$ TeV, $M_{\ell\ell} = M_Z$, $y_{\ell\ell} = 0$



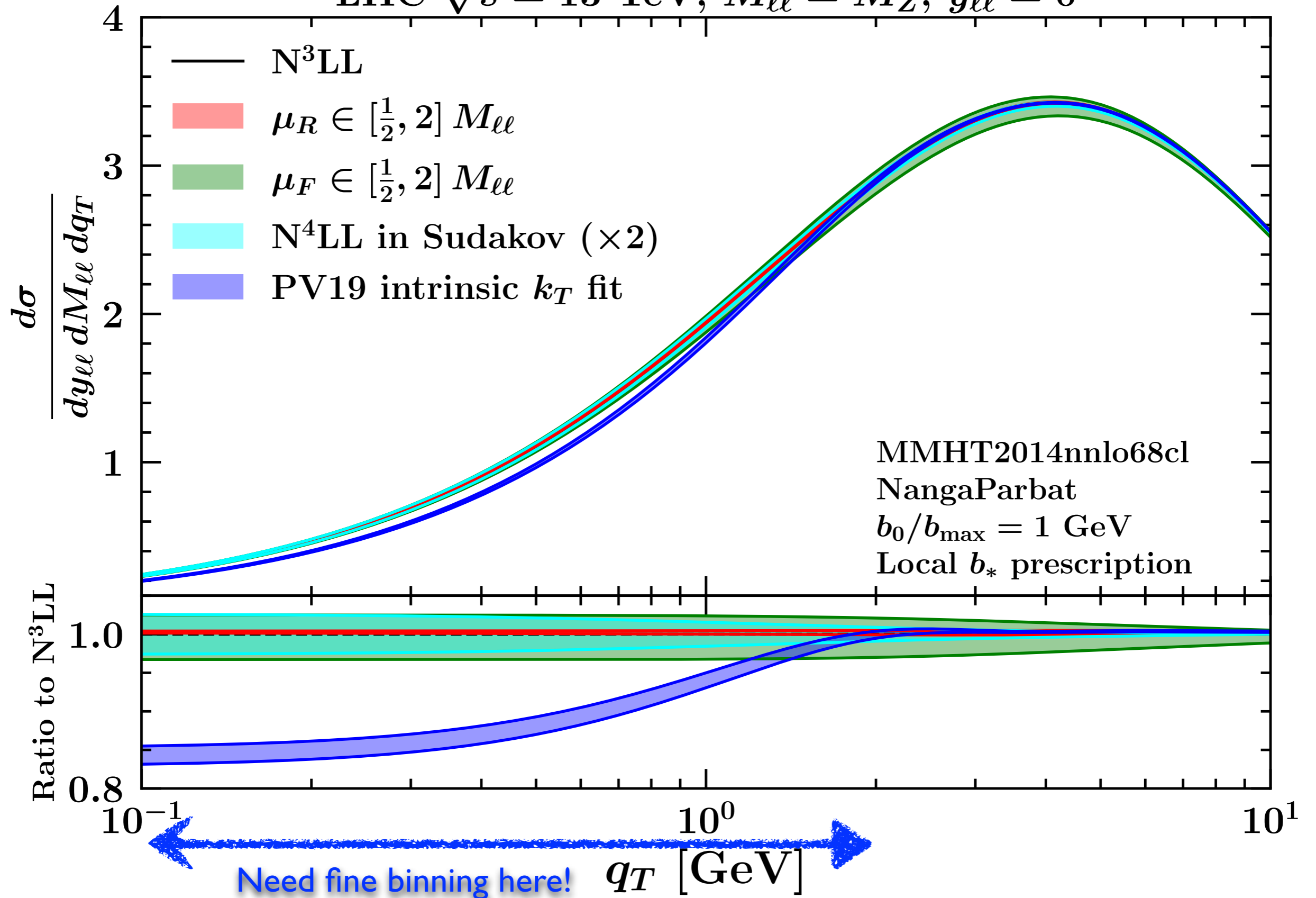
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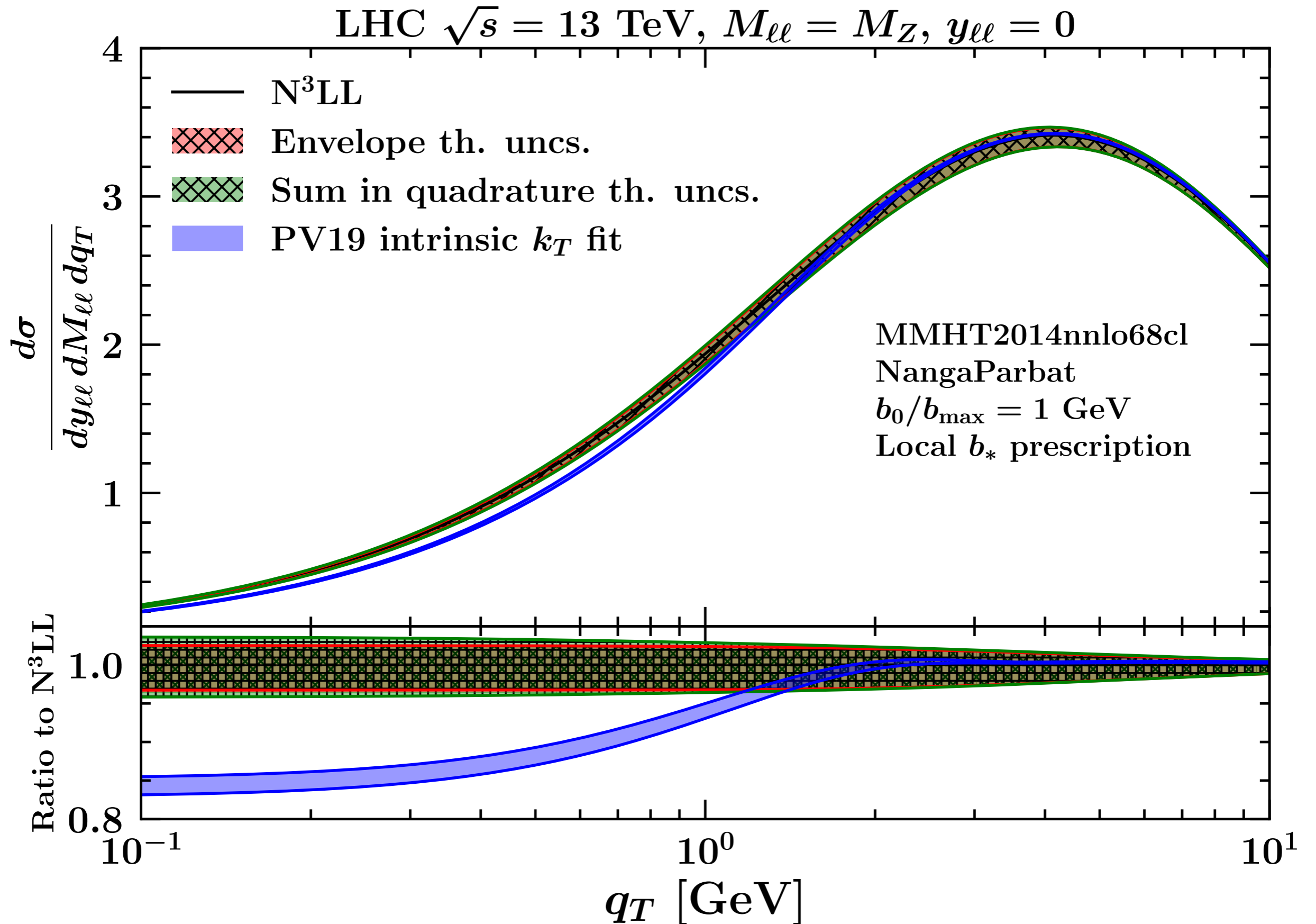


Estimate of the uncertainties

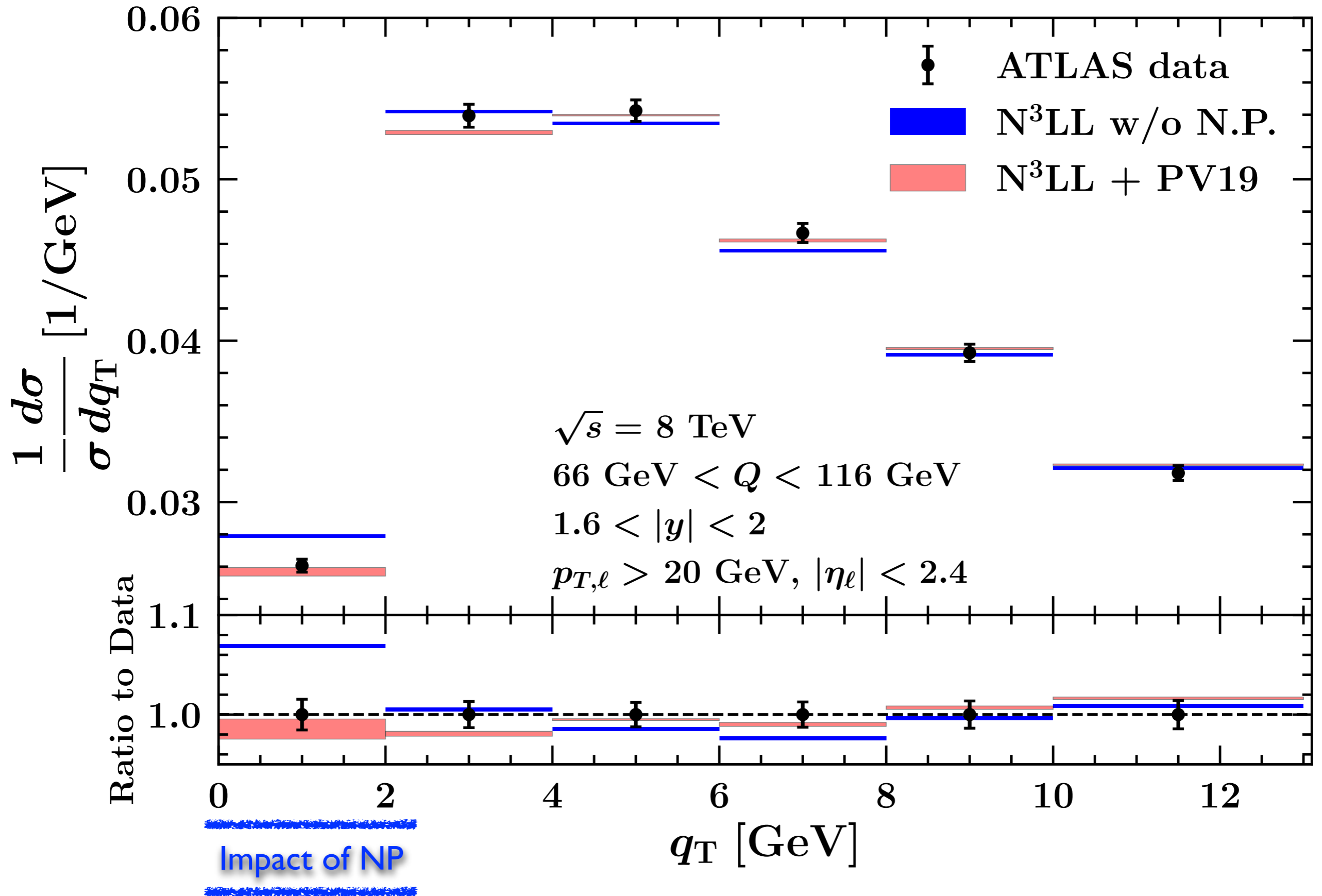
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Estimate of the uncertainties



Estimate of the uncertainties



Moving to level 3 (very preliminary)

