

HNL FLUXES GENERATION WITH MADGRAPH

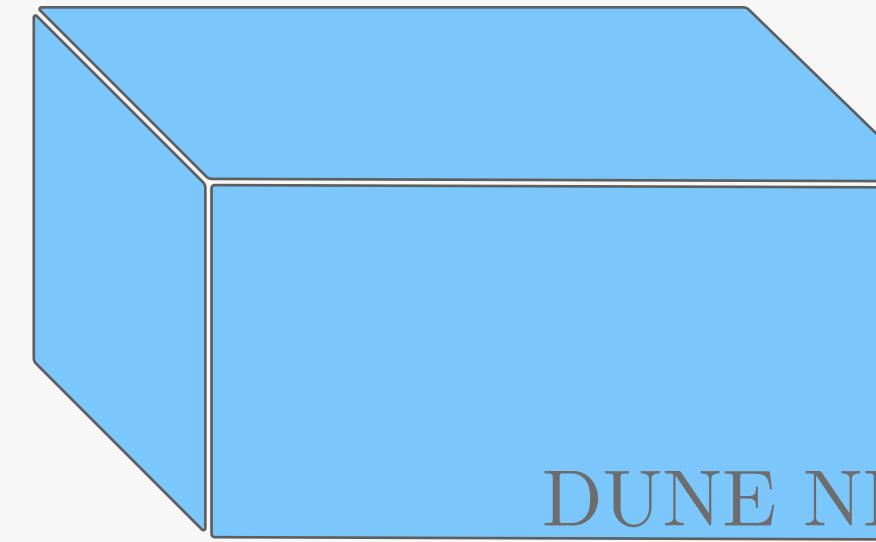
JOSU HERNANDEZ-GARCIA

INSTITUTE FOR THEORETICAL
PHYSICS



ELTE EÖTVÖS LORÁND
UNIVERSITY

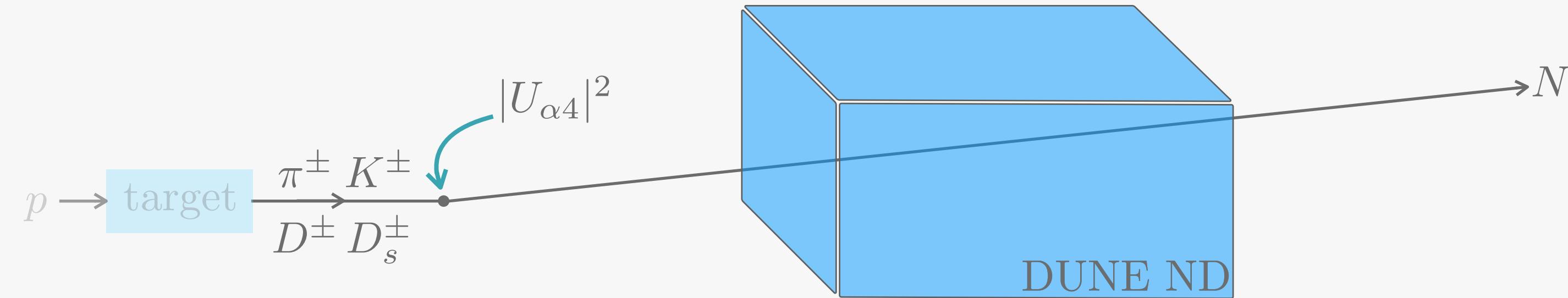
INGREDIENTS FOR HNL FLUXES GENERATION



- Fluxes of mesons produced in the target
 - π and K (D and D_s) from the TDR n-tuples*
 - D and D_s and τ simulated with Pythia + GEANT4 \rightarrow Z. Pavlovic

*most up to date optimized 3-horn design (1.5m target) by L. Fields et al.

INGREDIENTS FOR HNL FLUXES GENERATION

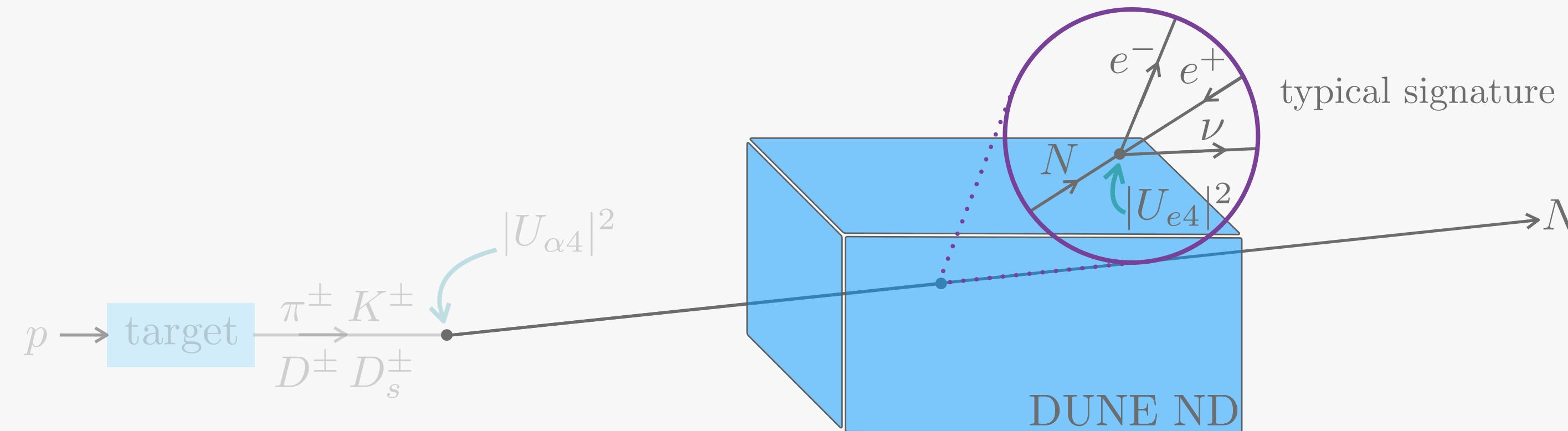


- Fluxes of mesons produced in the target
- Events of HNL production via meson decays

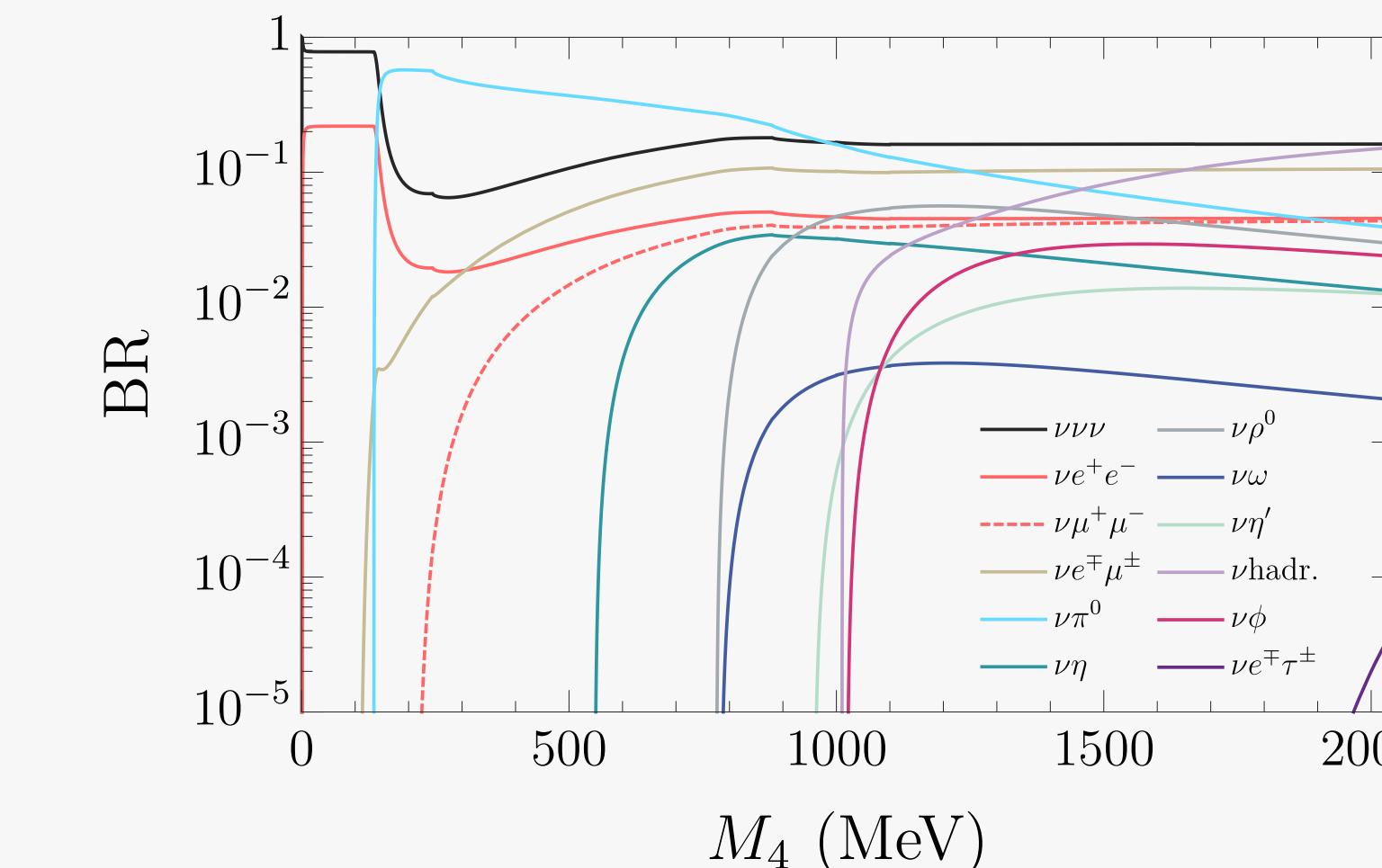
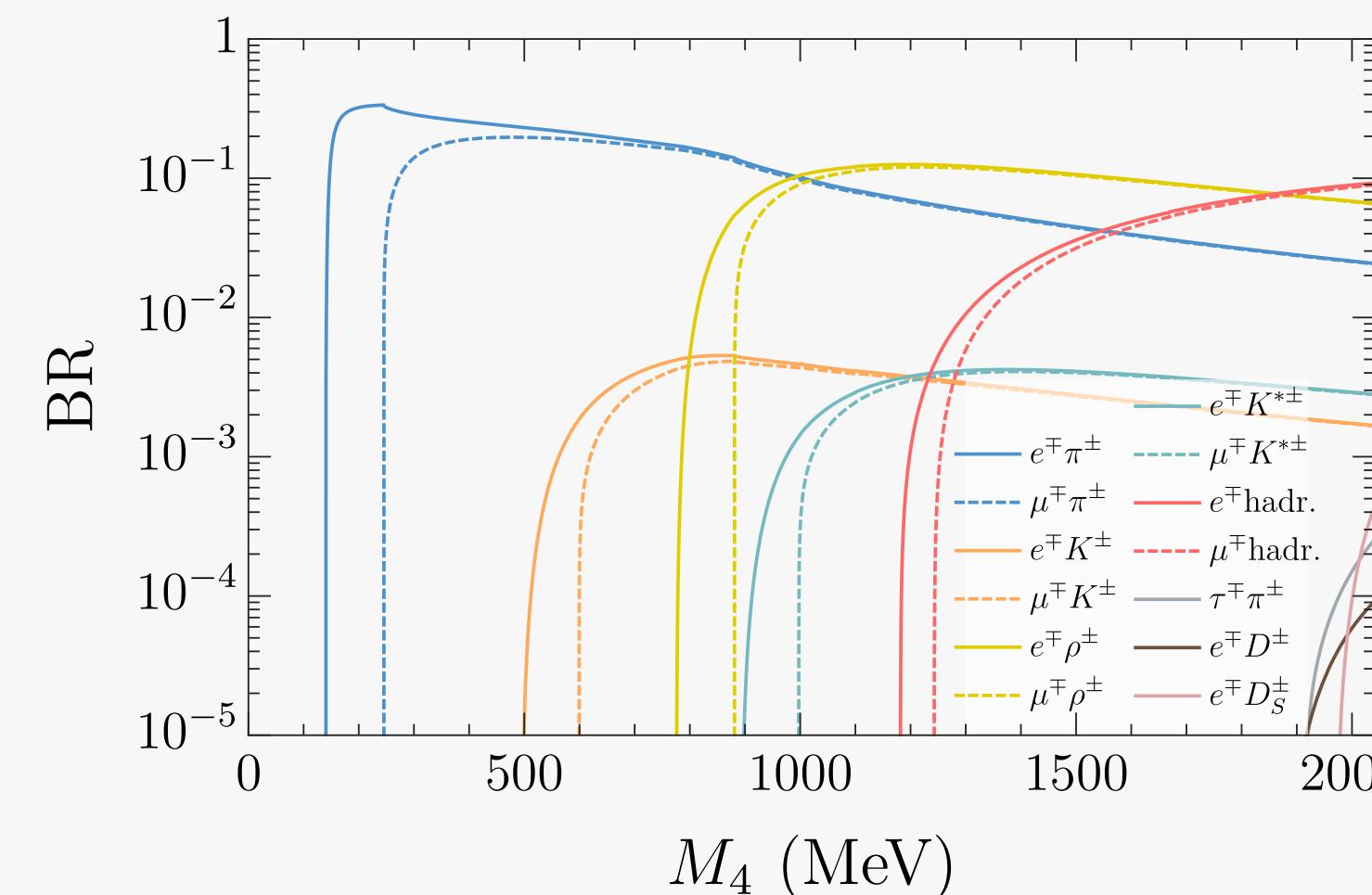
Parent	2-body decay	3-body decay
$\pi^+ \rightarrow$	$e^+ N_4$	—
	$\mu^+ N_4$	
$K^+ \rightarrow$	$e^+ N_4$	$\pi^0 e^+ N_4$
	$\mu^+ N_4$	$\pi^0 \mu^+ N_4$
$\tau^- \rightarrow$	$\pi^- N_4$	$e^- \bar{\nu} N_4$
	$\rho^- N_4$	$\mu^- \bar{\nu} N_4$

Parent	2-body decay	3-body decay
$D^+ \rightarrow$	$e^+ N_4$	$e^+ \bar{K}^0 N_4$
	$\mu^+ N_4$	$\mu^+ \bar{K}^0 N_4$
	$\tau^+ N_4$	
$D_s^+ \rightarrow$	$e^+ N_4$	—
	$\mu^+ N_4$	
	$\tau^+ N_4$	

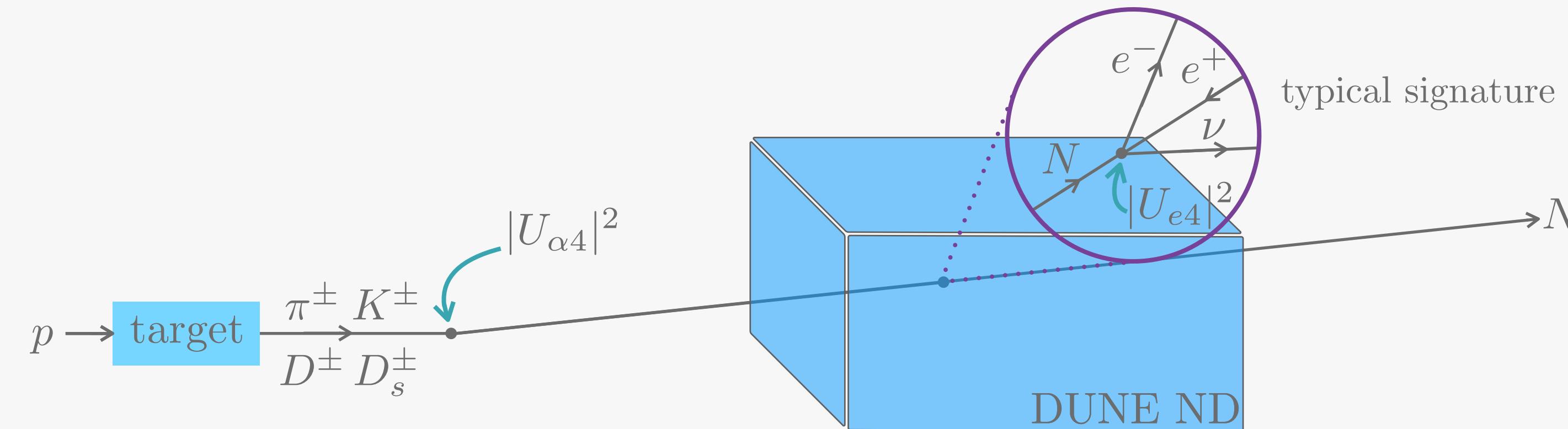
INGREDIENTS FOR HNL FLUXES GENERATION



- Fluxes of mesons produced in the target
- Events of HNL production via meson decays
- Events of HNL decays into SM particles



INGREDIENTS FOR HNL FLUXES GENERATION



- Fluxes of mesons produced in the target
- Events of HNL production via meson decays
- Events of HNL decays into SM particles

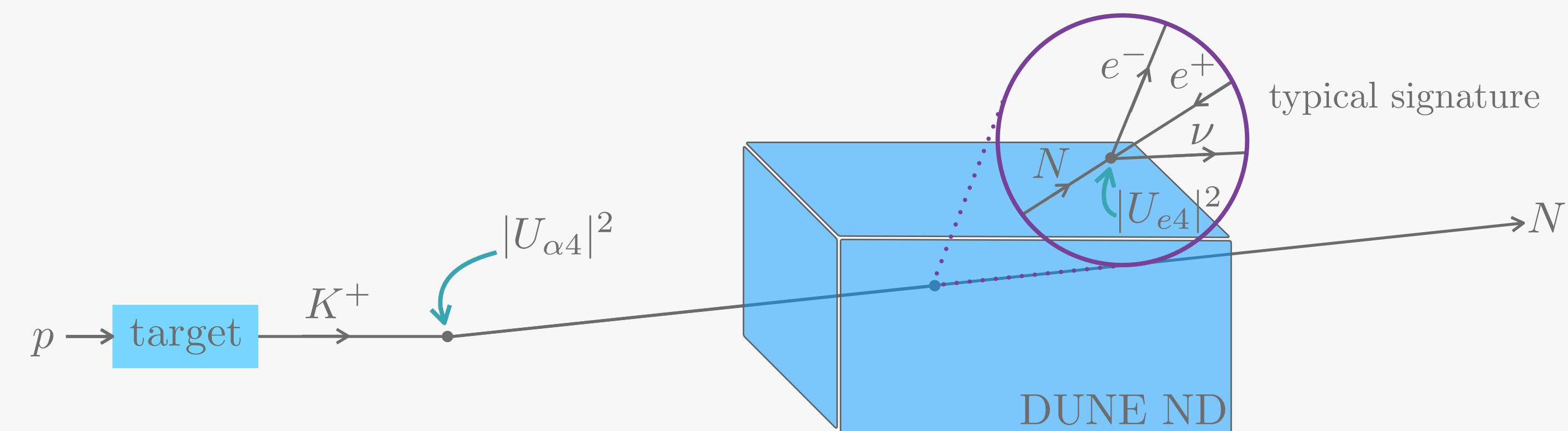
Generated with MadGraph5

FeynRules model file* with the
effective theory describing
HNL-meson interactions

*publicly available as ancillary file of arXiv: 2007.03701

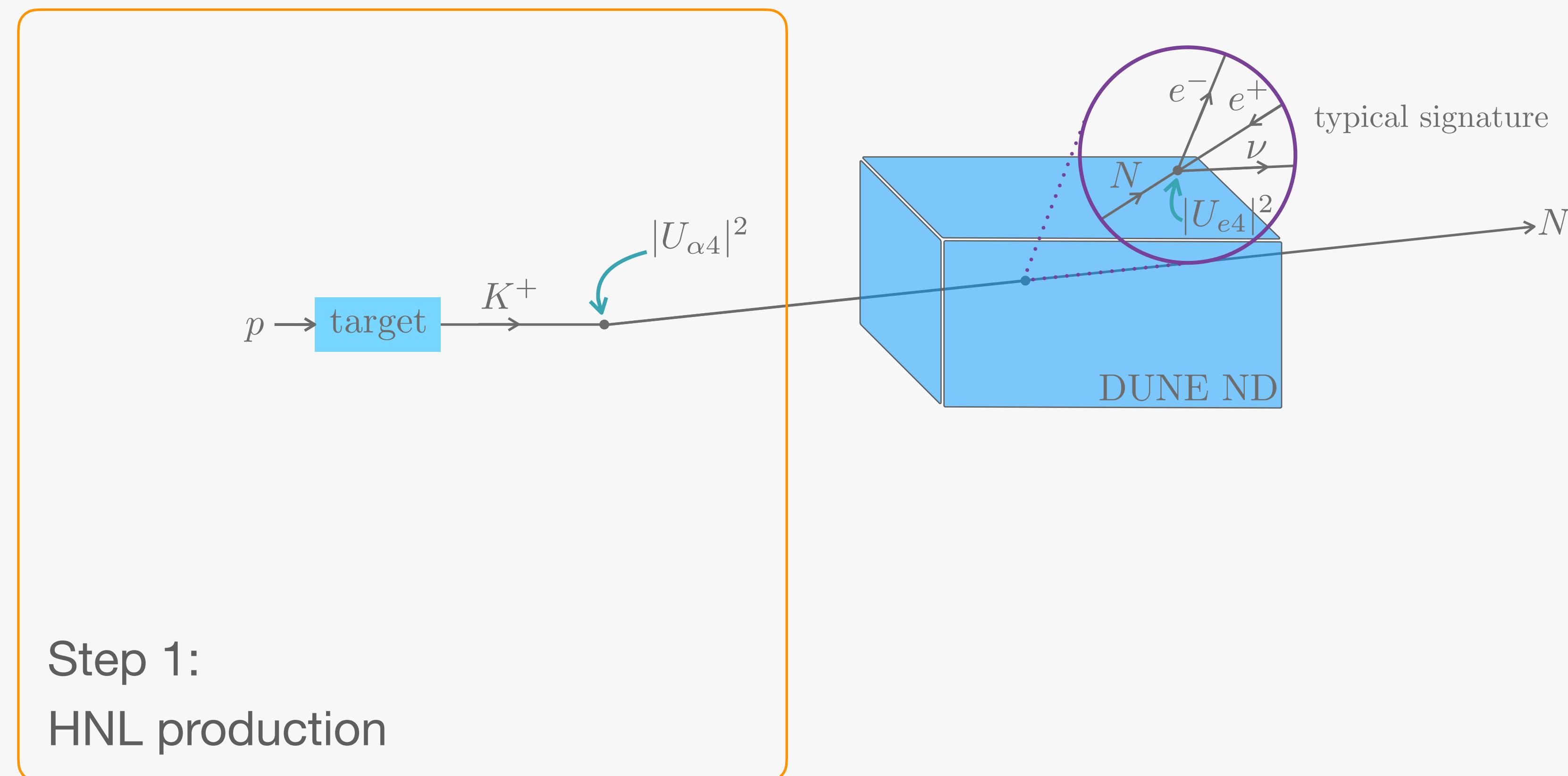
INGREDIENTS FOR HNL FLUXES GENERATION

Example considering HNL created via K^+ decay



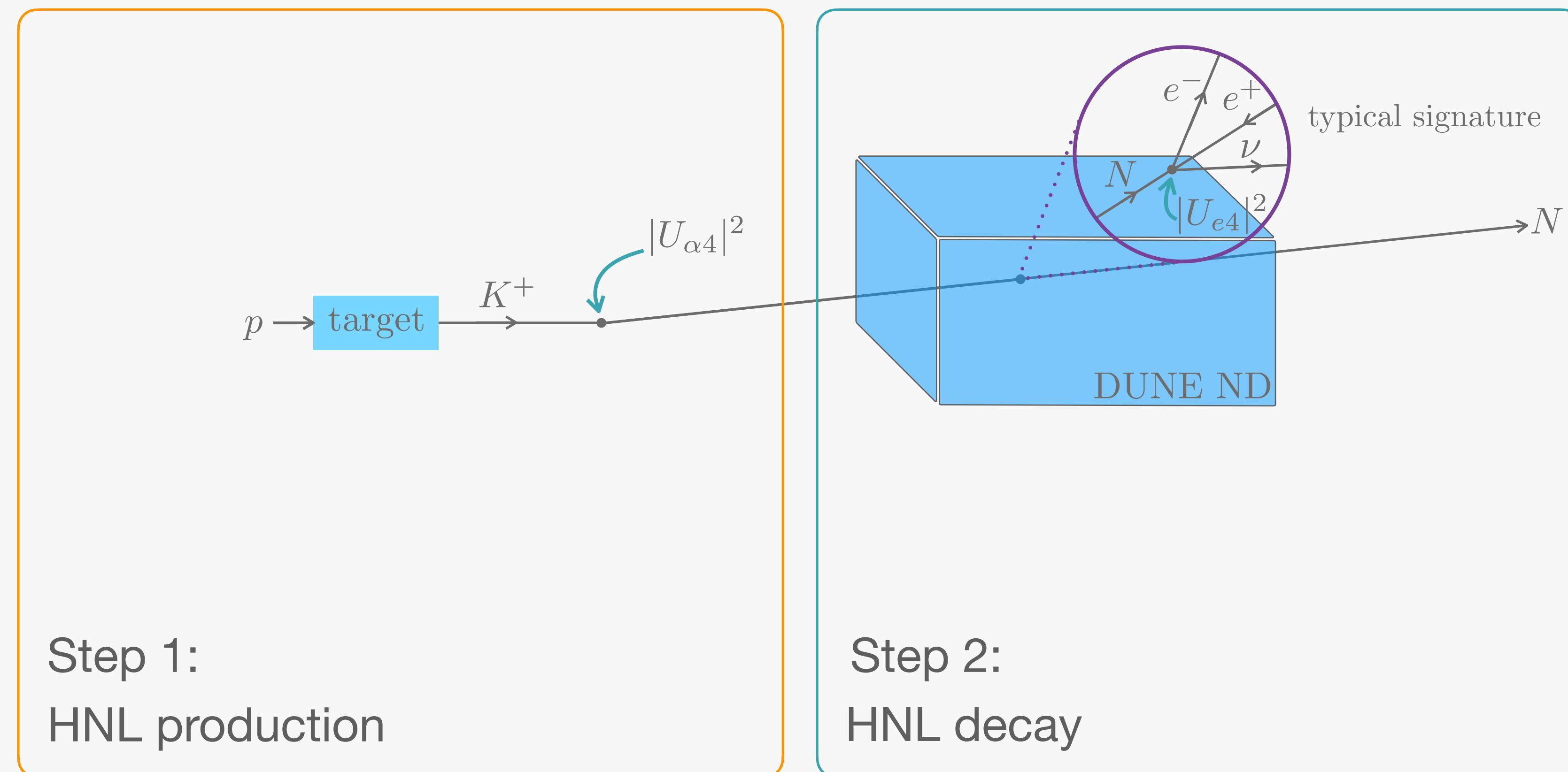
INGREDIENTS FOR HNL FLUXES GENERATION

Example considering HNL created via K^+ decay



INGREDIENTS FOR HNL FLUXES GENERATION

Example considering HNL created via K^+ decay



STEP 1: HNL PRODUCTION

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- MadGraph HNL events from meson decays

```
mg5_aMC>
  import model effective_HeavyN_Dirac_UFO
  generate k+ > n1 lepton QED <= 2
  add process k+ > n1 lepton meson QED <= 2
  launch
  set MN4 0.05
  set thetae 0.001
  set thetamu 0
  set thetatau 0
  set nevents 100000
```

The diagram illustrates the configuration of a MadGraph5 script. It shows a black terminal window with green text containing the script. Several lines of code are highlighted with colored rounded rectangles and connected by arrows to their corresponding descriptions:

- Yellow rounded rectangle around the first two lines: "generate k+ > n1 lepton QED <= 2" and "add process k+ > n1 lepton meson QED <= 2". An orange arrow points from this box to the text "2-body + 3-body kaon decays".
- Cyan rounded rectangle around "set MN4 0.05": A cyan arrow points from this box to the text "HNL mass".
- Yellow rounded rectangle around "set thetae 0.001", "set thetamu 0", and "set thetatau 0": A yellow arrow points from this box to the text " $|U_{\alpha 4}|^2$ ".
- Purple rounded rectangle around "set nevents 100000": A purple arrow points from this box to the text "# of events".

STEP 1: HNL PRODUCTION

- MadGraph HNL events from meson decays

MG output:



kaon_decay_50Mev.lhe

STEP 1: HNL PRODUCTION

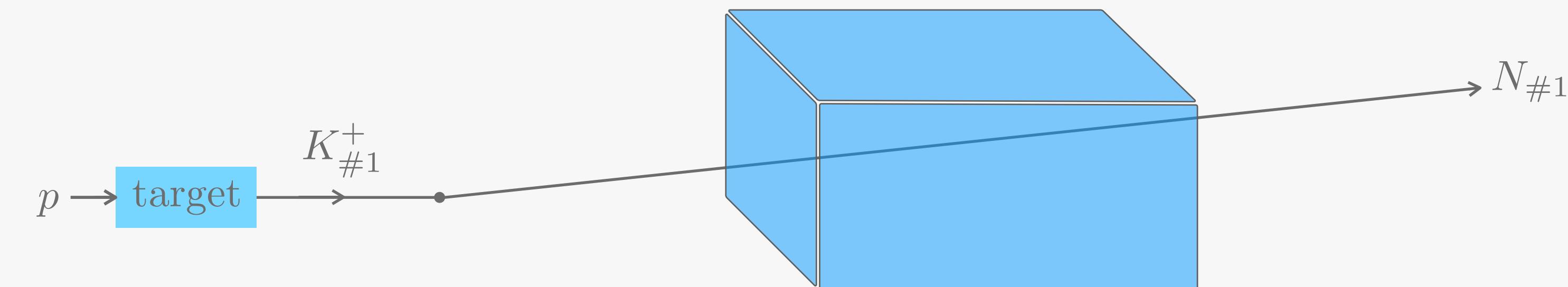
- MadGraph HNL events from meson decays
- K^+ fluxes from TDR n-tuple

MG output:

 kaon_decay_50Mev.lhe

#	x	y	z	px	py	pz	weight
-0.893351	-7.19023	306.405	0.00147399	-0.0722823	0.98955	120	
84.9599	-123.99	15384.6	0.237416	-0.348232	43.6417	4	
-3.32223	-0.496629	126.54	-0.127274	-0.041156	2.38537	109.091	
24.3667	-18.0481	2146.35	0.0378792	-0.0275051	3.01461	40	
...							

Each MG event **matched** to one K^+ in the histogram and boosted to the lab frame



STEP 1: HNL PRODUCTION

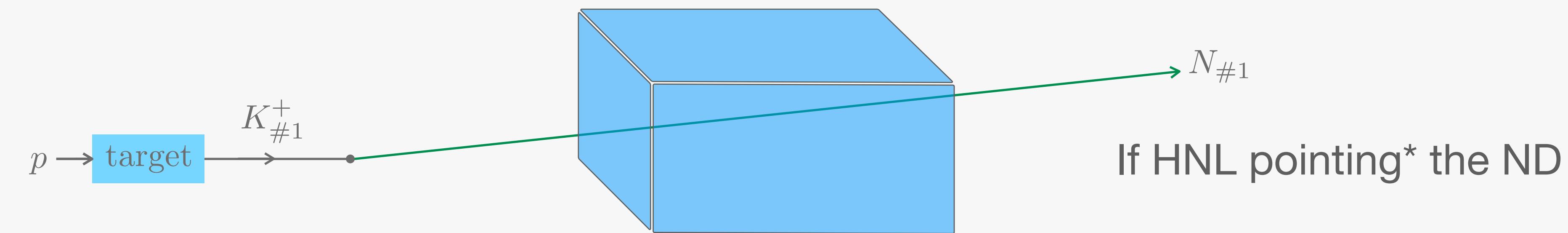
- MadGraph HNL events from meson decays
- K^+ fluxes from TDR n-tuple

MG output:



#	x	y	z	px	py	pz	weight
-0.893351	-7.19023	306.405	0.00147399	-0.0722823	0.98955	120	
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...							

Each MG event matched to one K^+ in the histogram and boosted to the lab frame



Step 1 output file: HNL flux file

#	Px	Py	Pz	MN	x_decay	y_decay	z_decay	Meson_width	BR_Meson	Meson_weight
0.00518398	-0.000368844	1.02619	0.05	-0.00893351	-0.0719023	3.06405	1.04313e-23	0.774359	120	

*a tilt angle $\alpha = 0.101$ due to the beam inclination with respect to the horizontal is considered

STEP 1: HNL PRODUCTION

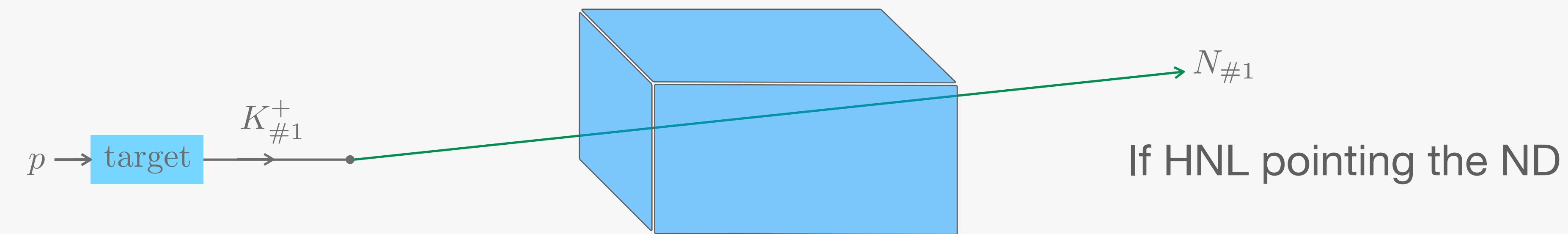
- MadGraph HNL events from meson decays
- K^+ fluxes from TDR n-tuple

MG output:

 kaon_decay_50Mev.lhe

#	x	y	z	px	py	pz	weight
-0.893351	-7.19023	306.405	0.00147399	-0.0722823	0.98955	120	
84.9599	-123.99	15384.6	0.237416	-0.348232	43.6417	4	
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taken from K^+ flux file

STEP 1: HNL PRODUCTION

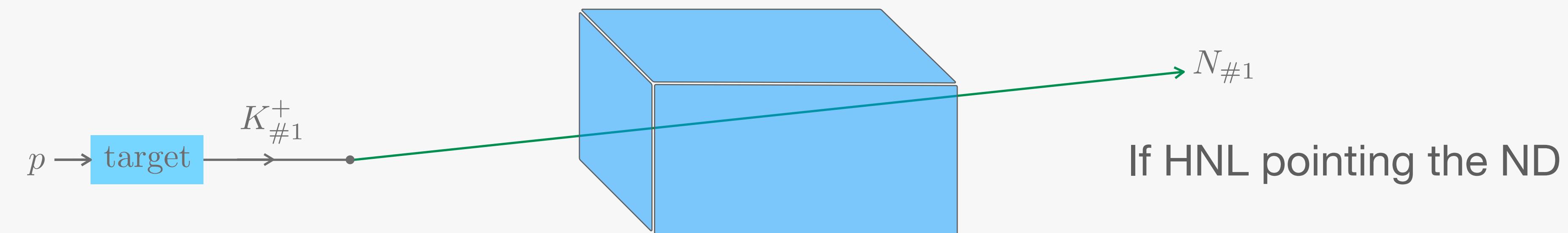
- MadGraph HNL events from meson decays
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MG output:

 kaon_decay_50Mev.lhe

#	x	y	z	px	py	pz	weight
-0.893351	-7.19023	306.405	0.00147399	-0.0722823	0.98955	120	
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taken from .lhe MG file

STEP 1: HNL PRODUCTION

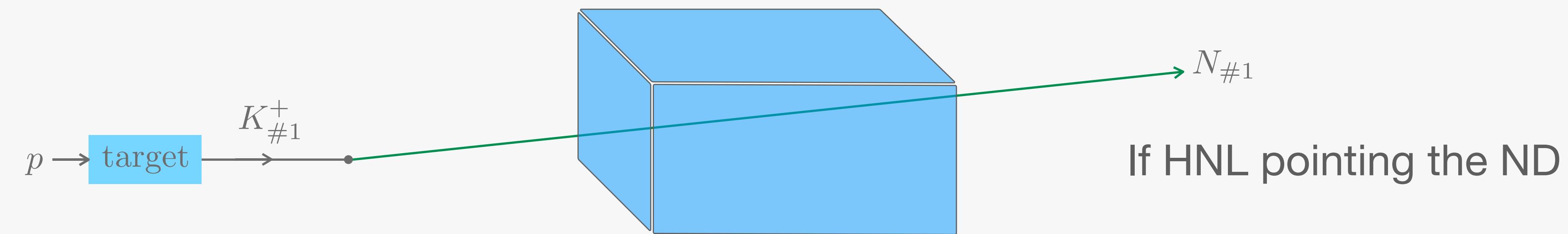
- MadGraph HNL events from meson decays
- K^+ fluxes from TDR n-tuple

MG output:

 kaon_decay_50Mev.lhe

#	x	y	z	px	py	pz	weight
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computed with the script

STEP 1: HNL PRODUCTION

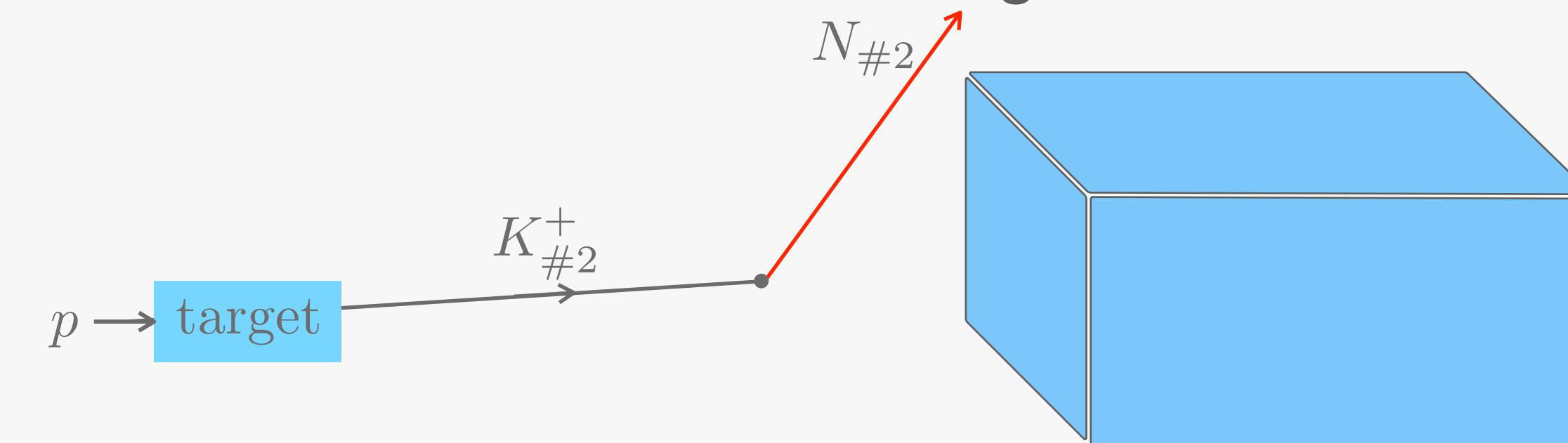
- MadGraph HNL events from meson decays
- K^+ fluxes from TDR n-tuple

MG output:

 kaon_decay_50Mev.lhe

#	x	y	z	px	py	pz	weight
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Each MG event **matched** to one K^+ in the histogram and boosted to the lab frame



If HNL pointing the ND

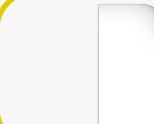
Step 1 output file: HNL flux file

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STEP 1: HNL PRODUCTION

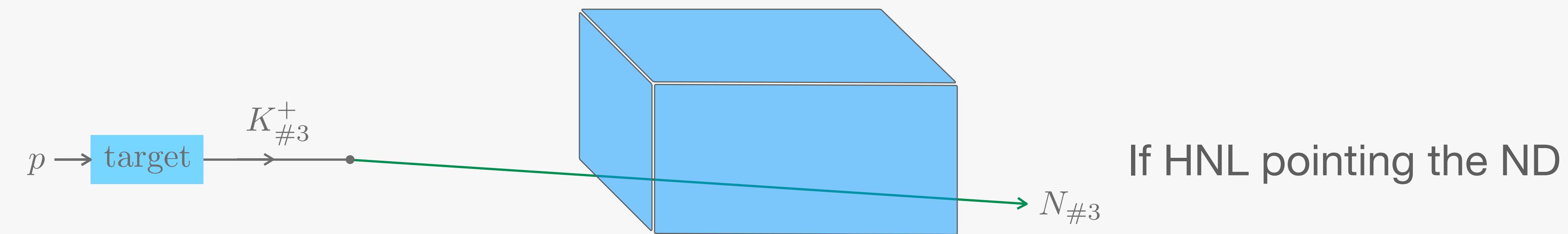
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MG output:

 kaon_decay_50Mev.lhe

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STEP 1: HNL PRODUCTION

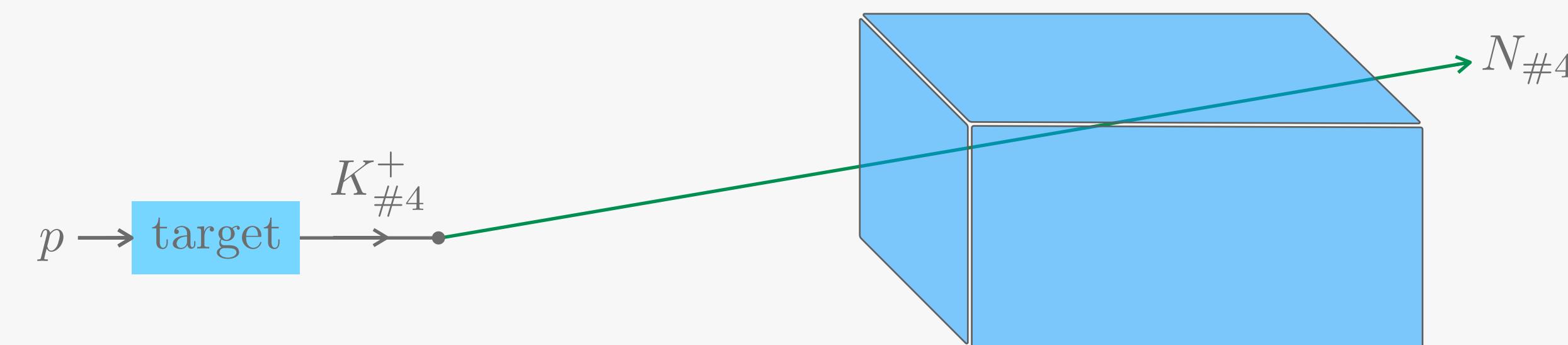
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kaon_decay_50Mev.lhe

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.	.	.					

Each MG event **matched** to one K^+ in the histogram and boosted to the lab frame



If HNL pointing the ND

Step 1 output file: HNL flux file

STEP 1: HNL PRODUCTION

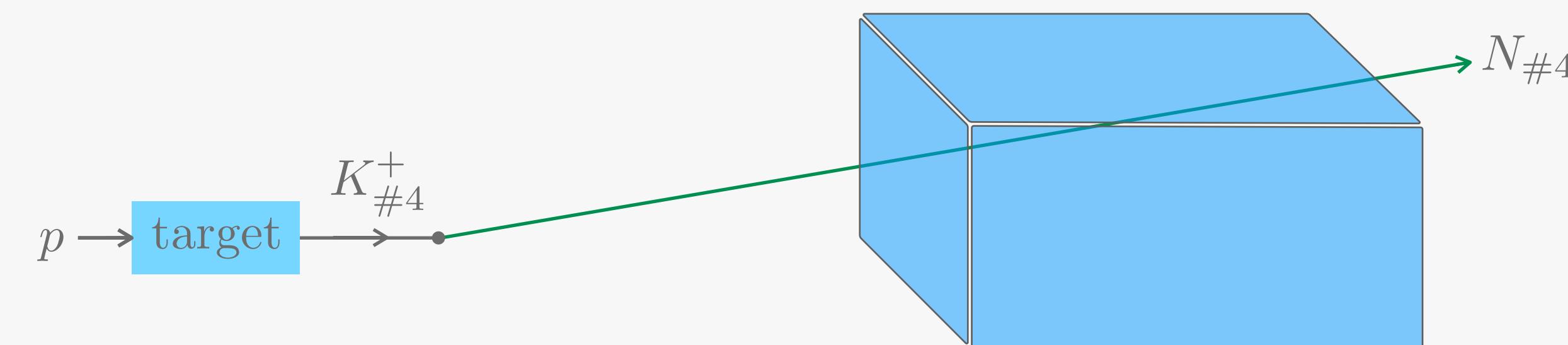
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MG output:

 kaon_decay_50Mev.lhe

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-3.32223	-0.496629	126.54	-0.127274	-0.041156	2.38537	109.091	
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Each MG event matched to one K^+ in the histogram and boosted to the lab frame



If HNL pointing the ND

Step 1 output file: HNL flux file

#	Px	Py	Pz	MN	x_decay	y_decay	z_decay	Meson_width	BR_Meson	Meson_weight
0.00518398	-0.000368844	1.02619	0.05	-0.00893351	-0.0719023	3.06405	1.04313e-23	0.774359	120	
0.0114722	-0.00399517	2.21981	0.05	-0.0332223	-0.00496629	1.2654	1.04313e-23	0.774359	109.091	
-0.00482478	0.000351083	1.08561	0.05	0.243667	-0.180481	21.4635	1.04313e-23	0.225641	40	
...										

2-body K^+ decay
3-body K^+ decay

 events-kaon+-50Mev-n1.dat

STEP 2: HNL DECAY

STEP 2: HNL DECAY. OPTION A: ONE DECAY CHANNEL

- MadGraph HNL decay events (one channel)

```
mg5_aMC>
  import model effective_HeavyN_Dirac_UFO
  generate n1 > e+ e- v QED <= 2
  launch
  set MN4 0.05
  set thetae 0.001
  set thetamu 0
  set thetatau 0
  set nevents 10000
```

A diagram illustrating a connection between a command in the MadGraph session and its corresponding decay channel. An orange oval surrounds the command `generate n1 > e+ e- v QED <= 2`. A solid orange line extends from the right side of this oval to a text block on the right. The text block contains the decay channel $N \rightarrow e^+ e^- \nu$ followed by the word "decays".

STEP 2: HNL DECAY. OPTION A: ONE DECAY CHANNEL

- MadGraph HNL decay events (one channel)

MG output:



ndecay_eev_50Mev.lhe

STEP 2: HNL DECAY. OPTION A: ONE DECAY CHANNEL

- MadGraph HNL decay events (one channel)
- HNL fluxes from Step 1

MG output:



ndecay_eev_50Mev.lhe

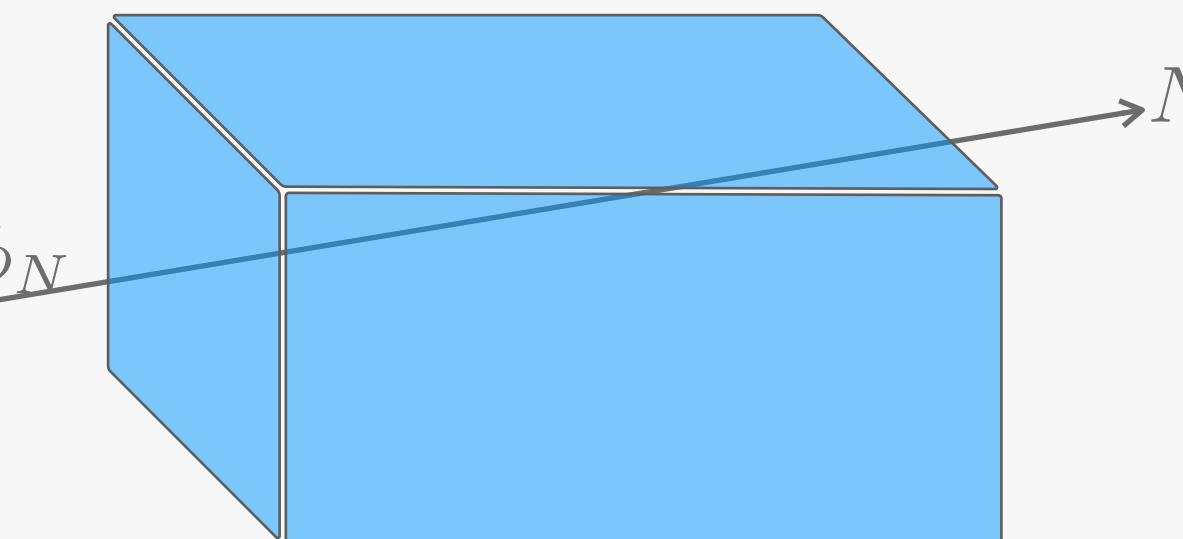
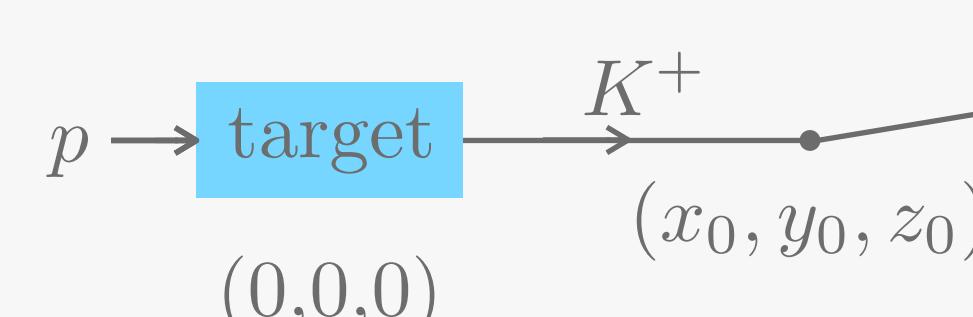
#	Px	...	MN	x_decay	...	Meson_width	BR_Meson	Meson_weight
0.00518398	...	0.05	-0.00893351	...	1.04313e-23	0.774359	120	
0.0114722	...	0.05	-0.0332223	...	1.04313e-23	0.774359	109.091	
-0.00482478	...	0.05	0.243667	...	1.04313e-23	0.225641	40	
...								

Each MG event **matched** to one HNL in the histogram and boosted to the lab frame (LF)

Information stored in the MD file

```
### 0
#M_w      N_w      MN USquared   L_lab_N    x_0          y_0          z_0        thetaN     phiN M_width_CM   BR_M      N_width_CM   BR_N      time_N
120  1.40438e-11  0.05   1e-06  3.5603e+11 -0.0089335 -0.071902   3.06405  0.0050644  1.64183  1.04313e-23  0.774359  1.13565e-26  0.371457  1.91365e-06
#particle.id EeBoost    PxlabBoost   PylabBoost   PzlabBoost
 12000  0.0266246  -0.0044687  0.00352943  0.0260085
    11   0.718403   -0.000989571  0.0100071   0.718332
   -11   0.282393    0.0106423   -0.0139054   0.281849
...
```

Trajectory of the HNL



$$\theta_N = \arccos\left(\frac{P_{zN}}{P_N}\right)$$

$$\phi_N = \arctan\left(\frac{P_{xN}}{P_{yN}}\right)$$

STEP 2: HNL DECAY. OPTION A: ONE DECAY CHANNEL

- MadGraph HNL decay events (one channel)
- HNL fluxes from Step 1

MG output:



ndecay_eev_50Mev.lhe

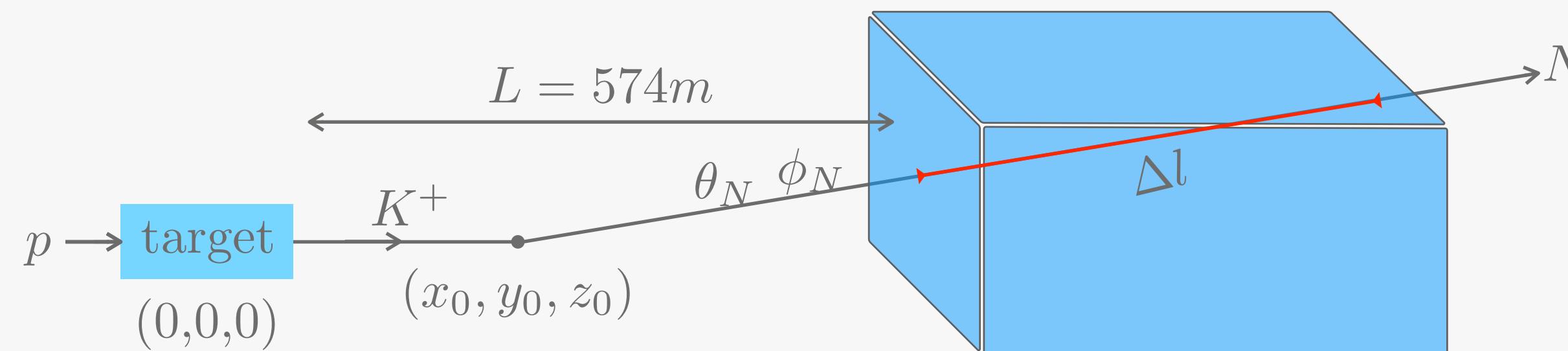
#	Px	...	MN	x_decay	...	Meson_width	BR_Meson	Meson_weight
0.00518398	...	0.05	-0.00893351	...	1.04313e-23	0.774359	120	
0.0114722	...	0.05	-0.0332223	...	1.04313e-23	0.774359	109.091	
-0.00482478	...	0.05	0.243667	...	1.04313e-23	0.225641	40	
...								

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Information stored in the MD file

```
### 0
#M_w N_w MN USquared L_lab_N x_0 y_0 z_0 thetaN phiN M_width_CM BR_M N_width_CM BR_N time_N
120 1.40438e-11 0.05 1e-06 3.5603e+11 -0.0089335 -0.071902 3.06405 0.0050644 1.64183 1.04313e-23 0.774359 1.13565e-26 0.371457 1.91365e-06
#particle.id EeBoost PxlabBoost PylabBoost PzlabBoost
 12000 0.0266246 -0.0044687 0.00352943 0.0260085
    11 0.718403 -0.000989571 0.0100071 0.718332
   -11 0.282393 0.0106423 -0.0139054 0.281849
...
```

HNL weight



$$N_w = e^{-\frac{\Gamma L}{\gamma \beta}} \left(1 - e^{-\frac{\Gamma \Delta l}{\gamma \beta}}\right) \approx \frac{\Gamma \Delta l}{\gamma \beta}$$

Γ total HNL decay width CM

STEP 2: HNL DECAY. OPTION A: ONE DECAY CHANNEL

- MadGraph HNL decay events (one channel)
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MG output:



ndecay_eev_50Mev.lhe

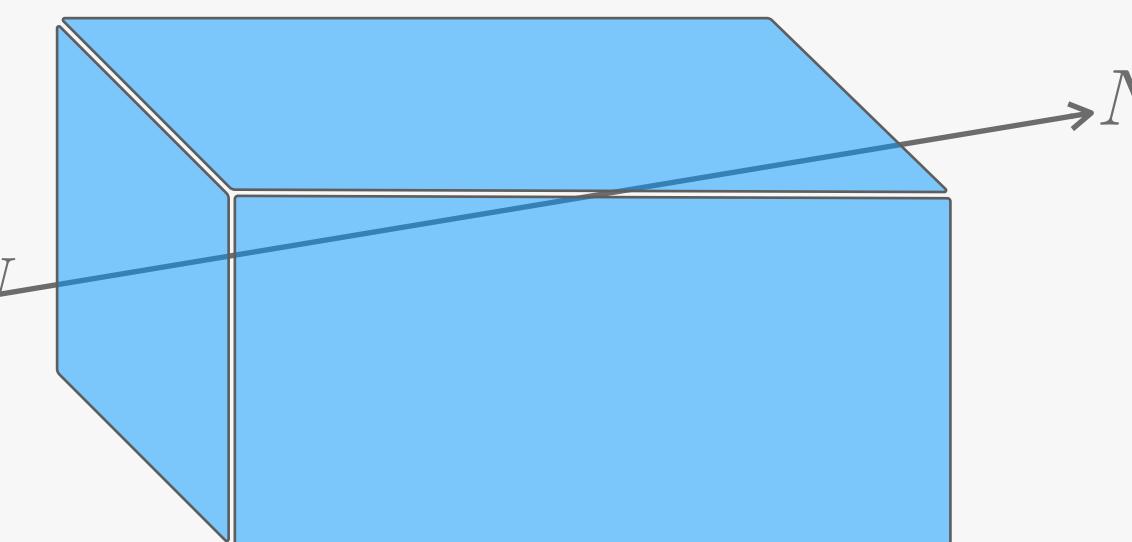
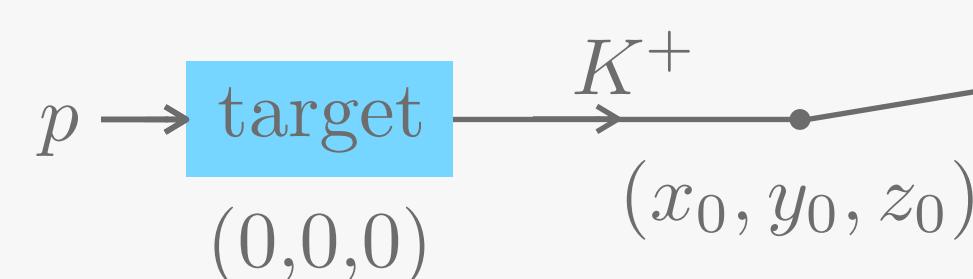
#	Px	...	MN	x_decay	...	Meson_width	BR_Meson	Meson_weight
0.00518398	...	0.05	-0.00893351	...	1.04313e-23	0.774359	120	
0.0114722	...	0.05	-0.0332223	...	1.04313e-23	0.774359	109.091	
-0.00482478	...	0.05	0.243667	...	1.04313e-23	0.225641	40	
...								

Each MG event **matched** to one HNL in the histogram and boosted to the lab frame (LF)

Information stored in the MD file

```
### 0
#M_w      N_w      MN USquared L_lab_N      x_0      y_0      z_0      thetaN      phiN      M_width_CM      BR_M      N_width_CM      BR_N      time_N
120  1.40438e-11  0.05    1e-06  3.5603e+11 -0.0089335 -0.071902  3.06405  0.0050644  1.64183  1.04313e-23  0.774359  1.13565e-26  0.371457  1.91365e-06
#particle.id   EeBoost   PxlabBoost   PylabBoost   PzlabBoost
  12000  0.0266246  -0.0044687  0.00352943  0.0260085
    11   0.718403   -0.000989571  0.0100071   0.718332
   -11   0.282393    0.0106423  -0.0139054   0.281849
...
```

HNL decay length (LF)



$$L_N = \frac{p_N}{M_4 \Gamma}$$

Γ total HNL decay width CM

STEP 2: HNL DECAY. OPTION A: ONE DECAY CHANNEL

- MadGraph HNL decay events (one channel)
- HNL fluxes from Step 1

MG output:



ndecay_eev_50Mev.lhe

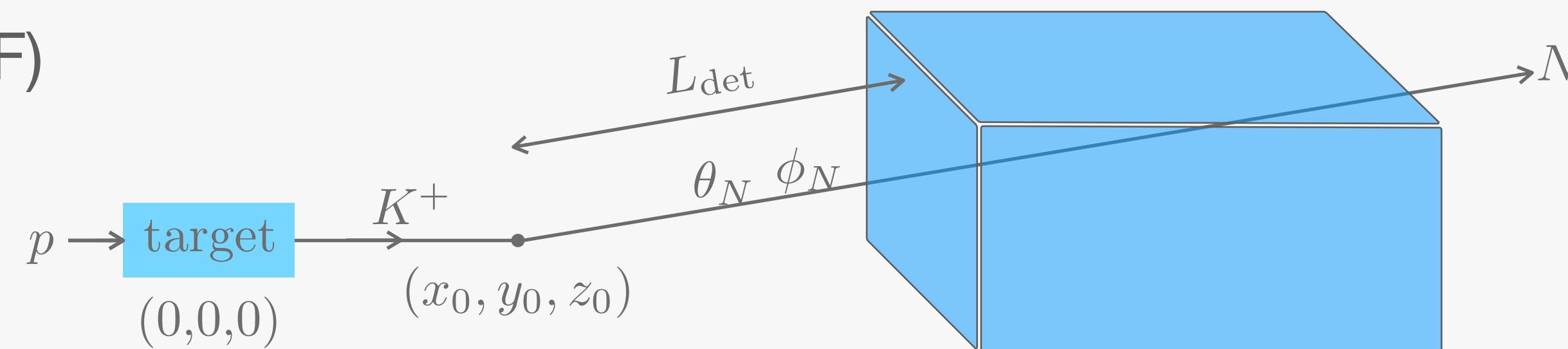
#	Px	...	MN	x_decay	...	Meson_width	BR_Meson	Meson_weight
0.00518398	...	0.05	-0.00893351	...	1.04313e-23	0.774359	120	
0.0114722	...	0.05	-0.0332223	...	1.04313e-23	0.774359	109.091	
-0.00482478	...	0.05	0.243667	...	1.04313e-23	0.225641	40	
...								

Each MG event **matched** to one HNL in the histogram and boosted to the lab frame (LF)

Information stored in the MD file

```
### 0
#M_w      N_w      MN USquared   L_lab_N      x_0      y_0      z_0      thetaN      phiN      M_width_CM      BR_M      N_width_CM      BR_N      time_N
120  1.40438e-11  0.05    1e-06  3.5603e+11 -0.0089335 -0.071902  3.06405  0.0050644  1.64183  1.04313e-23  0.774359  1.13565e-26  0.371457  1.91365e-06
#particle.id  EeBoost  PxlabBoost  PylabBoost  PzlabBoost
  12000  0.0266246  -0.0044687  0.00352943  0.0260085
    11   0.718403   -0.000989571  0.0100071   0.718332
   -11   0.282393    0.0106423   -0.0139054   0.281849
...
...
```

HNL time of flight (LF)



$$t_N = \frac{L_{\text{det}}}{\beta c}$$

STEP 2: HNL DECAY. OPTION A: ONE DECAY CHANNEL

- MadGraph HNL decay events (one channel)
- HNL fluxes from Step 1

MG output:



ndecay_eev_50Mev.lhe

#	Px	...	MN	x_decay	...	Meson_width	BR_Meson	Meson_weight
0.00518398	...	0.05	-0.00893351	...	1.04313e-23	0.774359	120	
0.0114722	...	0.05	-0.0332223	...	1.04313e-23	0.774359	109.091	
-0.00482478	...	0.05	0.243667	...	1.04313e-23	0.225641	40	
...								

Each MG event **matched** to one HNL in the histogram and boosted to the lab frame (LF)

Information stored in the MD file

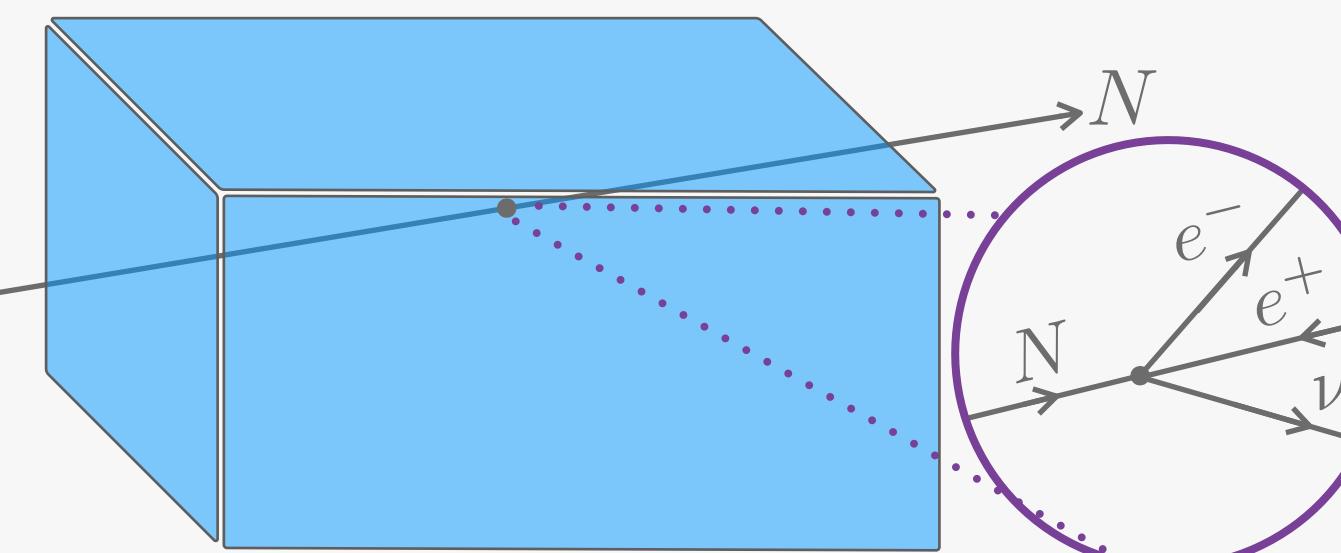
```
### 0
#M_w      N_w      MN USquared   L_lab_N      x_0      y_0      z_0      thetaN    phiN    M_width_CM    BR_M      N_width_CM    BR_N      time_N
120  1.40438e-11  0.05  1e-06  3.5603e+11 -0.0089335 -0.071902  3.06405  0.0050644  1.64183  1.04313e-23  0.774359  1.13565e-26  0.371457  1.91365e-06
#particle.id  EeBoost  PxlabBoost  PylabBoost  PzlabBoost
  12000  0.0266246  -0.0044687  0.00352943  0.0260085
    11   0.718403   -0.000989571  0.0100071  0.718332
   -11   0.282393    0.0106423  -0.0139054  0.281849
...

```

$$N \rightarrow e^+ e^- \nu$$

BR of the simulated decay channel

$$p \rightarrow \text{target} \rightarrow K^+$$



STEP 2: HNL DECAY. OPTION A: ONE DECAY CHANNEL

- MadGraph HNL decay events (one channel)
- HNL fluxes from Step 1

MG output:



ndecay_eev_50Mev.lhe

#	Px	...	MN	x_decay	...	Meson_width	BR_Meson	Meson_weight
0.00518398	...	0.05	-0.00893351	...	1.04313e-23	0.774359	120	
0.0114722	...	0.05	-0.0332223	...	1.04313e-23	0.774359	109.091	
-0.00482478	...	0.05	0.243667	...	1.04313e-23	0.225641	40	
...								

Each MG event **matched** to one HNL in the histogram and boosted to the lab frame (LF)

Information stored in the MD file

```
### 0
#M_w      N_w      MN USquared      L_lab_N      x_0      y_0      z_0      thetaN      phiN      M_width_CM      BR_M      N_width_CM      BR_N      time_N
120  1.40438e-11  0.05    1e-06  3.5603e+11 -0.0089335 -0.071902  3.06405  0.0050644  1.64183  1.04313e-23  0.774359  1.13565e-26  0.371457  1.91365e-06
#particle.id      EeBoost      PxlabBoost      PylabBoost      PzlabBoost
  12000  0.0266246      -0.0044687      0.00352943      0.0260085
   11    0.718403      -0.000989571      0.0100071      0.718332
  -11   0.282393      0.0106423      -0.0139054      0.281849
...
```

Output Step 2A:

Repeat Step 2A for all the accessible HNL decay channels

STEP 2: HNL DECAY. OPTION B: ALL DECAY CHANNEL

- MadGraph HNL decay events (all channel)

```
mg5_aMC>
  import model effective_HeavyN_Dirac_UFO
  generate n1 > meson lepton QED <= 2
  add process n1 > lepton lepton lepton QED <= 2
  launch
  set MN4 0.05
  set thetae 0.001
  set thetamu 0
  set thetatau 0
  set nevents 100000
```

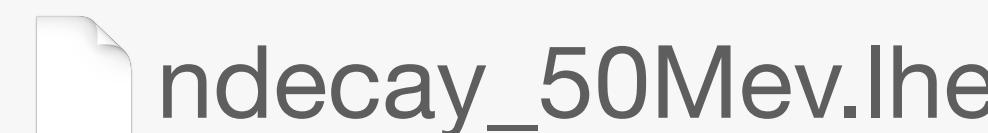
2-body + 3-body
HNL decays

bigger # events!
 10^6 limit

STEP 2: HNL DECAY. OPTION B: ALL DECAY CHANNEL

- MadGraph HNL decay events (all channel)

MG output:



- HNL fluxes from Step 1

#	Px	...	MN	x_decay	...	Meson_width	BR_Meson	Meson_weight
0.00518398	...	0.05	-0.00893351	...	1.04313e-23	0.774359	120	
0.0114722	...	0.05	-0.0332223	...	1.04313e-23	0.774359	109.091	
-0.00482478	...	0.05	0.243667	...	1.04313e-23	0.225641	40	
...								

Each MG event matched to one HNL in the histogram and boosted to the lab frame (LF)

Information stored in the MD file

```
### 0
#M_w      N_w      MN USquared   L_lab_N      x_0      y_0      z_0      thetaN    phiN    M_width_CM    BR_M      N_width_CM    BR_N      time_N
120  1.40438e-11  0.05  1e-06  3.5603e+11 -0.0089335 -0.071902  3.06405  0.0050644  1.64183  1.04313e-23  0.774359  1.13565e-26  0.371457  1.91365e-06
#particle.id  EeBoost    PxlabBoost   PylabBoost   PzlabBoost
  12000  0.0266246  -0.0044687  0.00352943  0.0260085
    11   0.718403   -0.000989571  0.0100071   0.718332
   -11   0.282393    0.0106423   -0.0139054  0.281849
### 1
109.091 6.49214e-12 0.05  1e-06  7.7015e+11 -0.033222 -0.0049663  1.2654  0.0054724  1.90591  1.04313e-23  0.774359  1.13565e-26  0.314661  1.91812e-06
  12000  1.15731   0.0265641  -0.0108905  1.15695
  12000  1.05248   -0.0134862  0.00638912  1.05237
 -12000  0.0106205 -0.00160576  0.000506223  0.0104862
...
```

$N \rightarrow e^+ e^- \nu$

$N \rightarrow \nu \nu \nu$

Output Step 2B: events-ndecay-50Mev-1e-6-fromkaon+.dat

GRID OF HNL MASSES AND MIXINGS

GRID OF HNL MASSES AND MIXINGS

- Grid of HNL masses

For every parent meson (π , K, D, D_s) perform Step1 + Step2B assuming different M_4

- n different values of M_4
- one single value $|U_{\alpha 4}|^2$ for each flavour

Output:

2n (3n) MD files for π and K (D and D_s)

- Grid of HNL mixings

Each MD file can be rescaled to a different value of $|U_{\alpha 4}|^2$: $\times \frac{|U_{\alpha 4}|^2_{\text{new}}}{|U_{\alpha 4}|^2_{\text{old}}}$

### 0	N_w*	MN	USquared	L_lab_N	x_0	y_0	z_0	thetaN	phiN	M_width_CM	BR_M	N_width_CM	BR_N	time_N
120	1.40438e-11	0.05	1e-06	3.5603e+11	-0.0089335	-0.071902	3.06405	0.0050644	1.64183	1.04313e-23	0.774359	1.13565e-26	0.371457	1.91365e-06
#particle.id	EeBoost	PxlabBoost		PylabBoost		PzlabBoost								
12000	0.0266246		-0.0044687		0.00352943		0.0260085							
11	0.718403		-0.000989571		0.0100071		0.718332							
-11	0.282393		0.0106423		-0.0139054		0.281849							
...														

*valid for $\Gamma L \ll \gamma \beta \Rightarrow N_w \approx \frac{\Gamma \Delta l}{\gamma \beta}$

GRID OF HNL MASSES AND MIXINGS

- Grid of HNL masses

For every parent meson (π , K, D, D_s) perform Step1 + Step2B assuming different M_4

- n different values of M_4
- one single value $|U_{\alpha 4}|^2$ for each flavour

Output:

2n (3n) MD files for π and K (D and D_s)

- Grid of HNL mixings

Each MD file can be rescaled to a different value of $|U_{\alpha 4}|^2$: $\times \frac{|U_{\alpha 4}^2|_{\text{old}}^2}{|U_{\alpha 4}^2|_{\text{new}}^2}$

```
### 0
#M_w      N_w      MN USquared    L_lab_N      x_0      y_0      z_0      thetaN      phiN      M_width_CM      BR_M      N_width_CM      BR_N      time_N
120  1.40438e-11  0.05   1e-06  3.5603e+11 -0.0089335 -0.071902  3.06405  0.0050644  1.64183  1.04313e-23  0.774359  1.13565e-26  0.371457  1.91365e-06
#particle.id      EeBoost      PxlabBoost      PylabBoost      PzlabBoost
  12000  0.0266246      -0.0044687      0.00352943      0.0260085
    11   0.718403      -0.000989571      0.0100071      0.718332
   -11   0.282393      0.0106423      -0.0139054      0.281849
...  
...
```

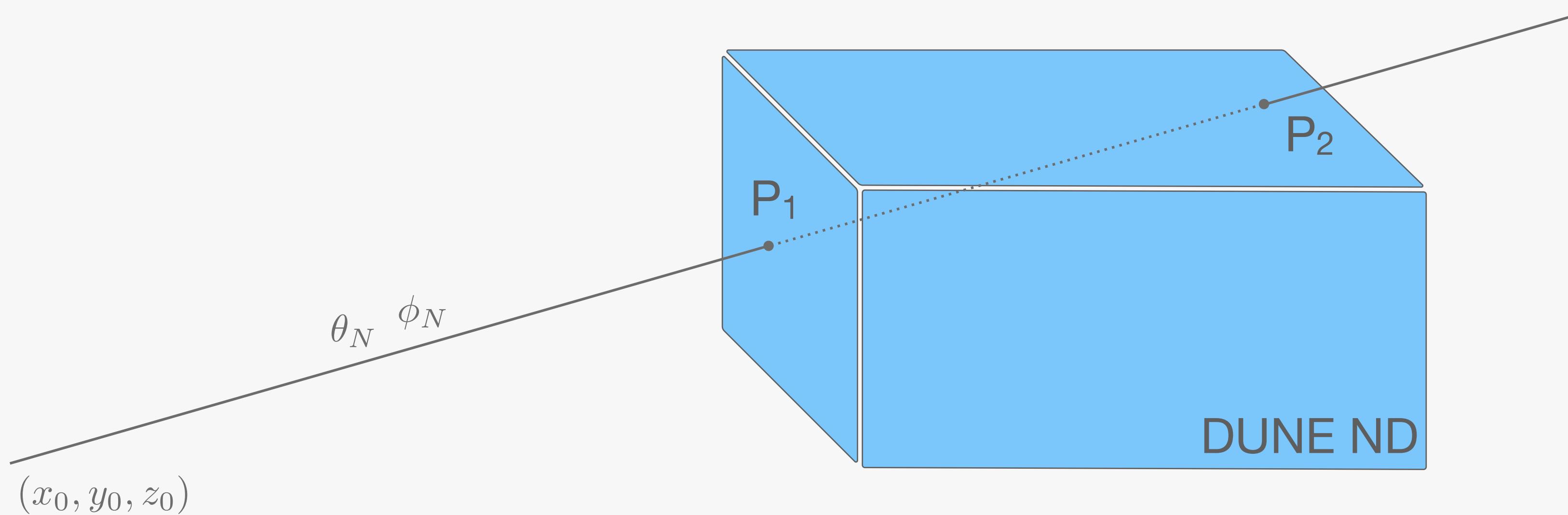
DETECTOR SIMULATION

DETECTOR SIMULATION

The MD files contain trajectories of the HNLs intersecting the ND

For each HNL event, the trajectory is defined by (x_0, y_0, z_0) and the angles θ_N and ϕ_N

The trajectory of a given HNL intersects the ND in two points P_1 and P_2

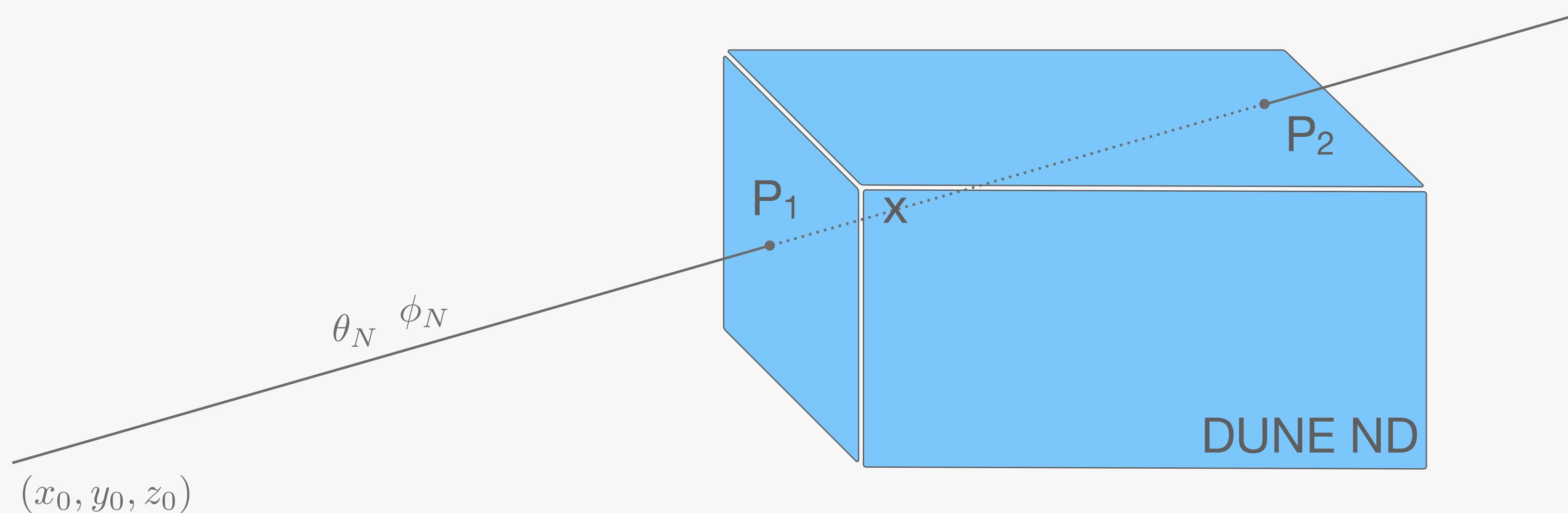


DETECTOR SIMULATION

The MD files contain trajectories of the HNLs intersecting the ND

For each HNL event, the trajectory is defined by (x_0, y_0, z_0) and the angles θ_N and ϕ_N

The trajectory of a given HNL intersects the ND in two points P_1 and P_2



A random point along the trajectory between P_1 and P_2 can be set as the decay point of the event

OPEN DISCUSSION

OPEN DISCUSSION

- Step 2A or Step 2B?
 - Which statistics is needed for proper event reconstruction?
 - Do 10^5 HNL decay events sample well all the different channels in Step 2B?
- Output of the MD file
 - Is the information provided in the MD enough for GArSoft reconstruction?
 - Does GArSoft work with weighted or unweighted events?