

$K_{\mu 3}^{\pm}$ Form Factors Measurement at NA48/2

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On behalf of the NA48/2 Collaboration

- Physics motivations
- The NA48/2 experiment and detector
- $K_{\mu 3}^{\pm}$ analysis
 - Event selection
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 - Fitting procedure
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 - DATA–MC comparison
 - Preliminary results
 - Systematics Check
- K_{e3}^{\pm} Analysis
- $K_{\ell 3}$ Form Factors @ NA62
- Summary

$K_{\ell 3}$ Form Factors: Physics Motivations

The $K_{\ell 3}$ decay is described by two form factors, $f_{\pm}(t)$

$$\mathfrak{M} = G_F/\sqrt{2} V_{us} [f_+(t) (P_K + P_\pi)^\mu \bar{u}_\ell \gamma_\mu (1 + \gamma_5) u_\nu + f_-(t) m_\ell \bar{u}_\ell (1 + \gamma_5) u_\nu]$$

t is the square of the four-momentum transfer to the lepton system

$$f_- \Rightarrow m_\ell^2/m_K^2$$

Can be measured only in $K_{\mu 3}$ decays

$f_0(t)$, which is a combination of the two, is used:

$$f_0(t) = f_+(t) + \frac{t}{(m_K^2 - m_\pi^2)} f_-(t)$$

$f_+(0) = f_0(0)$ by construction

$f_+(0)$ is not directly measurable

\Rightarrow factor out $f_+^{K^0\pi^-}(0)$ and normalize the ff of all channels

$$\bar{f}_+(t) = \frac{f_+(t)}{f_+(0)} \quad \bar{f}_0(t) = \frac{f_0(t)}{f_+(0)} \quad \bar{f}_+(0) = \bar{f}_0(0)$$

$K_{\ell 3}$ Form Factors Parametrizations

Class I: Make use of physical constraints - Only one parameter required

$$\bar{f}_{+,0}(t) = \frac{m_{V,S}^2}{m_{V,S}^2 - t} \quad \text{POLE}$$


Exchange of K^* resonances with spin-parity $1^-/0^+$ and mass m_V/m_S

For f_+ dominance of $K^*(892)$, no obvious dominance for f_0

$$\bar{f}_+(t) = \exp\left[\frac{t}{m_\pi^2}(\Lambda_+ + H(t))\right] \quad \text{DISPERSIVE}$$

$$\bar{f}_0(t) = \exp\left[\frac{t}{\Delta_{K\pi}}(\ln C - G(t))\right]$$

This parametrization is based on a dispersive approach with a relation subtracted twice ($t = 0$, $t = \Delta_{K\pi}$) [PLB 638(2006) 480, PRD 80(2009) 034034]

Accurate polynomial approximations for the dispersive integrals $G(t)$ and $H(t)$ 

$K_{\ell 3}$ Form Factors Parametrizations

Class II: No Physics input - Power series expansion

Well known and widely used are the linear and quadratic:

$$\bar{f}_{+,0}(t) = \left(1 + \lambda_{+,0} t/m_\pi^2 \right) \quad \text{LINEAR}$$
$$\bar{f}_{+,0}(t) = \left[1 + \lambda'_{+,0} t/m_\pi^2 + \frac{1}{2} \lambda''_{+,0} (t/m_\pi^2)^2 \right] \quad \text{QUADRATIC}$$

- More parameters to be determined by fit \Rightarrow Correlations
- Not possible to determine λ''_0 experimentally
 $\Rightarrow \bar{f}_+$ quadratic / \bar{f}_0 linear

z-fit parametrization (PRD74(2006) 096006) belongs to this class

$K_{\ell 3}$ Form Factors and $|V_{us}|$ Determination

$K_{\ell 3}$ decays \Rightarrow most accurate and theoretically clean way to access $|V_{us}|$

The master formula for $K_{\ell 3}$ decay rates:

$$\Gamma_{K_{\ell 3}(\gamma)} = \frac{C_K^2 G_F^2 m_K^5}{192\pi^3} S_{EW} |V_{us}|^2 |f_+(0)|^2 I_K^\ell(\lambda_{+0}) (1 + \delta_{SU(2)}^\ell + \delta_{EM}^\ell)^2$$

$$\kappa = \kappa^0, \kappa^\pm; \quad c_{\kappa^0}^2 = 1 \quad c_{\kappa^\pm}^2 = 1/2$$

Experimental Inputs

$\Gamma(K_{\ell 3}(\gamma))$	Branching Ratios Kaon lifetimes
$I_K^\ell [f_{+,0}(t)]$	Phase space integral Depends on ff

Theory Inputs

S_{EW}	Universal short distance EW correction (1.0232 ± 0.0003)
$f_+(0)$	Calculated ff at $t=0$ 2^{nd} order SU(3)
$\delta_{SU(2)}^\kappa$	Form factor correction for isospin breaking (K^\pm only) $f_+^{\kappa^\pm \pi^0}(0)/f_+^{\kappa^\pm \pi^-}(0) - 1 = 0.029 \pm 0.0004$
$\delta_{EM}^{K_\ell}$	Long distance EM effects $\delta_{EM}^{K_\ell} \approx 0$ for K^\pm

- The Callan–Treiman theorem gives the value of $f_0(t)$ at the unphysical point $t = \Delta_{K\pi} = (m_K^2 - m_\pi^2)$
- The dispersive parametrization provides the link from the experimentally accessible t region to $\Delta_{K\pi}$:

$$C = \bar{f}_0(\Delta_{K\pi}) = \frac{f_{K^+}}{f_{\pi^+} f_+(0)} + \Delta_{CT}$$

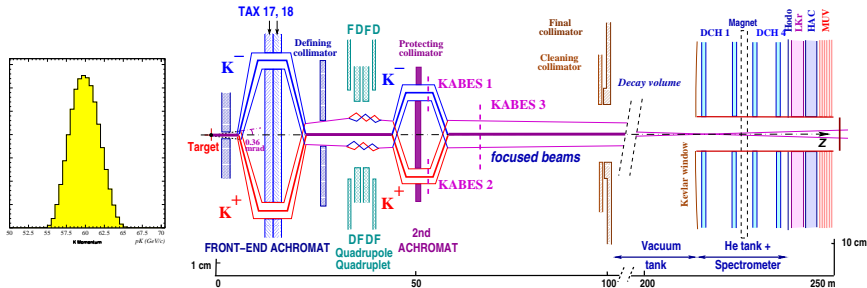
- Δ_{CT} evaluated at NLO in ChPT [Gasser and Leutwyler (85)] $\Delta_{CT} = (-3.5 \pm 8) 10^{-3}$
- For K^\pm the effect of isospin breaking is larger: $\Delta_{CT} \sim 1.5 10^{-2}$

Physics beyond SM can lead to small modifications of the fundamental QCD quantities f_{K^+} , f_{π^+} , $f_+(0)$

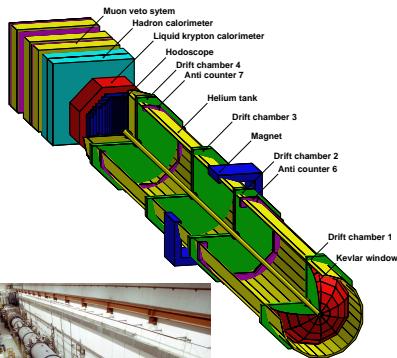
- Compare the C values obtained by BR measurements/Lattice calculations with those obtained by $K_{\mu 3}$ dispersive analysis
- If the standard values of decay constants are used lattice calculations of $f_+(0)$ can be cross-checked

$K_{\ell 3}^{\pm}$ Form Factors @ NA48/2 Experiment

- K^{\pm} collected during 2004 data taking: NA48/2 experiment
(Main purpose search for direct CP violation in $K^{\pm} \rightarrow 3\pi$ decays)
- Simultaneous K^+ and K^- beams
- K^+ flux $\simeq 3.2 \times 10^6$; $K^+/K^- \simeq 1.78$ (production rate @target)
- Dedicated run with minimum bias trigger and low intensity ($\times 1/4 I_0$)
- Reduced momentum spread: (60 ± 1.8) GeV/c
- K^+ and K^- beams coincide within 1 mm all along 114 m decay volume



The NA48 Detector



Min Bias trigger: $Q1 \times E_{LKR} > 10$

Magnetic Spectrometer

4 drift chambers

$$\frac{\sigma_p}{p}(\%) = 1 \oplus 0.044 p \text{ (GeV/c)}$$

Hodoscope

Two \perp planes of scintillator

Fast trigger

Precise track time measurement

$$\sigma_t \simeq 150 \text{ ps}$$

Liquid Krypton EM Calorimeter

Quasi-homogeneous - High granularity

13248 cells of $2 \times 2 \text{ cm}^2$

$$\frac{\sigma_E}{E}(\%) = \frac{3.2}{\sqrt{E}} \oplus \frac{9.0}{E} \oplus 0.42 \text{ (GeV)}$$

Muon Counter

3 planes of scintillator

Each shielded by 80 cm of iron

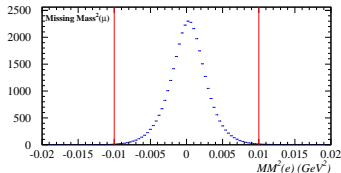
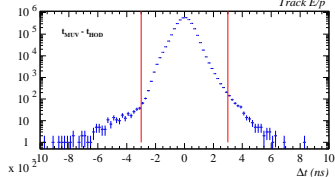
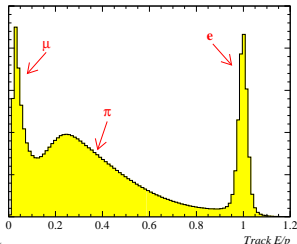
$25 \times 25 \text{ cm}^2$ cells

$$\sigma_t \simeq 350 \text{ ps}$$

$K_{\mu 3}^{\pm}$ Event Selection

- 1 "good" track and 1 π^0
 - Geometrical detector acceptance
 - Vertex - dCA track and K nominal axis
 - Track $P > 10$ GeV/c for MUC efficiency
 - Timing
 - $|m_{\gamma\gamma} - m_{\pi^0}^{PDG}| < 10$ MeV
- $E/p < 0.2$
- 1 MUC Hit matched to the track
- $|t_{MUC} - t_{HOD}| < 3$ ns
- $|\text{MM}(\mu)|^2 < 10$ MeV²
Missing Mass: $\text{MM}^2 = (P_K - P_{\mu} - P_{\pi^0})^2$
- $P_{\pi^0} > 15$ GeV
(Trigger efficiency)
- Cut to remove $\pi^{\pm}\pi^0$ BKG
(see following slide)

$3.4 \times 10^6 K_{\mu 3}^{\pm}$ events selected

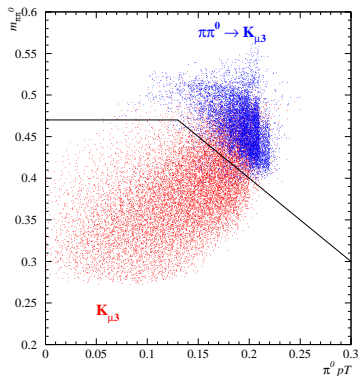
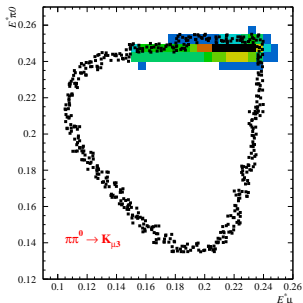


$\pi^\pm\pi^0$ Background

Decay	BR(%)	$\mathcal{P}(\pi^\pm\pi^0 \rightarrow K_{\mu 3})(\%)$
$\pi^\pm\pi^0$	20.66 ± 0.08	19.8

- $\pi^\pm\pi^0$ events with $\pi \rightarrow \mu$ can fake a $K_{\mu 3}^\pm$ decay
- This BKG is well localized on the Dalitz plot !!
- Apply cut on $m_{\pi\pi^0}$ vs $\pi^0 pT$ plane
- The loss of $K_{\mu 3}$ signal is about 24%

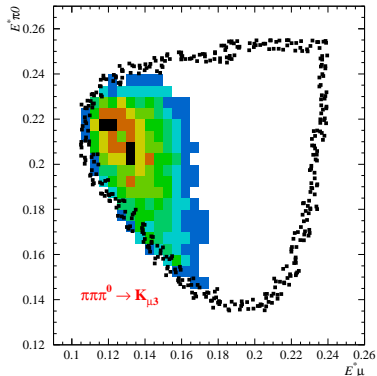
- $\pi^\pm\pi^0$ contamination reduced to 0.6%



$\pi^\pm\pi^0\pi^0$ Background

Decay	BR(%)	$\mathcal{P}(\pi^\pm\pi^0\pi^0 \rightarrow K_{\mu 3})(\%)$
$\pi^\pm\pi^0\pi^0$	1.761 ± 0.022	0.14

- Need to correct also for $\pi^\pm\pi^0\pi^0$ BKG
- Small contamination but localized on the Dalitz plot
- Shift of $\simeq 0.5 \sigma_{stat}$ if the correction is not applied



Fitting Procedure

Dalitz Plot analysis: to extract the form factors perform a fit to the DP density

$$\rho(E_\mu^*, E_\pi^*) = \frac{d^2 N(E_\mu^*, E_\pi^*)}{dE_\mu^* dE_\pi^*} \propto Af_+^2 + Bf_+ (f_0 - f_+) \frac{m_K^2 - m_\pi^2}{t} + C \left[(f_0 - f_+) \frac{m_K^2 - m_\pi^2}{t} \right]^2$$

E_μ^*, E_π^* are the energies of μ and π in the kaon CMS

A , B and C are kinematical terms

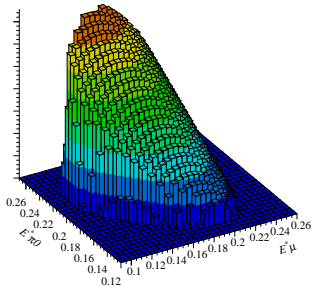
$5 \times 5 \text{ MeV}^2$ cells - Cells crossed by the Dalitz border are not used in the fit

Need to correct for:

- Acceptance

$$\epsilon = \frac{\rho(E_\mu^*, E_{\pi^0}^*)^{MC \text{ Rec}}}{\rho(E_\mu^*, E_{\pi^0}^*)^{MC \text{ Gen}}}$$

- Background subtraction
- Radiative corrections
 - Tree level parametrization
 - Need to cancel the distortion induced by radiative effects



Radiative Corrections

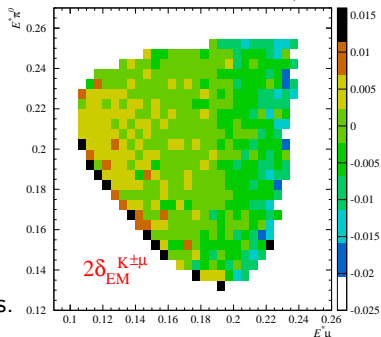
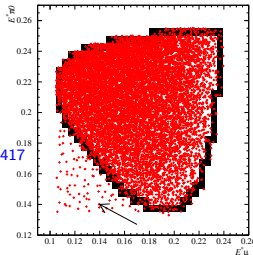
Including first order radiative corrections
the $K_{\ell 3}$ decay rate is:

$$\Gamma_{K_{\ell 3}} = \Gamma_{K_{\ell 3}}^0 + \Gamma_{K_{\ell 3}}^1 = \Gamma_{K_{\ell 3}}^0 (1 + 2\delta_{EM}^{K\ell})$$

- Simulation with C. Gatti code: EPJ C45 (2006) 417
- For the normalization use: JHEP 11 (2008) 006

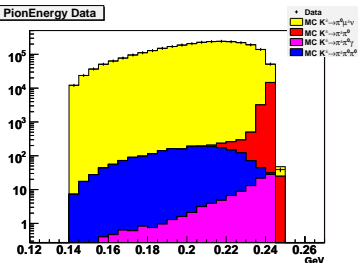
Mode	$\delta_{EM}^{K\ell}(\%)$
K_{e3}^0	0.495 ± 0.110
K_{e3}^{\pm}	0.050 ± 0.125
$K_{\mu 3}^0$	0.700 ± 0.110
$K_{\mu 3}^{\pm}$	0.008 ± 0.125

- Small effect on the acceptance
- Sign changes - Integral can be 0 even in presence of large corrections
- Smaller distortion w.r.t. the $K_{\mu 3}^0$ case
→ Only one charged particle in the f. s.

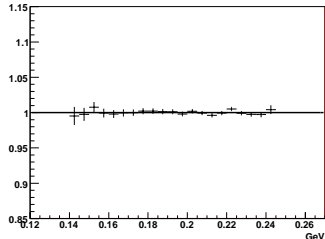


DATA-MC Comparison

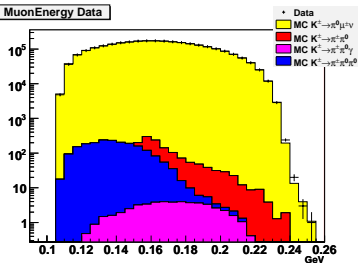
PionEnergy Data



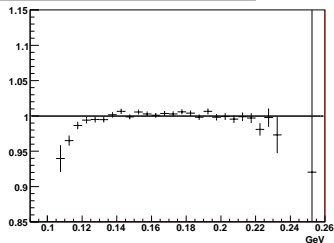
Pion energy in the Kaon restframe Data/MC



MuonEnergy Data



Muon energy in the Kaon restframe Data/MC



QUADRATIC ($\times 10^3$)

λ'_+	λ''_+	λ_0
$30.3 \pm 2.7 \pm 1.4$	$1.0 \pm 1.0 \pm 0.7$	$15.6 \pm 1.2 \pm 0.9$

POLE (MeV/c²)

m_V	m_S
$836 \pm 7 \pm 9$	$1210 \pm 25 \pm 10$

DISPERSIVE ($\times 10^3$)

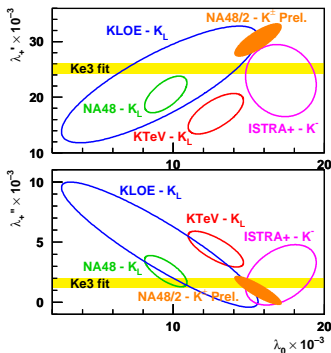
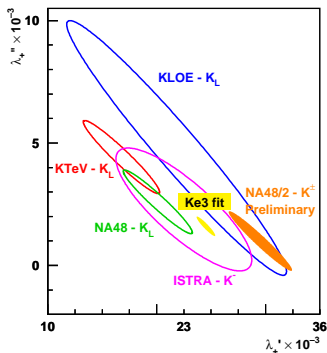
Λ_+	$\ln C$
$28.5 \pm 0.6 \pm 0.7 \pm 0.5$	$188.8 \pm 7.1 \pm 3.7 \pm 5.0$

- First error is stat, second is syst
- To the dispersive results the uncertainty has been added

V. Bernard et al., PRD80 (2009) 034034

z-fit in progress...

$K_{\mu 3}^{\pm}$ Form Factors - Quadratic Fits



K_{e3} averages from



WG1

1 σ contours

- Experimental situation on quadratic fit for $K_{\mu 3}$ decay
- $K_{\mu 3}^0$ results from KLOE, KTeV and NA48, ISTR A measures $K_{\mu 3}^-$
- First measurement which uses also $K_{\mu 3}^+$
- High precision - Very competitive with other results
- Small quadratic term - Larger λ_0 with respect to NA48 case
- Size and dispersion of ellipses indicate the difficulty of this measurement



Preliminary Survey of Systematics

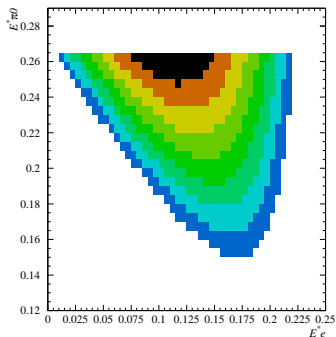
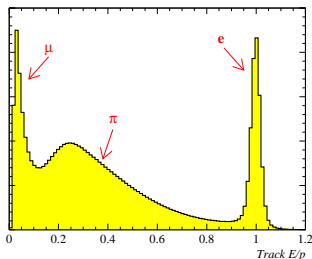
	$\Delta\lambda'_+$	$\Delta\lambda''_+$ $\times 10^{-3}$	$\Delta\lambda_0$	Δm_V	Δm_S MeV/c ²	$\Delta\Lambda_+$	$\Delta \ln C$ $\times 10^{-3}$
K^\pm Energy	± 0.7	± 0.5	± 0.6	± 7	± 2	± 0.5	± 2.6
Vertexing	± 1.0	± 0.4	± 0.6	± 2	± 4	± 0.1	± 1.1
Acceptance	± 0.3	± 0.1	± 0.2	± 2	± 7	± 0.1	± 1.8
$\pi \rightarrow \mu$ scale	± 0.4	± 0.2	± 0.2	± 1	± 1	± 0.0	± 0.0
2 nd analysis	± 0.4	± 0.1	± 0.2	± 6	± 6	± 0.5	± 1.5
Total Systematic	± 1.4	± 0.7	± 0.9	± 10	± 10	± 0.7	± 3.7
Statistical	± 2.7	± 1.0	± 1.3	± 7	± 26	± 0.6	± 7.1
Theory						± 0.5	± 5.0
Total Error	± 3.0	± 1.2	± 1.6	± 12	± 28	± 1.0	± 10.1

- K^\pm Energy - Calculate two energy solutions (as in K_L case) instead of using the nominal beam energy of 60 GeV
 \Rightarrow Better resolution on CMS variables
- KType2 (2 sol) - KType1 (1 sol) - KType0 (sol outside allowed range)
- $\pi \rightarrow \mu$ scale - Accounts for not perfect modeling of π decay in the region from LKR onwards

K_{e3}^{\pm} Form Factors

- Event selection is similar to $K_{\mu 3}^{\pm}$
- Require 1 "good" track and 1 π^0
- electron ID with $0.95 < E/p < 1.05$
- Event pT cut to remove $\pi^{\pm}\pi^0$ BKG
- "Easier" measurement
 - Only one form factor
 - Reduced correlations
 - BKG issues less critical
 - Need a π with $E/p > 0.95$
- Expected more precise results
- Analysis is in progress
- Results for the winter conferences

4.2×10^6 K_{e3}^{\pm} events selected



NA62, during the 2007 run, collected data for a dedicated measurement of $R_K = \Gamma(K_{e2})/\Gamma(K_{\mu 2})$ and tests for the future $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ experiment



- 4 months data taking with minimum bias trigger
→ 1 track+ 10 GeV deposition in EM calorimeter
- Simultaneous K^+ and K^- beams of $P=(74 \pm 1.6)$ GeV/c
- Better track momentum resolution (→ p_T kick doubled)
- Collected ~ 150000 K_{e2} events
- First results for 40% of stat presented at BEACH2010 and ICHEP2010
- Expected precision on the full data sample: $\sigma(R_K)/R_K \simeq \pm 0.4\%$

$K_{\ell 3}$ from NA62 2007 data

- Huge $K_{e3}^+/K_{\mu 3}^+$ statistics of $\approx 40/20 \times 10^6$
- Special K_L run (15 h) to measure electron ID efficiency
 K_{e3}^0 and $K_{\mu 3}^0$ statistics $\approx 4 \times 10^6$

NA48 analyses of $K_{\ell 3}^0$ and $K_{\ell 3}^{\pm}$ can be repeated with different/larger data sets

Summary

- NA48/2 has provided a new contribution to $|V_{us}|$ quest
- Preliminary results on $K_{\mu 3}^{\pm}$ form factors
- For the first time both K^+ and K^- decays have been studied
- High precision measurement very competitive with other results
- Soon also new results on $K_{e 3}^{\pm}$ will appear
- NA62 is ready to give its contribution with high statistics data samples of $K_{\ell 3}^{\pm}$ and $K_{\ell 3}^0$