

# Higgs Couplings at Muon Collider

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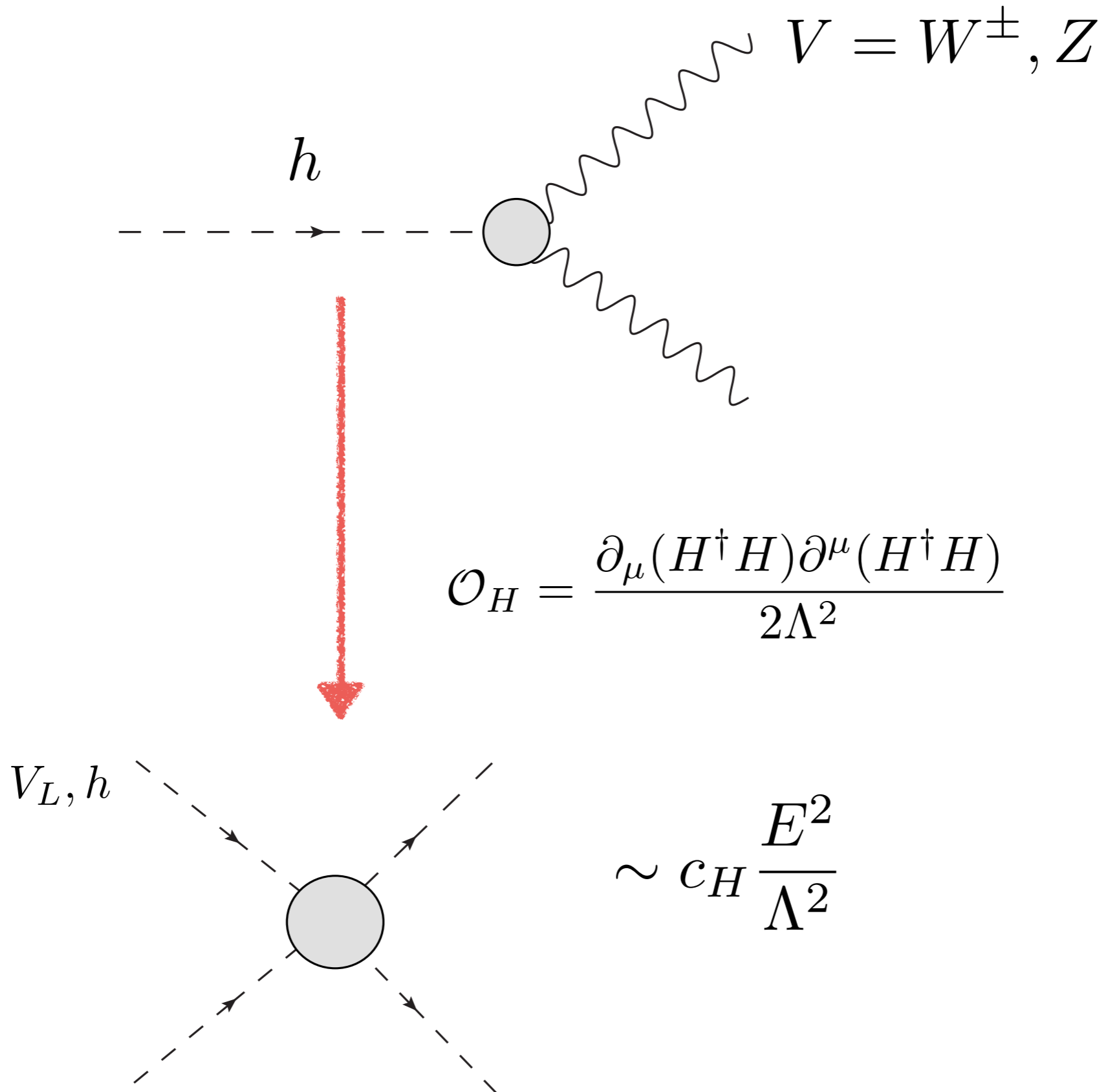
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2008.12204

# Outline

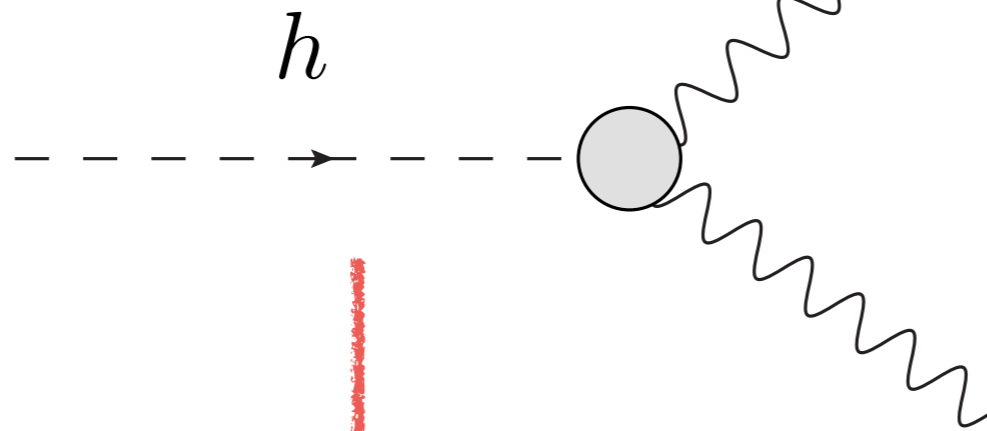
- Higgs coupling modification to energy growing behavior
- Higgs coupling measurements at Muon Collider

# Higgs-Gauge Boson couplings

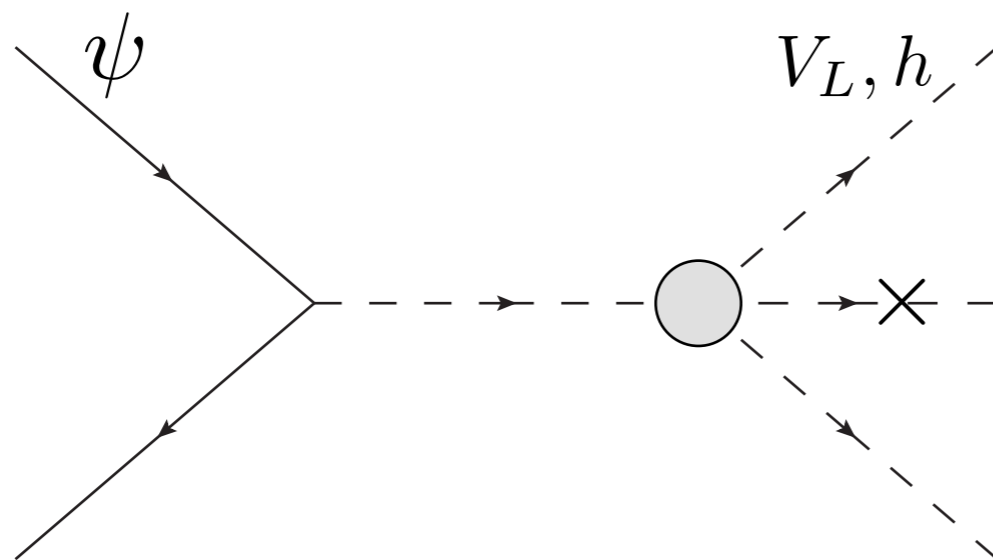


# Higgs-Gauge Boson couplings

$$V = W^\pm, Z$$

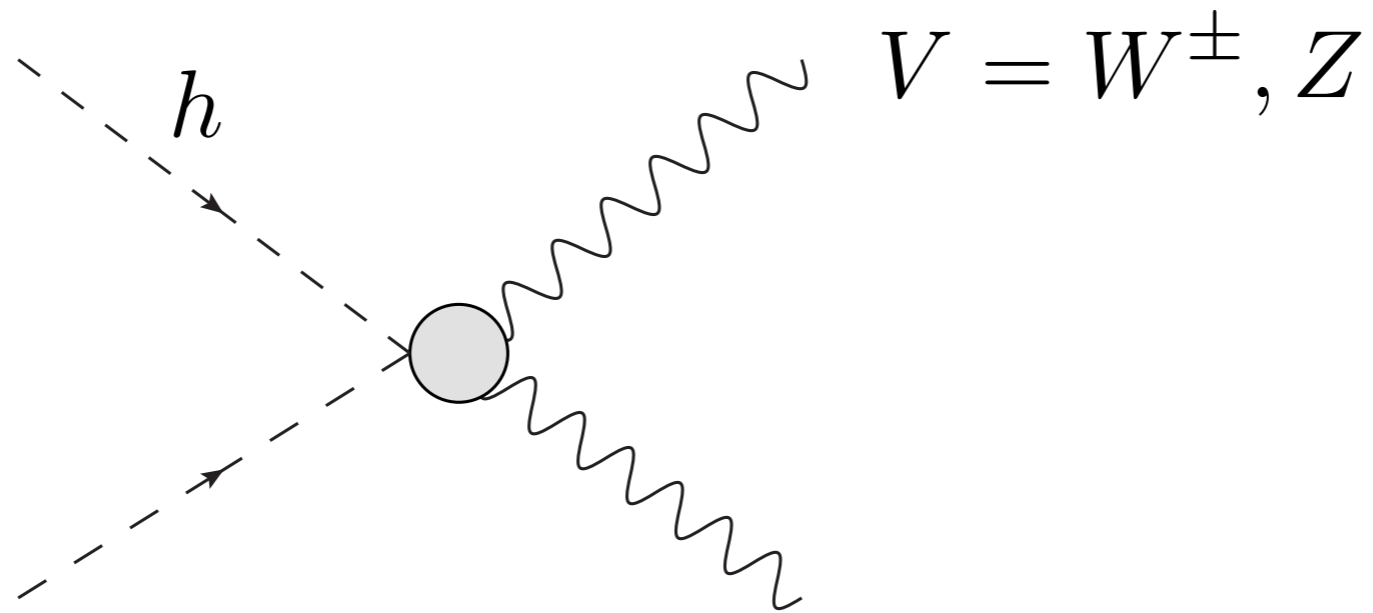


$$\mathcal{O}_H = \frac{\partial_\mu (H^\dagger H) \partial^\mu (H^\dagger H)}{2\Lambda^2}$$

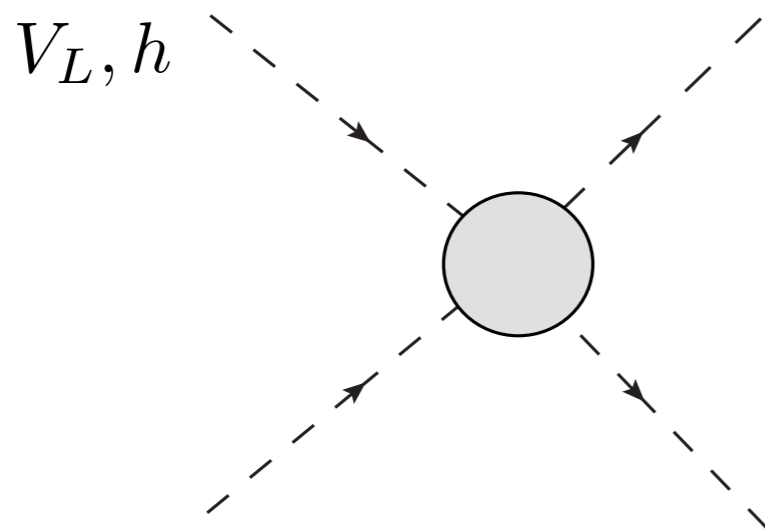


$$\sim c_H \frac{vE}{\Lambda^2}$$

# Higgs-Higgs-Gauge Boson couplings

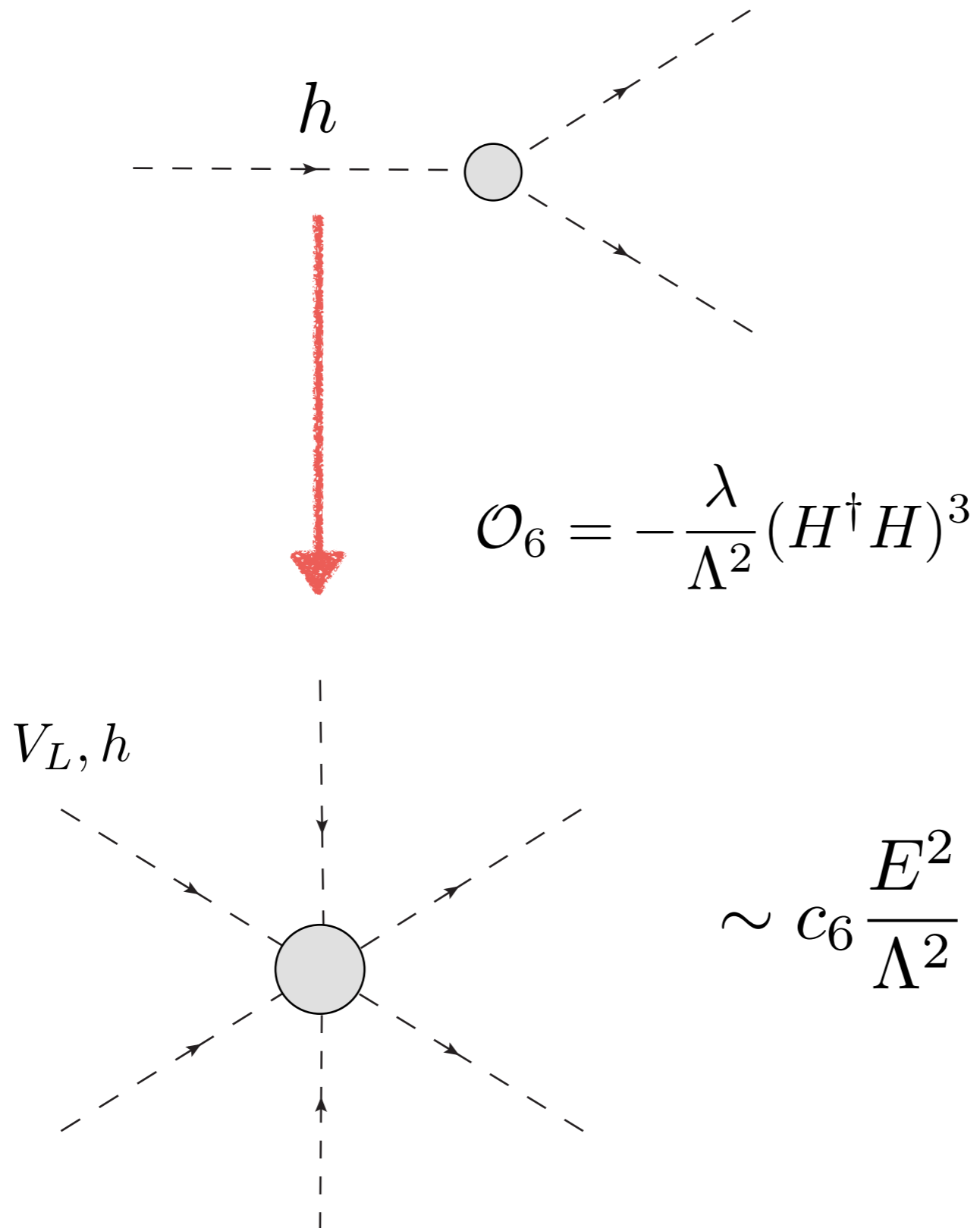


$$\mathcal{O}_H = \frac{\partial_\mu (H^\dagger H) \partial^\mu (H^\dagger H)}{2\Lambda^2}$$

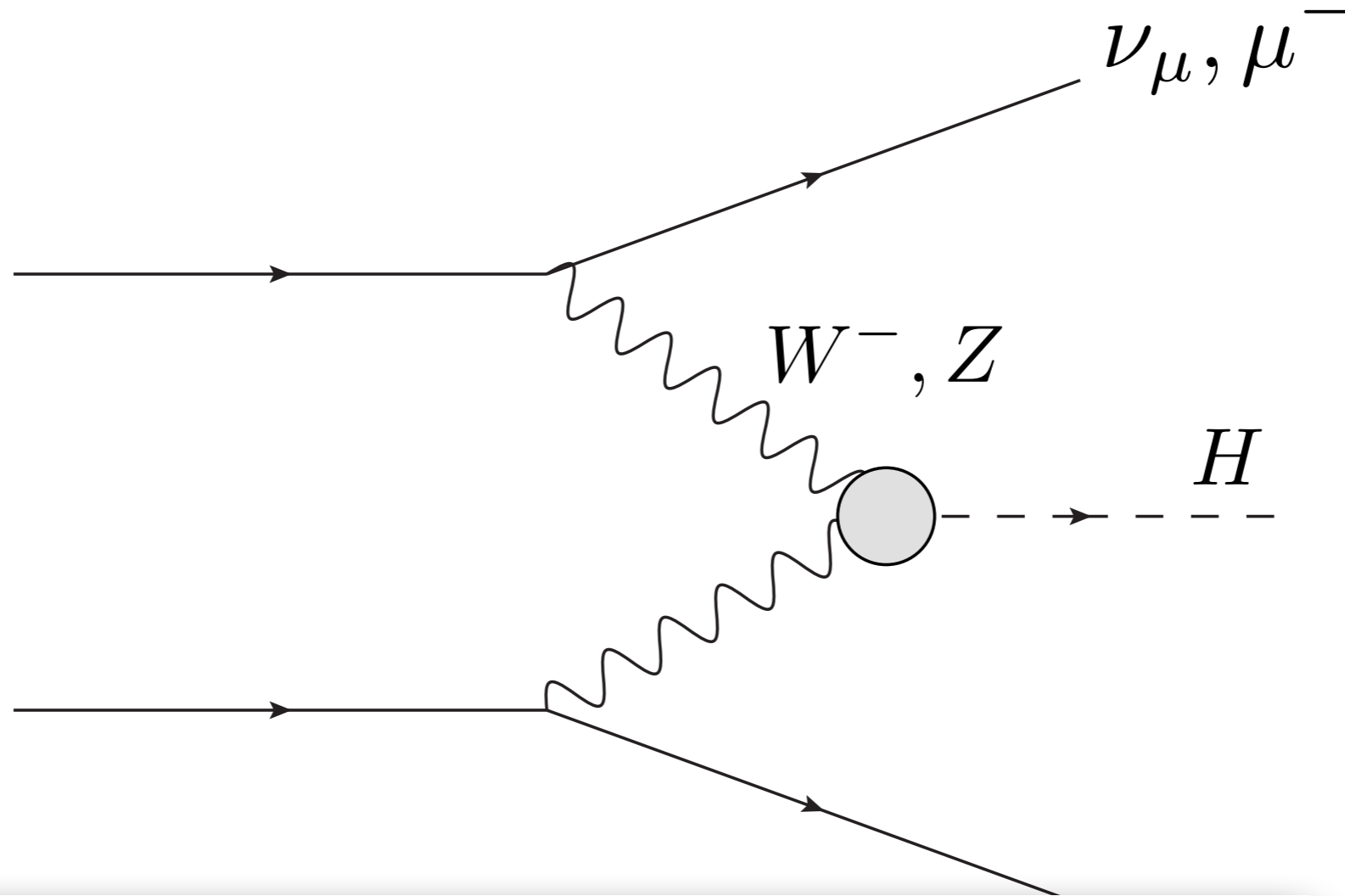


$$\sim c_H \frac{E^2}{\Lambda^2}$$

# Higgs self couplings



# VBF Single Higgs



|                                     |     |     |     |     |      |
|-------------------------------------|-----|-----|-----|-----|------|
| $\sqrt{s}$ (TeV)                    | 3   | 6   | 10  | 14  | 30   |
| benchmark lumi ( $\text{ab}^{-1}$ ) | 1   | 4   | 10  | 20  | 90   |
| $\sigma$ (fb): $WW \rightarrow H$   | 490 | 700 | 830 | 950 | 1200 |
| $ZZ \rightarrow H$                  | 51  | 72  | 89  | 96  | 120  |

|                     |      |      |      |      |      |
|---------------------|------|------|------|------|------|
| $WW \rightarrow Z$  | 2200 | 3100 | 3600 | 4200 | 5200 |
| $WW \rightarrow ZZ$ | 57   | 130  | 200  | 260  | 420  |

$\mathcal{O}(10^7) H$

$$\frac{S}{B} \sim \frac{1}{4}$$

# Basic Cuts: $H \rightarrow bb$

- Basic Acceptance cuts

$$p_{T,b} > 30 \text{ GeV} \quad 10^\circ < \theta_b < 170^\circ \quad (|\eta_b| < 2.44)$$

- Smearing Effects

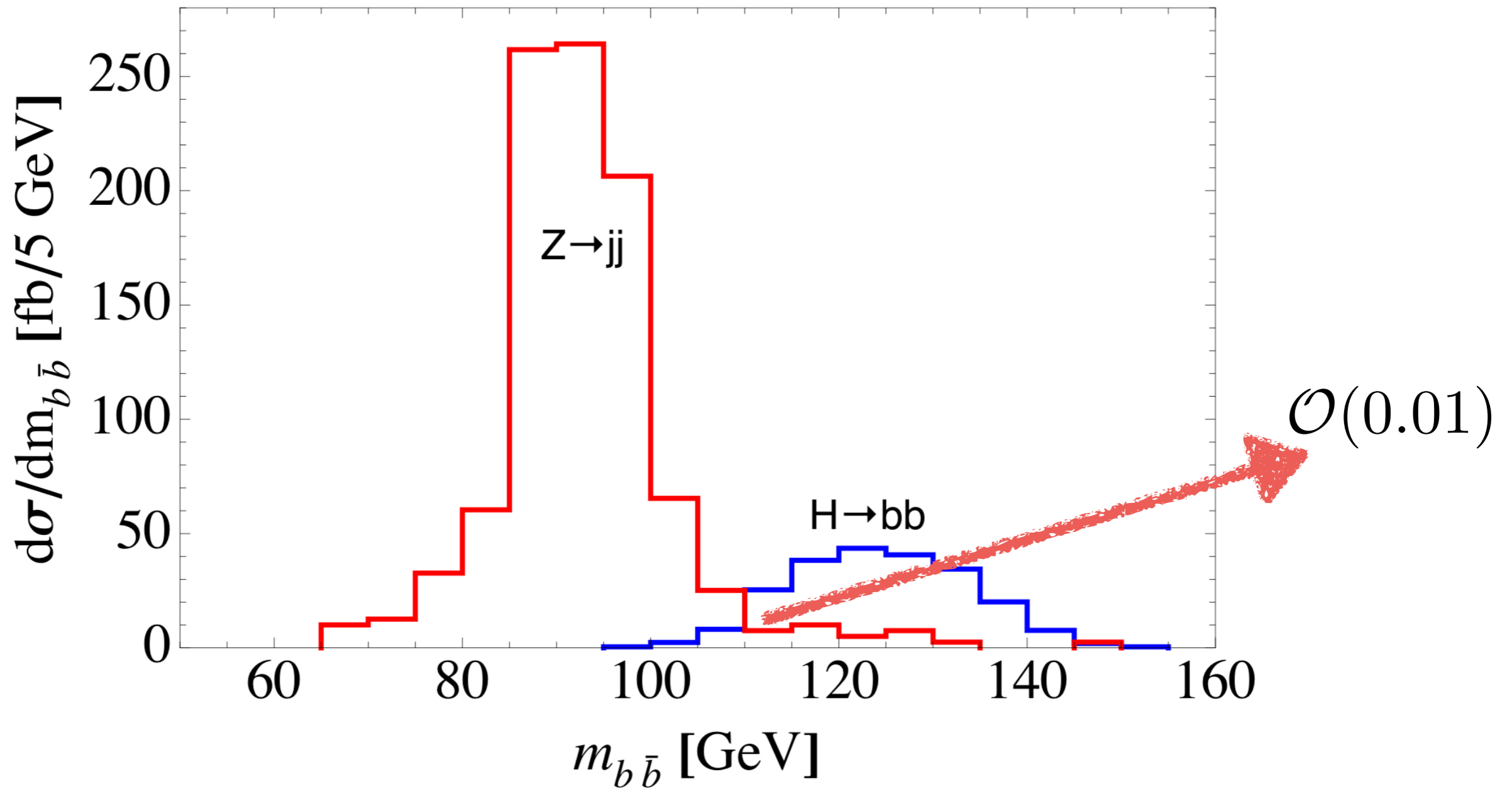
$$\frac{\Delta E}{E} = 10\%$$

- Recoil mass cut to suppress  $ZZ(\nu\nu)$  background

$$M_{\text{recoil}} = \sqrt{(p_{\mu^+} + p_{\mu^-} - p_{H,HH})^2} > 200 \text{ GeV}$$

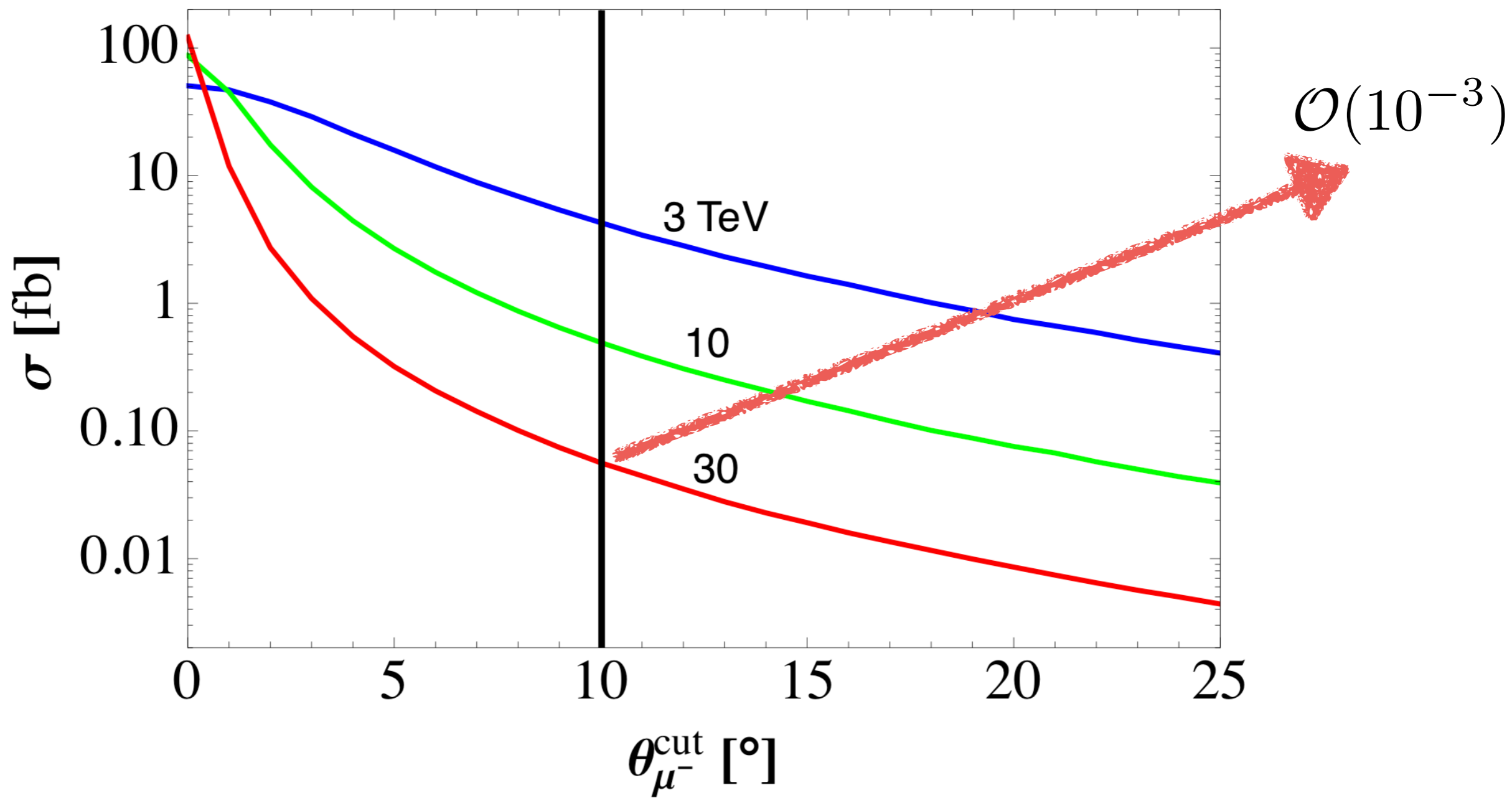


# Invariant Mass Distribution

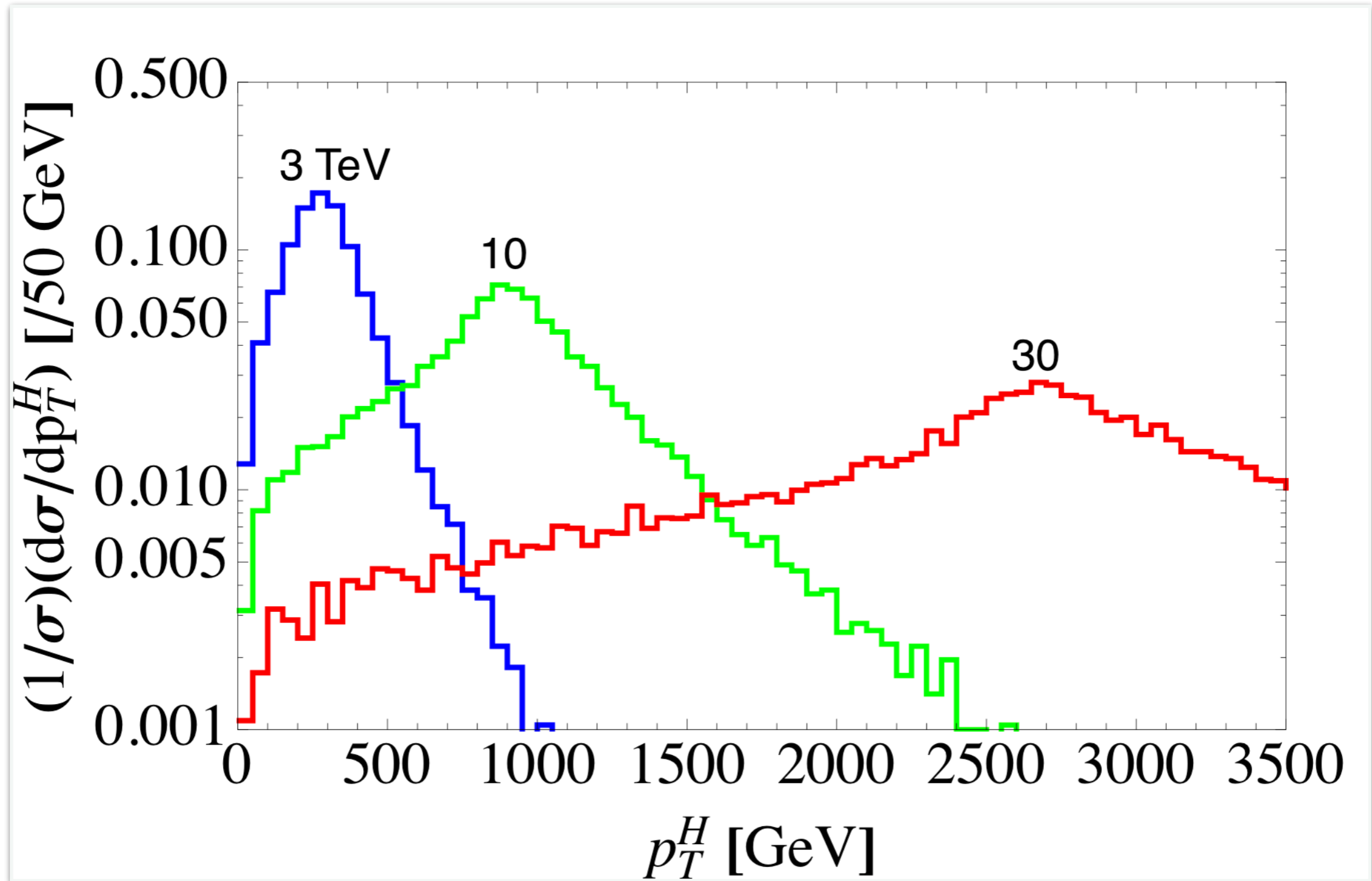


$$|m_{b\bar{b}} - m_H| < 15 \text{ GeV}$$

# HZZ: Forward muons



# One muon tagged



$$10^\circ < \theta_\mu < 170^\circ$$

$$p_T^\mu > 0.17 E_\mu$$

# Results: Efficiency

| $\sqrt{s}$ (TeV)                              | 3   | 6   | 10   | 14   | 30    |
|---|-----|-----|------|------|-------|
| $WW \rightarrow H : \epsilon_{\text{in}}$ (%) | 54  | 46  | 42   | 39   | 32    |
| $ZZ \rightarrow H : \epsilon_{\text{in}}$ (%) | 57  | 49  | 44   | 41   | 35    |
| Cross section $\sigma_{\text{in}}$ (fb)       | 170 | 200 | 220  | 240  | 240   |
| $ZZ \rightarrow H : \epsilon_{1\mu}$ (%)      | 11  | 2.7 | 0.84 | 0.37 | 0.071 |
| Cross section $\sigma_{1\mu}$ (fb)            | 3.1 | 1.1 | 0.43 | 0.20 | 0.050 |
| $VV \rightarrow HH : \epsilon_{hh}$ (%)       | 27  | 18  | 13   | 11   | 7.2   |
| Cross section $\sigma_{hh}$ (ab)              | 81  | 140 | 150  | 170  | 200   |

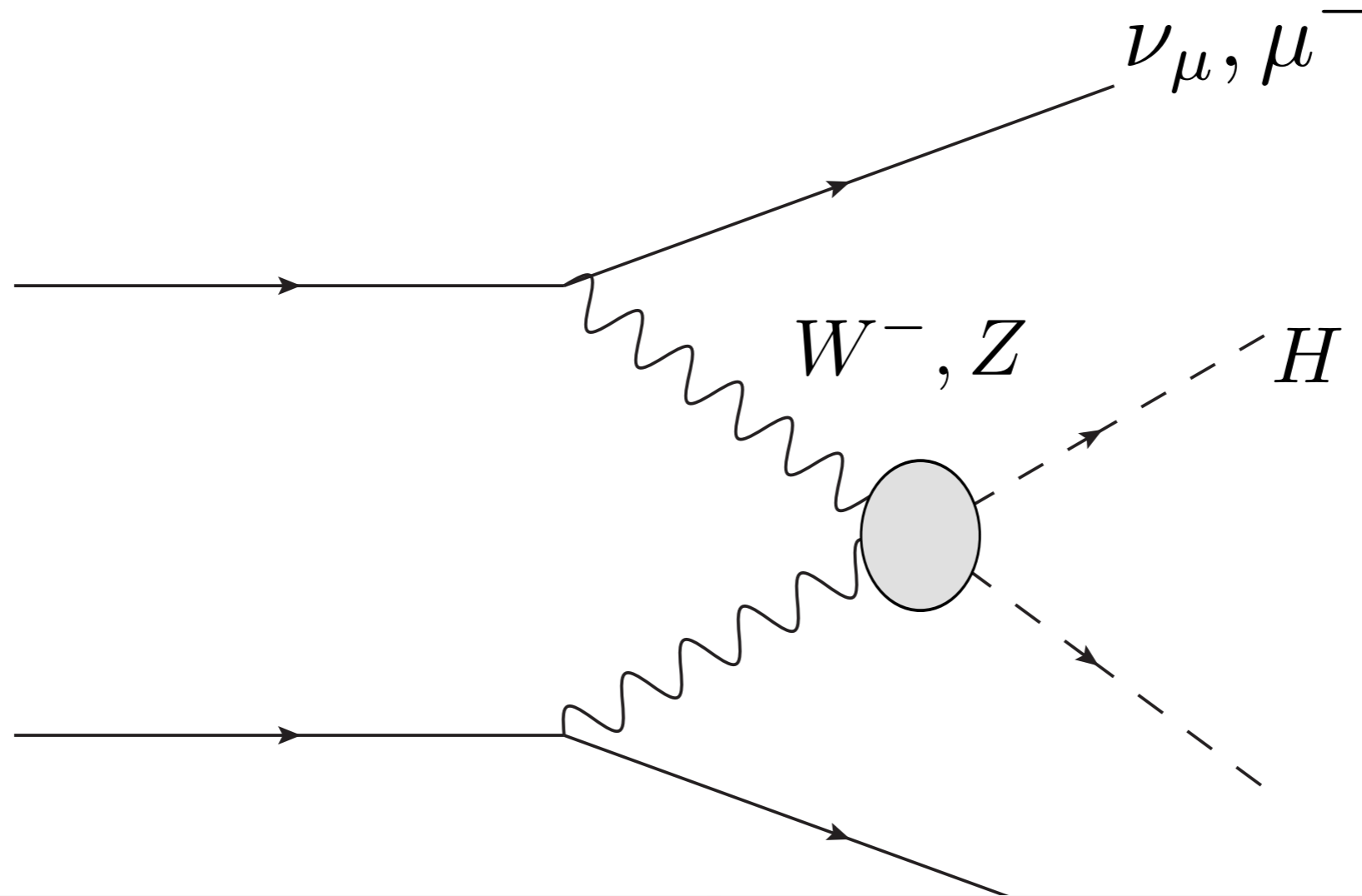
Forward muon effect

# Results: Sensitivity

| $\sqrt{s}$ (TeV)                    | 3     | 6     | 10     | 14     | 30     |
|-------------------------------------|-------|-------|--------|--------|--------|
| benchmark lumi ( $\text{ab}^{-1}$ ) | 1     | 4     | 10     | 20     | 90     |
| $(\Delta\kappa_W)_{\text{in}}$      | 0.26% | 0.12% | 0.073% | 0.050% | 0.023% |
| $(\Delta\kappa_Z)_{\text{in}}$      | 2.4%  | 1.1%  | 0.65%  | 0.46%  | 0.20%  |
| $(\Delta\kappa_Z)_{1\mu}$           | 1.7%  | 1.5%  | 1.5%   | 1.5%   | 1.5%   |

- 3 to 30 TeV, a factor of 10 improvement
- Mainly due to luminosity increase

# VBF Double Higgs



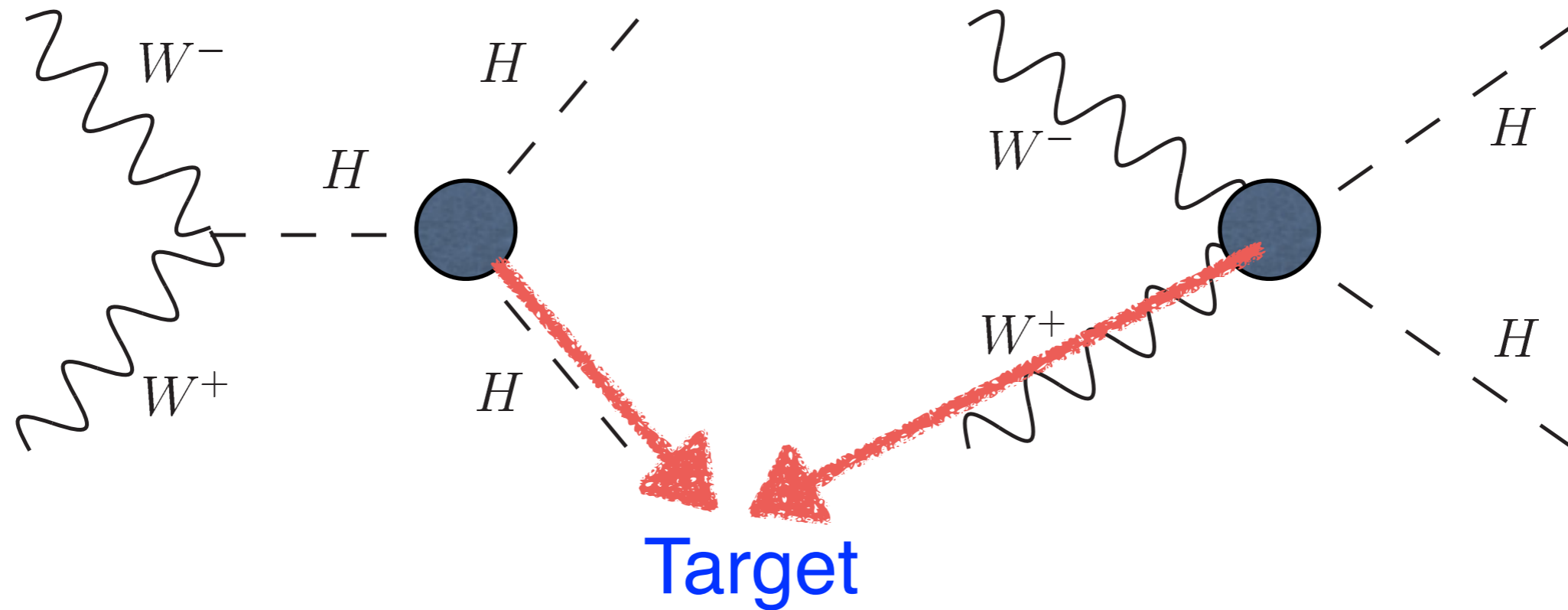
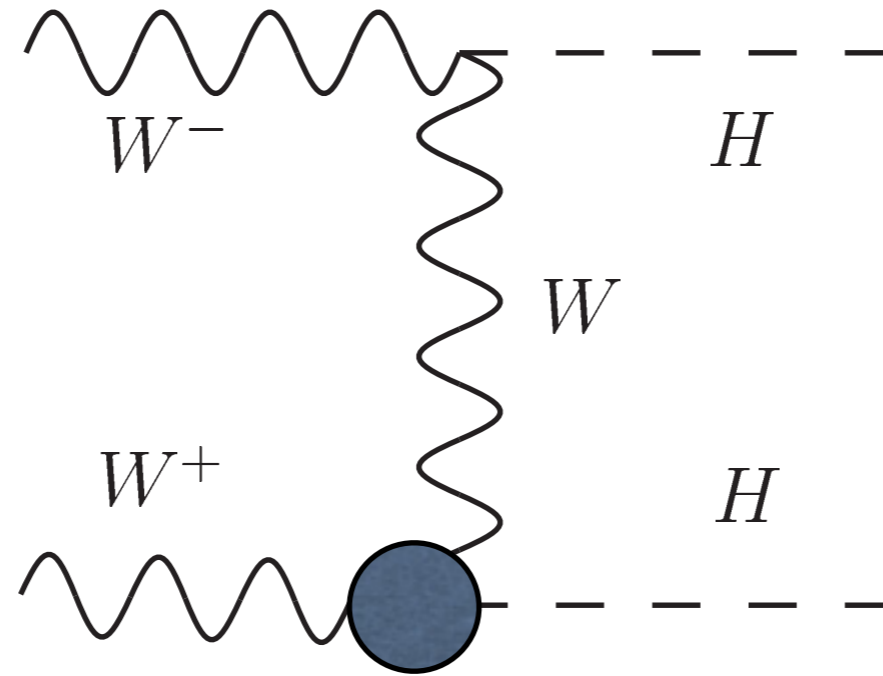
|                                     |      |      |      |      |      |
|-------------------------------------|------|------|------|------|------|
| $\sqrt{s}$ (TeV)                    | 3    | 6    | 10   | 14   | 30   |
| benchmark lumi ( $\text{ab}^{-1}$ ) | 1    | 4    | 10   | 20   | 90   |
| $WW \rightarrow HH$                 | 0.80 | 1.8  | 3.2  | 4.3  | 6.7  |
| $ZZ \rightarrow HH$                 | 0.11 | 0.24 | 0.43 | 0.57 | 0.91 |
| $WW \rightarrow ZZ$                 | 57   | 130  | 200  | 260  | 420  |

fb

$\mathcal{O}(10^4) HH$

$\frac{S}{B} \sim 0.02$

# VBF Double Higgs



# HHH vs HHVV

$$\sigma = \sigma_{\text{SM}} \left[ 1 + r_1 \Delta\kappa_{W_2} + r_2 \Delta\kappa_3 + r_3 \Delta\kappa_{W_2} \Delta\kappa_3 + r_4 (\Delta\kappa_{W_2})^2 + r_5 (\Delta\kappa_3)^2 \right]$$

| $m_{HH}$ [GeV] | $\sigma_{\text{SM}}$ [ab] | $r_1$ | $r_2$ | $r_3$ | $r_4$ | $r_5$ |
|----------------|---------------------------|-------|-------|-------|-------|-------|
| [0, 350)       | 15                        | -2.7  | -1.7  | 7.6   | 6.7   | 2.6   |
| [350, 450)     | 24                        | -3.4  | -1.2  | 5.2   | 7.8   | 0.95  |
| [450, 550)     | 24                        | -4.0  | -0.91 | 4.6   | 12    | 0.52  |
| [550, 650)     | 21                        | -4.6  | -0.70 | 4.7   | 17    | 0.36  |
| [650, 750)     | 17                        | -5.3  | -0.60 | 5.1   | 26    | 0.28  |
| [750, 950)     | 24                        | -6.9  | -0.52 | 6.3   | 46    | 0.23  |
| [950, 1350)    | 23                        | -11   | -0.47 | 8.7   | 120   | 0.19  |
| [1350, 5000)   | 15                        | -18   | -0.30 | 7.2   | 240   | 0.075 |



Sign of energy growing behavior

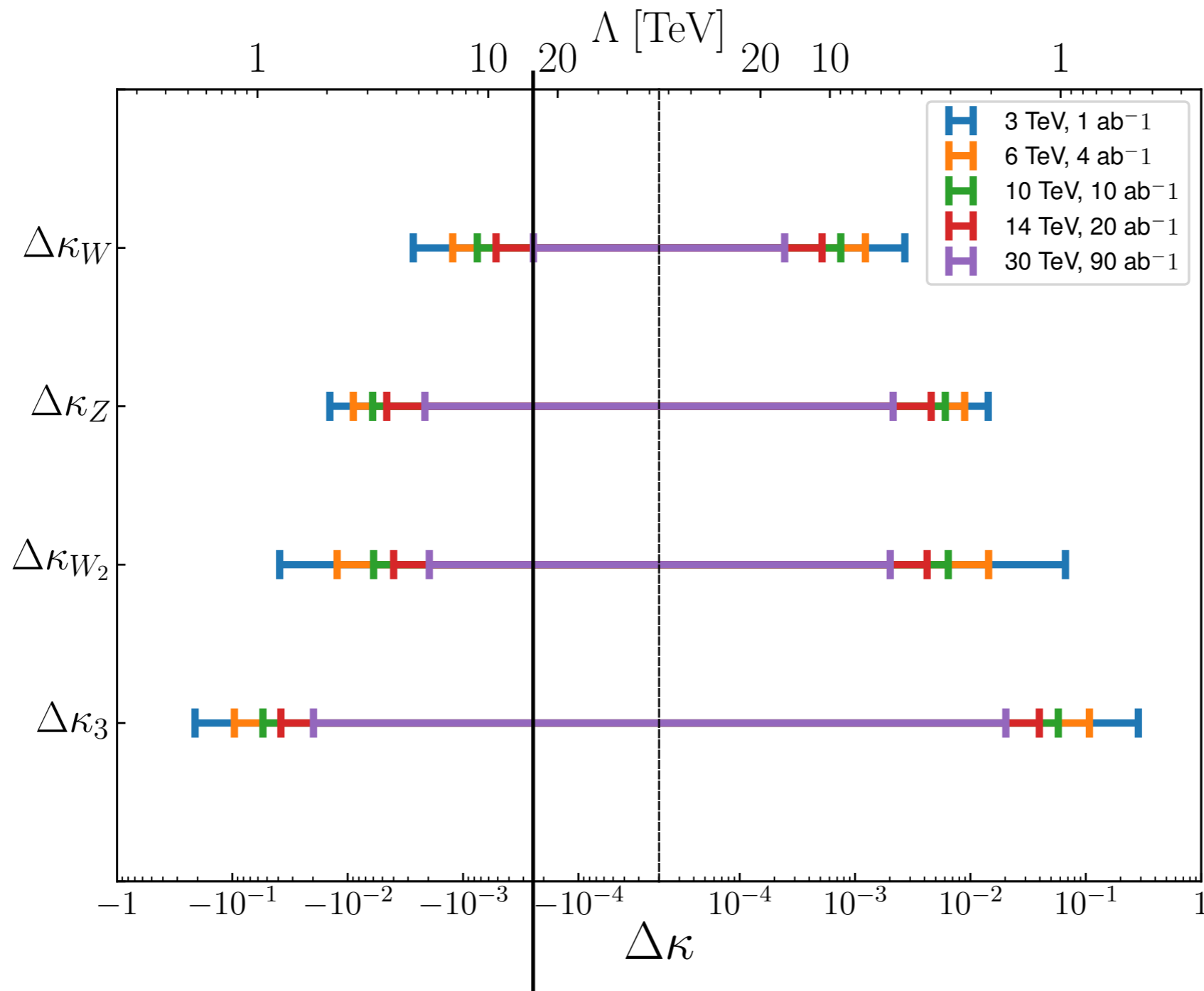


# HHH vs HHVV: Sensitivity

|                                     |      |      |       |       |       |
|-------------------------------------|------|------|-------|-------|-------|
| $\sqrt{s}$ (TeV)                    | 3    | 6    | 10    | 14    | 30    |
| benchmark lumi ( $\text{ab}^{-1}$ ) | 1    | 4    | 10    | 20    | 90    |
| $(\Delta\kappa_{W_2})_{\text{in}}$  | 5.3% | 1.3% | 0.62% | 0.41% | 0.20% |
| $(\Delta\kappa_3)_{\text{in}}$      | 25%  | 10%  | 5.6%  | 3.9%  | 2.0%  |

- 3 to 30 TeV, a factor of 25 improvement
- luminosity plus energy growing behavior

# Result Summary



10 - 20 TeV

# Implication: Composite Higgs Models

$$\Delta\kappa_W = -\frac{1}{2}\xi$$



$$\xi < 0.15\%$$



$$f > 6.4\text{TeV}$$

$$\Delta\kappa_{W_2} = -2\xi$$



$$\xi < 0.31\%$$



$$f > 4.4\text{TeV}$$

$$\xi = \frac{v^2}{f^2}$$

10 TeV @ 10 ab<sup>-1</sup>

95 %CL

# Implication: Nonlinearity Test

$$\mathcal{O}_H = \frac{c_H}{2f^2} \partial_\mu |H|^2 \partial^\mu |H|^2 \quad \mathcal{O}'_H = \frac{c'_H}{2f^4} |H|^2 \partial_\mu |H|^2 \partial^\mu |H|^2$$



$$\Delta\kappa_W = -\frac{1}{2}\xi + \left( \frac{3}{8}c_H^2 - \frac{c'_H}{4} \right) \xi^2$$
$$\Delta\kappa_{W_2} = -2\xi + \left( 3c_H^2 - \frac{3c'_H}{2} \right) \xi^2$$

PNGB



$$c'_H = 2c_H^2$$

Promising for  $\xi \gtrsim 0.1$

# Conclusion

- ✓ Sub-permille level on HVV
- ✓ Sub-percent level on HHVV
- ✓ Percent level on HHH

Back-up Slides

# Cross Section

| $\sqrt{s}$ (TeV)                    | 3     | 6     | 10    | 14   | 30   |
|-------------------------------------|-------|-------|-------|------|------|
| benchmark lumi ( $\text{ab}^{-1}$ ) | 1     | 4     | 10    | 20   | 90   |
| $\sigma$ (fb): $WW \rightarrow H$   | 490   | 700   | 830   | 950  | 1200 |
| $ZZ \rightarrow H$                  | 51    | 72    | 89    | 96   | 120  |
| $WW \rightarrow HH$                 | 0.80  | 1.8   | 3.2   | 4.3  | 6.7  |
| $ZZ \rightarrow HH$                 | 0.11  | 0.24  | 0.43  | 0.57 | 0.91 |
| $WW \rightarrow ZH$                 | 9.5   | 22    | 33    | 42   | 67   |
| $WW \rightarrow t\bar{t}H$          | 0.012 | 0.046 | 0.090 | 0.14 | 0.28 |
| $WW \rightarrow Z$                  | 2200  | 3100  | 3600  | 4200 | 5200 |
| $WW \rightarrow ZZ$                 | 57    | 130   | 200   | 260  | 420  |

# Cross Section

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| $\sqrt{s}$ [TeV] | $\sigma_{\text{SM}}$ [fb] | $R_1$ | $R_2$ | $R_3$ | $R_4$ | $R_5$ |
|------------------|---------------------------|-------|-------|-------|-------|-------|
| 3 TeV            | 0.91                      | -3.5  | -0.65 | 3.1   | 14    | 0.49  |
| 6 TeV            | 2.0                       | -3.9  | -0.50 | 2.8   | 29    | 0.35  |
| 10 TeV           | 3.6                       | -4.3  | -0.43 | 2.7   | 54    | 0.29  |
| 14 TeV           | 4.9                       | -4.4  | -0.38 | 2.6   | 80    | 0.25  |
| 30 TeV           | 7.6                       | -4.4  | -0.28 | 2.3   | 210   | 0.19  |

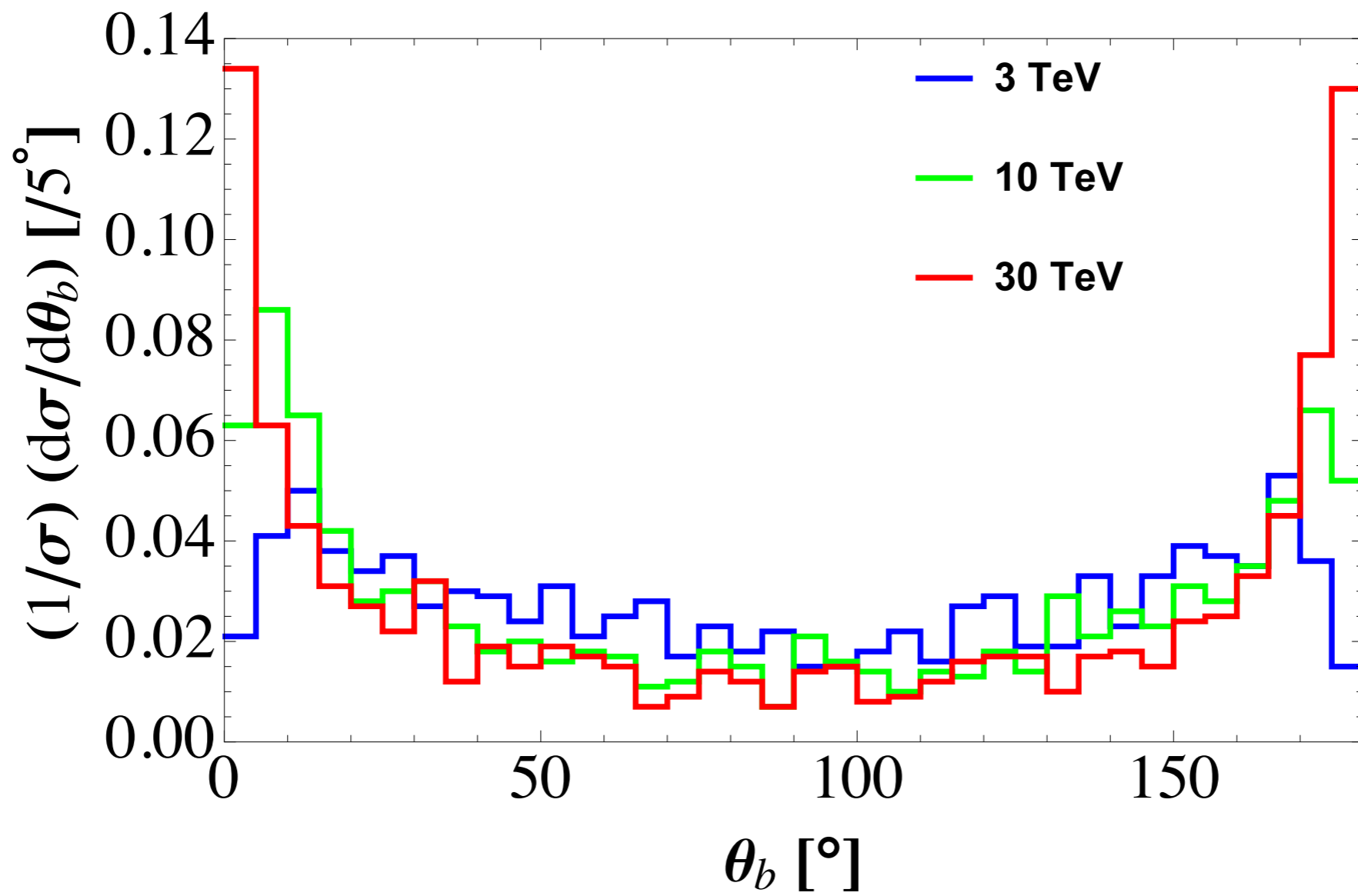
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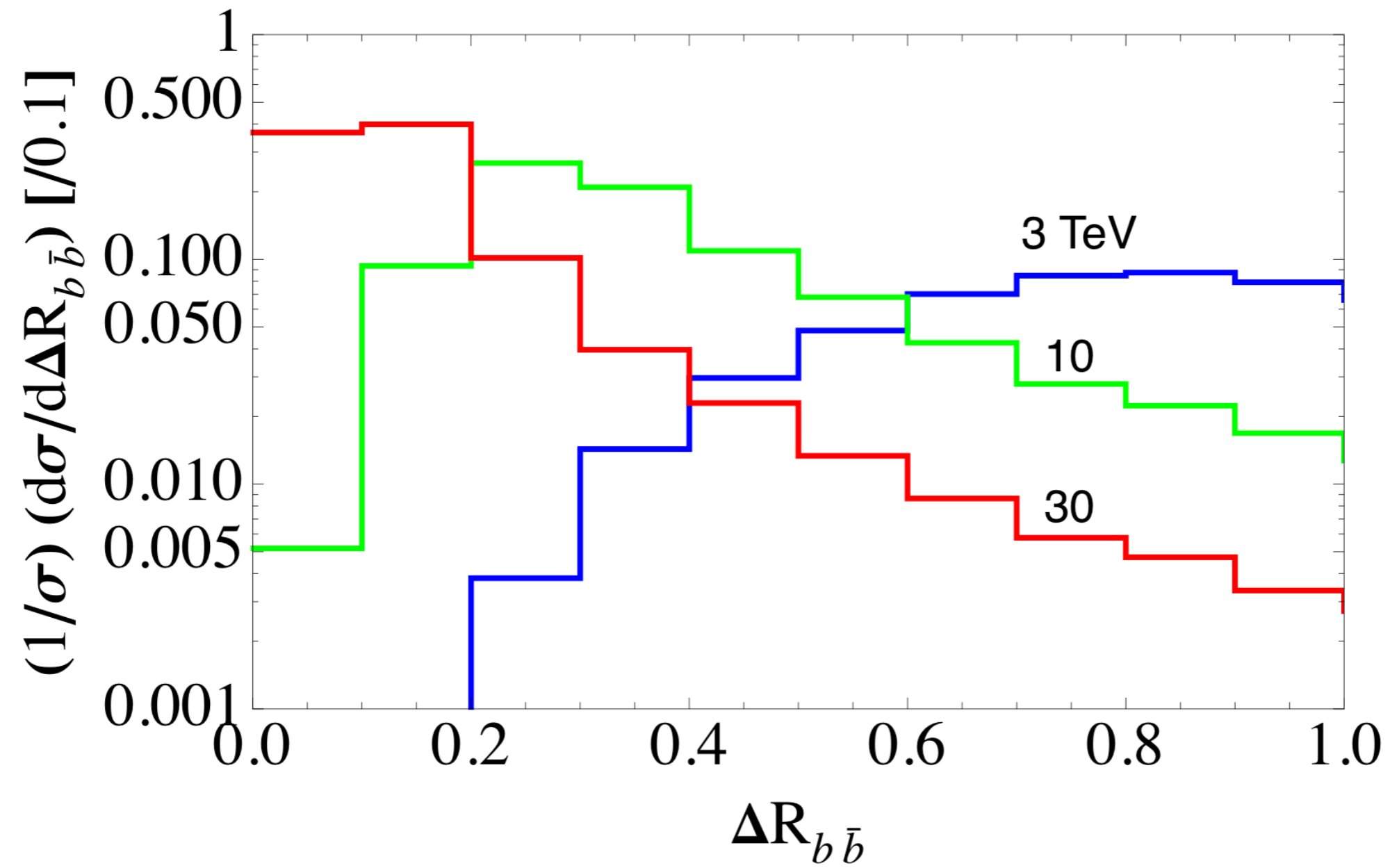
# Sensitivity Comparison

| $\sqrt{s}$ (lumi.)              | 3 TeV (1 ab <sup>-1</sup> ) | 6 (4) | 10 (10) | 14 (20) | 30 (90) | Comparison       |
|---------------------------------|-----------------------------|-------|---------|---------|---------|------------------|
| $WWH$ ( $\Delta\kappa_W$ )      | 0.26%                       | 0.12% | 0.073%  | 0.050%  | 0.023%  | 0.1% [43]        |
| $\Lambda/\sqrt{c_i}$ (TeV)      | 4.7                         | 7.0   | 9.0     | 11      | 16      | (68% C.L.)       |
| $ZZH$ ( $\Delta\kappa_Z$ )      | 1.4%                        | 0.89% | 0.61%   | 0.46%   | 0.21%   | 0.13% [17]       |
| $\Lambda/\sqrt{c_i}$ (TeV)      | 2.1                         | 2.6   | 3.2     | 3.6     | 5.3     | (95% C.L.)       |
| $WWHH$ ( $\Delta\kappa_{W_2}$ ) | 5.3%                        | 1.3%  | 0.62%   | 0.41%   | 0.20%   | 5% [38], 1% [24] |
| $\Lambda/\sqrt{c_i}$ (TeV)      | 1.1                         | 2.1   | 3.1     | 3.8     | 5.5     | (68% C.L.)       |
| $HHH$ ( $\Delta\kappa_3$ )      | 25%                         | 10%   | 5.6%    | 3.9%    | 2.0%    | 5% [22, 23]      |
| $\Lambda/\sqrt{c_i}$ (TeV)      | 0.49                        | 0.77  | 1.0     | 1.2     | 1.7     | (68% C.L.)       |

# Kinematical Variable Distribution



# Kinematical Variable Distribution



# HHH vs HHVV

