

EW SPHALERONS: DISCUSSION POINTS

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Topological Effects in the Standard Model: Instantons, Sphalerons and Beyond at LHC
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Implications

- Critical field strength where sphaleron energy vanishes is

$$B_{\text{crit}}^{(2)} = \frac{m_{\text{H}}^2}{e} \approx 5.2 \times 10^4 \text{ GeV} \approx 2.7 \times 10^{20} \text{ T}$$

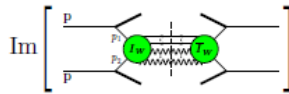
- Magnetic fields in LHC heavy-ion collisions $\sim 1 \text{ GeV}^2$ and scale linearly with energy, so $\sqrt{s} \sim 10^5 \text{ TeV}$ required.
- 10 TeV Pb-Pb collisions lower sphaleron energy by $\sim 0.1\%$.
- Unsuppressed sphaleron production due to magnetic fields not feasible in foreseeable future.
- Potential cosmological/astrophysical sources:
 - ▶ Superconducting cosmic strings
 - ▶ Magnetically charged black holes
 - ▶ Inflation produced large scale magnetic fields

Contribution by Kazuki Sakurai

- Theoretical prediction for cross-sections is largely unknown..

- Optical theorem**

[Khoze, Ringwald '91], ...



- Semi-Classical method**

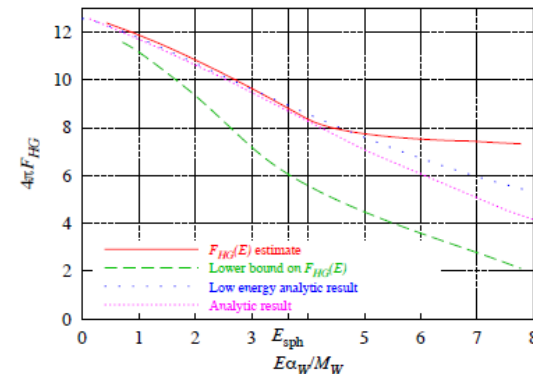
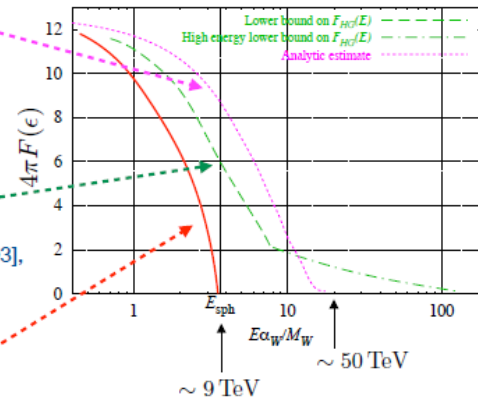
[Bezrukov, Levkov, Rebhi, Rubakov, Tinyakov '03],

[Rubakov, Tinyakov '92], ...

- Treating Ncs as a dynamical variable**

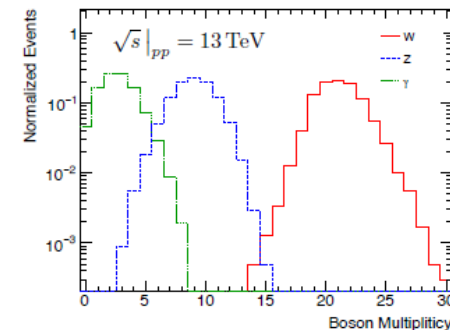
[Tye, Wong '15 '16]

[Bezrukov, Levkov, Rebhi, Rubakov, Tinyakov '03]



- Boson multiplicities in the final state?**

- LO instanton PT predicts large multiplicity of EW bosons.
- This estimate is valid only for $E \ll 10$ TeV, what do we expect for $E > 10$ TeV?
- Important to understand the experimental signatures: CMS sphaleron search assumes only fermion productions.



- Any effect from BSM physics?
- Where should be looked at? Colliders, Cosmic rays, ..
- If observed, how are we sure if it is instanton/sphaleron? Sphaleron vs BH?

- ① Production of multi particle states in 2 to n collisions is exponentially suppressed at weak coupling. Unless the state saturates entropy bounds. This happens at critical collective and 't Hooft couplings:

$$\lambda_c \equiv \alpha n = 1, \quad \lambda_t \equiv \alpha N = 1$$

at this point n- particle state (saturon) saturates unitarity.

The cross section at optimal truncation:

$$\sigma = \bullet f(\lambda_t)^{\frac{1}{\alpha}}$$

$\hookrightarrow = 1 \text{ for } \lambda_t \sim 1$



- ② Saturons behave as black holes:

$$S = ER = \frac{1}{\alpha} = (Rf)^2$$

- ③ Beyond the saturation point a renormalizable asymptotically free theory must either hit a fixed point or generate a mass gap: Either confine or enter the Higgs phase.

- ④ If theory is not asymptotically free or perturbatively hits a strong coupling, it can UV-complete by classicalization.

- ⑤ In QCD confinement is correlated with the saturation of entropy bound by instanton, and by multi- gluon states. It therefore appears to be a self-defense against violation of entropy bound and unitarity by colored states.

Further general discussion points

1. Theory uncertainty on SM xsec
 - “Holy grail” function
2. Model dependence on BSM xsec and possible final states

See, e.g. Cerdéño, Reimitz, Sakurai, Tamarit [1801.03492]

 - EFT treatment/Heavy particle (non-)decoupling
 - New chiral gauge $U(1)'$ models, e.g. baryon or lepton number
 - Also related: Possible axion effect on instanton rates (P. Schwaller)
3. Higher energy colliders or other synergistic experiments?