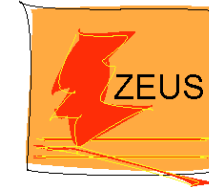




# HERAPDF Fits including Low Energy and Charm Data



Voica Radescu  
(Physikalisches Institut Heidelberg)



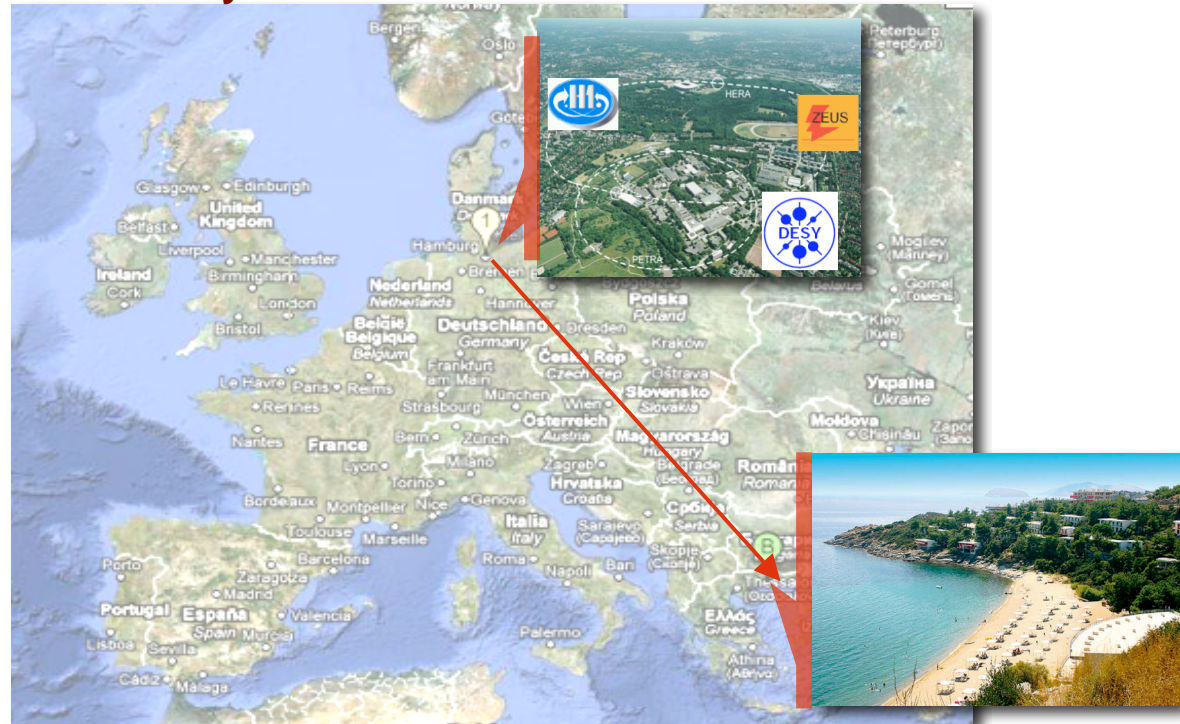
on behalf of the HI and ZEUS Collaborations

Low X 2010, Kavala

23 June 2010

## Outline:

- Introduction
- QCD fits including:
  - Low Energy Data
  - Charm Data
- Results and Comparisons
- Summary





# Extensions to HERAPDF1.0

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- New preliminary data are available and can be included in the HERA fits in addition to the data used for HERAPDF1.0:
  - HERA Combined Low Energy [H. Kowalski's presentation]
    - ▽ Accurate measurement in  $Q^2 \geq 2.5 \text{ GeV}^2$  range, sensitive to structure function  $F_L$ :
      - Study impact of those data on PDFs and investigate the low  $Q^2$  region;
      - Test sensitivity to different heavy flavour treatments;
      - Compare fit results and measured structure function  $F_L$ .
  - HERA Combined  $F_2$  Charm [V. Libov's presentation]
    - ▽ Charm data are sensitive to the charm mass and the heavy quark scheme:
      - Study impact of those data on PDFs and investigate charm mass dependence;
      - Test sensitivity to different heavy flavour treatments.
- HERA NNLO fits to HERA I data with and without Low Energy and Charm data.



# Settings

- **Data Sets:**

- HERA I combined data (same as used for HERAPDF1.0 [JHEP01 (2010) 109])
  - ▽ NC e<sup>-</sup>, CC e<sup>-</sup>, CC e<sup>+</sup> ( $Q^2 > 100 \text{ GeV}^2$ ) [J. Sztuk's presentation]
  - ▽ NC e<sup>+</sup> ( $Q^2 > 0.045 \text{ GeV}^2$ ) } 592 points
- Combined HERA Low Energy Data Set of  $E_p = 460, 575 \text{ GeV}$  with  $Q^2 > 2.5 \text{ GeV}^2$   
[H. Kowalski's presentation] → 224 points
- Combined HERA  $F_2$  Charm data with  $Q^2 > 1.5 \text{ GeV}^2$   
[V. Libov's presentation] → 41 points

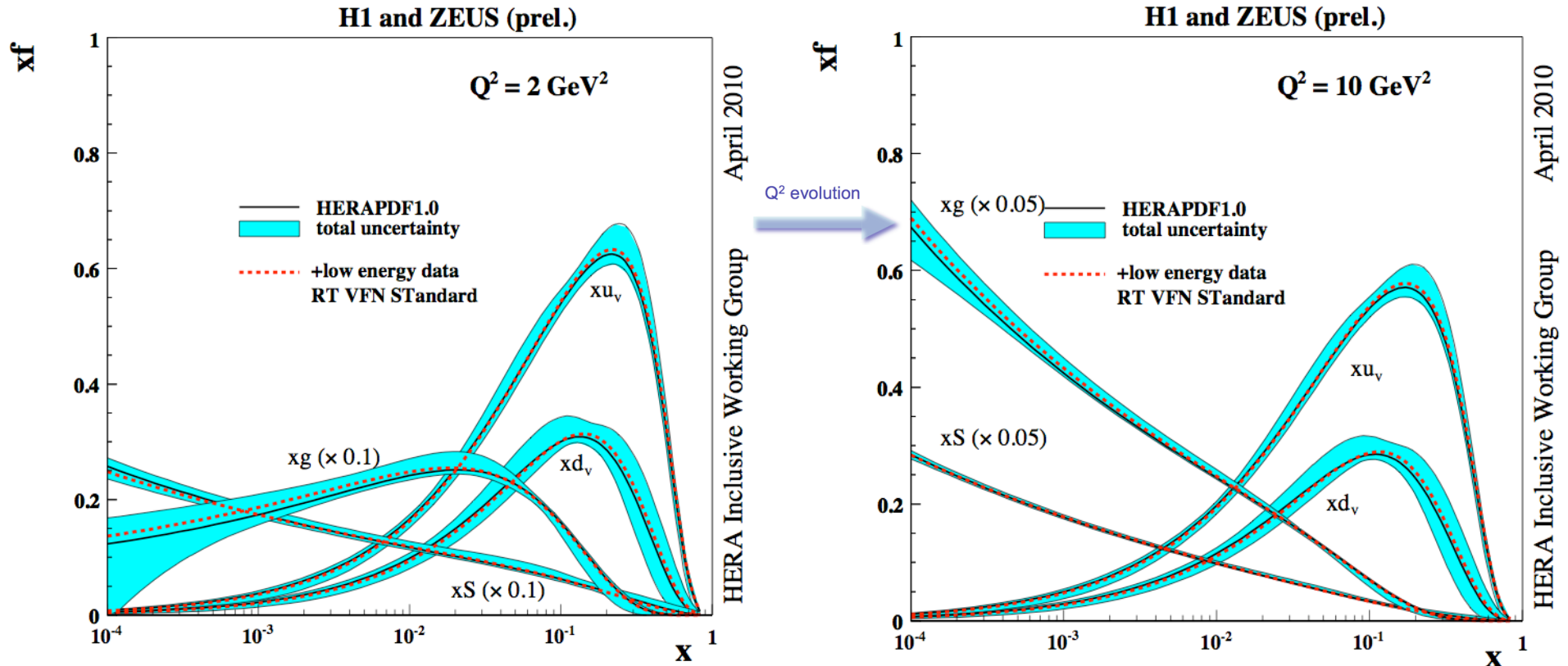
- **QCD Fit settings:** same settings as for HERAPDF1.0 [J. Sztuk's presentation]

$f_s$	0.31	
$m_c$ [GeV]	1.4	→ (1.4 - 1.65)
$m_b$ [GeV]	4.75	
$Q_{min}^2$ [GeV <sup>2</sup> ]	3.5	→ cut variation
$Q_0^2$ [GeV <sup>2</sup> ]	1.9	

- NLO (and NNLO) DGLAP evolution equations, RT-VFNS (as for MSTW08)
  - ▽ Other schemes were investigated as well: RT (optimal), ACOT (full and  $\chi$ ), FFNS



# HERAPDF including Low Energy data



- PDFs from the new fit agree very well with HERAPDF1.0
- But, inclusion of the new data gives slightly worse fit:

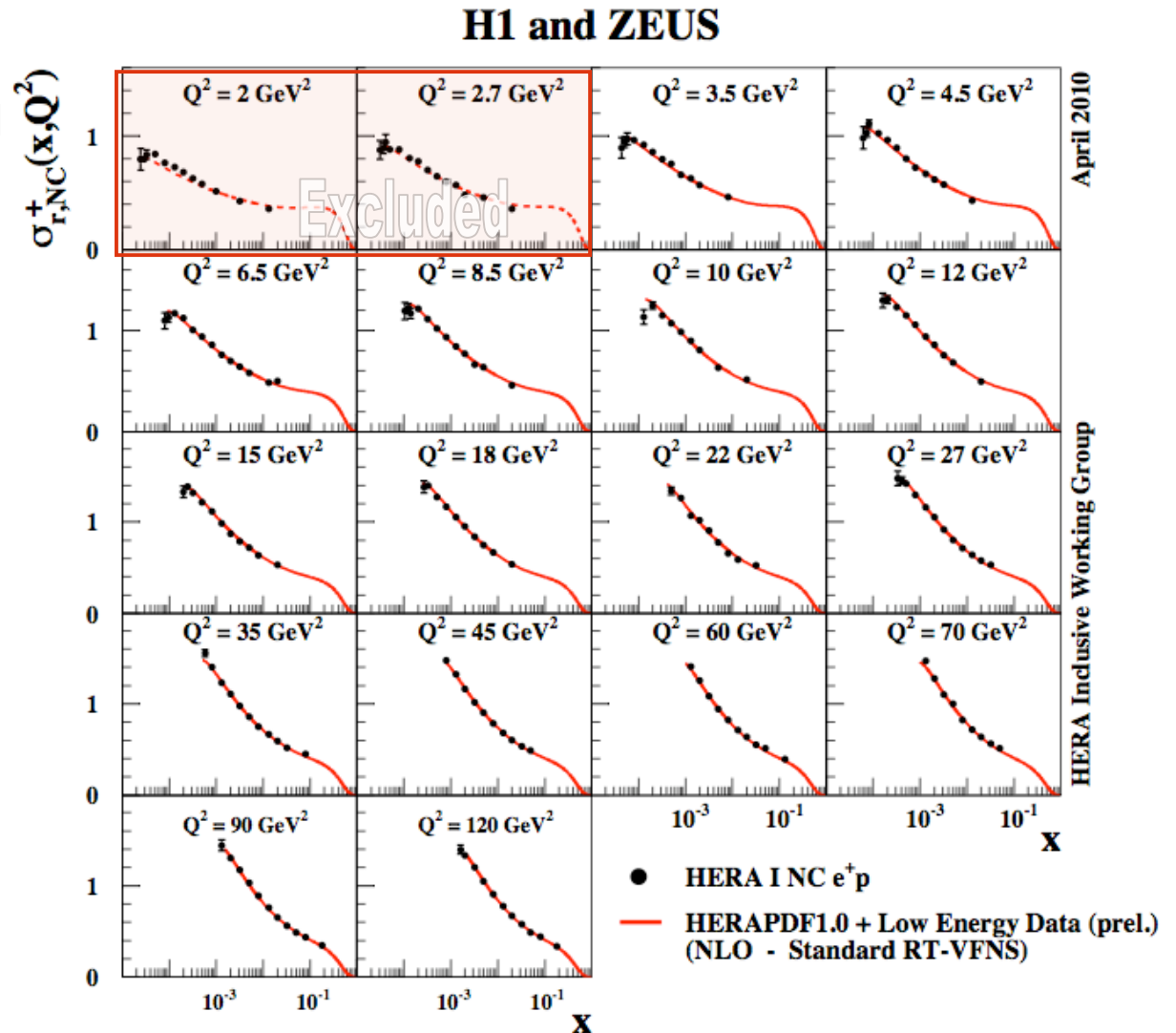
Data sets	HERAPDF1.0	+ Low Energy data
Total $\chi^2/\text{dof}$	574/582	<b>818/806</b>





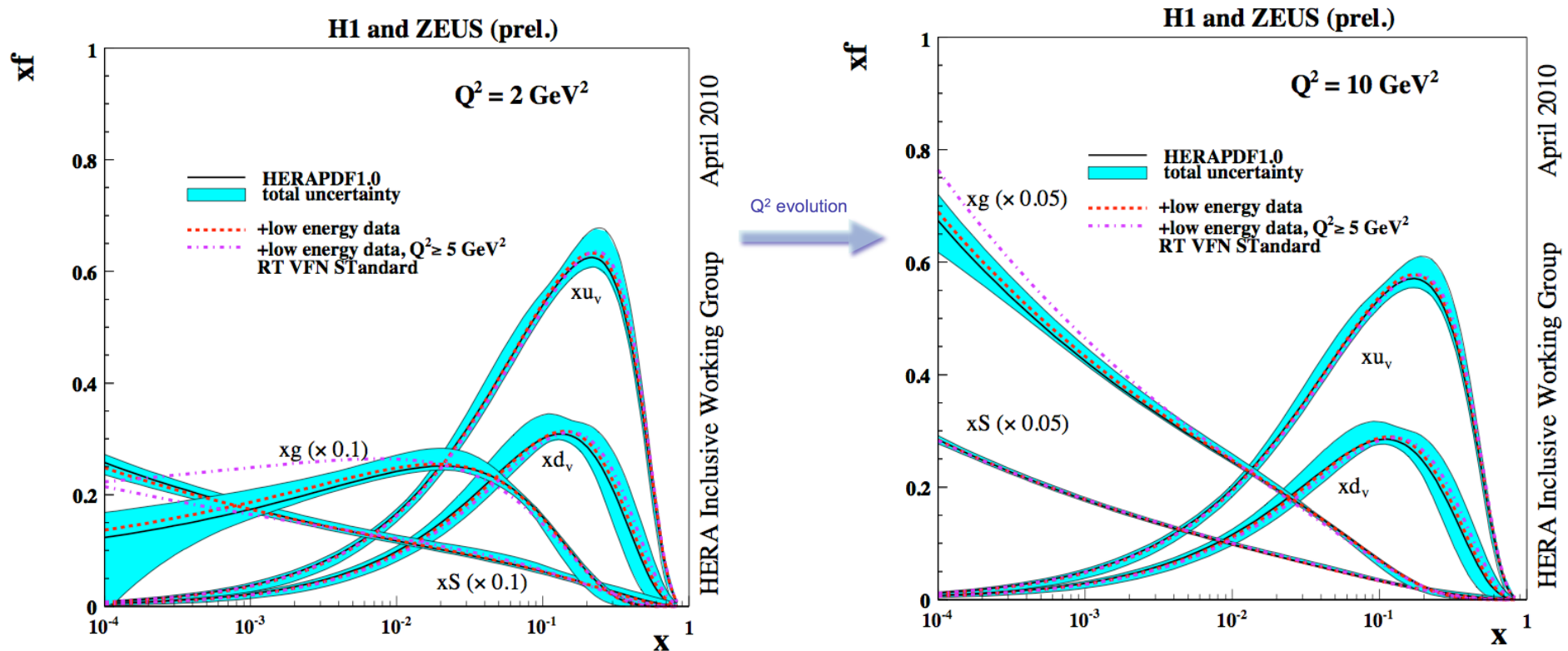
# Comparison with Data

- Line is produced fitting HERA I and Low Energy data ( $Q^2 \geq 3.5$   $\text{GeV}^2$  cut) using standard HERAPDF1.0 settings fit;
  - Turn over is observed for 920 GeV NC  $e^+p$  data at low  $x$  and  $Q^2$  (high  $y \rightarrow F_L$  sensitivity) which is not reproduced by the fit.
- Investigate the low  $x$  and  $Q^2$  region.





# Study $Q^2$ Cut Dependence

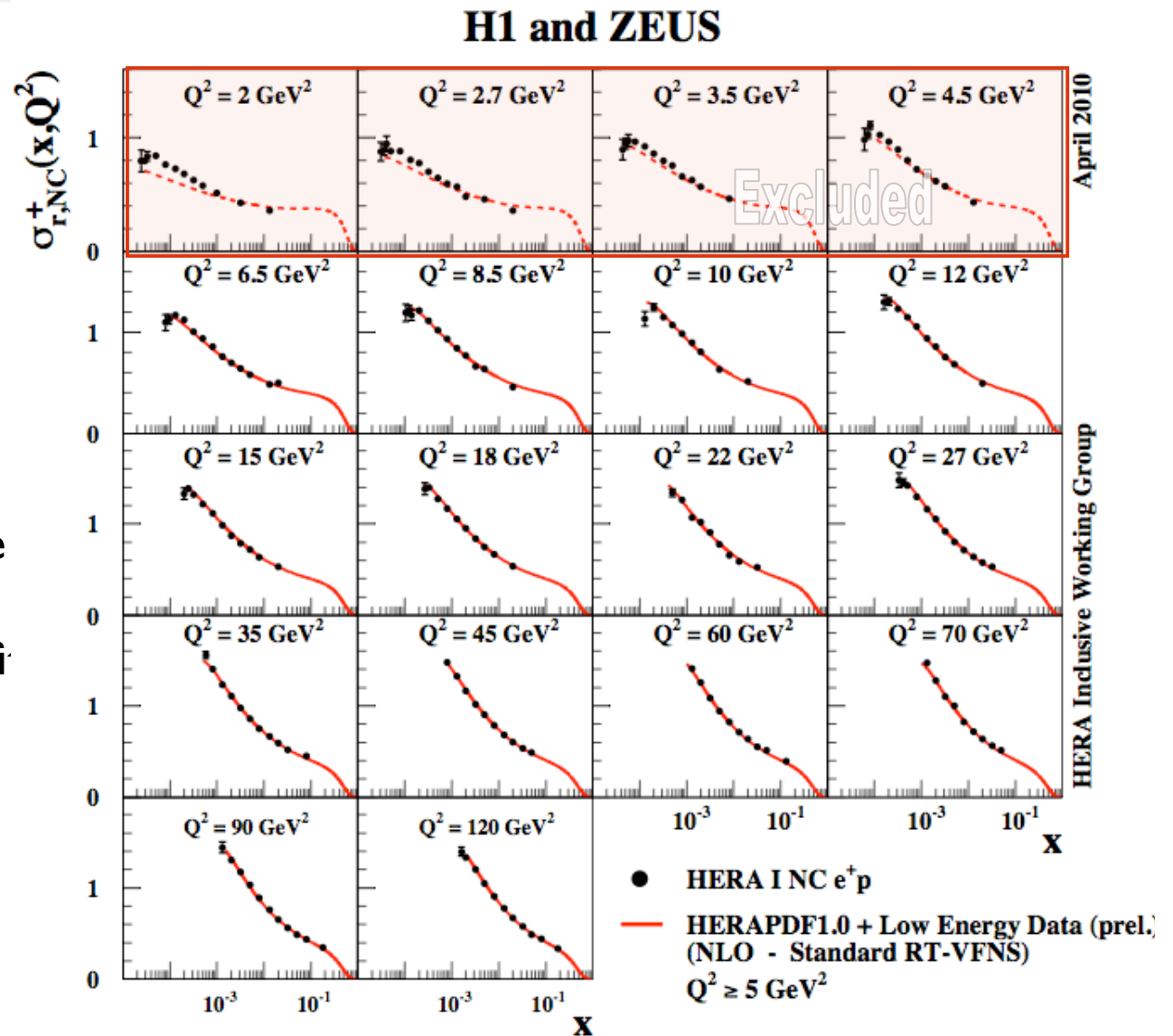


- The  $Q^2 \geq 5 \text{ GeV}^2$  cut brings large improvement in  $\chi^2$  [818/806  $\rightarrow$  698/771] and it yields different shapes for gluon and sea PDFs.
  - for the HERAPDF1.0,  $Q^2$  cut variation is included in the model uncertainty, but it had smaller effect (in the same direction).
- Compare **Red (before  $Q^2$  cut)** with **Magenta (after  $Q^2$  cut)**:
  - Gluon is visibly enhanced for  $Q^2 \geq 5 \text{ GeV}^2$  cut.



# Comparison with Data, Fit with $Q^2$ cut

- Line is produced fitting HERA I and Low Energy data (with  $Q^2 \geq 5 \text{ GeV}^2$ ) using standard HERAPDF1.0 settings
  - Bad description in the region where data do NOT enter into the fit

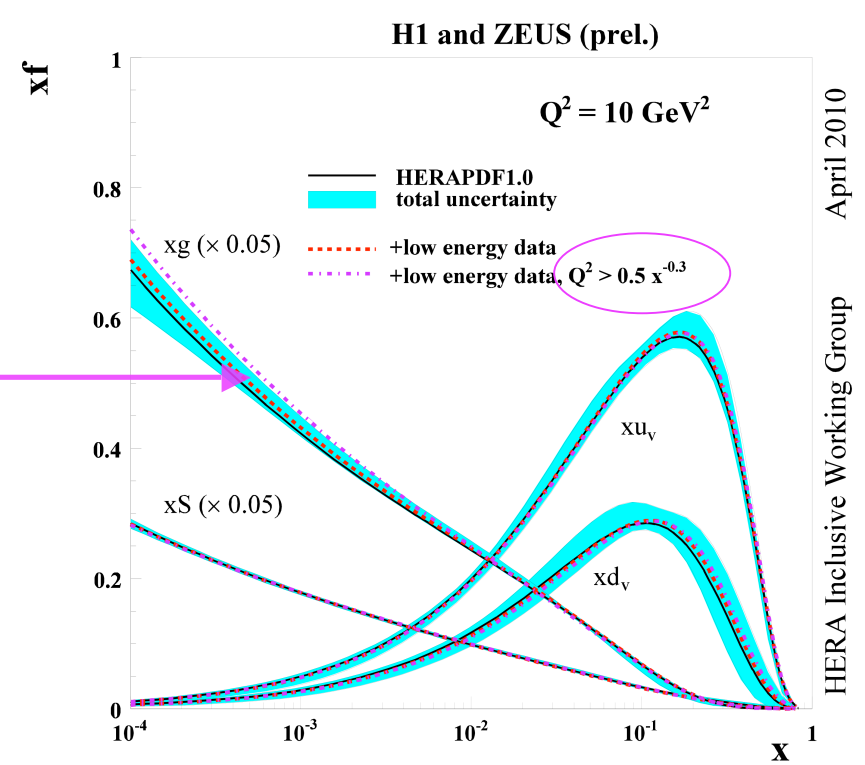
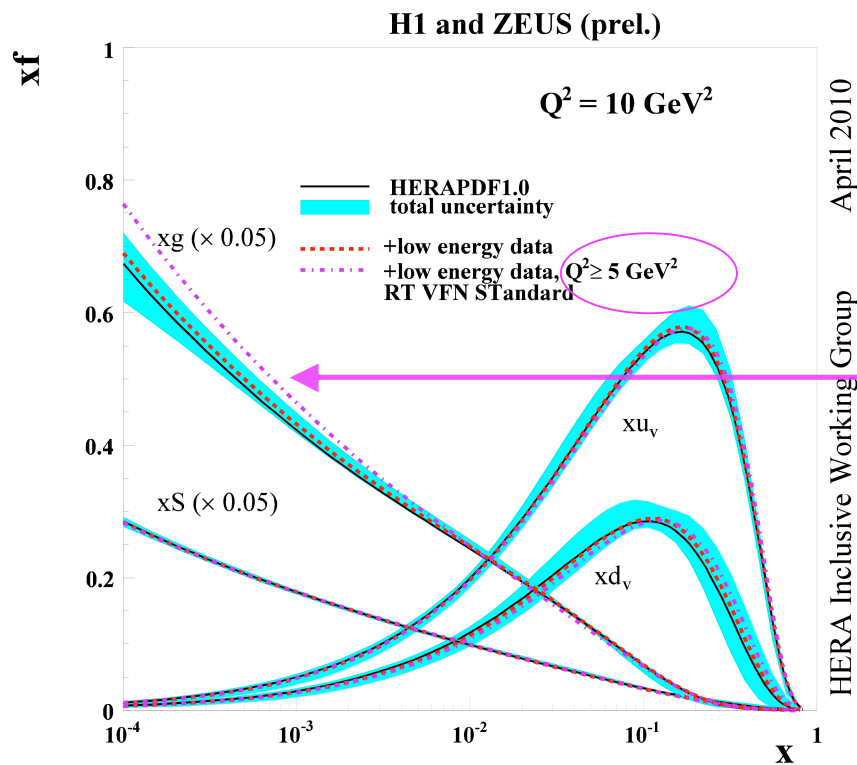




# Further Kinematic Cut Tests

- Inspired by Fabrizio Caola's presentation at DIS2010 Workshop [<http://indico.cern.ch/contributionDisplay.py?contribId=189&confId=86184>]:
  - Use a different cut criterion:  $Q^2 > Q_S(x)^2 = Ax^{-\lambda}$  with  $\lambda=0.3$  and varying A

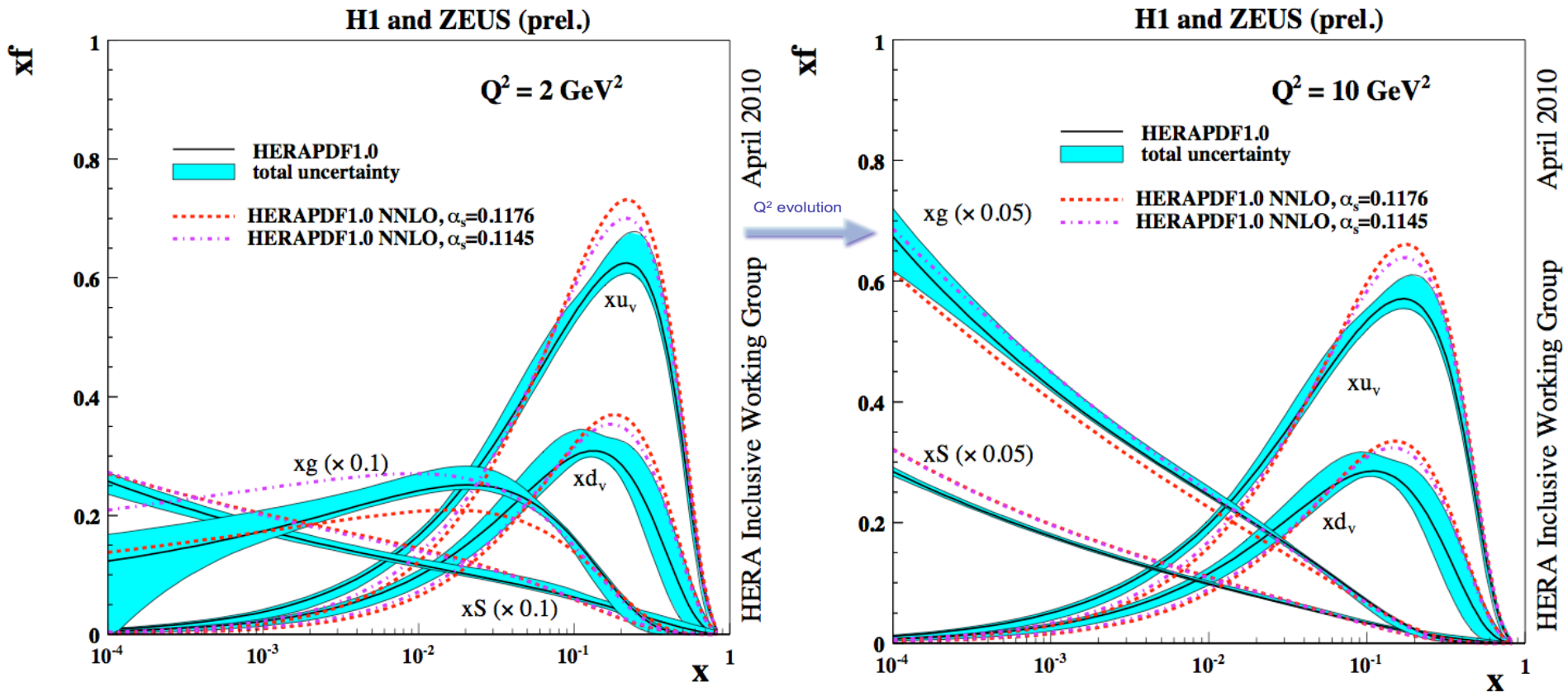
Cut	$Q^2 > 0.5x^{-0.3}$	$X > 5 \cdot 10^{-4}$	$Q^2 > 5$	No cut
All $\chi^2/\text{dof}$	683.4/760	598.2/686	698.3/771	818/806
Low Energy data $\chi^2/\text{npts}$	0.86 (199)	0.79 (161)	0.82 (215)	1.04 (224)





# HERAPDF fits at NNLO

- Fits performed to HERA I data (as used for HERAPDF1.0) at NNLO using RT-VFNS:
  - $\alpha_s(M_Z)$  at NLO = 0.1176 and  $\alpha_s(M_Z)$  at NNLO = 0.1145



- Using the same settings as for HERAPDF1.0 NNLO fit does not improve fit results.

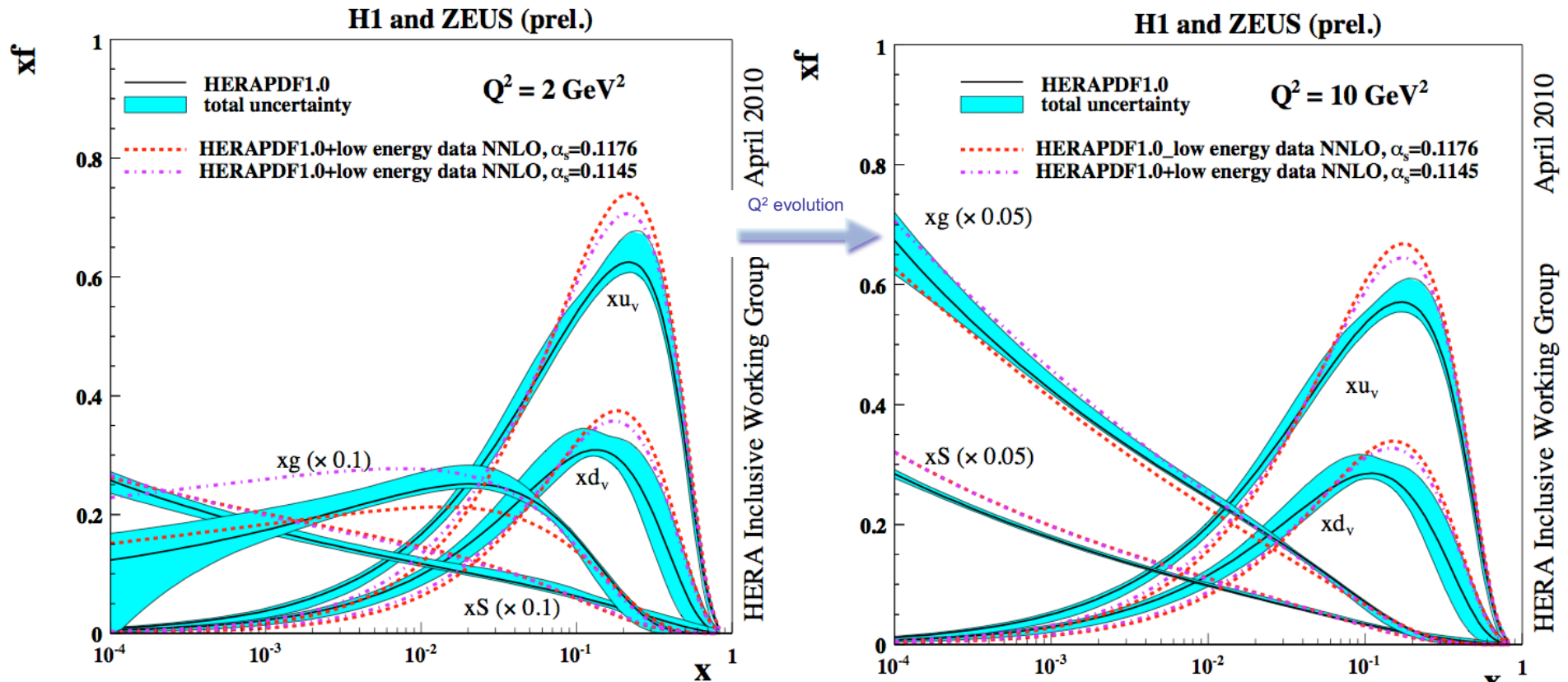
scheme	NNLO	NNLO	NLO
All $\chi^2/\text{dof}$	623.7/582	638.3/582	574.4/582





# NNLO HERAPDF fits including Low Energy Data

$\alpha_s(Mz)$  at NLO = 0.1176 and  $\alpha_s(Mz)$  at NNLO = 0.1145



- No significant change in PDFs is observed when including Low Energy Data.

scheme	NNLO	NNLO	NLO
All $\chi^2/\text{dof}$	911.5/806	893.2/806	818/806



# Various Heavy Flavour treatments at NLO

Low  $Q^2$  region is sensitive to the treatment of charm quark production.

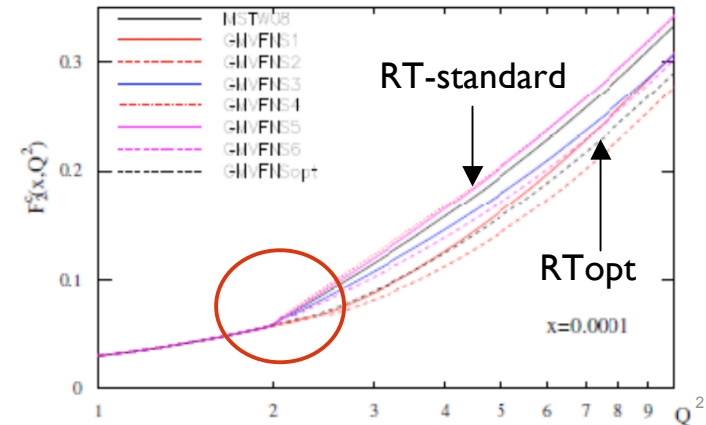
- Compare various schemes taking into account heavy quark production:
  - VFNS RT (standard [MSTW08] and optimal [R. Thorne's presentation])
  - VFNS ACOT (full [Phys.Rev.D50,1994] and  $\chi$  [Phys.Rev.D62,2000])

Schematic Summary of ACOT & TR Schemes

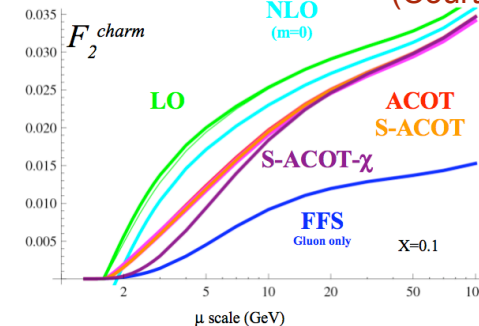
43

TR type schemes			ACOT type schemes		
$Q < m_H$	$Q > m_H$	constant term	$Q < m_H$	$Q > m_H$	constant term
LO		$Q = m_H$	LO		$+\emptyset$
NLO		$Q = m_H$	NLO		$+\emptyset$
NNLO		$Q = m_H$	NNLO		$+\emptyset$

(Courtesy of F. Olness)



(Courtesy of R. Thorne)

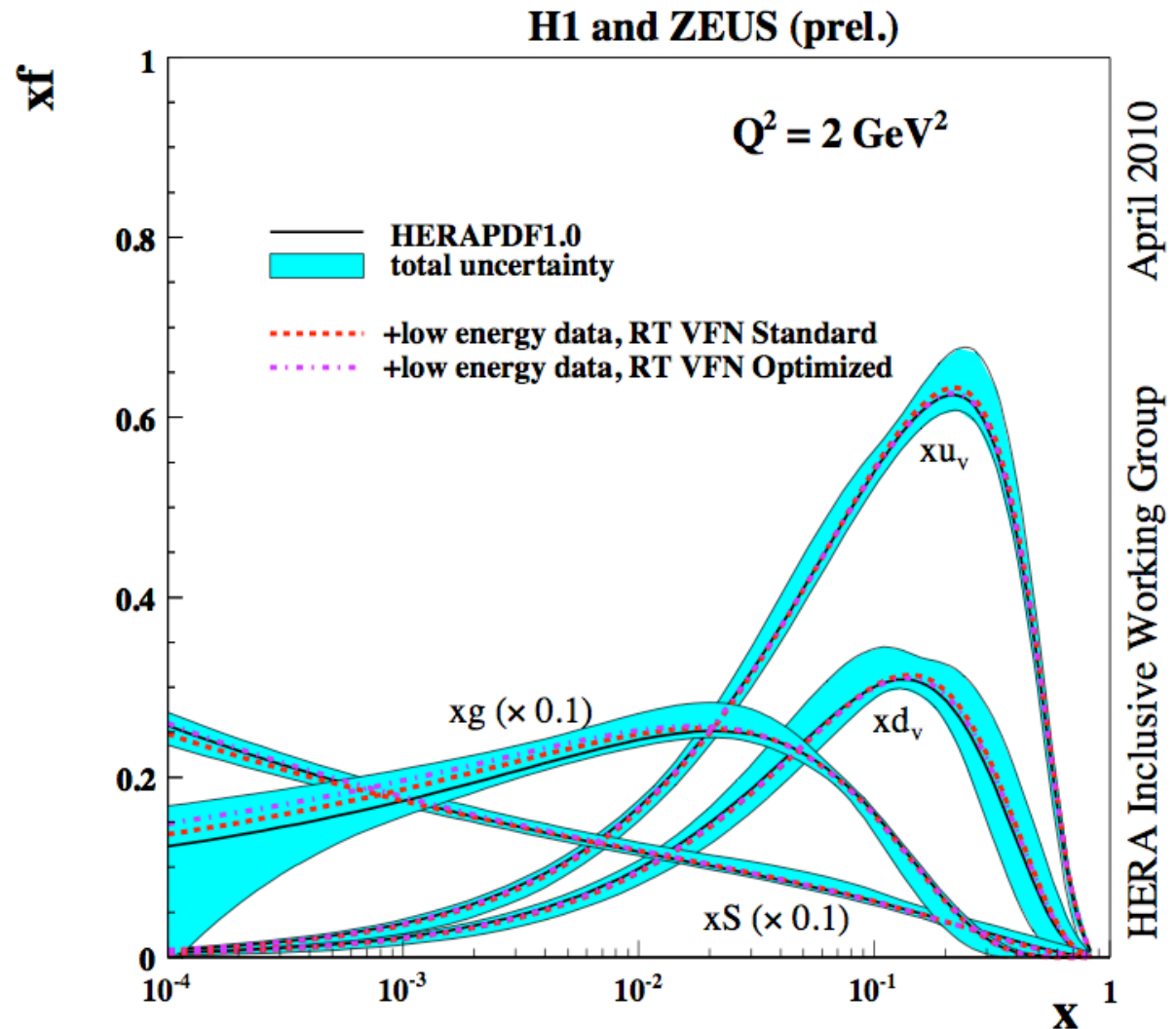


- FFNS (from QCDNUM17v06 [M. Botje])
- We observe significant differences among these schemes  $\rightarrow$  next slides.



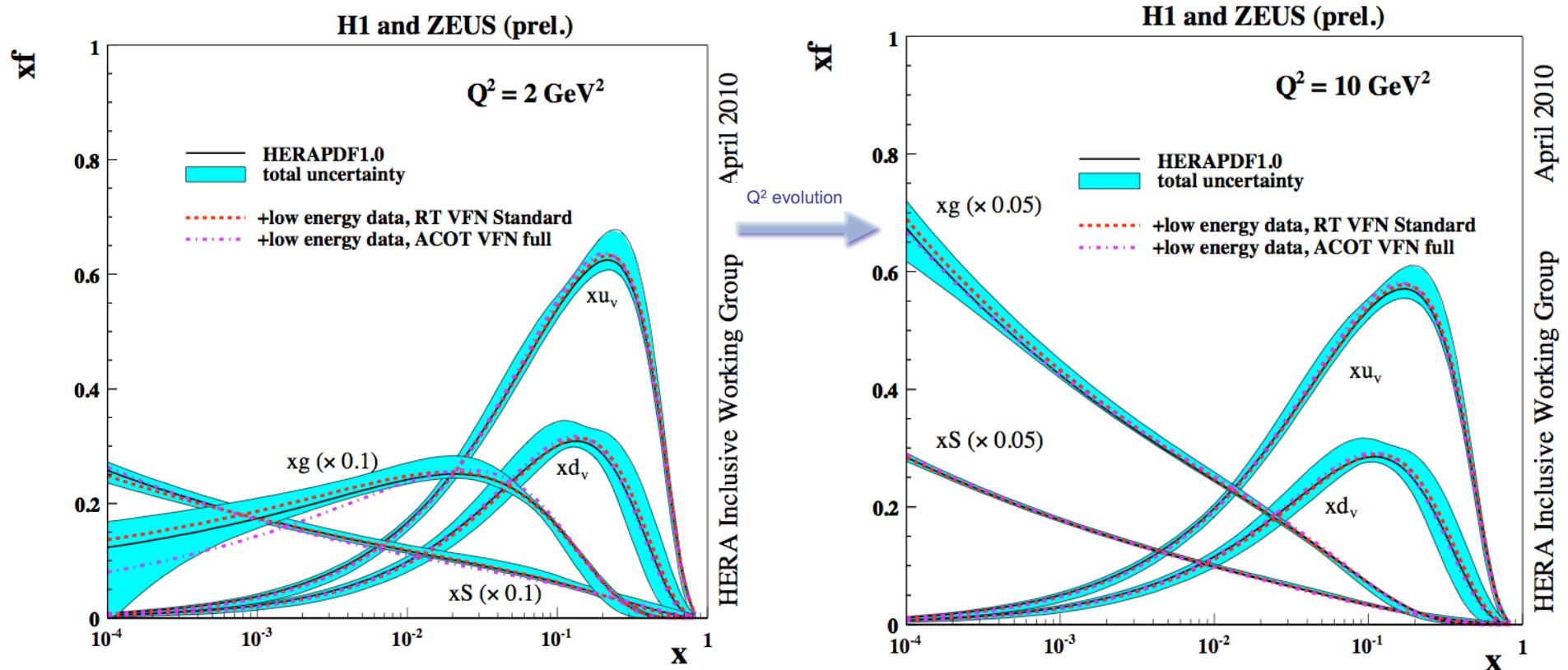
# RT schemes compared to HERAPDF1.0

- HERAPDF1.0 (blue) is compared to HERA NLO fits which include the low energy data using **Standard** and **Optimal** RT.
  - Little improvement is observed in  $\chi^2$  (7 units) and in PDF shapes from the **Standard** to **Optimal** RT VFN scheme.
  - The variations are within HERAPDF1.0 errors.





# ACOT (Full) scheme compared to HERAPDF1.0



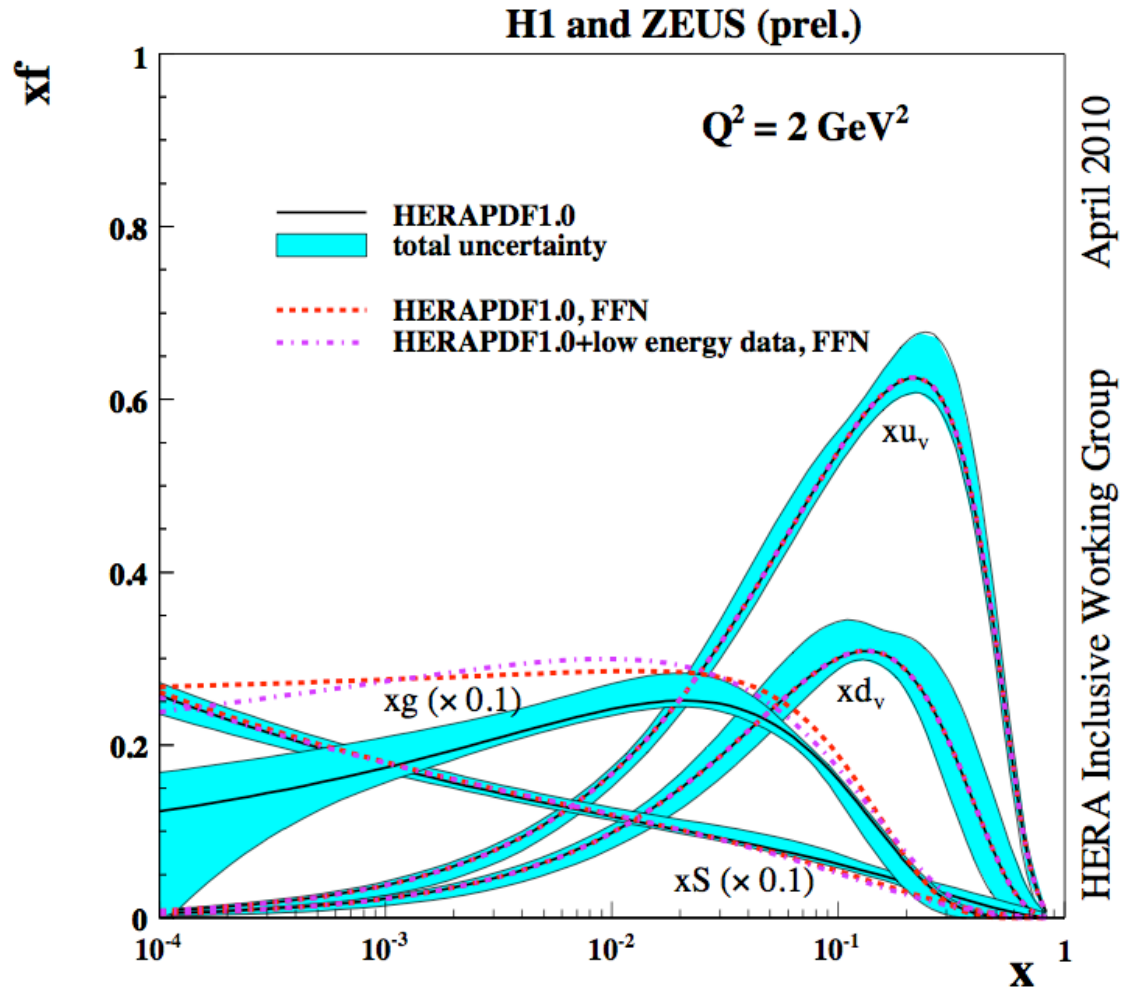
Compare fits to combined HERA I data including Low Energy Data using the **ACOT (full)** scheme to the **RT standard** scheme (VFNS):

- 30 Units improvement in  $\chi^2$  when using ACOT scheme!
- Large differences in the gluon at the starting scale, which are reduced with higher  $Q^2$



# FFNS fits including Low Energy Data

- FFNS ( $nf=3$ ) results in a similar improvement in  $\chi^2$  as observed for ACOT (VFNS) scheme in contrast to RT (VFNS).
  - $xF_3$  and CC predictions are not available within FFNS scheme, hence we freeze the valence parameters and do not fit for CC data.
- Not much difference is observed between FFNS scheme fits **with** or **without** low energy data.
- HERAPDF1.0 (VFNS) is shown as an illustration.

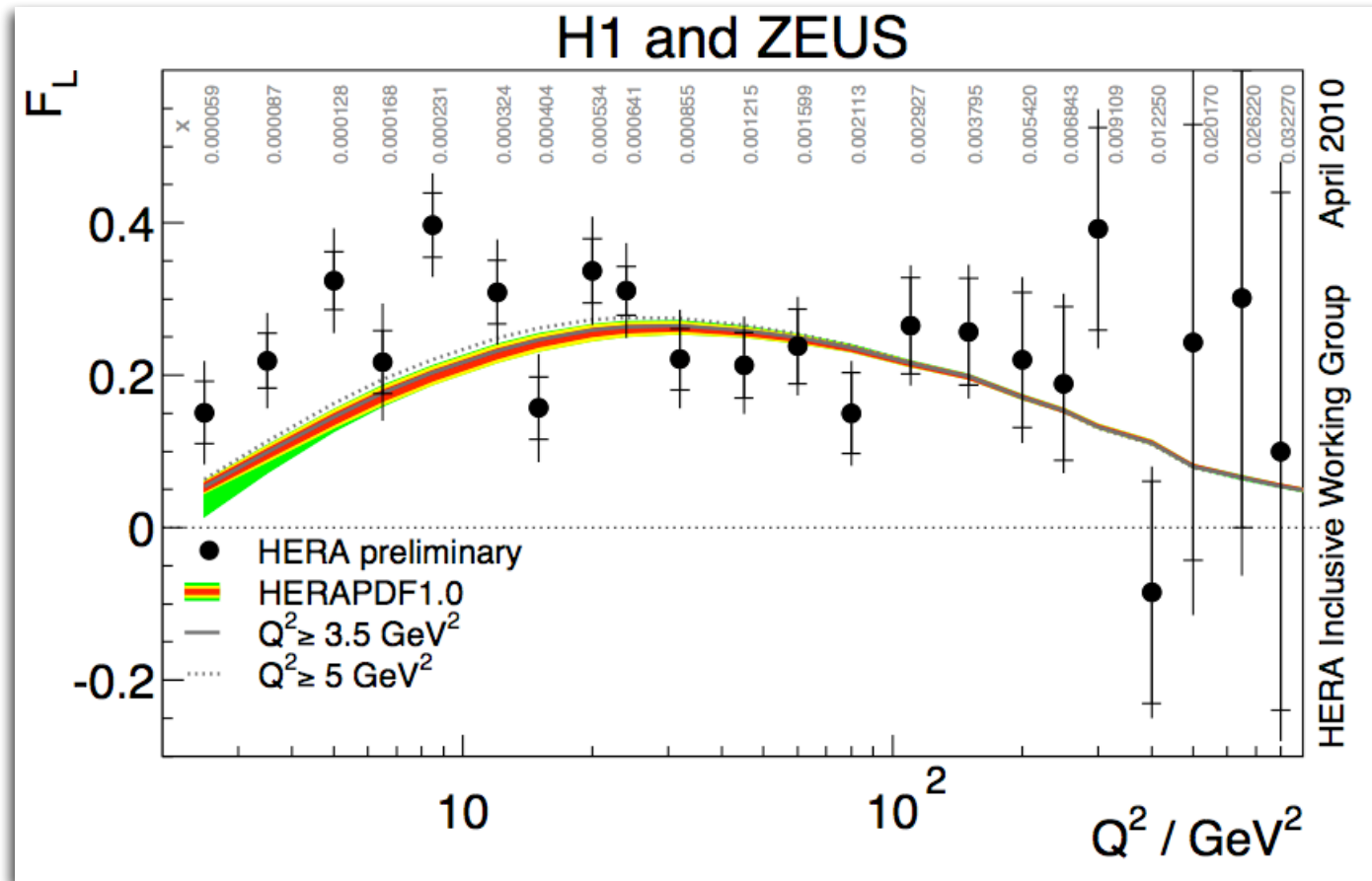






# HERA $F_L$ data vs $F_L$ predictions

The lines are  $F_L$  predictions using combined HERA I and low energy data.

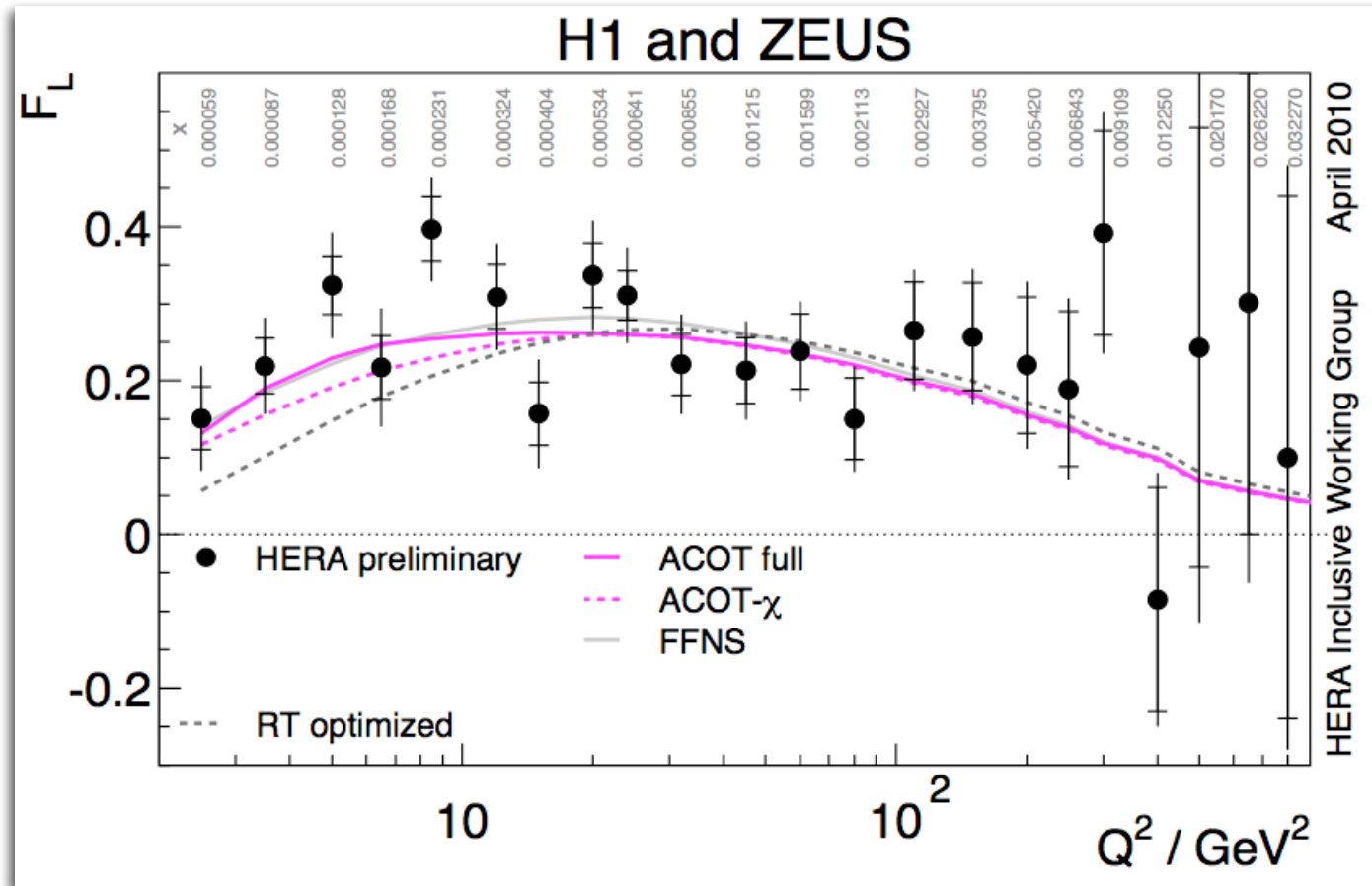


$Q^2$  cut does not bring improvement in  $F_L$  prediction.



# HERA $F_L$ data vs $F_L$ predictions

The lines are  $F_L$  predictions using combined HERA I and low energy data.

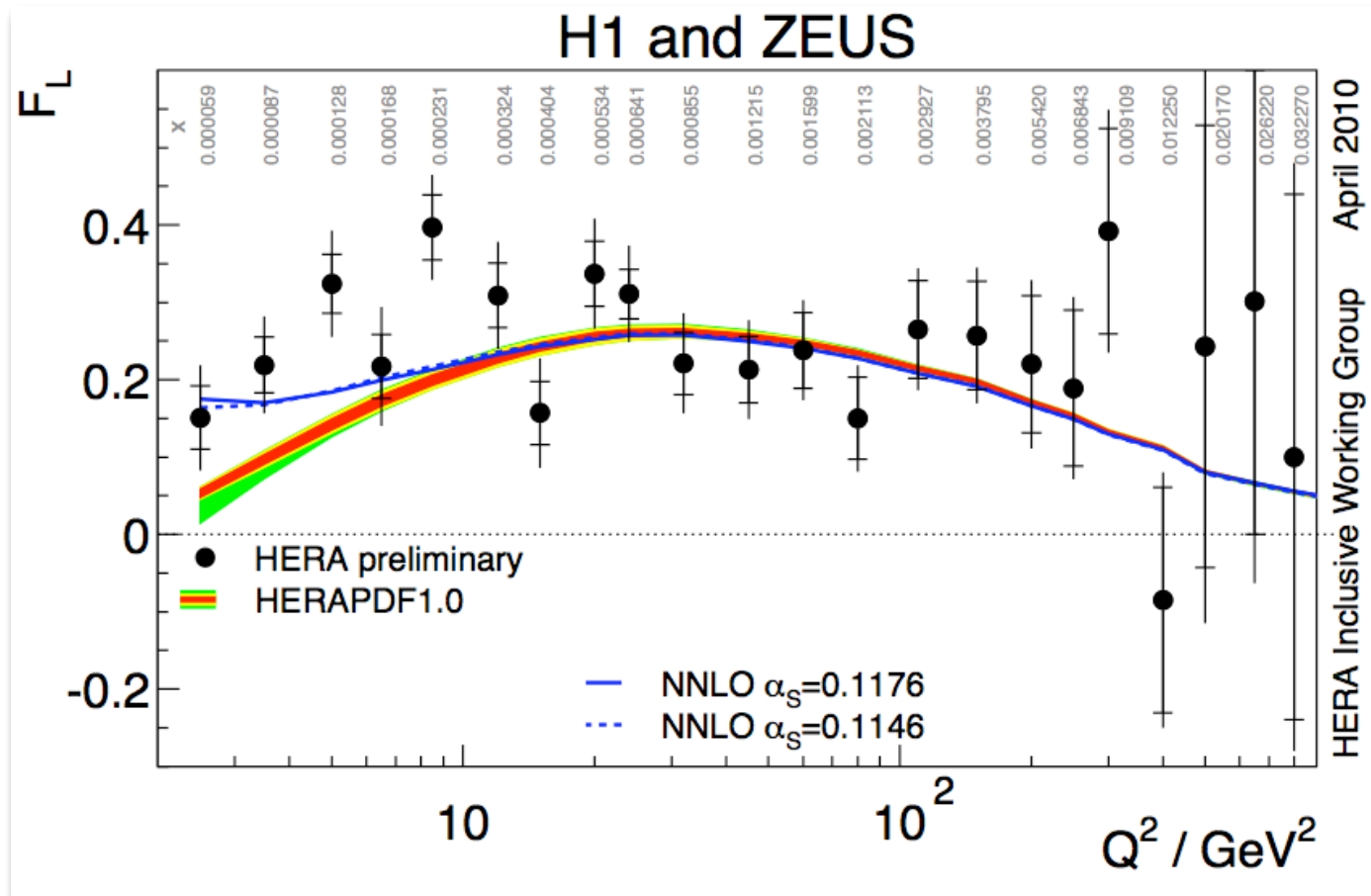


Various Heavy Flavour schemes: best ACOT(full) and FFNS



# HERA $F_L$ data vs $F_L$ predictions

The lines are  $F_L$  predictions using combined HERA I and low energy data.

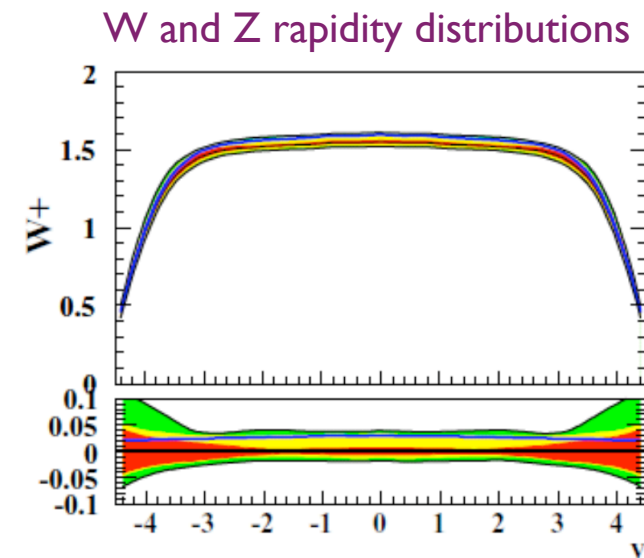
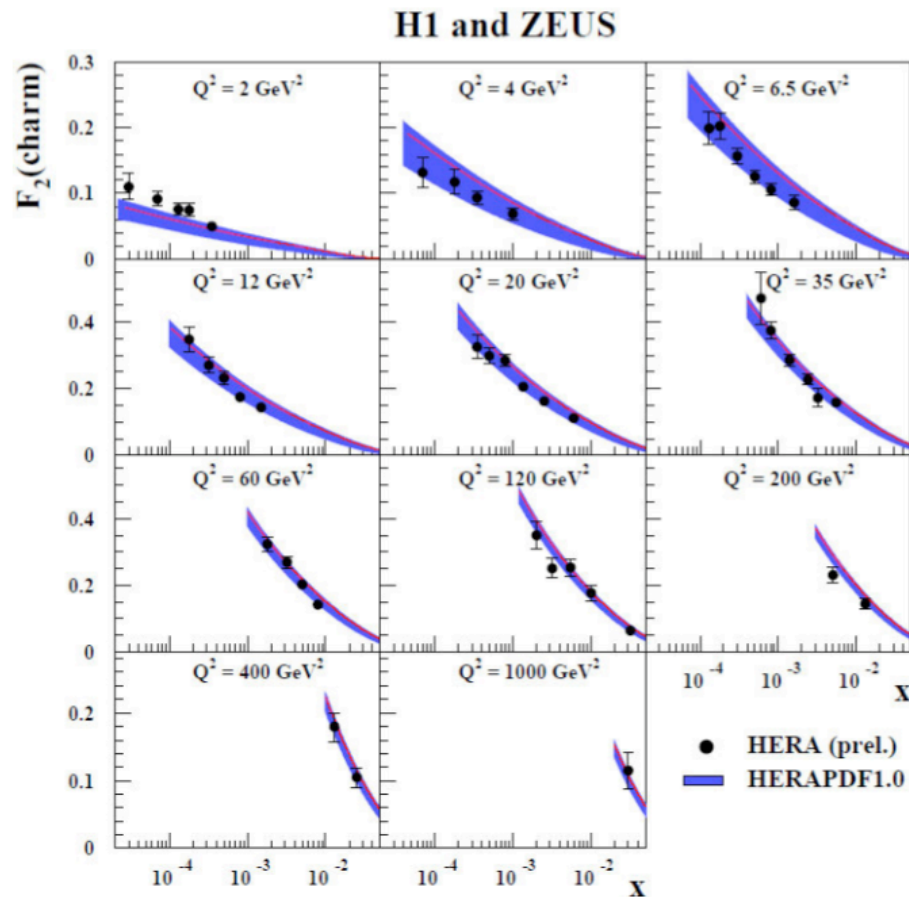


NNLO (RT) prediction yields interesting behaviour at low  $Q^2$



# PDF fit sensitivity to Charm mass

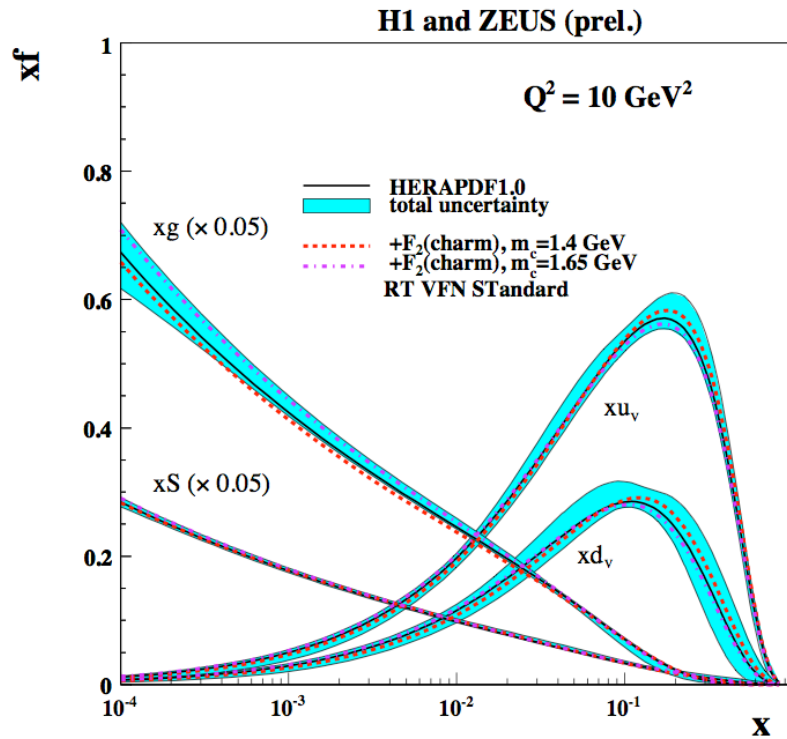
- Unlike inclusive data, fits to charm data are sensitive to the choice of the  $m_c$ :
  - PDF fits are usually done with  $m_c=1.4$  GeV, but the pole mass is  $m_c=1.65$  GeV.
    - ▽ In the published HERAPDF1.0 fit the charm mass varies between  $m_c=1.35$  GeV (top of error band) and  $m_c=1.65$  GeV (bottom of error band)



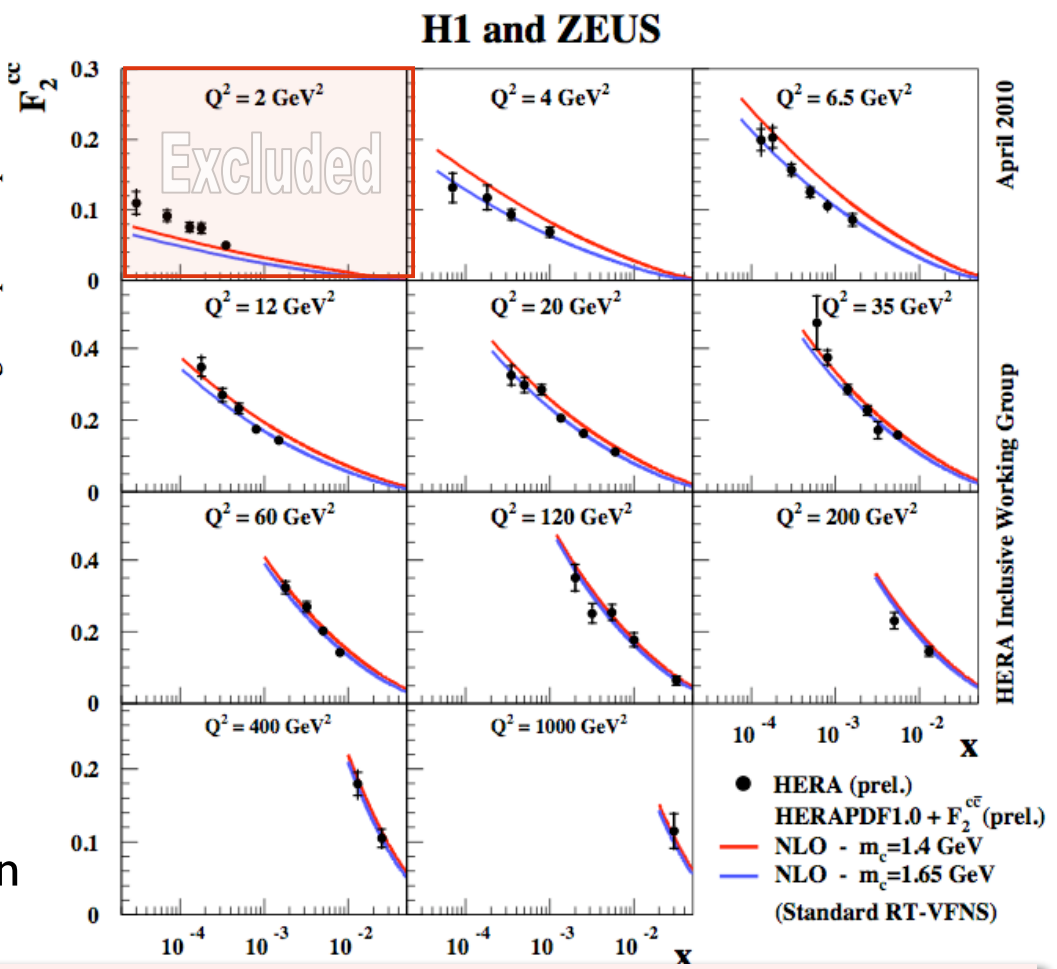
The choice of the charm mass has significant effect on the W/Z cross section predictions at the LHC, raising it by  $\sim 3\%$  (blue line)



# HERAPDF fits with Charm data: RT standard



HERA Inclusive Working Group  
April 2010



HERA Inclusive Working Group  
April 2010

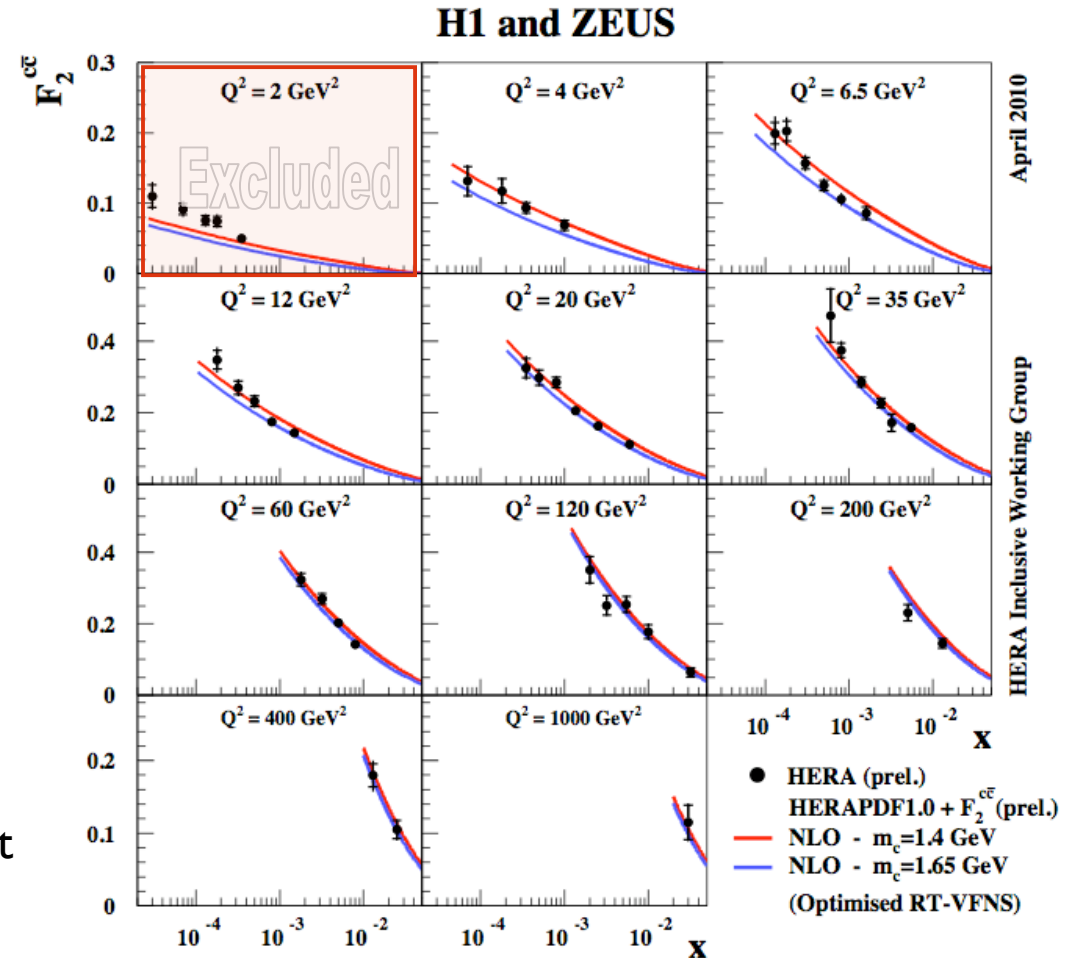
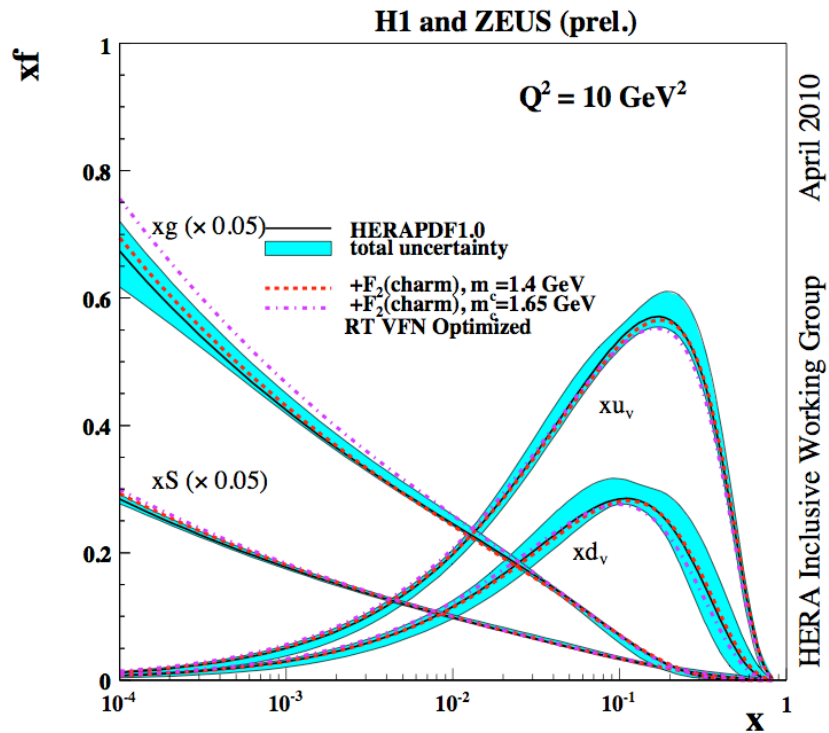
- Higher charm mass results in a suppressed  $F_2^c$ , but enhanced gluon at low- $x$

- When using RT VFN standard scheme, data prefer fit with  $m_c = 1.65 \text{ GeV}$ 
  - For  $m_c = 1.65 \text{ GeV}$ : Total:  $\chi^2/\text{ndf} = 627.5/633$
  - For  $m_c = 1.40 \text{ GeV}$ : Total:  $\chi^2/\text{ndf} = 730.7/633$





# HERAPDF fits with Charm data: RT optimised

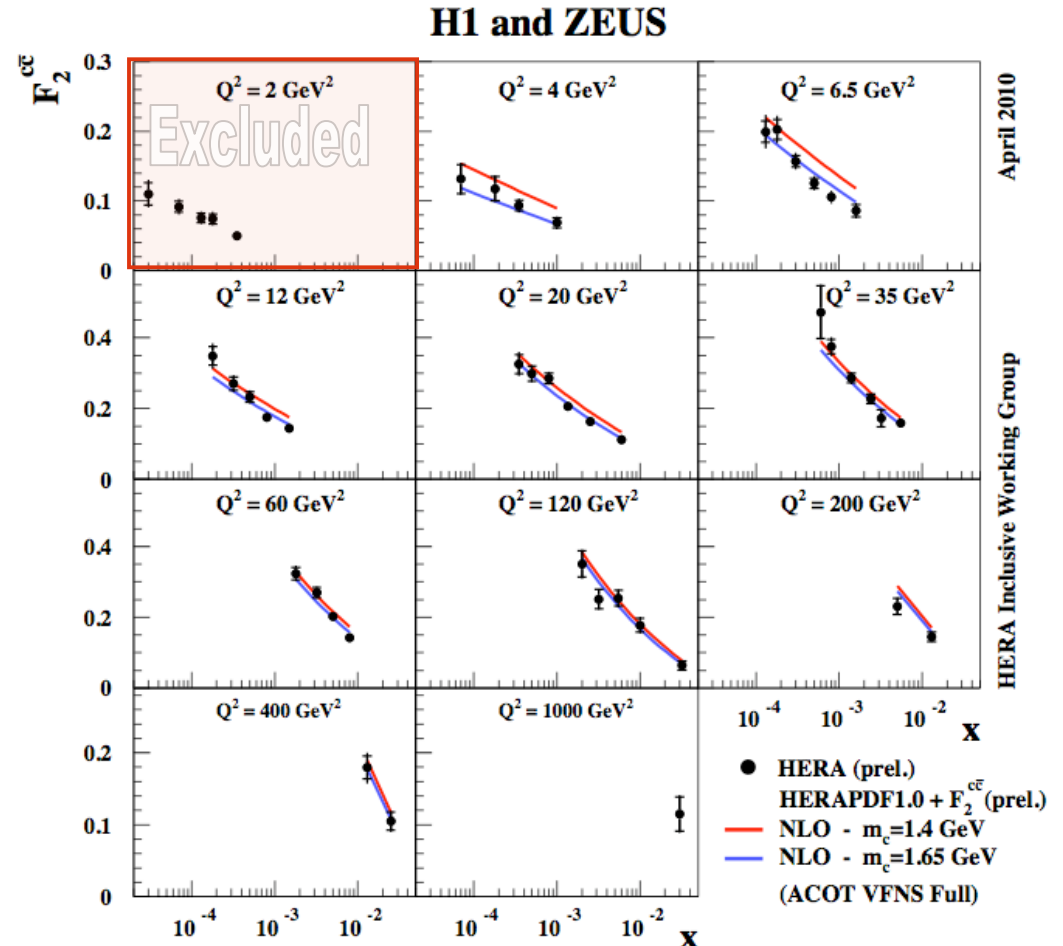
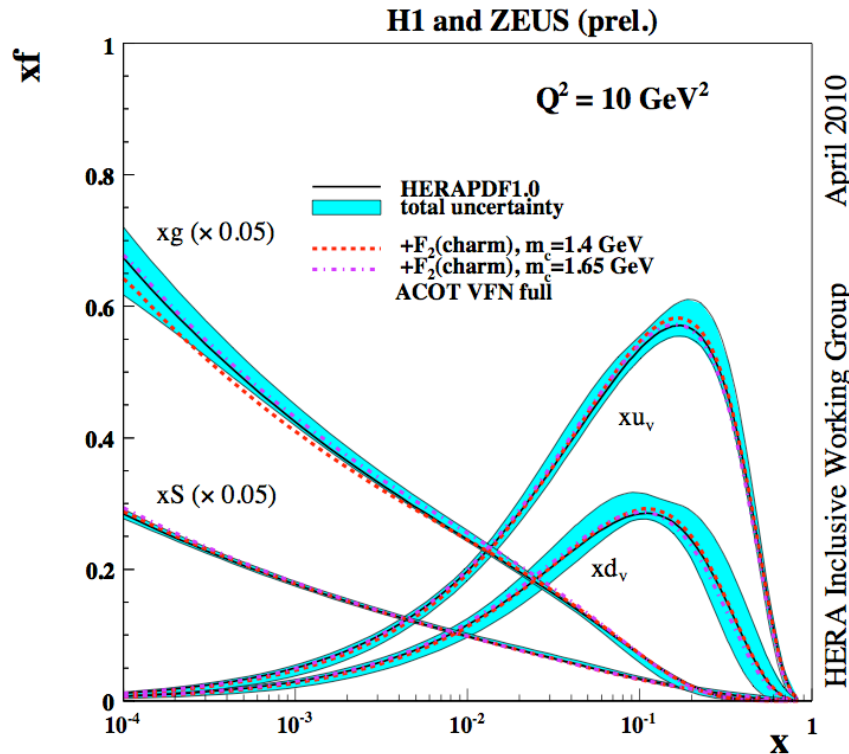


- Higher charm mass results in a suppressed  $F_2^c$ , but enhanced gluon at low- $x$

- When using RT optimal scheme, data prefer fit with  $m_c = 1.4 \text{ GeV}$ 
  - For  $m_c = 1.65 \text{ GeV}$ : Total:  $\chi^2/\text{ndf} = 695.4/633$
  - For  $m_c = 1.40 \text{ GeV}$ : Total:  $\chi^2/\text{ndf} = 644.6/633$



# HERAPDF fits with Charm data: ACOT



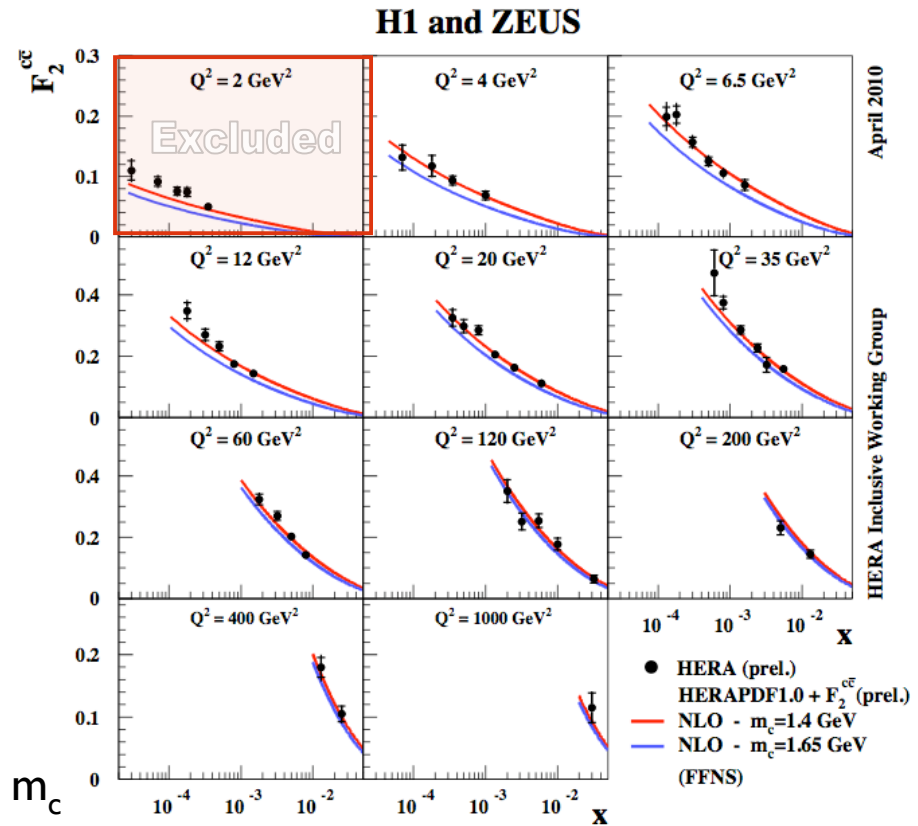
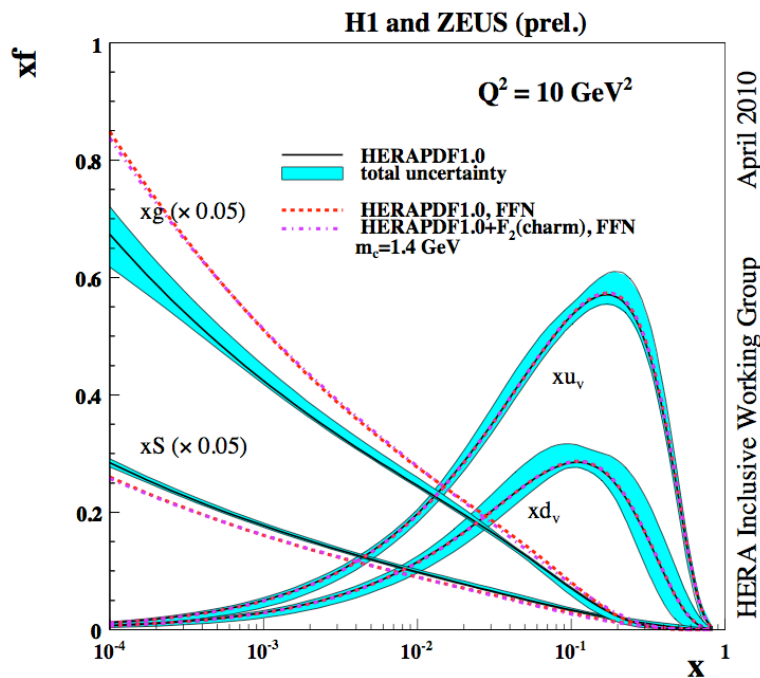
- ACOT gluon shape is suppressed compared to standard RT VFNS used for HERAPDF1.0

- When using ACOT full scheme, data prefer fit with  $m_c = 1.65 \text{ GeV}$ 
  - For  $m_c = 1.65 \text{ GeV}$ : Total:  $\chi^2/\text{ndf} = 605.7/633$
  - For  $m_c = 1.40 \text{ GeV}$ : Total:  $\chi^2/\text{ndf} = 653.9/633$



# HERAPDF fits with Charm data: FFNS

- Use heavy quark factorisation scale  $Q^2+4m_c^2$  (small difference to  $Q^2$  scale)
- FFNS for  $n_f=3$ , hence use  $\alpha_s$  for 3 flavours - with  $\alpha_s(M_Z^2) = 0.105$



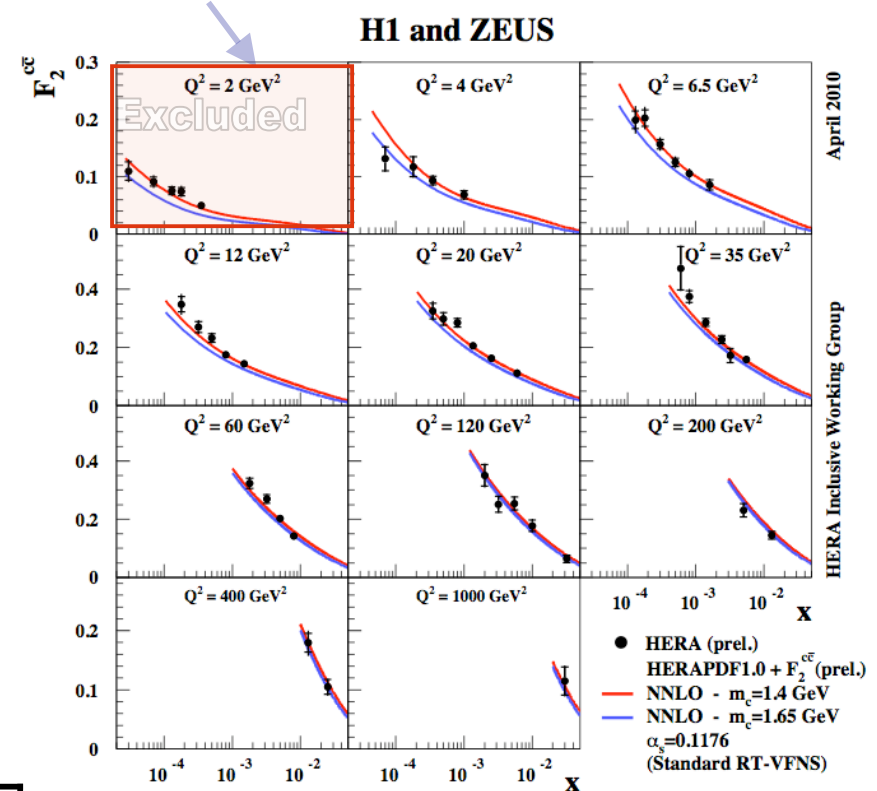
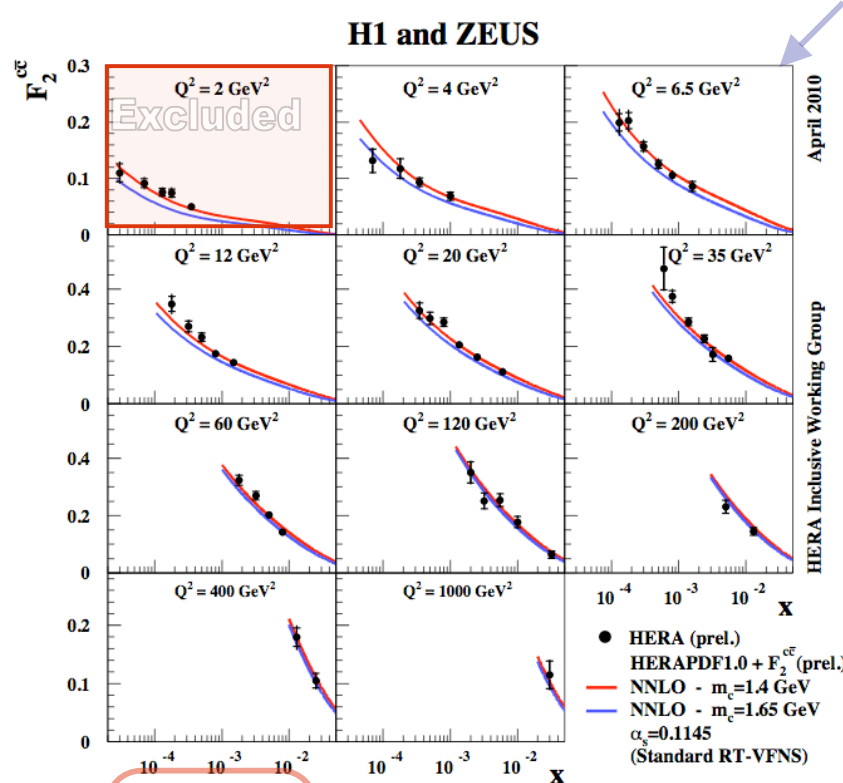
- $F_2^c$  in FFNS is relatively suppressed, hence does not need a larger value for  $m_c$  to suppress the  $F_2$  charm predictions.

- When using FFNS scheme, data prefer fit with  $m_c = 1.4 \text{ GeV}$ 
  - For  $m_c = 1.65 \text{ GeV}$ : Total:  $\chi^2/npts = 852.0/565$
  - For  $m_c = 1.40 \text{ GeV}$ : Total:  $\chi^2/npts = 567.0/565$



# HERAPDF fits with Charm data: NNLO fits

- NNLO fits to charm data are performed using the Standard RT VFNS
- Variations of schemes are considerably reduced at NNLO
  - Performed NNLO fits for  $\alpha_s(M_Z)=0.1145$  and  $0.1176$  and  $m_c=1.4$  and  $1.65$  GeV



NNLO	$\alpha_s=0.1145,$ $m_c=1.4$	$\alpha_s=0.1145,$ $m_c=1.65$	$\alpha_s=0.1176,$ $m_c=1.4$	$\alpha_s=0.1176,$ $m_c=1.65$
$\chi^2/\text{ndf}$	681/633	832/633	703/633	862/633

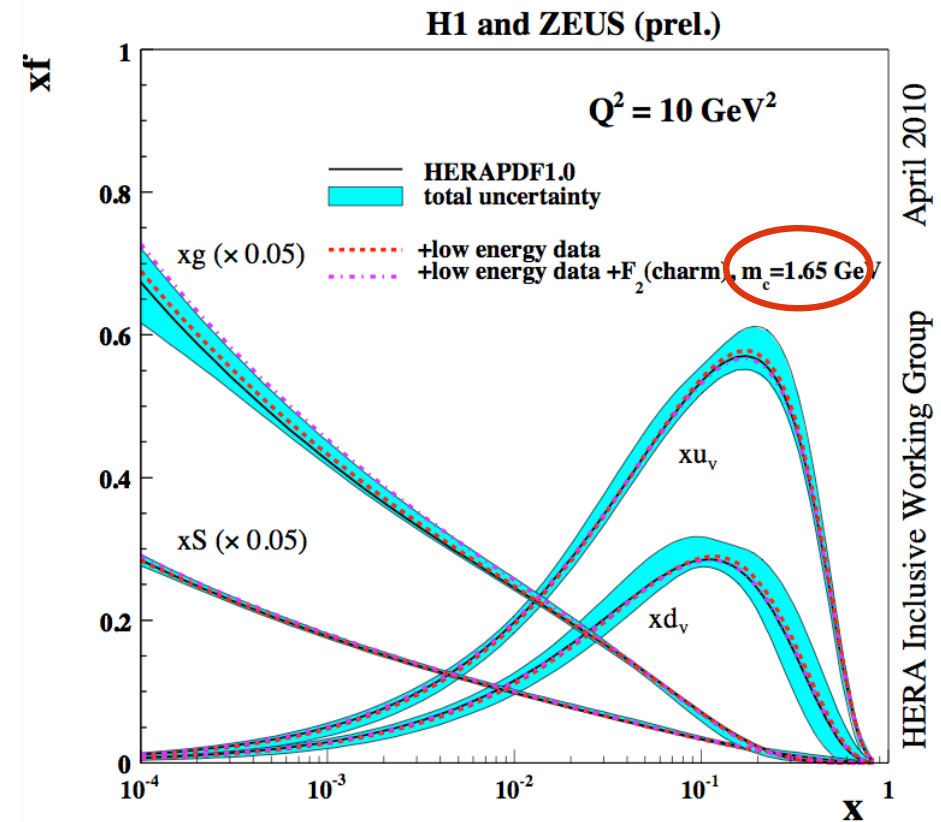
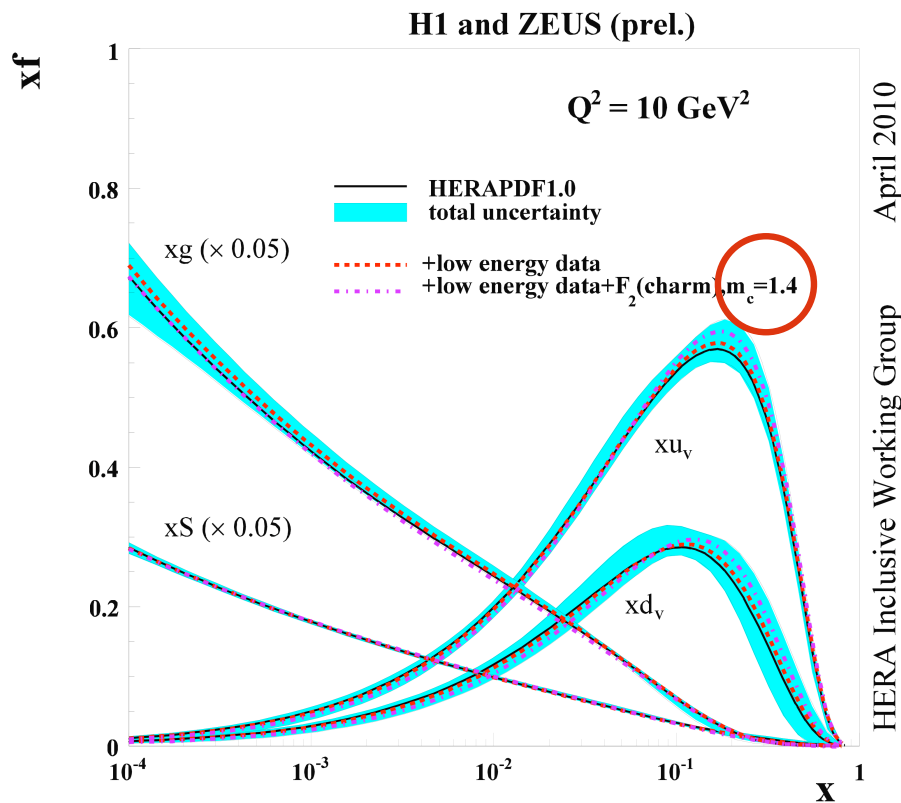


NNLO fit with  $\alpha_s(M_Z)=0.1145$   
And  $m_c=1.4$  is preferred.



# Fits including Low Energy and Charm data

- When including both Low Energy and Charm data in the HERA fits, conclusions about sensitivity to heavy quark schemes and charm mass are not altered.
- Conclusions about sensitivity to the kinematic cut dependence are not altered when including both data in the fit as long as the optimal choice for  $m_c$  is made.





# Summary

---

- New preliminary low energy data have been included in the HERAPDF QCD fits
- New fits are in general in agreement with HERAPDF1.0 fits, but do not provide a good fit of the low  $Q^2$  region:
  - Observe large sensitivity to kinematic cut at low  $Q^2$  and low  $x$
  - Inclusion of the new data brings sensitivity to Heavy Flavour model treatments:
    - ACOT (VFNS) and FFNS: decrease  $\chi^2$  considerably (compared to standard RT)
    - Different Heavy Flavour treatment in the fit yield interestingly different  $F_L$  prediction!
- With HERAPDF1.0 settings HERAPDF fits at NNLO (RT-VFNS) were presented:
  - NNLO fit does not improve when using HERAPDF1.0 settings
  - NNLO fits including the low energy data also don't bring improvement w/rt NLO
- New preliminary charm data have been included in the HERAPDF fits:
  - Fits of charm data are sensitive to the charm mass and the heavy quark scheme
- Simultaneous fits including low energy and charm data do not alter the conclusions from above.
- Low  $Q^2$  region remains very interesting for further QCD tests!





# HI-ZEUS combined results

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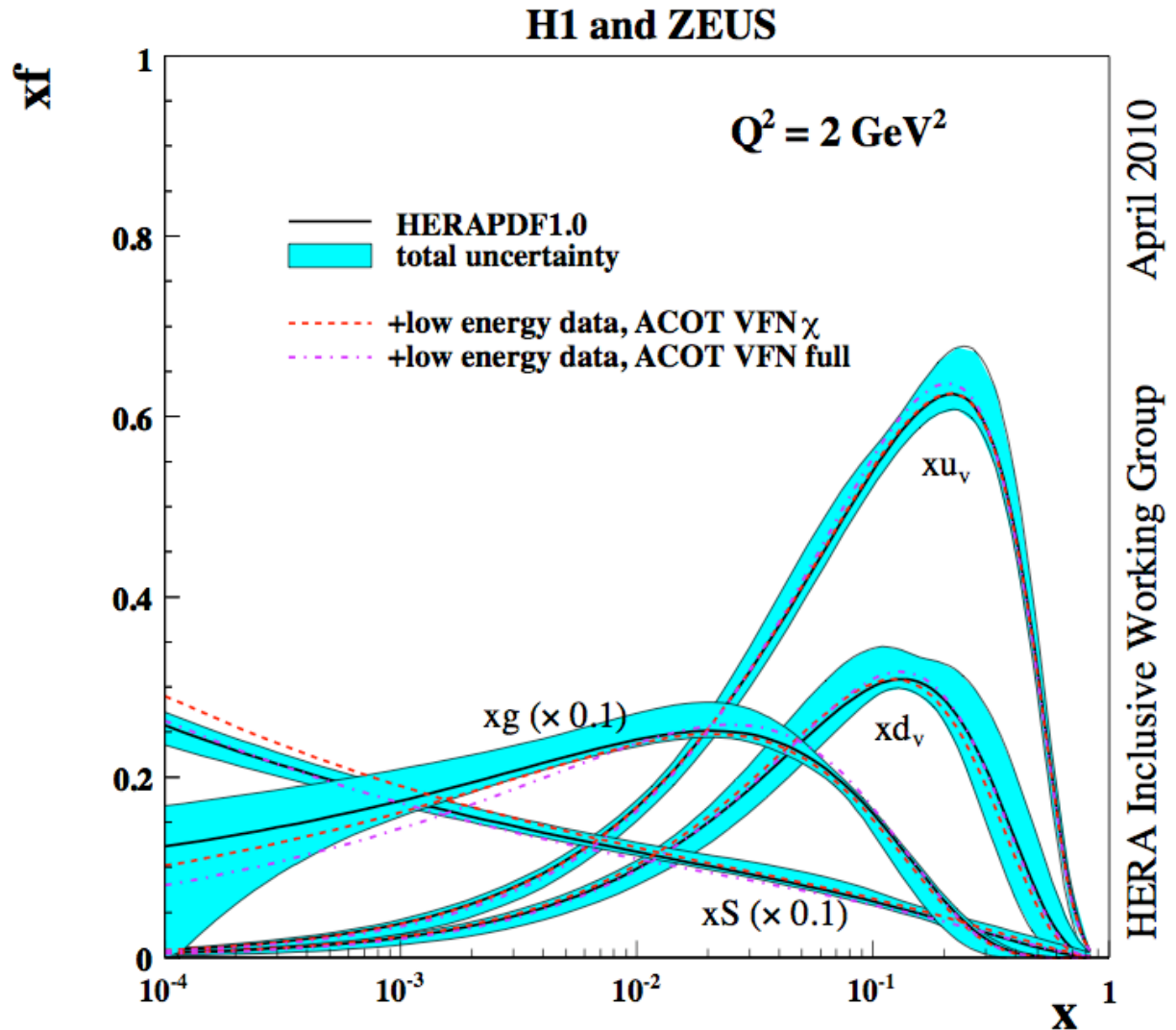
[https://www.desy.de/hlzeus/combined\\_results/index.php](https://www.desy.de/hlzeus/combined_results/index.php)



# Compare ACOT schemes to HERAPDF1.0

ACOT full fit results in a 5 units improvement in  $\chi^2$  compared to ACOT $\chi$

- **ACOT full:**
  - Slightly less steeper gluon and sea is not changed much
  - Better fit of the high energy data
- **ACOT $\chi$ :**
  - A steeper gluon and sea
  - Better fit of the low energy data





# Parametrisation and Model checks

---

Parameterisation variations and model assumptions were performed similarly to HERAPDF1.0 [J. Sztuk's presentation]

- **Parametrisation variations:**

- ▽ The 10 parameter fit for HERA-I fit still produces the best central fit parametrisation, other variations, including negative gluon terms bring no significant changes in  $\chi^2$ .

- **Model checks:**

- ▽ Variation of  $m_c$ ,  $m_b$  bring little change in  $\chi^2$  or parameters.
- ▽ Raising  $Q^2$  cut has a significant change on  $\chi^2$  and PDF parameters.

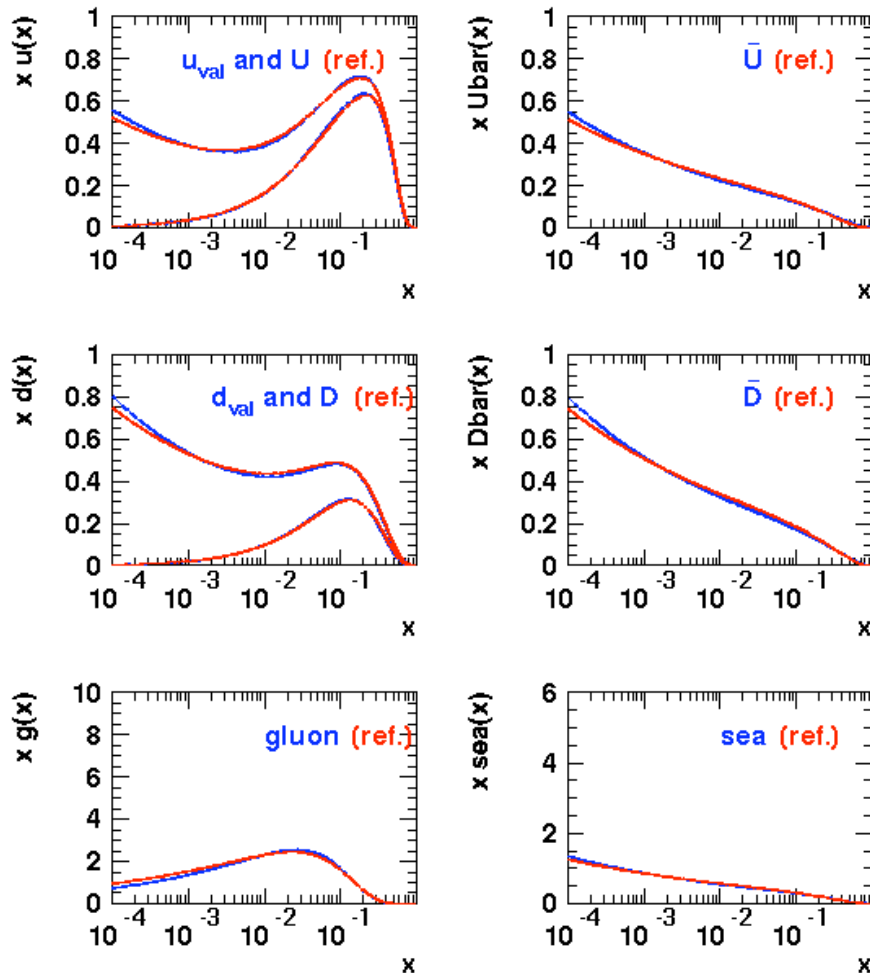


# Reminder on HF checks on HERA data alone

• RT:  $\chi^2/\text{dof} = 574/582$

ACOT:  $\chi^2/\text{dof}=562/582$

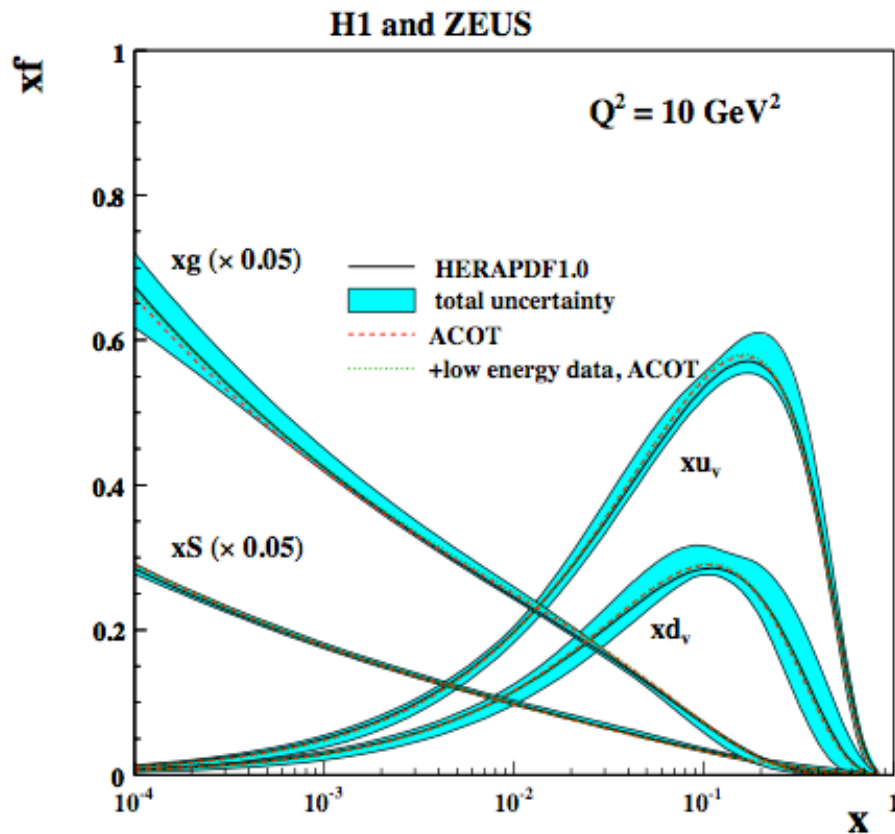
Fit vs HERAPDF1.0,  $Q^2 = 1.9. \text{ GeV}^2$



- RT heavy flavour scheme was cross checked against ACOT scheme for HERAPDF1.0
  - We did not observe much difference in the PDF distributions
  - ACOT line is shown in the HERAPDF1.0 paper



# Reminder on HF checks on HERA data alone

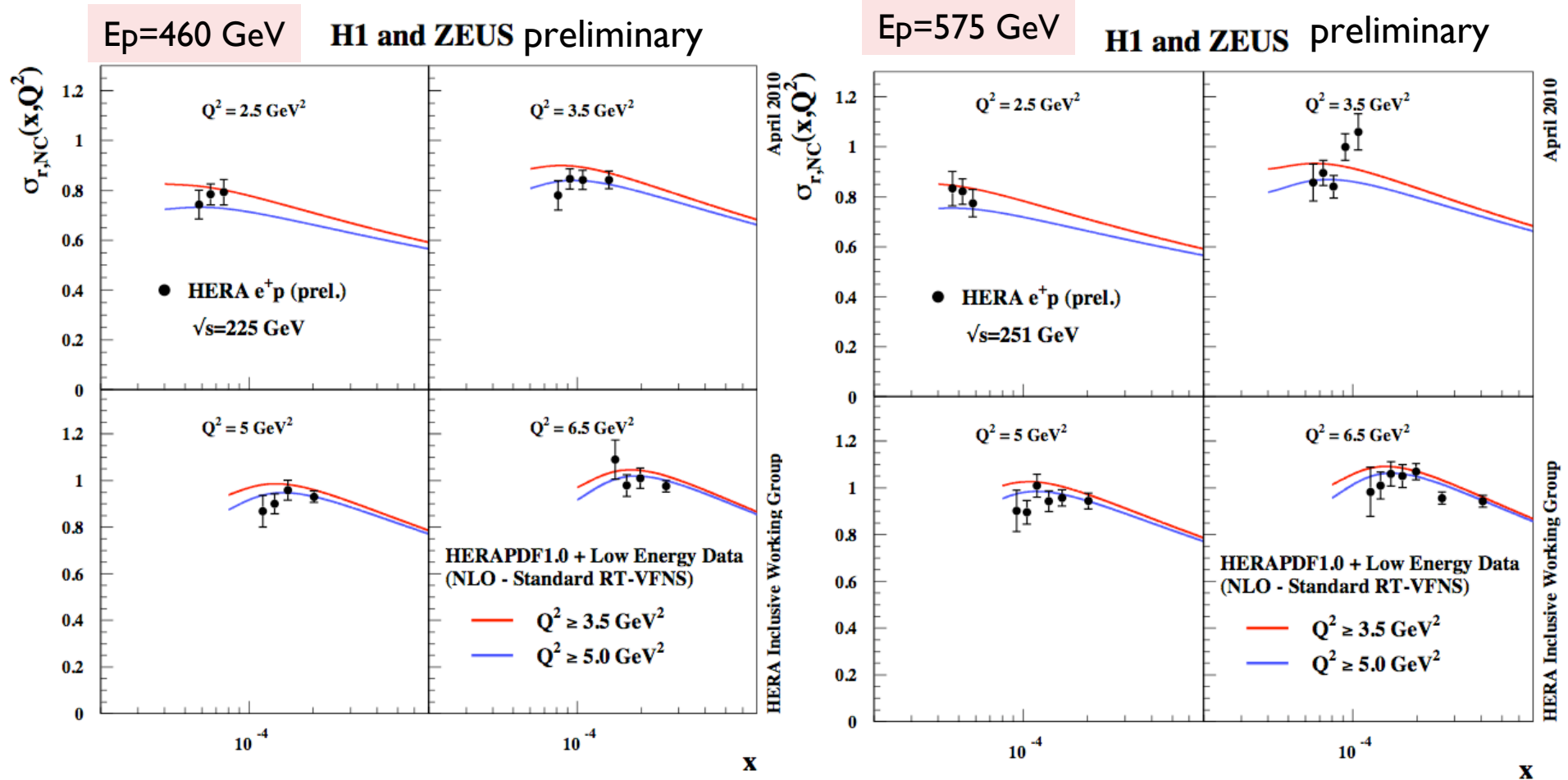


- RT:  $\chi^2/\text{dof} = 574/582$
- ACOT:  $\chi^2/\text{dof} = 562/582$
  
- RT heavy flavour scheme was cross checked against ACOT scheme for HERAPDF1.0
  - We did not observe much difference in the PDF distributions
  - ACOT line is shown in the HERAPDF1.0 paper



# Comparison with Low Energy data

- Note:  $Q^2 > 5 \text{ GeV}^2$  cut does not include first 2 bins in the fit.
  - The  $Q^2$  cut case (blue) fits better 460 GeV data which are all located at  $y > 0.35$ .







# ACOT schemes

- [Fred Olness]

## Effect of Kinematic Mass Re-Scaling

**ACOT** (Aivazis, Collins, Olness, Tung) A general framework for including the heavy quark components.

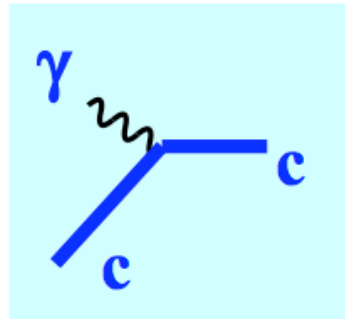
*Phys.Rev.D50:3102-3118,1994.*

**S-ACOT** (Simplified-ACOT) ACOT with the initial-state heavy quark masses set to zero.

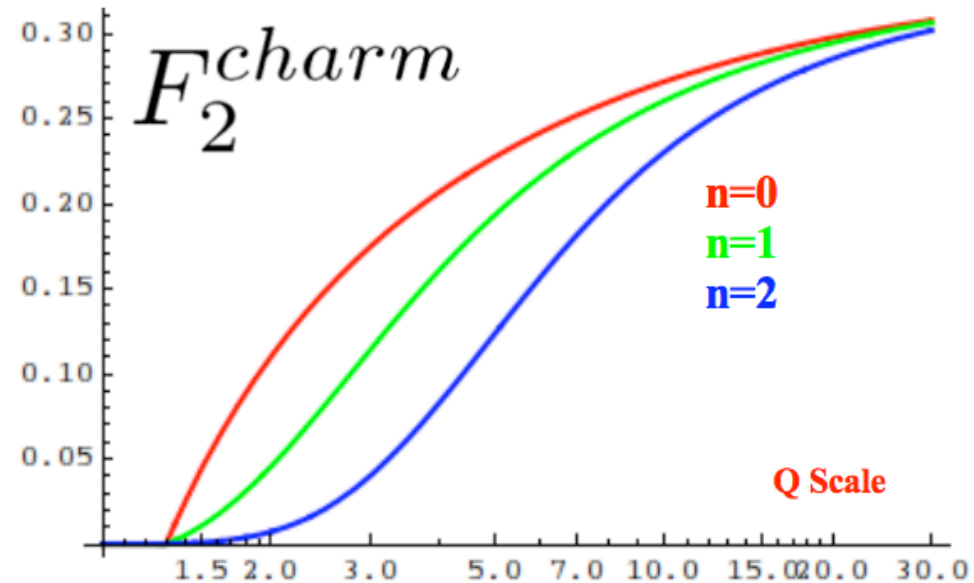
*Phys.Rev.D62:096007,2000.*

**ACOT- $\chi$  & S-ACOT- $\chi$** : As above with a generalized slow-rescaling

*Phys.Rev.D62:096007,2000.*



$$\chi = x \left[ 1 + \frac{(nm_c)^2}{Q^2} \right]$$





# Optimal cut?

- Is there a cut which can bring the high energy data alone and extension of the high energy data to low energy data into agreement?

Cut	$Q^2 > 1.0 x^{-0.3}$	$Q^2 > 1.0 x^{-0.3}$	$X > 5 \cdot 10^{-4}$	No cut
All $\chi^2/\text{dof}$	683.4/760	683.4/750	598.2/686	818.5/806
NCe+ $\chi^2/\text{dof}$	0.95 (330)	0.97 (330)	0.97 (322)	1.13 (379)
LER $\chi^2/\text{dof}$	N/A	0.82 (181)	0.79 (161)	1.04 (224)

- The saturation based cut looks optimal for  $A=1.0$ :
  - The high energy data and high energy + low energy data results look similar
  - This cut is no more dramatic than the low  $x$  cut.

→ Very interesting initial studies and more explorations are needed!



# Saturation inspired cut

