

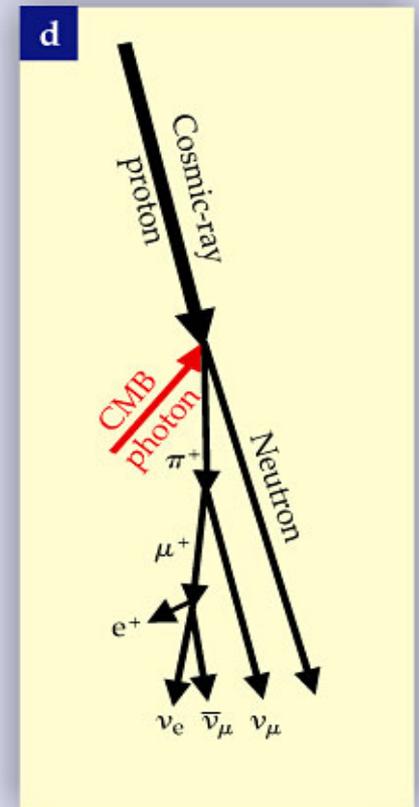
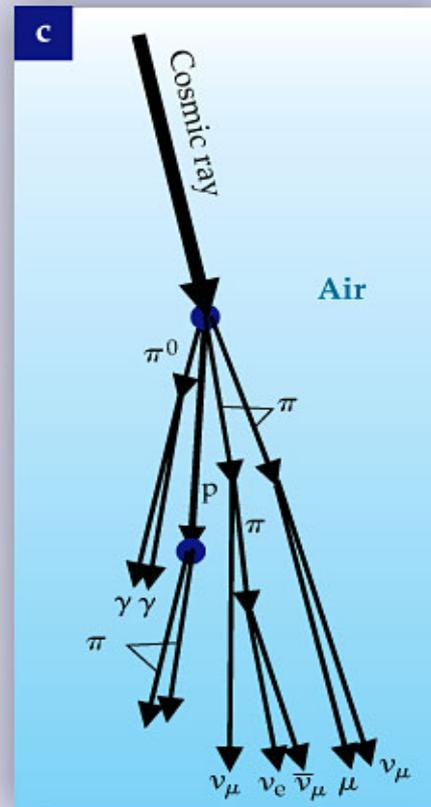
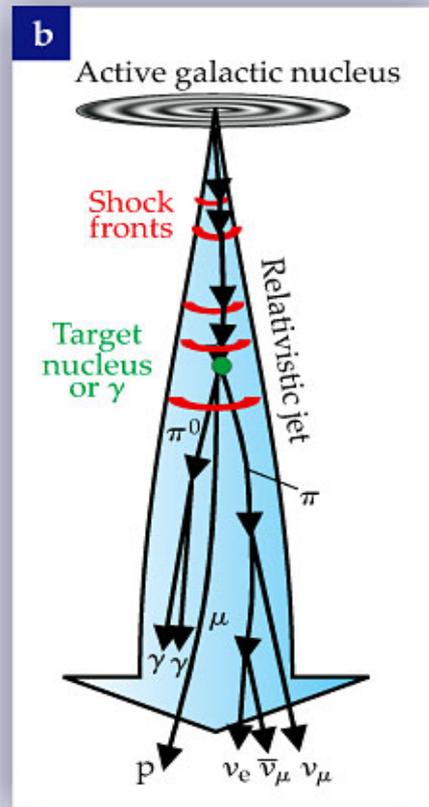
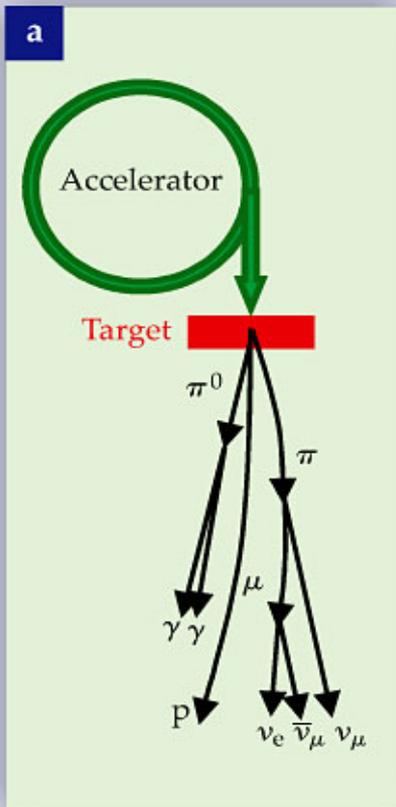
# Probing Small- $x$ QCD with Cosmic Neutrinos

**Ina Sarcevic**  
**University of Arizona**

# Cosmic accelerators

- Particles (electrons, protons, etc) are accelerated to high energies via Fermi shock acceleration
- High energy protons collide with ambient protons and photons
- Hadronic production of pions, kaons and D-mesons which decay into neutrinos

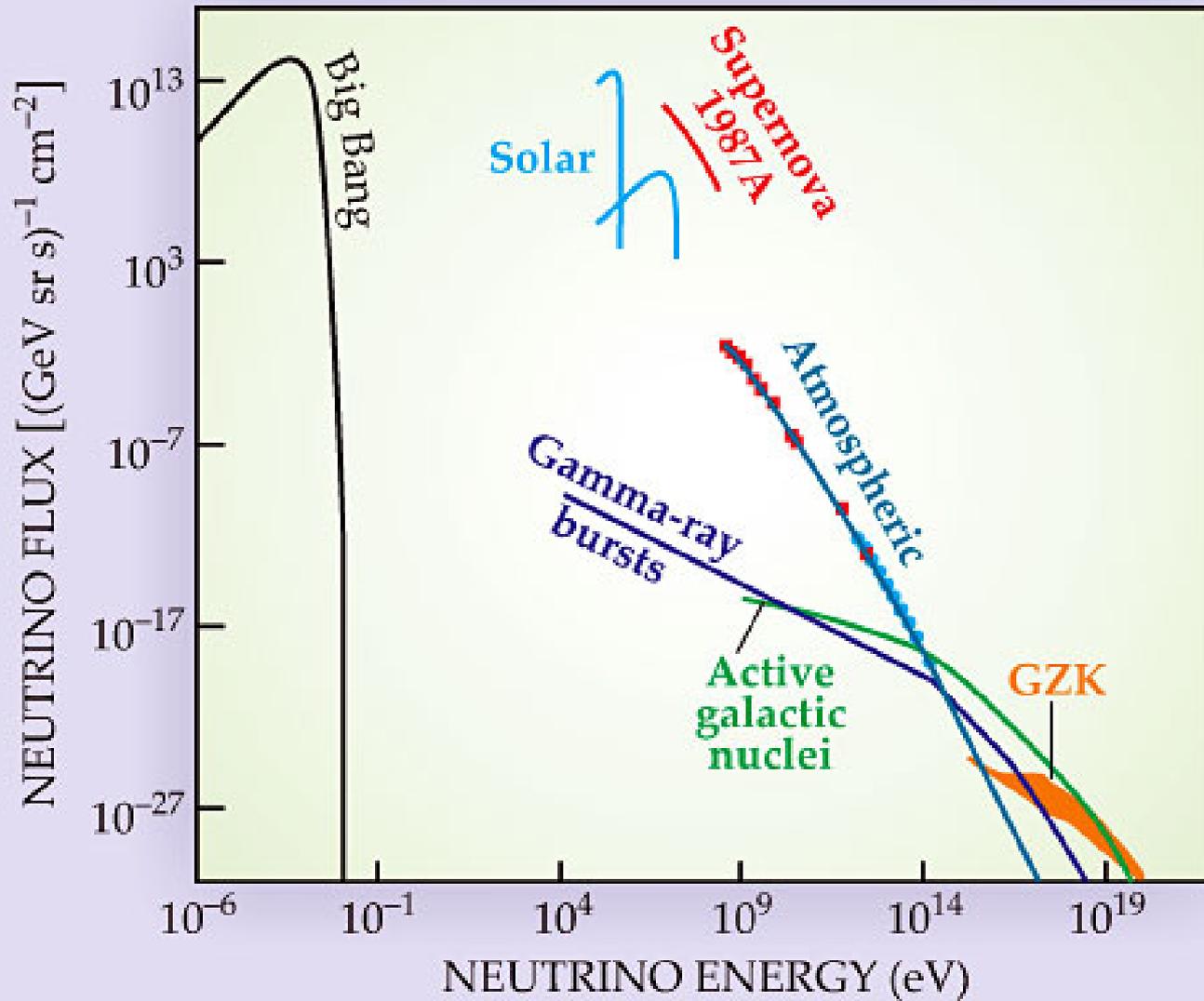
# Cosmic Accelerators



# Cosmic Neutrinos

- Solar Neutrinos (MeV energies)
- SN 1987A (MeV energies)
- Atmospheric Neutrinos (GeV to TeV energies)
- Extragalactic Neutrinos (AGN, GRB, cosmogenic; GeV to EeV energies)  
Cosmogenic Neutrinos (from interaction of cosmic rays with the microwave background radiation, guaranteed source of UHE neutrinos)

# Neutrino fluxes



# Neutrino Fluxes at Earth

Enberg, Reno and Sarcevic, Phys. Rev. D79(2009)

- ★ Cosmic neutrino flux is obtained by solving the evolution equations for nucleon, meson and neutrino fluxes:

$$\frac{d\phi_N}{dX} = -\frac{\phi_N}{\lambda_N} - \frac{\phi_N}{\lambda_{rad}} + S(Np \rightarrow NY)$$

$$\frac{d\phi_M}{dX} = -\frac{\phi_M}{\lambda^{dec}} - \frac{\phi_M}{\lambda^{had}} - \frac{\phi_M}{\lambda^{rad}} + S(Mp \rightarrow MY)$$

$$\frac{d\phi_l}{dX} = \sum_M S(M \rightarrow \nu)$$

where  $\lambda^{had}_{N,M}$  is the interaction length ( $\lambda_N = 1/(n_p \sigma_{pp})$ ),  
 $\lambda^{dec} = \gamma c \tau_M$  is the decay length

$S(k \rightarrow j)$  is the regeneration function for  
 $k=p, \pi^\pm, K^\pm, D^\pm, D^0,$

$$S(k \rightarrow j) = \int_E^\infty \frac{\phi_k(E_k)}{\lambda_k(E_k)} \frac{dn(k \rightarrow j; E_k, E_j)}{dE_j} dE_k$$

$dn(k \rightarrow j; E_k, E_j)/dE_j$  is the  $\pi^\pm, K^\pm, D^\pm, D^0$   
**production** or **decay** distribution :

$$\frac{dn(k \rightarrow j; E_k, E_j)}{dE_j} = \frac{1}{\sigma_{kA}(E_k)} \frac{d\sigma(kp \rightarrow jY, E_k, E_j)}{dE_j}$$

$$\frac{dn(k \rightarrow j; E_k, E_j)}{dE_k} = \frac{1}{\Gamma_k} \frac{d\Gamma(kj \rightarrow jY, E_j)}{dE_j}$$

# Charm Production and Cross Sections using pQCD and PDFs

$$\frac{d\sigma}{dx_F} = \int \frac{dM_{c\bar{c}}^2}{(x_1 + x_2)s} \sigma_{gg \rightarrow c\bar{c}}(\hat{s}) G(x_1, \mu^2) G(x_2, \mu^2)$$

The total charm cross section in pQCD is given by:

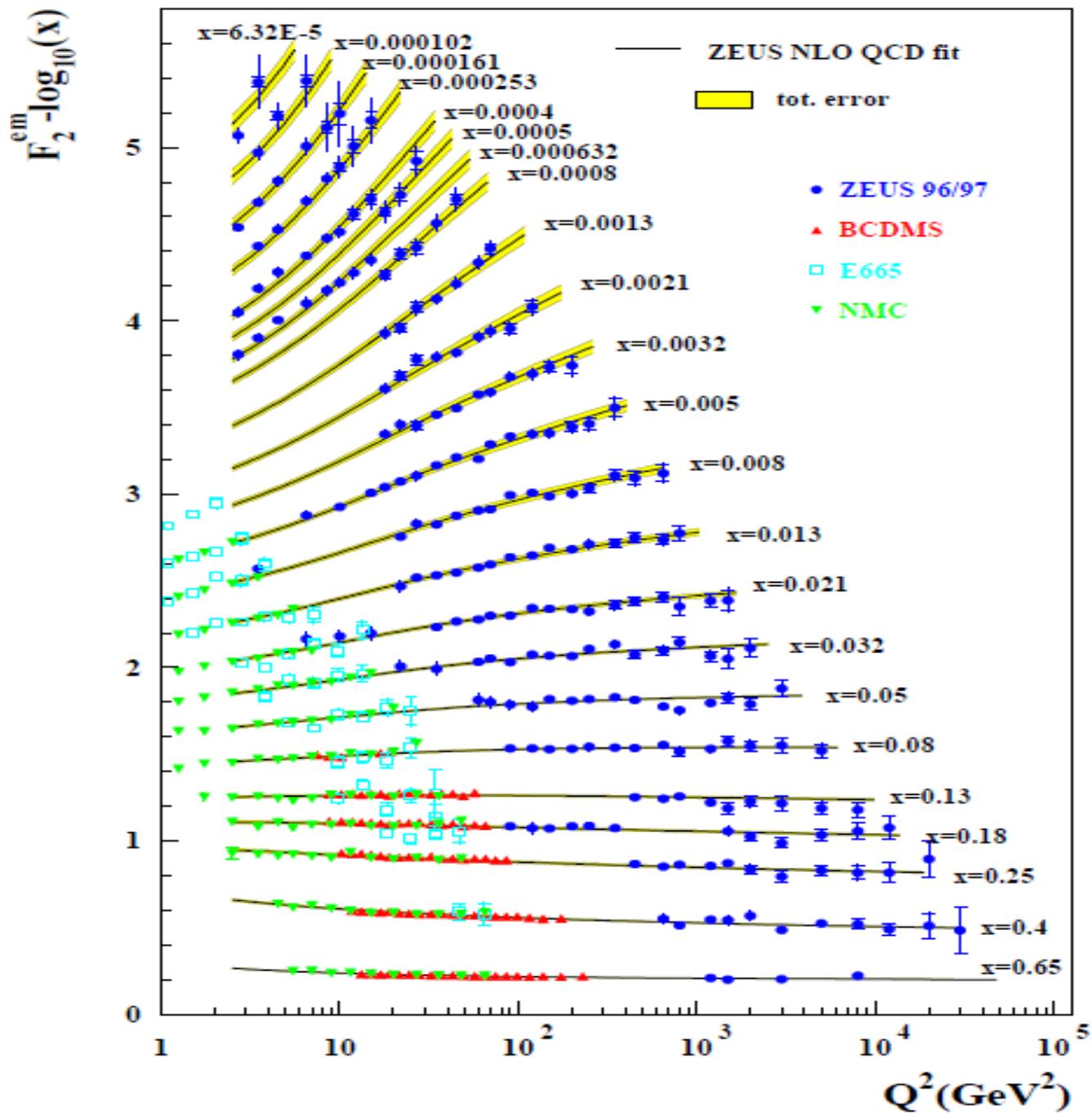
$$\sigma(pp \rightarrow c\bar{c}X) = \int dx_1 dx_2 G(x_1, \mu^2) G(x_2, \mu^2) \hat{\sigma}_{gg \rightarrow c\bar{c}}(x_1 x_2 s)$$

where

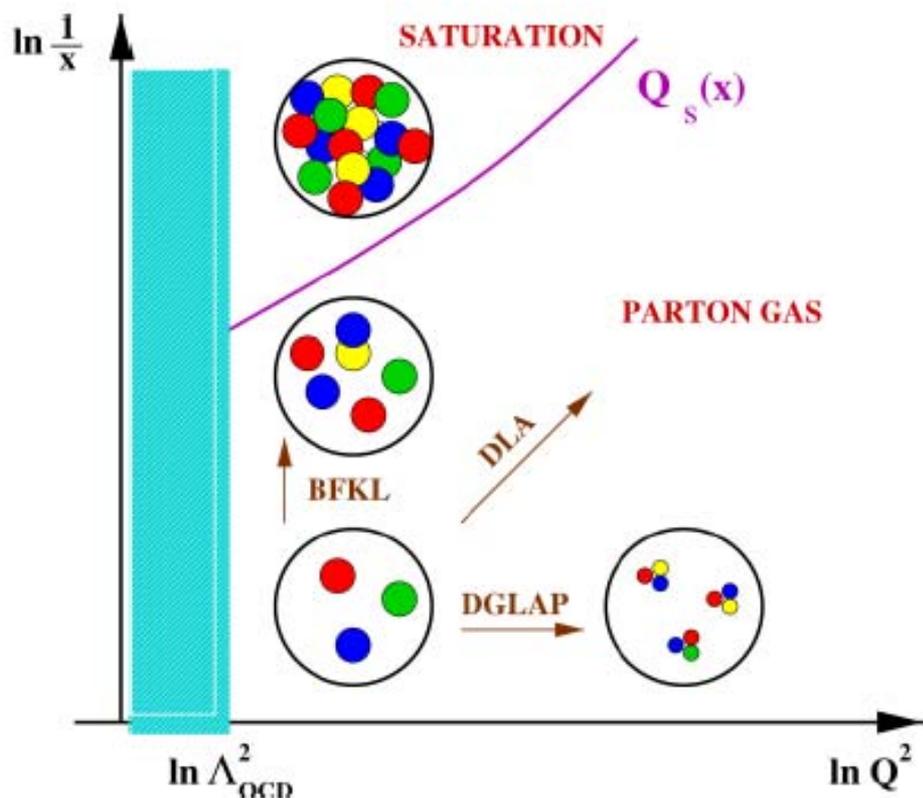
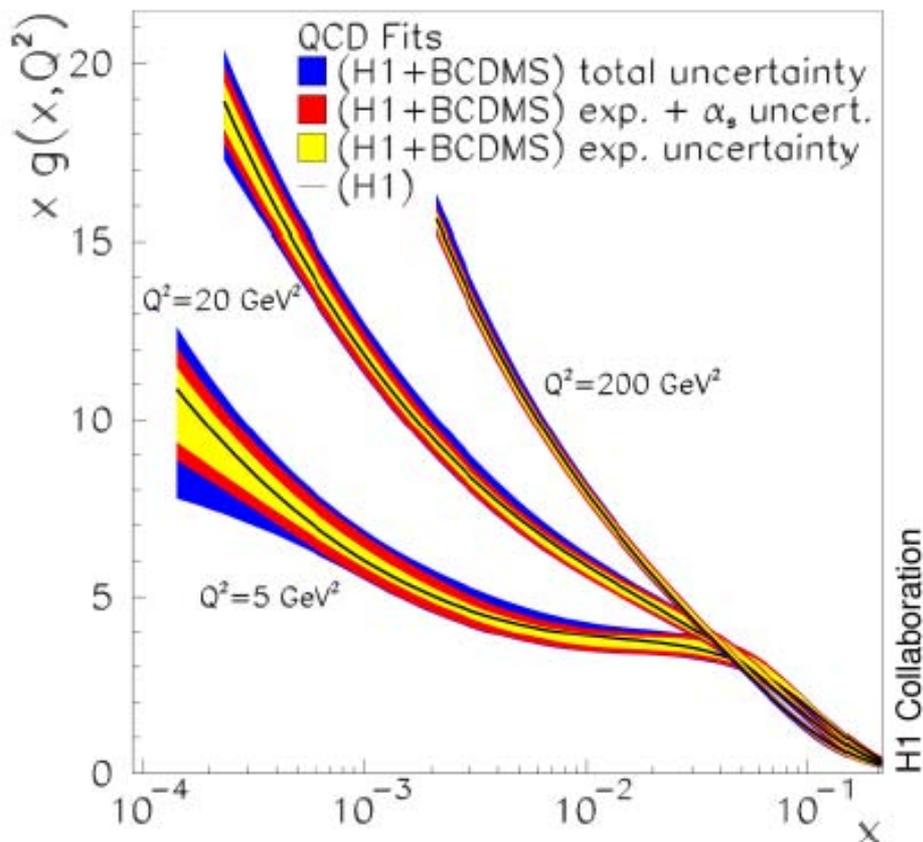
$$x_{1,2} \sim m_c / 2m_p E_\nu$$

For high energies we need gluon PDF for small  $x$ , and low  $Q^2$

# ZEUS

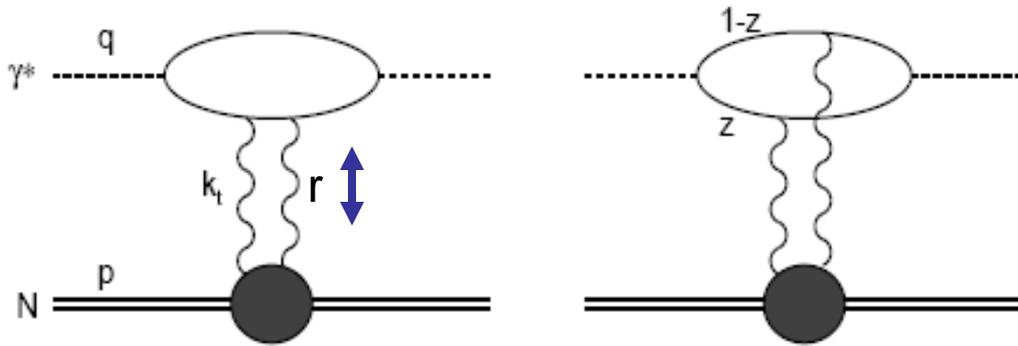


# The problem of small $x$



Glueon distribution grows rapidly as  $x \rightarrow 0$ : gluons start overlapping  
and may start recombining: **saturation** of cross section

# Charm Production: dipole approach



$$\gamma^* \rightarrow q\bar{q}$$

$$q\bar{q}N \rightarrow X$$

heavy quarks:

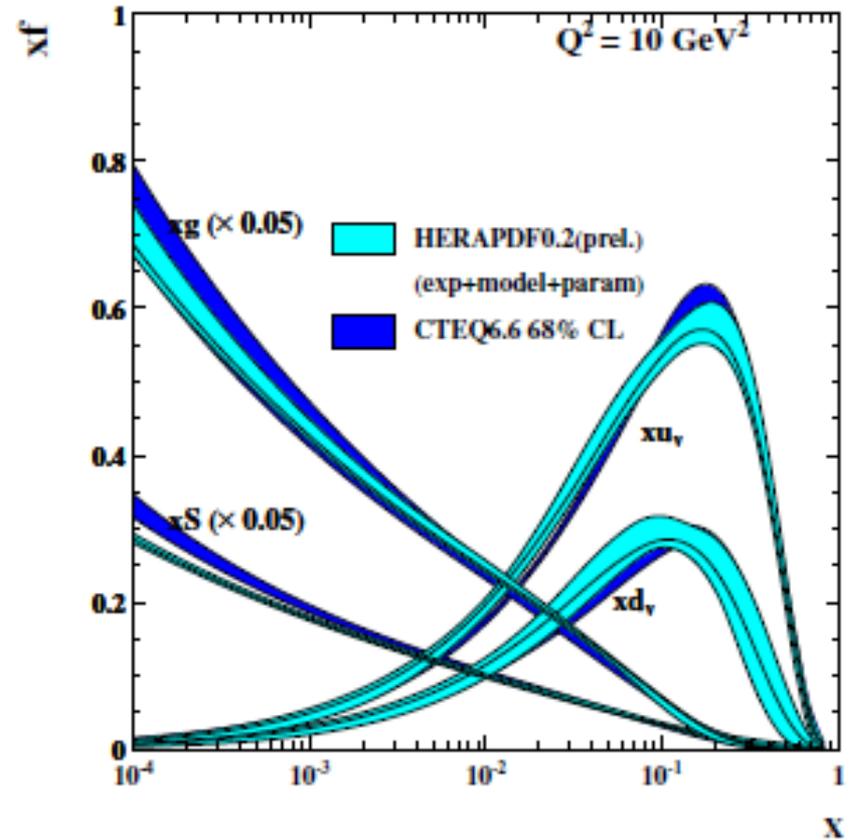
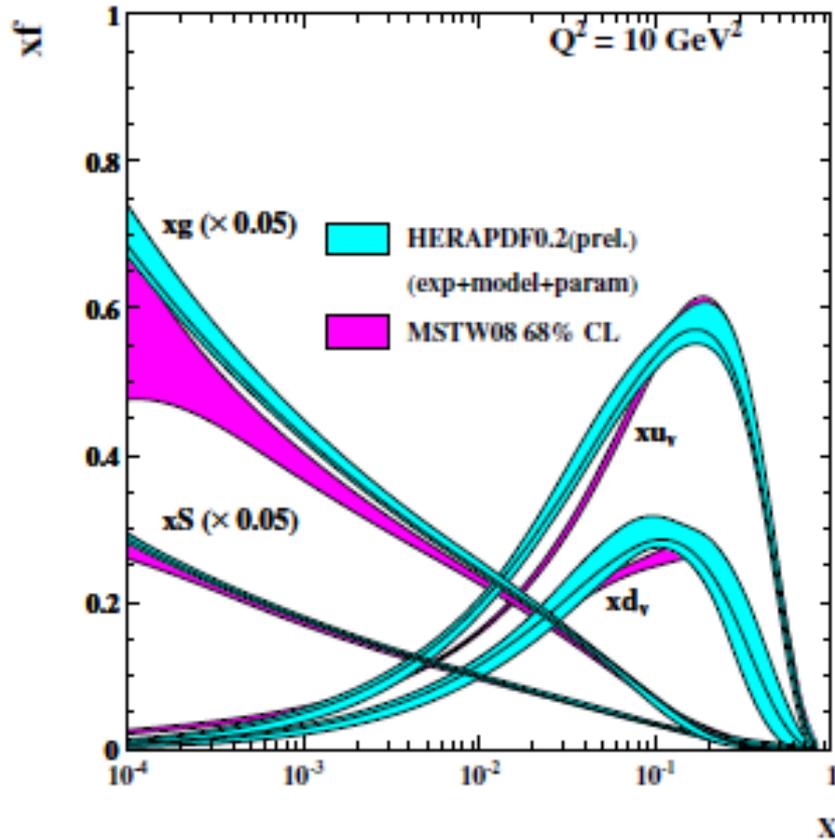
$$\gamma^* \rightarrow c\bar{c}$$

$$c\bar{c}N \rightarrow c\bar{c}X$$

$$\sigma_T(\gamma^* N) = \int_0^1 dz \int d^2\mathbf{r} |\Psi_T(z, \mathbf{r}, Q^2)|^2 \sigma_{dN}(x, \mathbf{r})$$

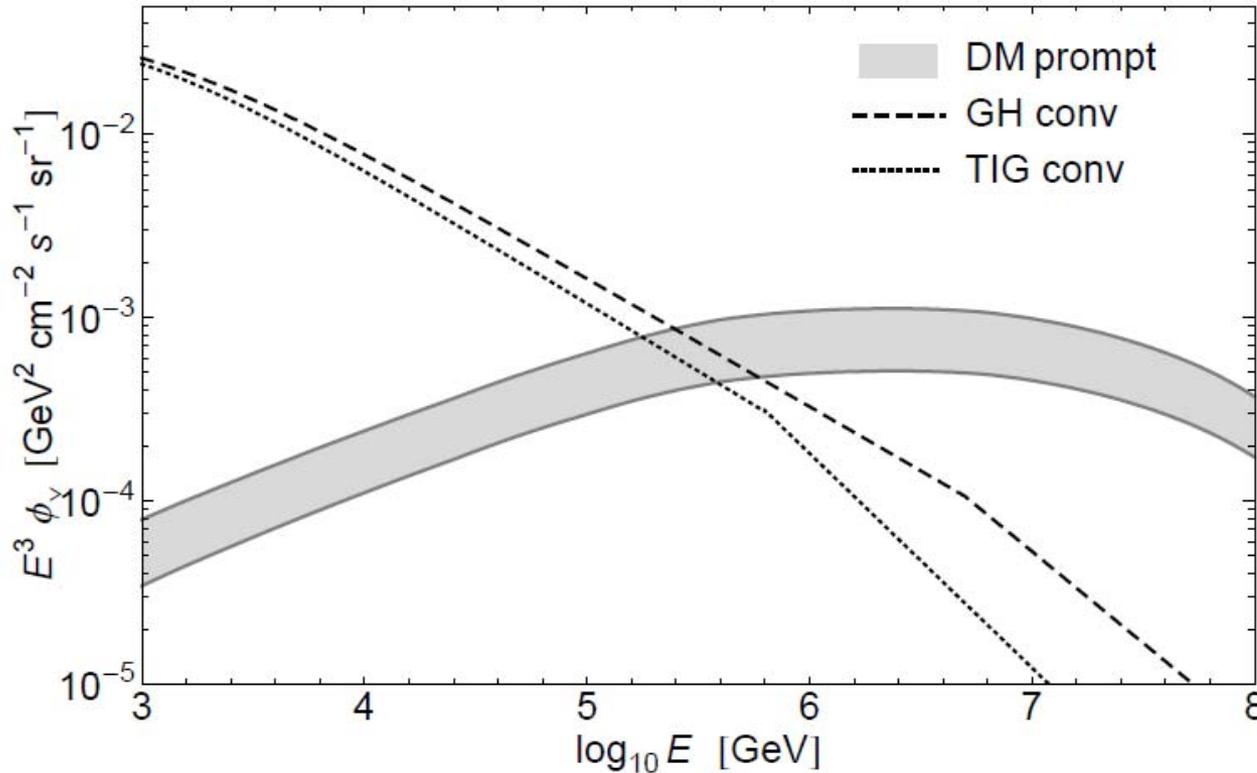
- Dipole model fits small  $x$  data HERA data (Stasto, et al., PRL 86 (2001))
- Improved QCD motivated form - Balitsky-Kovchegov (BK) evolution modified for gluon  $\rightarrow$  charm anticharm pair

# HERA PDF comparison with MRSTW and CTEQ



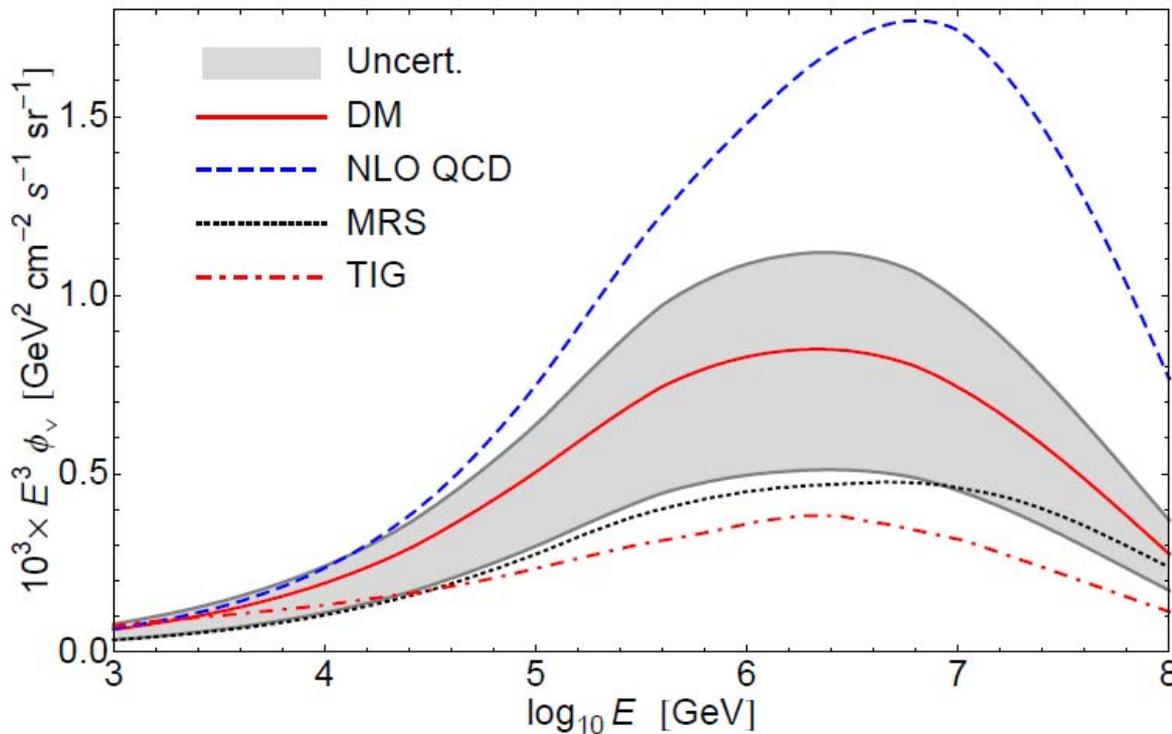
Raicevic (H1 and ZEUS), Nucl. Phys. B198 (2010)

# Prompt Atmospheric Neutrino Flux



**DM=dipole model**  
**GH=Gaisser-Honda**  
**TIG=Thunman et al.**  
**(PDF + pythia, small**  
**x extrapolation)**

# Prompt ATM Neutrino Flux



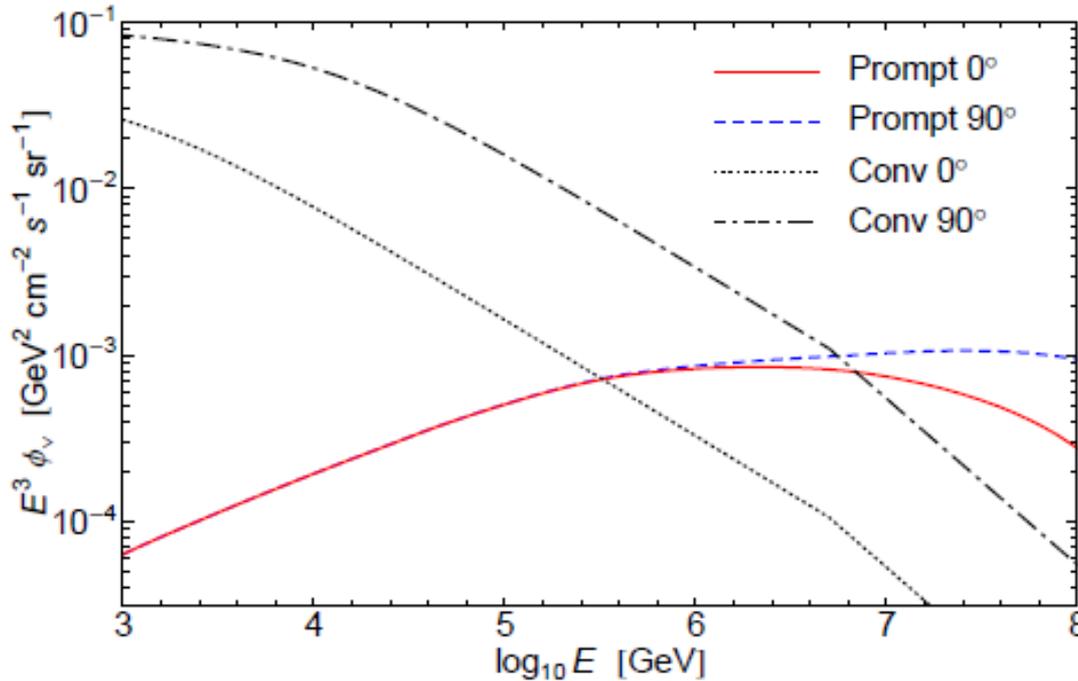
Range of predictions:

DM=our dipole model

MRS=Martin,  
Roberts, Stasto,  
Acta Phys. Polon.  
B34 (2003), uses a  
simpler form for  
dipole model cross  
section.

Enberg, Reno, Sarcevic, Phys. Rev. D 78  
(2008) 043005

# Atmospheric neutrinos-angular dependence



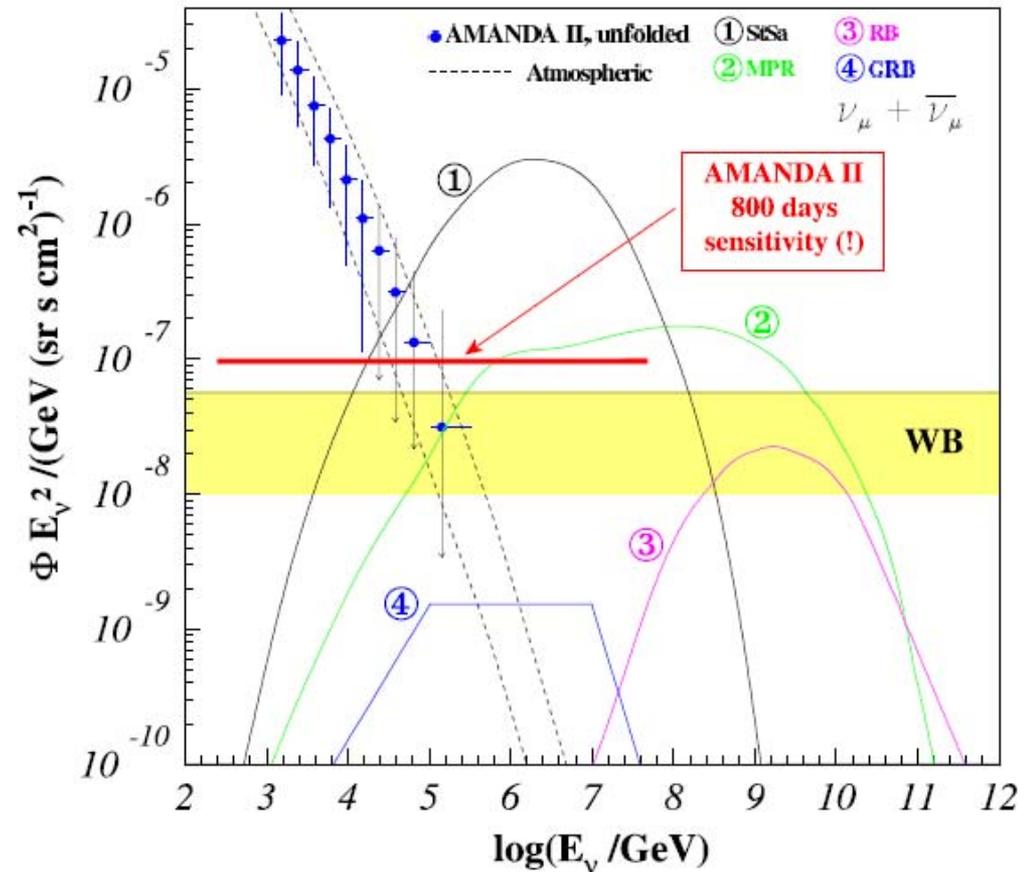
Muon neutrino plus antineutrino flux, from our dipole model "prompt" calculation.

Conventional flux from Gaisser-Honda.

Enberg, Reno, Sarcevic, Phys. Rev. D 78 (2008) 043005

# Measurement of ATM Neutrino Flux

Icecube will be able to get more data at high energies



# Neutrino Detection

- Detection of neutrinos depends on their interactions, i.e. cross section
- Muon neutrinos interacting with “matter”, i.e. nucleons, producing muons
- Muons are “charged”, so they leave charged tracks in the neutrino detector

- The event rate for “downward” muons from neutrino interactions

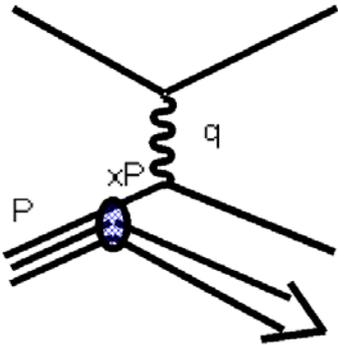
$$R = V \int dE_\nu \sigma_{cc}(E_\nu) F_\nu(E_\nu)$$

- The event rate for “upward” muons from neutrino interactions

$$R = N_A A \int dE_\nu \sigma_{cc} R_\mu S(E_\nu) F(E_\nu)$$

where  $F_\nu(E_\nu)$  is neutrino flux at the source,  $S(E_\nu)$  is neutrino attenuation and  $R_\mu$  is muon range

# Ultrahigh energy neutrino-nucleon scattering



Medium energy,  $\sigma \sim G_F^2 s \simeq 2.8 \cdot 10^{-39} \text{ cm}^2 \cdot s/\text{GeV}^2$

High energy:  $Q^2 \rightarrow M_W^2$

$$x_{\min} = M_W^2 / 2m_N E_\nu$$

$$\frac{d^2 \sigma}{dx dy} = \frac{2G_F^2 M E_\nu}{\pi} \left( \frac{M_W^2}{Q^2 + M_W^2} \right)^2 \left[ xq(x, Q) + x\bar{q}(x, Q)(1-y)^2 \right]$$

W boson propagator

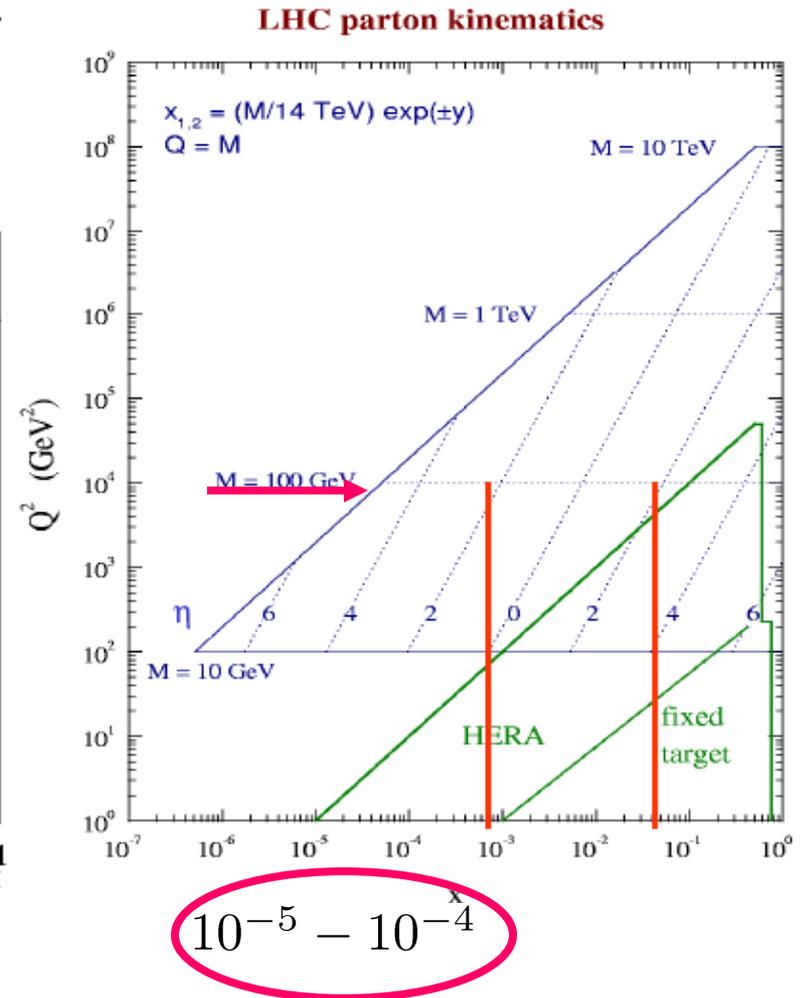
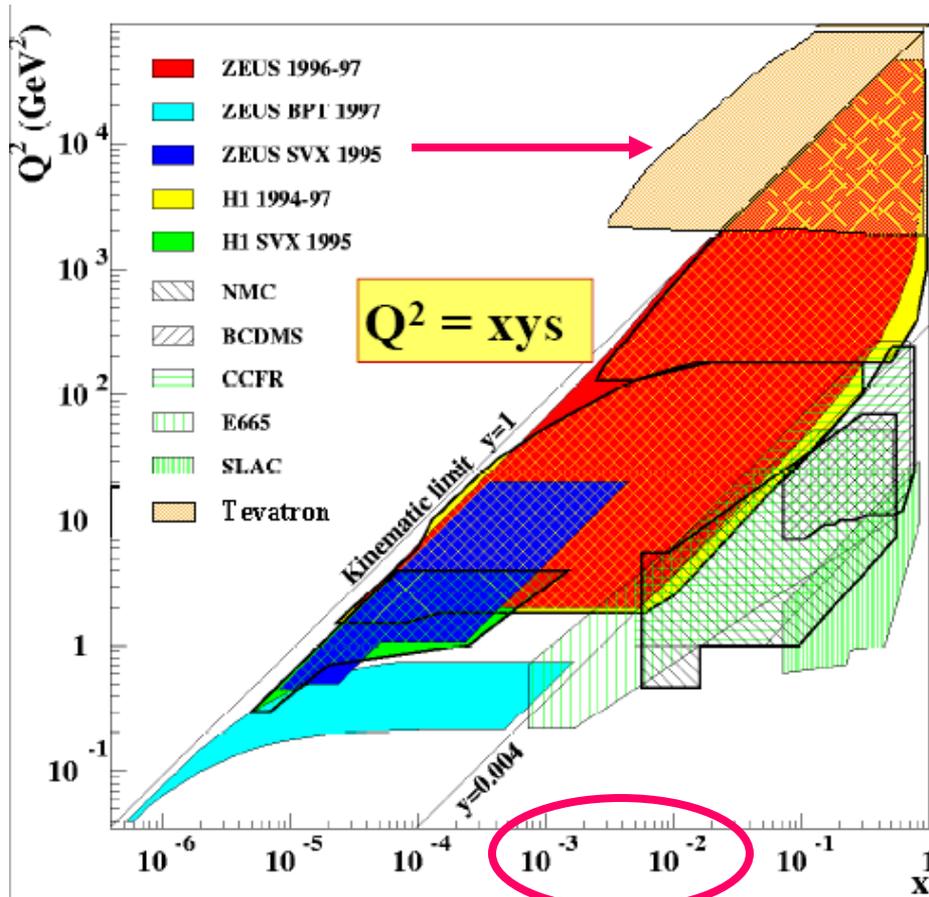
Quark distribution functions

For  $E_\nu > 10^8 \text{ GeV}$ ,  $x_{\min} < 10^{-5}$ , we need parton distributions at small  $x$  and  $Q \sim M_W$

Gandhi, Reno, Quigg and Sarcevic, PRD 58 (1998);  
Astropart. Phys. 5 (1996)

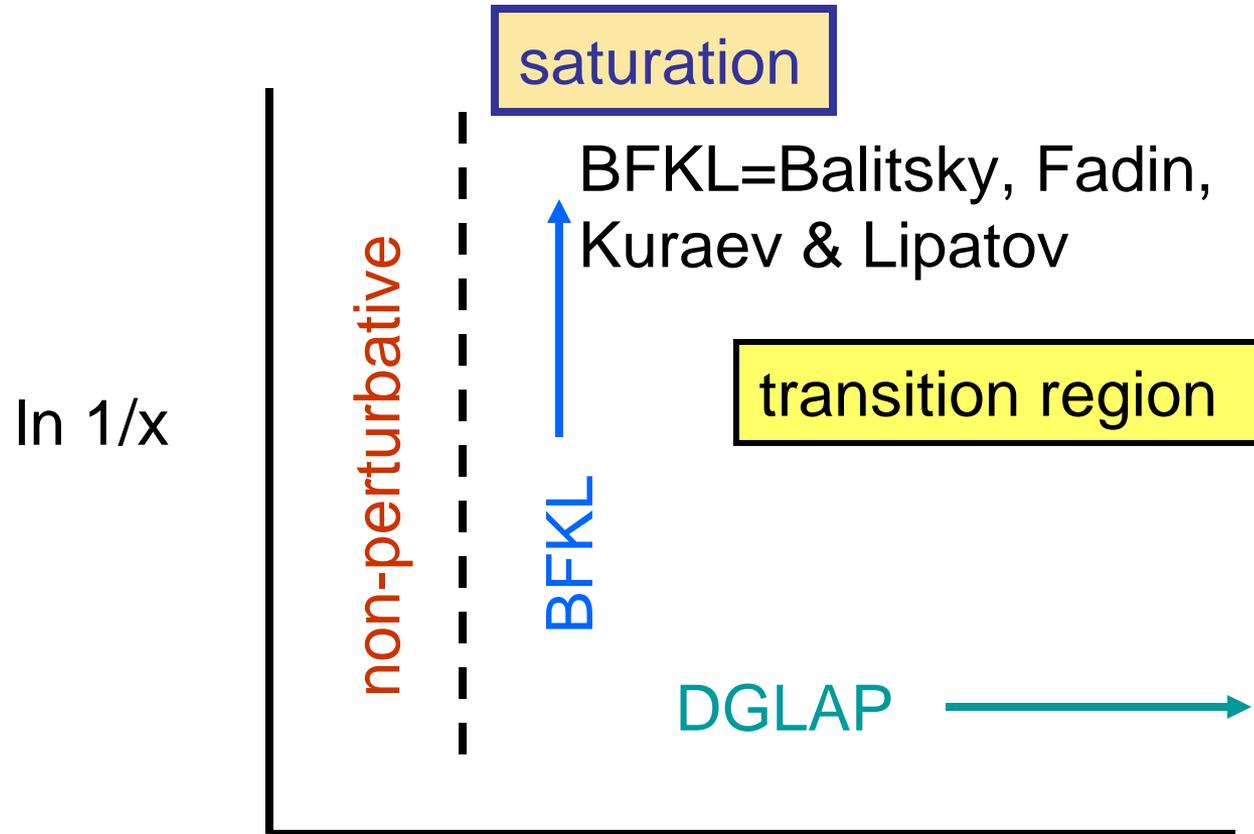
# Structure functions (to get PDFs)

LHC up to  $s \sim 10^9 \text{ GeV}^2$



From B. Foster's 2002 Frascati Talk

# Theory Issues: how to extrapolate?

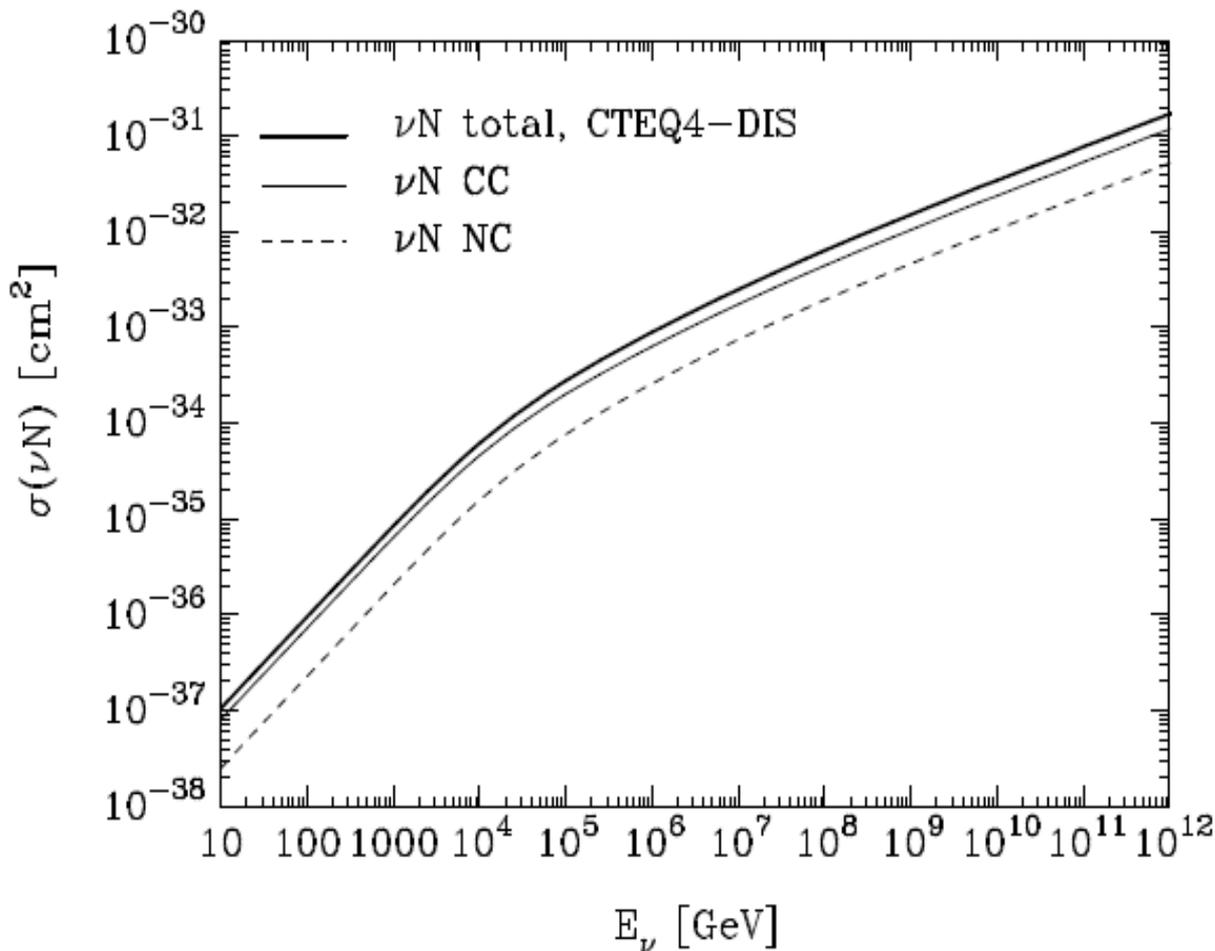


Deep Inelastic Scattering  
Devenish & Cooper-Sarkar,  
Oxford (2004)

ln Q

DGLAP=Dokshitzer,  
Gribov, Lipatov, Altarelli  
& Parisi

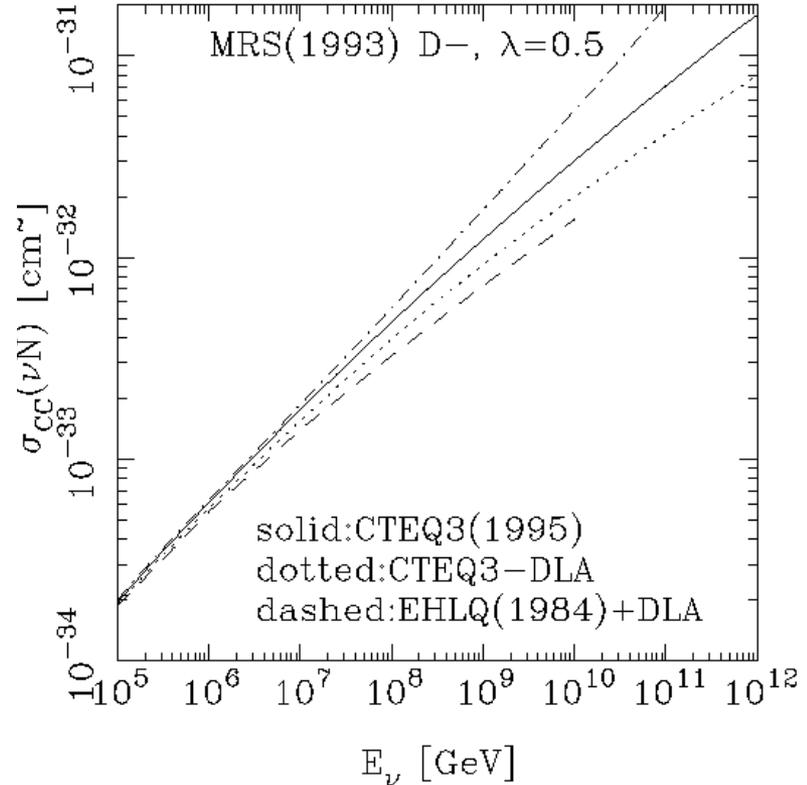
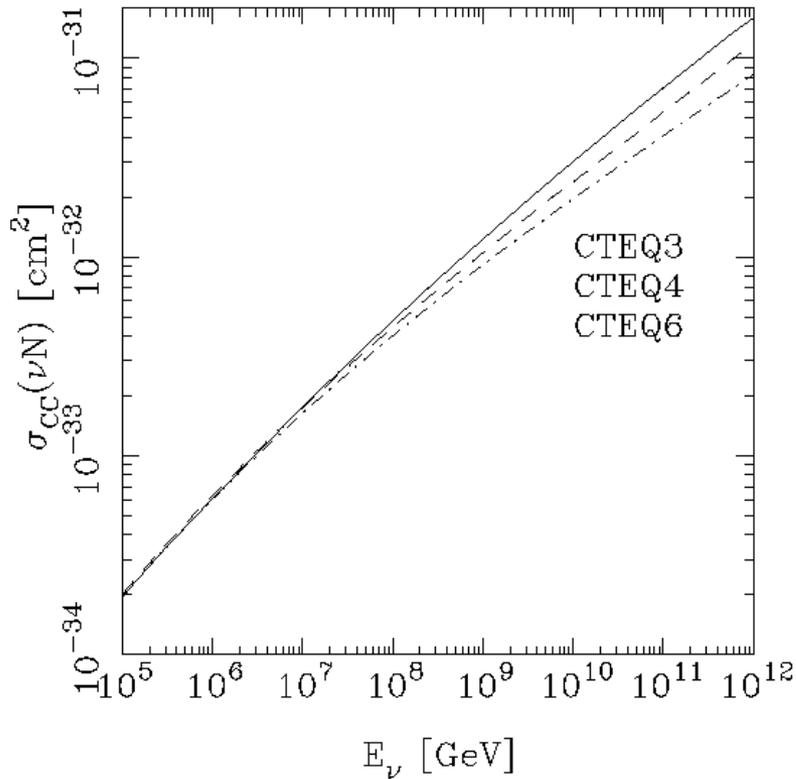
# Neutrino Cross Sections



R. Gandhi, C. Quigg, M.H. Reno and I.S., PRD58 (1998)

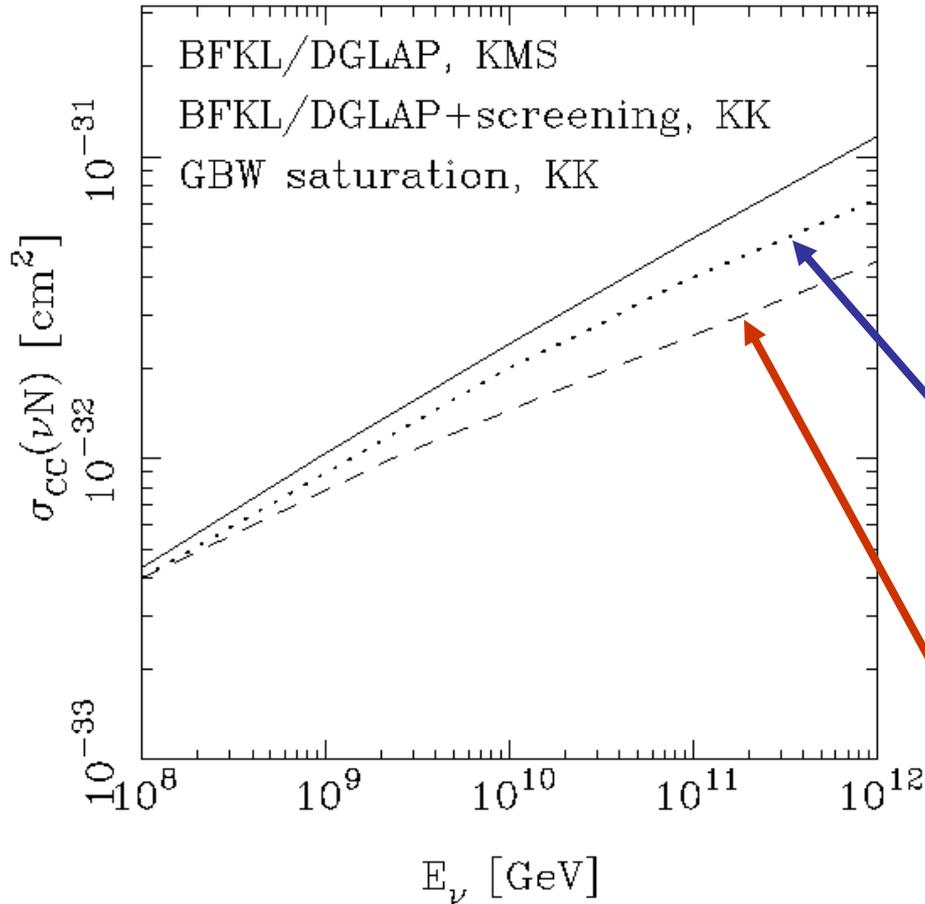
At high energy  $\sigma(\nu N)$  sensitive to small- $x$  QCD

# Small x extrapolations



Gandhi, Reno, Quigg and Sarcevic, PRD 58 (1998),  
Astropart. Phys. 5 (1996)

# CC Cross Sections

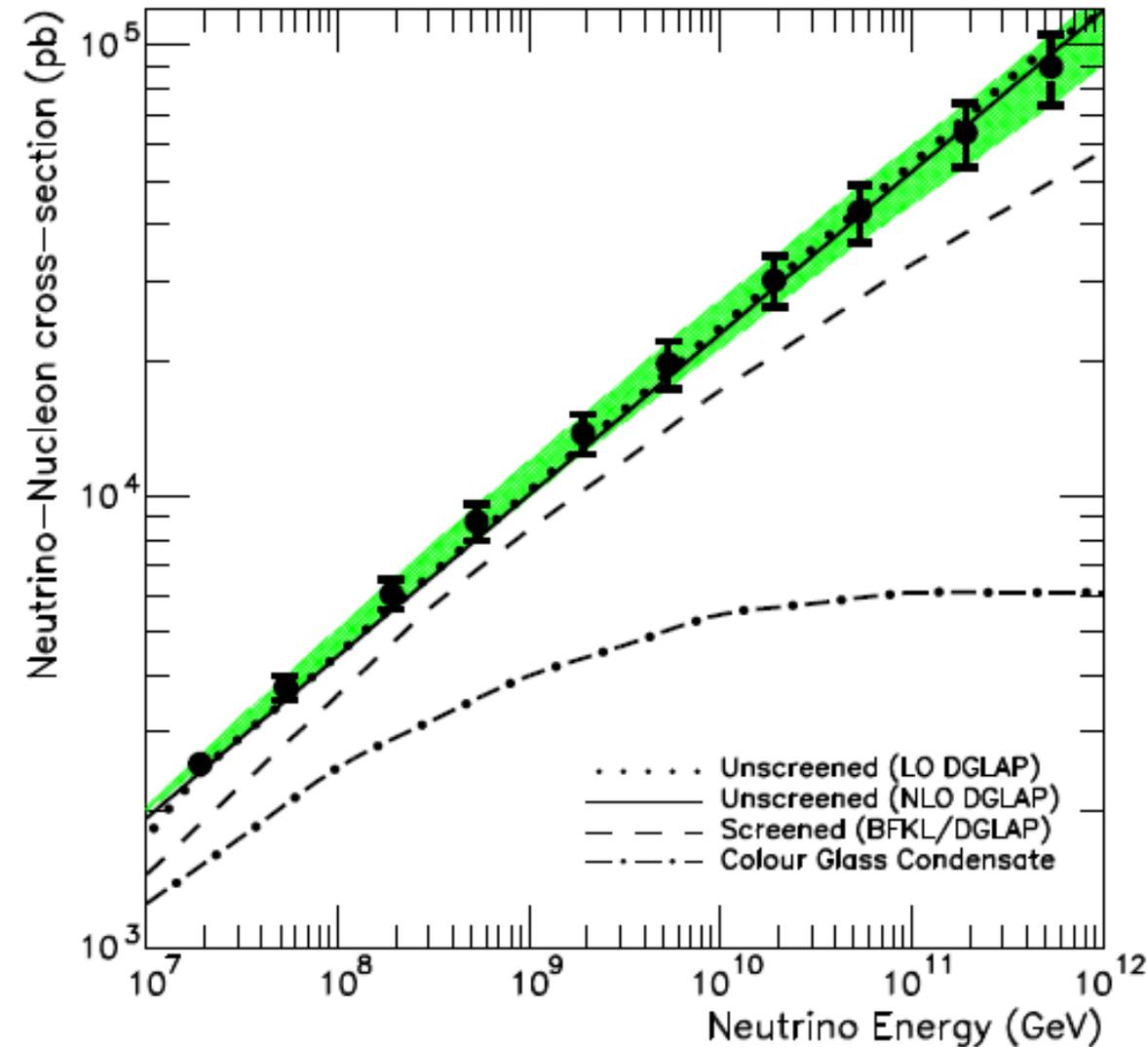


**KMS: Kwiecinski, Martin & Stasto, PRD56(1997)3991;**

**KK: Kutak & Kwiecinski, EPJ,C29(2003)521**

more realistic screening, incl. QCD evolution

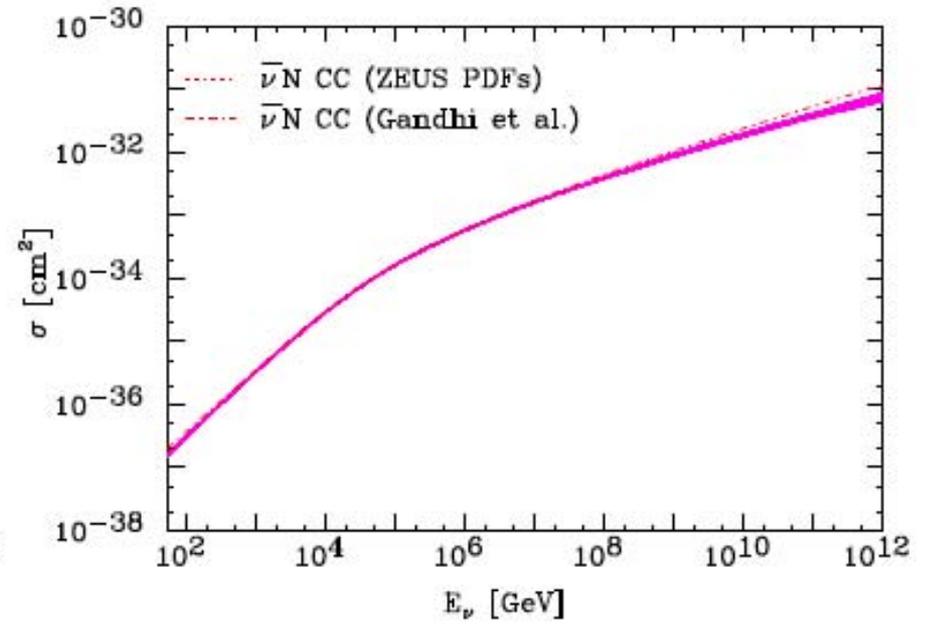
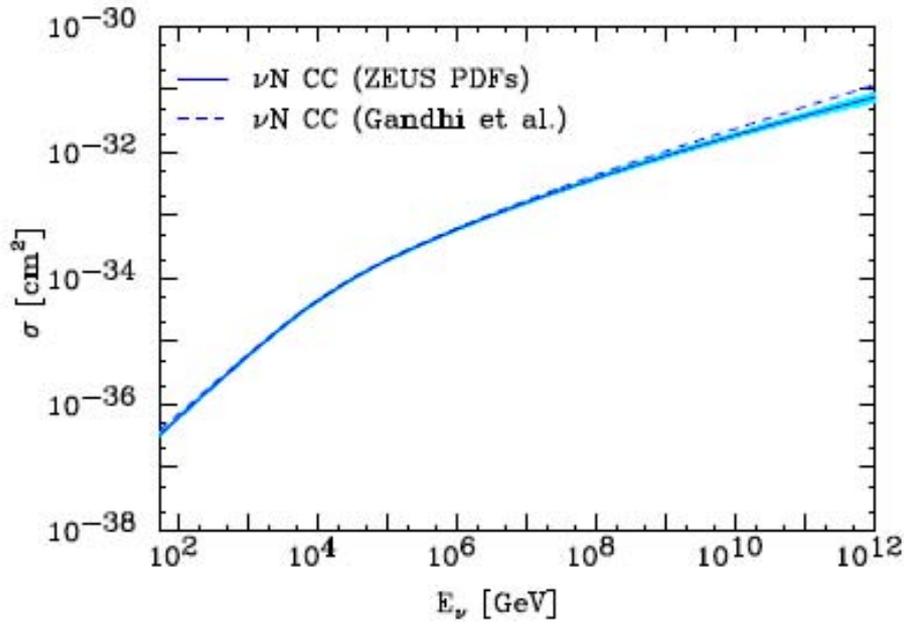
**Golec-Biernat & Wusthoff model (1999), color dipole interactions for screening.**



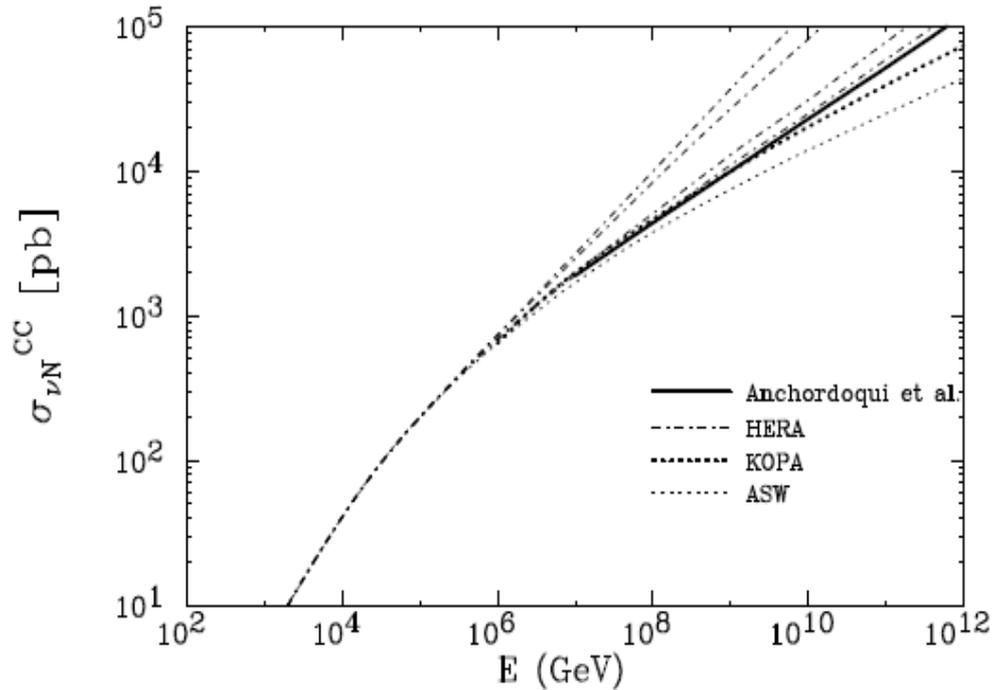
KK

Henley & Jalilian-Marian  
PRD73 (2006) 094004

Anchordoqui, Cooper-Sarkar, Hooper & Sarkar,  
Phys. Rev. D 74 (2006) 043008



**Cooper-Sarkar & Sarkar, JHEP 0801 (2008), new analysis of HERA data incl. heavy flavor, lower cross section at UHE (closer to CTEQ6 results)**



**HERA: extrapolations with  $\lambda=0.5, 0.4, 0.38$**

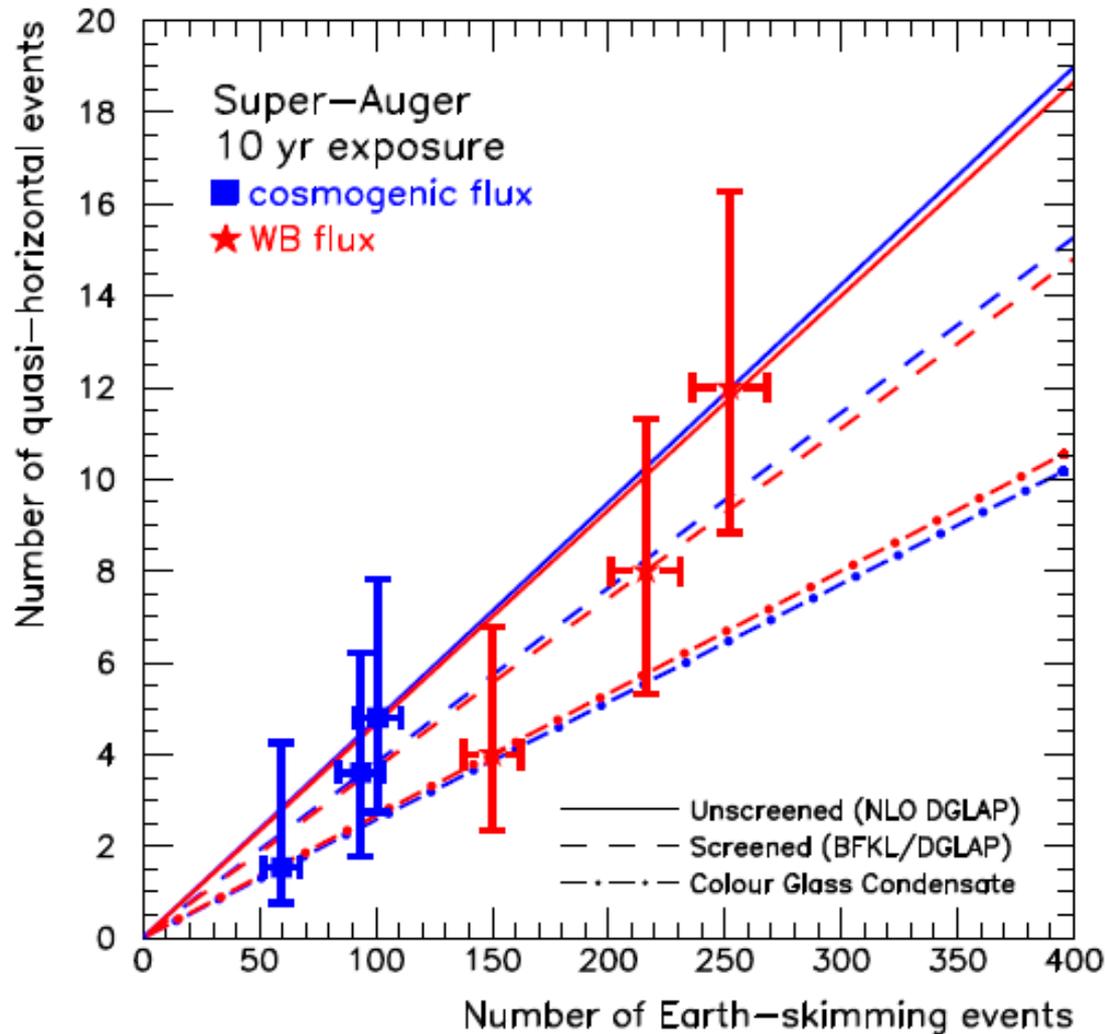
**KOPA: DLA, Kotikov & Parente**

**ASW: saturation effects, Armesto, Salgado & Wiedeman**

**Armesto, Merino, Parente & Zas, PR D 77 (2008)**

**Anchordoqui, Cooper-Sarkar, Hooper & Sarkar, Phys. Rev. D 74 (2006)**

# Determining UHE Neutrino Cross Sections



Anchordoqui et al.,  
PR D76 (2007)

$$\mathcal{N}_{\text{QH}} \propto \int dE_{\text{sh}} \sigma_{\nu N}(E_{\nu}) A_{\text{QH}}(E_{\text{sh}}, \theta_z) \phi^{\nu}(E_{\nu})$$

# Conclusions

- Charm contribution to neutrino production is important at high energies.
- Measurement of atmospheric neutrinos at high energies can provide information about small- $x$  (small  $Q^2$ ) parton distributions.
- Neutrino detection depends on neutrino cross section which relies on small- $x$  extrapolations of parton distributions (large  $Q^2$ ) well beyond the experimental measurements
- Cosmic neutrinos can be used as probes of small- $x$  QCD

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search ID: shr1284

"QUARKS, NEUTRONS, MESONS. ALL THOSE DAMN PARTICLES  
YOU CAN'T SEE. THAT'S WHAT DROVE ME TO DRINK.  
BUT NOW I CAN SEE THEM!"