# Forward energy and jet flows in high energy factorisation

#### Michal Deák

Instituto de Física Teórica, Universidad Autonoma de Madrid

# Contents

- Short introduction and motivation
- High energy factorisation framework
- High energy factorisation vs. multi parton interactions (MPI)
- Energy and jet flows
- Summary and conclusions

#### Forward jets - motivation

- Probes small-x parton densities
- Important signal for BFKL dynamics

(Kepka et al., Phys. Lett. B655, 236 (2007). hep-ph/0609299, Eur. Phys. J. C55, 259 (2008). hep-ph/0612261)

- Extensive coverage of large rapidity regions at the LHC experiments ( $3<|\eta|<5$  and  $-5.2>\eta>-6.6$ )
  - Possibility to study two jet correlations

## Forward jets - relevant kinematics

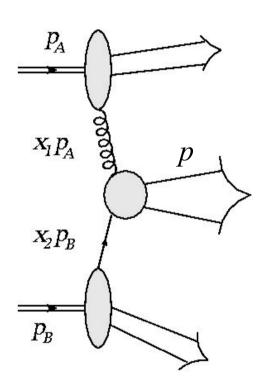
Equation for the rapidity of the hard subprocess final state

$$p = (p_0, p_3, p_2, p_1)$$

$$p_A = \left(\frac{\sqrt{s}}{2}, \frac{\sqrt{s}}{2}, 0, 0\right)$$

$$p_B = \left(-\frac{\sqrt{s}}{2}, \frac{\sqrt{s}}{2}, 0, 0\right)$$

$$y = \frac{1}{2} \ln \frac{p_0 + p_3}{p_0 - p_3} = \frac{1}{2} \ln \frac{x_1}{x_2}$$



## Forward jets - relevant kinematics

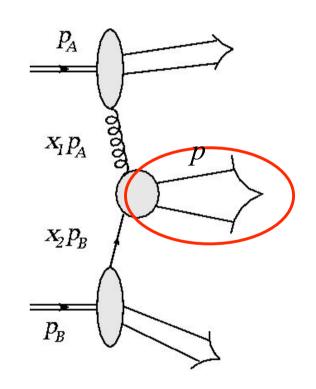
Equation for the rapidity of the hard subprocess final state

$$p = (p_0, p_3, p_2, p_1)$$

$$p_A = \left(\frac{\sqrt{s}}{2}, \frac{\sqrt{s}}{2}, 0, 0\right)$$

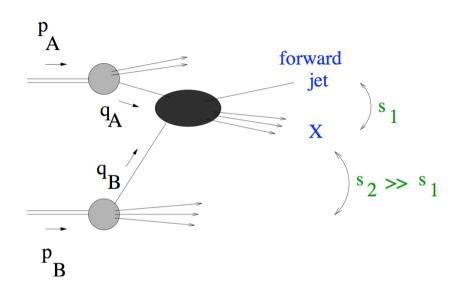
$$p_B = \left(-\frac{\sqrt{s}}{2}, \frac{\sqrt{s}}{2}, 0, 0\right)$$

$$y = \frac{1}{2} \ln \frac{p_0 + p_3}{p_0 - p_3} = \frac{1}{2} \ln \frac{x_1}{x_2}$$



• If  $x_1 \sim 10^{-5}$  and  $x_2 \sim 0.1$  then  $y \sim 4.5$  - very forward!

## Simple kinematics + dynamics



- 2 distinct scales  $s_1$  and  $s_2$
- In the cross section of this process will appear logarithms of the form

$$\ln\left(\frac{s_2}{s_1}\right) \sim \ln\left(\frac{x_2}{x_1}\right)^{x_2} \sim \ln\left(\frac{1}{x_1}\right)$$

- Can be resummed by the BFKL equation
  - Works in inclusive case
- Exclusive states possible with CCFM equation implemented in Monte Carlo Cascade
- Parton showers based on the CCFM equation

#### **Cross section**

The dominant processes for forward jet production

$$qg^* \to qg$$
$$gg^* \to gg$$
$$gg^* \to q\bar{q}$$

- One parton off-shell carrying a small x
- Goal is to calculate the cross section

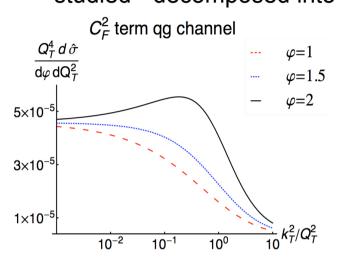
$$rac{d\sigma}{dQ_t^2 darphi} = \sum_a \int \; \phi_{a/A} \; \otimes \; rac{d\widehat{\sigma}}{dQ_t^2 darphi} \; \otimes \; \phi_{g^*/B}$$

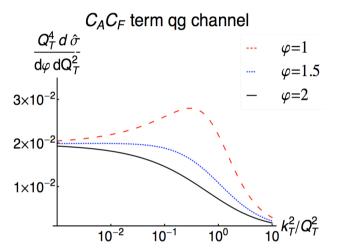
M. D., F. Hautmann, H. Jung, K. Kutak, JHEP 09, 121 (2009). 0908.0538

- Off-shell matrix element convoluted with unintegrated parton density functions (uPDFs)
- In Cascade done by generating emissions in a parton shower

# **Matrix element study**

 Some properties of the off-shell matrix elements of the relevant processes studied - decomposed into non-abelian and abelian part





- $qg^* \to qg$
- $gg^* \rightarrow gg$
- $gg^* \to q\bar{q}$

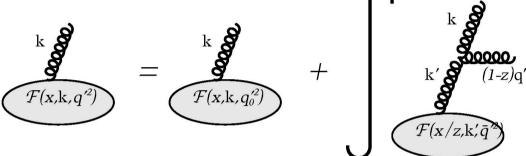
Q<sub>T</sub>=transversal energy in terms of final state pt's

- Dependence on transvrsal momentum of the off-shell gluon
- Dynamical cut-off at  $k_T \sim Q_T$  set by coherence effects
  - Non-negligible contribution from finite tail
- DGLAP based parton showers do not allow for such a hard emissions in the chain

M. D., F. Hautmann, H. Jung, K. Kutak, JHEP 09, 121 (2009). 0908.0538

## **CCFM** equation

- The CCFM equation
  - Includes BFKL kernel
  - Coherence effects
  - Angular ordering
- The equation



$$\mathcal{F}(x, \mathbf{k}, \mathbf{q'}^2) = \mathcal{F}(x, \mathbf{k}, \mathbf{q'}^2) + \int_{\mathbf{q'}^2}^{\mathbf{q'}^2} \frac{d^2 \bar{\mathbf{q}'}}{\bar{\mathbf{q}'}^2} \frac{N_C \alpha_S}{\pi}$$

$$\int_{x}^{1-\frac{Q_0}{|\mathbf{q'}|}} \frac{dz}{z} \mathcal{F}(x/z, \mathbf{k'}, \bar{\mathbf{q}}^{\prime 2}) \left( \frac{\Delta_{NS}(\mathbf{k'}^2, (z\bar{\mathbf{q}}^{\prime})^2)}{z} + \frac{1}{1-z} \right) \Delta_{S}(\mathbf{q'}_0^2, (z\bar{\mathbf{q}}^{\prime})^2)$$

- M. Ciafaloni, Nucl. Phys. B296, 49 (1988);
- S. Catani, F. Fiorani, and G. Marchesini, Phys. Lett. B234, 339 (1990);
- S. Catani, F. Fiorani, and G. Marchesini, Nucl. Phys. B336, 18 (1990);
- G. Marchesini, Nucl. Phys. B445, 49 (1995)

#### **CASCADE**

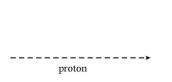
- Monte Carlo generator Cascade (H. Jung, Comput. Phys. Commun. 143, 100 (2002). hep-ph/0109102) - implementation of the CCFM equation
  - Backward evolution algorithm for initial state parton showers for
    - Exact kinematics in each step of the parton shower
    - No difference between parton shower evolved uPDF and CCFM evolved uPDF
    - Gluon chains
    - Valence quarks/Non-singlet uPDFs from one-loop CCFM equation
  - Final state parton showers by Pythia algorithm
  - Hadronisation of partons by the Lund String Model
  - Gluon uPDFs obtained from fits to HERA data

#### **Details of the convolution**

 The initial state off-shell gluon directly from the CCFM-parton shower-evolved uPDF

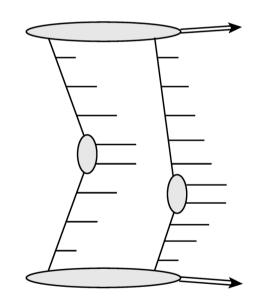
$$qg^* \to qg$$
$$gg^* \to gg$$
$$qq^* \to q\bar{q}$$

- On-shell parton obtained from CCFM evolved uPDF
  - Transversal momentum neglected in the matrix element of the hard subprocess, but included in the kinematics of the final state
  - $k_{\perp}$  integrated up to the hard scale given by the angle
  - Quarks evolved by one-loop CCFM: only valence component included

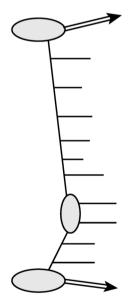


## High energy factorisation and MPI

- 1. MPI effectively generate certain amount of pt-non-ordering of showered partons
- 2. MPI increase the jet multiplicity of the parton showers
- 3. MPI increase the number of hard jets in the process
- pt-unordered parton showers (1.) increase jet Multiplicity (2.) and number of hard jets (3.)
- Natural to compare MPI with pt-unordered parton
  Showers
- Different mechanisms



multiple pt-ordered chains



one pt-unordered chain

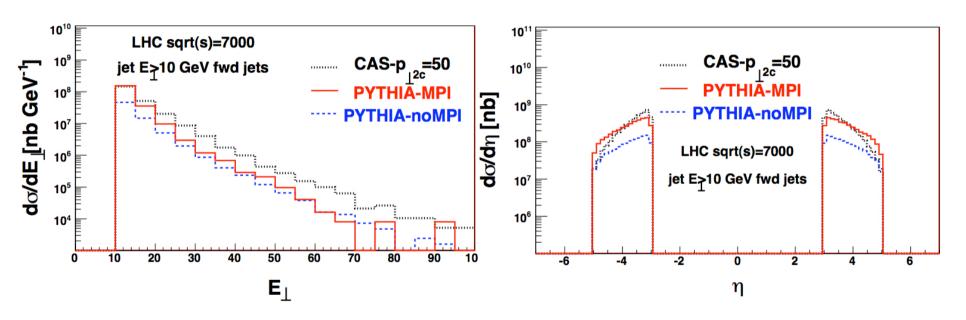
#### Phenomenological results

#### Parameters and settings

- Hard matrix elements included in Cascade MC generator:
  - gluon uPDFs fitted from HERA data
  - quark CTEQ6.0 PDF evolved by CCFM
- Pythia settings: CTEQ 5L PDFs
  - q<sup>2</sup> ordering for initial state parton shower, with and without MPI
- Jets on parton level; jet algorithm kt-clus
- Forward jets rapidity:  $-3 < \eta < -5$
- Central jets rapidity:  $-2 < \eta < 2$
- E<sub>⊥</sub>>10 GeV

## Pt and rapidity spectra of forward jets

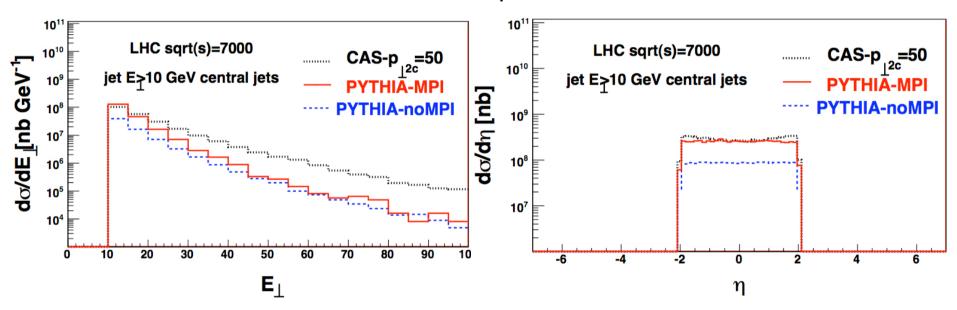
Forward jet  $-3 < \eta < -5$ 



- Different slopes of cross sections
- $k_T$  of incoming gluon allows for harder spectrum CCFM parton showers not ordered in  $k_T$
- MPI only shift the jet rapidity cross section by a factor

## Pt and rapidity spectra of central jets

Central jet  $-2 < \eta < 2$ 



- Different slopes of cross sections
- $k_T$  of incoming gluon allows for harder spectrum CCFM parton showers not ordered in  $k_T$
- MPI only shift the jet rapidity cross section by a factor
- Rapidity cross sections agree for central rapidity region

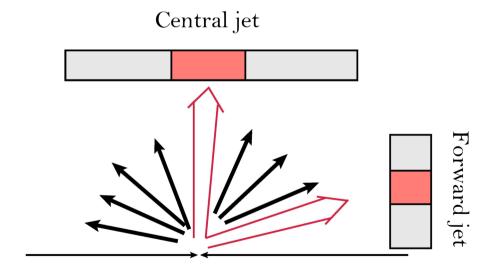
# Phenomenological results

- Select:
  - a central jet  $-2 < \eta < -1$
  - and a forward jet  $4 < \eta < 5$
- Looking at:
  - particle flow and minijets

particle flow and minijets

away from jets

between the jets



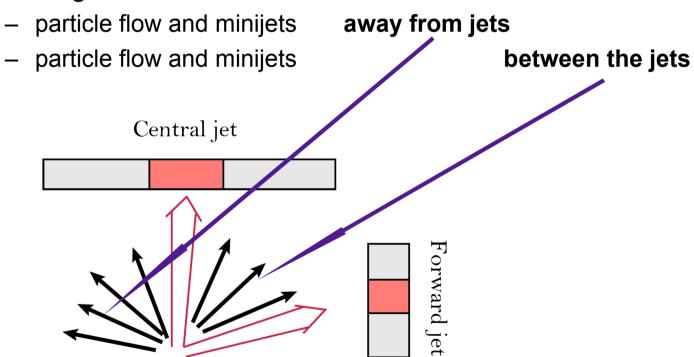
# Phenomenological results

• Select:

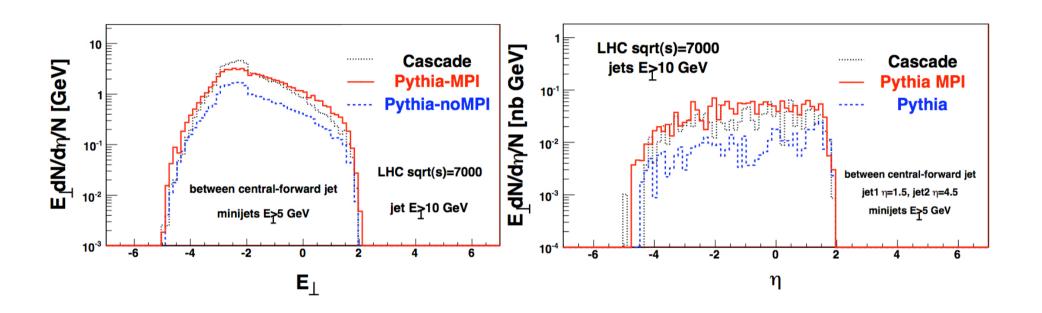
- a central jet  $-2 < \eta < -1$ 

- and a forward jet  $4 < \eta < 5$ 

Looking at:

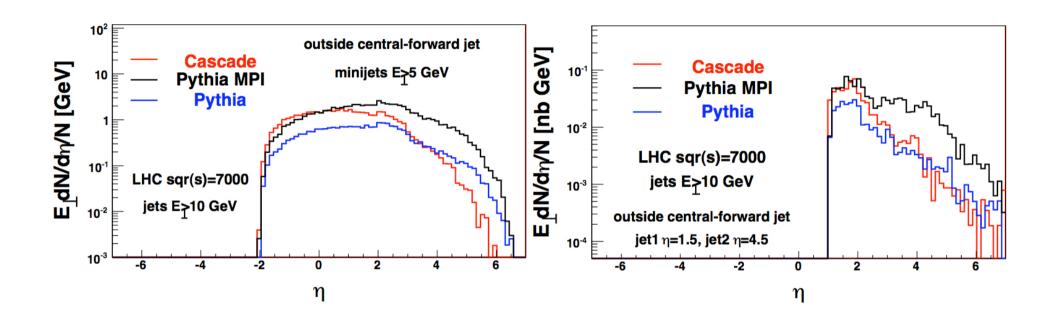


# Minijet and particle energy flow between central and forward jet



• Both MPI and high energy factorisation produce more jets with higher transversal energy

# Minijet and particle energy flow away from central and forward jet



 Both MPI and high energy factorisation produce more jets with higher transversal energy

## Forward jets - Summary

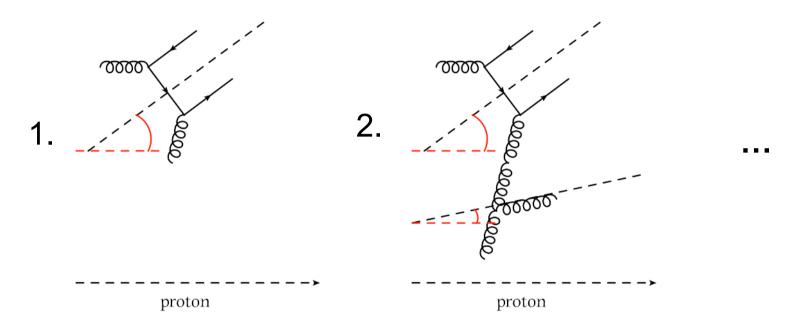
- Calculations of gauge invariant matrix elements of relevant processes in Monte Carlo implementation suitable form
- Convolution with the uPDFs in Monte Carlo generator CASCADE
- Study of jet transversal energy and rapidity cross sections of forward jets and a central jet
- Comparison with PYTHIA Monte Carlo generator with multiparton interactions (MPI)
- Difference between the high energy factorisation enhanced jet activity and MPI jet activity

#### **Conclusions**

- LHC opens phase space for large center of mass energies and for presence of multiscales
- This brings perturbative corrections which are summed up by high energy factorisation
- An approach which allows for studies of forward jets at the LHC
- Proposal of observables which allow for discrimination between different approaches

#### **CASCADE**

 The largest angle = the angle of the hard subprocess final state system



Angular ordering for small angles

$$\frac{|\mathbf{q}_i|}{1 - z_i} > \frac{z_{i-1}|\mathbf{q}_{i-1}|}{1 - z_{i-1}}$$