

Hadron production spectra in Collider Experiments

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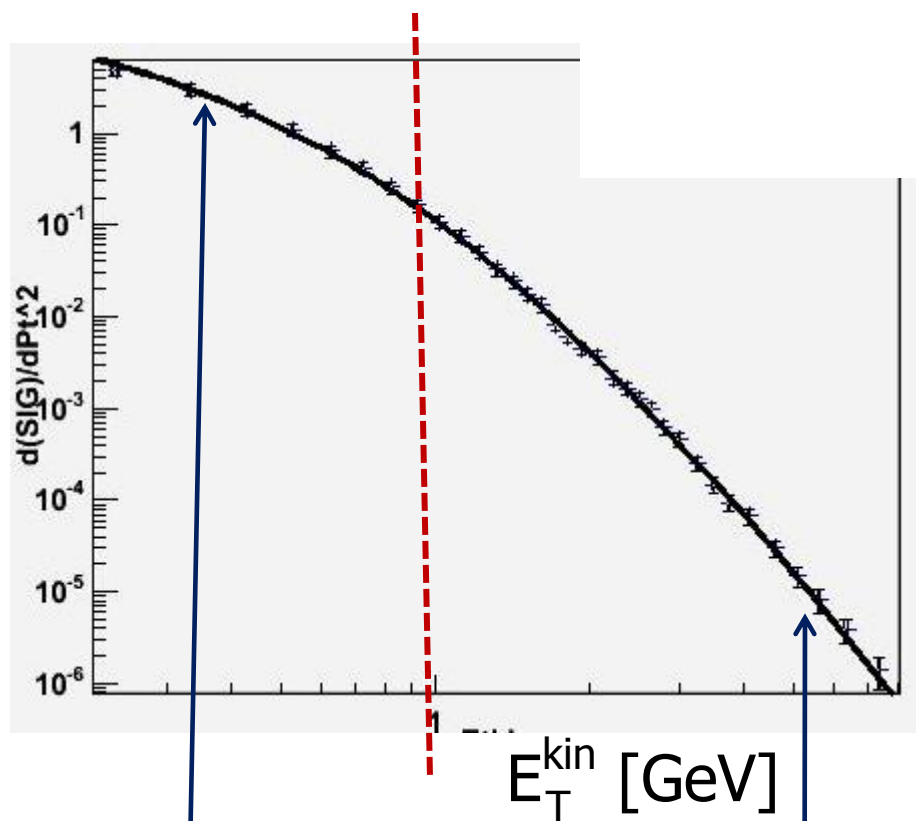
Moscow, ITEP

There exists a large body of high precision experimental data on hadron production in high energy particle collisions.

| Collisions | Energy Range | Experiments |
|-----------------|---|---------------------|
| Proton – Proton | 23 – 2360 GeV | ISR, SppS, CDF, CMS |
| Gamma - Proton | 200 GeV | H1, ZEUS, Omega |
| Gamma - Gamma | 100 GeV | Opal, L3 |
| DIS | 120 – 213 GeV $7 < Q^2 < 28 \text{ GeV}^2$ | H1, ZEUS |
| Aurum - Aurum | 200 GeV | RHIC |

Transverse Momentum Spectra of Charged Particles

(Differential Invariant Cross-Section)



Nonperturbative
thermodynamics

pQCD

$$E \frac{d^3 \sigma}{d^3 p} (y \approx 0) = \frac{A}{\left(1 + \frac{E_T^{kin}}{T \cdot N}\right)^N}$$

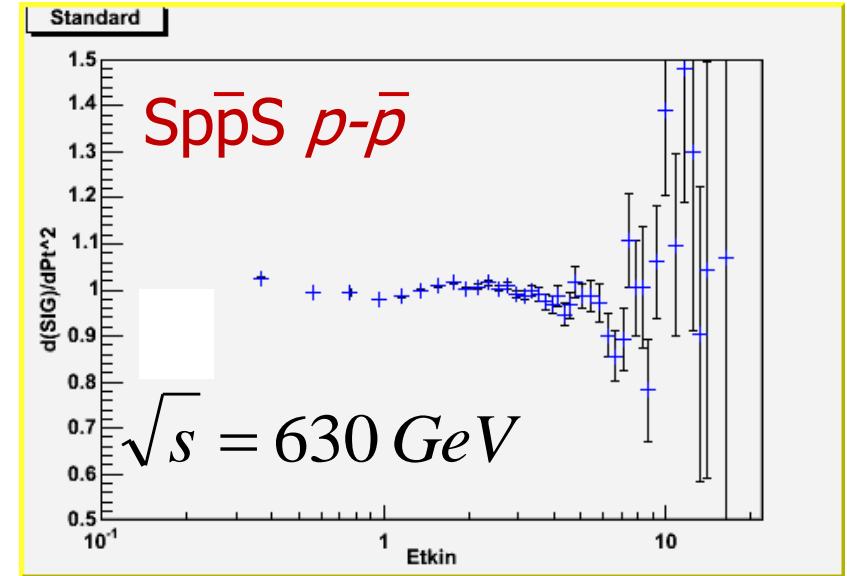
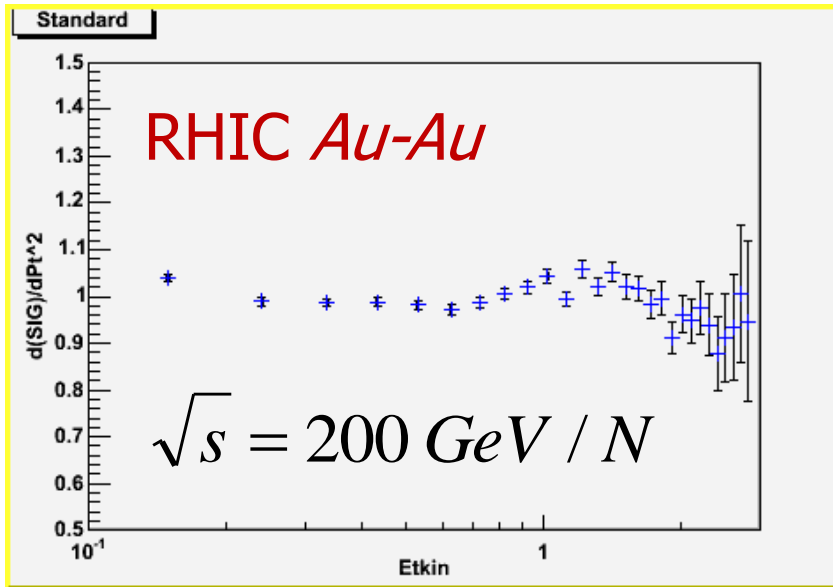
$$E_T^{kin} = \sqrt{p_T^2 + m_\pi^2} - m_\pi$$

A single smooth
Tsallis-type function
for the whole
kinematical region

*A common statistical
distribution in the Nature.*

Does Tsallis-type power law distribution really describe the hadron production spectra?

To answer this question let's plot a ratio = data / fit function



On both plots one observes a shallow dip at E_{T} values below 1 GeV followed by a broad bump above 1 GeV.

These defects are hidden on usual logarithmic plots!

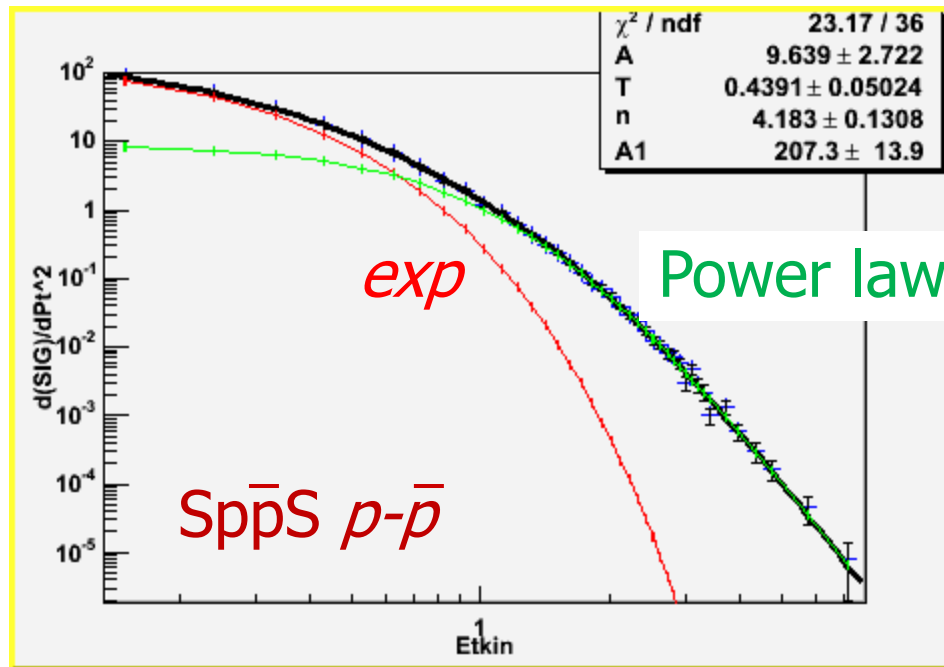
Observed systematic defects require to modify the fit function

A modification of the Tsallis function

Take two contributions: Exponential + Power law functions

Generalized forms: $\exp(-F(P_T)/T_e)$ $1/(1 + F'(P_T)/TN)^N$

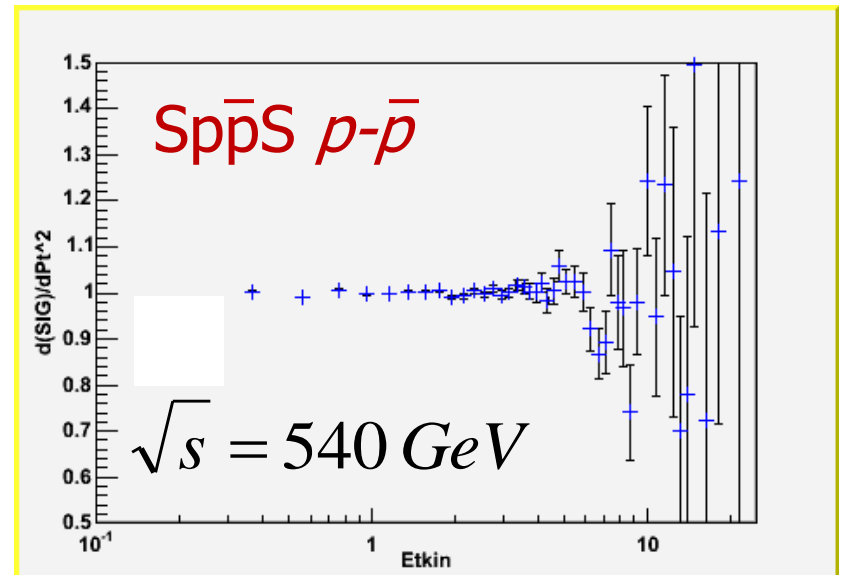
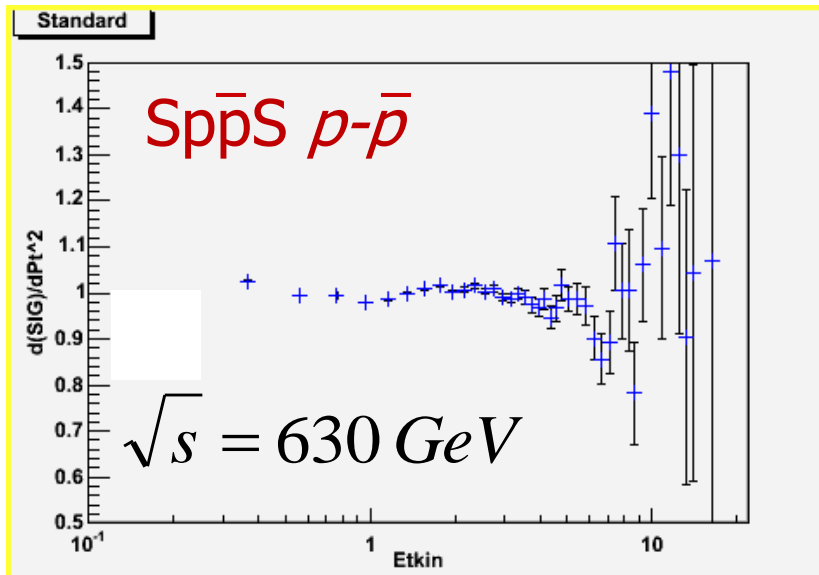
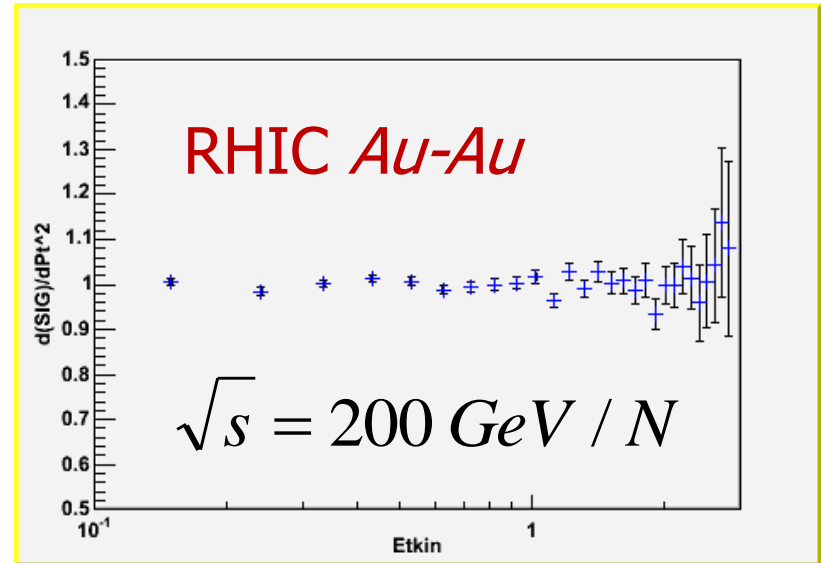
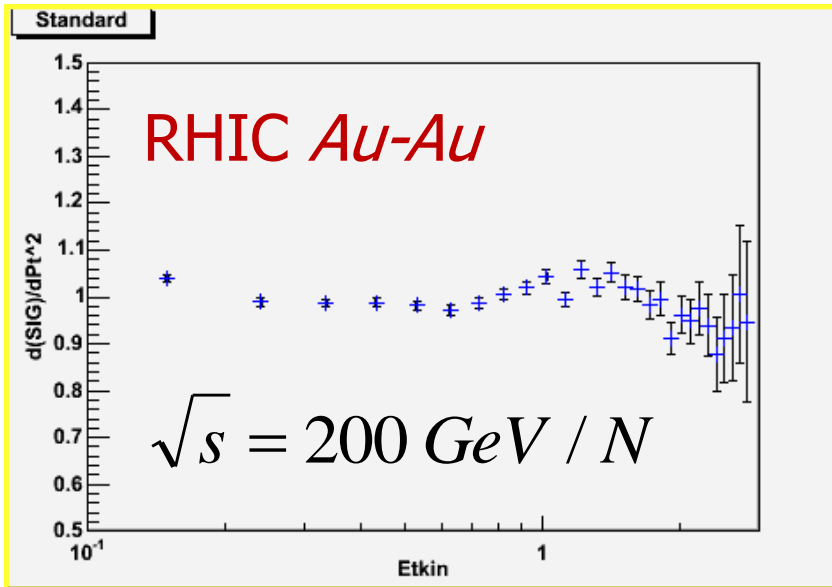
With scalar $F, F' = P_T^2$ or E_T^{kin} (not P_T or P_T^3)



The best fits are given by

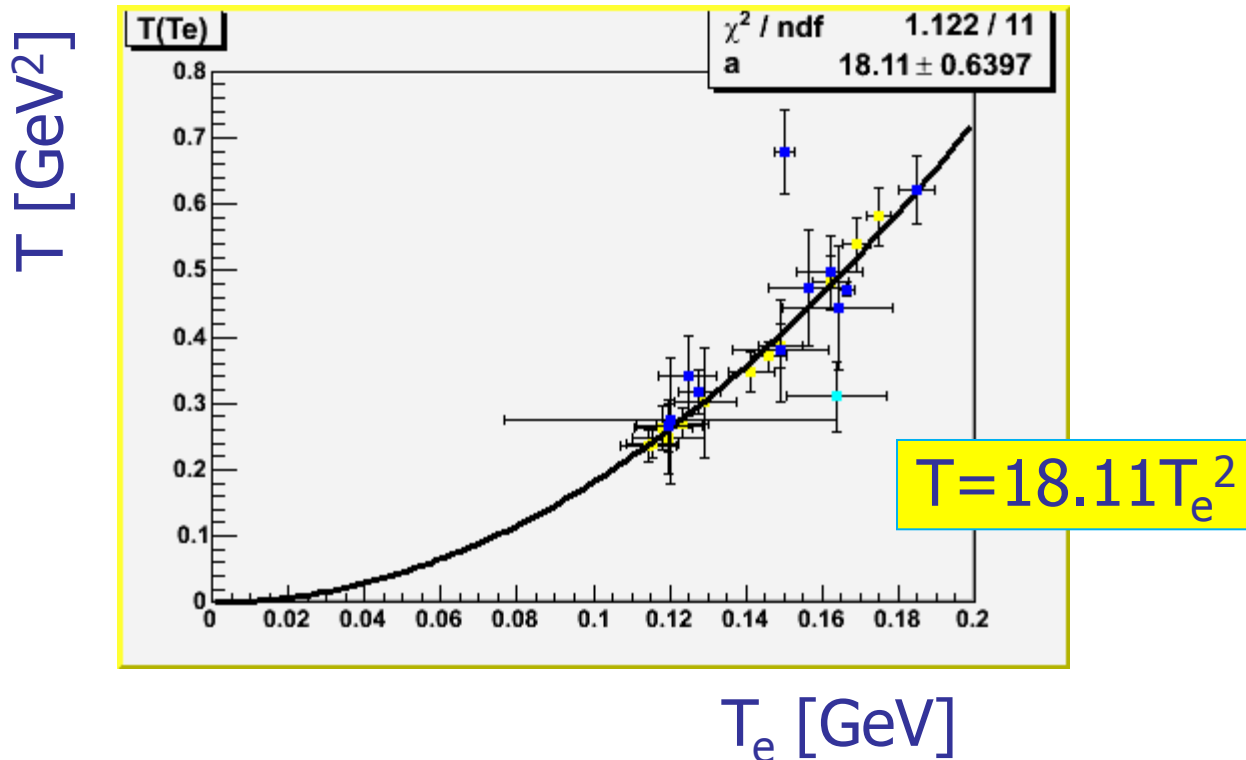
$$A_e \cdot \exp(-E_T^{kin} / T_e) + A / (1 + P_T^2 / TN)^N$$

Look back at the Ratios = data / fit function



A strong correlation between the fit-function parameters

Fit-function: $A_e \cdot \exp(-E_T^{kin} / T_e) + A / (1 + P_T^2 / TN)^N$



The observed correlation might indicate that the exponential and power law terms are integral parts of more complicated function describing the statistical distribution.

Modified spectrum fit-function. Interpretation.

Exponential term – “thermolized” hadrons, or a hadronic cloud accompanying the interactions. Boltzmann-type.

Power-law term – originates from partonic hard interactions?

The modified function could be rewritten as:

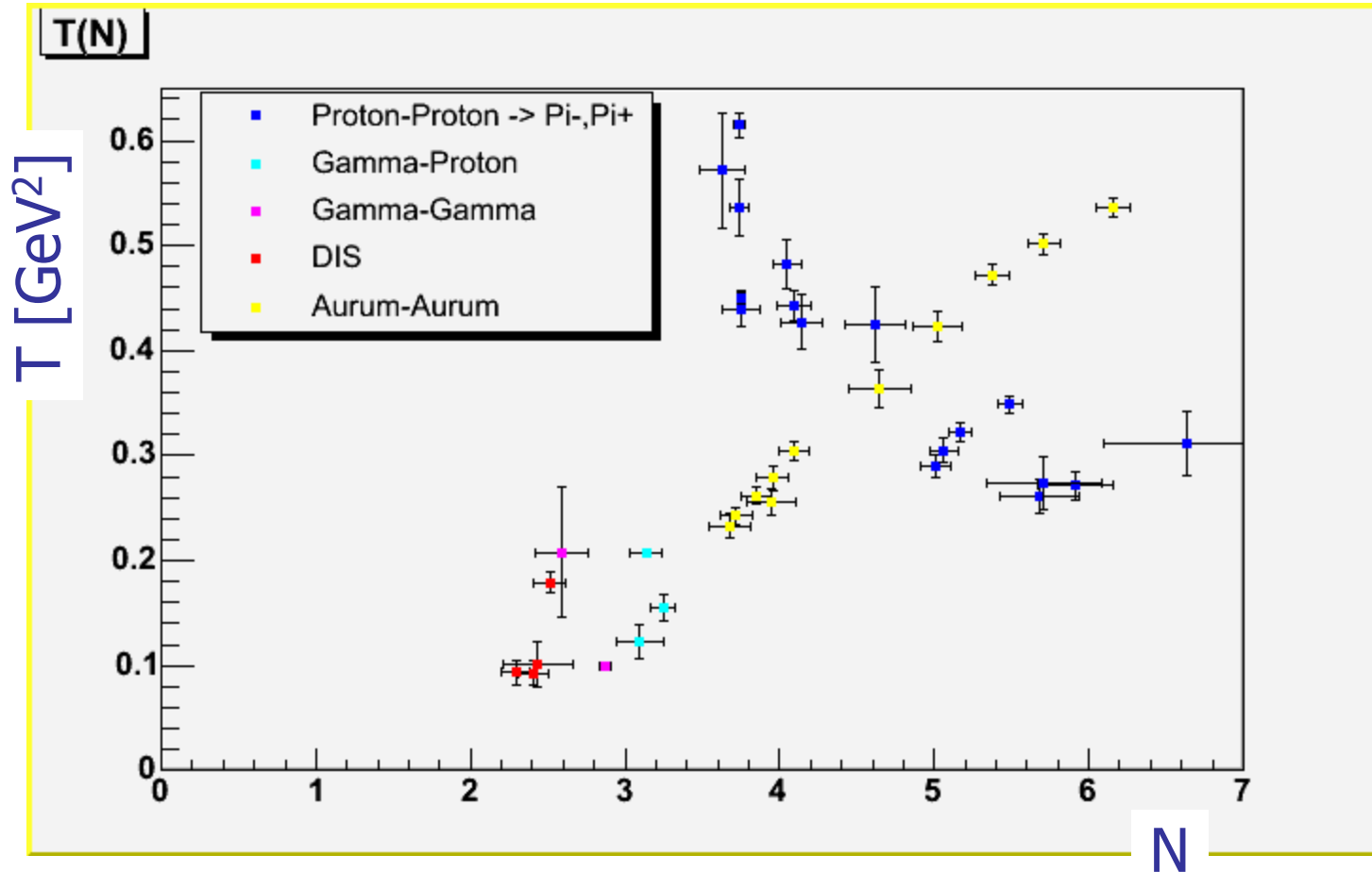
$$\begin{aligned}\frac{d\sigma}{dP_T^2}(y \approx 0) &= A_e \cdot \exp(-E_T^{kin} / T_e) + A / (1 + P_T^2 / TN)^N = \\ &= A_e \cdot \exp(-\varepsilon) + A / (1 + \varepsilon^2 / bN)^N\end{aligned}$$

$$\text{with } \varepsilon = \frac{E_T}{T_e}$$

The fit-function parameter map

$$\frac{d\sigma}{dP_T^2} = A_e \cdot \exp(-E_T^{kin} / T_e) + A / (1 + P_T^2 / TN)^N \quad \leftarrow$$

$$T = 18.11 T_e^2$$



Observations made with the fit parameter map

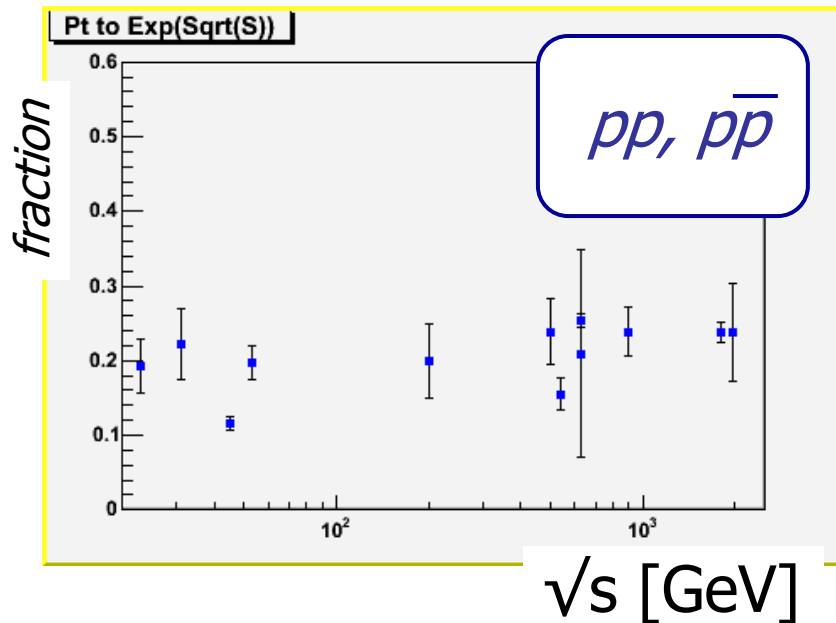
1. There are two distinct trends:
 - with change of \sqrt{s} in pp
 - for different colliding particles and fixed \sqrt{s}
2. The two trends cross each other in a point
 - with $\sqrt{s} = 200$ GeV in pp and Au-Au
 - for minimum bias centrality in Au-Au
3. DIS, γp , $\gamma\gamma$ sit on the same band as Au-Au with different centralities and look similar to very peripheral Heavy Ion interactions

Surprise:

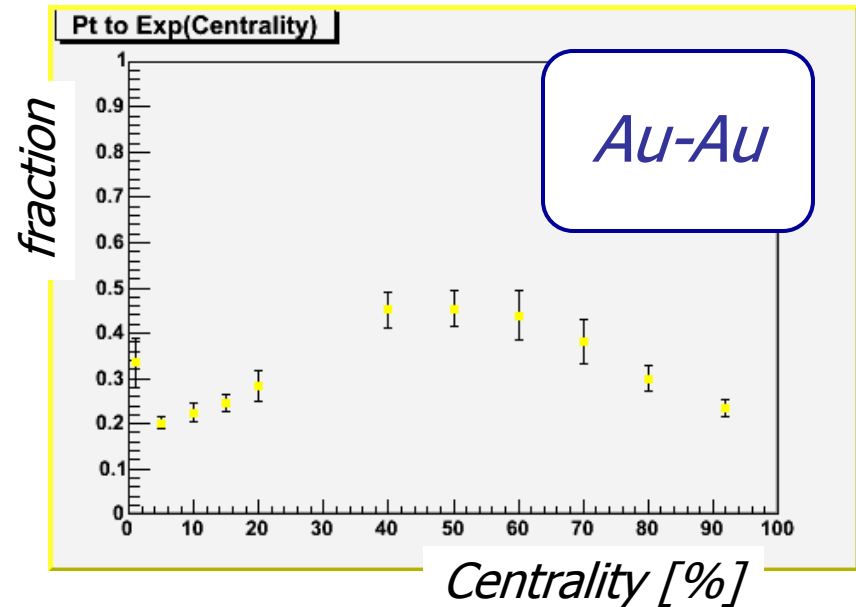
Heavy Ion low centrality (multiplicity) presumably very peripheral interactions differ significantly from single pp-interactions and at the same time are "close relatives" of interactions with photons.

Further observations: relative contributions of the exponential and power-law terms in the spectra

Power law term fraction in pp spectra as function of \sqrt{s}

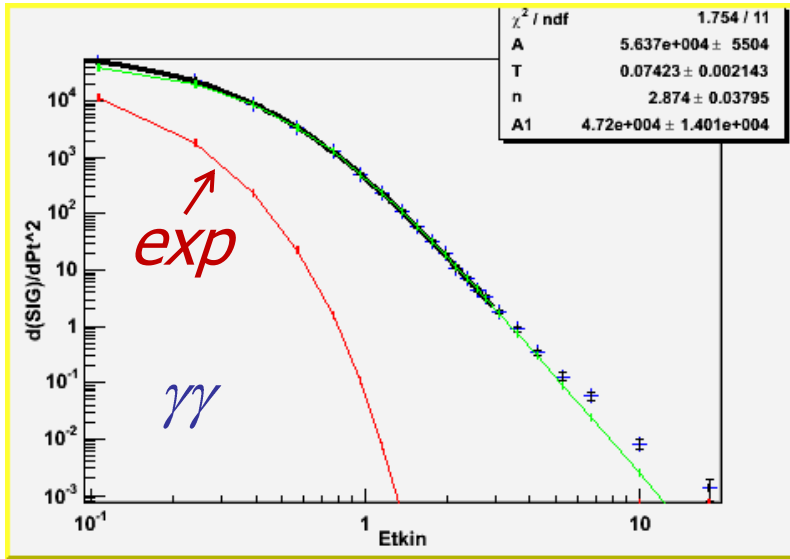


Power law term fraction as function of centrality in Au-Au at $\sqrt{s}=200$ GeV

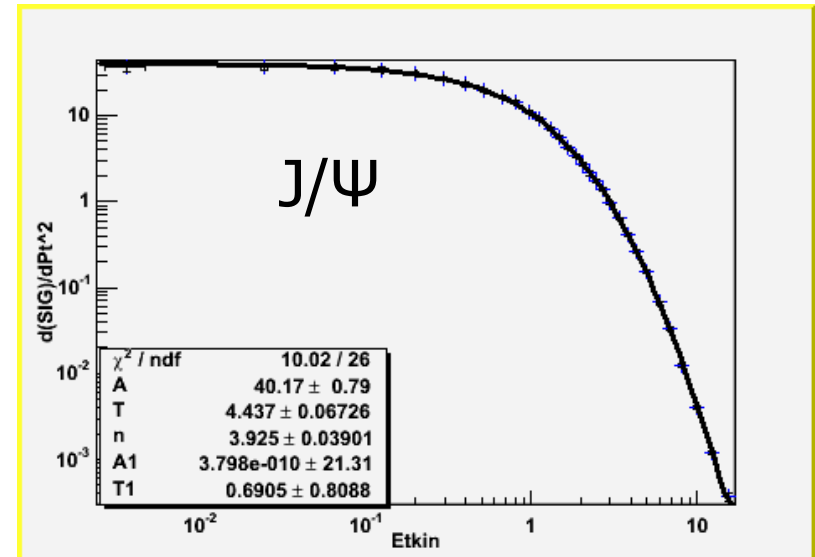
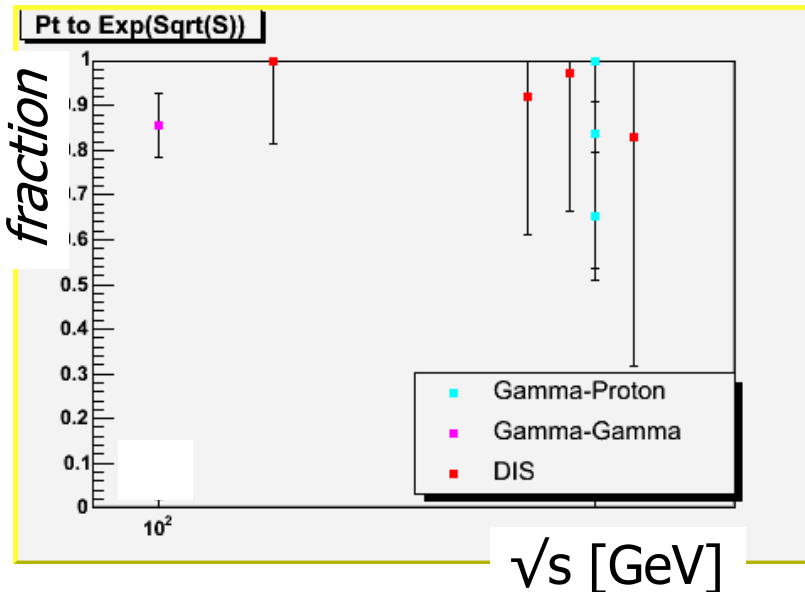


- In pp interactions: exp / power-law ≈ 4 independent of \sqrt{s}
- Power-law fraction has maximum at mid centralities in Heavy Ion int.
- What is about "point-like" interactions?

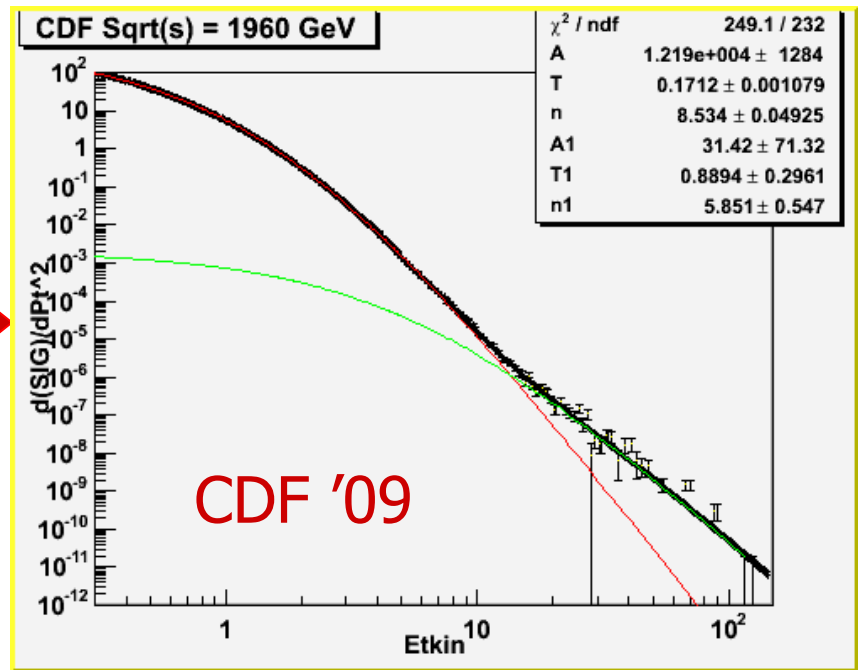
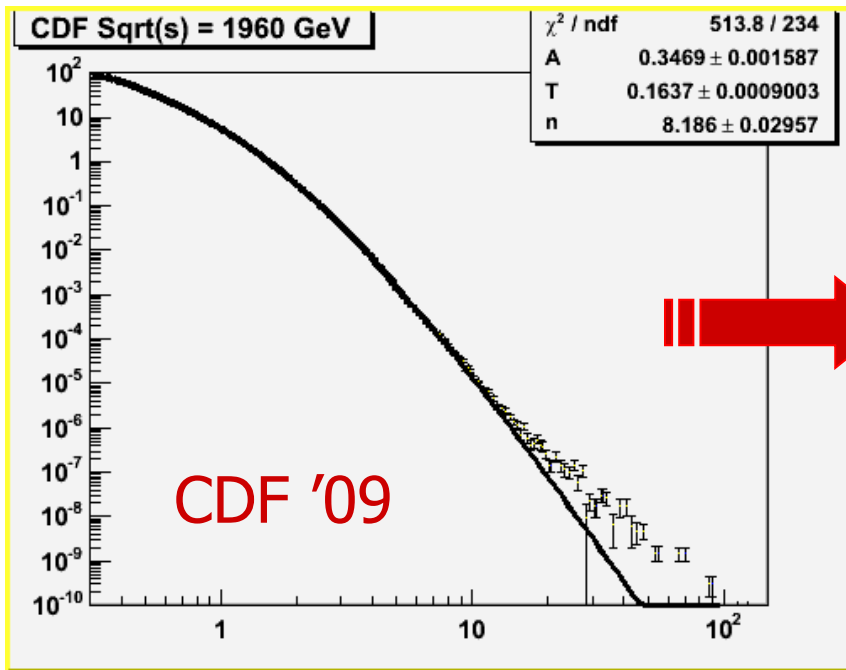
In DIS, γp , $\gamma\gamma$ the power-law contribution dominates ($\sim 100\%$)



Inclusive J/ψ production doesn't leave any room for the exponential term in the spectrum shape



More surprises in high-Pt data



$$\chi^2/\text{ndf} = 513.8/234$$

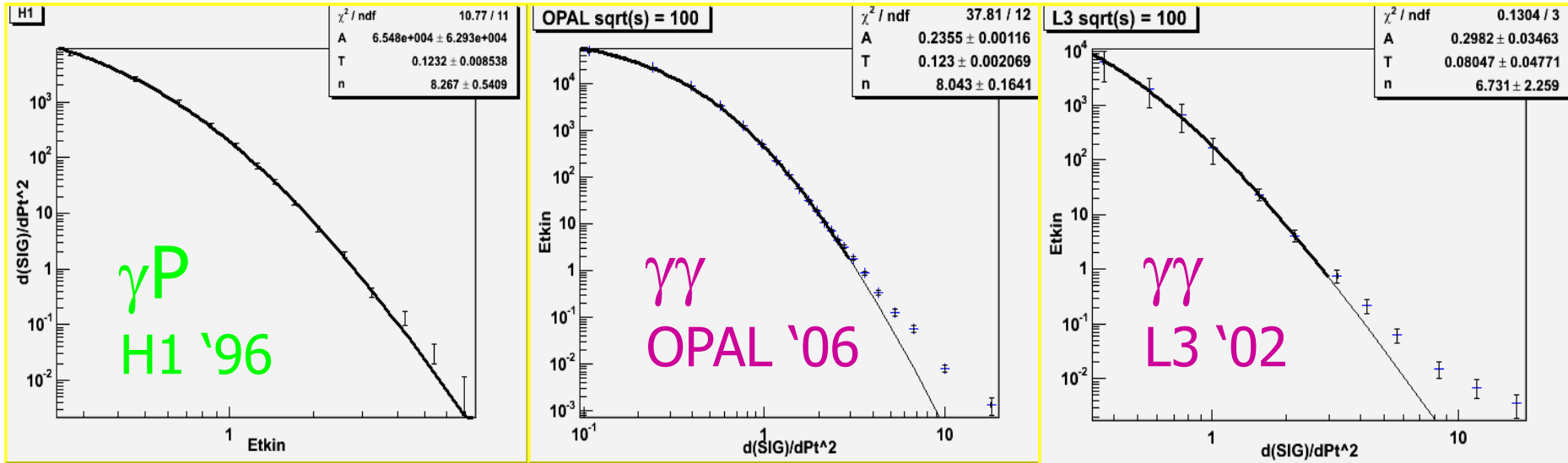
$$\chi^2/\text{ndf} = 249.1/232$$

$$\frac{d\sigma}{dP_T^2} = A_1 \cdot (1 + E_T^{\text{kin}} / T_1 / N_1)^{N_1} + A_2 \cdot (1 + E_T^{\text{kin}} / T_2 / N_2)^{N_2}$$

$$A_1 / A_2 \approx 10^3; \quad T_1 = 0.17 \quad T_2 = 0.89 \text{ GeV}; \quad N_1 = 8.5 \quad N_2 = 5.8$$

For $P_T > 80 \text{ GeV}$ is of order of inclusive jet cross section Only at CDF?

The onset of high- P_T power-law tail in gamma collisions



The onset of the high- P_T power-law term is visible for:

$P_T > 10$ GeV in pp - collisions

$P_T > 4$ GeV in γp - collisions

$P_T > 3$ GeV in $\gamma\gamma$ - collisions

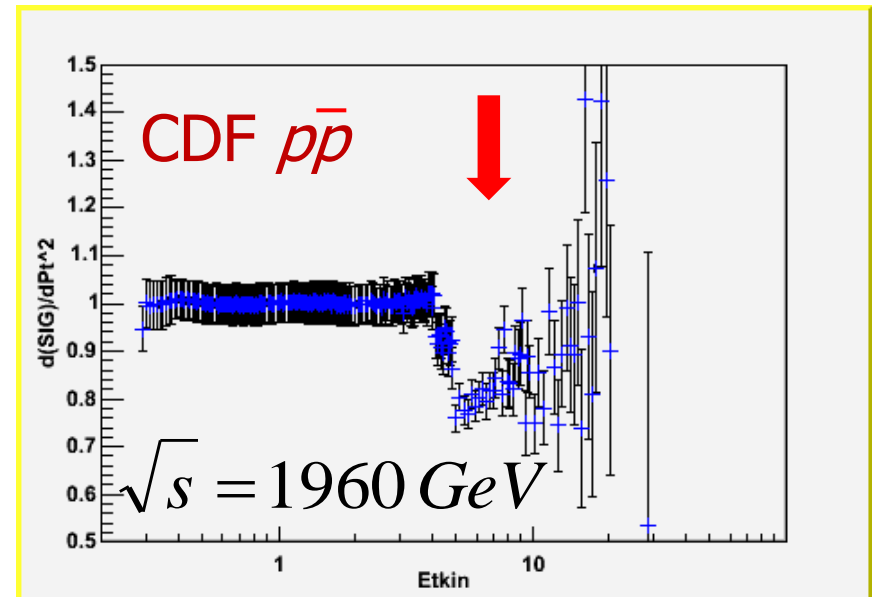
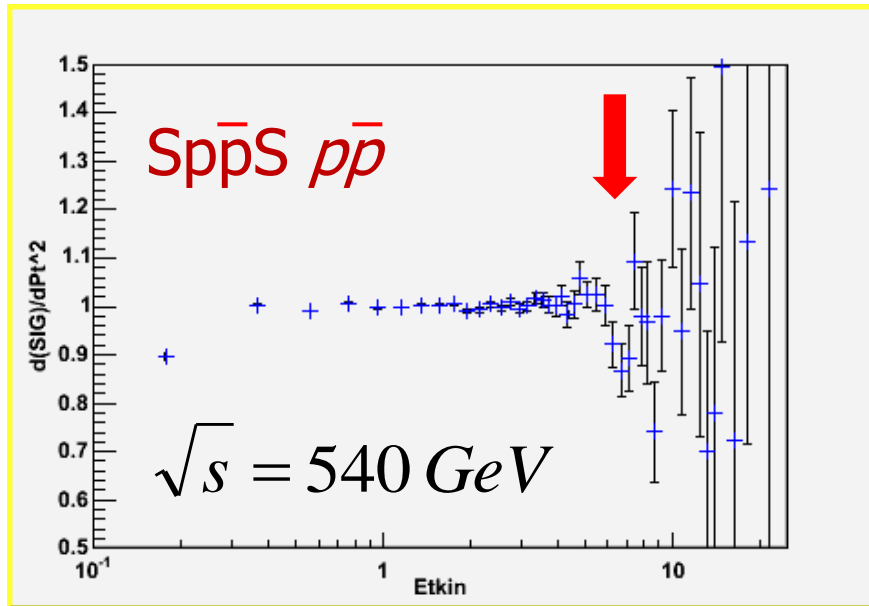
Disagreement with CDF jet spectrum & Fragmentation (A.S.Yoon et al)

Two different regimes for charged hadron production?

Diffraction-type dips in the inclusive particle spectra?

Provocative examples of the data to fit ratio:

The only two accurate sets of pp -data extended to high P_T



Looking forward to see the LHC (7 GeV) spectra soon.

Conclusions:

- the large body of high precision data on hadron production in collider experiments allow systematic measurements of the fine details of the spectra shape;
- a simple power law type statistical distribution (Tsallis, kappa, Levy,...) provides a good approximation, but fail to describe the details of spectra shape both at low and high P_t ;
- a modified statistical distribution is proposed
- despite the hadron spectra have been studied for decades, there is a number of puzzles to be solved:
 1. *Hadron production parameter map*
 2. *High P_T tails*
 3. *Dips*

Wanted:

High statistics LHC charged particle spectra.