

PITT-PACC Workshop: Muon Collider Physics

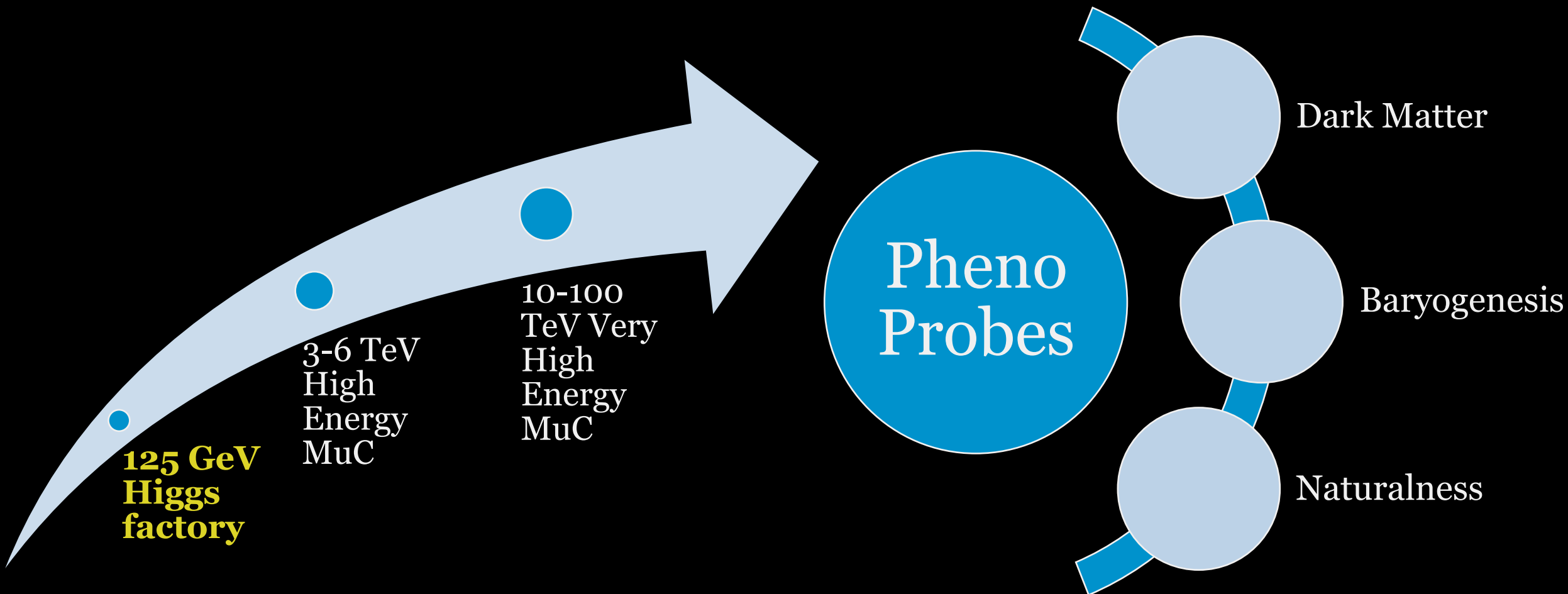
Physics at Higgs factories



Zhen Liu
University of Maryland
(→University of Minnesota)
12/01/2020

Exciting Muon Collider Program ahead

Physics Driver

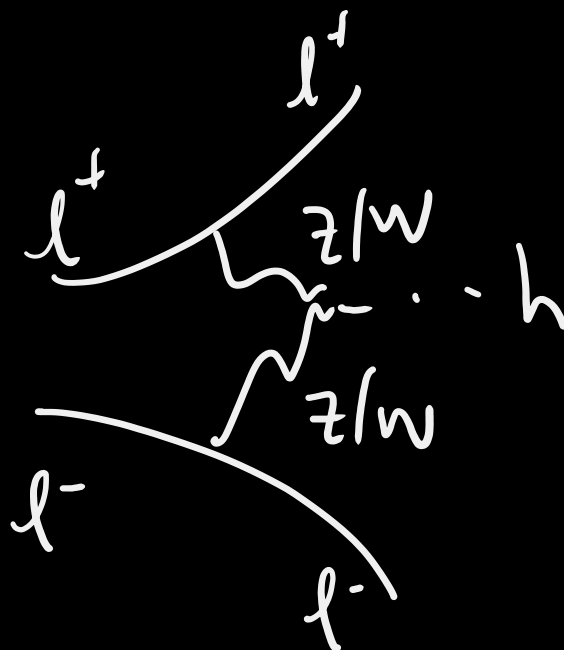
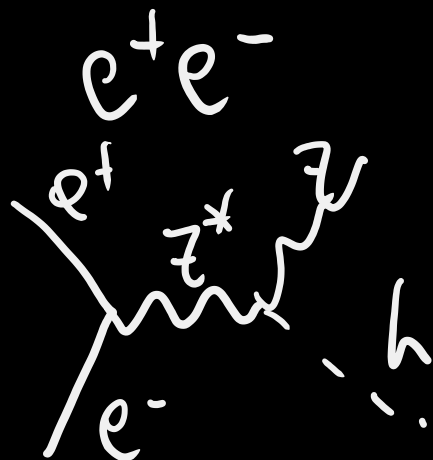
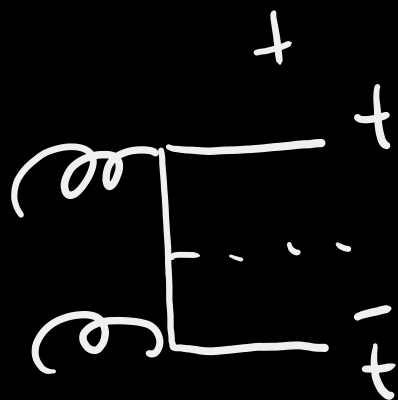


Every future collider is a Higgs factory!

PP



+
VBF, Wh, Zh, hh



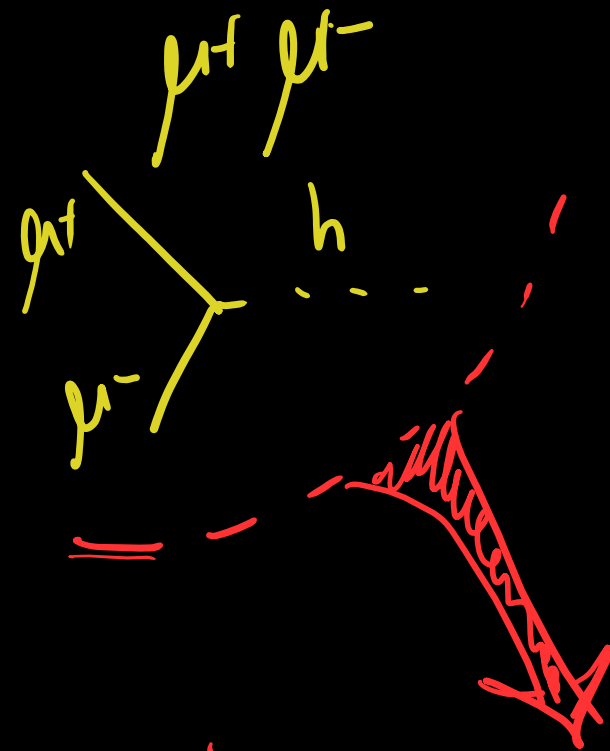
LEAST understood
FOCUS of this
talk

Outline

- Overall picture
- Higgs Width
- Higgs Couplings
- Higgs Exotic Decays

Mark Palmer's talk (as well as talks by Diktys Stratakis, Daniel Schulte, Nadia Pastrone) nicely addressed the technological status of a 125 GeV Higgs factory.

Here I focus on the **unique physics capabilities**.



LEAST understood
FOCUS of this
talk

Basics:

clean lepton collider environment matters!

pp

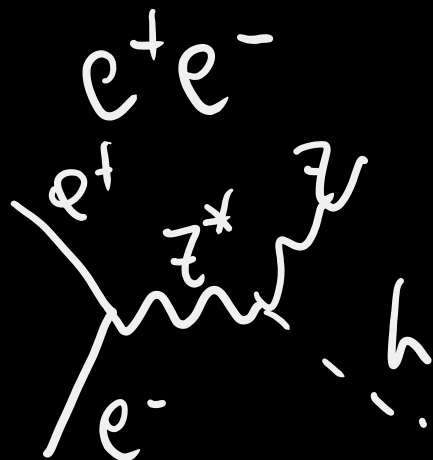


LHC 14 TeV

50 pb

3 ab⁻¹

0.15 billion Higgs

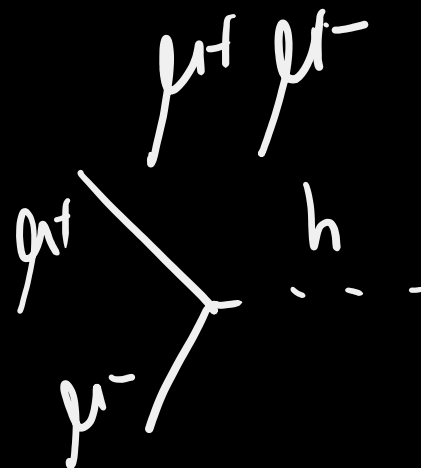


e⁺e⁻ 240~280 GeV

200 fb

5 ab⁻¹

1 million Higgs



μ⁺μ⁻ 125 GeV

20 pb

1 fb⁻¹

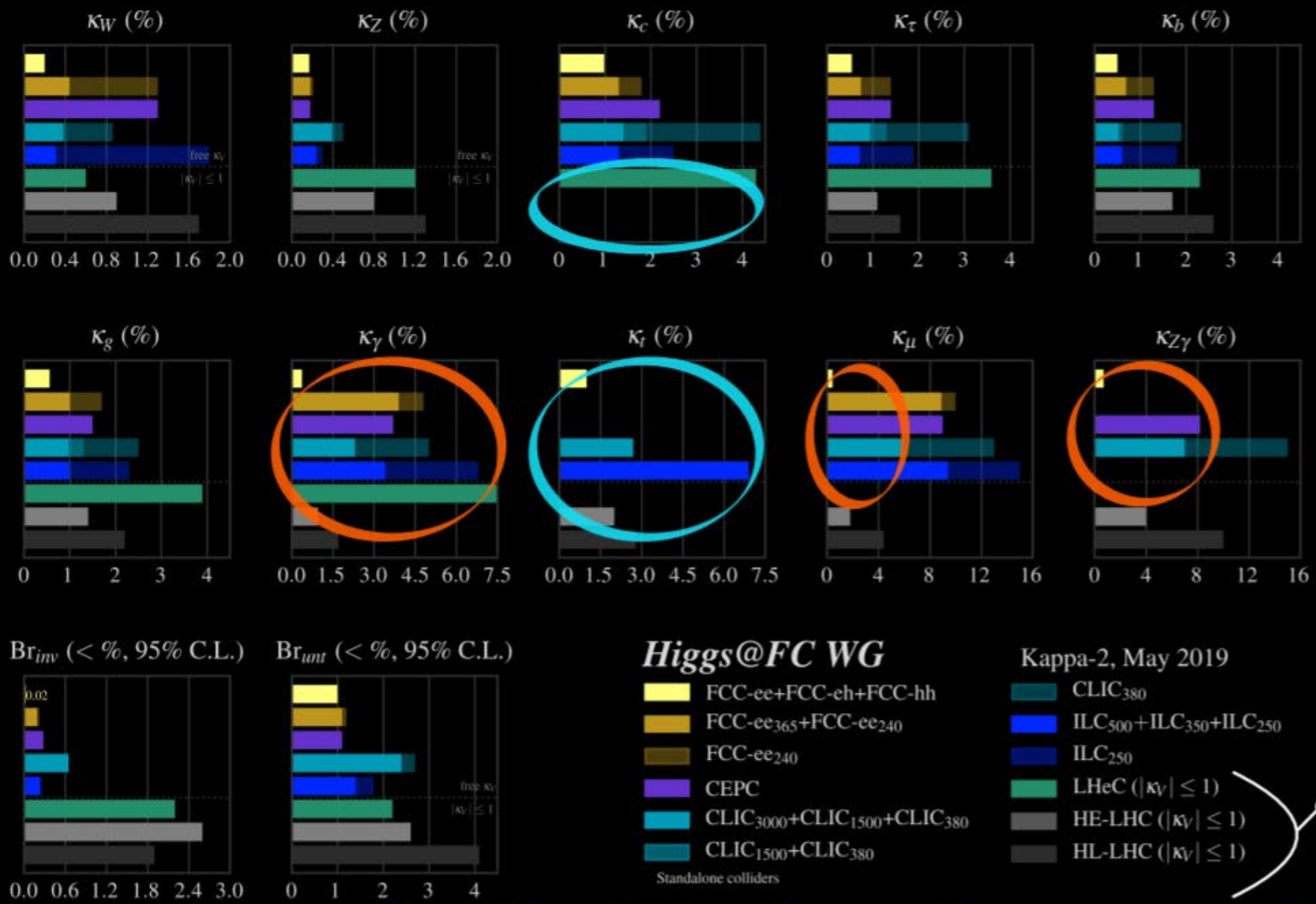
20 thousand Higgs

Higgs Coupling Fit (Future Collider Standalone)

ECFA Higgs study group '19

Scenario	BR_{inv}	BR_{unt}	include HL-LHC
kappa-2	measured	measured	no

hadron collider cannot measure width
need an assumption to close the fit
e.g. $k_V < 1$

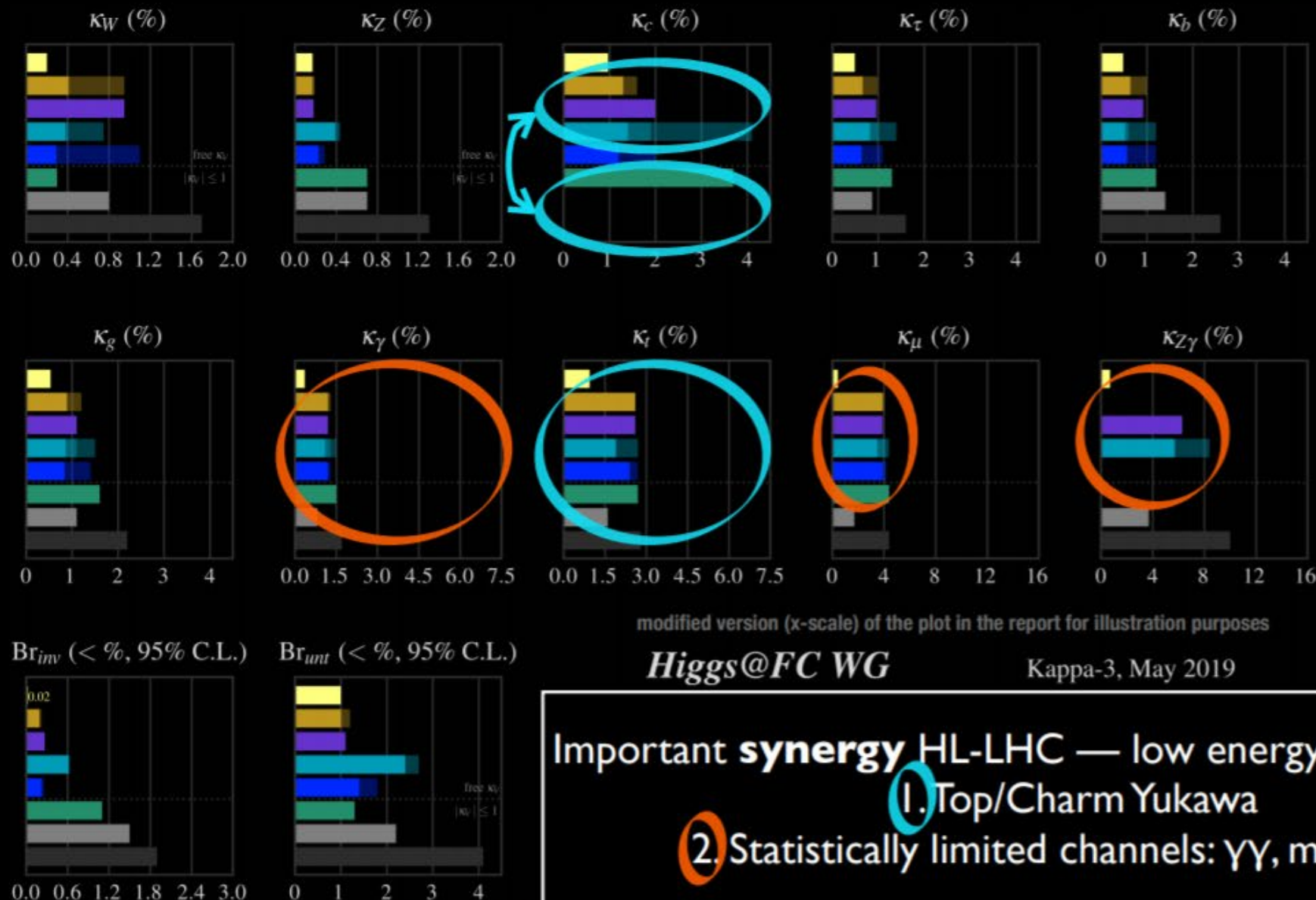


assumption
needed for the fit
to close at hadron
machines

Higgs Coupling Fit (HL-LHC+Future Collider)

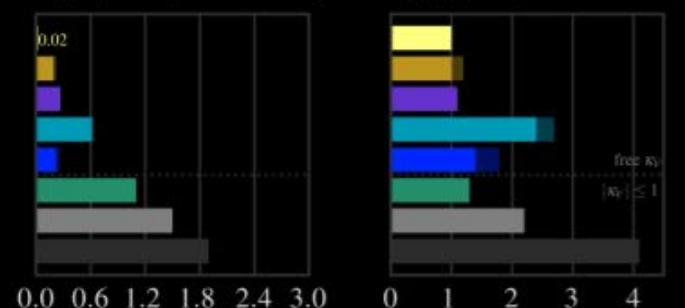
ECFA Higgs study group '19

Scenario	BR_{inv}	BR_{unt}	include HL-LHC
kappa-3	measured	measured	yes



Synergy ee-hh

$Br_{inv} (< \%, 95\% \text{ C.L.})$ $Br_{unt} (< \%, 95\% \text{ C.L.})$



Higgs@FC WG

FCC-ee+FCC-eh+FCC-hh
 FCC-ee₃₆₅+FCC-ee₂₄₀
 FCC-ee₂₄₀
 CEPC
 CLIC₃₀₀₀+CLIC₁₅₀₀+CLIC₃₈₀
 CLIC₁₅₀₀+CLIC₃₈₀
 All future colliders combined with HL-LHC

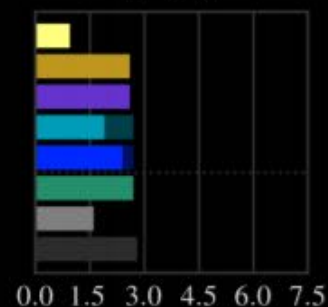
Kappa-3, May 2019

CLIC₃₈₀
 ILC₅₀₀+ILC₃₅₀+ILC₂₅₀
 ILC₂₅₀
 LHeC ($|\kappa_V| \leq 1$)
 HE-LHC ($|\kappa_V| \leq 1$)
 HL-LHC ($|\kappa_V| \leq 1$)

FCC-hh without ee could still bound Br_{inv}

but it could say nothing about Br_{unt}

κ_t (%)

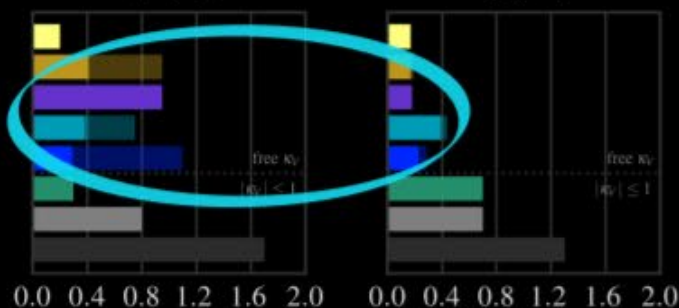


FCC-hh is determining top Yukawa through ratio $t\bar{t}h/t\bar{t}Z$

So the extraction of top Yukawa heavily relies on the knowledge of $t\bar{t}Z$ from FCC-ee

κ_W (%)

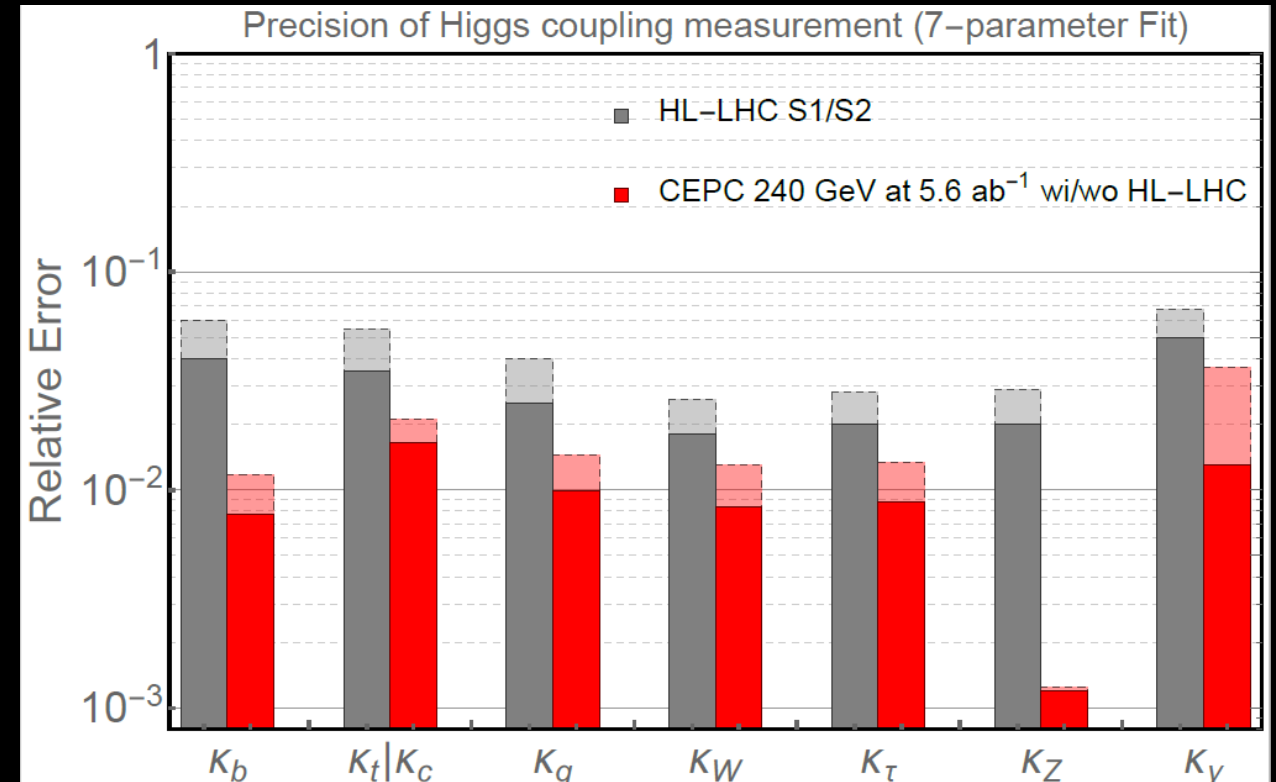
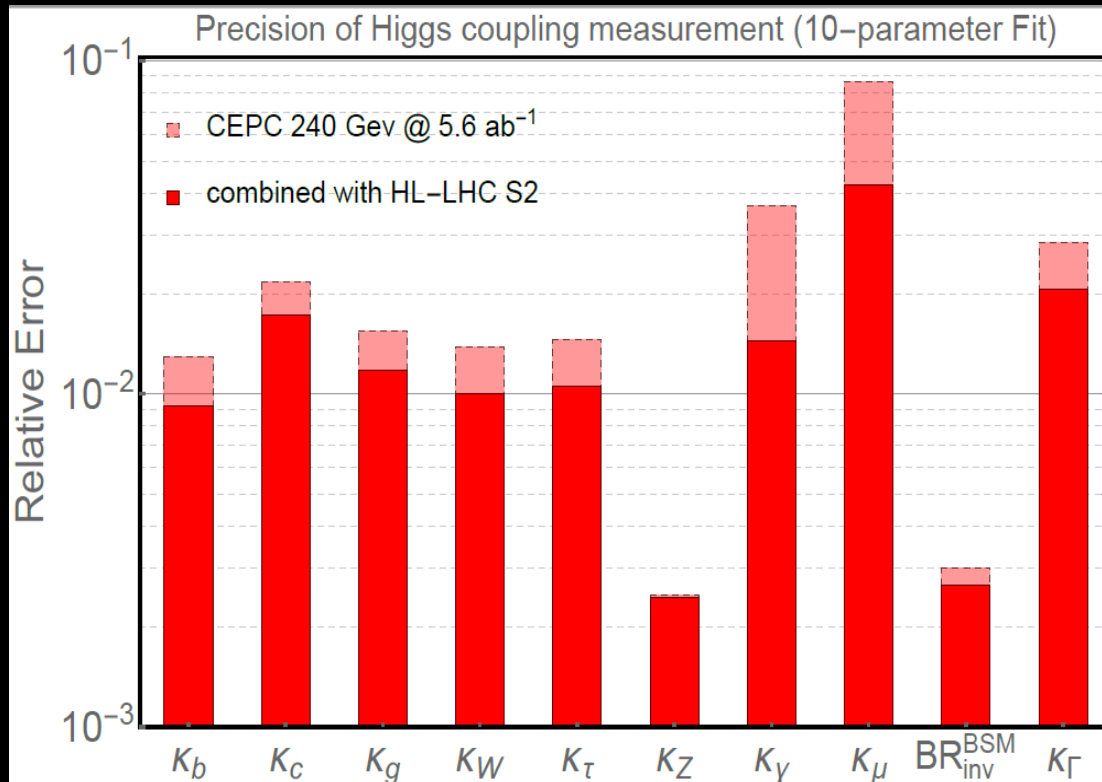
κ_Z (%)



κ_W improves significantly with energy increase

But it also benefits a lot from a synergy with EW measurements. This cannot be captured by the kappa's and requires a full EFT analysis

Switch to a representative view (CEPC/FCC-ee/ILC)



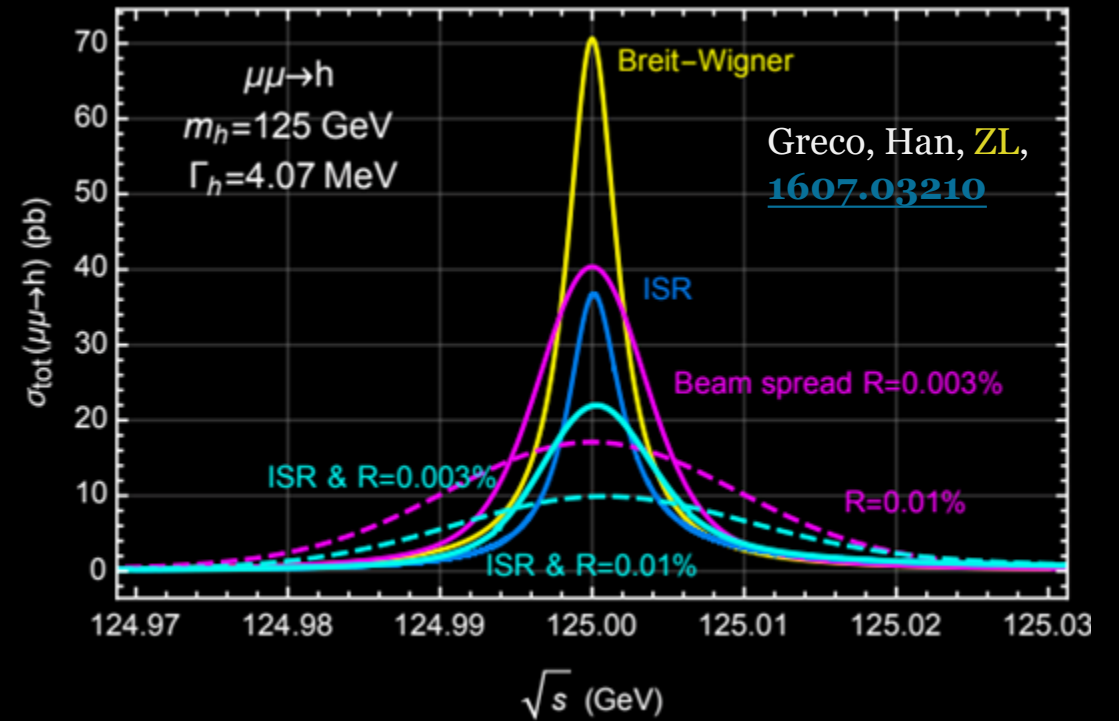
Without external constraints on the coupling strength (width), HL-LHC fit has huge flat direction (the fit does not close)*

*since LHC width measurement is poor, putting a universal floor of around 10%~20% for LHC measurements interpreted in this framework, assuming additional input from off-shell ZZ measurements to bound the Higgs total width)

Higgs factories improves in b, c, g, W, and especially Z coupling.
HL-LHC provide crucial inputs for muon Yukawa, Higgs to $\gamma\gamma$, etc.

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Measurements to be interpreted

Observables at the colliders are the cross sections, a convolution of PDF (including CEPC, treating the beam energy spread), hard scattering, parton shower, detector response ...

For the hard scattering*:

$$\kappa_i = \frac{g_i}{g_i^{SM}}, \kappa_\Gamma = \frac{\Gamma_{tot}}{\Gamma_{tot}^{SM}}$$

$$\sigma(i \rightarrow H \rightarrow j) \propto \frac{\Gamma_i \Gamma_j}{\Gamma_{tot}} \propto \frac{\kappa_i^2 \kappa_j^2}{\kappa_\Gamma}$$

(Almost) all channels can be parametrized this way, simple extension possible for more channels/observables.

*zero-width approximation, Higgs width 10^{-5} of its mass, in general valid. Violations (% level correction) see Campbell, Carena, Harnik, [ZL et al, 1704.08259](#)

Measurements to be interpreted

Observables at the colliders are the cross sections, a convolution of PDF (including CEPC, treating the beam energy spread), hard scattering, parton shower, detector response ...

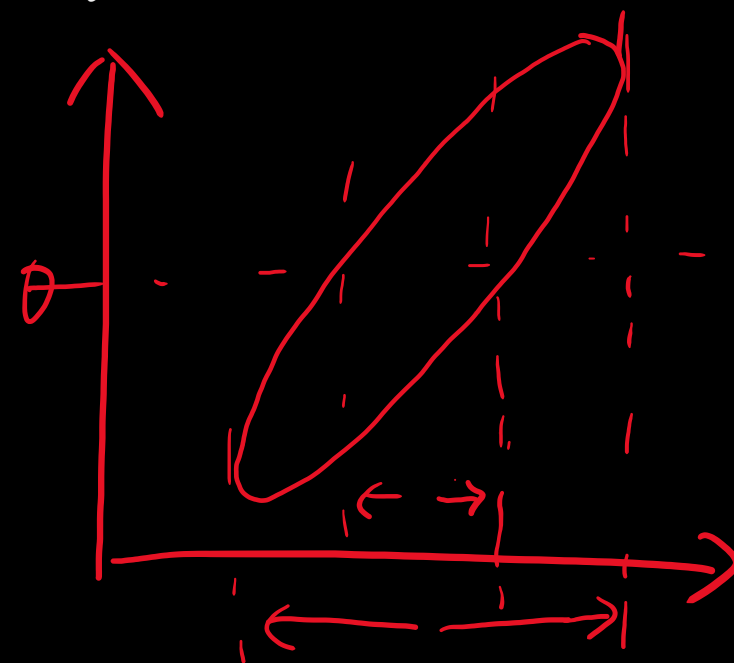
For the hard scattering:

$$\sigma(i \rightarrow H \rightarrow j) \propto \frac{\Gamma_i \Gamma_j}{\Gamma_{tot}} \propto \frac{\kappa_i^2 \kappa_j^2}{\kappa_\Gamma}$$

If $\kappa_\Gamma = \kappa_i^2 \kappa_j^2$, the observed rates do not change.

- All κ s are positively correlated with the total width (from the point of cross sections);
- The naïve scaling of $\kappa_{tot} \propto \kappa_{i,f}^2$, does not reflect this flat direction, one needs additional particle width to enter.
- This highlights the importance and complementarity of the exotic decay program.

$$\kappa_i = \frac{g_i}{g_i^{SM}}, \kappa_\Gamma = \frac{\Gamma_{tot}}{\Gamma_{tot}^{SM}}$$



***Flat direction is not disastrous, just give some seemingly worse results when projected to useful basis.

Resolving flat direction: e+e-'s option

For the hard scattering:

$$\sigma(i \rightarrow H \rightarrow j) \propto \frac{\Gamma_i \Gamma_j}{\Gamma_{tot}} \propto \frac{\kappa_i^2 \kappa_j^2}{\kappa_\Gamma}$$

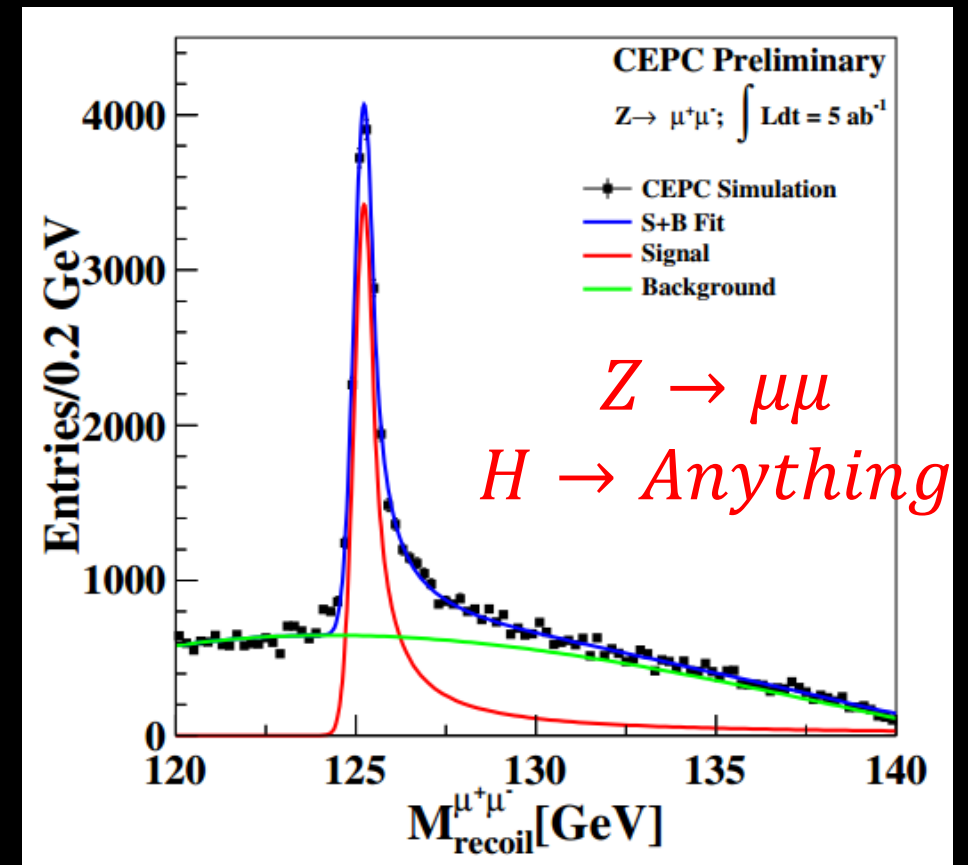
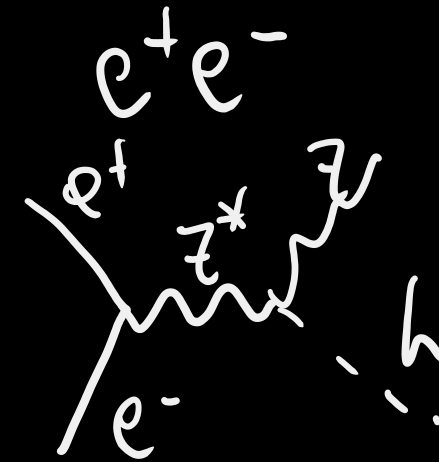
If $\kappa_\Gamma = \kappa_i^2 \kappa_j^2$, the observed rates do not change.

This leads to a large flat direction of the Higgs coupling extraction, the future lepton colliders such as ILC/FCC-ee/CEPC can handle this by the **unique inclusive cross section measurement**

$$\sigma(ee \rightarrow ZH, H \rightarrow anything) \propto \kappa_Z^2$$

Unique physics for 250~400 GeV lepton collider, direct determination of the HZZ coupling. At higher energies, one might rely on ZZ-fusion for such a inclusive measurement (Han, ZL, Qian, Sayre, [1504.01399](#)).

PP collider closes the fit by assuming zero $\Gamma_{undetected}$ or $|\kappa_V| < 1$

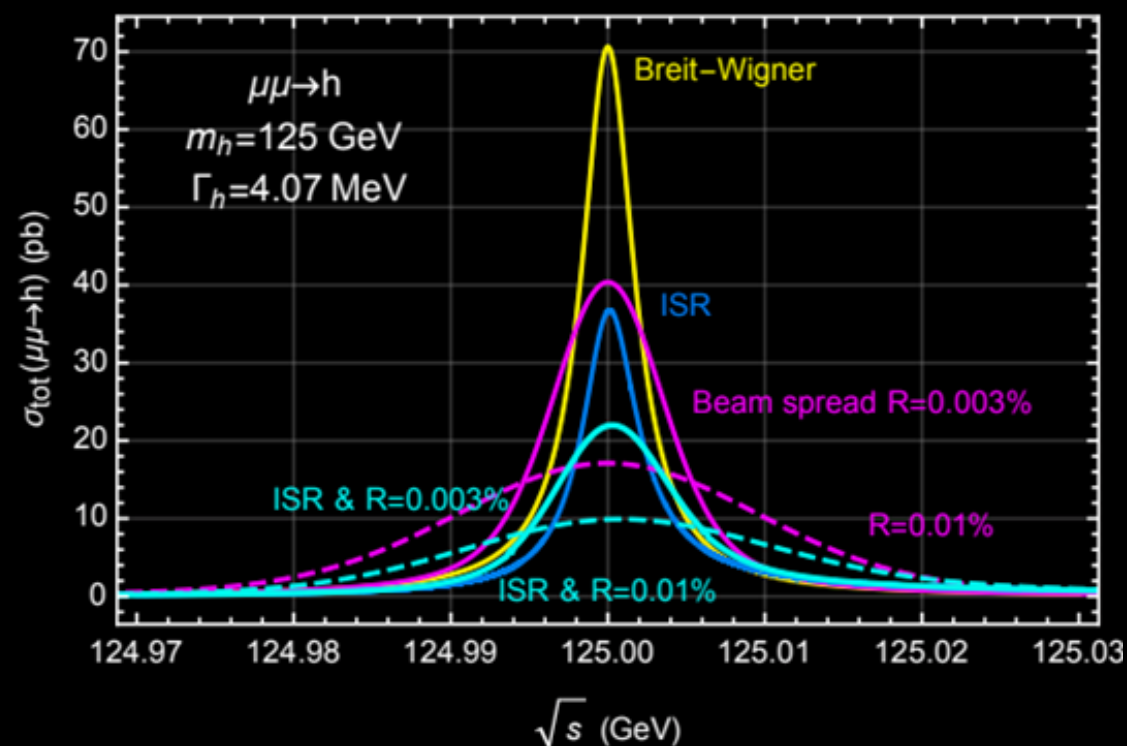
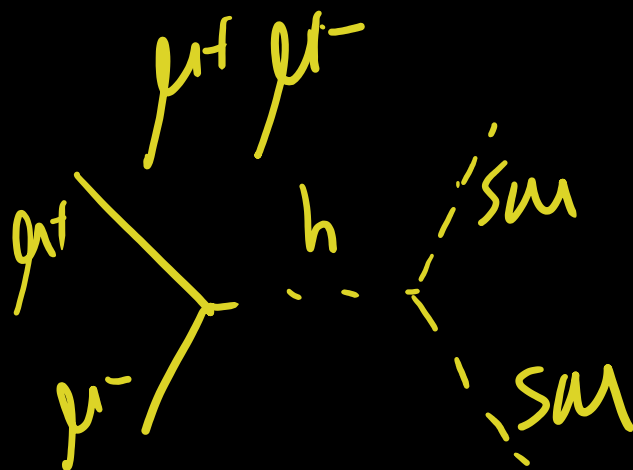


Hitting the resonance & scan

$\sigma(\text{BW})$	ISR alone	R (%)	BES alone	BES+ISR
$\mu^+\mu^-: 71 \text{ pb}$	37	0.01	17	10
		0.003	41	22

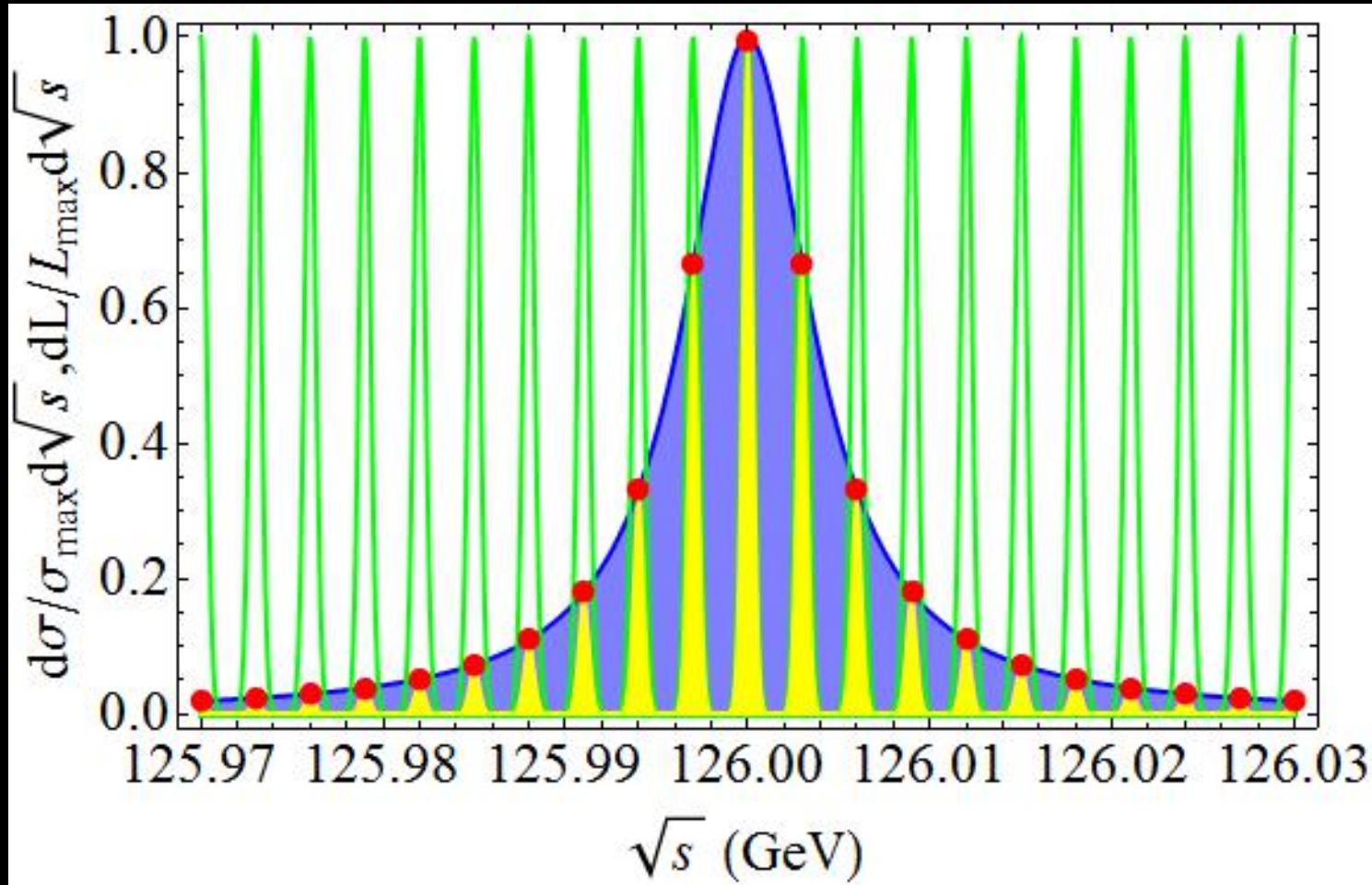
Han, [ZL, 1210.7803](#);
With ISR effects
Greco, Han, [ZL, 1607.03210](#)

$$\sigma(\mu^+\mu^- \rightarrow h \rightarrow X) = \frac{4\pi\Gamma_h^2 \text{Br}(h \rightarrow \mu^+\mu^-) \text{Br}(h \rightarrow X)}{(\hat{s} - m_h^2)^2 + \Gamma_h^2 m_h^2}.$$



$$\sigma_{\text{eff}}(s) = \int d\sqrt{\hat{s}} \frac{dL(\sqrt{s})}{d\sqrt{\hat{s}}} \sigma(\ell^+\ell^- \rightarrow h \rightarrow X)(\hat{s})$$

Extreme (good) Case:



Energy Spread much
narrower than the
physical width:

$$\Delta = 0.3 \text{ MeV}$$

$$\Gamma_h = 4.2 \text{ MeV}$$

Breit-Wigner

Gaussian Profile (beam)

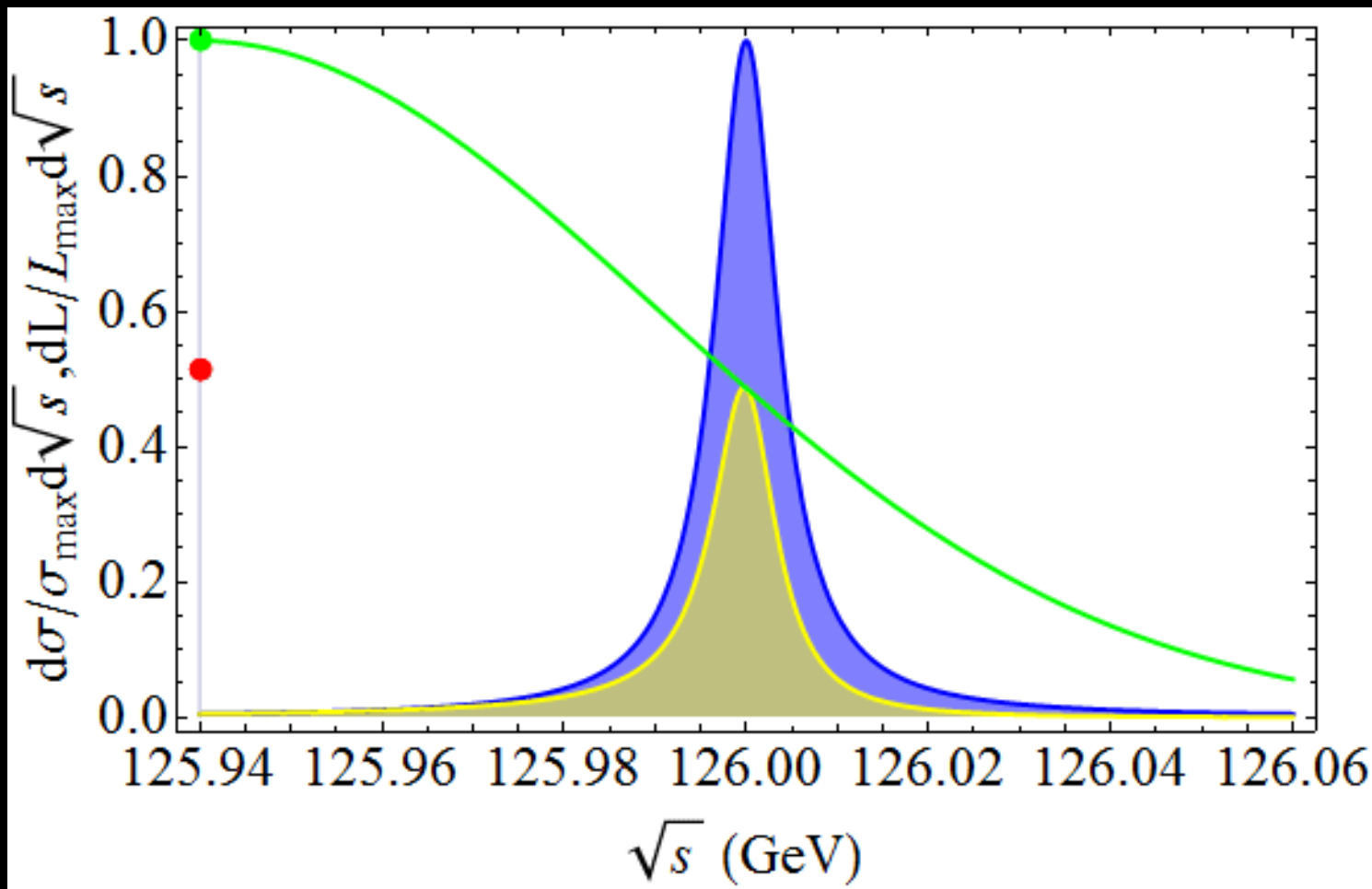
Overlap (observable rate)

**Effective cross section
(observable scan)**

Recall: **Z scan @LEP**

$$\Gamma = 2.5 \text{ GeV}$$

Extreme (bad) Case:



Energy Spread
much **broader** than
the physical width:

$$\Delta = 50 \text{ MeV}$$

$$\Gamma_h = 4.2 \text{ MeV}$$

Breit-Wigner

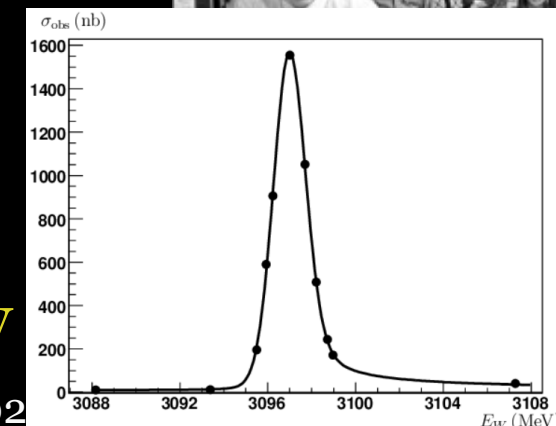
Gaussian Profile (beam)

Overlap (observable rate)

Effective cross section
(observable scan)

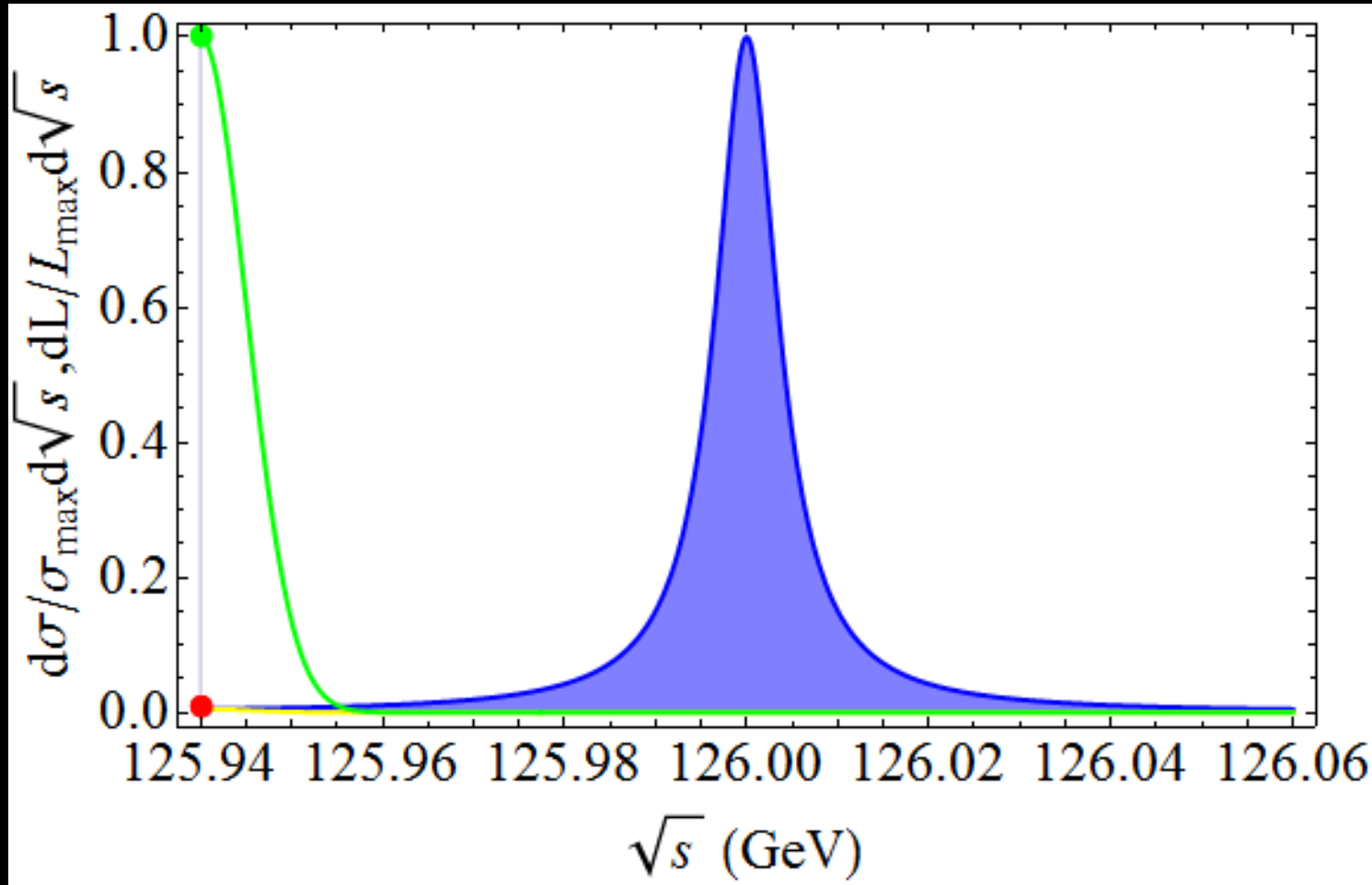


Recall: J/ψ scan $\Gamma \approx 93 \text{ keV}$



Close to reality:

Han, [ZL](#), [1210.7803](#);



Energy Spread
comparable to the
physical width:

$$\Delta = 5 \text{ MeV}$$

$$(R=0.003\%)$$

$$\Gamma_h = 4.2 \text{ MeV}$$

Breit-Wigner

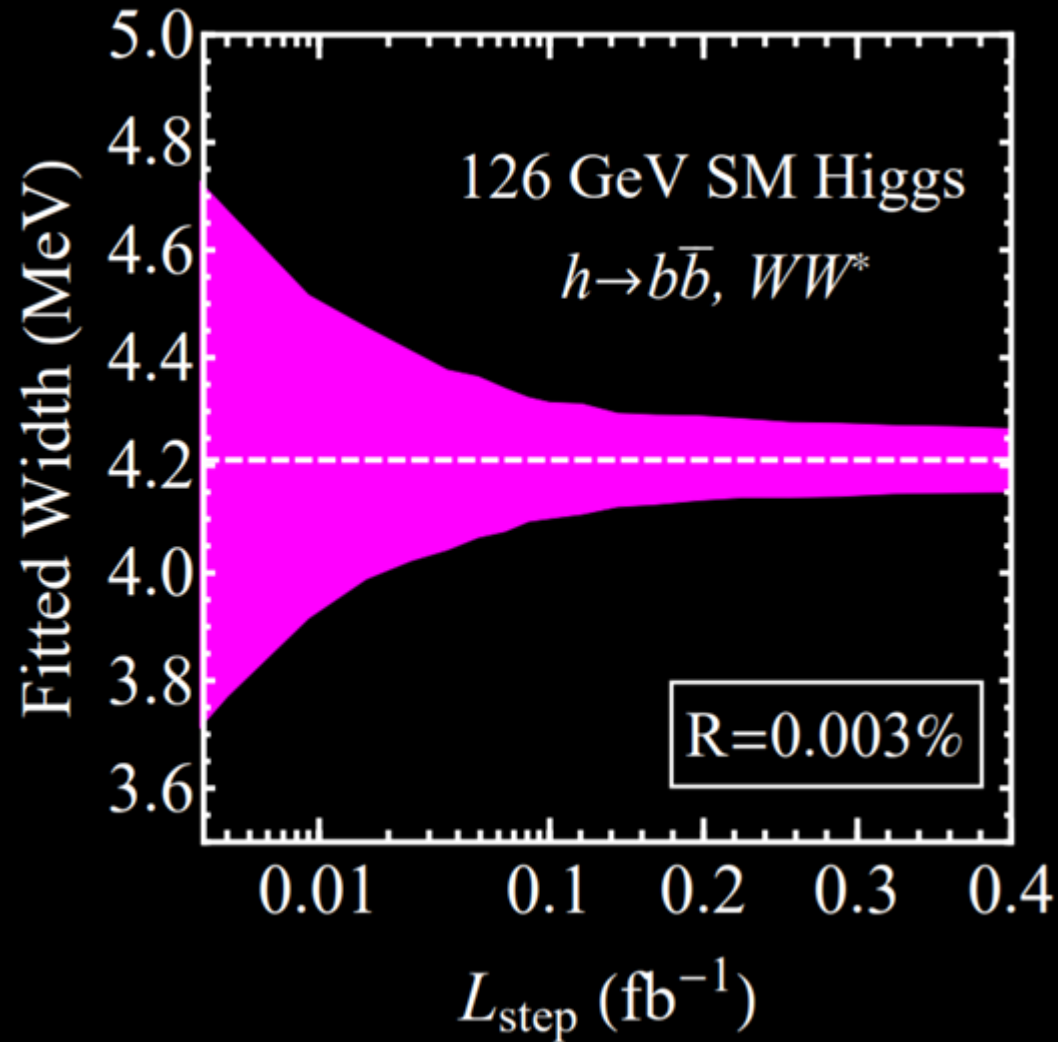
Gaussian Profile (beam)

Overlap (observable rate)

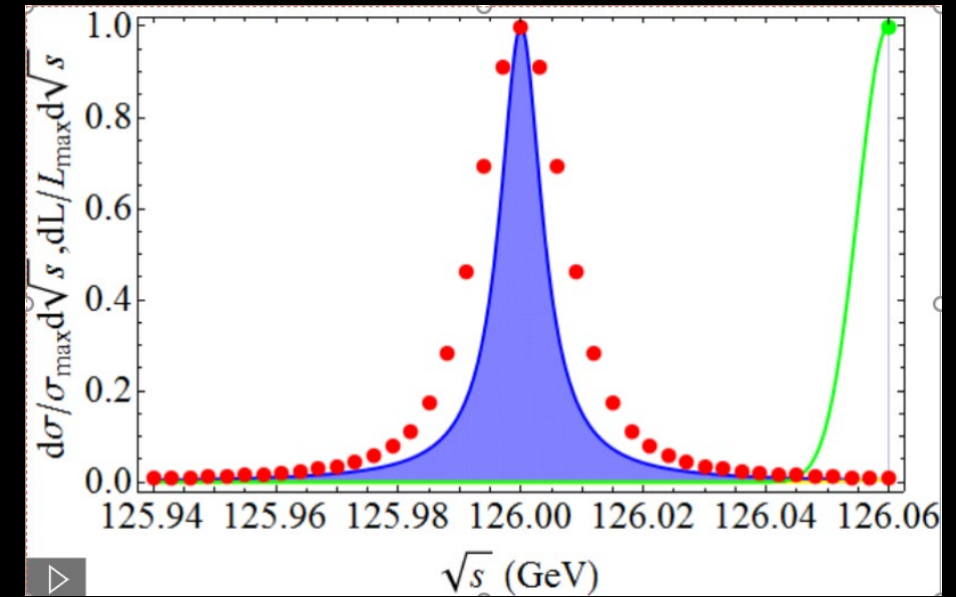
Effective cross section
(observable scan)

An optimal fitting would reveal Γ_h

Fitting the **SM** Higgs



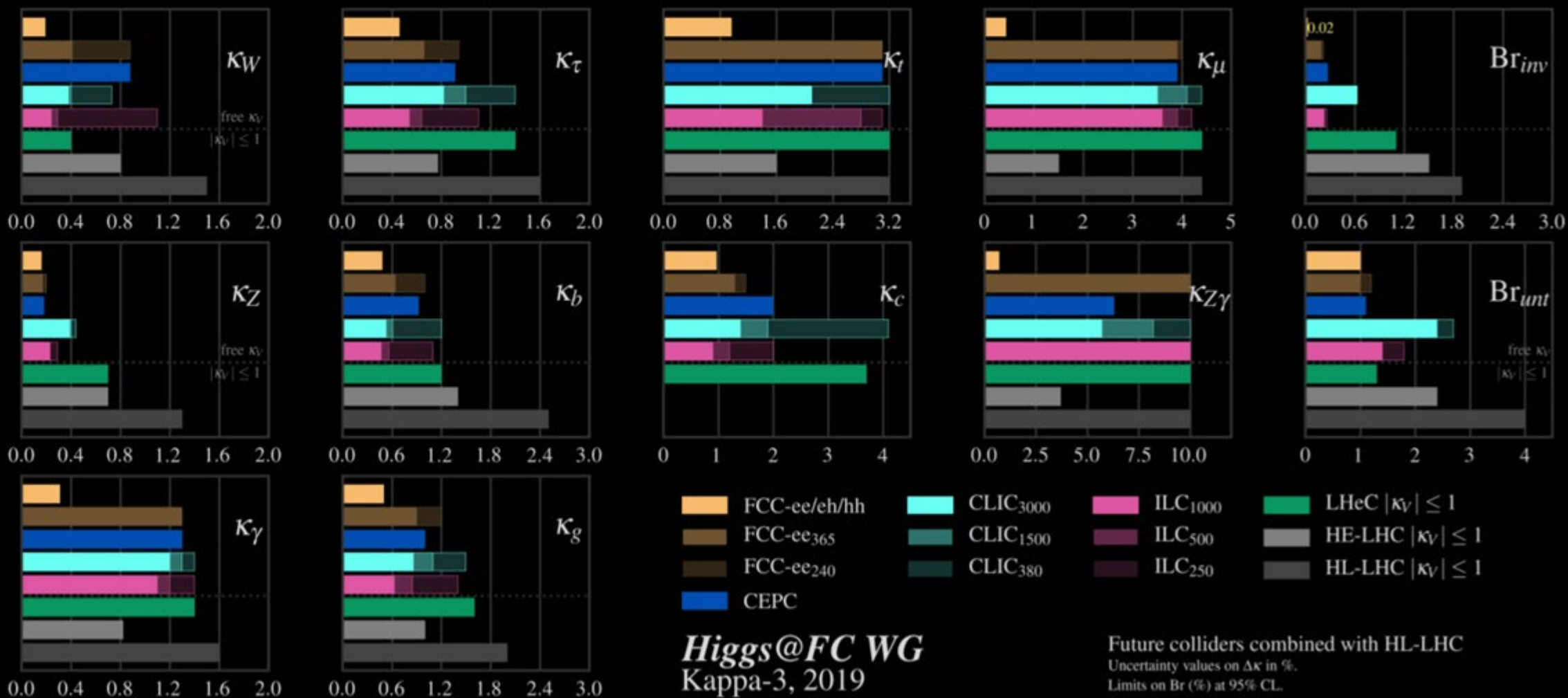
$\Gamma_h = 4.07 \text{ MeV}$	$L_{\text{step}} \text{ (fb}^{-1}\text{)}$	$\delta\Gamma_h \text{ (MeV)}$	δB	$\delta m_h \text{ (MeV)}$
$R = 0.01\%$	0.05	0.79	3.0%	0.36
	0.2	0.39	1.1%	0.18
$R = 0.003\%$	0.05	0.30	2.5%	0.14
	0.2	0.14	0.8%	0.07



Outline

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- Higgs Width
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- Higgs Exotic Decays

Where would MuC Higgs factory stand?



Basics:

pp

e^+e^-

$\mu^+\mu^-$

SORRY...



Table 1-18. Muon collider statistical precisions on Higgs production rates into various final states X from a 5-point energy scan centered at m_H with a combined yield of 39,000 Higgs bosons. The $\tau\tau$ uncertainty is an average of asymmetric uncertainties. The rates are proportional to $\text{BR}(H \rightarrow \mu\mu) \times \text{BR}(H \rightarrow X) \propto \kappa_\mu^2 \kappa_X^2 / \Gamma_H^2$.

Snowmass Higgs Report 1310.8361

Final state	$b\bar{b}$	WW^*	$\tau\tau$	$c\bar{c}$	gg	$\gamma\gamma$	ZZ^*	$Z\gamma$	$\mu\mu$	Γ_H	m_H
$\sigma(\mu\mu \rightarrow H \rightarrow X)$	9%	5%	60%	—	—	—	—	—	—	4.3%	0.06 MeV

50 pb

3 ab^{-1}

0.15 billion Higgs

200 fb

5 ab^{-1}

1 million Higgs

20 pb

1 fb^{-1}

20 thousand Higgs

HOPE LESS?

General κ fit (so called “model independent fit”)

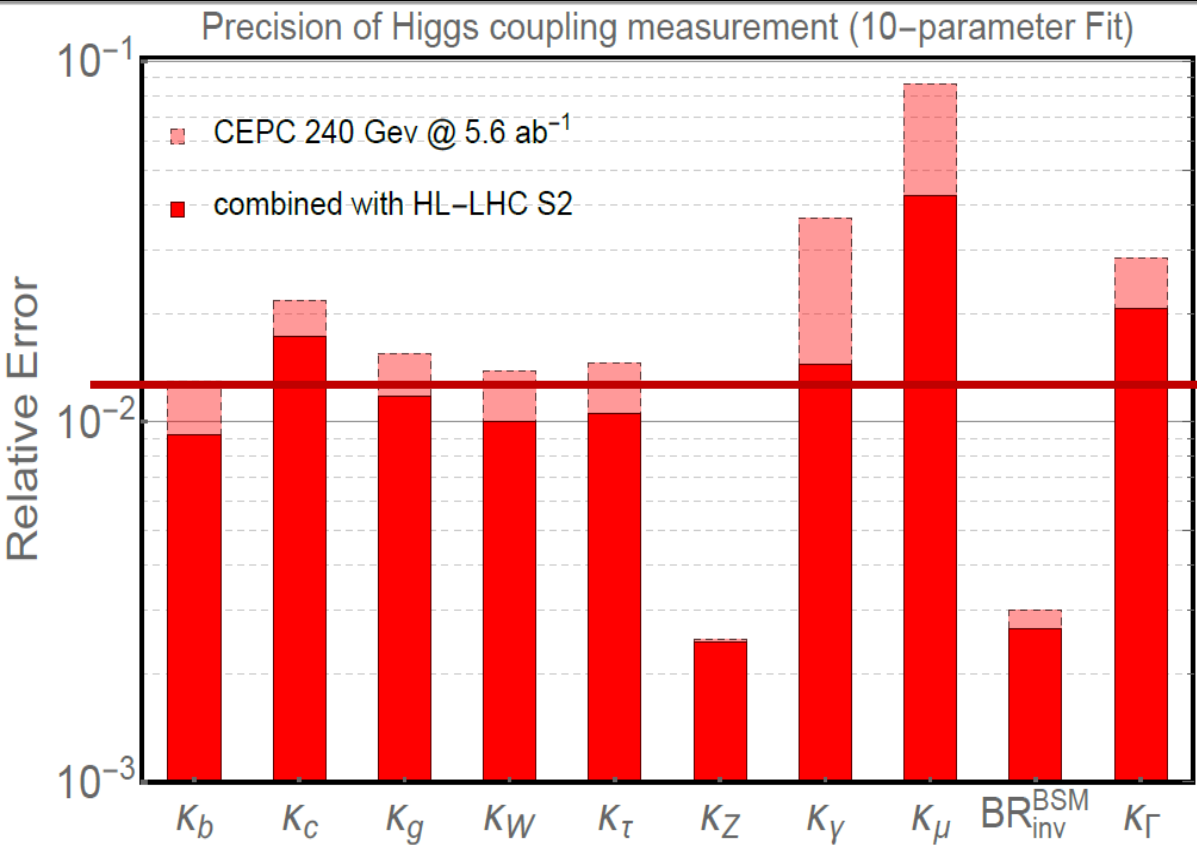
ΔM_H	Γ_H	$\sigma(ZH)$
5.5 MeV	2.8%	0.51%
CEPC per channel precision		
Decay mode	$\sigma(ZH) \times \text{BR}$	
$H \rightarrow bb$	Signature numbers	0.28%
$H \rightarrow cc$		2.2%
$H \rightarrow gg$		κ_Γ 2.8% 1.6%
$H \rightarrow \tau\tau$		κ_Z 0.25% 1.2%
$H \rightarrow WW$		κ_b 1.3% 1.5%
$H \rightarrow ZZ$		κ_τ 1.5% 4.3%
$H \rightarrow \gamma\gamma$		9.0%
$H \rightarrow \mu\mu$		17%
$H \rightarrow \text{inv}$		0.28%

New Insight: the total width sets a floor for the individual coupling extraction as:

$$\sigma(i \rightarrow H \rightarrow j) \propto \frac{\Gamma_i \Gamma_j}{\Gamma_{tot}} \propto \frac{\kappa_i^2 \kappa_j^2}{\kappa_\Gamma} \Rightarrow$$

$$\Delta \kappa_j = 1/2(\Delta \kappa_j^2)$$

$$= 1/2(\Delta \kappa_\Gamma \oplus \Delta \sigma(i \rightarrow H \rightarrow j) \oplus \Delta \kappa_i^2)$$



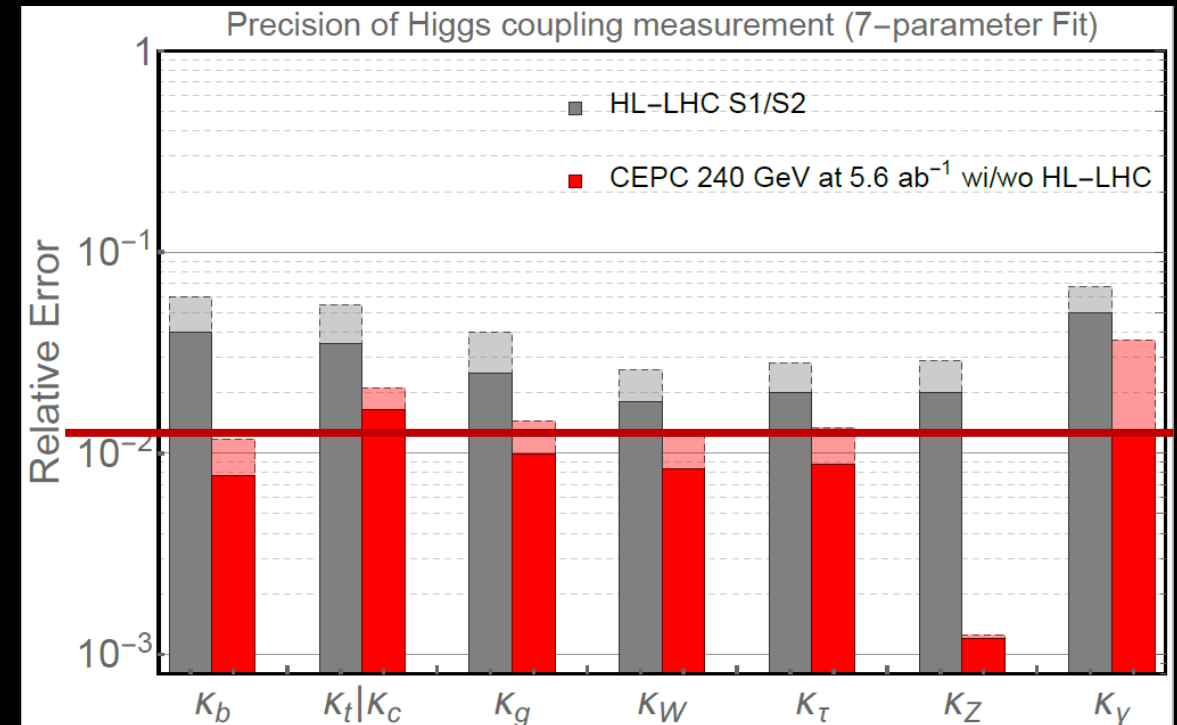
Constrained κ fit (No BR(undetectable)—Width not free)

New Insight: The total width (still!) sets a floor for the individual coupling extraction.

- Can be compared with the HL-LHC
- Large improvement (\sim one order of magnitude)
- Result improved from additional constraints
- Signature numbers
 - κ_Γ 2.8% \rightarrow (2.4%)*
 - κ_Z 0.25% \rightarrow 0.13%
 - κ_b 1.3% \rightarrow 1.2%

*not a free parameter; but useful intermediate quantity

*Significant “improvement” for the κ_Z from the additional constraints (fit assumption are critical in comparing results, always be careful)



Now the Model-Independent MuC Width matters!

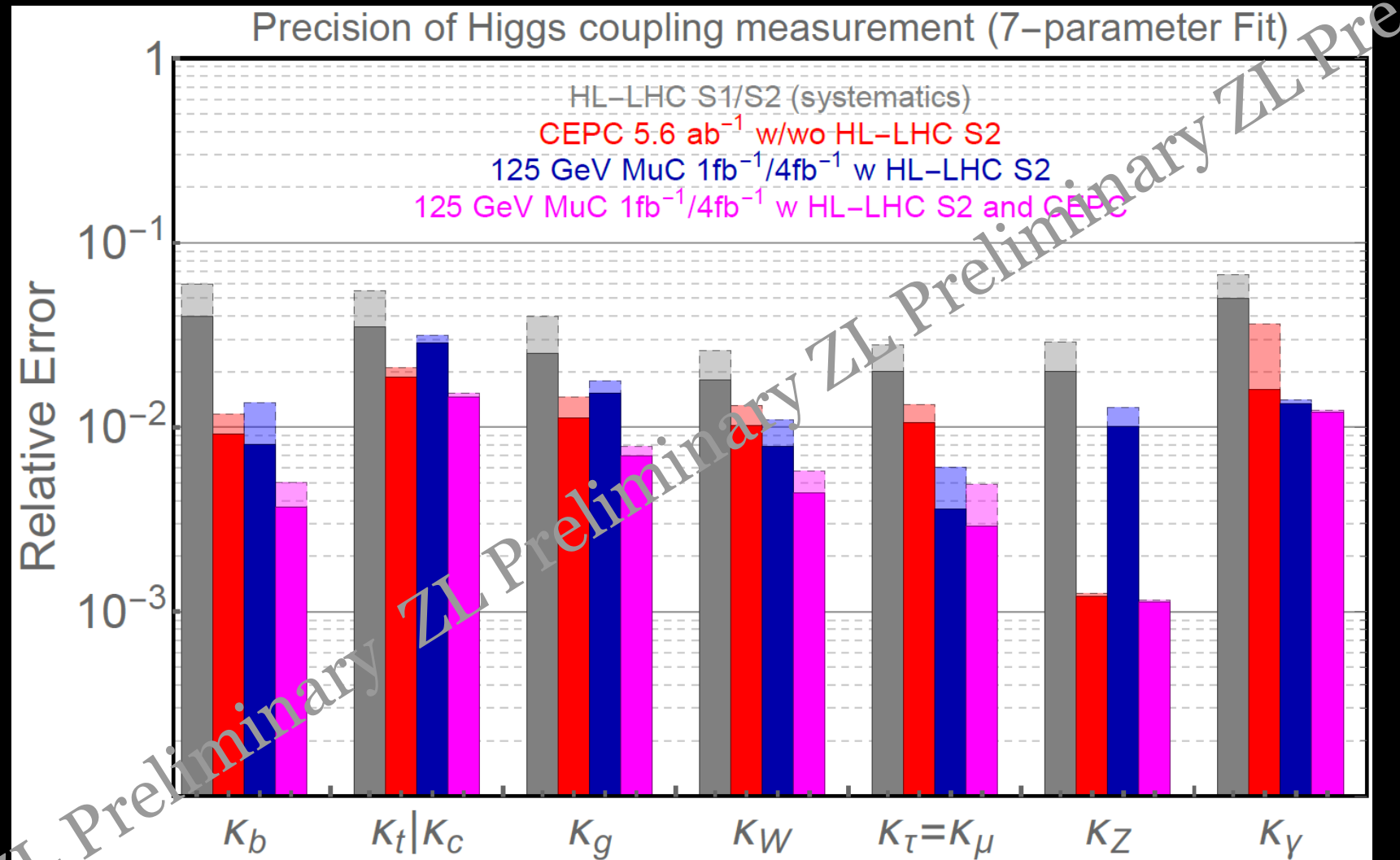
Let's check precision with 1/50 statistics (with different bkg)

ΔM_H	Γ_H	$\sigma(ZH)$
5.5 MeV	2.8%	0.51%
CEPC per channel precision		
Decay mode	$\sigma(ZH) \times \text{BR}$	
$H \rightarrow bb$	0.28%	
$H \rightarrow cc$	2.2%	
$H \rightarrow gg$	1.6%	
$H \rightarrow \tau\tau$	1.2%	
$H \rightarrow WW$	1.5%	
$H \rightarrow ZZ$	4.3%	
$H \rightarrow \gamma\gamma$	9.0%	
$H \rightarrow \mu\mu$	17%	
$H \rightarrow \text{inv}$	0.28%	

	Br	Rate (pb)	Precision
Inclusive	100%	22	---
bbar	57.80%	12.72	1.7%
tautau	6.37%	1.40	18%
mumu	0.02%	0.00	2005%
cc	2.68%	0.59	25%
gg	8.56%	1.88	13%
$\gamma\gamma$	0.23%	0.05	374%
WW*	21.60%	4.75	1.6%
ZZ*	2.67%	0.59	4.5%
invisible	0.01%	0.00	---
Γ_{total}	4.2 (MeV)		3.3%

Good results with 1/50 (1/12) Higgs statistics!

- This MuC Width is a pure measurement, uncorrelated with all the other parameters;
- When combined with the HL-LHC, **comparable** to other lepton collider Higgs factories (except for k_Z)
- **Sub-percent muon Yukawa**
- Good lumi scaling with couplings
- **Excellent improvement when combined with CEPC** (kb, kg, kW, kmu)

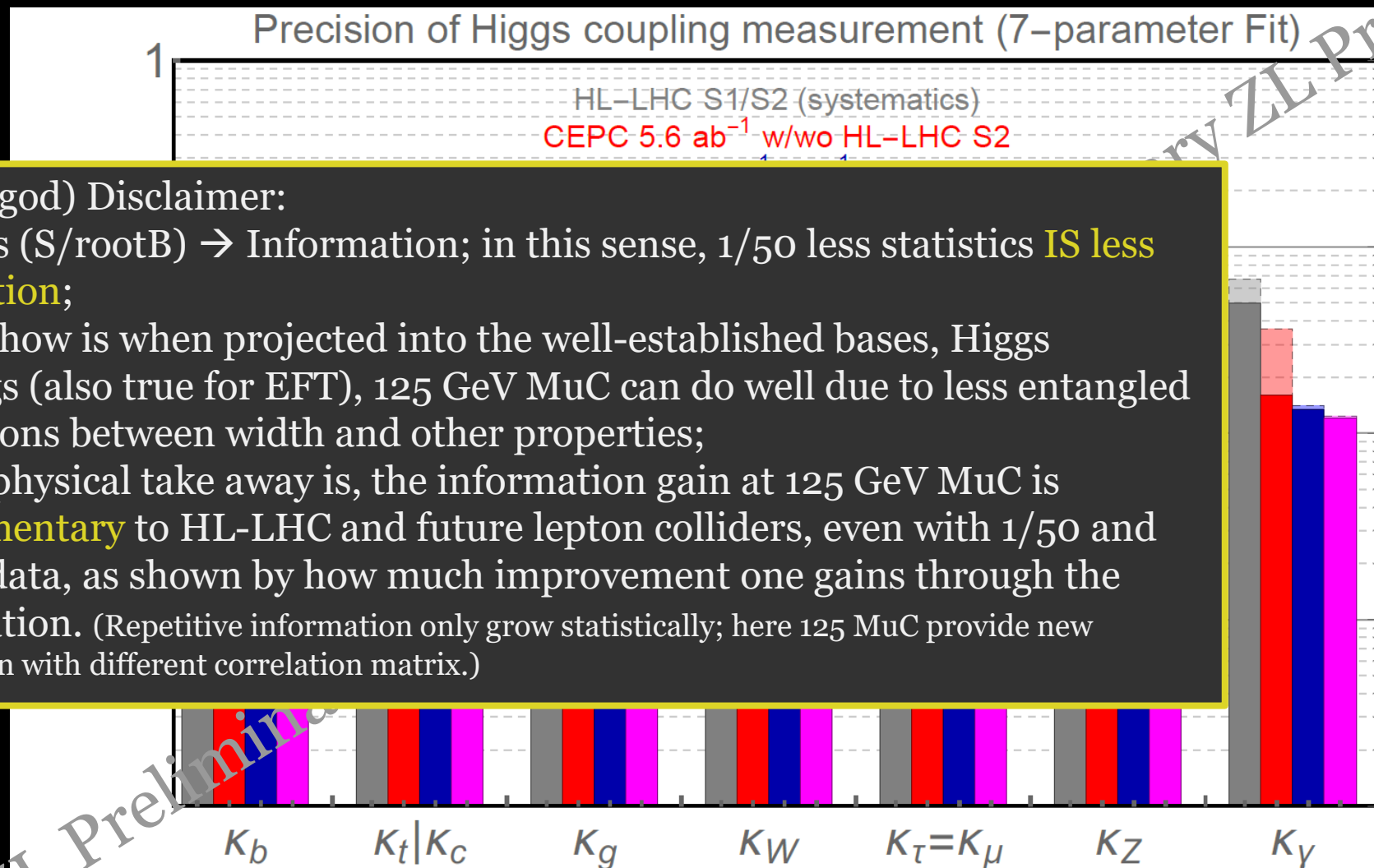


Good results with 1/50 (1/12) Higgs statistics!

- This MuC Width is a pure measurement, uncorrelated with all the other parameters
- When combined with the HL-LHC, the MuC is **comparable** to lepton colliders (e.g. kZ)
- **Sub-percent** **Yukawa**
- Good luminosity for couplings
- **Excellent improvement** when combined with CEPC (kb, kg, kW, kmu)

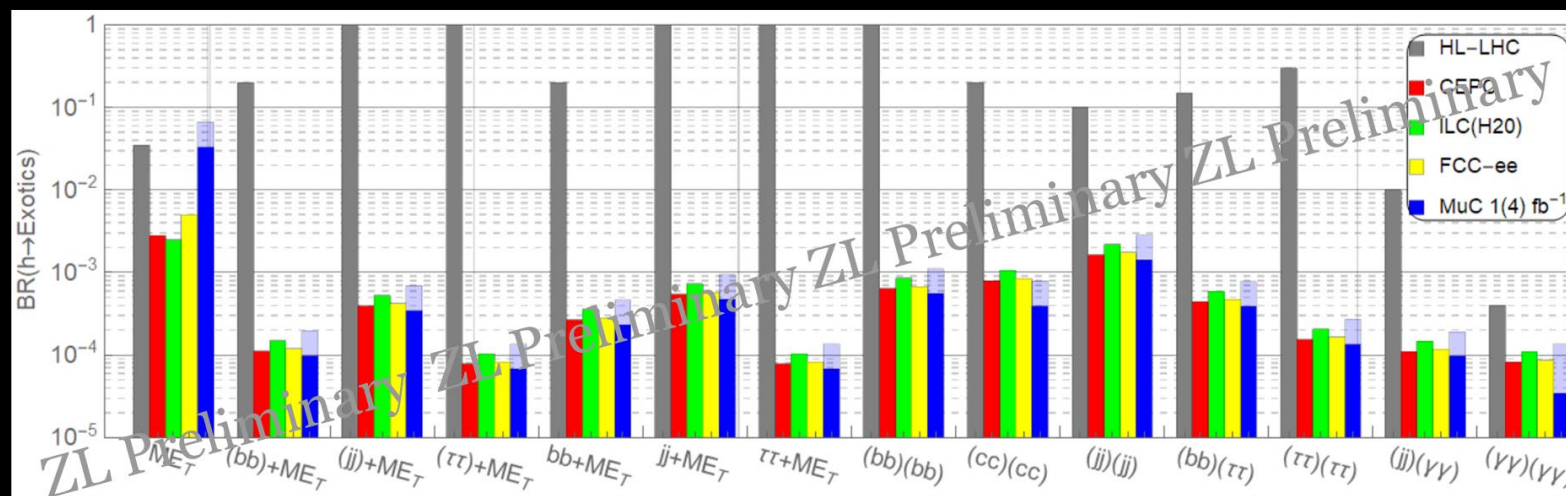
(Honest to god) Disclaimer:

- Statistics (S/\sqrt{B}) \rightarrow Information; in this sense, 1/50 less statistics **IS less information**;
- What I show is when projected into the well-established bases, Higgs couplings (also true for EFT), 125 GeV MuC can do well due to less entangled correlations between width and other properties;
- A more physical take away is, the information gain at 125 GeV MuC is **complementary** to HL-LHC and future lepton colliders, even with 1/50 and 1/7500 data, as shown by how much improvement one gains through the combination. (Repetitive information only grow statistically; here 125 MuC provide new information with different correlation matrix.)



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Why Exotic Decays?

- While most current searches focus on heavy BSM particles, there is a whole zoo of light BSM particle not well explored at colliders.

(checking all the possibility; theoretical interests.)

$((H^+ H)$ lowest mass dimensional spinless gauge singlet structure, easily a portal to BSM)

- The precision does not pin-point a scale, the exotic decays are to fully probe the scale below Higgs mass. **

(complementarity)

ARE WE ALONE ?
From Raman Sundrum's talk this morning.
Gauge Field Theory naturally divides into
"socially-distanced pods" (sectors)

Why Exotic Decays? (continued)

- Higgs has **tiny width** ~ 4 MeV

$$\frac{\Gamma}{M} = O(10^{-5})$$

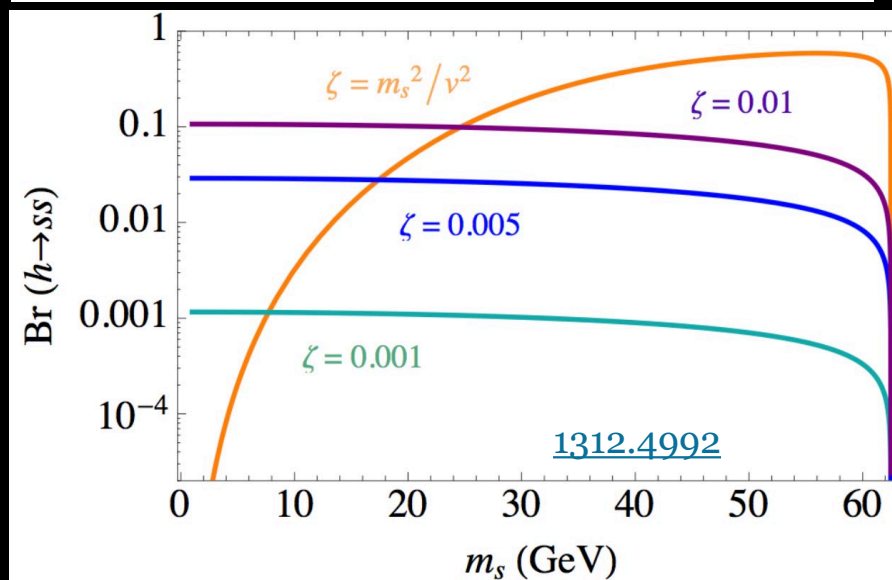
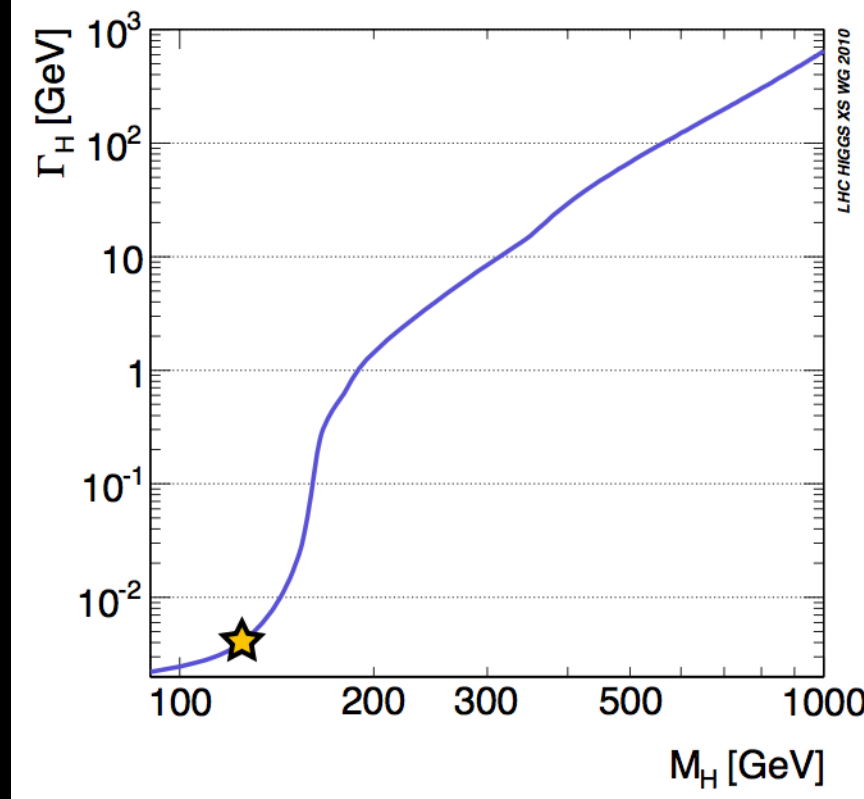
all its decay modes are suppressed by various factors, couplings, loop-factors, phase-space, etc.

Dominant decays into bottom quark pairs are suppressed by the tiny coupling $y_b = 0.017$

- small couplings** to BSM could have **sizeable** branching, e.g.,

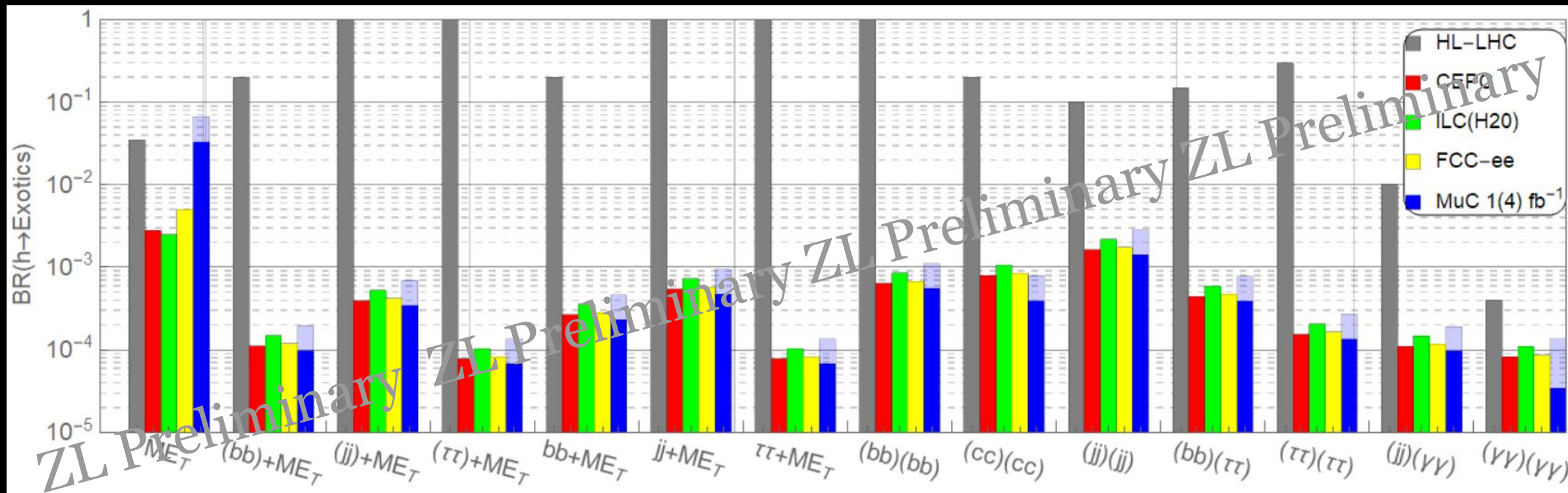
$$\mathcal{L} = \frac{\zeta}{2} s^2 |H|^2$$

(common building block in extended Higgs sectors) can give $\text{BR}(h \rightarrow ss) \sim O(10\%)$ for ζ as small as 0.01 !



Exotic Decay Overall Picture

Our study on CEPC/ILC/FCC-ee only used $Z(\rightarrow ll)H$, there is 10x statistics yet to be used.



125 GeV MuC: no tagging spectator Z issues and less combinatoric background.

with missing Energy (SUSY motivated, DM motivated channels)

3-4 orders of magnitude improvement for the constraints on such exotic branching fractions

$h \rightarrow 4f$ generic Higgs sector extensions, also Higgs portals

2-3 orders of magnitude improvement for the constraints on such exotic branching fractions

Original plot without MuC, ZL, Wang, Zhang, [1612.09284](#), updated by ZL following future collider program updates; MuC pre-preliminary results compiled by ZL.

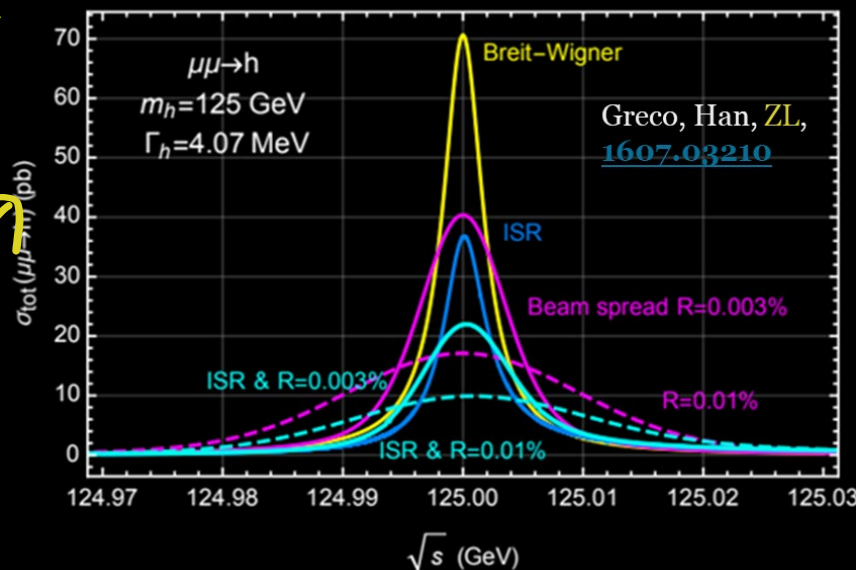
Summary

- Overall picture
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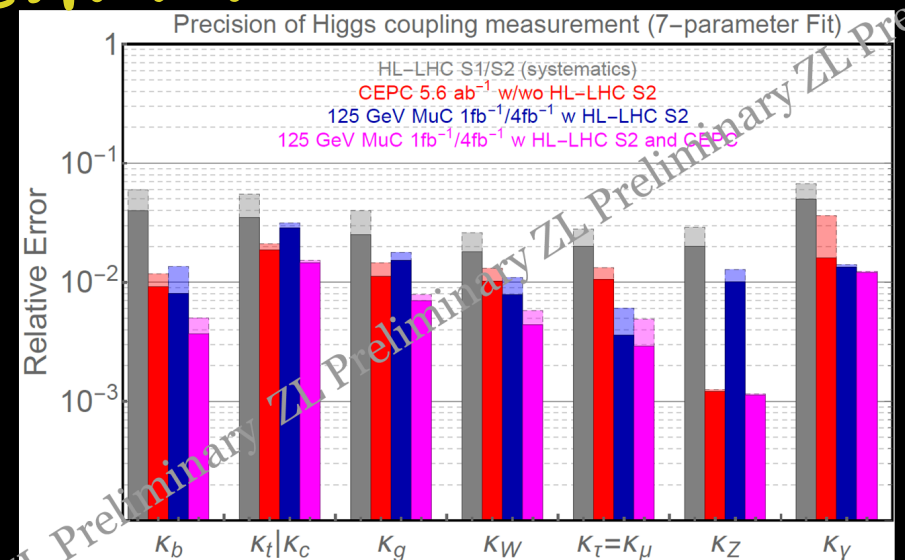
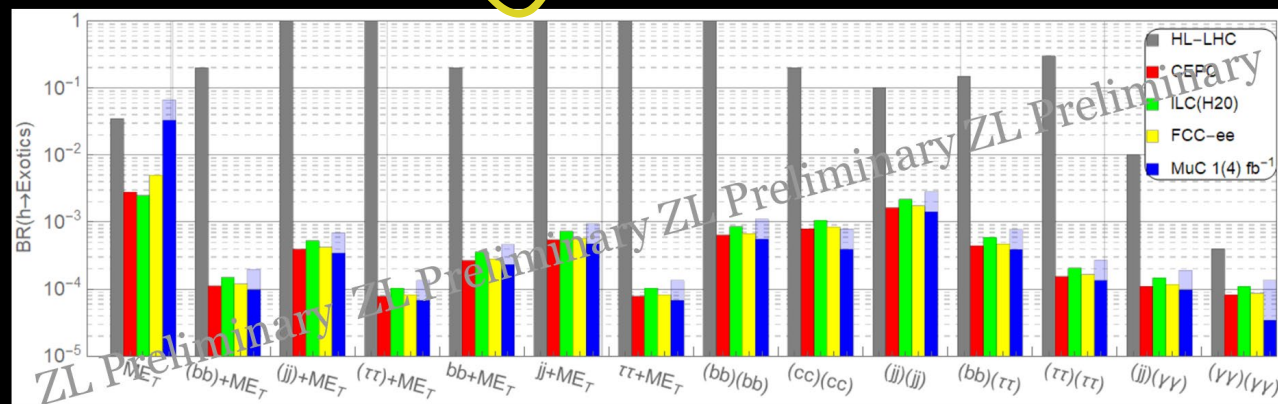
State-of-art

LEAST understood
Focus of this talk



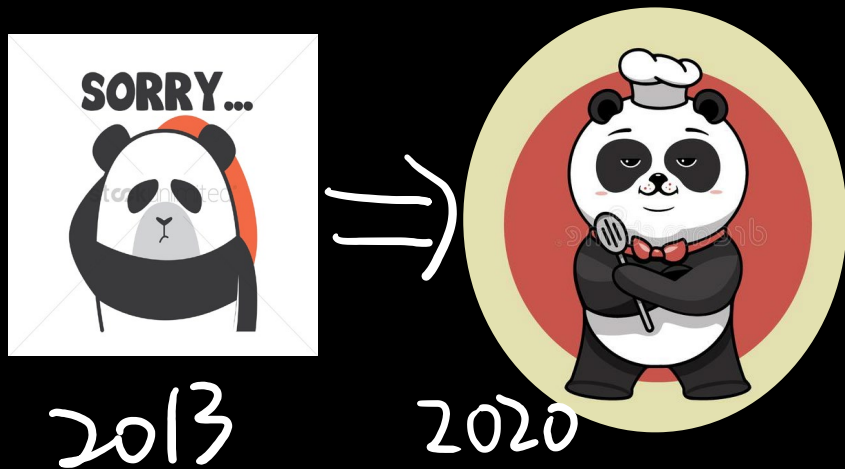
A First Estimation!

A FIRST Estimation



Summary: Outlook

- Overall picture
- Higgs Width
- Higgs Couplings
- Higgs Exotic Decays



Many more to do:

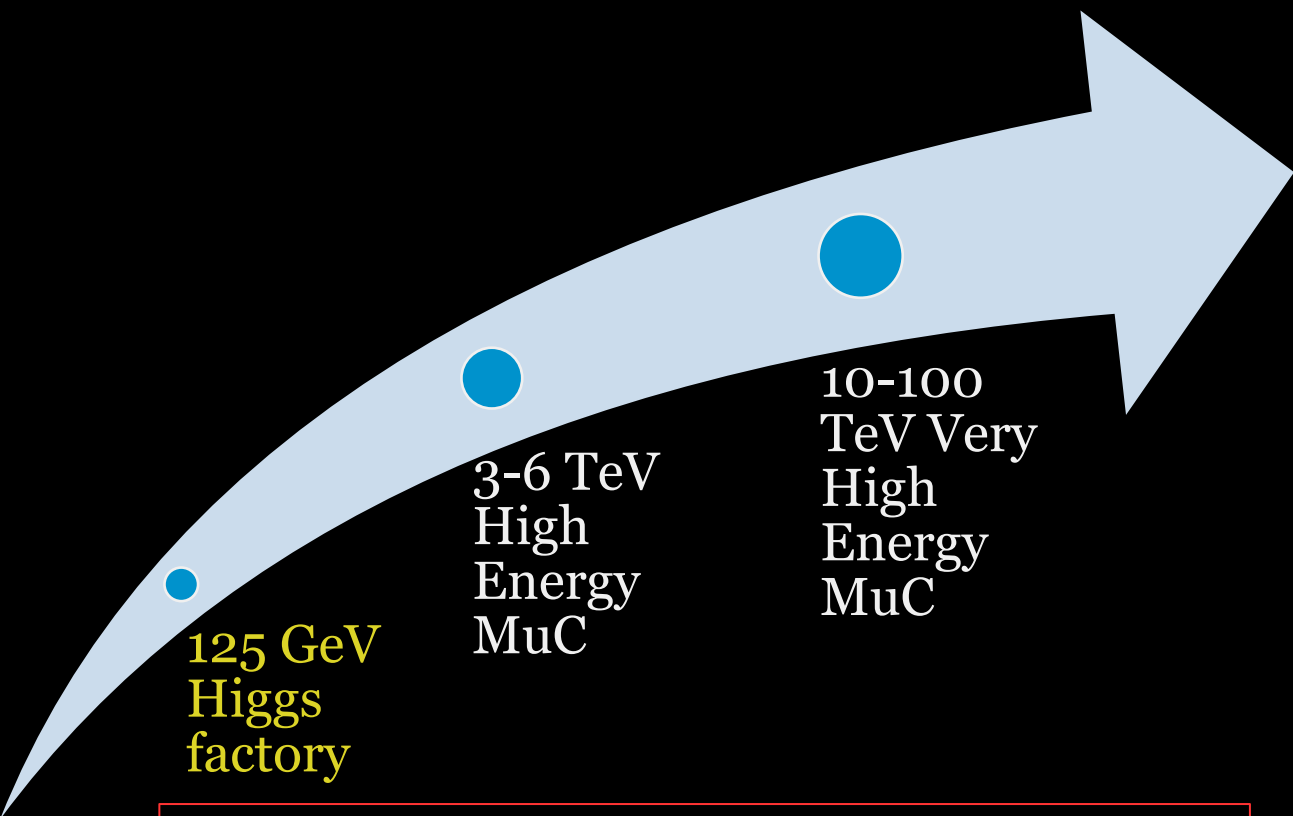
A Comprehensive Physics Case for 125 GeV MuC Higgs Factory is “structured”

(Do we need it?)

Some core tasks:

- (Semi-)optimal scanning strategy development (width v.s. BES, step size, and step luminosity);
- Fast detector simulation for major Higgs channels for Higgs precision;
- Fast simulation for exotic decays;

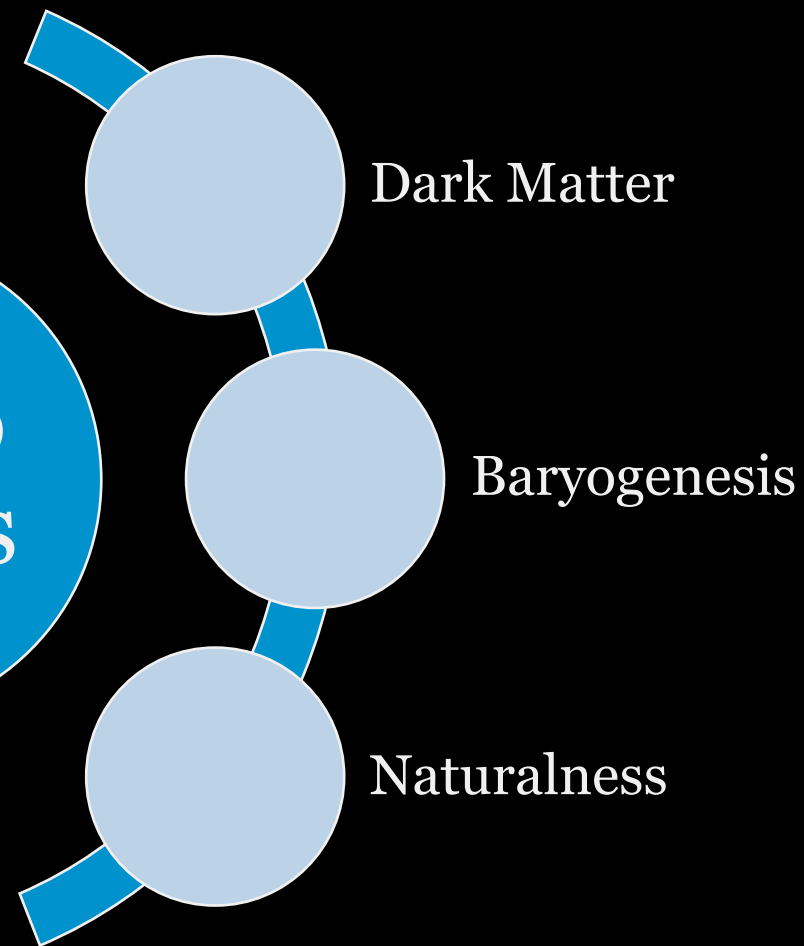
The Dream Machine



This new set of analysis shows its unique physics cases with 10^2 less Higgs bosons. A physics-wise motivated step towards high energy MuC.



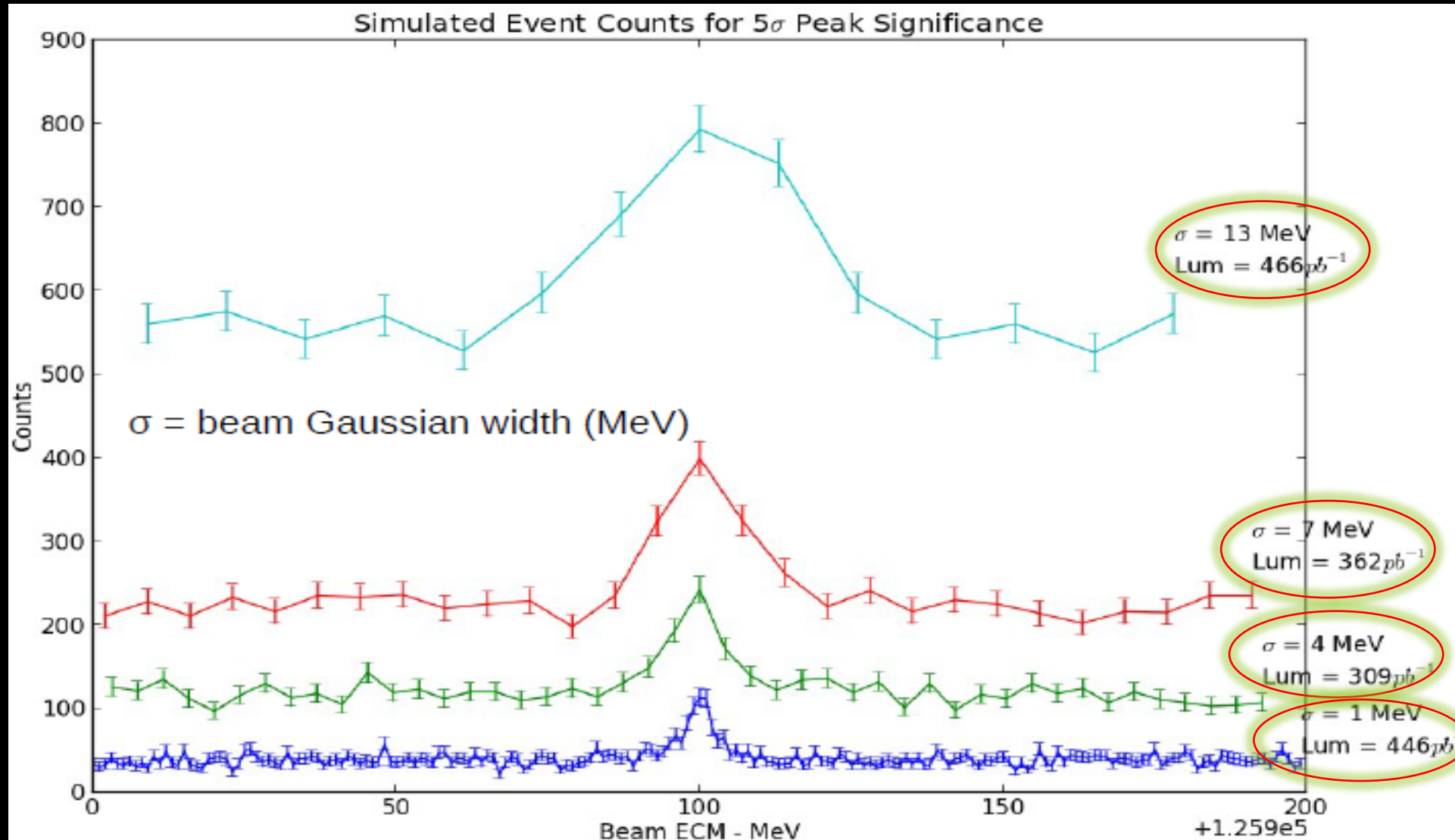
Physics Driver



Thank you!

Backup

Pinning down the mass of the Higgs

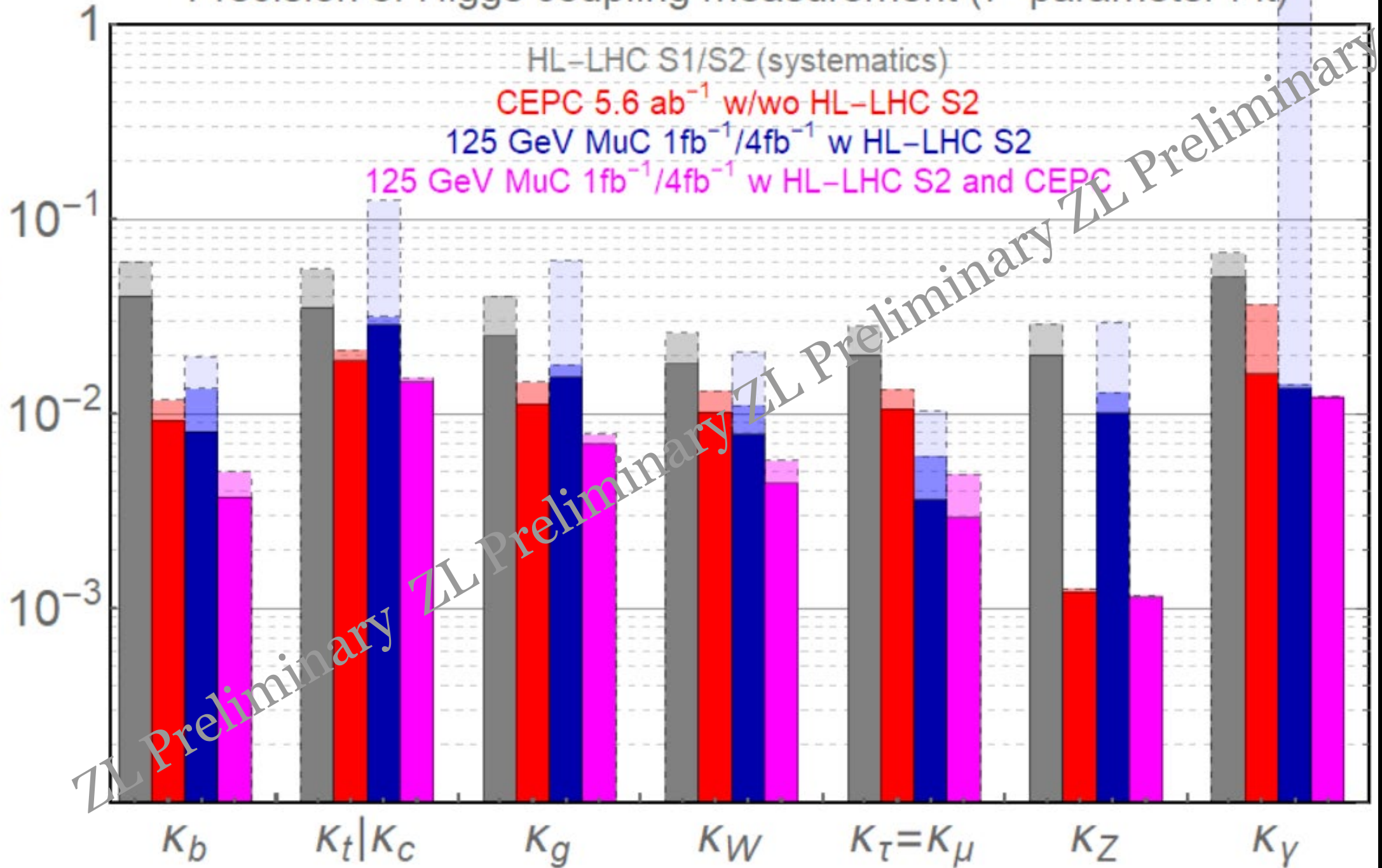


arxiv:1304.5270

	Br	Rate (pb)	Used Sig Rate	Bkg Rate	Composed Bkg Rate	Precision
Inclusive	100%	22				---
bbar	57.80%	12.72	10.30	18.71	21.24	1.72%
tautau	6.37%	1.40	0.59	9.50	10.45	17.75%
mumu	0.02%	0.00	0.00	9.50	9.50	2005.62%
ss	0.04%	0.01	0.01	18.71	56.13	2447.71%
cc	2.68%	0.59	0.59	19.66	21.53	25.23%
gg	8.56%	1.88	1.88	0.00	56.13	12.79%
$\gamma\gamma$	0.23%	0.05	0.05	35.78	35.78	374.09%
WW*	21.60%	4.75	3.85	0.05	0.05	1.62%
ZZ*	2.67%	0.59	0.54	0.05	0.05	4.49%
invisible	0.01%	0.00				---

Precision of Higgs coupling measurement (7-parameter Fit)

Relative Error



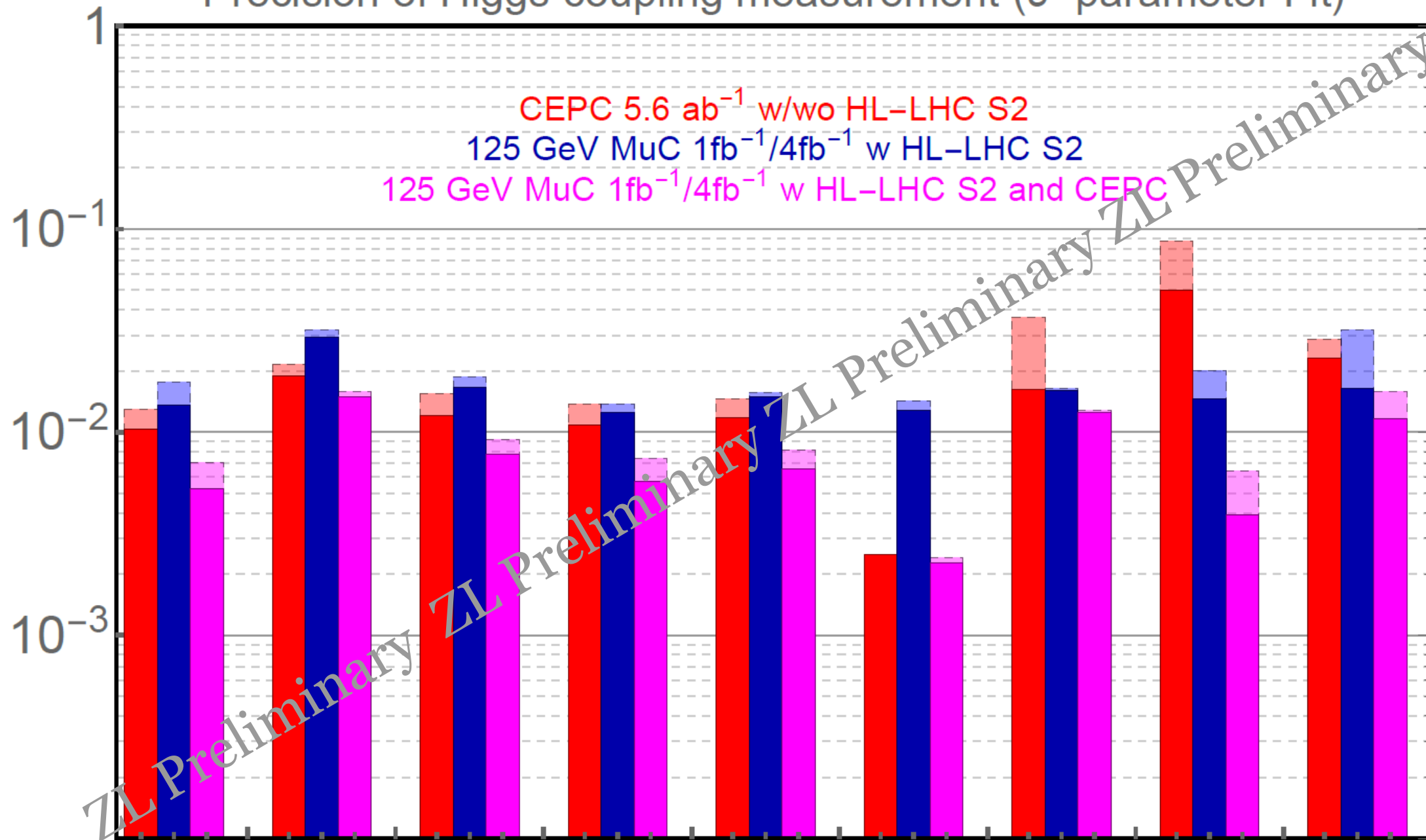
Precision of Higgs coupling measurement (9-parameter Fit)

Relative Error

CEPC 5.6 ab^{-1} w/wo HL-LHC S2

125 GeV MuC 1 fb^{-1} /4 fb^{-1} w HL-LHC S2

125 GeV MuC 1 fb^{-1} /4 fb^{-1} w HL-LHC S2 and CEPC

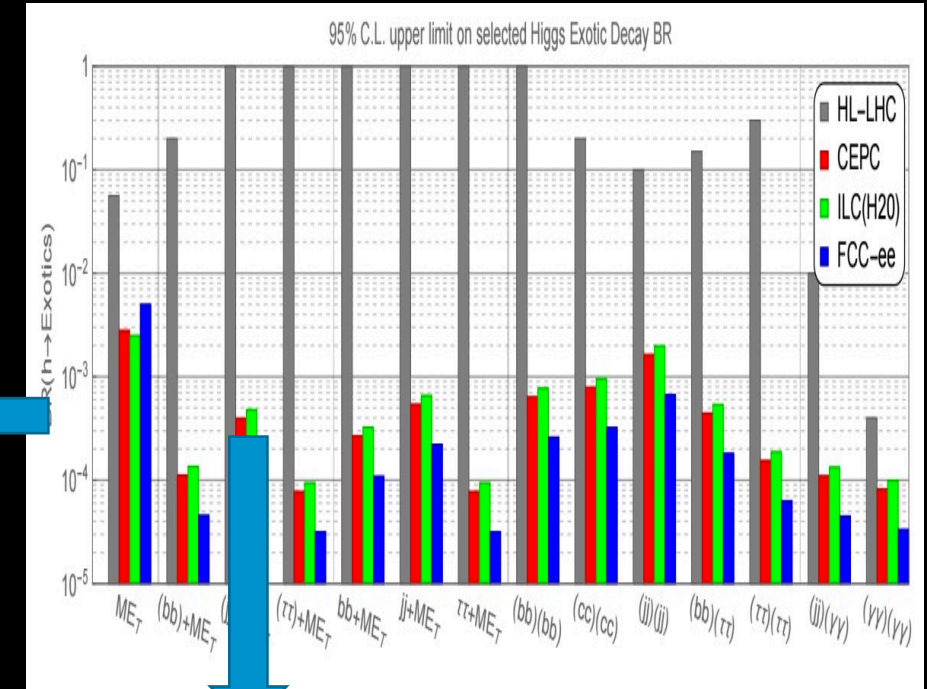


κ_γ	1.00	0.66	0.57	0.29	0.18	0.65	0.66	0.27
κ_W	0.66	1.00	0.58	0.39	0.25	0.74	0.59	0.27
κ_Z	0.57	0.58	1.00	0.24	0.24	0.56	0.50	0.23
κ_g	0.29	0.39	0.24	1.00	0.34	0.67	0.43	0.09
κ_t	0.18	0.25	0.24	0.34	1.00	0.38	0.26	0.09
κ_b	0.65	0.74	0.56	0.67	0.38	1.00	0.70	0.26
κ_τ	0.66	0.59	0.50	0.43	0.26	0.70	1.00	0.25
κ_μ	0.27	0.27	0.23	0.09	0.09	0.26	0.25	1.00
	κ_γ	κ_W	κ_Z	κ_g	κ_t	κ_b	κ_τ	κ_μ

L = 3000 fb ⁻¹		Expected uncertainty [%]				
POI	Scenario	Total	Stat	SigTh	BkgTh	Expt
κ_γ	S1	2.9	1.1	1.8	1.0	1.7
	S2	2.0	1.1	0.9	0.8	1.2
κ_W	S1	2.6	1.0	1.7	1.1	1.1
	S2	1.8	1.0	0.9	0.8	0.8
κ_Z	S1	2.4	1.0	1.7	0.9	0.9
	S2	1.7	1.0	0.9	0.7	0.7
κ_g	S1	4.0	1.1	3.4	1.3	1.2
	S2	2.5	1.1	1.7	1.1	1.0
κ_t	S1	5.5	1.0	4.4	2.7	1.6
	S2	3.5	1.0	2.2	2.1	1.2
κ_b	S1	6.0	2.0	4.3	2.9	2.3
	S2	4.0	2.0	2.0	2.2	1.8
κ_τ	S1	2.8	1.2	1.8	1.1	1.4
	S2	2.0	1.2	1.0	0.9	1.0
κ_μ	S1	6.7	4.7	2.5	1.0	3.9
	S2	5.0	4.7	1.3	0.8	1.1

Exotic Decay Outlook

- Higgs Exotic decays is a very important component of Higgs program at future colliders
- Lepton colliders show great advantage for decays that are very challenging at the LHC, such as Higgs decays into jets and Higgs decays with missing energy
- Hadron colliders and lepton colliders are complementary* in probing Higgs exotic decays and could together provide a much more coherent picture for discovery
- Many more interesting work for Higgs exotic decays at both the LHC and future colliders are needed**:
 - More channels (potential statistical improvement)
 - Light masses
 - Semi-visible
 - Higgs into dark showers
 - Weird signatures (LLPs, Quirks, etc.)



Statistical limit

* LC usually have 1 Million clean Higgs boson produced, HL-LHC has 0.2 Billion.

Also complementary to the Z-pole runs of Lepton colliders. For instance, heavy neutral leptons (HNLs) are better probed at Tera-Z factories. Flavor non-Universal theories induced Higgs exotic decays, e.g., Chiu, ZL, Wang, [1909.04549](#)

**See many of the [Snowmass Energy Frontier LOIs](#)