

2HDM @ a High Energy Muon Collider



Shufang Su • U. of Arizona

T. Han, S. Li, SS, W. Su, Y. Wu,
work in progress

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Outline

- Higgses in 2HDM
- Pair Production of BSM Higgs @ muon collider
- Fermion associated single production
- Conclusion

Why 2HDM?

Models with extended Higgs sector: arise in natural theories of EWSB

- Higgs sector of MSSM/NMSSM
- Generic 2HDM
- Little Higgs, twin Higgs ...
- Composite Higgs models ...

- SM+singlet: parametrized by a simple mixing parameter
- 2HDM: covers board class of known models
- Allow for convenient parametrization
- Many features shared by many extended EWSB sectors

2HDM Higgs Sector

Two Higgs Doublet Model (CP-conserving)

$$\Phi_i = \begin{pmatrix} \phi_i^+ \\ (v_i + \phi_i^0 + iG_i)/\sqrt{2} \end{pmatrix}$$

$$v_u^2 + v_d^2 = v^2 = (246\text{GeV})^2$$
$$\tan \beta = v_u/v_d$$

$$\begin{pmatrix} H^0 \\ h^0 \end{pmatrix} = \begin{pmatrix} \cos \alpha & \sin \alpha \\ -\sin \alpha & \cos \alpha \end{pmatrix} \begin{pmatrix} \phi_1^0 \\ \phi_2^0 \end{pmatrix}, \quad \begin{aligned} A &= -G_1 \sin \beta + G_2 \cos \beta \\ H^\pm &= -\phi_1^\pm \sin \beta + \phi_2^\pm \cos \beta \end{aligned}$$

after EWSB, 5 physical Higgses

CP-even Higgses: h, H , CP-odd Higgs: A , Charged Higgses: H^\pm

Search for extra Higgses

→ Precision Higgs study: couplings of the SM-like Higgs

→ Direct search of extra Higgses: direct evidence for BSM new physics

2HDM Higgs Sector

- h/H VV coupling

$$g_{H^0 VV} = \frac{m_V^2}{v} \cos(\beta - \alpha), \quad g_{h^0 VV} = \frac{m_V^2}{v} \sin(\beta - \alpha).$$

- Higgs-Higgs-V coupling

$$\begin{aligned} g_{AH^0 Z} &= -\frac{g \sin(\beta - \alpha)}{2 \cos \theta_w} (p_{H^0} - p_A)^\mu, & g_{Ah^0 Z} &= \frac{g \cos(\beta - \alpha)}{2 \cos \theta_w} (p_{h^0} - p_A)^\mu, \\ g_{H^\pm H^0 W^\mp} &= \frac{g \sin(\beta - \alpha)}{2} (p_{H^0} - p_{H^\pm})^\mu, & g_{H^\pm h^0 W^\mp} &= \frac{g \cos(\beta - \alpha)}{2} (p_{h^0} - p_{H^\pm})^\mu, \\ g_{H^\pm A W^\mp} &= \frac{g}{2} (p_A - p_{H^\pm})^\mu, \end{aligned}$$

Two non-SM like Higgses have unsuppressed couplings to gauge boson.

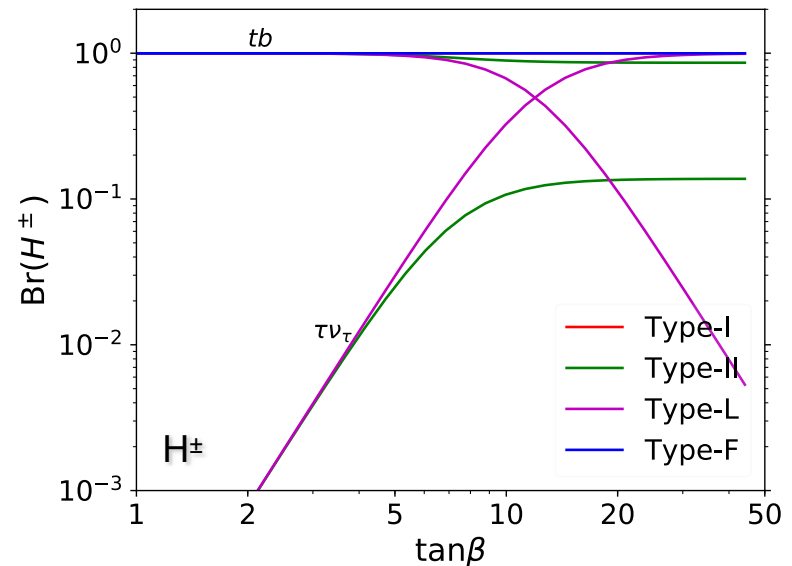
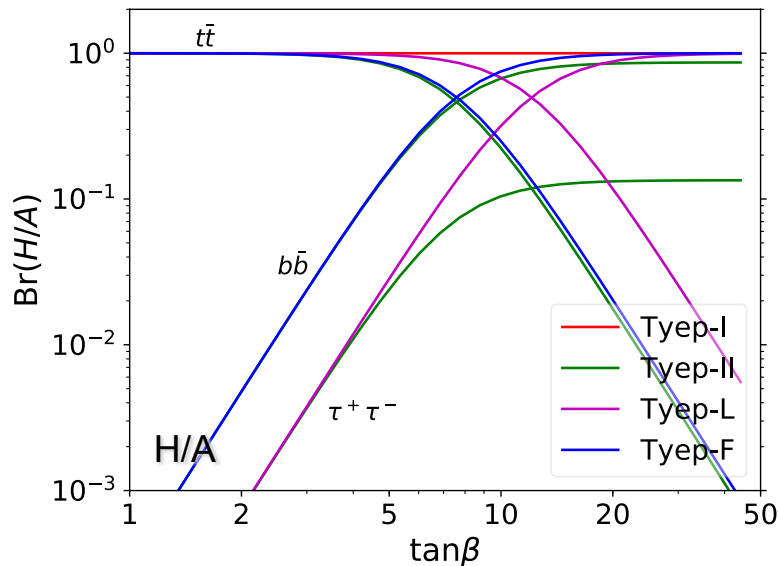
Alignment limit

• h 125 GeV, $\cos(\beta - \alpha) \sim 0$

Four Types of 2HDMs

- Flavor limits: Type I, Type II, lepton-specific, flipped, ...

Types	Φ_1	Φ_2	κ_A^u	κ_A^d	κ_A^e
Type-I		u, d, ℓ	$\cot \beta$	$-\cot \beta$	$-\cot \beta$
Type-II	d, ℓ	u	$\cot \beta$	$\tan \beta$	$\tan \beta$
Type-L	ℓ	$u, d,$	$\cot \beta$	$-\cot \beta$	$\tan \beta$
Type-F	d	u, ℓ	$\cot \beta$	$\tan \beta$	$-\cot \beta$



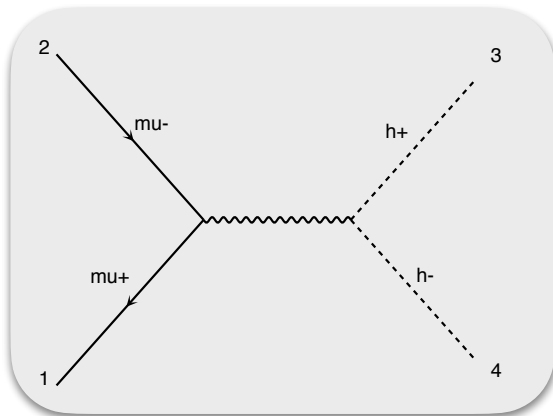
Pair Production

◎ Pair production

Annihilation

$$\mu^+ \mu^- \rightarrow \gamma^*, Z^* \rightarrow H^+ H^-$$

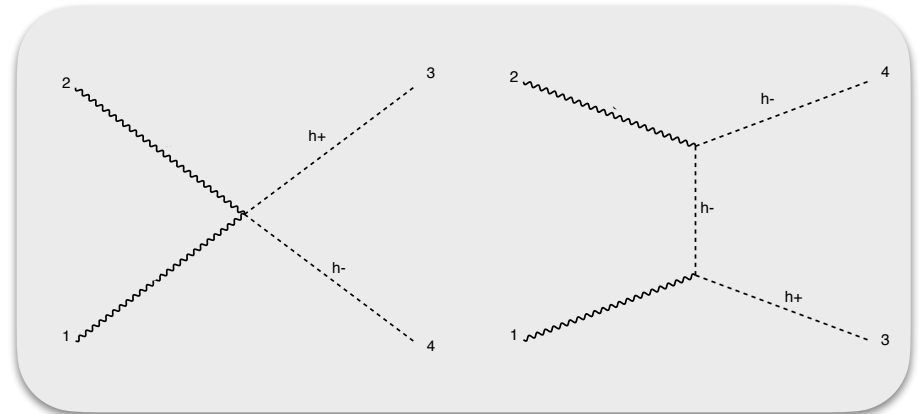
$$\mu^+ \mu^- \rightarrow Z^* \rightarrow H A$$



VBF

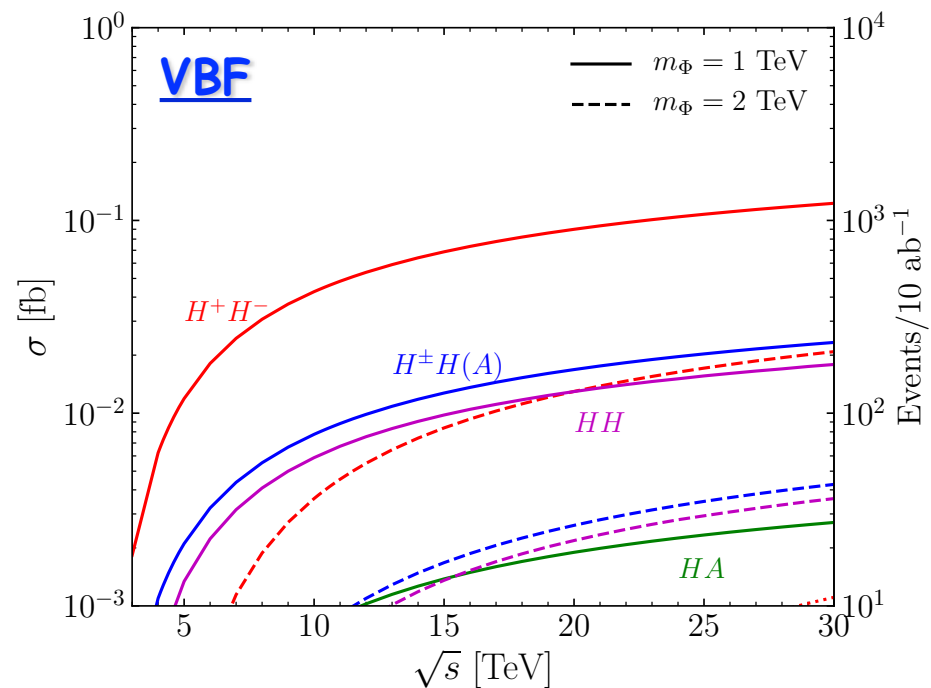
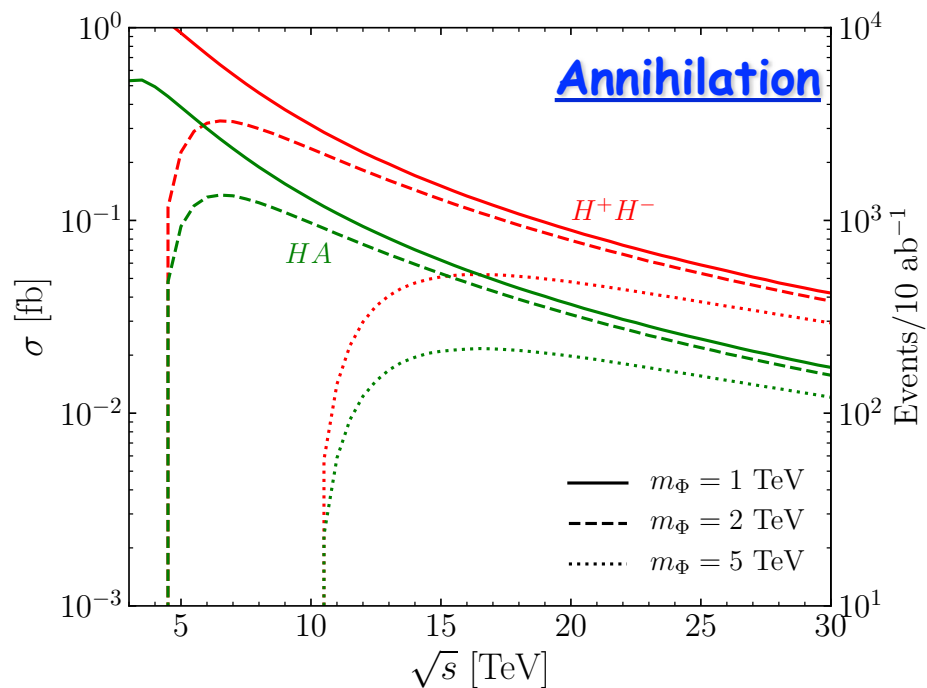
$$\mu^+ \mu^- \rightarrow V_1 V_2 \rightarrow$$

$$H^+ H^-, H A, H^\pm H(A), H H / A A$$



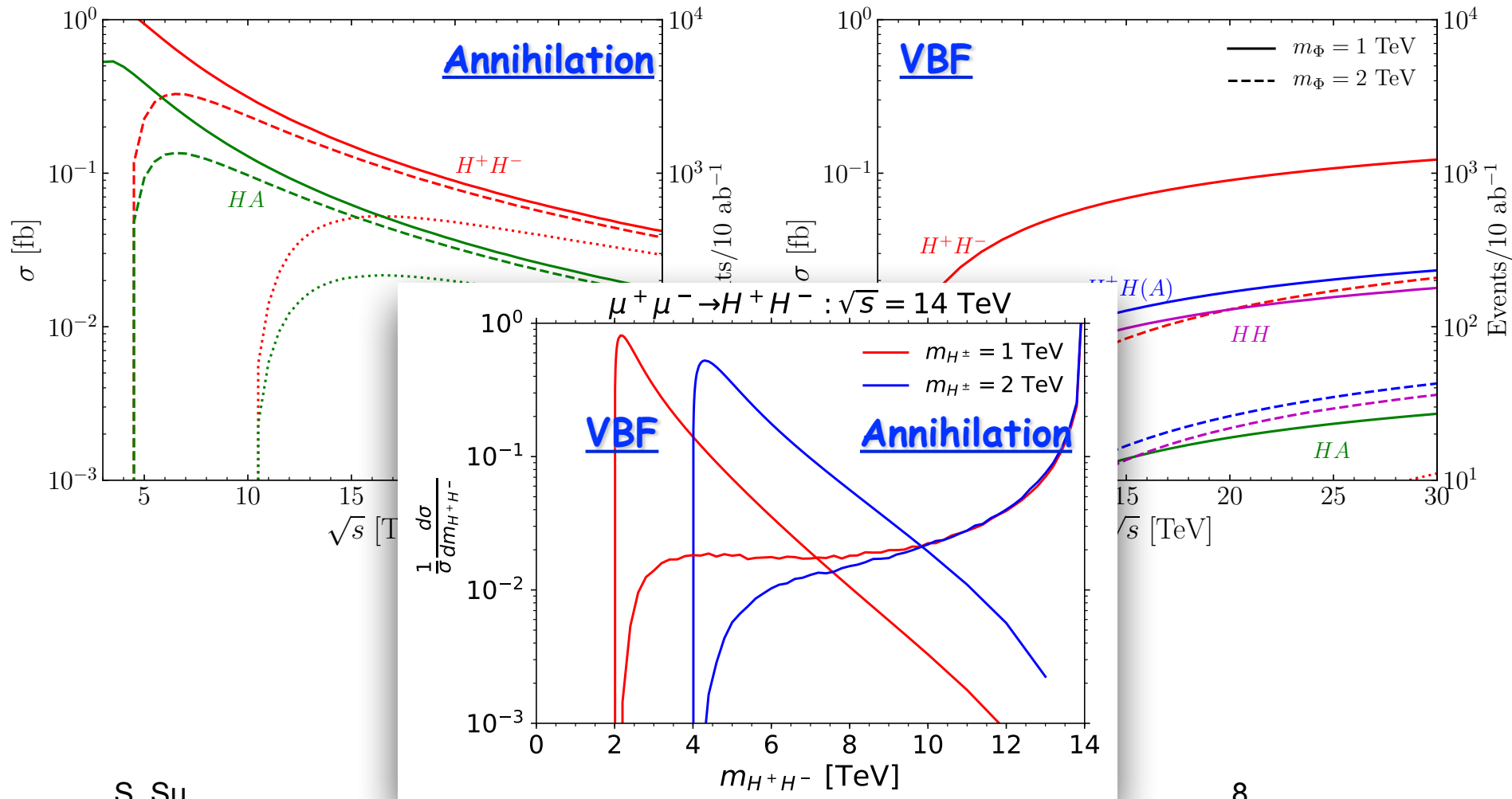
Pair Production

Pair production

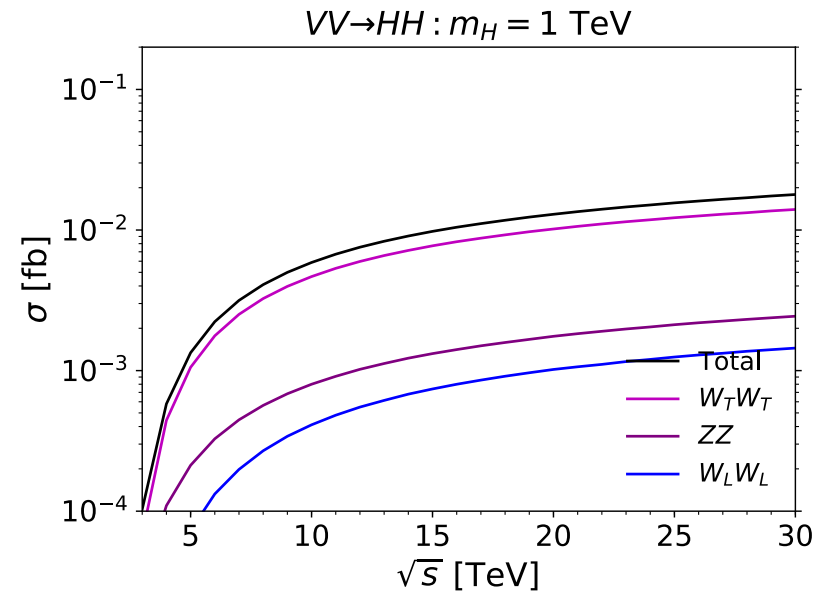
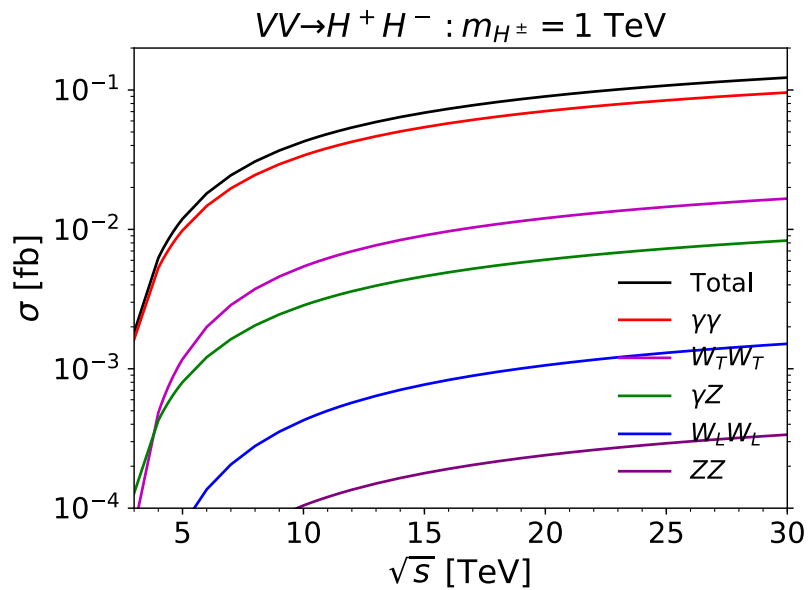


Pair Production

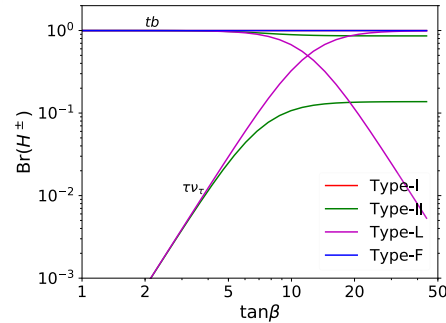
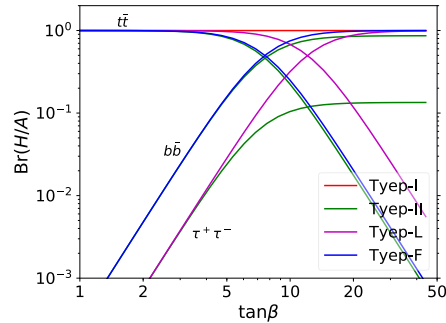
Pair production



Four Types of 2HDMs



Distinguish 2HDMs



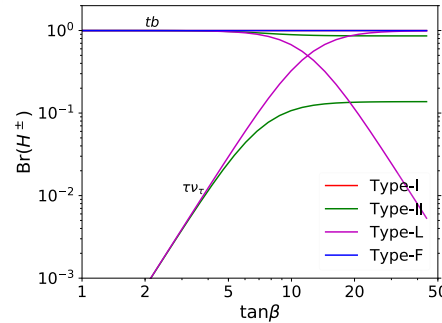
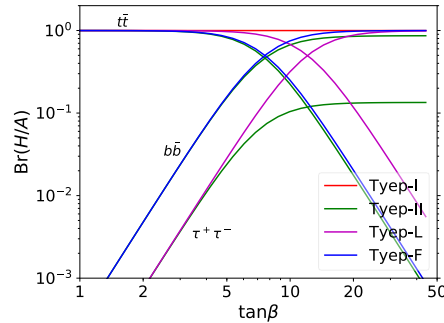
$$Hbb \propto \tan \beta$$

$$H\tau\tau \propto \tan \beta$$

	production	Type-I	Type-II	Type-F	Type-L
small $\tan \beta < 5$	H^+H^- $HA/HH/AA$ $H^\pm H/A$	$t\bar{b}, \bar{t}b$ $t\bar{t}, t\bar{t}$ $tb, t\bar{t}$			
intermediate $\tan \beta$	H^+H^- $HA/HH/AA$ $H^\pm H/A$	$t\bar{t}, t\bar{t}$ $tb, t\bar{t}$	$t\bar{b}, \bar{t}b$ $t\bar{t}, b\bar{b}$ $tb, t\bar{t}; tb, b\bar{b}$	$tb, \tau\nu_\tau$ $t\bar{t}, \tau^+\tau^-$ $tb, t\bar{t}; tb, \tau^+\tau^-;$ $\tau\nu_\tau, t\bar{t}; \tau\nu_\tau, \tau^+\tau^-$	
large $\tan \beta > 10$	H^+H^- $HA/HH/AA$ $H^\pm H/A$	$t\bar{b}, \bar{t}b$ $t\bar{t}, t\bar{t}$ $tb, t\bar{t}$	$tb, tb(\tau\nu_\tau)$ $b\bar{b}, b\bar{b}(\tau^+\tau^-)$ $tb(\tau\nu_\tau), b\bar{b}(\tau^+\tau^-)$	$t\bar{b}, \bar{t}b$ $b\bar{b}, b\bar{b}$ $tb, b\bar{b}$	$\tau^+\nu_\tau, \tau^-\nu_\tau$ $\tau^+\tau^-, \tau^+\tau^-$ $\tau^\pm\nu_\tau, \tau^+\tau^-$

$$H\tau\tau \propto \tan \beta$$

Distinguish 2HDMs



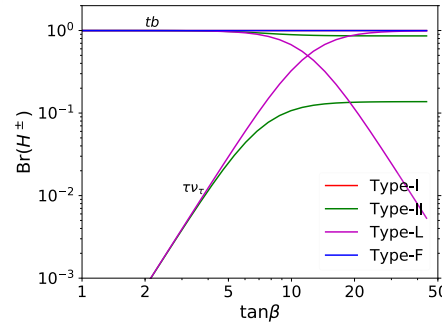
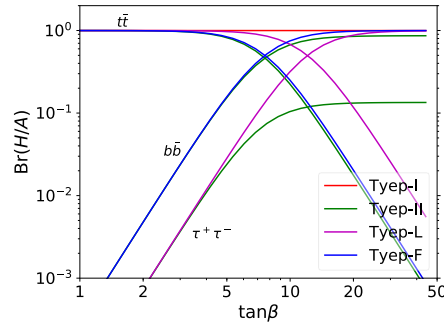
$$Hbb \propto \tan \beta$$

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	production	Type-I	Type-II	Type-F	Type-L
small $\tan \beta < 5$	H^+H^- $HA/HH/AA$ $H^\pm H/A$	<div style="border: 2px solid red; padding: 5px; display: inline-block;"> $tb, \bar{t}\bar{b}$ $t\bar{t}, t\bar{t}$ $tb, t\bar{t}$ </div>			
intermediate $\tan \beta$	H^+H^- $HA/HH/AA$ $H^\pm H/A$	$t\bar{t}, t\bar{t}$ $tb, t\bar{t}$	$t\bar{b}, \bar{t}\bar{b}$ $t\bar{t}, b\bar{b}$ $tb, t\bar{t}; tb, b\bar{b}$		$tb, \tau\nu_\tau$ $t\bar{t}, \tau^+\tau^-$ $tb, t\bar{t}; tb, \tau^+\tau^-;$ $\tau\nu_\tau, t\bar{t}; \tau\nu_\tau, \tau^+\tau^-$
large $\tan \beta > 10$	H^+H^- $HA/HH/AA$ $H^\pm H/A$	$t\bar{b}, \bar{t}\bar{b}$ $t\bar{t}, t\bar{t}$ $tb, t\bar{t}$	$tb, tb(\tau\nu_\tau)$ $b\bar{b}, b\bar{b}(\tau^+\tau^-)$ $tb(\tau\nu_\tau), b\bar{b}(\tau^+\tau^-)$	$t\bar{b}, \bar{t}\bar{b}$ $b\bar{b}, b\bar{b}$ $tb, b\bar{b}$	$\tau^+\nu_\tau, \tau^-\nu_\tau$ $\tau^+\tau^-, \tau^+\tau^-$ $\tau^\pm\nu_\tau, \tau^+\tau^-$

$$H\tau\tau \propto \tan \beta$$

Distinguish 2HDMs



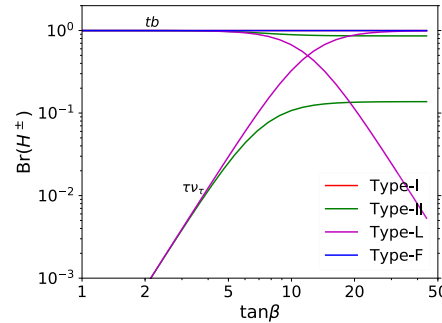
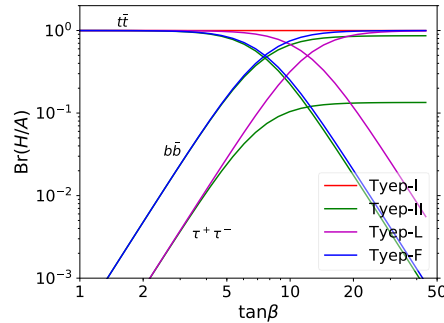
$$Hbb \propto \tan \beta$$

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intermediate $\tan \beta$	$H^+ H^-$ $HA/HH/AA$ $H^\pm H/A$	$t\bar{b}, \bar{t}b$			$tb, \tau\nu_\tau$ $t\bar{t}, \tau^+\tau^-$ $tb, t\bar{t}; tb, \tau^+\tau^-;$ $\tau\nu_\tau, t\bar{t}; \tau\nu_\tau, \tau^+\tau^-$
		$t\bar{t}, t\bar{t}$ $tb, t\bar{t}$	$t\bar{t}, b\bar{b}$ $tb, t\bar{t}; tb, b\bar{b}$		
large $\tan \beta > 10$	$H^+ H^-$ $HA/HH/AA$ $H^\pm H/A$	$t\bar{b}, \bar{t}b$ $t\bar{t}, t\bar{t}$ $tb, t\bar{t}$	$tb, tb(\tau\nu_\tau)$ $b\bar{b}, b\bar{b}(\tau^+\tau^-)$ $tb(\tau\nu_\tau), b\bar{b}(\tau^+\tau^-)$	$t\bar{b}, \bar{t}b$ $b\bar{b}, b\bar{b}$ $tb, b\bar{b}$	$\tau^+\nu_\tau, \tau^-\nu_\tau$ $\tau^+\tau^-, \tau^+\tau^-$ $\tau^\pm\nu_\tau, \tau^+\tau^-$

$$H\tau\tau \propto \tan \beta$$

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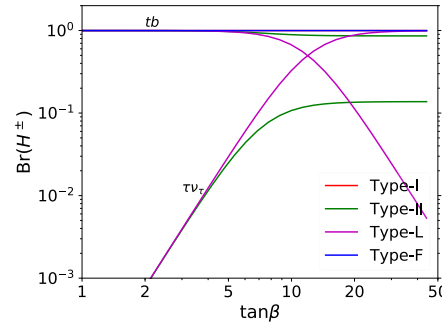
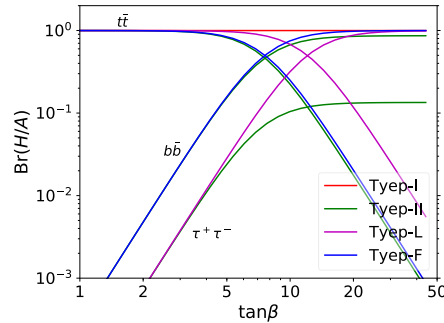
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large $\tan \beta > 10$	H^+H^- $HA/HH/AA$ $H^\pm H/A$	$t\bar{b}, \bar{t}b$ $t\bar{t}, t\bar{t}$ $tb, t\bar{t}$	$tb, tb(\tau\nu_\tau)$ $b\bar{b}, b\bar{b}(\tau^+\tau^-)$ $tb(\tau\nu_\tau), b\bar{b}(\tau^+\tau^-)$	$t\bar{b}, \bar{t}b$ $b\bar{b}, b\bar{b}$ $tb, b\bar{b}$	$\tau^+\nu_\tau, \tau^-\nu_\tau$ $\tau^+\tau^-, \tau^+\tau^-$ $\tau^\pm\nu_\tau, \tau^+\tau^-$

$$H\tau\tau \propto \tan \beta$$

Distinguish 2HDMs



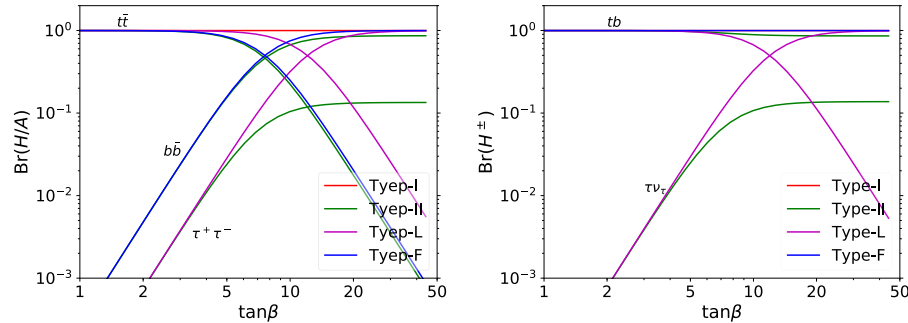
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intermediate $\tan \beta$	H^+H^- $HA/HH/AA$ $H^\pm H/A$	$t\bar{t}, t\bar{t}$ $tb, t\bar{t}$	$t\bar{b}, \bar{t}b$ $t\bar{t}, b\bar{b}$ $tb, t\bar{t}; tb, b\bar{b}$	$tb, \tau\nu_\tau$ $t\bar{t}, \tau^+\tau^-$ $tb, t\bar{t}; tb, \tau^+\tau^-;$ $\tau\nu_\tau, t\bar{t}; \tau\nu_\tau, \tau^+\tau^-$	
large $\tan \beta > 10$	H^+H^- $HA/HH/AA$ $H^\pm H/A$	$t\bar{b}, \bar{t}b$ $t\bar{t}, t\bar{t}$ $tb, t\bar{t}$	$tb, tb(\tau\nu_\tau)$ $b\bar{b}, b\bar{b}(\tau^+\tau^-)$ $tb(\tau\nu_\tau), b\bar{b}(\tau^+\tau^-)$	$t\bar{b}, \bar{t}b$ $b\bar{b}, b\bar{b}$ $tb, b\bar{b}$	$\tau^+\nu_\tau, \tau^-\nu_\tau$ $\tau^+\tau^-, \tau^+\tau^-$ $\tau^\pm\nu_\tau, \tau^+\tau^-$

$$H\tau\tau \propto \tan \beta$$

Distinguish 2HDMs



$$Hbb \propto \tan \beta$$

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	production	Type-I	Type-II	Type-F	Type-L
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intermediate $\tan \beta$	$H^+ H^-$ $HA/HH/AA$ $H^\pm H/A$	$t\bar{t}, t\bar{t}$ $tb, t\bar{t}$	$t\bar{b}, \bar{t}b$ $t\bar{t}, b\bar{b}$ $tb, t\bar{t}; tb, b\bar{b}$	$tb, \tau\nu_\tau$ $t\bar{t}, \tau^+\tau^-$ $tb, t\bar{t}; tb, \tau^+\tau^-;$ $\tau\nu_\tau, t\bar{t}; \tau\nu_\tau, \tau^+\tau^-$	
large $\tan \beta > 10$	$H^+ H^-$ $HA/HH/AA$ $H^\pm H/A$	$t\bar{b}, \bar{t}b$ $t\bar{t}, t\bar{t}$ $tb, t\bar{t}$	$tb, tb(\tau\nu_\tau)$ $b\bar{b}, b\bar{b}(\tau^+\tau^-)$ $tb(\tau\nu_\tau), b\bar{b}(\tau^+\tau^-)$	$t\bar{b}, \bar{t}b$ $b\bar{b}, b\bar{b}$ $tb, b\bar{b}$	$\tau^+\nu_\tau, \tau^-\nu_\tau$ $\tau^+\tau^-, \tau^+\tau^-$ $\tau^\pm\nu_\tau, \tau^+\tau^-$

$$H\tau\tau \propto \tan \beta$$

SM Backgrounds

- Signal: four 3rd generation quarks/leptons
- SM backgrounds

$$p_T(t) > 100 \text{ GeV}, \quad p_T(b) > m_\Phi/5, \quad 10^\circ < \theta < 170^\circ. \quad \Delta R_{bb} > 0.4$$

for H^+H^- channel: $m(t\bar{b}) > 0.9M_{H^\pm}$, $\theta_{tb} < 150^\circ$,

for HA channel: $m(t\bar{t}), m(b\bar{b}) > 0.9M_{H/A}$, $\theta_{tt}, \theta_{bb} < 150^\circ$.

σ (fb)	\sqrt{s} (TeV)	$t\bar{t}b\bar{b}$		$t\bar{t}t\bar{t}$		$b\bar{b}b\bar{b}$	
		$\mu^+\mu^-$	VBF	$\mu^+\mu^-$	VBF	$\mu^+\mu^-$	VBF
H^+H^-	6	6.7×10^{-4}	$\lesssim 10^{-13}$	—	—	—	—
	14	2.3×10^{-3}	1.1×10^{-4}	—	—	—	—
	30	1.4×10^{-3}	5.2×10^{-4}	—	—	—	—
HA	6	$1.4 \times 10^{-3*}$	4.0×10^{-8}	6.1×10^{-5}	$\lesssim 10^{-14}$	7.3×10^{-6}	$\lesssim 10^{-14}$
	14	1.7×10^{-3}	1.7×10^{-4}	9.0×10^{-4}	2.5×10^{-5}	1.4×10^{-4}	3.9×10^{-6}
	30	7.9×10^{-4}	6.8×10^{-4}	6.5×10^{-4}	1.7×10^{-4}	$\sim 10^{-4}$	2.7×10^{-5}

Can be sufficiently suppressed!

Fermion Associated Production

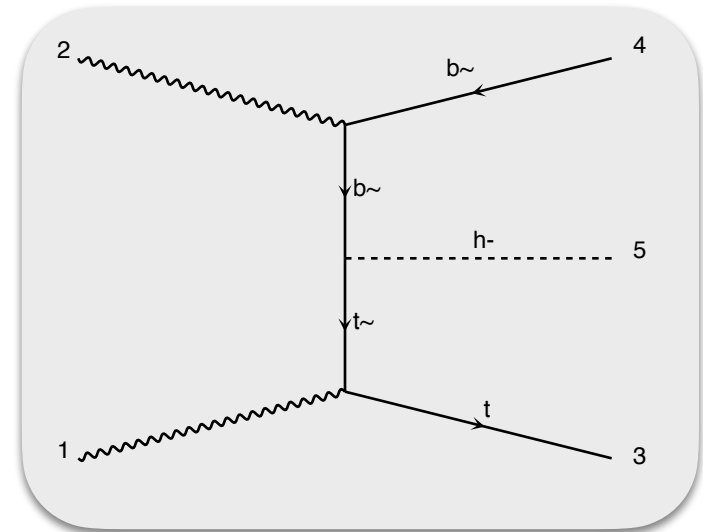
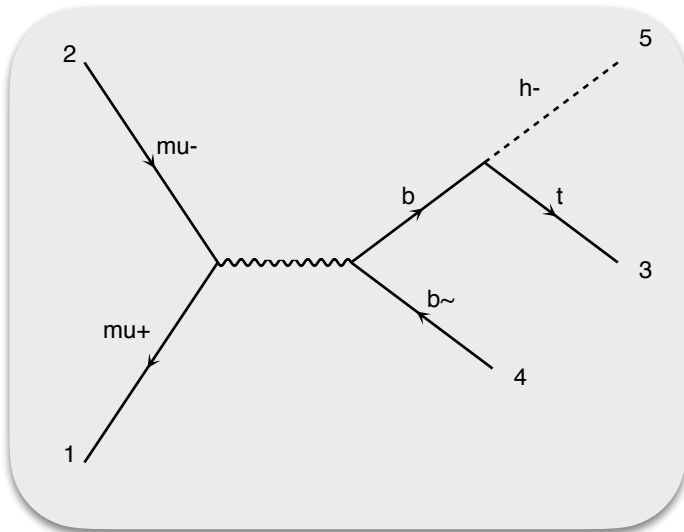
◎ Fermion associated production

Annihilation

$$\begin{aligned} \mu^+ \mu^- &\rightarrow b\bar{b}H/A, t\bar{t}H/A, tbH^\pm, \\ &\rightarrow \tau^+ \tau^- H/A, \tau^\pm \nu_\tau H^\mp, \end{aligned}$$

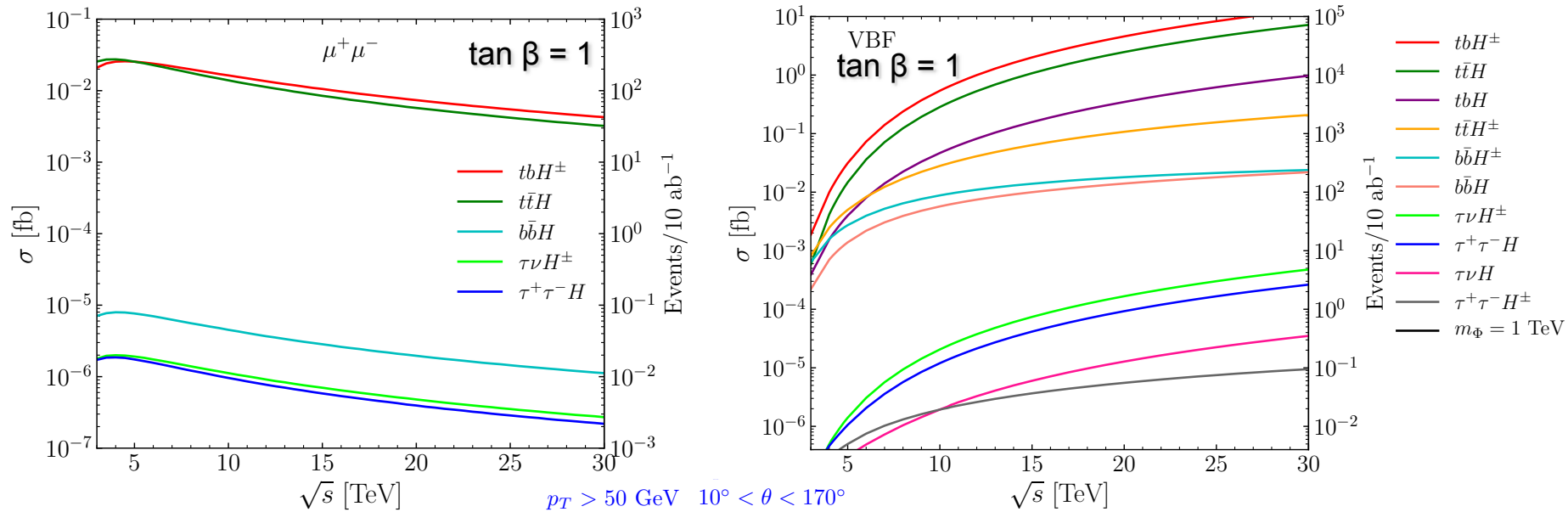
VBF

$$\begin{aligned} \mu^+ \mu^- &\rightarrow b\bar{b}H/A, t\bar{t}H/A, tbH^\pm, t\bar{t}H^\pm, b\bar{b}H^\pm, tbH/A, \\ &\rightarrow \tau^+ \tau^- H/A, \tau^\pm \nu_\tau H^\mp, \tau^+ \tau^- H^\pm, \tau^\pm \nu_\tau H/A. \end{aligned}$$

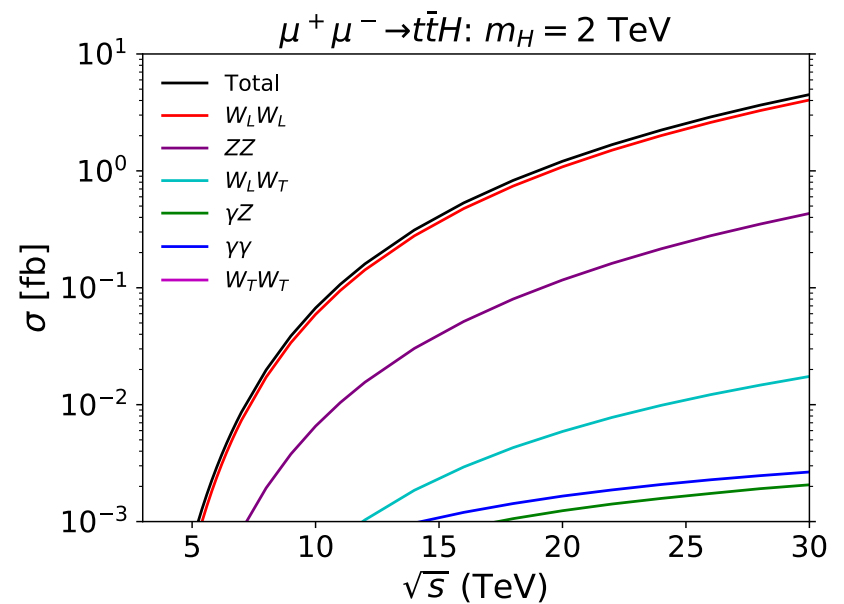
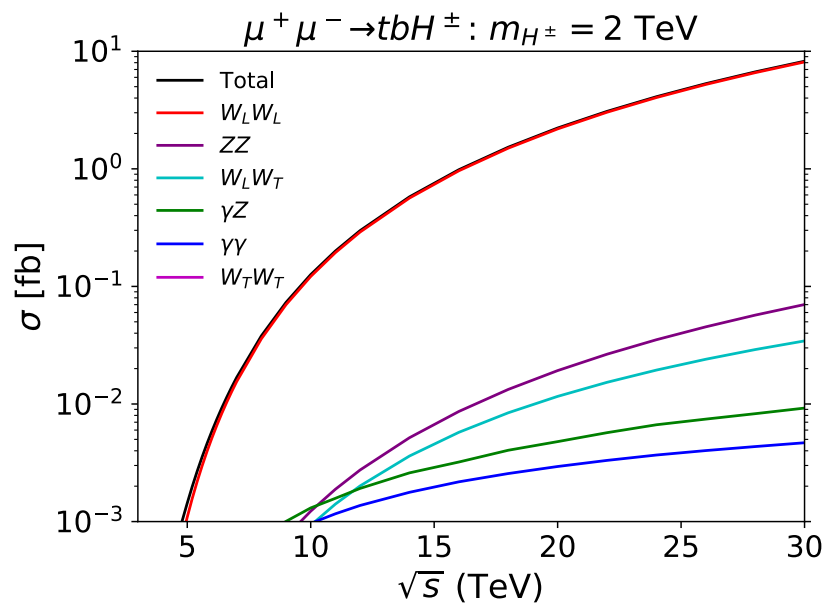


Fermion Associated Production

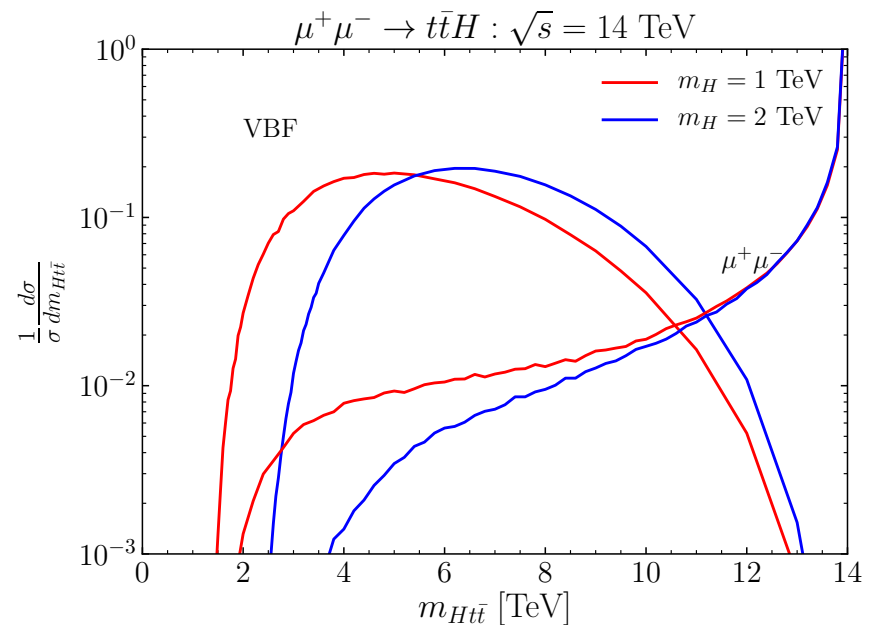
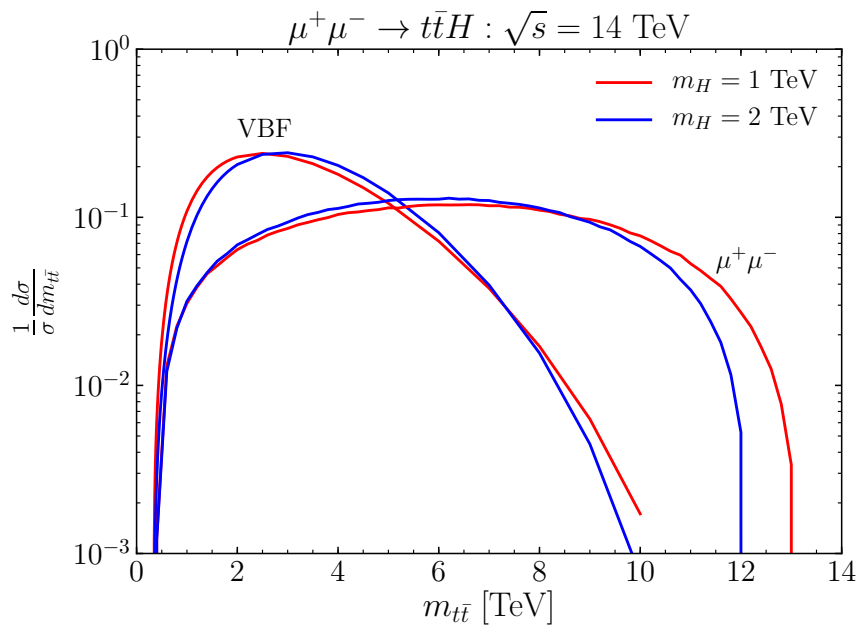
● Fermion associated production



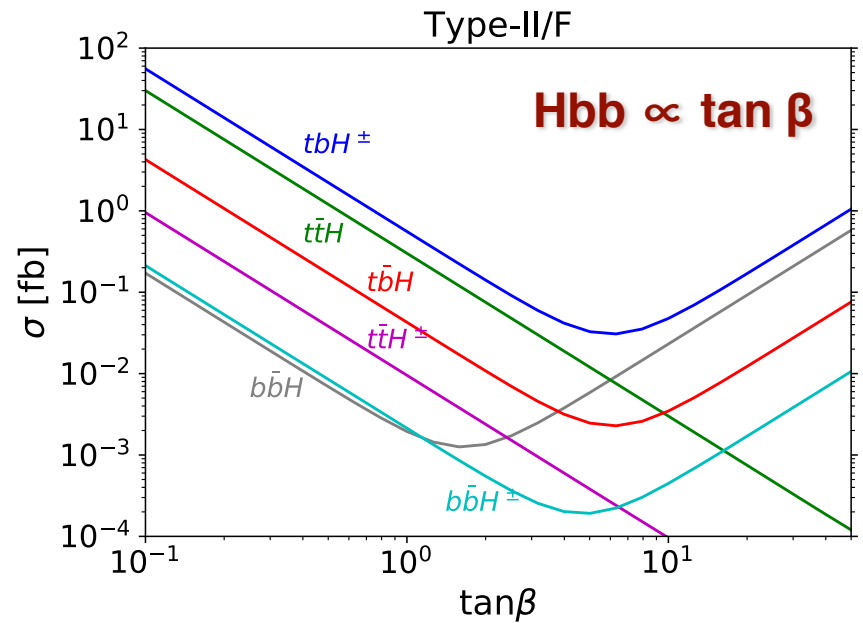
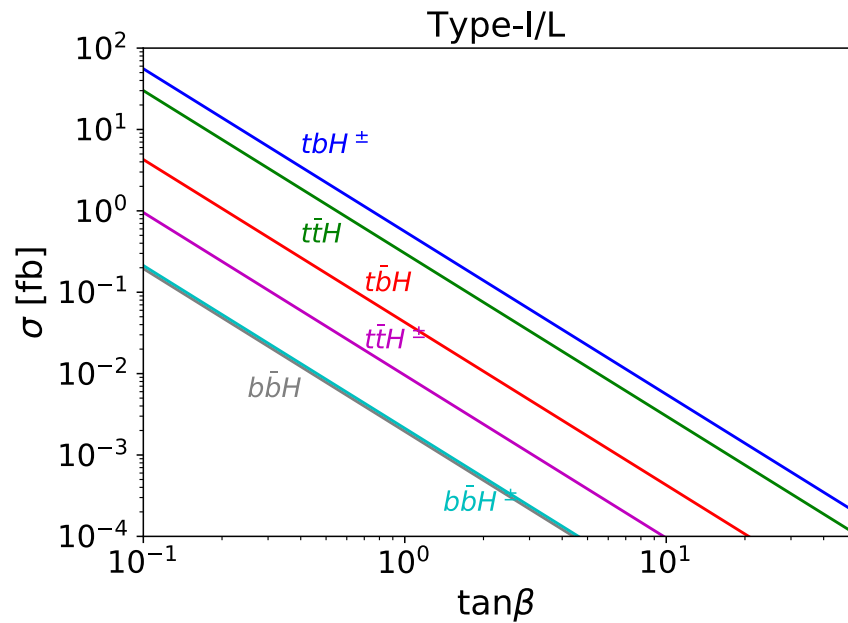
Four Types of 2HDMs



Annihilation vs. VBF



Distinguish 2HDMs



Distinguish 2HDMs

	production	Type-I	Type-II	Type-F	Type-L
small $\tan \beta < 5$	tbH^\pm $t\bar{t}H/A$ (tbH/A)	tb, tb $t\bar{t}, t\bar{t}$ ($tb, t\bar{t}$)			
intermediate $\tan \beta$	tbH^\pm	tb, tb			$tb, tb; tb, \tau\nu_\tau$
	$t\bar{t}H/A$ $b\bar{b}H/A$ (tbH/A)	$t\bar{t}, t\bar{t}$ — ($tb, t\bar{t}$)	$t\bar{t}, t\bar{t}; t\bar{t}, b\bar{b}$ $b\bar{b}, t\bar{t}; b\bar{b}, b\bar{b}$ ($tb, t\bar{t}; tb, b\bar{b}$)		$t\bar{t}, t\bar{t}; t\bar{t}, \tau^+\tau^-$ — ($tb, t\bar{t}; tb, \tau^+\tau^-$)
large $\tan \beta > 10$	tbH^\pm	tb, tb	$tb, tb(\tau\nu_\tau)$	tb, tb	$tb, \tau\nu_\tau$
	$t\bar{t}H/A$	$t\bar{t}, t\bar{t}$	—		$t\bar{t}, \tau^+\tau^-$
	$b\bar{b}H/A$	—	$b\bar{b}, b\bar{b}(\tau^+\tau^-)$	$b\bar{b}, b\bar{b}$	—
	(tbH/A)	($tb, t\bar{t}$)	($tb, b\bar{b}$)		($tb, \tau^+\tau^-$)
very large $\tan \beta > 50$	$\tau^+\tau^-H/A$	—			$\tau^+\tau^-, \tau^+\tau^-$
	$\tau\nu_\tau H^\pm$	—			$\tau\nu_\tau, \tau\nu_\tau$

Conclusion

- ⦿ High energy muon collider: discovery machine for BSM Higgses
- ⦿ BSM Higgs pair production: annihilation dominant
- ⦿ BSM Higgs single production in associated with fermion: VBF dominant
- ⦿ SM BG: manageable
- ⦿ possible to distinguish different types of 2HDM

An exciting journey ahead of us!