

# Dead or Alive? Implications of the Muon Anomalous Magnetic Moment for 3-3-1 Models

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- 1 Introduction  
⇒ Muon Anomalous Magnetic Moment
- 2 3-3-1 Models
- 3 General analytical expressions for the corrections to  $g_\mu - 2$
- 4 Implications of  $g_\mu - 2$  for 3-3-1 Models
- 5 Conclusions

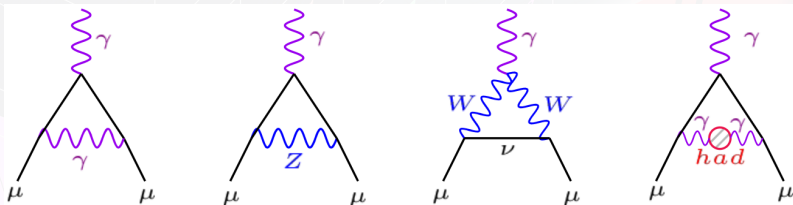
# Introduction: Muon Anomalous Magnetic Moment

$$\vec{\mu}_\mu = g_\mu \frac{q}{2m_\mu} \vec{S} \Rightarrow a_\mu \equiv \frac{g_\mu - 2}{2} = 116591802(2)(42)(26) \times 10^{-11}, \quad a_\mu^{\text{SM}} = a_\mu^{\text{QED}} + a_\mu^{\text{EW}} + a_\mu^{\text{QCD}}$$

1) **Current discrepancy:**  $\Delta a_\mu c = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (261 \pm 78) \times 10^{-11}$  ( $3.3\sigma$ ).<sup>1</sup> Limited by:

**Experimental uncertain:** FERMILAB and J-PARC and **Theoretical uncertain:** hadronic effects

2) **Projected discrepancy:**  $\Delta a_\mu p = a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (261 \pm 34) \times 10^{-11}$  ( $5\sigma$ ).



**Figure 1:** Feynman diagrams of the corrections to  $a_\mu$  on SM interactions.

<sup>1</sup>M. Tanabashi et al. (Particle Data Group), Phys. Rev. D98, 030001 (2018).

## 3-3-1 Models

$$\mathbf{SU(3)}_C \times \mathbf{SU(3)}_L \times \mathbf{U(1)}_X \Rightarrow \frac{Q}{e} = \frac{1}{2} (\lambda_3 + \alpha \lambda_8) + XI, \quad \alpha = -\sqrt{3}, \pm \frac{1}{\sqrt{3}}$$

- 1 MINIMAL 3-3-1 Model, <sup>2</sup>  $\alpha = -\sqrt{3}$
- 2 3-3-1 R.H.N Model<sup>3</sup>,  $\alpha = -\frac{1}{\sqrt{3}}$
- 3 3-3-1 LHN Model (with neutral lepton)<sup>4</sup>,  $\alpha = -\frac{1}{\sqrt{3}}$ ,
- 4 ECONOMICAL 3-3-1 Model <sup>5</sup>
- 5 3-3-1 MODEL WITH EXOTIC LEPTONS,  $\alpha = -\sqrt{3}$ <sup>6</sup>

$$\mathbf{SU(3)}_L \times \mathbf{U(1)}_X \xrightarrow{\langle \chi \rangle} \mathbf{SU(2)}_L \times \mathbf{U(1)}_Y, \text{ and } \mathbf{SU(2)}_L \times \mathbf{U(1)}_Y \xrightarrow{\langle \eta \rangle, \langle \rho \rangle} \mathbf{U(1)}_Q$$

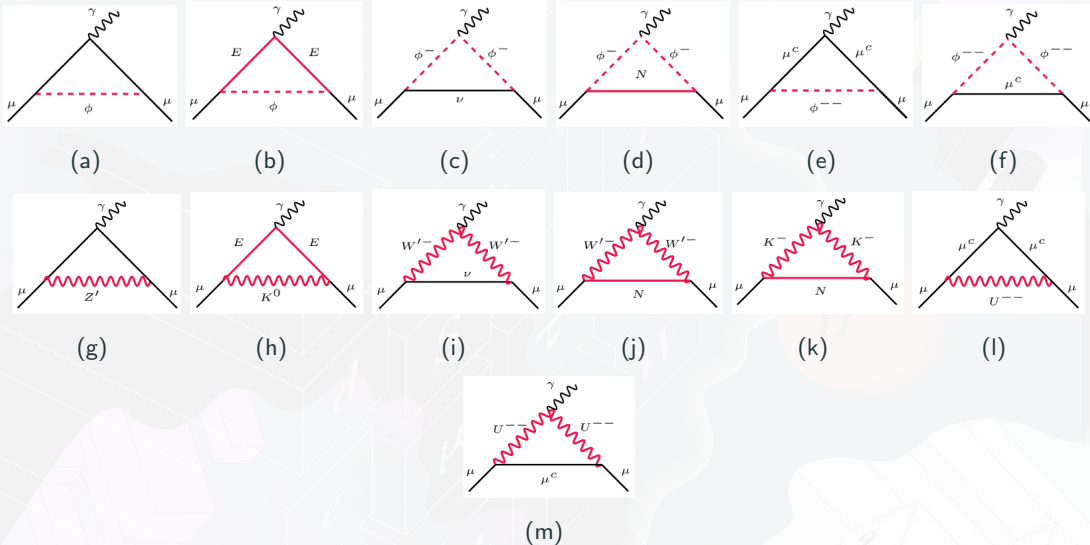
<sup>2</sup>[F. Pisano and V. Pleitez, Phys. Rev. D, 46 (1992), p. 410 arXiv:hep-ph/9206242 [hep-ph]]

<sup>3</sup>[H.N. Long Phys. Rev. D, 54 (1996), p. 4691 arXiv:hep-ph/9607439 [hep-ph]]

<sup>4</sup>M.E. Catano, R. Martinez and F. Ochoa Phys. Rev. D, 86 (2012), Article 073015 arXiv:1206.1966 [hep-ph]

<sup>5</sup>P.V. Dong and H.N. Long Adv. High Energy Phys., 2008 (2008), Article 739492 arXiv:0804.3239 [hep-ph]

<sup>6</sup>W.A. Ponce, J.B. Florez and L.A. Sanchez Int. J. Mod. Phys. A, 17 (2002), p. 643 arXiv:hep-ph/0103100 [hep-ph]



**Figure 2:** Feynman diagrams that contribute to the muon anomalous magnetic moment in the 3-3-1 models investigated in this work.

# Minimal 3-3-1 Model

$$\chi = \begin{pmatrix} \chi^- \\ \chi^{--} \\ \chi^0 \end{pmatrix}, \rho = \begin{pmatrix} \rho^+ \\ \rho^0 \\ \rho^{++} \end{pmatrix}, \eta = \begin{pmatrix} \eta^0 \\ \eta_1^+ \\ \eta_2^+ \end{pmatrix}$$

$$S = \begin{pmatrix} \sigma_1^0 & h_2^- & h_1^+ \\ h_2^- & H_1^{--} & \sigma_2^0 \\ h_1^+ & \sigma_2^0 & H_1^{++} \end{pmatrix}, f_L^a = \begin{pmatrix} \nu^a \\ \ell^a \\ (\ell^c)^a \end{pmatrix}$$

$$\mathcal{L}_1^{CC} \supset -\frac{g}{2\sqrt{2}} \left[ \bar{\nu} \gamma^\mu (1 - \gamma_5) C \bar{I}^T W_\mu'^- - \bar{l} \gamma^\mu \gamma_5 C \bar{I}^T U_\mu^{--} \right]$$

$$\mathcal{L}^{NC} \supset \bar{f} \gamma^\mu [g_V(f) + g_A(f) \gamma_5] f Z_\mu'$$

$$\mathcal{L}_{Yuk} \supset G_I \left[ \bar{l}_R \nu_L \eta_1^- + \bar{l}_R^c \nu_L h_1^+ + \bar{l}_R \nu_L h_2^+ + \bar{l}_R l_L R_{\sigma_2} \right] + h.c.,$$

$$G_I = m_I \sqrt{2} / v_\eta$$

$$v_\eta^2 + v_\rho^2 + v_{\sigma_2}^2 = v^2, \quad v_\eta = v_\rho = 174 \text{ GeV}$$

Masses of the new bosons:

$$M_{W'}^2 = \frac{g^2}{4} \left( v_\eta^2 + v_\chi^2 + v_{\sigma_2}^2 + 2v_{\sigma_1}^2 \right)$$

$$M_U^2 = \frac{g^2}{4} \left( v_\rho^2 + v_\chi^2 + 4v_{\sigma_2}^2 \right)$$

$$M_{Z'}^2 \approx \left( \frac{g^2 + \frac{g'^2}{3}}{3} \right) v_\chi^2$$

$$M_{\eta_1^+}^2 \sim f v_\chi$$

$$M_{h_1^+, h_2^+} \sim v_\chi$$

$$M_{R_{\sigma_2}} \sim v_\chi$$

### 3-3-1 R.H.N Model (with right-handed neutrino)

$$f_L^a = \begin{pmatrix} \nu^a \\ l^a \\ (\nu^c)^a \end{pmatrix}; l_R^i \quad \chi = \begin{pmatrix} \chi^0 \\ \chi^- \\ \chi^{0'} \end{pmatrix}, \rho = \begin{pmatrix} \rho^+ \\ \rho^0 \\ \rho^{+'} \end{pmatrix}, \eta = \begin{pmatrix} \eta^0 \\ \eta^- \\ \eta^{0'} \end{pmatrix}$$

$$\mathcal{L}^{CC} \supset -\frac{g}{2\sqrt{2}} [\bar{\nu}_R^c \gamma^\mu (1 - \gamma_5) \bar{l} W_\mu'^-]$$

$$\mathcal{L}_{Yuk} \supset G_{ab} \bar{f}_{aL} \rho e_{bR} \xrightarrow{\text{leads to}} \mathcal{L} \supset G_s \bar{\mu} \mu S_2, \text{ with } G_s = m_\mu \sqrt{2}/(2v)$$

$$M_{Z'}^2 = \frac{g^2}{4(3 - 4s_W^2)} \left( 4c_W^2 v_\chi^2 + \frac{v_\rho^2}{c_W^2} + \frac{v_\eta^2 (1 - 2s_W^2)^2}{c_W^2} \right), \quad M_{W'}^2 = M_{X^0}^2 = \frac{g^2}{4} (v_\eta^2 + v_\chi^2)$$

$$M_{S_2}^2 = \frac{1}{2} (v_\chi^2 + 2v^2(2\lambda_2 - \lambda_6)) \quad \text{and} \quad M_{h^+}^2 = \frac{\lambda_8 + \frac{1}{2}}{2} (v^2 + v_\chi^2)$$

$$v_\eta^2 + v_\rho^2 = v^2 \Rightarrow v_\rho = v_\eta = v/\sqrt{2}$$

## 3-3-1 LHN Model

$$f_L^a = \begin{pmatrix} v^a \\ l^a \\ N^a \end{pmatrix}; l_R^a, N_R^a$$

$$\mathcal{L}^{\text{L.H.N}} \supset -\frac{g}{\sqrt{2}} [N_L \gamma^\mu \bar{l}_L W_\mu^-]$$

$$\mathcal{L}_{\text{Yuk.}}^{\text{L.H.N}} \supset G_{\ell} \bar{l}_R N_L h_1^- + G_{\ell} \bar{\nu}_L h_2^+ + G_s \bar{\mu} \mu S_2$$

$$M_{h_1^-}^2 = \frac{\lambda_8 + \frac{1}{2}}{2} (v^2 + v_\chi^2), \quad M_{h_2^+}^2 = \frac{v_\chi^2}{2} + \lambda_9 v^2.$$

## ECONOMICAL 3-3-1 Model

$$\chi = \begin{pmatrix} \chi_1^0 \\ \chi_2^- \\ \chi_3^0 \end{pmatrix}, \quad \eta = \begin{pmatrix} \eta_1^+ \\ \eta_2^0 \\ \eta_3^+ \end{pmatrix}$$

$$\langle \eta_2^0 \rangle = v_{\eta_2^0} = v/\sqrt{2}, \quad \langle \chi_1^0 \rangle = v_{\chi_1} = u/\sqrt{2}, \\ \langle \chi_3^0 \rangle = v_{\chi_3^0} = v_\chi/\sqrt{2}u, \quad v \ll v_\chi$$

$$\mathcal{L} \supset G_{ij}^{\ell} \bar{f}_{iL} \eta_{jR} + G_{ij}^{\epsilon} \epsilon_{pmn} (\bar{f}_{iL}^c)_p (f_{jL})_m (\eta)_n \\ \Rightarrow G_{lR} \nu_L \eta_1^+ \text{ and } G_s \bar{\mu} \mu S_2$$

$$M_{\eta_1^+}^2 = \frac{\lambda_4}{2} (u^2 + v^2 + v_\chi^2),$$

$$M_{S_2}^2 = 2\lambda_1 v_\chi^2$$



## 3-3-1 LHN Model

$$f_L^a = \begin{pmatrix} \nu^a \\ l^a \\ N^a \end{pmatrix}; l_R^a, N_R^a$$

$$\mathcal{L}^{\text{L.H.N}} \supset -\frac{g}{\sqrt{2}} [\overline{N}_L \gamma^\mu \bar{l}_L W_\mu']$$

$$\mathcal{L}_{\text{Yuk.}}^{\text{L.H.N}} \supset G_{\ell} \overline{l}_R N_L h_1^- + G_{\ell} \overline{\nu}_L h_2^+ + G_s \bar{\mu} \mu S_2$$

$$M_{h_1^-}^2 = \frac{\lambda_8 + \frac{1}{2}}{2} (v^2 + v_\chi^2), \quad M_{h_2^+}^2 = \frac{v_\chi^2}{2} + \lambda_9 v^2.$$

## ECONOMICAL 3-3-1 Model

$$\chi = \begin{pmatrix} \chi_1^0 \\ \chi_2^- \\ \chi_3^0 \end{pmatrix}, \quad \eta = \begin{pmatrix} \eta_1^+ \\ \eta_2^0 \\ \eta_3^+ \end{pmatrix}$$

$$\langle \eta_2^0 \rangle = v_{\eta_2^0} = v/\sqrt{2}, \quad \langle \chi_1^0 \rangle = v_{\chi_1} = u/\sqrt{2}, \\ \langle \chi_3^0 \rangle = v_{\chi_3^0} = v_\chi/\sqrt{2}u, \quad v \ll v_\chi$$

$$\mathcal{L} \supset G_{ij}^{\ell} \bar{f}_{iL} \eta_{jR} + G_{ij}^{\varepsilon} \varepsilon_{pmn} (\bar{f}_{iL}^c)_p (f_{iL})_m (\eta)_n \\ \Rightarrow G_{lR} v_L \eta_1^+ \text{ and } G_s \bar{\mu} \mu S_2$$

$$M_{\eta_1^+}^2 = \frac{\lambda_4}{2} (u^2 + v^2 + v_\chi^2), \\ M_{S_2}^2 = 2\lambda_1 v_\chi^2$$

### 3-3-1 Model with Exotic Leptons

$$f_{1L} = \begin{pmatrix} \nu_1 \\ l_1 \\ E_1^- \end{pmatrix}; l_1^c; f_{2,3L} = \begin{pmatrix} \nu_{2,3} \\ l_{2,3} \\ N_{2,3} \end{pmatrix}; l_{2,3}^c; f_{4L} = \begin{pmatrix} E_2^- \\ N_3 \\ N_4 \end{pmatrix}; E_2^c; f_{5L} = \begin{pmatrix} N_5 \\ E_3^+ \\ l_3^+ \end{pmatrix}; E_3^c$$

$$\chi_i = \begin{pmatrix} \chi_i^- \\ \chi_i^0 \\ \chi_i^{0'} \end{pmatrix}, \chi_3 = \begin{pmatrix} \chi_3^0 \\ \chi_3^+ \\ \chi_3^{'+} \end{pmatrix}, \quad i = 1, 2,$$

with  $\langle \chi_1 \rangle = (0, 0, v_\chi)^T$ ,  $\langle \chi_2 \rangle = (0, v/\sqrt{2}, 0)^T$  and  $\langle \phi_3 \rangle = (v'/\sqrt{2}, 0, 0)^T$ ,  $v_\chi \gg v$ ,  $v'$ ,  $v' \sim v$

$$\mathcal{L} \supset \frac{g'}{2\sqrt{3}g_W g_W} \bar{\mu} \gamma_\mu (g_V + g_A) \mu Z' - \frac{g}{\sqrt{2}} (\bar{N}_{1L} \gamma_\mu \mu_L + \bar{\mu}_L \gamma_\mu N_{4L}) K_\mu^+ - \frac{g}{\sqrt{2}} (\bar{\mu}_L \gamma_\mu E_L) K_\mu^0 \\ + h_1 \bar{\mu} (1 - \gamma_5) N \chi^+ + h_2 \bar{\mu} E^- \chi^0 + h_3 \bar{\mu} E_2^- \chi^0 + \text{H.c.}$$

$$M_{Z'}^2 = \frac{2}{9} (3g^2 + g'^2) v_\chi^2, \quad M_{K^+}^2 = M_{K^0}^2 = \frac{g^2}{4} (2v_\chi^2 + v^2)$$



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# A call for new physics: The muon anomalous magnetic moment and lepton flavor violation

Manfred Lindner , Moritz Platscher , Farinaldo S. Queiroz  

New Physics Contributions to the Muon Anomalous Magnetic Moment: A Numerical Code  
([arXiv:1403.2309](https://arxiv.org/abs/1403.2309))

## The corrections to $g_\mu - 2$ : Minimal 3-3-1 for heavy bosons

The corrections to  $g_\mu - 2$  arise from the presence of new gauge bosons  $U^{++}$ ,  $Z'$  and  $W'$ , and charged scalar  $\eta_1^-$ . The contributions for **heavy bosons** are given as:

$$\Delta a_\mu (U^{++}) \simeq -2 \frac{1}{\pi^2} \frac{m_\mu^2}{M_U^2} \left| \frac{g}{2\sqrt{2}} \right|^2, \text{ with } M_U \gg m_\mu$$

$$\Delta a_\mu (\nu, W') \simeq \frac{1}{4\pi^2} \frac{m_\mu^2}{M_{W'}^2} \left| \frac{g}{2\sqrt{2}} \right|^2 \left( \frac{5}{3} \right)$$

$$\Delta a_\mu (\mu, Z') \simeq \frac{-1}{4\pi^2} \frac{m_\mu^2}{M_{Z'}^2} \left| \frac{g}{2c_W} \frac{\sqrt{3}\sqrt{1-4s_W^2}}{2} \right|^2 \left( -\frac{4}{27} \right)$$

$$\Delta a_\mu (\eta_1^+) \simeq \frac{-1}{4\pi^2} \frac{m_\mu^2}{M_{\eta_1^+}^2} \left| \frac{m_\mu \sqrt{2}}{2v_\eta} \right|^2 \left( \frac{1}{6} \right), \text{ with } M_{\eta_1^+} \gg m_\mu, m_{\nu_L}$$

## 3-3-1 R.H.N Model

This model induces several corrections to  $g - 2$ , coming from the  $Z', W', h^+$  and  $S_2$ .

$$\Delta a_{\mu}(v, W') \simeq \frac{1}{4\pi^2} \frac{m_{\mu}^2}{M_W^2} \left| \frac{g}{2\sqrt{2}} \right|^2 \left( \frac{5}{3} \right),$$

$$\Delta a_{\mu}(\mu, Z') \simeq \frac{-1}{4\pi^2} \frac{m_{\mu}^2}{M_Z^2} \frac{1}{3} \left| -\frac{g}{4c_W \sqrt{3-4s_W^2}} \right|^2 \left[ -|1-4s_W^2|^2 + 5 \right],$$

$$\Delta a_{\mu}(h^+) \simeq \frac{-1}{4\pi^2} \frac{m_{\mu}^2}{M_{h^+}^2} \left| \frac{m_{\mu} \sqrt{2}}{2v\eta} \right|^2 \frac{1}{6},$$

$$\Delta a_{\mu}(S_2) \simeq \frac{1}{4\pi^2} \frac{m_{\mu}^2}{M_{S_2}^2} \left( \frac{m_{\mu} \sqrt{2}}{2v\eta} \right)^2 \left[ \frac{1}{6} - \left( \frac{3}{4} + \log \left( \frac{m_{\mu}}{M_{S_2}} \right) \right) \right].$$

## 3-3-1 L.H.N Model

The contributions to  $g - 2$  coming from the  $Z', h_1^-$  and  $S_2$  fields are identical to the 3-3-1 r.h.n model.

$$\Delta a_{\mu}(N, W') \simeq \frac{1}{4\pi^2} \frac{m_{\mu}^2}{M_W^2} \left| \frac{g}{2\sqrt{2}} \right|^2 \frac{5}{3},$$

$$\Delta a_{\mu}(h_2^+) \simeq \frac{-1}{4\pi^2} \frac{m_{\mu}^2}{M_{h_2^+}^2} \left| \frac{m_{\mu} \sqrt{2}}{2v\eta} \right|^2 \frac{1}{6}.$$

## 3-3-1 R.H.N Model

This model induces several corrections to  $g - 2$ , coming from the  $Z', W', h^+$  and  $S_2$ .

$$\Delta a_\mu(\nu, W') \simeq \frac{1}{4\pi^2} \frac{m_\mu^2}{M_W^2} \left| \frac{g}{2\sqrt{2}} \right|^2 \left( \frac{5}{3} \right),$$

$$\Delta a_\mu(\mu, Z') \simeq \frac{-1}{4\pi^2} \frac{m_\mu^2}{M_Z^2} \frac{1}{3} \left| -\frac{g}{4c_W \sqrt{3-4s_W^2}} \right|^2 \left[ -|1-4s_W^2|^2 + 5 \right],$$

$$\Delta a_\mu(h^+) \simeq \frac{-1}{4\pi^2} \frac{m_\mu^2}{M_{h^+}^2} \left| \frac{m_\mu \sqrt{2}}{2v_\eta} \right|^2 \frac{1}{6},$$

$$\Delta a_\mu(S_2) \simeq \frac{1}{4\pi^2} \frac{m_\mu^2}{M_{S_2}^2} \left( \frac{m_\mu \sqrt{2}}{2v_\eta} \right)^2 \left[ \frac{1}{6} - \left( \frac{3}{4} + \log \left( \frac{m_\mu}{M_{S_2}} \right) \right) \right].$$

## 3-3-1 L.H.N Model

The contributions to  $g - 2$  coming from the  $Z', h_1^-$  and  $S_2$  fields are identical to the 3-3-1 r.h.n model.

$$\Delta a_\mu(N, W') \simeq \frac{1}{4\pi^2} \frac{m_\mu^2}{M_W^2} \left| \frac{g}{2\sqrt{2}} \right|^2 \frac{5}{3},$$

$$\Delta a_\mu(h_2^+) \simeq \frac{-1}{4\pi^2} \frac{m_\mu^2}{M_{h_2^+}^2} \left| \frac{m_\mu \sqrt{2}}{2v_\eta} \right|^2 \frac{1}{6}.$$

# The corrections to $g_\mu - 2$ : Economical 3-3-1 and 3-3-1 with exotic leptons for heavy bosons

## ECONOMICAL3-3-1 Model

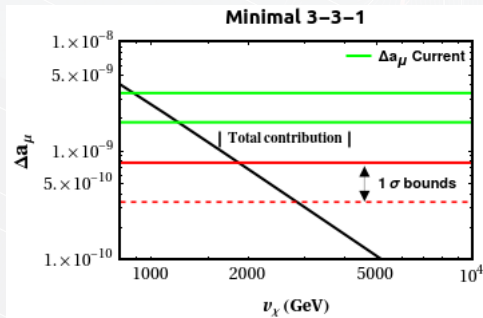
The corrections to  $\Delta a_\mu$  that arise from  $Z'$  and  $W'$  have nearly the same magnitude as in the 3-3-1 R.H.N model.

$$\Delta a_\mu (\eta_1^+) \simeq \frac{-1}{4\pi^2} \frac{m_\mu^2}{M_{\eta_1^+}^2} \left| \frac{m_\mu \sqrt{2}}{2v_\eta} \right|^2 \frac{1}{6}, \quad \Delta a_\mu (S_2) \simeq \frac{1}{4\pi^2} \frac{m_\mu^2}{M_{S_2}^2} \left( \frac{m_\mu \sqrt{2}}{2v_\eta} \right)^2 \left[ \frac{1}{6} - \left( \frac{3}{4} + \log \left( \frac{m_\mu}{M_{S_2}} \right) \right) \right].$$

## 3-3-1 Model with exotic leptons

The corrections to  $g - 2$  coming from the  $Z', K^0$  and  $K^+$  bosons.

$$\Delta a_\mu (N, K^+) \simeq \frac{1}{4\pi^2} \frac{m_\mu^2}{M_{K^+}^2} \left| \frac{g}{\sqrt{2}} \right|^2 \frac{5}{3}, \quad \Delta a_\mu (E, K^0) \simeq \frac{-1}{4\pi^2} \frac{m_\mu^2}{M_{K^0}^2} \left| \frac{g}{\sqrt{2}} \right|^2 \left( \frac{4}{3} \right),$$
$$\Delta a_\mu (\mu, Z') \simeq \frac{-1}{4\pi^2} \frac{m_\mu^2}{M_{Z'}^2} \left| \frac{g'}{2\sqrt{3}s_W c_W} \right|^2 \frac{1}{12} \left[ - \left| (-c_{2W} + 2s_W^2) \right|^2 + 5 \left| (c_{2W} + 2s_W^2) \right|^2 \right].$$



**Figure 3:** Overall contribution to  $\Delta a_\mu$  from the Minimal 3-3-1 model. The green bands are delimited by  $\Delta a_\mu = (261 \pm 78) \times 10^{-11}$ . The current  $1\sigma$  bound is found by requiring  $\Delta a_\mu < 78 \times 10^{-11}$  while the projected bound is obtained for  $\Delta a_\mu < 34 \times 10^{-11}$ .

We used  $M_{Z'} = 0.395v_\chi$ ,  
 $M_{W'} = M_{U^{\pm\pm}} = 0.33v_\chi$ .

**LHC-13 TeV:**

$M_{Z'} > 3.7$  TeV

$M_{W'} > 3.2$  TeV

**$\Delta a_\mu$  Current:**

$M_{Z'} > 434.5$  GeV,

$M_{W'} > 646$  GeV.

**$\Delta a_\mu$  p projected:**

$M_{Z'} > 632$  GeV,

$M_{W'} > 996.1$  GeV.

LHC's limit: A. Nepomuceno and B. Meirose Phys. Rev. D, 101 (2020), Article 035017 arXiv:1911.12783 [hep-ph]



# Results: 3-3-1 R.H.N and Economical Model

We used  $M_{Z'} = 0.395v_\chi$ ,  $M_{W'} = 0.33v_\chi$ .

## 3-3-1 R.H.N Model

LHC-13 TeV:

$M_{Z'} > 2.64$  TeV

$\Delta a_\mu$  Current:  $M_{Z'} > 158$  GeV,  
 $M_{W'} > 133$  GeV.

$\Delta a_\mu$  projected:  $M_{Z'} > 276.5$  GeV,  
 $M_{W'} > 239$  GeV.

## 3-3-1 Economical Model

LHC-13 TeV:

$M_{Z'} > 2.64$  TeV

$\Delta a_\mu$  Current:  $M_{Z'} > 59.3$  GeV,  
 $M_{W'} > 49.5$  GeV.

$\Delta a_\mu$  projected:  $M_{Z'} > 271.4$  GeV,  
 $M_{W'} > 226.7$  GeV.

LHC's limits: M. Lindner, M. Platscher and F.S. Queiroz, Phys. Rep., 731 (2018), p. 1

3-3-1 L.H.N Model: We used  $M_{Z'} = 0.395v_\chi$ ,  $M_{W'} = 0.33v_\chi$ .

LHC-13 TeV<sup>7</sup>:  $M_{Z'} > 2$  TeV

$M_N = 1$  GeV:

$\Delta a_\mu c$ :  $M_{Z'} > 160$  GeV,  $M_{W'} > 134.3$  GeV.

$\Delta a_\mu p$ :  $M_{Z'} > 285$  GeV,  $M_{W'} > 238.3$  GeV.

$M_N = 100$  GeV :

$\Delta a_\mu c$ :  $M_{Z'} > 136.7$  GeV,  $M_{W'} > 114.2$  GeV.

$\Delta a_\mu p$ :  $M_{Z'} > 276.5$  GeV,  $M_{W'} > 231$  GeV.

Model 3-3-1 with exotic leptons: We used  $M_{Z'} = 0.55v_\chi$ ,  $M_{K'} = M_{K^0} = 0.46v_\chi$ .

LHC-13 TeV<sup>8</sup>:  $M_{Z'} > 2.91$  TeV

$M_N = 10$  GeV  $M_E = 150$  GeV:

$\Delta a_\mu c$ :  $M_{Z'} > 429$  GeV,  $M_{W'} > 359$  GeV.

$\Delta a_\mu p$ :  $M_{Z'} > 693$  GeV,  $M_{W'} > 579.6$  GeV.

$M_N = 100$  GeV  $M_E = 150$  GeV:

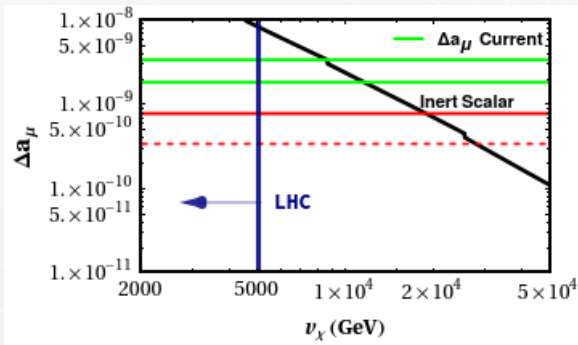
$\Delta a_\mu c$ :  $M_{Z'} > 369$  GeV,  $M_{W'} > 309.1$  GeV.

$\Delta a_\mu p$ :  $M_{Z'} > 600$  GeV,  $M_{W'} > 501.4$  GeV.

<sup>7</sup> M. Lindner, M. Platscher and F.S. Queiroz, Phys. Rep., 731 (2018), p. 1

<sup>8</sup> C. Salazar, R.H. Benavides, W.A. Ponce and E. Rojas J. High Energy Phys., 07 (2015), Article 096 arXiv:1503.03519 [hep-ph]

# Results: Extended version of the 3-3-1 LHN Model



**Figure 4:** Overall contribution of the 3-3-1 LHN model augmented by an inert scalar triplet  $\phi$ .

The inert triplet scalar allows us to include  $\mathcal{L} \supset y_{ab} \bar{f}_a \phi e_{bR}$ .

With  $y_{22} = 1$

Mass scalar:

come from  $\lambda \phi^\dagger \phi \chi^\dagger \chi$

$$M_\phi \sim \lambda v_\chi, \quad \lambda = 0.1$$

This extended version successfully accommodates the  $a_\mu$  anomaly for  $v_\chi \sim 10$  TeV.

# Conclusions

- We concluded that none of the five models investigated here are capable of accommodating the anomaly.
- We derived robust and complementary  $1\sigma$  lower mass bounds on the masses of the new gauge bosons, namely the  $Z'$  and  $W'$  bosons.
- If the anomaly observed in the muon anomalous magnetic moment is confirmed by the  $g-2$  experiment at FERMILAB these models must be extended.
- We presented a plausible extension to the 3-3-1 LHN model, which features an inert scalar triplet.

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## Are 3-4-1 models able to explain the upcoming results of the muon anomalous magnetic moment?

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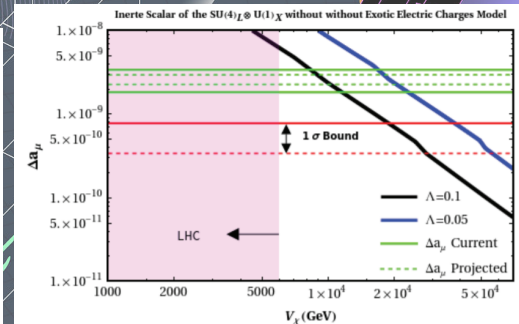
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In light of the upcoming measurement of the muon anomalous magnetic moment ( $g-2$ ), we revisit the corrections to  $g-2$  in the context of the  $SU(4)_L \times U(1)_X$  gauge symmetry. We investigate three models based on this gauge symmetry and express our results in terms of the energy scale at which the  $SU(4)_L \times U(1)_X$  symmetry is broken. To draw solid conclusions we put our findings into perspective with existing collider bounds. Lastly, we highlight the difference between our results and those rising from  $SU(3)_L \times U(1)_X$  constructions.

**Keywords:** Extra gauge bosons; muon anomalous magnetic moment.

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Thank you!