

Transport properties and evolution of the QGP in HICs

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Physics and Compact Stars
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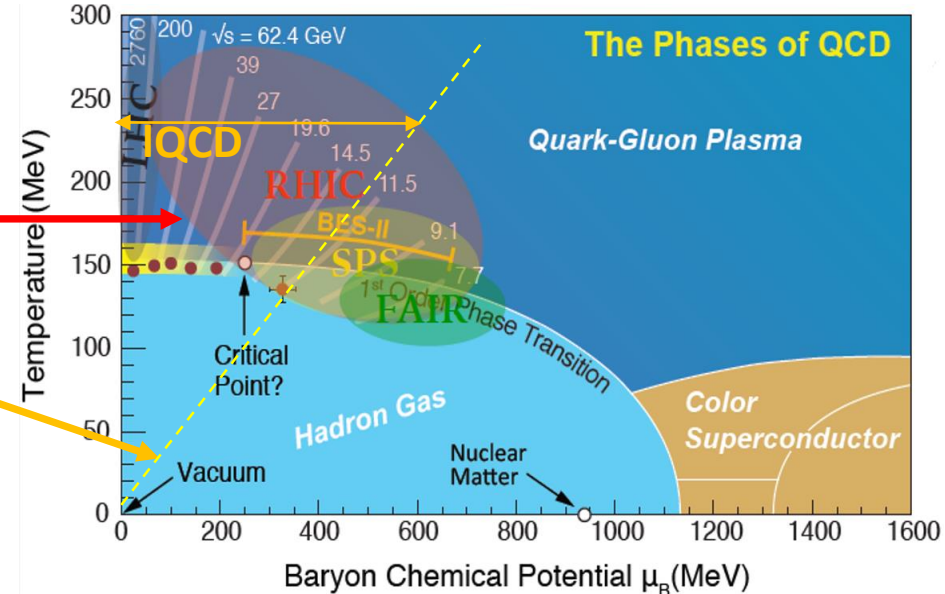


Hipstars

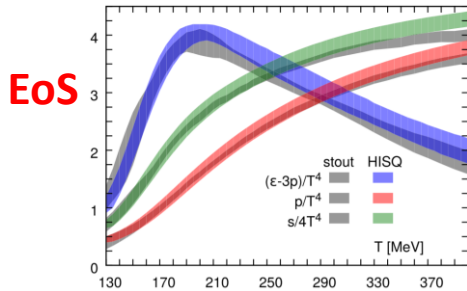
Motivation: QGP at finite baryon density

- Explore the **QCD phase diagram** at finite temperature and chemical potential through heavy-ion collisions
- Available information:
 - Experimental data at SPS, BES at RHIC
 - Lattice QCD calculations

Theoretical sketch of phase diagram



(only for vanishing μ_B)



$$\sigma(\sqrt{s}, m_q, m_q, T, \mu_B)$$

$$m(T, \mu_B)$$

- How to learn about degrees-of-freedom of **QGP** ? →

HIC simulations – transport models



! Problem: Transport models need an input for the **partonic phase**: cross-sections, masses, ...

Solution: effective models

QGP in equilibrium: DQPM and PNJL

Properties of QGP: transport coefficients

Hydrodynamics

$$T^{\mu\nu} = -Pg^{\mu\nu} + wu^\mu u^\nu + \Delta T^{\mu\nu}$$

$$J_B^\mu = n_B u^\mu + \Delta J_B^\mu$$

$$\begin{cases} \partial_\mu J_B^\mu = 0 \\ \partial_\mu T^{\mu\nu} = 0 \end{cases}$$

input for hydro simulations

$$\Delta T^{\mu\nu} = \eta \left(D^\mu u^\nu + D^\nu u^\mu + \frac{2}{3} \Delta^{\mu\nu} \partial_\rho u^\rho \right) - \zeta \Delta^{\mu\nu} \partial_\rho u^\rho$$

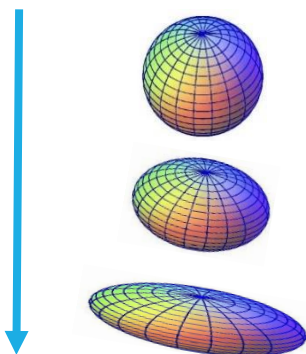
$$\Delta J_B^\mu = \kappa_B D^\mu \left(\frac{\mu_B}{T} \right)$$

$$D^\mu = \Delta^{\alpha\nu} \partial_\nu \quad \Delta^{\mu\nu} = g^{\mu\nu} - u^\mu u^\nu$$

Shear viscosity

Resistance to deformation

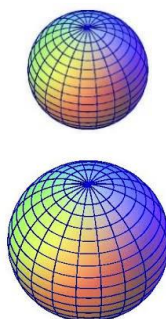
$$\eta \nabla^{\langle\mu} u^{\nu\rangle}$$



Bulk viscosity

Resistance to expansion

$$-\zeta \nabla u$$



Baryon/electric charge
diffusion coefficients

$$\kappa_B \nabla^\mu \frac{\mu_B}{T}$$



Transport coefficients of QGP

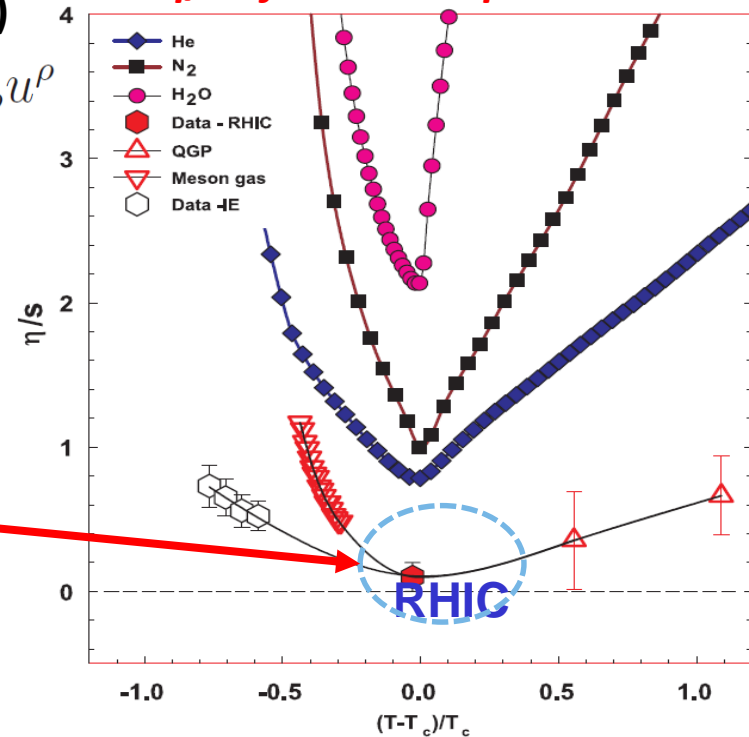
Hydrodynamical model (macroscopic description)

$$\Delta T^{\mu\nu} = \eta \left(D^\mu u^\nu + D^\nu u^\mu + \frac{2}{3} \Delta^{\mu\nu} \partial_\rho u^\rho \right) - \zeta \Delta^{\mu\nu} \partial_\rho u^\rho$$

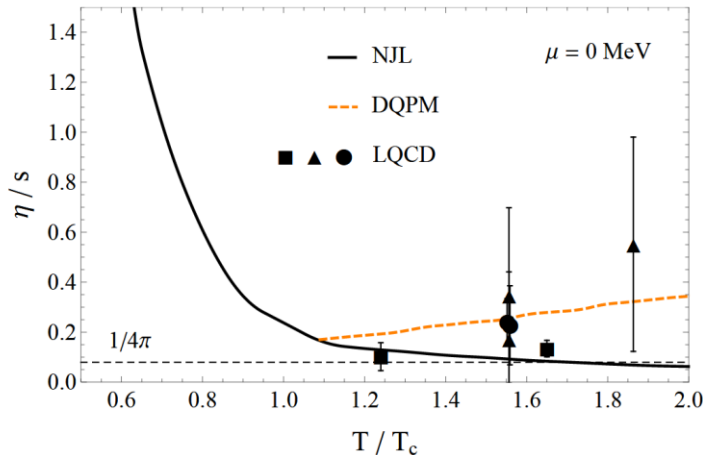
input for hydro simulations

Shear viscosity to entropy density ratio **is extremely small**
QGP is the most ideal liquid!

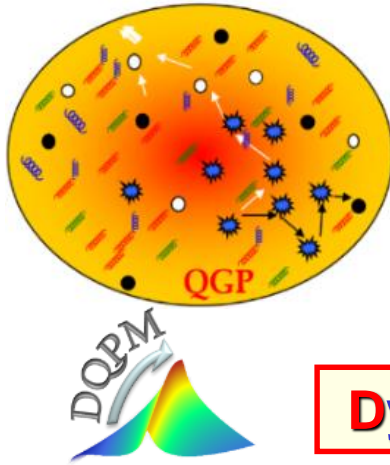
η/s of various liquids



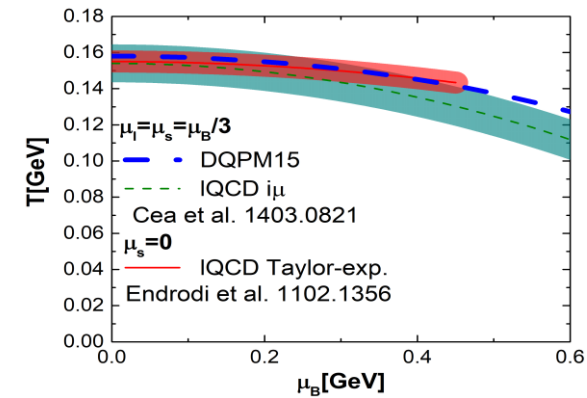
Model predictions:



! Different models using the same EoS can have completely different transport coefficients!



QGP in equilibrium:



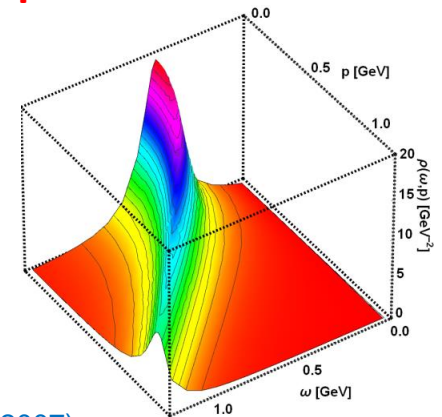
Dynamical QuasiParticle Model (DQPM)

DQPM: consider the **effects of the nonperturbative nature** of the strongly interacting quark-gluon plasma (**sQGP**) constituents (vs. pQCD models)

- The QGP phase is described in terms of **interacting quasiparticles: quarks and gluons** with Lorentzian spectral functions:

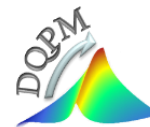
$$\rho_j(\omega, \mathbf{p}) = \frac{\gamma_j}{\tilde{E}_j} \left(\frac{1}{(\omega - \tilde{E}_j)^2 + \gamma_j^2} - \frac{1}{(\omega + \tilde{E}_j)^2 + \gamma_j^2} \right)$$

$$\equiv \frac{4\omega\gamma_j}{(\omega^2 - \mathbf{p}^2 - M_j^2)^2 + 4\gamma_j^2\omega^2}$$



Peshier, Cassing, PRL 94 (2005) 172301; Cassing, NPA 791 (2007) 365; NPA 793 (2007)

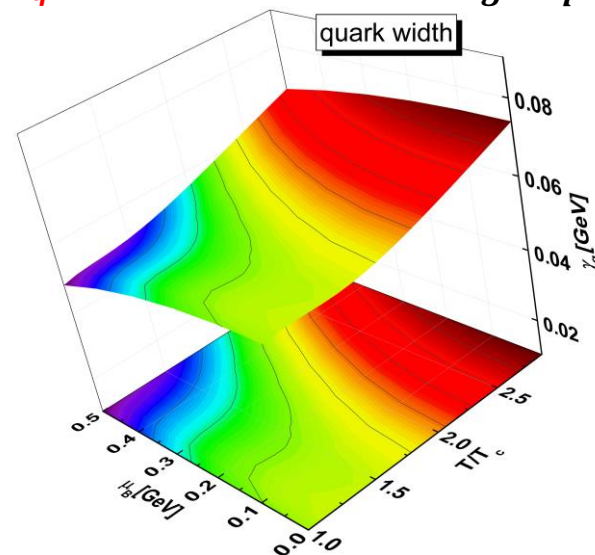
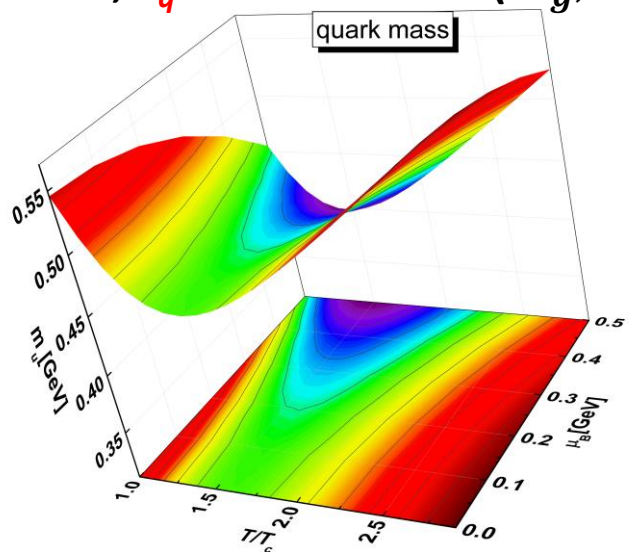
Dynamical QuasiParticle Model (DQPM)



- Resummed properties of the quasiparticles are specified by scalar complex self-energies:

$$\begin{aligned} \text{gluon propagator: } \Delta^{-1} &= P^2 - \Pi & \& \quad \text{quark propagator } S_q^{-1} &= P^2 - \Sigma_q \\ \text{gluon self-energy: } \Pi &= M_g^2 - i2\gamma_g\omega & \& \quad \text{quark self-energy: } \Sigma_q &= M_q^2 - i2\gamma_q\omega \end{aligned}$$

- $\text{Re } \Pi, \Sigma_q$: thermal mass (M_g, M_q) $\text{Im } \Pi, \Sigma_q$: interaction width (γ_g, γ_q)



$$M_{q(\bar{q})}^2(T, \mu_B) = \frac{N_c^2 - 1}{8N_c} g^2(T, \mu_B) \left(T^2 + \frac{\mu_q^2}{\pi^2} \right) \quad \gamma_{q,g}(T, \mu_B) = \frac{c_{A,F}}{3} \frac{g^2(T, \mu_B) T}{8\pi} \ln \left(\frac{2c}{g^2(T, \mu_B)} + 1 \right)$$

- Modeling of the quark/gluon masses and widths (inspired by HTL calculations)

Peshier, Cassing, PRL 94 (2005) 172301; Cassing, NPA 791 (2007) 365; NPA 793 (2007)

DQPM g^2 : fixed within $s(\text{IQCD})$ at $\mu_B=0$

- Input: entropy density as a $f(T, \mu_B = 0)$

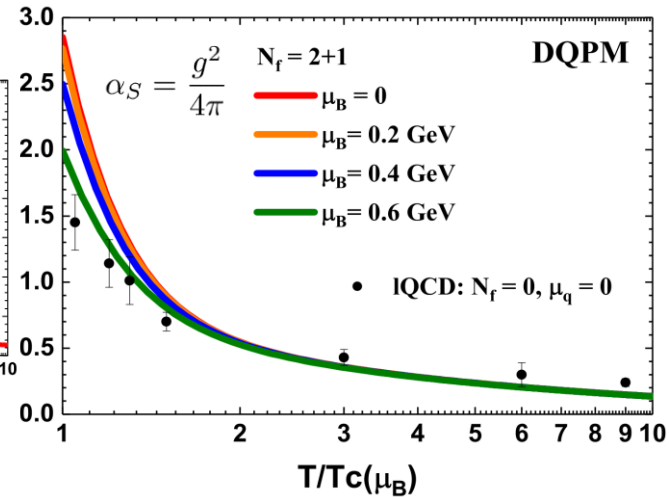
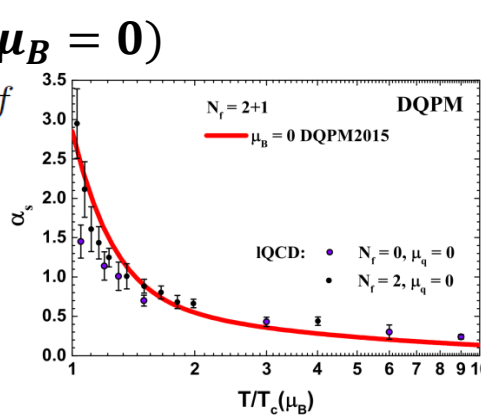
$$g^2(s/s_{SB}) = d((s/s_{SB})^e - 1)^f$$

$$s_{SB}^{QCD} = 19/9\pi^2 T^3$$

$$s^{DQPM}(\Pi, \Delta, S_q, \Sigma) = s^{lattice}$$

fit S from QP to S from IQCD

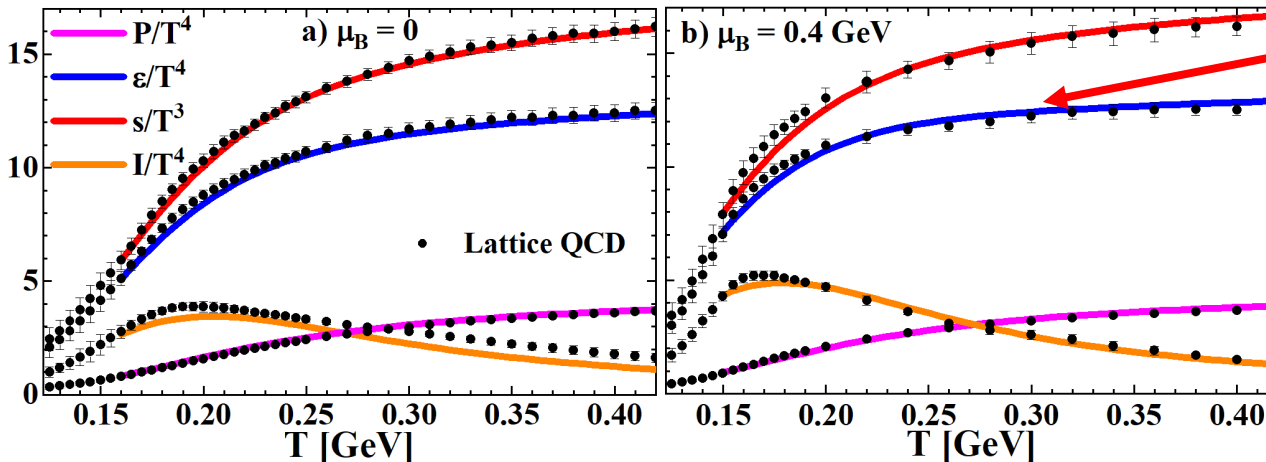
fix the model parameters



- Scaling hypothesis at finite $\mu_B \approx 3\mu_q$

$$g^2(T/T_c, \mu_B) = g^2\left(\frac{T^*}{T_c(\mu_B)}, \mu_B = 0\right) \text{ with the effective temperature } T^* = \sqrt{T^2 + \mu_q^2/\pi^2}$$

Input:
lattice EoS
 $\mu_B = 0$ (dots)

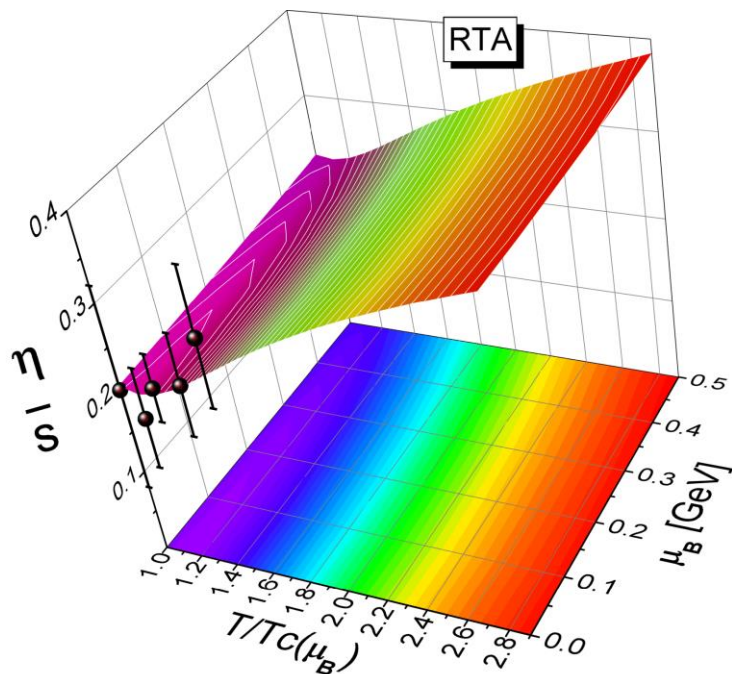
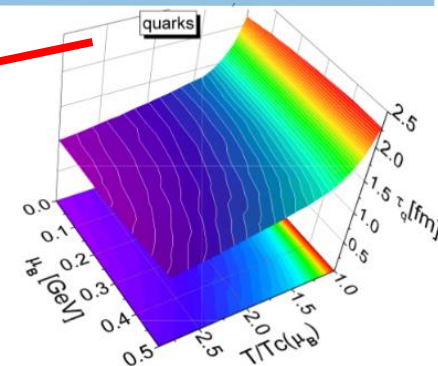


Output:
(lines)
DQPM EoS
 $\mu_B > 0$

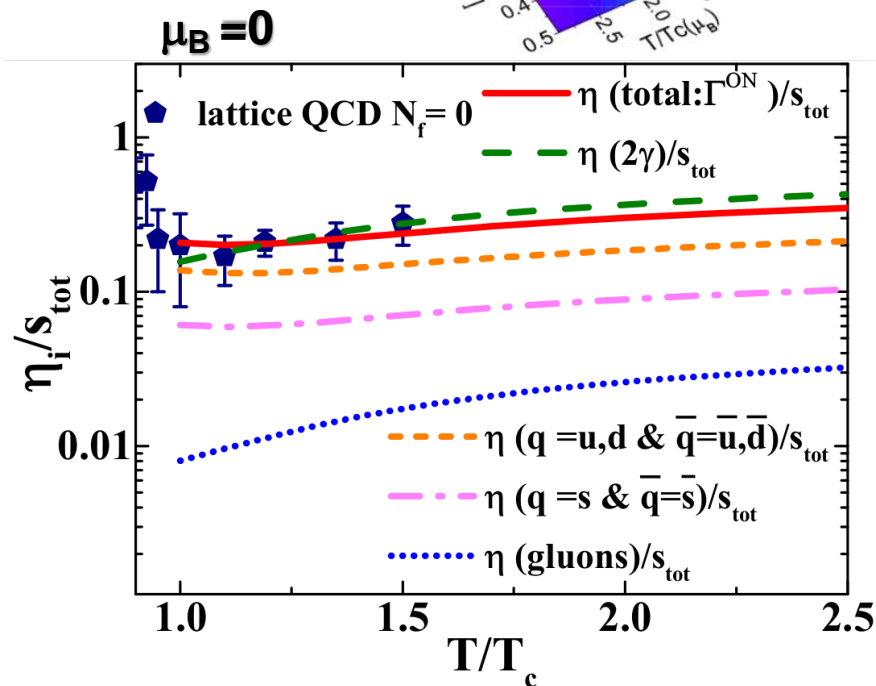
Transport coefficients: specific shear viscosity

$$\eta^{\text{RTA}}(T, \mu_B) = \frac{1}{15T} \sum_{i=q, \bar{q}, g} \int \frac{d^3p}{(2\pi)^3} \frac{\mathbf{p}^4}{E_i^2} \tau_i(\mathbf{p}, T, \mu_B) d_i (1 \pm f_i) f_i$$

Relaxation times



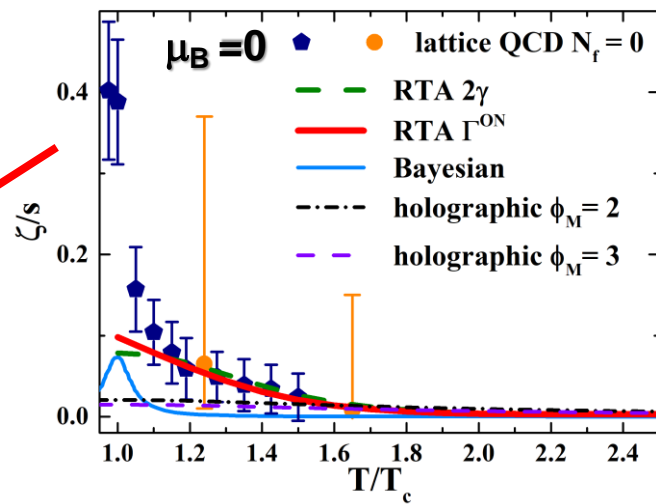
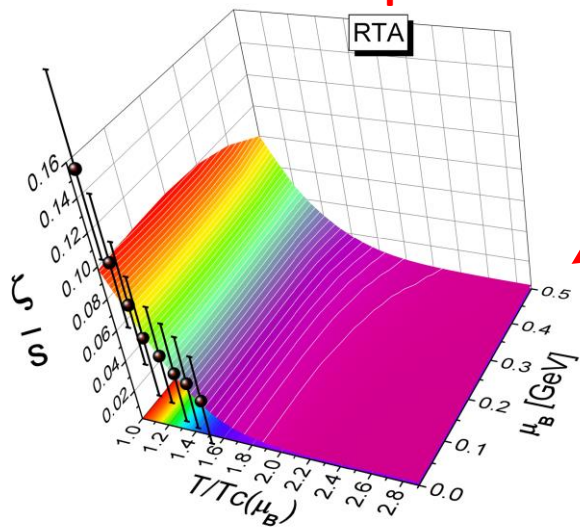
μ_B



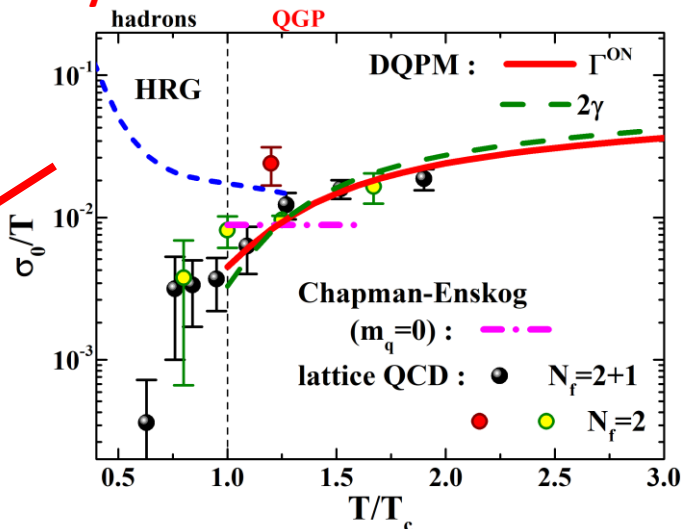
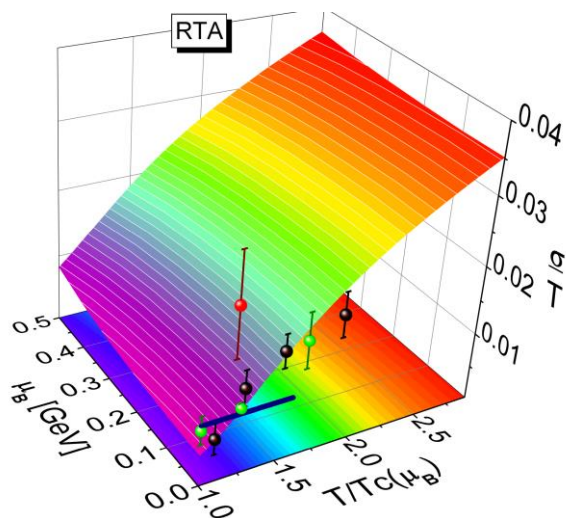
➤ Main contribution comes from light quarks and anti-quarks

Transport coefficients: increasing with μ_B

Specific bulk viscosity



Electric conductivity



Polyakov Nambu Jona-Lasinio (PNJL) model

- Effective lagrangian with the **same symmetries** for the **quark** dof as QCD

$$\mathcal{L}_{PNJL} = \sum_i \bar{\psi}_i (iD - m_{0i} + \mu_i \gamma_0) \psi_i$$

$$+ G \sum_a \sum_{ijkl} \left[(\bar{\psi}_i i\gamma_5 \tau_{ij}^a \psi_j) (\bar{\psi}_k i\gamma_5 \tau_{kl}^a \psi_l) + (\bar{\psi}_i \tau_{ij}^a \psi_j) (\bar{\psi}_k \tau_{kl}^a \psi_l) \right]$$

$$- K \det_{ij} [\bar{\psi}_i (-\gamma_5) \psi_j] - K \det_{ij} [\bar{\psi}_i (+\gamma_5) \psi_j]$$

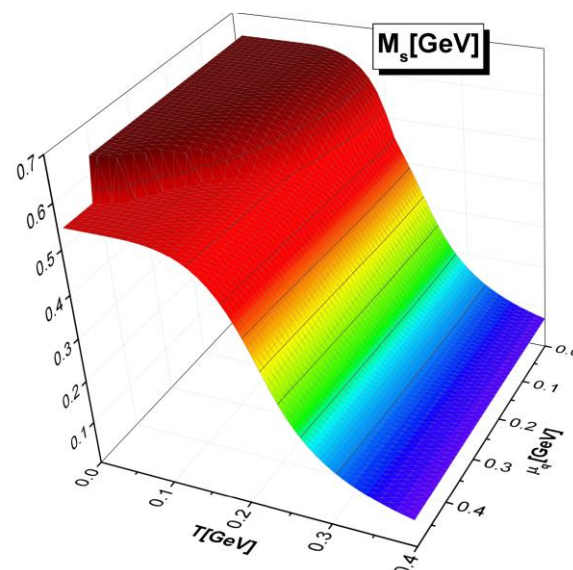
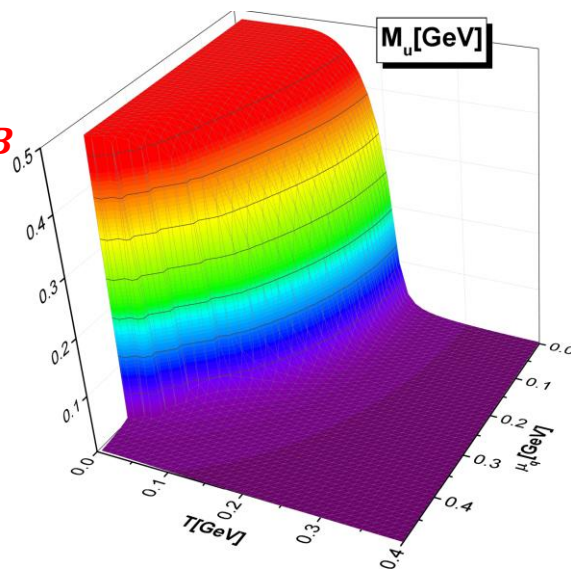
$$- \mathcal{U}(T; \Phi, \bar{\Phi}) \leftarrow \text{Polyakov potential fitted to the YM}$$

5 parameters fixed by vacuum values K, π masses, η - η' mass splitting, π decay constant, Chiral condensate

D.Fuseau, T.Steinernert, J.Aichelin PRC 101 (2020) 6 065203

- Gap equation + minimization of the grand potential \rightarrow **Chiral masses** (M_l, M_s)

- **1st order PT** at high μ_B (sudden change of q and meson masses)

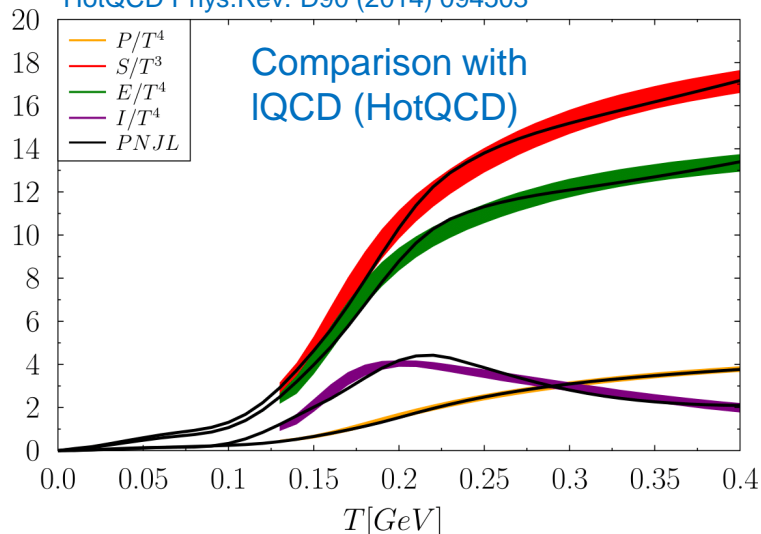


Polyakov Nambu Jona-Lasinio (PNJL) model: EOS

- PNJL allow for predictions for finite T and μ_B : D. Fuseau, T. Steinernert, J. Aichelin
PRC 101 (2020) 6 065203

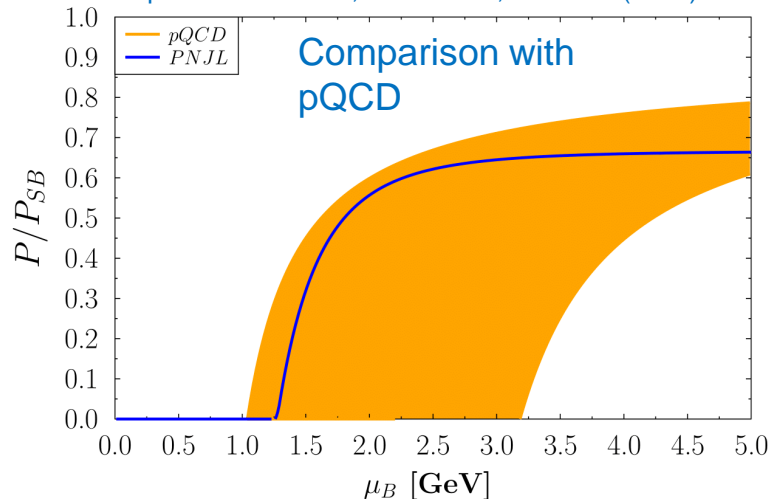
- Parameters fixed, EoS at $\mu_B = 0$:

HotQCD Phys.Rev. D90 (2014) 094503

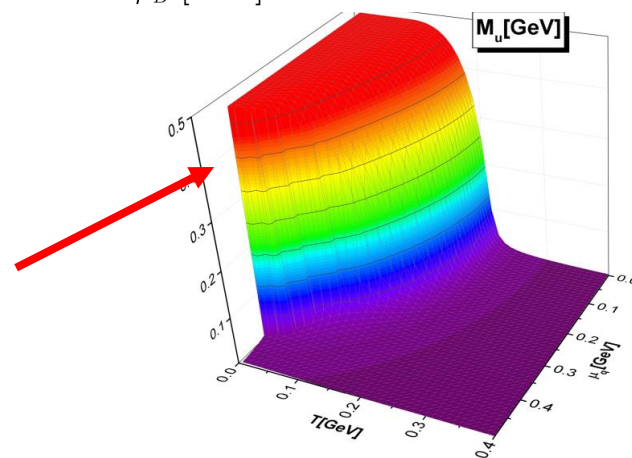


- EoS at high μ_B :

pQCD: A. Kurkela, A. Vuorinen, PRL 117 (2016) 4 042501



- CEP: $(T, \mu_B) = (110, 960)$ MeV, $\mu_B/T = 8.73$
- 1st order PT at high μ_B (sudden change of q and meson masses)

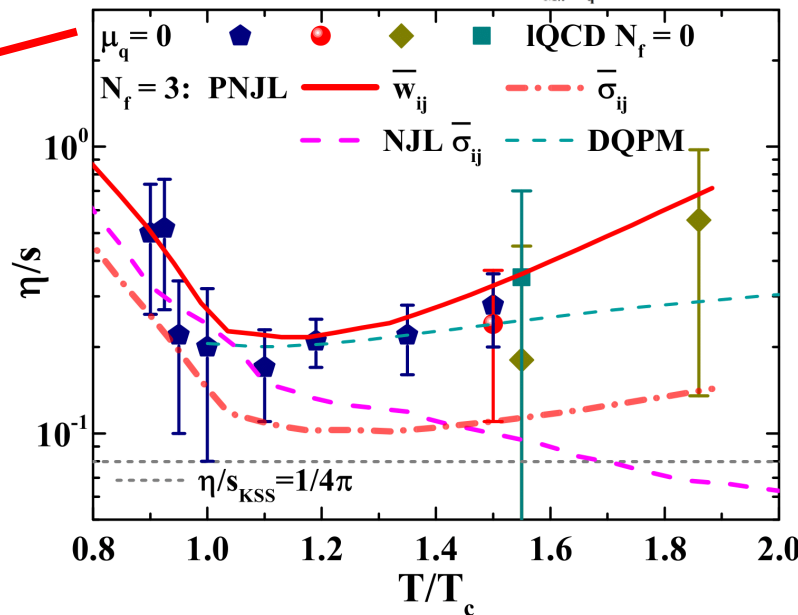
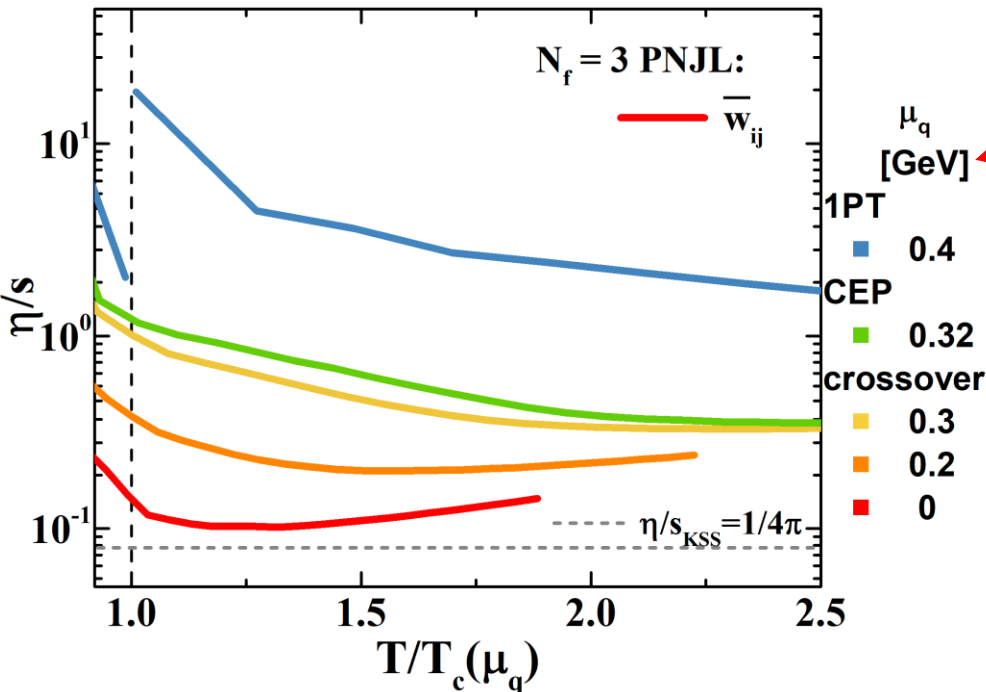
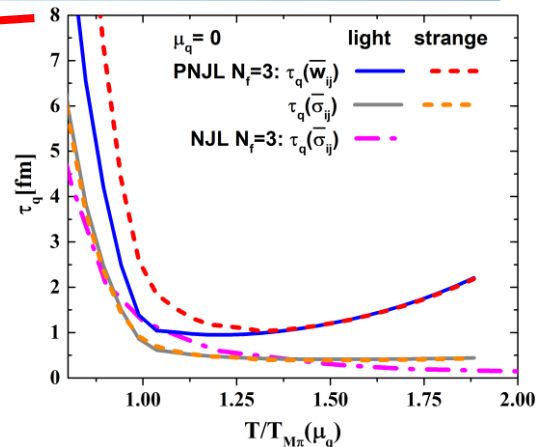


Specific shear viscosity at high μ_B

$$\eta^{\text{RTA}}(T, \mu_B) = \frac{1}{15T} \sum_{i=q, \bar{q}, g} \int \frac{d^3p}{(2\pi)^3} \frac{\mathbf{p}^4}{E_i^2} \tau_i(\mathbf{p}, T, \mu_B) d_q f_i^\phi$$

$$f_i^\phi = \frac{\phi e^{-(E_i \mp \mu)/T} + 2\bar{\phi} e^{-2(E_i \mp \mu)/T} + e^{-3(E_i \mp \mu)/T}}{1 + 3\phi e^{-(E_i \mp \mu)/T} + 3\bar{\phi} e^{-2(E_i \mp \mu)/T} + e^{-3(E_i \mp \mu)/T}}$$

with Polyakov loops



In agreement w $N_f=2$ NJL results C.Sasaki et al, NPA 832 (2010)

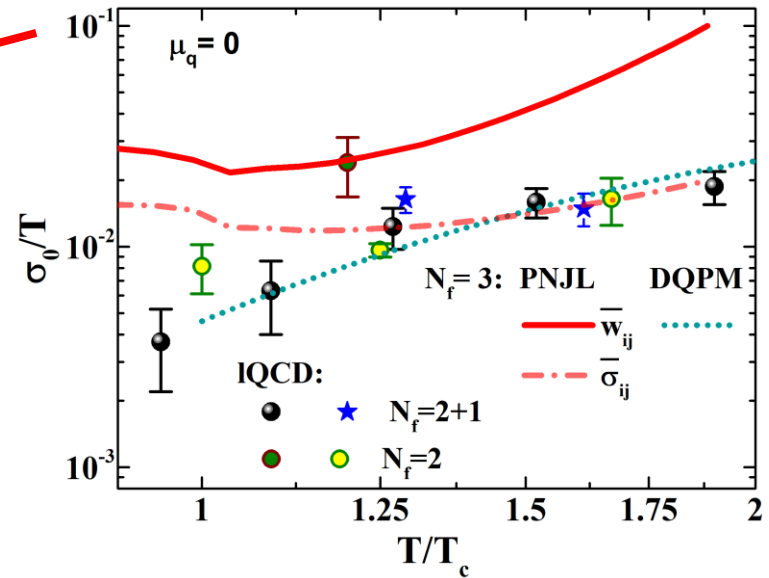
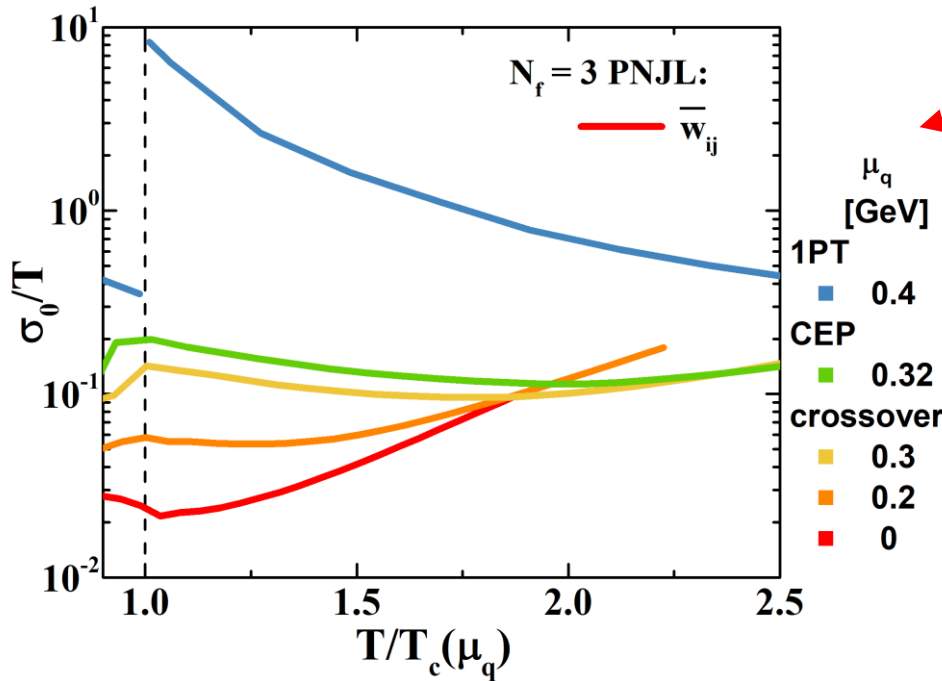
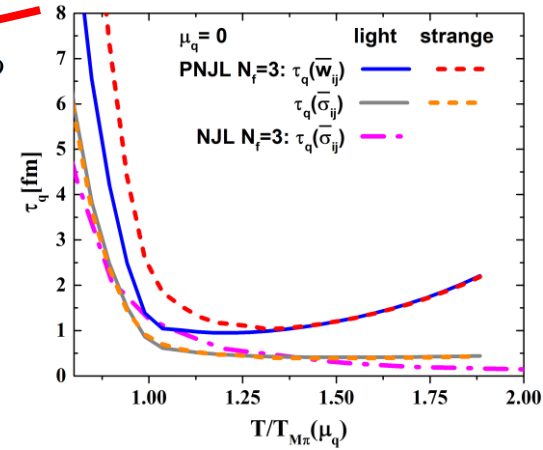
PNJL results: arXiv:2011.03505

Electric conductivity at high μ_B

$$\sigma_0^{\text{RTA}}(T, \mu_B) = \frac{e^2}{3T} \sum_{i=q, \bar{q}} q_i^2 \int \frac{d^3 p}{(2\pi)^3} \frac{\mathbf{p}^2}{E_i^2} \tau_i(\mathbf{p}, T, \mu_B) d_q f_i^\phi$$

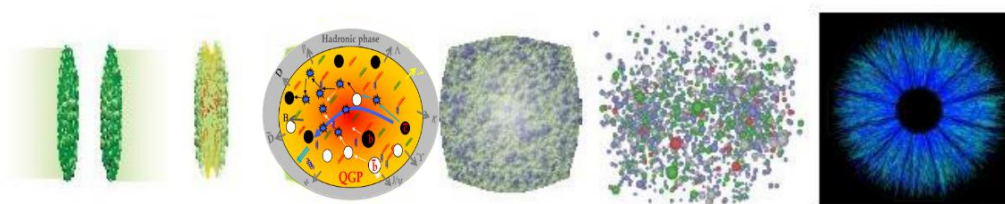
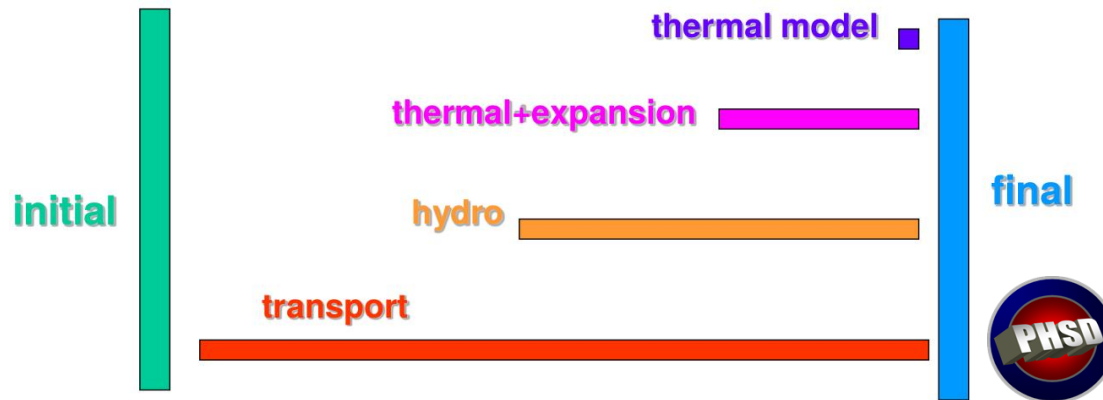
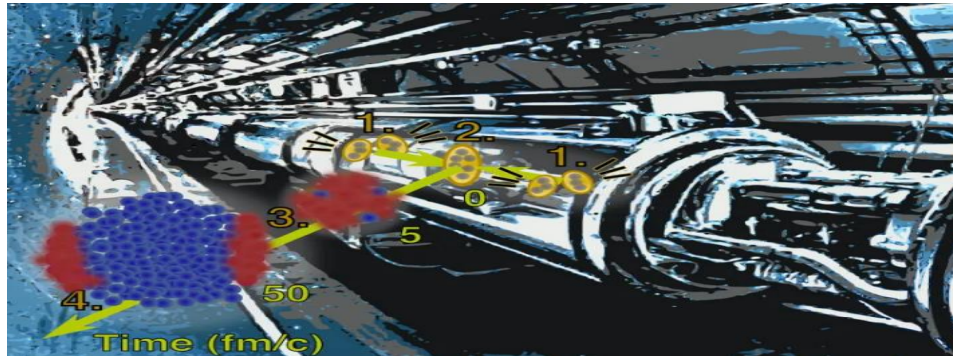
$$f_i^\phi = \frac{\phi e^{-(E_i \mp \mu)/T} + 2\bar{\phi} e^{-2(E_i \mp \mu)/T} + e^{-3(E_i \mp \mu)/T}}{1 + 3\phi e^{-(E_i \mp \mu)/T} + 3\bar{\phi} e^{-2(E_i \mp \mu)/T} + e^{-3(E_i \mp \mu)/T}}$$

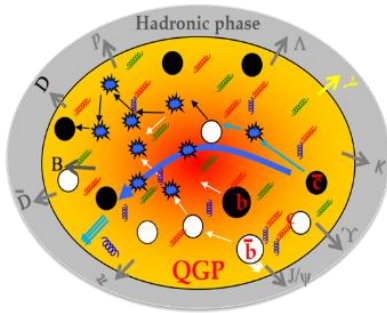
with Polyakov loops



PNJL results: arXiv:2011.03505

QGP out-of-equilibrium \leftrightarrow HIC



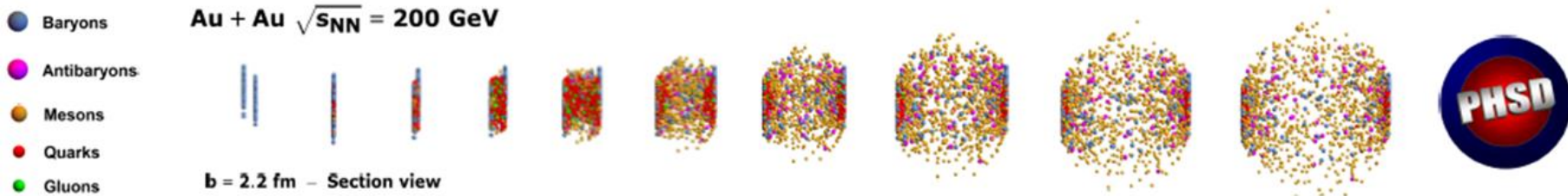


QGP out-of-equilibrium \leftrightarrow HIC



Parton-Hadron-String-Dynamics (PHSD)

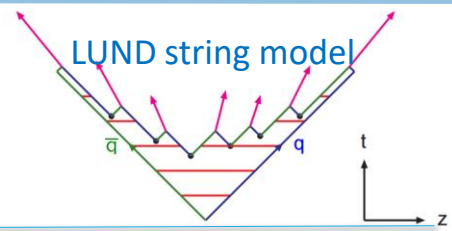
- **Transport theory:** off-shell transport equations in phase-space representation based on Kadanoff-Baym equations for the **partonic** and **hadronic phase**



Stages of a collision in the PHSD

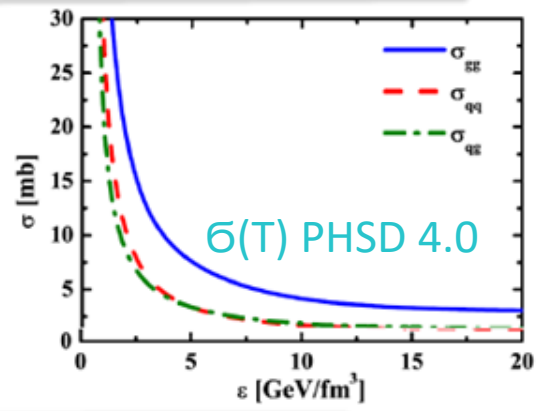
Initial A+A collision

- String formation in primary NN collisions
- ➔ decays to pre-hadrons (baryons and mesons)



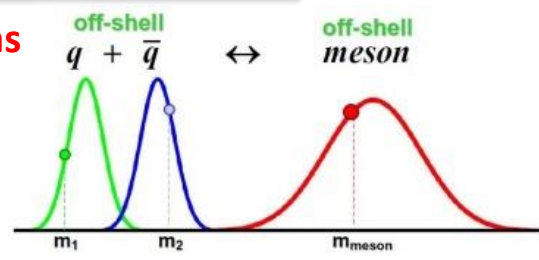
Partonic phase

- Formation of a **QGP** state if $\epsilon > \epsilon_{critical}$:
Dissolution of pre-hadrons \rightarrow DQPM
 - ➔ massive quarks/gluons and mean-field energy
- (quasi-)elastic collisions : inelastic collisions:
- | | | |
|---|---------------------------------------|-----------------------------|
| $q + q \rightarrow q + q$ | $g + q \rightarrow g + q$ | $q + \bar{q} \rightarrow g$ |
| $q + \bar{q} \rightarrow q + \bar{q}$ | $g + \bar{q} \rightarrow g + \bar{q}$ | $g \rightarrow q + \bar{q}$ |
| $\bar{q} + \bar{q} \rightarrow \bar{q} + \bar{q}$ | $g + g \rightarrow g + g$ | |



Hadronization

- Hadronization to colorless off-shell mesons and baryons
- $g \rightarrow q + \bar{q}, \quad q + \bar{q} \leftrightarrow meson$ ('string')
- $q + q + q \leftrightarrow baryon$ ('string')
- Strict 4-momentum and quantum number conservation



Hadronic phase

- Hadron-string interactions – off-shell HSD

W. Cassing, E. Bratkovskaya, PRC 78 (2008) 034919; NPA831 (2009) 215;
W. Cassing, EPJ ST 168 (2009) 3

Extraction of (T, μ_B) in PHSD

For each space-time cell of the PHSD: $T^{\mu\nu} = \sum_i \frac{p_i^\mu p_i^\nu}{E_i} \rightarrow$ Diagonalize in LRF $\rightarrow \varepsilon^{\text{PHSD}}$

➤ Calculate the local energy density $\varepsilon^{\text{PHSD}}$ and baryon density n_B^{PHSD}

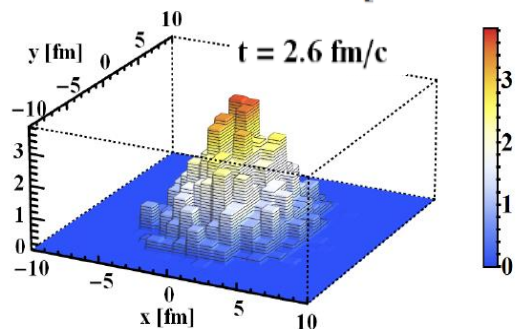
➤ use IQCD relations (up to 6th order):

$$\left\{ \begin{array}{l} \frac{n_B}{T^3} \approx \chi_2^B(T) \left(\frac{\mu_B}{T} \right) + \dots \\ \Delta\varepsilon/T^4 \approx \frac{1}{2} \left(T \frac{\partial \chi_2^B(T)}{\partial T} + 3\chi_2^B(T) \right) \left(\frac{\mu_B}{T} \right)^2 + \dots \end{array} \right.$$

Use baryon number susceptibilities χ_n from IQCD

➔ obtain (T, μ_B) by solving the system of coupled equations using $\varepsilon^{\text{PHSD}}$ and n_B^{PHSD}

$e(x, y, z=0)$ e [GeV.fm⁻³]



Input:
 $\varepsilon^{\text{PHSD}}$ and n_B^{PHSD}



Output:
 T, μ_B

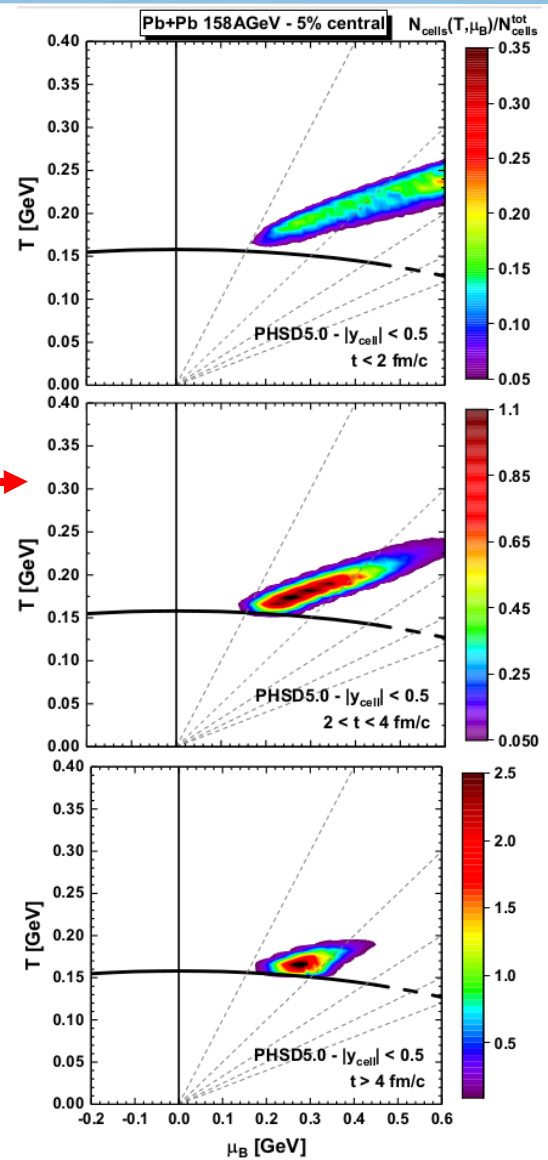
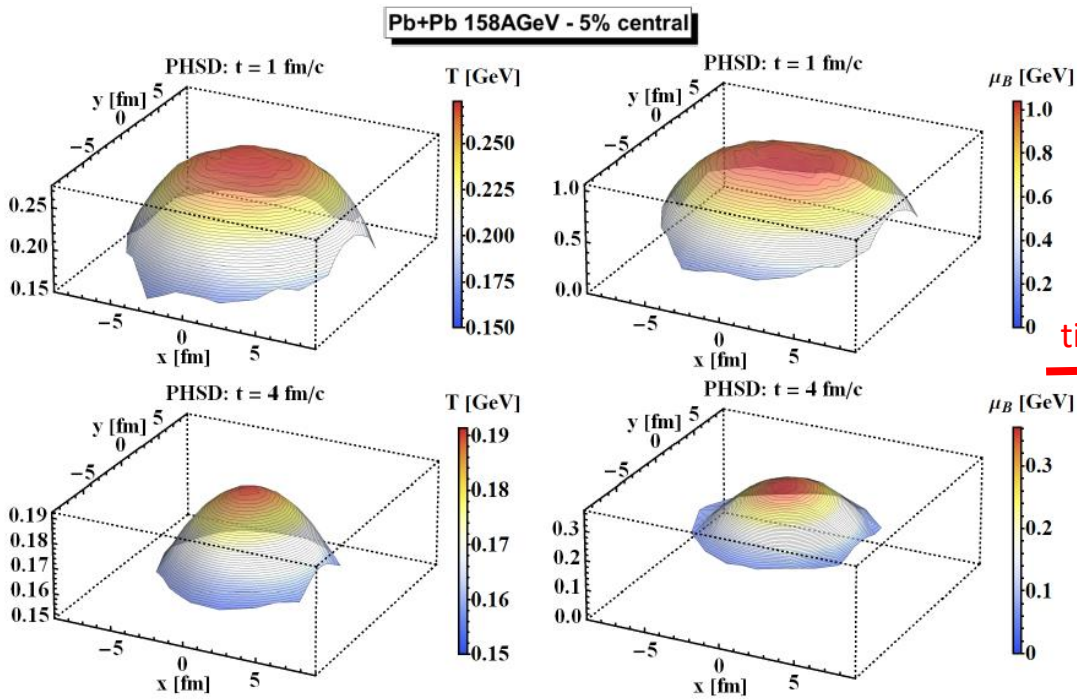
for details see P. Moreau, O. Soloveva, L. Oliva, T. Song, W. Cassing, E. Bratkovskaya
arXiv:1903.10157, PRC 100 (2019) no. 1, 014911

QGP evolution for HIC ($\sqrt{s_{NN}} = 17$ GeV)



The **T** profile in (x;y) at midrapidity ($|y_{cell}| < 1$) at fixed times (1 and 4 fm/c)

μ_B profile in (x;y)



for details see P. Moreau, O. Soloveva, L. Oliva, T. Song, W. Cassing, E. Bratkovskaya
arXiv:1903.10157, PRC 100 (2019) no. 1, 014911

Results for HIC: compare 3 versions

➤ Comparison between three different results:

- **PHSD 4.0 : only isotropic $\sigma(T)$ and $\rho(T)$**
 - partonic cross sections
 - parton spectral function (masses and widths)

new PHSD 5 : angular dependence of $d\sigma/d \cos\theta$

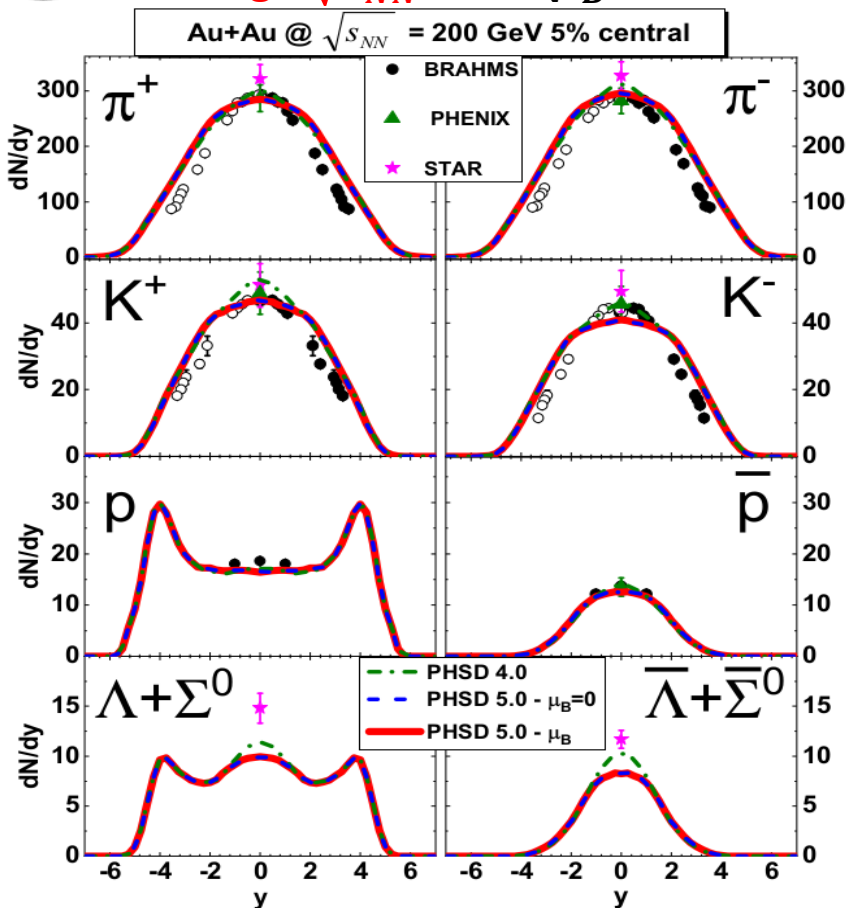
- **PHSD 5.0 : with $\sigma(\sqrt{s}, m_1, m_2, T, \mu_B = 0)$ and $\rho(T, \mu_B = 0)$**
- **PHSD 5.0 : with $\sigma(\sqrt{s}, m_1, m_2, T, \mu_B)$ and $\rho(T, \mu_B)$**

Results for ($\sqrt{s_{NN}} = 200$ GeV vs $\sqrt{s_{NN}} = 17$ GeV)

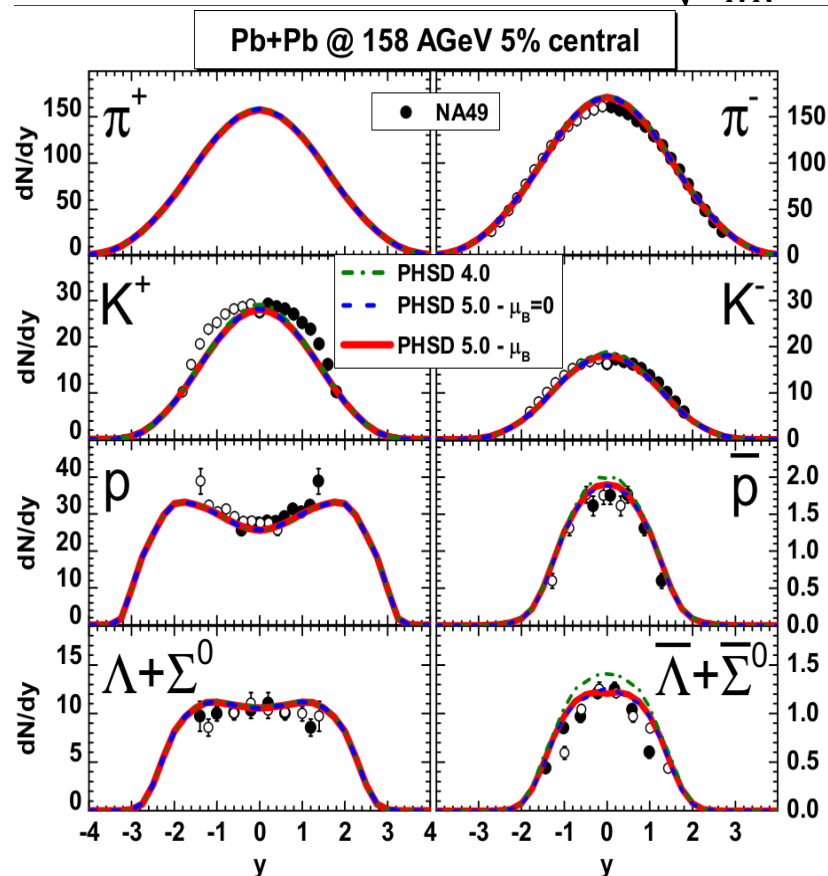
- No visible effects of μ_B dependence
- Small effect of the angular dependence of $d\sigma/d\cos\theta$



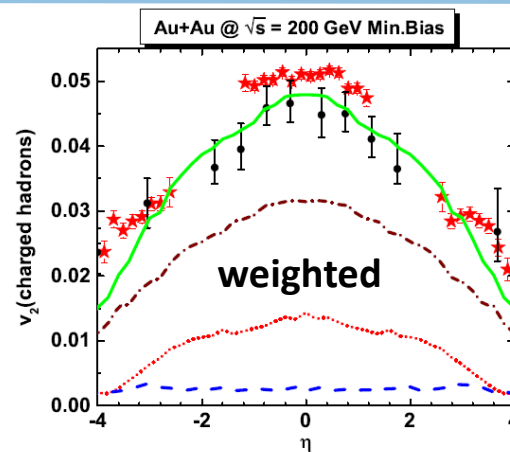
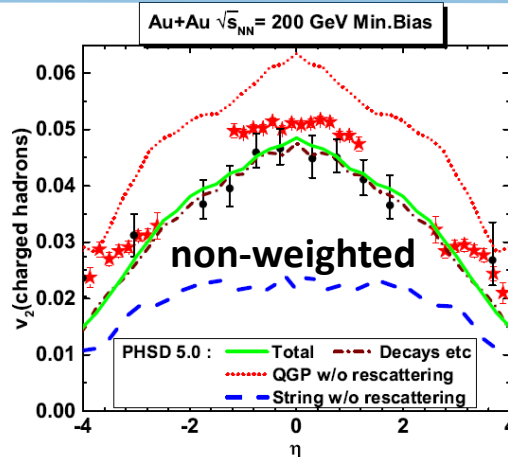
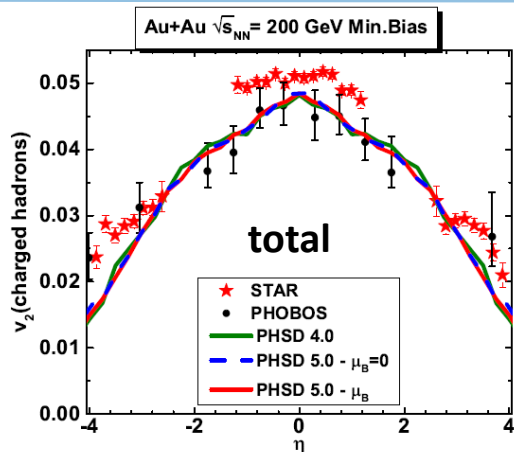
at high $\sqrt{s_{NN}}$ - low μ_B



! QGP fraction is small at low $\sqrt{s_{NN}}$

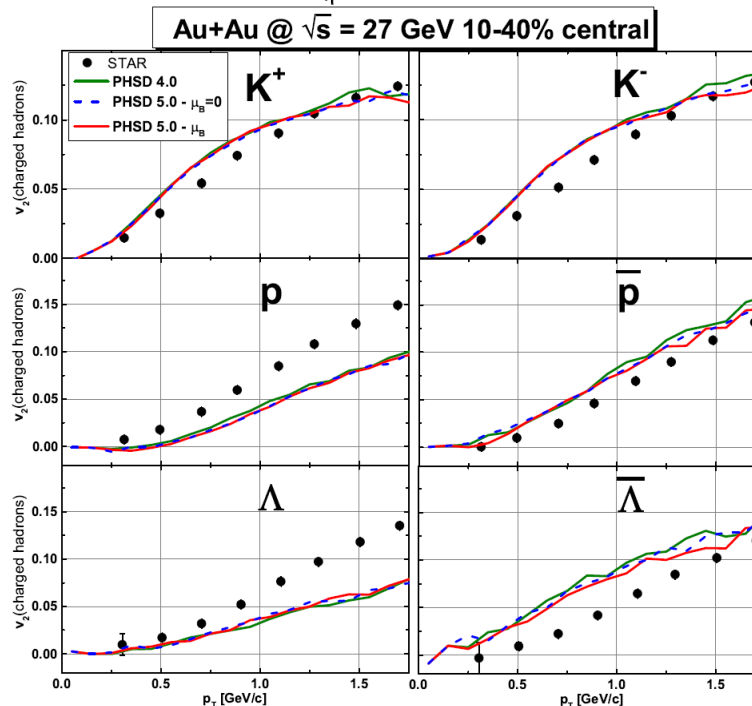
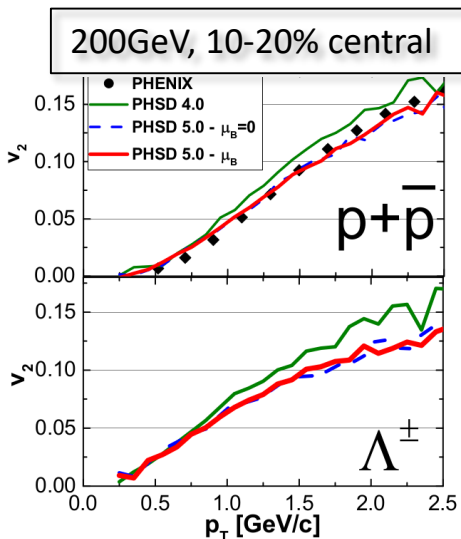


Elliptic flow ($\sqrt{s_{NN}} = 200 \text{ GeV vs } 27 \text{ GeV}$)



$$\frac{dN}{d\varphi} \propto \left(1 + 2 \sum_{n=1}^{+\infty} v_n \cos[n(\varphi - \psi_n)] \right)$$

$$v_n = \langle \cos n(\varphi - \psi_n) \rangle, \quad n=1,2,3,\dots$$



- No visible effects of μ_B dependence
- Small effect of the angular dependence of $d\sigma/d\cos\theta$ for v_1

arXiv:2001.05395

Summary / Outlook

- Transport coefficients at finite T and μ_B have been found using the (T, μ_B) -dependent cross sections (for cross-sections see DQPM[1] and PNJL[4])
- At $\mu_B = 0$ good agreement with the Bayesian analysis estimations and IQCD estimations of QGP transport coefficients[2]
- Bulk observables have been studied within the PHSD transport approach[1,3]:
- High- μ_B regions are probed at **low** $\sqrt{s_{NN}}$ or **high rapidity** regions
But, **QGP** fraction **is small** at low $\sqrt{s_{NN}}$: no effects seen in **bulk** observables[1,3]
- Directed and elliptic flows also don't show μ_B dependence, while v_2 is sensitive to the explicit \sqrt{s} dependence and angular dependence of partonic $d\sigma/d\cos\theta$ [3]
- **Outlook:**
 - More precise EoS large μ_B
 - Possible 1st order phase transition at large μ_B , comparison w PNJL model



Thank you for your attention!



PHSD group meeting 2019

[1] P. Moreau, OS , L. Oliva, T. Song, W. Cassing, E. Bratkovskaya, arXiv:1903.10157

[2] OS, P. Moreau, E. Bratkovskaya, arXiv:1911.08547 [nucl-th].

[3] OS, P. Moreau, L. Oliva, V. Voronyuk, V. Kireyeu, T. Song, E. Bratkovskaya, arXiv:2001.05395

[4] OS, D.Fuseau, J.Aichelin, E.Bratkovskaya, arXiv:2011.03505

