



**Hipstars**

# Collective flow measurements with HADES in Au+Au collisions at 1.23 AGeV

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for the  
HADES Collaboration

HIPSTARS  
Workshop on Heavy Ion Physics  
and Compact Stars

4<sup>th</sup> December, 2020



**H-QM** | Helmholtz Research School  
Quark Matter Studies

**HIC** | **FAIR**  
for  
Helmholtz International Center

**HADES**





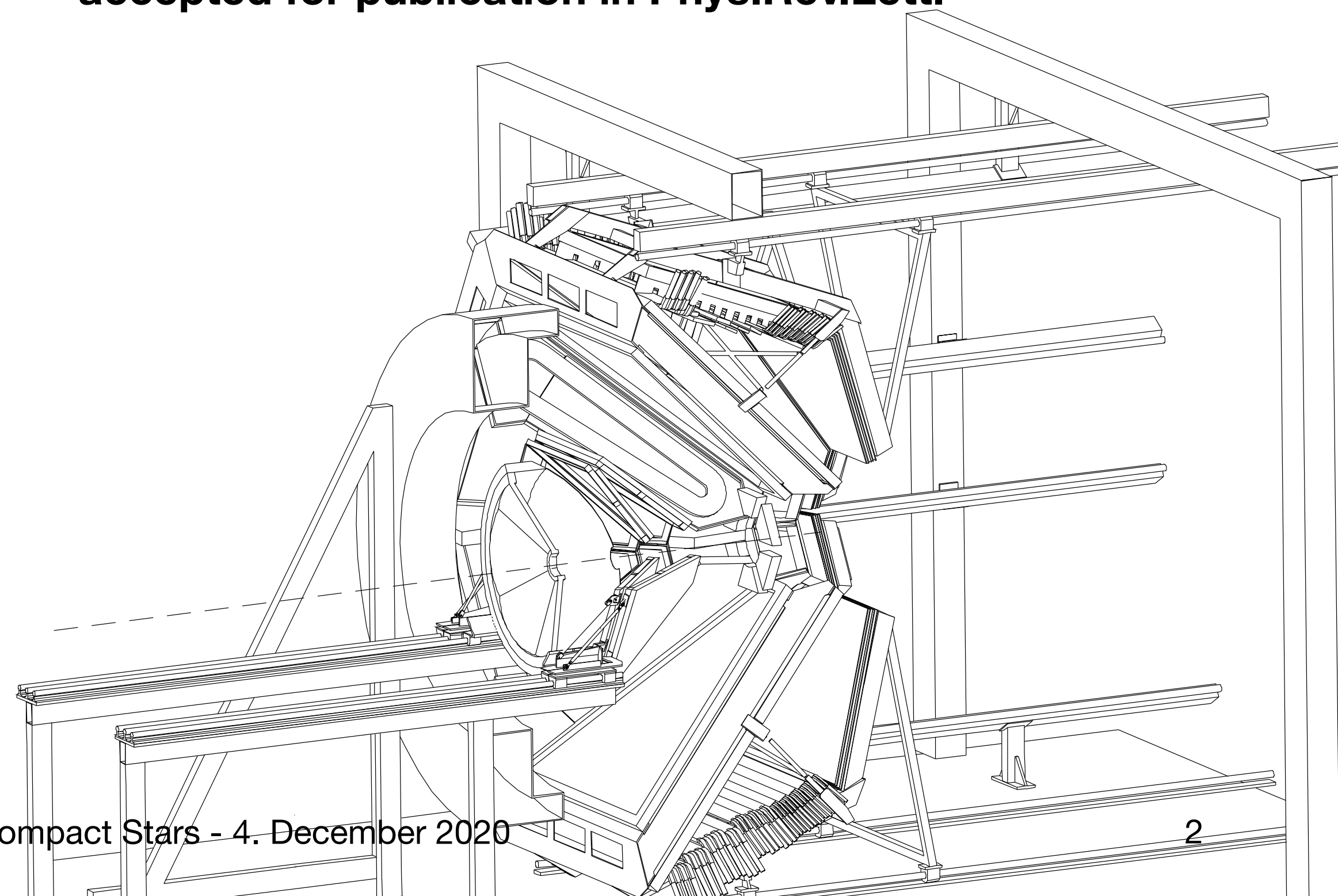
# Outline

- Motivation: Properties of Dense Nuclear Matter
  - ▶ Macroscopic:  
Equation-of-State or Mean-Field Potentials
  - ▶ Microscopic:  
Transport coefficients (shear viscosity)  
or “effective in-medium” cross sections
- HADES and Au+Au data at 1.23 AGeV
- Flow harmonics  $v_n$  of order  $n = 1 - 6$   
of protons, deuterons and tritons
- Scaling properties of Flow

**Presentation based on following publication:**

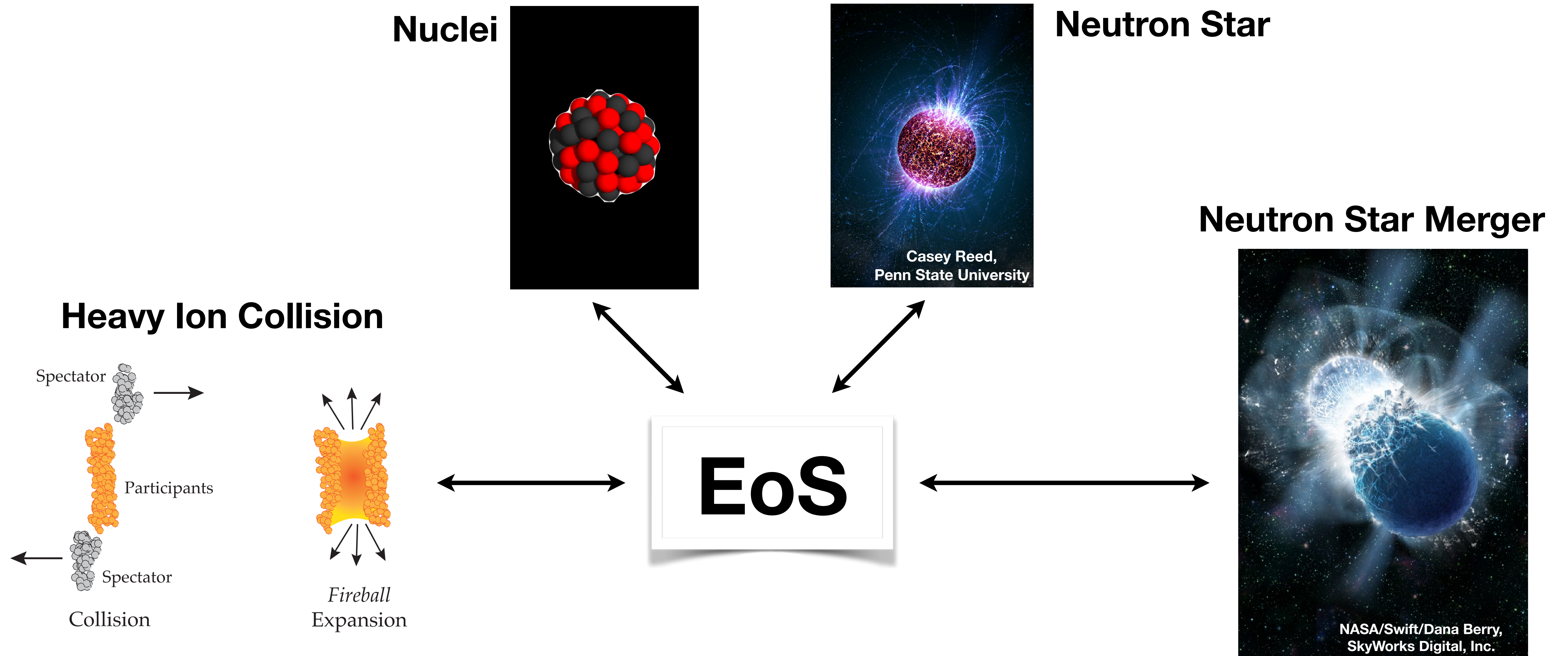
**Directed, elliptic and higher order flow harmonics of protons, deuterons and tritons in Au+Au collisions at  $\sqrt{s_{NN}}=2.4$  GeV**

**HADES, [arXiv:2005.12217 \[nucl-ex\]](https://arxiv.org/abs/2005.12217),  
accepted for publication in Phys.Rev.Lett.**



# Motivation

## Nuclear and Neutron Star Matter

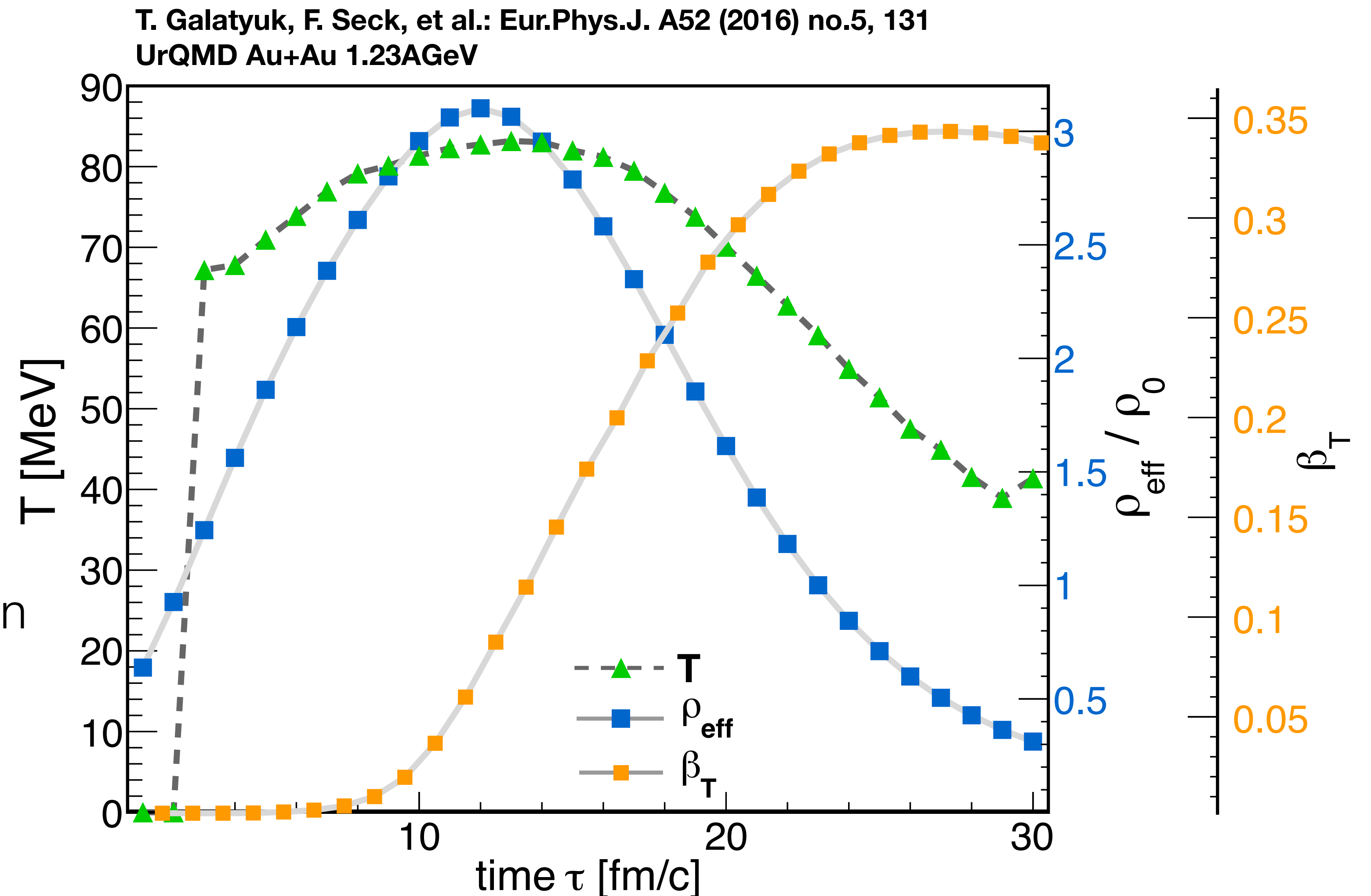




# Motivation

## Heavy Ion Collisions at 1.23A GeV

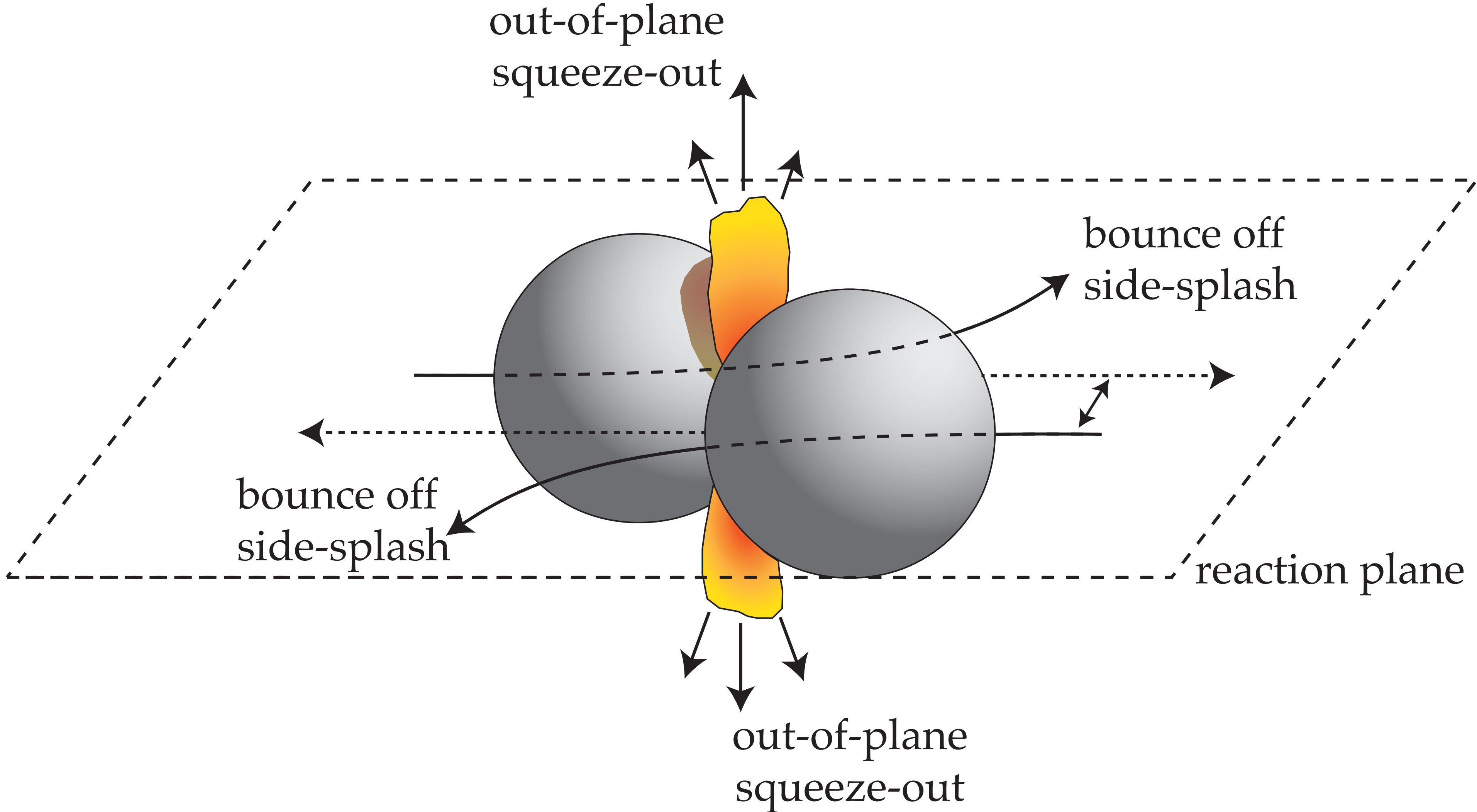
- High densities:  
 $\rho_{\text{max}} = 1-3\rho_0$
- Moderate temperatures:  
 $T = 50-100 \text{ MeV}$
- Relatively long lifetime of fireball
- Significant transverse expansion expected





# Motivation

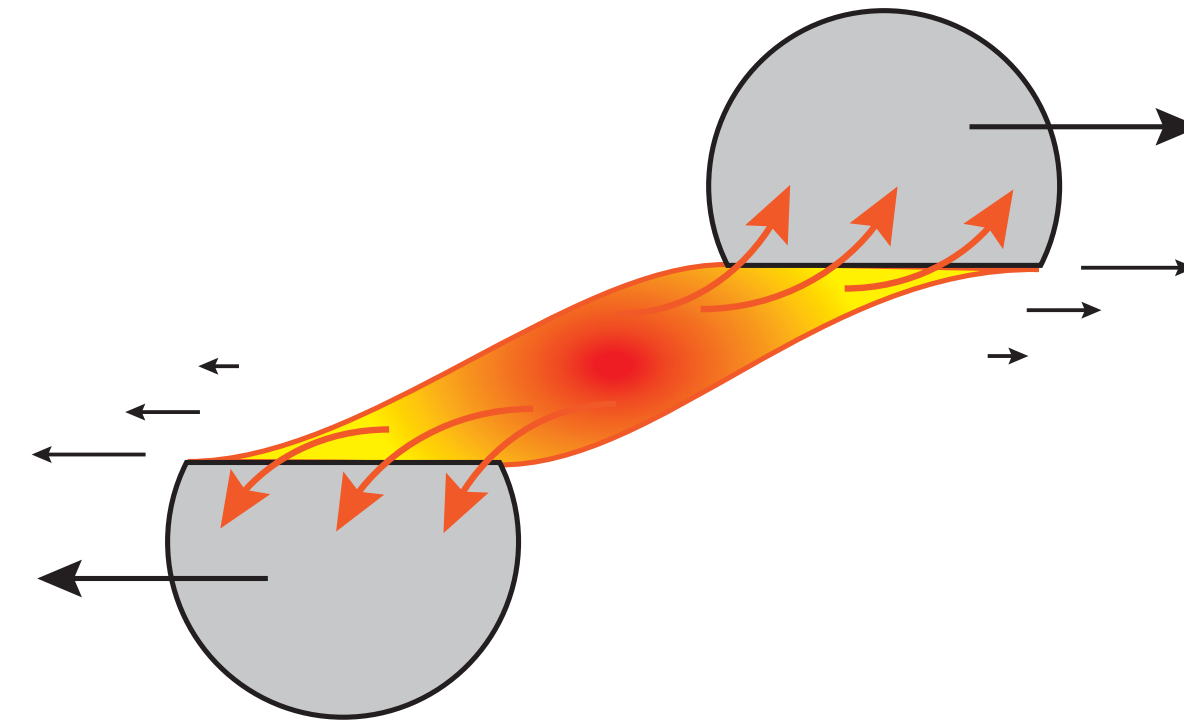
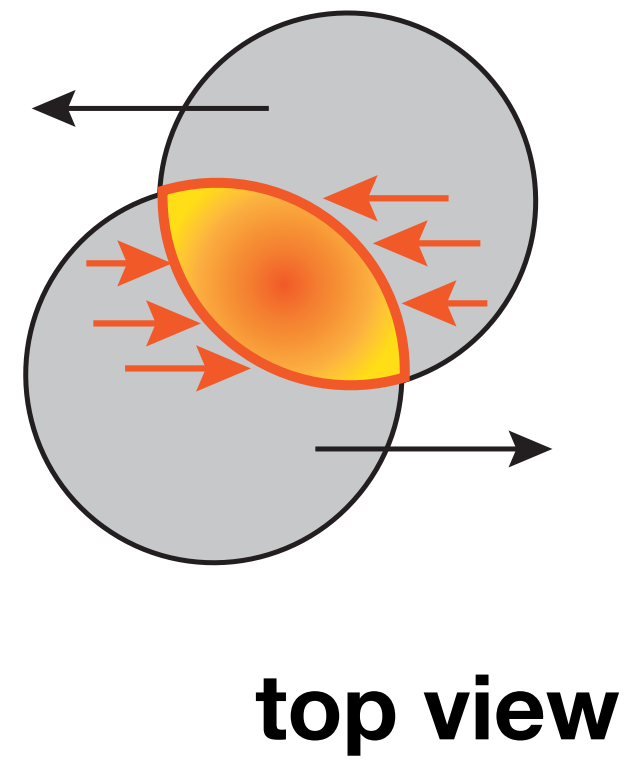
## Flow





# Motivation

## Flow Components



**directed flow**

**V1**

$$v_1 = \langle \cos(\phi) \rangle$$

$$= \left\langle \frac{p_x}{p_t} \right\rangle$$

**triangular flow**

**V3**

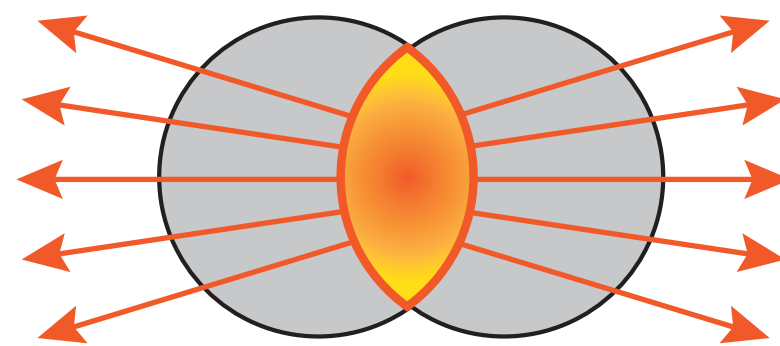
....

$$v_3 = \langle \cos(3\phi) \rangle$$

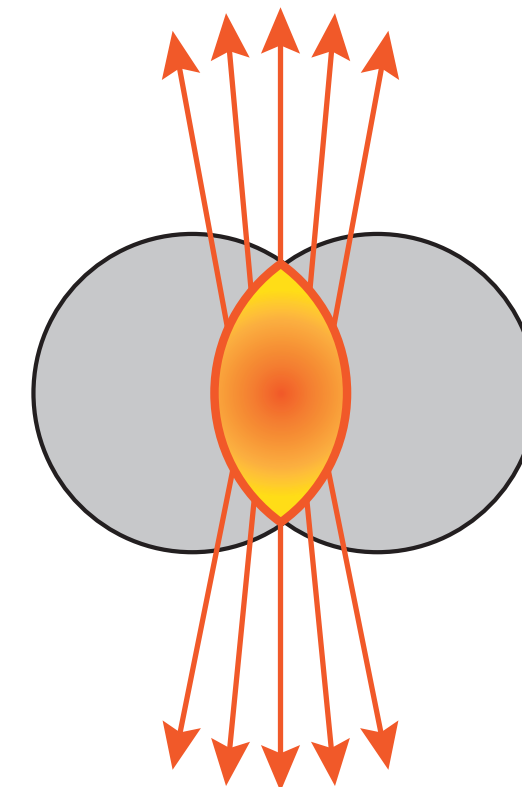
$$= \left\langle \frac{p_x^3 - 3p_x p_y^2}{p_t^3} \right\rangle$$

$$\phi = (\varphi - \Psi_{RP})$$

**front view**



**in-plane**



**out-of-plane**

**elliptic flow**

**V2**

$$v_2 = \langle \cos(2\phi) \rangle$$

$$= \left\langle \frac{p_x^2 - p_y^2}{p_t^2} \right\rangle$$

**V4**

....

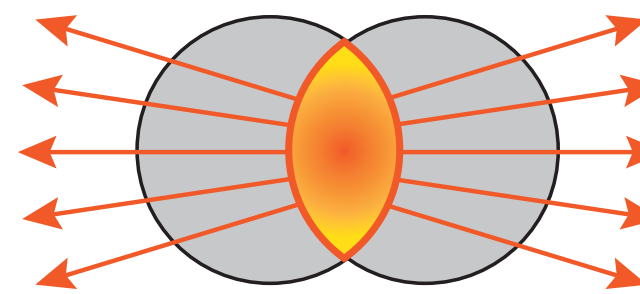


# Motivation

## Energy Dependence of Elliptic Flow

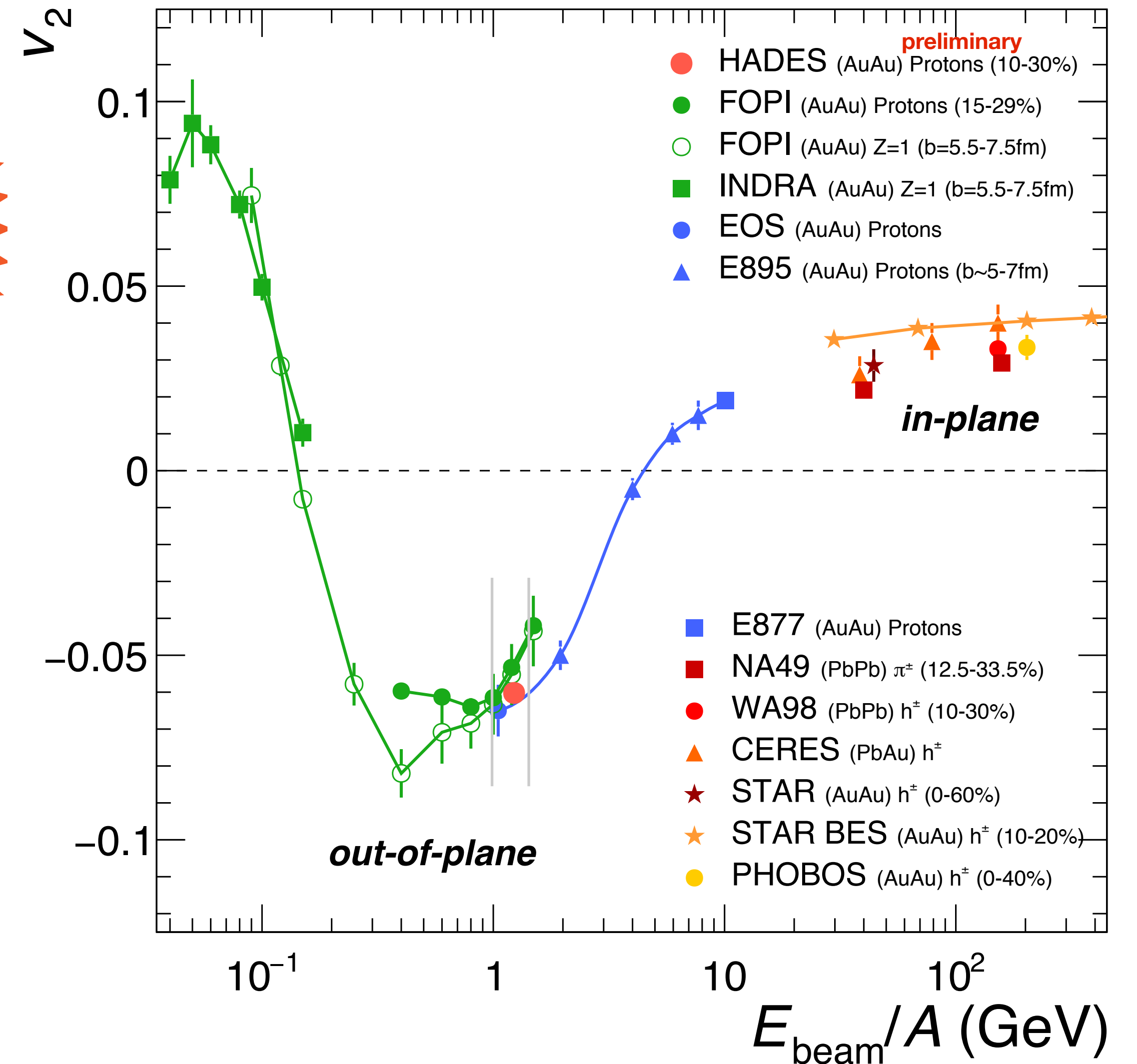
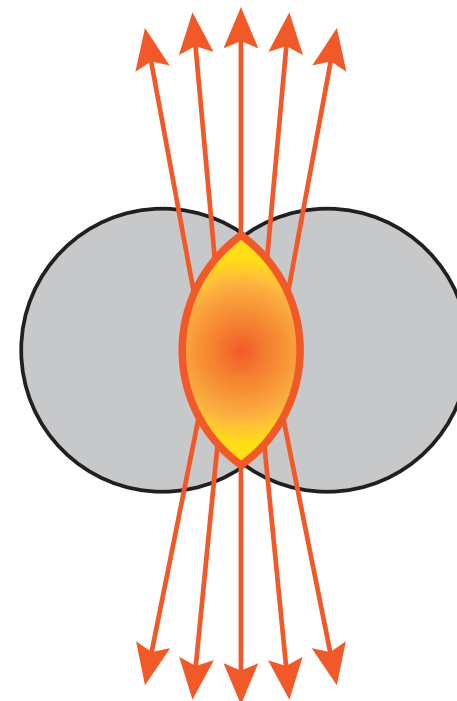
- In-plane  $v_2 > 0$

- ▶ Short spectator passing time  
 $\tau_{\text{passing}} \ll \tau_{\text{expansion}}$
- ▶ Pressure gradient



- Out-of-plane  $v_2 < 0$

- ▶ Long spectator passing time  
 $\tau_{\text{passing}} \geq \tau_{\text{expansion}}$
- ▶ Squeeze-out

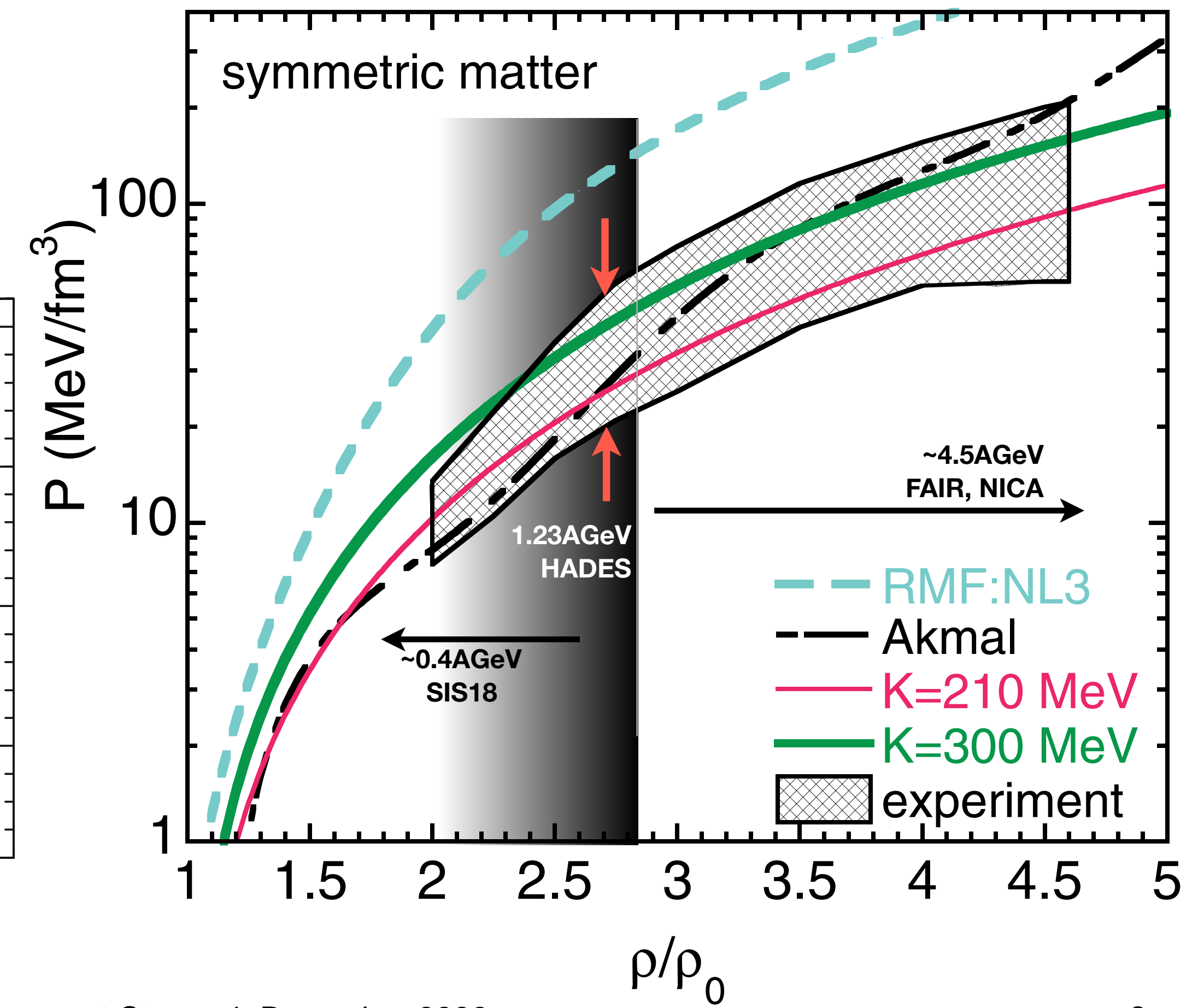
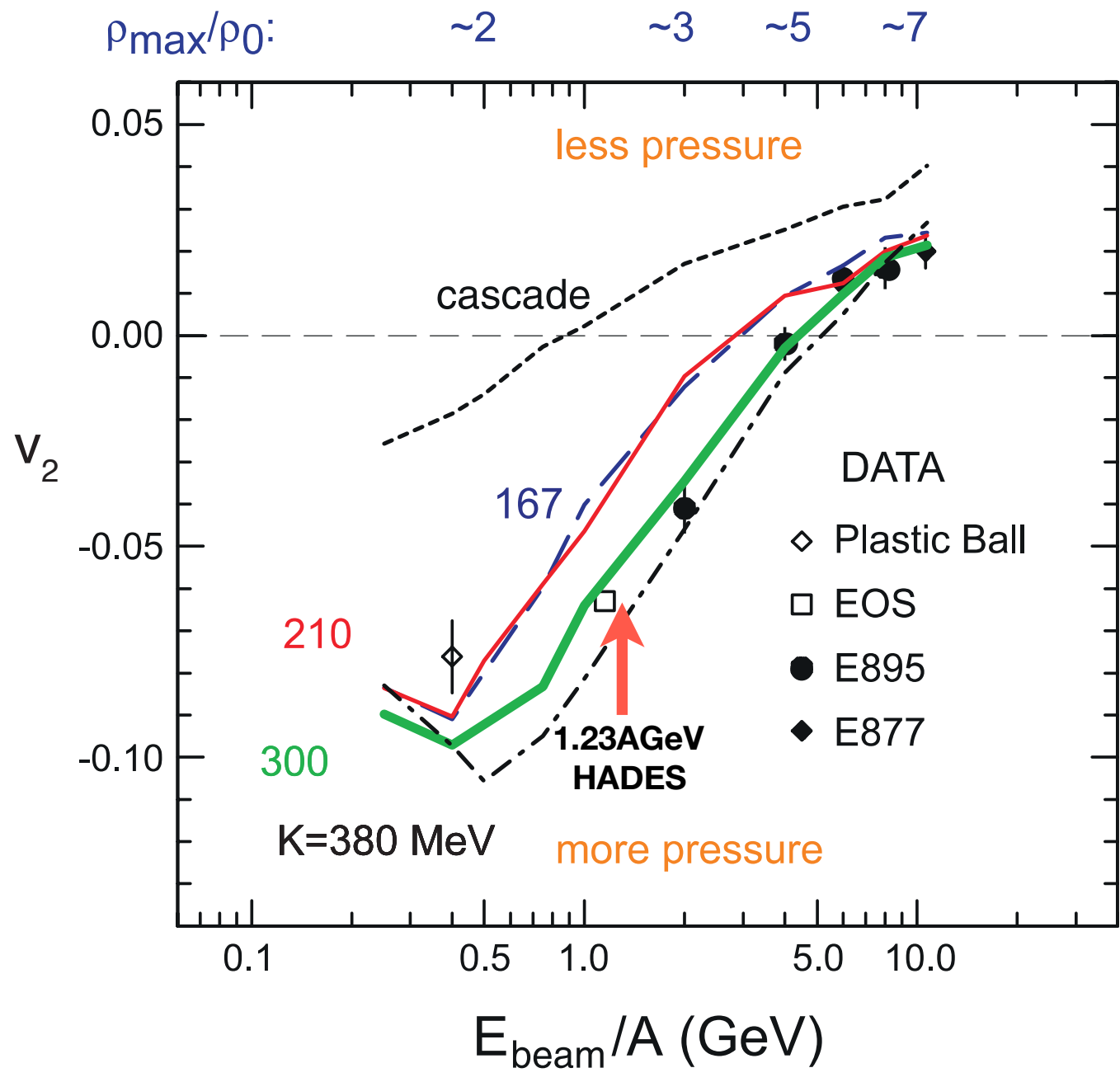
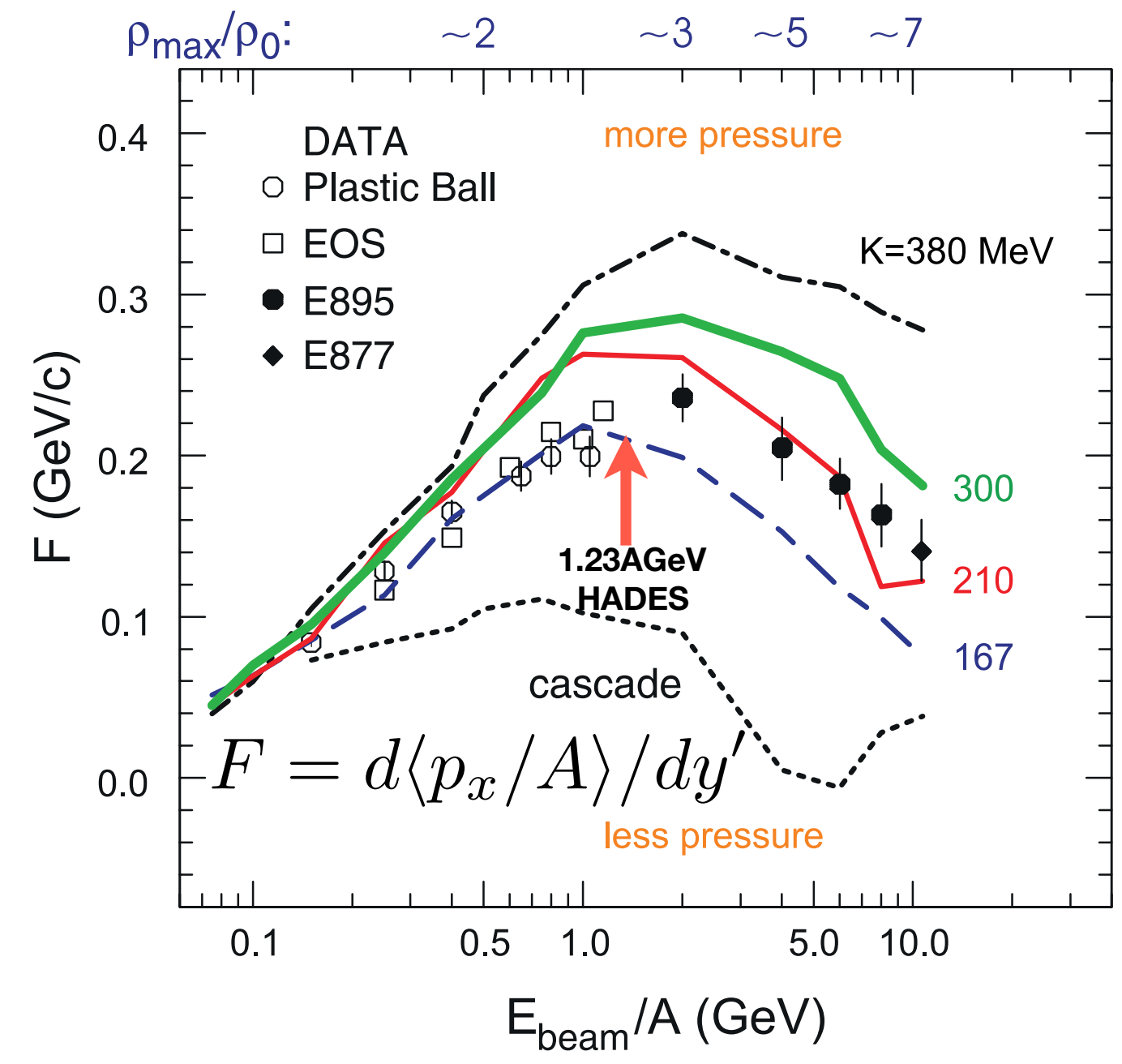




# Equation of State of Dense Matter

- EoS is the *equilibrium* property of Hydrodynamical simulations
- *Non-equilibrium dissipative* effects described by transport coefficients (shear viscosity  $\eta$ )
- In microscopic transport models implemented via *averaged mean-field potentials* (Skyrme-like or RMF)

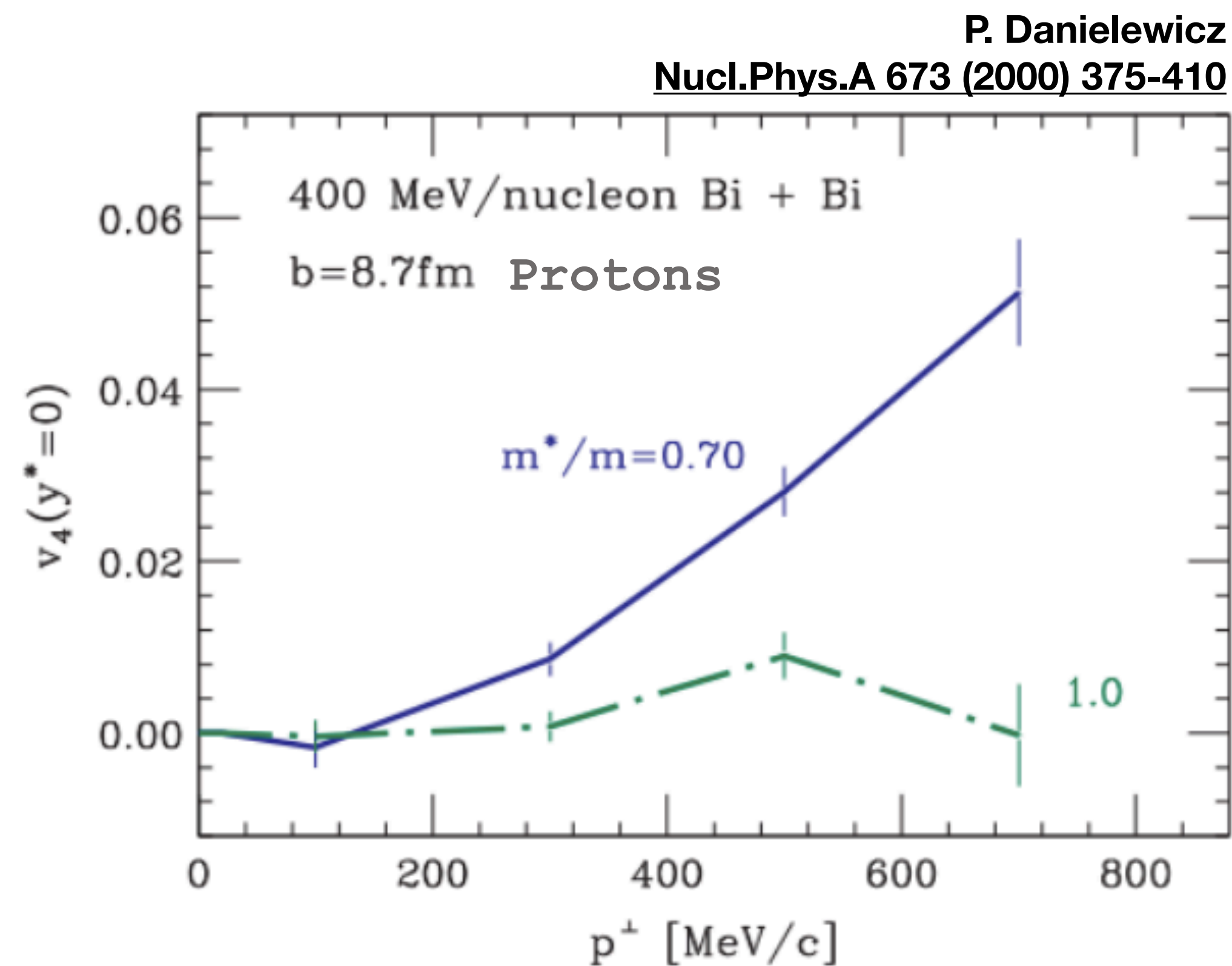
P. Danielewicz, R. Lacey, W.G. Lynch  
 Science 298 (2002) 1592-1596



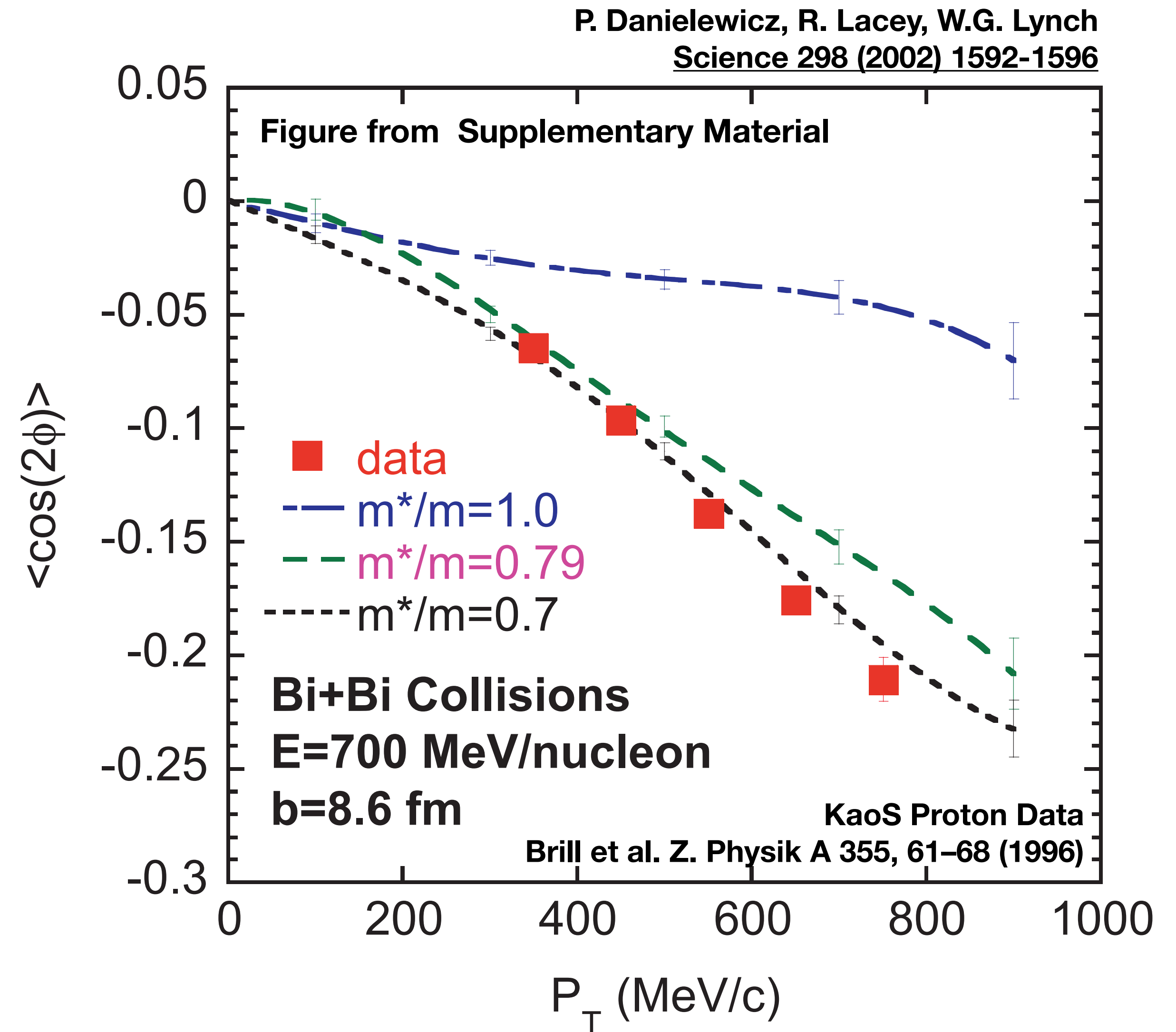
# Equation of State of Dense Matter

Momentum Dependence of the mean fields

- Momentum dependence characterized by  $m^*=0.7m_N$



**First prediction of  $v_4\{RP\}$  in 2000!**

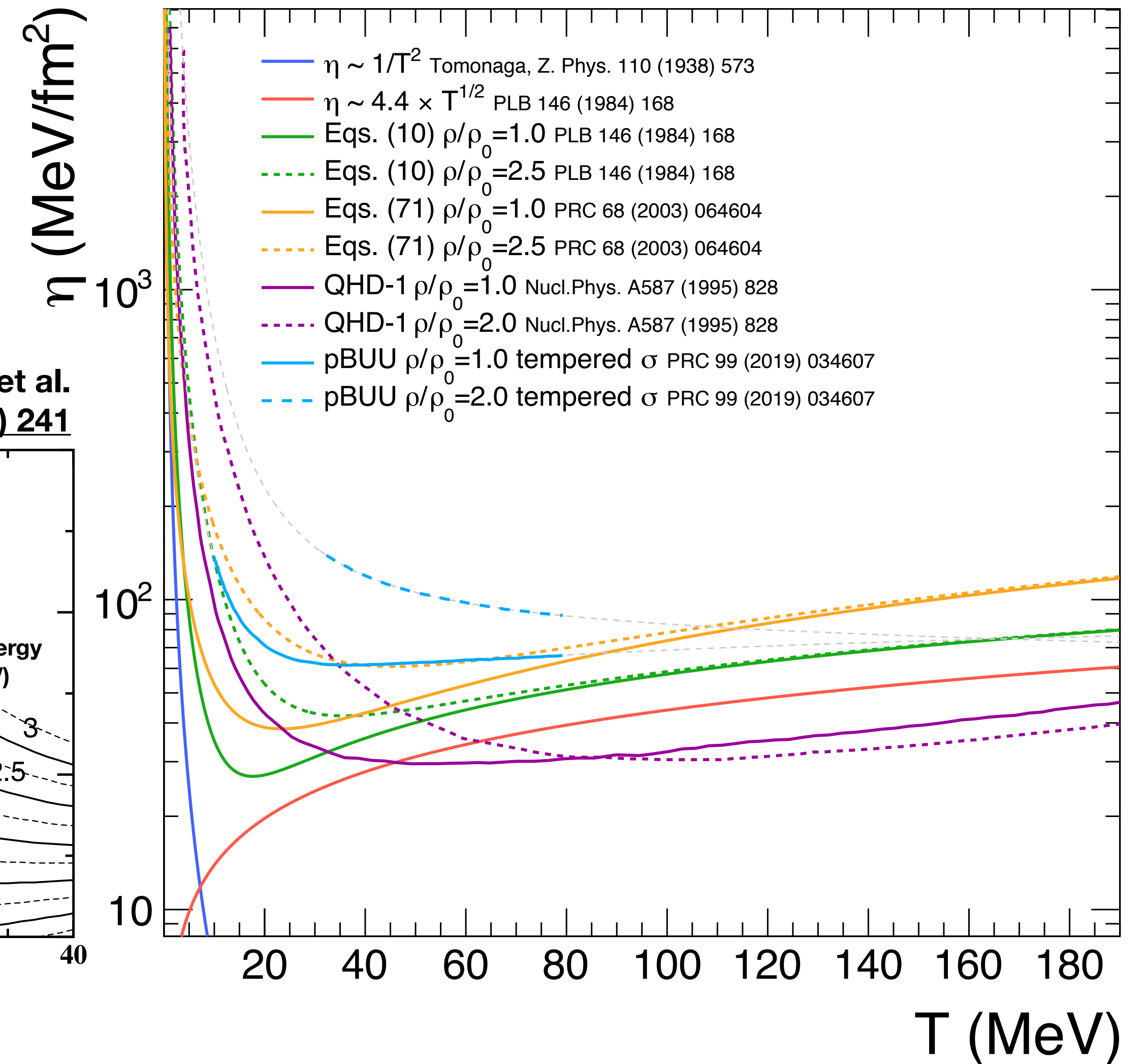
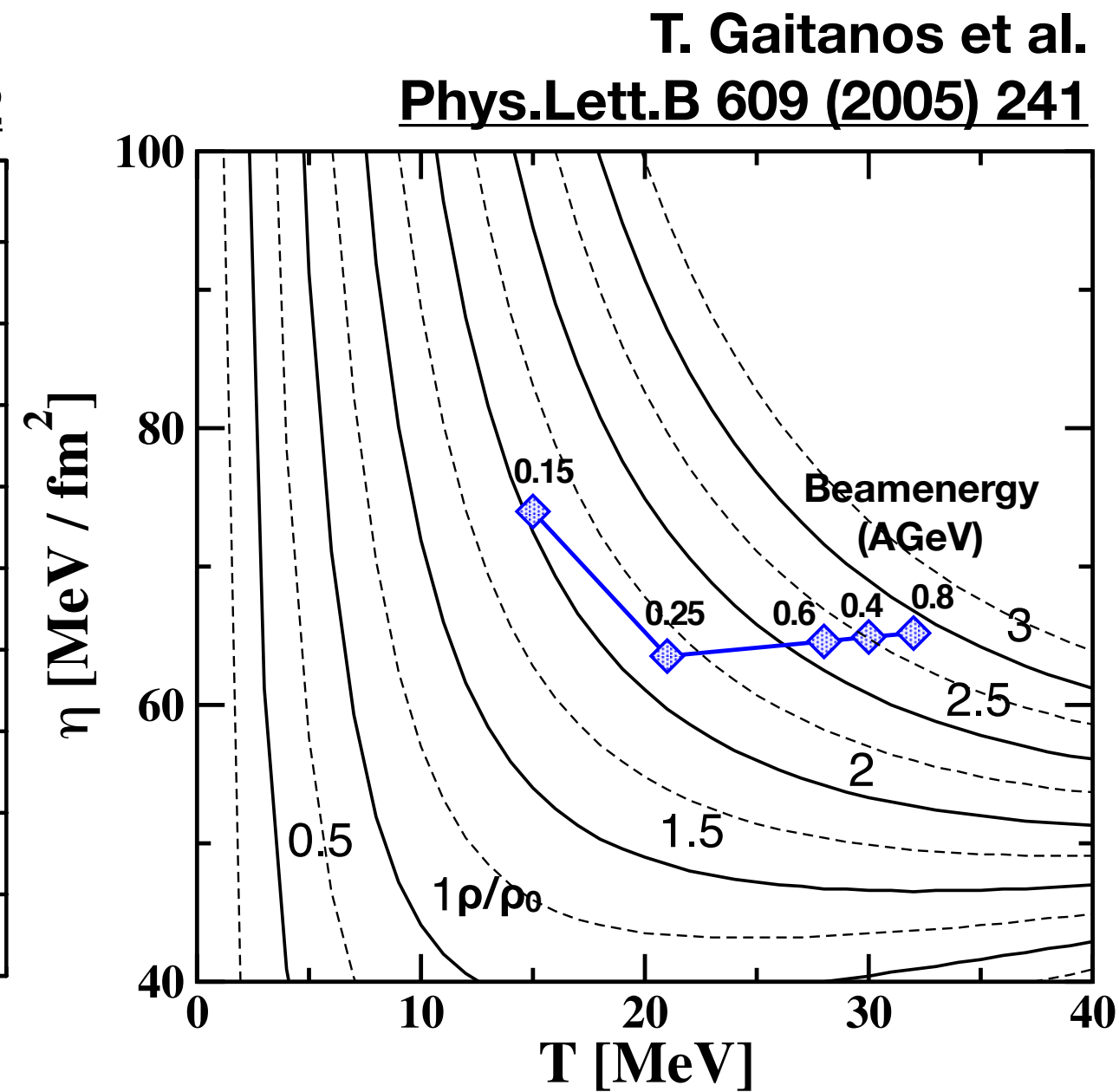
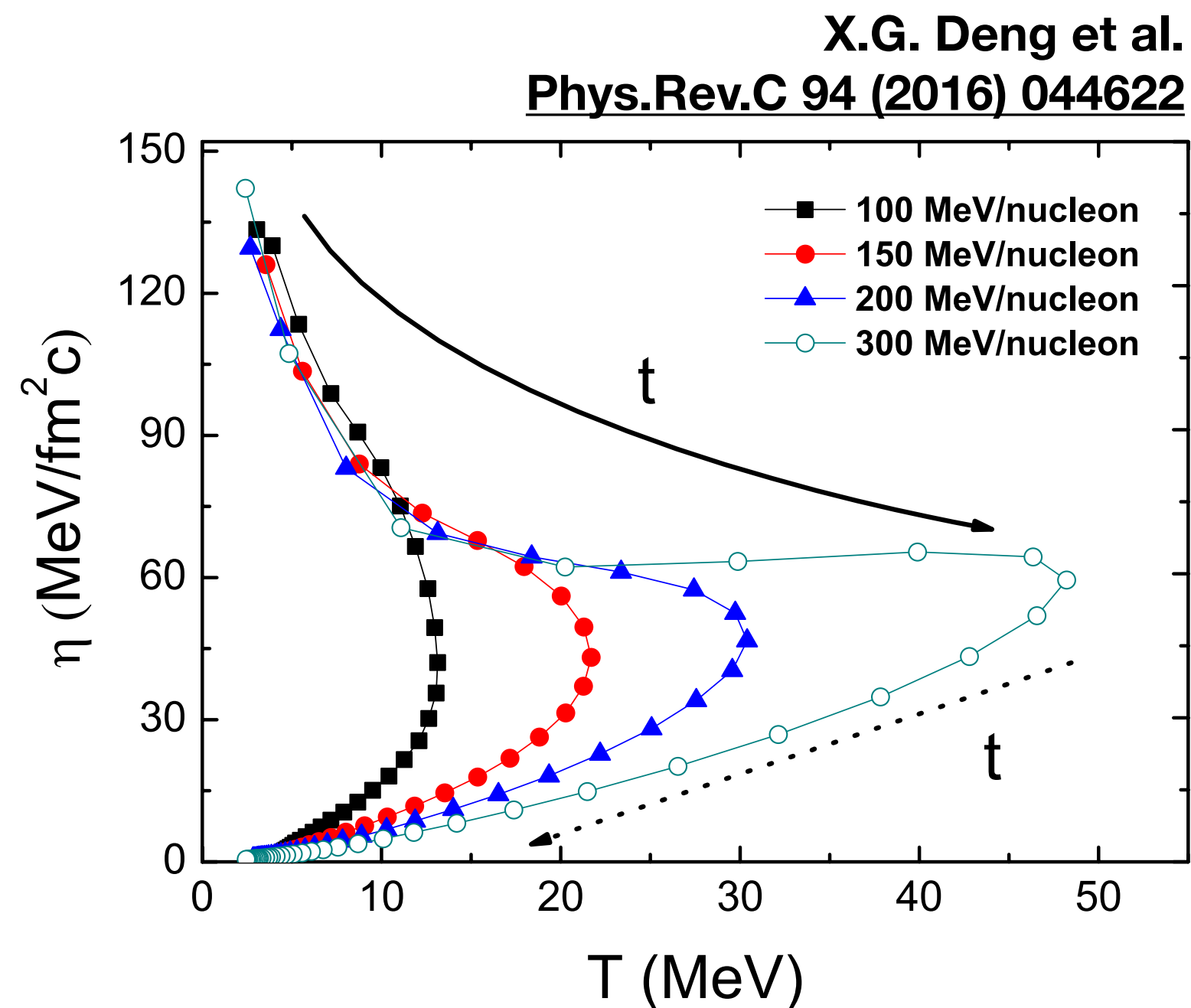




# Properties of Dense Nuclear Matter

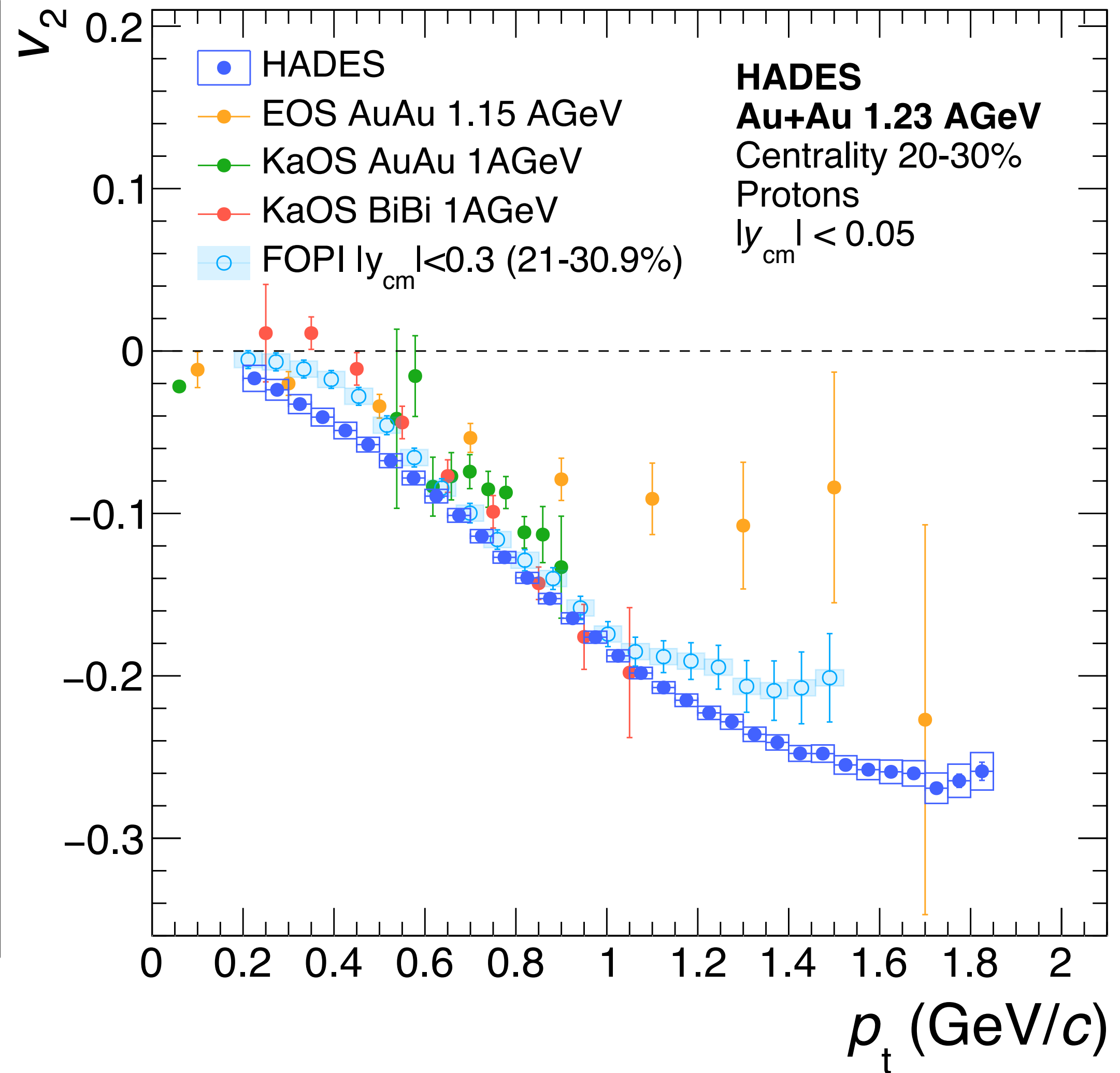
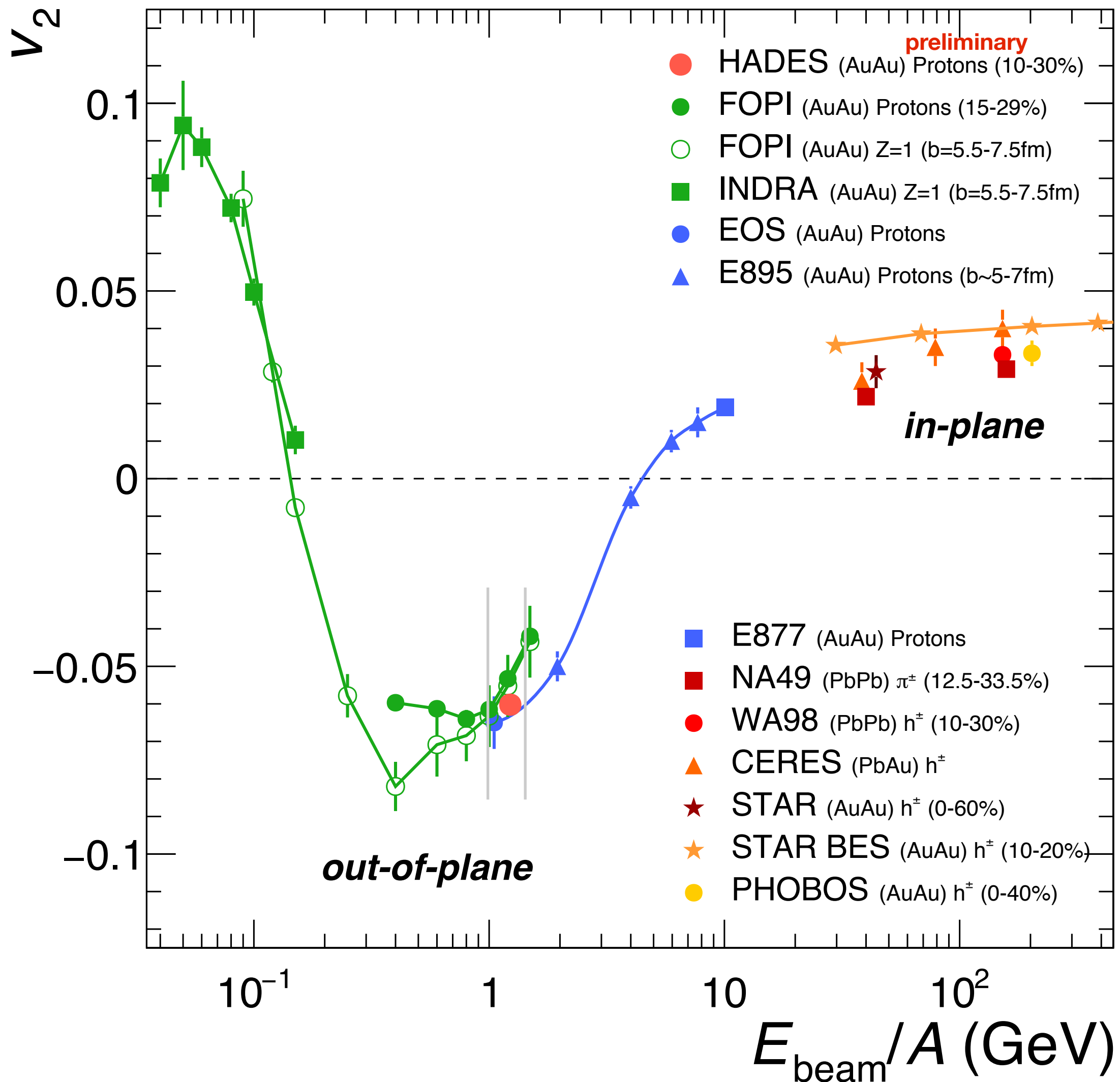
## Shear viscosity

- Nuclear shear viscosity extracted from transport models
- Mean-field potentials and in-medium cross section are constrained by stopping and flow observables



# Elliptic Flow $v_2$

Energy- and  $p_t$ -Dependence



**EOS:**  
 J. Kintner, Squeeze-Out and Flow of Pions from 1.5 GeV/Nucleon Au+Au. Dissertation, University of California Davis (1993)

**KaoS AuAu:**  
 D. Brill, Azimutal anisotrope Teilchenemission in relativistischen Schwerionenstößen. Dissertation, Goethe-University, 1993

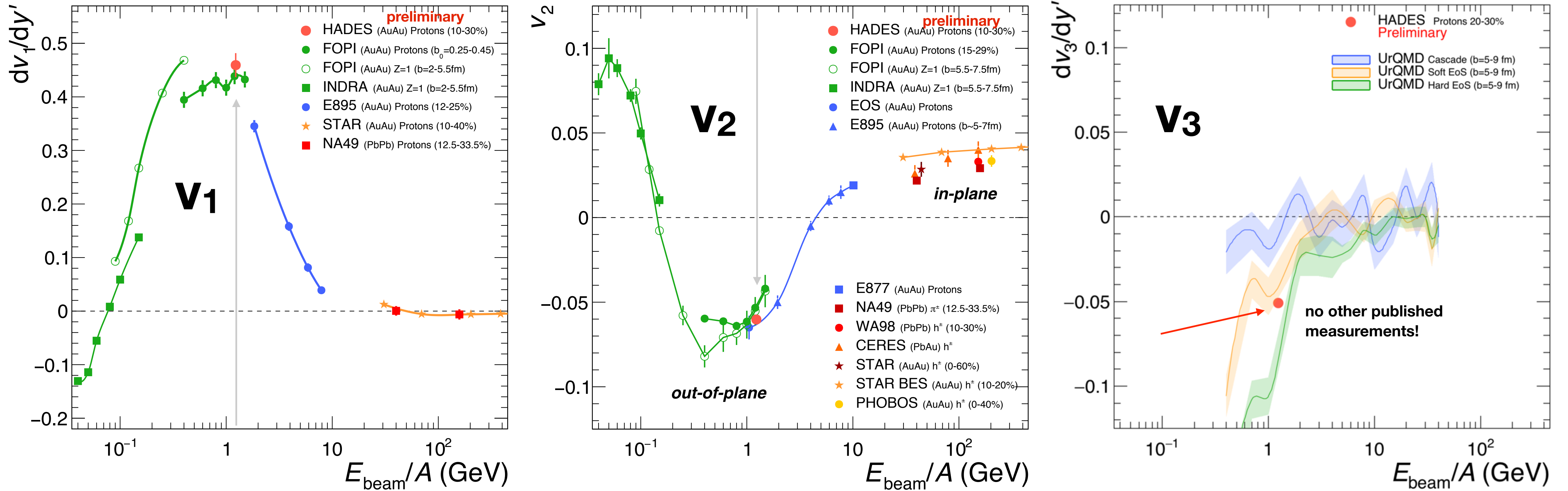
**KaoS BiBi:**  
 D. Brill, et al., Z. Phys. A355, 61 (1996).

**FOPI:**  
 Nucl.Phys. A876 (2012) 1-60



# Motivation

## Energy Dependence and Systematics of Flow

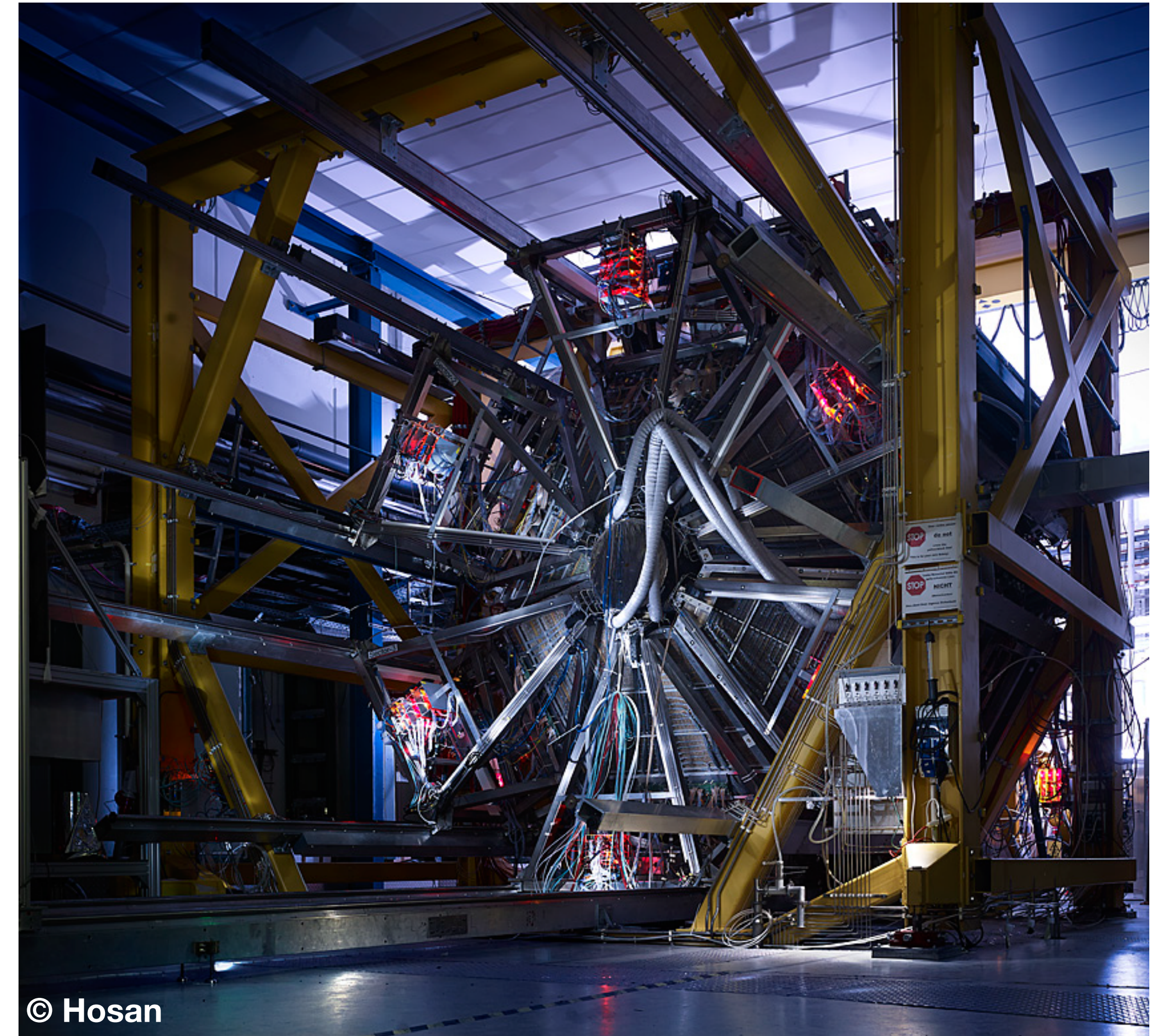


- Fully multi-differential measurement in Centrality and Phase Space (Pt and Rapidity)
  - Directed  $v_1\{\Psi_{RP}\}$  and Elliptic  $v_2\{\Psi_{RP}\}$
- First measurement at SIS energies of
  - Triangular  $v_3\{\Psi_{RP}\}$  and higher flow harmonics



# High Acceptance Di-Electron Spectrometer

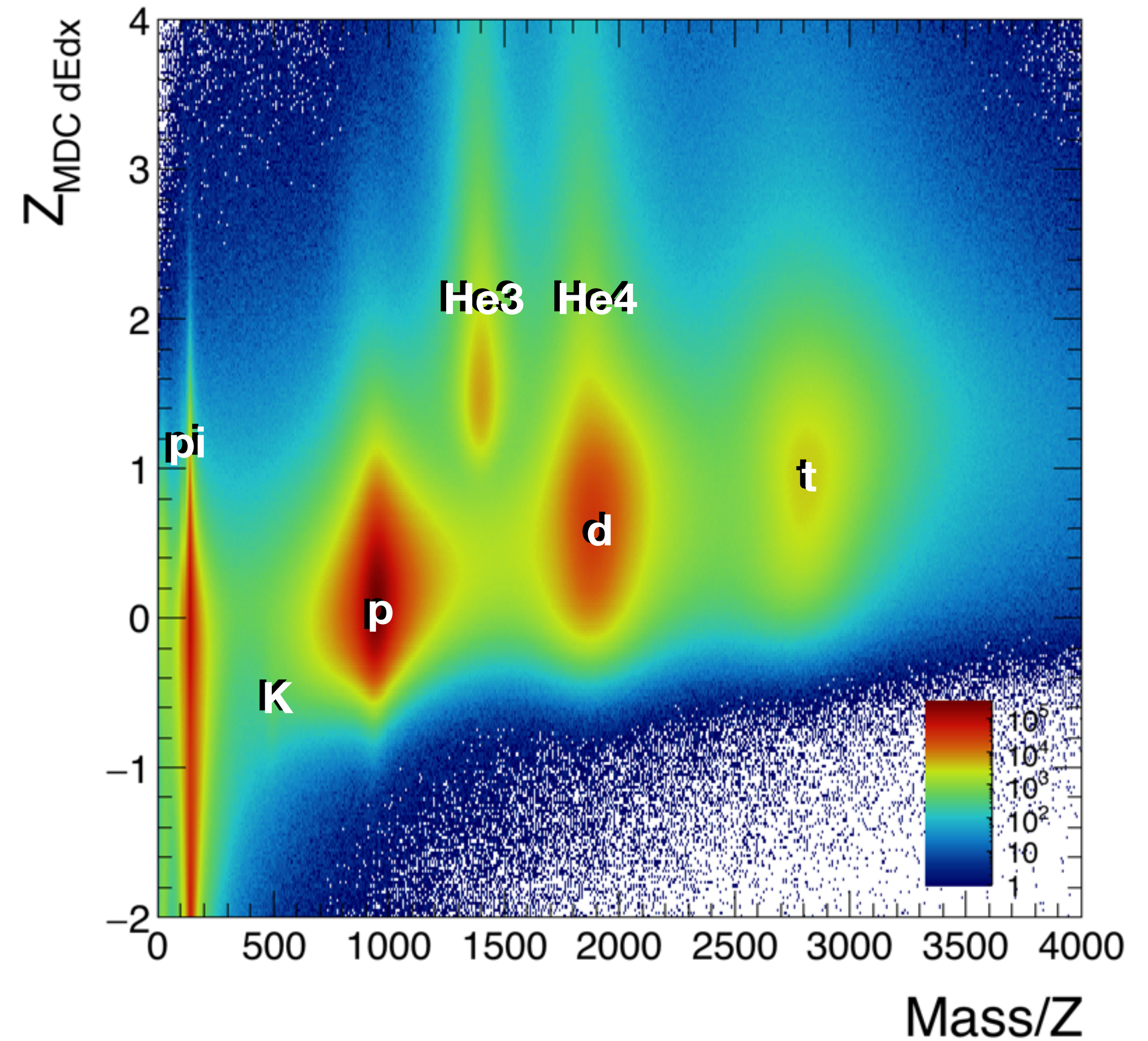
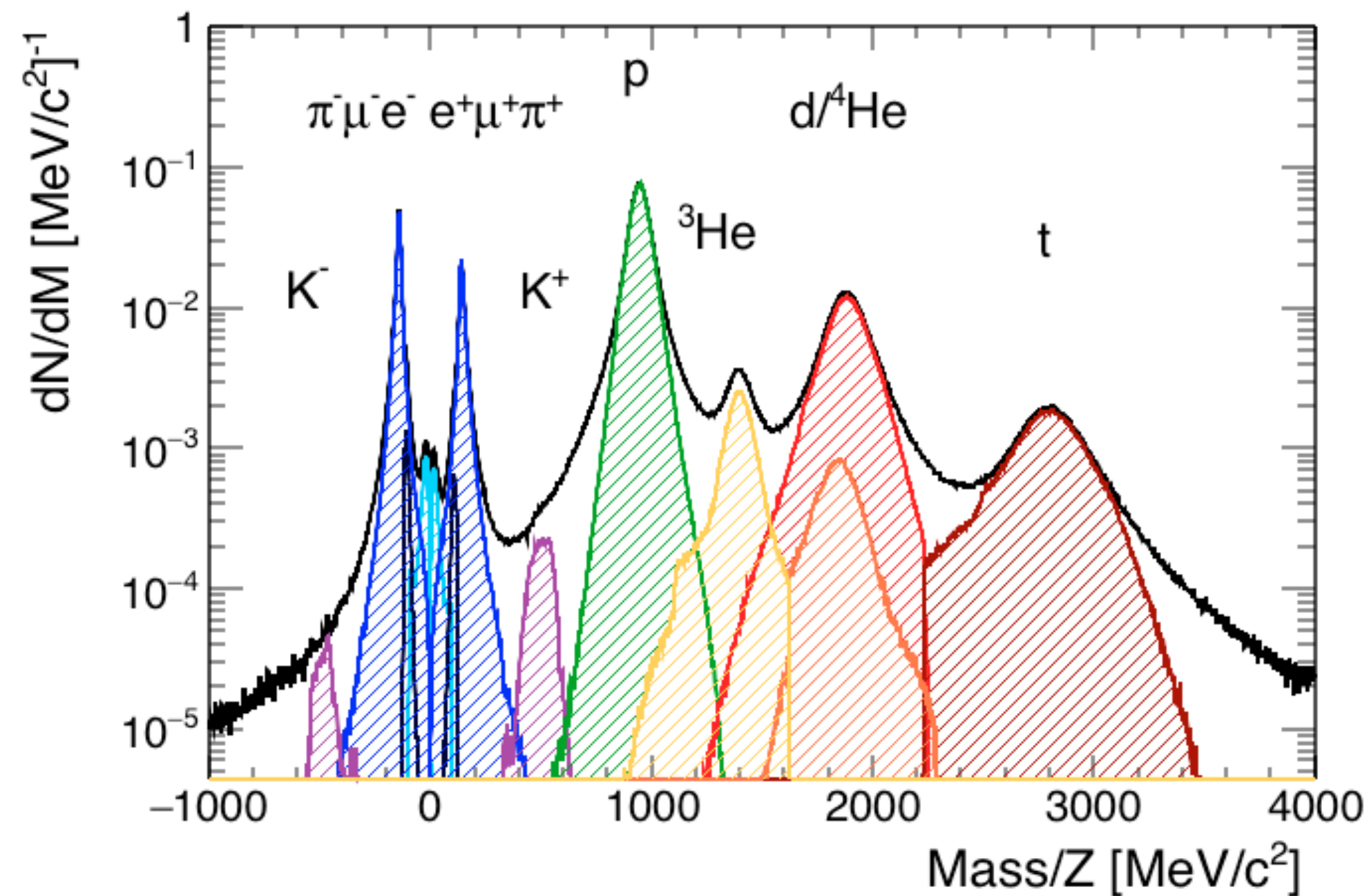
- High interaction rates and statistics
  - ▶ 5 weeks of beamtime with 558.3 hours of data taking
  - ▶ Beam intensities between  $1.2 - 2.2 \times 10^6$
  - ▶ Total number of events recorded:  $7 \times 10^9$
- Large acceptance
  - ▶ Symmetric azimuthal coverage
  - ▶  $18^\circ - 85^\circ$  in polar angle
- Tracking system and magnetic spectrometer
  - ▶ 4 planes of low-mass mini-drift chambers (MDC)
  - ▶ Superconducting toroidal magnet
- Forward Wall
  - ▶ Reaction plane reconstruction





# Particle identification

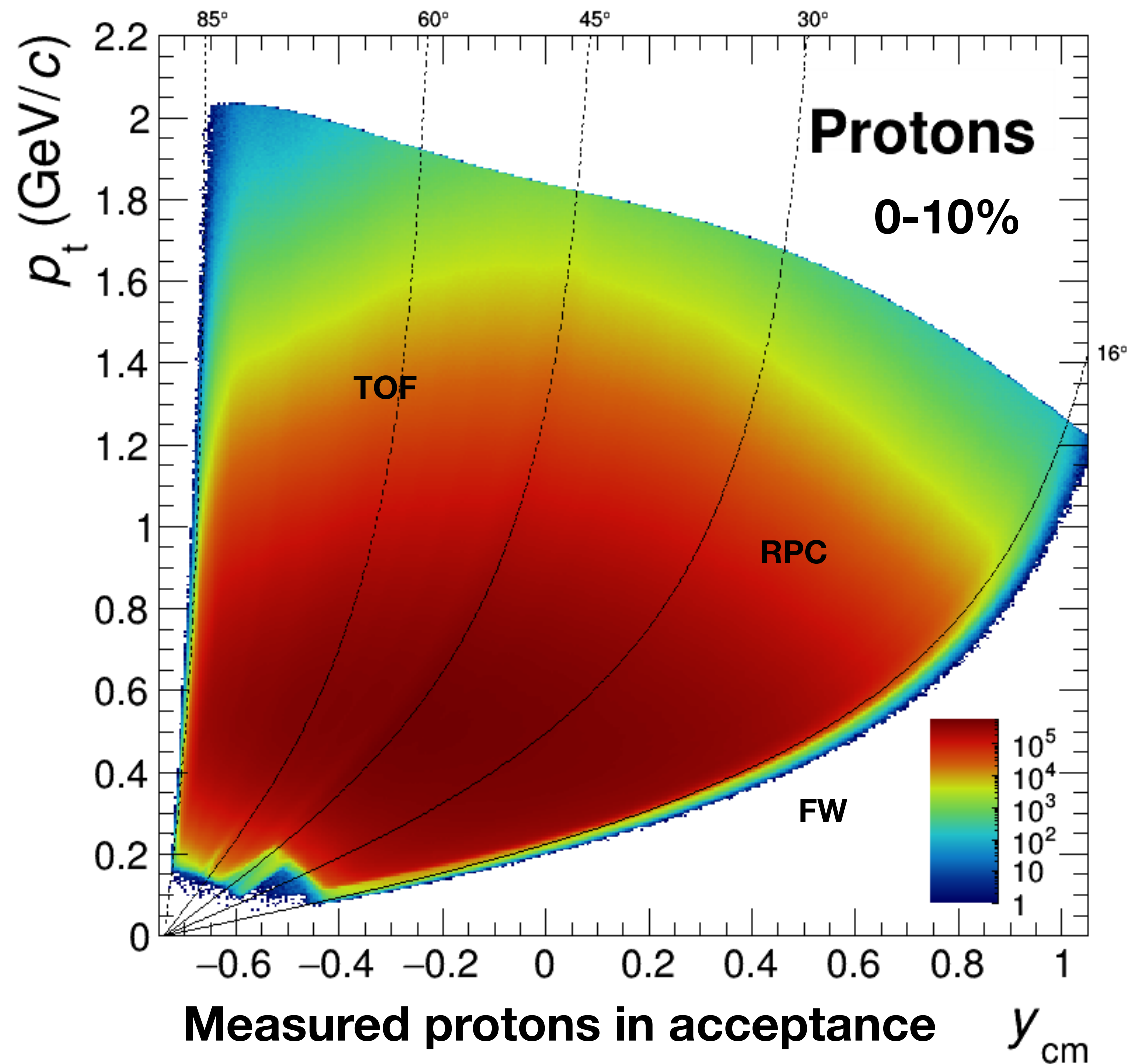
- Time-of-Flight (TOF and RPC)
- Energy loss in the MDC  $Z_{MDC} = \ln\left[\frac{(dE/dx)_{measured}}{(dE/dx)_{proton}}\right]$ 
  - ▶ Separation deuterons and He





# HADES Performance

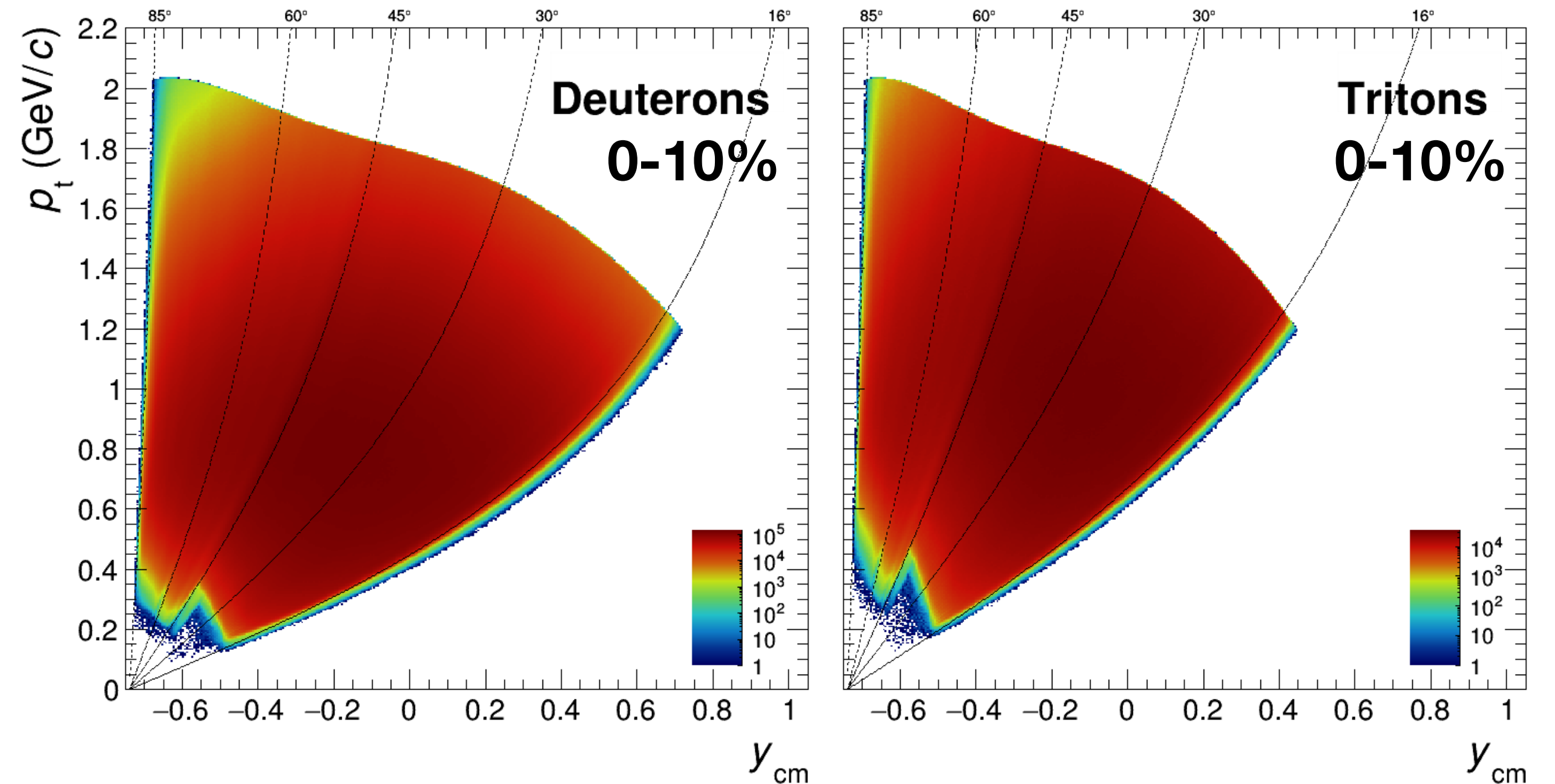
## Multidifferential Analysis



**4x 10% Centrality Classes**  
**6x Flow Harmonics**  
Total yield of individual  $p_t$ - $y$  bins:

**8k protons, 6k deuteron, 5k tritons**

with ~20 systematic variations  
to estimate uncertainties





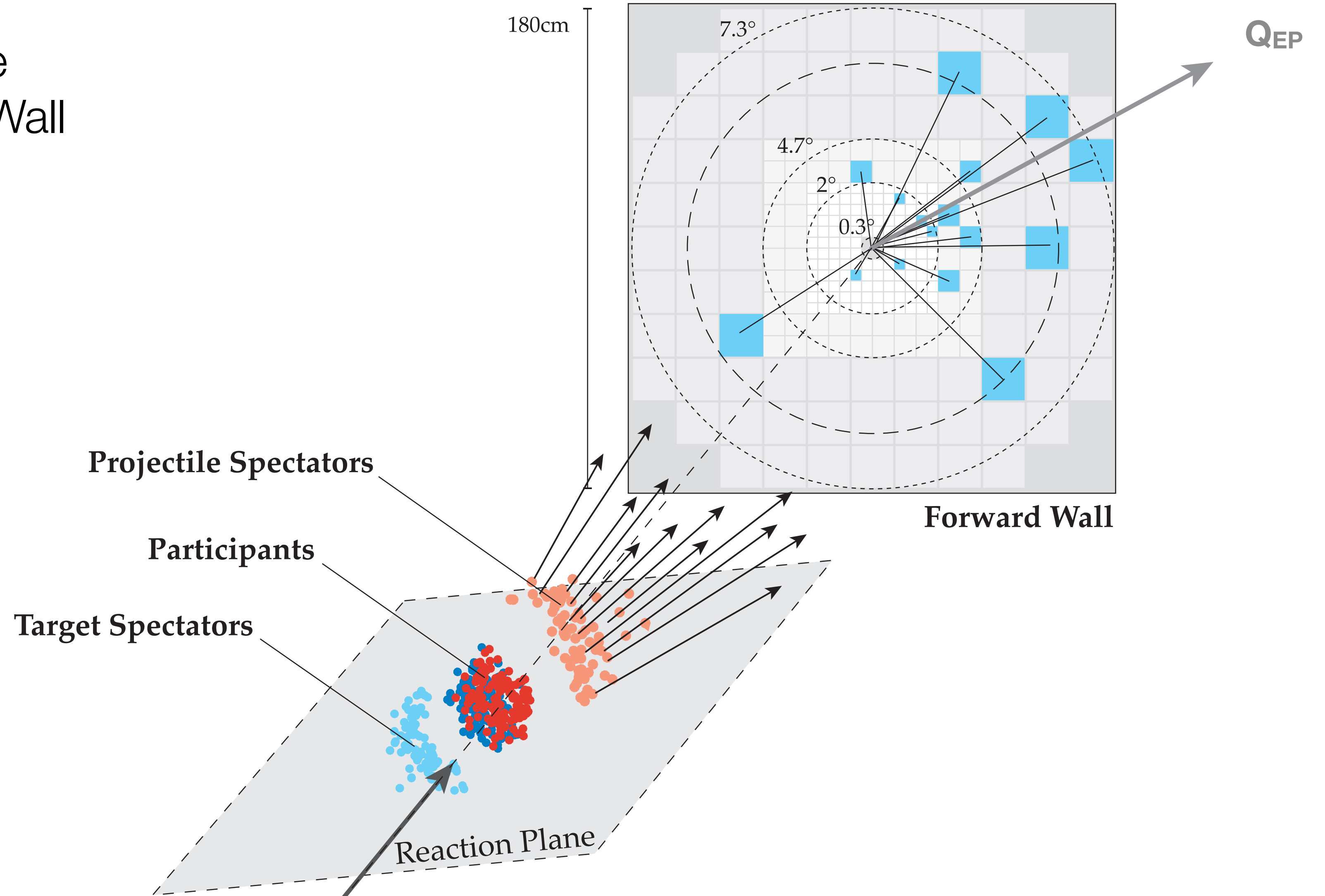
# Event Plane Reconstruction

- Based on the angle of projectile spectators hits in the Forward Wall

$$Q_{n,x} = \sum_{i=0}^{N_{FW}} w_i \cos(n \phi_{FW,i})$$

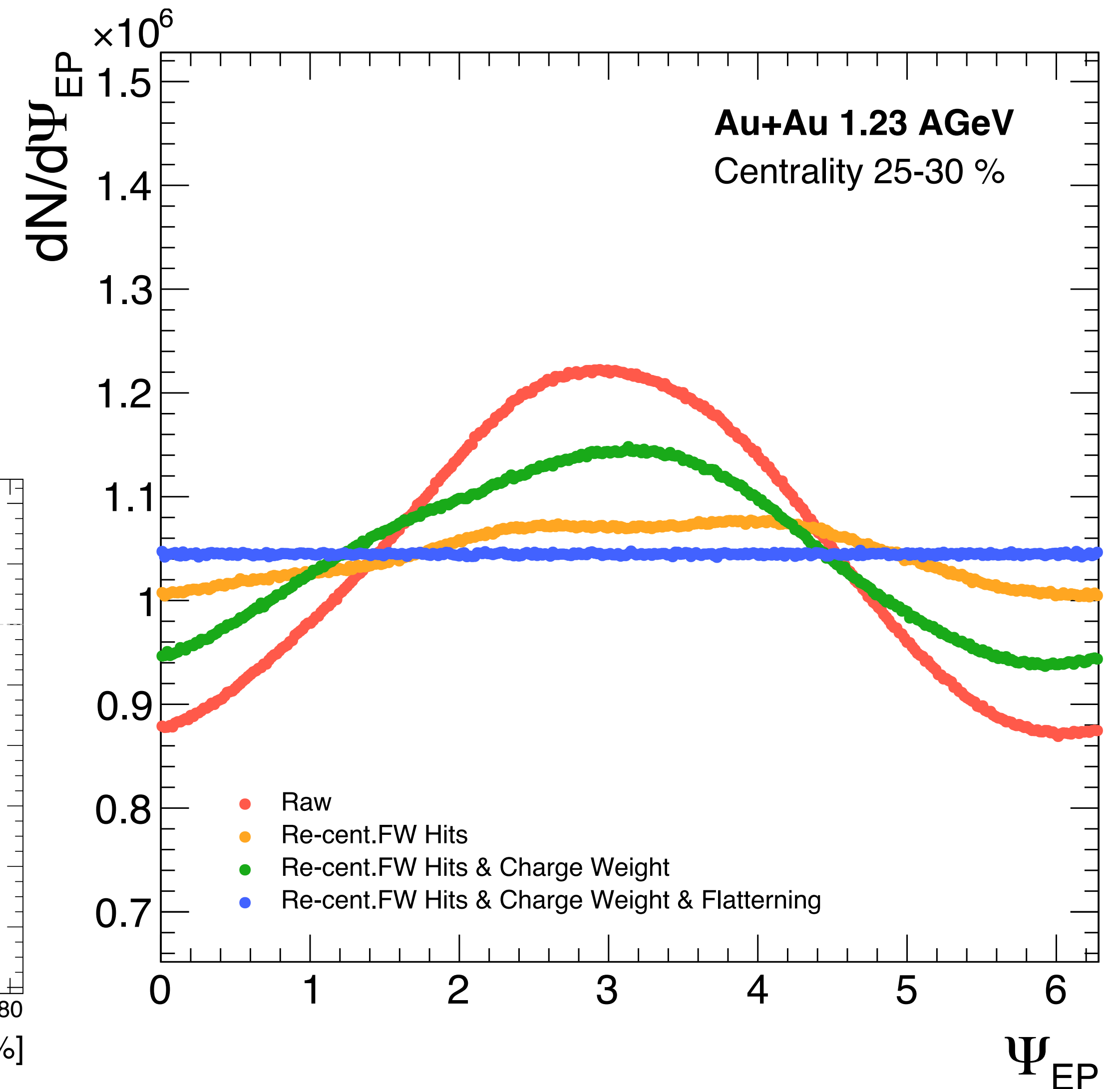
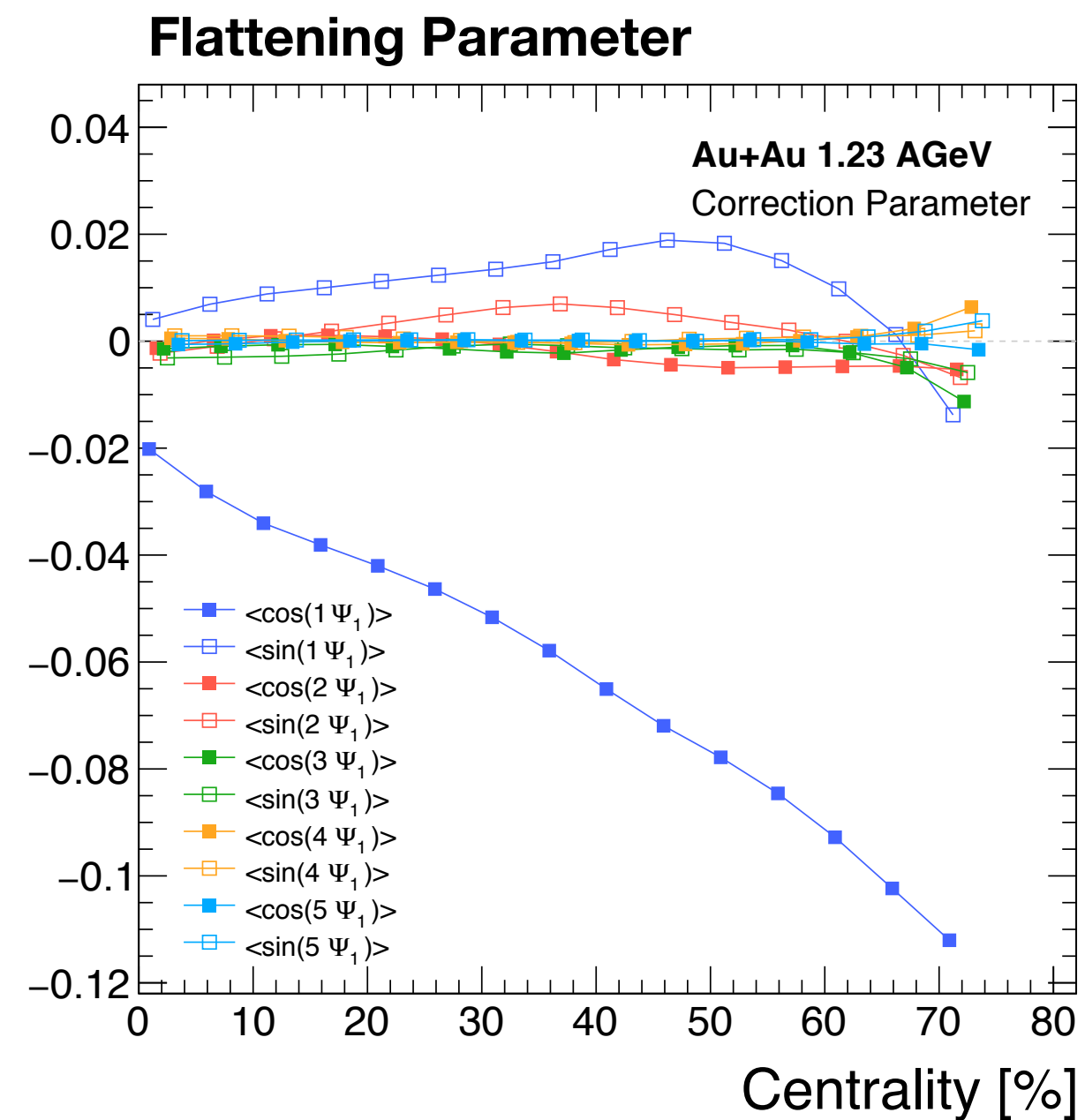
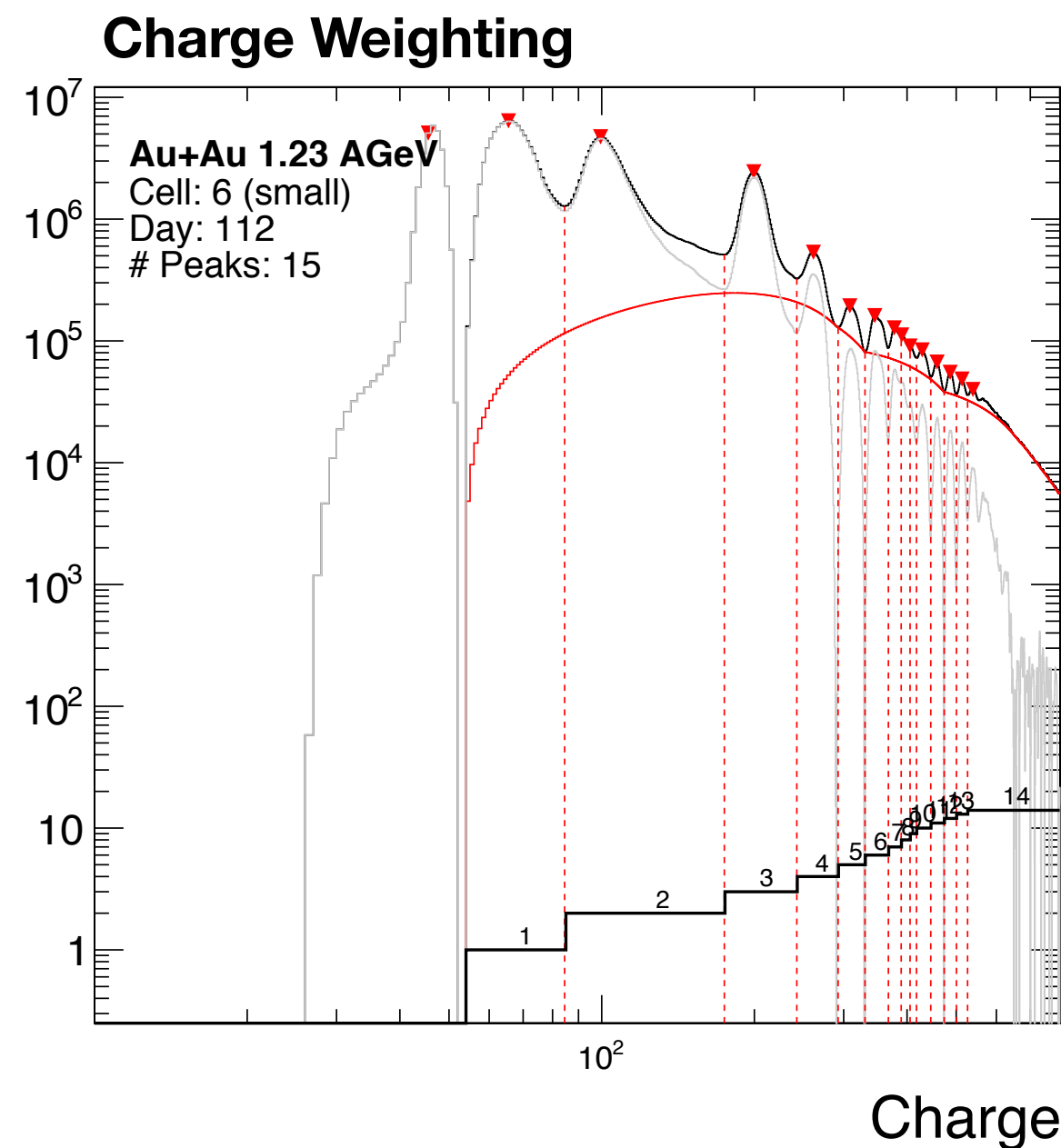
$$Q_{n,y} = \sum_{i=0}^{N_{FW}} w_i \sin(n \phi_{FW,i}) .$$

$$\tan \psi_{EP,1} = \frac{Q_{1,y}}{Q_{1,x}}$$



# Event Plane Determination

- Re-Centering of X and Y of all FW hits (day-by-day and Centrality)
- Z-Weighting up to Charge 14
- Flattening of residual Fourier components with 8x Cos- and 8x Sin-Terms



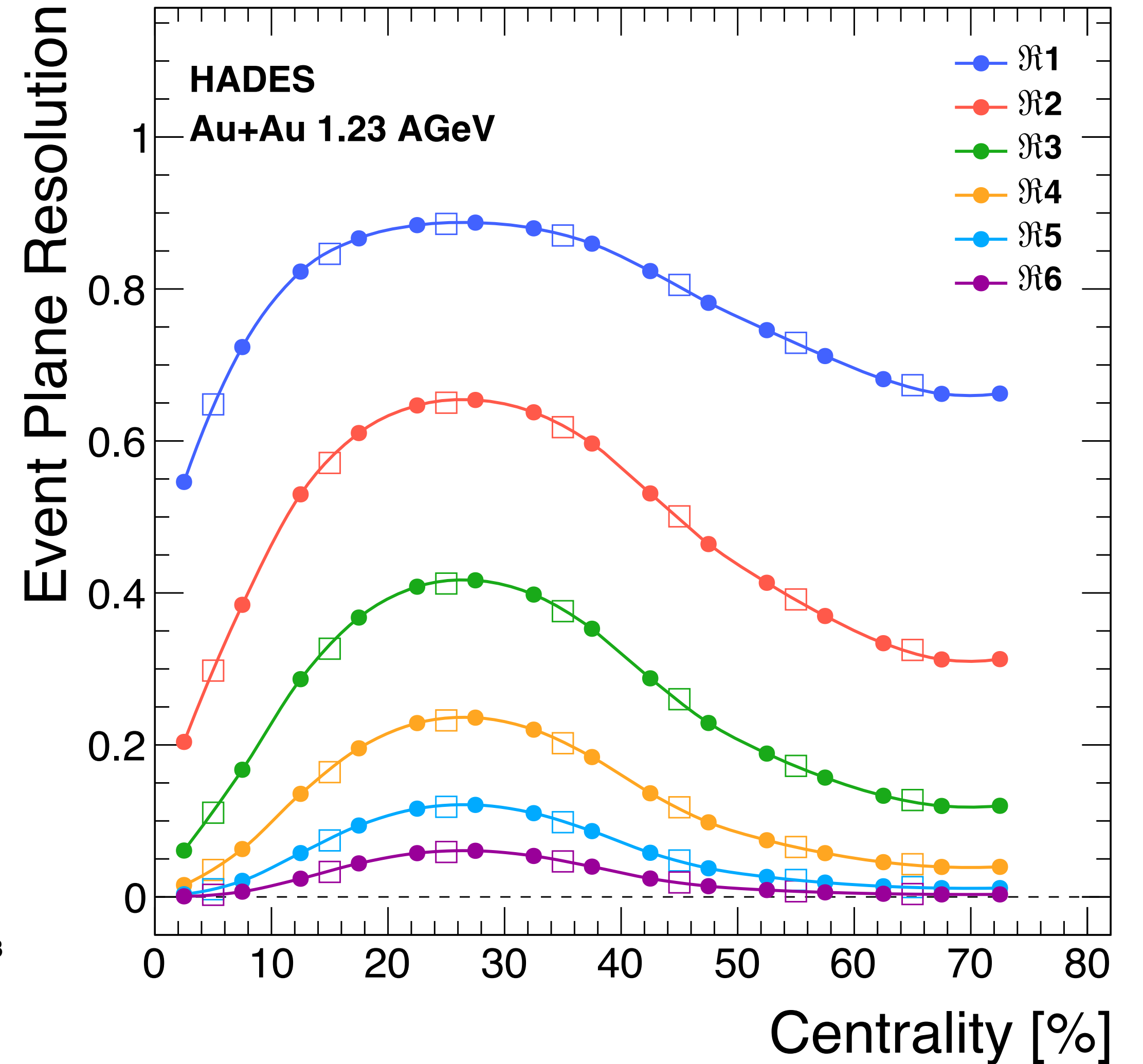
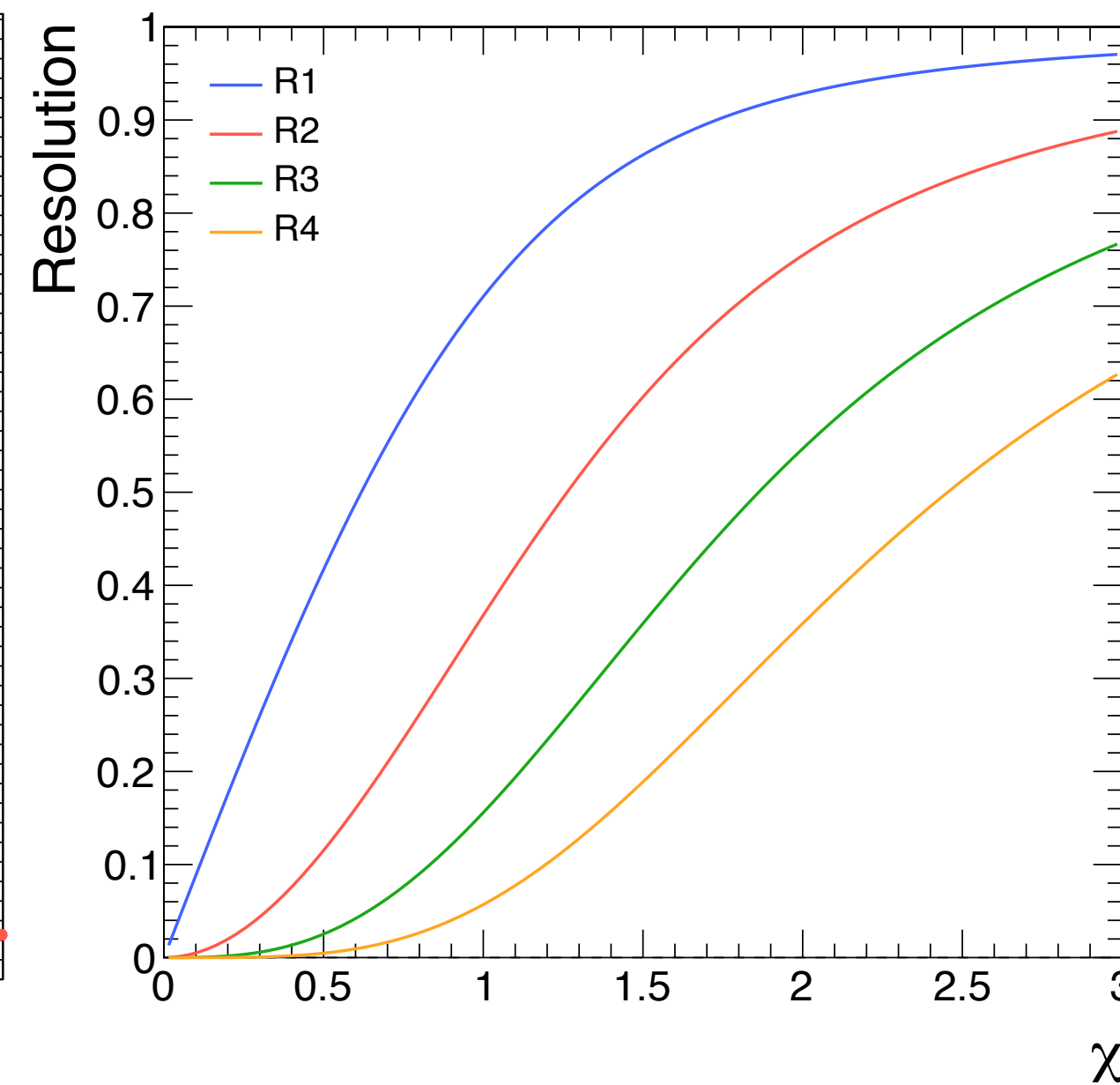
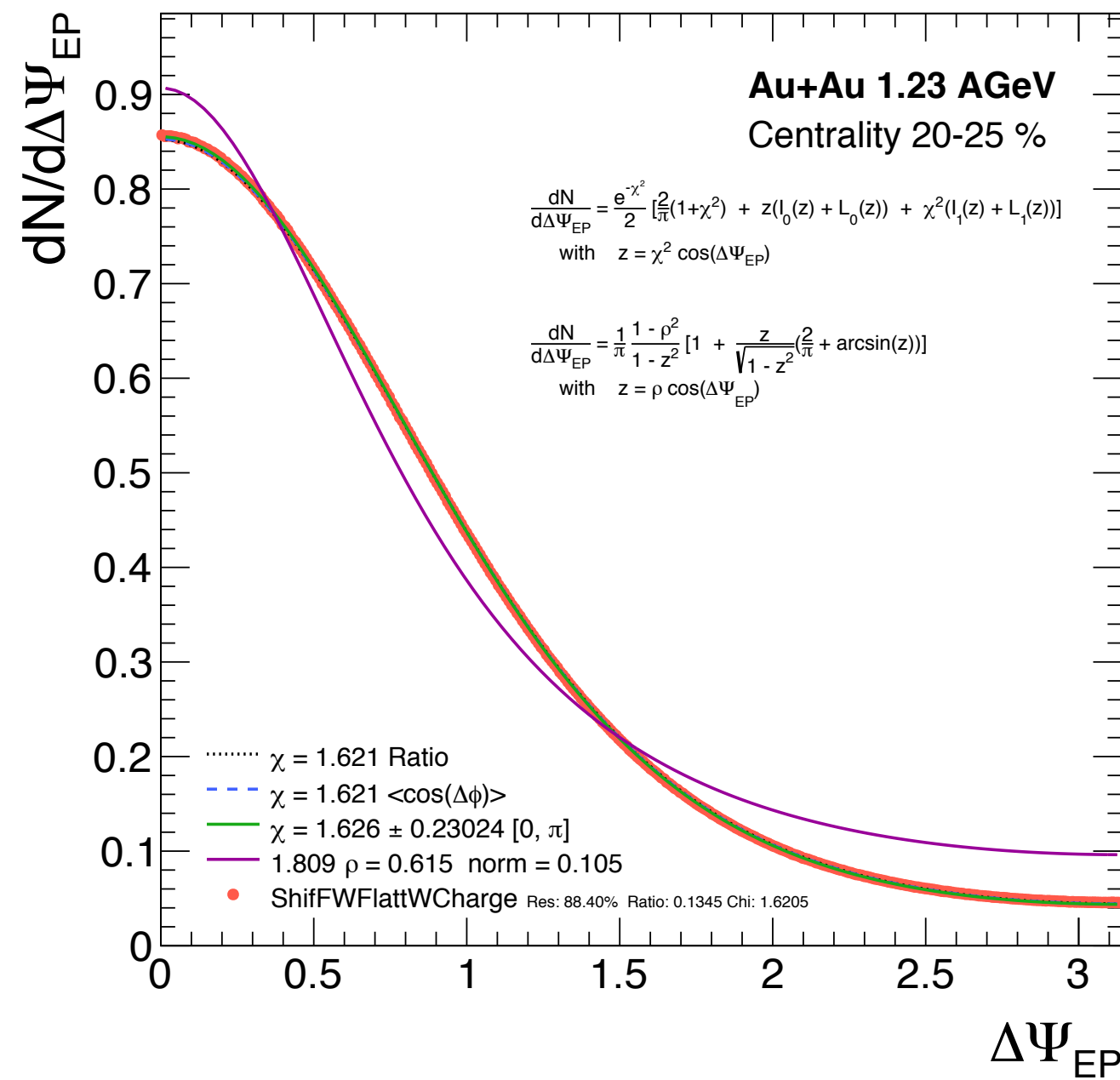


# Event Plane Resolution

- EP-Resolution determined by Ratio-,  $\langle \cos(\Delta\Phi) \rangle$  and Fit-Method in Sub-Events

$$v_n = v_n^{obs} / \mathcal{R}_n$$

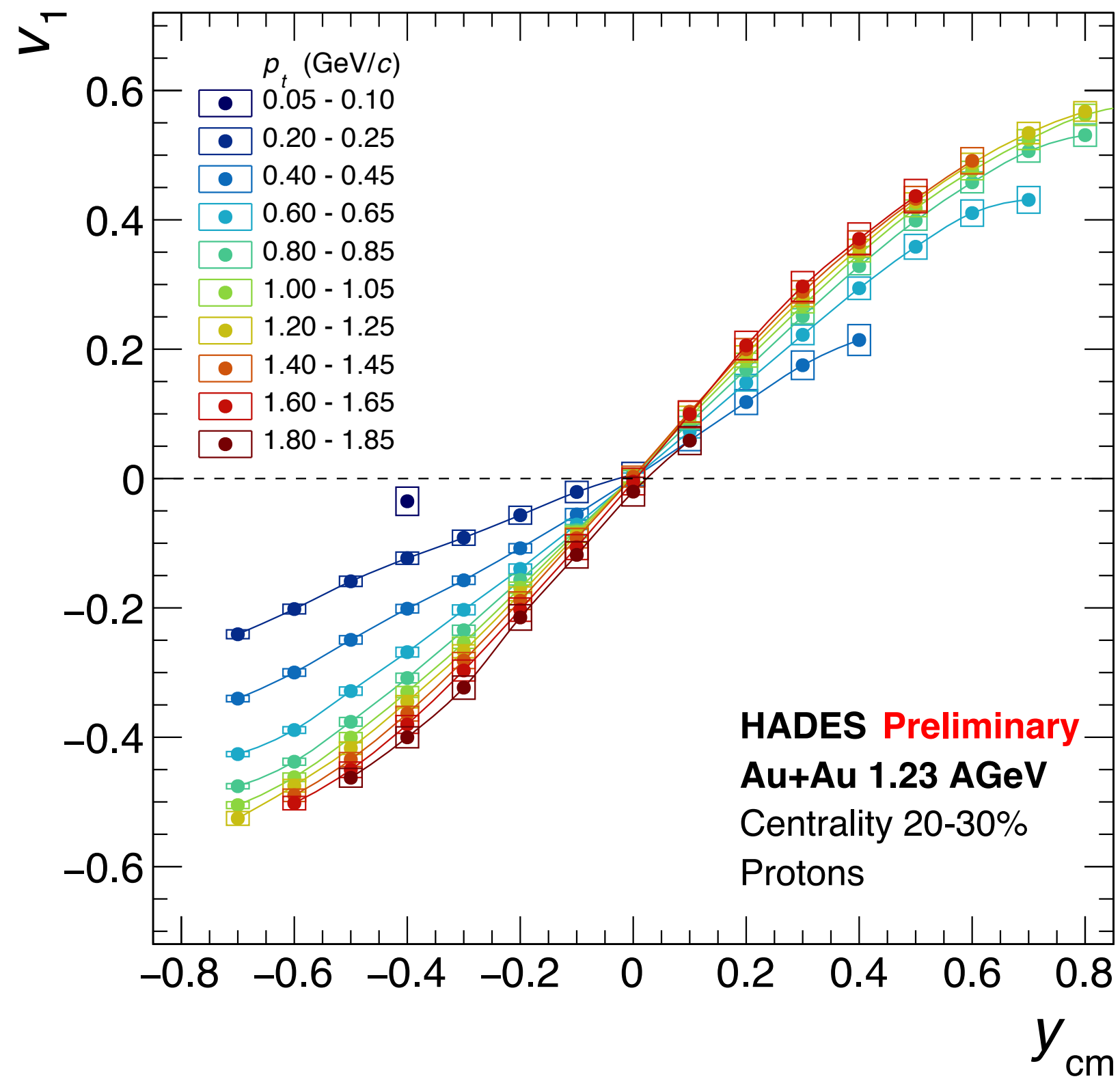
$$\mathcal{R}_n = \langle \cos[n(\Psi_n - \Psi_{RP})] \rangle$$



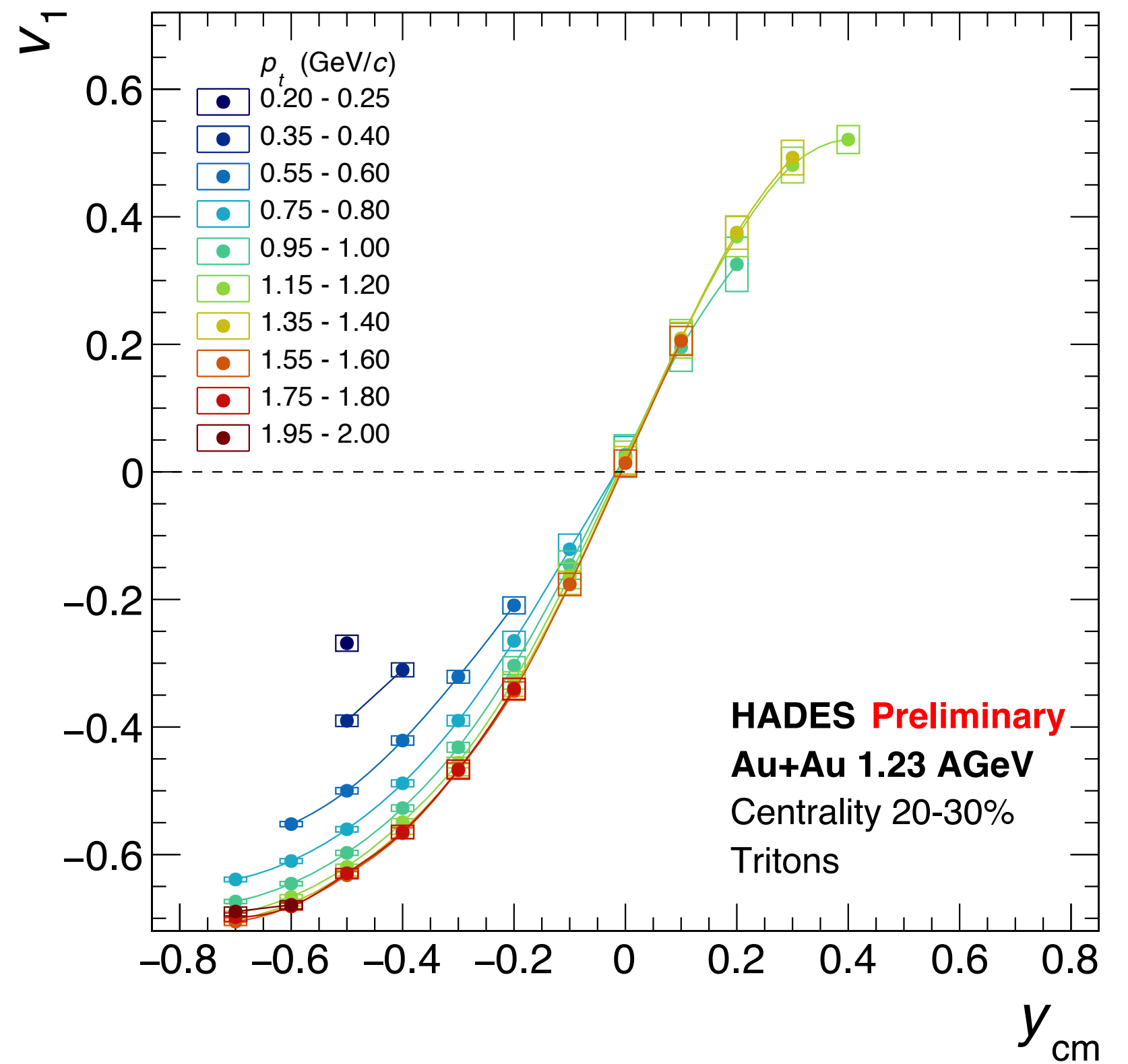
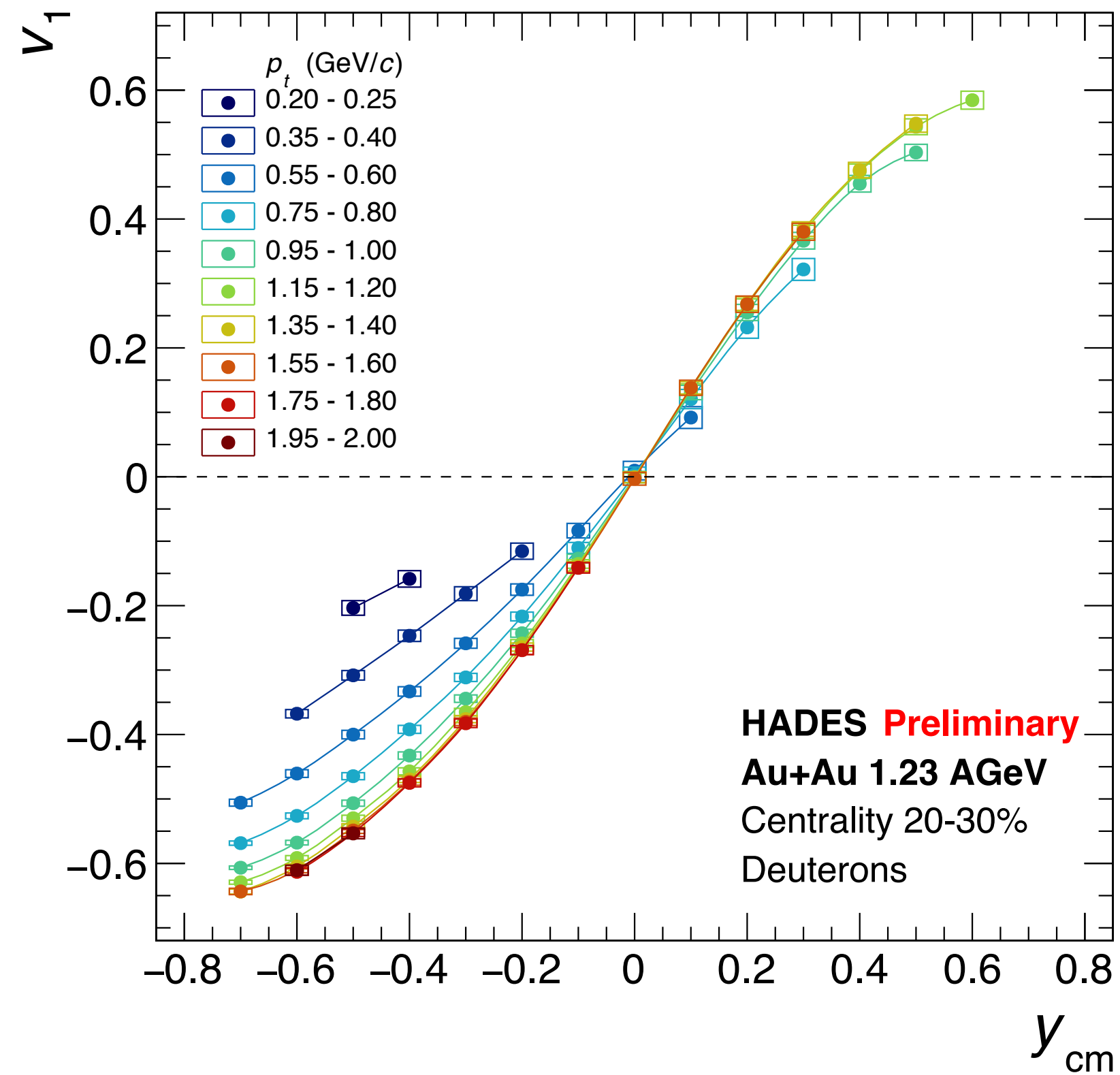
# Directed Flow $v_1$ : Protons and Light Nuclei

$p_t$ -Dependence

QM17, Nucl.Phys. A967 (2017) 812-815



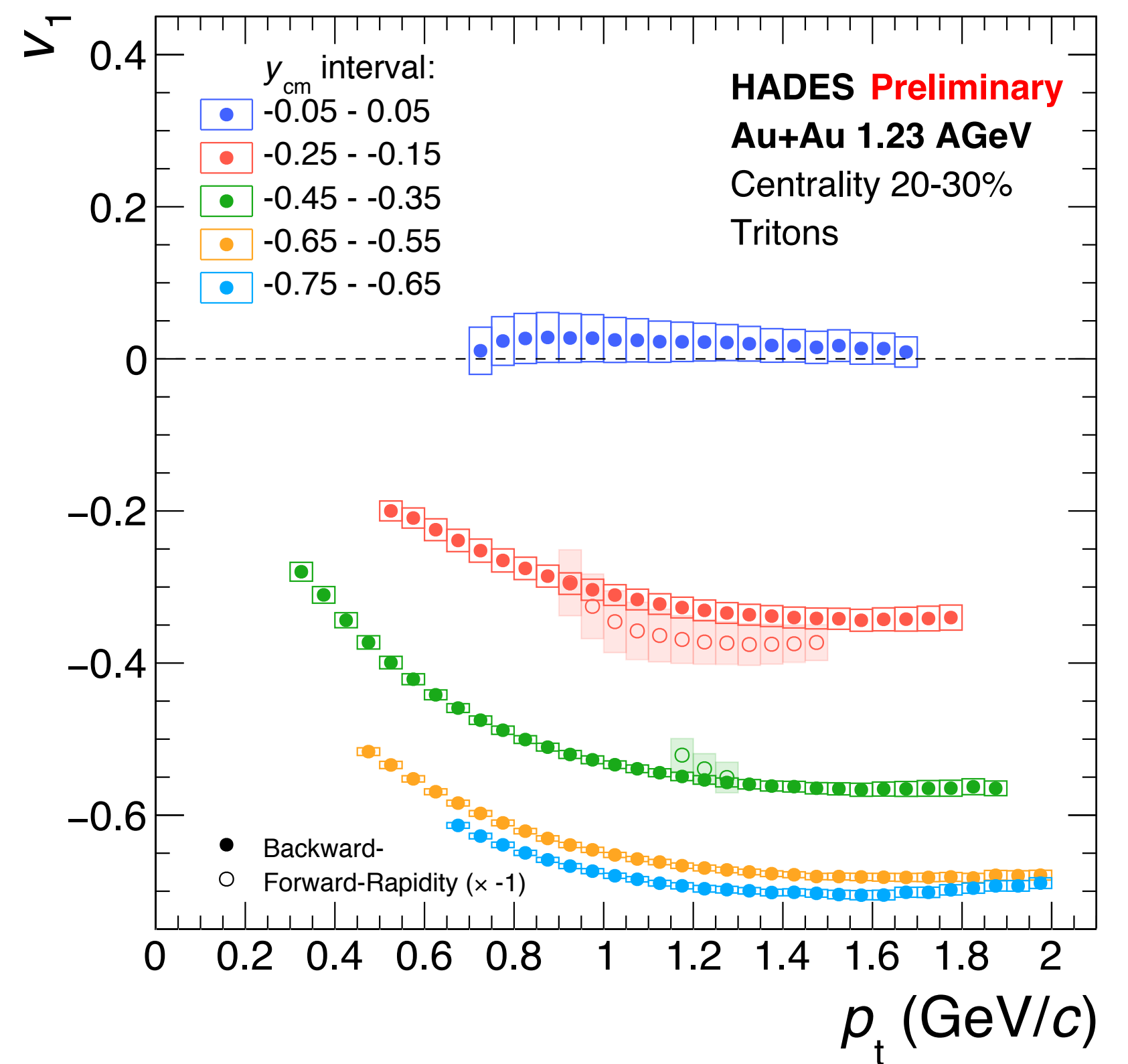
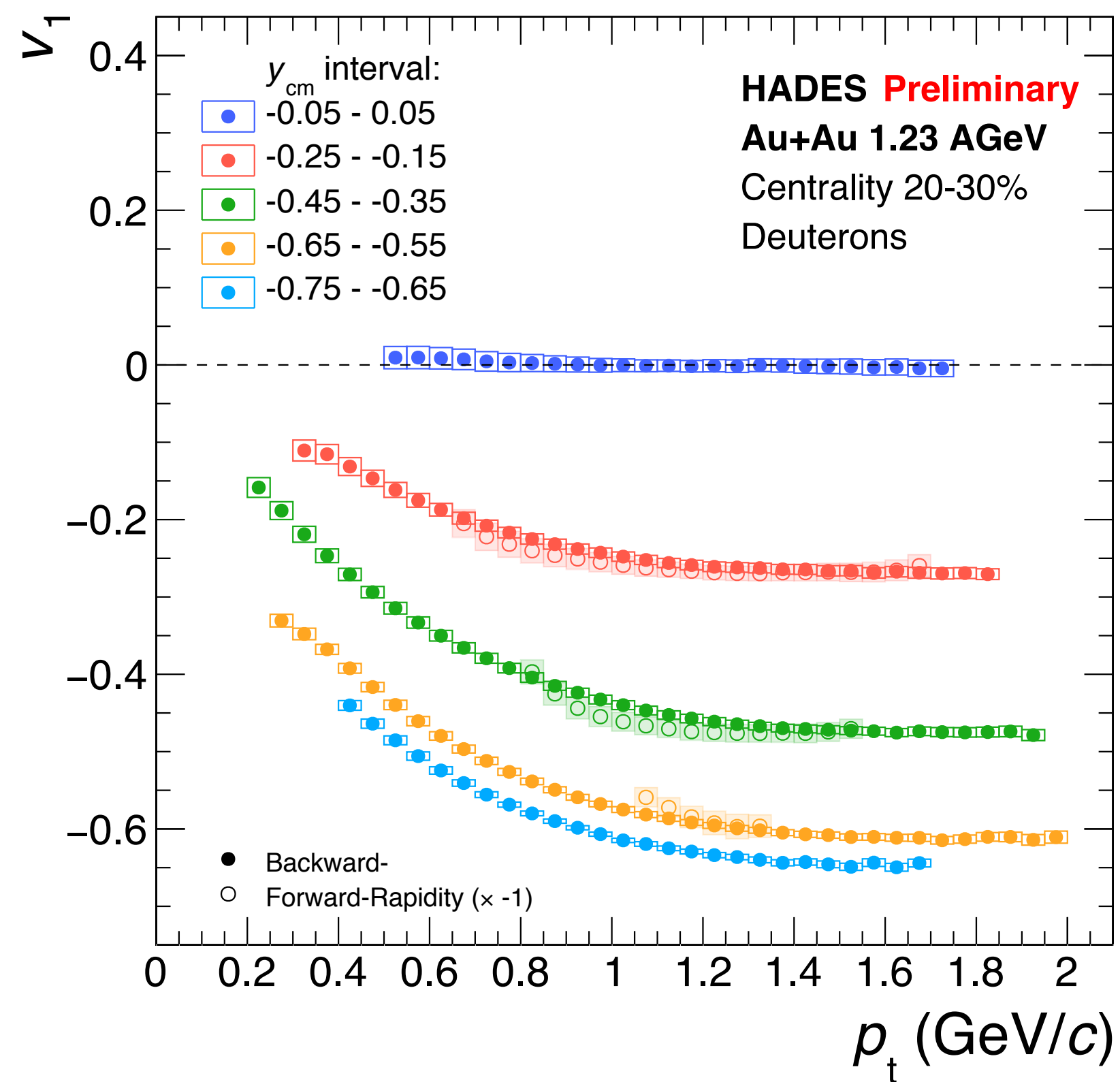
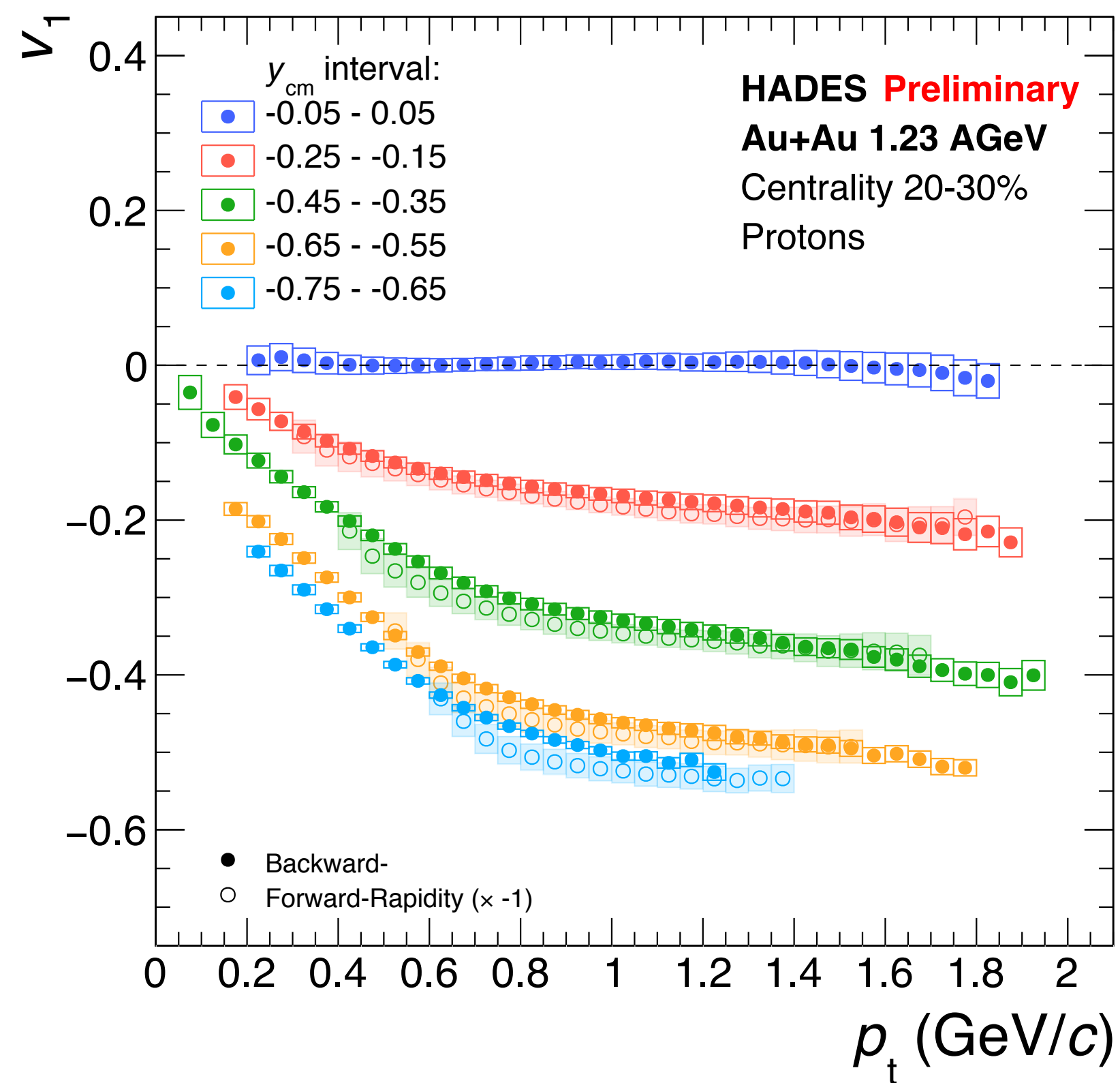
QM18, Nucl.Phys. A982 (2019) 431-434, arXiv:1809.07821





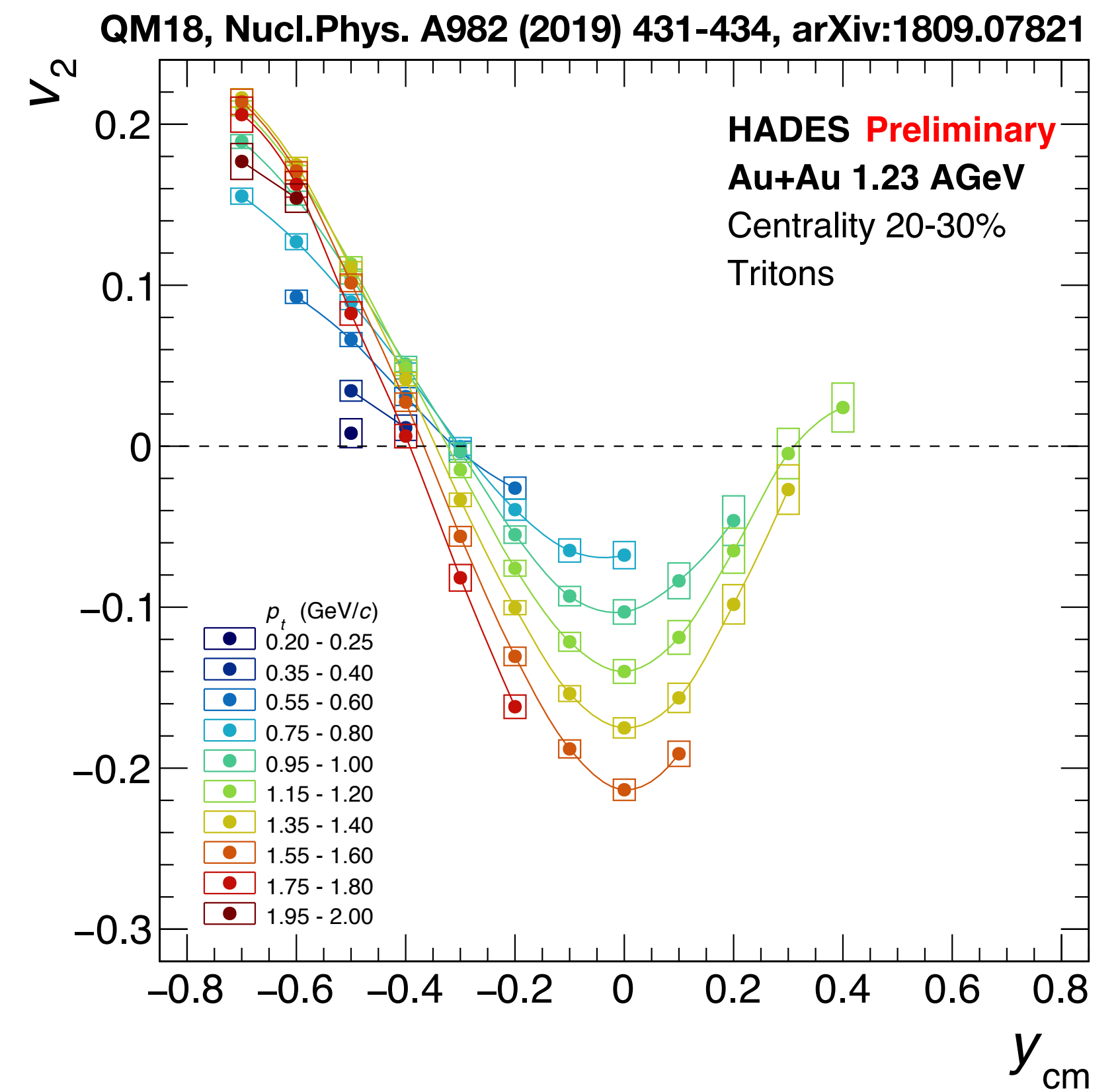
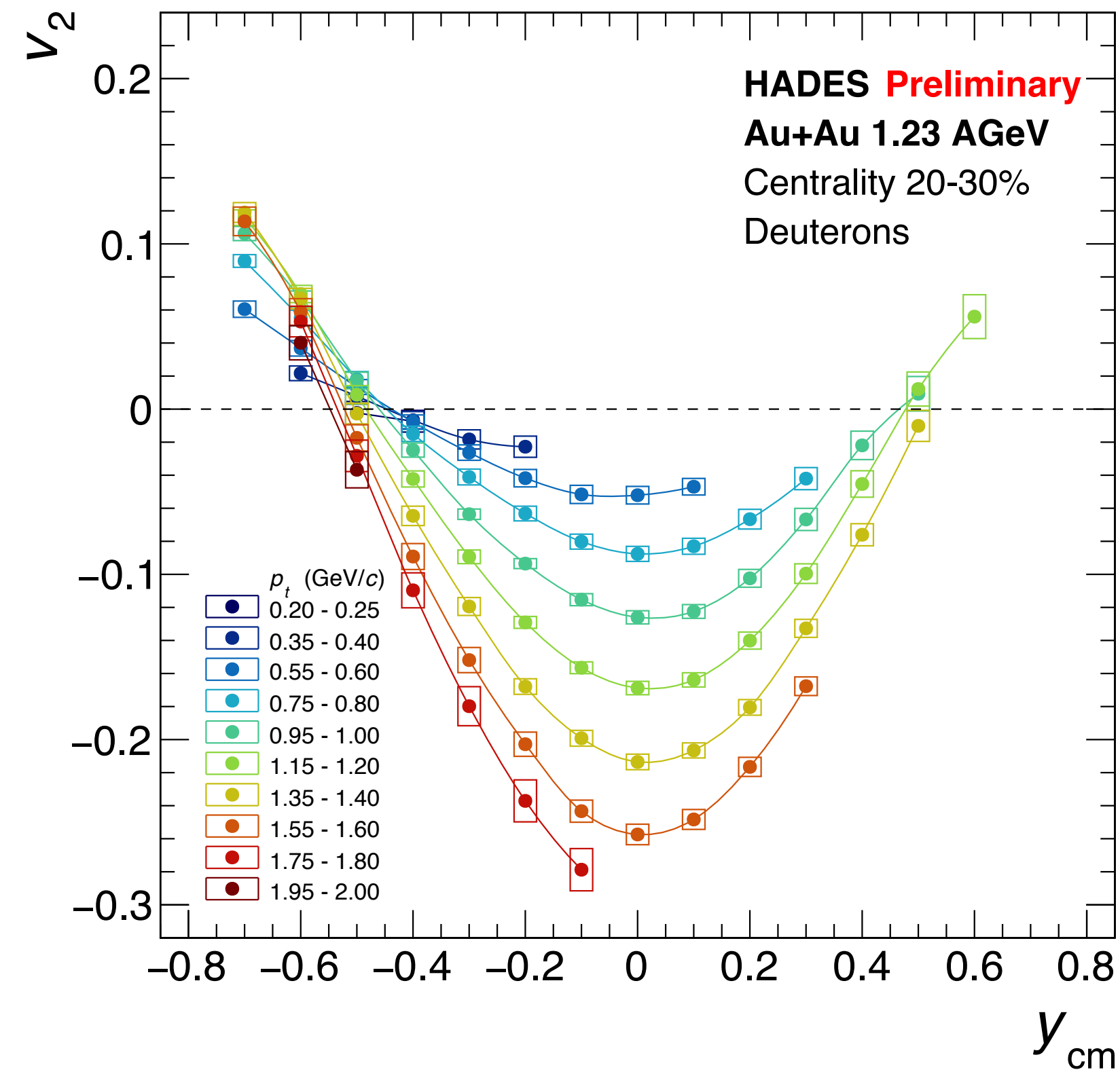
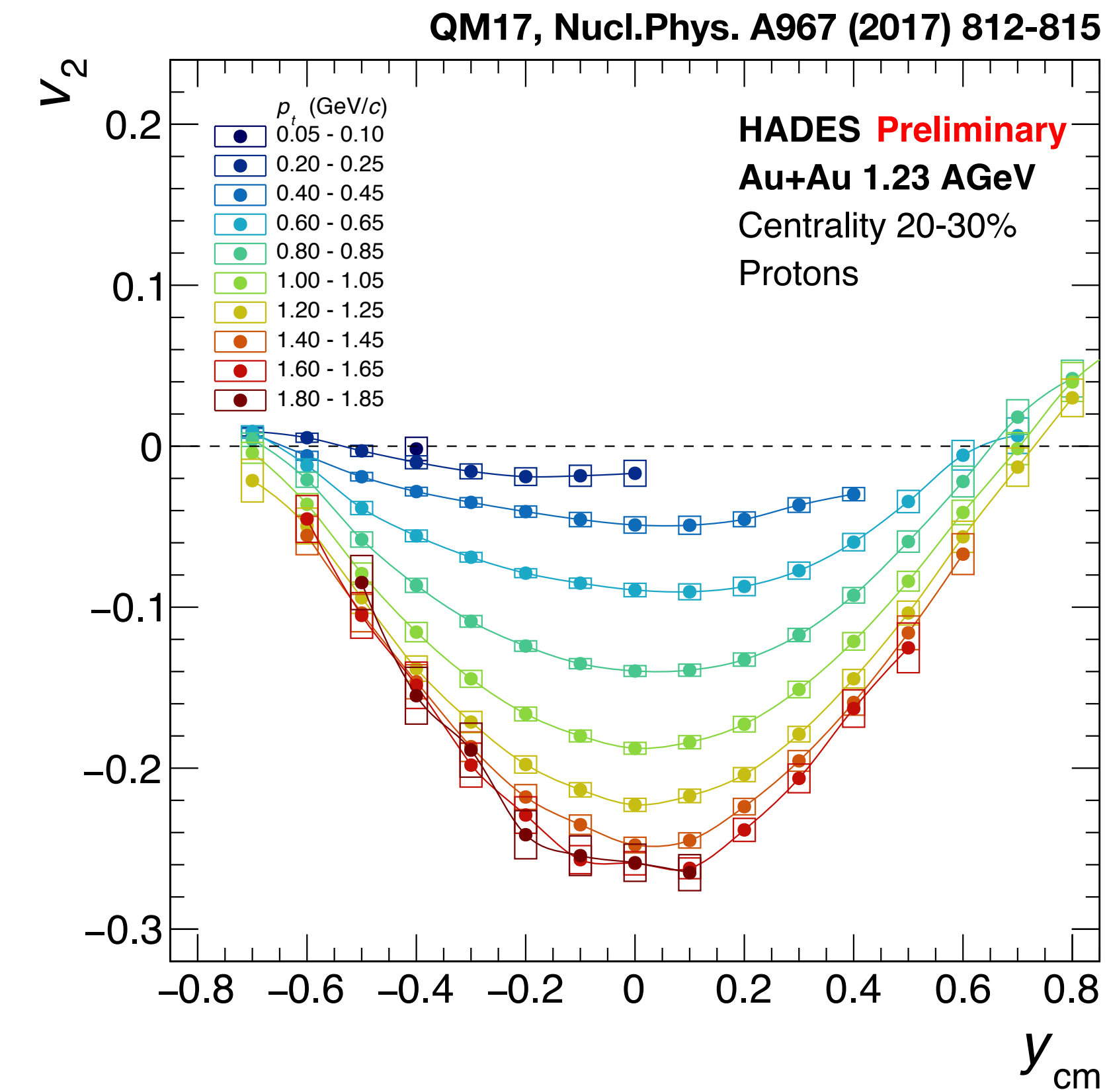
# Directed Flow $v_1$ : Protons and Light Nuclei

$p_t$ -Dependence



# Elliptic Flow $v_2$ : Proton and Light Nuclei

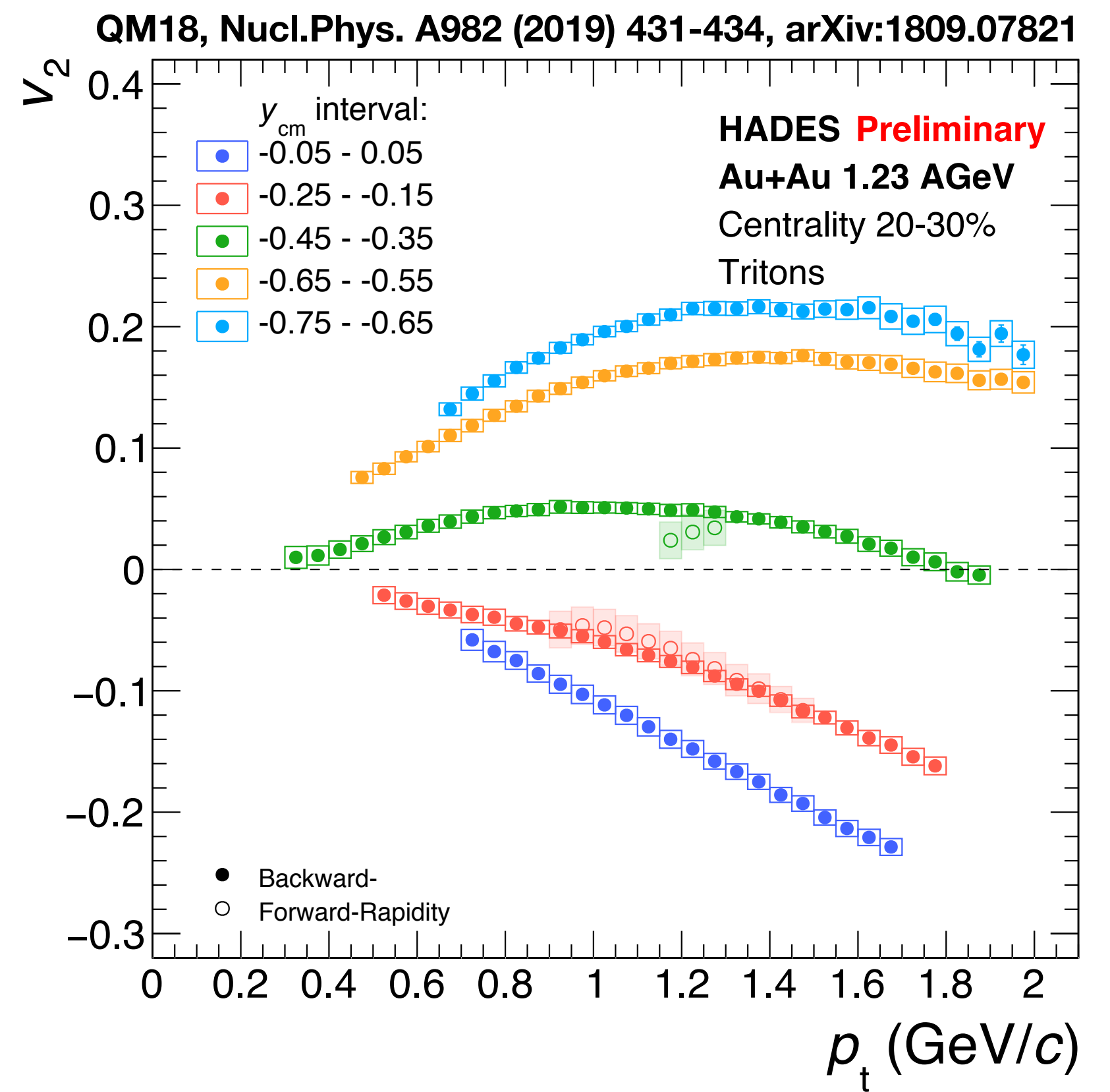
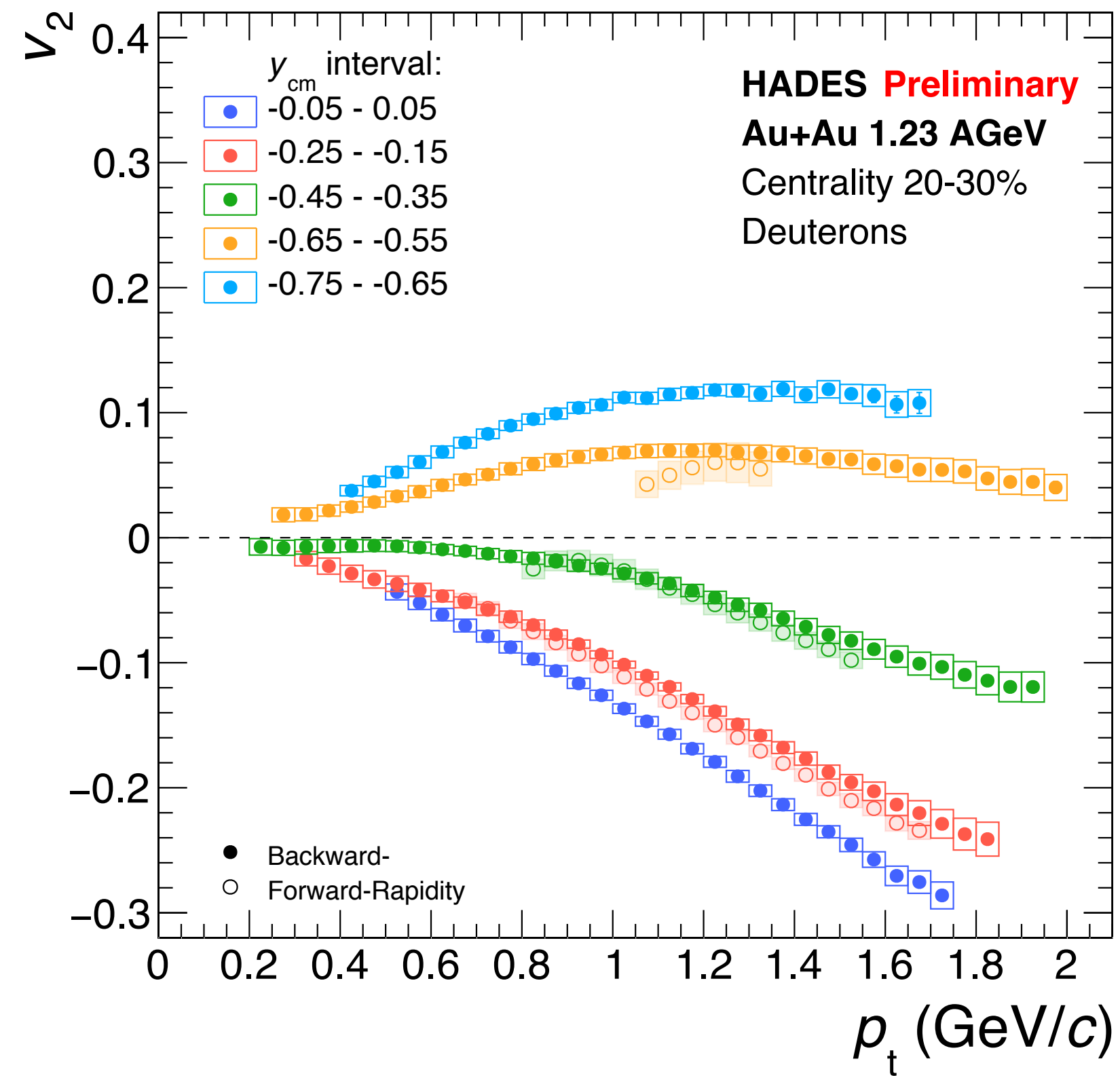
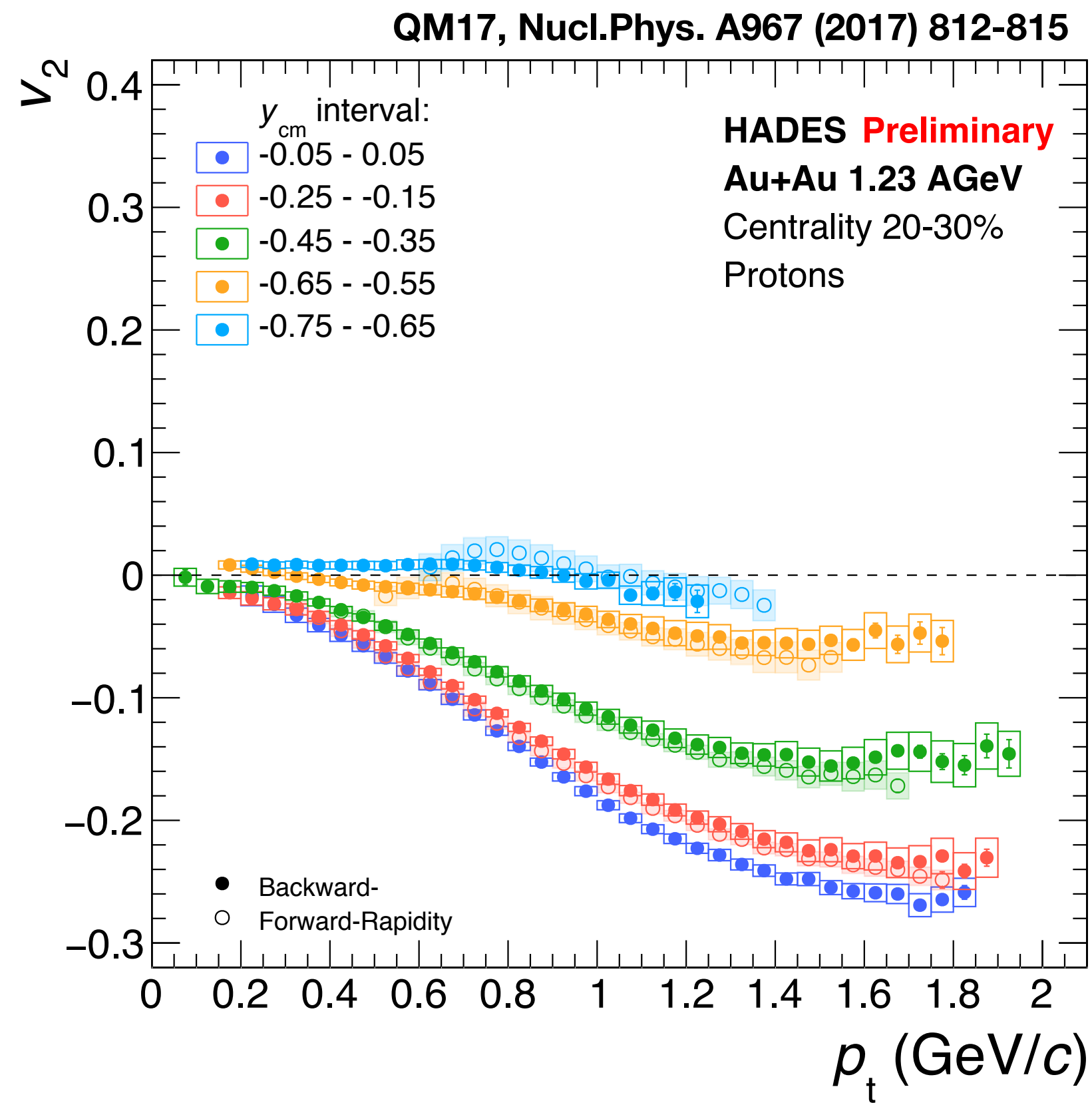
$p_t$ -Dependence





# Elliptic Flow $v_2$ : Proton and Light Nuclei

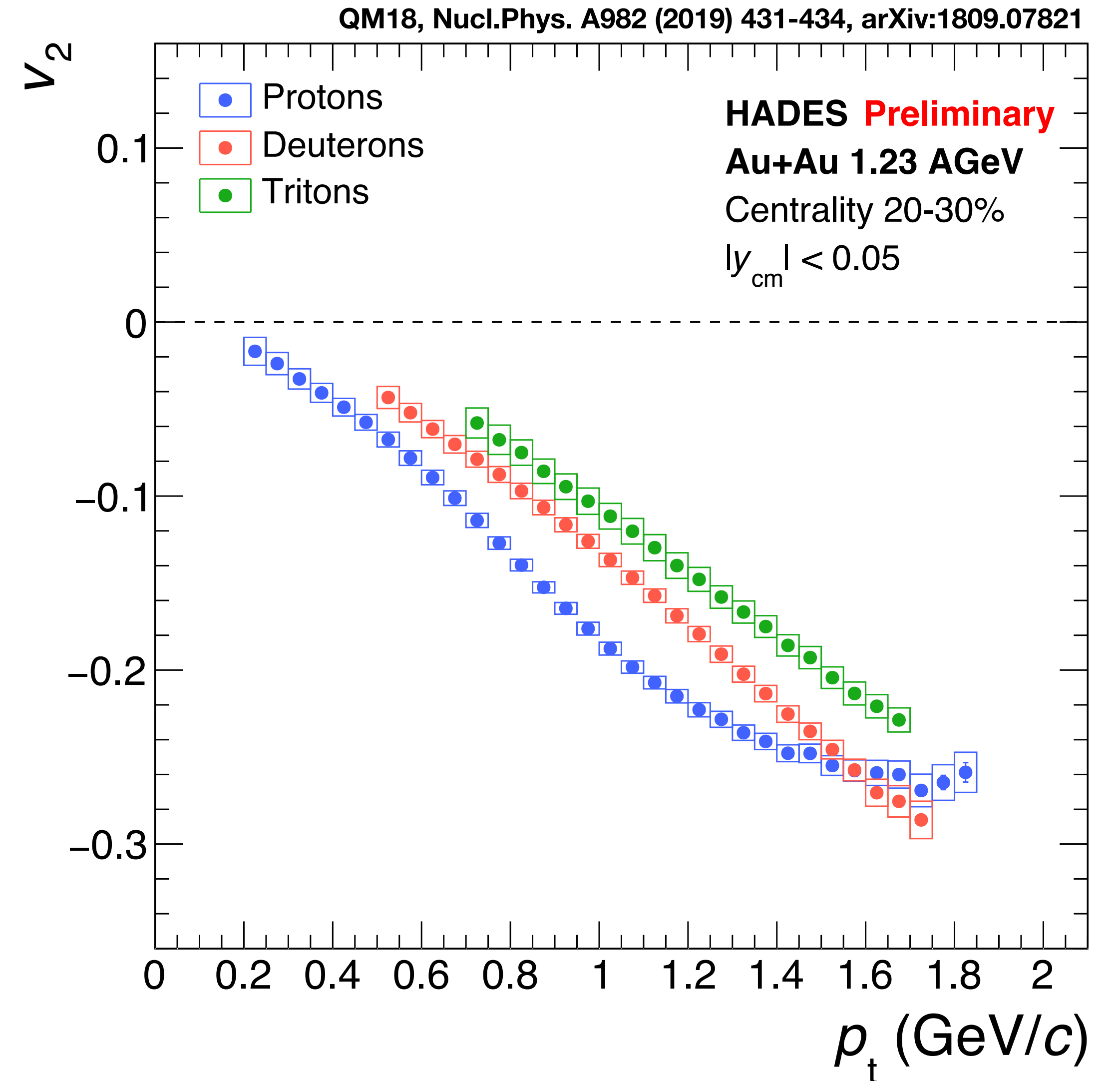
$p_t$ -Dependence



# Elliptic Flow $v_2$ : Light Nuclei

## Nucleon Coalescence

- Comparison of p, d, t  $v_2$  at mid-rapidity

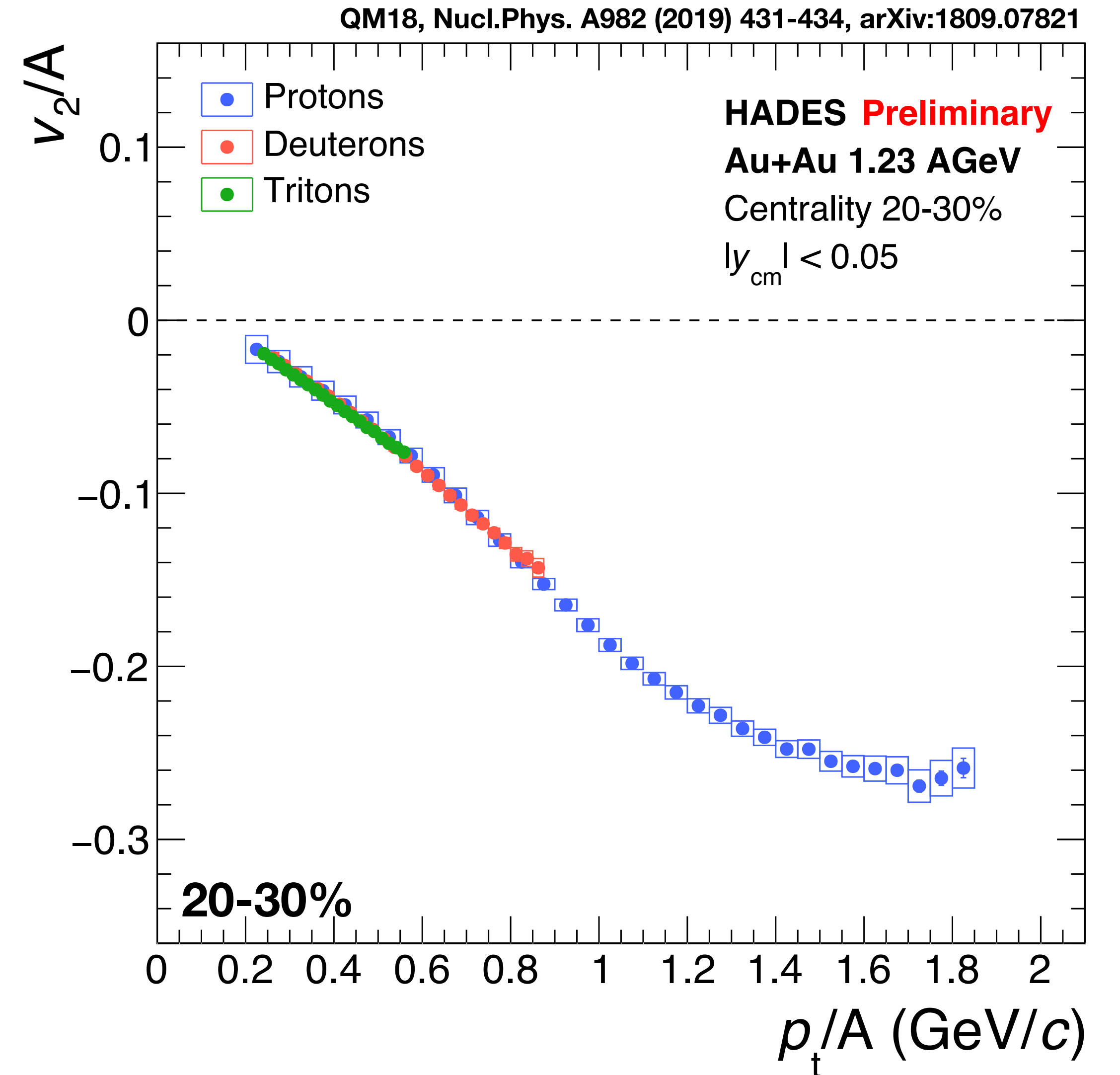
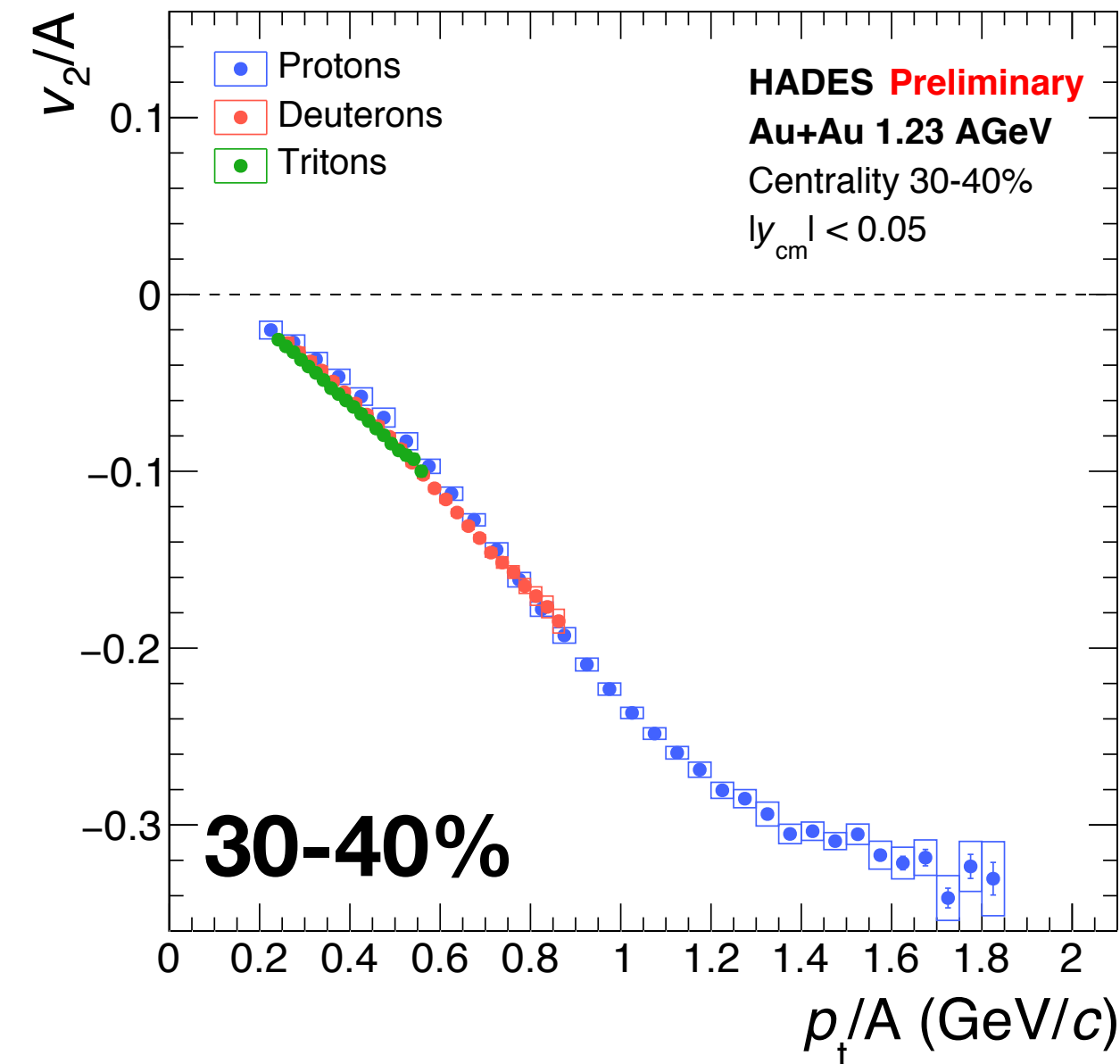
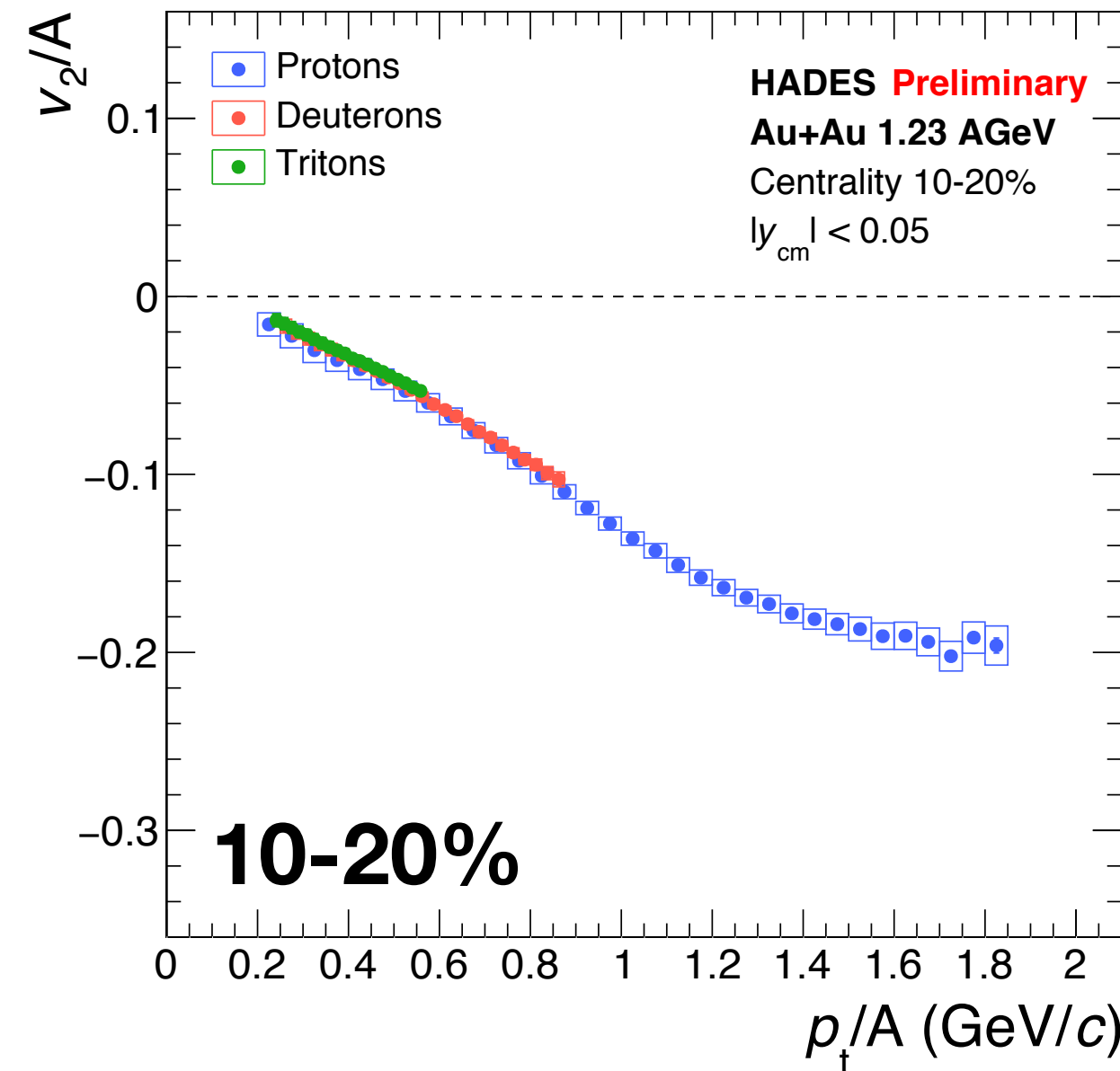




# Elliptic Flow $v_2$ : Light Nuclei

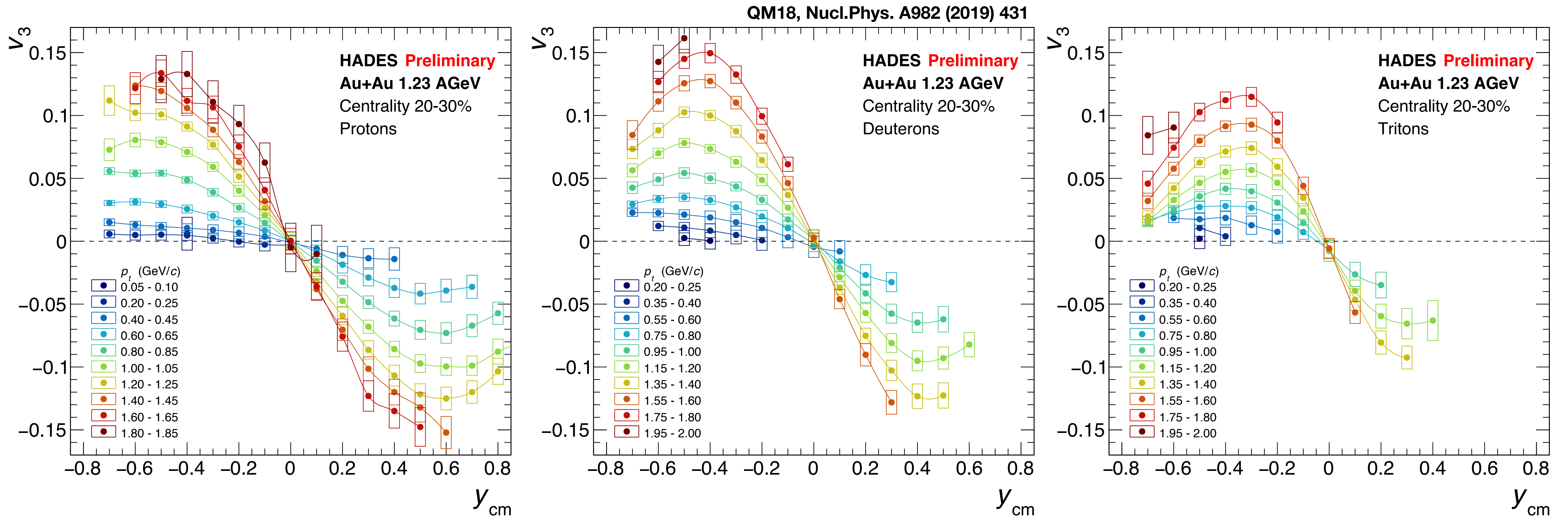
## Nucleon Coalescence

- Comparison of p, d, t  $v_2$  at mid-rapidity
- Scaling of  $v_2$  and  $p_t$  with nuclear mass number A
- As expected for nucleon coalescence



# Triangular Flow $v_3\{\Psi_{RP}\}$

Protons and Light Nuclei



**Note:  $v_3\{\Psi_{RP}\}$  w.r.t reaction plane**

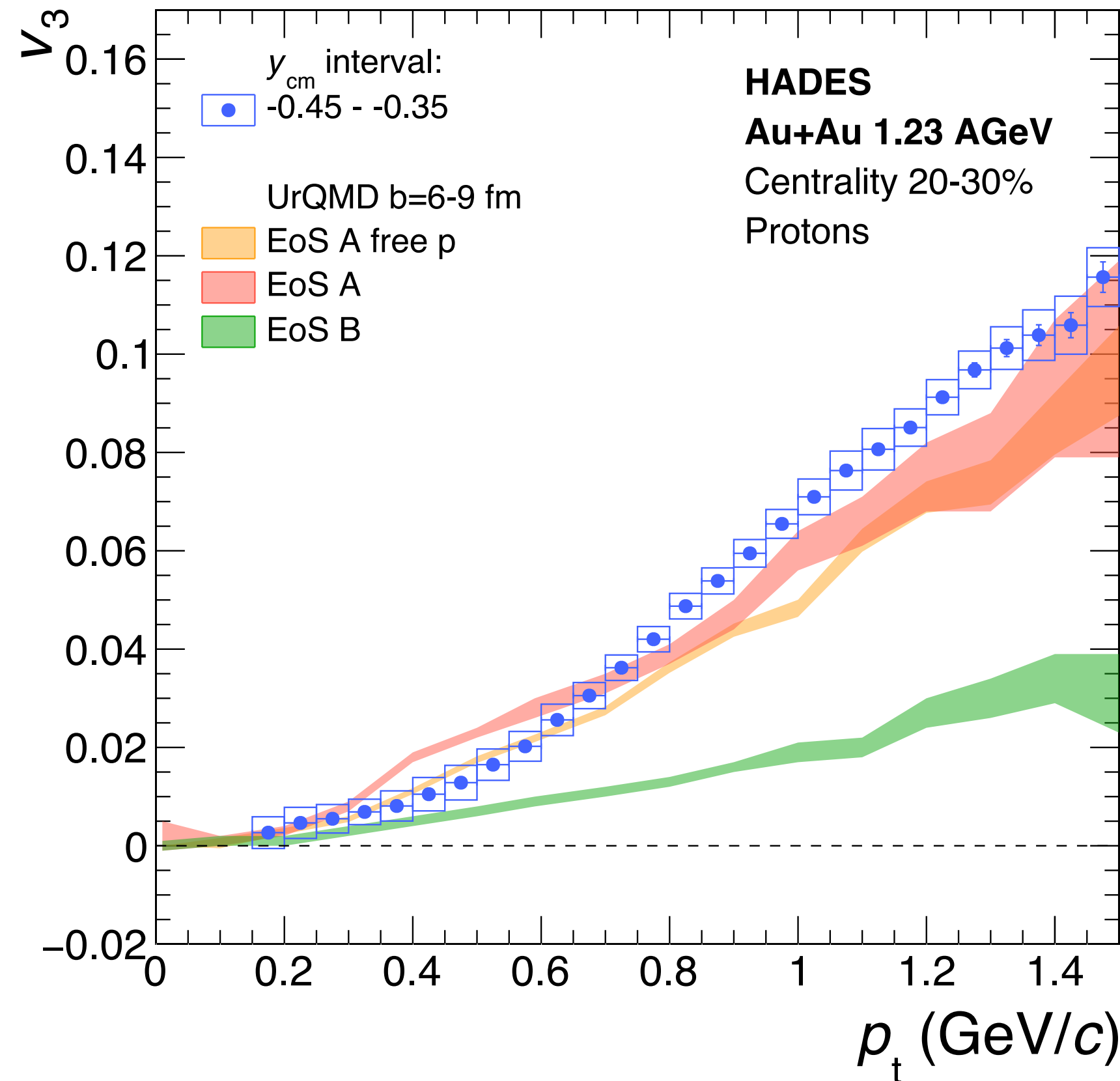
$$v_3\{\Psi_{RP}\} = \langle\langle \cos 3(\varphi - \Psi_{RP}) \rangle\rangle$$



# Triangular Flow $v_3\{\Psi_{RP}\}$

## Comparison of Protons and Deuterons to UrQMD

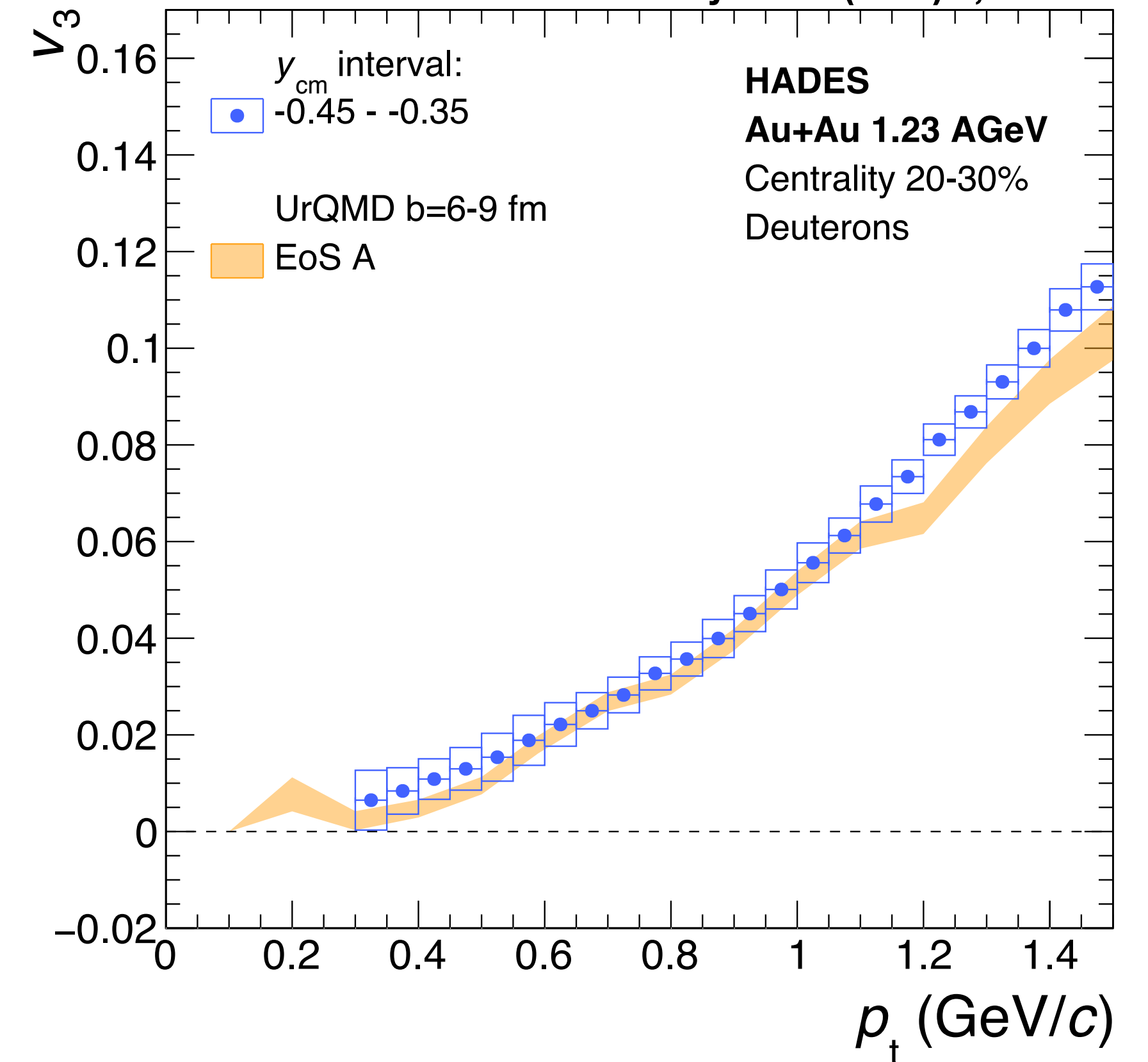
P. Hillmann, J. Steinheimer, M. Bleicher,  
J.Phys. G45 (2018) no.8, 085101



**UrQMD predicts high sensitivity of  $v_3$  to EoS**

Parameters	hard EoS	soft EoS
$\alpha$ [MeV]	-124	-356
$\beta$ [MeV]	71	303
$\gamma$	2.00	1.17

P. Hillmann et al.  
J.Phys. G47 (2020) 5, 055101



**UrQMD (hard EoS) with a coalescence in space-coordinates and momentum-space**  
 $\Delta r = 3.575 \text{ fm}^{-3}$  and  $\Delta p_{max} = 0.285 \text{ GeV}$

# Odd Flow Harmonics $v_1$ $v_3$ $v_5$

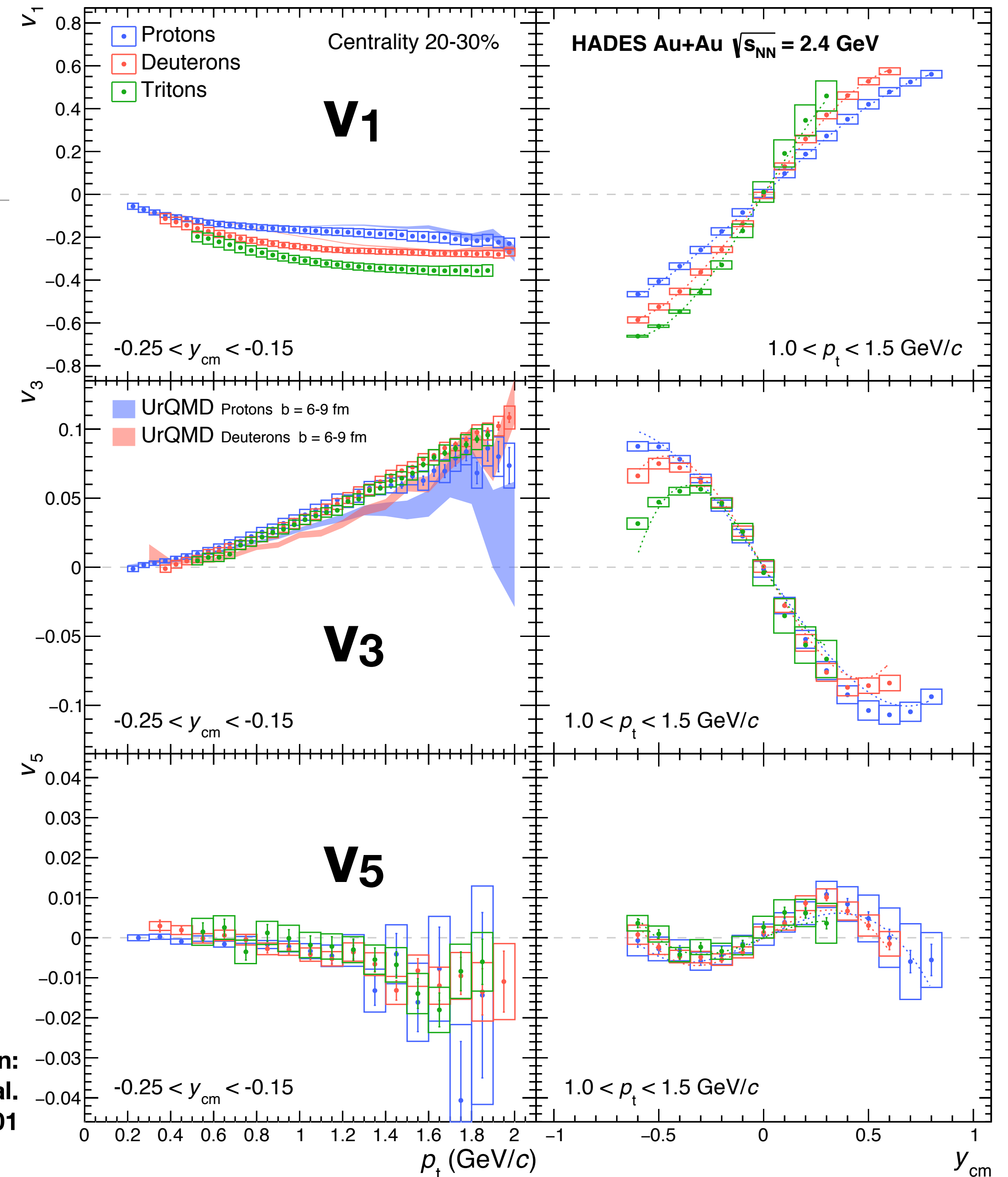
Protons and light nuclei

- $v_1$  develops a strong mass dependence when moving away from mid-rapidity, not in the case of  $v_3$  and  $v_5$
- UrQMD model with hard EOS provides a general good description of  $v_1$  and  $v_3$ , but discrepancies can be observed

**Rapidity dependence of odd harmonic parameterised with:**

$$v_{1,3,5}(y_{cm}) = a y_{cm} + b y_{cm}^3$$

UrQMD calculation:  
P. Hillmann et al.  
J.Phys. G47 (2020) 5, 055101





# Even Flow Harmonics $v_2$ $v_4$ $v_6$

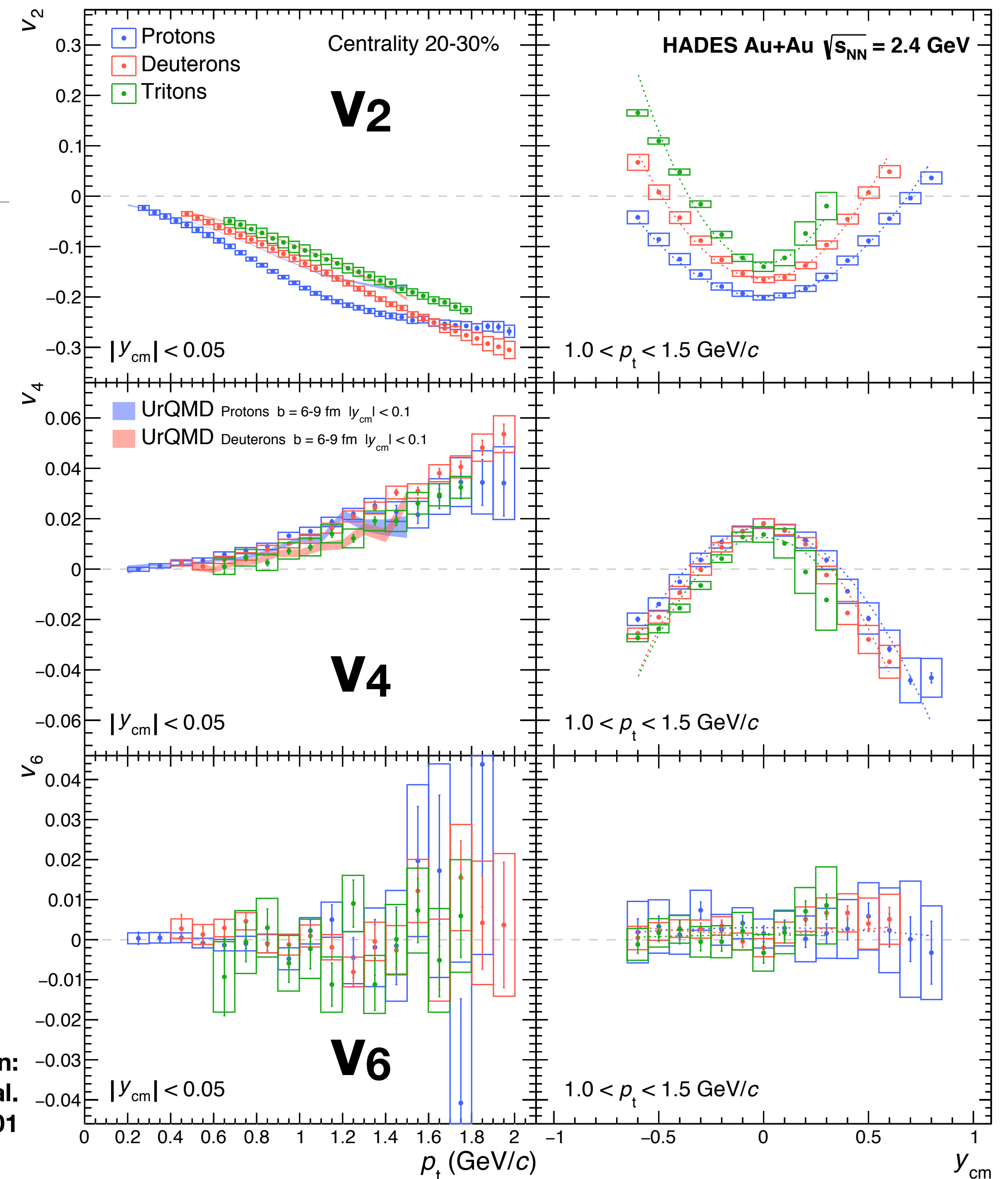
Protons and light nuclei

- $v_2$  around mid-rapidity a clear mass ordering can again be observed, not so strong for  $v_4$
- good description of  $v_4$  with UrQMD with hard EOS, but deviation of  $v_2$  at high momenta
- Upper limit for  $v_6$  values

**Rapidity dependence of even harmonic parameterised with:**

$$v_{2,4,6}(y_{cm}) = c + d y_{cm}^2$$

UrQMD calculation:  
P. Hillmann et al.  
J.Phys. G47 (2020) 5, 055101



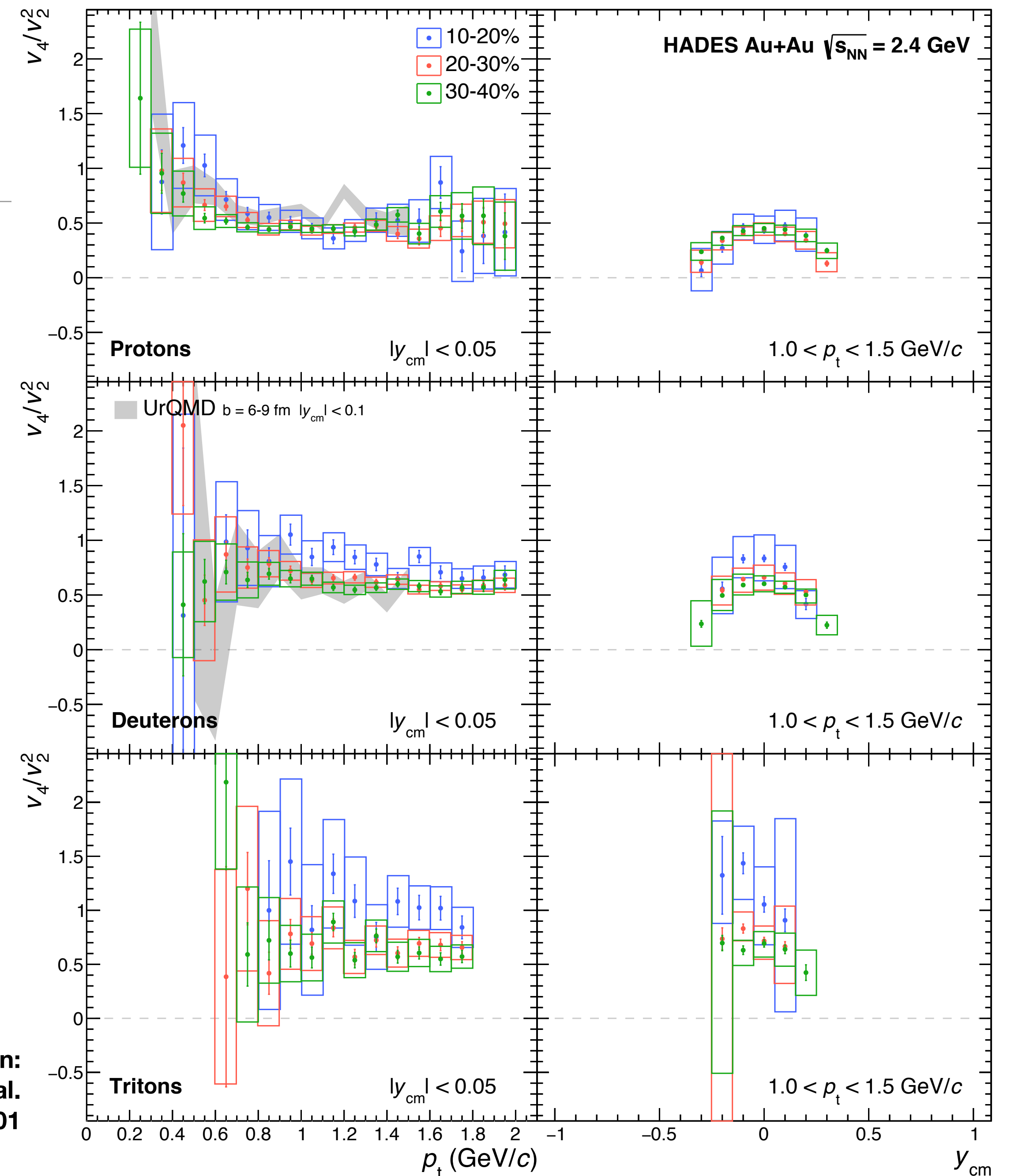
# “Ideal fluid scaling”

Protons and light nuclei

- Ideal fluid dynamics predicts contribution to  $v_4$  from  $v_2$  at large  $p_t$  by  $v_4 = 0.5(v_2)^2$
- Realistic hydro calculation at RHIC  
 $v_4/(v_2)^2 \sim 0.63$
- Good agreement with UrQMD simulations with “hard” mean-field potential

**Systematic Error are evaluated for each individual Variation Calculation (errors treated as correlated)**

UrQMD calculation:  
 P. Hillmann et al.  
 J.Phys. G47 (2020) 5, 055101





# Emission Pattern

## Protons

- Enables to reconstruct a full 3D-picture of the emission pattern in momentum space

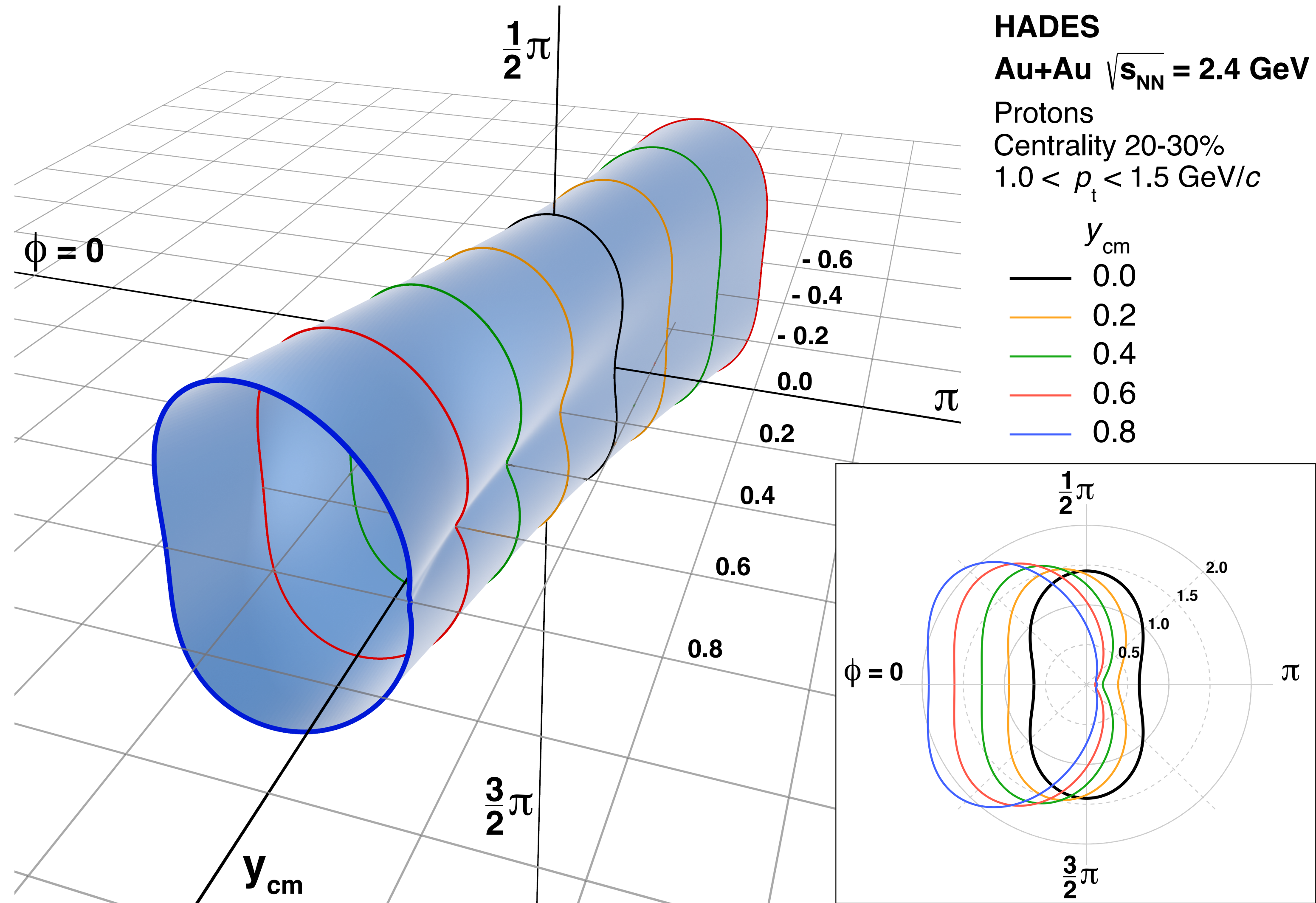
First Proposed in  
**S. Voloshin and Y. Zhang**  
**Z.Phys. C70 (1996) 665-672**

$$1 + 2 \sum_{n=1}^{\infty} v_n(y_{cm}) \cos n(\phi - \psi_{RP})$$

with rapidity depend  
 parameterisation  $n=1-6$

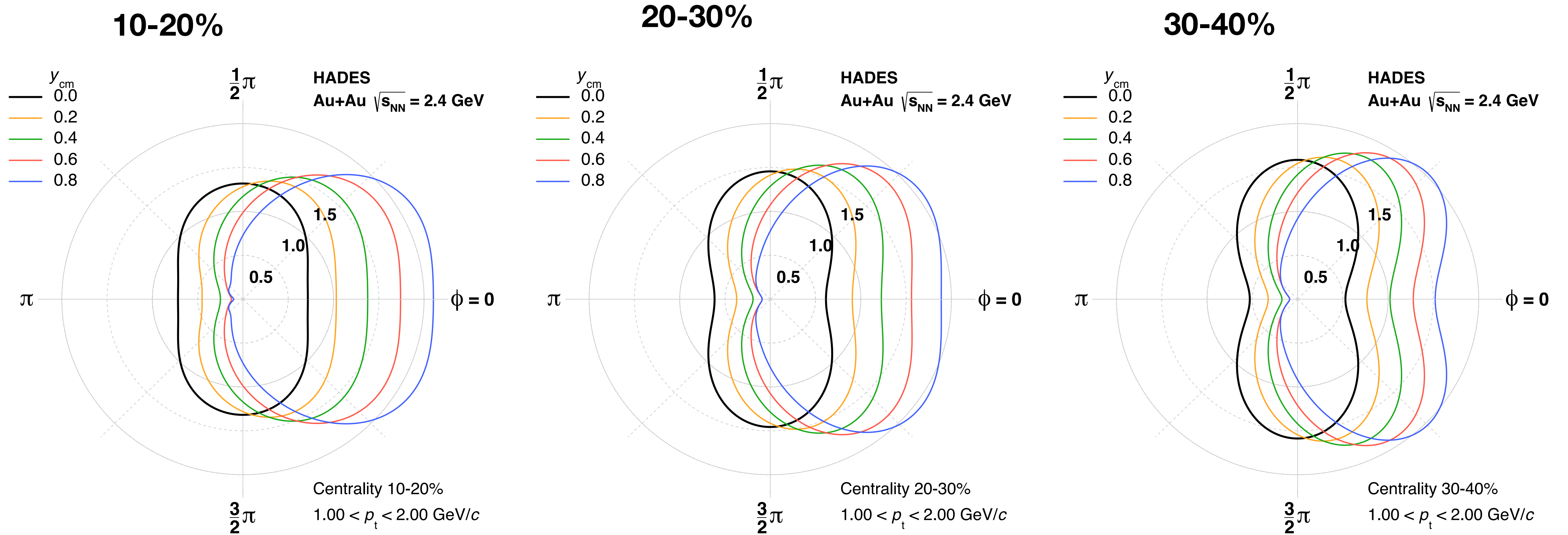
$$v_{1,3,5}(y_{cm}) = a y_{cm} + b y_{cm}^3$$

$$v_{2,4,6}(y_{cm}) = c + d y_{cm}^2$$



# Emission Pattern

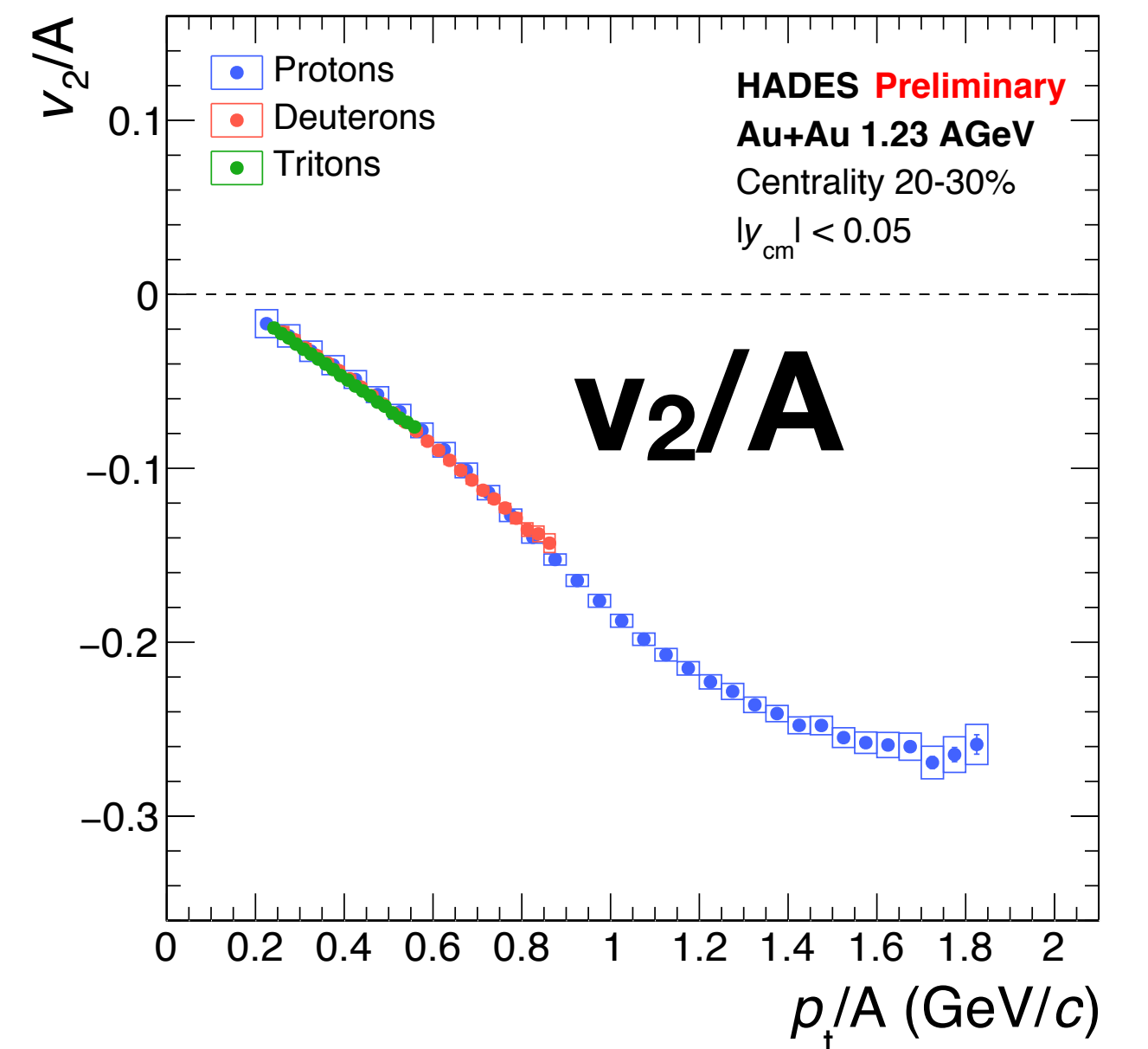
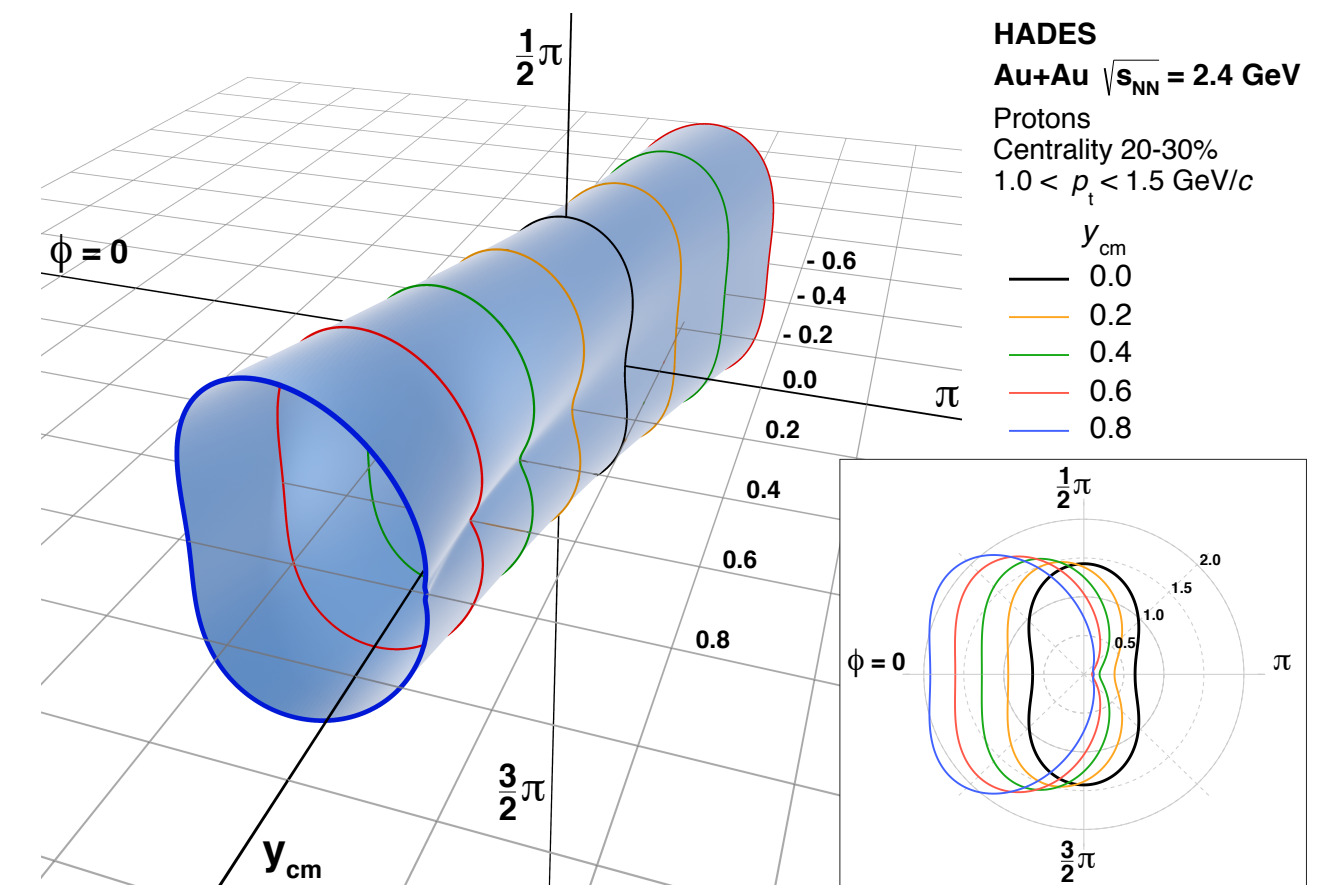
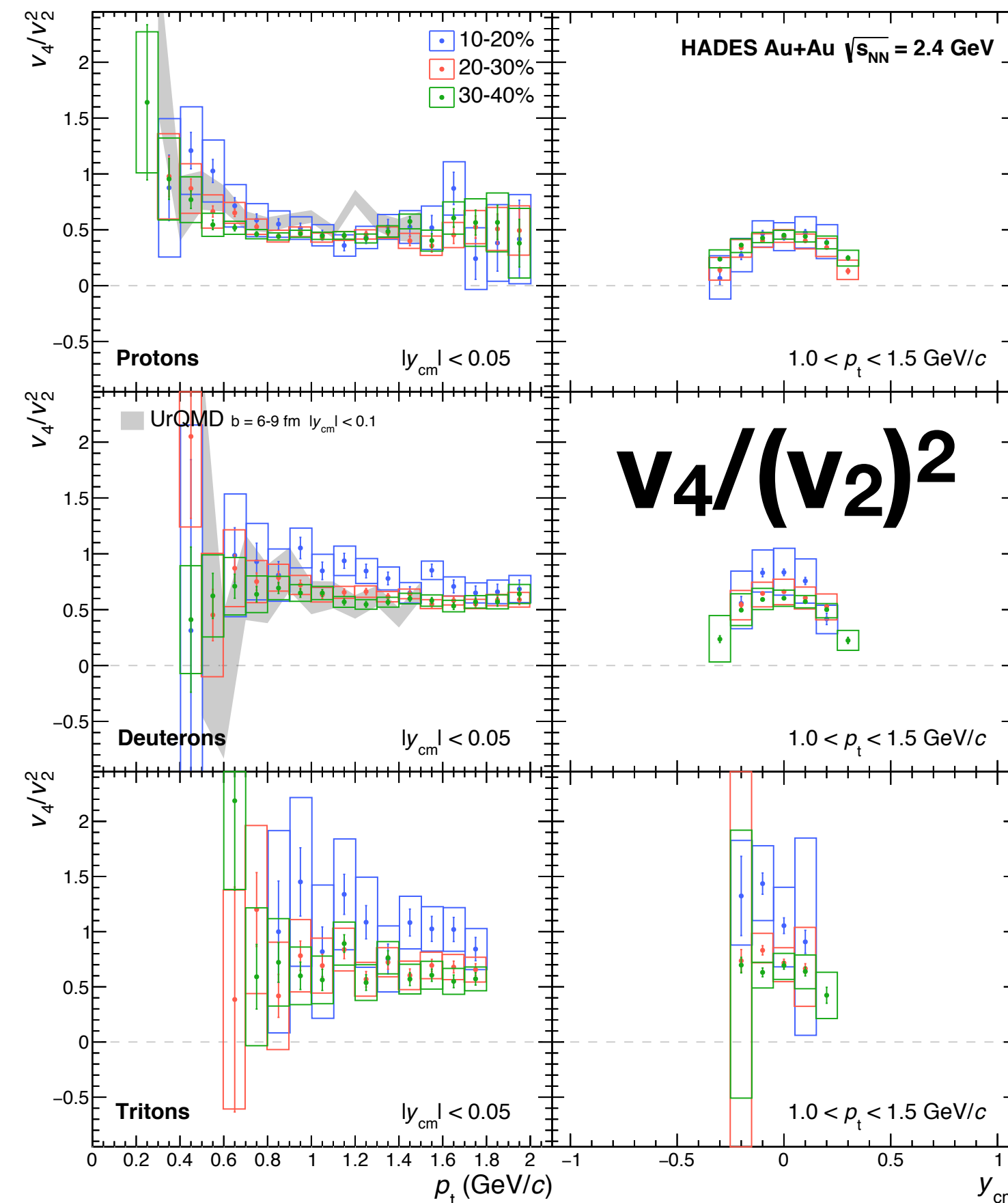
## Protons





# Conclusions

- Precision data on higher order flow is a major step forward in constraining the EOS and transport properties of dense matter
- Fully multi-differential measurement in Centrality and Phase Space (Pt and Rapidity)
- First measurement at SIS energies of
  - ▶ Triangular  $v_3\{\Psi_{RP}\}$ , quadrangular  $v_4\{\Psi_{RP}\}$  and higher flow harmonics of protons, deuterons and tritons
- Scaling properties observed
  - ▶ Elliptic flow at mid-rapidity scales with A
  - ▶ Ratio  $v_4/(v_2)^2$  shows constant scaling







Dresden 2020

HADES Collaboration

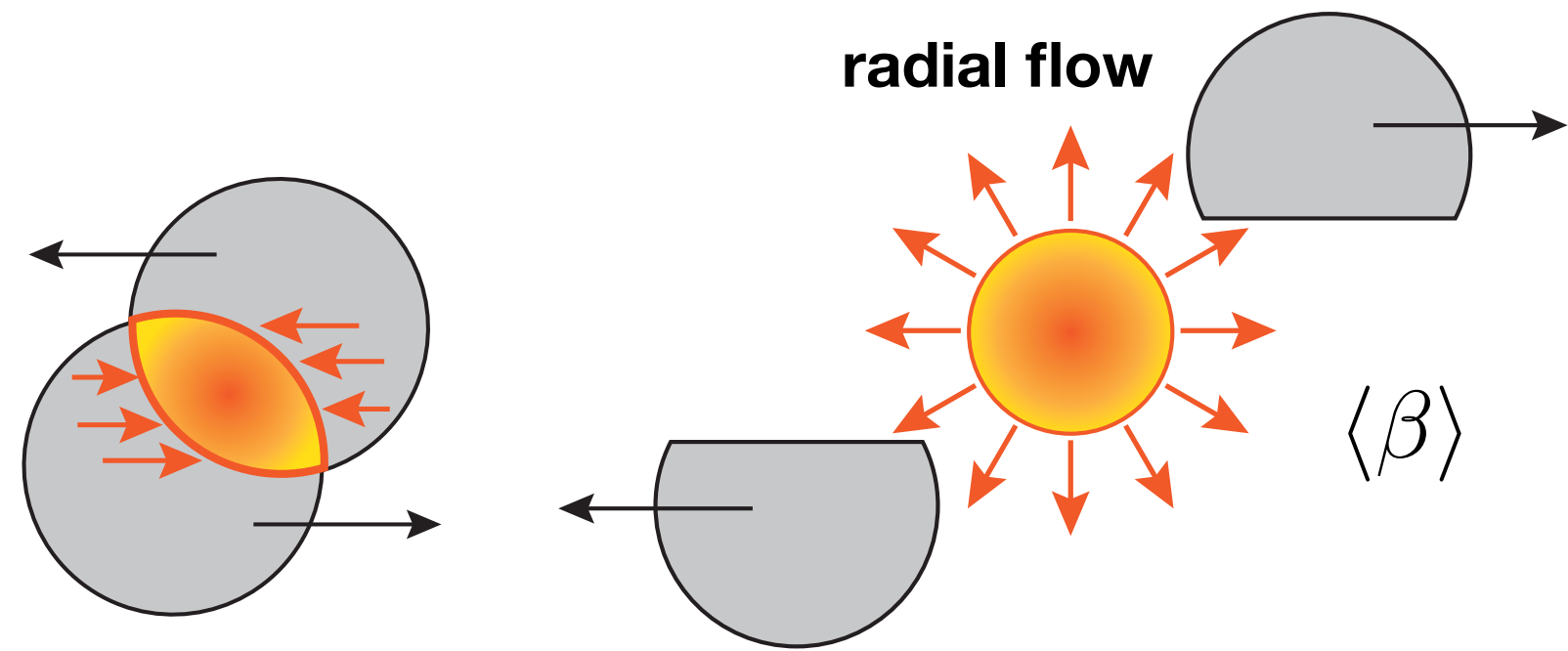
Thank you for your attention!



# Motivation

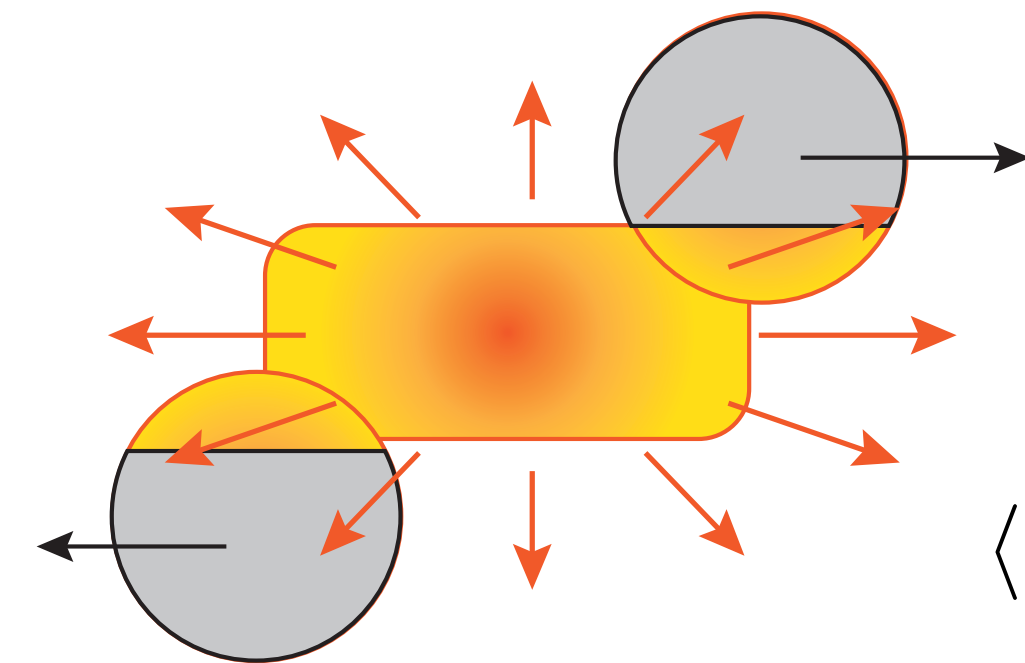
## Flow and Event Shapes

top view



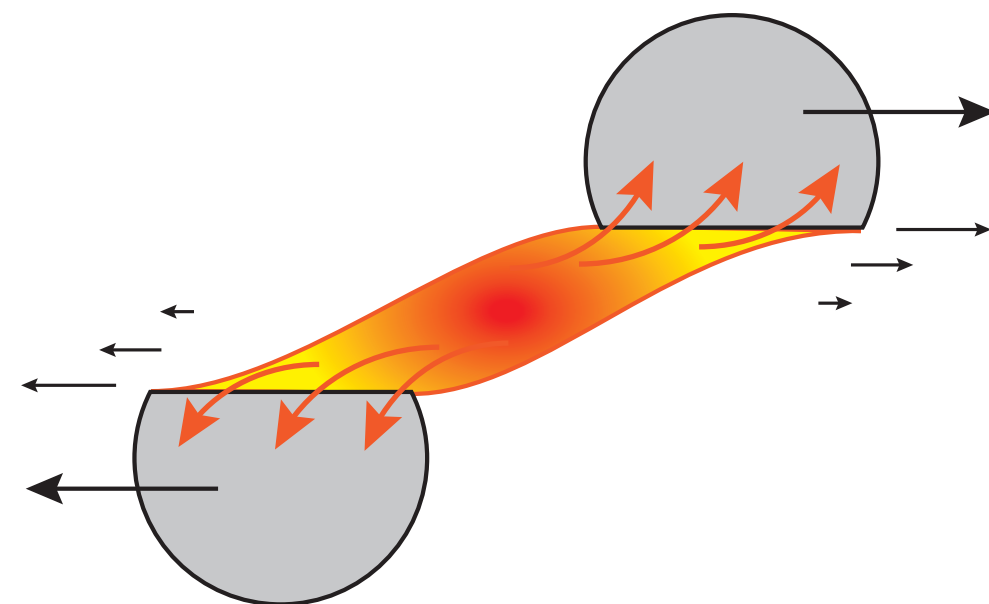
**Landau scenario**  
total stopping

$$\langle \beta \rangle$$

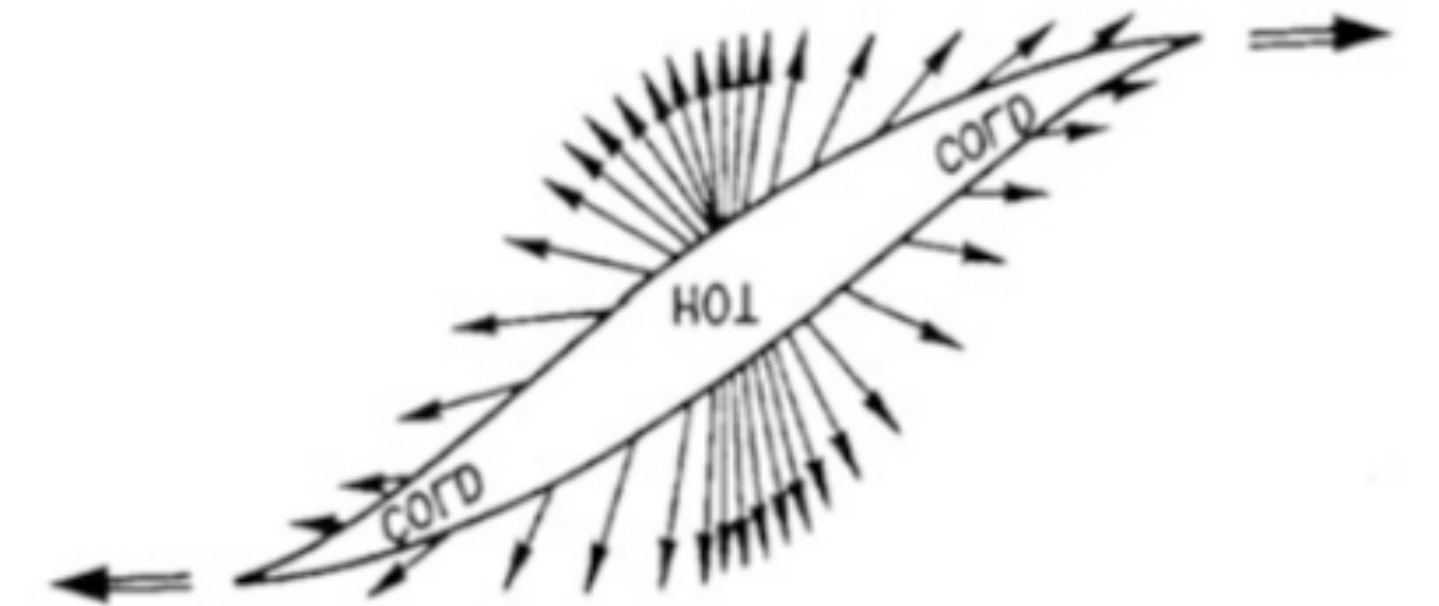


**Bjorken scenario**  
partial stopping  
initial longitudinal flow

$$\langle \beta_t \rangle \quad \langle \beta_l \rangle$$



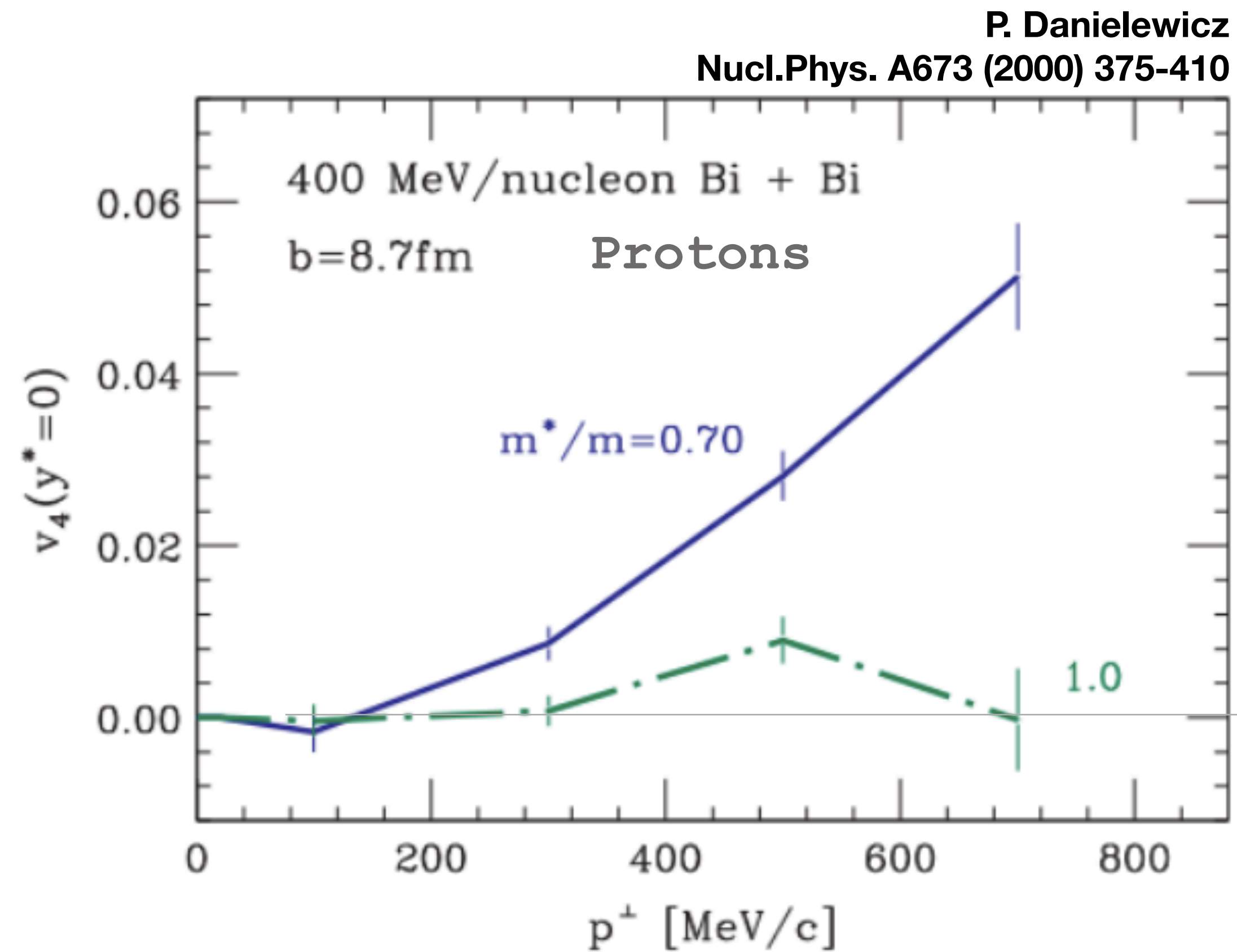
**Hagedorn-Myers scenario**  
(similar to "firestreak" model)  
stopping dependent on nuclear density  
partial stopped matter moves with  
different rapidities



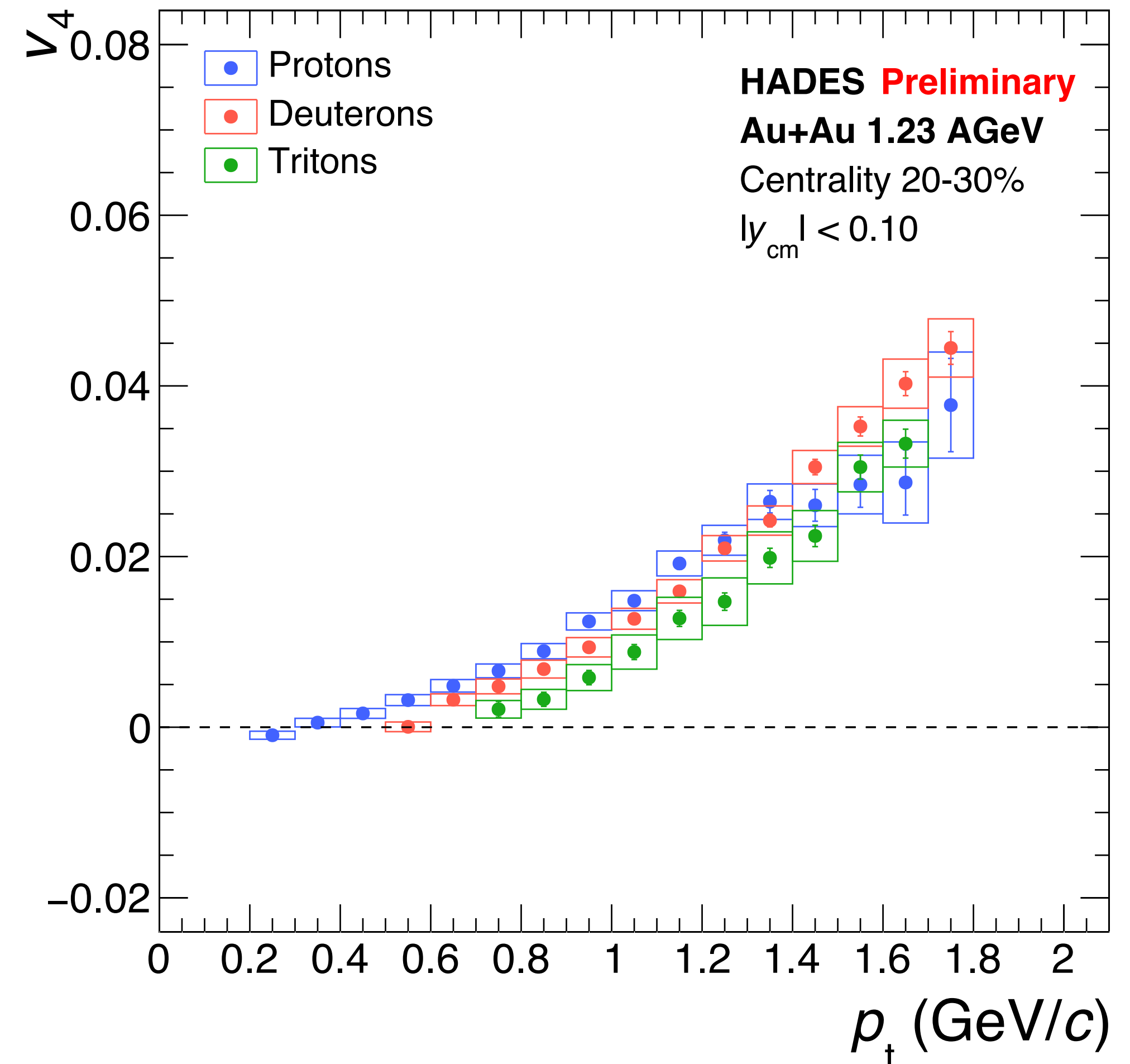
**How to Deal with Relativistic Heavy Ion Collisions**  
**R. Hagedorn (1981)**

# Quadrangular Flow $v_4\{\Psi_{RP}\}$

Protons and Light Nuclei



**First prediction of  $v_4$  with sensitive to EoS**



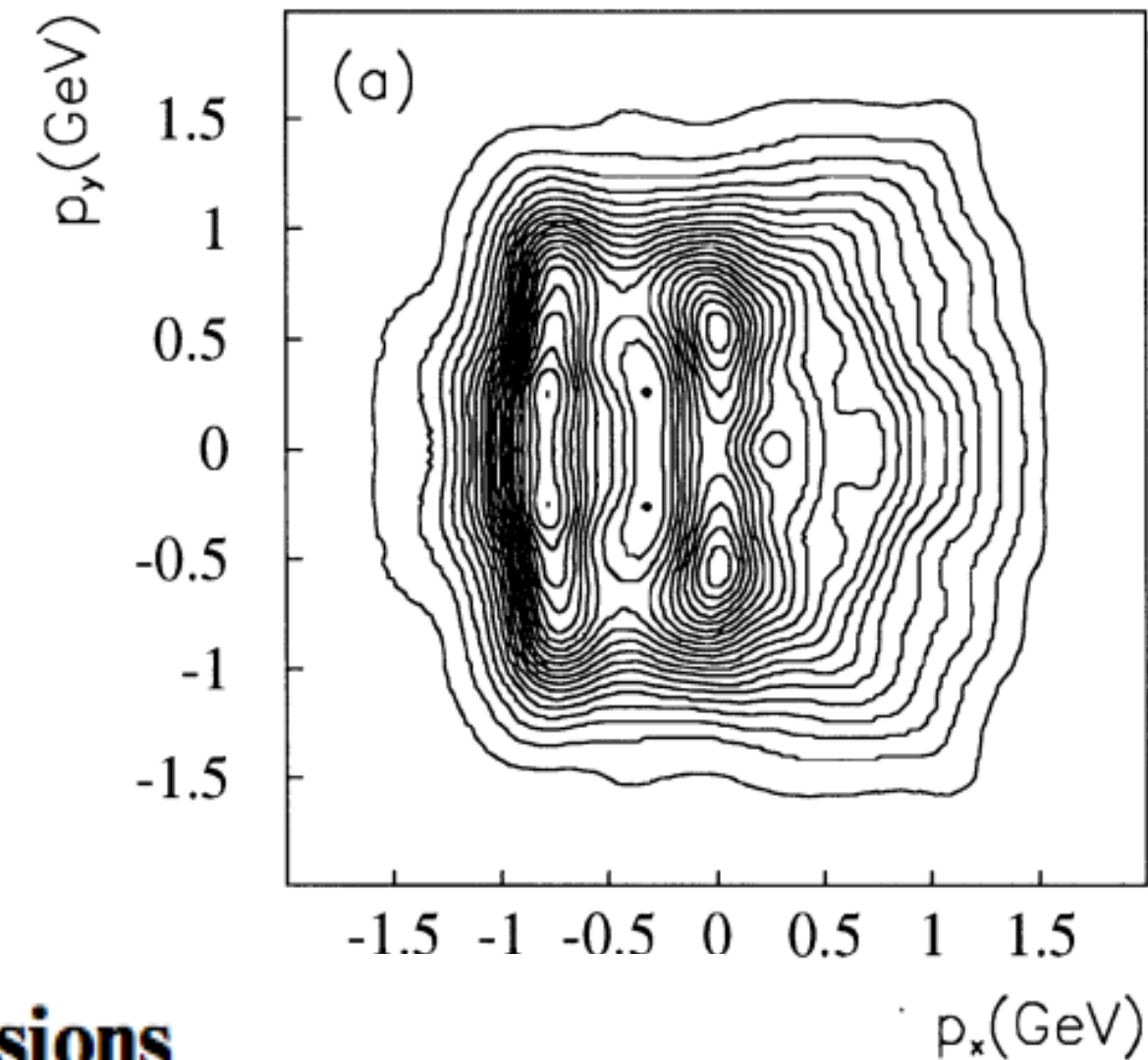
$$v_4\{\Psi_{RP}\} = \langle\langle \cos 4(\varphi - \Psi_{RP}) \rangle\rangle$$

**Note:  $v_4\{\Psi_{RP}\}$  w.r.t reaction plane**



# Quadrangular Flow $v_4\{\Psi_{RP}\}$

Protons and Light Nuclei

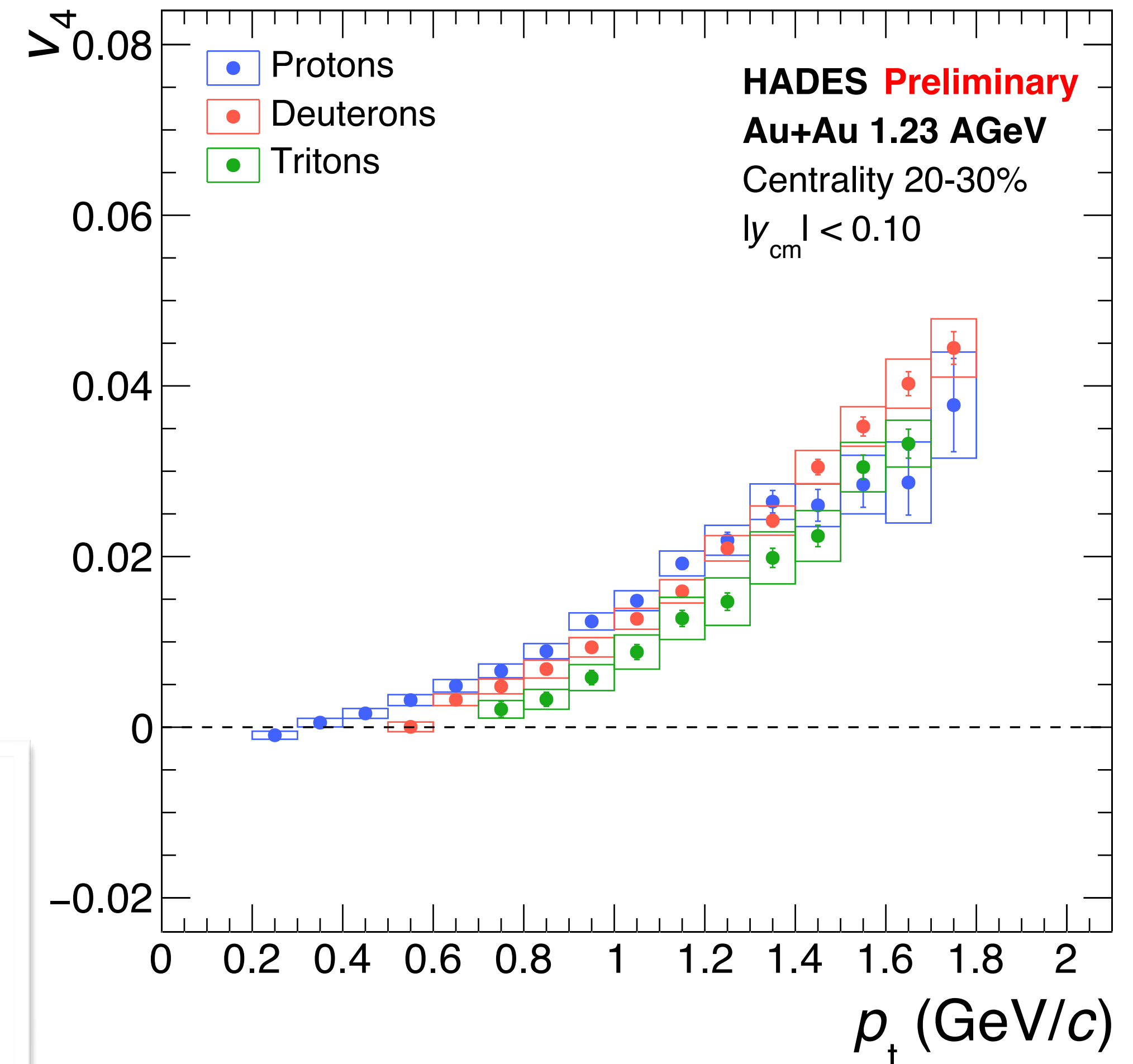


Z. Phys. C 70, 665–671 (1996)

**Flow study in relativistic nuclear collisions  
by Fourier expansion of azimuthal particle distributions**

S. Voloshin<sup>1,\*</sup>, Y. Zhang<sup>2</sup>

The rectangle-type deformation amplitude  $v_4$  could be non-zero, for example, for rapidity windows close to the center of mass, where both squeeze-out emitting preferentially more particles in the direction perpendicular to the reaction plane, and “side-splash” effects can be important.



$$v_4\{\Psi_{RP}\} = \langle\langle \cos 4(\varphi - \Psi_{RP}) \rangle\rangle$$

**Note:  $v_4\{\Psi_{RP}\}$  w.r.t reaction plane**

# HADES Performance

- High interaction rates and statistics

- ▶ Total number of events recorded  $10^9$
- ▶  $2.1 \times 10^9$  most central events analysed

- Centrality

- ▶ 0-40% most central
- ▶ Deduced from a Glauber MC model

