

Basic requirements (to be spelled out more precisely)

At any moment during the run:

- run at nominal centre-of-mass energy that is stable well within Higgs width (± 4 MeV OK?)
- know the nominal center of mass energy to much better precision (± 1 MeV OK?)
- know the centre-of-mass energy spread with similar precision (± 1 MeV OK?)

reference [arXiv:1909.12245](https://arxiv.org/abs/1909.12245)

-- **know the centre-of-mass energy spread with similar precision (± 1 MeV OK?)**

→ this requires use of the transverse polarization and resonant depolarization.

One condition is that the beam energies should be located around the half integer spin tune $\nu_s = E_b / 0.4406486$

if $m_H = 125.09$ GeV, then: $\nu_s = (m_H/2) / 0.4406486 = 141.938$ which is too close to integer.

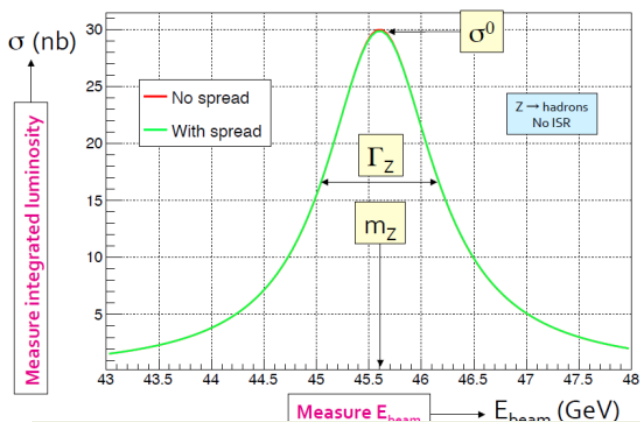
-- A possibility is to shift the energies of the two beams in opposite way by $\Delta\nu_s = +$ and $- 0.5$,
to 141.438 and 142.438 (Oide)

(There might be an elegant way to combine this with OSVD)

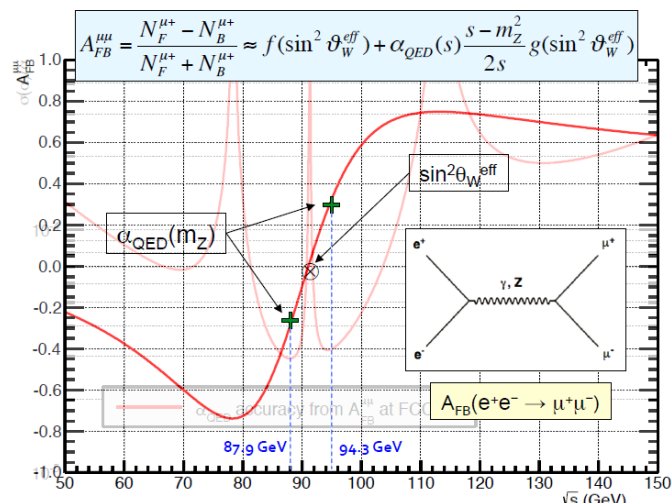
→ then we should use the same method as for the Z run which should be somewhat easier since the **polarization time is ~ 5 times shorter $(125/91)^5$**

Precision at time of measurement will be similar (± 100 keV) as for the Z run and should be sufficient

However it is important that it is tracked very well....



Z line shape $\rightarrow m_Z$ and Γ_Z



at the same time $A_{FB}^{\mu\mu}(\sqrt{s})$
 $\rightarrow \sin^2\theta_W^{eff}, \alpha_{QED}(m_Z)$

11/25/2020

Use half integer spin tune energies for Z line shape, lucky:

$\nu = 99.5, 103.5, 106.5/107.5$

and

W W threshold $\nu = 178.5, 184.5$

for the Higgs, bad luck!

$\nu = m_H/2/.4406486(1) = 141.94$

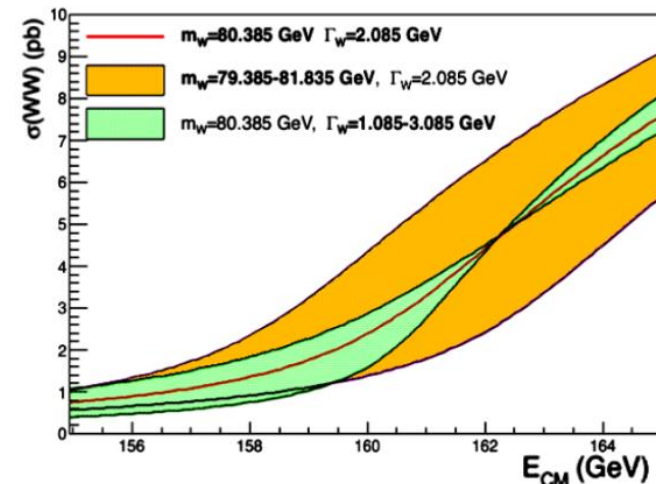
--too close to integer for polarization--

$\rightarrow 141.44$ for e^+ and 142.44 for e^-

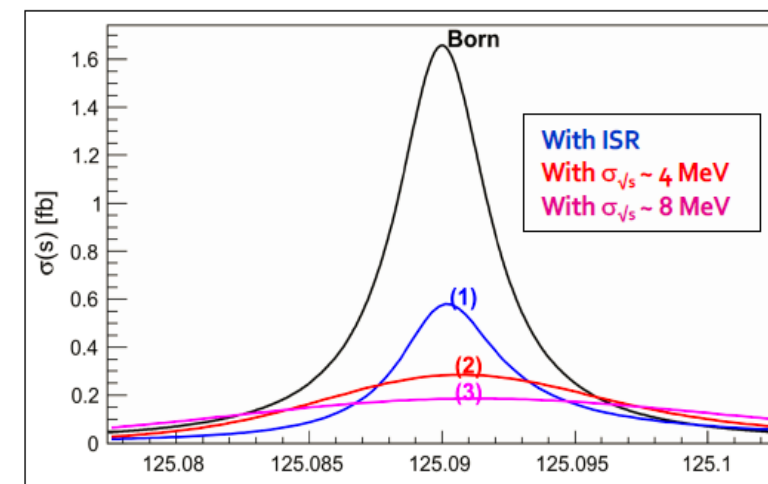
at Z: 200 'pilot' bunches will be stored at the beginning of fills with polarization wigglers ON, for about 1 hour to develop about 5-10% transverse polarization.

After a first energy calibration, the full luminosity run will comprise regular calibrations (1/10 min) on pilot bunches.

Alain Blondel EPOL at FCC-ee



WW threshold $\rightarrow m_W$ and Γ_W



Higgs s-channel production

need to know $E_{cm} \sigma_{ECM} \rightarrow y_e = m_e?$

At any moment during the run:

-- run at nominal centre-of-mass energy that is stable well within Higgs width (± 4 MeV OK?)

Large machines like FCC-ee will be subject to earth tides with circumference changes by $\Delta C \simeq \pm 2$ mm for C of 100 km [22, 66, 67]. For a momentum compaction factor of $\chi \simeq 10^{-5}$ the corresponding energy changes reaches $\pm 2 \cdot 10^{-3}$ or ± 90 MeV around the Z

This requirement is more stringent than that for the Z line shape scan where the requirement is well within the center-of-mass energy spread (so that it does not worsen it) of O(80 MeV)

The full swing at the Higgs will be ± 125 MeV... for each beam, i.e. ± 250 MeV for E_{CM}

This corresponds to a maximum variation of 125 MeV per hour, or ~ 2 MeV per minute.

This will require a good model of the FCC-ee machine and its energy variations

-- benchmarked at the Z pole with great precision

and a correction mechanism using the RF frequency, based on e.g. beam position monitors, that is valid at that precision.

Must also use the 'spectrometer' function of the polarimeter in an operational way.

The beam energy measurements by RDP might need to be performed more often than every 10 minutes.

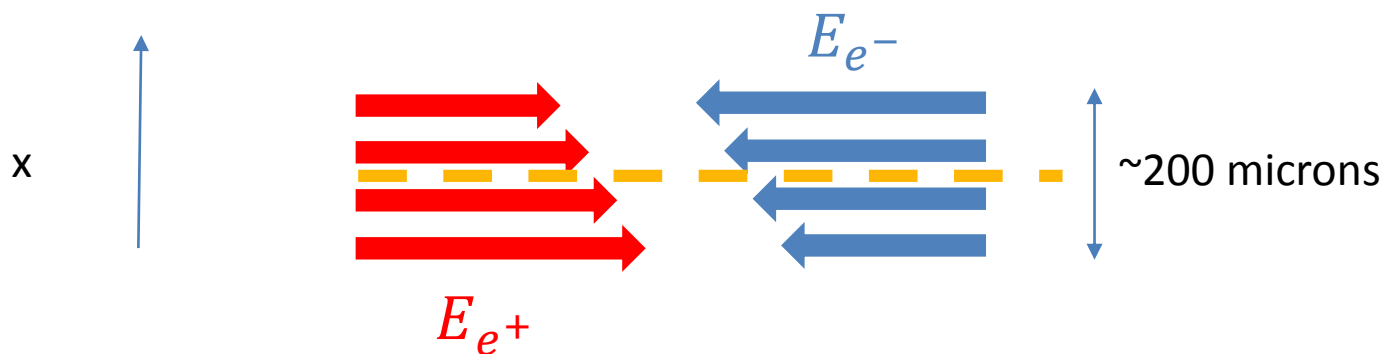
→ it is essential that the ee → H measurement is performed after the Z line shape run

As discussed in arXiv:1909.12245 the centre-of-mass energy spread σ_{ECM} cannot be measured from the bunch length when using crab-waist crossing.

A method was therefore devised to measure σ_{ECM} from the resulting spread in the measured boost of $\mu+\mu^-$ pairs.

However that analysis was made without taking into account the possibility of horizontal dispersion. In this scheme for monochromatization the average boost varies with horizontal position and integrating it leads to a measurement of the centre-of-mass energy spread in absence of monochromatization. Not good.

We are saved by the fact that the beam is artificially spread around for the monochromatization ($\sigma_x \sim \pm 100 \mu\text{m}$) and that the detector should be able to measure the production point of each event with a precision of $\pm 3 \mu\text{m}$.



Monochromatization $D_x(e+) = -D_x(e-)$

$\langle ECM \rangle(x) \sim \text{constant}$

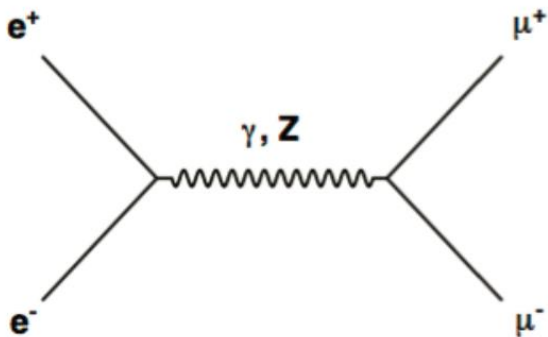
$\sigma_{ECM}(x) \sim \text{constant} \sim \langle \sigma_{ECM}(x) \rangle$

Boost measurement:

$\langle (E(e+) - E(e-)) \rangle \propto x (D_x(e+) - D_x(e-))$

$\text{rms}((E(e+) - E(e-))(x)) \sim \text{constant} \ll \langle \text{rms}((E(e+) - E(e-))) \rangle$

this is very elegant: we can measure from the {boost of the muon pairs vs. x} the true energy spread *and* verify the variation of boost across the beam crossing point -- this is the very principle of monochromatization. NB we can and should also maybe verify the ECM is constant vx x. Detailed analysis is needed to ascertain the errors.



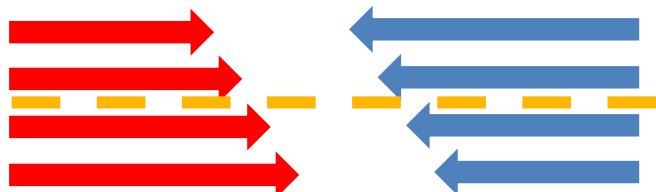
E,P conservation → allow E_{CM} and P_{CM} on event-per-event basis.

10^6 evts/5 min/expt @Z

$\sim 10^4$ evts/5 min/exp @H

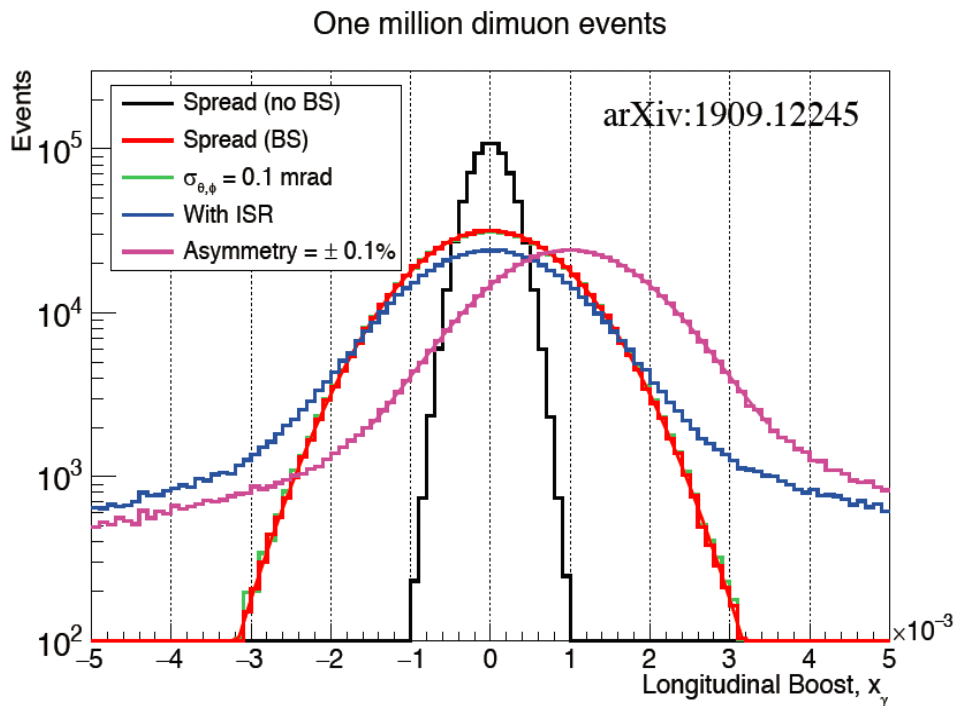
→ Determine E_{CM} , E_{CM} spread and collision angle, in addition to $A_{FB}^{\mu\mu}(\sqrt{s})$! (also: control of ISR spectrum)

E_{e^-}



11/25/2020

E_{e^+}

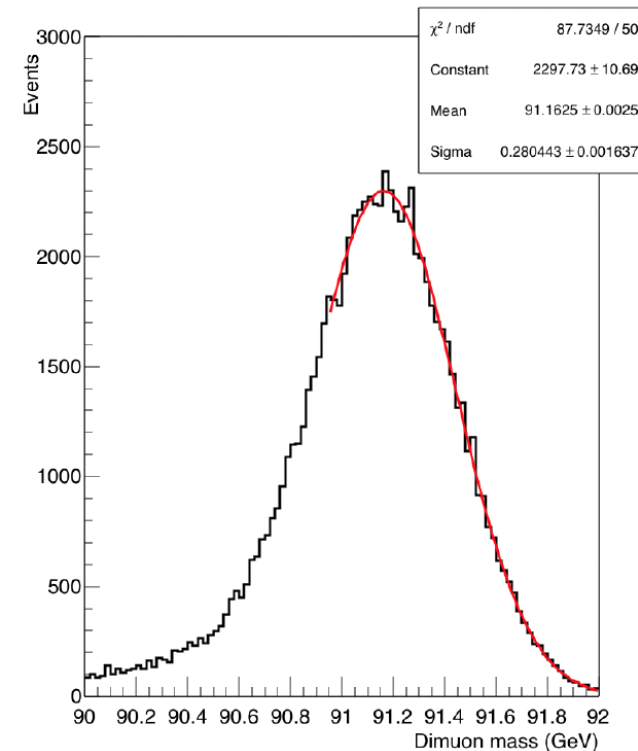


The measurement of CM boost distribution allows control of beam energy spread as well as the difference between e+ vs. e- energies.

Very useful also for control of Monochromatization!

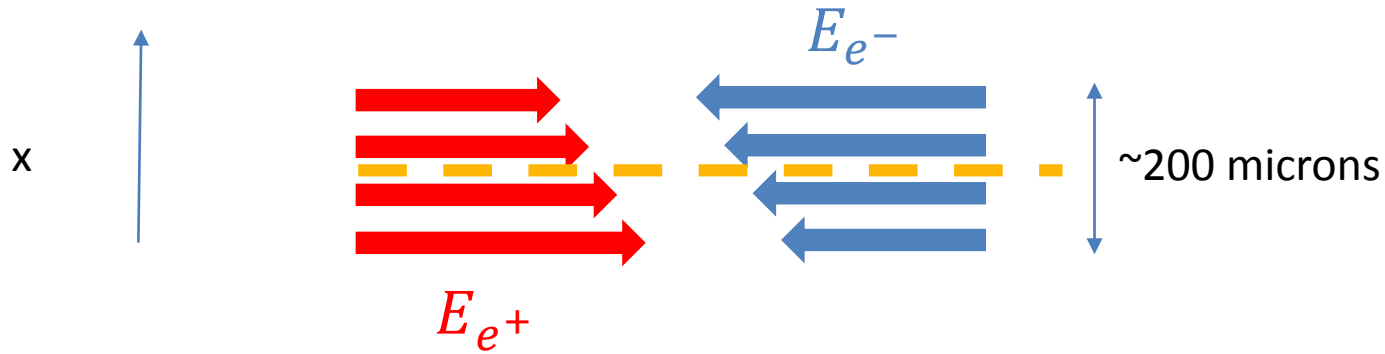
Alain Blondel EPOL at FCC-ee

$\sqrt{s} = 91.2 \text{ GeV}$



± 2.5 MeV E_{CM} meast in 30 seconds of data ~ 40 keV per day at each scan point... challenge for QED calculations!

For the s-channel Higgs production



Monochromatization

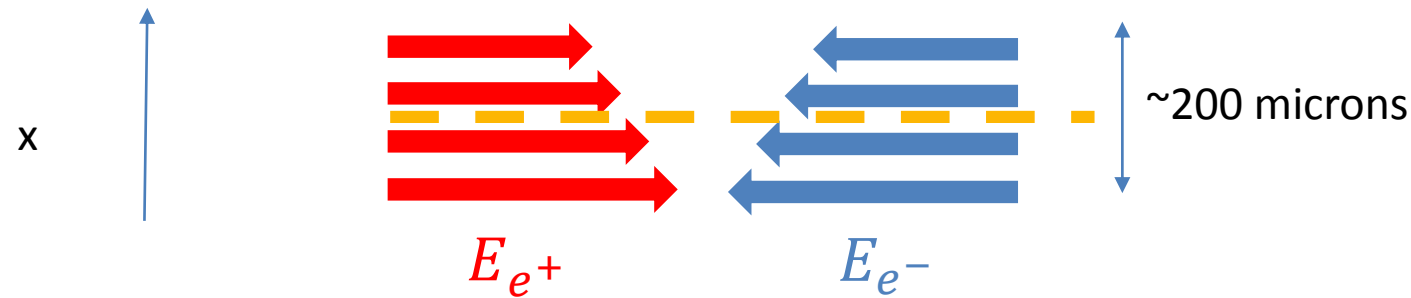
$$\langle \text{ECM} \rangle(x) \sim \text{constant}$$

$$\sigma_{\text{ECM}}(x) \sim \text{constant} \sim \langle \sigma_{\text{ECM}}(x) \rangle$$

Boost measurement:

$$\langle (E(e^+) - E(e^-)) \rangle \propto x (D_x(e^+) - D_x(e^-))$$

$$\text{rms}((E(e^+) - E(e^-))(x)) \sim \text{constant} < \langle \text{rms}((E(e^+) - E(e^-))) \rangle$$



Chromatization along x axis:

across the x axis:

$$\langle \text{ECM} \rangle(x) \sim x (D_x(e^+) + D_x(e^-))$$

$$\sigma_{\text{ECM}}(x) \sim \text{constant} < \langle \sigma_{\text{ECM}}(x) \rangle$$

Boost measurement:

$$\langle (E(e^+) - E(e^-)) \rangle(x)$$

$$\text{Rms}((E(e^+) - E(e^-))(x)) \sim \text{constant} \sim \langle \text{Rms}((E(e^+) - E(e^-))) \rangle$$

“Measure” ECM on evt by evt basis

Measurement uncertainty in x for muon pairs $\approx 3 \text{ microns} / \sin(\phi)$
 Investigate other variables (z or time coordinates)

MORE TO DO

Specify the requirements from the experiment on

- ECM stability,
- ECM measurements and
- Centre-of-mass energy spread measurement

It seems possible (but not easy) to get in the right ball park with the techniques used for the Z pole see [arXiv:1909.12245](#); but we should go through the exercise to make sure we are not forgetting anything.

Also the muon-pair analysis needs to be investigated, taking into account the large amount of radiative Z-return to see how many of the events are really useable.