

Light vectors from baryonic and lepton family numbers with harmless Wess-Zumino terms

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based on the work with Marco Nardecchia and Luca Di Luzio
published in *Phys.Rev.D* 105 (2022) 11, 115042

Light vectors from abelian SM extension

- Light vectors provide a possible solution to many low-energy anomalies (e.g. muon's $g-2$) or a good candidate as mediator to dark sectors.
- Many BSM models including a light vector have been proposed in the past few years.
- We proposed a BSM extension including a light vector coming from the gauging of a new abelian symmetry.
- The gauge group of our model is then:

$$G_{SM} \times U(1)_X = SU(3)_c \times SU(2)_L \times U(1)_Y \times U(1)_X$$

- For simplicity, we assumed the SM Yukawa sector to be invariant under the new gauge symmetry.
- X is then a combination of the SM incidental symmetries, i.e. the baryonic number and lepton family numbers:

$$X = \alpha_B B + \sum_{i=e, \mu, \tau} \alpha_i L_i$$

Light vectors and anomalous currents

- Unless few specific cases, if no new fermions are introduced, the new gauge current is conserved at tree level but broken at loop by chiral anomaly.
- An example is the current of the baryon number:

$$\partial^\mu J_\mu^{\text{baryon}} = \frac{\mathcal{A}}{16\pi^2} \left(g^2 W_{\mu\nu}^a (\tilde{W}^a)^{\mu\nu} - g'^2 B_{\mu\nu} \tilde{B}^{\mu\nu} \right)$$

- If a light vector couples to a non conserved current, there are (energy/vector mass)² enhanced processes involving the longitudinal mode of the new vector.
- Such energy-enhanced processes can be the dominant production mechanism in high-energy experiments, and can place strong constraints on its coupling.

Example: let's consider a light vector with $m = 1$ MeV emitted in a physical process whose energy is around 1 GeV



Enhanced by a factor of $(1 \text{ GeV}/1 \text{ MeV})^2 = 10^6!$

WZ coefficient at 1-loop matching

- For example, a model of gauged baryon number requires anomalous to be consistent.
- Once integrated out, anomaly cancellation is preserved by WZ terms.

$$\begin{array}{l}
 SU(2)_L^2 U(1)_B = \frac{3}{2} \\
 U(1)_Y^2 U(1)_B = -\frac{3}{2}
 \end{array}
 \quad \longrightarrow \quad
 \begin{array}{l}
 \mathcal{L} \supset C_B g_X g'^2 \epsilon^{\mu\nu\rho\sigma} X_\mu B_\nu \partial_\rho B_\sigma \\
 + C_W g_X g^2 \epsilon^{\mu\nu\rho\sigma} X_\mu (W_\nu^a \partial_\rho W_\sigma^a + \frac{1}{3} g \epsilon^{abc} W_\nu^a W_\rho^b W_\sigma^c)
 \end{array}$$

- Only the combinations $L_e - L_\mu$, $L_\tau - L_\mu$ and $L_e - L_\tau$ are free-anomaly in the SM.
- The gauging of a general linear combination of SM accidental symmetries is anomalous.

$$\begin{array}{l}
 SU(2)_L^2 \times U(1)_X \\
 U(1)_Y^2 \times U(1)_X
 \end{array}
 \quad \text{proportional to} \quad 3\alpha_B + \alpha_e + \alpha_\mu + \alpha_\tau \equiv 3\alpha_{B+L}$$

- The values of the WZ coefficients depend on the UV completion.

FCNC from WZ terms

- XWW operator leads to flavor changing neutral current (FCNC) interactions

$$\mathcal{L} \supset g_{Xd_i d_j} X_\mu \bar{d}_j \gamma^\mu \mathcal{P}_L d_i + \text{h.c.} + \dots$$

The diagram illustrates the decomposition of the XWW operator into two diagrams. On the left, a quark line d_i enters a shaded vertex, and a quark line d_j exits, with a wavy line labeled X attached to the vertex. This is equal to the sum of two diagrams: the first shows a quark line d_i entering a vertex, with a quark line $u/c/t$ exiting, and a wavy line labeled W attached to the vertex; the second diagram shows a quark line d_i entering a vertex, with a quark line d_j exiting, and a wavy line labeled W attached to the vertex.

FCNC from WZ terms

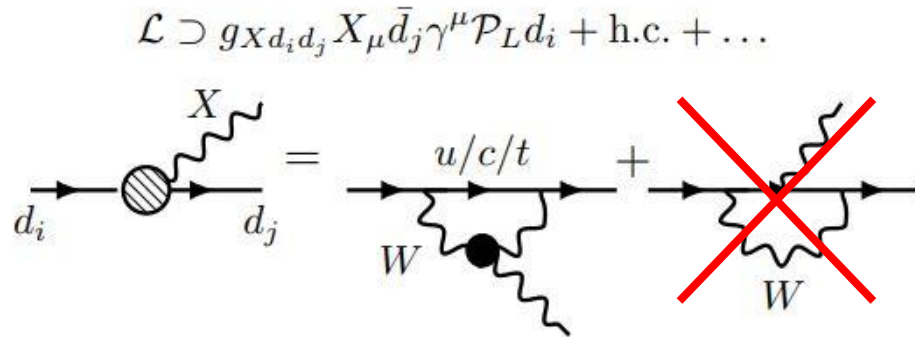
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The diagram illustrates the decomposition of the XWW operator. On the left, a fermion line d_i enters a shaded circle representing the operator, and a fermion line d_j exits. A wavy line labeled X connects the two vertices. This is set equal to the sum of two diagrams. The first diagram shows a fermion line d_i entering a vertex, which then connects to a W boson loop. The loop contains a fermion line with a mass insertion $u/c/t$. The loop then connects to a vertex from which a fermion line d_j exits. The second diagram is identical to the first but with a Z boson loop instead of a W loop. This second diagram is crossed out with a large red 'X', indicating that it is not present in the decomposition.

FCNC from WZ terms

- XWW operator leads to flavor changing neutral current (FCNC) interactions



- Meson decay rates through longitudinal light vector emission
- $g_{d_i d_j X}$ are the effective FCNC couplings originated from WZ operators

$$\Gamma(B \rightarrow K X) \simeq \frac{m_B^3}{64\pi m_X^2} |g_{bsX}|^2 \left(1 - \frac{m_K^2}{m_B^2}\right)^2 |f_K(m_X^2)|^2 \frac{2Q}{m_B}$$

$$\Gamma(B \rightarrow K^* X) \simeq \frac{m_B^3}{64\pi m_X^2} |g_{bsX}|^2 |f_{K^*}(m_X^2)|^2 \left(\frac{2Q}{m_B}\right)^3$$

$$\Gamma(K^\pm \rightarrow \pi^\pm X) \simeq \frac{m_{K^\pm}^3}{64\pi m_X^2} \left(1 - \frac{m_{\pi^\pm}^2}{m_{K^\pm}^2}\right)^2 |g_{sdX}|^2 \frac{2Q}{m_{K^\pm}}$$

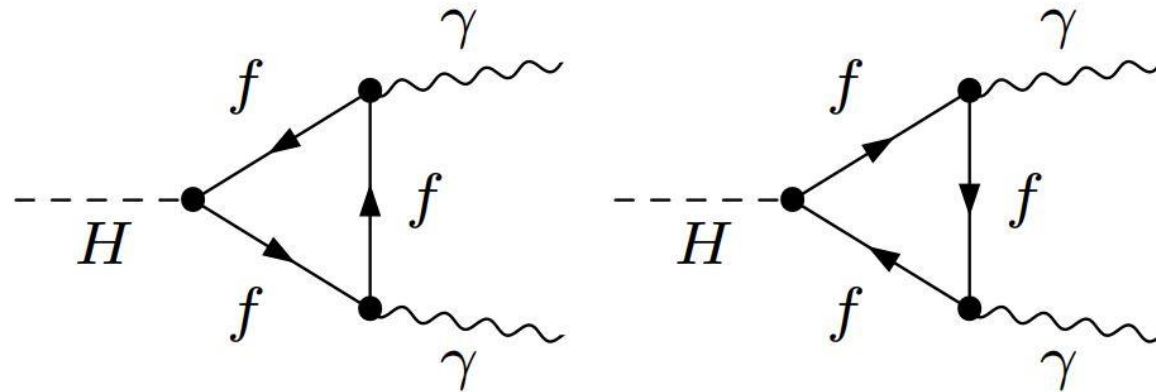
$$\Gamma(K_L \rightarrow \pi^0 X) \simeq \frac{m_{K_L}^3}{64\pi m_X^2} \left(1 - \frac{m_{\pi^0}^2}{m_{K_L}^2}\right)^2 \text{Im}(g_{sdX})^2 \frac{2Q}{m_{K_L}}$$

Gauging the accidental symmetries

- The main question of our work was: can we avoid such strong constraints?
- The answer is yes: mostly chiral anomalies suppress the coefficients of the WZ terms involving the electroweak gauge bosons, thus relaxing the bounds!

Gauging the accidental symmetries

- The main question of our work was: can we avoid such strong constraints?
- The answer is yes: mostly chiral anomalous suppress the coefficients of the WZ terms involving the electroweak gauge bosons, thus relaxing the bounds!
- However, mostly chiral fermions would modify the SM prediction of the Higgs decay channels.



- The goal is then to introduce a UV completion made of mostly chiral anomalous while being compatible with experimental measurements of Higgs decays.

UV completion

Field	Lorentz	SU(3) _C	SU(2) _L	U(1) _Y	U(1) _X
q_L^i	$(\frac{1}{2}, 0)$	3	2	1/6	$\alpha_B/3$
u_R^i	$(0, \frac{1}{2})$	3	1	2/3	$\alpha_B/3$
d_R^i	$(0, \frac{1}{2})$	3	1	-1/3	$\alpha_B/3$
ℓ_L^i	$(\frac{1}{2}, 0)$	1	2	-1/2	α_i
e_R^i	$(0, \frac{1}{2})$	1	1	-1	α_i
H	$(0, 0)$	1	2	1/2	0
\mathcal{L}_L	$(\frac{1}{2}, 0)$	1	2	$\mathcal{Y} - 1/2$	$X_{\mathcal{L}_L}$
\mathcal{L}_R	$(0, \frac{1}{2})$	1	2	$\mathcal{Y} - 1/2$	$X_{\mathcal{L}_L} + 3\alpha_{B+L}$
\mathcal{E}_L	$(\frac{1}{2}, 0)$	1	1	$\mathcal{Y} - 1$	$X_{\mathcal{L}_L} + 3\alpha_{B+L}$
\mathcal{E}_R	$(0, \frac{1}{2})$	1	1	$\mathcal{Y} - 1$	$X_{\mathcal{L}_L}$
\mathcal{N}_L	$(\frac{1}{2}, 0)$	1	1	\mathcal{Y}	$X_{\mathcal{L}_L} + 3\alpha_{B+L}$
\mathcal{N}_R	$(0, \frac{1}{2})$	1	1	\mathcal{Y}	$X_{\mathcal{L}_L}$
ν_R^α	$(0, \frac{1}{2})$	1	1	0	$X_{\nu_R}^\alpha$
\mathcal{S}	$(0, 0)$	1	1	0	$X_{\mathcal{S}}$

➤ Anomaly-cancelling fermions are highlighted in pink.

➤ Anomalous $U(1)_X$ charges were chosen by the requirement that the electroweak-charged anomalous pick up mass from the SM Higgs

$$-\mathcal{L}_Y = y_1 \bar{\mathcal{L}}_L \mathcal{E}_R H + y_2 \bar{\mathcal{L}}_R \mathcal{E}_L H + y_3 \bar{\mathcal{L}}_L \mathcal{N}_R \tilde{H} + y_4 \bar{\mathcal{L}}_R \mathcal{N}_L \tilde{H} + \text{h.c.}$$

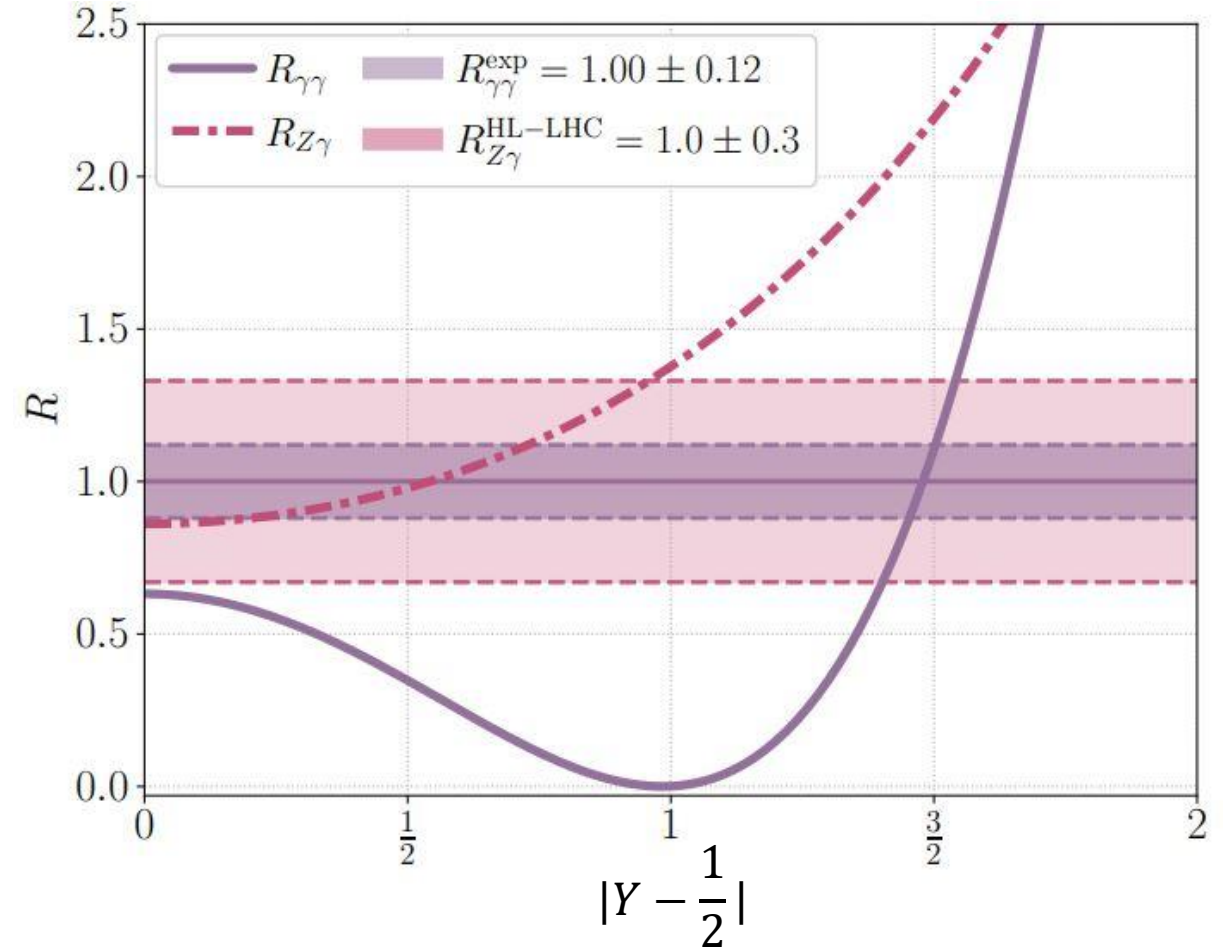
➤ A SM-singlet Higgs is added to give mass to the new gauge bosons but not to the electroweak-charged anomalous.

Higgs decay channels

- Mostly-chiral electroweak anomalous, needed to decouple dangerous WZ terms, would produced a signal in Higgs decays

$$R_{\gamma\gamma} = \frac{|\mathcal{A}_{\gamma\gamma}^{\text{SM}} + \mathcal{A}_{\gamma\gamma}^{\text{NP}}|^2}{|\mathcal{A}_{\gamma\gamma}^{\text{SM}}|^2} \quad \mathcal{A}_{\gamma\gamma}^{\text{NP}} \approx -2\mathcal{A}_{\gamma\gamma}^{\text{SM}}$$

- In the limit of heavy fermions, the anomalous contribution to the decays depends on the Y parameter.
- Our prediction is compatible with the di-photon channel for $|Y - 1/2| \approx 3/2$, while leading a large deviation to the correlated signal in the γZ channel to be tested at the High Luminosity phase at LHC.



Direct searches

Stable anomalous

- $|Y-1/2| \approx 3/2$ but $|Y-1/2| \neq 3/2$
- EW anomalon-SM mixing terms are forbidden and the lightest state of the electroweak anomalous is electrically charged and stable
- Need to invoke low-scale inflation to avoid cosmological problems
- Stable charged particles yield striking signatures at colliders in the forms of charged track, anomalous energy loss in calorimeters, longer time of flights, etc
- Actual experimental limits from CMS at 13 TeV LHC yielding $m \geq 800$ GeV

Unstable anomalous

- $|Y-1/2| = 3/2$
- EW anomalous can actually mix with the SM leptons, opening new decay channels
- Anomalous with electric charge $|Q| = 2$ can decay into a W and a $|Q| = 1$ fermion, while the latter can mix with SM leptons and decay into $Z\ell$ or $h\ell$
- Bounds appear to be of the same order of those obtained in the case of stable charged leptons.

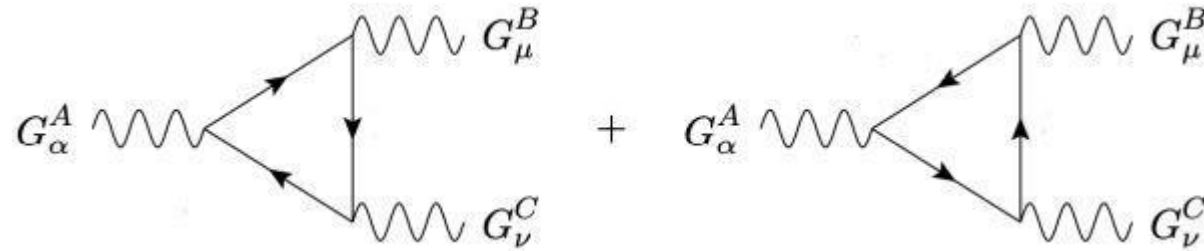
Yukawas of the anomalous to the boundary of perturbativity!

THANKS FOR THE ATTENTION!

BACK UP

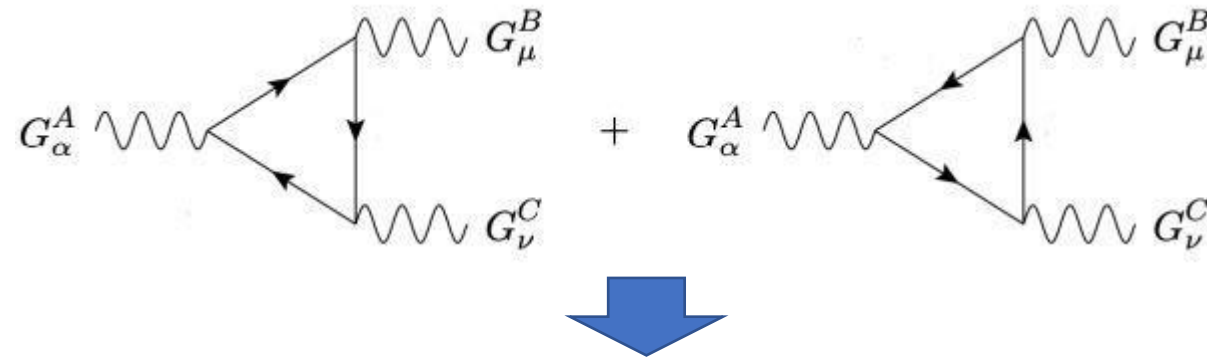
Chiral anomaly and anomalous fermions

- At quantum level, chiral anomaly can break classical symmetry.
- Chiral anomaly occurs at one-loop level through triangle with fermion fields:



Chiral anomaly and anomalon fermions

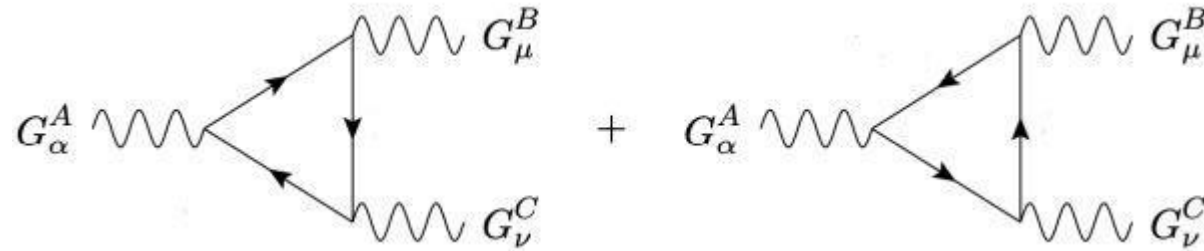
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$$\partial_\mu J_{Q^A}^\mu = \sum_{BC} \frac{g_B g_C}{48\pi^2} [\text{Tr } Q_R^A \{Q_R^B, Q_R^C\} - \text{Tr } Q_L^A \{Q_L^B, Q_L^C\}] \partial_\alpha G_\mu^B \partial_\beta G_\nu^C \epsilon^{\alpha\mu\beta\nu}$$

Chiral anomaly and anomalon fermions

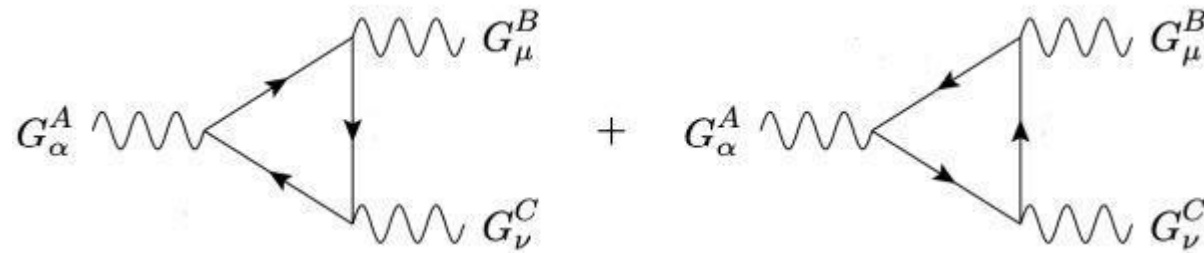
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- A gauge symmetry is conserved (and hence the theory is consistent) if


$$\sum_{\text{fermions}} [\text{Tr } Q_R^A \{Q_R^B, Q_R^C\} - \text{Tr } Q_L^A \{Q_L^B, Q_L^C\}] = 0$$

- Uncancelled chiral anomalies requires new fermions to have a consistent gauge theory!

Anomaly matching and WZ operators

- One of the most important EFT operator is the Wess-Zumino (WZ) term Γ_{WZ} .
- The WZ term is a functional of gauge vector bosons and Goldstone fields of the theory.
- WZ operators appear once we integrate out a fermion field from the theory.

$$\mathcal{L}_{UV} \supset \sum_i \bar{\psi}_i i \not{\partial} \psi_i - \sum_{i,j} (\bar{\psi}_{iL} \mathcal{M}_{ij} \psi_{jR} + \text{h.c.}) - \sum_{a,i,j} \tilde{H}_a (\bar{\psi}_{iL} \mathcal{Y}_{ij}^a \psi_{jR} + \text{h.c.})$$

$$- \sum_{i,j,A} g_A G_\mu^A \left[\bar{\psi}_{iL} \gamma^\mu (Q_L^A)_{ij} \psi_{jL} + \bar{\psi}_{iR} \gamma^\mu (Q_R^A)_{ij} \psi_{jR} \right]$$


$$\mathcal{S}_{eff} \supset \Gamma_{WZ}(G_\mu^A, \tilde{H}^a)$$

- The WZ term matches the chiral anomaly of the UV fermions we integrated out from the theory.
- They are crucial to keep the theory free-anomaly and hence consistent.

$$\delta \Gamma_{WZ}|_{Q^A} = \sum_{BC} \frac{g_B g_C}{48\pi^2} \left[\text{Tr} Q_R^A \{Q_R^B, Q_R^C\} - \text{Tr} Q_L^A \{Q_L^B, Q_L^C\} \right] \int d^4x \alpha_A \partial_\alpha G_\mu^B \partial_\beta G_\nu^C \epsilon^{\alpha\mu\beta\nu}$$

EFT framework

- Uncancelled anomalies requires new fermion fields (the “anomalous”) otherwise no gauging is possible.
- Anomalous fermions are supposed to be heavy, masses above hundreds of GeV, since we have not observed them so far.

Heavy physics:
Anomalous fields



Light physics:
SM + light vector

Energy or mass scale

EFT framework

- Uncancelled anomalies requires new fermion fields (the “anomalons”) otherwise no gauging is possible.
- Anomalon fermions are supposed to be heavy, masses above hundreds of GeV, since we have not observed them so far.



- At low energy, we work with Effective Field Theory (EFT).
- Anomalon fields are integrated out.
- EFT operators are introduced to match the UV physics.

~~Heavy physics:
Anomalon fields~~



Light physics:
SM + light vector

$$\mathcal{L}_{\text{EFT}} = \sum_{\mathcal{D} \geq 0, i} \frac{c_i^{(\mathcal{D})} O_i^{(\mathcal{D})}}{\Lambda^{\mathcal{D}-d}}$$



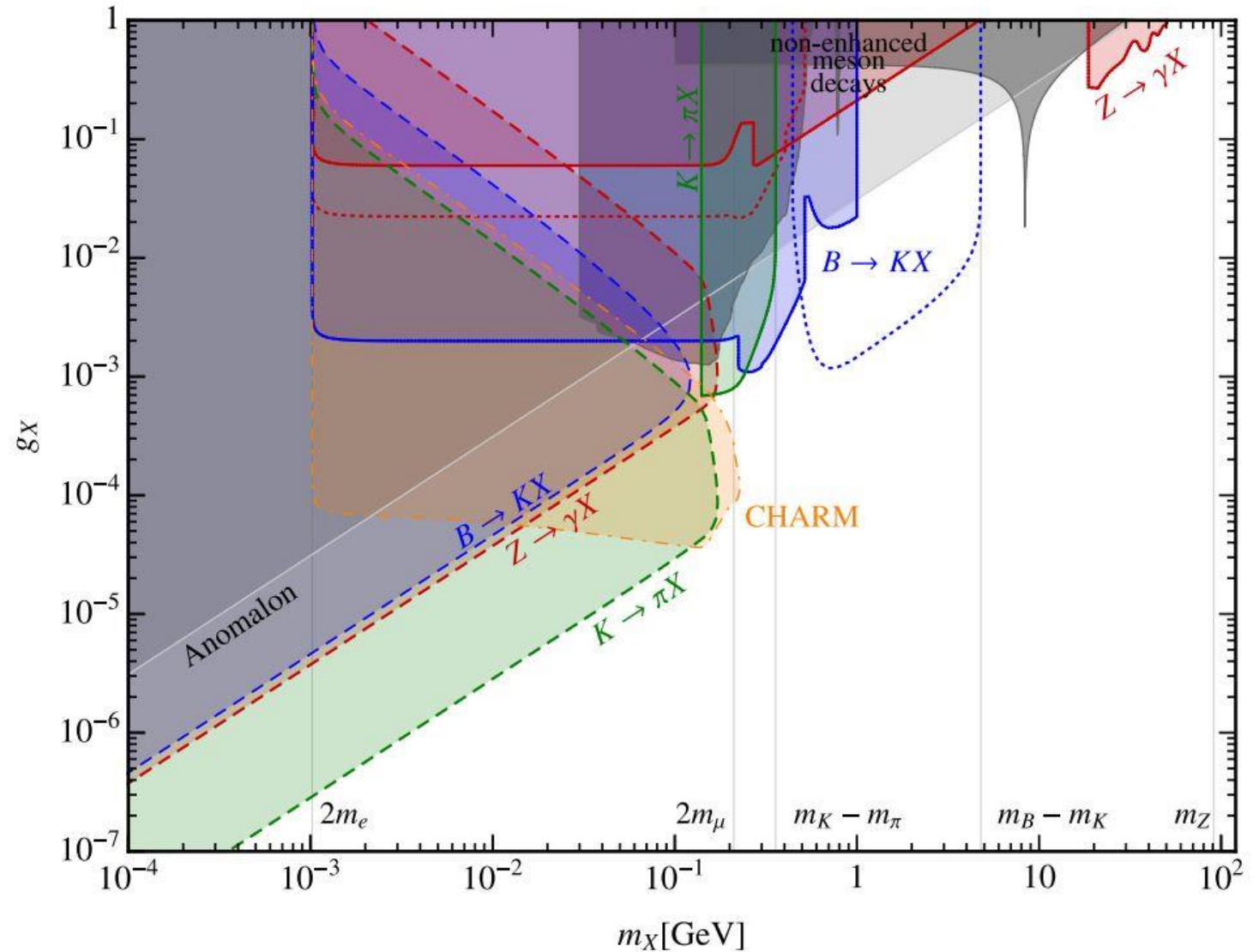
Energy or mass scale

FCNC from WZ terms

- Collection of experimental bounds from arxiv:1705.06726
- Here is considered the case of gauged baryonic number with SM-vector-like UV anomalon fields

$$g_{Xd_i d_j} = -\frac{3g^4 \mathcal{A}}{(16\pi^2)^2} g_X \sum_{\alpha \in \{u, c, t\}} V_{\alpha i} V_{\alpha j}^* F\left(\frac{m_\alpha^2}{m_W^2}\right)$$

Assumed kinetic mixing $\epsilon \sim eg_X / (4\pi)^2$



Neutrino masses

Field	Lorentz	SU(3) _C	SU(2) _L	U(1) _Y	U(1) _X
q_L^i	$(\frac{1}{2}, 0)$	3	2	1/6	$\alpha_B/3$
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ℓ_L^i	$(\frac{1}{2}, 0)$	1	2	-1/2	α_i
e_R^i	$(0, \frac{1}{2})$	1	1	-1	α_i
H	$(0, 0)$	1	2	1/2	0
\mathcal{L}_L	$(\frac{1}{2}, 0)$	1	2	$\mathcal{Y} - 1/2$	$X_{\mathcal{L}_L}$
\mathcal{L}_R	$(0, \frac{1}{2})$	1	2	$\mathcal{Y} - 1/2$	$X_{\mathcal{L}_L} + 3\alpha_{B+L}$
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\mathcal{N}_L	$(\frac{1}{2}, 0)$	1	1	\mathcal{Y}	$X_{\mathcal{L}_L} + 3\alpha_{B+L}$
\mathcal{N}_R	$(0, \frac{1}{2})$	1	1	\mathcal{Y}	$X_{\mathcal{L}_L}$
ν_R^α	$(0, \frac{1}{2})$	1	1	0	$X_{\nu_R}^\alpha$
\mathcal{S}	$(0, 0)$	1	1	0	$X_{\mathcal{S}}$

- SM Higgs and SM-singlet Higgs yield Dirac and Majorana masses respectively for neutrinos

$$\begin{aligned}
 -\mathcal{L}_Y^{\nu R} &= y_D^{i\beta} \bar{\ell}_L^i \nu_R^\beta \tilde{H} + \frac{1}{2} y_{\nu R}^{\alpha\beta} \nu_R^\alpha \nu_R^\beta \mathcal{S}^* + \text{h.c.} \\
 &\longrightarrow m_D^{i\beta} \bar{\ell}_L^i \nu_R^\beta + \frac{1}{2} M_R^{\alpha\beta} \nu_R^\alpha \nu_R^\beta + \text{h.c.}
 \end{aligned}$$

- Our model can accommodate a type-I see-saw mechanism:

$$m_\nu = m_D M_R^{-1} m_D^T$$