

# Ideas for extended interaction region magnet slicing

**Tracking through IR using field descriptions** ( tilted solenoid + fringe + quad overlap )

**implemented in direct tracking** FieldStep, [MDISim](#)-GEANT4

**and applied to FCC-ee,**

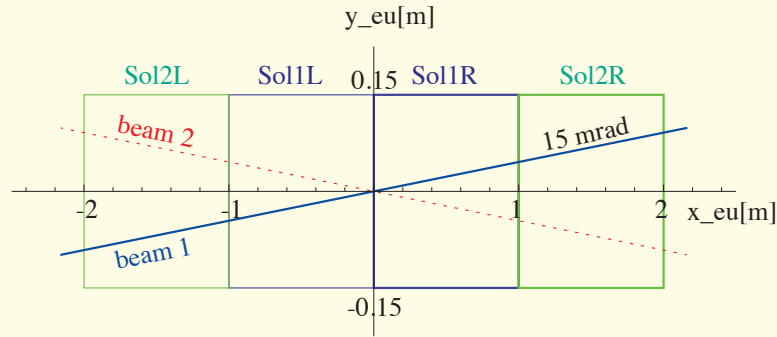
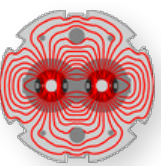
**as previously presented**

## **FCC-ee optics meetings**

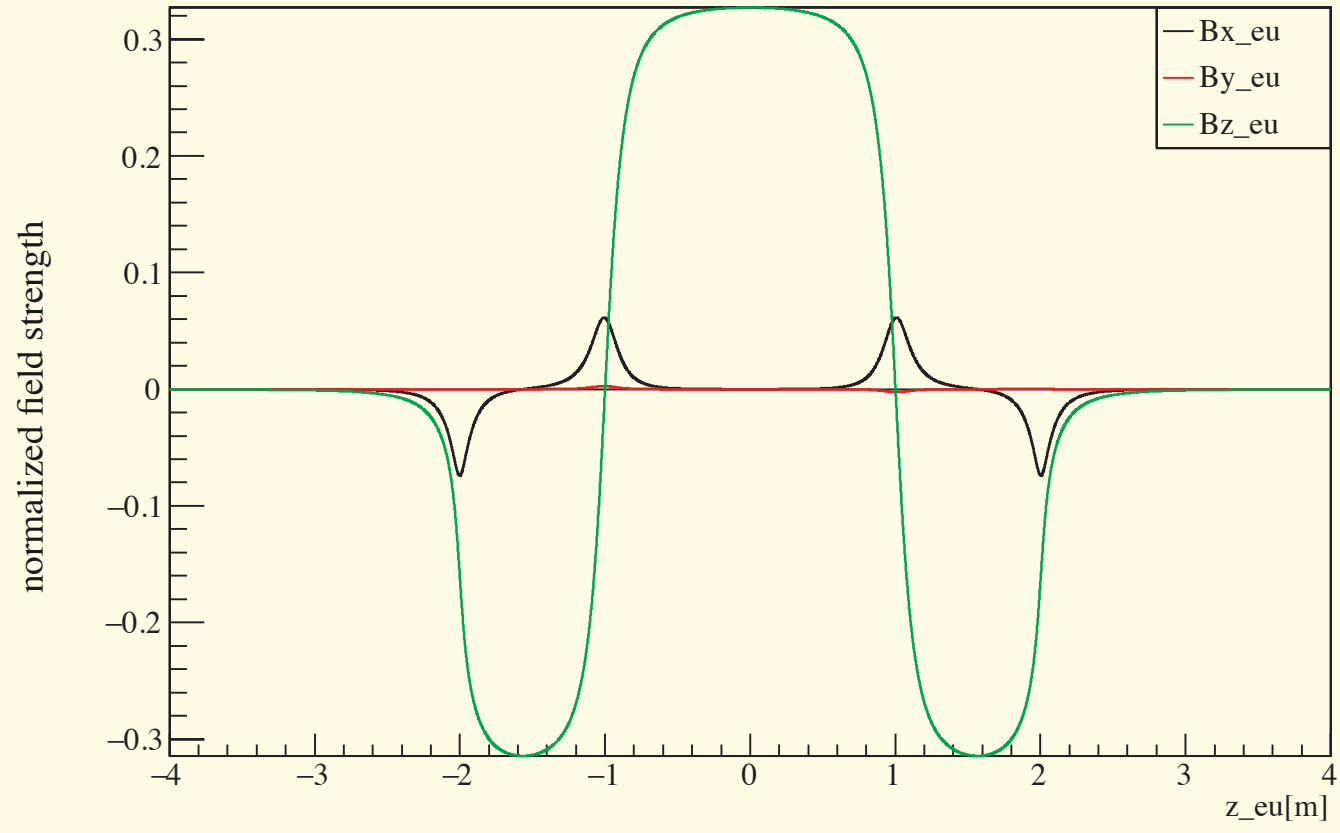
[#95](#) 05/04/2019 Comparison of tracking and maps for tilted solenoid with fringe fields

[#96](#) 03/05/2019 Tracking through solenoid with overlapping fields in quadrupole using Geant4

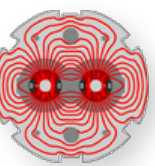
[#105](#) 11/10/2019 Radiation generated at the IP ~ 40 kW solenoid + ~ 400 kW beamstrahlung at FCC-ee Z  
hitting the beam pipe 49 - 55 m from IP



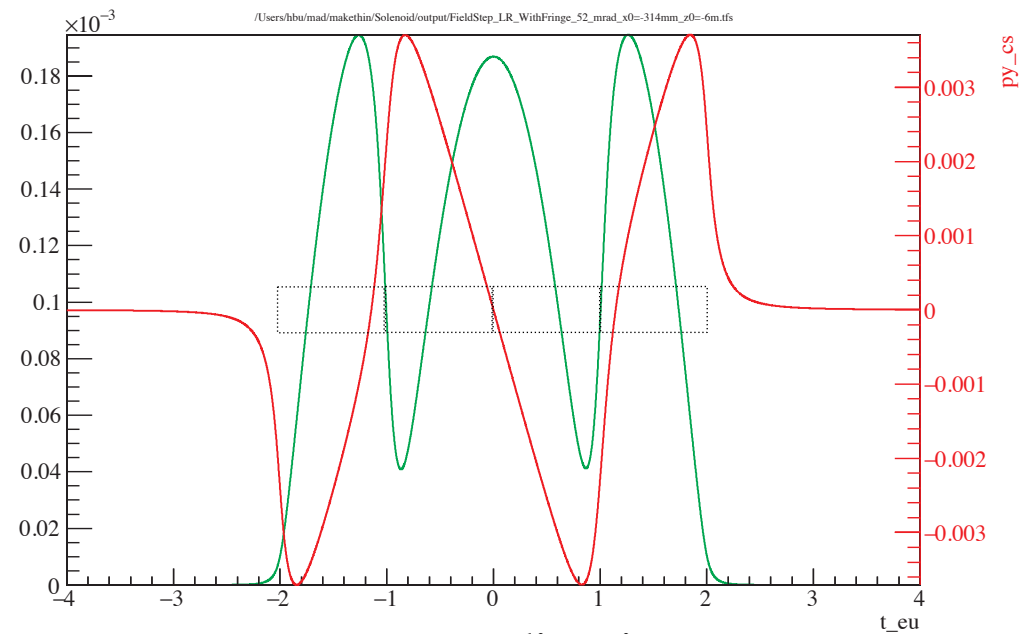
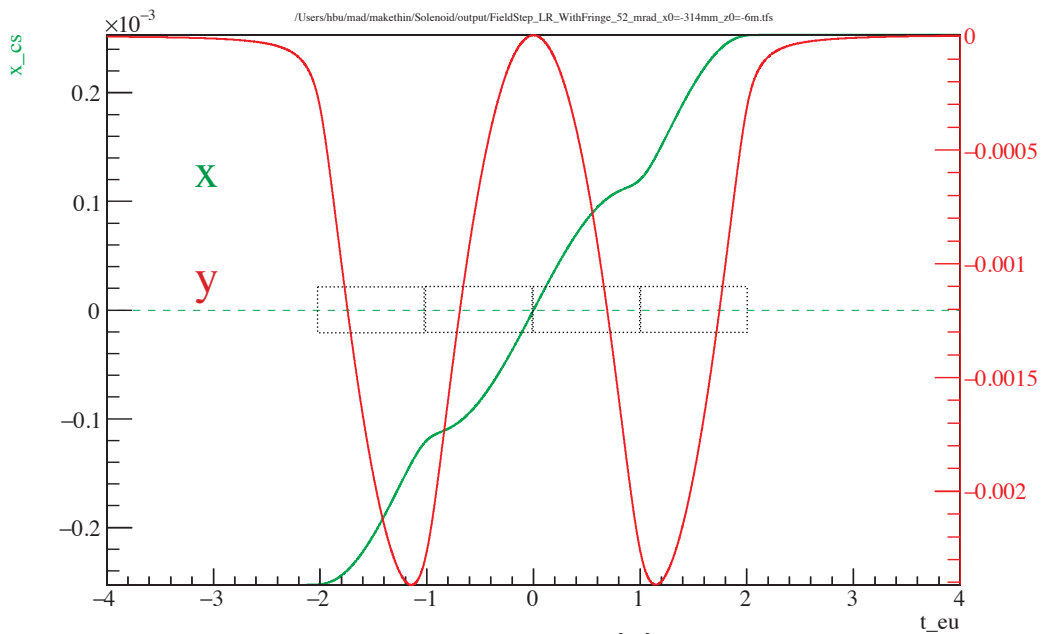
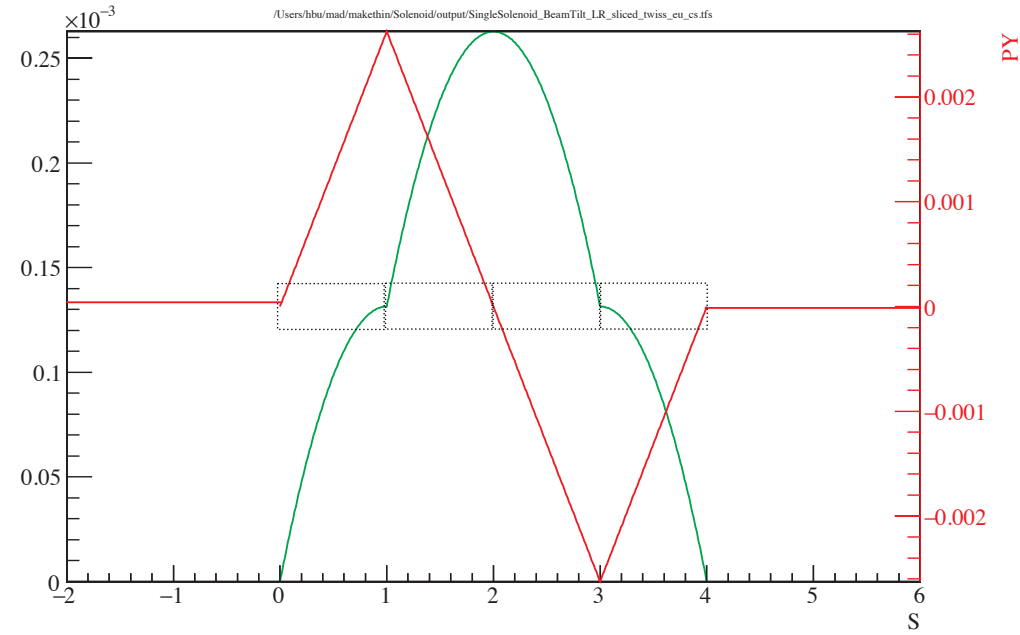
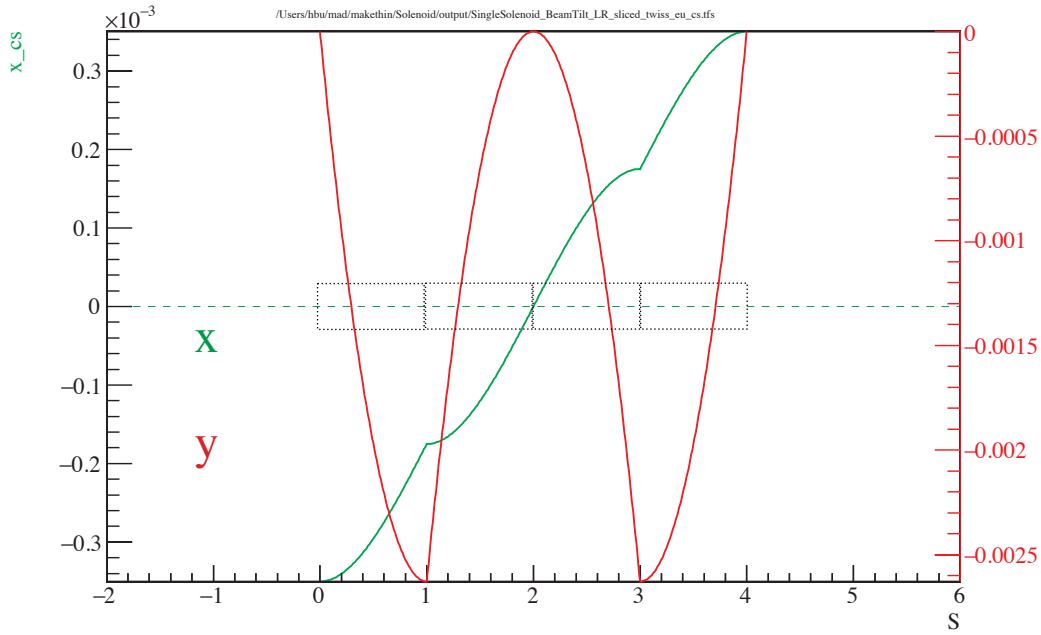
four 1m solenoid  
anti-solenoid  
pieces



# Comparison



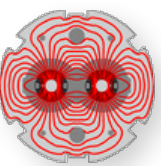
$\pm 15$  mrad crossing angle, 2 T, 45.6 GeV



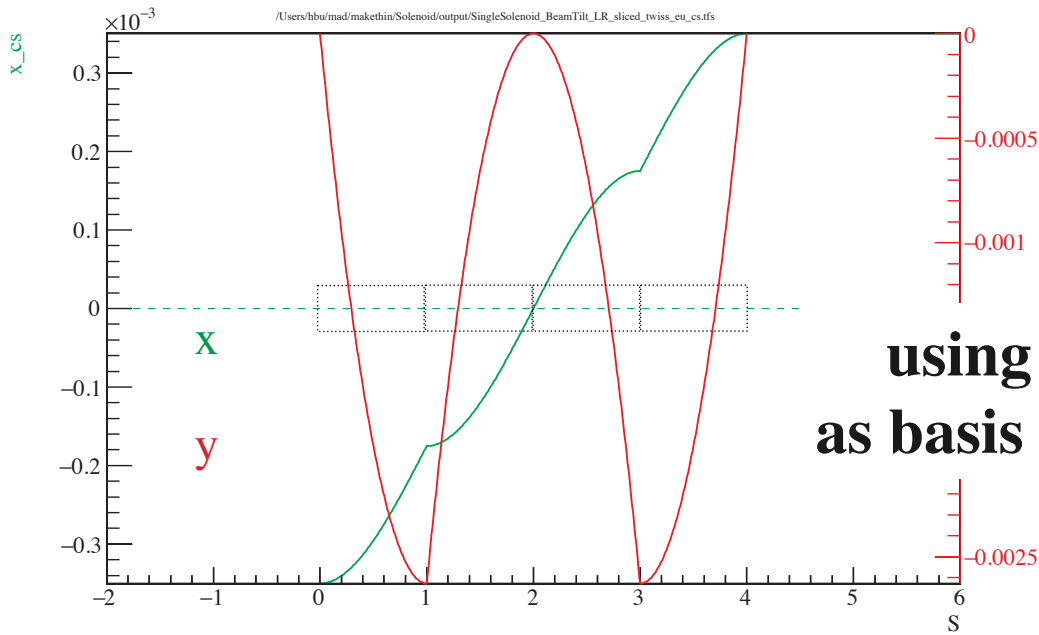
position

direction

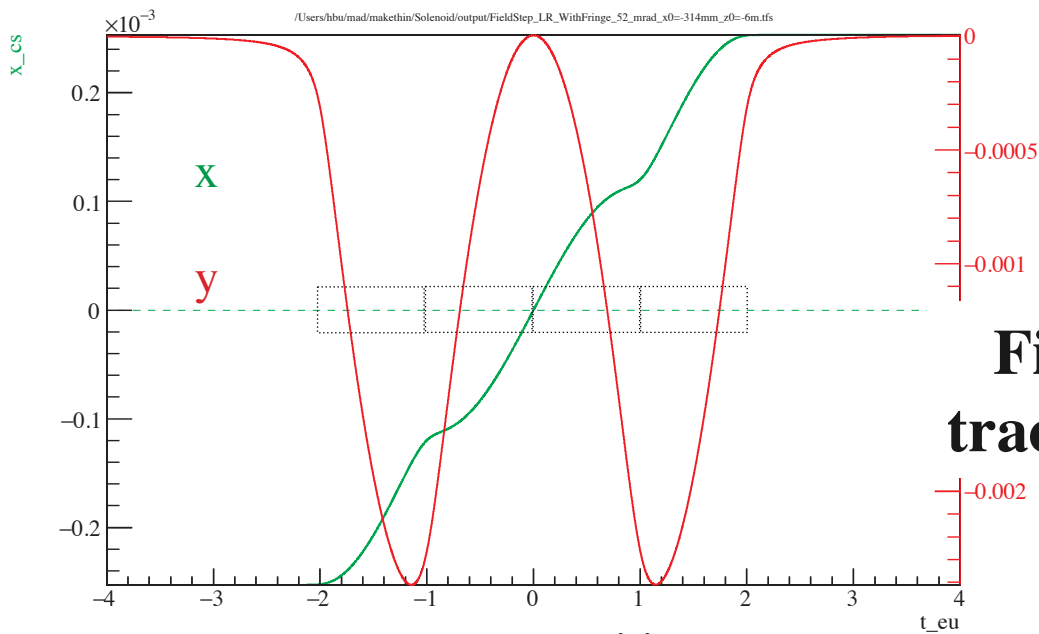
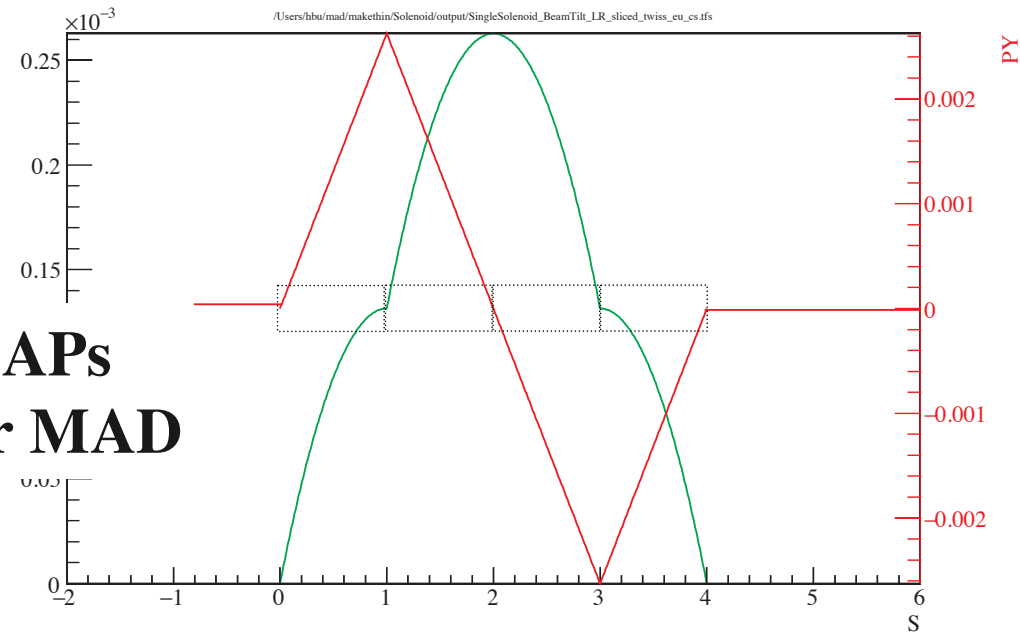
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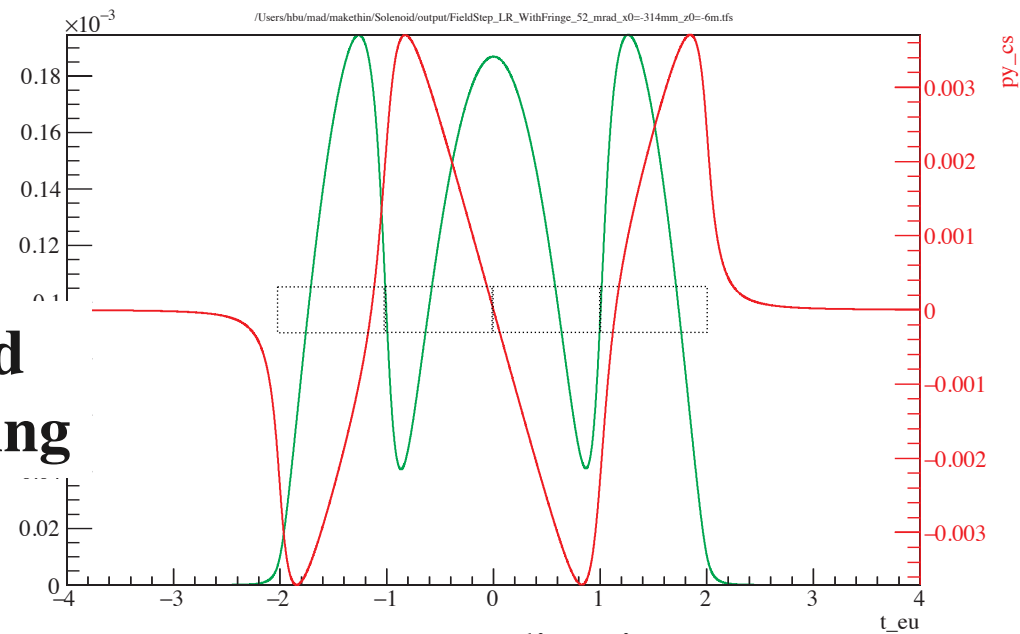
$\pm 15$  mrad crossing angle, 2 T, 45.6 GeV



using MAPs  
as basis for MAD



Field  
tracking

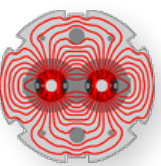


position

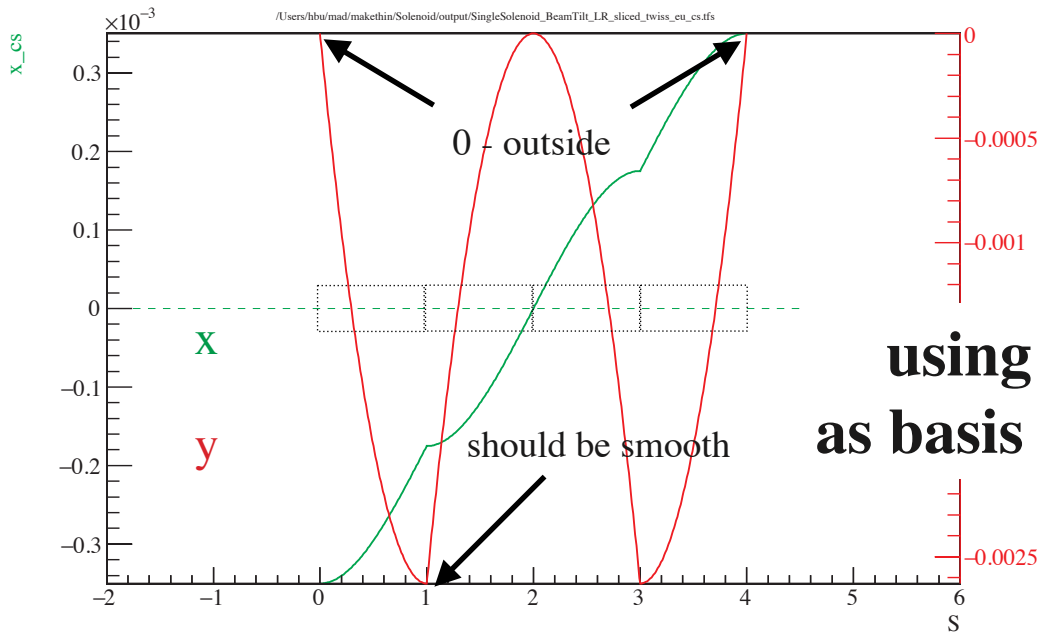
direction



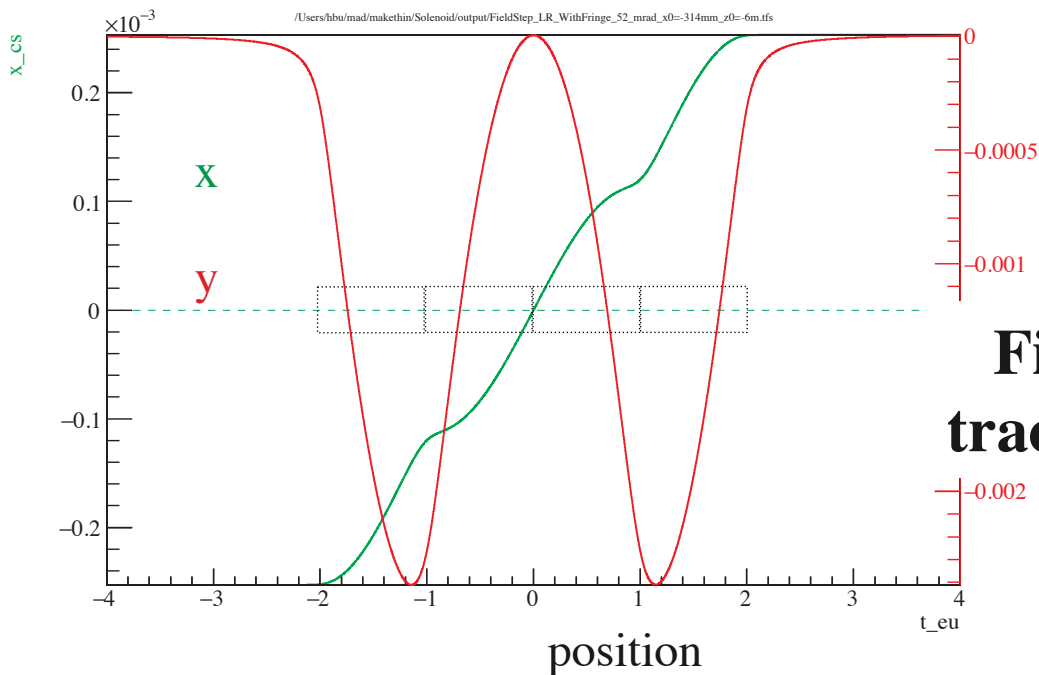
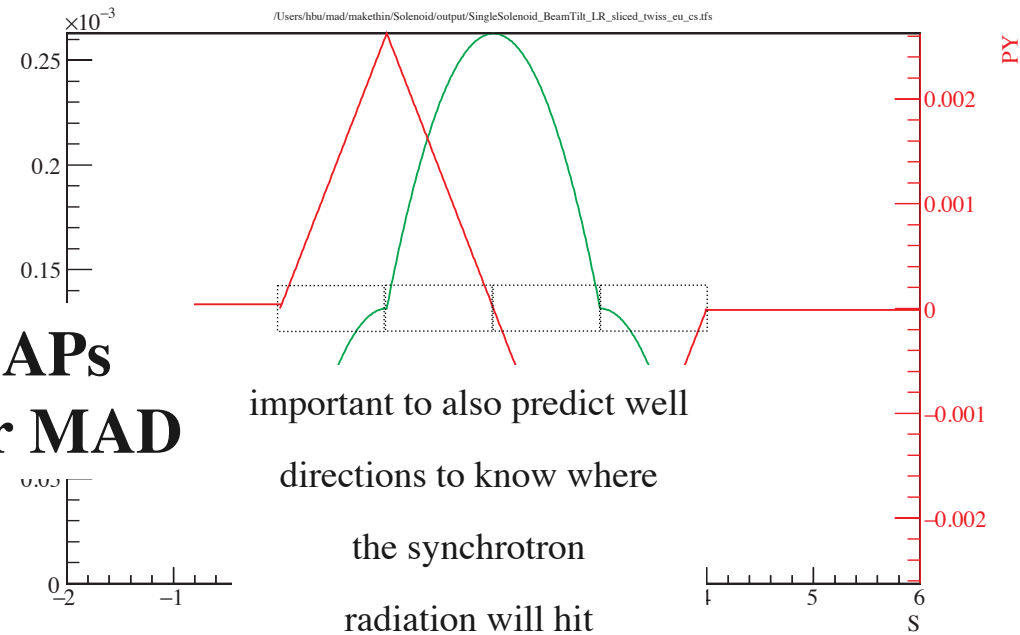
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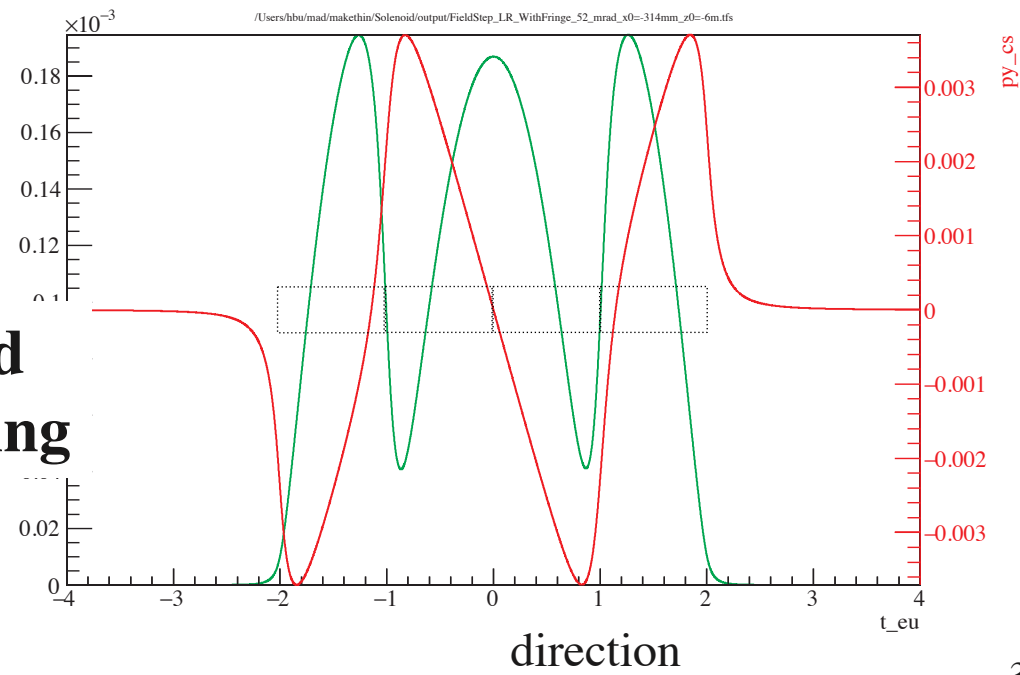
$\pm 15$  mrad crossing angle, 2 T, 45.6 GeV

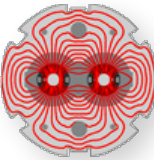


using MAPs  
as basis for MAD



Field  
tracking





**Sector Maps** : derived from Hamiltonian by A. Dragt, G. Ripken et al.

provide transformation by element — **as seen from outside**

**very powerful for optics design**

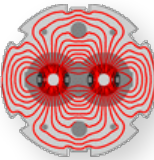
**slicing** (module MAKETHIN) designed to well approximate the element transformation

to reproduce twiss parameters as relevant (far) outside the element

but usually giving a **good approximation** for tracking through standard elements like bending magnets

**Not adequate** for solenoids with crossing angle (tilted solenoids in beam coordinates)

with major fringe and overlapping fields as required **for the FCC-ee IP fields**



**Determine the particle trajectories by direct tracking  
using an analytic field description or field maps**

**Direct tracking allows to integrate synchrotron radiation (including beamstrahlung)  
in a natural way** ( FCC-ee optics [#105](#) presentation )

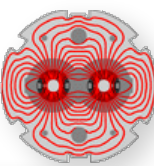
**Use this as a basis in complicated cases ( IP fields ) to obtain all required information**

**As in a real machine, beta functions, dispersion .. can be measured based on orbit/trajectory  
information**

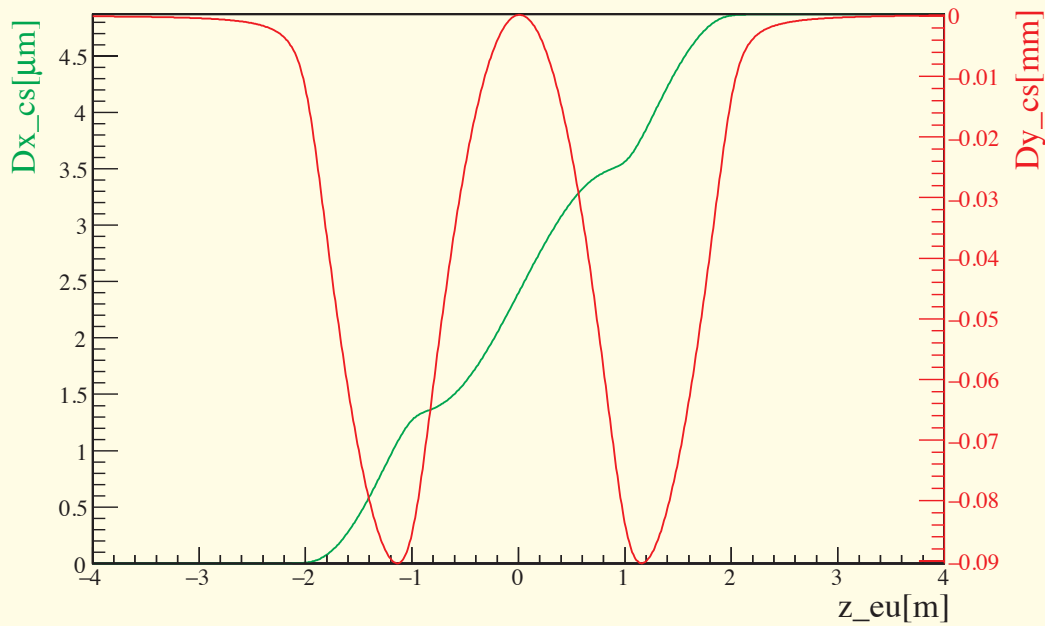
**On a more abstract level direct tracking can be considered as**

- **numerically solving (stepwise integrating) the equations of motions**
- **can be approximated by a sequence of kicks, provided by thin multipoles**  
( symplectic kick-drift-kick integration )

**Construct a new “GenerateThin” module to describe the whole IP region as a sequence  
of thin multipoles, that can be plugged in the machine lattice description (sequence file)  
readable by MAD-X**



dispersion from tracking with  $\delta p = 10^{-6}$



GeneratedThin.seq read by MAD-X

Using multipoles slices,  
kick strength fitted to fields  
evaluated (in the first iteration)  
for a straight line tilted by  
15 mrad horizontally through IP

