

# Longitudinal Dynamics in the Drive Beam Accelerator

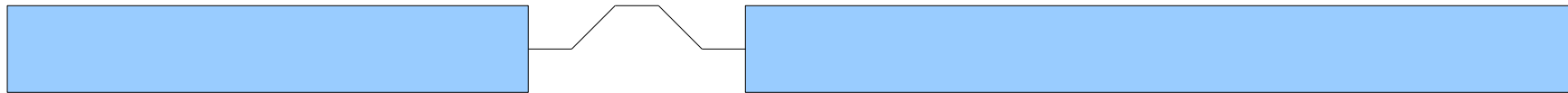
A.Aksoy

# Layout

**DBL1**

Bunc  
Compressor

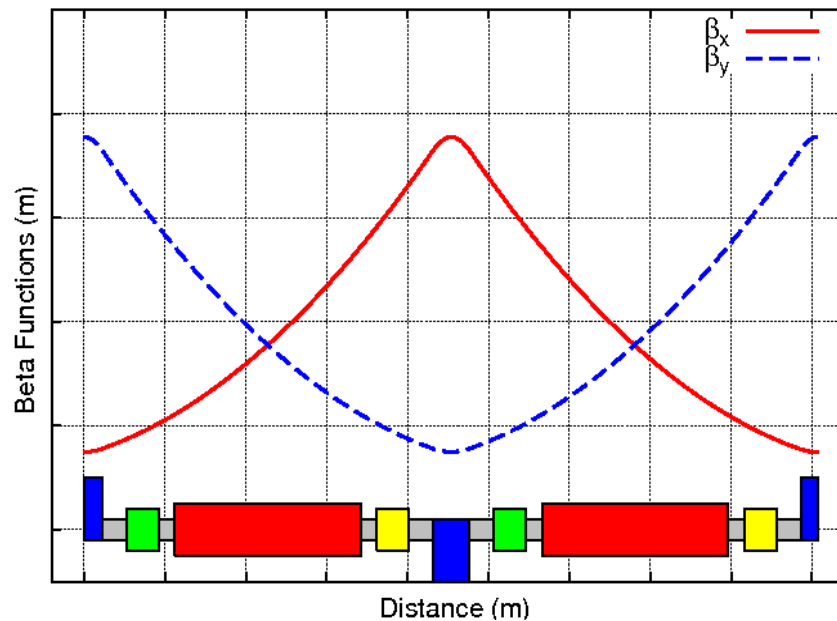
**DBL2**



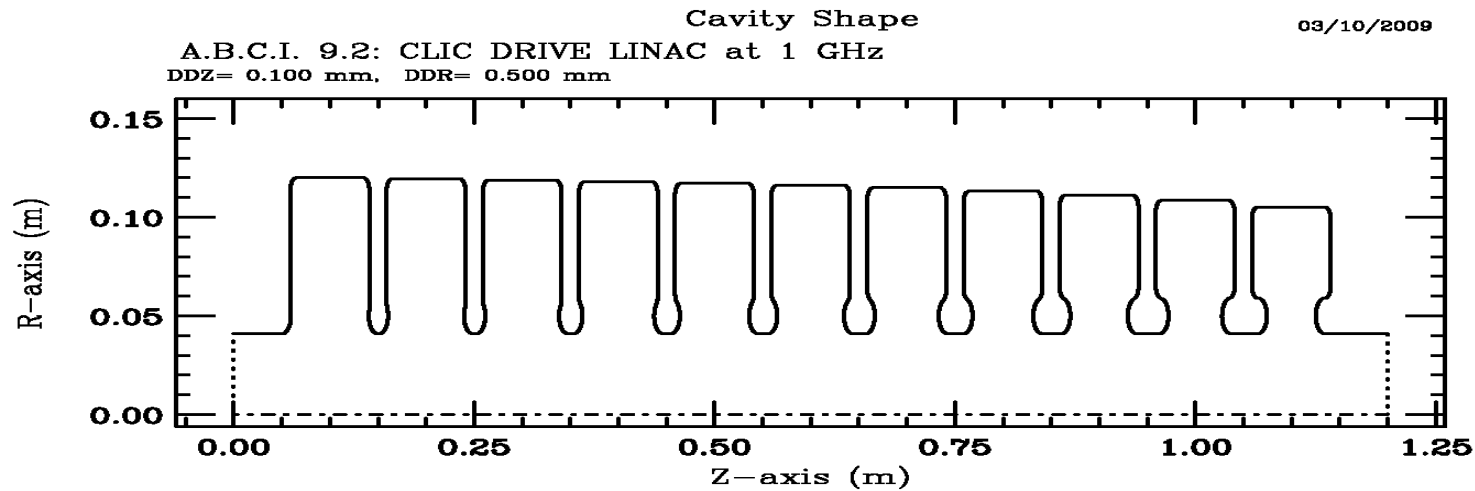
Beam energy  
50 → 250-300 MeV  
Bunch length:  
3 mm  
No of structures:  
62 - 92

Compression  
3mm → 1mm

Beam energy  
250-300 → 2500 MeV  
Bunch length:  
1 mm  
No of structures:  
698-1046



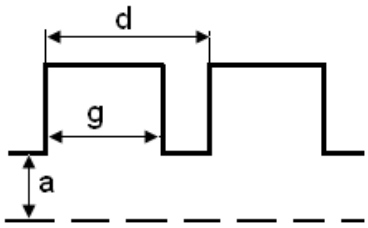
# Structures



Strucutre	Cell Length (mm)	Bore Radius (mm)	Diameter (mm)	Gap Lenght (mm)	Input power (MW)
11 Cell	99.97	41	240-210	80-50	10
14 Cell	99.97	47	245-189	80-32	10
16 Cell	99.97	47	240-209	75-46	12.5
17 Cell	99.97	49	244-204	78-36	12.5
18 Cell	99.97	47	242-215	78-51	15
19 Cell	99.97	49	246-204	80-40	15

# Short Range Longitudinal Wakes

## Karl Bane's Formula

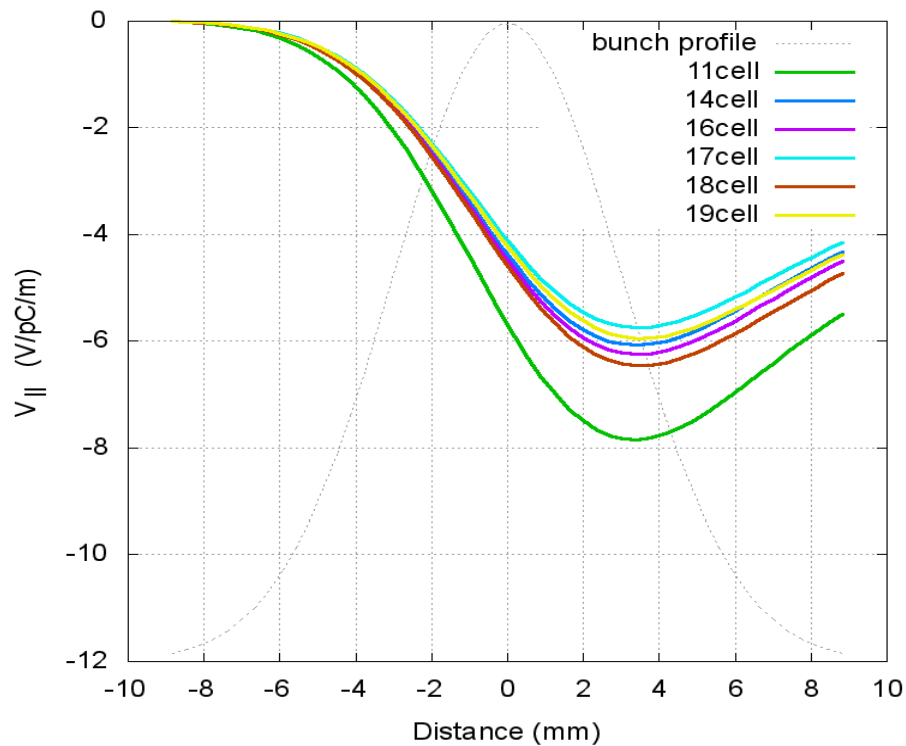


$$s_{0,i} = 0.41 \frac{a^{0.18} g_i^{1.6}}{d^{2.5}}, \quad Z_0 = 120 \pi \Omega$$

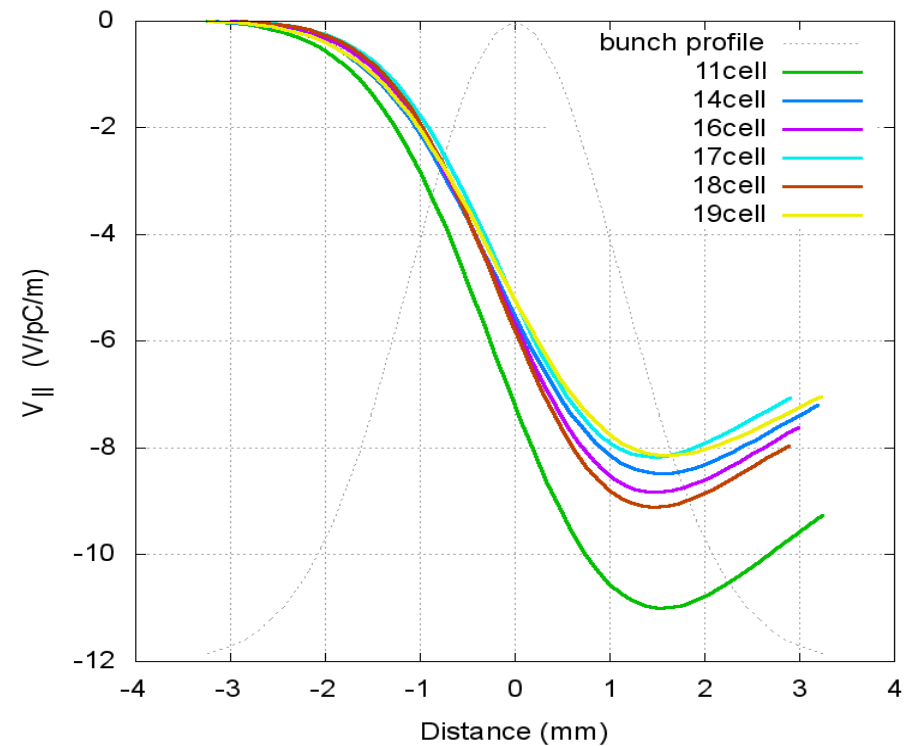
$$W_{\parallel,i}(s) = \frac{4Z_{0c}}{\pi a^2} \exp\left(-\sqrt{\frac{s}{s_{0,i}}}\right), \quad W_{\parallel}(s) = \frac{1}{n} \sum_{i=1}^n W_{\parallel,i}(s)$$

$$V_{\parallel}(s) = \int_{-\infty}^s W_{\parallel}(s-x) \sigma(x) dx$$

Longitudinal wake potential for 3 mm bunch

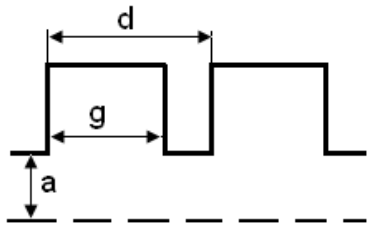


Longitudinal wake potential for 1 mm bunch



# Short Range Transverse Wakes

## Karl Bane's Formula

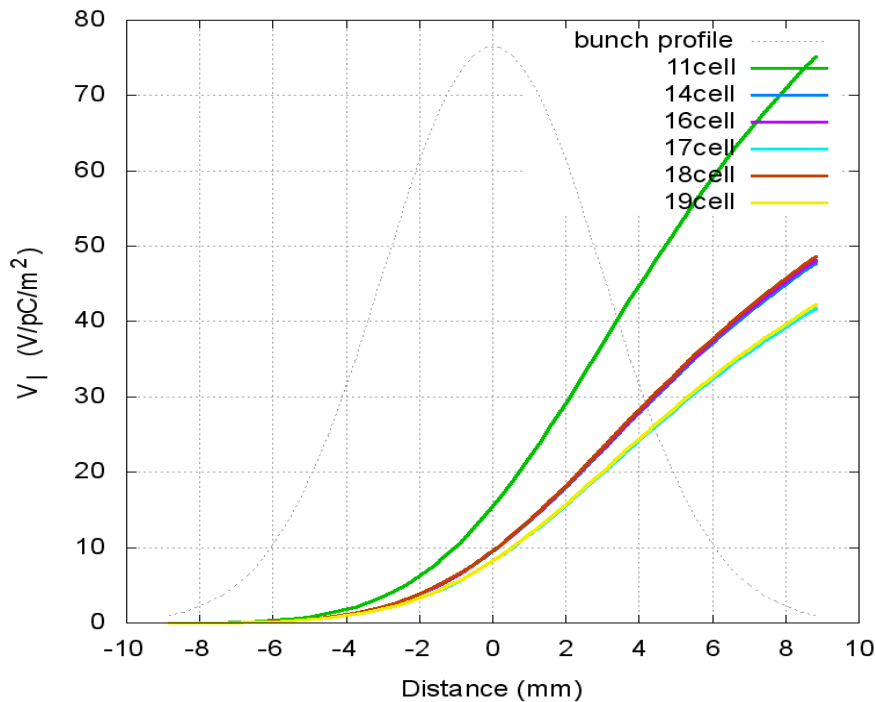


$$s_{0,i} = 1.69 \frac{a^{1.79} g_i^{0.38}}{d^{1.17}}, \quad Z_0 = 120 \pi \Omega$$

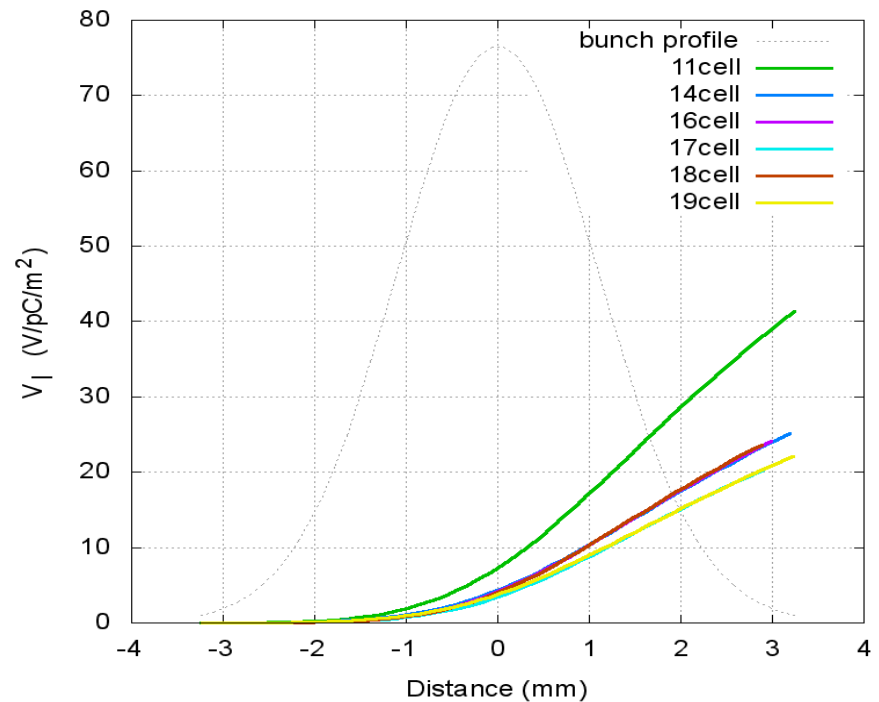
$$W_{\perp,i}(s) = \frac{4 Z_0 c s_{0,i}}{\pi a^4} \left[ 1 - \left( 1 + \sqrt{\frac{s}{s_{0,i}}} \right) \exp\left(-\sqrt{\frac{s}{s_{0,i}}}\right) \right], \quad W_{\perp}(s) = \frac{1}{n} \sum_{i=1}^n W_{\perp,i}(s)$$

$$V_{\perp}(s) = \int_0^s W_{\perp}(s-x) \sigma(x) dx$$

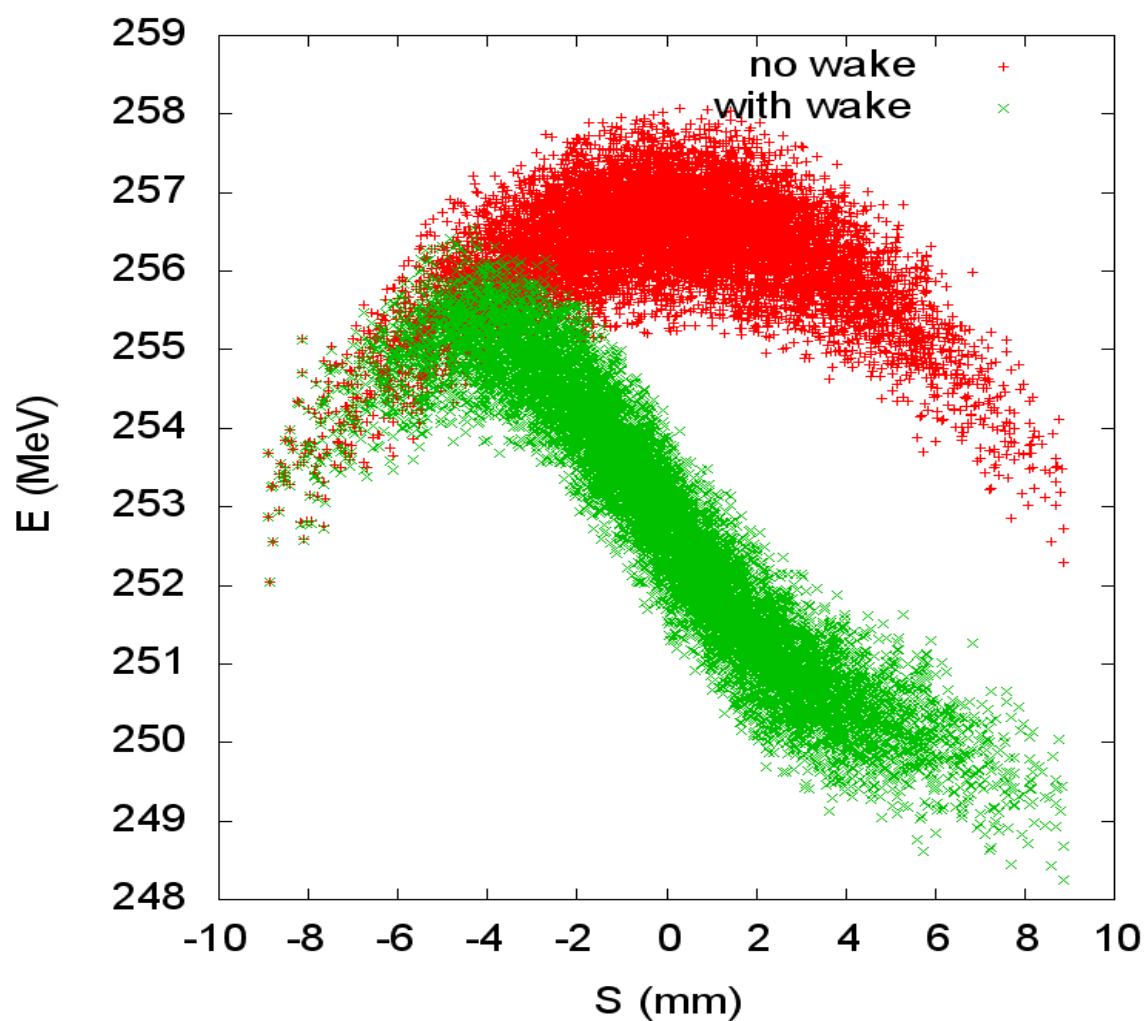
Transverse wake potential for 3 mm bunch



Transverse wake potential for 1 mm bunch



# Effect of longitudinal wake



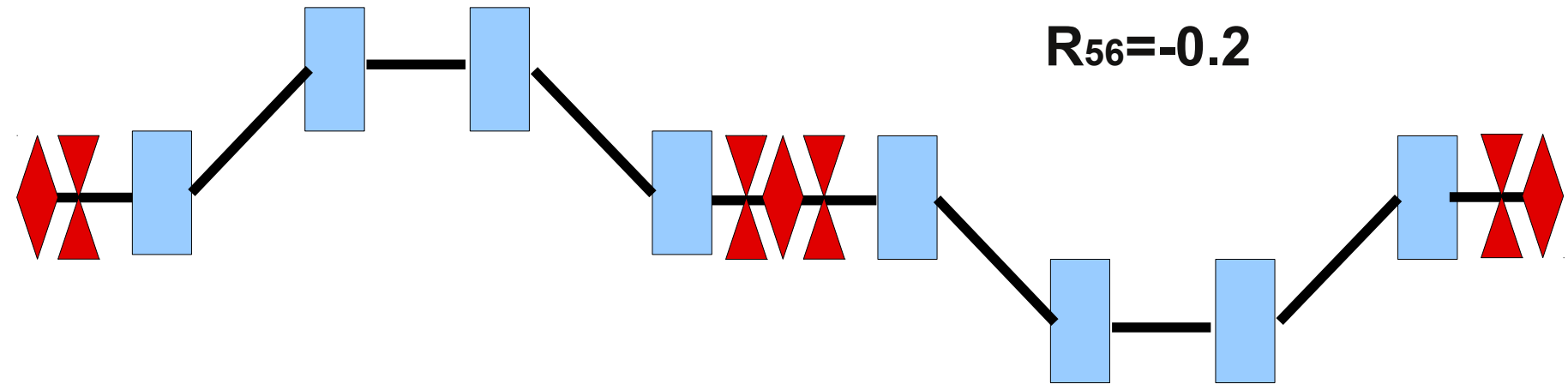
$$\Delta E = - \int_{-\infty}^{\infty} \rho(z) V_{\parallel}(z)$$

Trailing particles loses energy due to wake field generated leading particles

This case generated large energy spread

Solution is off-crest acceleration

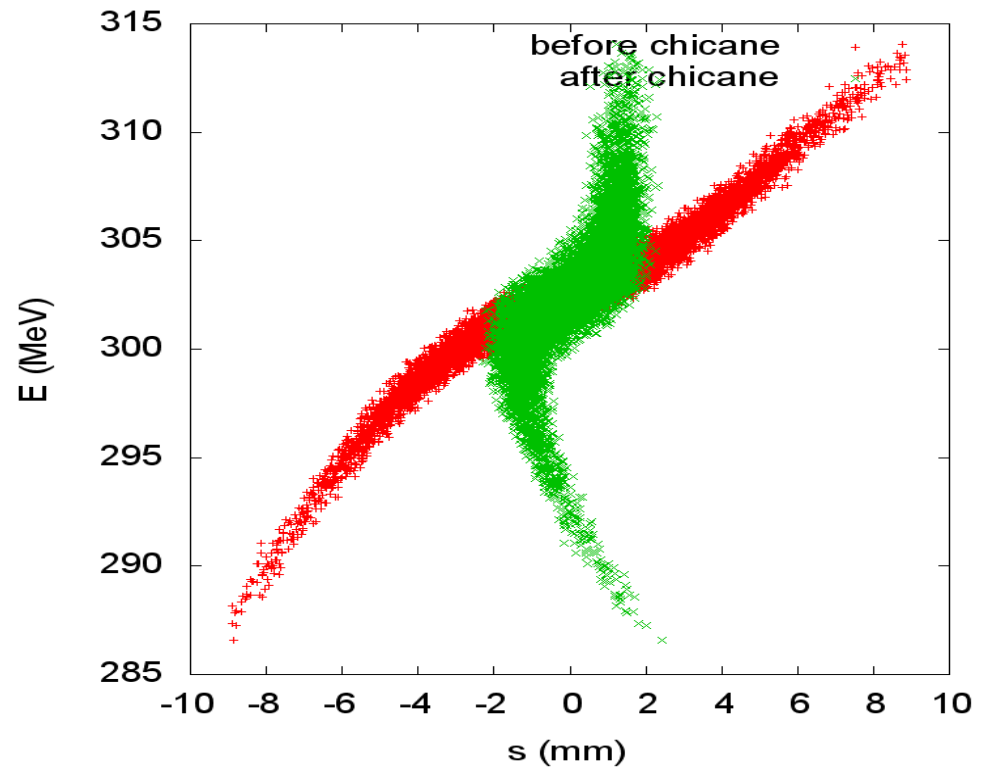
# CHICANE



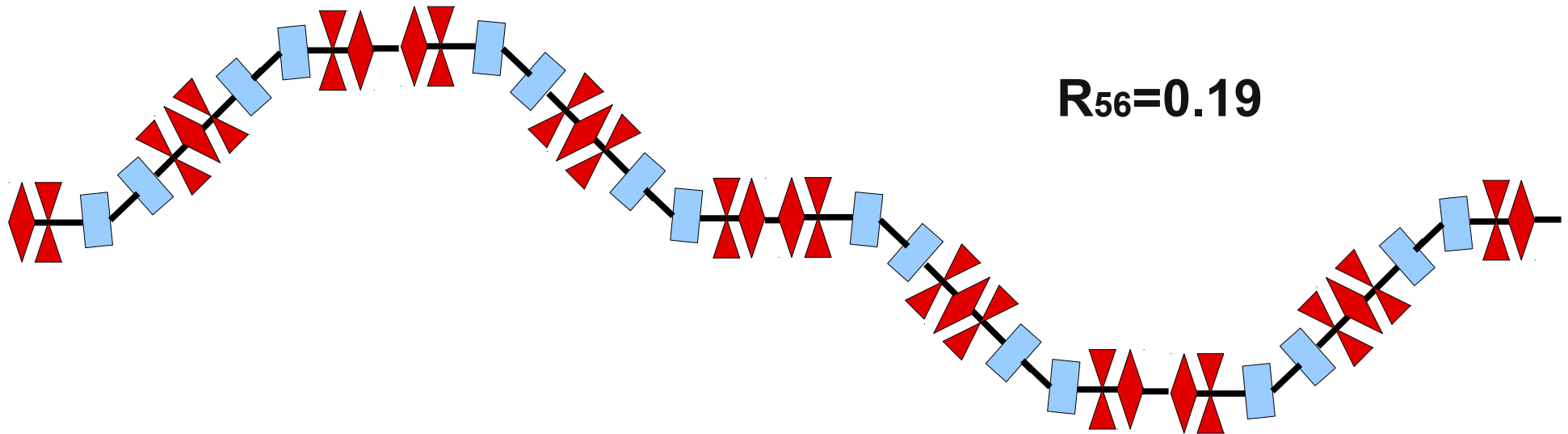
**Chicane located at 300 MeV**

**DBL1 off-crest 18 degree**

**No of accelerator in DB1  
76**



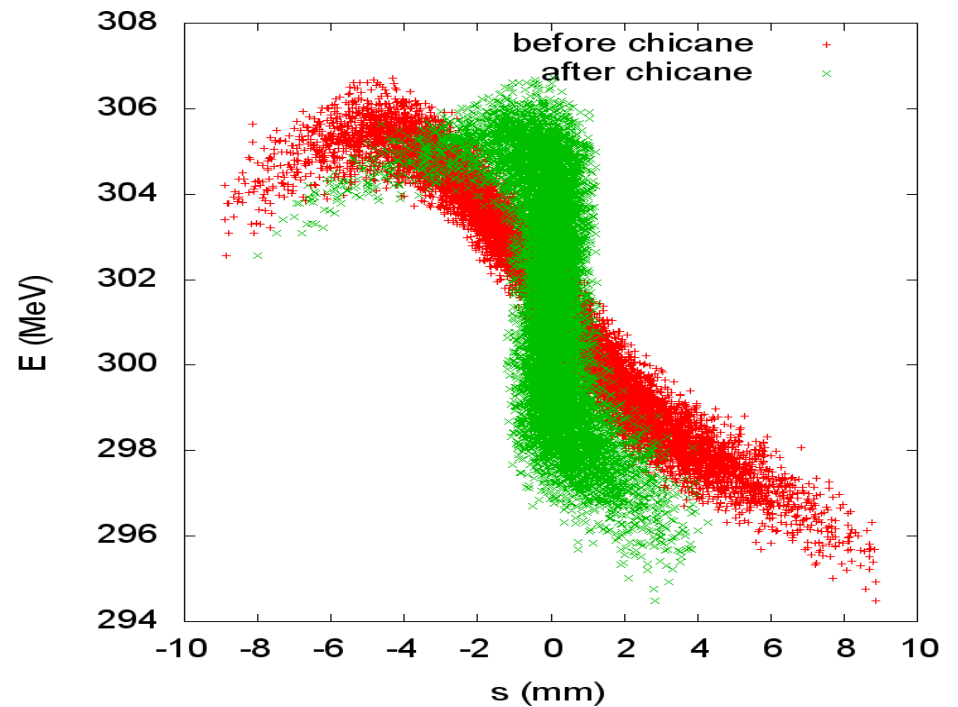
# Positive $R_{56}$



**Compressor located at 300 MeV**

**DBL1 linac off-crest -2 degree**

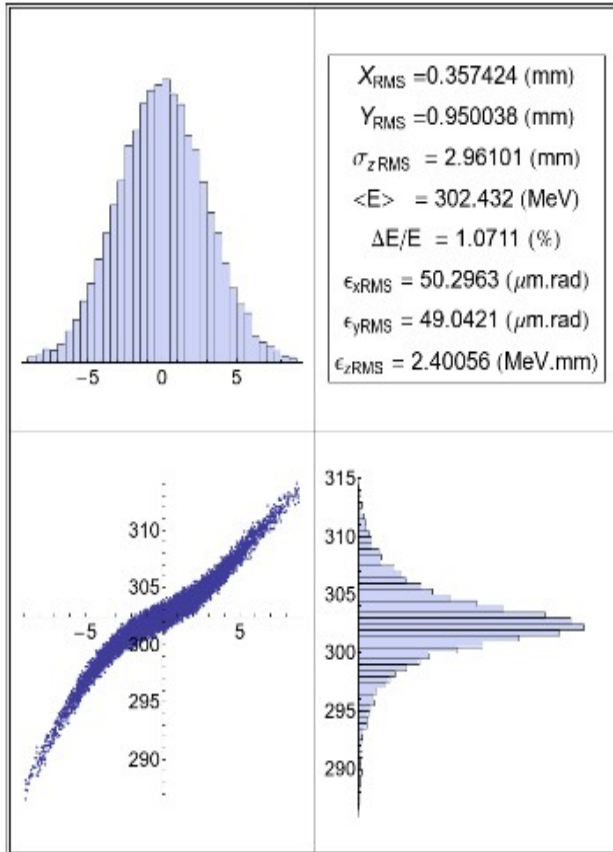
**No of accelerator in DB1**  
**72**



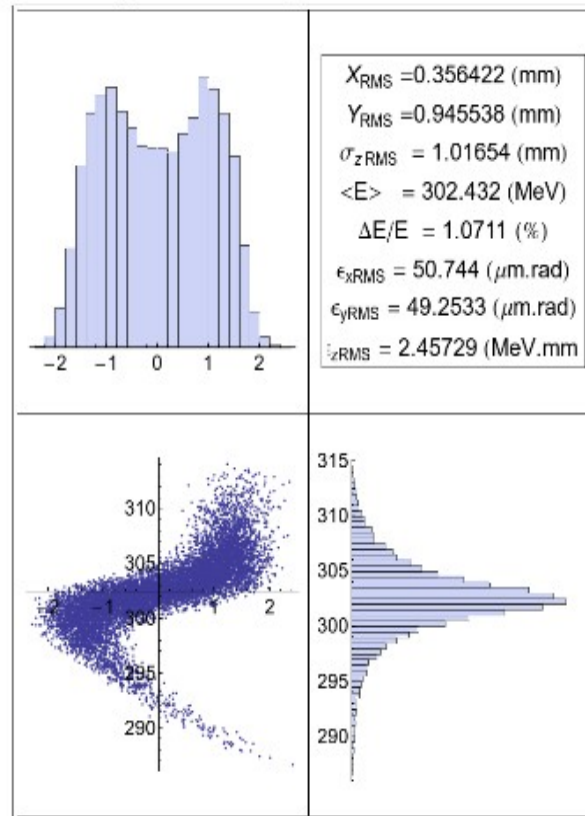


# Results for Chicane

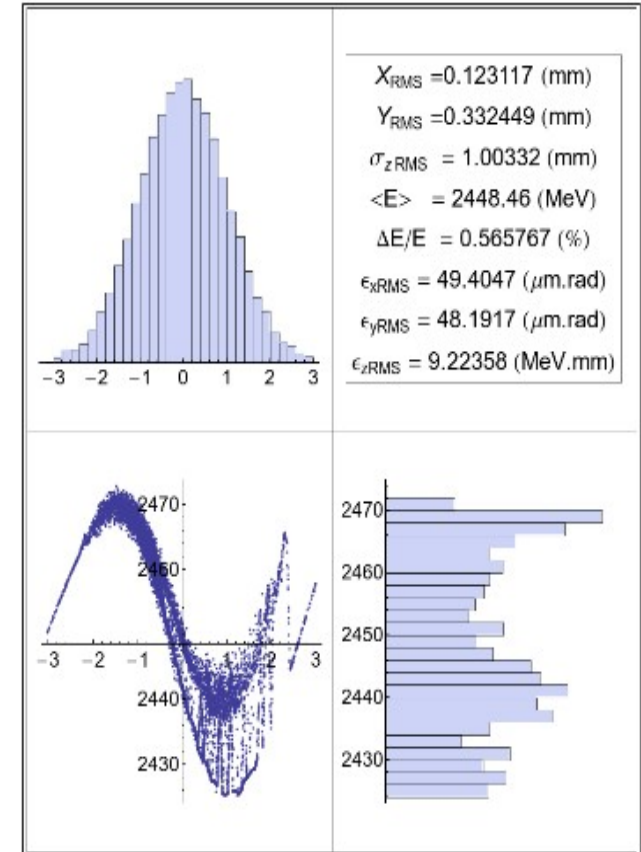
Longitudinal Phase plot at the end of DB1



Longitudinal Phase plot at the end of chicane



Longitudinal Phase plot at the end of DB2



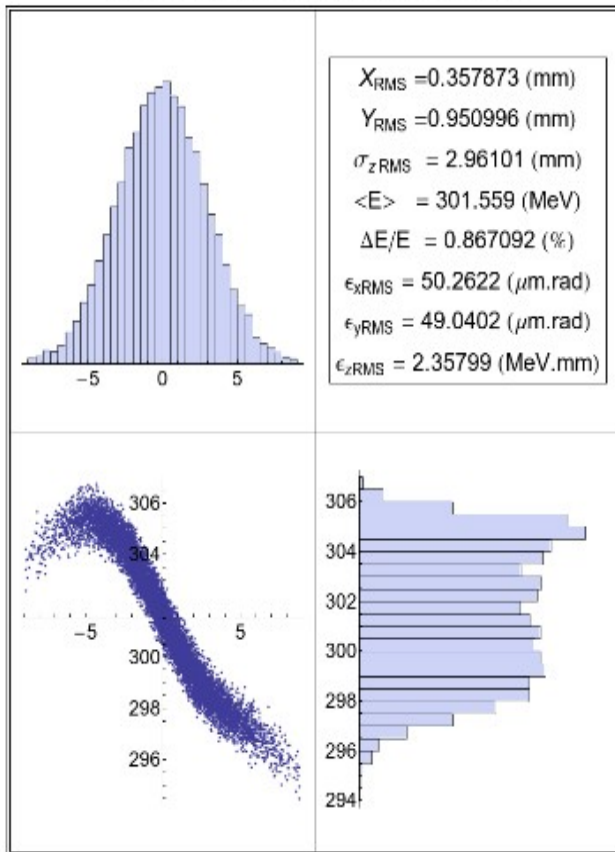
**No of structure: 76**  
**Phase : 18**

**No of structure: 654**  
**Phase: 19**

**Total structure : 730**

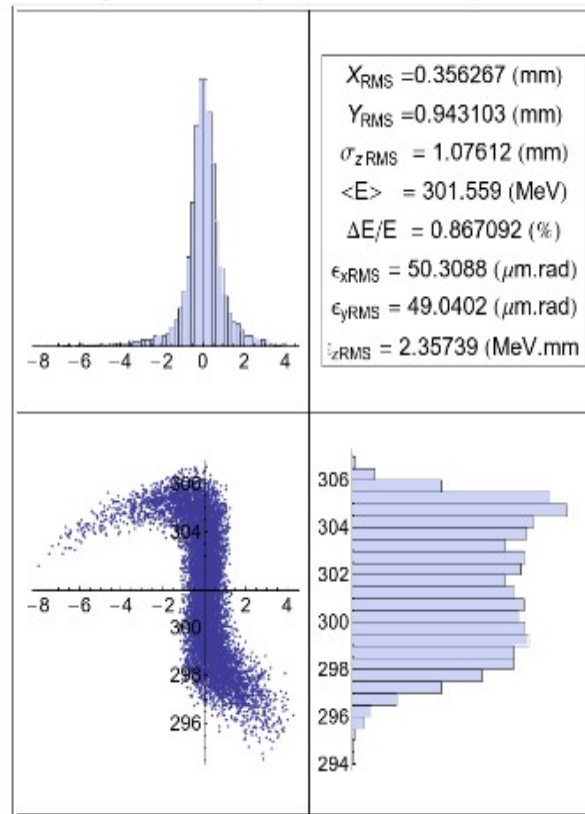
# Results for positive $R_{56}$ compressor

Longitudinal Phase plot at the end of DB1



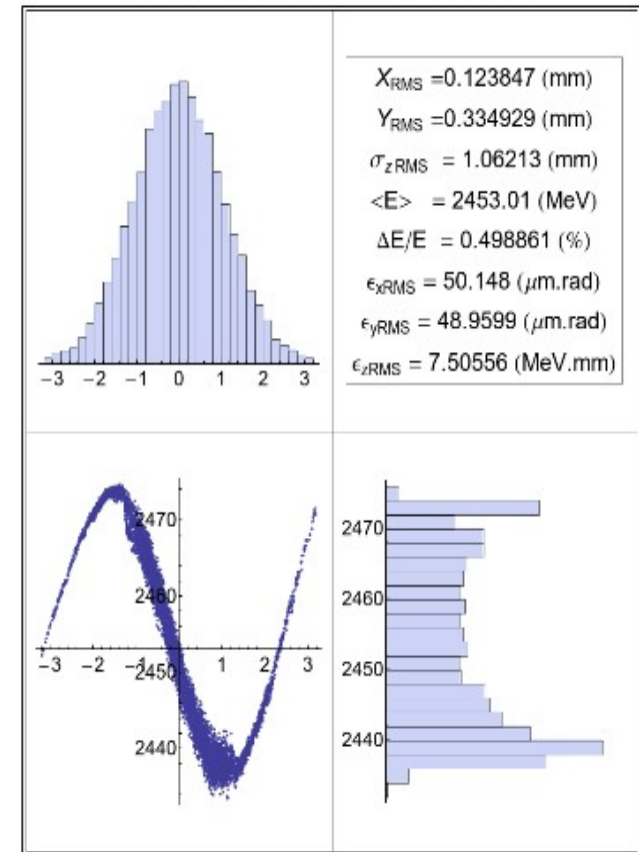
No of structure: 72  
Phase : -2

Longitudinal Phase plot at the end of compression



Total structure : 726

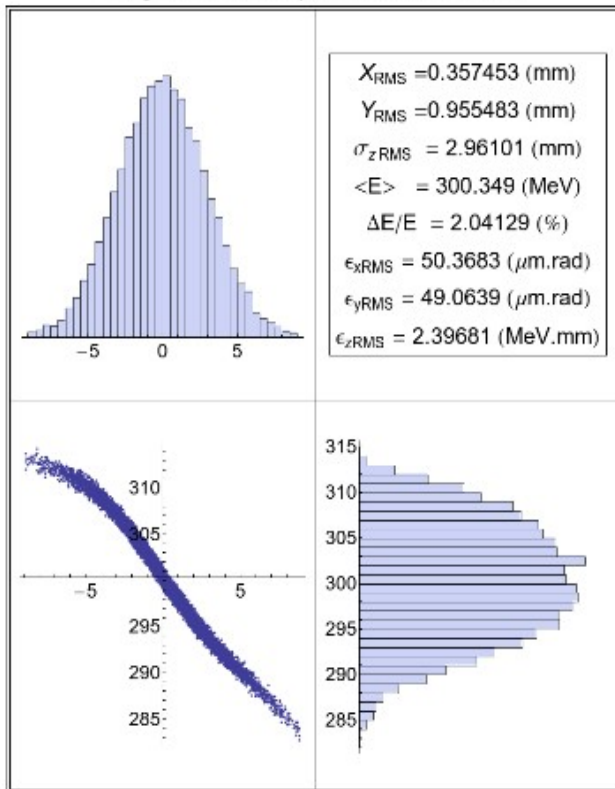
Longitudinal Phase plot at the end of DB2



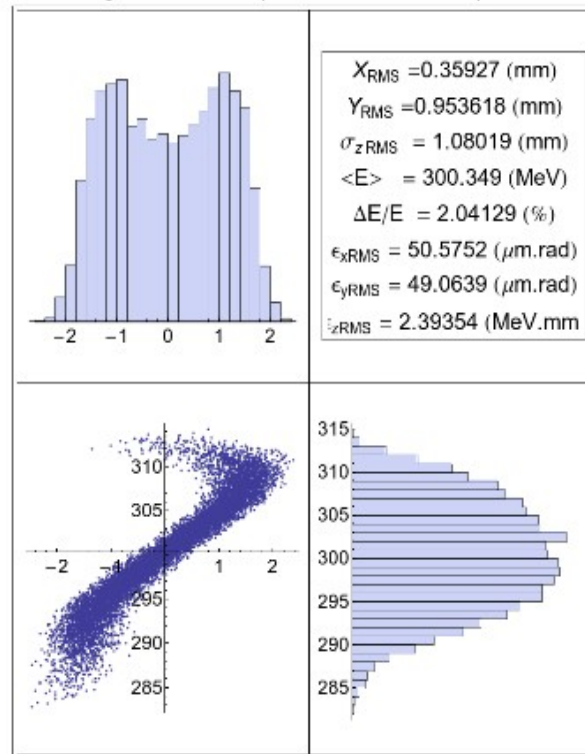
No of structure: 654  
Phase: 19

# Results for positive $R_{56}$ compressor 2

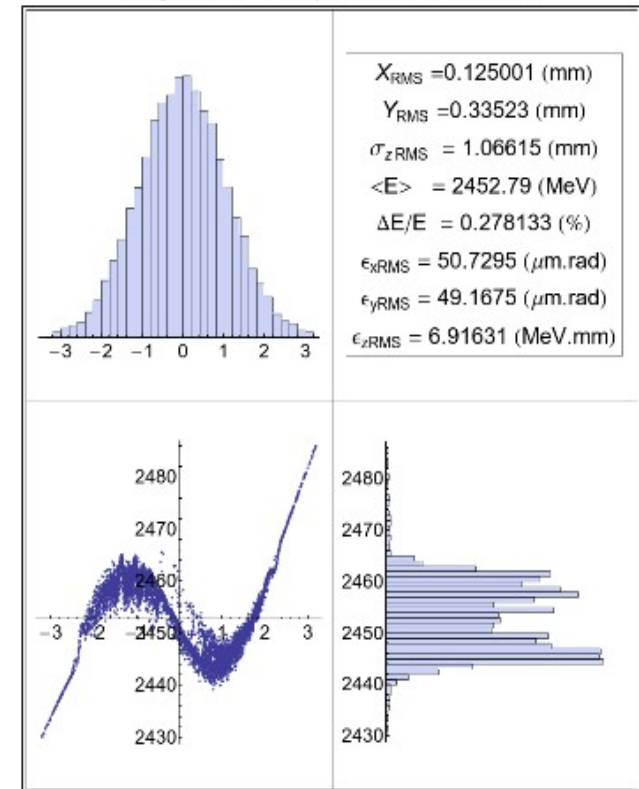
Longitudinal Phase plot at the end of DBL1



Longitudinal Phase plot at the end of compressor



Longitudinal Phase plot at the end of DBL2



**No of structure: 74**  
**Phase : - 14.5**

**No of structure: 654**  
**Phase: 19**

**Total structure : 728**

<b>BEAM PARAMETERS FOR DIFFERENT ACCELERATING STRUCTURES</b>							
<b>ACCELERATOR</b>	Input RF power (MW)	10.00	10.00	12.50	12.50	15.00	15.00
	No of acc cell	11	14	16	17	18	19
	Beam Pipe Radius (mm)	41.00	47.00	47.00	49.00	47.00	49.00
	Accel length with edge (m)	1.20	1.50	1.70	1.80	1.90	2.00
	Accel gradient per struc (MeV)	2.3753	2.3753	2.9691	2.9691	3.56	3.5629
	Accel gradient (MeV/m)	2.15	1.69	1.85	1.74	1.98	1.87
	RF phase of DBL1 (deg)	19	19	19	19	19	19
	RF phase of DBL2 (deg)	25	25	25	25	25	25
<b>DBL1 SECTION</b>	Quad strength (1/m <sup>2</sup> )	2.70	2.65	2.70	2.75	2.75	2.75
	Quad length (m)	0.25	0.23	0.21	0.20	0.19	0.18
	One FODO cell length (m)	4.70	5.26	5.62	5.80	5.98	6.16
	Number of accel used in DBL1	92	92	74	74	62	62
	Length of DBL1 (m)	216.32	242.07	208.04	214.7	185.47	191.05
<b>B at DBL1 end</b>	Rms bunch length (um)	2961.00	2961.00	961.00	2961.00	2961	2961.00
	Average energy (GeV)	0.2519	0.2520	0.2534	0.2535	0.25	0.2547
	Rms energy spread (%)	1.0550	1.0606	1.0972	1.1106	1.11	1.1295
	Rms energy width (MeV)	2.6577	2.6728	2.7799	2.8149	2.834	2.8770
<b>CHICANE</b>	Chicane bending angle (deg)	5.5000	5.5000	5.5000	5.5000	5.500	5.5000
	Number of hicane used	4	4	4	4	4	4
	Length of one one chicane (m)	7.3253	7.3253	7.3253	7.3253	7.325	7.325
	Total length of chicane section (m)	48.8511	48.8311	48.8111	49.2011	49.59	50.131
<b>B at CHI end</b>	Rms bunch length (um)	1107.54	1091.72	1013.69	986.06	979.10	947.39
	Average energy (GeV)	0.2519	0.2520	0.2534	0.2535	0.254	0.2547
	Rms energy spread (%)	1.0550	1.0606	1.0972	1.1106	1.113	1.1295
	Rms energy width (MeV)	2.6577	2.6728	2.7799	2.8149	2.834	2.8770
<b>DBL2 SECTION</b>	Number of accel used in DBL2	1046	1046	836	836	698	698
	Length of DBL2 (m)	2458.2250	2751.095	2349.265	2424.50	2087.1	2149.93
	Total number of accel used DBL1&DBL2	1138	1138	910	910	760	760
	Total bealine length (m)	2723.4011	3042.0011	2606.1211	2688.401	2322.1	2391.1
<b>B at DBL2 end</b>	Rms bunch ength (um)	1107.54	1091.72	1013.69	986.06	979.10	947.39
	Average energy (GeV)	2.4384	2.4400	2.4429	2.4442	2.450	2.4523
	Rms energy spread (%)	0.4641	0.4473	0.4370	0.4340	0.416	0.4122
	Rms energy width (MeV)	11.3167	10.9139	10.6753	10.6069	10.20	10.109
<b>INTEGRATION ALL LINAC</b>							
	$\int_{(0 \rightarrow L)} \text{Beta}_x(s)/E(s) \text{ (m/MeV)}$	7.0918	10.1608	9.9004	10.9121	9.96	10.89
	$\int_{(0 \rightarrow L)} \text{Beta}_y(s)/E(s) \text{ (m/MeV)}$	7.0907	10.1566	9.8999	10.9107	9.96	10.89