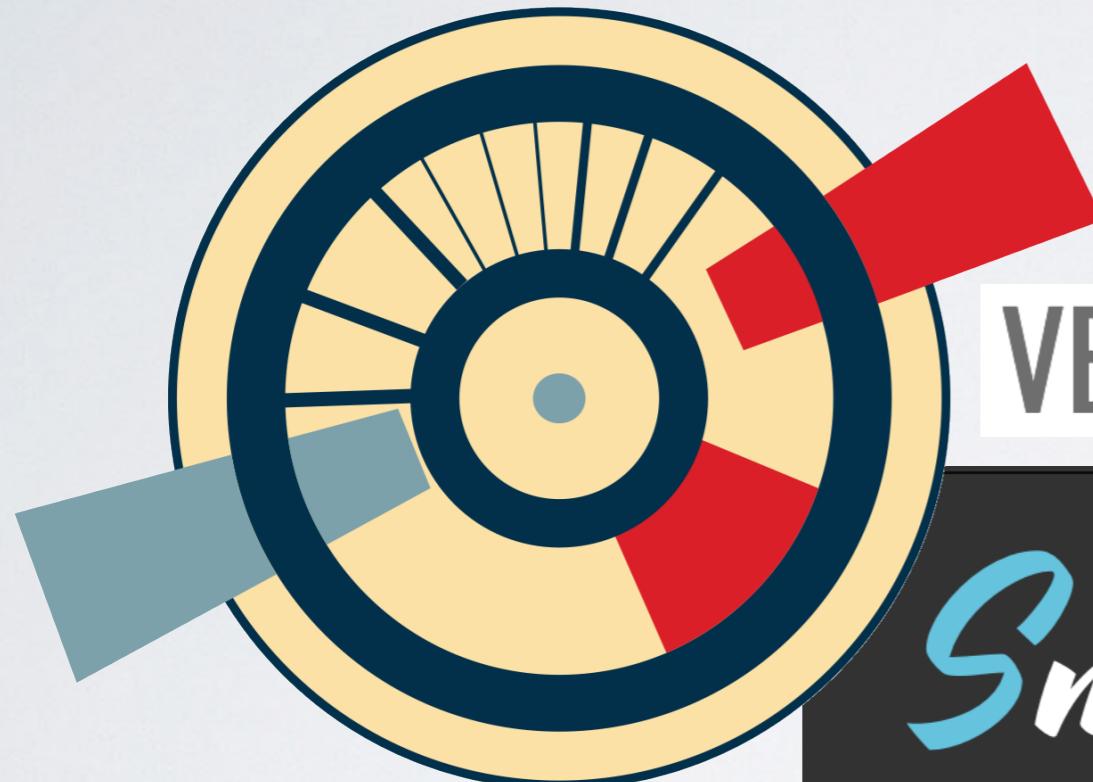


Vector Boson Scattering at Electron Colliders



VBSCan COST Network



SnowMass2021



Jürgen R. Reuter, DESY

HELMHOLTZ
RESEARCH FOR GRAND CHALLENGES



J.R.Reuter

VBS at e^+e^- colliders |

VBS to Snowmass Virtual Meeting, 29.01.21

Motivation for Vector Boson Scattering

Physics potential of Vector Boson Scattering:

1. Precision test of the electroweak SM at high energies
2. The Higgs Mechanism at work
3. Non-standard Higgs couplings
4. New Higgs-sector physics: the Higgs Portal
 - ▶ Extra Higgses
 - ▶ Resonances excited by VBF
 - ▶ Strong interactions, continuum, compositeness, top quarks
 - ▶ New final states (Dark Matter ?)

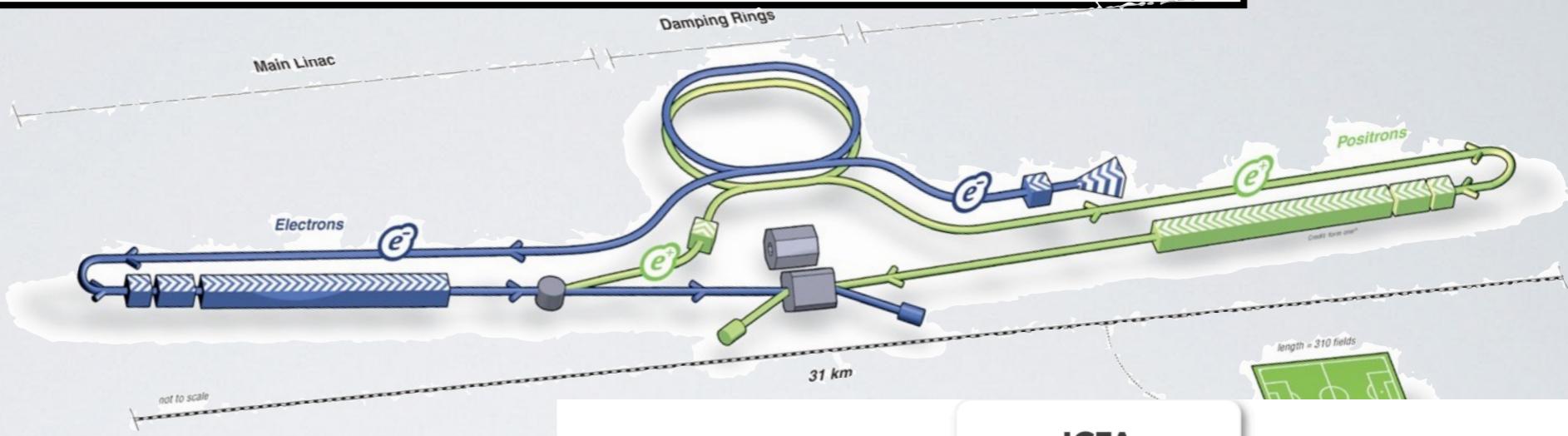
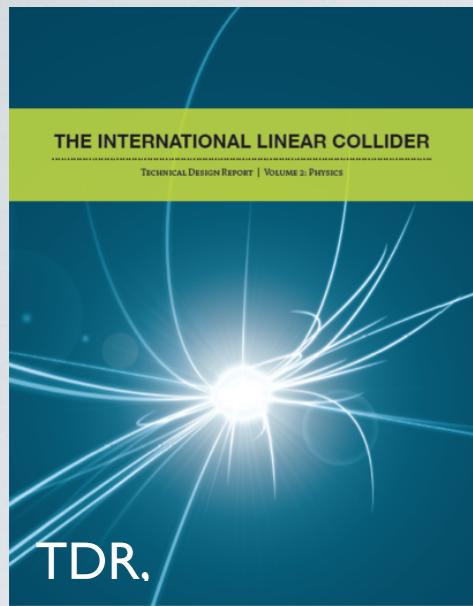
Requirements / Benefits at High-Energy Electron colliders $s \gtrsim 1 \text{ TeV}^2$

1. High energy: $s \gtrsim 1 \text{ TeV}^2$
2. Well-defined initial state: electroweak production (small theory errors)
3. High precision, triggerless operation: complete coverage of final states
4. Separation of spin, isospin, CP quantum number
5. Discriminating power even on (some) light quark flavors



ILC — 0.250–1 TeV e^+e^- Collider

Main Linac



ILC International Development Team



Executive Board

Americas Liaison	Andrew Lankford (UC Irvine)
Working Group 2 Chair	Shinichiro Michizono (KEK)
Working Group 3 Chair	Hitoshi Murayama (UC Berkeley/U. Tokyo)
Executive Board Chair and Working Group 1 Chair	Tatsuya Nakada (EPFL)
KEK Liaison	Yasuhiro Okada (KEK)
Europe Liaison	Steinar Stapnes (CERN)
Asia-Pacific Liaison	Geoffrey Taylor (U. Melbourne)

Working Group 1
Pre-Lab Setup

Working Group 2
Accelerator

Working Group 3
Physics & Detectors

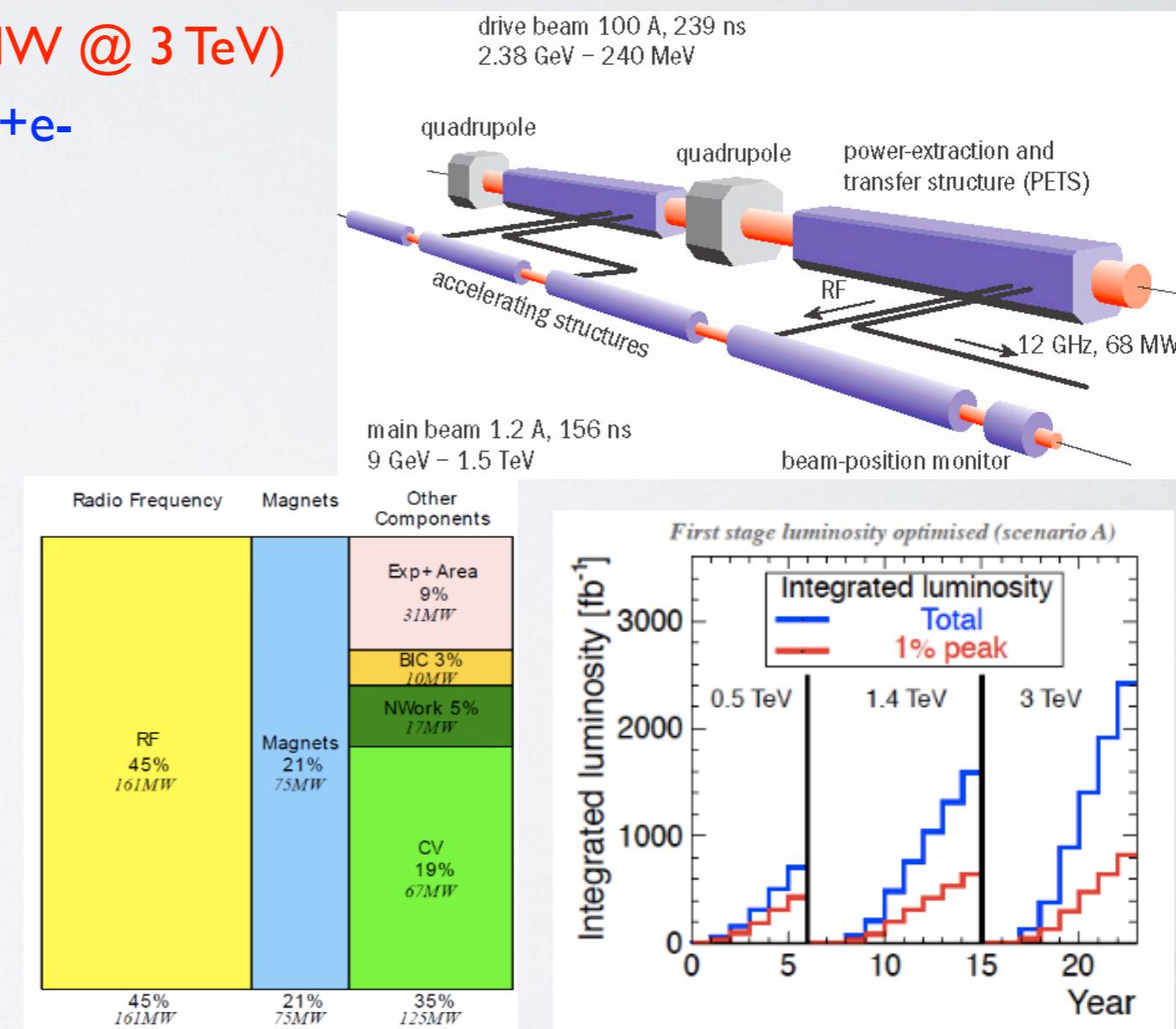
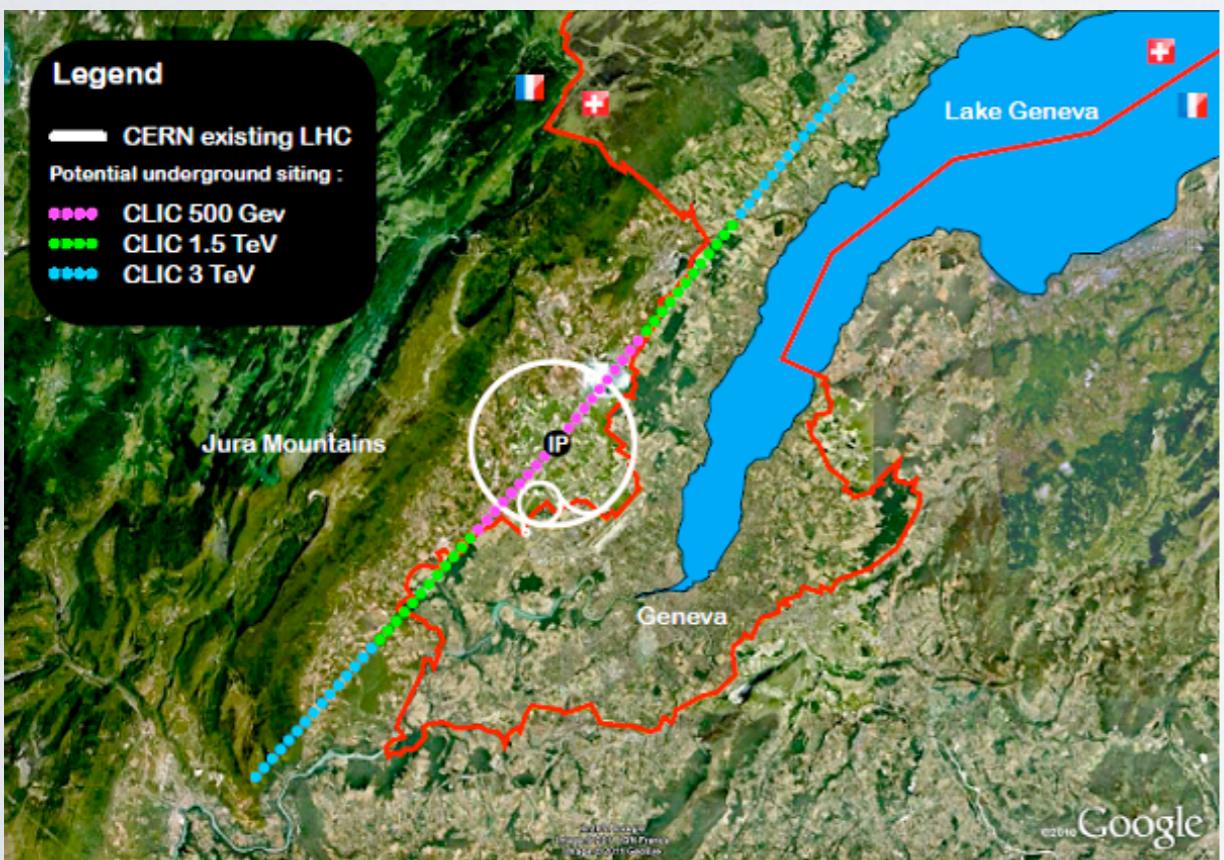
- e^+e^- collider, 20.5–31 km length, **c.m. energy: 250–500 GeV (tunable)** [Upgrade: 1 TeV]
- Based on superconducting RF cavities (31.5 MV/m design, 35 MV/m goal, 41–45 MV/m max.)
- Two detectors/experiments **ILD & SiD** (shared interaction point)
- Japan to start pre-lab phase 2022
- Deliverable: Engineering Design Report (EDR)



CLIC — 1.5–3 TeV e⁺e⁻ Collider



- Normalconducting RF cavities: drive beam with ca. 100 MV/m
- Conceptual Design Report (CDR): [01/2012]
- Linear tunnel of ca. 30-50 km at CERN
- staged approach: .38, 1.5, 3 TeV
- Main challenge I: large scale test facility → CLEAR 0.22 GeV
- Main challenge II: power consumption (590 MW @ 3 TeV)
- Only presently feasible multi-TeV option for e⁺e⁻



Setup of ILC / CLIC

(HE-)ILC: energies & staging

- [$E_1 = 0.25 \text{ TeV}$, $\mathcal{L}_{\text{int}} = 2,000 \text{ fb}^{-1}$]
- [$E_2 = 0.35 \text{ TeV}$, $\mathcal{L}_{\text{int}} = 200 \text{ fb}^{-1}$]
- : $E_3 = 0.5 \text{ TeV}$, $\mathcal{L}_{\text{int}} = 4,000 \text{ fb}^{-1}$:
- $E_4 = 1.0 \text{ TeV}$, $\mathcal{L}_{\text{int}} = 8,000 \text{ fb}^{-1}$

Initial state polarization: 80% e^- , $\geq 30\%$ e^+

CLIC: energies & staging

- [$E_1 = 0.35/0.38 \text{ TeV}$, $\mathcal{L}_{\text{int}} = 100+500 \text{ fb}^{-1}$]
- $E_2 = 1.5 \text{ TeV}$, $\mathcal{L}_{\text{int}} = 1,500 \text{ fb}^{-1}$
- $E_3 = 3.0 \text{ TeV}$, $\mathcal{L}_{\text{int}} = 5,000 \text{ fb}^{-1}$

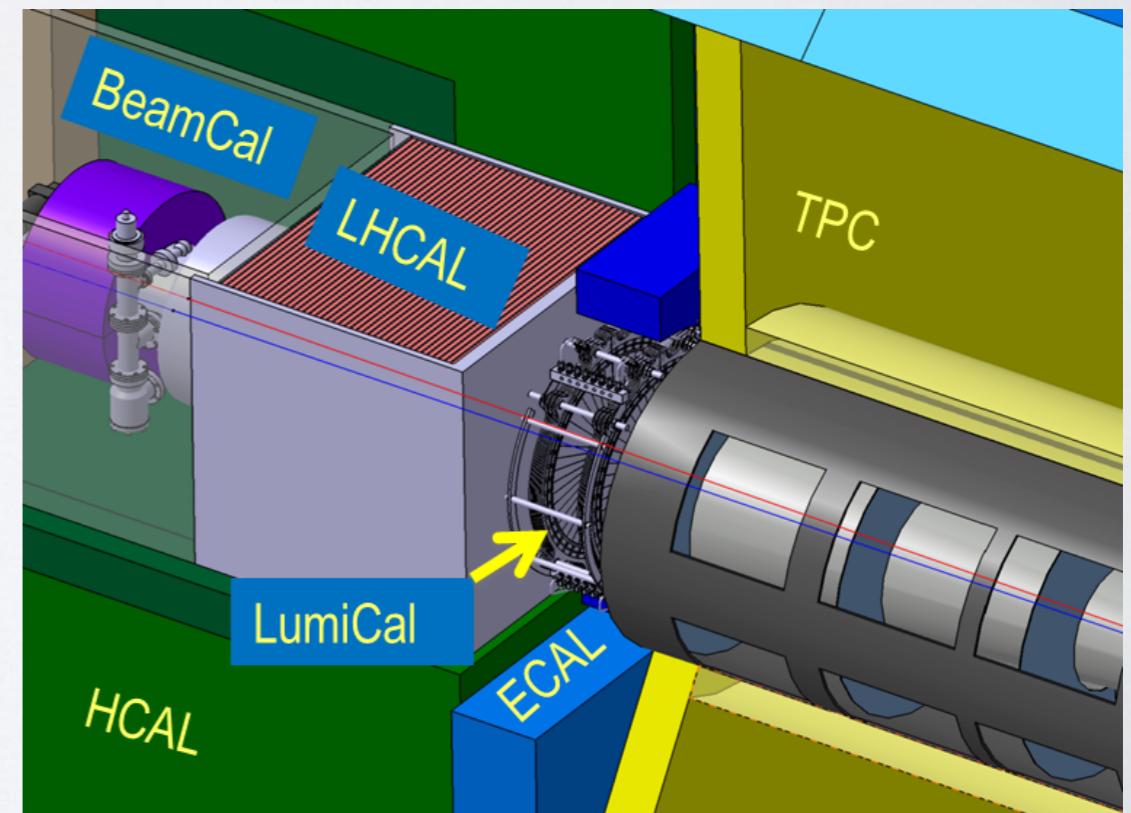
Initial state polarization: 80% e^- , 0% e^+

Low angle coverage

M. Idzik: A.Phys. Pol. B46 (2015) 1297

- LumiCal: 38 — 110 mrad
- BeamCal: 15 — 38 mrad

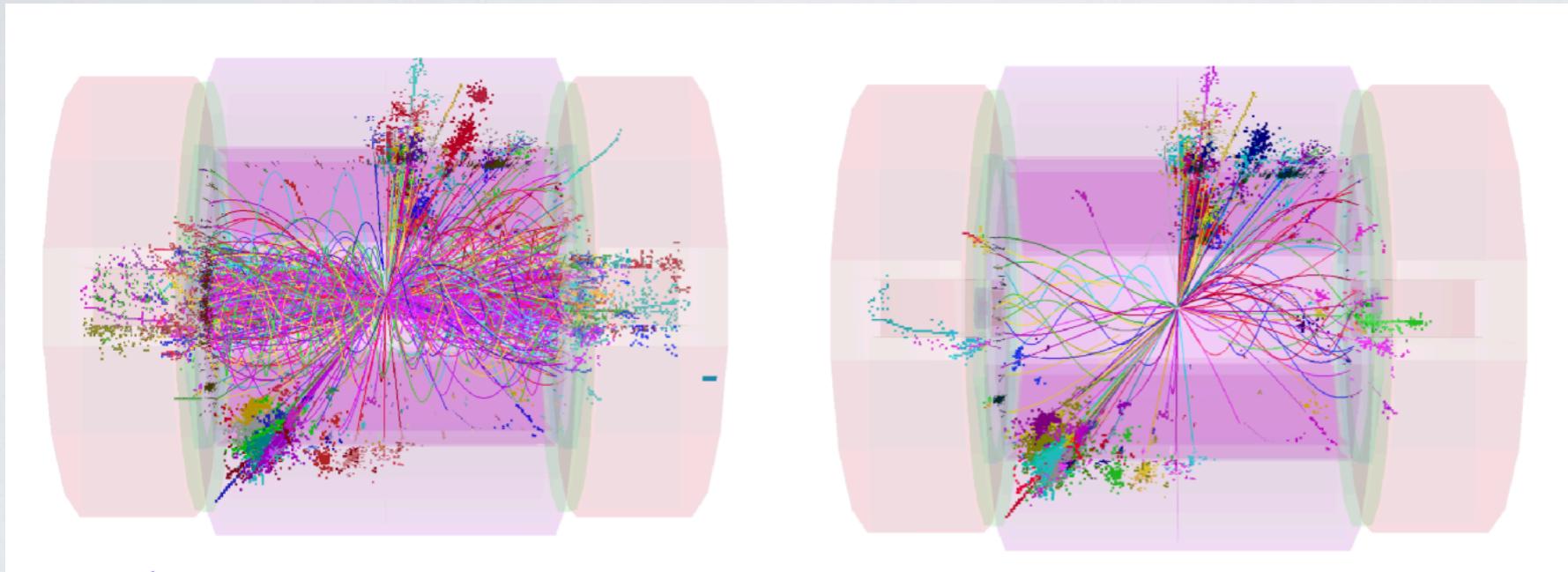
can go down to 15 mrad, i.e. $\eta \approx 4.9$



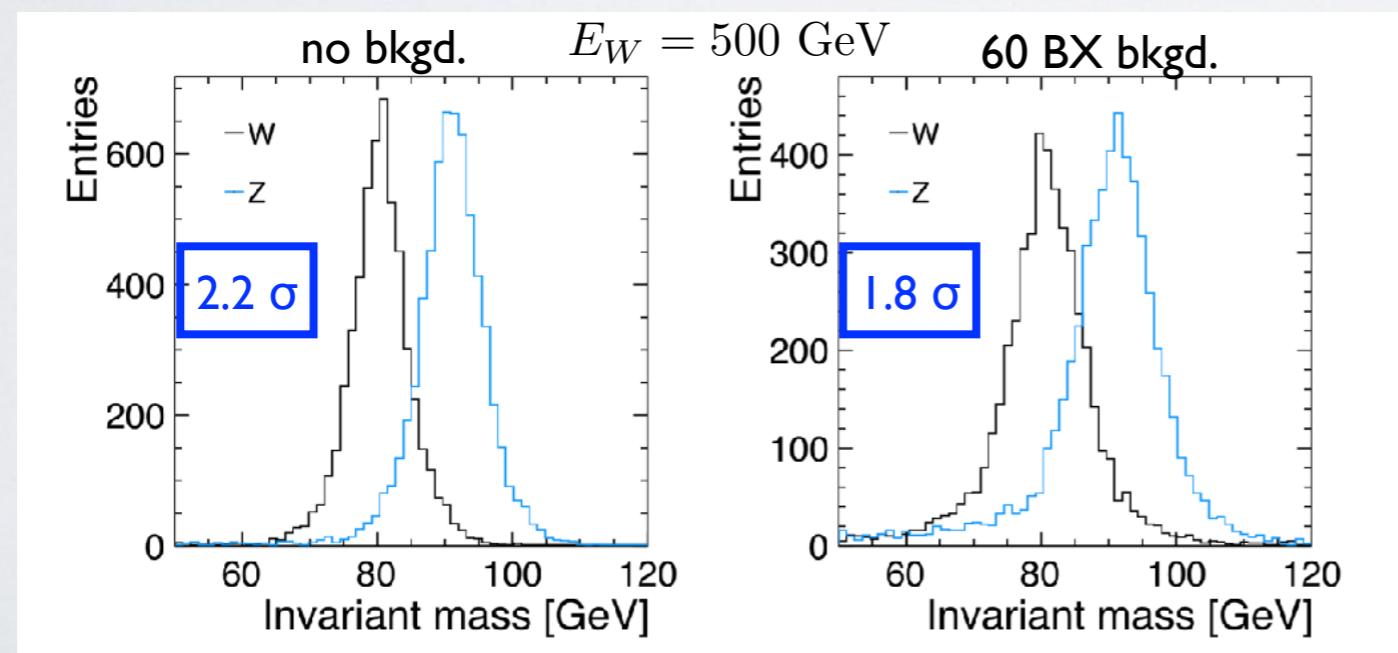
Identification of hadronic W / Z

J.S. Marshall / A. Münnich / M.A.Thomson , arXiv: 1209.4039

Particle Flow Algorithm (PFA) allows very good particle ID for ILD detector



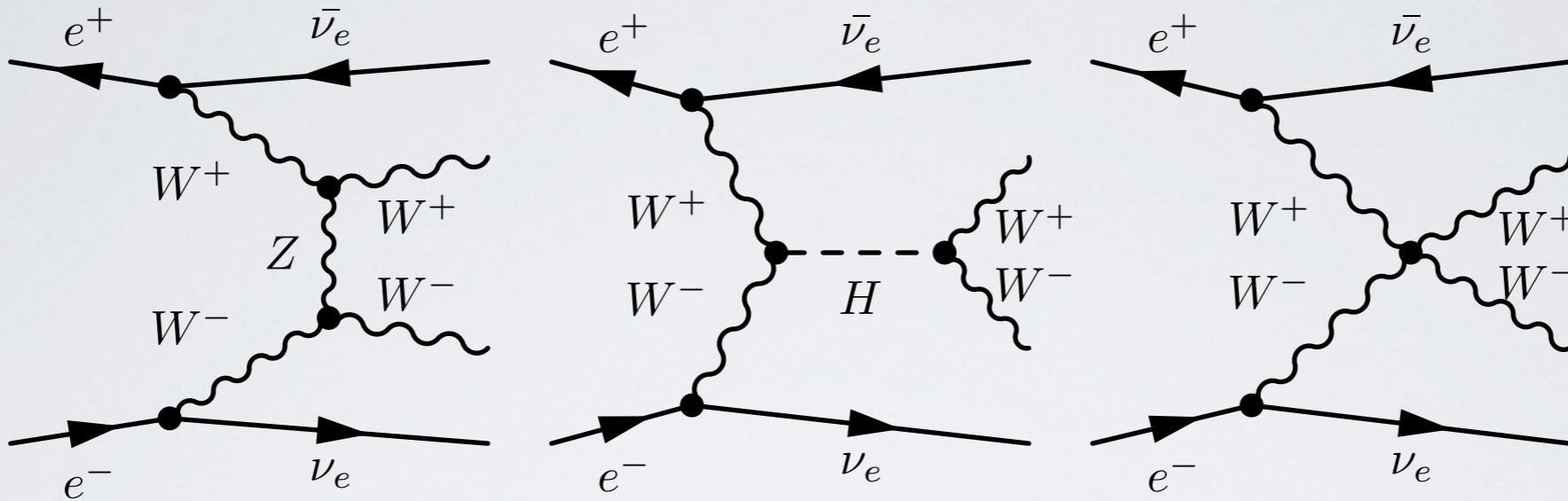
Tight PF0 removes photon-induced background from 1.2 TeV to 100 GeV



- ▶ W/Z discrimination: 88% efficiency
- ▶ With γ -induced bkgd: 71 — 79 %

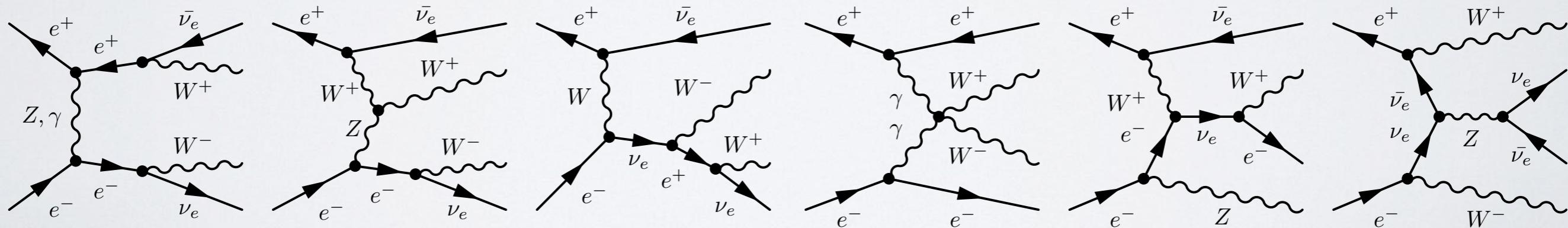
Vector Boson Scattering in $e^+ e^-$

Signal process: triple gauge couplings, Higgs-V-V couplings, quartic gauge couplings



same for WZ and ZZ , using all W/Z decays, particularly $W/Z \rightarrow jj$

Background: di fermions with EW radiation, single W, tribosons, radiative dibosons etc.



(Non-exhaustive) Literatur: VBS in $e^+ e^-$ / $e^- e^-$

- Gunion/Tofighi-Niaki, PRD36 (1987) 2671: full MEs for VBS (WW) and heavy Higgs production [0.5, 1, 2 TeV]
- Gunion/Tofighi-Niaki, PRD38 (1988) 1433: same for ZZ final states [0.5, 1, 2 TeV]
- Barger/Cheung/Han/Phillips, PRD52 (1995) 3815: measurements of WW/ZZ ratios [1.5 – 2 TeV]
- Dominici, Riv.Nuo.Cim.20 (1997) 1: access to parameters of EW chiral Lagrangian in WW VBS [1.5 TeV]
- Denner/Dittmaier/Hahn, PRD56 (1997) 117: EW corrections to $ZZ \rightarrow ZZ$
- Denner/Hahn, NPB525 (1998) 27: EW corrections to $WW \rightarrow WW$
- Han/He/Yuan, PLB422 (1998) 294: interplay of WW VBS and WWZ/ZZZ production [0.5, 0.8, 1, 1.6 TeV]
- Boos/He/Kilian/Pukhov/Yuan/Zerwas, PRD57 (1998) 1553: EW chiral Lagrangian (strong EW) [1.6 TeV]
- Boos/He/Kilian/Pukhov/Yuan/Zerwas, PRD61 (2000) 077901: strong EW: ZZ/W⁻W⁻ channels [1.6 TeV]
- Kilian, Int.J.Mod.Phys.A15 (2000) 2387: strong EW in e^-e^- [1 TeV]
- Linear Collider Physics Ressource Book 2001, Part 3: Studies of Exotic and SM Physics [hep-ex/0106057]
- Chierici/Rosati/Kobel, LC-PHSM-2001-038 : experimental study for strong EW [0.18–0.8 TeV]
- Rosati, CERN-THESIS-2002-083 : experimental study for strong EW [0.18–0.8 TeV]
- Beyer/Kilian/Krstonošić/Mönig/JRR/Schmidt/Schröder, EPJC48 (2006) 353: a parameters, VBS+VVV [1 TeV]
- Accomando/Denner/Pozzorini, JHEP 0703 (2007) 078: EW Sudakov logarithms in VBS [3 TeV]
- Liebler/Moortgat-Pick/Weiglein, JHEP 1506 (2015) 093: Off-shell Higgs effects in $ee \rightarrow vvVV$ [0.25 – 1 TeV]
- Fleper/Kilian/JRR/Sekulla, EPJC77.2 (2017) 120: VBS for SMEFT with dim 8 / simplified models [1, 1.4, 3 TeV]

VBS in $e^+ e^-$: SM rates and Backgrounds (I)

Experimentally: study all processes that lead to VBS-like signatures [1 TeV]:

Vector-Boson Scattering

Triboson Production

Vector-Boson Scattering / Radiative Bhabha

Top [pair] production

Diboson Production

Single W Production

Radiative Z Production

QCD Di-/Multijets

Process	Subprocess	σ [fb]
$e^+ e^- \rightarrow \nu_e \bar{\nu}_e q \bar{q} q \bar{q}$	$W^+ W^- \rightarrow W^+ W^-$	23.19
$e^+ e^- \rightarrow \nu_e \bar{\nu}_e q \bar{q} q \bar{q}$	$W^+ W^- \rightarrow ZZ$	7.624
$e^+ e^- \rightarrow \nu \bar{\nu} q \bar{q} q \bar{q}$	$V \rightarrow VVV$	9.344
$e^+ e^- \rightarrow \nu e q \bar{q} q \bar{q}$	$WZ \rightarrow WZ$	132.3
$e^+ e^- \rightarrow e^+ e^- q \bar{q} q \bar{q}$	$ZZ \rightarrow ZZ$	2.09
$e^+ e^- \rightarrow e^+ e^- q \bar{q} q \bar{q}$	$ZZ \rightarrow W^+ W^-$	414.
$e^+ e^- \rightarrow b b X$	$e^+ e^- \rightarrow t \bar{t}$	331.768
$e^+ e^- \rightarrow q \bar{q} q \bar{q}$	$e^+ e^- \rightarrow W^+ W^-$	3560.108
$e^+ e^- \rightarrow q \bar{q} q \bar{q}$	$e^+ e^- \rightarrow ZZ$	173.221
$e^+ e^- \rightarrow e \nu q \bar{q}$	$e^+ e^- \rightarrow e \nu W$	279.588
$e^+ e^- \rightarrow e^+ e^- q \bar{q}$	$e^+ e^- \rightarrow e^+ e^- Z$	134.935
$e^+ e^- \rightarrow X$	$e^+ e^- \rightarrow q \bar{q}$	1637.405

[80% e^- , 40% e^+ polarization]

[Beyer/Kilian/Krstonošić/Mönig/JRR/Schmidt/Schröder, EPJC48 (2006) 353]

VBS in $e^+ e^-$: SM rates and Backgrounds (II)

Process	1400 GeV	3000 GeV	Factor	Total cross sections [fb], no cuts
$W^+ W^- \nu \bar{\nu}$	47.1	132	1	
$W^+ W^- e^+ e^-$	1570	3820	1	
$W^\pm Z e^\mp \nu$	138	408	0.136	
$Z Z e^+ e^-$	3.78	4.70	0.019	
$W^+ W^- (Z \rightarrow \nu \bar{\nu})$	11.7	9.35	1	
$Z Z \nu \bar{\nu}$	15.7	57.5	1	
$Z Z e^+ e^-$	3.78	4.70	1	
$W^\pm Z e^\mp \nu$	138	408	0.136	
$W^+ W^- e^+ e^-$	1570	3820	0.019	
$Z Z (Z \rightarrow \nu \bar{\nu})$	0.484	0.237	1	

[80% e^- , 0% e^+ polarization]

Fleper/Kilian/JRR/Sekulla: 1607.03030

- Signal cross sections rise factor 3–4 from 1.4 to 3 TeV
- Mistagging from W/Z conversions in hadronic bosons: severe for WZ scattering
- Irreducible backgrounds from tribosons (Gauge invariance connects full processes)

VBS in $e^+ e^-$: Selection / isolation cuts

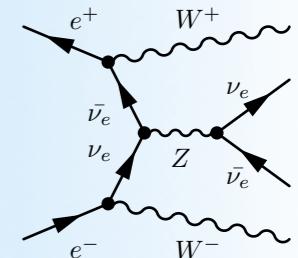
Cuts for 1 TeV ILC — 1.4 TeV CLIC — 3 TeV CLIC

> Suppression of background from $Z \rightarrow \nu\nu$, W^+W^- , and QCD 4-jet production

$$M_{inv}(\bar{\nu}\nu) > 150 \text{ GeV}$$

$$M_{inv}(\bar{\nu}\nu) > 175 \text{ GeV}$$

$$M_{inv}(\bar{\nu}\nu) > 230 \text{ GeV}$$



> Suppression of background from t-channel exchange in subprocess

$$p_{\perp,W/Z} > 150 \text{ GeV}$$

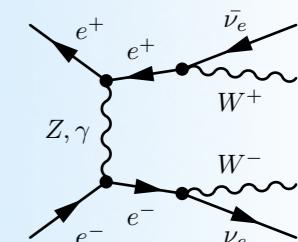
$$|\cos \theta(W/Z)| < 0.8$$

$$p_{\perp,W/Z} > 180 \text{ GeV}$$

$$|\cos \theta(W/Z)| < 0.8$$

$$p_{\perp,W/Z} > 300 \text{ GeV}$$

$$|\cos \theta(W/Z)| < 0.8$$



> Suppression of $\gamma\gamma$ -fusion induced backgrounds

$$p_{\perp}(WW) > 45 \text{ GeV}$$

$$p_{\perp}(ZZ) > 40 \text{ GeV}$$

$$\theta(e) > 15 \text{ mrad}$$

$$p_{\perp}(WW) > 50 \text{ GeV}$$

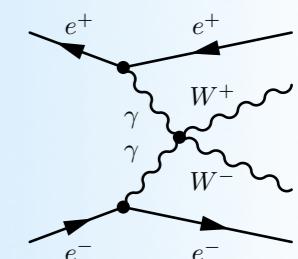
$$p_{\perp}(ZZ) > 40 \text{ GeV}$$

$$\theta(e) > 15 \text{ mrad}$$

$$p_{\perp}(WW) > 100 \text{ GeV}$$

$$p_{\perp}(ZZ) > 60 \text{ GeV}$$

$$\theta(e) > 15 \text{ mrad}$$



> Suppression of non-scattering vector boson processes [i.e. massive EW radiation]

$$M_{inv}^{WW} \in [575, 800] \text{ GeV}$$

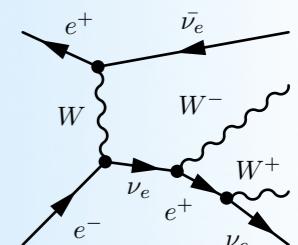
$$M_{inv}^{ZZ} \in [600, 800] \text{ GeV}$$

$$M_{inv}^{WW} \in [800, 1175] \text{ GeV}$$

$$M_{inv}^{ZZ} \in [800, 1175] \text{ GeV}$$

$$M_{inv}^{WW} \in [900, 1900] \text{ GeV}$$

$$M_{inv}^{ZZ} \in [850, 1900] \text{ GeV}$$



Deviations as EFT — Dim 8 Operators

Motivated by SMEFT:

$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i \left[\frac{c_i^{(5)}}{\Lambda} \mathcal{O}_i^{(5)} + \frac{c_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{(6)} + \frac{c_i^{(7)}}{\Lambda^3} \mathcal{O}_i^{(7)} + \boxed{\frac{c_i^{(8)}}{\Lambda^4} \mathcal{O}_i^{(8)}} + \dots \right]$$

Longitudinal operators

$$\mathcal{L}_{S,0} = F_{S,0} \text{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger (\mathbf{D}_\nu \mathbf{H}) \right] \text{tr} \left[(\mathbf{D}^\mu \mathbf{H})^\dagger (\mathbf{D}^\nu \mathbf{H}) \right]$$

$$\mathcal{L}_{S,1} = F_{S,1} \text{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger (\mathbf{D}^\mu \mathbf{H}) \right] \text{tr} \left[(\mathbf{D}_\nu \mathbf{H})^\dagger (\mathbf{D}^\nu \mathbf{H}) \right]$$

S. Weinberg, 1979

Buchmüller/Wyler, 1986

Grzadkowski/Iskrzynski/Misiak/Rosiek, 2010

Eboli/Gonzalez-Garcia/Mizukoshi, 2006

Alboteanu/Kilian/JRR, 2008

Kilian/Ohl/JRR/Sekulla, 2014

Transversal operators

Mixed operators

$$\mathcal{L}_{M,0} = -g^2 F_{M_0} \text{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger (\mathbf{D}^\mu \mathbf{H}) \right] \text{tr} \left[\mathbf{W}_{\nu\rho} \mathbf{W}^{\nu\rho} \right]$$

$$\mathcal{L}_{M,1} = -g^2 F_{M_1} \text{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger (\mathbf{D}^\rho \mathbf{H}) \right] \text{tr} \left[\mathbf{W}_{\nu\rho} \mathbf{W}^{\nu\rho} \right]$$

$$\mathcal{L}_{M,2} = -g'^2 F_{M_2} \text{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger (\mathbf{D}^\mu \mathbf{H}) \right] \text{tr} \left[\mathbf{B}_{\nu\rho} \mathbf{B}^{\nu\rho} \right]$$

$$\mathcal{L}_{M,3} = -g'^2 F_{M_3} \text{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger (\mathbf{D}^\rho \mathbf{H}) \right] \text{tr} \left[\mathbf{B}_{\nu\rho} \mathbf{B}^{\nu\rho} \right]$$

$$\mathcal{L}_{M,4} = -gg' F_{M_4} \text{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger \mathbf{W}_{\nu\rho} (\mathbf{D}^\mu \mathbf{H}) \mathbf{B}^{\nu\rho} \right],$$

$$\mathcal{L}_{M,5} = -gg' F_{M_5} \text{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger \mathbf{W}_{\nu\rho} (\mathbf{D}^\rho \mathbf{H}) \mathbf{B}^{\nu\rho} \right],$$

$$\mathcal{L}_{M,7} = -g^2 F_{M_7} \text{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger \mathbf{W}_{\nu\rho} \mathbf{W}^{\nu\rho} (\mathbf{D}^\rho \mathbf{H}) \right];$$

$$\mathcal{L}_{T,0} = g^4 F_{T_0} \text{tr} \left[\mathbf{W}_{\mu\nu} \mathbf{W}^{\mu\nu} \right] \text{tr} \left[\mathbf{W}_{\alpha\beta} \mathbf{W}^{\alpha\beta} \right],$$

$$\mathcal{L}_{T,1} = g^4 F_{T_1} \text{tr} \left[\mathbf{W}_{\alpha\nu} \mathbf{W}^{\mu\beta} \right] \text{tr} \left[\mathbf{W}_{\mu\beta} \mathbf{W}^{\alpha\nu} \right],$$

$$\mathcal{L}_{T,2} = g^4 F_{T_2} \text{tr} \left[\mathbf{W}_{\alpha\mu} \mathbf{W}^{\mu\beta} \right] \text{tr} \left[\mathbf{W}_{\beta\nu} \mathbf{W}^{\nu\alpha} \right],$$

$$\mathcal{L}_{T,5} = g^2 g'^2 F_{T_5} \text{tr} \left[\mathbf{W}_{\mu\nu} \mathbf{W}^{\mu\nu} \right] \text{tr} \left[\mathbf{B}_{\alpha\beta} \mathbf{B}^{\alpha\beta} \right],$$

$$\mathcal{L}_{T,6} = g^2 g'^2 F_{T_6} \text{tr} \left[\mathbf{W}_{\alpha\nu} \mathbf{W}^{\mu\beta} \right] \text{tr} \left[\mathbf{B}_{\mu\beta} \mathbf{B}^{\alpha\nu} \right],$$

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$$\mathcal{L}_{T,8} = g'^4 F_{T_8} \text{tr} \left[\mathbf{B}_{\mu\nu} \mathbf{B}^{\mu\nu} \right] \text{tr} \left[\mathbf{B}_{\alpha\beta} \mathbf{B}^{\alpha\beta} \right],$$

$$\mathcal{L}_{T,9} = g'^4 F_{T_9} \text{tr} \left[\mathbf{B}_{\alpha\mu} \mathbf{B}^{\mu\beta} \right] \text{tr} \left[\mathbf{B}_{\beta\nu} \mathbf{B}^{\nu\alpha} \right].$$



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$$\mathcal{L}_{M,7} = -g^2 F_{M_7} \text{tr} \left[(\mathbf{D}_\mu \mathbf{H})^\dagger \mathbf{W}_{\nu\rho} \mathbf{W}^{\nu\rho} (\mathbf{D}^\rho \mathbf{H}) \right];$$

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$$\mathcal{L}_{T,2} = g^4 F_{T_2} \text{tr} \left[\mathbf{W}_{\alpha\mu} \mathbf{W}^{\mu\beta} \right] \text{tr} \left[\mathbf{W}_{\beta\nu} \mathbf{W}^{\nu\alpha} \right],$$

$$\mathcal{L}_{T,5} = g^2 g'^2 F_{T_5} \text{tr} \left[\mathbf{W}_{\mu\nu} \mathbf{W}^{\mu\nu} \right] \text{tr} \left[\mathbf{B}_{\alpha\beta} \mathbf{B}^{\alpha\beta} \right],$$

$$\mathcal{L}_{T,6} = g^2 g'^2 F_{T_6} \text{tr} \left[\mathbf{W}_{\alpha\nu} \mathbf{W}^{\mu\beta} \right] \text{tr} \left[\mathbf{B}_{\mu\beta} \mathbf{B}^{\alpha\nu} \right],$$

Much more leeway for new physics in
transversal gauge bosons and di-Higgs

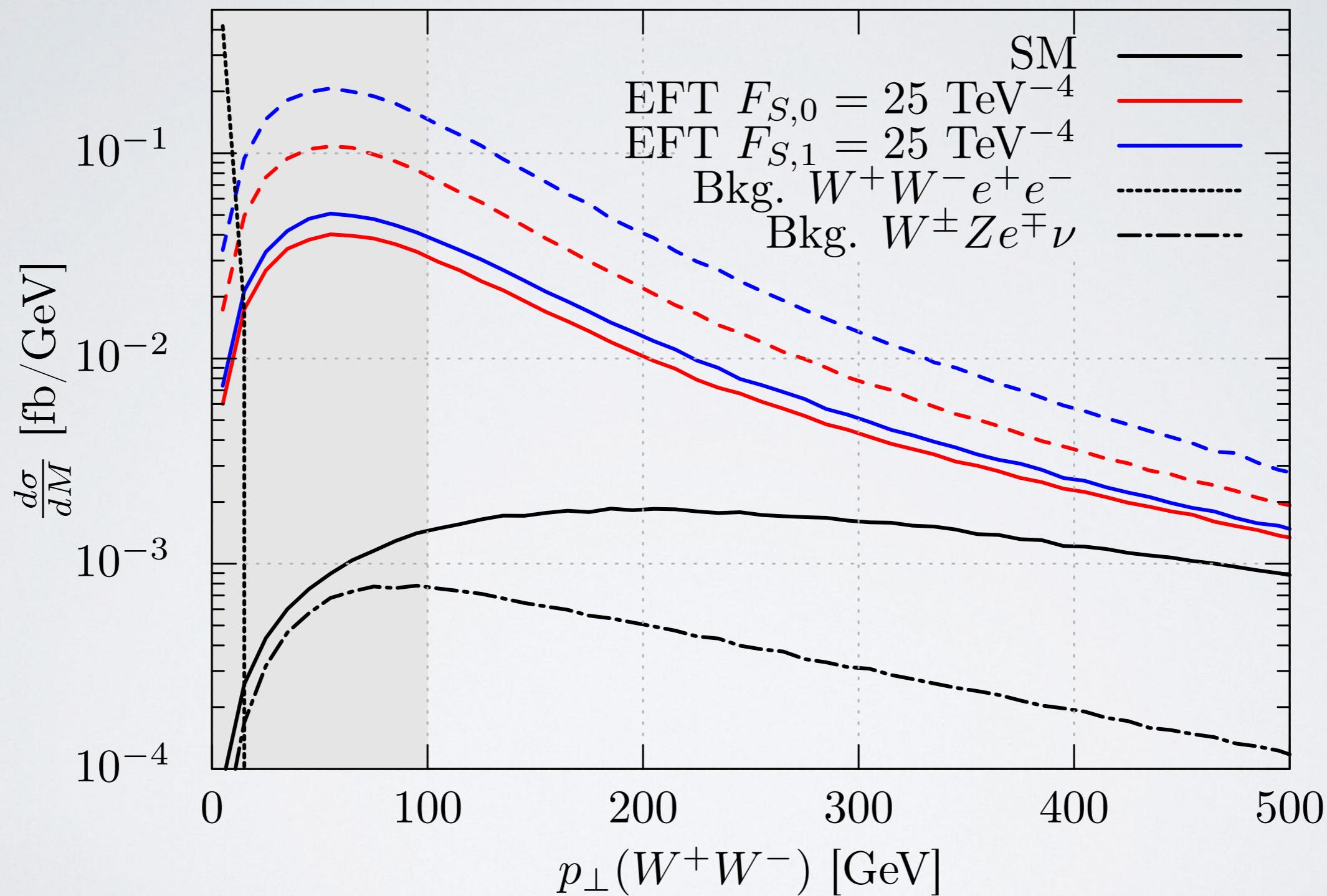
$$\mathcal{L}_{T,9} = g'^4 F_{T_9} \text{tr} \left[\mathbf{B}_{\alpha\mu} \mathbf{B}^{\mu\beta} \right] \text{tr} \left[\mathbf{B}_{\beta\nu} \mathbf{B}^{\nu\alpha} \right].$$



Longitudinal Vector Boson Scattering in $e^+ e^-$

$e^+ e^- \rightarrow \bar{\nu} \nu W^+ W^-$

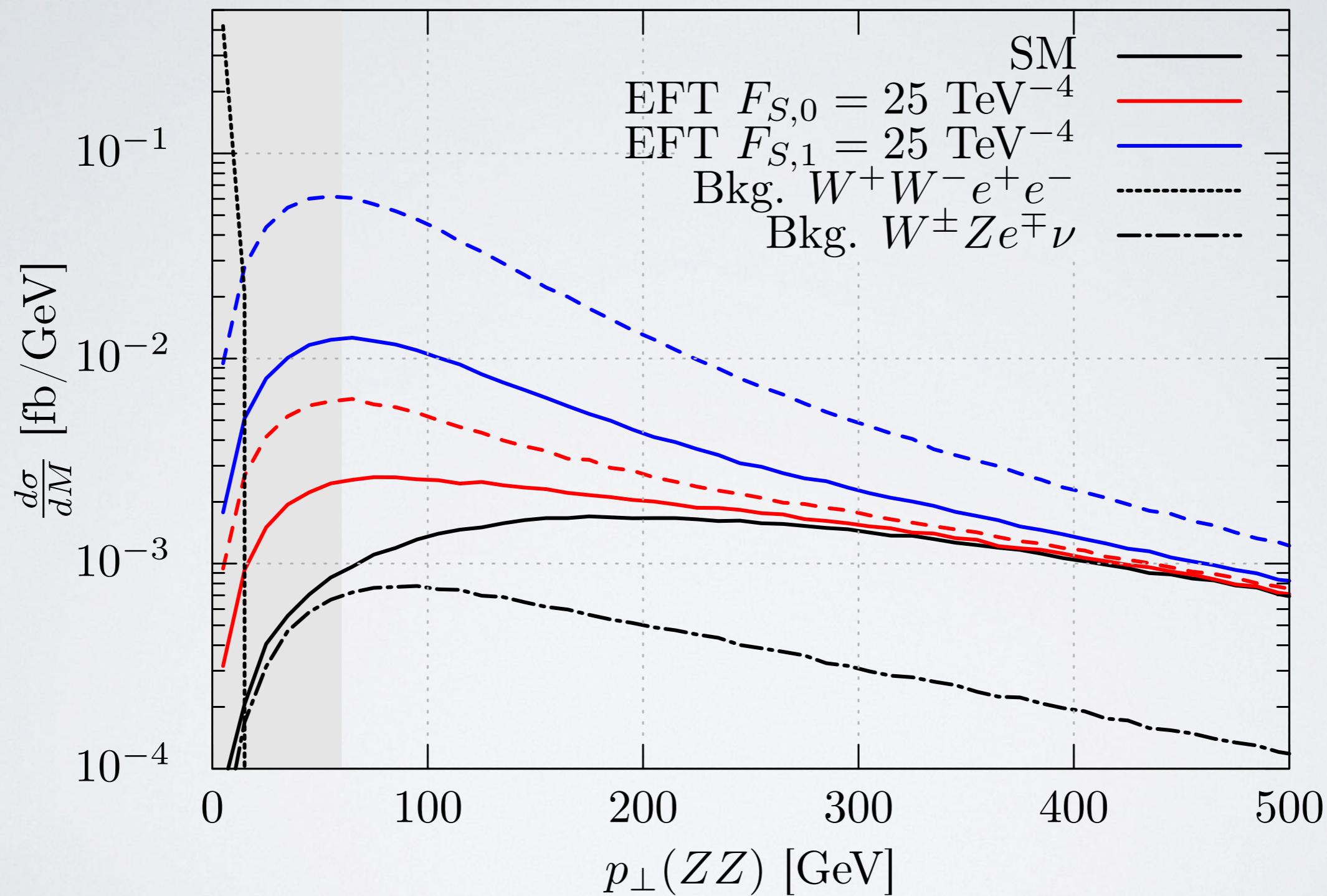
CLIC 3 TeV



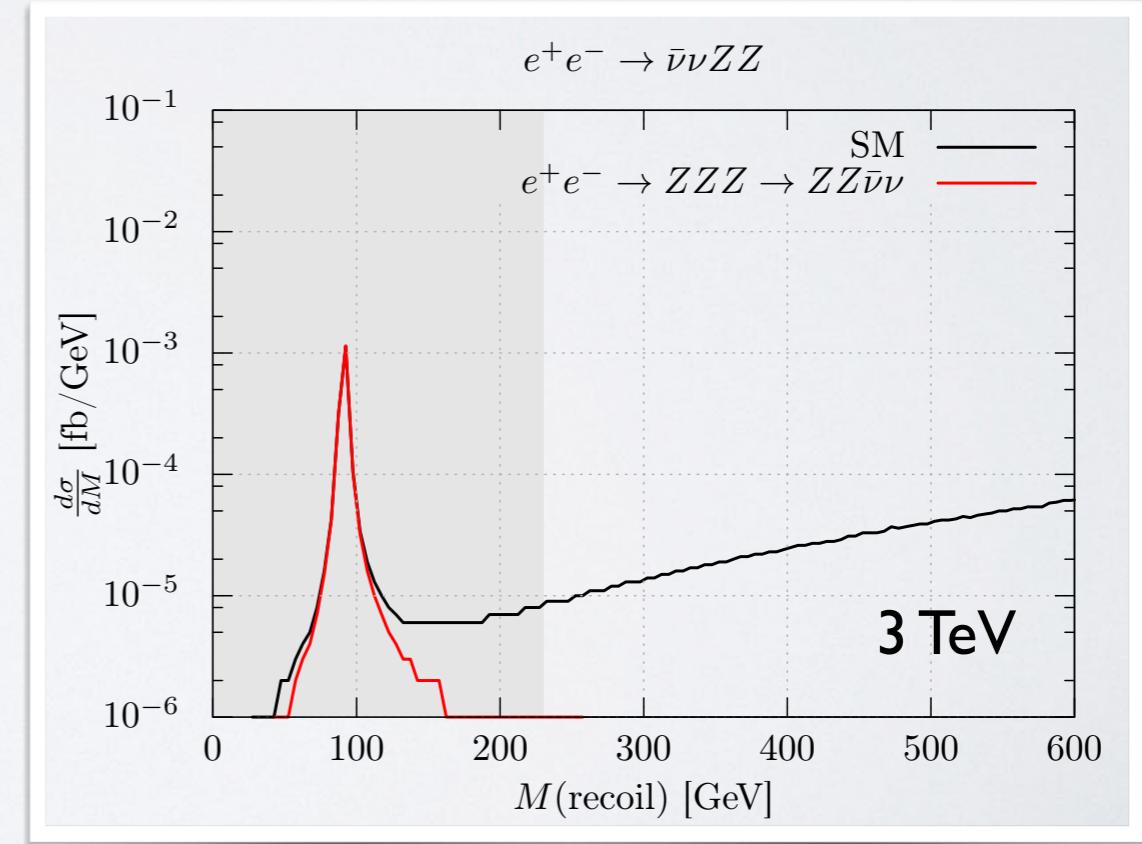
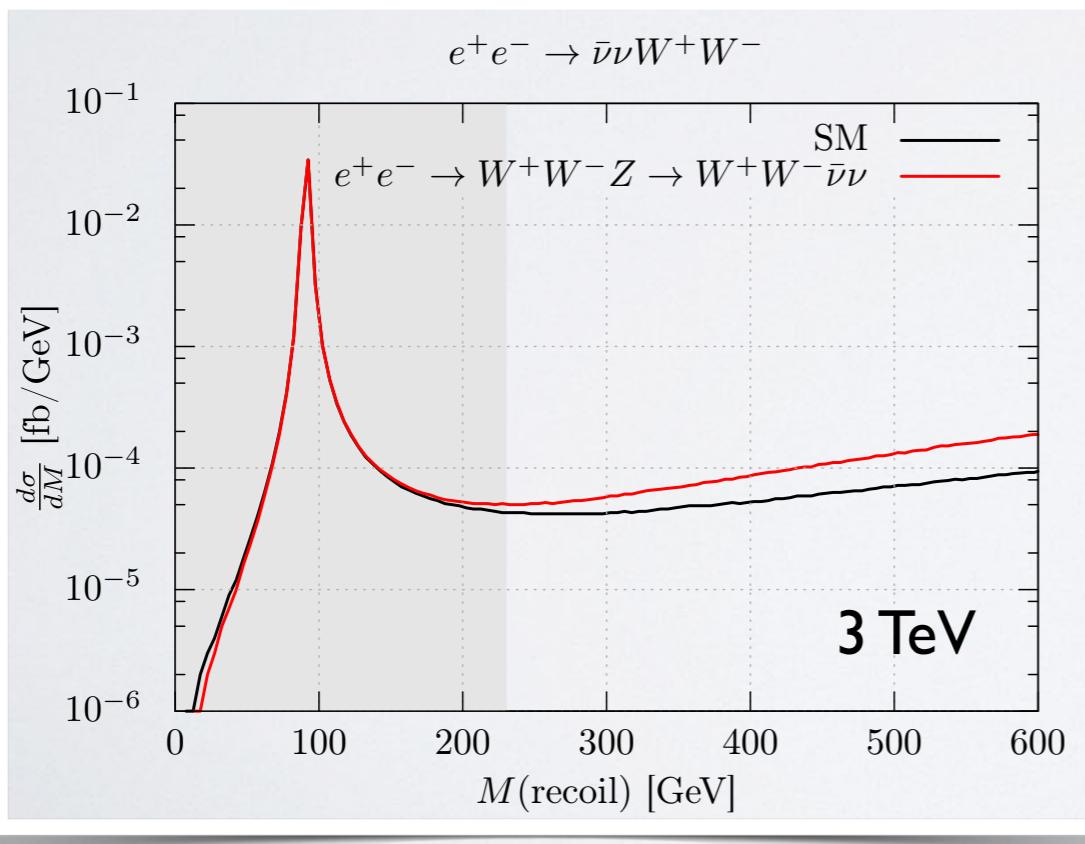
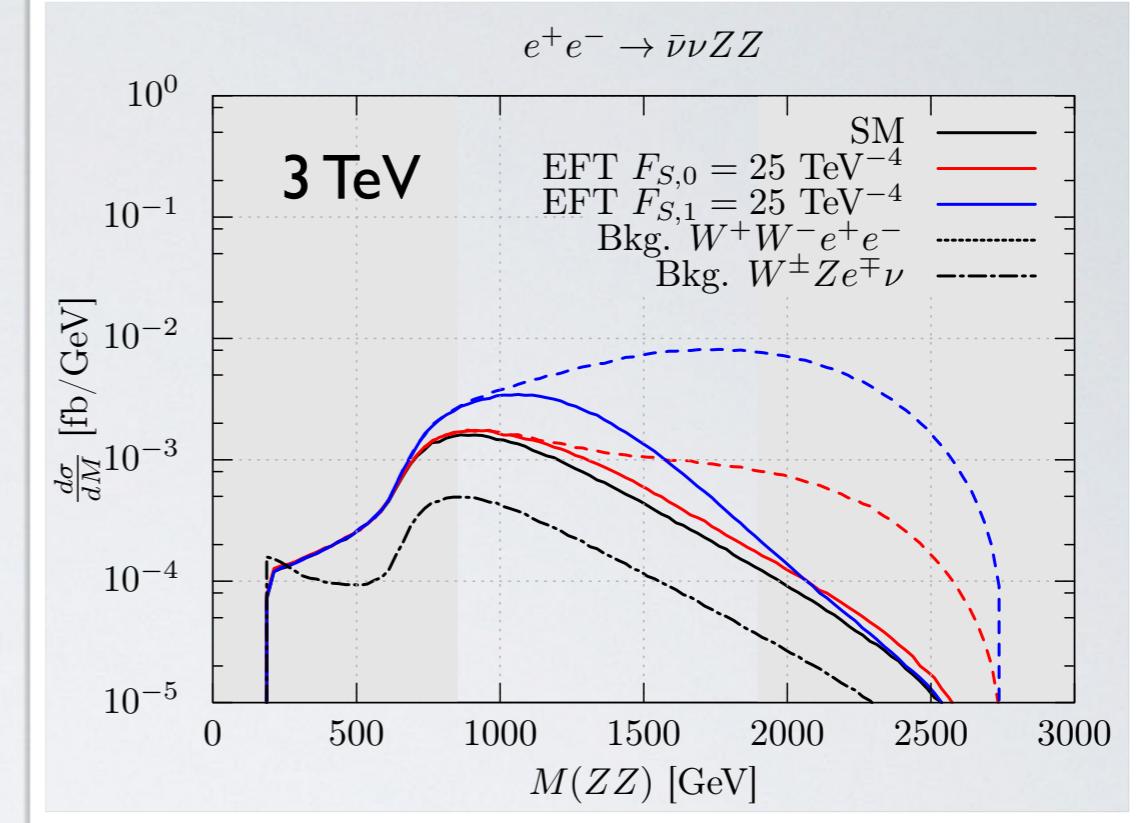
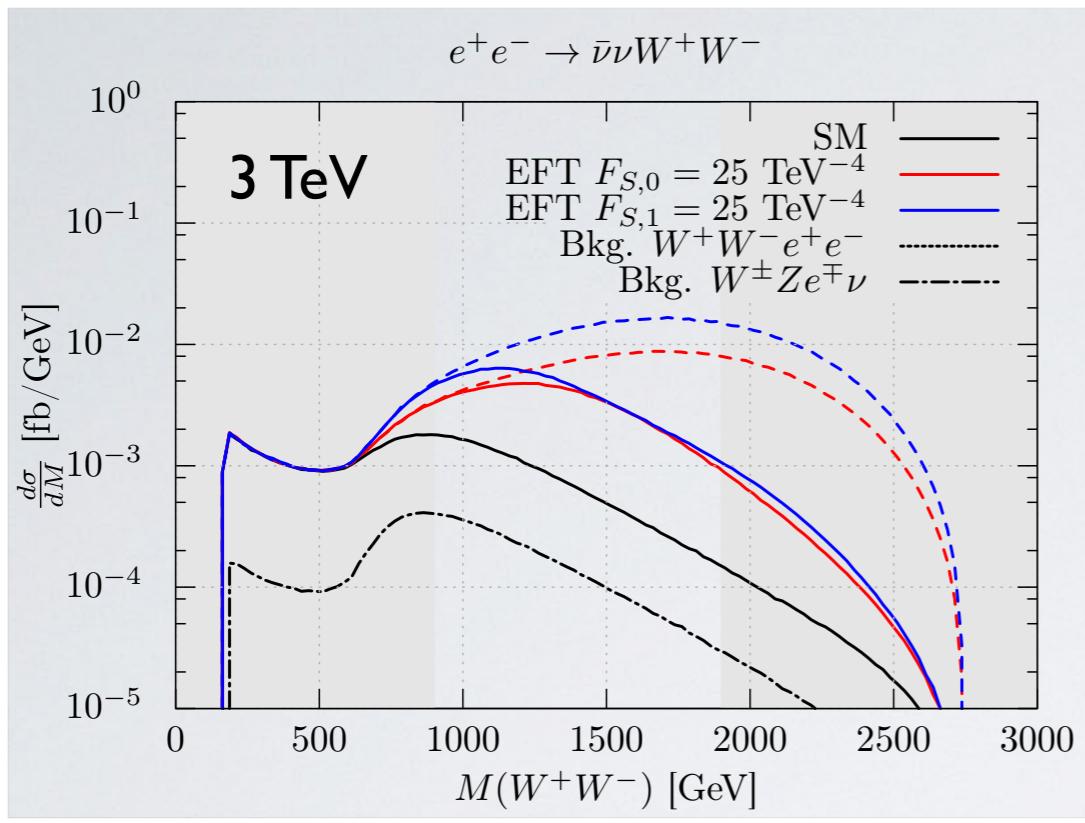
Longitudinal Vector Boson Scattering in $e^+ e^-$

$e^+ e^- \rightarrow \bar{\nu} \nu ZZ$

CLIC 3 TeV



Separability of signal and triboson backgrounds



VBS in $e^+ e^-$: SM rates and Backgrounds (III)

15/22

Fleper/Kilian/JRR/Sekulla: 1607.03030

Process	1400 GeV	3000 GeV	Factor
$W^+ W^- \nu \bar{\nu}$	0.119	0.790	1
$W^+ W^- e^+ e^-$	0.000	0.000	1
$W^\pm Z e^\mp \nu$	0.269	1.200	0.136
$Z Z e^+ e^-$	0.000	0.000	0.019
$W^+ W^- (Z \rightarrow \nu \bar{\nu})$	0.039	0.610	1
<hr/>			
$Z Z \nu \bar{\nu}$	0.084	0.790	1
$Z Z e^+ e^-$	0.000	0.000	1
$W^\pm Z e^\mp \nu$	0.288	1.593	0.136
$W^+ W^- e^+ e^-$	0.000	0.000	0.019
$Z Z (Z \rightarrow \nu \bar{\nu})$	0.000	0.000	1

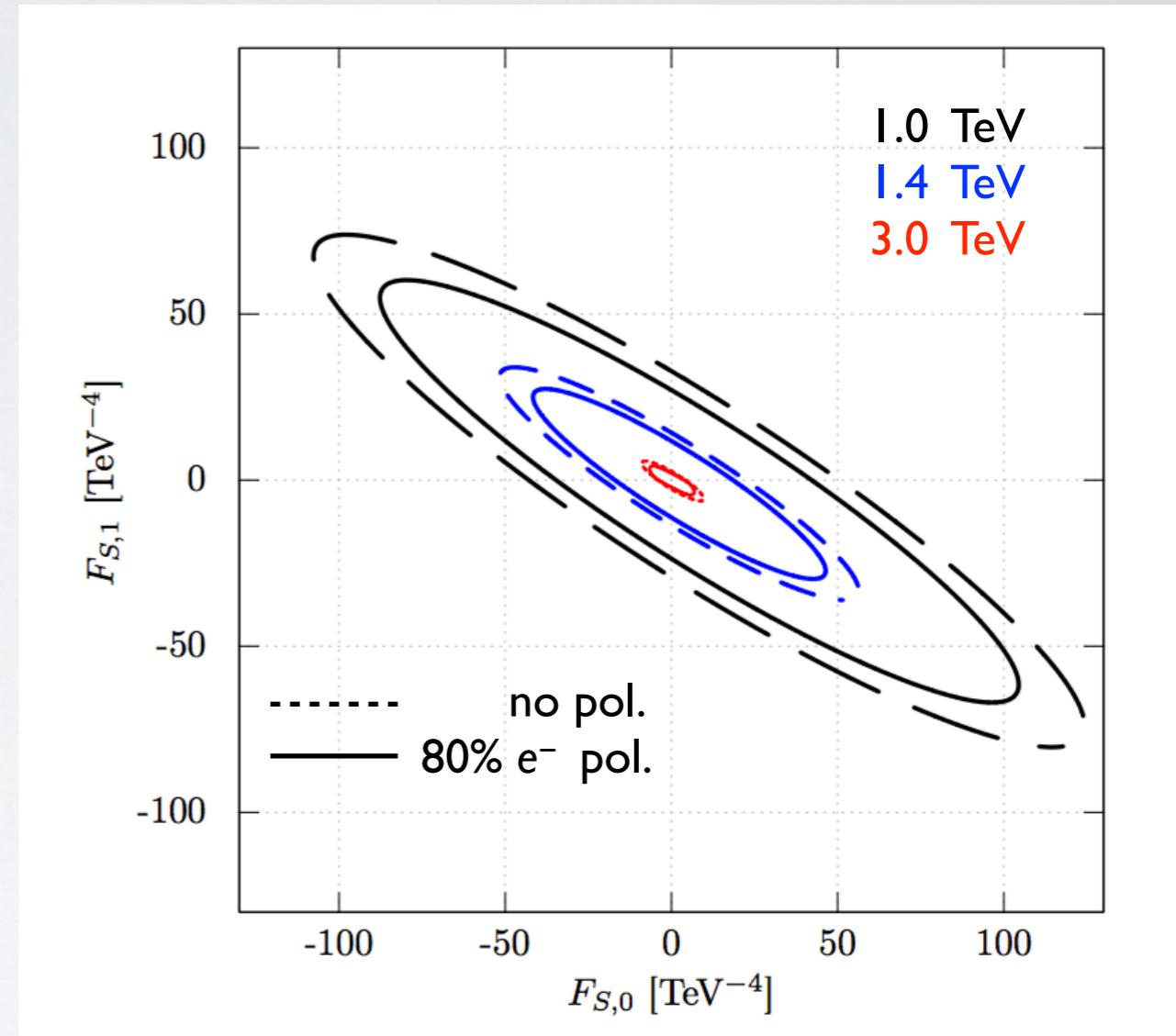
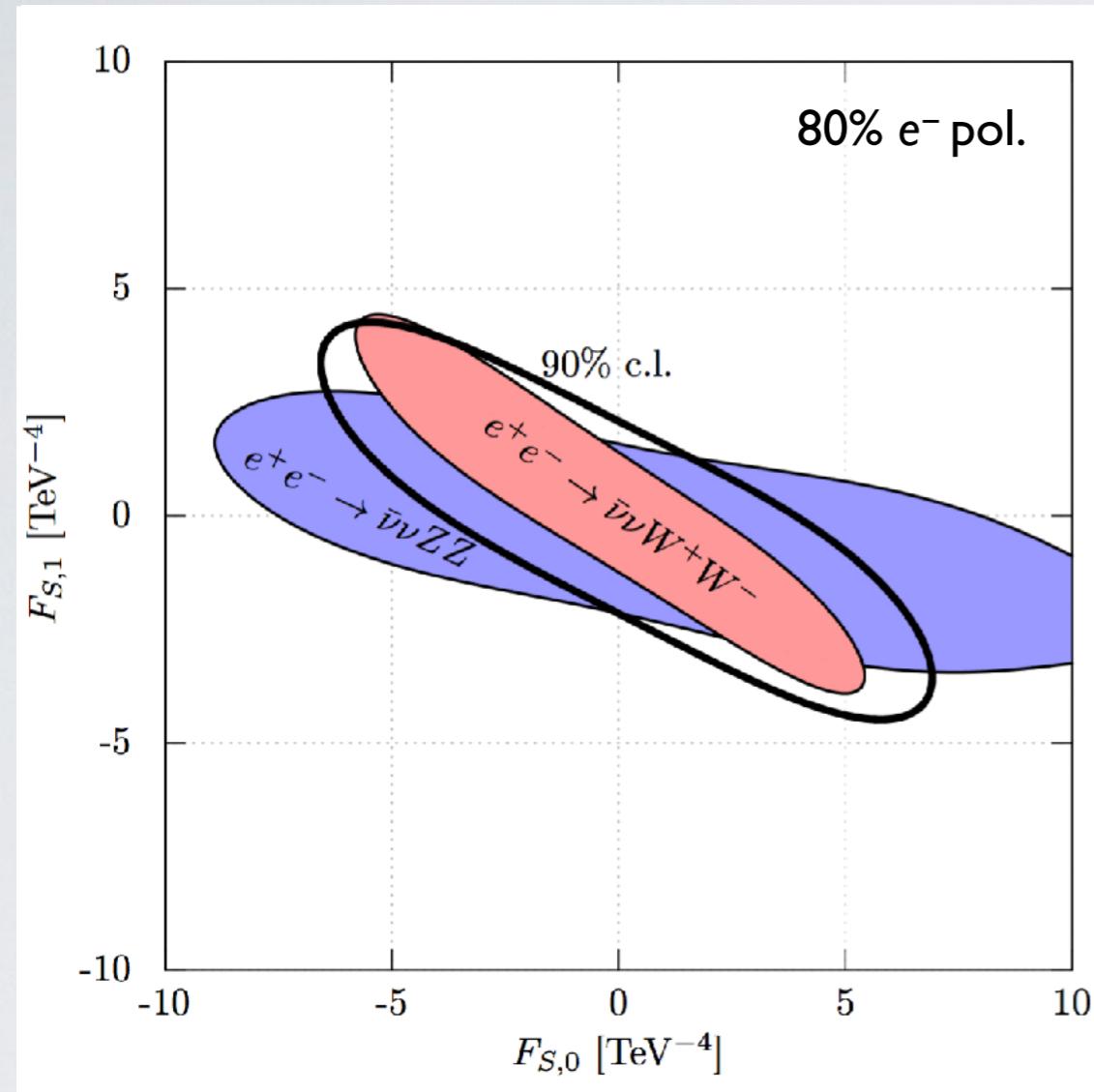
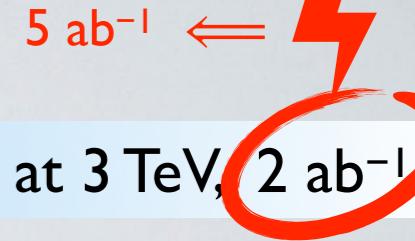
Total cross sections
[fb], all cuts

MC error are
 $\approx 1\%$ on average

Exclusion sensitivities

16/22

Continuum model matched to low-energy SMEFT with two Dim 8-coefficients at 3 TeV, 2 ab^{-1}



- All cuts have been applied
- Detector efficiencies are included
- All cross sections use T -matrix unitarization

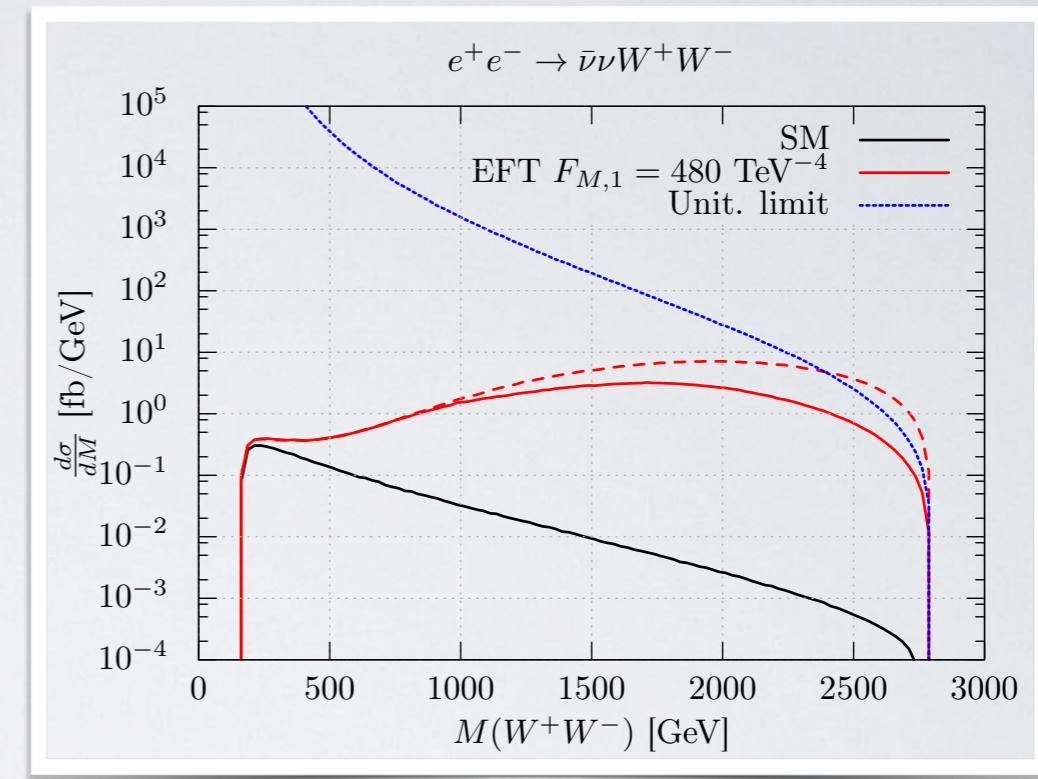
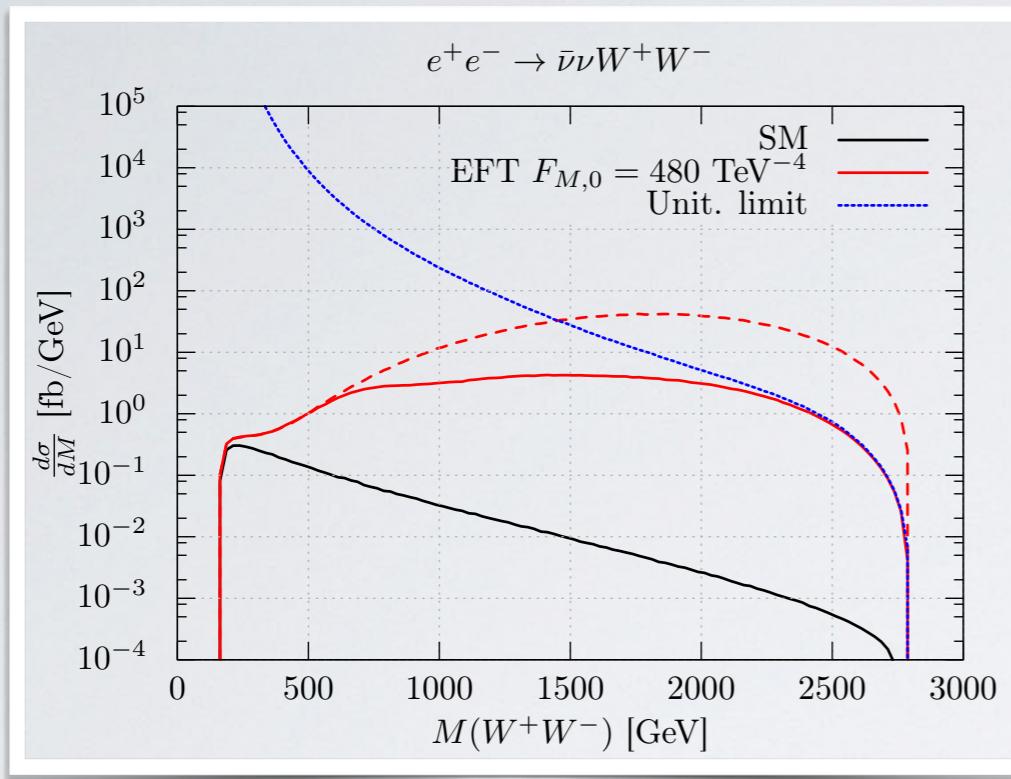
Fleper/Kilian/JRR/Sekulla: I 607.03030

- Confirmed by full simulation [CLICdp]

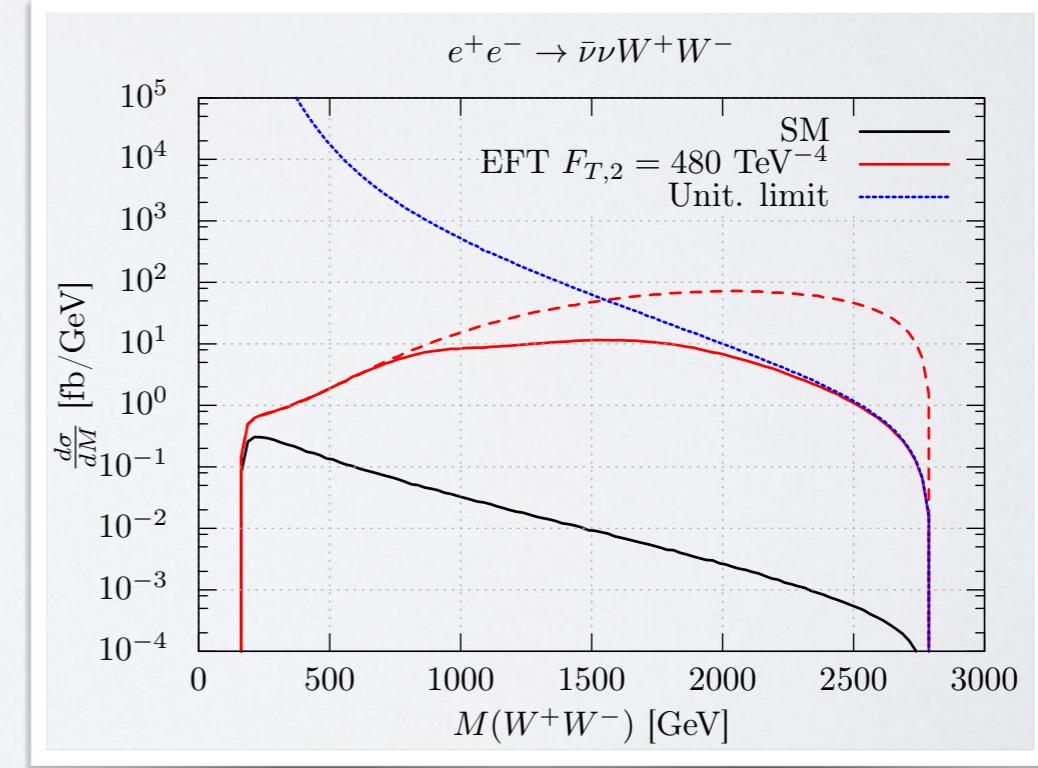
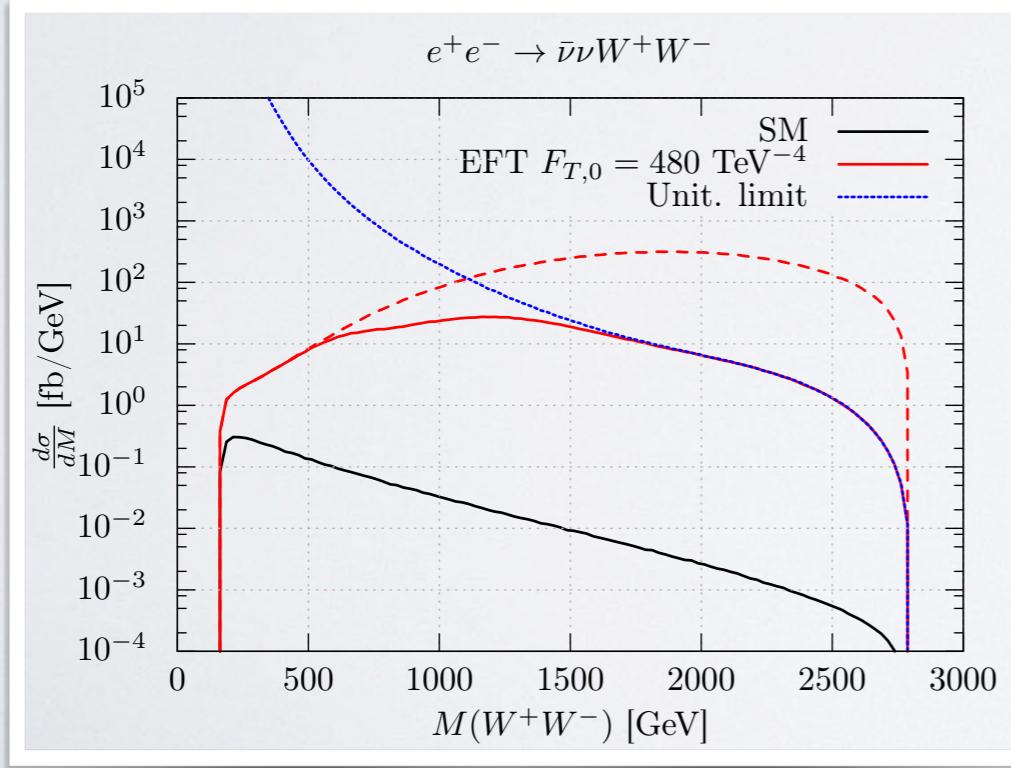
SMEFT dim. 8: longitudinal vs. mixed operators

$e^+e^- \rightarrow \nu\bar{\nu}W^+W^-$

LT op. (upper panel), T operators (lower panel); continuum, no cuts



3 TeV



Simplified Models & New Resonances

- Rise of amplitude / anomalous coupling: Taylor expansion below a resonance
- Resonances might be in direct reach of LHC
- EFT framework EW-restored regime: $SU(2)_L \times SU(2)_R$, $SU(2)_L \times U(1)_Y$ gauged
- Include EFT operators in addition (more resonances, continuum contribution)
- Apply T -matrix unitarization beyond resonance (“UV-incomplete” model)

Consider four simple cases (resonances)

- ▶ Isoscalar scalar (neutral)
- ▶ Isotensor scalar (5 states: ++, +, 0, -, --)
- ▶ Isoscalar tensor (neutral)
- ▶ Isotensor tensor (5 states)

	isoscalar	isotensor
scalar	σ^0	$\phi_t^{--}, \phi_t^-, \phi_t^0, \phi_t^+, \phi_t^{++}$ $\phi_v^-, \phi_v^0, \phi_v^+$ ϕ_s^0
tensor	f^0	$(X_t^{--}, X_t^-, X_t^0, X_t^+, X_t^{++})$ X_v^-, X_v^0, X_v^+ X_s^0
...

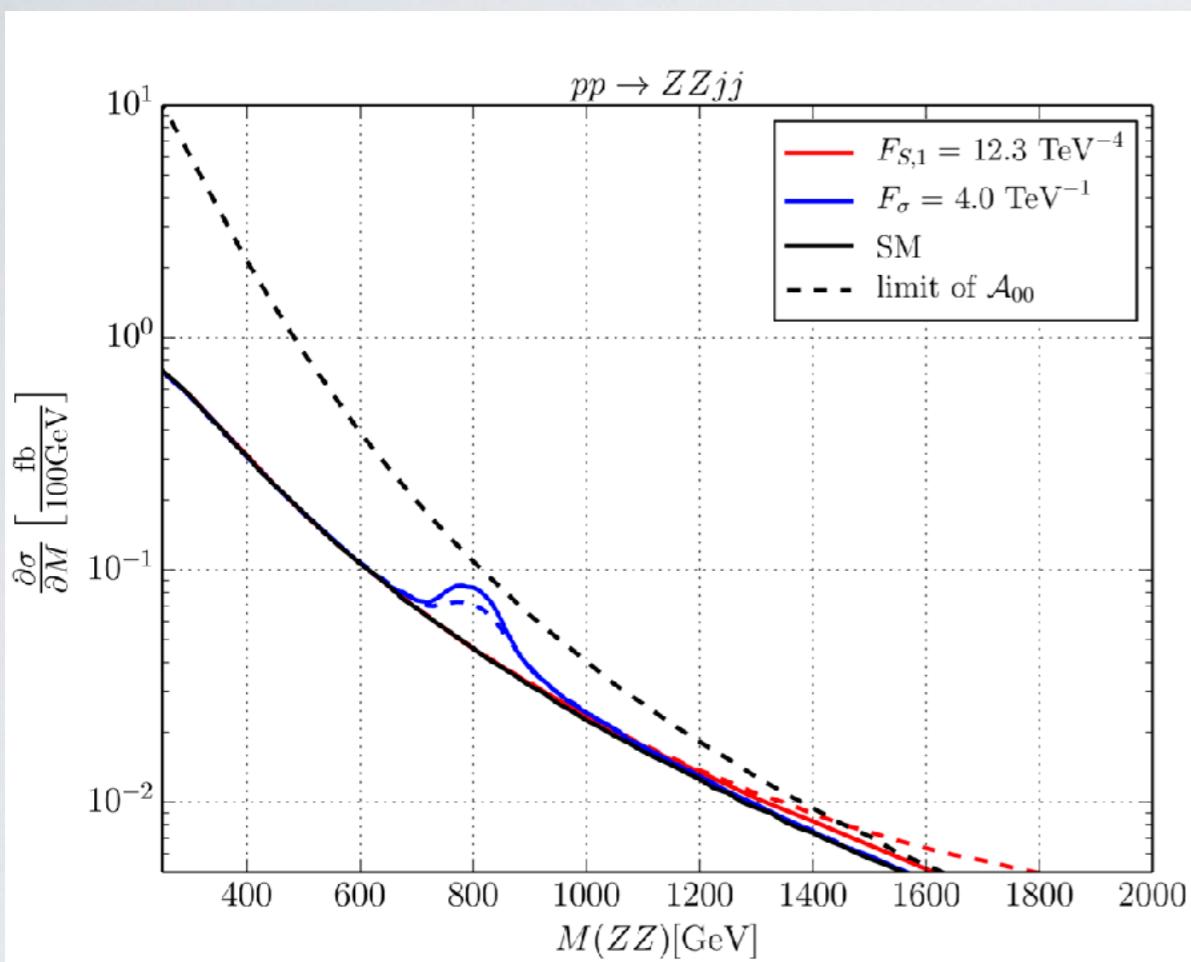
Spin 1 has different physics
(mixing with W/Z)

$$32\pi\Gamma/M^5$$

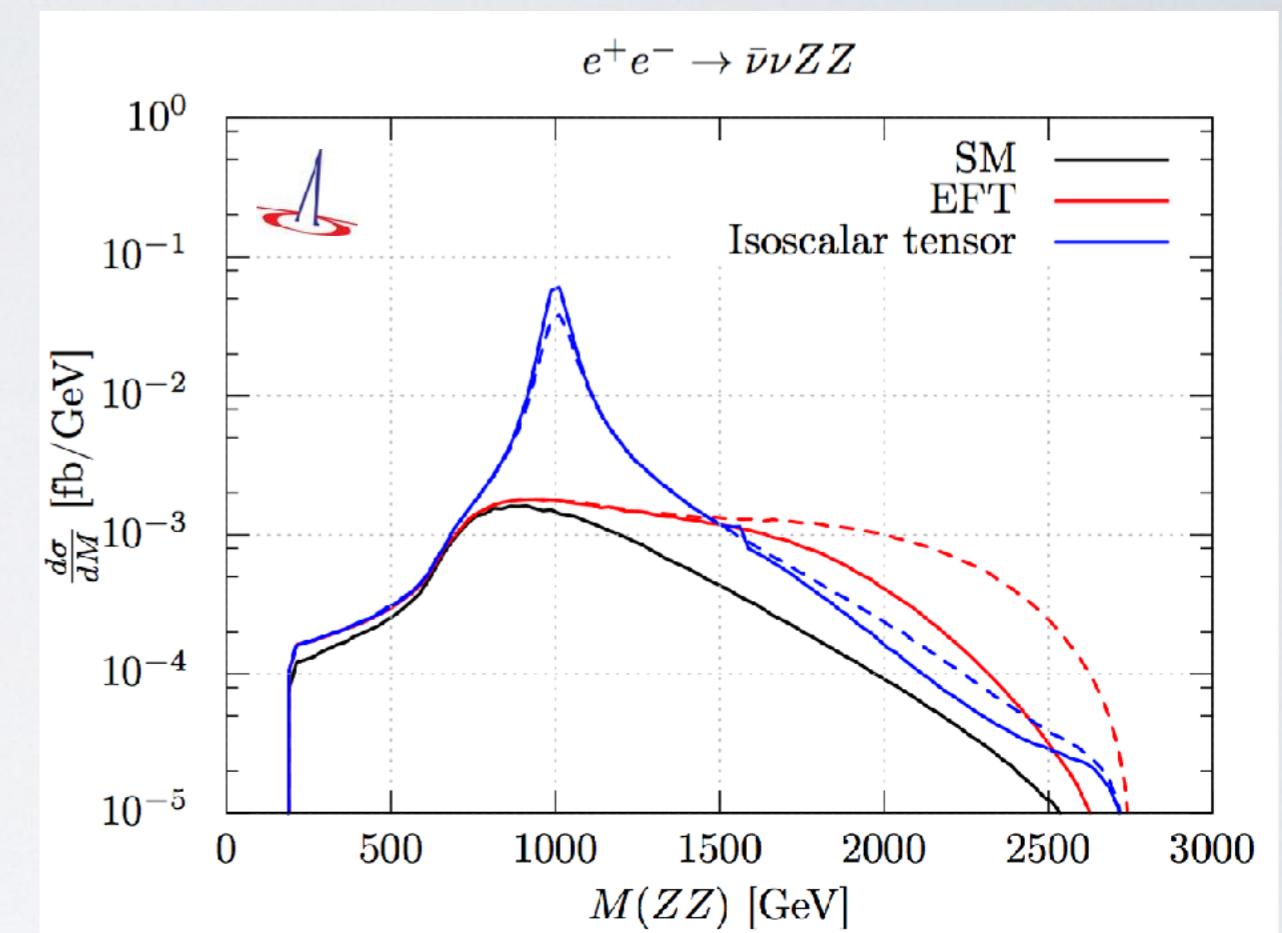
	σ	ϕ	f	X
$F_{S,0}$	$\frac{1}{2}$	2	15	5
$F_{S,1}$	—	$-\frac{1}{2}$	-5	-35

Simplified Models: New Resonances in VBS

Comparison: Isoscalar scalar resonance , with cuts



LHC (14 TeV)



CLIC (3 TeV)

ILC Study Questions document

arXiv:2007.03650v3 [hep-ph] 20 Jan 2021

DESY 20-112,
 KEK Preprint 2020-8,
 IFIC/20-34, LCTP-20-14
 SLAC-PUB-17543
 July, 2020

ILC Study Questions for Snowmass 2021

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ABSTRACT

To aid contributions to the Snowmass 2021 US Community Study on physics at the International Linear Collider and other proposed e^+e^- colliders we present a list of study questions that could be the basis of

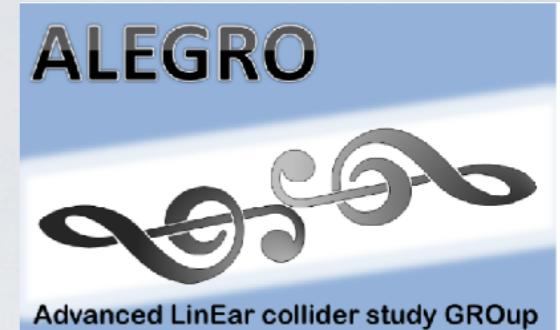
arXiv: 2007.03650v3

- 5 Questions about general e^+e^- event analysis
- 6 Questions about Higgs boson physics: $e^+e^- \rightarrow Zh$
- 7 Questions about Higgs boson physics: WW fusion and higher energy reactions
- 8 Questions about top quark physics
- 9 Questions about $e^+e^- \rightarrow f\bar{f}$
- 10 Questions about W boson physics
- 11 Questions about precision electroweak measurements
- 12 Questions about QCD and jets
- 13 Questions about searches for new particles
- 14 Questions about ILC fixed-target capabilities
- 15 Questions about the theory of Higgs boson couplings
- 16 Questions about SM Effective Field Theory interpretation of e^+e^- measurements
- 17 Contact information for the SiD and ILD detector groups
- 18 R&D collaborations, and contact information for joining them



The ultimate VBS measurement

- ➊ Ultimate machines: plasma-driven e^+e^- accelerators
- ➋ **ALEGRO: Advanced LinEar collider study GROup**
- ➌ RF cavities: 50 MV/m, Drive beam: 100–150 MV/m
- ➍ Dielectric Laser (DLA): 1 GV/m , Plasma Wakefield (PWFA): 10–100 GV/m
- ➎ Idea for linear ultra-high energy e^+e^- collider: 10 TeV / 30 TeV / 50 TeV
- ➏ Problem: needed peak luminosity: $10^{36} \text{ cm}^{-2} \text{ s}^{-1}$, beam power: 50 MW (?), size: $\approx 1 \times 1 \text{ nm}^2$
- ➐ Beam spectrum: only fraction will be in highest bin, non-linear regime
- ➑ Effectively becomes a photon collider: $\gamma\gamma \rightarrow W^+W^-$ quite favorable
- ➒ VBS cross sections tremendous: 0.8 pb [30 TeV] \rightarrow 1.1 pb [50 TeV]
- ➓ Regime of EW radiation [VBS is just EW parton scattering]:
W radiation probability: $2 \times \frac{\alpha_w}{\pi} \log^2 \frac{\sqrt{s}}{m_W} \sim 0.44$
- ➔ Very boosted objects: macroscopic lifetimes $b: 40 \text{ cm} \quad c: 20 \text{ cm} \quad \tau: 70 \text{ cm}$



Perspectives & Study Questions for Snowmass

- Precision discovery reach in VBS for high-energy e^+e^- colliders
- Fully hadronic final states available in VBS in e^+e^- colliders
- Hence: invariant mass of diboson system is fully reconstructable
- Gauge invariance: VBS and tribosons cannot be disentangled in signal model

Theory challenges, tasks, study questions

- Precision predictions: EW corrections, Sudakov logarithms, EW showers
- Connections to BSM models, access to CP -odd operators
- Importance of e^-e^- for VBS ?

Experimental challenges, tasks, study questions

- Hadronic W/Z discrimination in TeV regime
- BDT-based separation of VBS vs. multi-bosons
- Improvement on forward-lepton tagging and vetoes
- Ultimate VBS measurement might be in plasma-driven 10-50 TeV e^+e^-



BACKUP

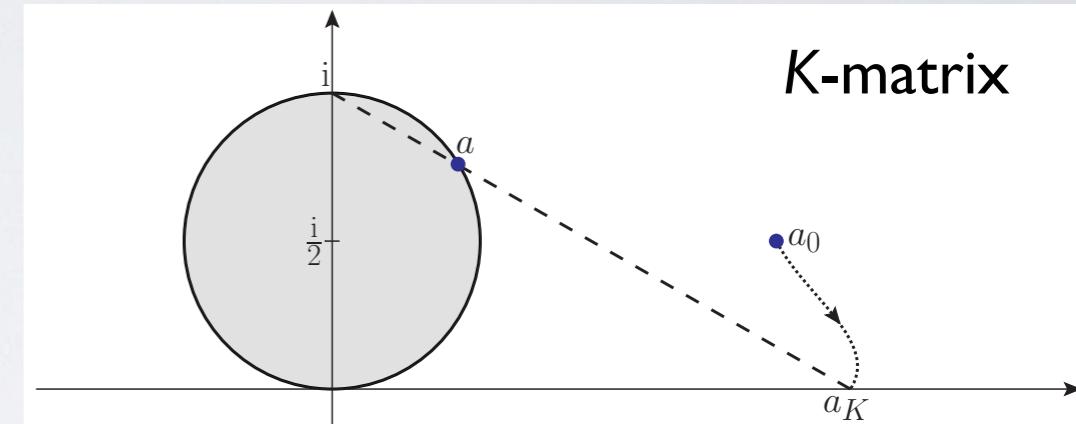


Quick remark on validity and unitarization

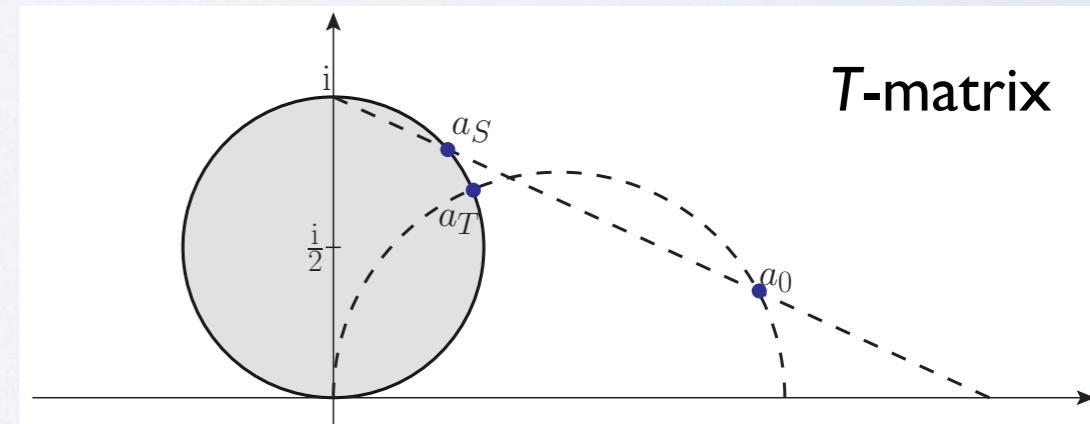
- EFT only valid for energy scales well below new degrees of freedom
- Higher-dimensional operators: amplitudes rise with energy
- High-energy regime could lead to unphysical results**
 - Truncate reach (“event clipping”)
 - Measurement only in low-energy bins
 - Unitarization procedure
- K-matrix: Stereographic projection to Argand circle
- ... is partial resummation of perturbative series
- Gives bin-wise highest event yield compatible with QFT**
- Problem for amplitudes with intrinsic imaginary part (e.g. resonances)
- T-matrix:** Thales circle construction
- Identical to K-matrix for real amplitudes**
- Does not rely on perturbative description

$$\left| a - \frac{a_K}{2} \right| = \frac{a_K}{2} \quad \Rightarrow \quad a = \frac{1}{\operatorname{Re}\left(\frac{1}{a_0}\right) - i}$$

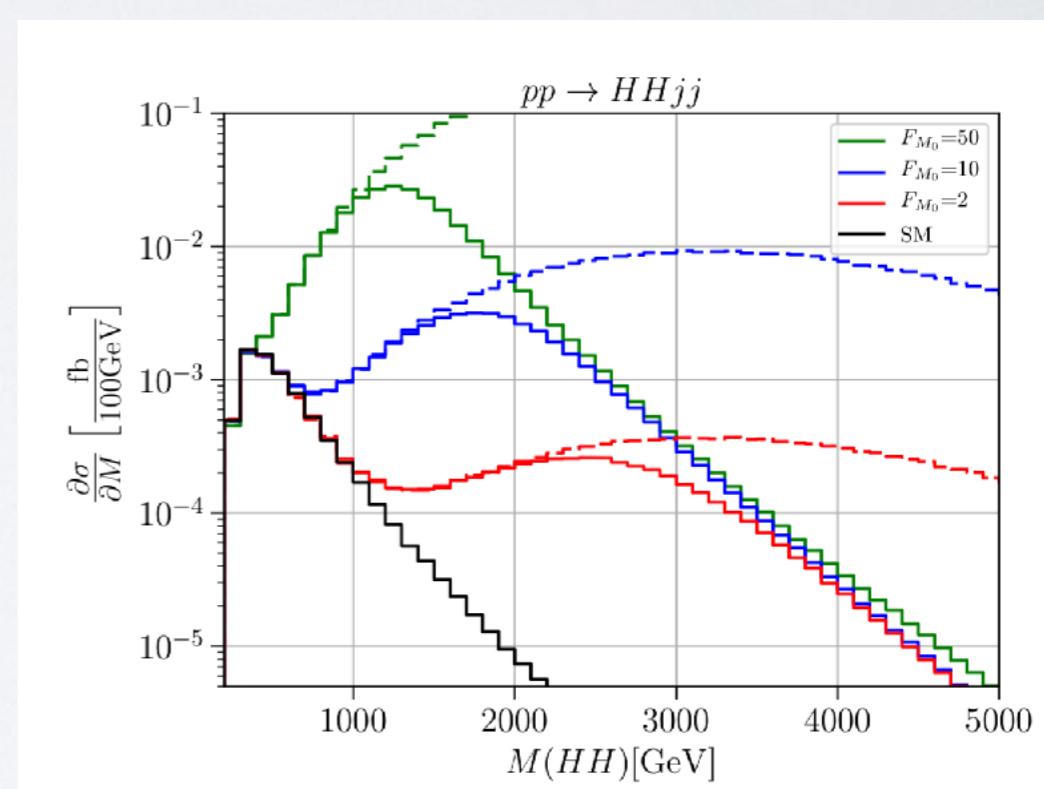
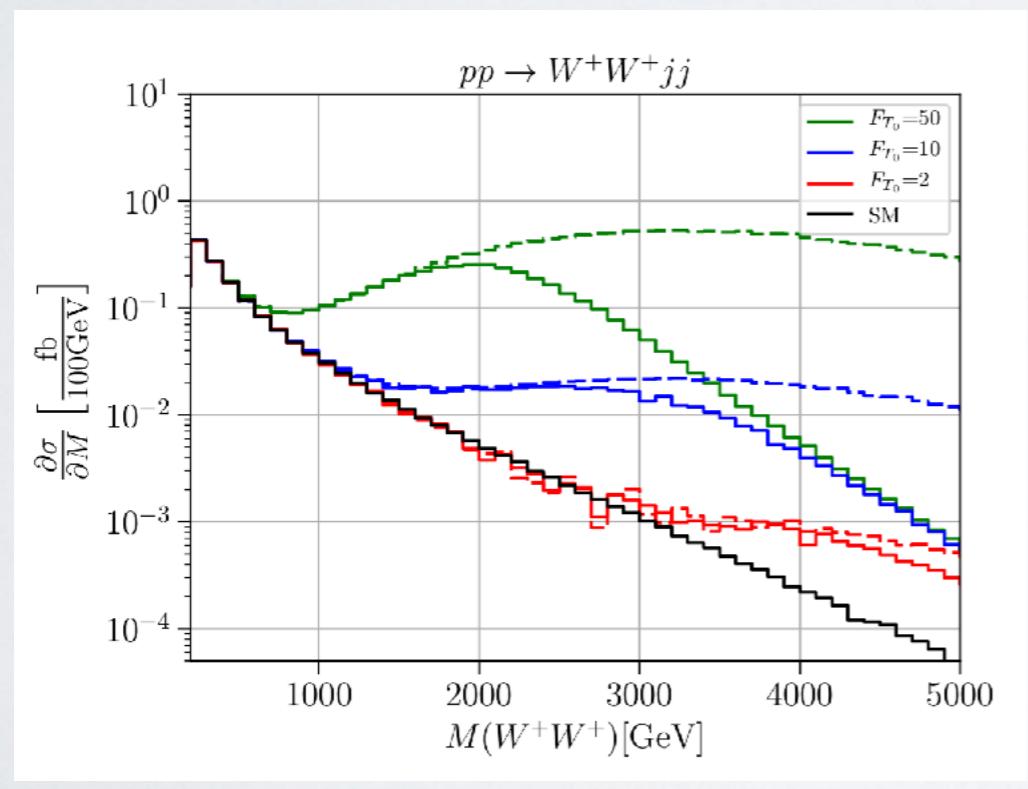
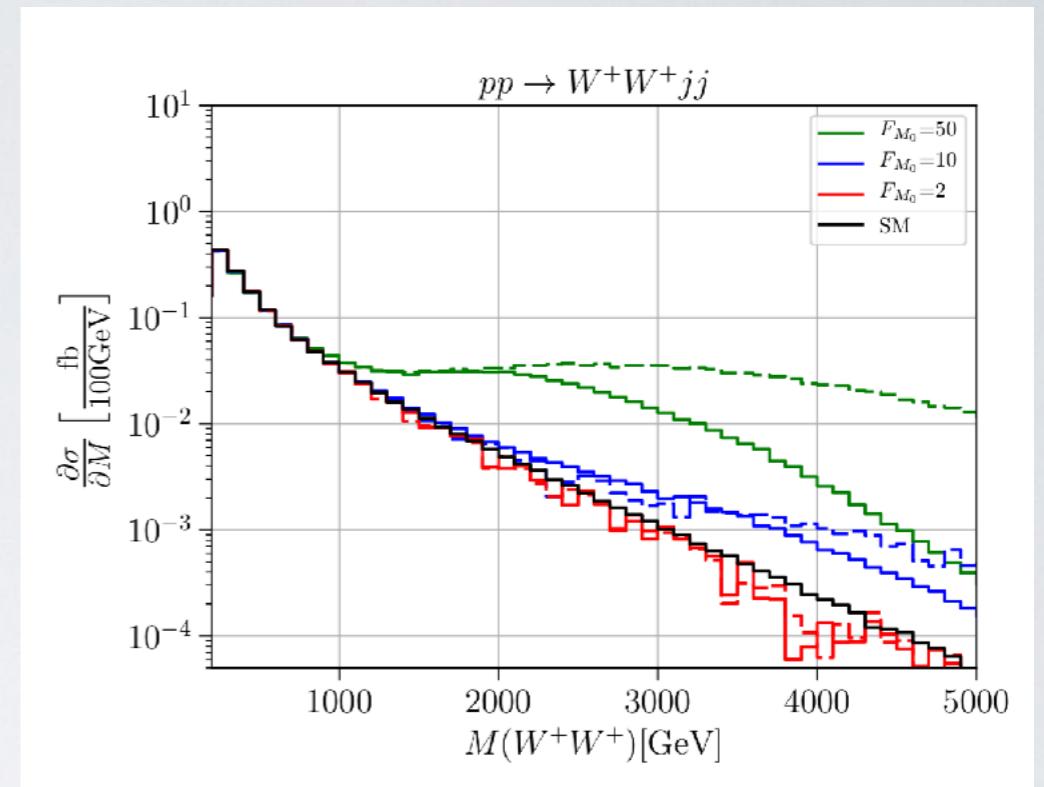
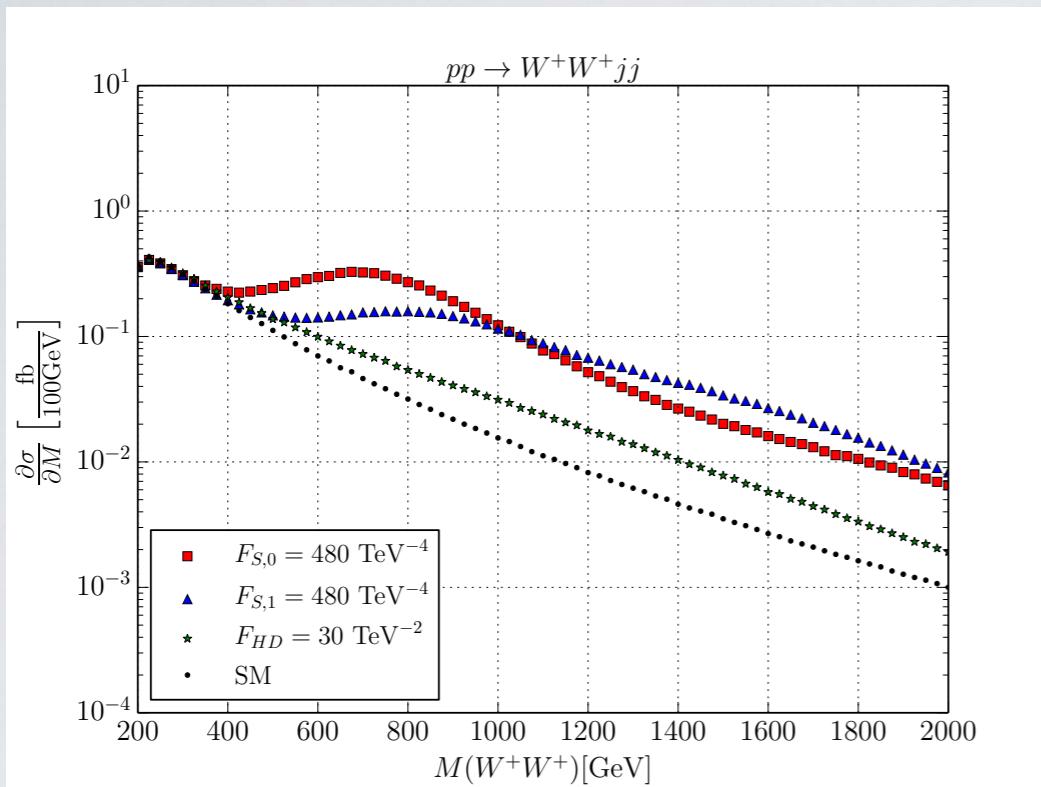
$$S = \frac{1+iK/2}{1-iK/2} \quad a_K(s) = \frac{a(s)}{1-ia(s)}$$



[Kilian/Ohl/JRR/Sekulla 2014]

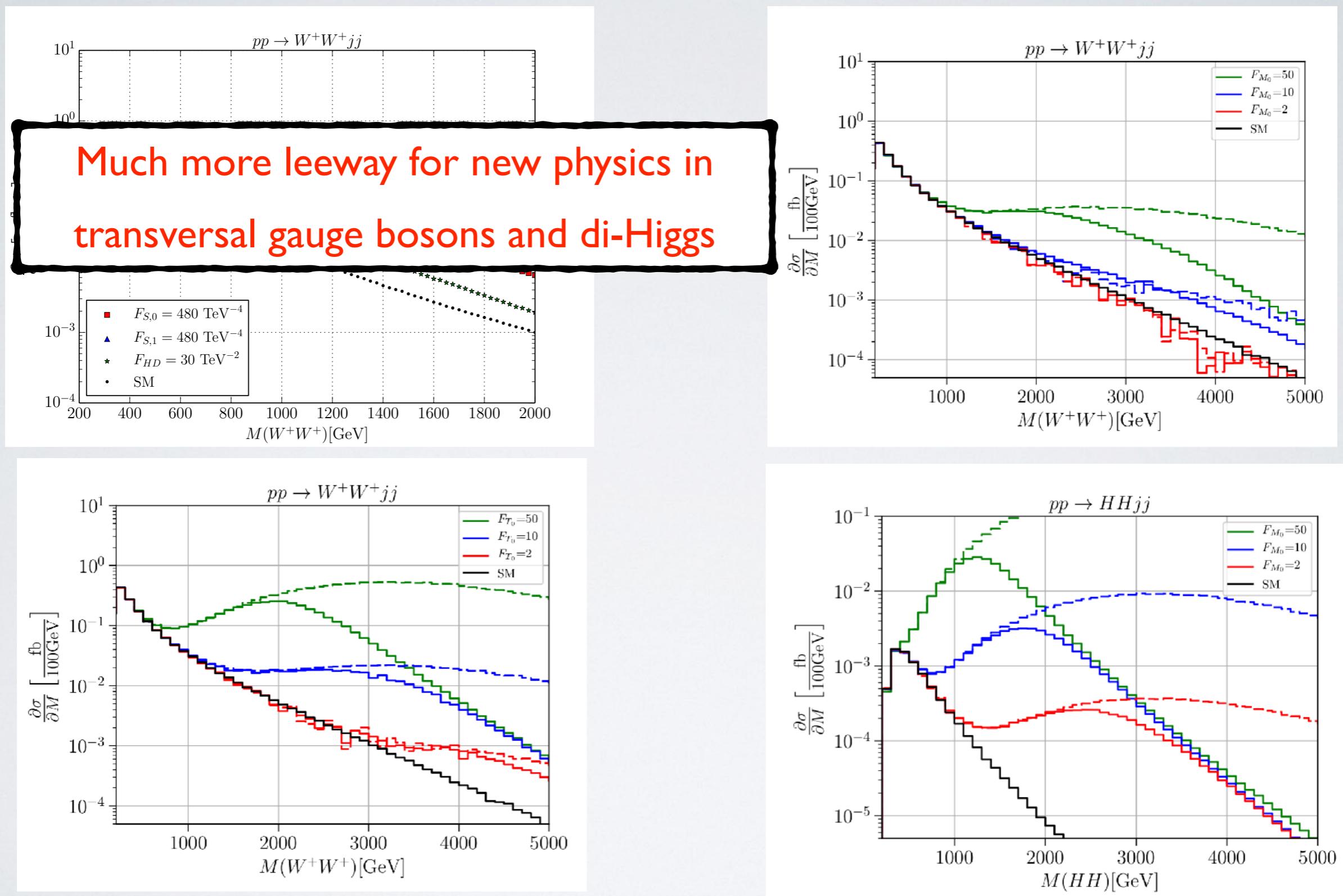


VBS diboson spectra



General cuts: $M_{jj} > 500 \text{ GeV}; \Delta\eta_{jj} > 2.4; p_T^j > 20 \text{ GeV}; |\Delta\eta_j| < 4.5$

VBS diboson spectra



General cuts: $M_{jj} > 500 \text{ GeV}; \Delta\eta_{jj} > 2.4; p_T^j > 20 \text{ GeV}; |\Delta\eta_j| < 4.5$

