



VBS prospects in SMEFT at a future muon collider

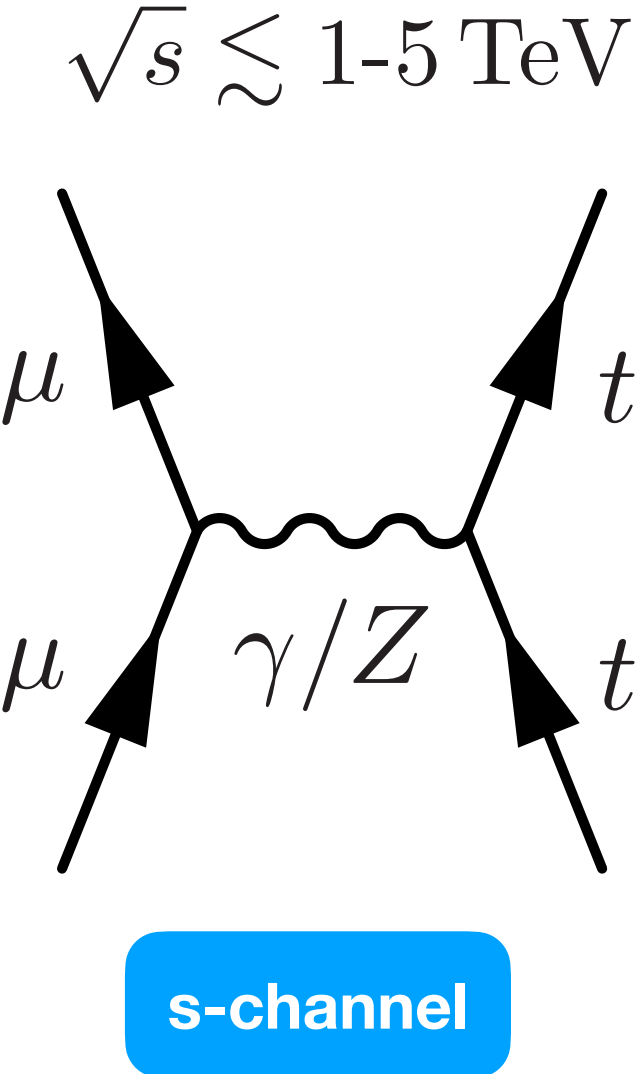
Luca Mantani



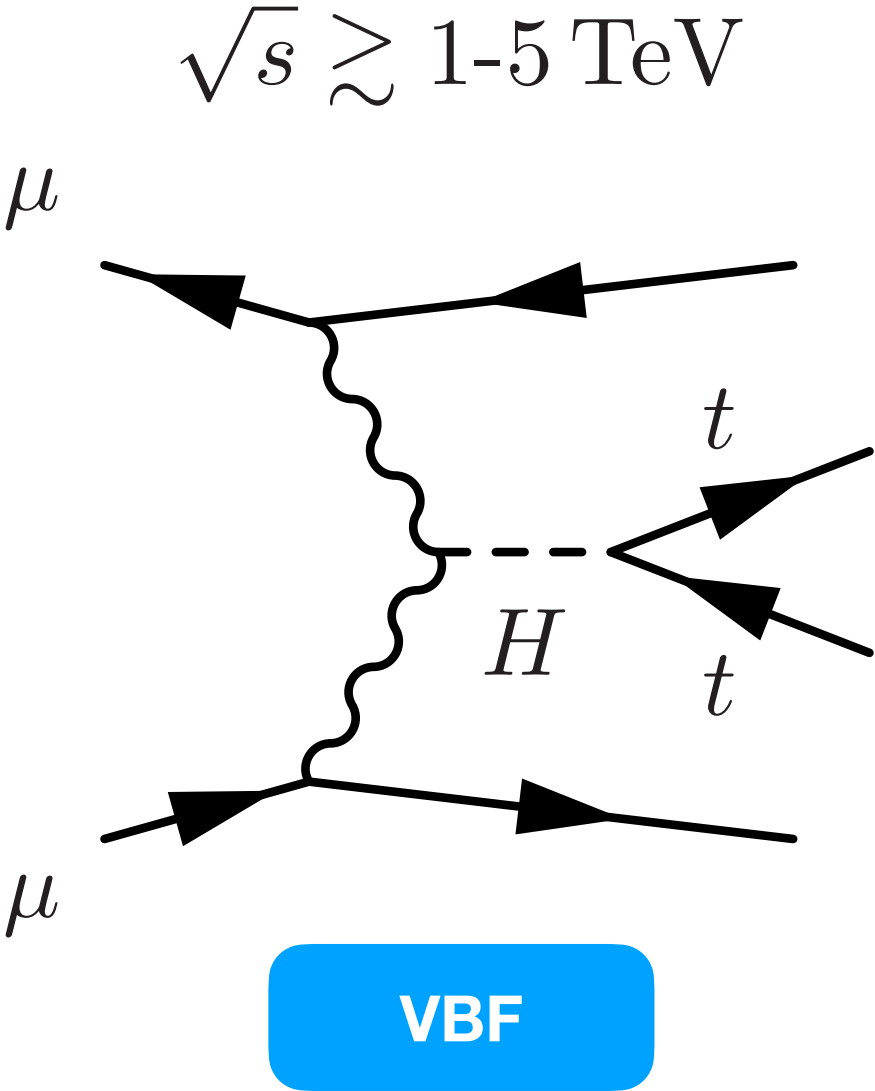
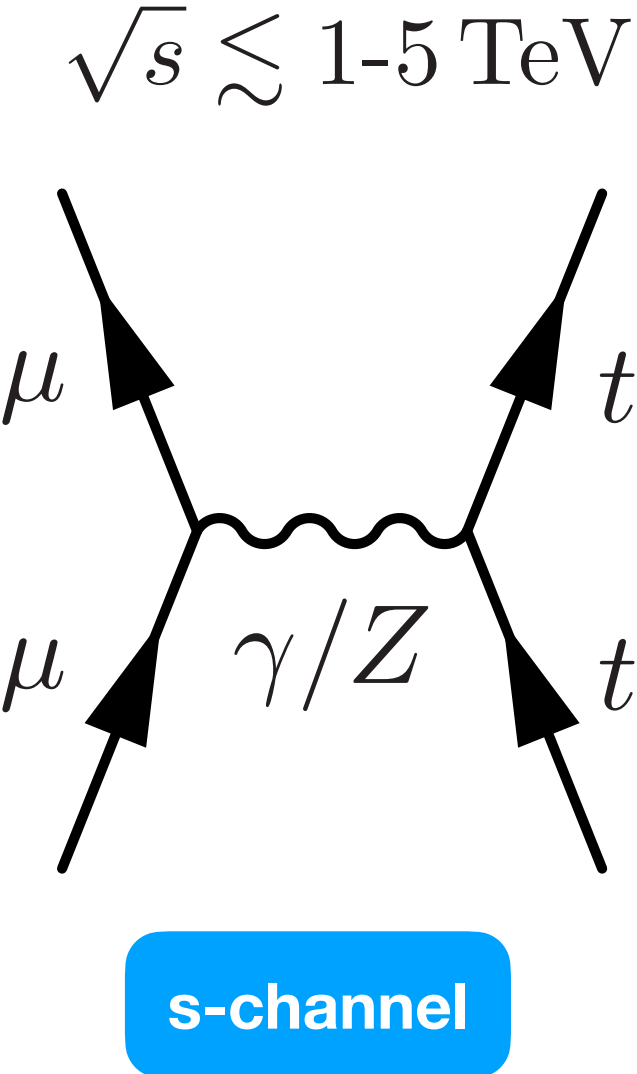
Different mode of production at different energies

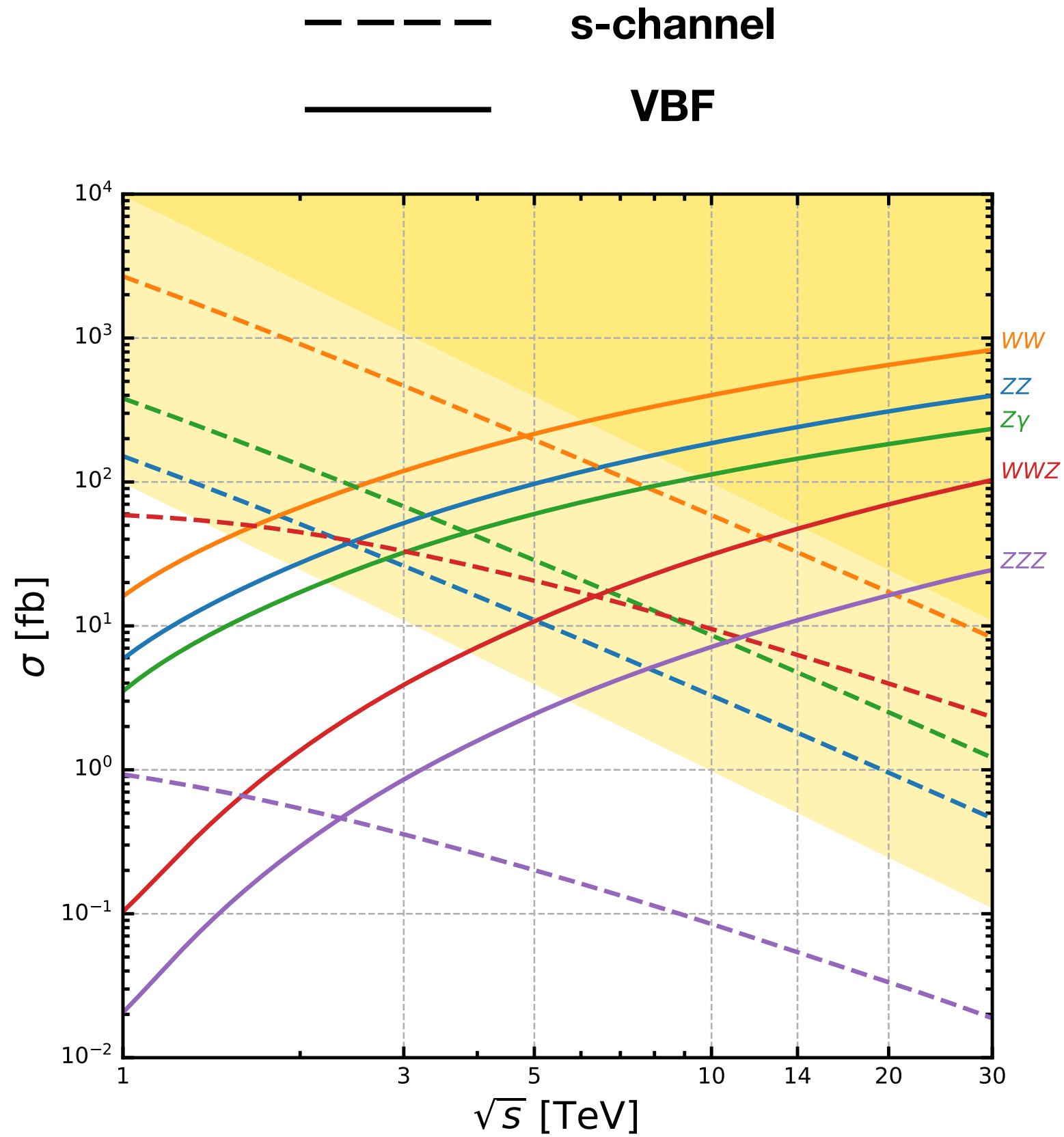


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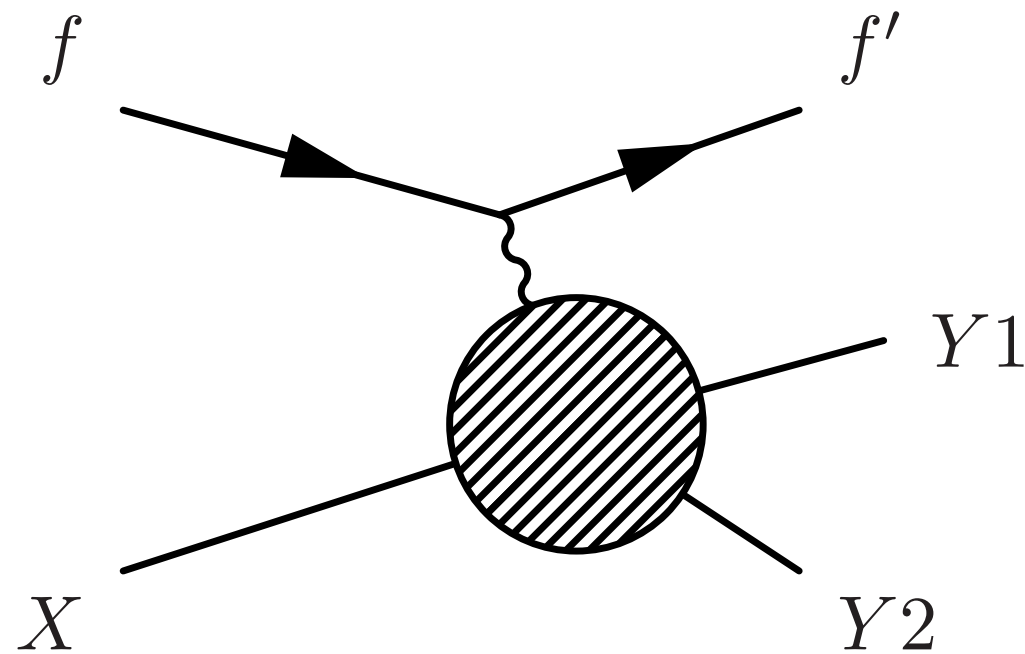


Different mode of production at different energies





We can have an analytical insight with EWA



$$E \sim xE \sim (1-x)E, \quad \frac{m}{E} \ll 1, \quad \frac{p_{\perp}}{E} \ll 1$$

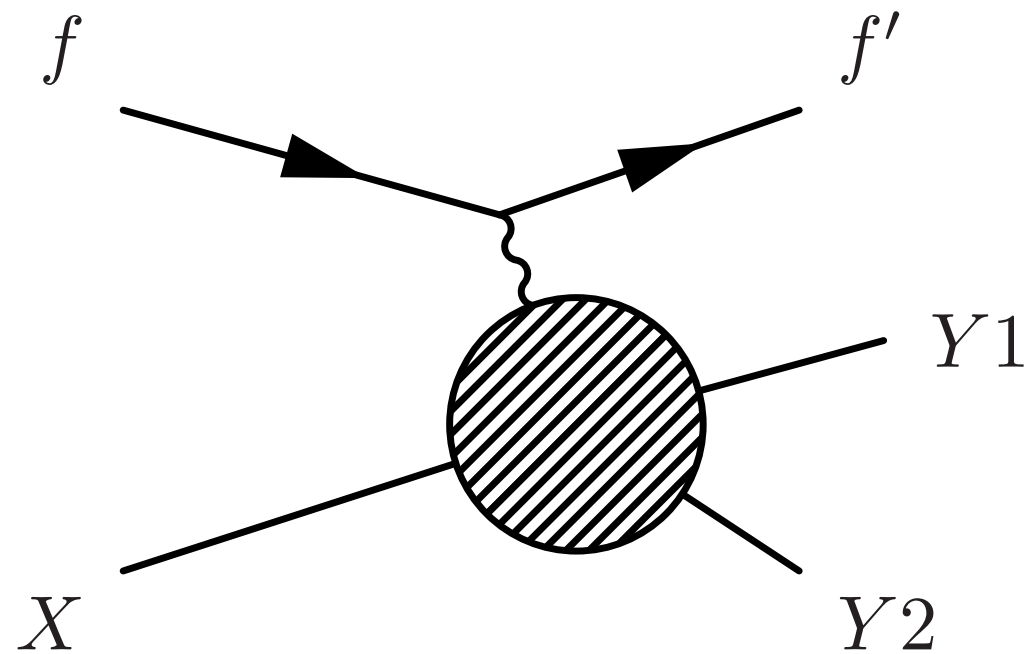
$$f_{+} = \frac{(1-x)^2}{x} \frac{p_{\perp}^3}{(m^2(1-x) + p_{\perp}^2)^2},$$

$$f_{-} = \frac{1}{x} \frac{p_{\perp}^3}{(m^2(1-x) + p_{\perp}^2)^2},$$

$$f_0 = \frac{(1-x)^2}{x} \frac{2m^2 p_{\perp}}{(m^2(1-x) + p_{\perp}^2)^2}.$$

[P. Borel et al. arXiv:1202.1904]

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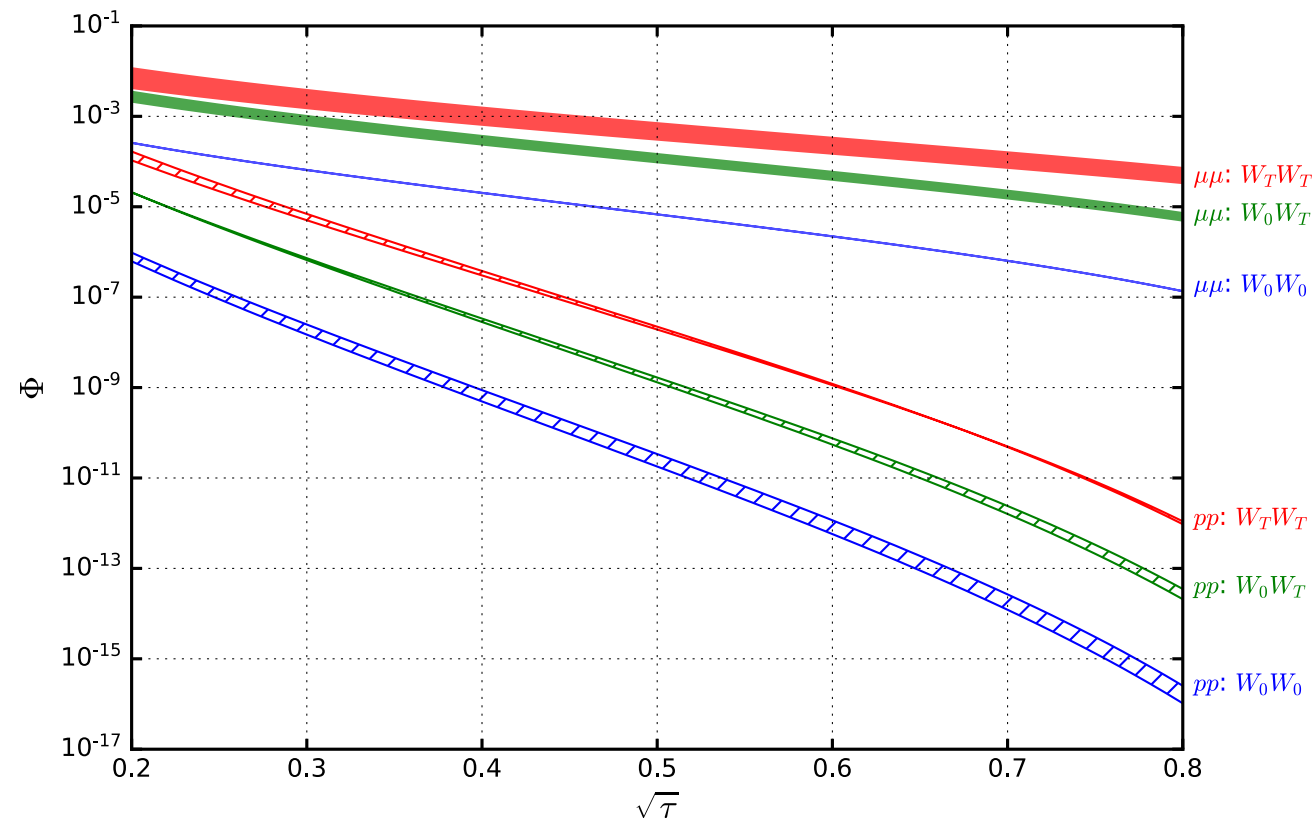
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$$\frac{d\sigma_{EWA}}{dx dp_{\perp}} (fX \rightarrow f'Y) = \frac{C^2}{2\pi^2} \sum_{i=+,-,0} f_i \times d\sigma(W_i X \rightarrow Y)$$

Weak bosons can be described as partons!

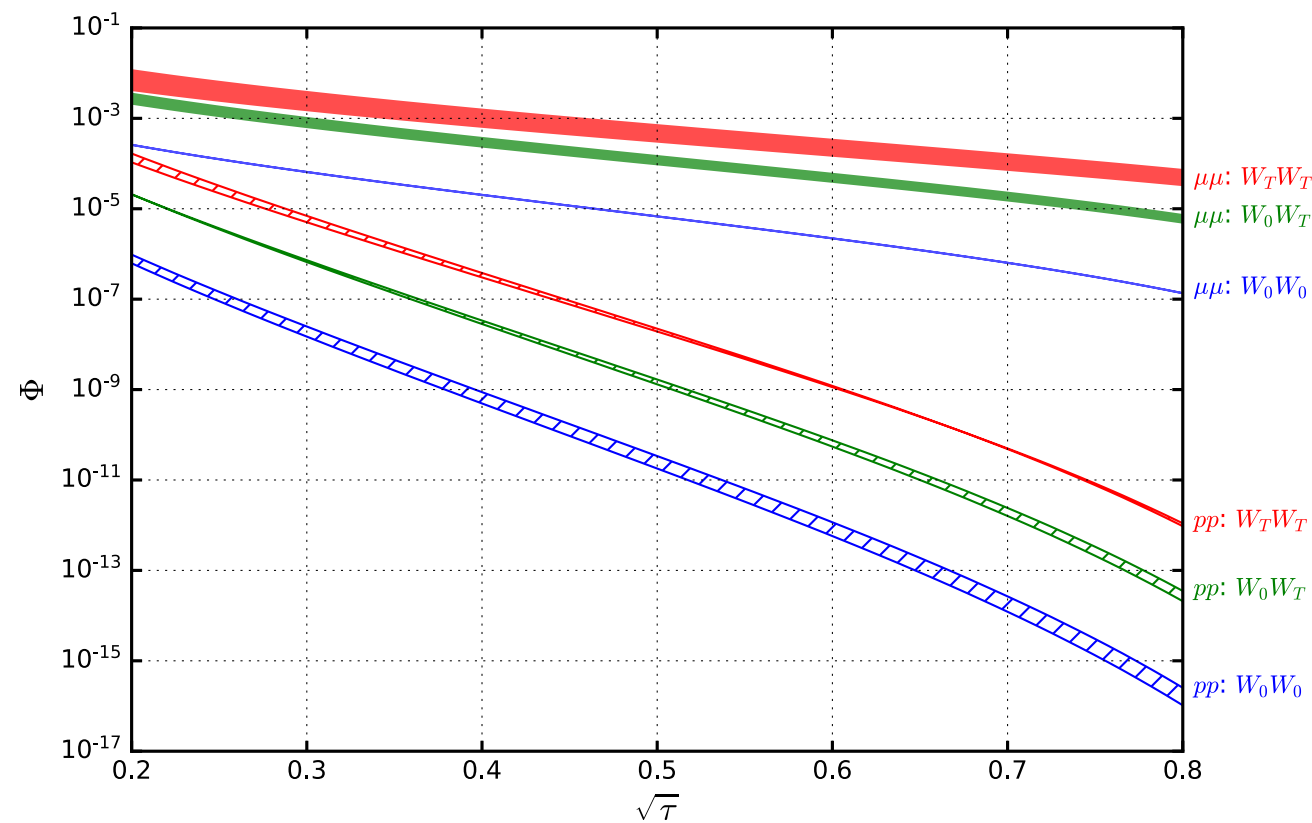
$$\Phi_{W_{\lambda_1}^+ W_{\lambda_2}^-}(\tau, \mu_f) = \int_{\tau}^1 \frac{d\xi}{\xi} f_{W_{\lambda_1}/\mu}(\xi, \mu_f) f_{W_{\lambda_2}/\mu}\left(\frac{\tau}{\xi}, \mu_f\right)$$

Muon vs Proton

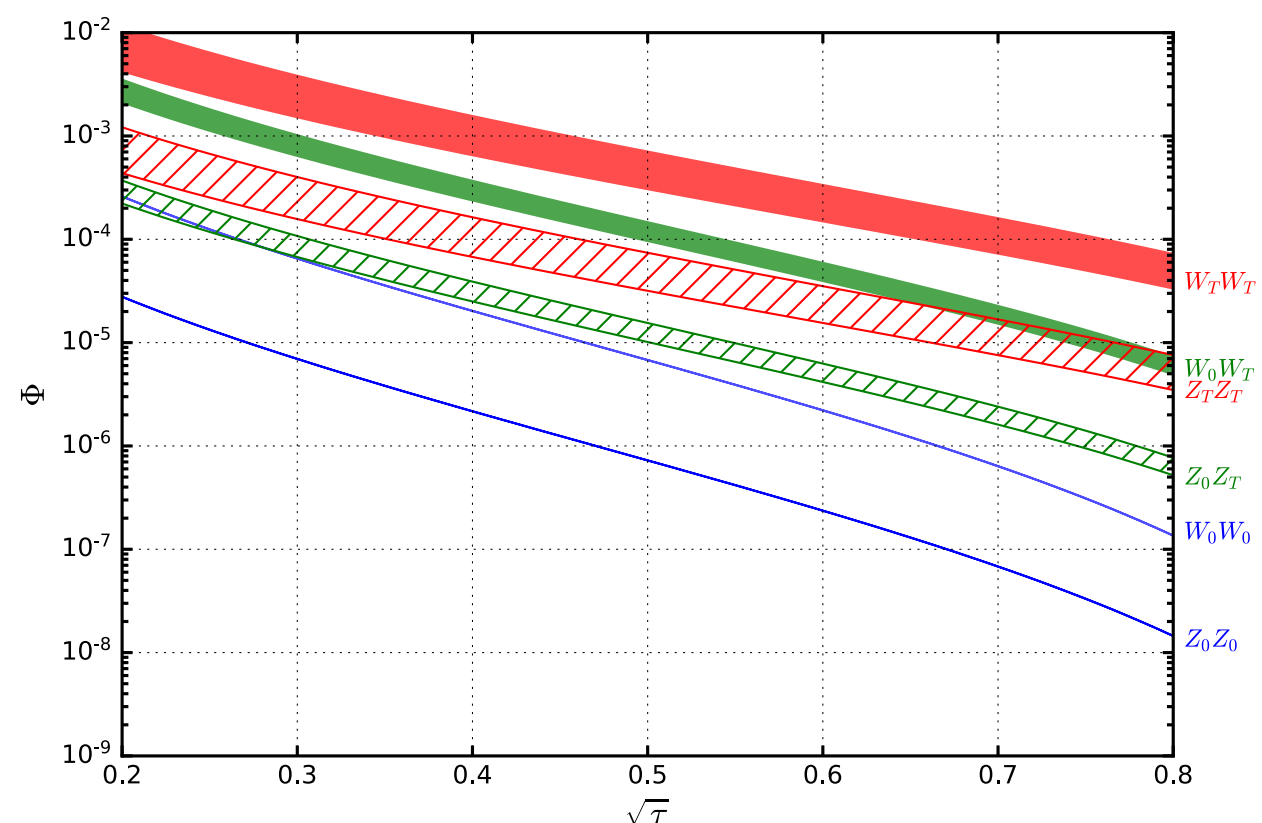


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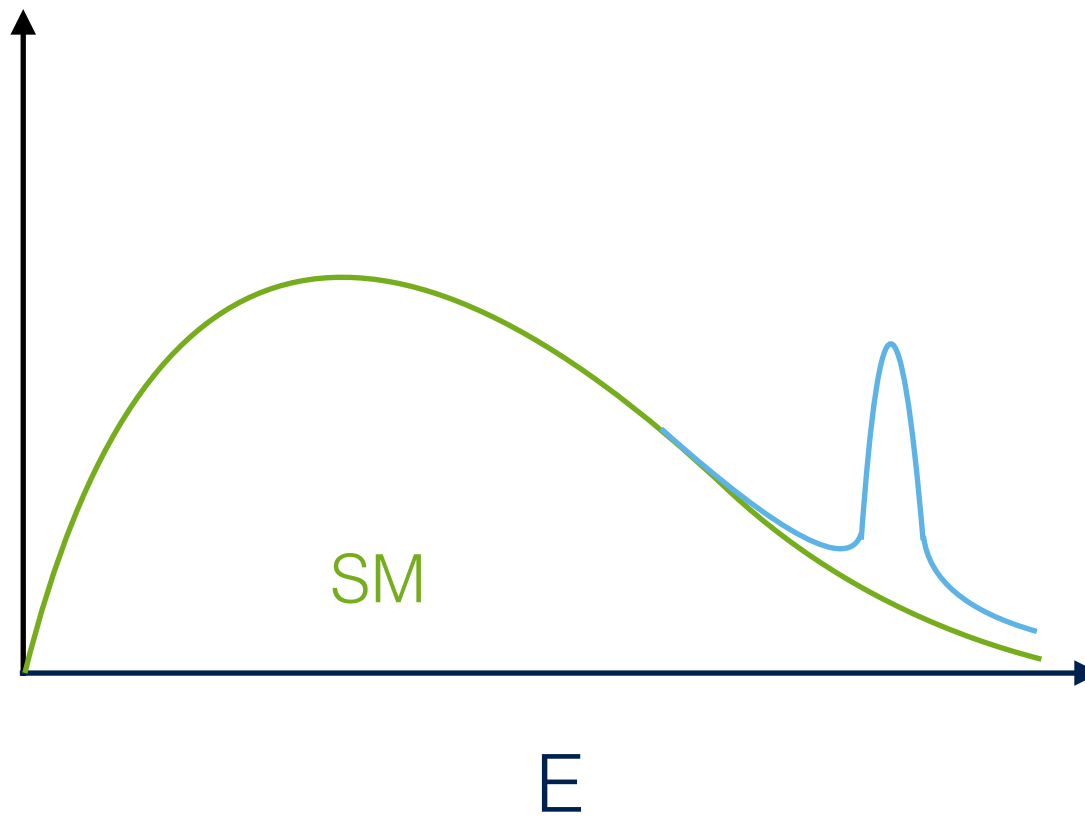
Muon vs Proton



Muon: WW vs ZZ

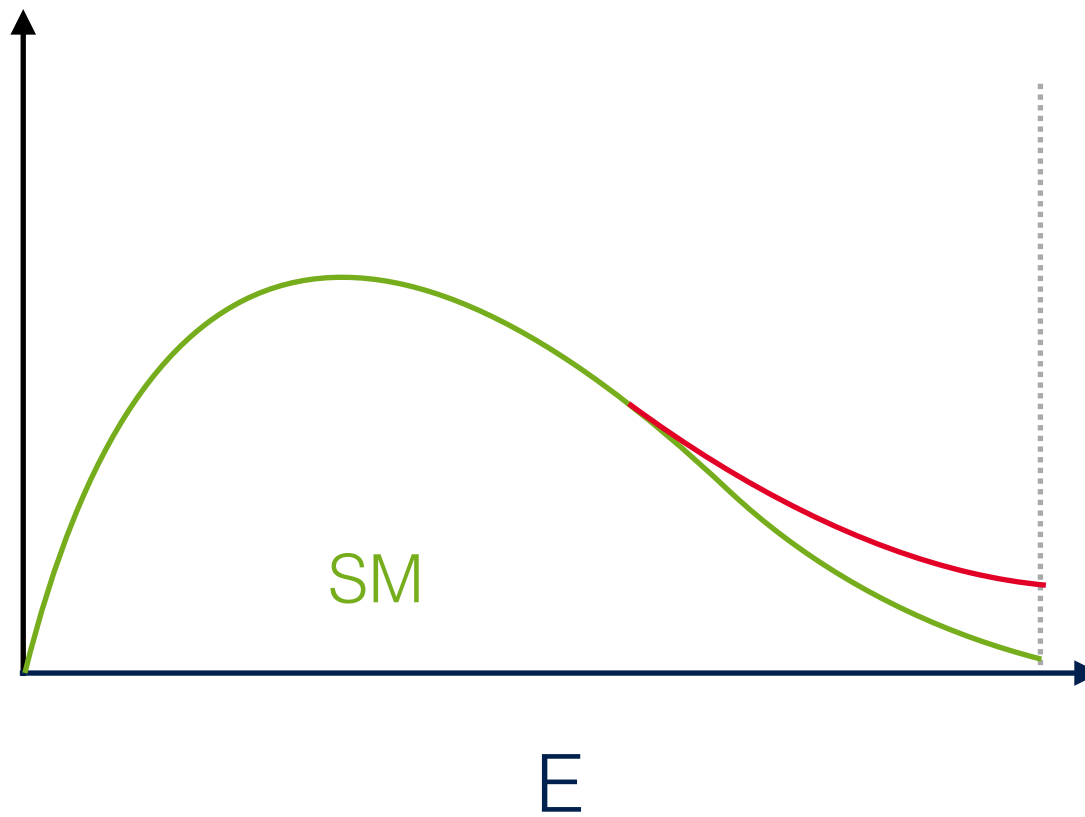


Direct search (Bumps)



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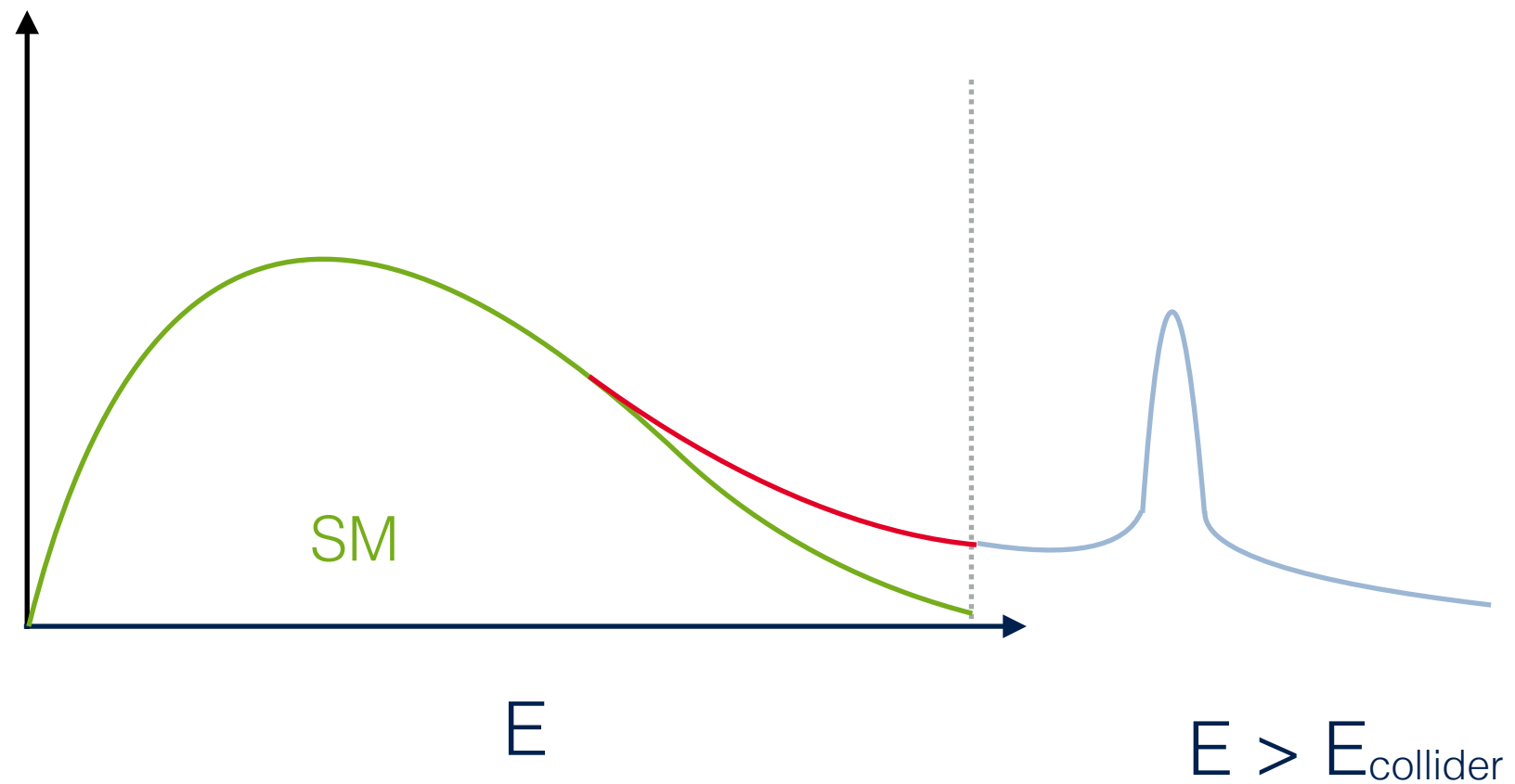
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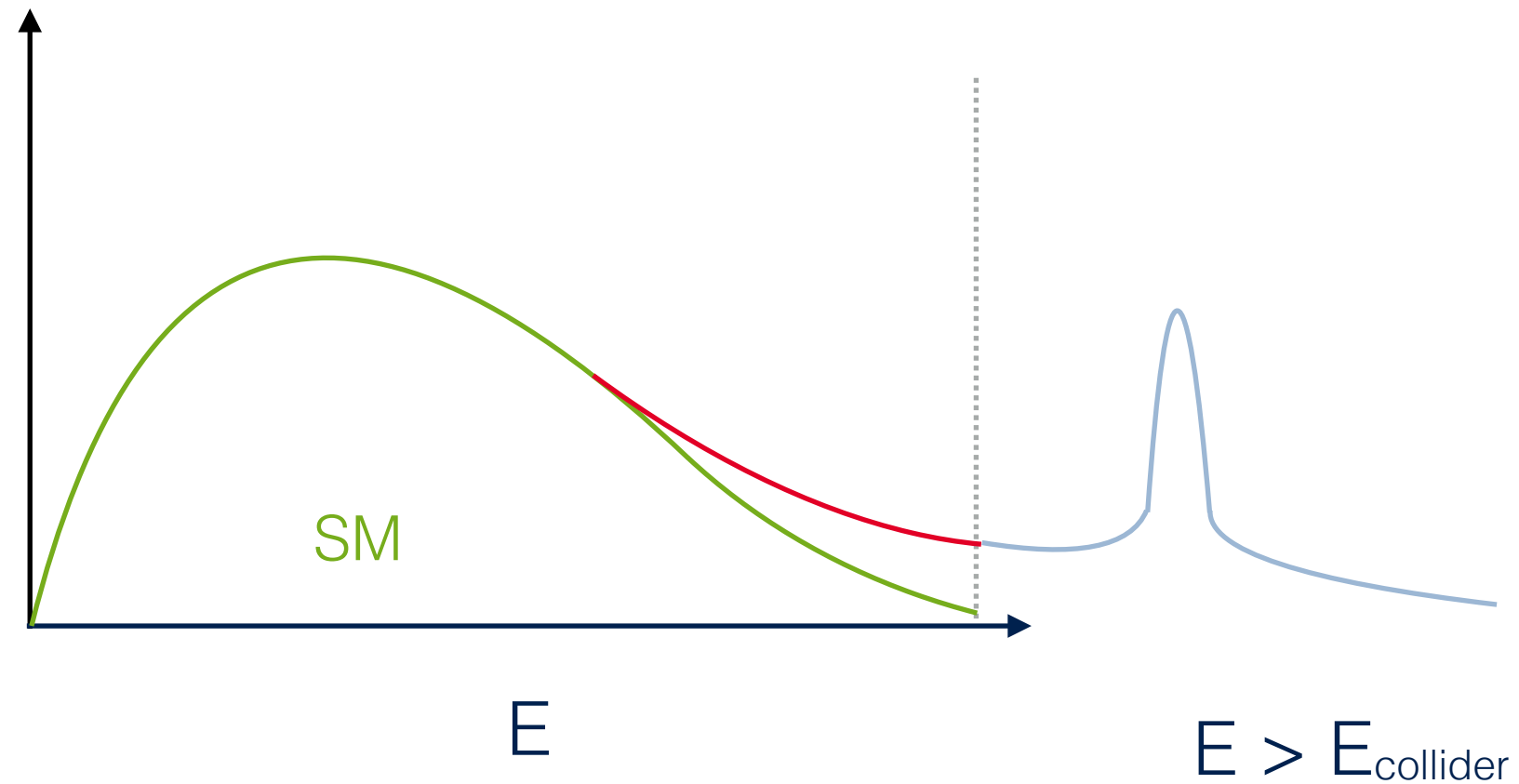
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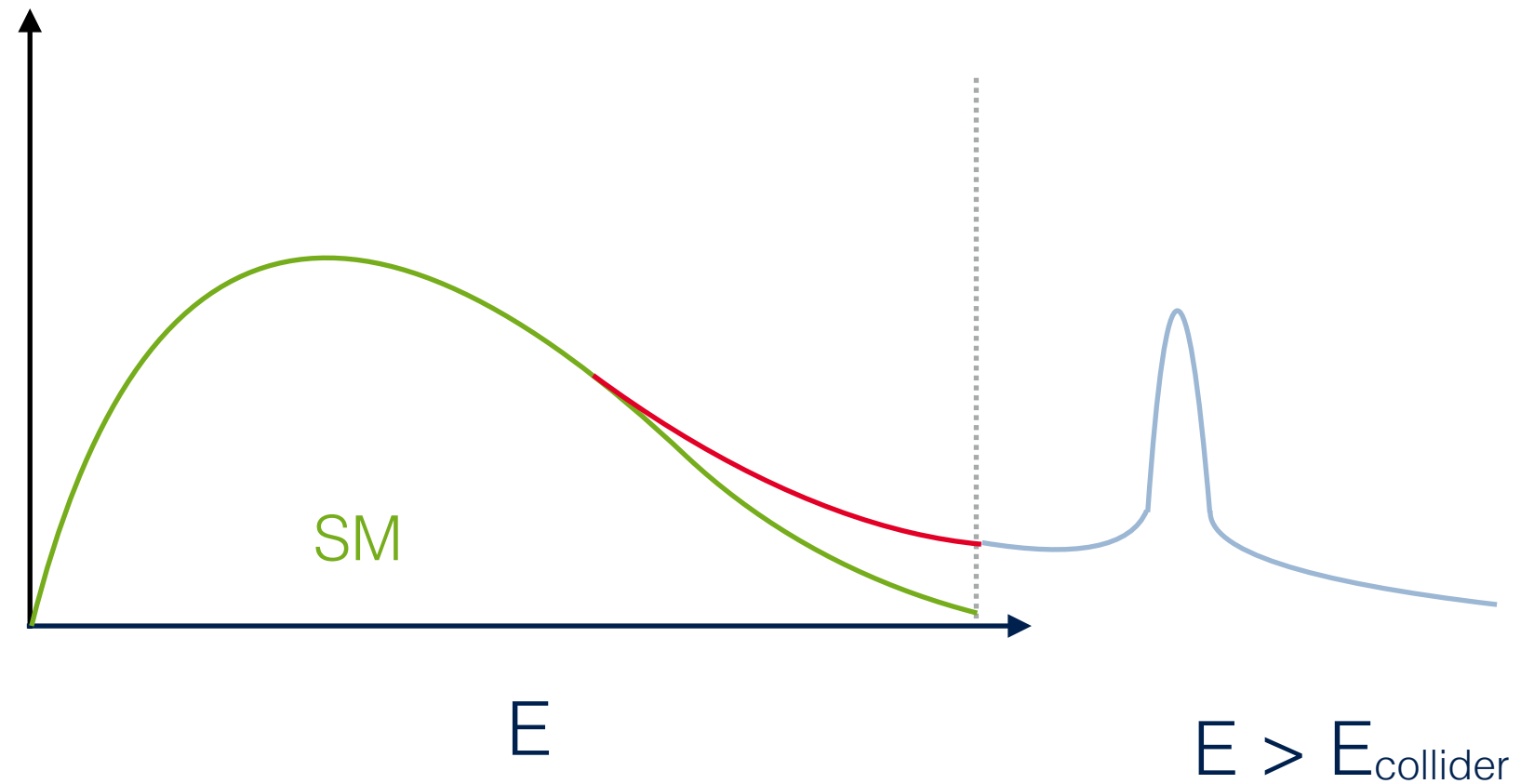


Important to assess the potential of a muon collider in indirect searches

Direct search (Bumps)

Indirect (scouting tails)

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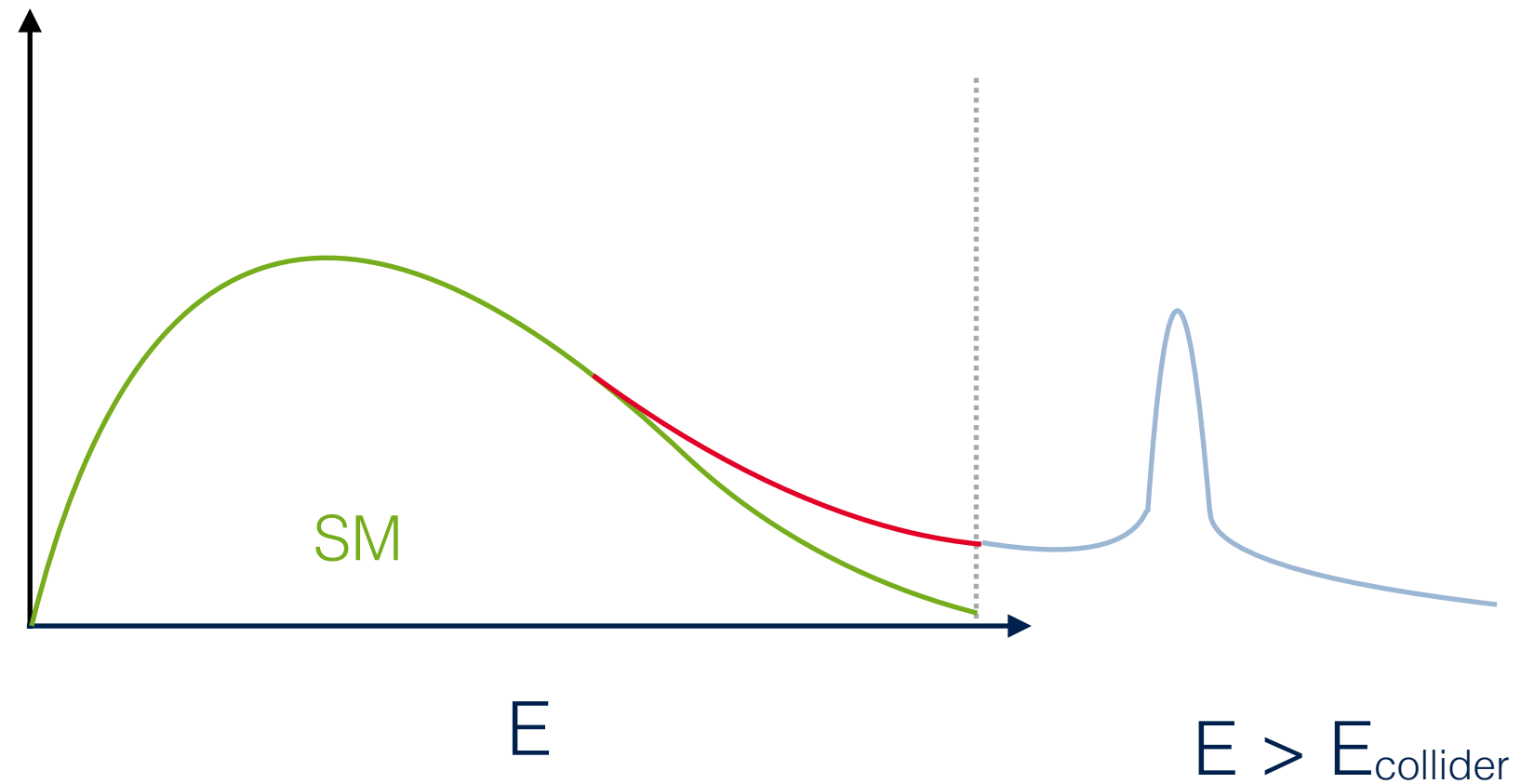
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New physics effects can lead to **unitarity violation** at high energy

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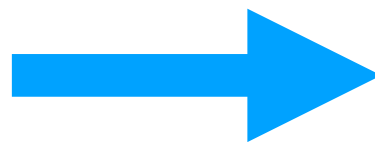
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High energy tails

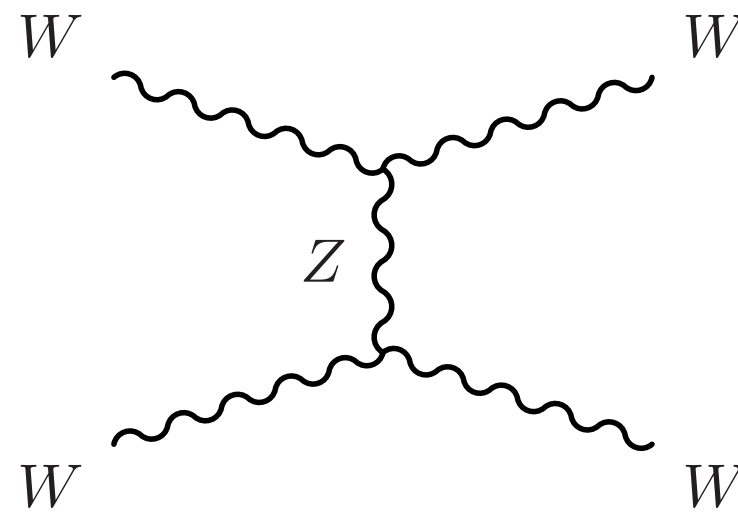
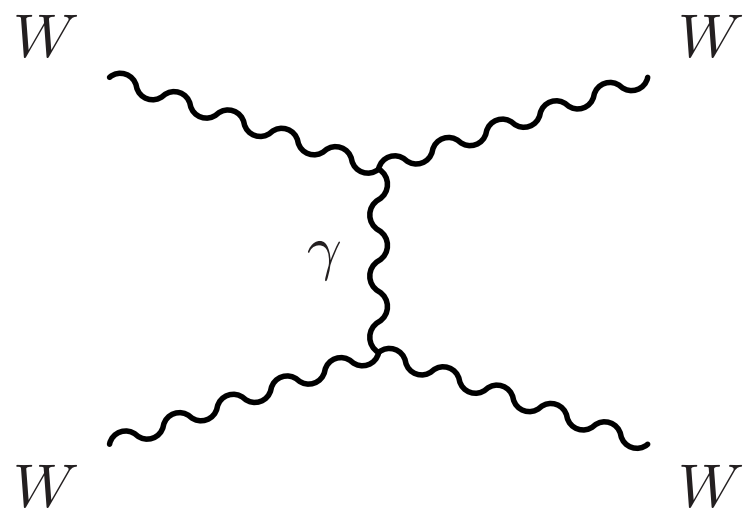


Less statistics, more sensitivity



The most well-known example is longitudinal W-boson scattering

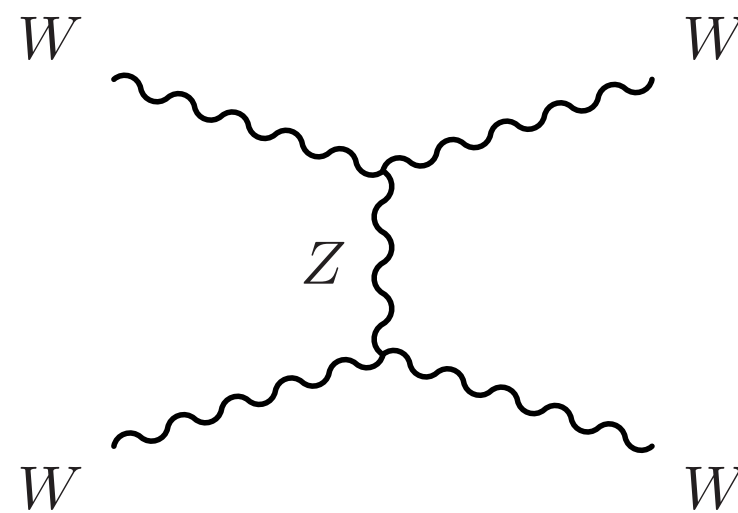
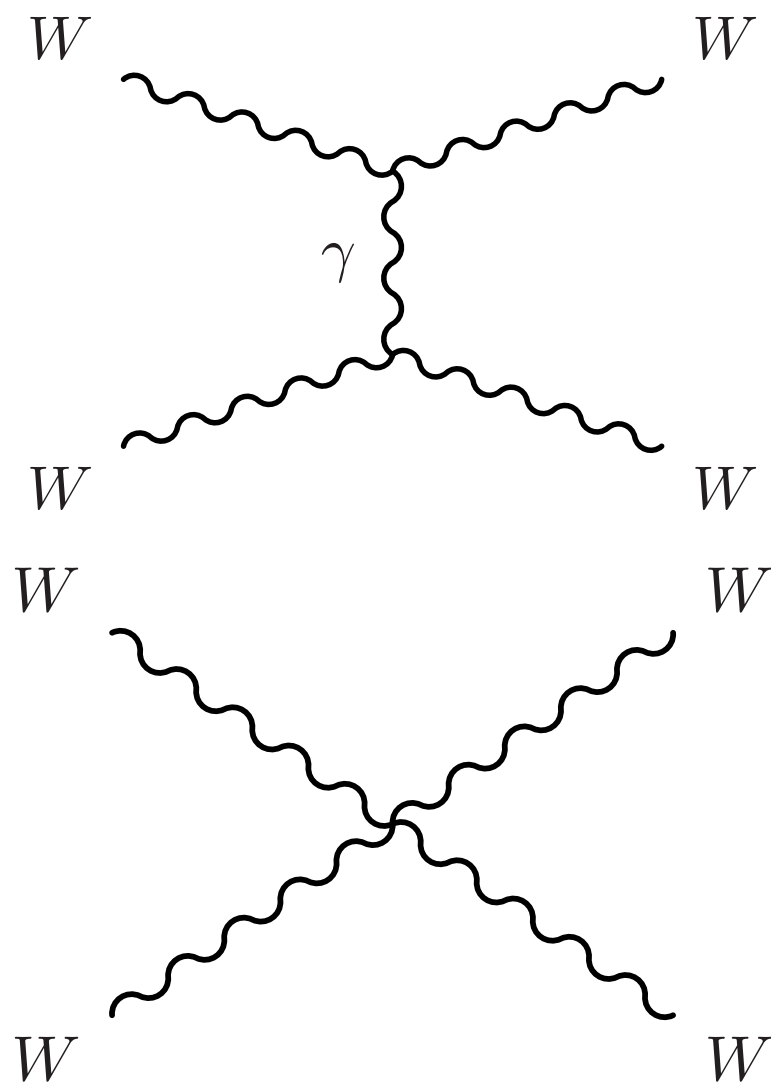
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$$\propto E^4$$

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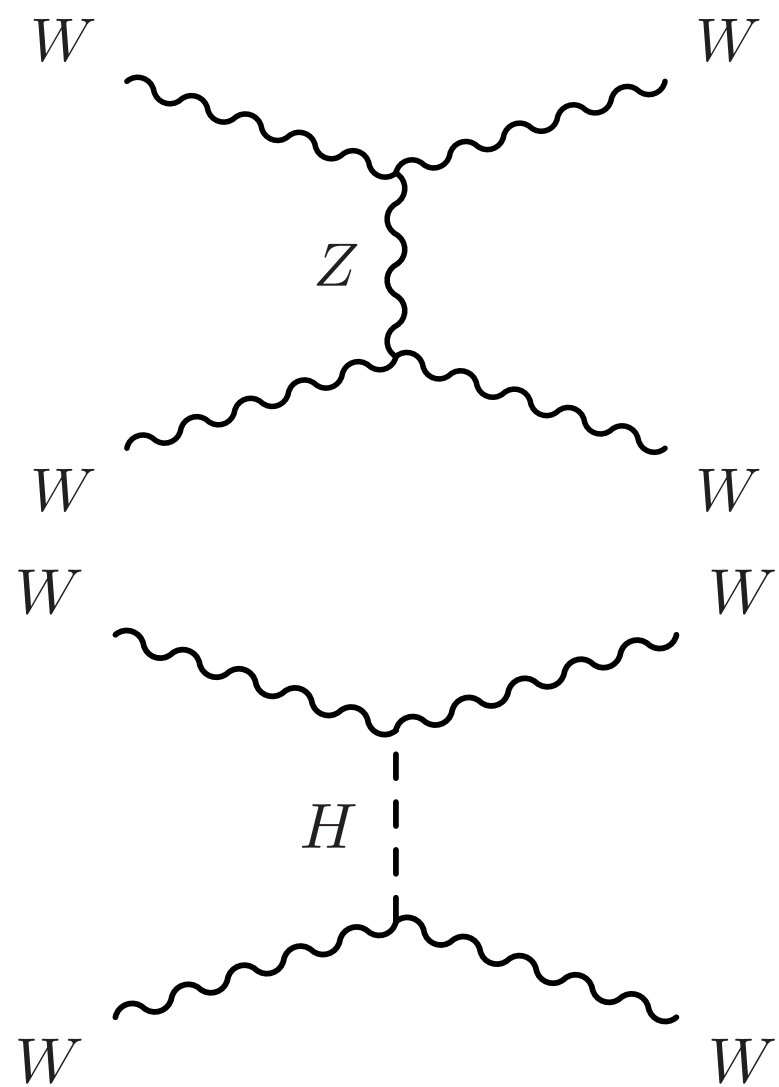
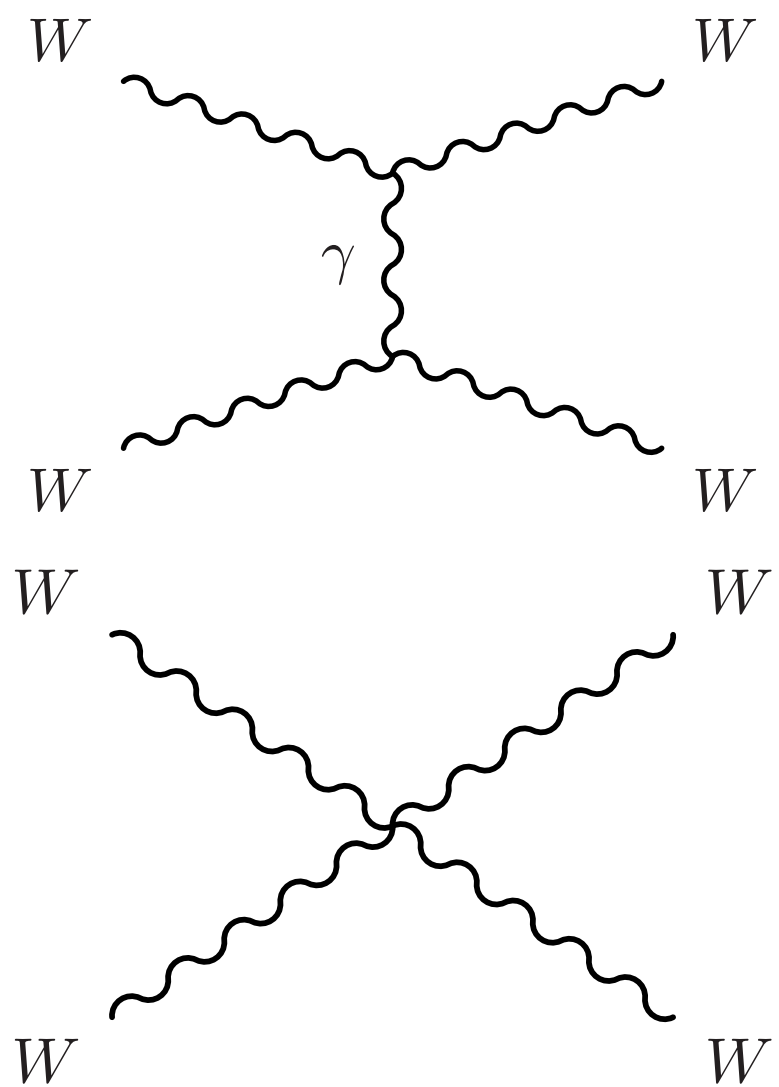
$$W_L W_L \rightarrow W_L W_L$$



$$\propto E^2$$

The most well-known example is longitudinal W-boson scattering

$$W_L W_L \rightarrow W_L W_L$$



$$\propto E^0$$



$$\mathcal{L} = \mathcal{L}_{SM} + \sum_i \frac{1}{\Lambda} \mathcal{O}_i^5 + \sum_i \frac{1}{\Lambda^2} \mathcal{O}_i^6 + \dots$$

- ❖ Higher dimensional operators preserve **SM** symmetries.
- ❖ Mappable to a large class of **BSM** models.
- ❖ Lambda is scale of NP, allows us to truncated the series.

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Dim 6 operators introduce energy growing effects

$$\mathcal{M} \sim \mathcal{M}_{SM} \left(1 + C_i \frac{v^2}{\Lambda^2} + C_j \frac{vE}{\Lambda^2} + C_k \frac{E^2}{\Lambda^2} \right) \quad E < \Lambda$$

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$$\sigma = \sigma_{SM} + \sum_i c_i \sigma_{Int}^i + \sum_{i,j} c_{i,j} \sigma_{Sq}^{i,j}$$

Sensitivity linear

Sensitivity quadratic

$$R(c_i) \equiv \frac{\sigma}{\sigma_{SM}} = 1 + c_i \frac{\sigma_{Int}^i}{\sigma_{SM}} + c_i^2 \frac{\sigma_{Sq}^{i,i}}{\sigma_{SM}} = 1 + c_i r_i + c_i^2 r_{i,i}$$

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@LHC

**Significant challenges: signal to background ratio not good.
Diboson production dominates.**

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Caveat: SMEFT should be treated **globally.
Currently no global analysis including VBS exists.**

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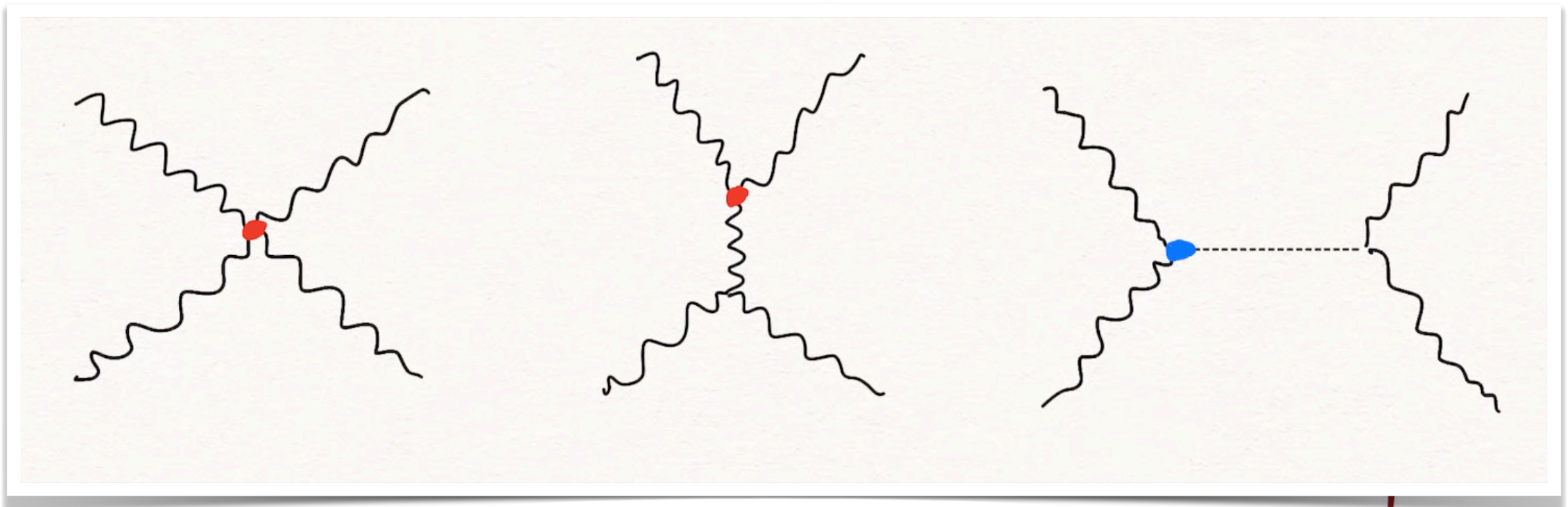
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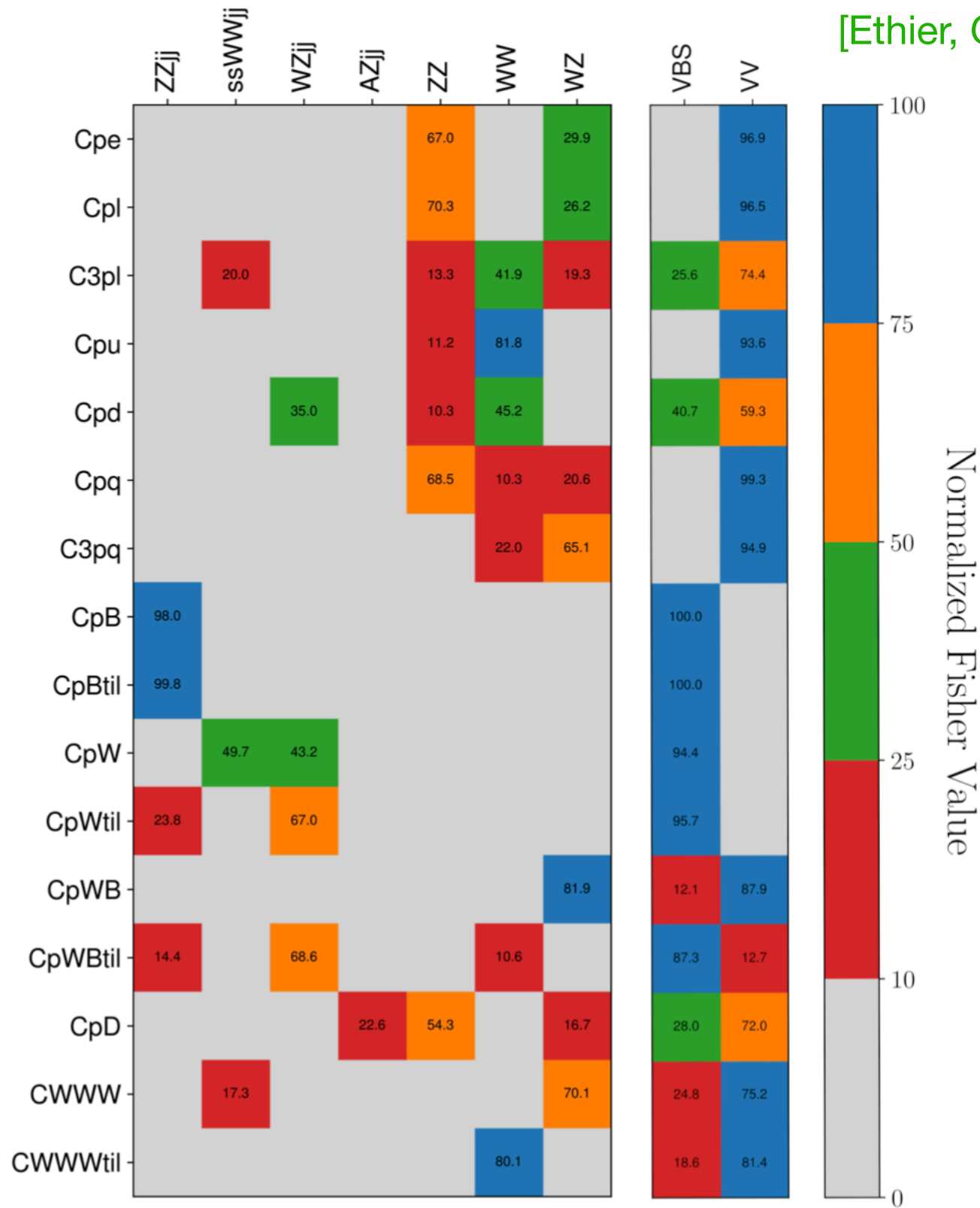
**Simplified analysis can nonetheless bring useful information
and help in understanding the underlying phenomenology.**



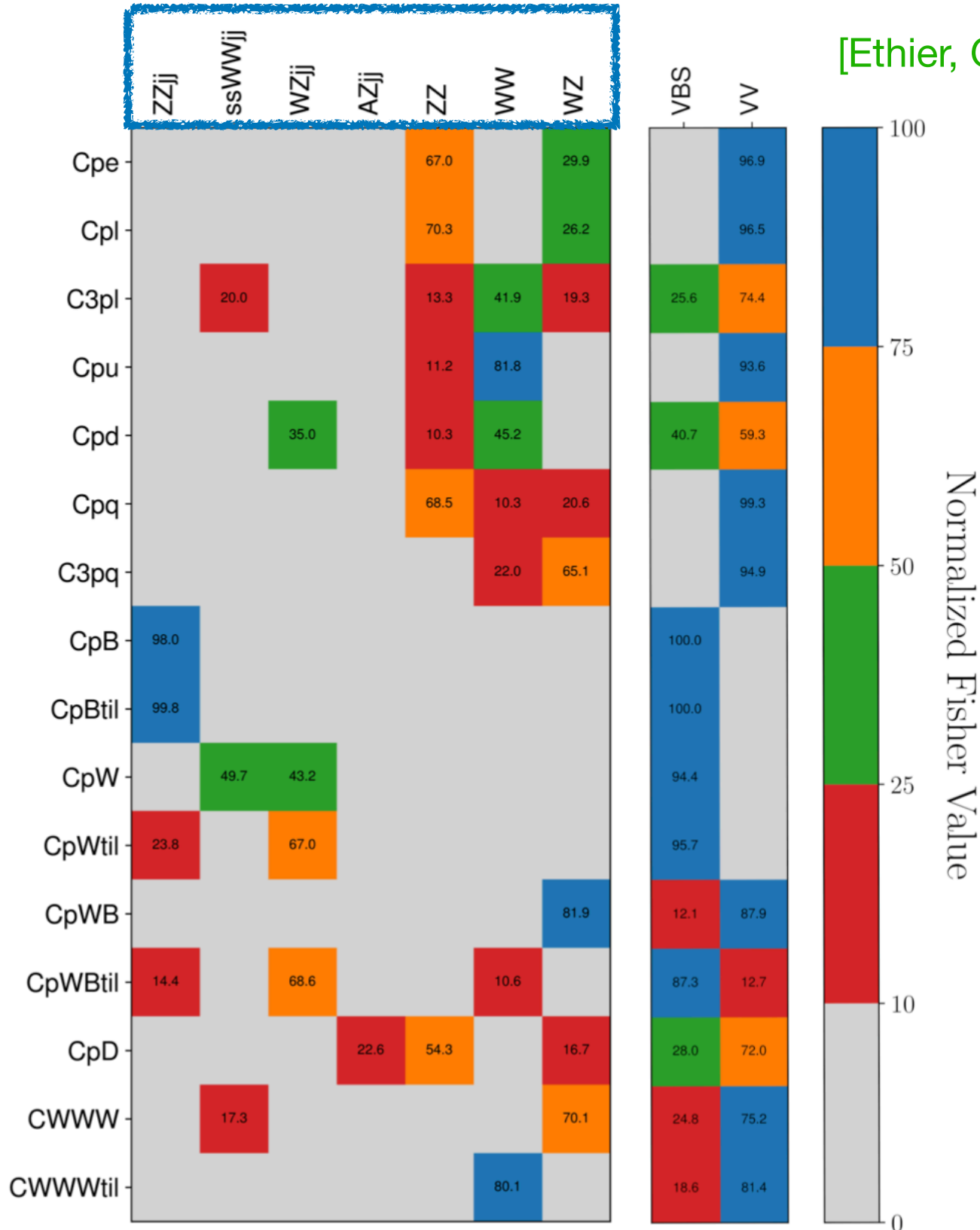
Operator	Coefficient	Definition
\mathcal{O}_W	c_W	$\epsilon^{IJK} W_{\mu}^{I\nu} W_{\nu}^{J\rho} W_{\rho}^{K\mu}$
$\mathcal{O}_{\varphi W}$	$c_{\varphi W}$	$(\varphi^\dagger \varphi - \frac{v^2}{2}) W_{\mu\nu}^I W^{I\mu\nu}$
$\mathcal{O}_{\varphi B}$	$c_{\varphi B}$	$(\varphi^\dagger \varphi - \frac{v^2}{2}) B_{\mu\nu} B^{\mu\nu}$
$\mathcal{O}_{\varphi WB}$	$c_{\varphi WB}$	$(\varphi^\dagger \sigma_I \varphi) W_{\mu\nu}^I B^{\mu\nu}$
$\mathcal{O}_{\varphi D}$	$c_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$



[Ethier, Gomez-Ambrosio, Magni, Rojo arXiv:2101.03180]



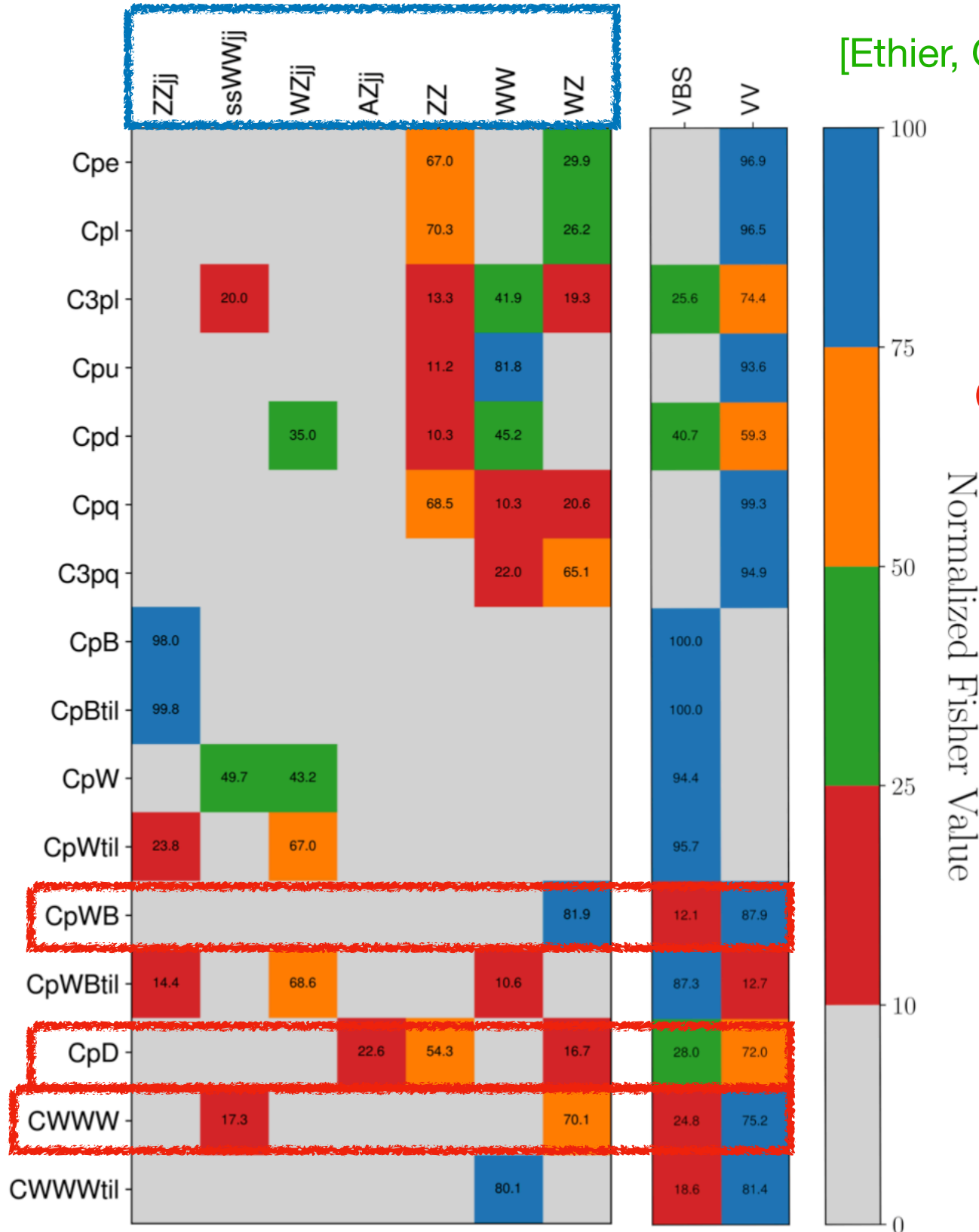
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Processes included in the fit



[Ethier, Gomez-Ambrosio, Magni, Rojo arXiv:2101.03180]

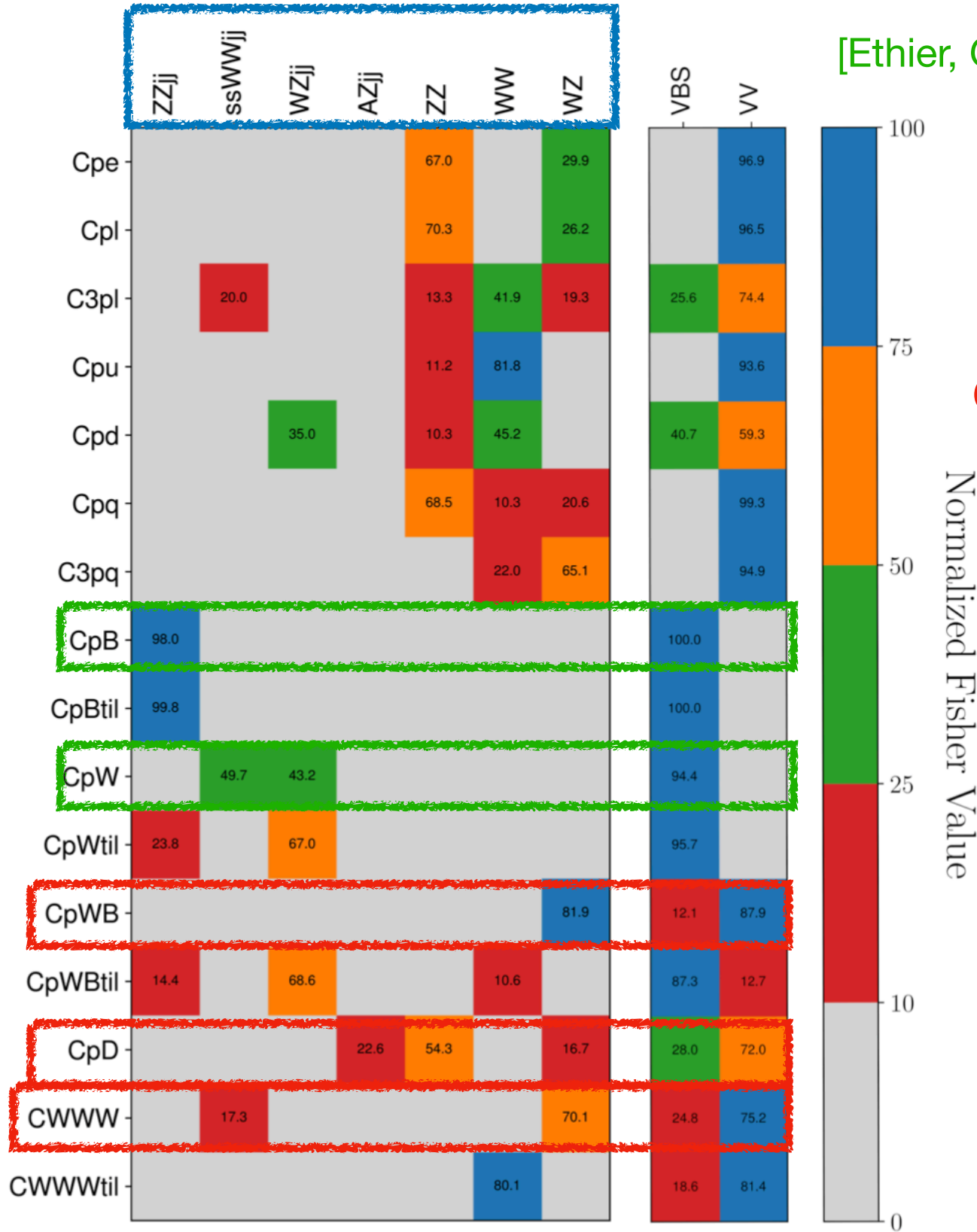


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More information in diboson.
CpD and CpWB also constrained by EWPO



[Ethier, Gomez-Ambrosio, Magni, Rojo arXiv:2101.03180]

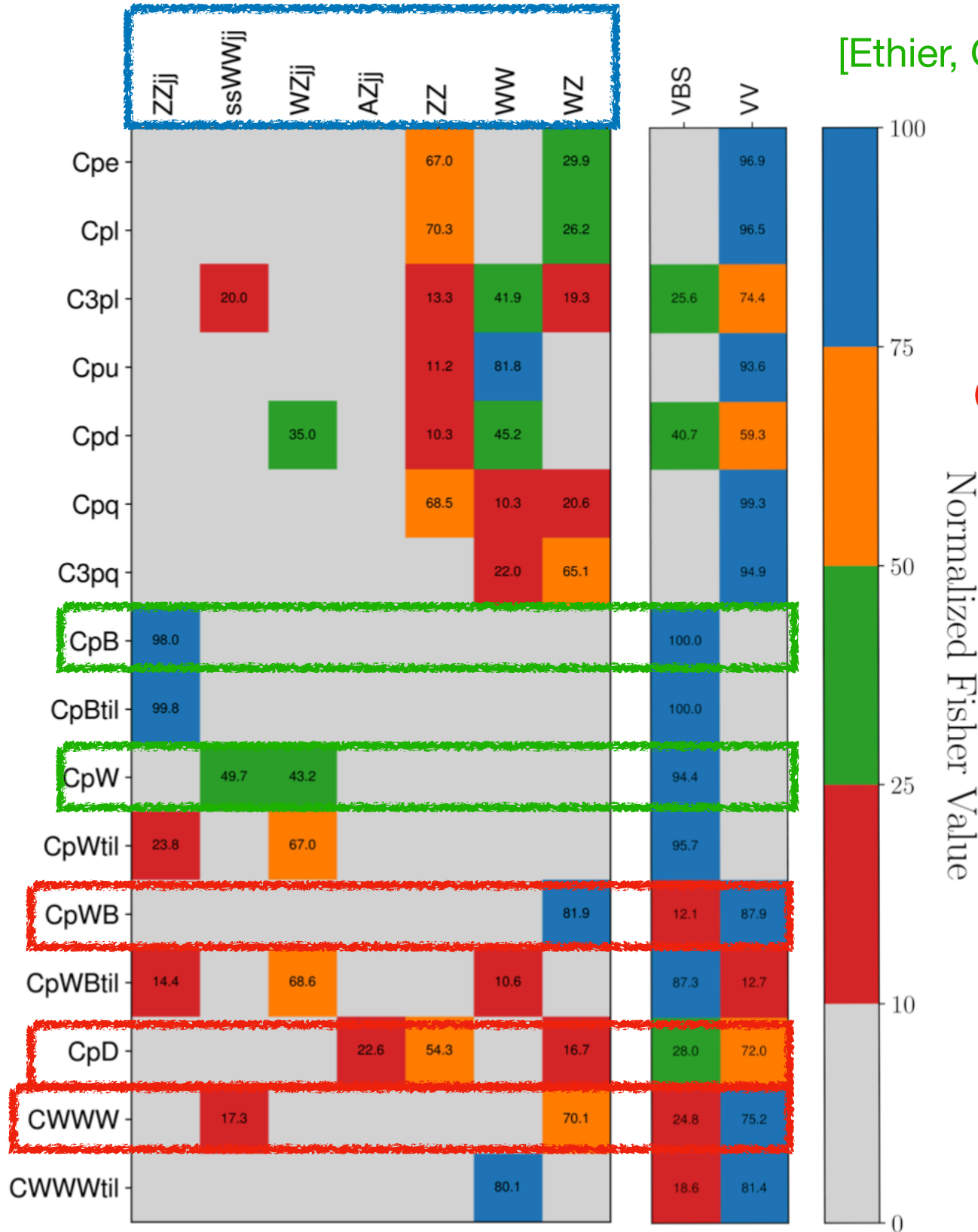


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Basically unconstrained by diboson.
This is where VBS brings useful info.

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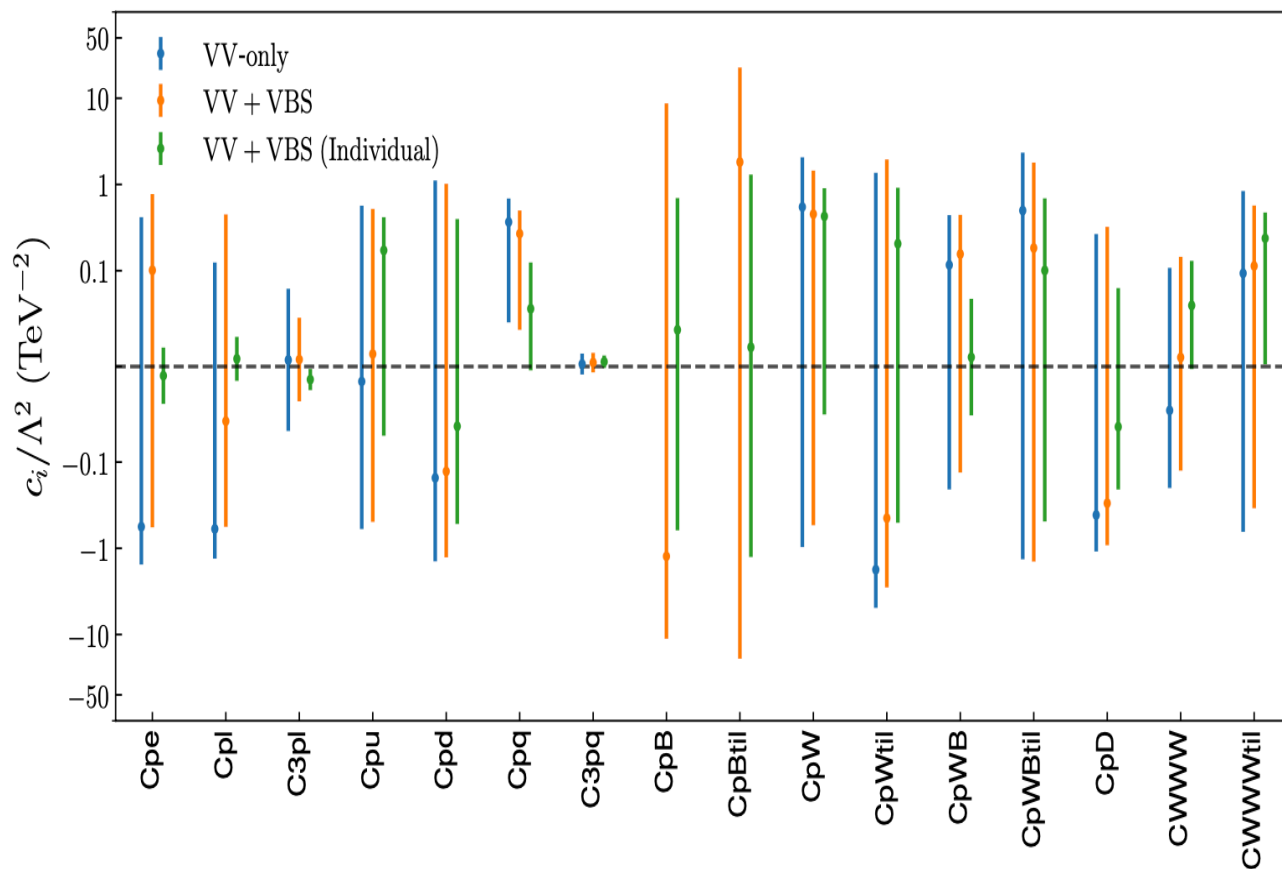
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This is where VBS brings useful info.

All the 2F operators included
in this broad analysis are better
constrained by other processes.

[Ethier, Gomez-Ambrosio, Magni, Rojo
arXiv:2101.03180] **Talk by Raquel**
for more details

Linear fit



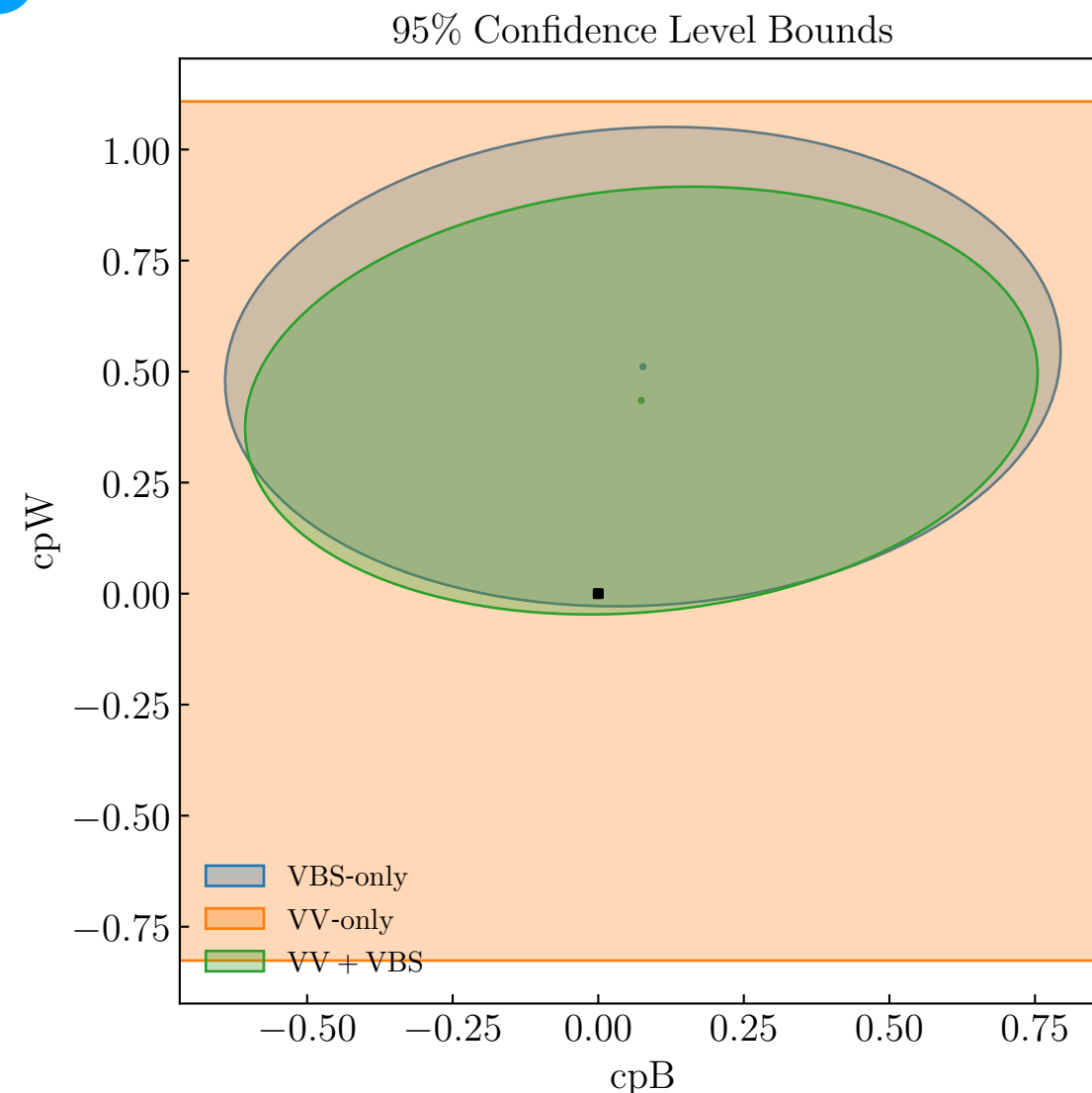
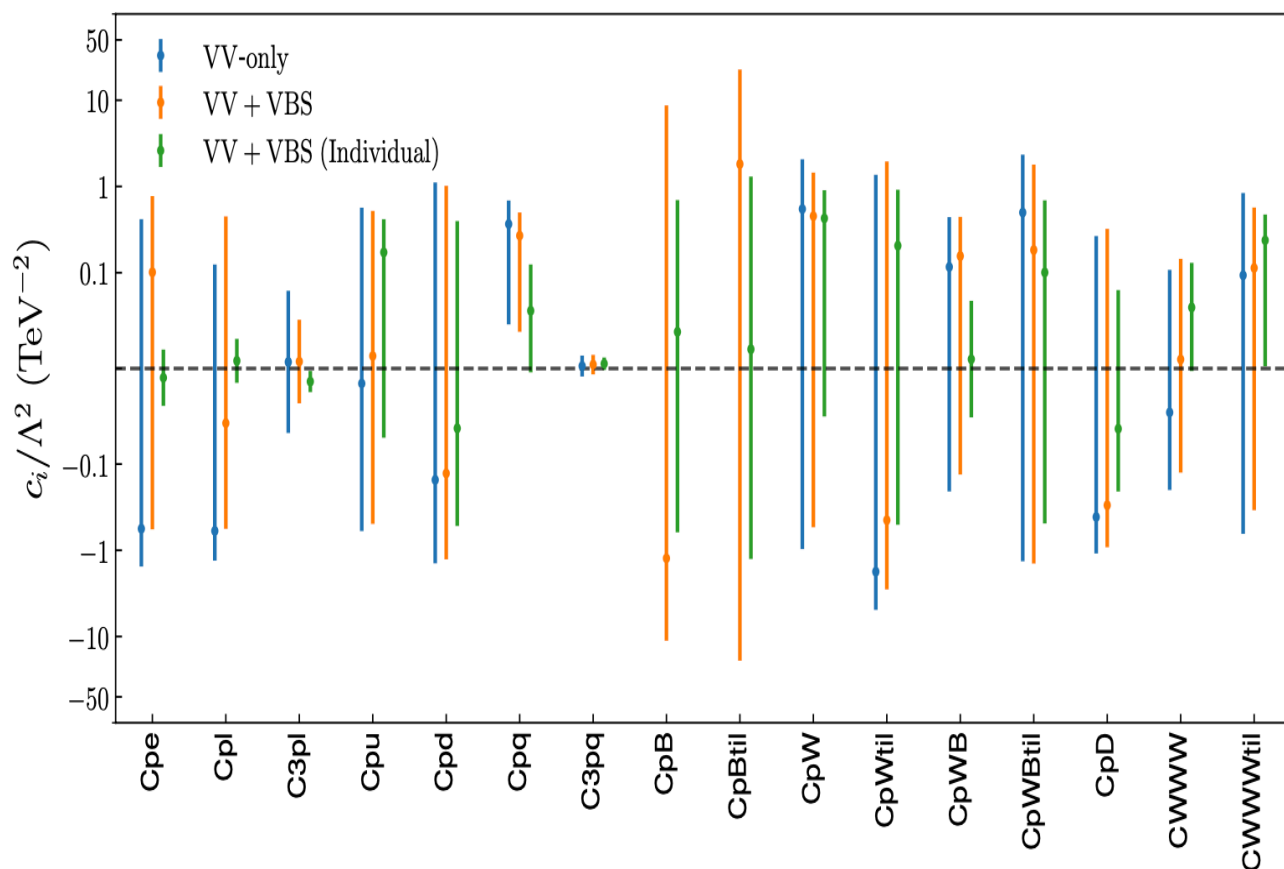
$$C_{\varphi W} \sim [-0.55, 1.4]$$

$$C_{\varphi B} \sim [-11, 8.8]$$



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$$C_{\varphi W} \sim [-0.05, 0.92]$$

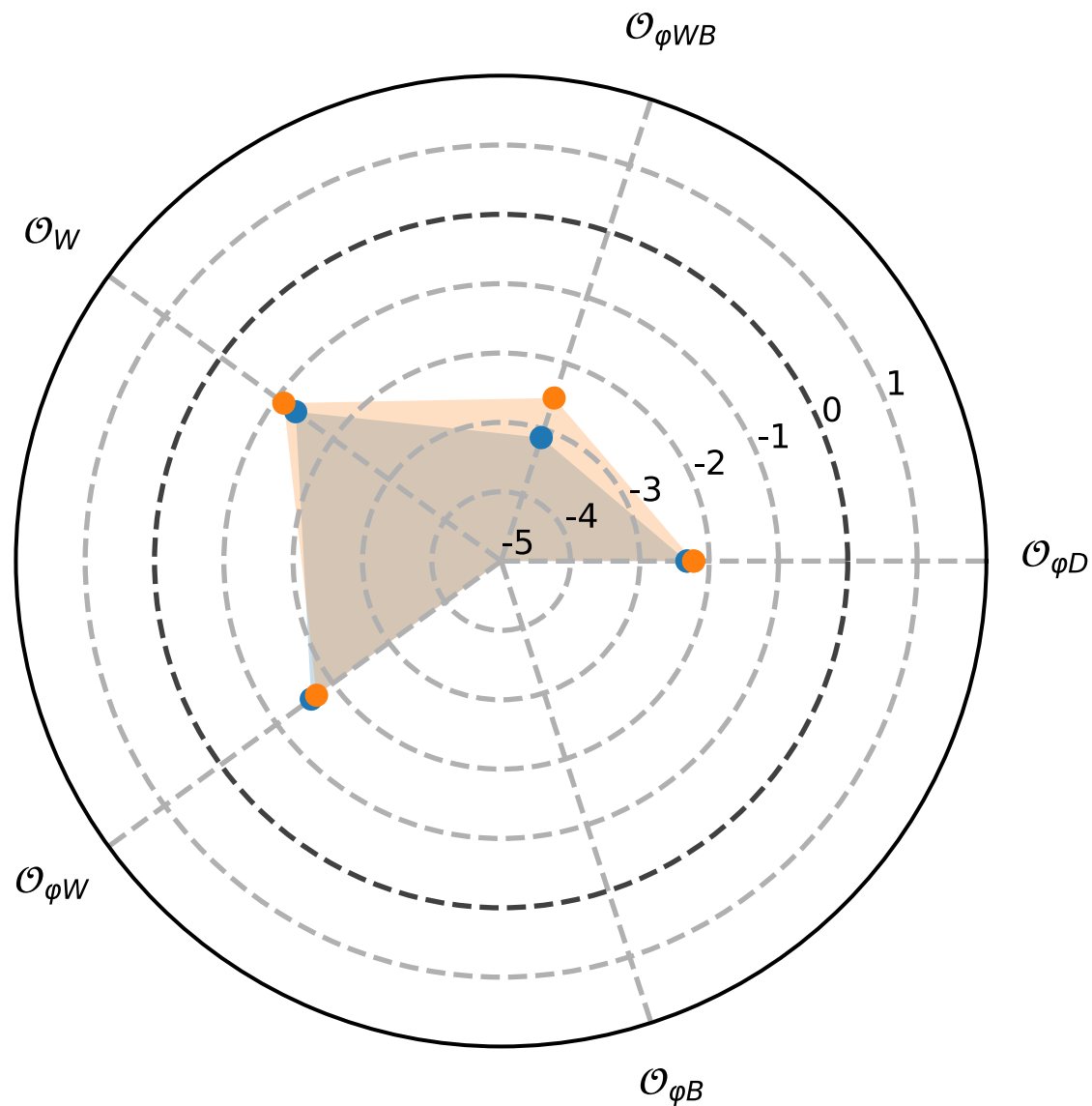
$$C_{\varphi B} \sim [-0.60, 0.75]$$



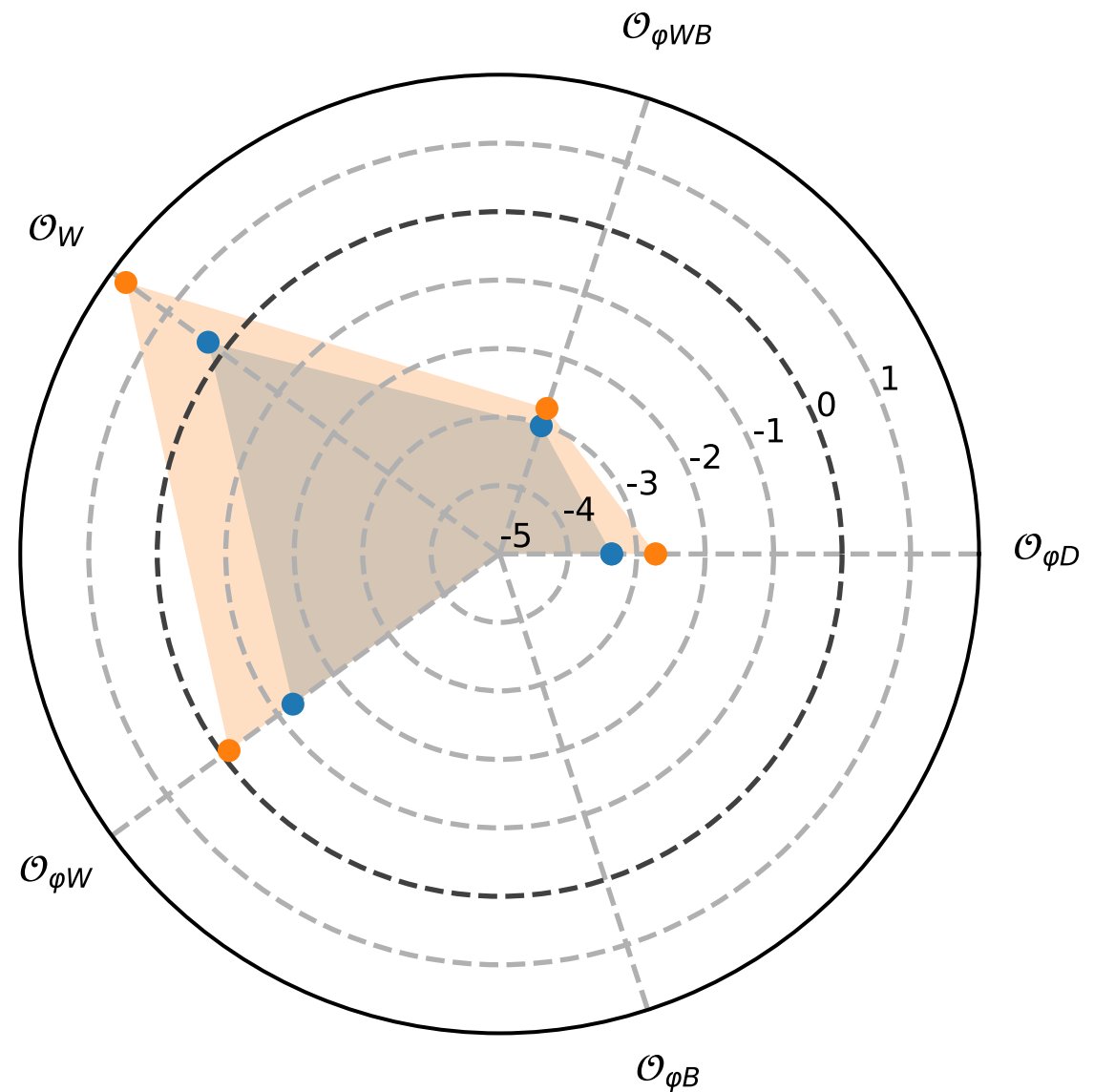
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$WW \rightarrow W^+ W^-$

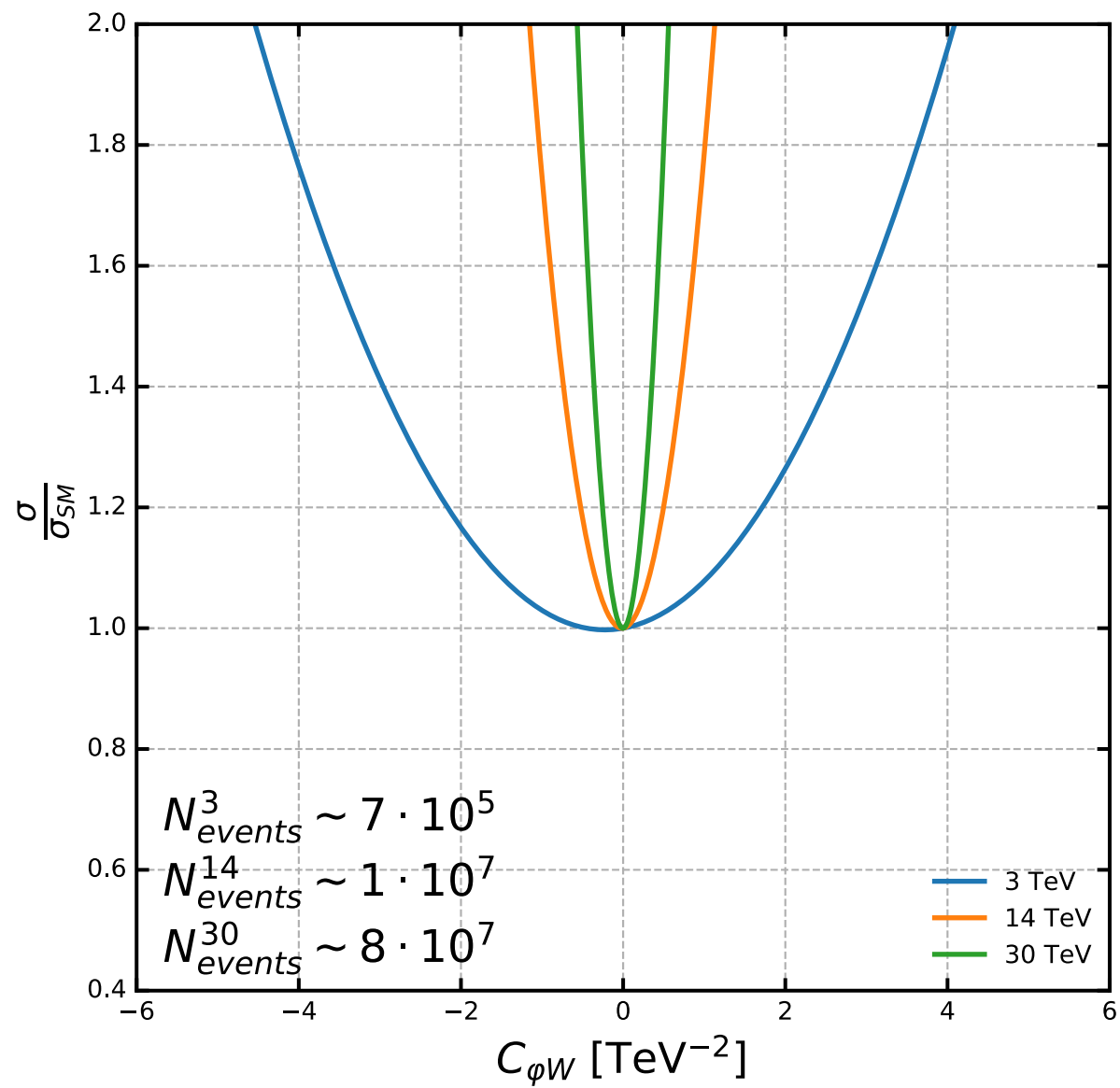
$\log(r_i)$



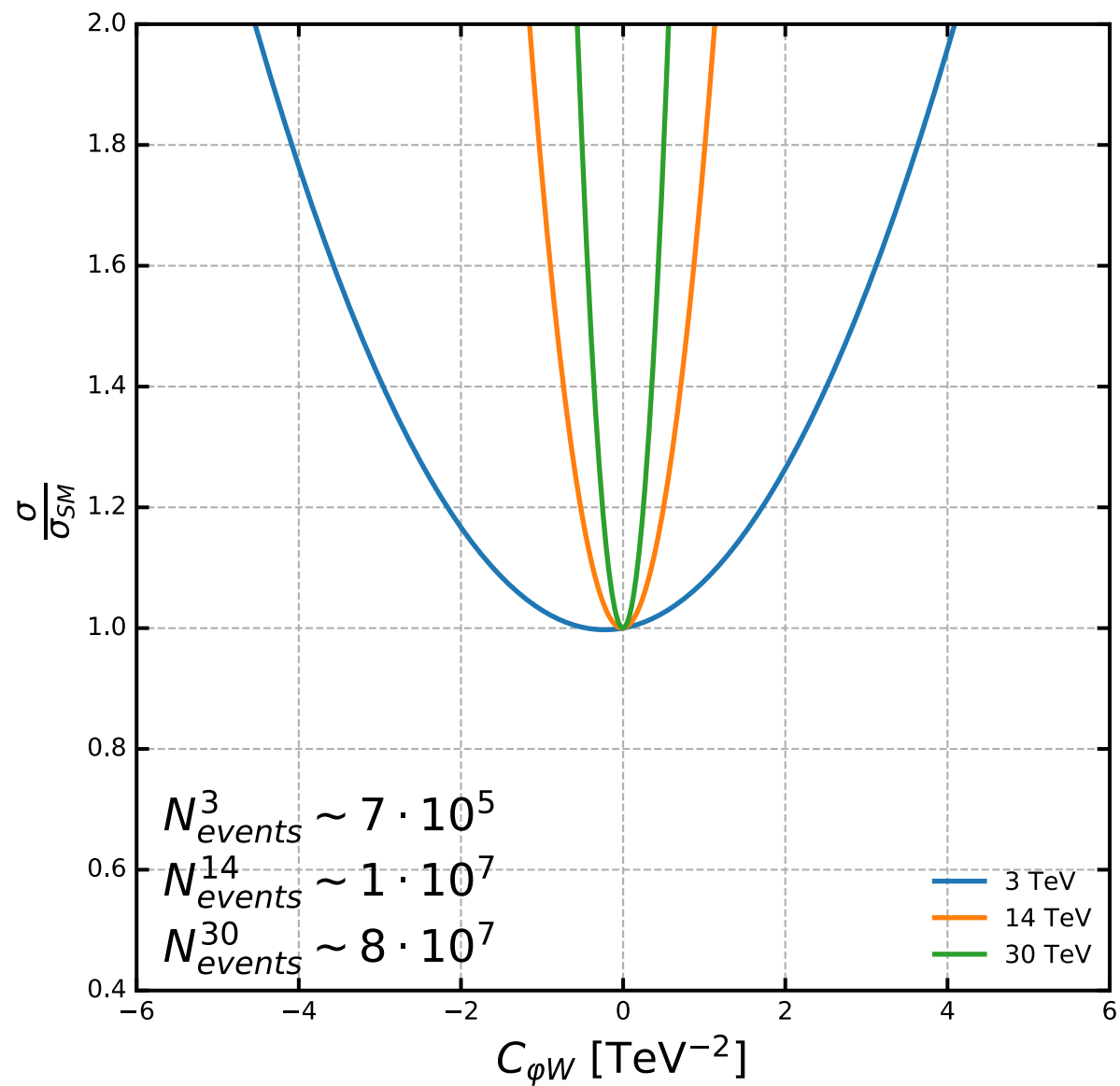
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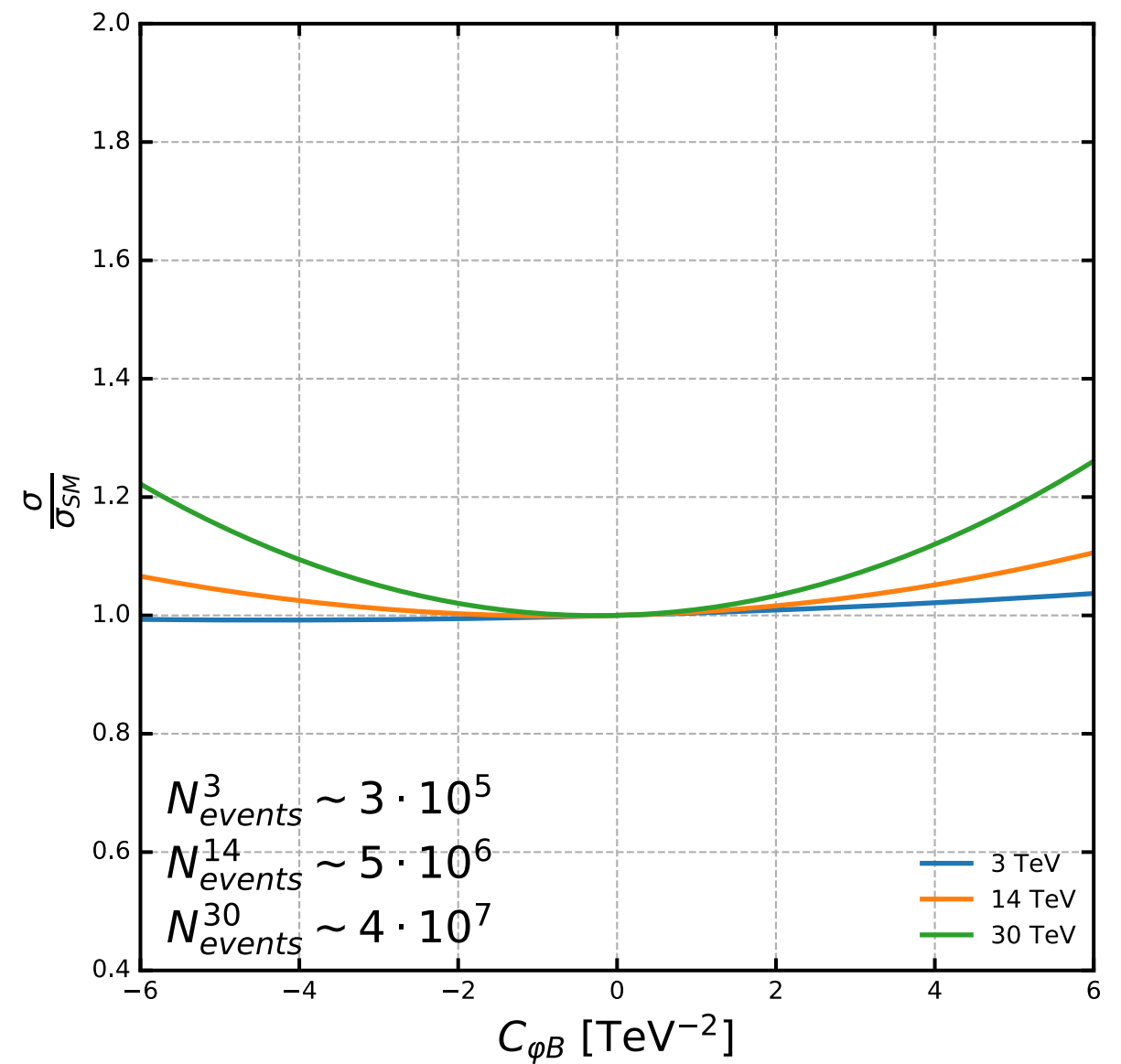
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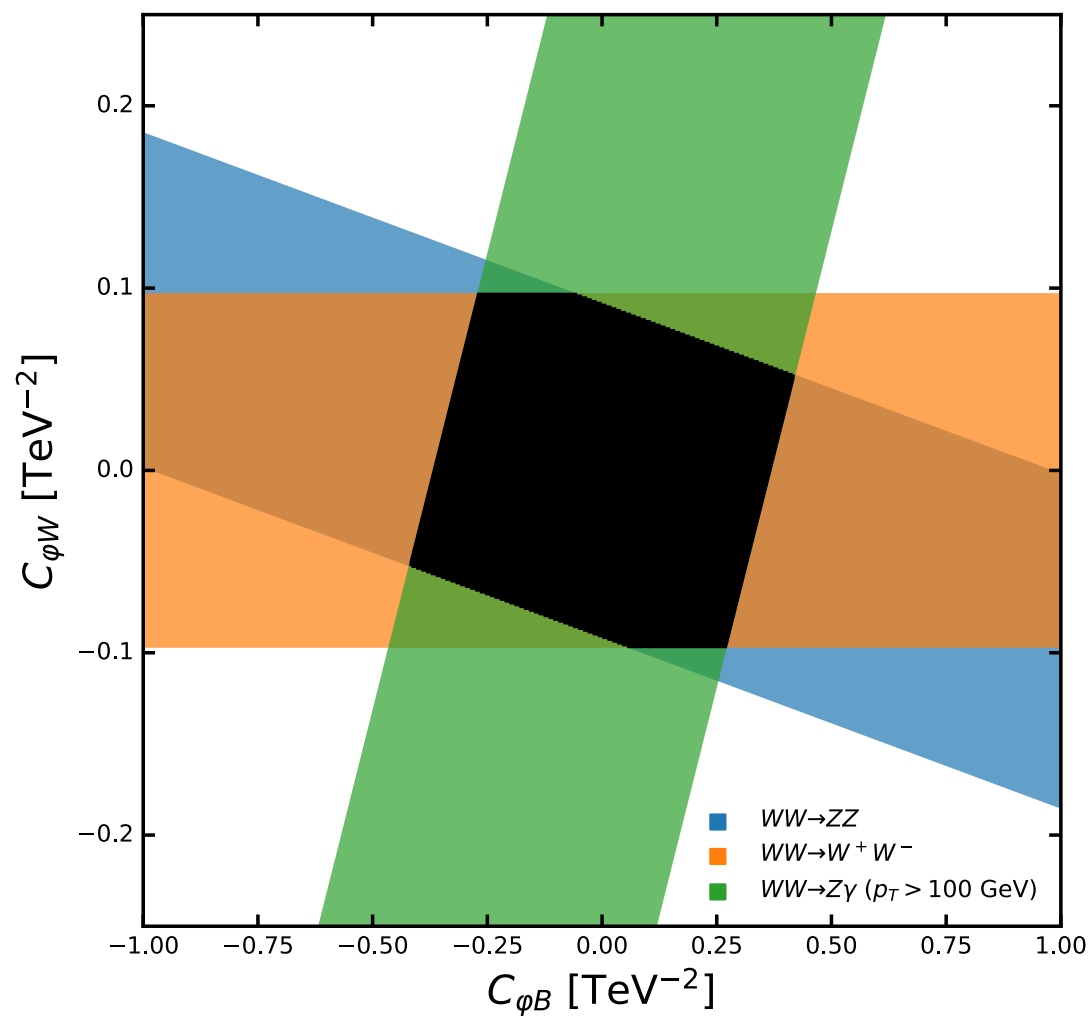
ZZ



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3 TeV

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$$C_{\phi B} \sim [-0.42, 0.42]$$

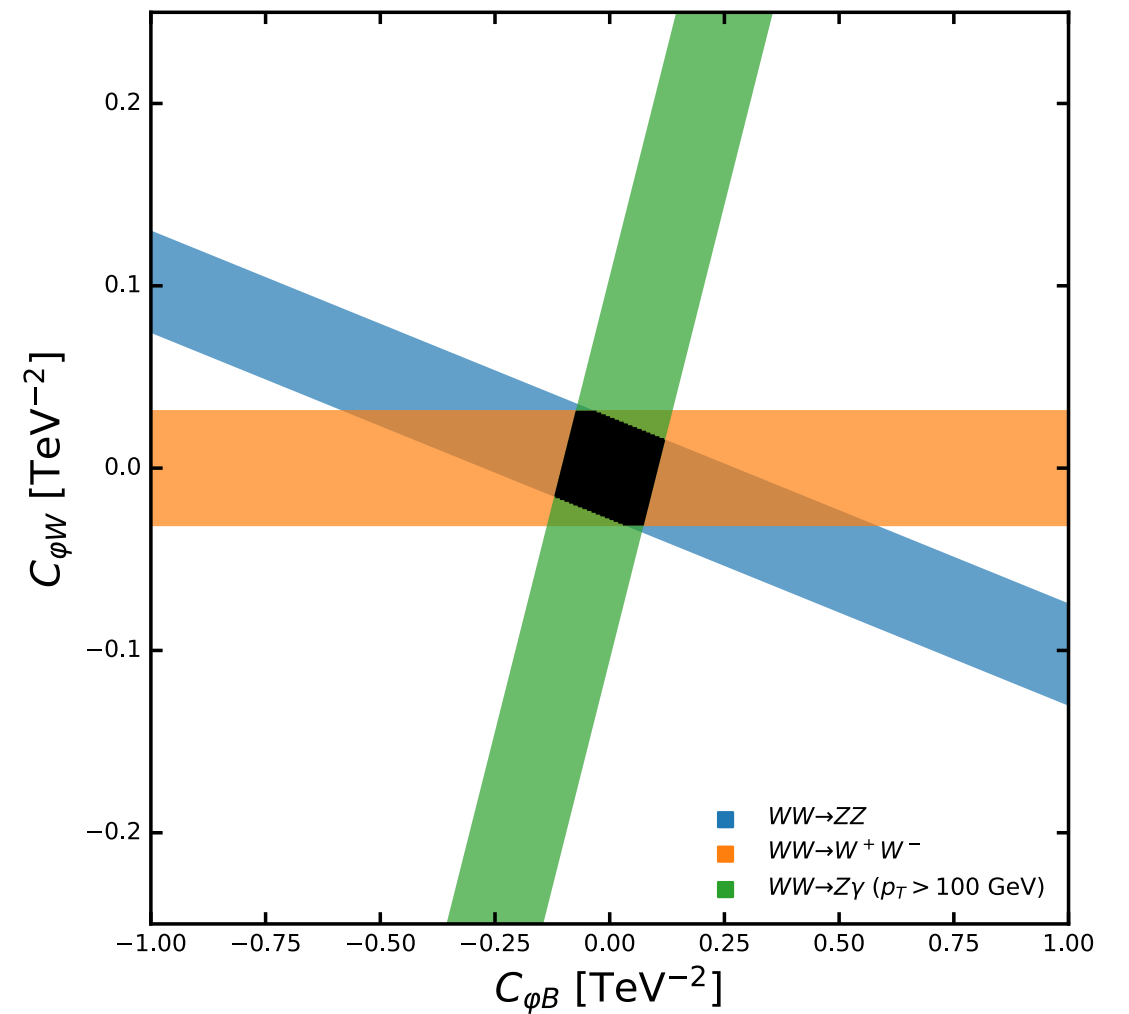
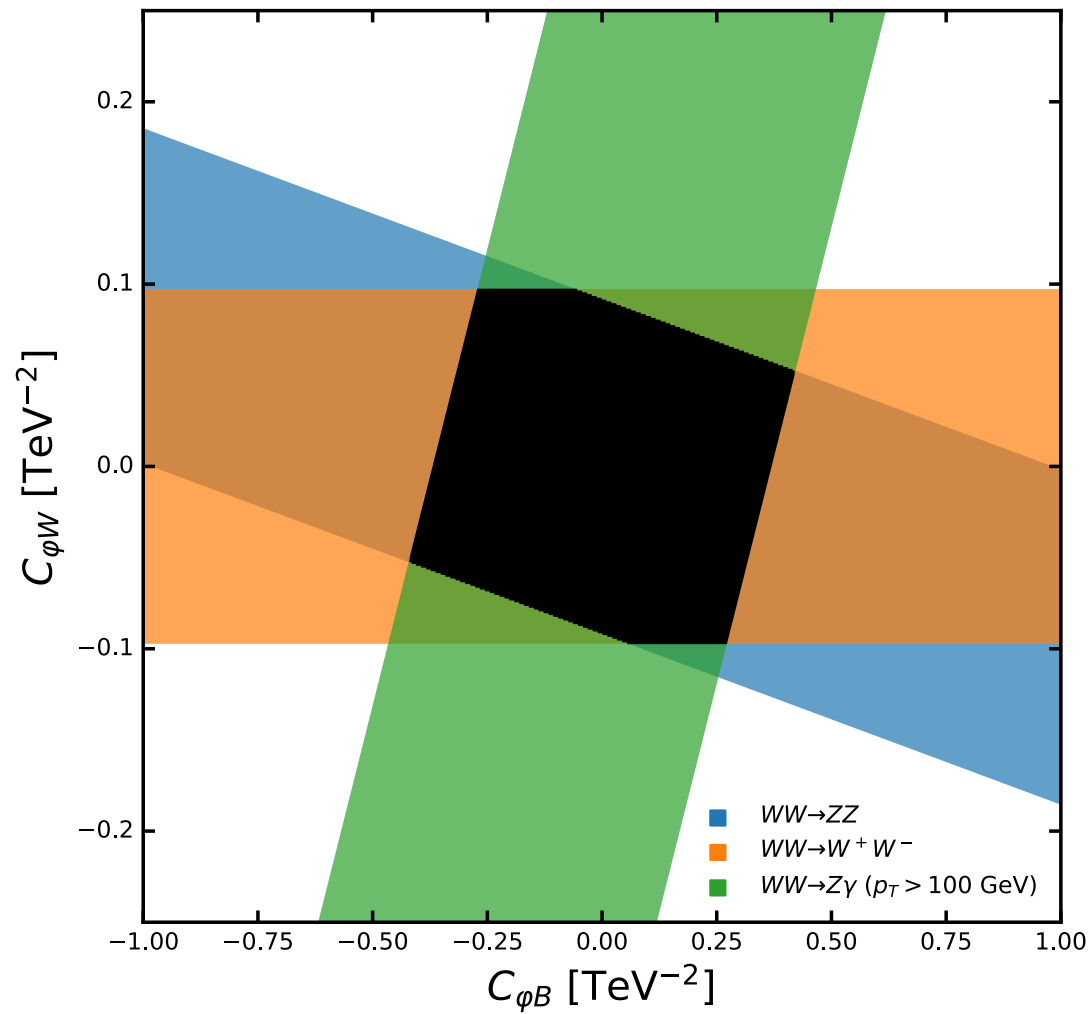
$$C_{\phi W} \sim [-0.097, 0.097]$$



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14 TeV



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$$C_{\phi W} \sim [-0.097, 0.097]$$

$$C_{\phi W} \sim [-0.03, 0.03]$$

$$C_{\phi B} \sim [-0.12, 0.12]$$



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- ❖ **Both precision and discovery potential are top notch**
- ❖ **A multi-TeV machine would be effectively a EW boson**
- ❖ **A naive projection was performed, considering only inclusive cross sections. No observable optimisation was performed, likely a very conservative projection.**
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