

Evaluation of thermal neutron scattering law of nuclear-grade isotropic graphite

Shinsuke Nakayama^{1,*},

*Osamu Iwamoto*¹, and *Atsushi Kimura*¹

¹Nuclear Data Center, Japan Atomic Energy Agency (JAEA), Japan

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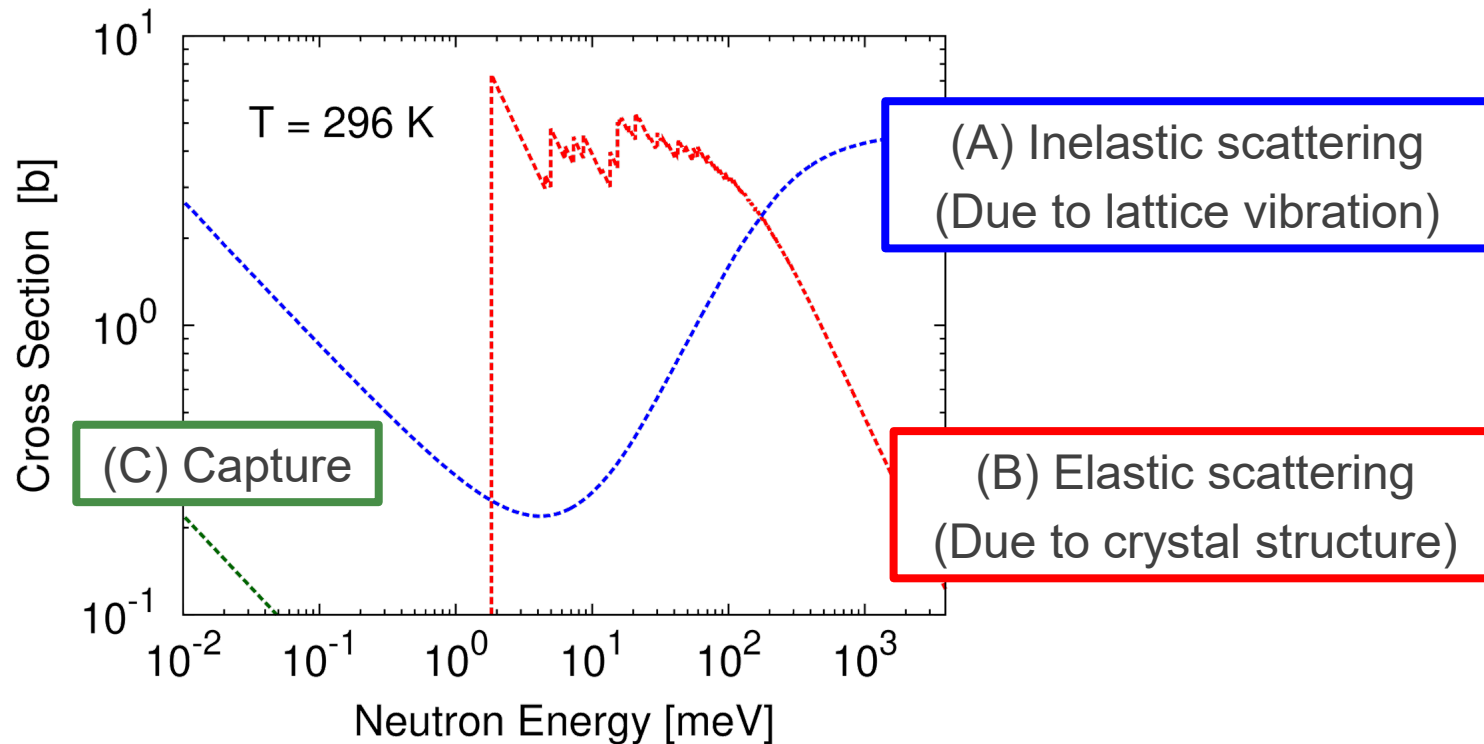
- 1. Introduction**
2. Evaluation of inelastic scattering
3. Evaluation of elastic scattering
4. Summary and outlook

Introduction

- ✓ We have started a 3-year project entitled "Development of Nuclear Data Evaluation Framework for Innovative Reactor" in 2021.
 - The objective is to establish a scheme to improve the accuracy of nuclear data required in the development of innovative nuclear reactors within a short time period through **collaboration** between experiments and evaluations.
- ✓ Scattering and transmission experiments on nuclear-grade **isotropic graphite** in the meV region were conducted by Kimura et al. (presented at 3 p.m. Monday).
- ✓ **Thermal neutron scattering law** (TSL) data of isotropic graphite is evaluated considering the above experimental results.

Cross section of JENDL-5 for graphite (crystalline)

* TSL data are taken from ENDF/B-VIII.0



- ✓ Inelastic and (coherent) elastic components are the targets of evaluation.
- Small-angle neutron scattering (**SANS**) due to structures larger than the crystal structure (pores and inter-grain voids) is discussed later.

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Evaluation method of inelastic scattering

- ✓ Inelastic scattering component was evaluated by the theoretical calculation.
 1. Compute the phonon density of states (DOS) with the **first-principles lattice dynamics simulations**.
 2. Obtain TSL for inelastic scattering by processing the above DOS with the LEAPR module of NJOY-2016.

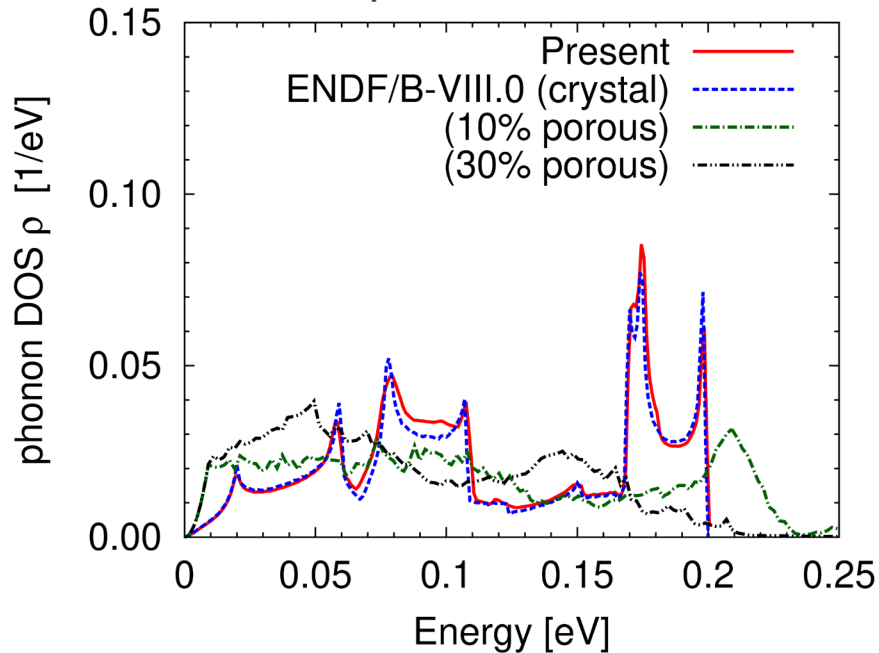
- ✓ Quantum ESPRESSO [1] was used for the first-principles calculation code.
 - Perform first-principles simulations with **pseudopotentials** and **plane-wave basis**.

Conditions of first-principles simulation

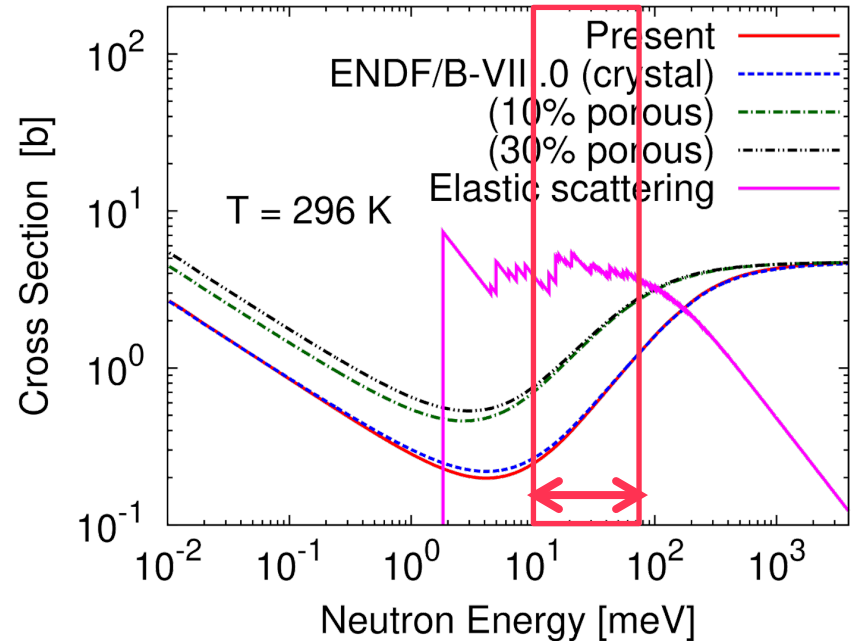
- ✓ Although the target of evaluation is **graphite with pores**, the simulations were performed for **ideal crystalline graphite**.
- The vacancies in graphite are larger than the crystals and other non-vacant region (where inelastic scattering occurs) are highly crystalline [1].
- **This contrasts with the modelling in ENDF/B-III.0 evaluation for nuclear-grade graphite** (carbon atoms are randomly removed from crystalline graphite).
- ✓ Parameters having significant impact the results (e.g., pseudopotential, k-points mesh, plane wave cutoff energy) were determined with references the previous study on crystalline graphite [2].

Results of simulation

phonon DOS

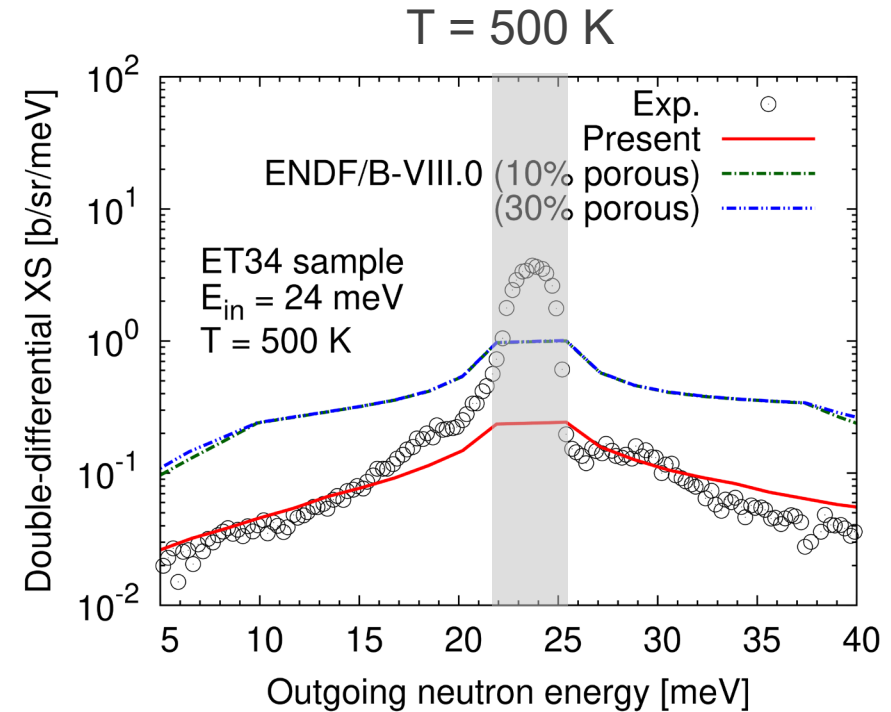
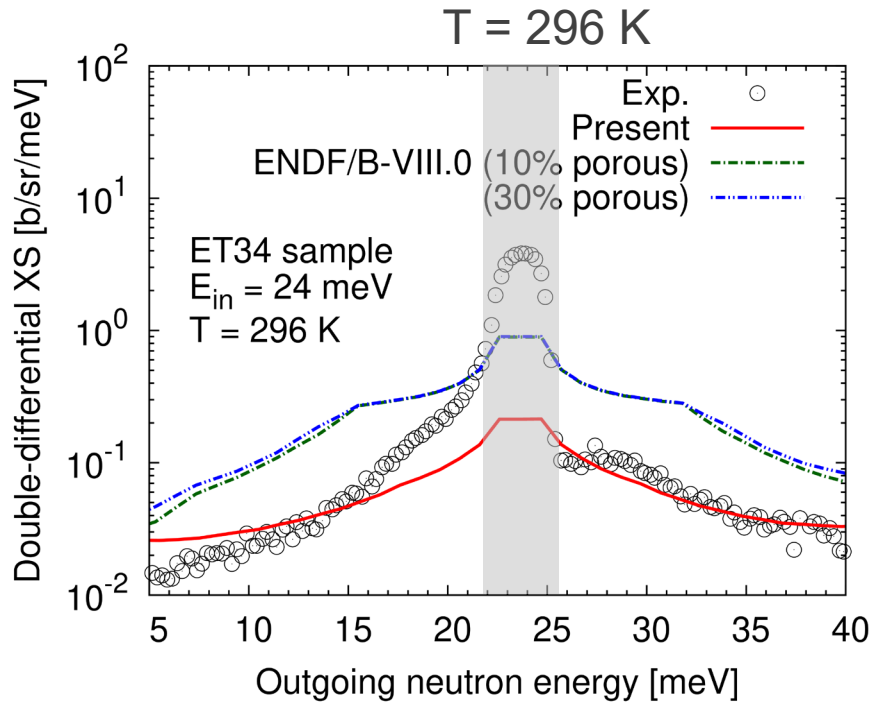


Cross section



- ✓ The present results are close to the evaluated values for crystalline graphite of ENDF/B-VIII.0 (evaluated based on the first-principles simulations).
- ✓ The present results are **largely different** from the values for porous graphite.
- It is difficult to judge which is better in the tens of meV region by comparison with the experimental total cross section.

Double-differential cross sections ($E_{in} = 24$ meV)



* The porosity of the sample in the experiment is approximately 11%.

- ✓ The present results for crystallin graphite **reproduce the experimental data** better than the evaluated values for porous graphite of ENDF/B-VIII.0.
- The regions in graphite where inelastic scattering occurs are highly crystalline.

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Evaluation method of elastic scattering

- ✓ The elastic scattering component is evaluated by **the positions and intensities of the Bragg peaks**.
- Cross section and angular distribution are uniquely determined from the peak position and intensity.

$$\sigma(E, T) = \frac{1}{E} \sum_{i=1}^{E_i < E} S_i(T), \quad \frac{d\sigma}{d\Omega}(E, \mu, T) = \frac{1}{2\pi} \frac{1}{E} \sum_{i=1}^{E_i < E} S_i(T) \delta(\mu - \mu_i)$$

$\left(\mu_i = 1 - \frac{2E_i}{E} \right)$

E incident energy

T temperature

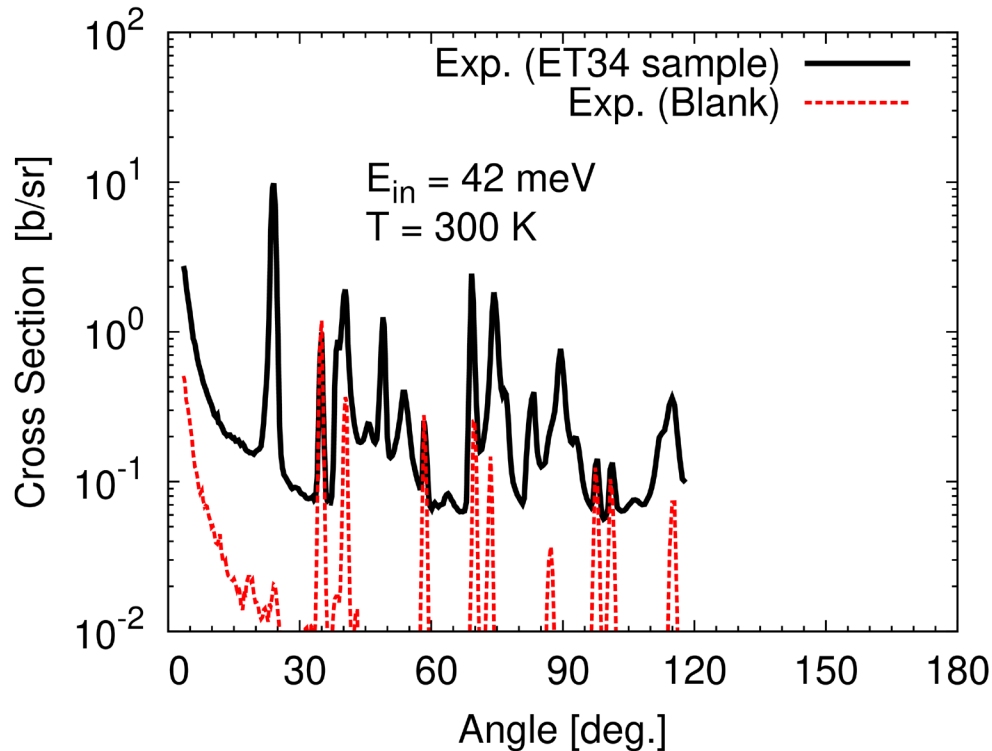
E_i i -th peak position (eV)

S_i i -th peak intensity (eV b)

μ cosine of scattering angle

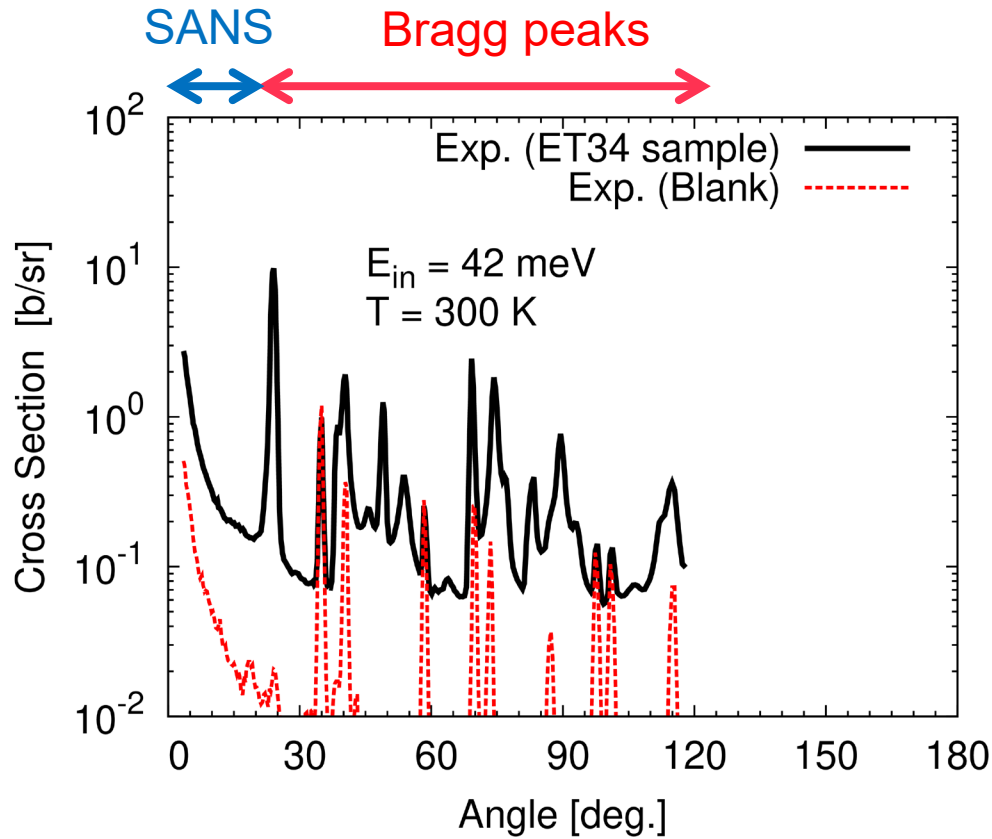
Differential cross section ($E_{in} = 42 \text{ meV}$) (1)

- ✓ The angular distributions of **the neutron scattering experiments performed in this project** were used to evaluate the Bragg peaks.



- ✓ Contributions from the aluminum container are seen in the blank measurement.
→ **Not negligible** in evaluating the Bragg peaks of graphite sample.

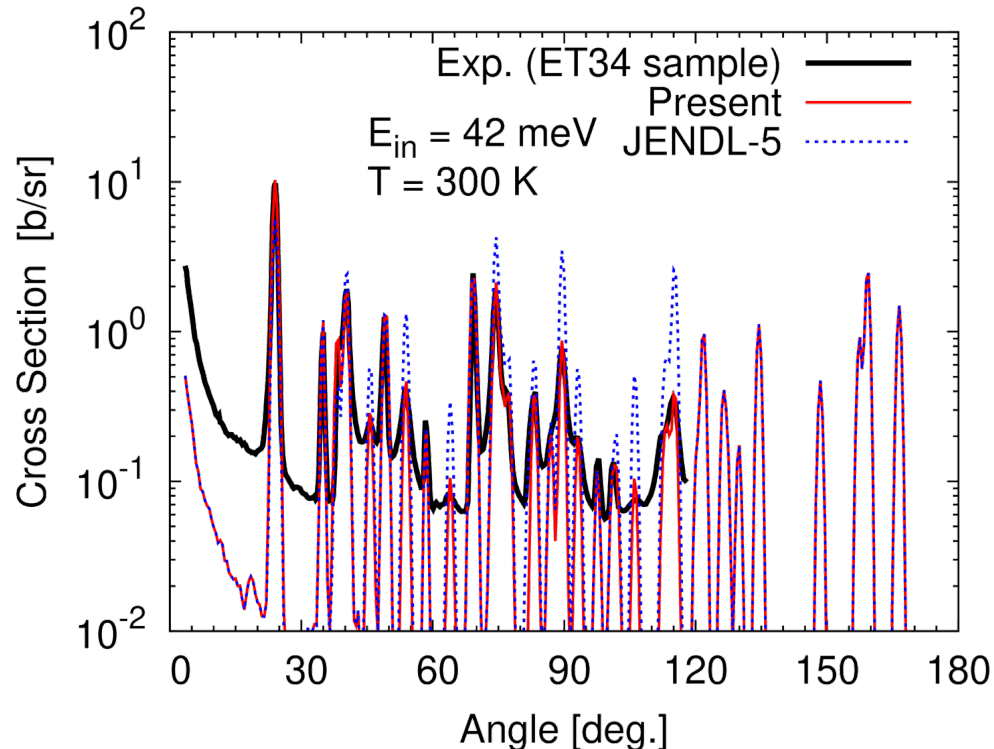
Differential cross section ($E_{in} = 42 \text{ meV}$) (1)



- ✓ Small angle neutron scattering (SANS) is seen in the most forward angles.
- This **does not affect** the evaluation of the Bragg peaks.

Differential cross section ($E_{in} = 42 \text{ meV}$) (2)

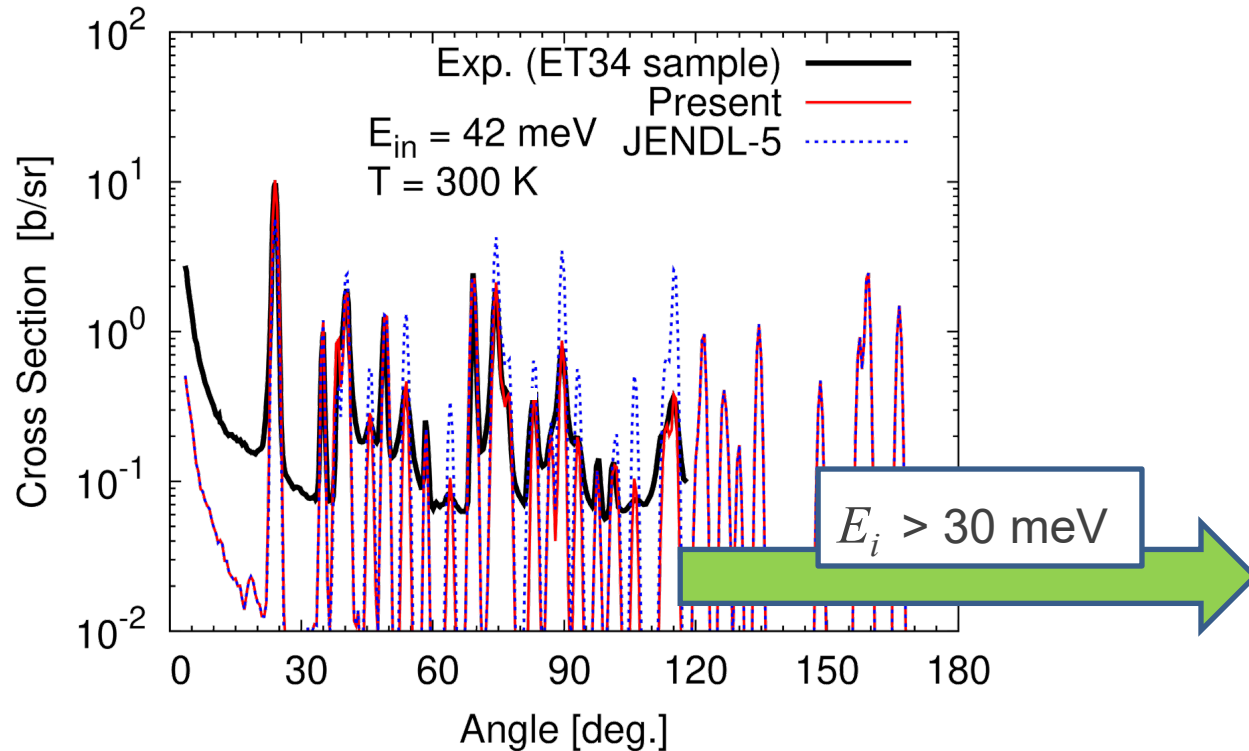
- ✓ We compare the evaluated values (+ contribution from the aluminum container) with the experimental values.



- ✓ JENDL-5 (=ENDF/B-VIII.0) data overestimate the present experimental data.
- **The intensities of the Bragg peaks** were evaluated (positions were not changed).

Differential cross section ($E_{in} = 42 \text{ meV}$) (2)

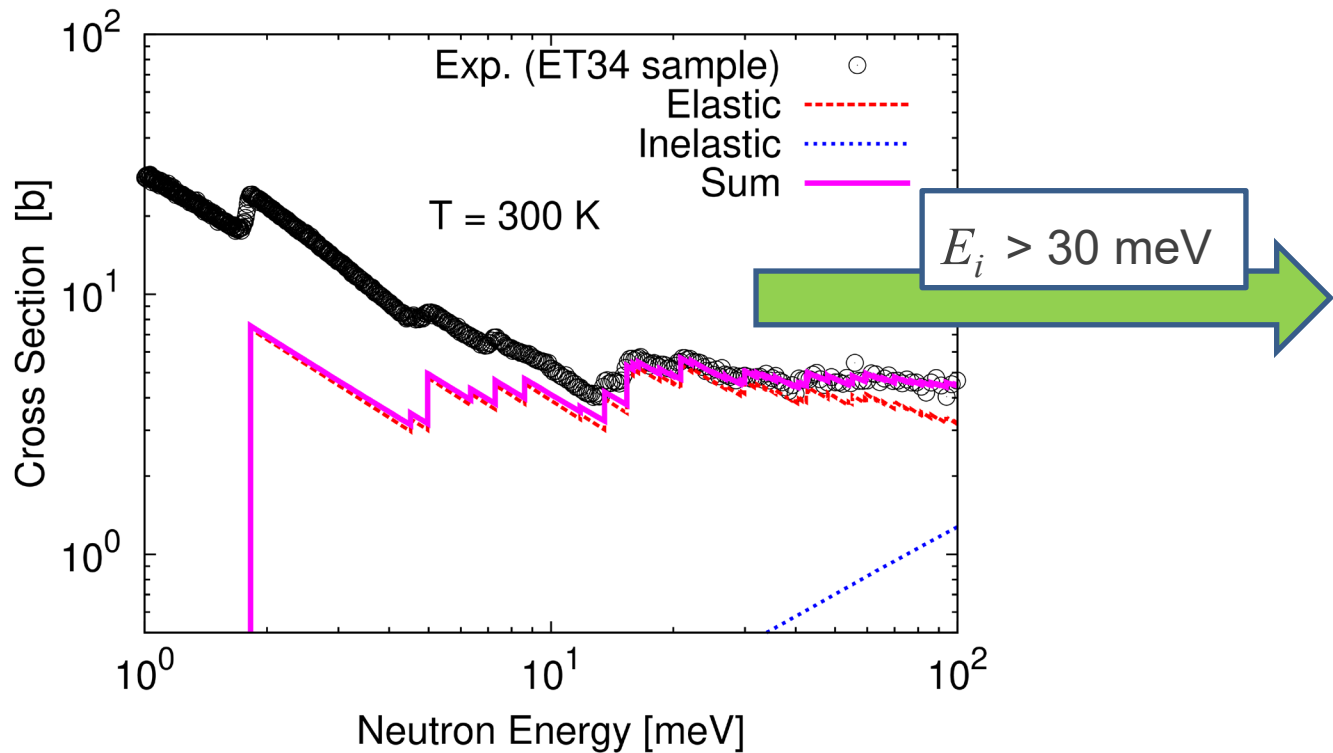
- ✓ In the present experiment, the data above 120° were not measured due to the limitation of equipment.



- ✓ Intensities at peak energies above 30 meV are unchanged at this stage.

Comparison with experimental total cross section

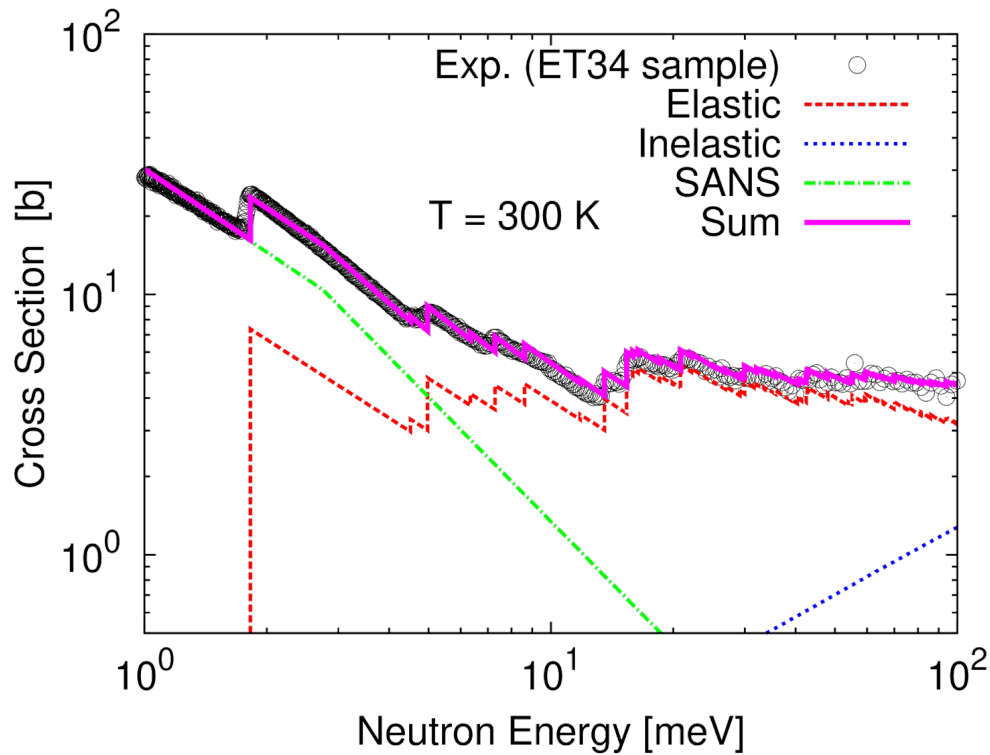
- ✓ Sum of evaluated inelastic and elastic scattering cross sections compared to **the total cross sections measured in this project.**



- ✓ The Bragg peak intensities above 30 meV were slightly adjusted.
- ✓ The evaluated values **largely underestimate** the experimental one below 10 meV.

Estimation of SANS component

- ✓ We estimate the small angle neutron scattering (**SANS**) components using the formulae proposed in the previous studies [1,2].



- ✓ By considering SANS, it is confirmed that the Bragg peak components below 30 meV are **in good agreement also with the experimental total cross section**.

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Summary

- ✓ **Thermal neutron scattering law** (TSL) of **isotropic graphite** was evaluated considering the experimental results obtained in the project we have organized.
- ✓ **Inelastic scattering** was evaluated by the first-principles calculations for **crystalline graphite**, and the evaluated values reproduced the experimental data better than the ENDF/B-VIII.0 evaluation for reactor-grade (porous) graphite.
- ✓ **Elastic scattering** was evaluated based on the experimental data for angular distribution of outgoing neutron and total cross sections.
- It was found that the quantification of **small angle neutron scattering** (SANS) is important in the comparison with total cross sections.

Outlook

- ✓ Compilation of **the ENDF-6 formatted TSL file** consisting of coherent elastic (Brag peaks) and inelastic scattering components.
 - **SANS is not included** since the official version of current nuclear data formats (ENDF-6, GNDS) have no place to store SANS.
- ✓ Derivation of inelastic scattering components from phonon density of states without **incoherent approximation** (assumed in NJOY).
 - We plan to use OCLIMAX [1] instead of NJOY.
 - Expected to improve data especially below a few meV.
- ✓ Evaluation of **other samples** used in the present experiment.