



Resolving a Challenging Supersymmetric Low-Scale Seesaw Scenario at the ILC

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Based on the following work:

N. Cerna, T. Faber, JJP, W. Porod (1705.06583)
N. Cerna, JJP, J. Masias, W. Porod (2102.06236)

SUSY Seesaw

We know neutrinos need a mass, but the MSSM doesn't care.

Simplest solution: GUT-scale SUSY Seesaw.

$$\mathcal{W} = \mathcal{W}_{\text{MSSM}} + Y_\nu \left(\hat{\nu}_R^c \hat{L} \cdot \hat{H}_u \right) + \frac{1}{2} M_R \left(\hat{\nu}_R^c \hat{\nu}_R^c \right)$$

Our question: what do colliders have to say about a low-scale SUSY Seesaw?

Our setup

- Set the R-sneutrino as the LSP.
- Keep μ as low as possible \rightarrow Higgsino-like electroweakinos.
- Ignore squarks and gluinos.
- Objective: Explore collider bounds on sleptons.

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Possible hierarchy:

$$m_{\tilde{\nu}_R}^2 < \mu < m_{\tilde{L}}^2, m_{\tilde{E}}^2$$

$$m_{\tilde{\nu}_R}^2 < m_{\tilde{L}}^2, m_{\tilde{E}}^2 < \mu$$

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Strong constraints

(2017, 13.3 fb⁻¹):

$$\mu \gtrsim 400 \text{ GeV}$$

$$m_{\tilde{L}} \gtrsim 600 \text{ GeV}$$

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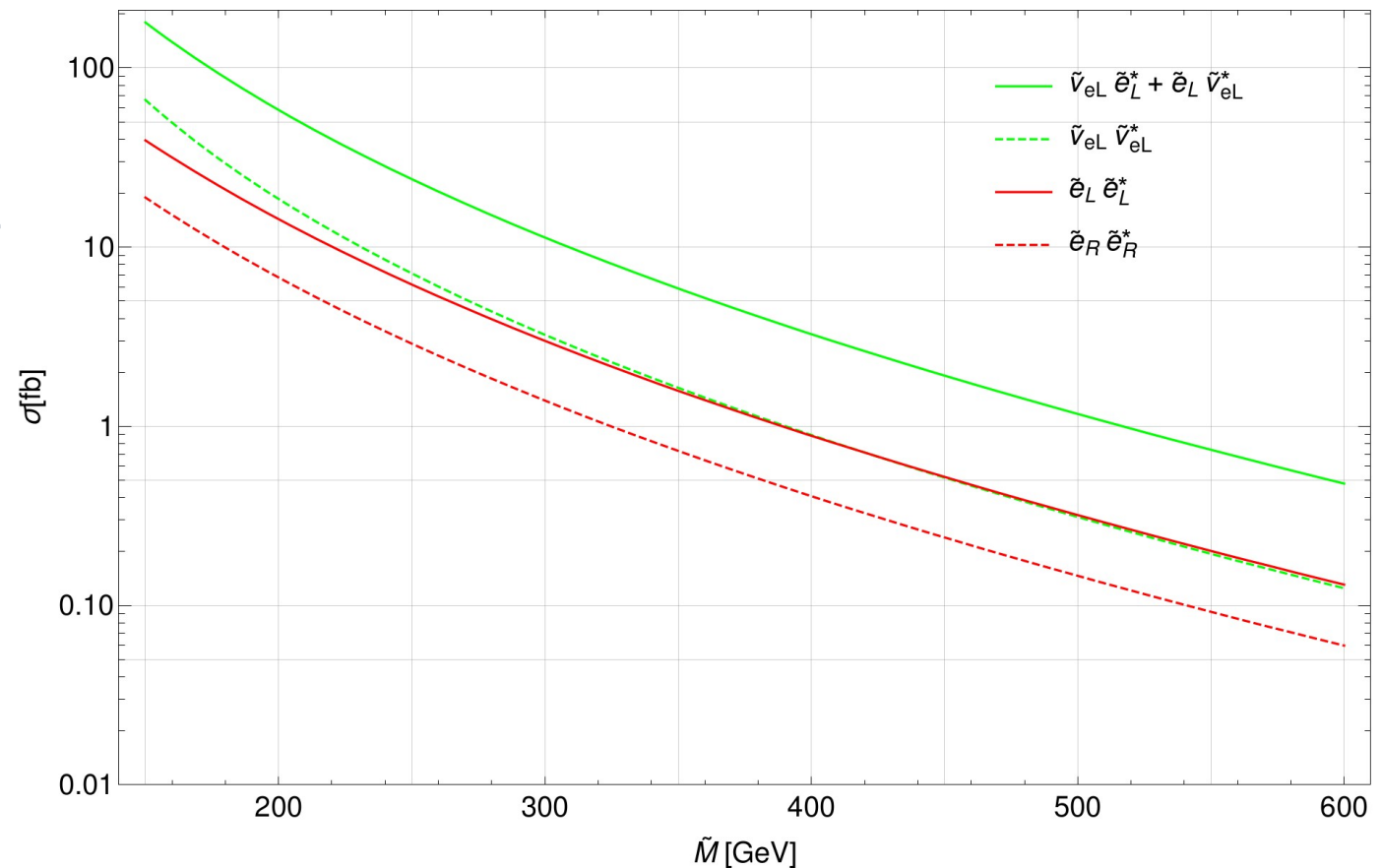
LHC Bounds (N. Cerna)

Sleptons at the LHC

$$m_{\tilde{\nu}_R}^2 < m_{\tilde{L}}^2 = m_{\tilde{E}}^2 < \mu$$

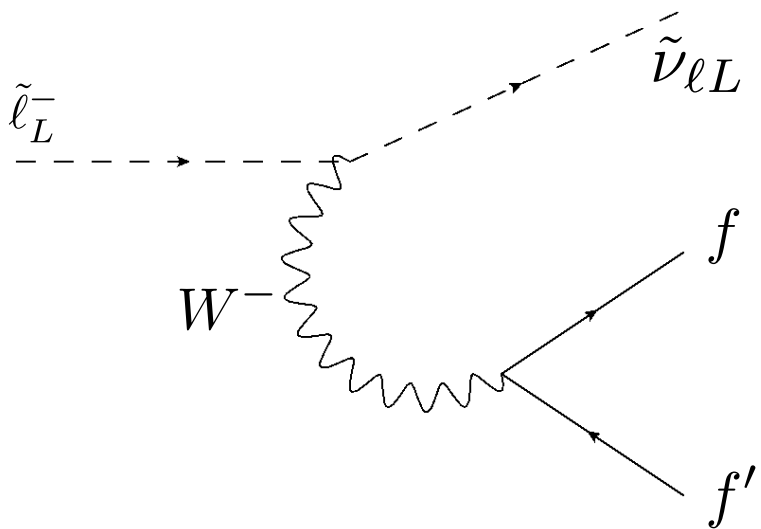
We will concentrate on slepton pair production:

Cross-section at the LHC (13 TeV), according to MadGraph.



Slepton Decay modes:

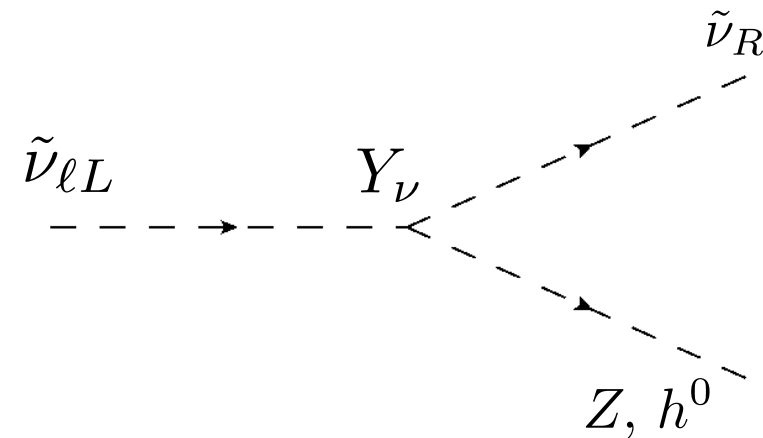
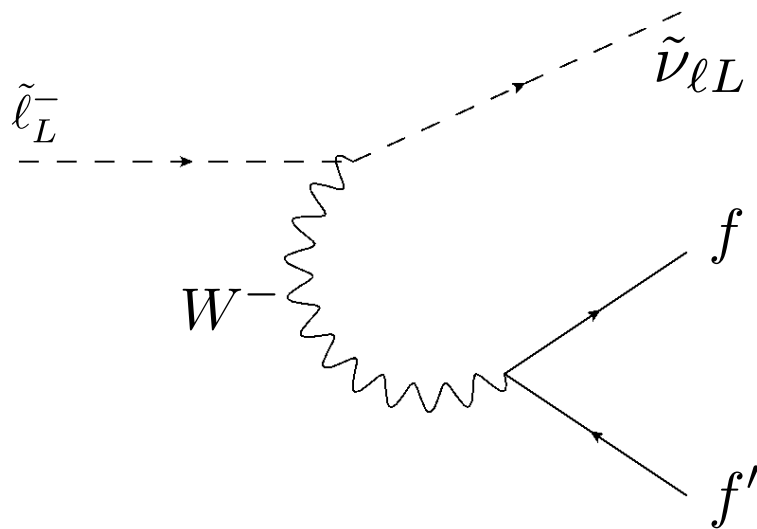
Selectrons, smuons: $(m_{\tilde{\ell}_L} - m_{\tilde{\nu}_L})_D \approx \frac{(\sin^2 \theta_W - 1)m_Z^2 \cos 2\beta}{2m_{\tilde{L}}} > 0$



We end up with two L-sneutrinos
and very soft fermions

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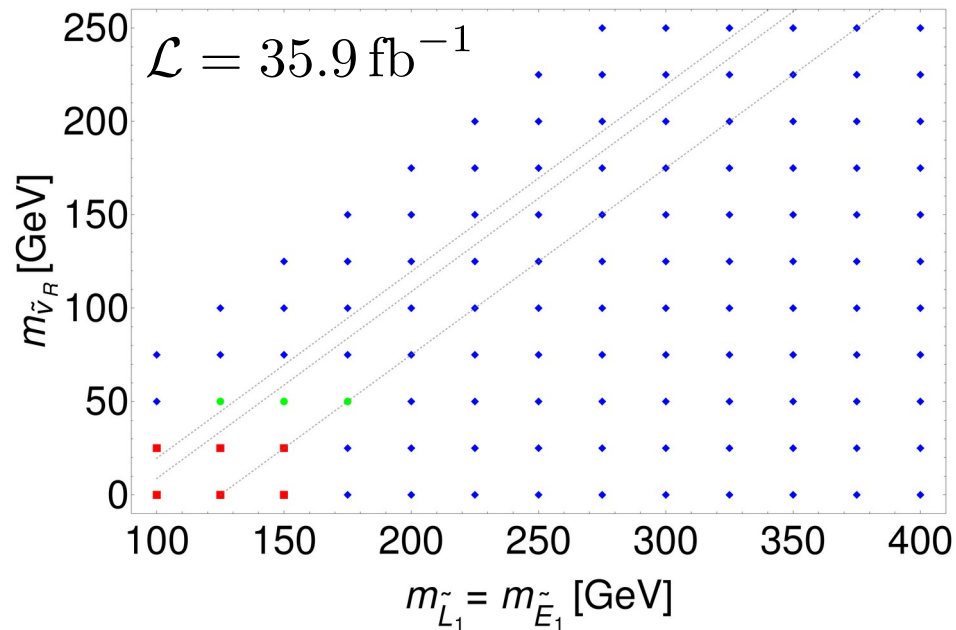
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Final states have SM bosons and missing energy

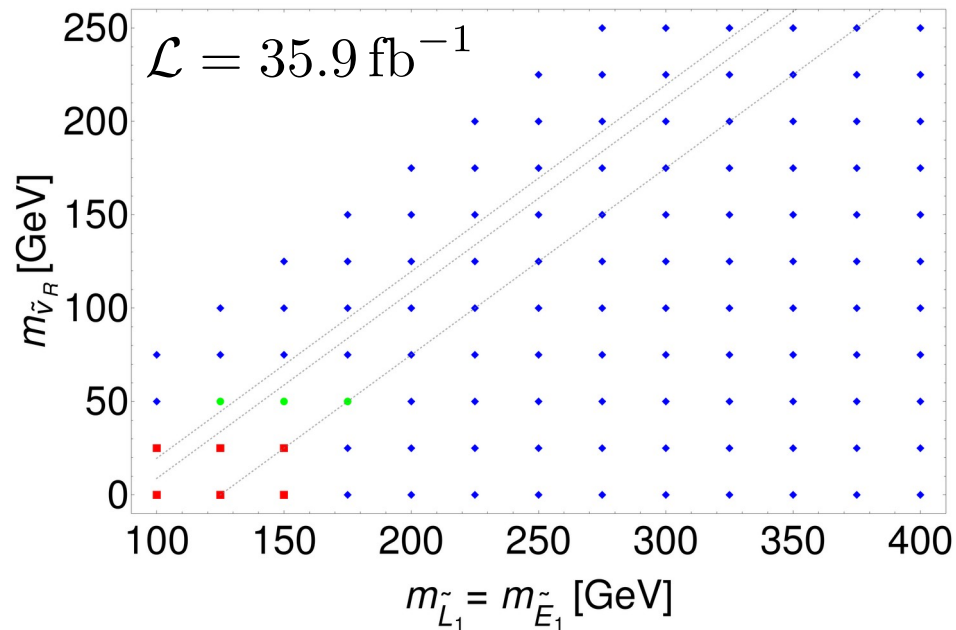
Search for selectrons at LHC:



Constrained mainly by multi-lepton searches

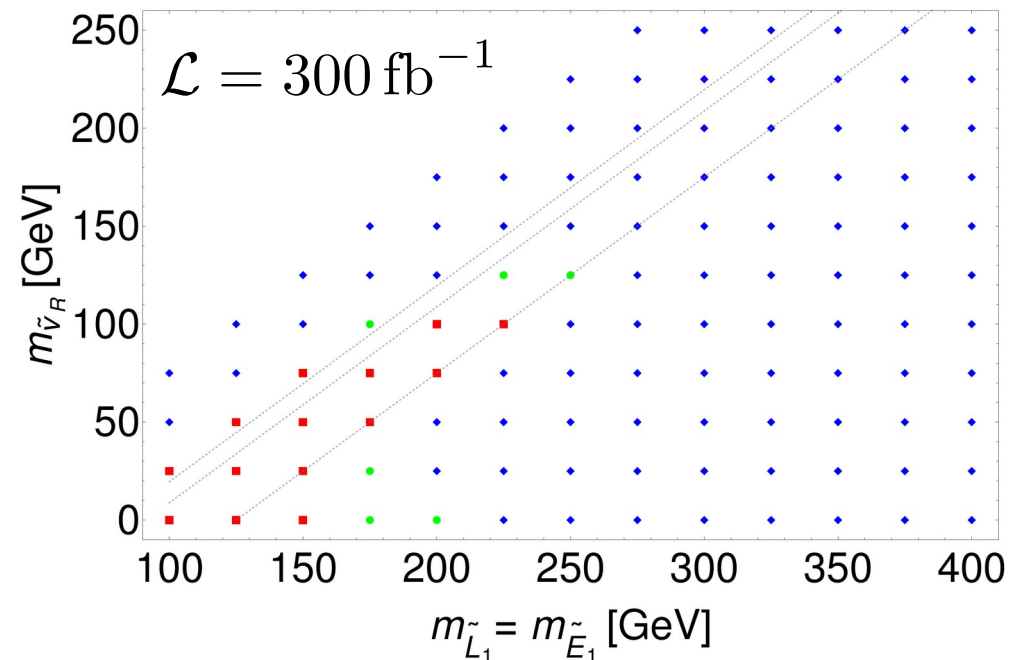
■ Ruled out ◆ Allowed ● Ambiguous

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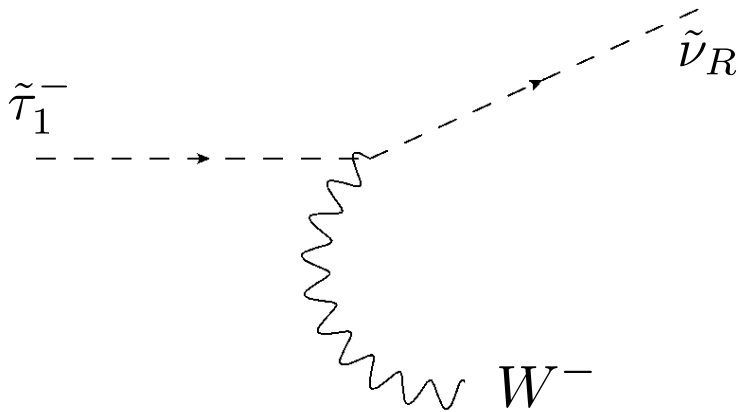


Projection at the end of LHC lifetime has a hard time extending the reach above ~ 175 GeV.

Slepton Decay modes:

Staus:

$$(m_{\tilde{\tau}_1} - m_{\tilde{\ell}})_{LR} \sim -\frac{m_\tau \mu \tan \beta}{2m_{\tilde{L}}} < 0$$

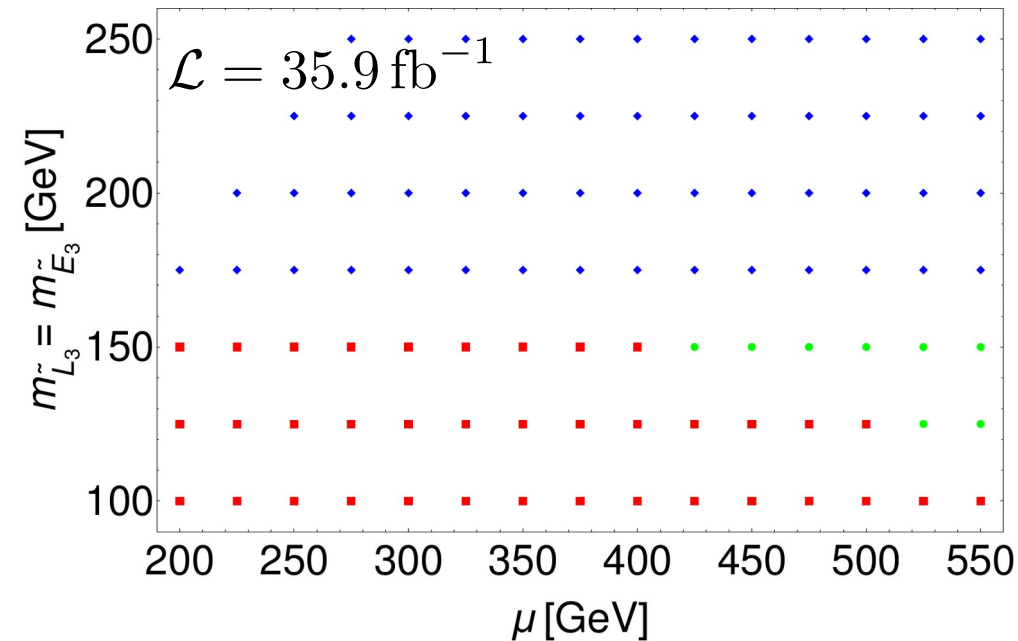


In this work, we only considered cases where L-sneutrinos would not decay into staus.

The μ parameter plays an important role in determining the physical mass.

Search for staus at LHC:

$$m_{\tilde{\nu}_R}^2 = 0$$

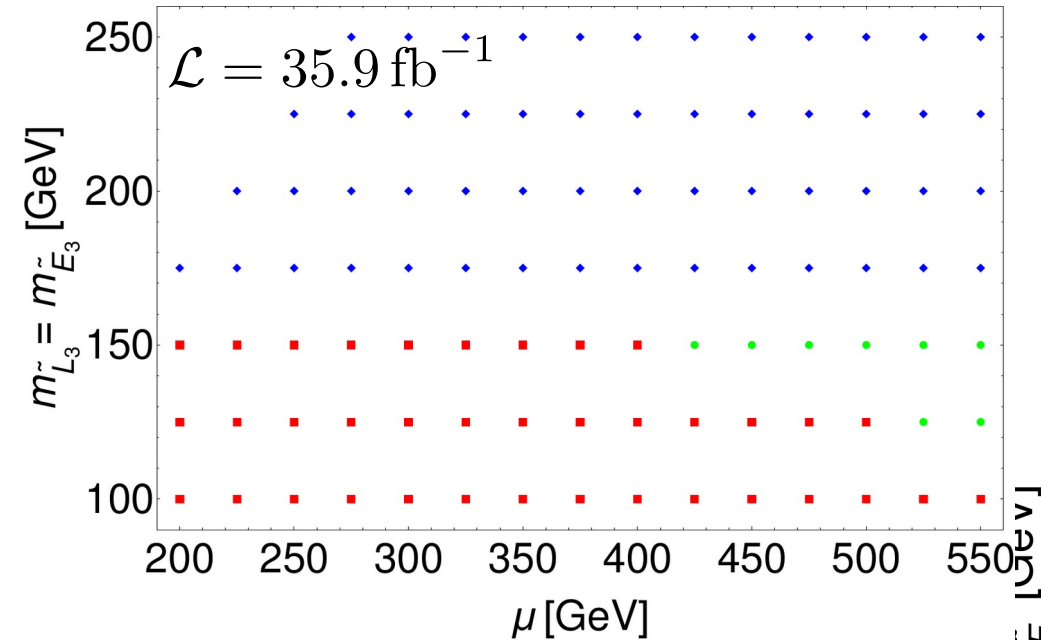


Multi-lepton searches still most sensitive.

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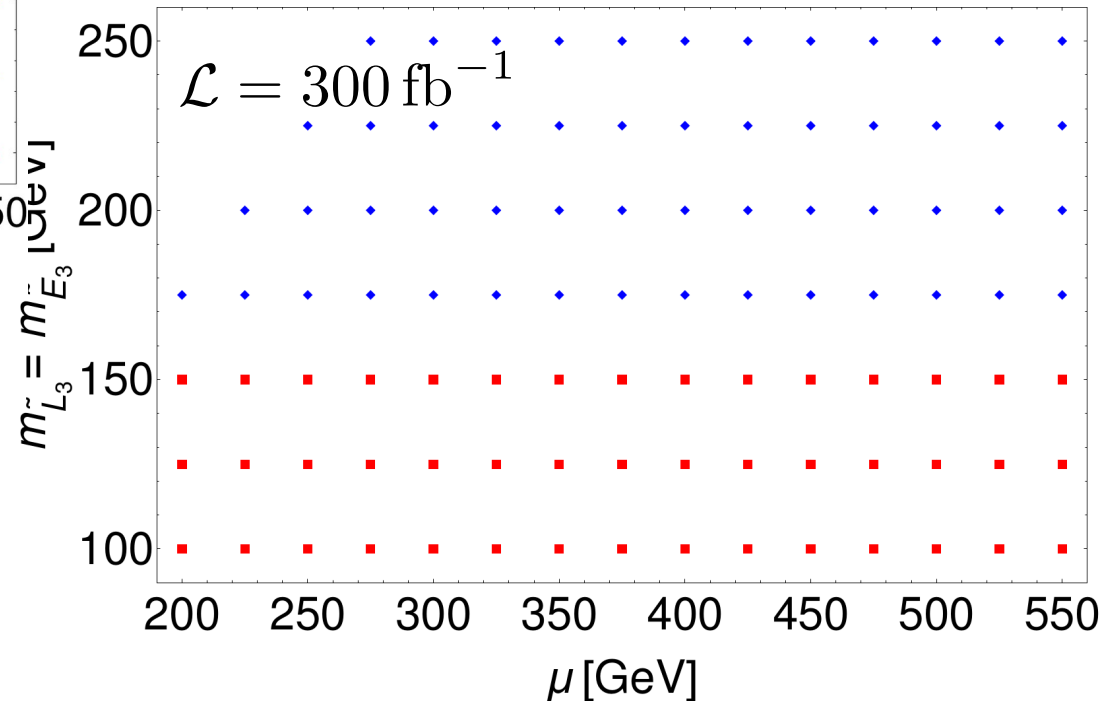
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For stau masses above 150 GeV, there are no constraints.

Prospects at the ILC (J. Masias)

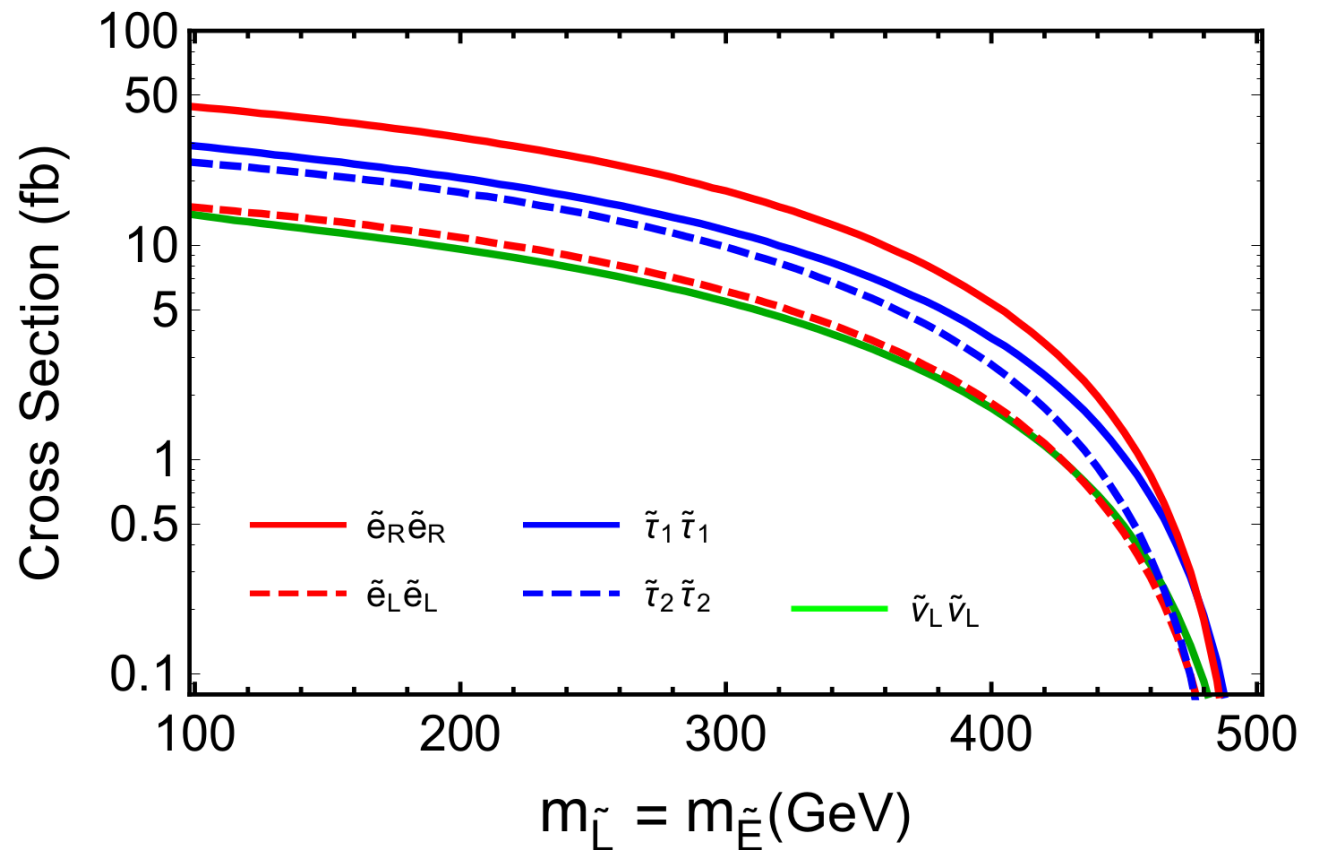
Sleptons at the ILC

We will start producing slepton pairs:

Cross-section at the ILC (1 TeV), according to WHIZARD.

Type **B** polarization.

$(e_R^- e_L^+)$



Sleptons at the ILC

Cutflow, 500 fb⁻¹ integrated luminosity

Scenario	SE	ST
No cuts	14713	14745
$p_{\text{miss}} > 50 \text{ GeV}$	12941	12997
Exactly four jets with $p > 20 \text{ GeV}$	4740	3770
Exactly two reconstructed SM bosons	869	1092
$p_{\text{lepton}} < 25 \text{ GeV}$	862	1084
$ \cos(\theta_{\text{miss}}) < 0.99$	758	922
Efficiency (%)	5.2	6.3

SE: $m_{\tilde{E}_1} = m_{\tilde{L}_1}$

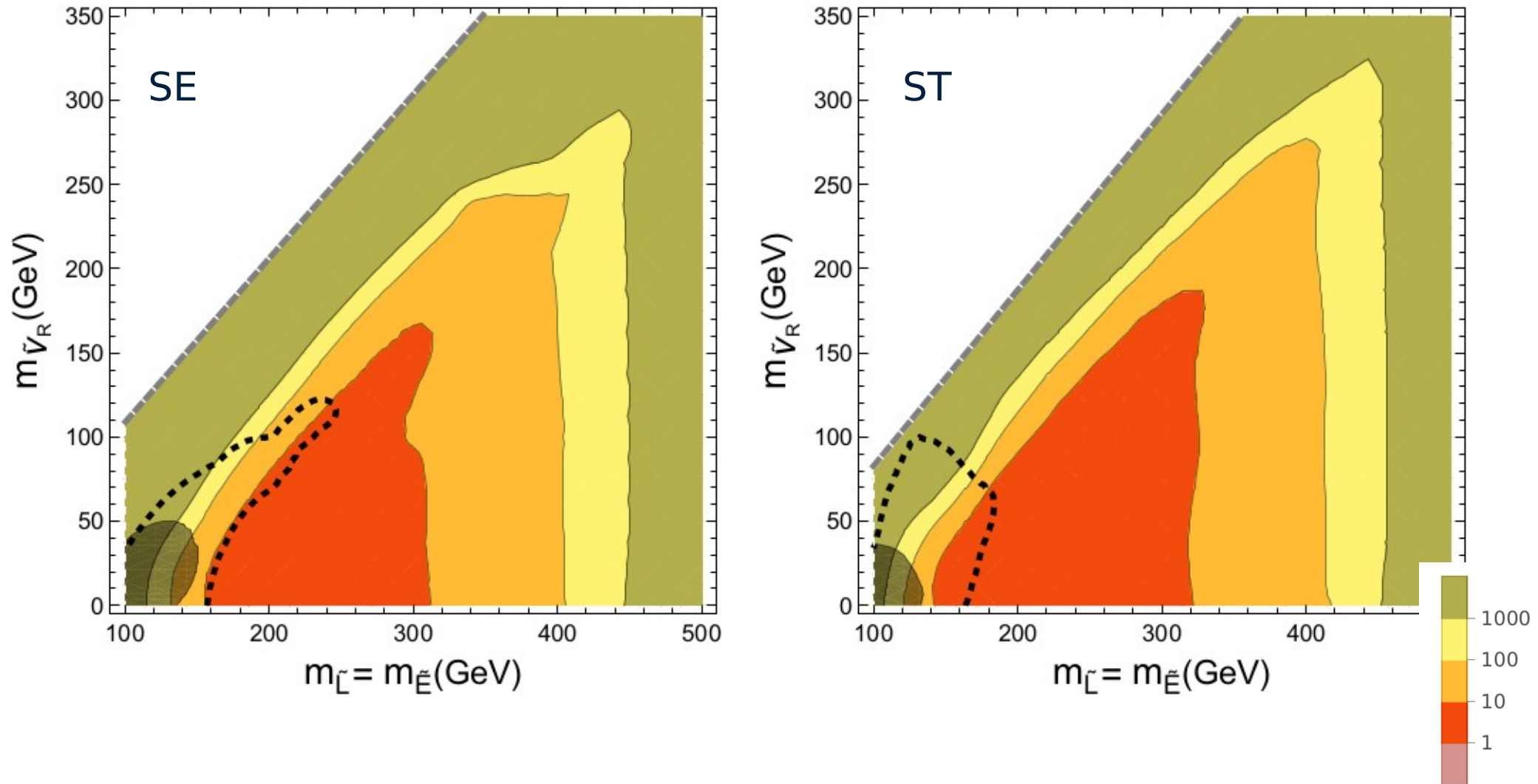
ST: $m_{\tilde{E}_3} = m_{\tilde{L}_3}$

All background: 417 events

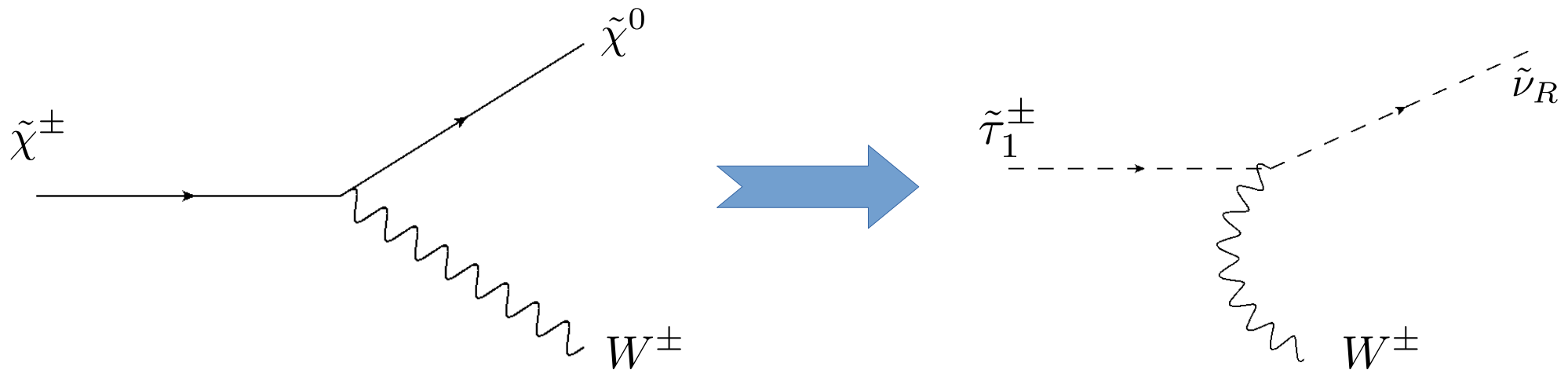
Efficiency: 0.08%

Main sources: $t\bar{t}$, $Z W^+ W^-$, $2\nu W^+ W^-$

Required luminosity (fb^{-1}) at ILC to get 5σ



Slepton Mass Reconstruction: Endpoint Method



Reconstruct W boson and measure its energy.

Min / max values of W boson energy: **endpoints**, E_{B-} , E_{B+}

Slepton Mass Reconstruction: Endpoint Method

$$m_{\tilde{\ell}} = \frac{2E_{\text{beam}}}{E_{B+} + E_{B-}} E'_B$$

← W boson energy in slepton rest frame

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$$E'_B = \frac{1}{\sqrt{2}} \sqrt{(E_{B+} E_{B-} + m_B^2) \pm \sqrt{(E_{B+}^2 - m_B^2)(E_{B-}^2 - m_B^2)}}$$

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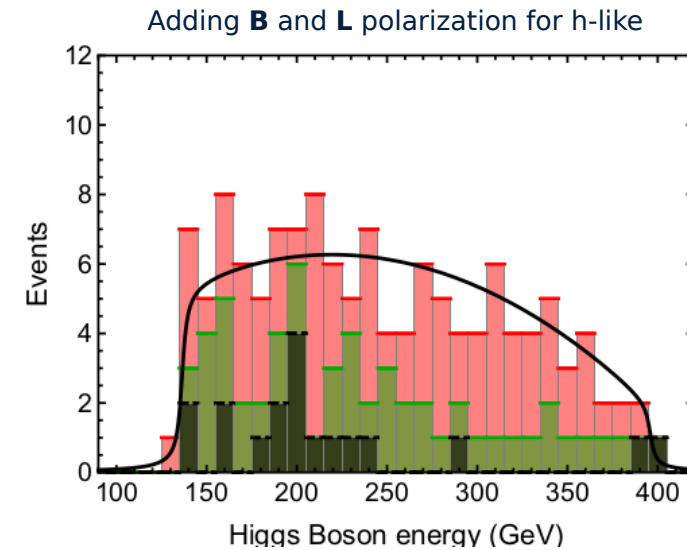
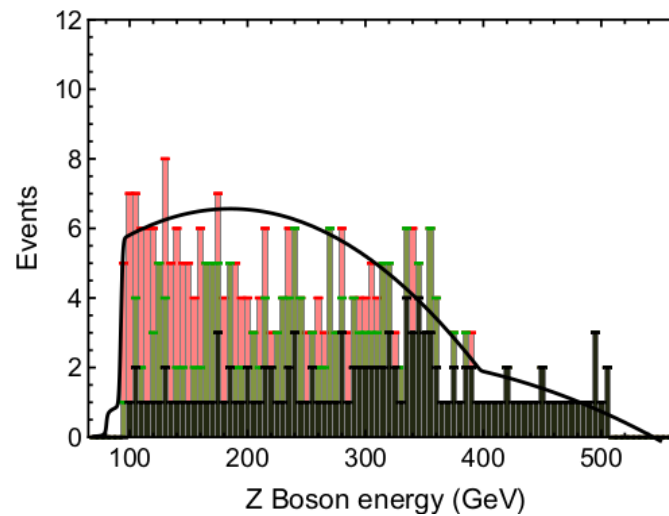
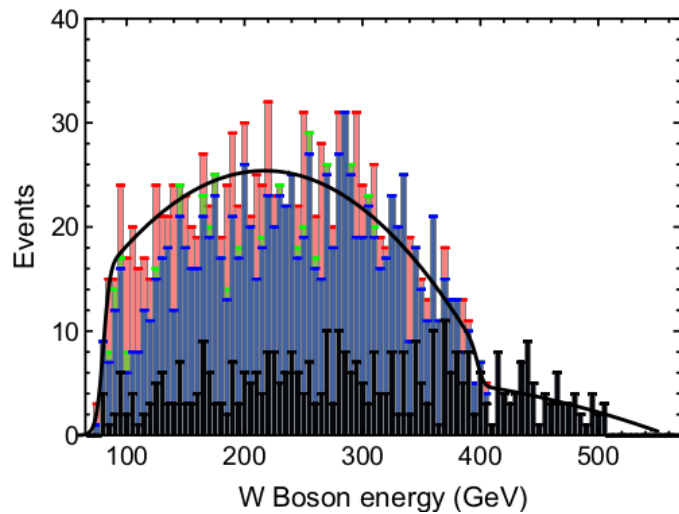
$$E'_B = \frac{1}{\sqrt{2}} \sqrt{(E_{B+} E_{B-} + m_B^2) \pm \sqrt{(E_{B+}^2 - m_B^2)(E_{B-}^2 - m_B^2)}}$$

Need two datasets, for example, decays into W and Z bosons.

Require that both datasets reproduce same LSP mass:

$$m_{\tilde{\nu}_R} = \sqrt{m_{\tilde{\ell}}^2 + m_B^2 - 2E'_B m_{\tilde{\ell}}}$$

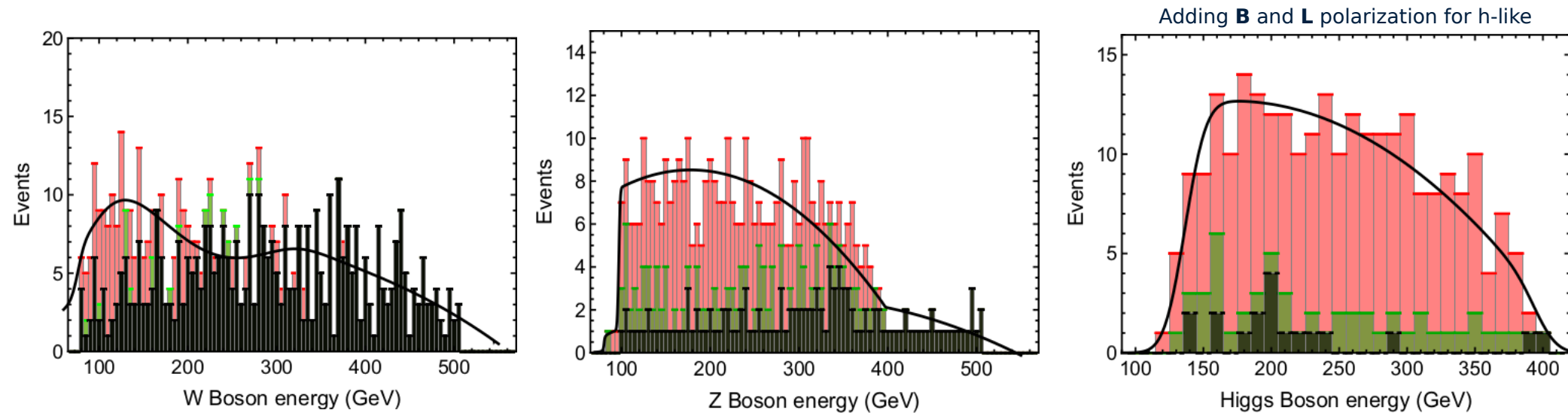
Slepton Mass Reconstruction: Light Staus with 500 fb⁻¹



- SM Background
- $\tilde{\tau}_1 \tilde{\tau}_1$
- $\tilde{\nu}_L \tilde{\nu}_L$
- Other SUSY

Scenario	ST	Theory
$m_{\tilde{\tau}_1}$ (GeV)	296.91 ± 10.69	294.47
$m_{\tilde{\nu}_L}$ (GeV)	293.32 ± 3.61	293.37
$m_{\tilde{\nu}_R}$ (GeV)	101.14 ± 1.36	101.98

Slepton Mass Reconstruction: Light Selectrons with 500 fb⁻¹



- SM Background
- $\tilde{\nu}_L \tilde{\nu}_L$
- $\tilde{e}_L \tilde{e}_L + \tilde{e}_R \tilde{e}_R$

Scenario	SE	Theory
$m_{\tilde{\nu}_L}$ (GeV)	293.63 ± 3.12	293.37
$m_{\tilde{\nu}_R}$ (GeV)	100.52 ± 1.65	101.98

Conclusions

- The LHC is not really sensitive to SUSY models where $m_{\tilde{\nu}_R}^2 < m_{\tilde{L}}^2 = m_{\tilde{E}}^2 < \mu$, single slepton families constrained to be heavier than ~ 150 GeV.
- A 1 TeV run of the ILC can probe a much larger part of the parameter space, most of it leading to a discovery with less than 1000 fb^{-1} .
- Endpoint method can reconstruct masses with 500 fb^{-1} , as long as sleptons decay into on-shell SM bosons.



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Thanks!



Backup

Neutrino Sector

After diagonalizing the neutrino mass matrix:

$$\begin{array}{ccc}
 3 \text{ active } \nu_L & \longleftrightarrow & 3 \text{ light } \nu_l \\
 3 \text{ sterile } \nu_R & & 3 \text{ heavy } \nu_h
 \end{array}
 \quad
 U = \begin{pmatrix} U_{al} & U_{ah} \\ U_{sl} & U_{sh} \end{pmatrix}$$

Using a Casas-Ibarra parametrization, we can reconstruct the Yukawa matrices:

$$Y_\nu = -i \frac{\sqrt{2}}{v_u} U_{\text{PMNS}}^* H^* m_\ell^{1/2} \left(m_\ell R^\dagger + R^T M_h \right) M_h^{-1/2} \bar{H}$$

$$H \sim I \quad \bar{H} \sim I$$

Complex orthogonal matrix

Neutrino Sector

Yukawa couplings can be enhanced by taking a large γ_{56} .

$$(Y_\nu)_{a5} = \pm (Z_a^{\text{NH}})^* \sqrt{\frac{2m_3 M_5}{v_u^2}} \cosh \gamma_{56} e^{\mp i\rho_{56}}$$

$$(Y_\nu)_{a6} = -i (Z_a^{\text{NH}})^* \sqrt{\frac{2m_3 M_6}{v_u^2}} \cosh \gamma_{56} e^{\mp i\rho_{56}}$$

With this, the mass matrix gets a structure similar to the inverse seesaw.

Neutrino Sector

For definiteness, we set:

$$M_5 = M_6$$

(So we do not exceed $0\nu\beta\beta$)

$$M_{5,6} = 20 \text{ GeV}$$

(So they do not contribute
much to R-sneutrino masses)

$$\gamma_{56} = 8$$

(So we do not exceed LFV)

Neutrino sector is **fixed**.

Sneutrino Sector

We need to add new soft SUSY breaking terms:

$$\mathcal{V}^{soft} = \mathcal{V}_{\text{MSSM}}^{soft} + (m_{\tilde{\nu}_R}^2)_{ij} \tilde{\nu}_{R,i}^* \tilde{\nu}_{R,j} + \frac{1}{2} (B_{\tilde{\nu}})_{ij} \tilde{\nu}_{R,i} \tilde{\nu}_{R,j} \\ + (T_{\nu})_{ij} \tilde{L}_i \cdot H_u \tilde{\nu}_{R,j}$$

Additional simplifications:

T_{ν} Assumed proportional to Y_{ν} , so negligible

$B_{\tilde{\nu}}$ New source of LNV, taken equal to zero for this work

Sneutrino Sector

Sneutrino mass matrix:

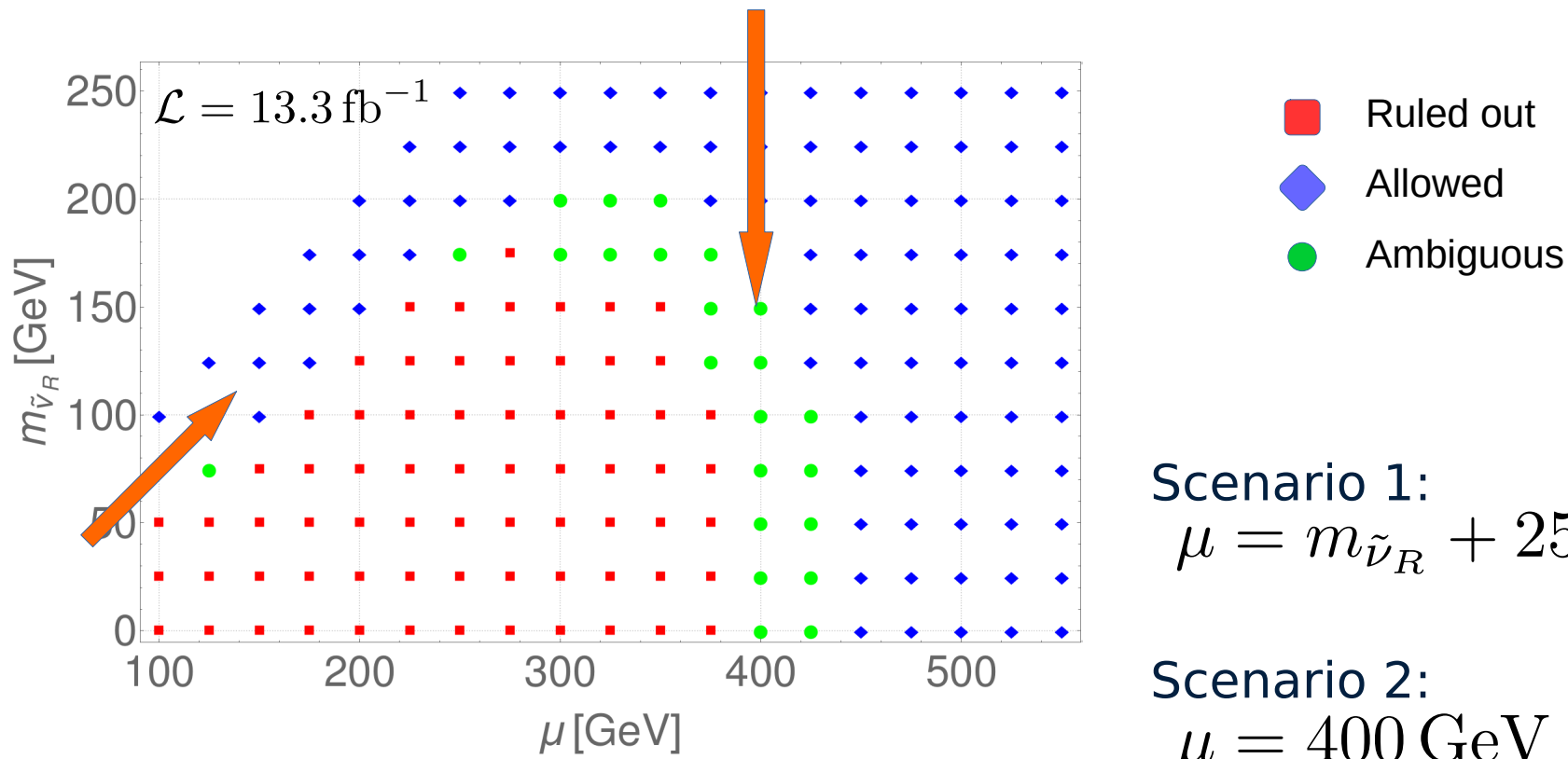
$$M_{\tilde{\nu}}^2 = \begin{pmatrix} m_{\tilde{L}}^2 + \frac{1}{2}m_Z^2 \cos 2\beta & 0 \\ 0 & m_{\tilde{\nu}_R}^2 + M_R^\dagger M_R \end{pmatrix}$$

Negligible LR mixing. For simplicity, soft masses are taken diagonal and degenerate.

On sneutrino sector, the only **variables** are the universal $m_{\tilde{L}}^2$, $m_{\tilde{\nu}_R}^2$

$$m_{\tilde{\nu}_R}^2 < \mu < m_{\tilde{L}}^2 = m_{\tilde{E}}^2$$

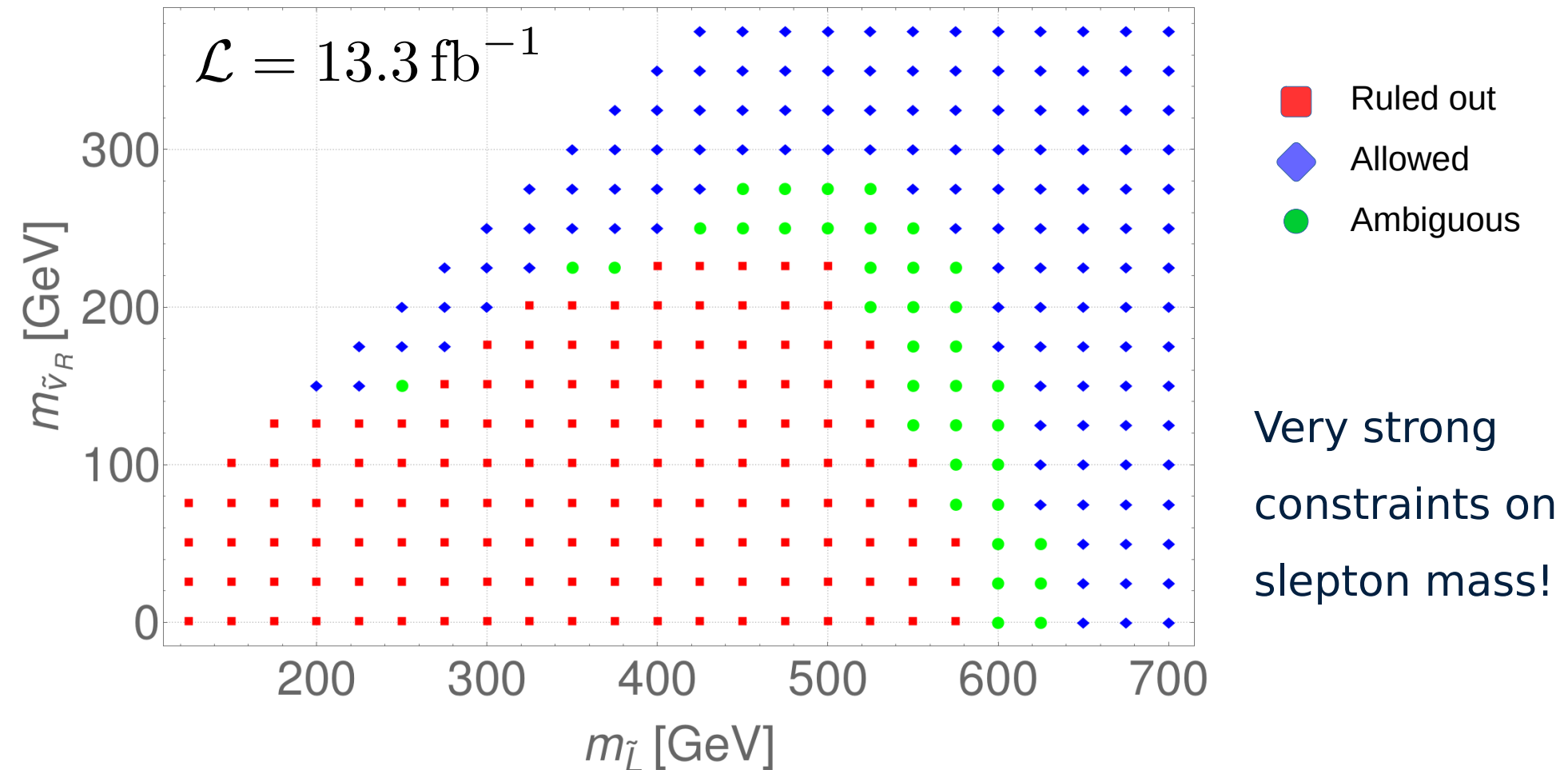
Chargino production: $pp \rightarrow \tilde{\chi}^+ \tilde{\chi}^- \rightarrow \ell^+ \ell^- \tilde{\nu}_R \tilde{\nu}_R^*$



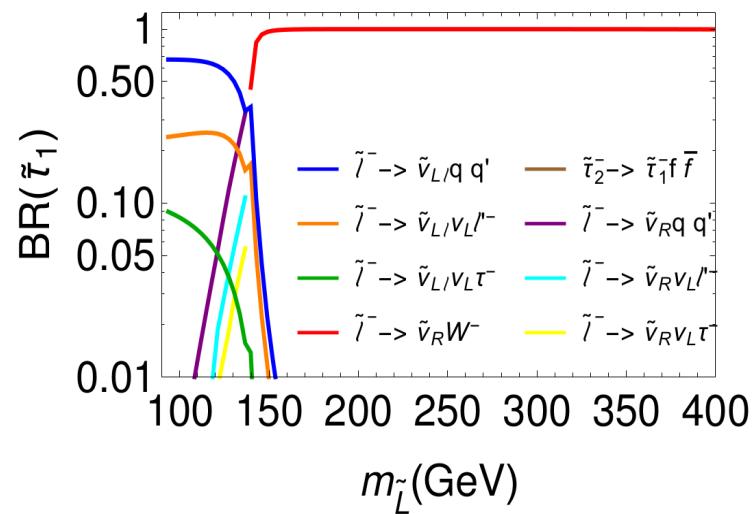
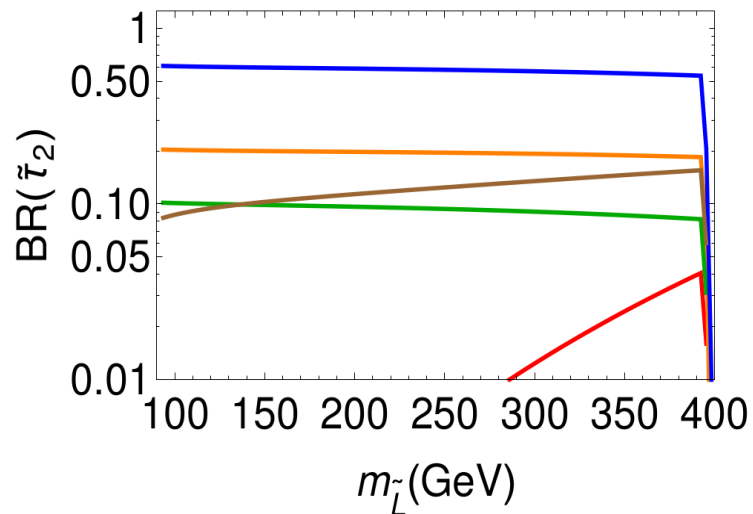
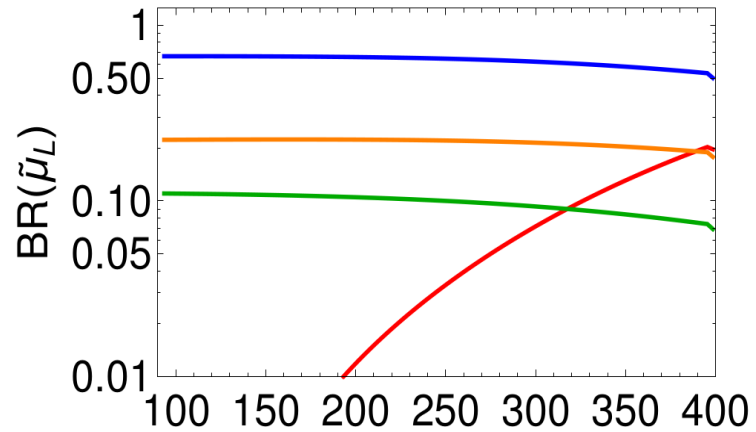
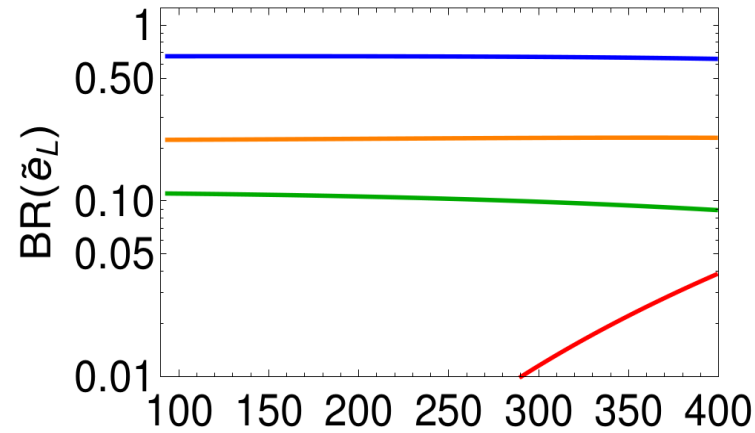
$$m_{\tilde{\nu}_R}^2 < \mu < m_{\tilde{L}}^2 = m_{\tilde{E}}^2$$

Scenario 1

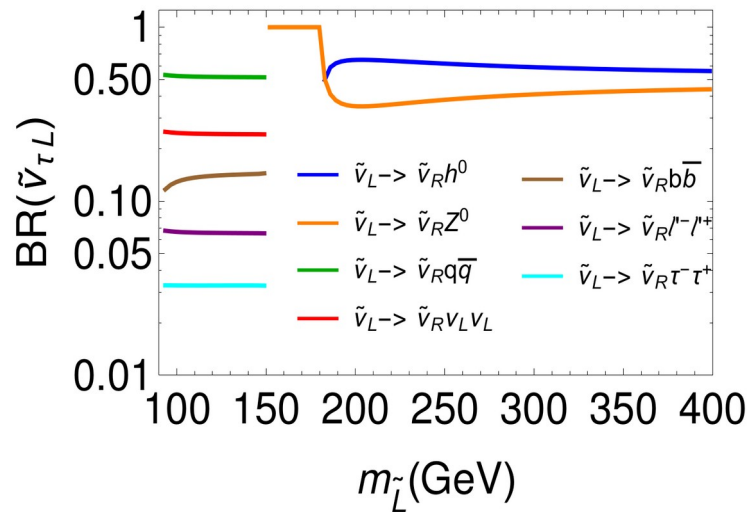
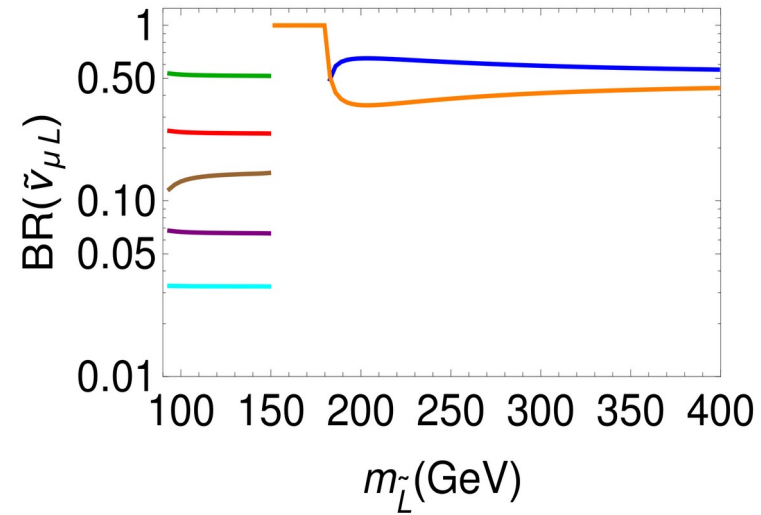
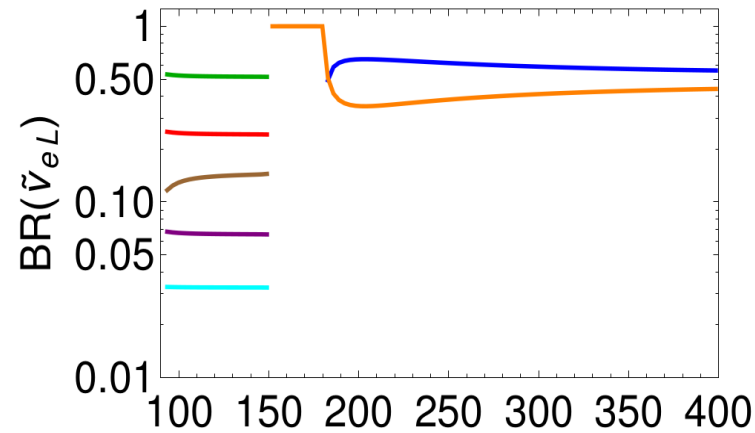
$$\mu = m_{\tilde{\nu}_R} + 25 \text{ GeV}$$



Branching Ratios $m_{\tilde{\nu}_R} < m_{\tilde{\ell}} < \mu$



Branching Ratios $m_{\tilde{\nu}_R} < m_{\tilde{\ell}} < \mu$



$$\mu = 400 \text{ GeV}$$

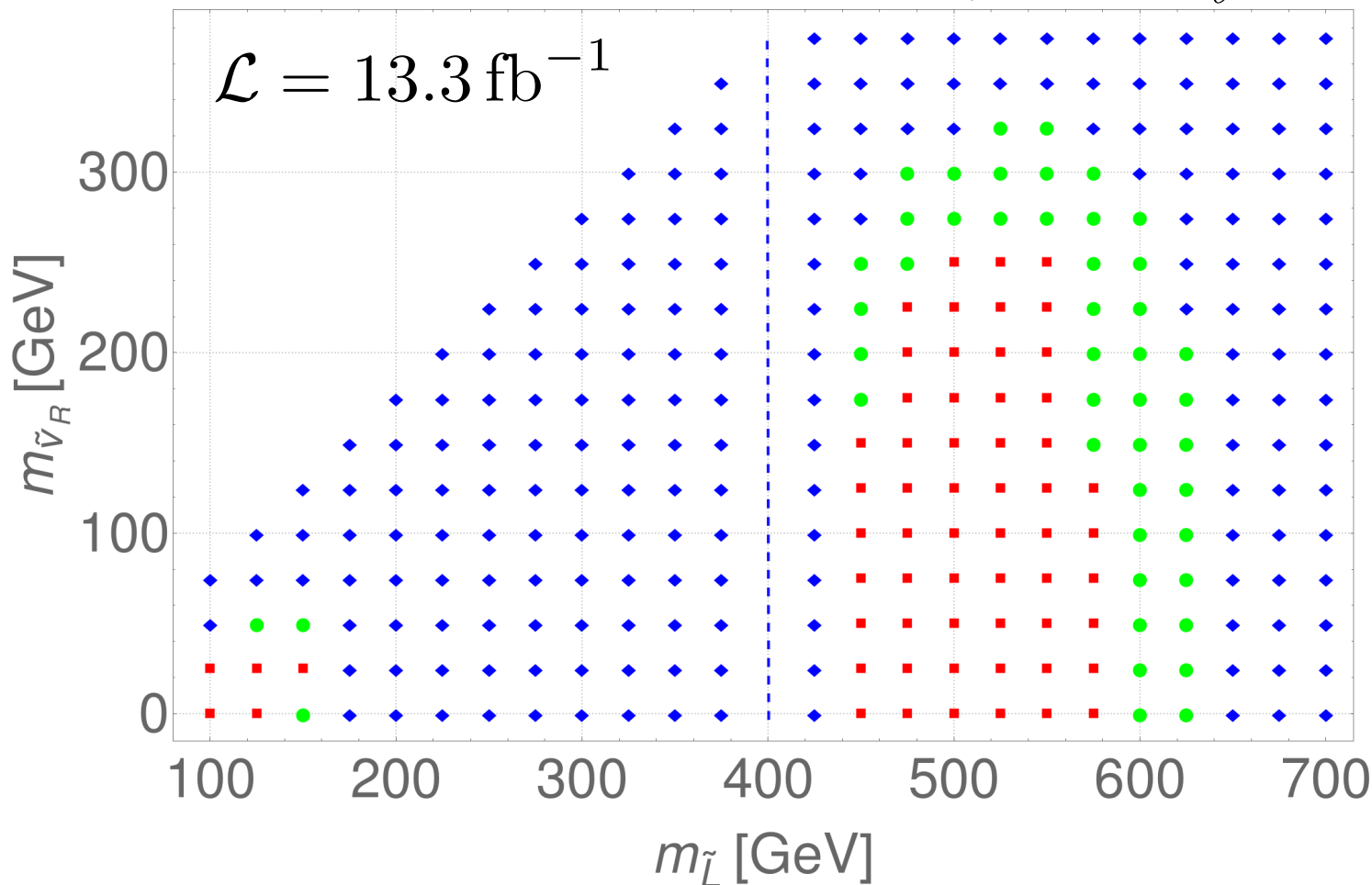
$$m_{\tilde{\nu}_R} < m_{\tilde{\ell}} < \mu$$

$$m_{\tilde{\nu}_R} < \mu < m_{\tilde{\ell}}$$

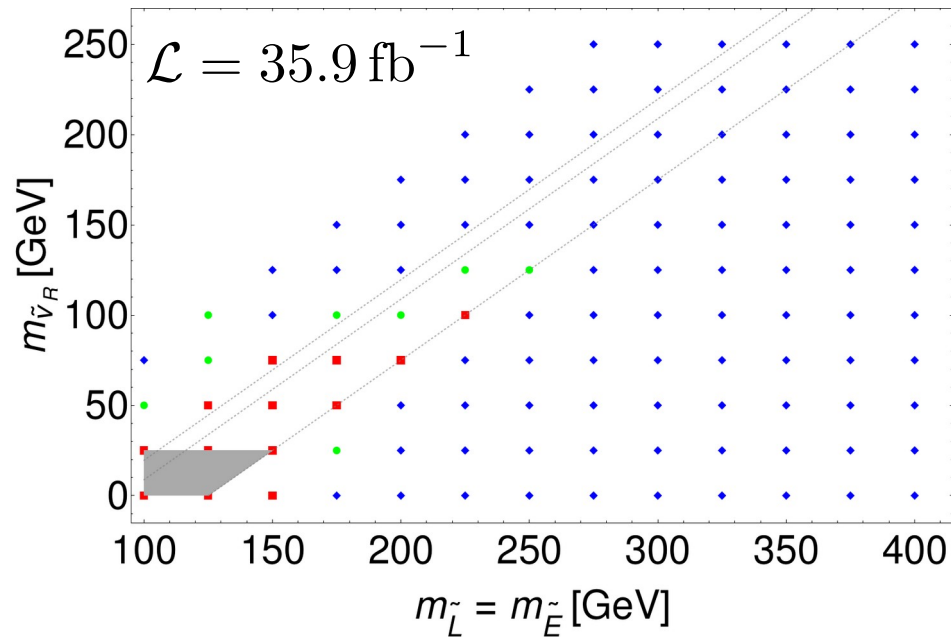
$$\mathcal{L} = 13.3 \text{ fb}^{-1}$$

- Ruled out
- ◆ Allowed
- Ambiguous

If electroweakinos are heavy, we have weak constraint!

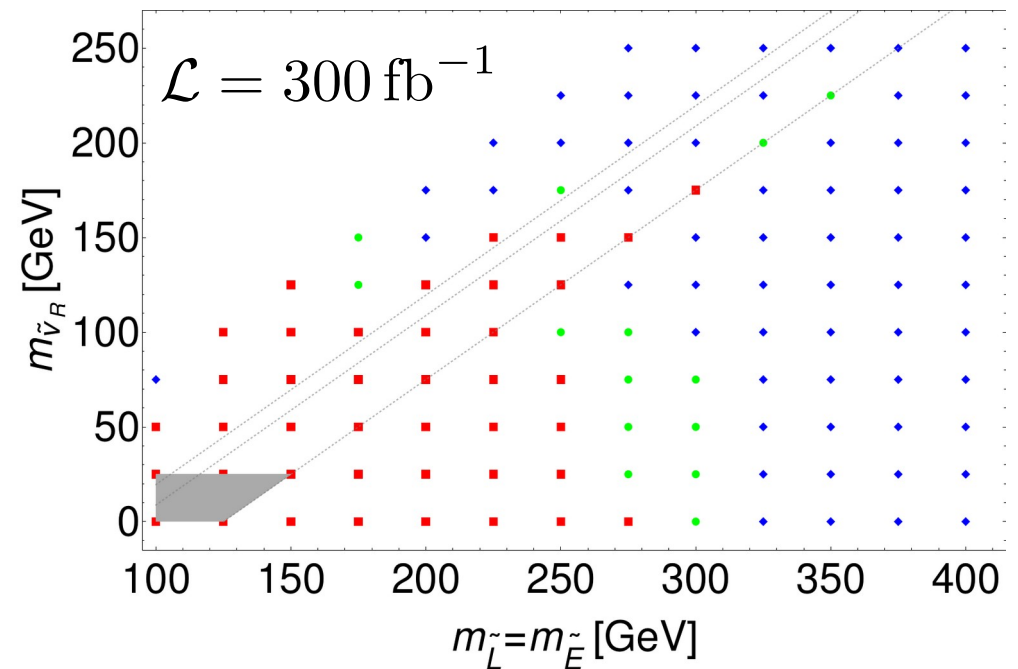


Degenerate scenario at LHC:



Constrained mainly by multi-lepton searches

■ Ruled out
 ◆ Allowed
 ● Ambiguous



Projection at the end of LHC lifetime has a hard time extending the reach above 250 GeV.

Getting the endpoints

1. Group all events into W-like, Z-like, and h-like datasets:

$$\chi_W^2(m_1, m_2) = \frac{(m_1 - m_W)^2 + (m_2 - m_W)^2}{\sigma^2}$$

$$\chi_Z^2(m_1, m_2) = \frac{(m_1 - m_Z)^2 + (m_2 - m_Z)^2}{\sigma^2}$$

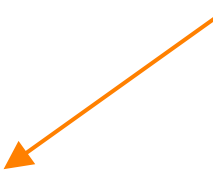
$$\chi_h^2(m_1, m_2) = \frac{(m_1 - m_h)^2 + (m_2 - m_h)^2}{\sigma^2}$$

Getting the endpoints

2. Generate a SM distribution from MC events, by fitting parameters:

$$f_{SM}(E; E_{SM-}, a_{0-2}, \sigma_{SM}, \Gamma_{SM})$$
$$= \int_{E_{SM-}}^{\infty} (a_2 E'^2 + a_1 E' + a_0) V(E' - E, \sigma_{SM}, \Gamma_{SM}) dE'$$

Voigt function



3. Generate 100 samples of SM background using SM distribution.

Implement statistical errors by modifying number of events in each bin using a Poisson distribution.

Getting the endpoints

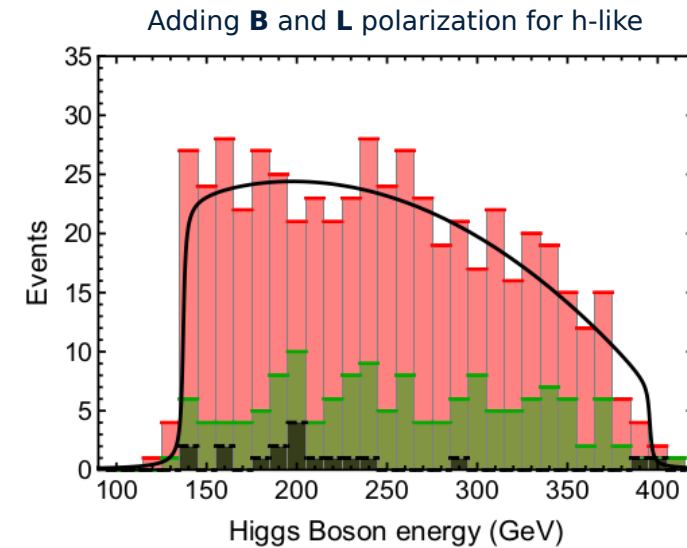
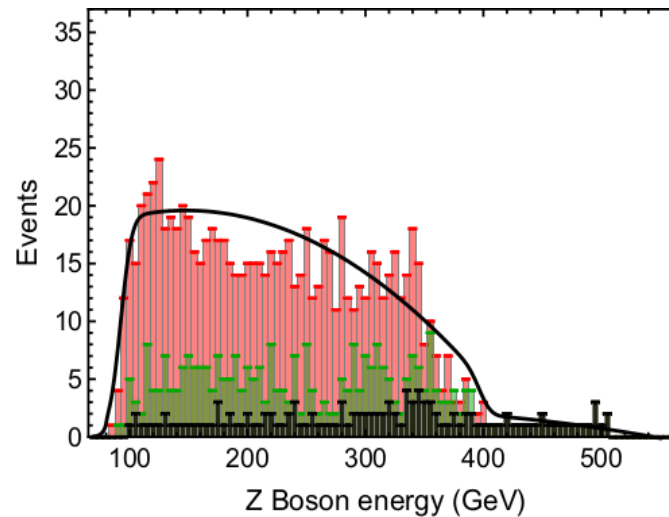
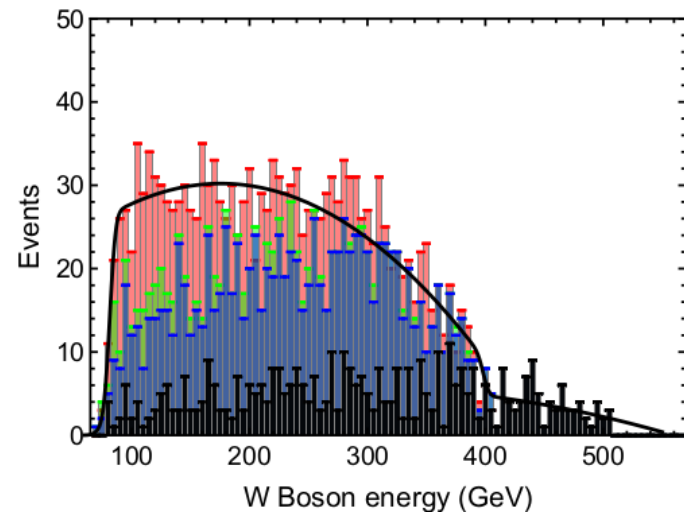
4. For each SM sample, fit the sum of SUSY and SM spectra:

$$\begin{aligned} f(E; E_{B-}, E_{B+}, b_{0-2}, \sigma_1, \Gamma_1) \\ = f_{SM}(E; E_{SM-}, a_{0-2}, \sigma_{SM}, \Gamma_{SM}) \\ + \int_{E_{B-}}^{E_{B+}} (b_2 E'^2 + b_1 E' + b_0) V(E' - E, \sigma_1, \Gamma_1) dE' \end{aligned}$$

5. Get endpoints from fit. Use 100 samples to get average and standard deviation.

6. For h-like events, background is negligible. Divide into subsets.

Slepton Mass Reconstruction: Degenerate Soft Masses with 500 fb⁻¹



- SM Background
- $\tilde{\tau}_1 \tilde{\tau}_1$
- $\tilde{\nu}_L \tilde{\nu}_L$
- Other SUSY

Scenario	DEG	Theory
$m_{\tilde{\ell}_1}$ (GeV)	290.51 ± 10.01	294.47
$m_{\tilde{\nu}_L}$ (GeV)	293.41 ± 2.15	293.37
$m_{\tilde{\nu}_R}$ (GeV)	100.05 ± 0.67	101.98