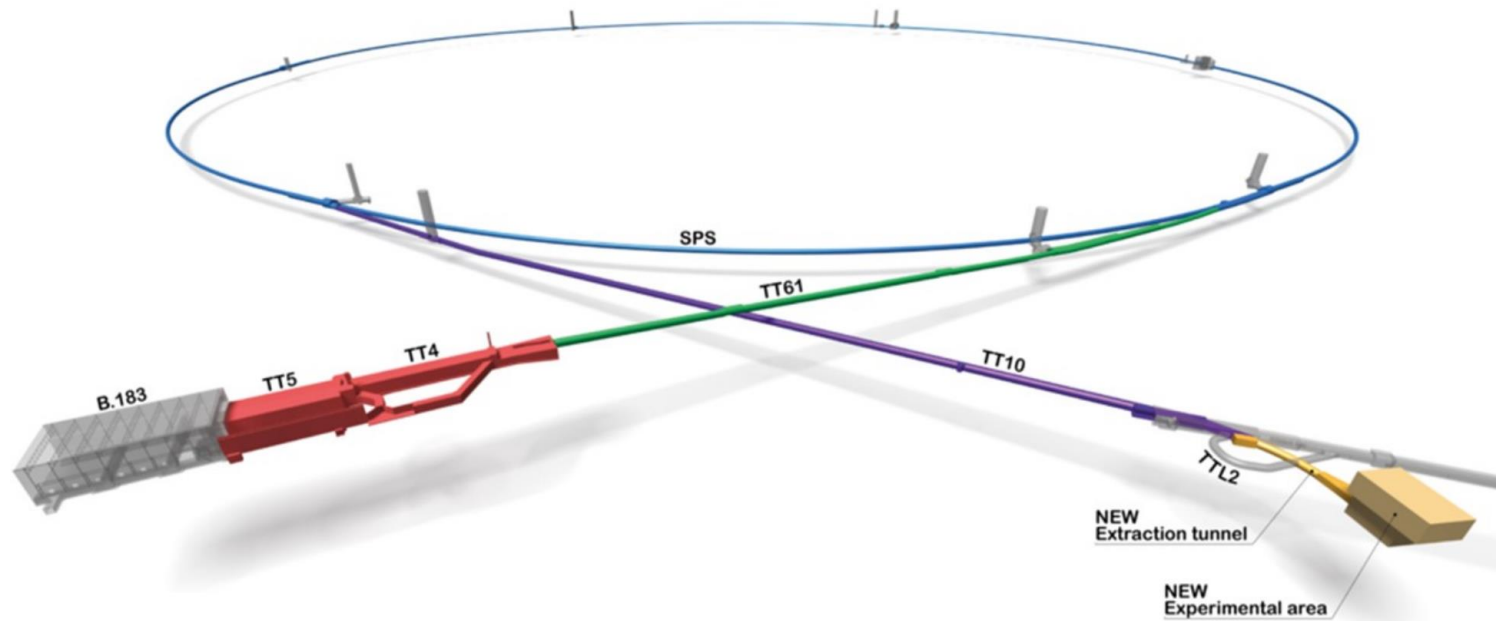


eSPS Design Study

Student Design Project 2020-2021



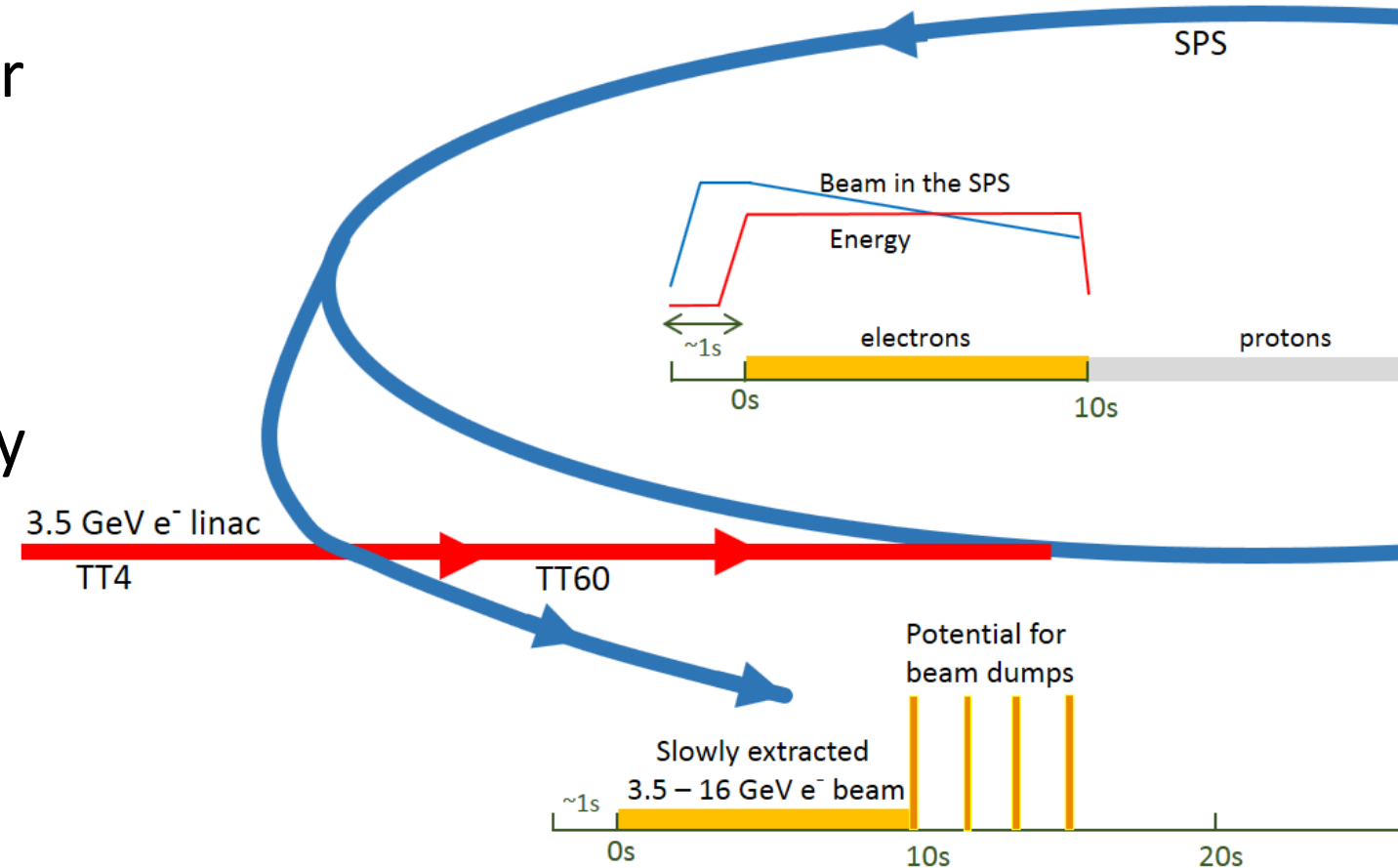
Majid Ali, Emily Archer, Pablo Arrutia, Joseph Bateman, Robert Murphy,
Cameron Robertson and Rebecca Taylor

Contents

Introduction	Motivations		
Lattice	Injection Line	Aperture & Acceptance	Dispersion Effects
Magnets	Injection & Extraction	FEMM Simulations	B-Field Analysis
RF Cavities	Infrastructure	Voltage Requirements	Cavity Design

eSPS Introduction

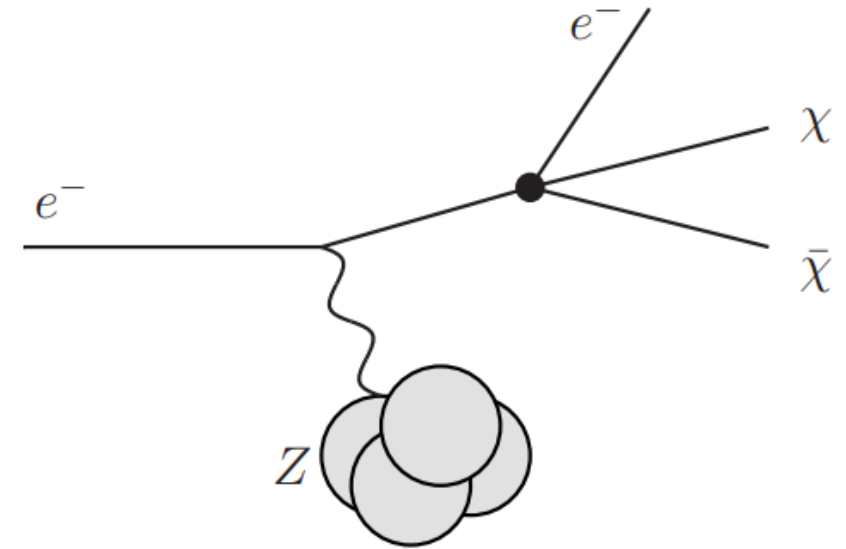
- Proposed electron accelerator using **SPS infrastructure**
- **3.5 GeV linac** with CLIC X-band technology
- Synchrotron extraction energy up to **16 GeV (18 GeV)**
- Electron target experimental area
 - Low-rate & beam dump experiments



A primary electron beam facility at CERN (2018)
<https://cds.cern.ch/record/2624786>

Physics Motivations: Dark Sector Physics

- Studying Light Dark Matter (**LDM**) candidates
 - MeV – GeV range
 - χ particle & corresponding A' boson
- Require **low-rate, high current** e^- beam
 - DM has low cross-section, so want high statistics, with low pile-up for individual measurements
- Precise electron beam gives good probe of **missing momenta** experiments
 - Axion-like particles, dark photons, etc
 - Electron-nucleus precision measurements for neutrino oscillation experiments

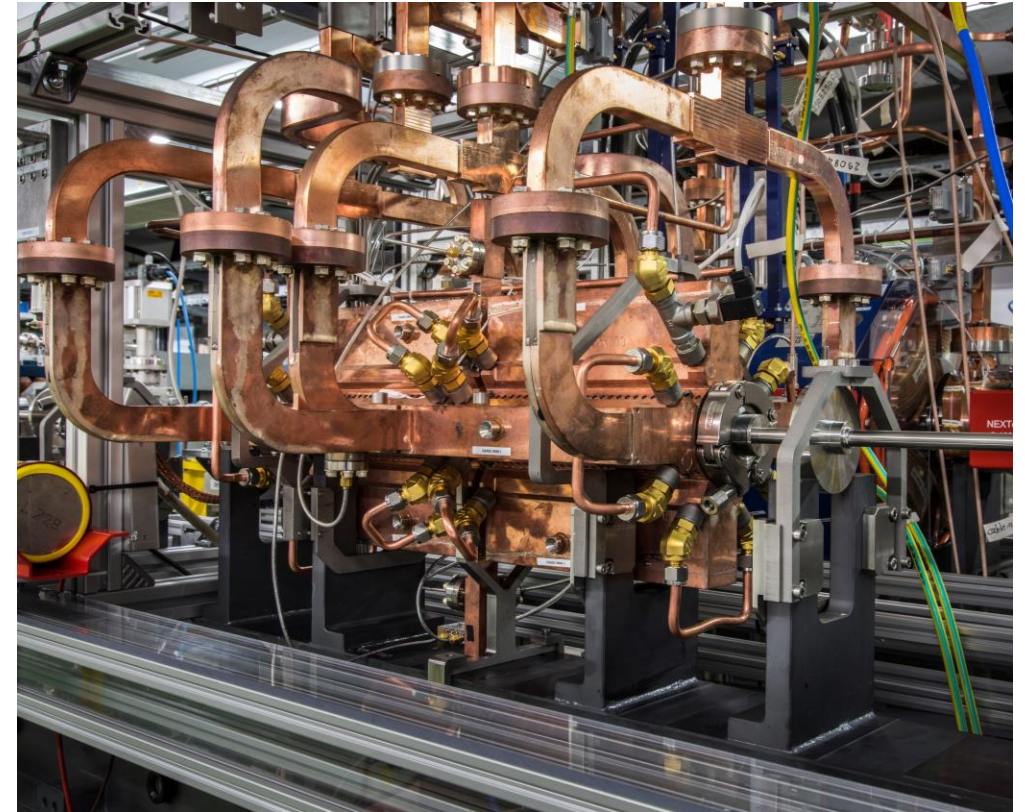


A primary electron beam facility at CERN - eSPS CDR (2020)

<http://cds.cern.ch/record/2730589>

Accelerator Motivations

- Demonstration of **CLIC X-band technology** with test site
 - 12 GHz linac from technology developed for CLIC
 - Next step in high-gradient acceleration
- Circular electron accelerator **infrastructure & training**
 - Preparation for next-generation Higgs-factories
- Wakefield accelerator **test facilities**
 - Can adapt for plasma wakefield electron bunches
- Producing **RF cavity R&D** to match FCC-ee requirements
 - 800 MHz superconducting cavities



*New module installed in CLIC test facility (2015)
Brice, Maximilien cds.cern.ch/record/1982610*

Lattice Team

Rob Murphy and Rebecca Taylor

Injection Line

Aperture &
Acceptance

Dispersion
Effects

Injection line sections

LINAC matching

Match Twiss parameters into FODO line

FODO

Will transport the beam to TT61

TT60

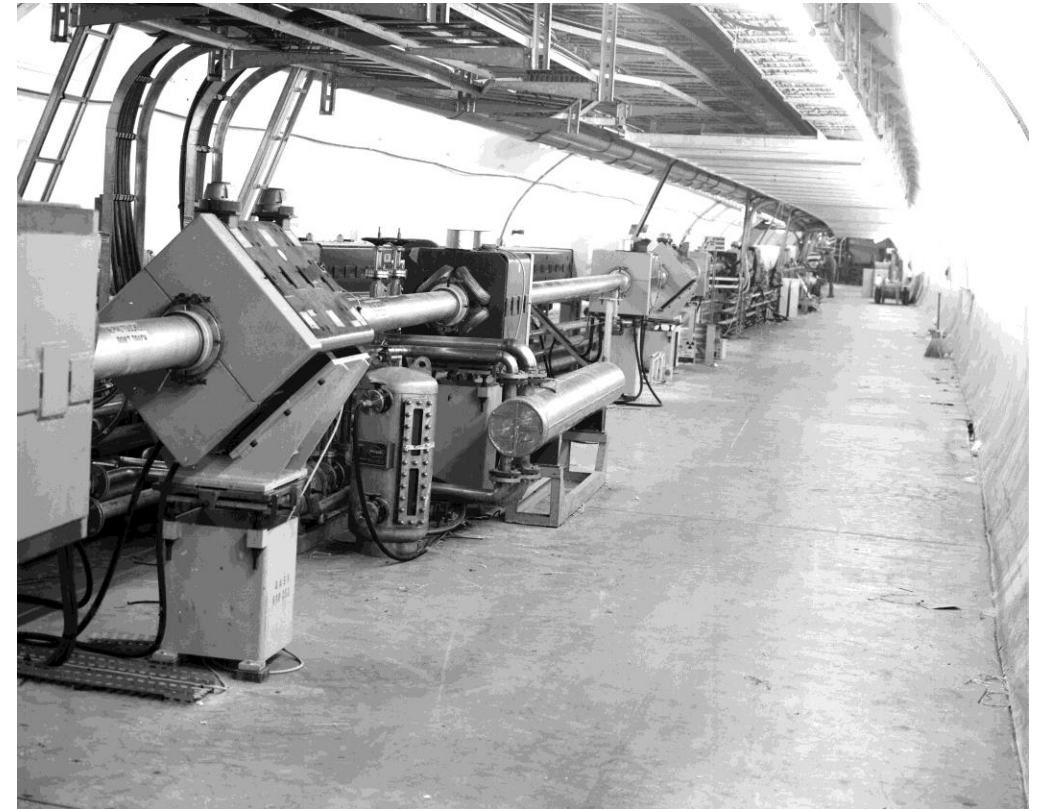
Currently proton injection into LHC. Will transport electrons into eSPS

SPS

Synchrotron, completed in 1970s. Has accelerated e^- , e^+ , \bar{p} and p .
Readapting for electrons

Injector Line

- LINAC in TT5/TT4 provides bunch of 5- \rightarrow 40 ns.
 - High repetition rate (200 ns at 100 Hz).
- TT60 Previously used to transfer protons to West Area.
- e^- injected in opposite direction to p .
 - 3.5 GeV kicker at 100Hz repetition rate.



View of beam traffic in TT60 tunnel, looking towards the SPS (1981)
<http://cds.cern.ch/record/754068>

Method

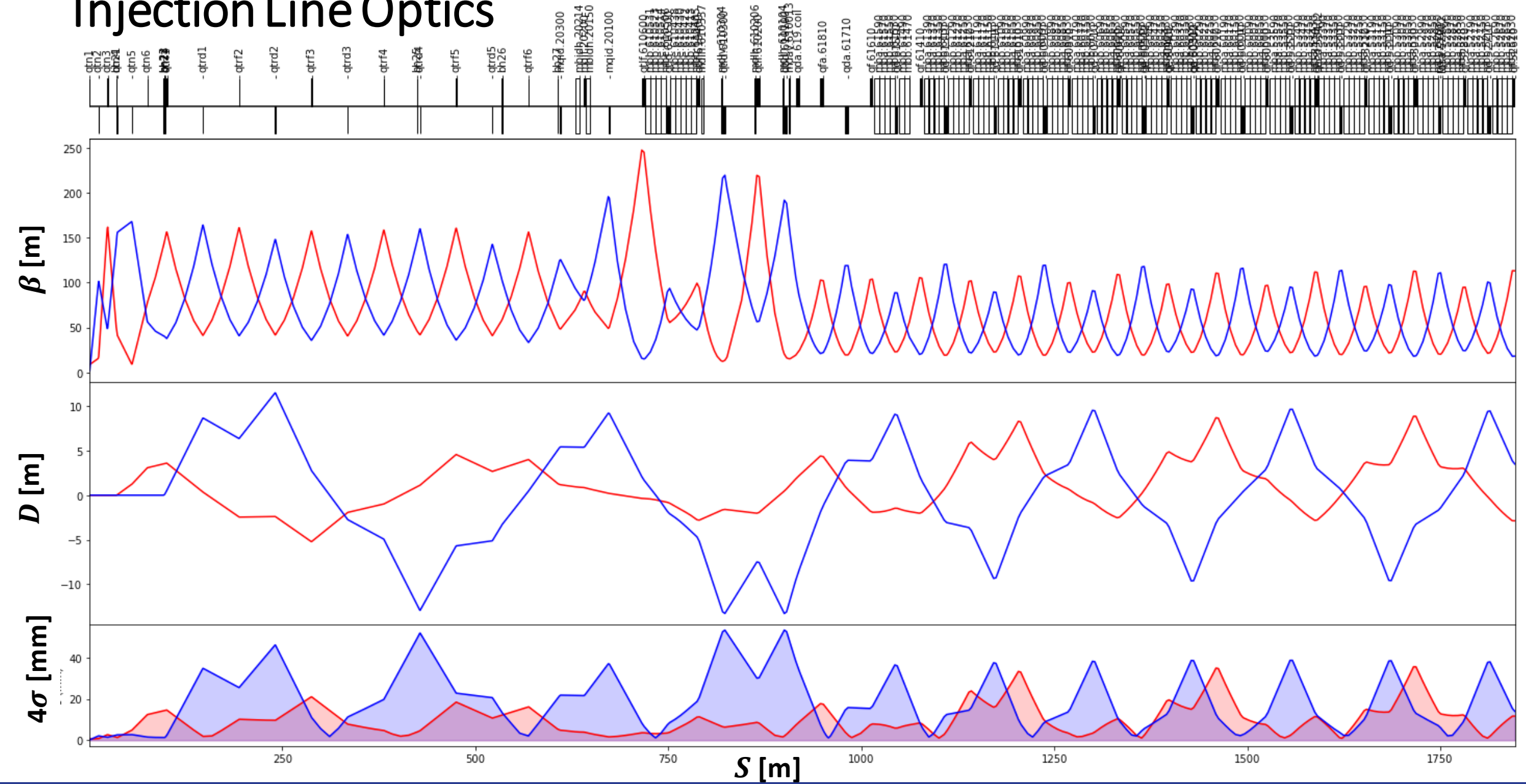
- Start with Twiss parameters (alpha, beta, dispersion) and working backwards from SPS (fixed optics).
- Use Twiss parameters, track backwards through TT61. Provides target Twiss parameters at start of TT61.
- Match parameters from LINAC into TT61 using matching routine in MADX e.g. Simplex.
- Use full Twiss parameters to calculate beam envelope.
- Compare beam envelope to physical aperture.

NAME	COMPONENT	BETX (m)	BETY (m)	ALFX	ALFY	DX
START_FODO	MARKER	295.43	19.15	-3.37	1.17	5.41
DRIFT_6	DRIFT	306.91	15.56	-3.45	0.96	5.62
QTRF1	QUAD	306.81	14.91	3.69	0.56	5.65

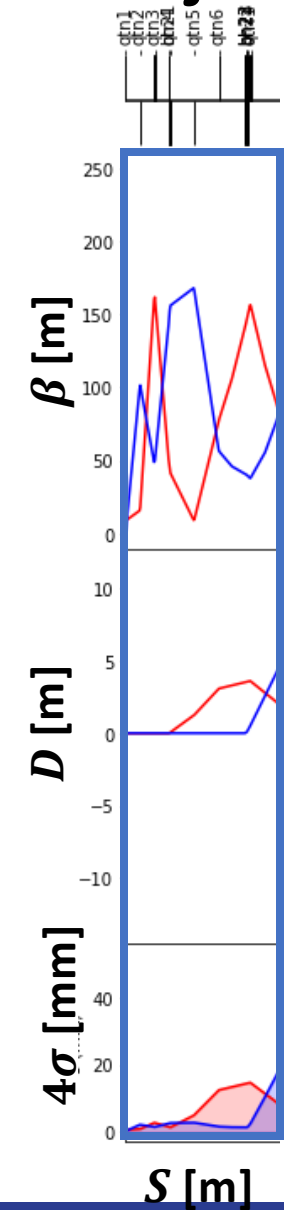
Challenges of eSPS lattice design

Pros	Cons
Existing Infrastructure	Limited Space
Development time	Constrained apertures (magnets)
Reusable components	Operational requirements
NEW PHYSICS!	Activation products/materials

Injection Line Optics



Injection Line Optics

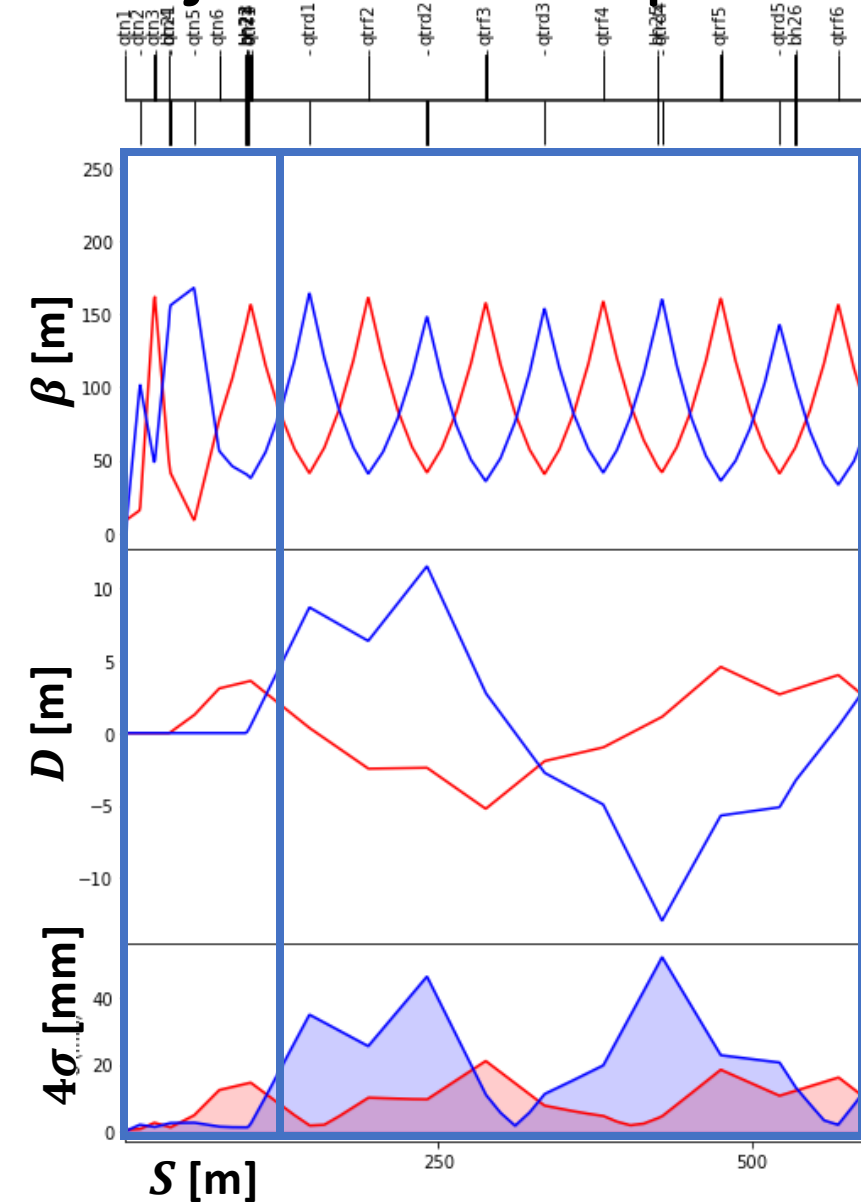


Linac Matching:

- Initial optics calculated from a FODO cell of 5.3 m length and 90° phase advance
 - $\beta_x = 9\text{m}$, $\beta_y = 1.5\text{m}$
- **98.5 m long** – to match small linac beam to larger beam for the FODO transport
- 6 QTN magnets & 4 BH2 magnets
- 20° slope causes large dispersion in y
 - 36.4% tunnel downwards

Credit to Pablo Arrutia for the MADX sequence

Injection Line Optics

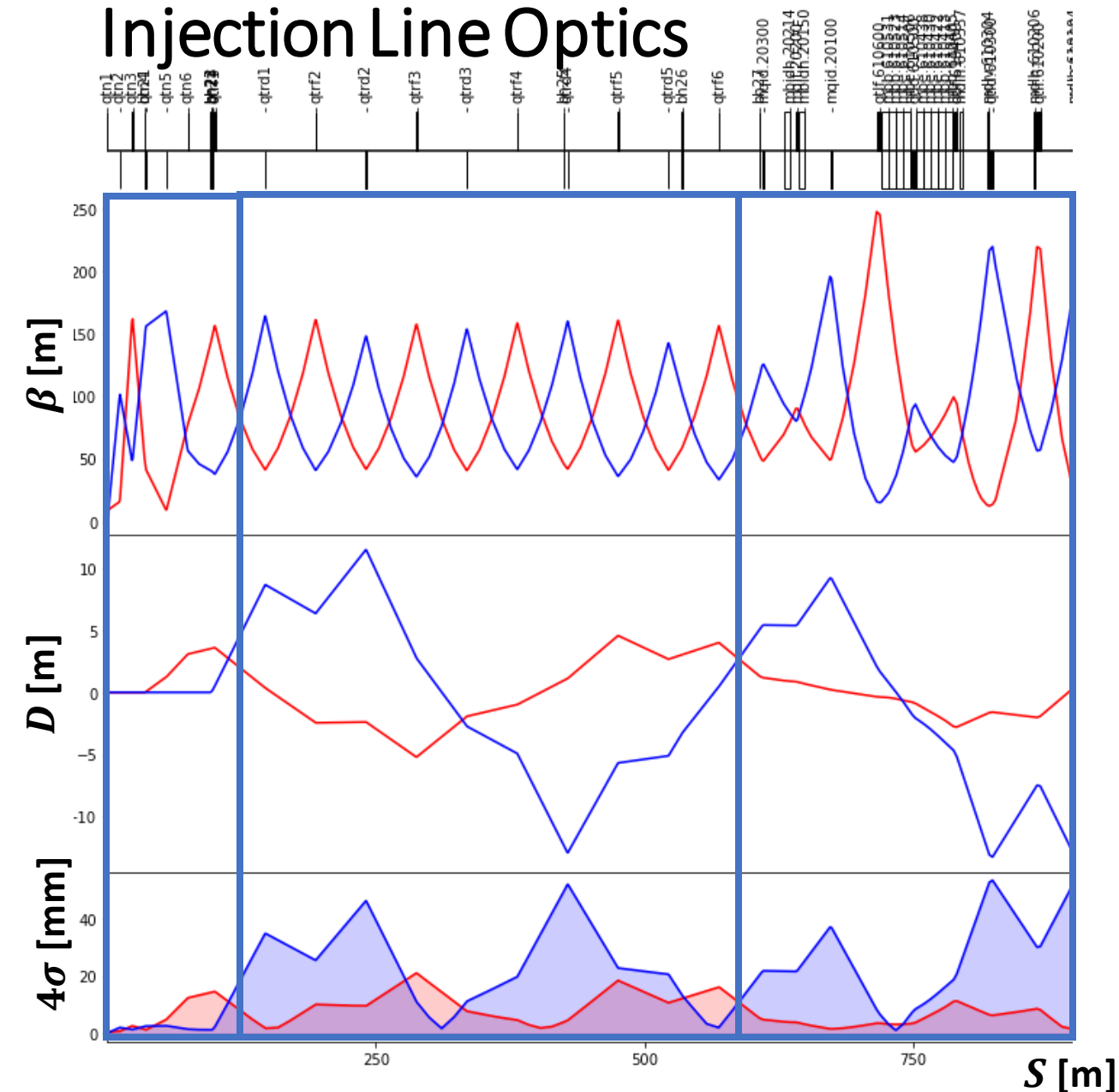


FODO line:

- Transporting beam from linac towards SPS
- **510 m long** – want quadrupoles with large focusing length
- 10 QTR magnets & 3 BH2 magnets

Credit to Pablo Arrutia for the MADX sequence

Injection Line Optics

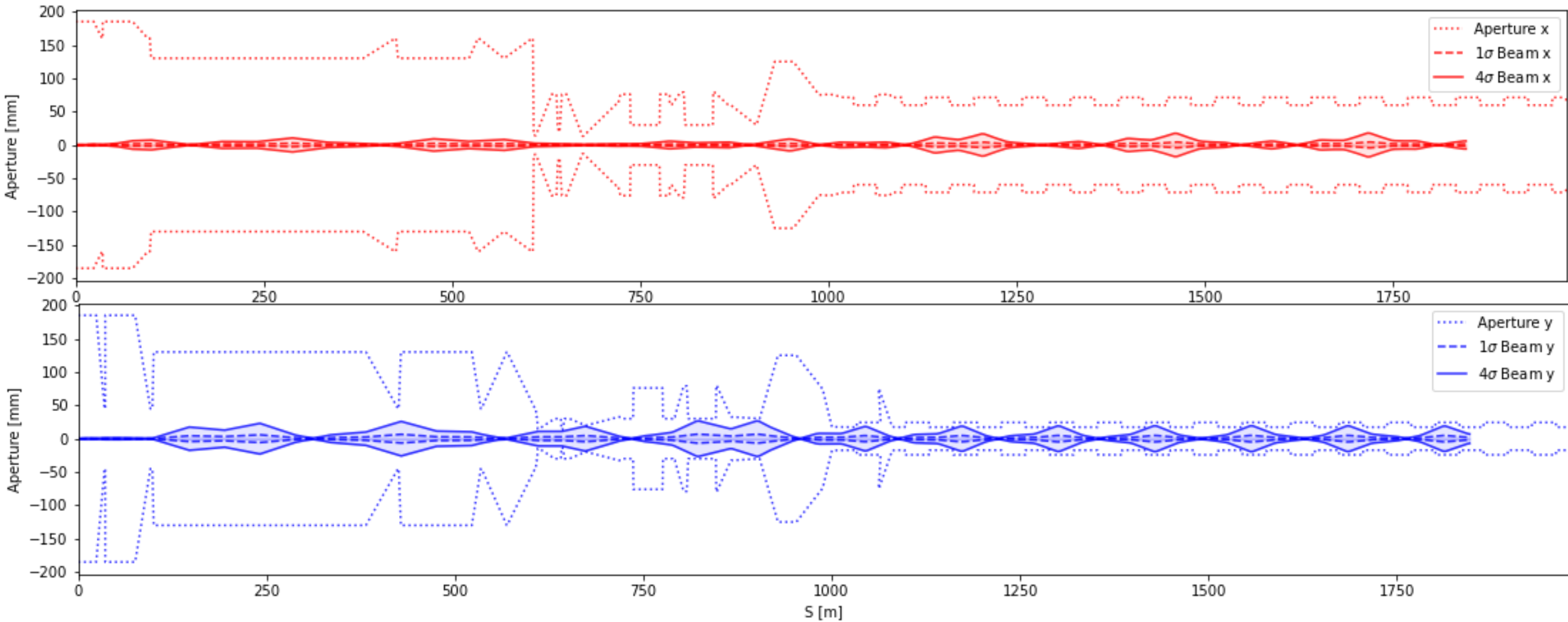


TT61 Line:

- Same as existing line
 - Reversed it and matched to SPS injection
- **307 m long**

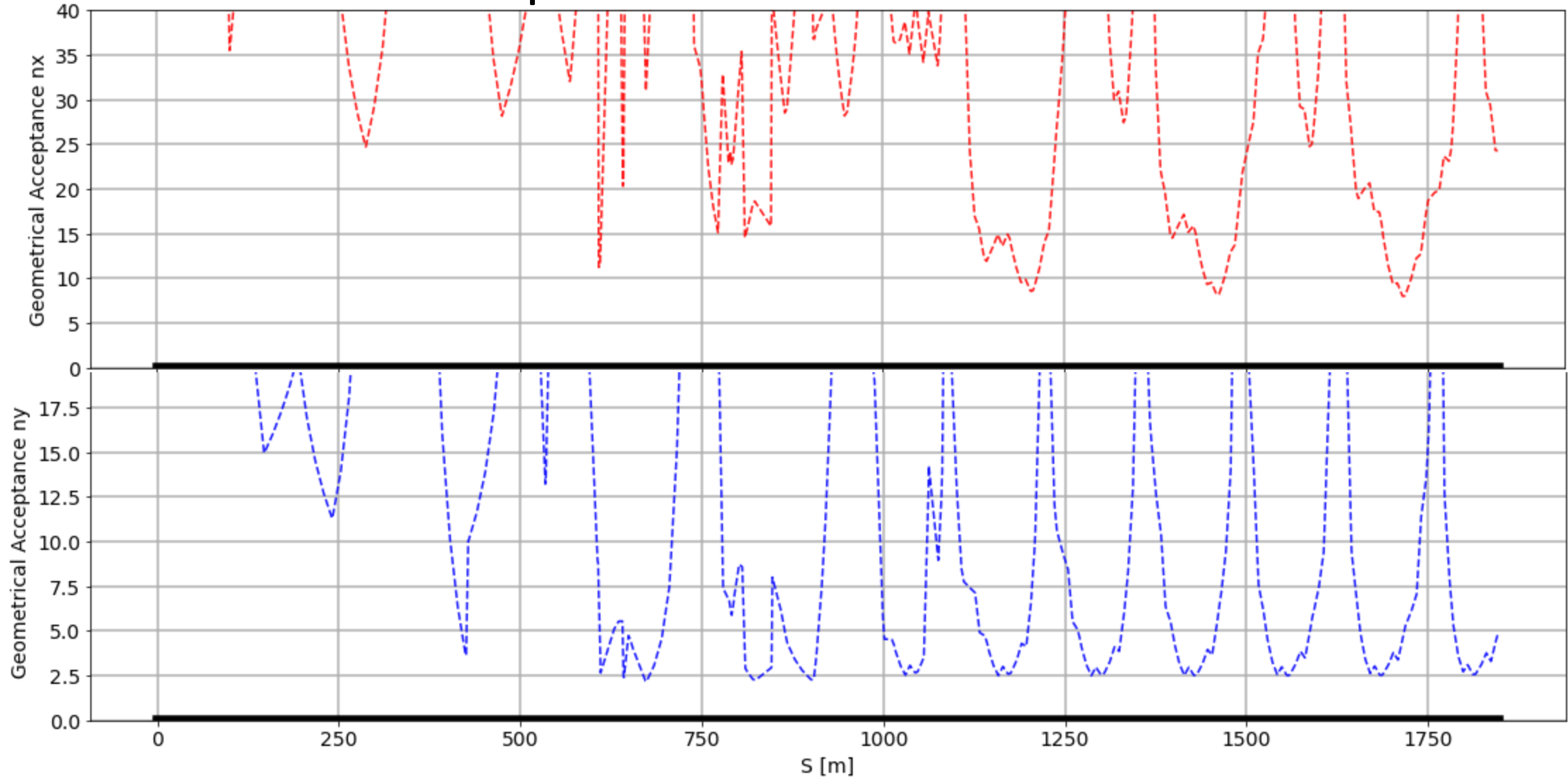
Credit to Pablo Arrutia for the MADX sequence

Beam size & apertures



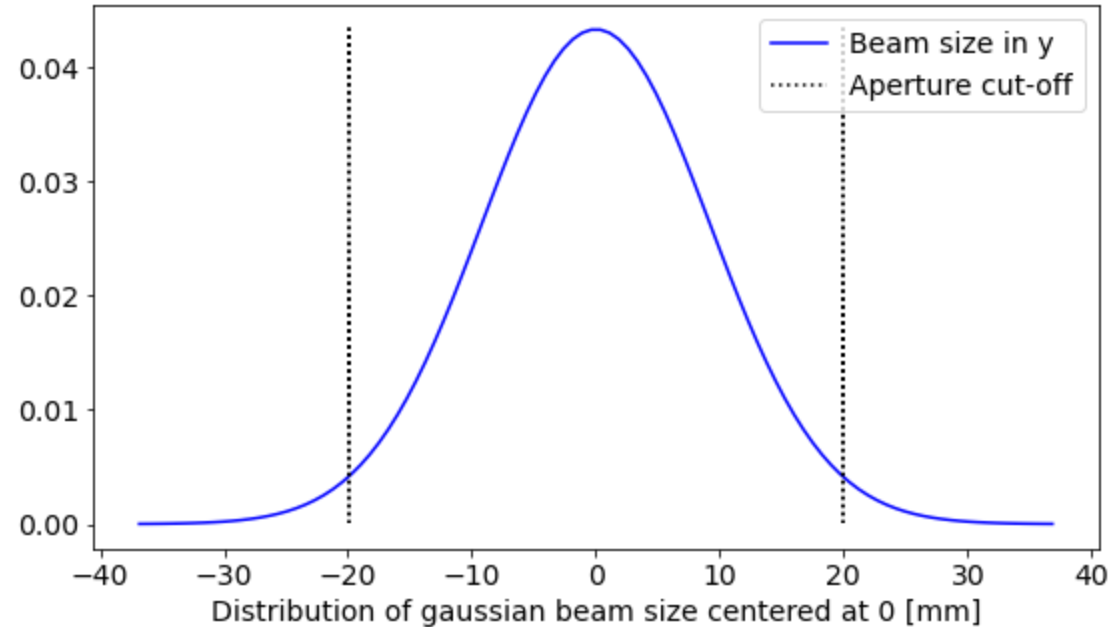
Beam size & apertures

$$n_x = \frac{A_x}{\sigma_x}, \quad n_y = \frac{A_y}{\sigma_y}$$

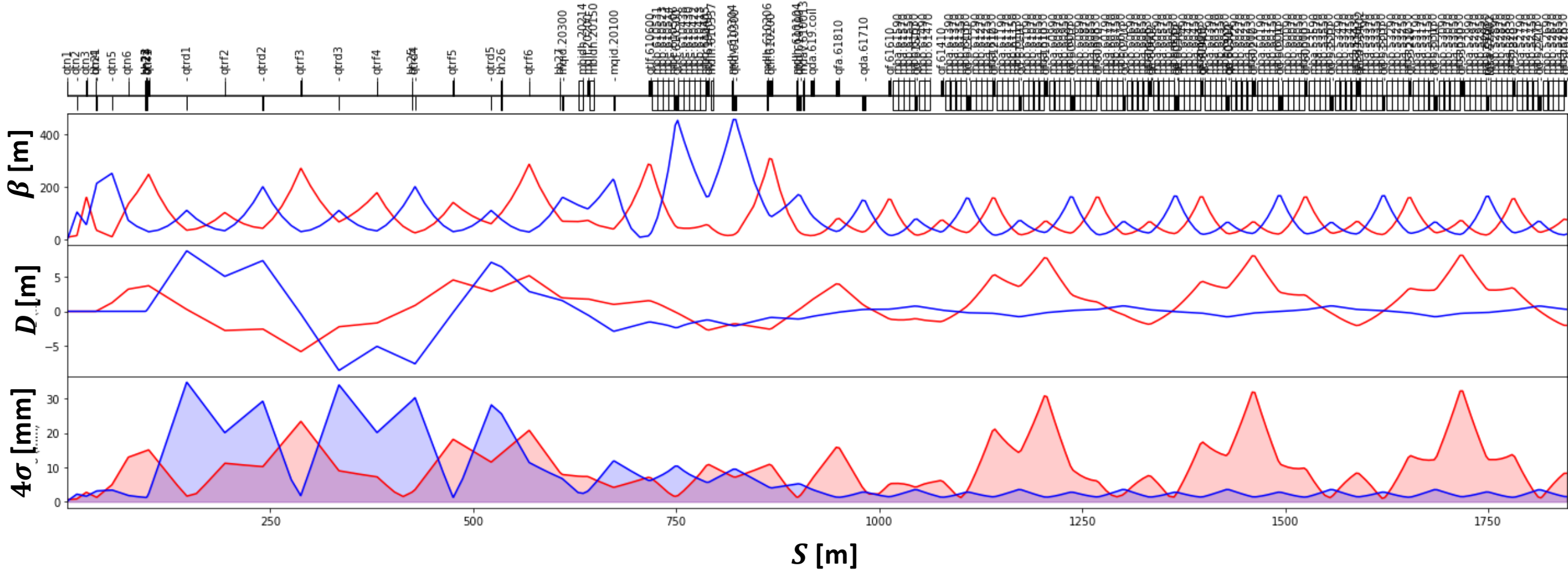


Beam size & apertures

- Large y dispersion from the 20° slope
 - Large beam envelope 2.1σ away from the aperture
 - Beam transmission: **97.0%**
- To reduce y -plane dispersion:
 - Adjust phase advance
 - Dispersion cancelling techniques
- It is possible to increase beam current to replace losses
- Try matching but reduce dy and dyp

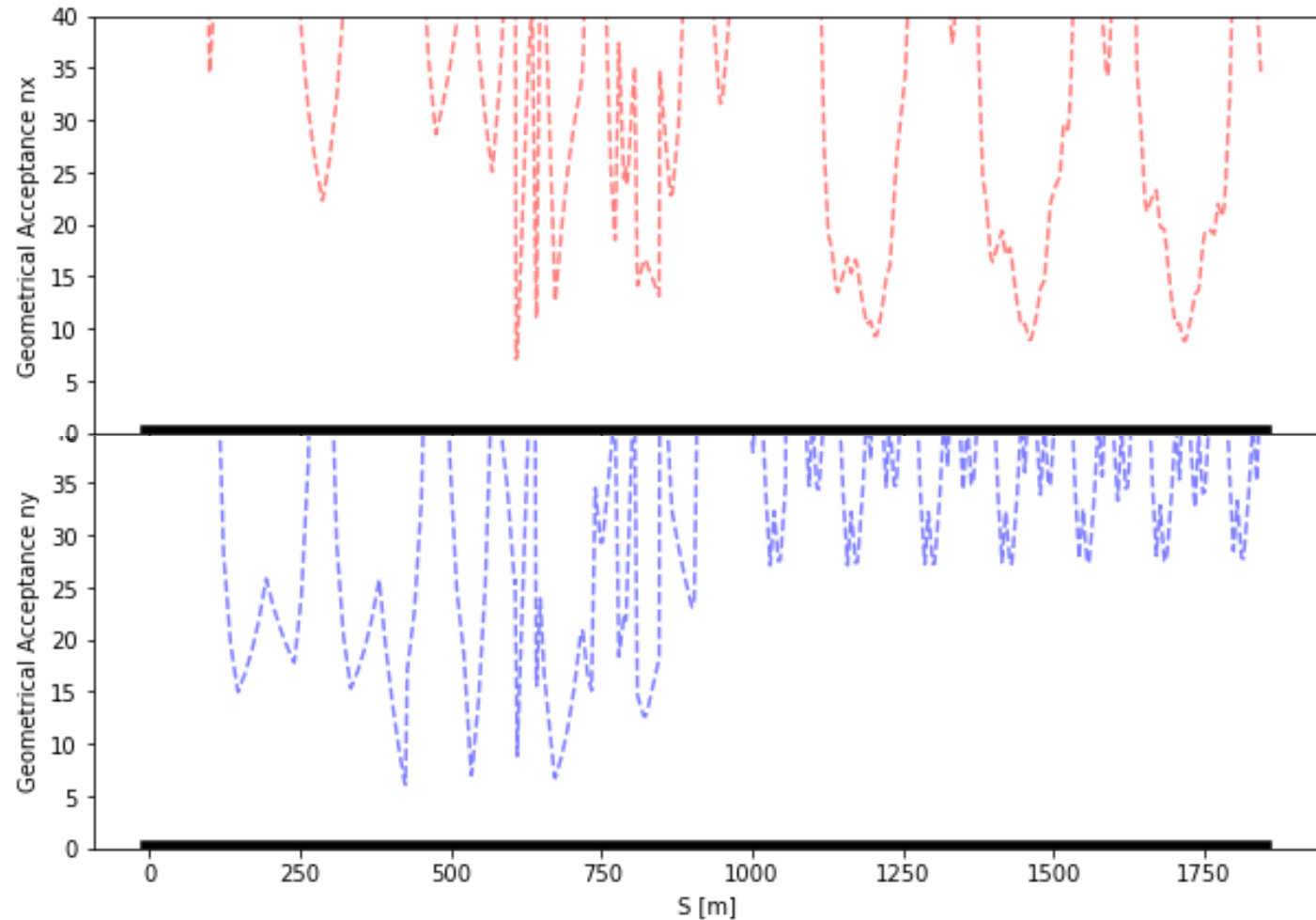


Optics solution with reduced dispersion



Optics solution with reduced dispersion

- Matching with $dy < 1$, $dpy < 0.1$
 - Less periodic solution
 - Reduces beam size
- Sigma from aperture is 7σ in x and 6σ in y
- Further investigations can find more appropriate solutions



Future Lattice Studies

To observe beam optics through many turns of the SPS

Incorporating RF cavity design and observing effects to the beam

To ensure injection phase-space matches those required for the SPS

Less requirements on e^- matching due to synchrotron radiation

To find periodic solutions with reduced x & y-dispersion

Ensure beam transmission remains good throughout turns of the SPS

Apply dispersion cancelling techniques to cancel effect of 20° slope

Apply the same techniques to design extraction line

Design new beamline with a large defocusing for the target area

Use existing TT10 line to see if beam fits after extraction

Magnets Team

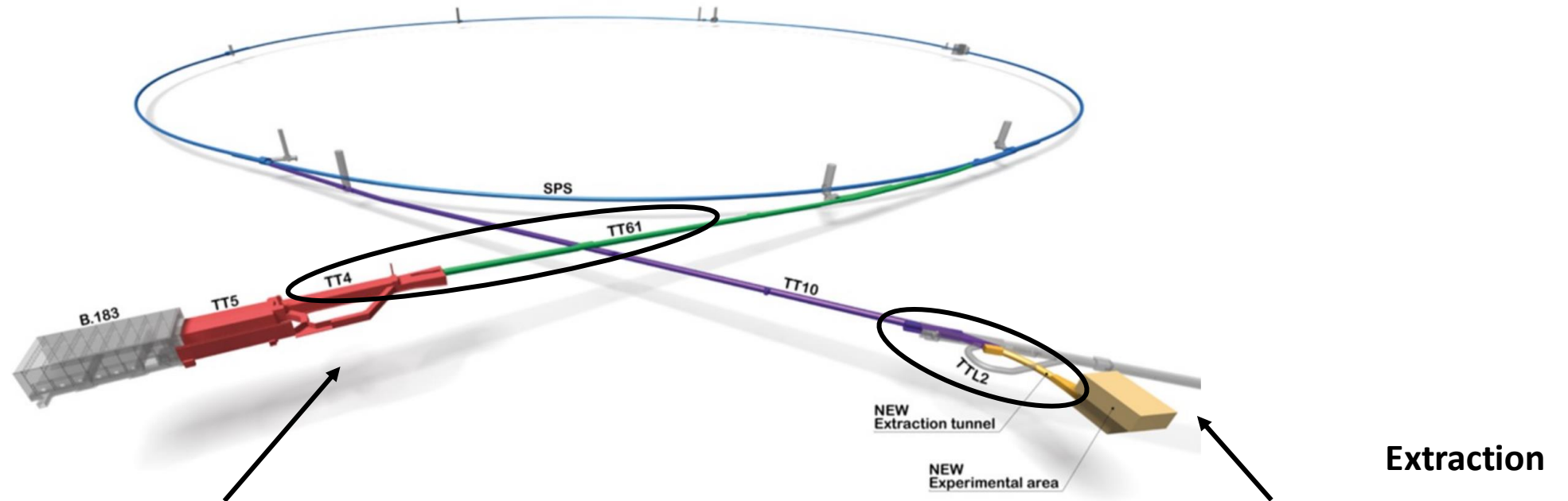
Emily Archer and Joe Bateman

Injection &
Extraction

FEMM
Simulations

B-Field
Analysis

eSPS Magnets



Injection

- 3.5 GeV Compact X-band Linac to existing TT61 transfer line.
- The magnets in TT61 line should be air-cooled to avoid installation of a new water supply.

Using existing magnets!

Extraction

- Existing TT10 transfer line to new experimental hall
- Electrons extracted from the SPS cross protons being injected from the PS

Dipole Bending Angle

$$\alpha = \frac{L}{\rho},$$

magnet length (pointing to L)
bending radius (pointing to ρ)

$\rho \approx \frac{3.3356 \bar{p} }{B} = \frac{11.6746 \text{ T m}}{B \text{ T}},$	$ \bar{p} = 3.5 \text{ GeV}/c$ injection from the linac
$\rho \approx \frac{3.3356 \bar{p} }{B} = \frac{53.3696 \text{ T m}}{B \text{ T}},$	$ \bar{p} = 16 \text{ GeV}/c$ extraction to the experimental hall

INJECTION

$$\alpha = \frac{L * B \text{ T m}}{11.6746 \text{ T m}},$$

EXTRACTION

$$\alpha = \frac{L * B \text{ T m}}{53.3696 \text{ T m}},$$

Quadrupole Focusing Strength

Normalised field gradient coefficient (K1 in MADX), often k in literature

$$K = \frac{1}{B\rho} \frac{\partial B_y}{\partial x}$$

$$B\rho \approx 3.3356|\bar{p}| = 11.6746 \text{ T m}$$

injection from the linac

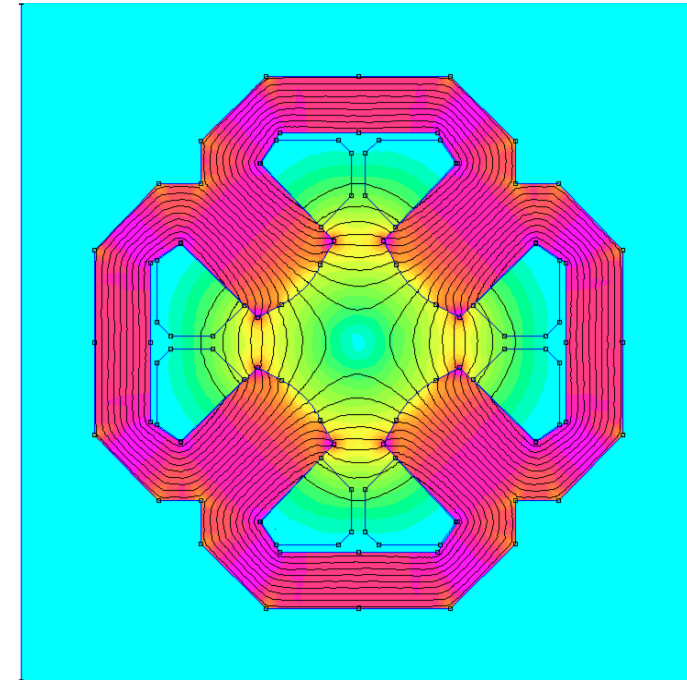
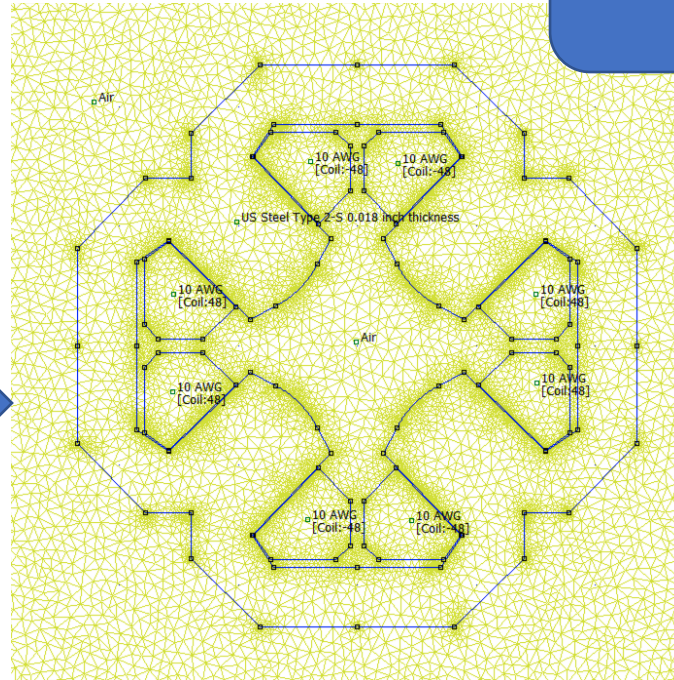
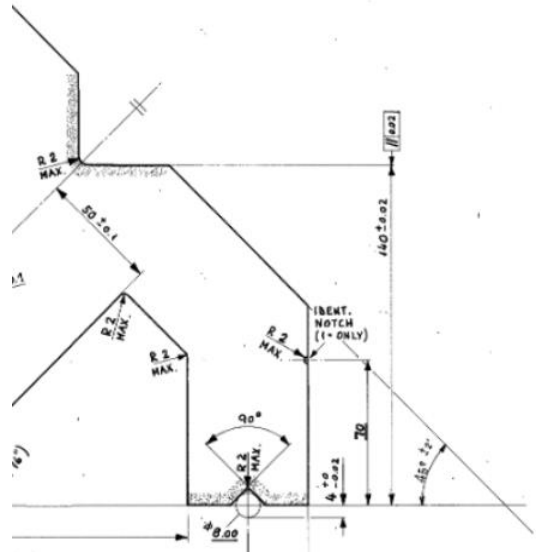
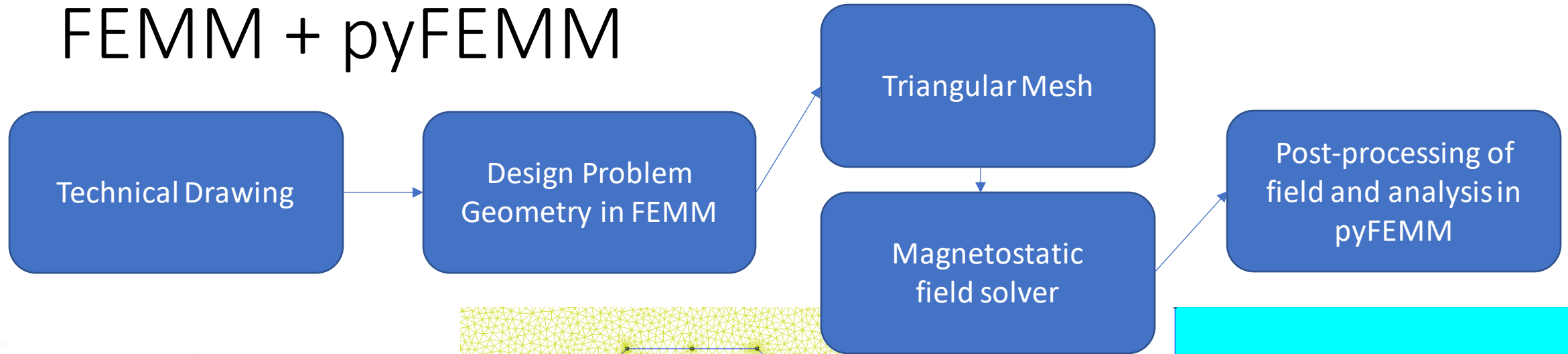
$$B\rho \approx 3.3356|\bar{p}| = 53.3696 \text{ T m}$$

extraction to the experimental hall

use the gradient nominal field B_{nom} at peak current to estimate $\partial B_y / \partial x$

$$f = \frac{1}{KL} \quad L \text{ is the length of the magnet}$$

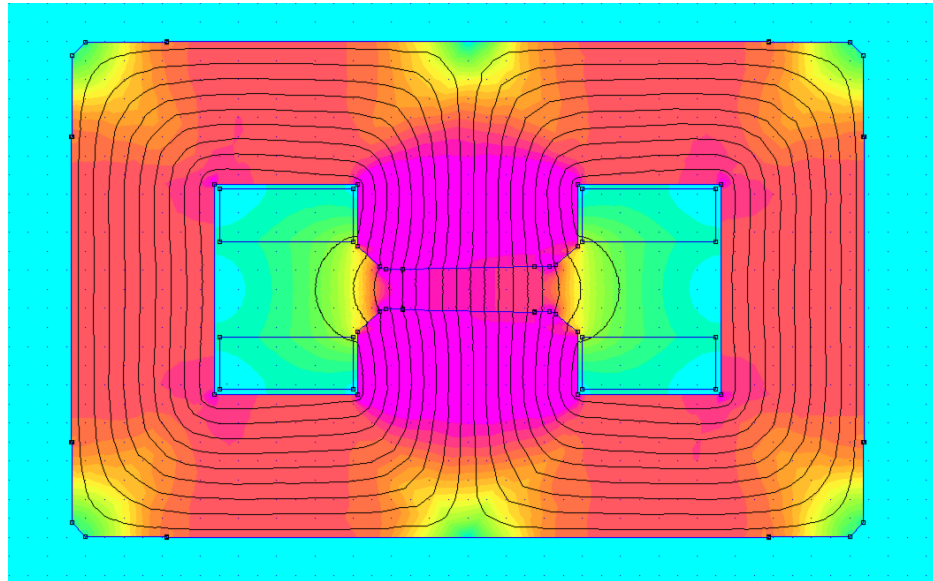
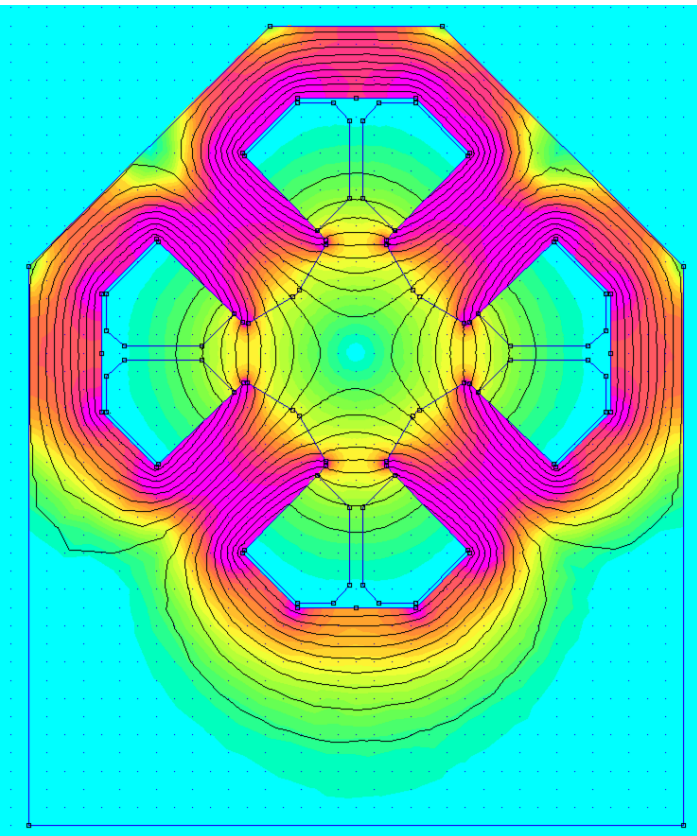
FEMM + pyFEMM



CERN Database (Accessed: 2020)

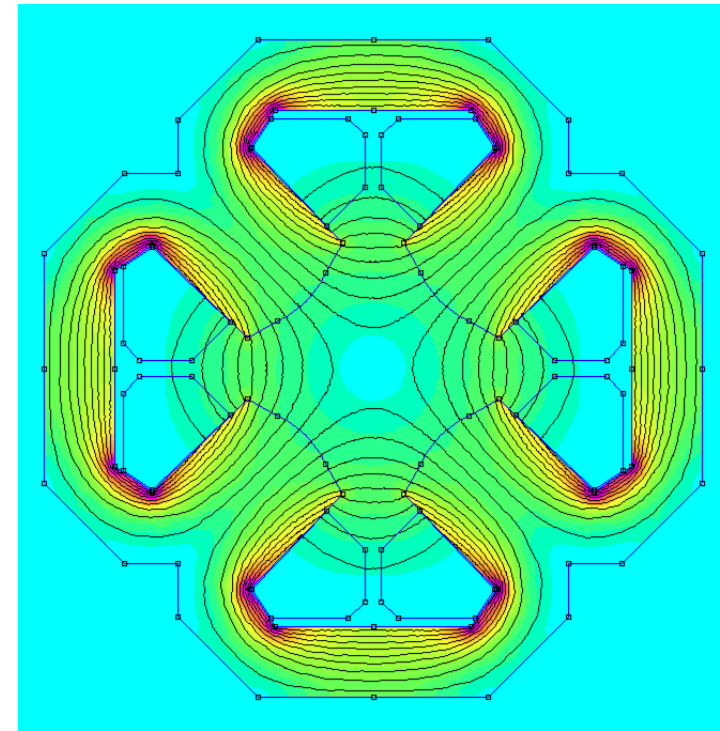
FEMM Models - Injection

QTN Quadrupole

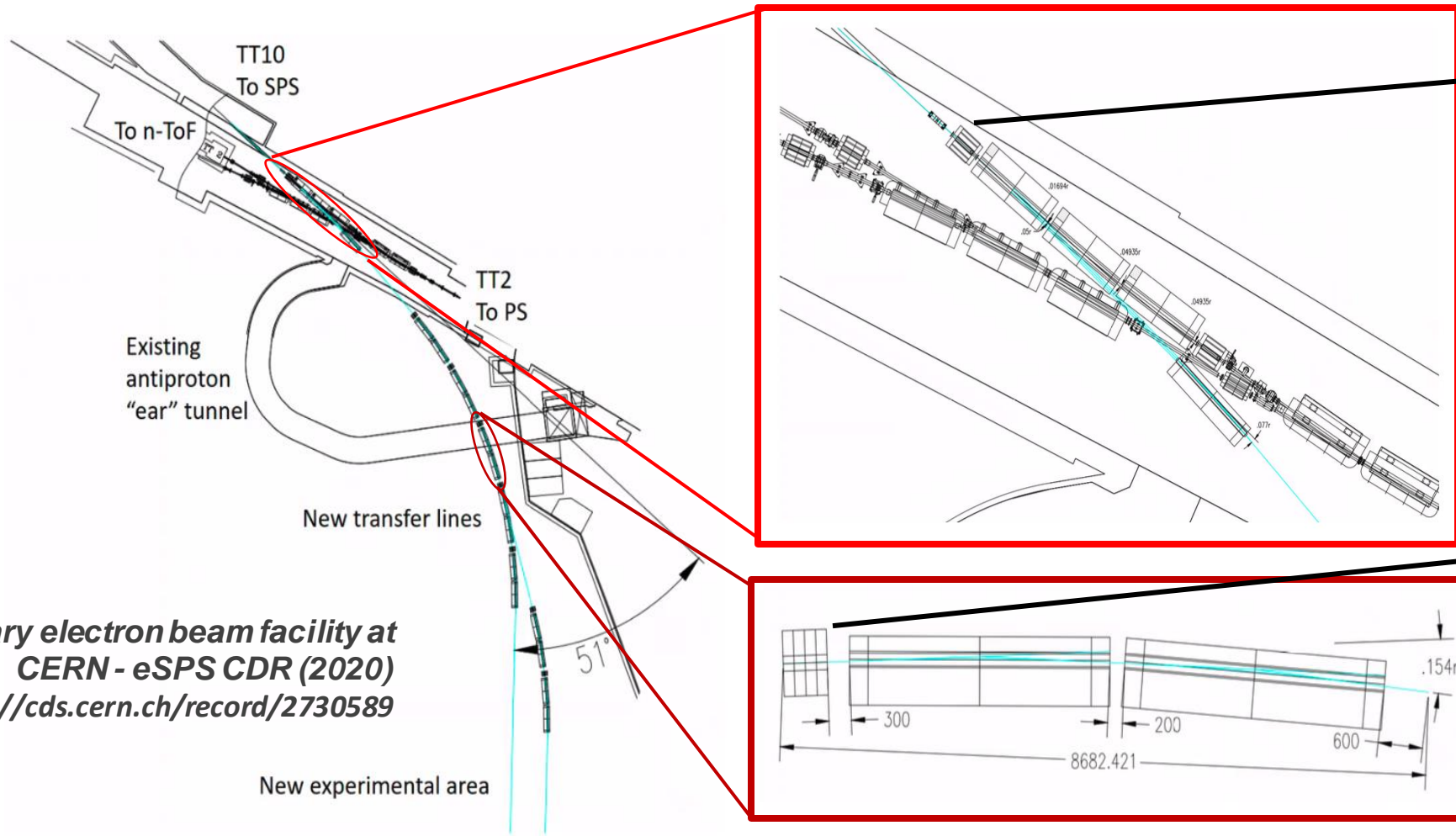


BH2 Dipole

QTR Quadrupole



Extraction Line Magnets



CDR: BH2 – 50 mrad.
 (would require 4)
 Or MCW at 258.75 A.

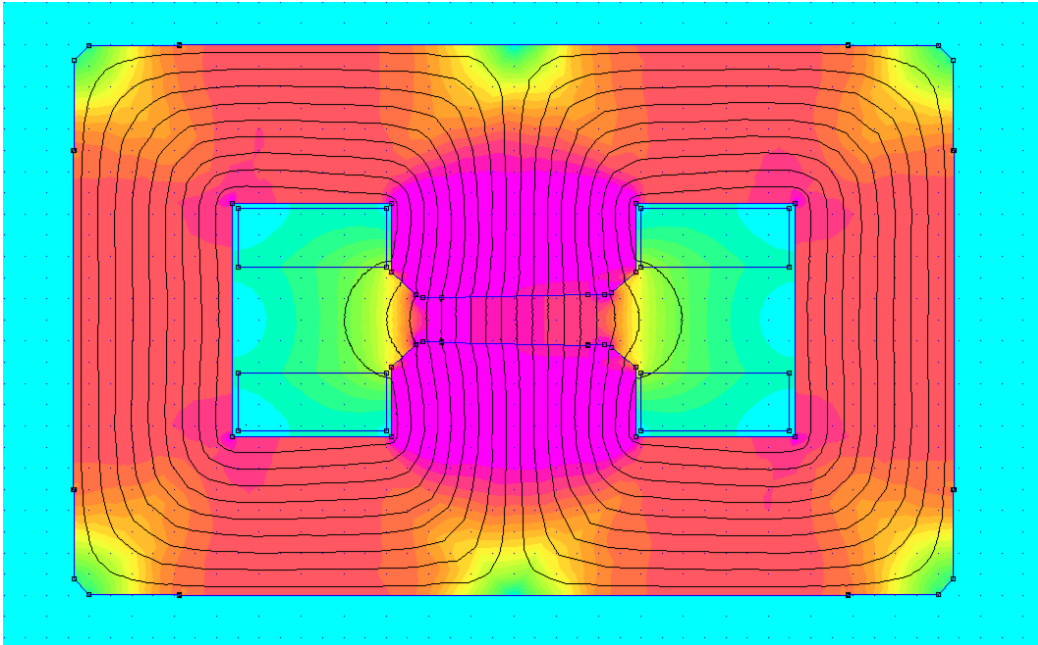
Bending Cell – 2 MCW at
 414.5 A (77 mrad each)
 and FODO arrangement.

*A primary electron beam facility at
 CERN - eSPS CDR (2020)
<http://cds.cern.ch/record/2730589>*

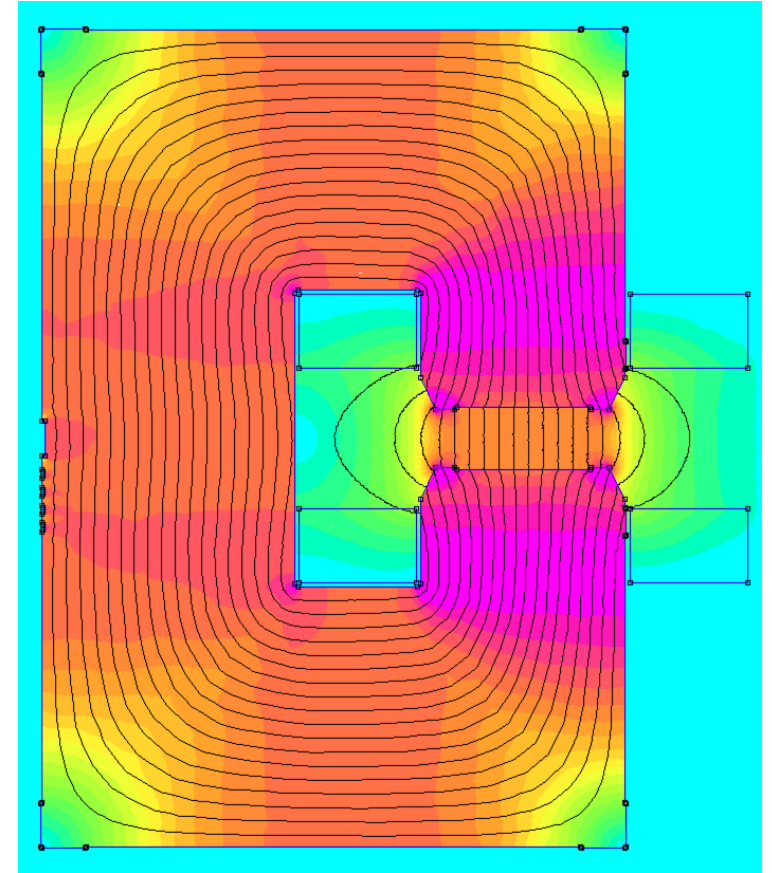
New experimental area

FEMM Models – Extraction

BH2 Dipole

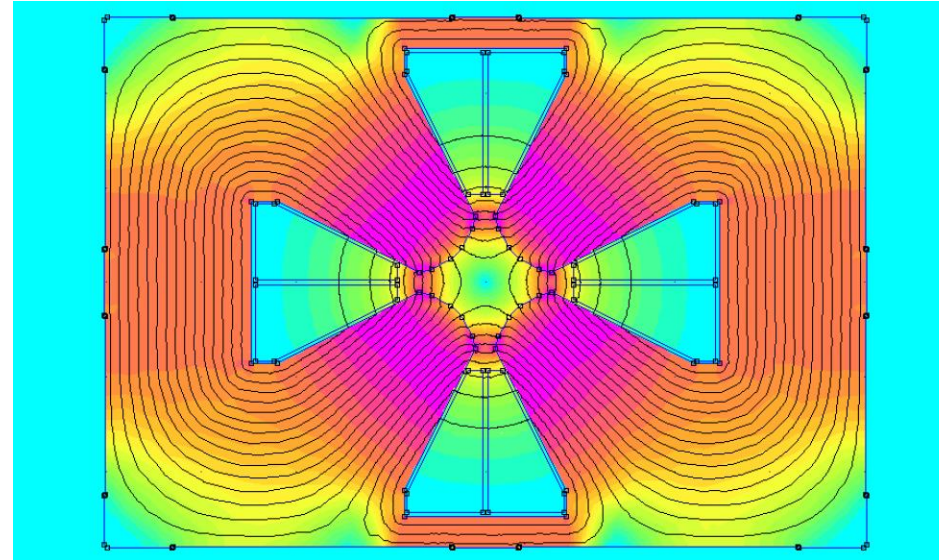
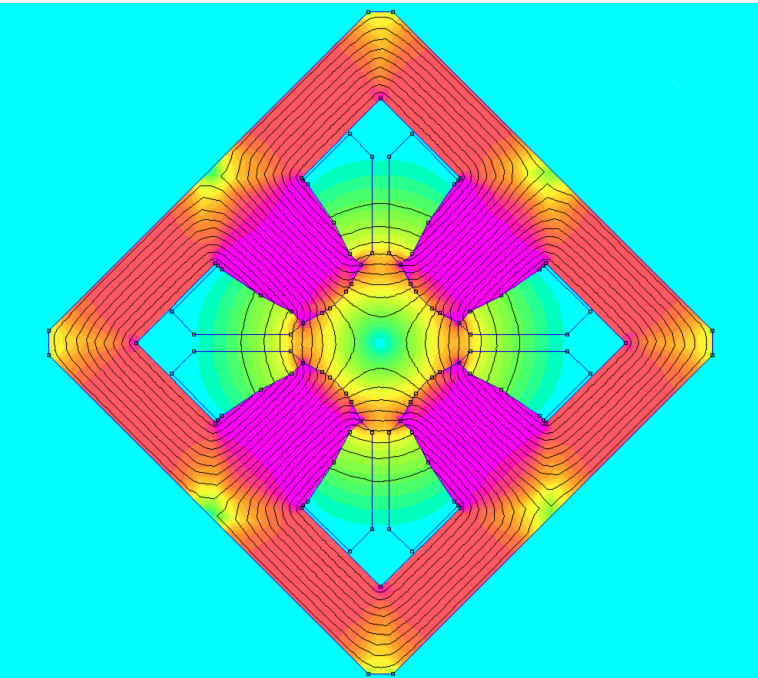


MCW Dipole



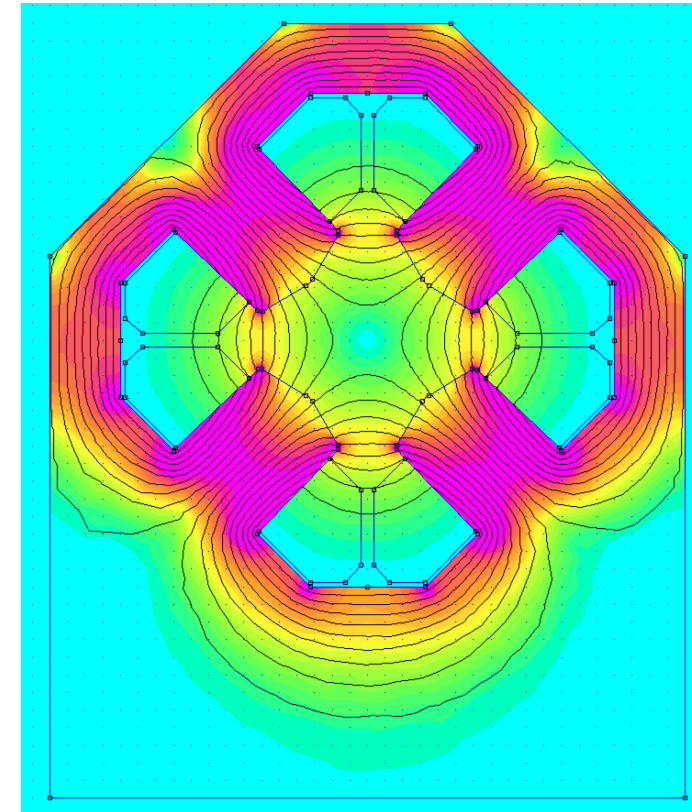
FEMM Models – Extraction

Q200 Quadrupole

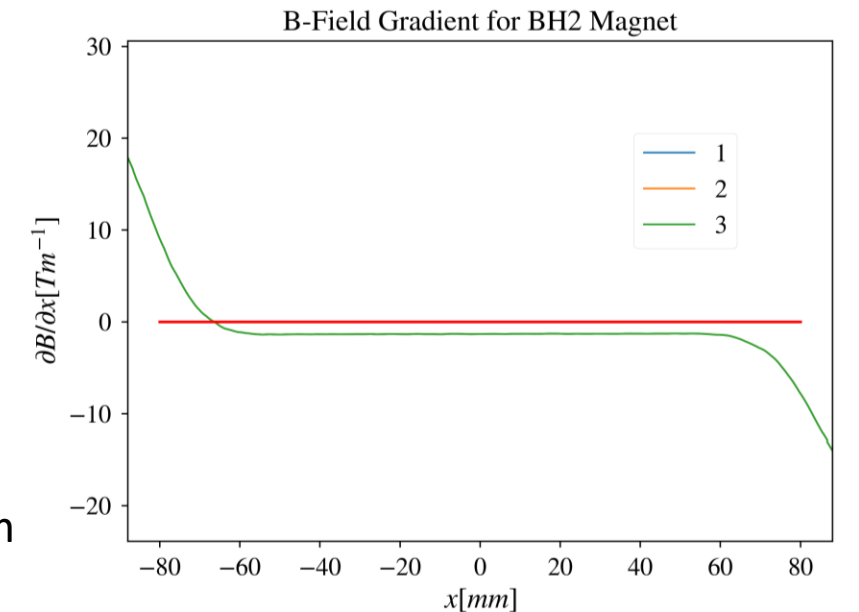
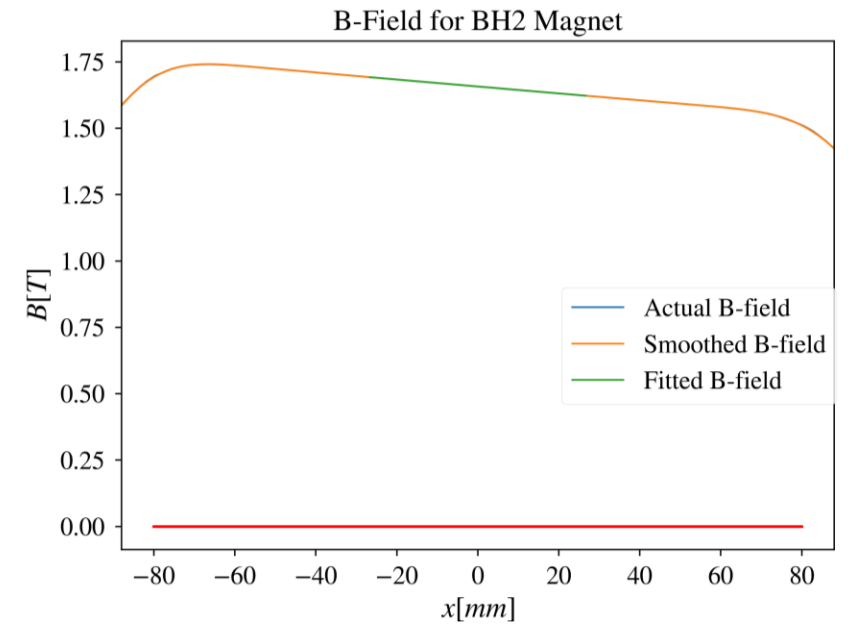
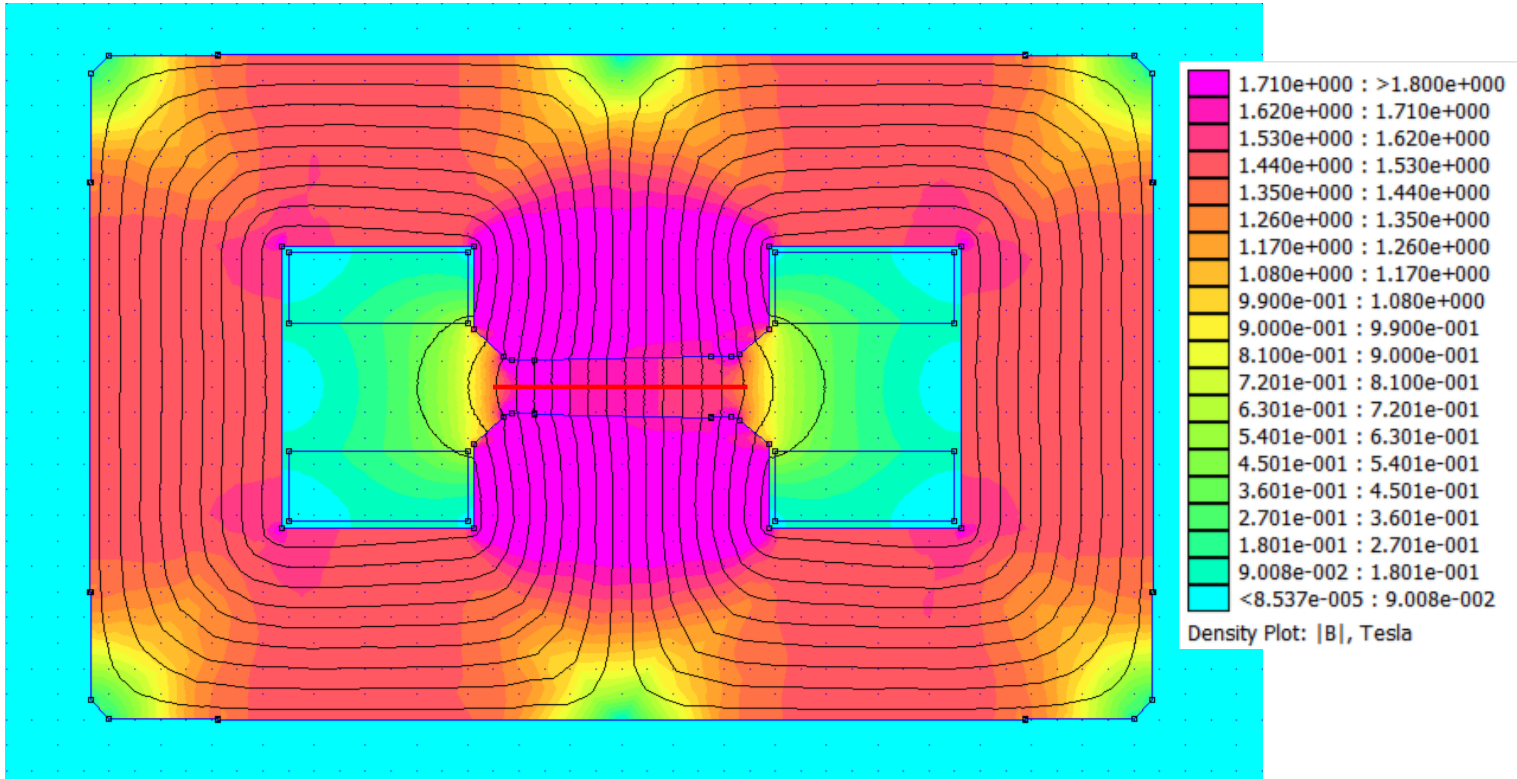


QTS Quadrupole

QTN Quadrupole



Field Analysis- BH2



48 turns/pole, 650 A (peak)
 Aperture width and height: 160 mm, 45 mm
 Total width and height: 915 mm, 570 mm

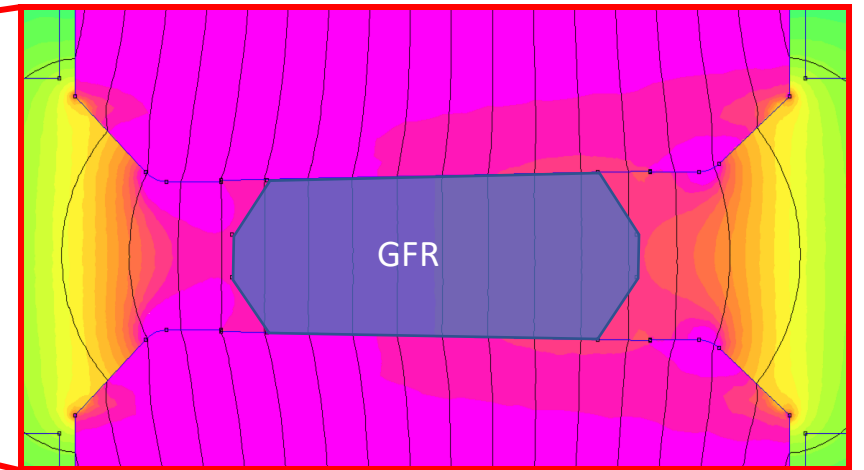
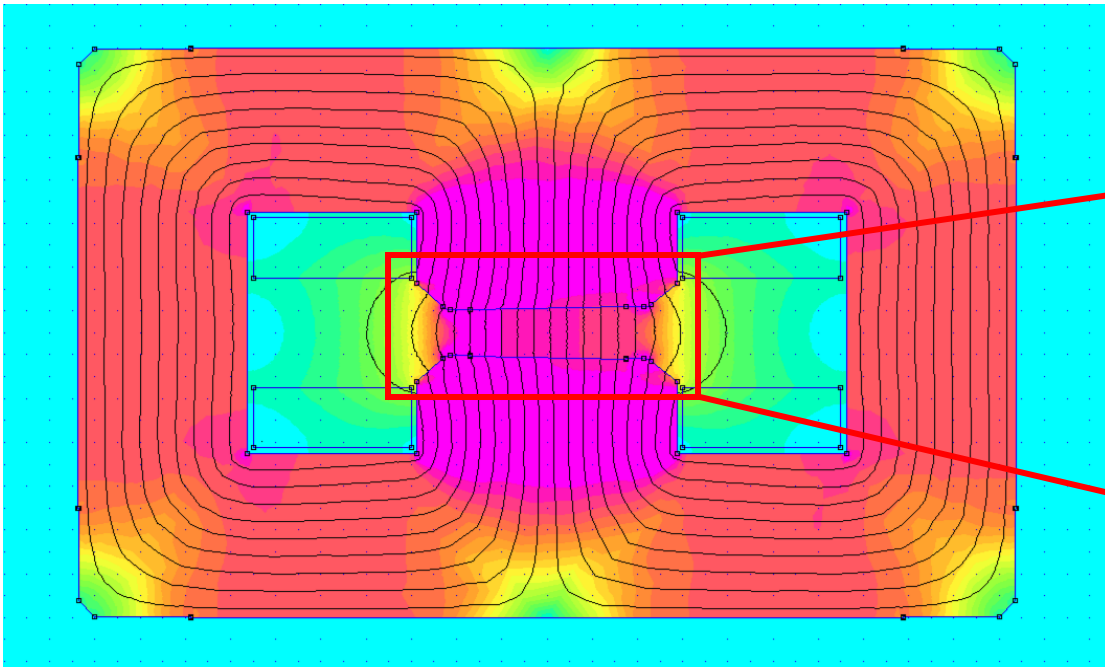
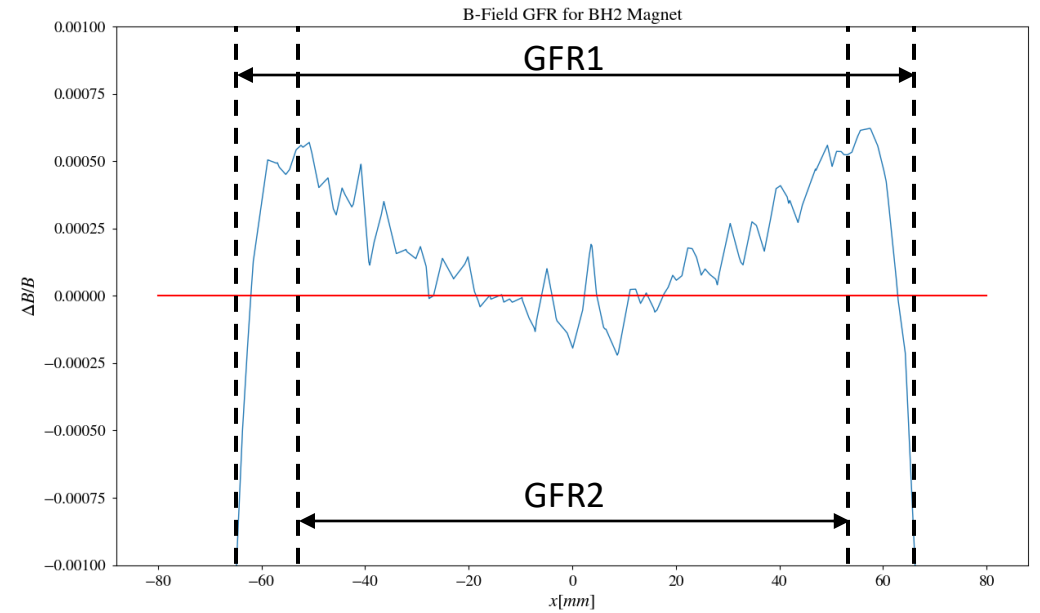
Max field strength:
 1.5-1.75T
 Field gradient = -1.3099 T/m

Good Field Region - BH2

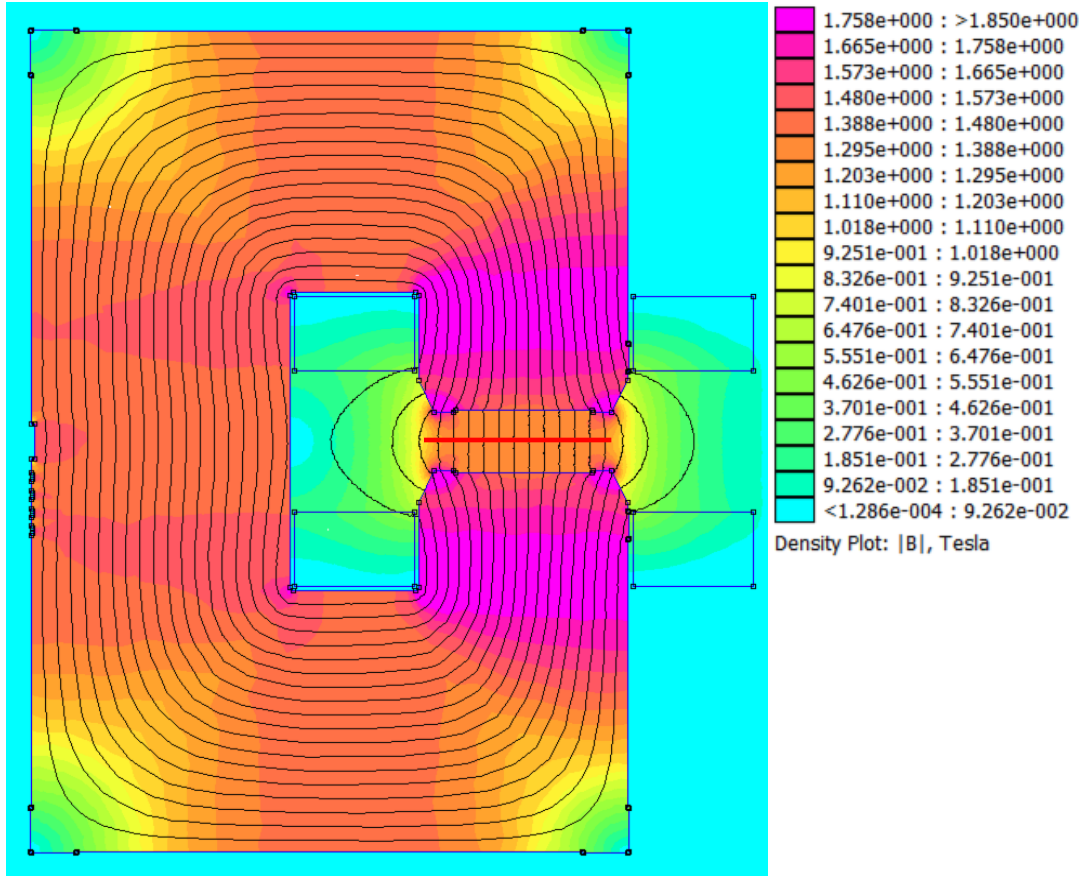
$$\left(\frac{\Delta B}{B_{id}} < 1 \times 10^{-3}\right)$$

GFR1 = 130 mm x 12 mm

GFR2 = 106.6 mm x 45 mm

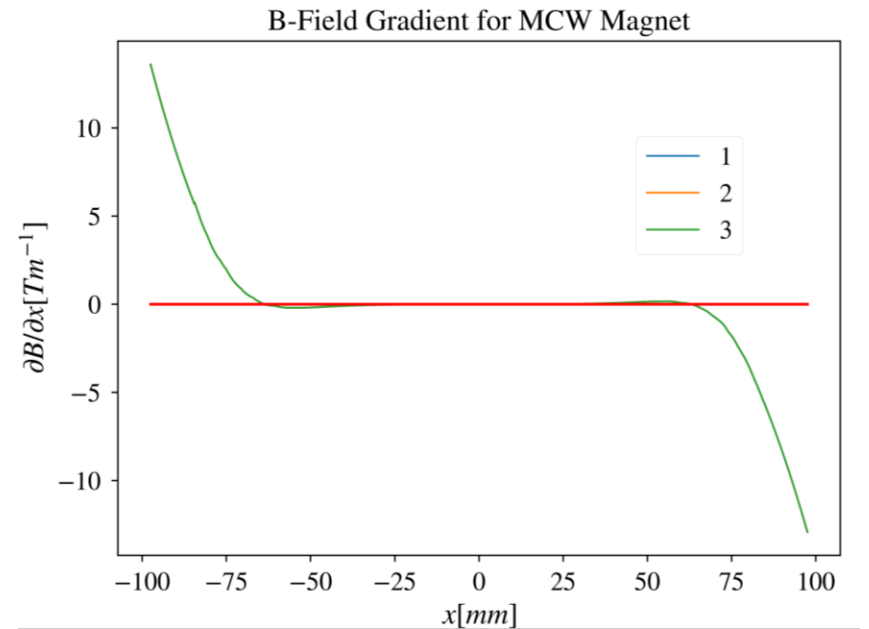
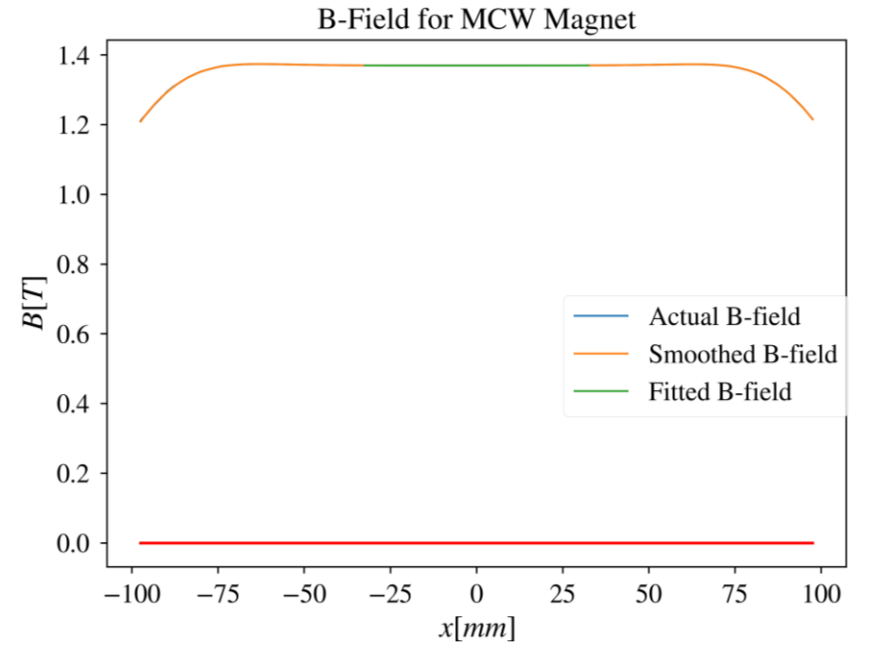


Field Analysis - MCW



96 turns, 1000 A (peak), 414.46 A
 Aperture width and height: 195 mm, 70 mm
 Total width and height: 850 mm, 1130 mm

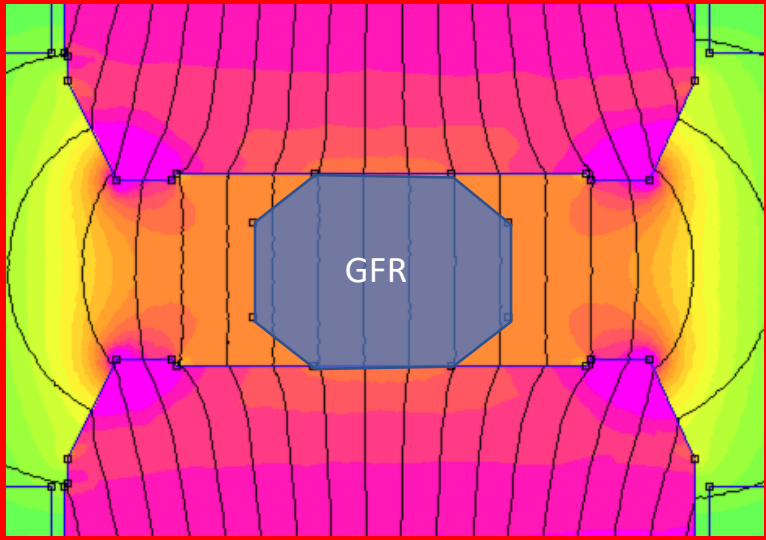
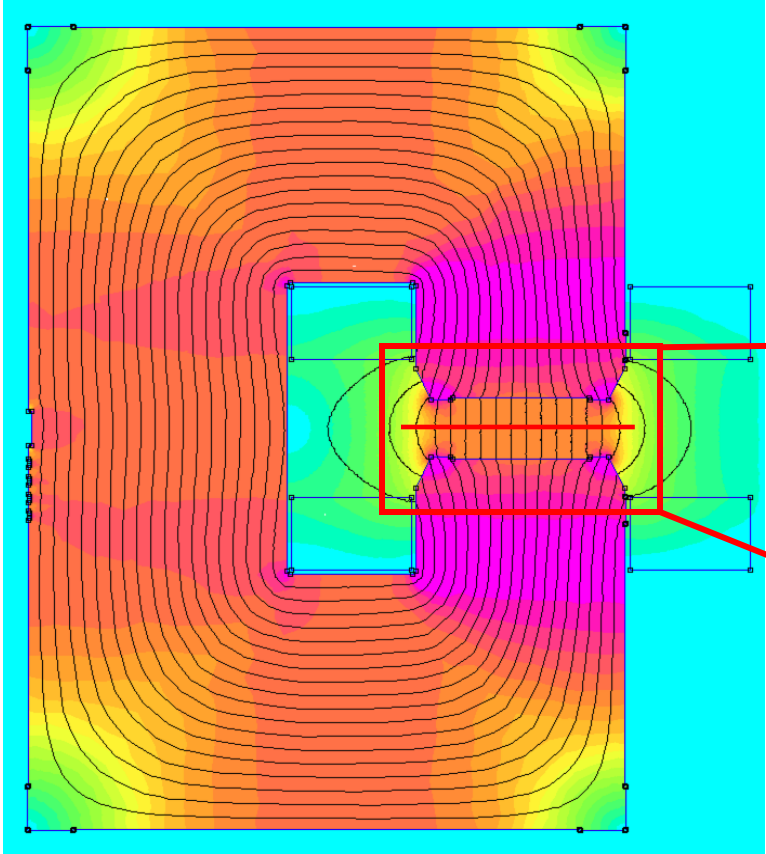
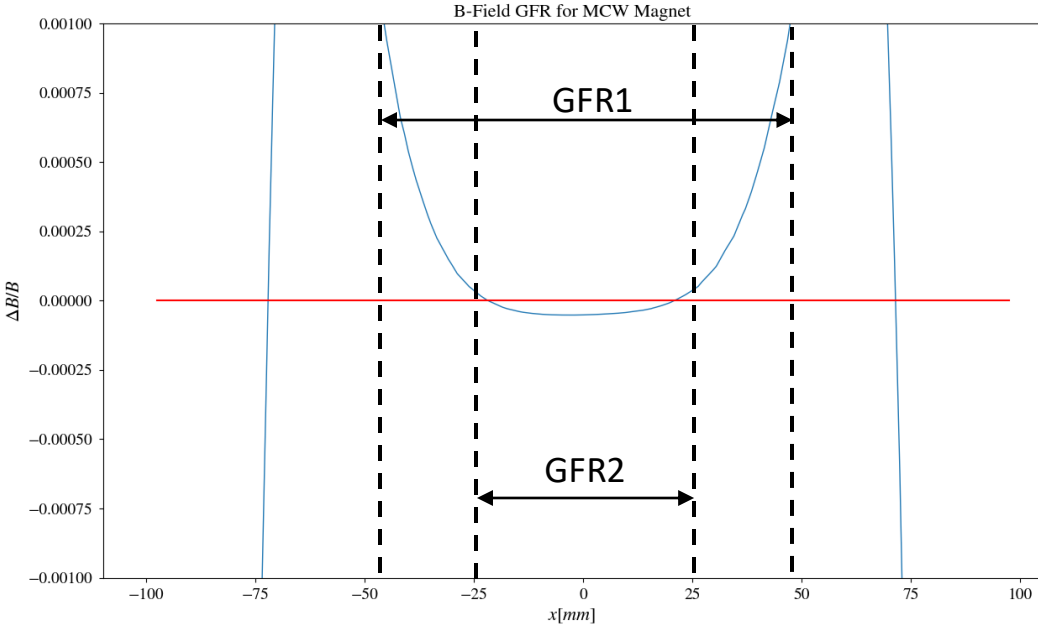
Max field strength:
 1.37T
 (about 2T at peak current)



Good Field Region - MCW

$$\left(\frac{\Delta B}{B_{id}} < 1 \times 10^{-3}\right)$$

GFR1 = 93 mm x 34 mm
GFR2 = 50 mm x 70 mm

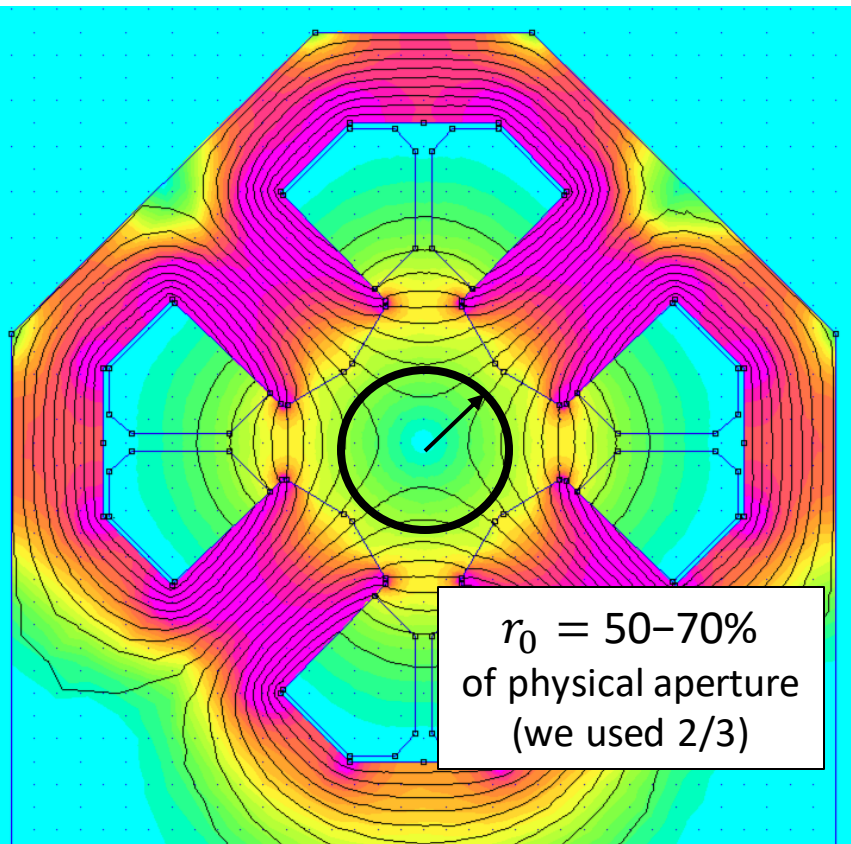


Multipole Contributions

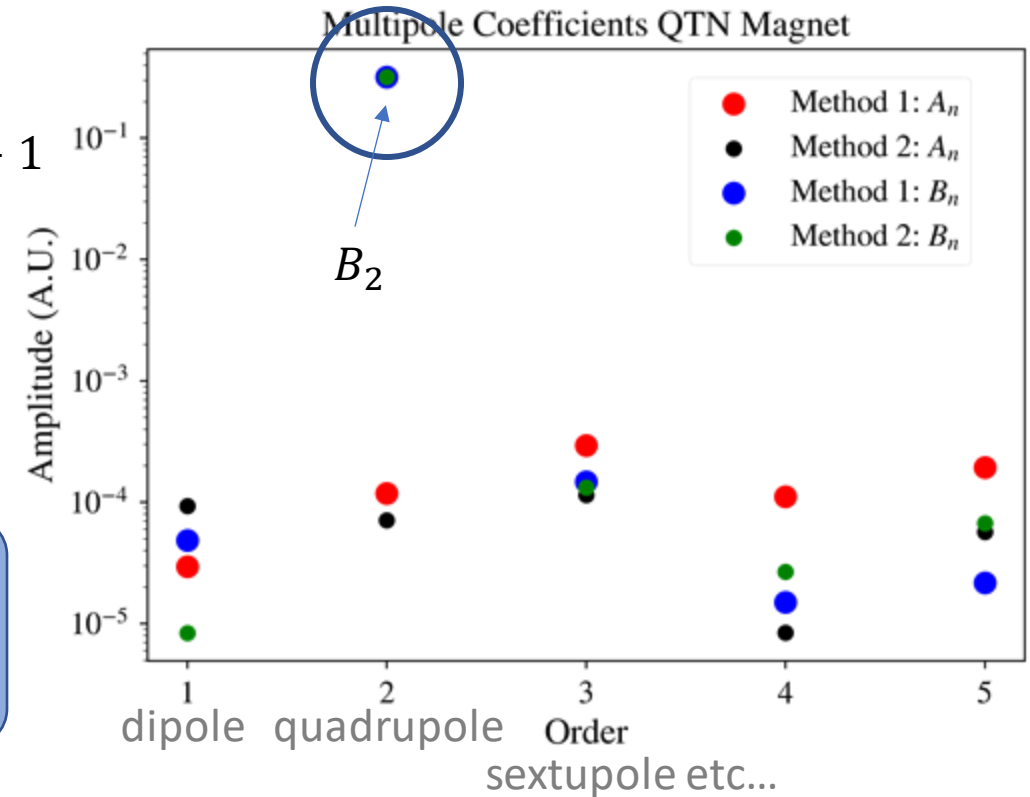
Allowed multipole contributions 'fit into' the symmetry of the device...

$$\text{Sample at } r_0 \text{ for } \theta_m = \frac{2\pi m}{M}, \quad m = 0, 1, 2, \dots, M - 1$$

m : discrete angles 0,1,2...
 n : multipole order 1,2,3...

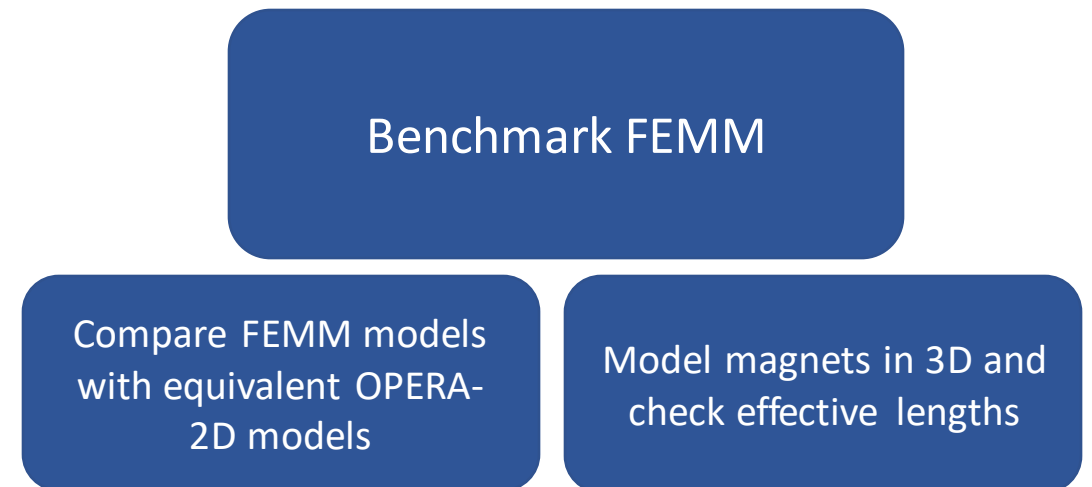
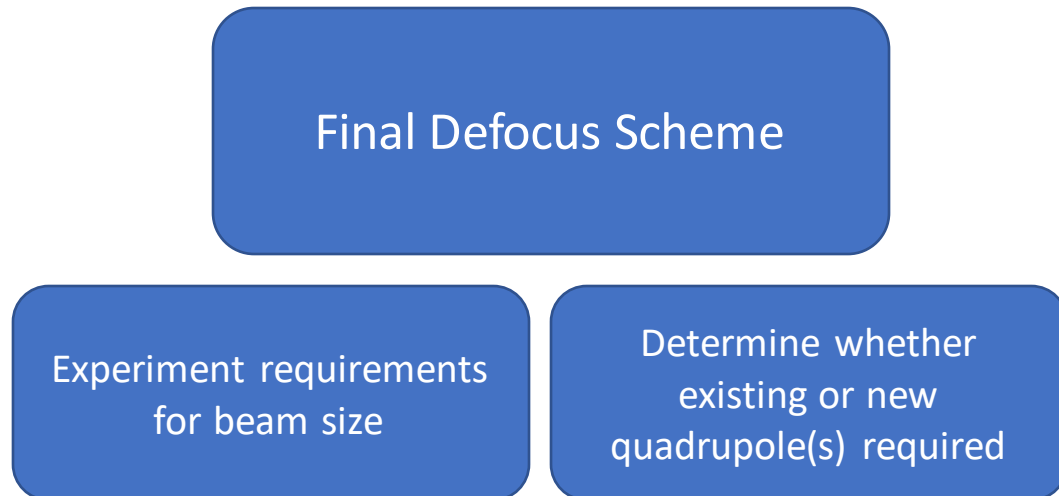


Discrete Fourier transform



- ✓ Only B_2 **normal quadrupole** term contributes, as hoped
- ✓ Reasonable agreement using two slightly different methods as a sanity check

Future Magnet Studies



RF Cavity Team

Majid Ali, Pablo Arrutia and Cameron Robertson

Infrastructure

Voltage
Requirements

Cavity Design

Infrastructure

Cavity: **800MHz 5 cell Superconducting Cavity**

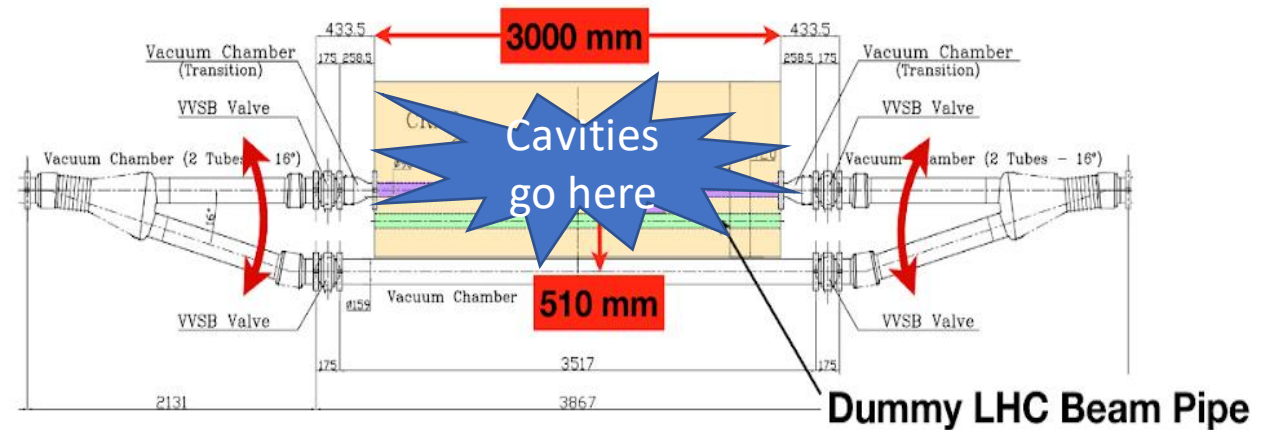
- Multiple of 200MHz RF frequency -> 5 ns bunch spacing
- High acceleration gradient



802 MHz ERL Cavity Design and Development (2018)
<http://cds.cern.ch/records/26538533/>

Location: **LSS6 Crab Cavity Testing Zone**

- Minimise additional impedance; **HL-LHC**
- Allow rapid changeover between electron/proton modes (10 min)



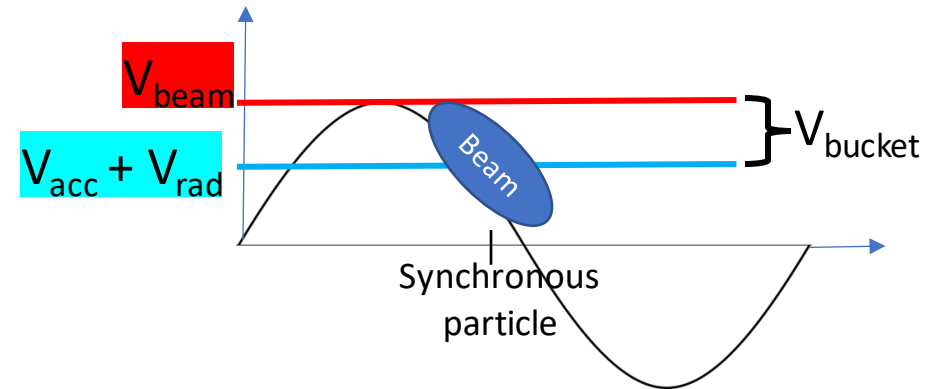
Crab Cavity Testing in the SPS (2013)
<https://indico.cern.ch/event/257368/>

Voltage Requirements

- Important to
 - Determine if voltage and fields achievable with the chosen technology
 - Specify the consequences of different voltage choices
- Two beam energies considered: 16 GeV and 18 GeV (for possible upgrade)

$$V_{beam} = V_{acc} + V_{rad} + V_{bucket}$$

- V_{beam} : effective peak voltage visible by the beam
- V_{acc} : voltage for acceleration
- V_{rad} : voltage for synchrotron radiation
- V_{bucket} : voltage for bucket area

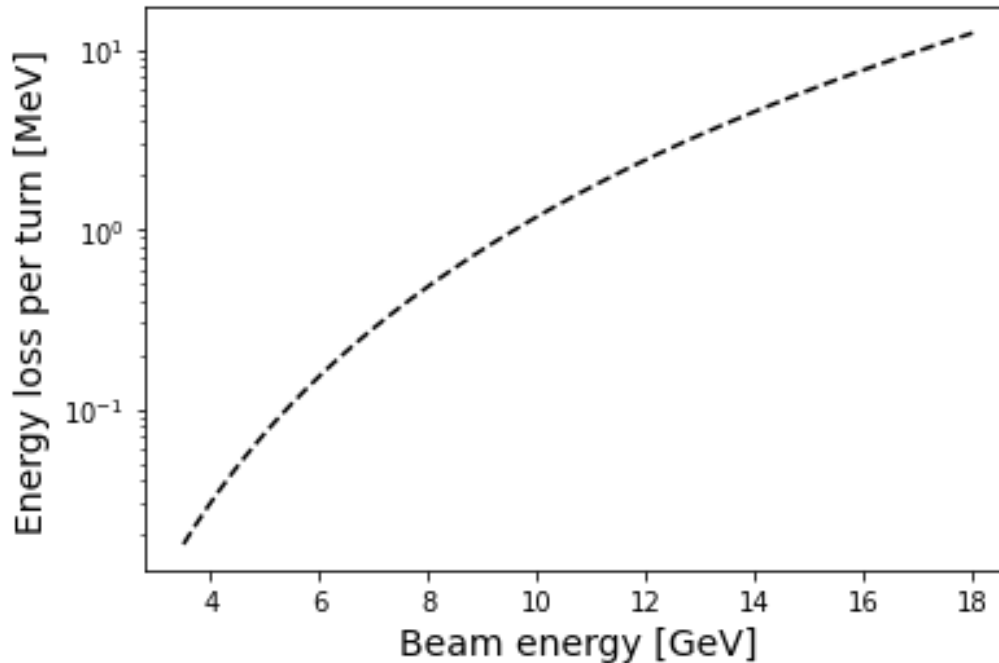


V_{acc} and V_{rad}

$$V_{acc} = (E_{extraction} - E_{injection}) \frac{\text{one turn time} \rightarrow 23 \text{ us}}{\text{acceleration time} \rightarrow 0.2 \text{ s}}$$

↓
↓
 16 or 18 GeV 3.5 GeV

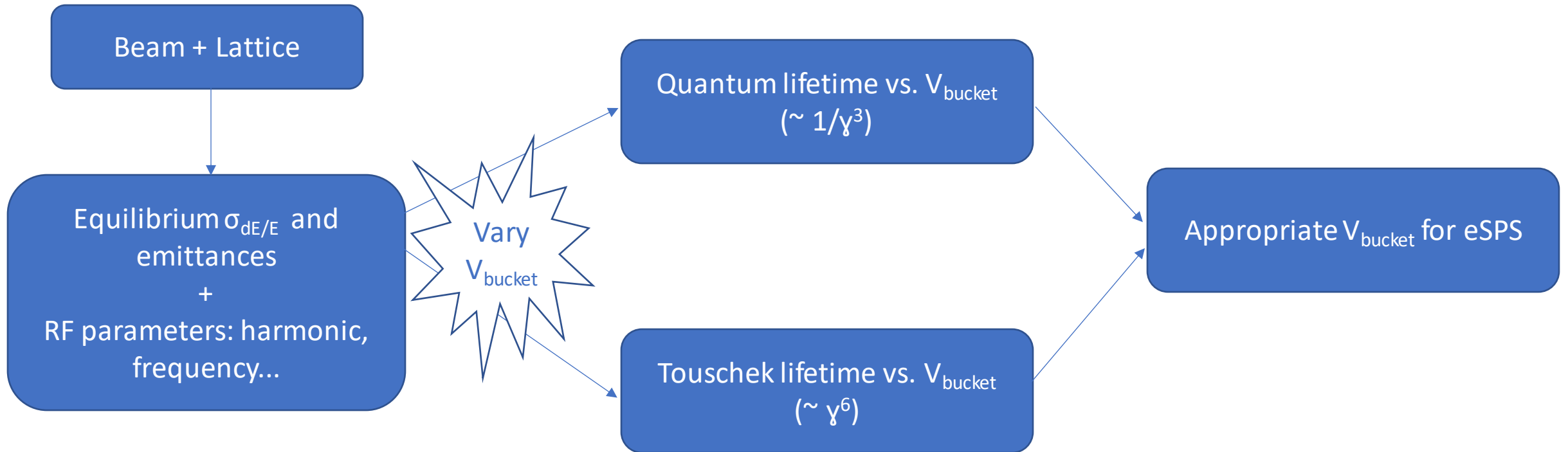
$$V_{rad} =$$



Beam Energy	V_{acc} ($\sim \gamma$)	V_{rad} ($\sim \gamma^4$)
16 GeV	1.4 MV	7.7 MV
18 GeV	1.7 MV	12.4 MV

V_{bucket}

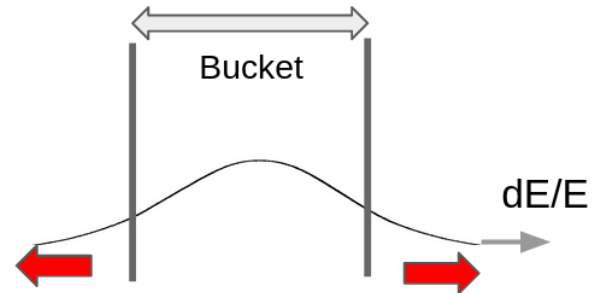
- V_{bucket} chosen to ensure a long enough beam lifetime



V_{bucket}

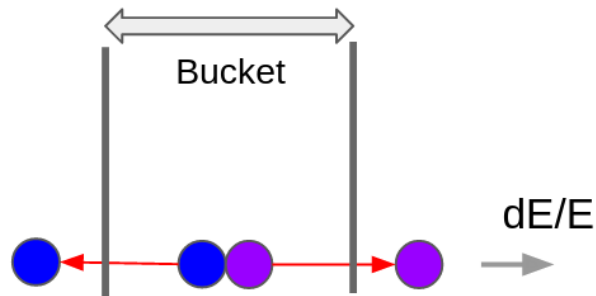
Quantum lifetime

Beam diffuses from quantum excitation

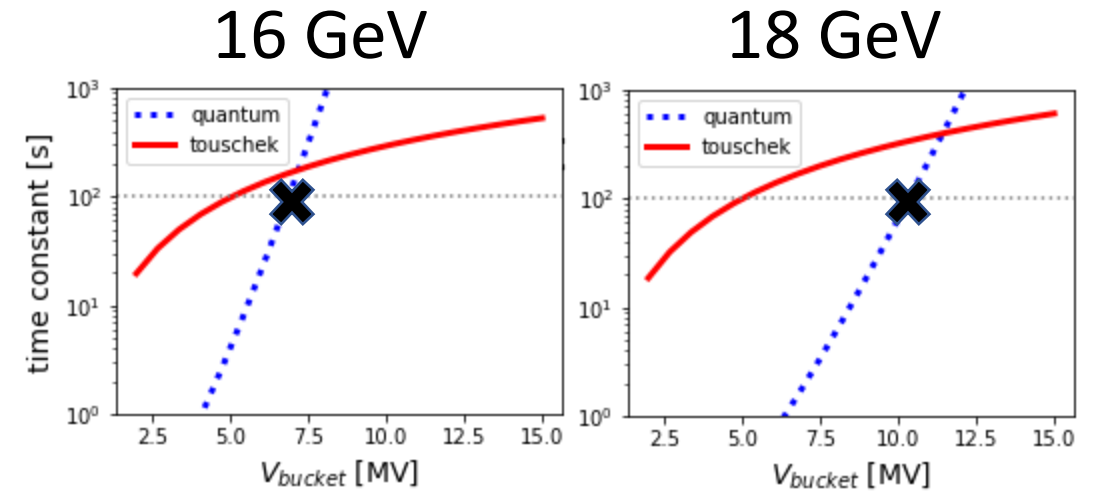


Touschek lifetime

Beam scatters from e-e scattering



- Lifetimes characterised by their time constants
- We aim for time constants >100 s (~ 10 x cycle)



Need $V > 7$ MV

Need $V > 10$ MV

Quantum dominates, but Touschek also relevant!

V_{beam} and E_0

The on-axis accelerating electric field E_0 is important for R&D considerations:

$$E_0 = \frac{V_{beam}}{(\# \text{ of cavities})(\text{transit time factor})(\text{cavity length})}$$

↓ ↓ ↓
 2 0.7 94 cm

Beam Energy	V_{acc}	V_{rad}	V_{bucket}	V_{beam}	E_0
16 Gev	1.4 MV	7.7 MV	7.0 MV	16.1 MV	12.2 MV/m
18 Gev	1.7 MV	12.4 MV	10.0 MV	24.1 MV	18.3 MV/m

} Achievable
 (will show comparison to other projects in upcoming slides)

Cavity Design

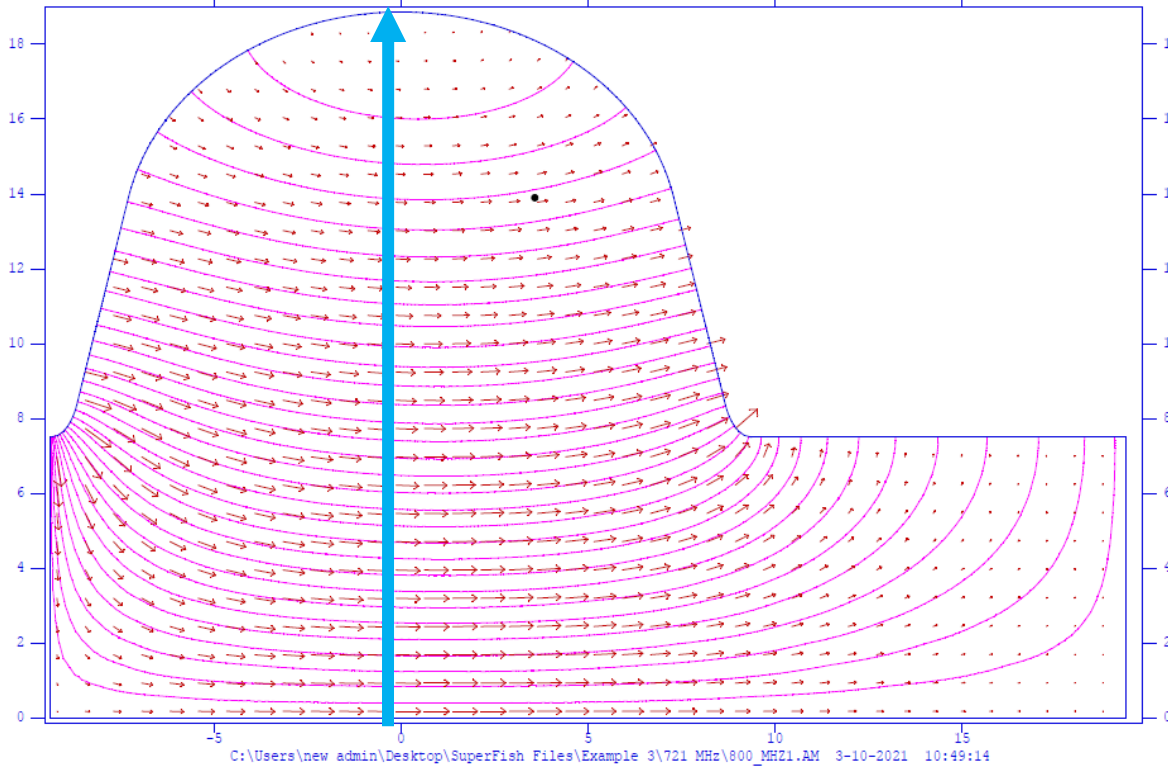
- Minimize the peak surface electric field (E_p/E_0)
Field emission limit (E_0 limit)
- Ratio of the magnetic peak with respect to the accelerating gradient (H_p/E_0) . Quench limit (SC thermal breakdown)
- (Large geometrical factor (G) and R/Q, Lower power dissipation)
- Efficient use of RF energy (end-cell design)
Have good field flatness

2D Model in Superfish

Equator radius used to tune cavity frequency

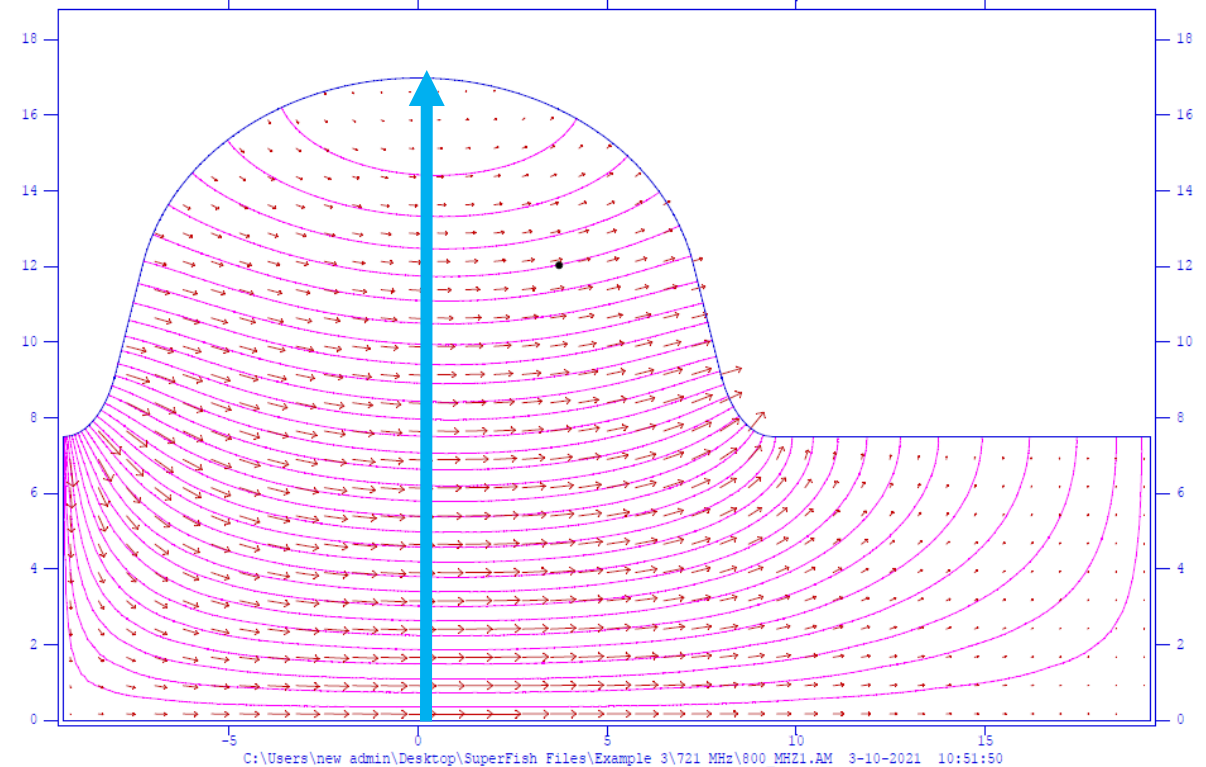
Before

800 MHz elliptical cavity for eSPS $F = 715.43936$ MHz



After

800 MHz elliptical cavity for eSPS $F = 800.00002$ MHz

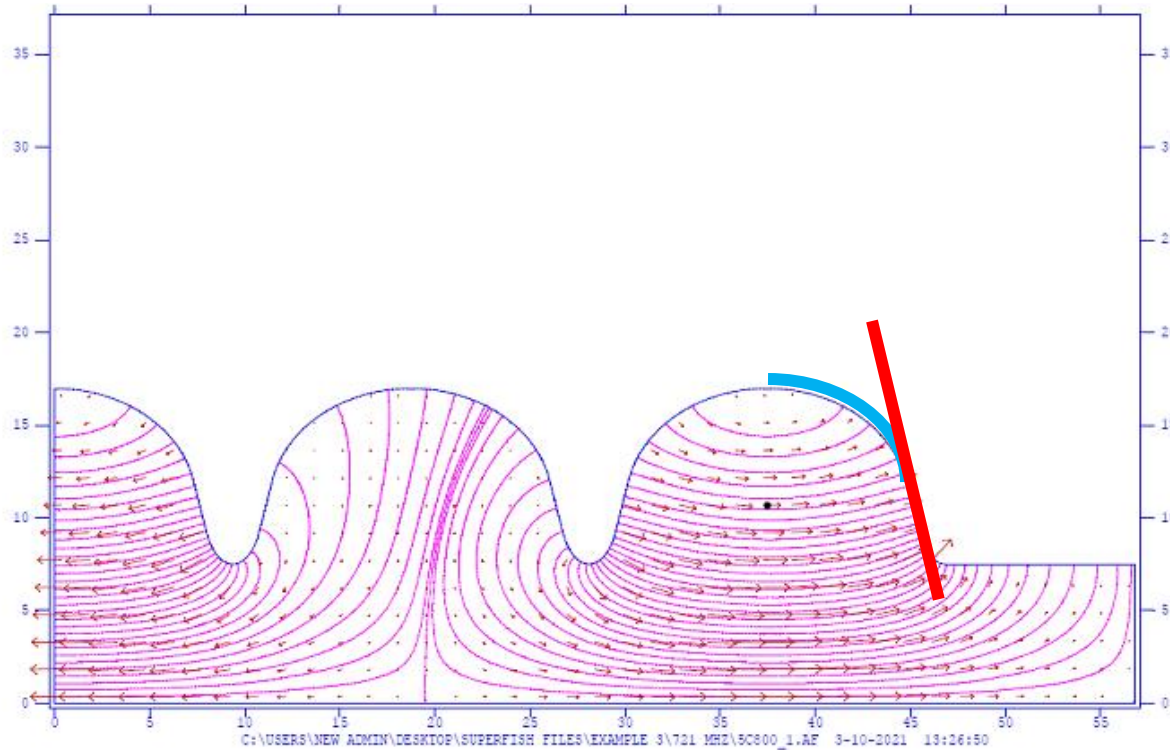


2D Model

Varied **dome ellipse** + **wall slope** to optimize end-cell

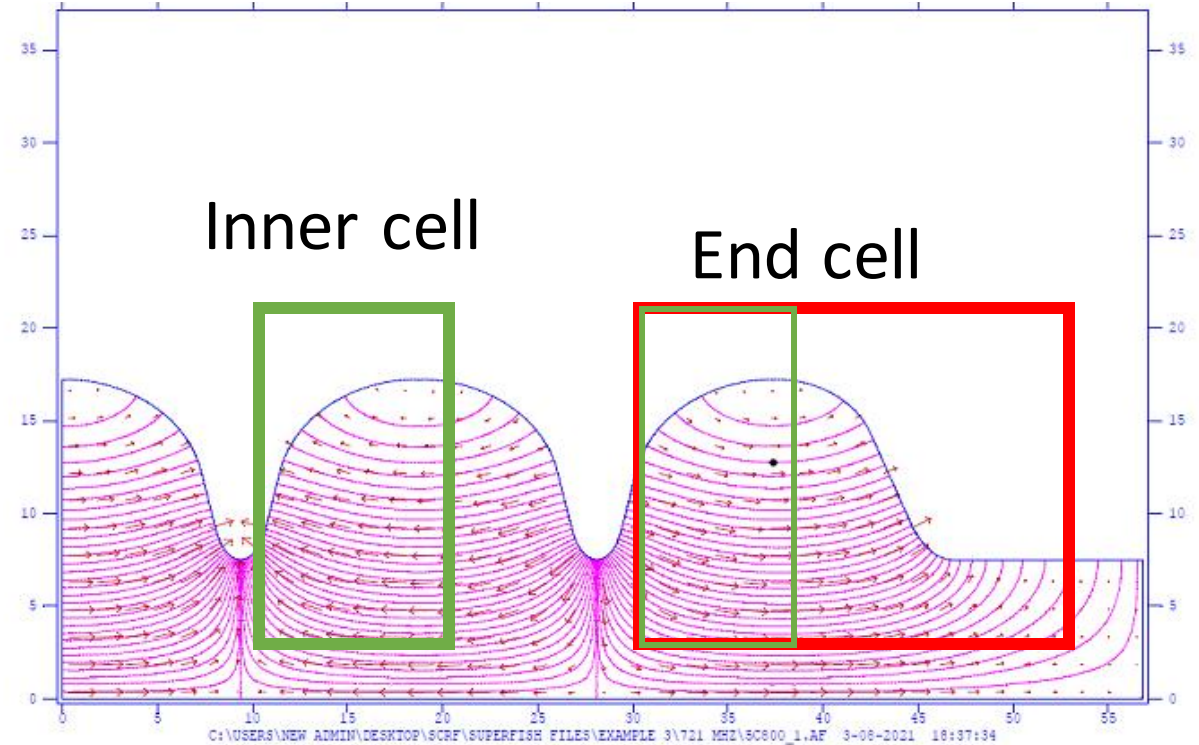
Before Tuning

800 MHz elliptical cavity for eSPS $F = 788.21672$ MHz



After Tuning

800 MHz elliptical cavity for eSPS $F = 799.99288$ MHz

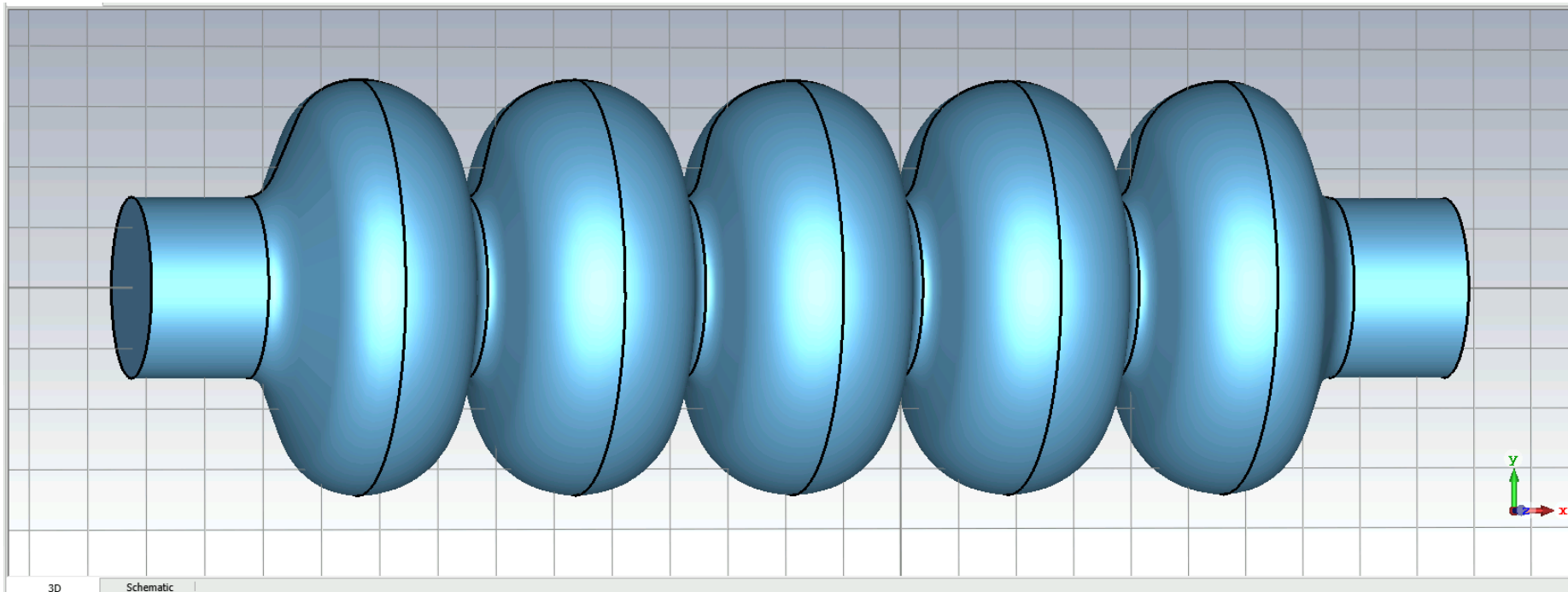


A five-cell 800 MHz cavity parameters are listed for comparison

	JLab	ESS	OUR DESIGN 16 GeV (18 GeV)
Number of cells	5	5	5
Freq (MHz)	800	704.42	800
L_{act} Length (cm)	93.5	85.5	93.68
E_o (MV/m)	11.8	19.9	12.2 (18.3)
E_p (MV/m)	30.68	43.75	29.38 (44.07)
B_p (mT)	57.82	85.57	43.63 (65.45)
R/Q (ohm)	523.9	518	427.58

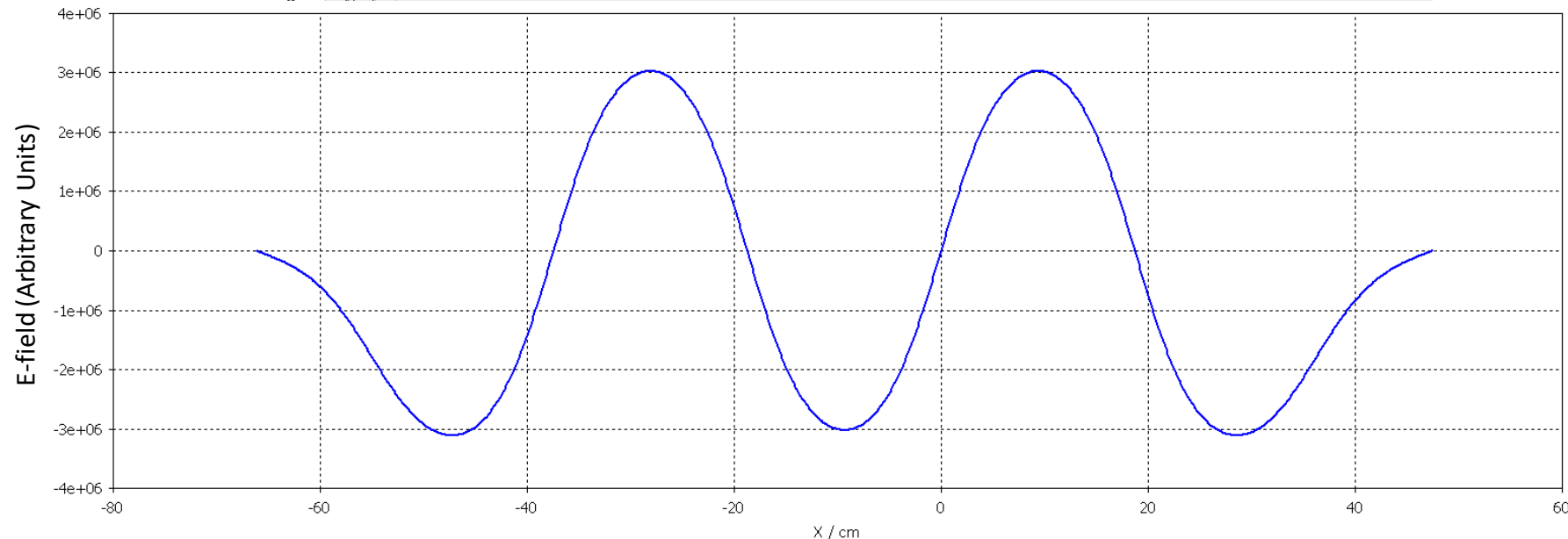
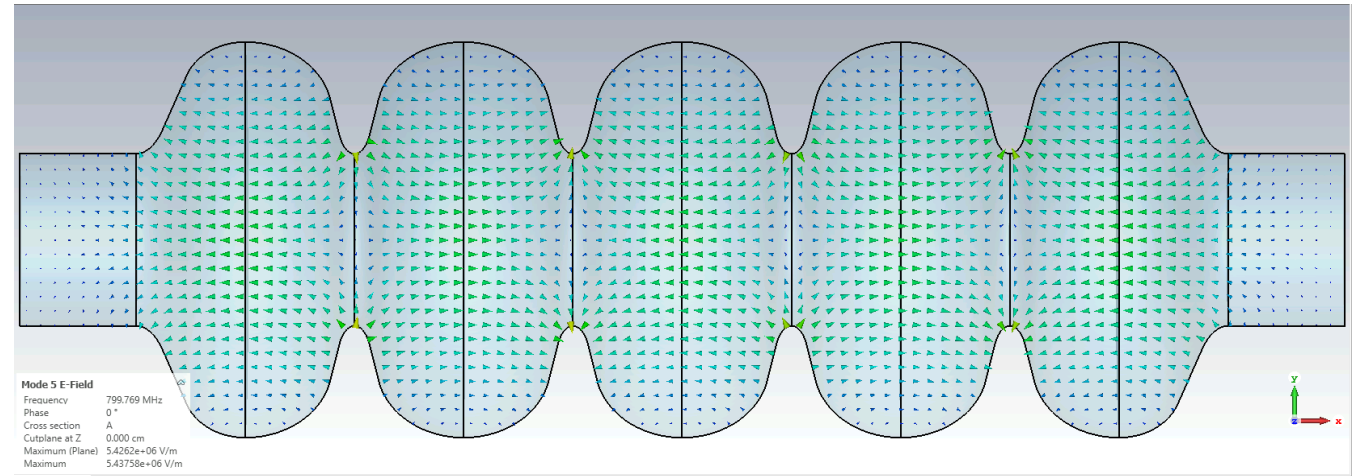
3D model

- CST Studio Suite – Electromagnetic field simulation software
- Geometry imported from Superfish input files
- Complete 3D model, eigenmode solver, mode analysis, EM visualisation



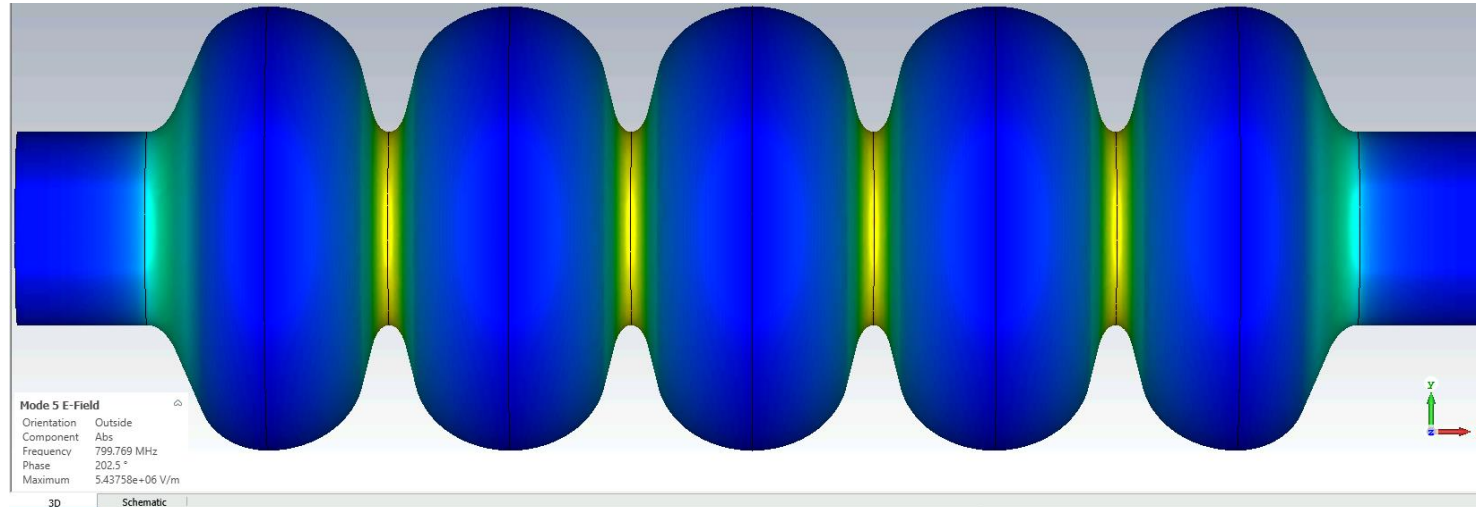
3D model

- Multiple modes
 - Mode 1 – 0 mode, 757.6815MHz
 - Mode 5 - π mode, 799.769MHz
- Asymmetric effects
 - Good field flatness
- 'Hot spots'

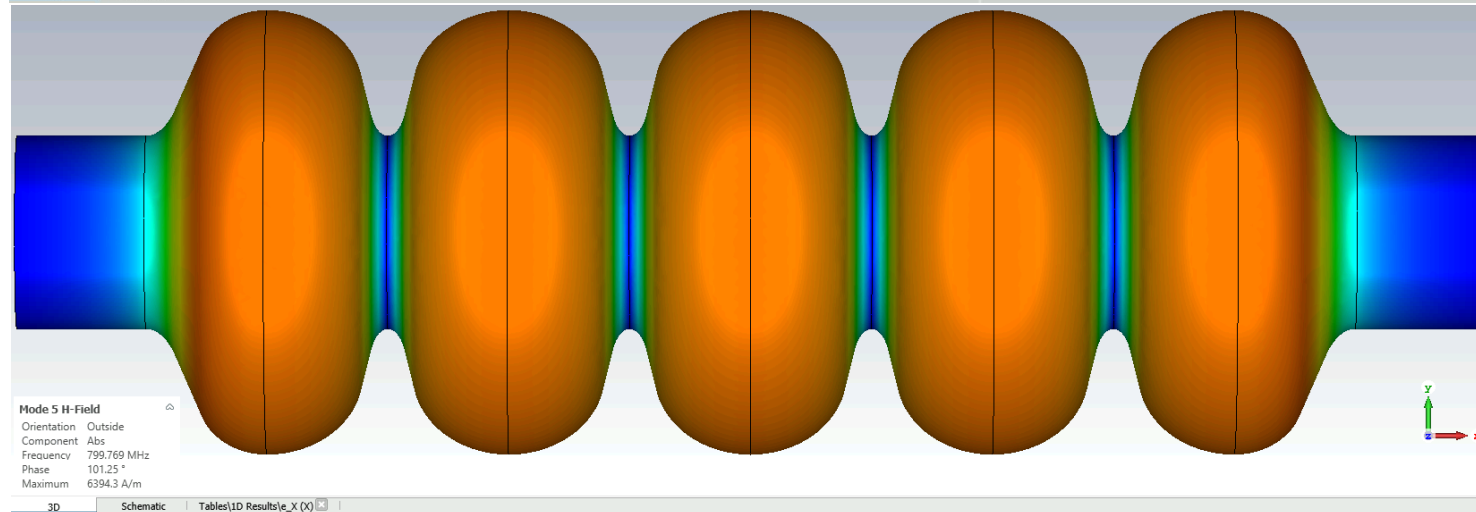


3D model

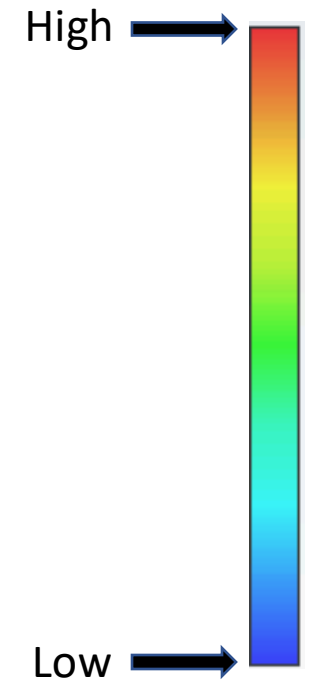
E-Field



H-Field



Arbitrary field strength units

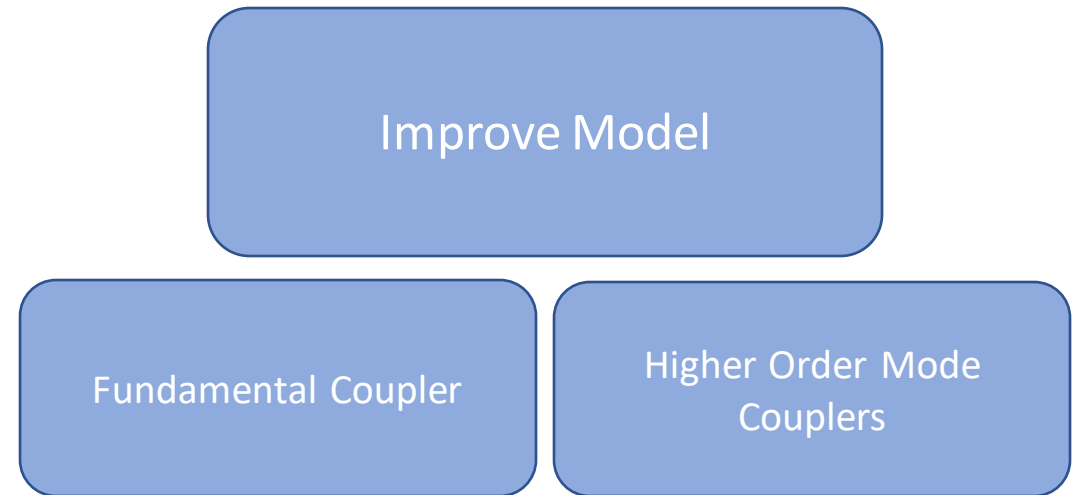
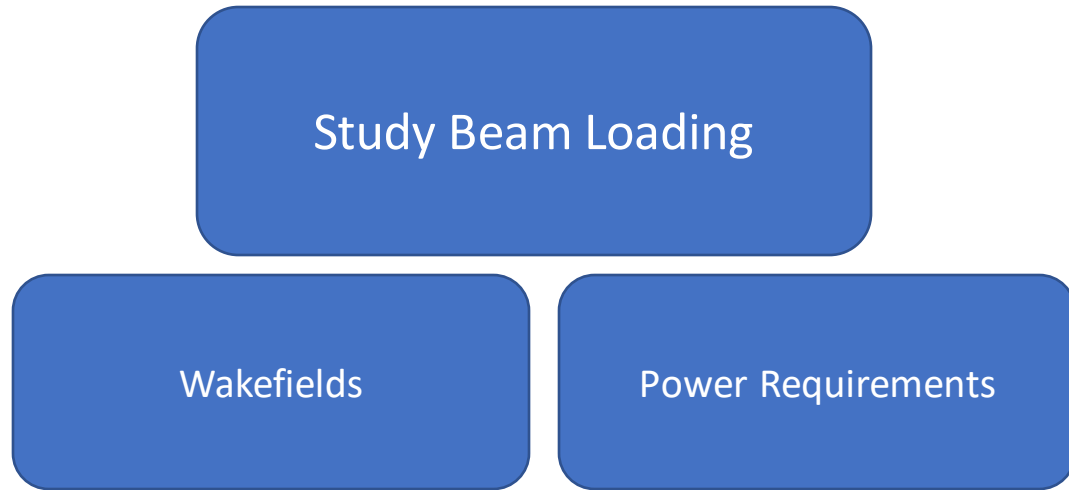


3D model

Parameter	Superfish Design	CST Design	Difference
U at $E_0=10\text{MV/m}$ (J)	19.90	19.86	<1%
E_{max}/E_0	2.4080	2.5419	5%
$B_{\text{max}}/E_0(\text{mT/MV})$	3.796	3.755	5%
$r/Q(\Omega)$	427.58	428.37	<1%

- Geometrical properties near-identical; necessary quality check
 - Imported directly from Superfish
- Peak field strength discrepancies
 - Limitations from mesh size
 - CST optimisation required

Future RF Studies



Conclusions

eSPS can produce a **unique Light Dark Matter physics programme** with relatively small costs and time-scales.

Conclusions

eSPS can produce a **unique Light Dark Matter physics programme** with relatively small costs and time-scales.

Electron beam successfully transported from linac to SPS, but adjustments required to reduce y-plane dispersion.

Conclusions

eSPS can produce a **unique Light Dark Matter physics programme** with relatively small costs and time-scales.

Electron beam successfully transported from linac to SPS, but adjustments required to reduce y-plane dispersion.

Existing **CERN magnets modelled and analysed** (good field region + multipoles). Field quality satisfies transfer line requirements.

Conclusions

eSPS can produce a **unique Light Dark Matter physics programme** with relatively small costs and time-scales.

Electron beam successfully transported from linac to SPS, but adjustments required to reduce y -plane dispersion.

Existing **CERN magnets modelled and analysed** (good field region + multipoles). Field quality satisfies transfer line requirements.

2 Superconducting 800MHz RF cavities in LSS6 bypass **fulfil requirements** for 16 and 18 GeV operation.

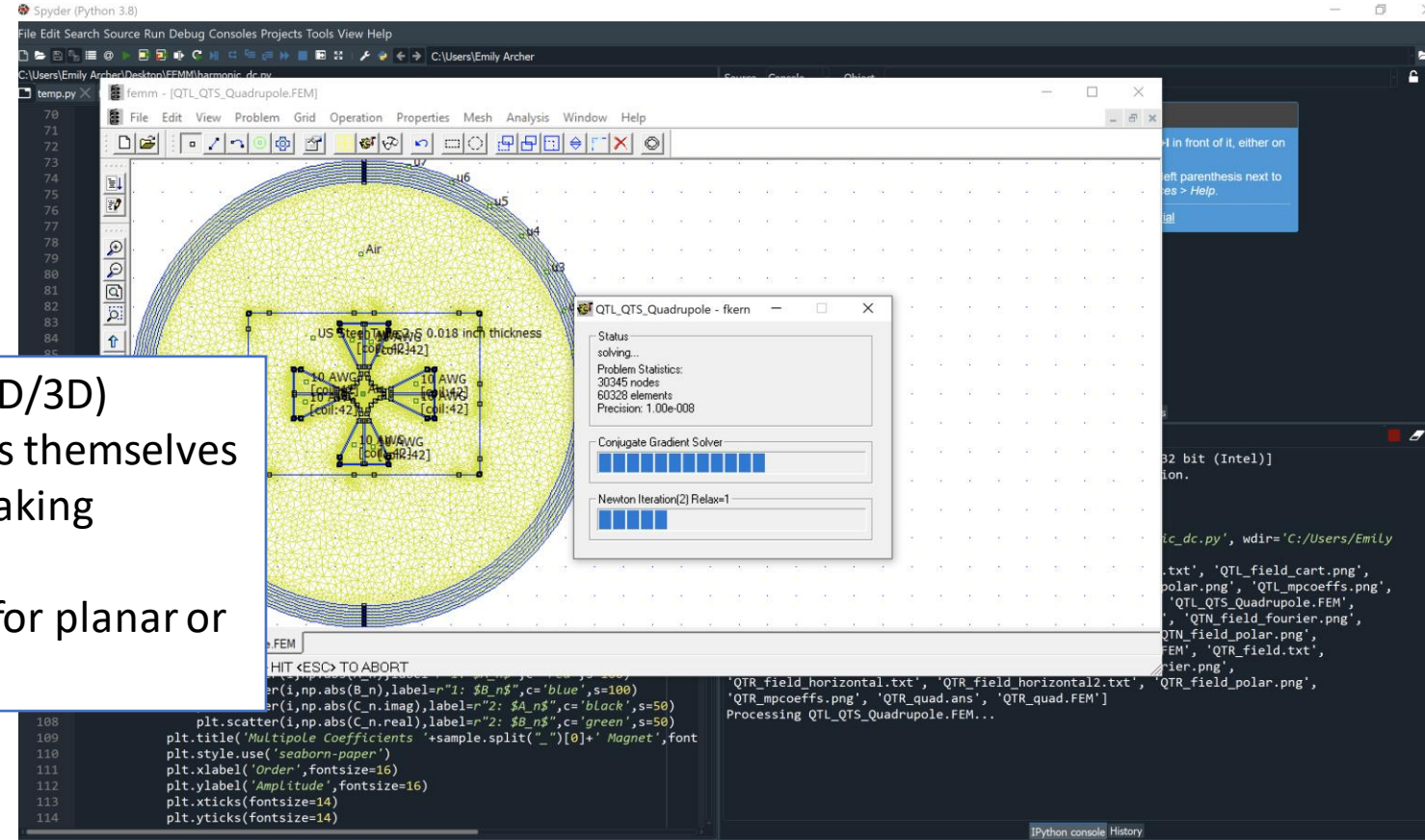
Extra slides

FEMM + pyFEMM

(Finite Element Method Magnetics + Python wrapper library)

- Finite element method used to solve
 - magnetostatic
 - time harmonic magnetic
 - electrostatic and
 - steady-state heat flow problems

- + Free open-source software (unlike Opera-2D/3D)
- + User-friendly GUI for designing the magnets themselves
- + Controllable via pyFEMM Python library, making integrated analysis possible
 - Only for 2D problems, but with the option for planar or axisymmetric domains



Using CERN technical drawings, we modelled existing CERN magnets in FEMM

Field Analysis

- Linear transect of the central field plotted
- Savinsky-Golay filter
- Numerical gradient calculated (three different methods)
- Linear fitting to determine 'ideal field'
- **Good field region determined:**

$$\text{Good Field Region} \rightarrow \frac{\Delta B}{B_{id}} = \frac{B(x,y) - B_{id}(x,y)}{B_{id}(x,y)} < 1 \times 10^{-3}$$

Dipole Bending Angles: Injection

Dipole Bending Magnets				
Magnet Type	Iron Length L (m)	Nominal Field Strength B (T)	Bending Angle (mrad)	Bending Angle (deg)
206	0.16	0.15	2.056	0.117
BH2 Type 2	0.51	1.52	66.401	3.804
MBB/E	6.20	2.02	1072	61.421
MCW	3.00	1.50	385.45	22.085
MTR	3.60	2.04	629.057	36.042

Note: all values assume max. operating current

Quadrupole Focusing Strength: Injection

Quadrupole Focusing Magnets				
Magnet Type	Iron Length L (m)	Nominal Field Strength $\partial B_y / \partial x$ (Tm ⁻¹)	Normal Quadrupole Coefficient $K1$ (m ⁻²)	Focal Length f (m)
CLIC	0.08	-	-	-
Q100	1.00	11.0	0.942	1.061
QFS	0.80	18.9	1.619	0.772
QTL	3.00	24.0	2.0557	0.162
QTN	0.30	5.33	0.4565	7.302
QTR	0.308	1.4	0.1199	27.079
QTS	1.5	24.0	2.0557	0.324

Note: all values assume max. operating current

Dipole Bending Magnets				
Magnet Type	Iron Length L (m)	Nominal Field Strength B (T)	Bending Angle (mrad)	Bending Angle (deg)
206	0.16	0.15	0.450	0.0258
BH2 Type 2	0.51	1.52	14.525	0.832
MBB/E	6.20	2.02	234.67	13.446
MCW	3.00	1.50	84.318	4.831
MTR	3.60	2.04	137.61	7.884

Quadrupole Focusing Magnets				
Magnet Type	Iron Length L (m)	Nominal Field Strength $\partial B_y/\partial x$ (Tm ⁻¹)	Normal Quadrupole Coefficient $K1$ (m ⁻²)	Focal Length f (m)
CLIC	0.08	-	-	-
Q100	1.00	11.0	0.2061	4.852
QFS	0.80	18.9	0.3541	3.530
QTL	3.00	24.0	0.4497	0.7412
QTN	0.30	5.33	0.0999	33.367
QTR	0.308	1.4	0.0262	123.92
QTS	1.5	24.0	0.4497	1.482

Note: all values assume max. operating current

Multipole Decomposition

- Generally, the fields in accelerator magnets can be decomposed as a superposition of the different multipole contributions
- Radial field at any location within the aperture can be expanded in terms of the harmonics as

$$B_r(r, \theta) = \sum_{n=1}^{\infty} \left(\frac{r}{r_0}\right)^{n-1} B_n(r_0) \sin n\theta + A_n(r_0) \cos n\theta \quad (\text{European convention})$$

Clearly we can find a multipole field by summing up these contributions, but what about decomposing our field simulated in FEMM to check the strength of these terms?

where $n = 1$ is the **dipole** contribution
 $n = 2$ is the **quadrupole** contribution
 $n = 3$ is the **sextupole** contribution
and so on...

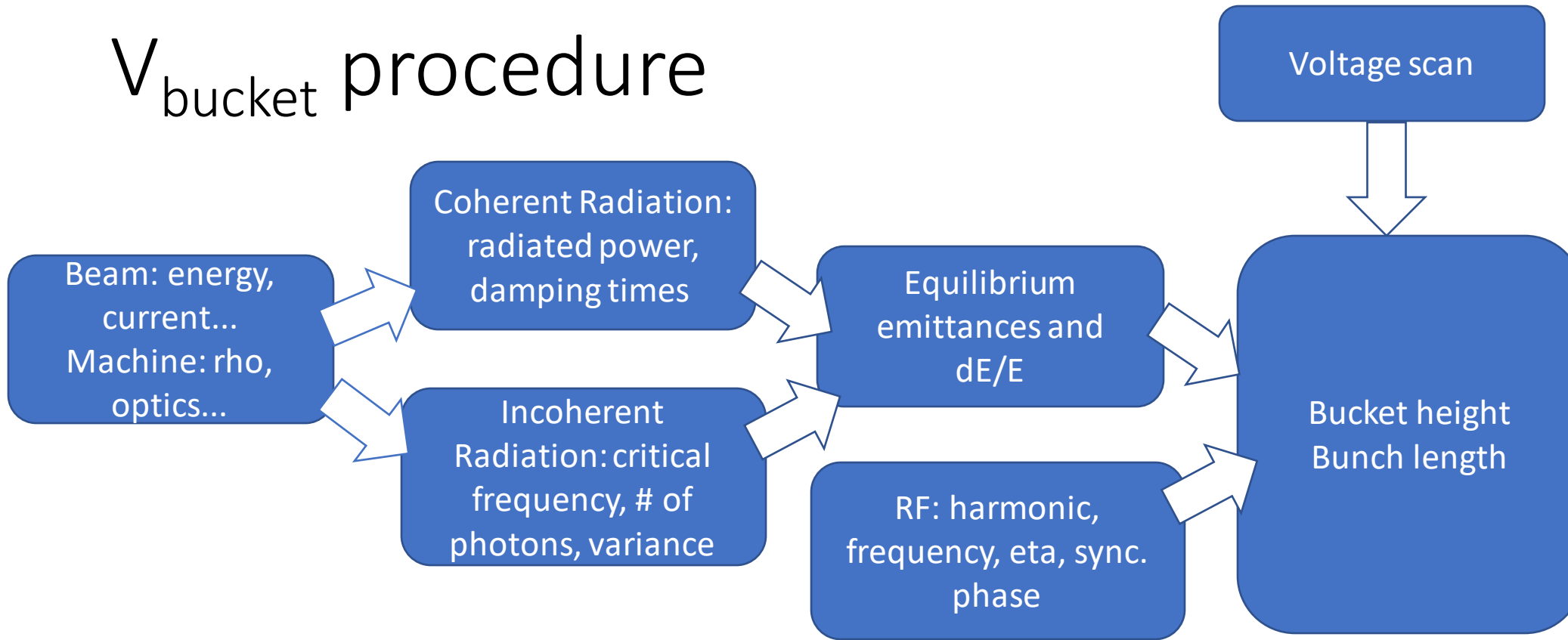
Sample the field and inverse Fourier transform, either normal/skew separately or complex coefficient as shown

$$1: \quad B_n(r_0) = \frac{2}{M} \sum_{m=0}^{M-1} B_r(r_0) \sin n\theta_m \quad \text{NORMAL}$$

$$A_n(r_0) = \frac{2}{M} \sum_{m=0}^{M-1} B_r(r_0) \cos n\theta_m \quad \text{SKEW}$$

$$2: \quad C_n(r_0) = \frac{1}{M} \sum_{m=0}^{M-1} B_m e^{-in\theta_m} = B_n(r_0) + iA_n(r_0)$$

V_{bucket} procedure



$$\tau_{quantum} = \frac{\tau_E}{(\#\sigma_{bucket}^2)} \exp(\#\sigma_{bucket}^2/2)$$

$$\tau_{touschek} = \frac{48\pi\gamma^2 \sigma_x \sigma_y \sigma_s}{Nr_0^2 c} \left(\frac{dE}{E}\right)_{bucket}^3$$

$$\left(\frac{\Delta E}{E_s}\right)_{max} = \sqrt{\frac{qV\beta^2}{\pi h\eta E_s} [2\cos\phi_s + (2\phi_s - \pi)\sin\phi_s]}$$

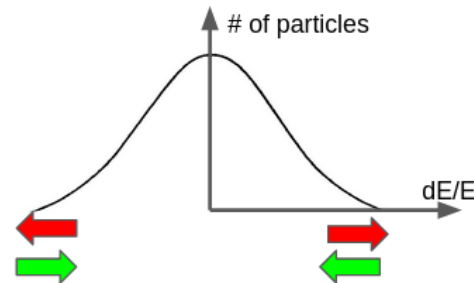
Quantum and Touschek effects

Quantum:

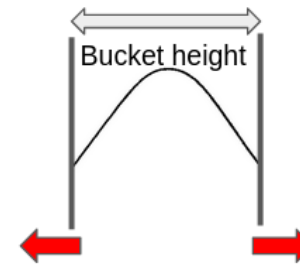
- Coherent synchrotron radiation vs. Incoherent quantum excitation

- RF bucket has finite area
- Particles outside bucket lose energy until lost in the aperture

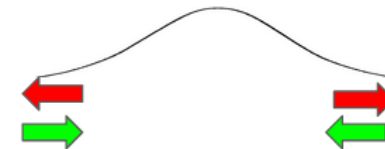
1. Equilibrium dE/E :



2. Bucket 'cuts' beam



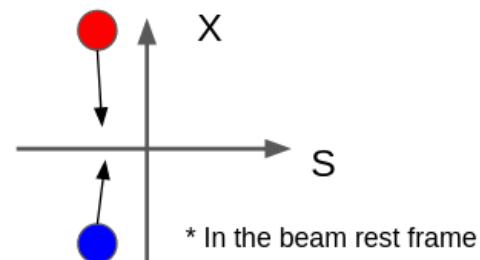
3. Diffuse and back to 1.



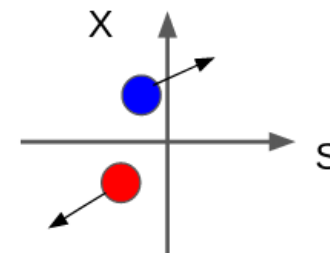
Touschek:

- Beam has most momentum spread in x
- Intra beam scattering transfers momentum between planes
- If transfer to longitudinal plane too large, particle ends up outside bucket
- Particles outside bucket lose energy until lost in the aperture

1. Most momentum in x



2. Momentum transfer to s



3. If $P_s >$ bucket height \rightarrow loss

